

Defending a Non Standard Supersymmetric Spectrum

A bottom-up viewpoint

Riccardo Barbieri

Workshop on Heavy Particles at the LHC

Pauli Center, ETH, January 5 - 7, 2011

B, Bertuzzo, Farina, Lodone, Pappadopulo, Zhuridov

(Quite a change relative to most of yesterday's talks.

A healthy blending, I suppose, hopefully soon driven by data)

The “weak coupling” way to EWSB

Favoured by indirect-data

EWPT, unification (susy), ν -masses (?)

Which problems, if susy?

No Higgs boson so far

No s -particle yet

Flavour and CP (The SM works in a quantitative way)

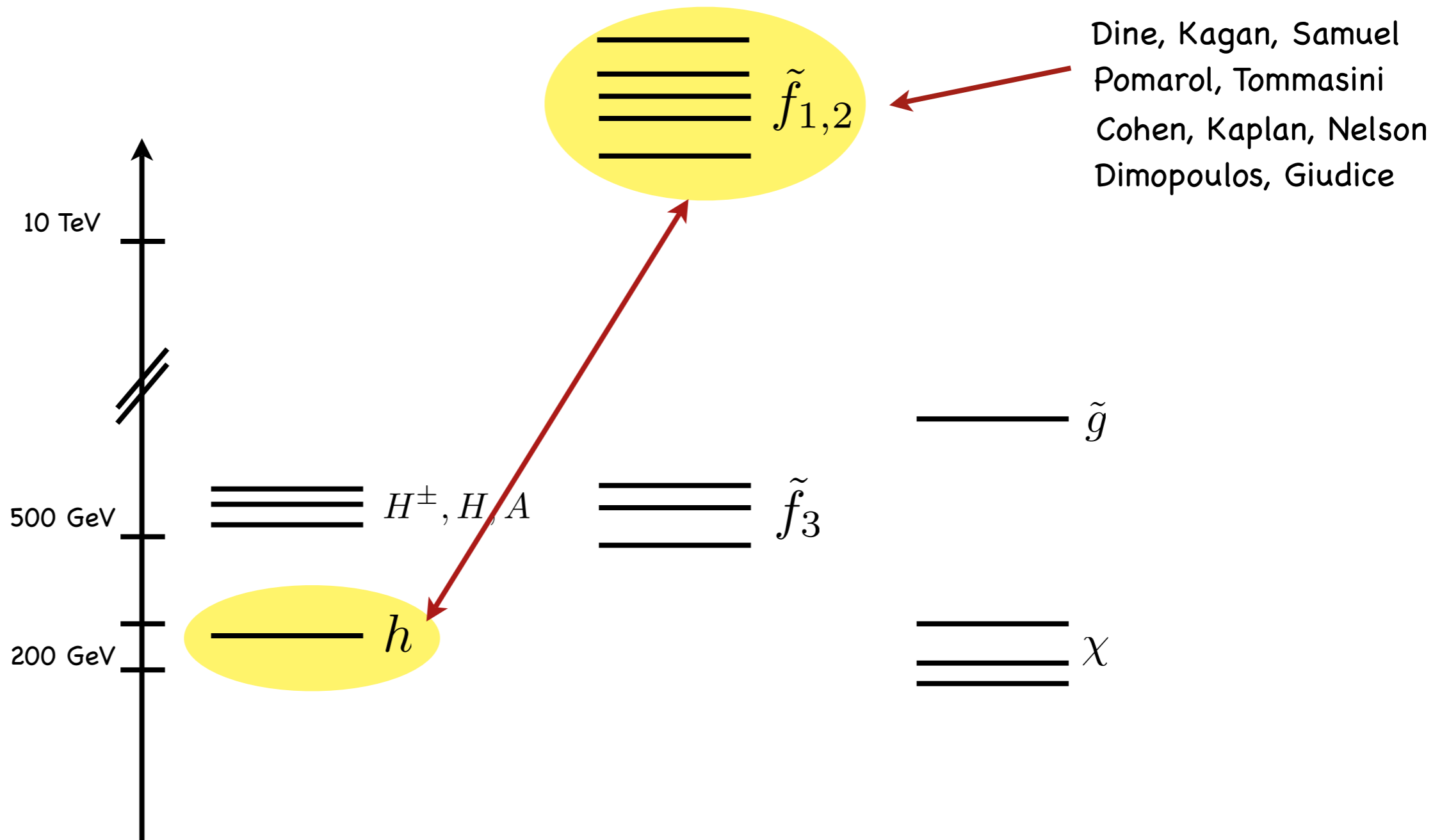
The MSSM as the only paradigm?

Claim \Leftrightarrow All problems of fine Tuning

(It could be right and we might never know)

A non-standard Supersymmetric Spectrum

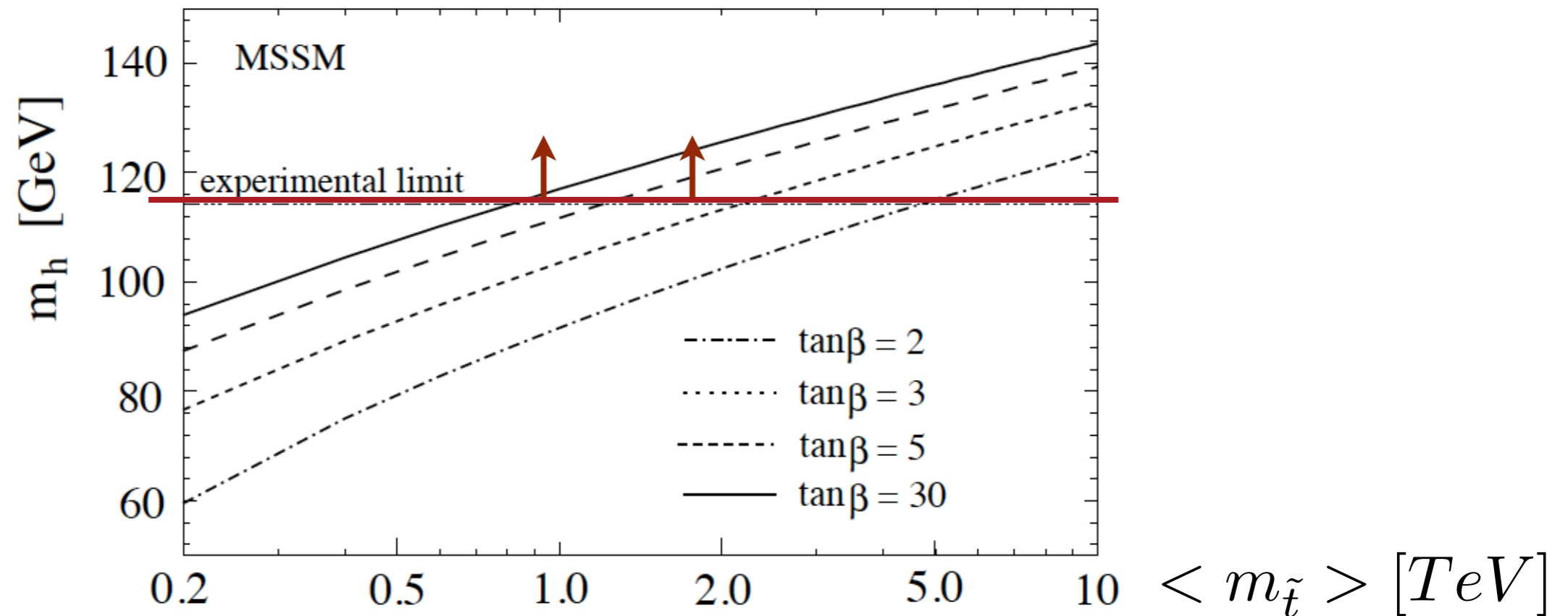
Motivated? Possible at all?



⇒ the Higgs boson mass problem
⇒ the flavour problem

Where is the supersymmetric Higgs boson?

MSSM



⇒ Take large $\tan\beta$ (muon anomaly?) **and large stop mass**
 but swallow, e.g. in SUGRA, a large contribution to M_Z
 to be fine-tuned away

$$\Delta M_Z^2 \approx (2 \div 3) m_{\tilde{t}}^2 \geq 100 M_Z^2$$

⇒ *h just around the corner and quasi-standard*

Supersymmetry without a light Higgs boson

Want to keep the success of the EWPT
 \Rightarrow Effective theories not enough

- ★ MSSM $m_h^2 \leq m_Z^2 \cos^2 2\beta$ + rad. corr.
- ★ Extra U(1) $m_h^2 \leq \left(m_Z^2 + \frac{g_x^2 v^2}{2\left(1 + \frac{M_X^2}{2M_\phi^2}\right)}\right) \cos^2 2\beta$ Batra, Delgado, Kaplan, Tait
- ★ Extra SU(2) $m_h^2 \leq m_Z^2 \frac{g'^2 + \Delta g^2}{g'^2 + g^2} \cos^2 2\beta$ $\Delta = \frac{1 + \frac{M_\Sigma^2}{M_X^2} \frac{g_I^2}{g^2}}{1 + \frac{M_\Sigma^2}{M_X^2}}$
- ★ $\Delta f = \lambda S H_1 H_2$
(NMSSM $\Rightarrow \lambda$ susy) $m_h^2 \leq m_Z^2 \left(\cos^2 2\beta + \frac{2\lambda^2}{g^2 + g'^2} \sin^2 2\beta\right)$
Harnik, Kribs, Larson, Murayama
B, Hall, Nomura, Rychkov

$\Rightarrow h$ not standard and not even light

ElectroWeak Precision Tests in λ SUSY

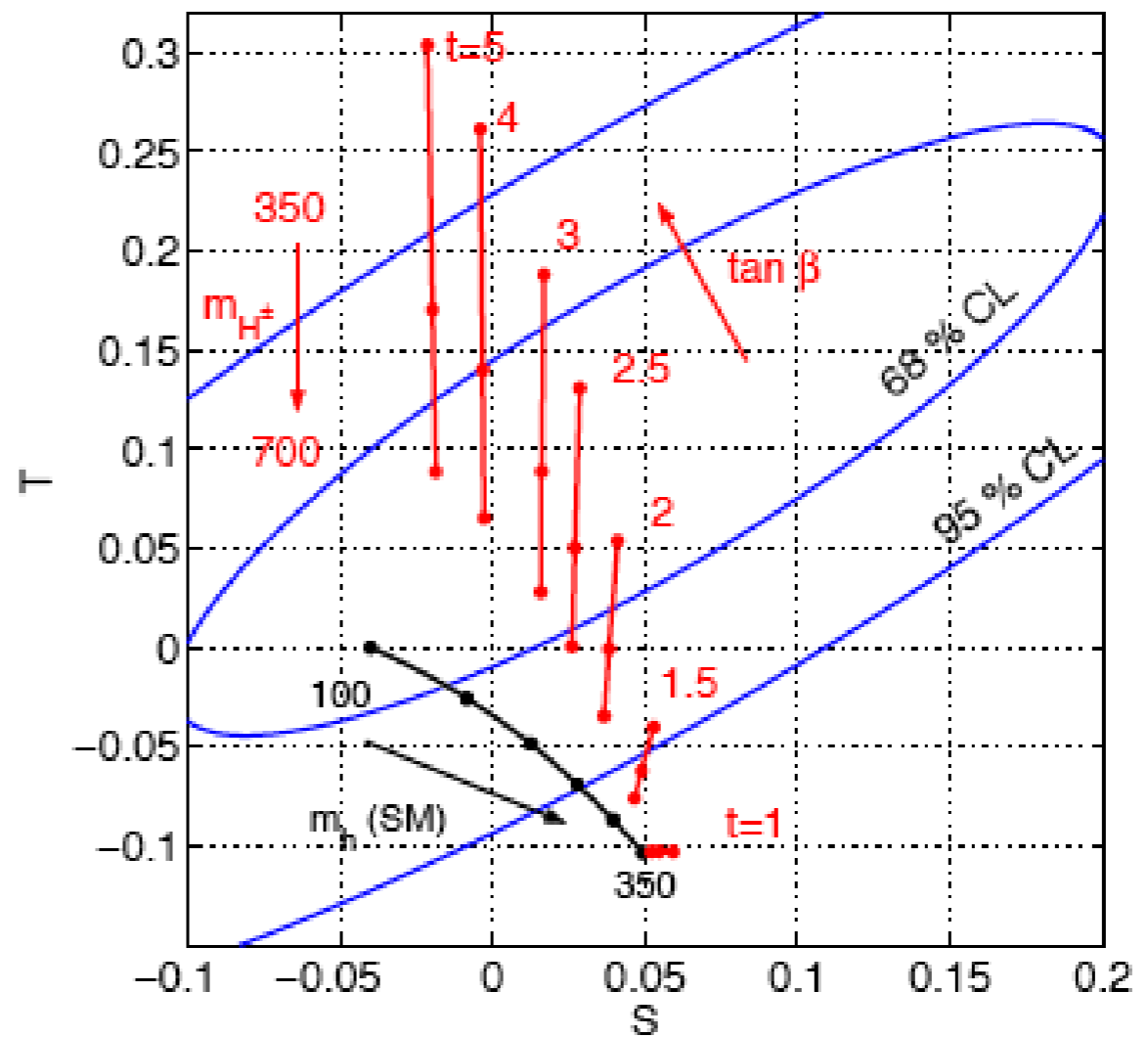
$$\lambda(G_F^{-1/2}) \approx 2$$

one loop effects but

$$\Delta T \propto \lambda^4$$

$\lambda \uparrow \Rightarrow m_h \uparrow$
compensated by $\Delta T \uparrow$

S and T from Higgs's

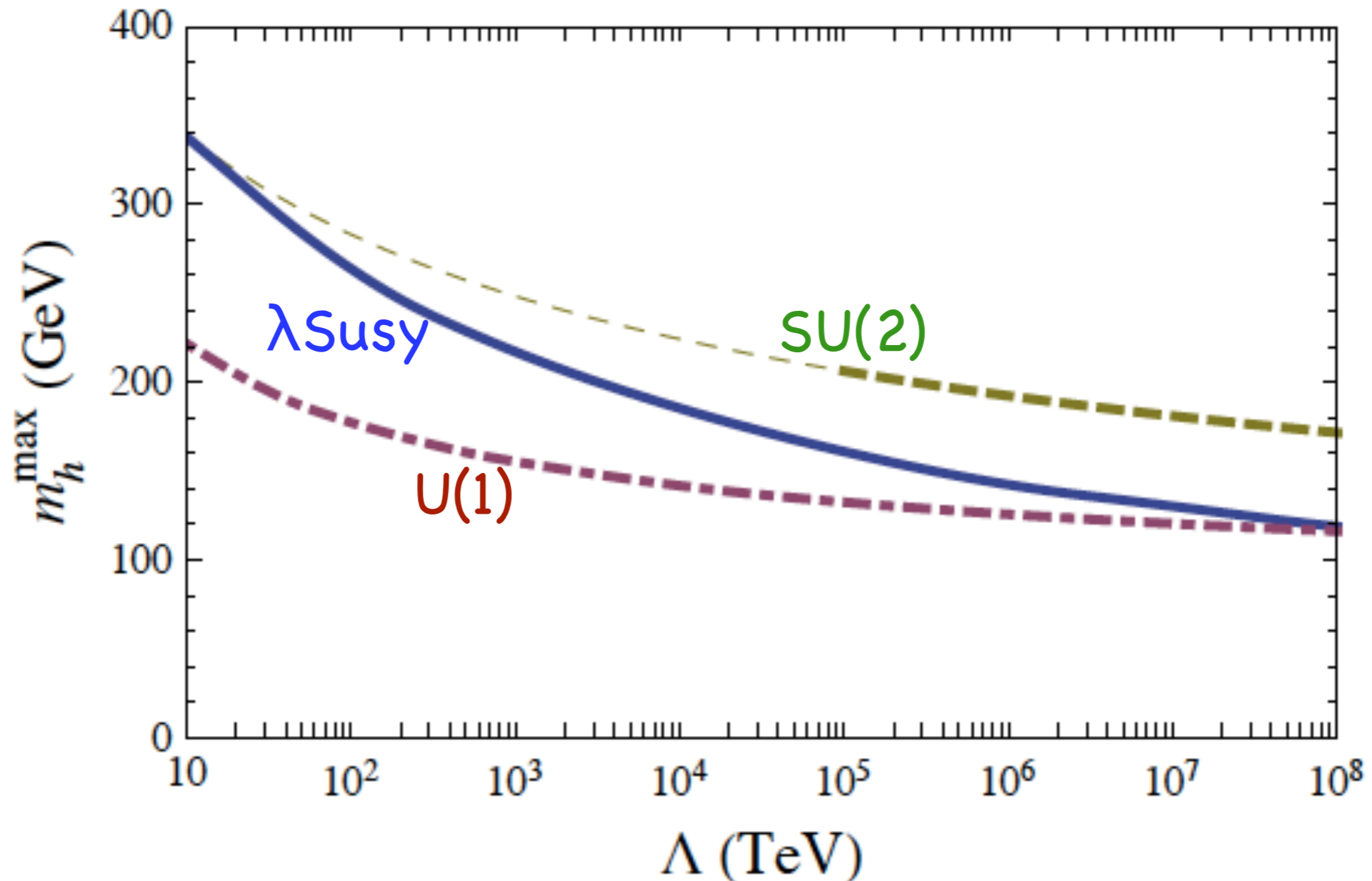


B, Hall, Nomura, Rychkov

The price to pay

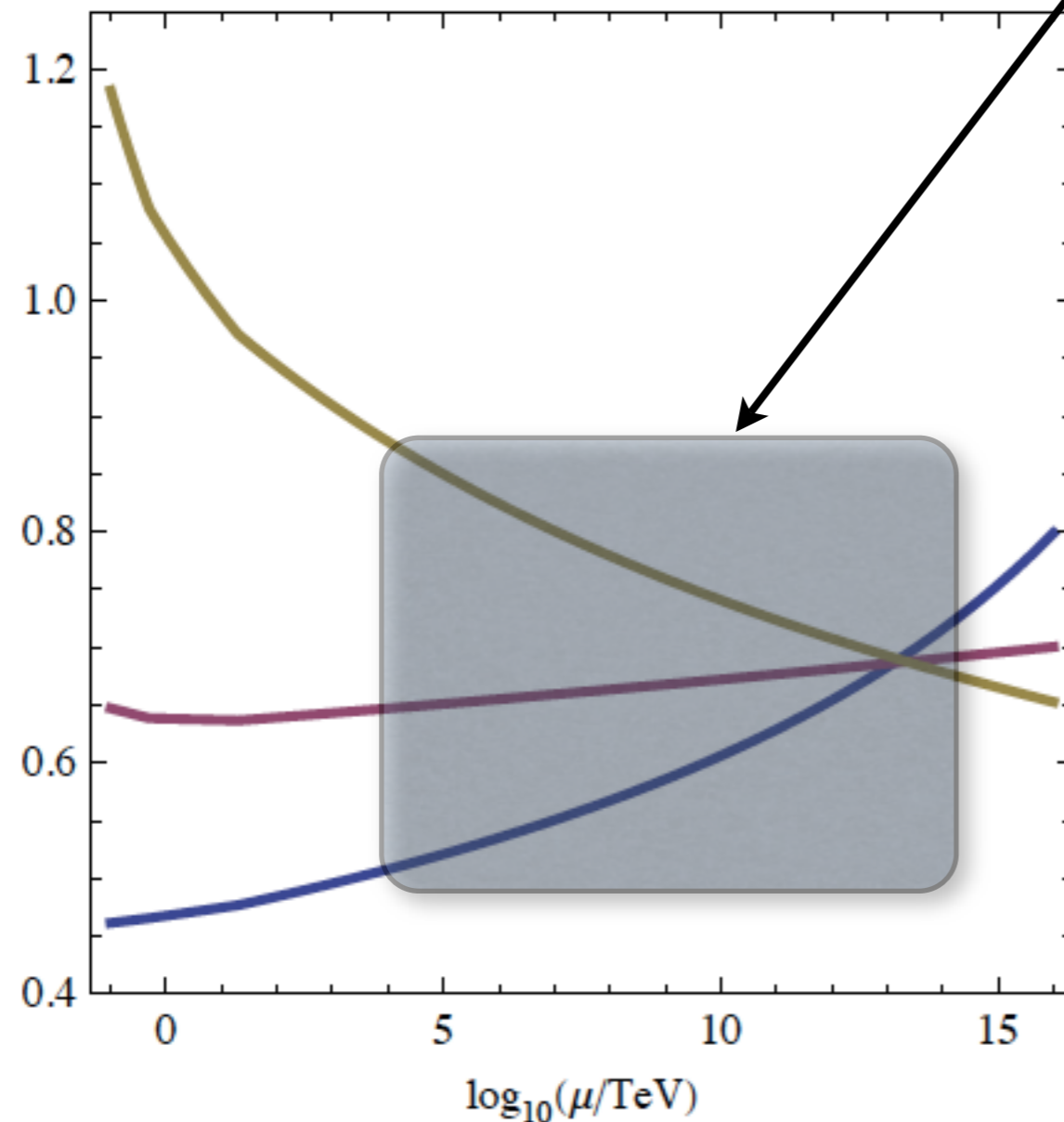
(big, according to standard wisdom, but...)

At a scale Λ some coupling starts blowing



unless some change of regime occurs before

What about gauge-coupling unification, then?



a grey box

It depends on what happens
at $M \gtrsim 10^4 \text{ TeV}$

At $M \approx 10^4 \text{ TeV}$:
 $g_1 \approx 0.5$, $g_2 \approx 0.7$, $g_3 \approx 0.85$
as opposed to
"precise" unification
at $M \approx 10^{13} \text{ TeV}$

an unbearable step backward?!

Flavour and CP violation

2000÷2010: The CKM picture quantitatively successful

⇒ Generic BSM physics highly constrained

Operator	Bounds on Λ in TeV ($c_{ij} = 1$)		Bounds on c_{ij} ($\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	9.8×10^2	1.6×10^4	9.0×10^{-7}	3.4×10^{-9}	$\Delta m_K; \epsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	1.8×10^4	3.2×10^5	6.9×10^{-9}	2.6×10^{-11}	$\Delta m_K; \epsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	1.2×10^3	2.9×10^3	5.6×10^{-7}	1.0×10^{-7}	$\Delta m_D; q/p , \phi_D$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	6.2×10^3	1.5×10^4	5.7×10^{-8}	1.1×10^{-8}	$\Delta m_D; q/p , \phi_D$
$(\bar{b}_L \gamma^\mu d_L)^2$	5.1×10^2	9.3×10^2	3.3×10^{-6}	1.0×10^{-6}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	1.9×10^3	3.6×10^3	5.6×10^{-7}	1.7×10^{-7}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_L \gamma^\mu s_L)^2$		1.1×10^2		7.6×10^{-5}	Δm_{B_s}
$(\bar{b}_R s_L)(\bar{b}_L s_R)$		3.7×10^2		1.3×10^{-5}	Δm_{B_s}

Isidori, Nir, Perez
2010

*especially with new degrees of freedom
carrying flavour at the Fermi scale*

What about supersymmetry?

A - The prevailing answer:

$$U(3)_{\hat{Q}} \times U(3)_{\hat{u}} \times U(3)_{\hat{d}} \quad \text{only broken by} \quad Y = (3, \bar{3})$$
$$\Rightarrow m_{\tilde{q}}^2 = m^2(\mathbf{1} + aY^+Y), \quad A = A_0Y$$

Goes a long way in addressing the flavour problem:

Under mild further hypotheses:

$$V_{CKM} \text{ as the only mixing matrix in } d_L \rightarrow V_{CKM}d_L \text{ and}$$
$$\mathcal{A}_{\alpha\beta}^{\Delta F=2,1} = \mathcal{A}_{\alpha\beta}^{\Delta F=2,1}|_{SM}(1 + \epsilon^{\Delta F=2,1}) \quad \text{with } \alpha, \beta = d, s, b$$

(often called "Minimal Flavour Violation")

but for flavour-blind CP-phases

$$d_e \Rightarrow m_{\tilde{l}_1} \gtrsim 4 \text{ TeV} (\sin \phi_\mu \tan \beta)^{1/2}$$
$$d_n \Rightarrow m_{\tilde{q}_1} \gtrsim 3 \text{ TeV} (\sin \phi_\mu \tan \beta)^{1/2} \quad \text{or} \quad 3 \text{ TeV} (\sin \phi_A \frac{A_0}{m_{\tilde{q}}})^{1/2}$$

B - Our proposal:

- 1 - Only squarks coupled to H by Y_{top} light: $\tilde{t}_L, \tilde{t}_R, \tilde{b}_L$
- 2 - With Y_u switched on, but not Y_d , individual flavours conserved

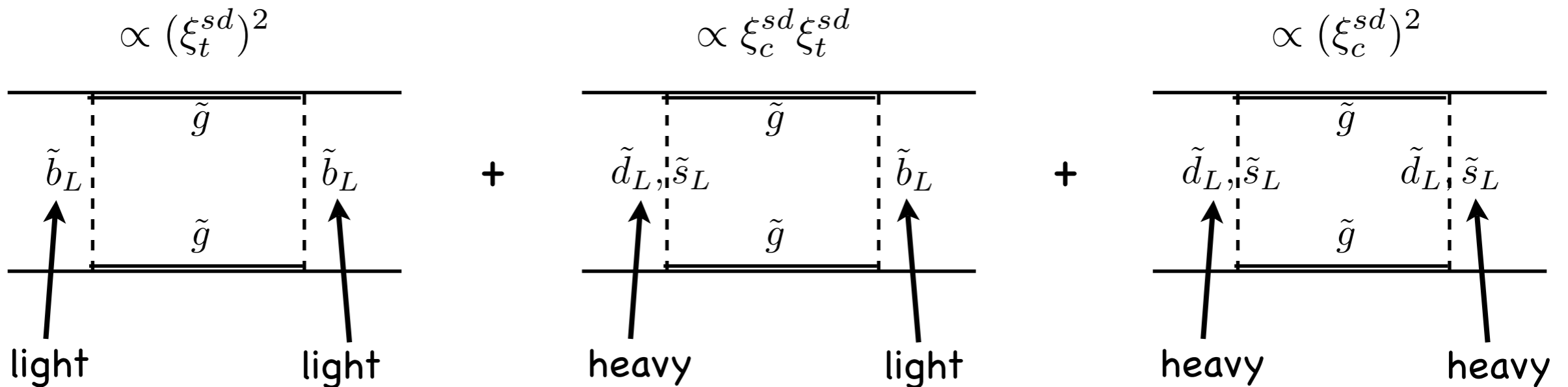
$$U(1)_{\tilde{B}_1} \times U(1)_{\tilde{B}_2} \times U(1)_{\tilde{B}_3} \times U(3)_{d_R} \quad \text{only broken by } Y_{d_i} = (\mathbf{1}_{B_i}, \mathbf{3})$$

\Rightarrow As in A, V_{CKM} still the only mixing matrix from $d_L \rightarrow V_{CKM}d_L$, without degenerate \tilde{Q}_i, \tilde{u}_i

general structure of susy effects, e.g., in $\Delta S=2$:

$$\xi_i^{sd} = V_{is}V_{id}^*, \quad i = u, c, t$$

$$\propto (\xi_c^{sd})^2$$

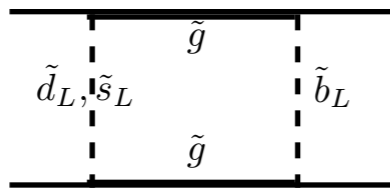


\Rightarrow Effective Minimal Flavour Violation, if "lh" and "hh" negligible

Rigorous (lower) bounds on $m_{\tilde{f}_{1,2}}$

Dominant effects:

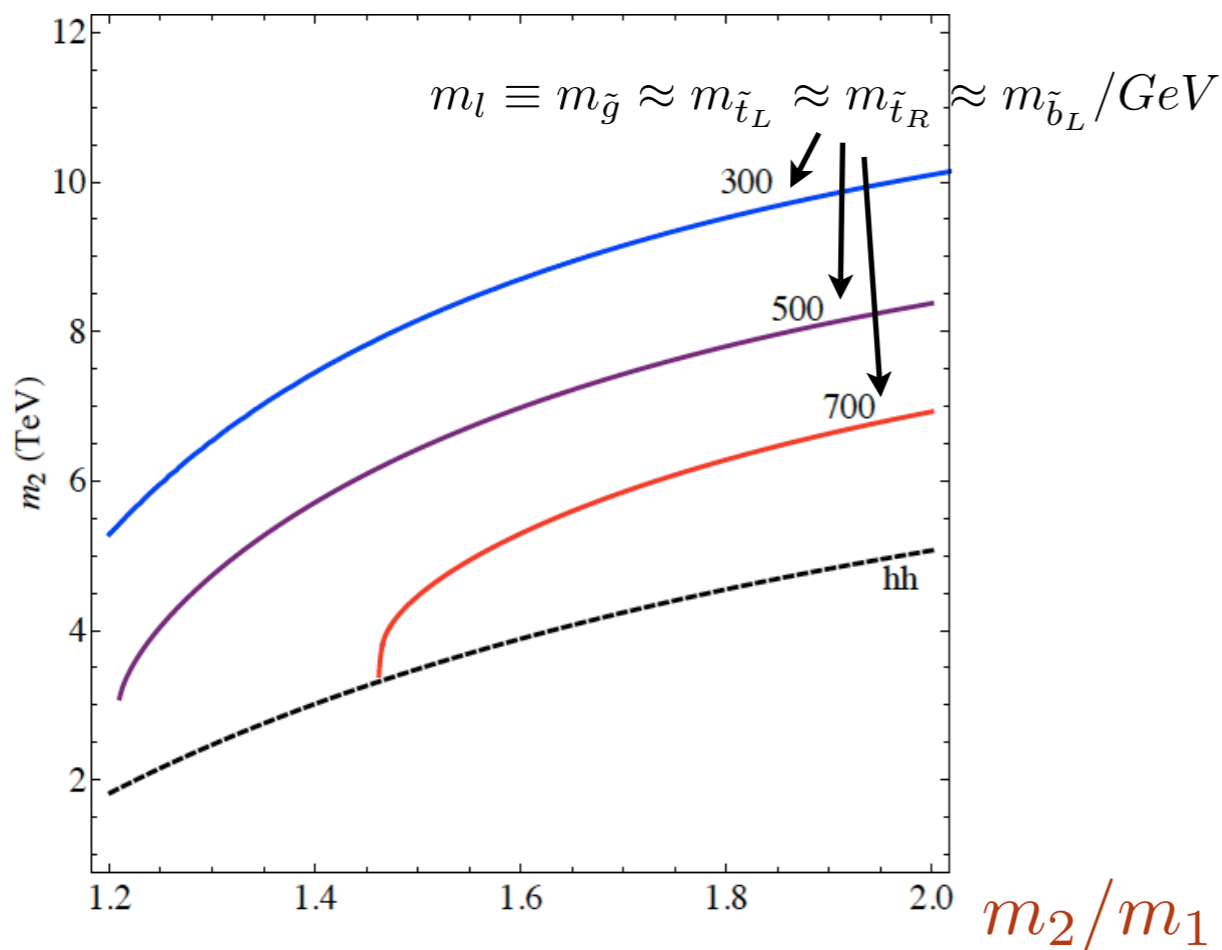
Im($\Delta S=2$) from lh exchange



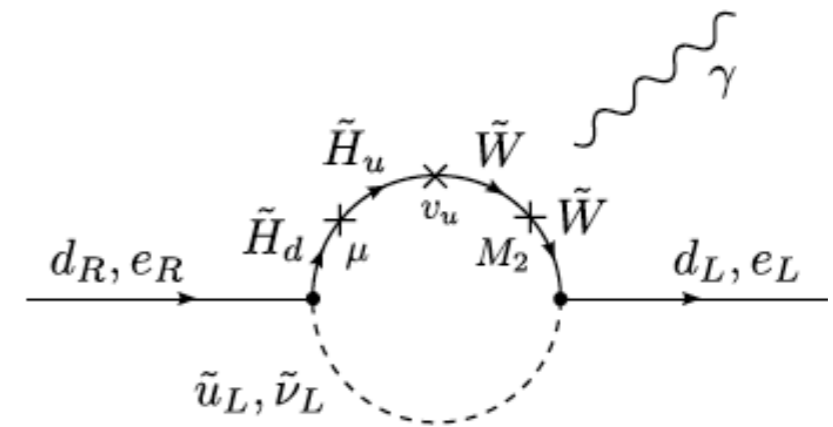
EDM's

only one diagram not suppressed by high powers of m_h or small angles

m_2 (TeV)



$$m_i \equiv m_{\tilde{u}_{R_i}} \approx m_{\tilde{u}_{L_i}} \approx m_{\tilde{d}_{L_i}}, \quad i = 1, 2$$



$$d_e \Rightarrow m_{\tilde{l}_1} \gtrsim 4 \text{ TeV} (\sin \phi_\mu \tan \beta)^{1/2}$$

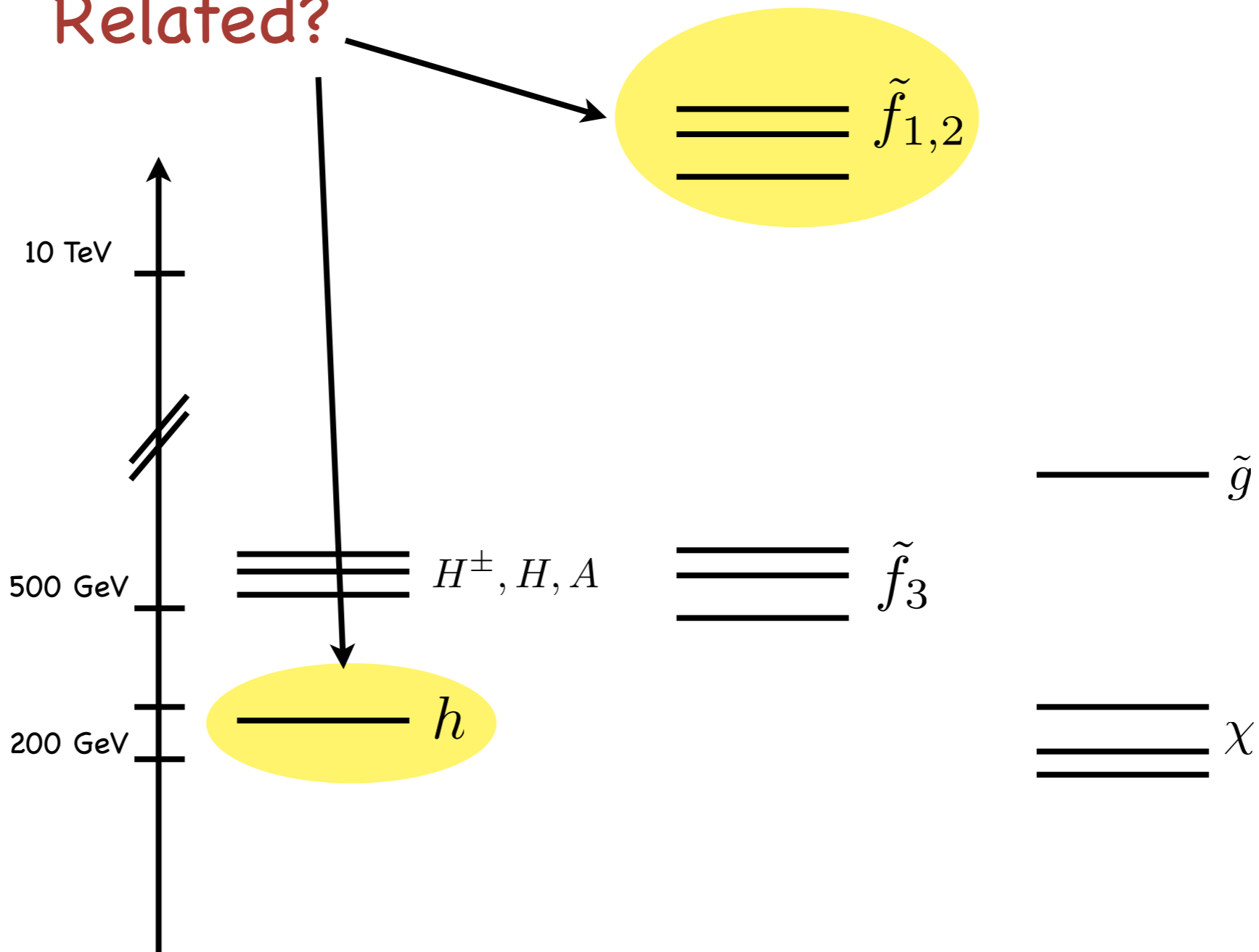
$$d_n \Rightarrow m_{\tilde{q}_1} \gtrsim 3 \text{ TeV} (\sin \phi_\mu \tan \beta)^{1/2}$$

\Rightarrow Need $m_{\tilde{f}_{1,2}} \gtrsim 10 \text{ TeV}$ to be on the safe side

A non-standard Supersymmetric Spectrum

Motivated? Yes

Related?



⇒ the Higgs boson mass problem
⇒ the flavour problem

A matter of naturalness, once again

the Higgs mass problem

\Leftrightarrow

$$\frac{m_{\tilde{t}}^2}{m_h^2} \frac{\delta m_h^2}{\delta m_{\tilde{t}^2}}$$

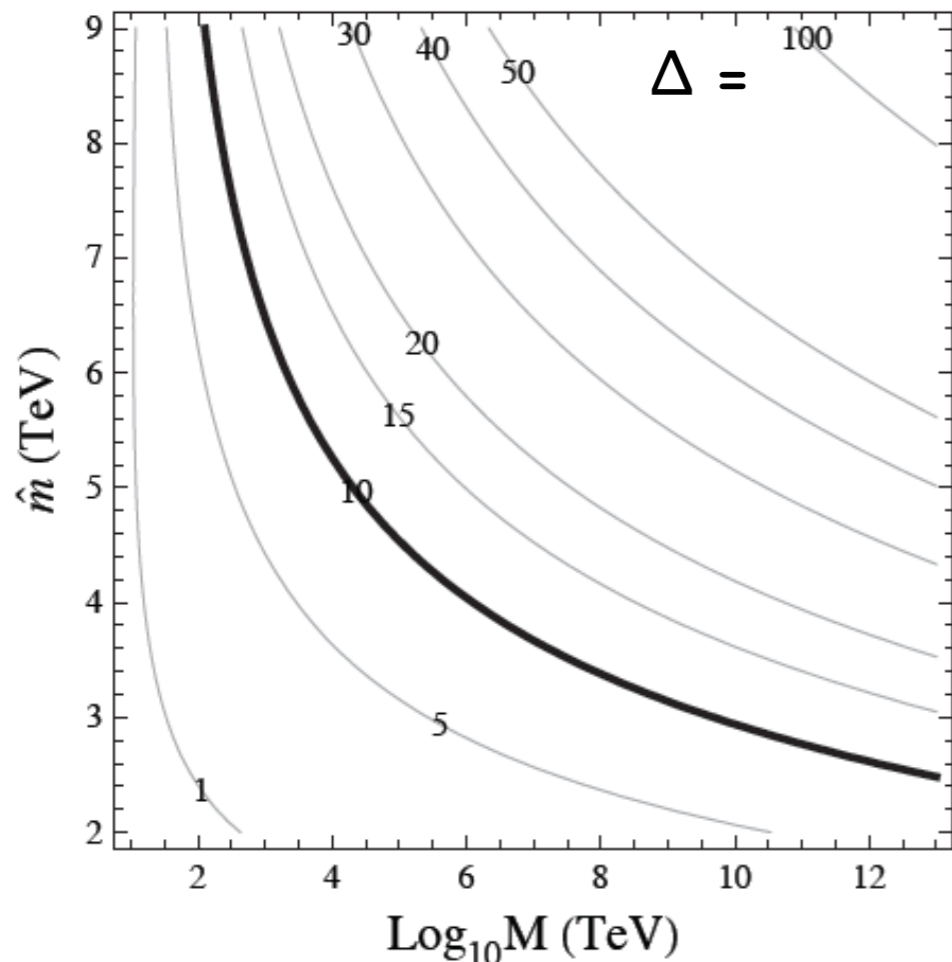
the flavour problem

\Leftrightarrow

$$\frac{m_{\tilde{f}_{1,2}}^2}{m_h^2} \frac{\delta m_h^2}{\delta m_{\tilde{f}_{1,2}}^2}$$

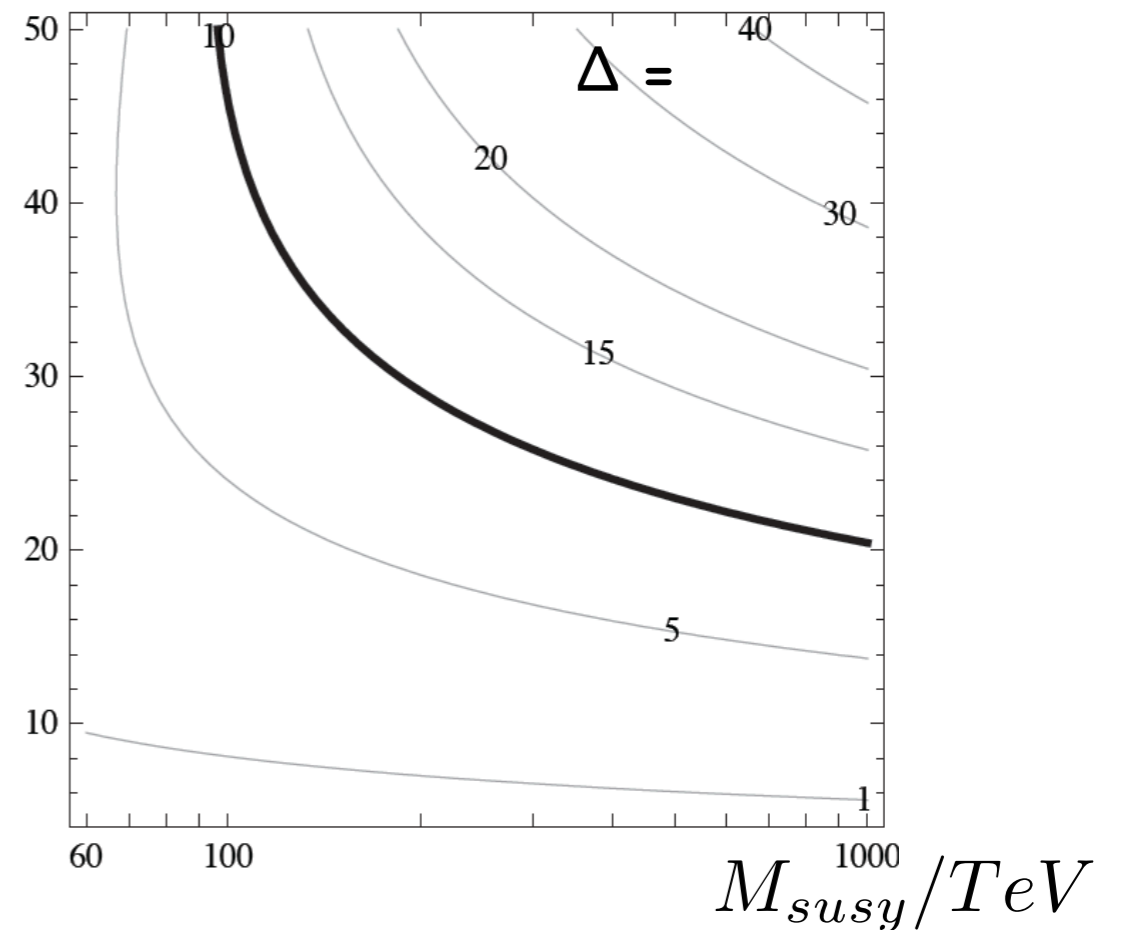
Both problems ameliorated by a heavier m_h

MSSM $m_h^{max} = 91 \text{ GeV}$



λ Susy $m_h^{max} = 250 \text{ GeV}$

$m_{\tilde{f}_{1,2}}/TeV$

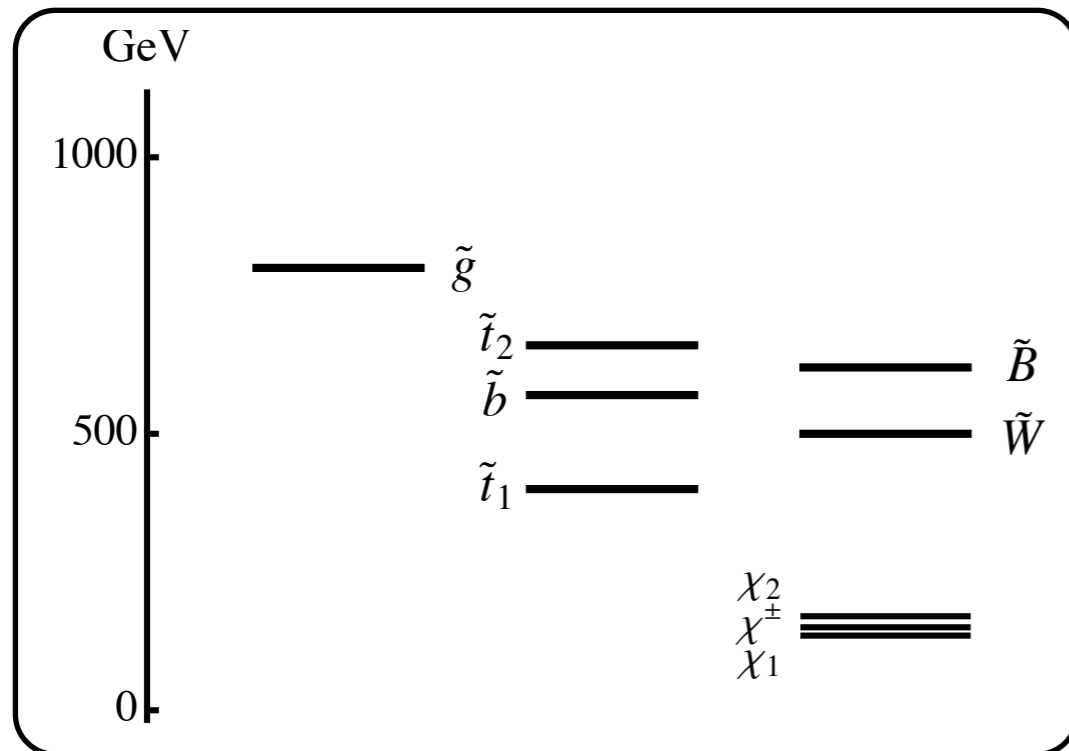


Phenomenological consequences

- ★ gluino pair production and decays
into top/bottom-rich final states
- ★ a largely unconventional Higgs sector
(non MSSM-like)
- ★ Dark Matter: relic abundance and detection
affected
- ★ Flavour signals in EDM's and
direct CP violation in b-physics (at low $\tan\beta$)

4.1 Gluino pair production and decays

A typical configuration



More in general

$$m_{\tilde{g}} = 400 \div 1800 \text{ GeV}$$

$$m_{\tilde{t}_1} < m_{\tilde{t}_2} < 800 \text{ GeV} \quad \theta_t = 0 \div \pi/2$$

$$\mu = 100 \div 400 \text{ GeV}$$

$$M_1, M_2 = 100 \div 500 \text{ GeV}$$

(s-lepton masses almost always unimportant)

3 relevant semi-inclusive BR's

$$\tilde{g} \rightarrow t\bar{t}\chi$$

$$\tilde{g} \rightarrow t\bar{b}\chi \quad (\bar{t}b\chi)$$

$$\tilde{g} \rightarrow b\bar{b}\chi$$

with $B_{tt} + 2B_{tb} + B_{bb} \approx 1$

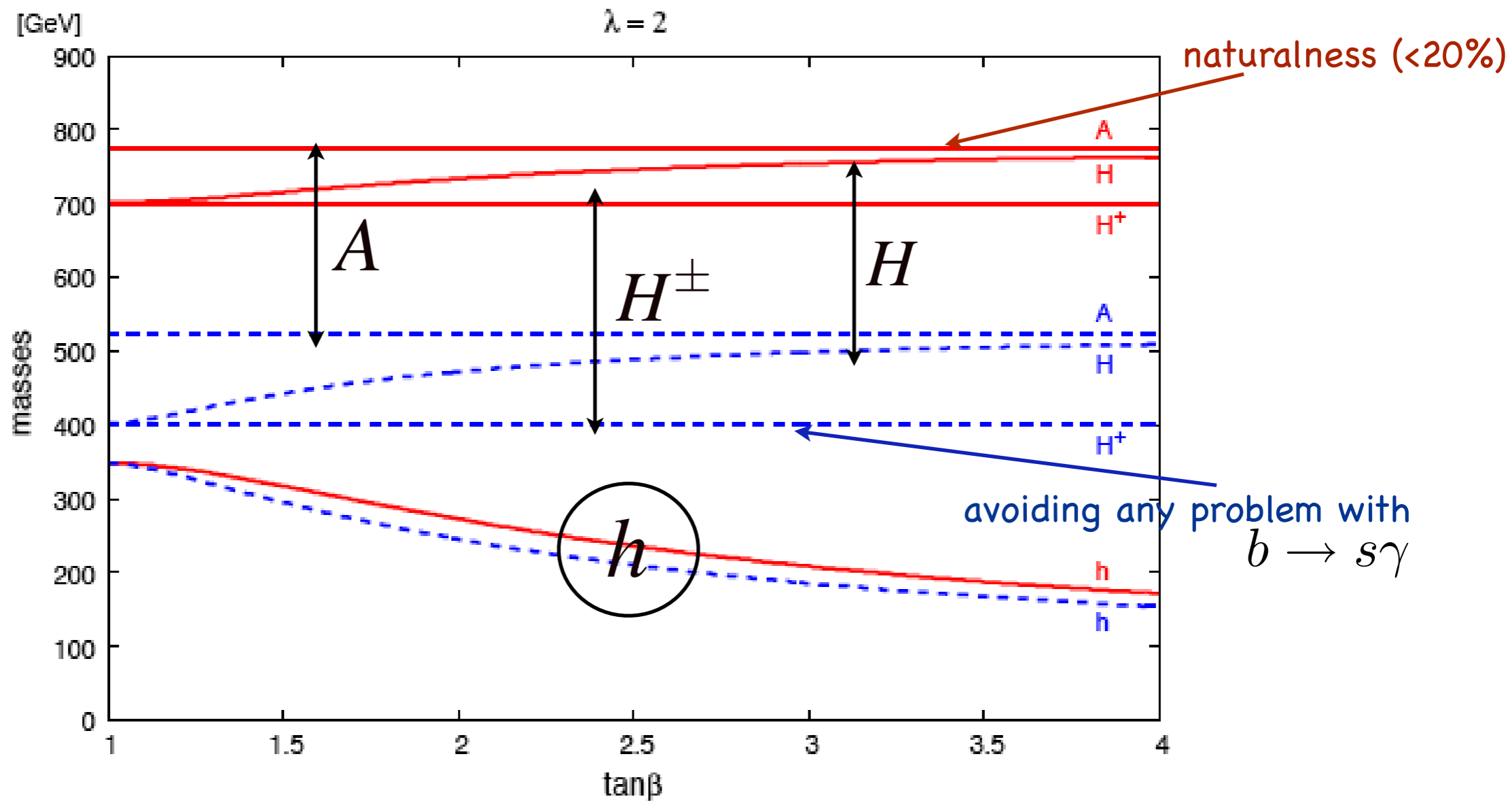
and $\chi = \chi_{LSP} + W, Z's$

⇒ multi top events

⇒ spherical events

⇒ 4 b's always

4.2 A largely unconventional Higgs sector



$h \rightarrow ZZ \rightarrow l^+l^- l^+l^-$ or even $h \rightarrow aa \rightarrow \tau\tau bb$ with a large rate

$H \rightarrow hh \rightarrow 4V \rightarrow l^+l^- 6j$ $BR \propto \lambda^2$ much larger than normal

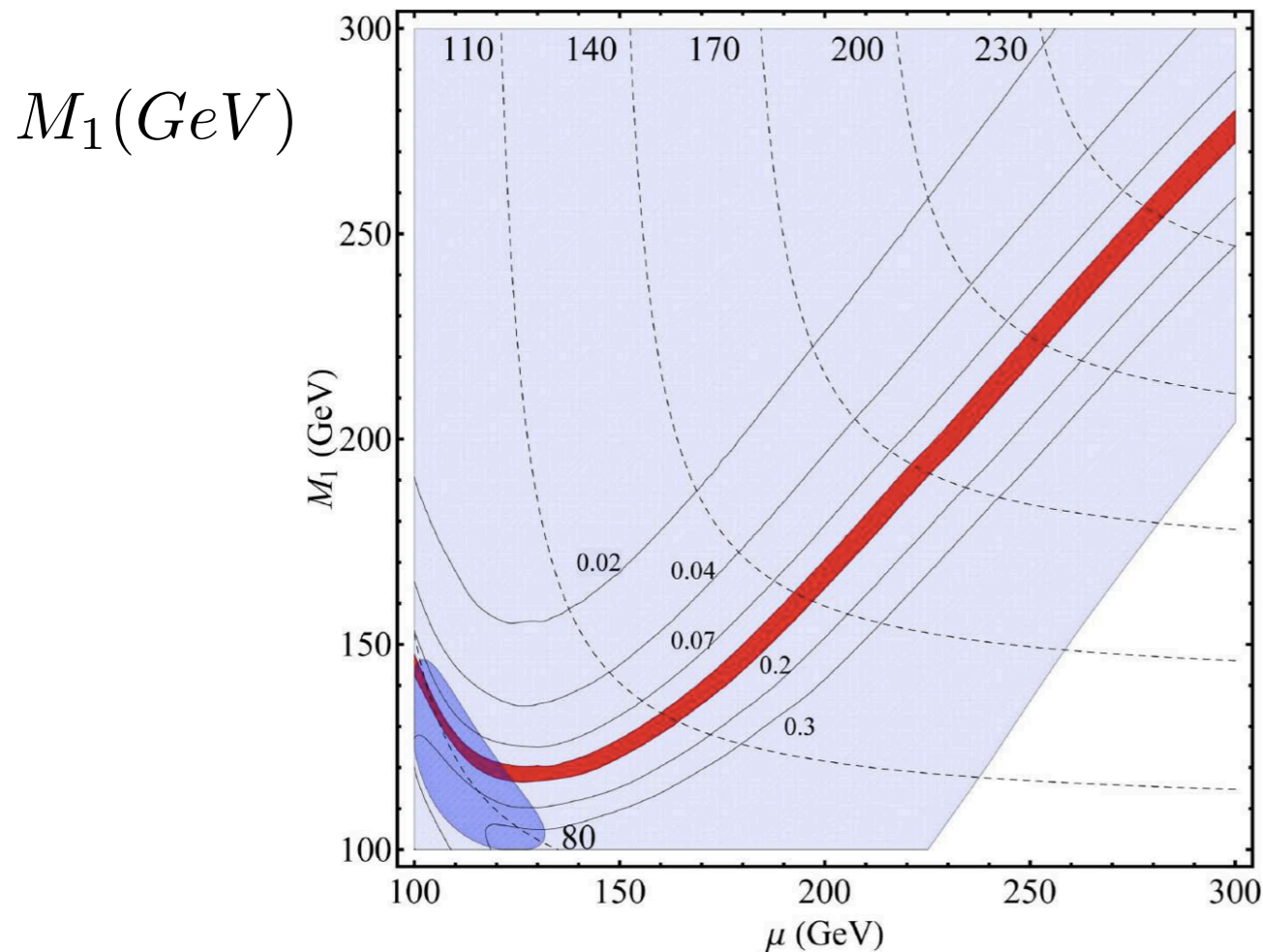
$A \rightarrow hZ \rightarrow VV Z \rightarrow l^+l^- 4j$

4.3 Dark Matter: relic abundance and detection

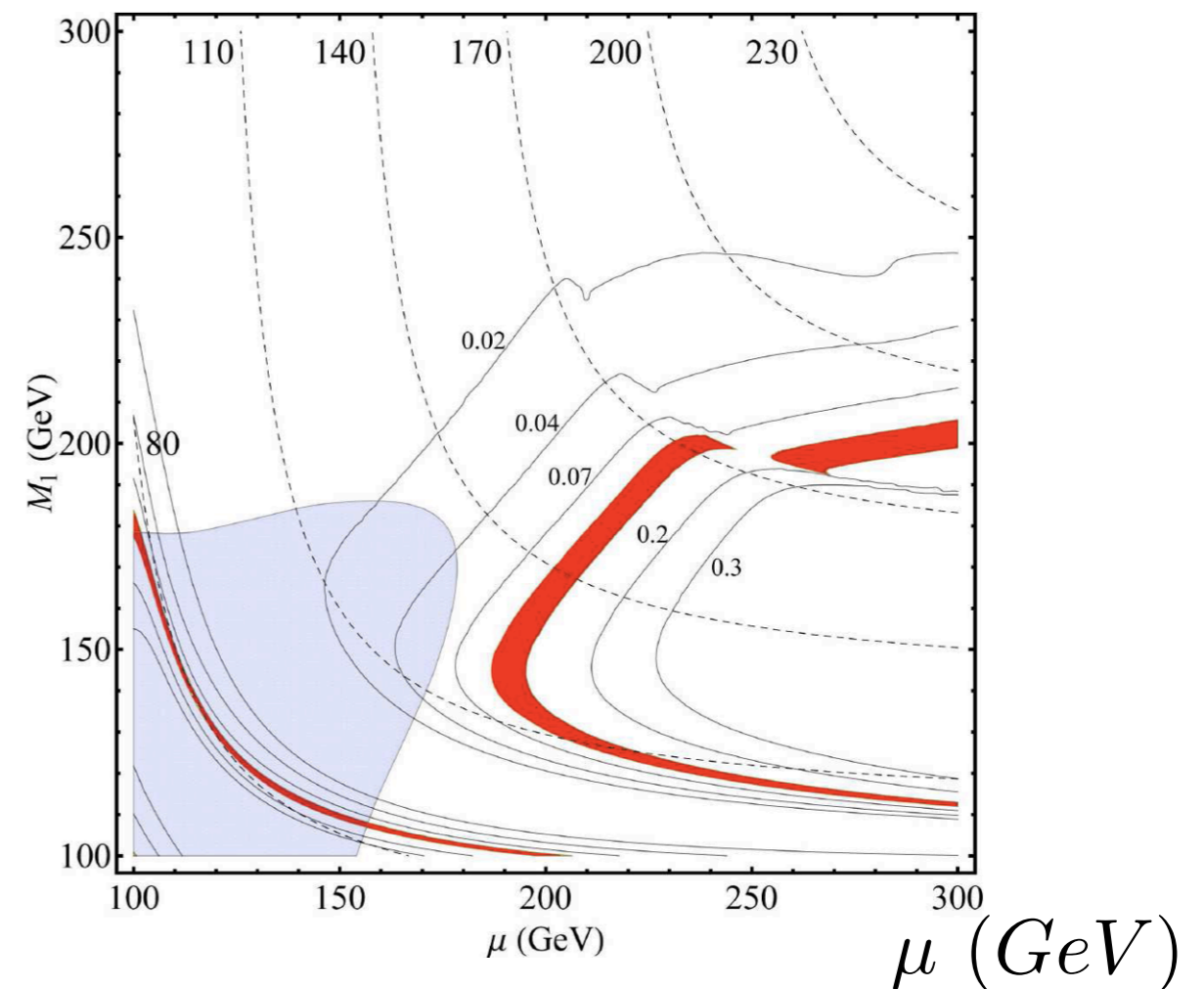
Relic abundance:

A strong effect of the s-channel heavier Higgs exchange
 No "well-temperament"

M_2 large



MSSM $m_h = 120$ GeV



λ Susy: $m_h = 200$ GeV

Direct detection affected by $\sigma \propto \frac{1}{m_h^4}$

and different mixing
 dark blu: CDMS now
 light blu: "XENON100"

Conclusions

- ★ The elusiveness of supersymmetry so far suggests giving consideration to a **Non Standard Supersymmetric Spectrum** where:

$$m_h = 200 \div 250 \text{ GeV}$$

$$m_{\tilde{f}_{1,2}} \gtrsim 10 \text{ TeV} \gg m_{\tilde{f}_3}$$

- ★ **Naturally** possible at least in λ Susy
(although with canonical unification under threat)

- ★ Phenomenology (non MSSM-like):

$$\Rightarrow \tilde{g} \rightarrow t\bar{t}\chi, t\bar{b}\chi (\bar{t}b\chi), b\bar{b}\chi$$

$$\Rightarrow h \rightarrow ZZ, aa; H \rightarrow hh, hhh$$

$$\Rightarrow \text{DM: no "well-temperated"} \\ \text{Direct Detection affected}$$

$$\Rightarrow \text{CP-violation signals in EDM's and b-physics}$$

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \mathcal{L}_{eff}^{NP}$$

$$\mathcal{L}_{eff}^{NP} = \sum_i \frac{c_i}{\Lambda_{NP}^2} \mathcal{O}_i$$

Taking $c_i = \pm 1$ and considering one operator at a time

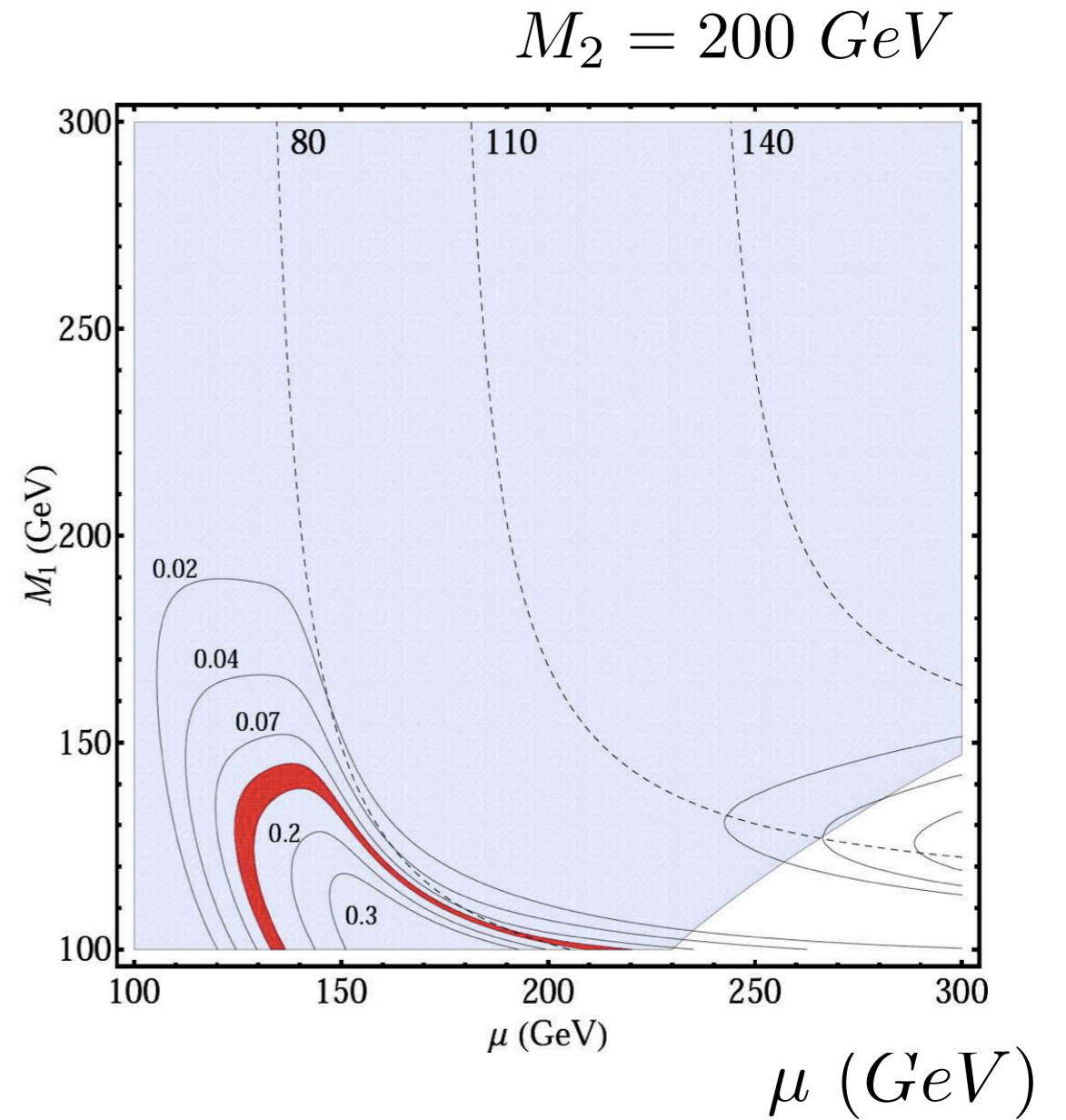
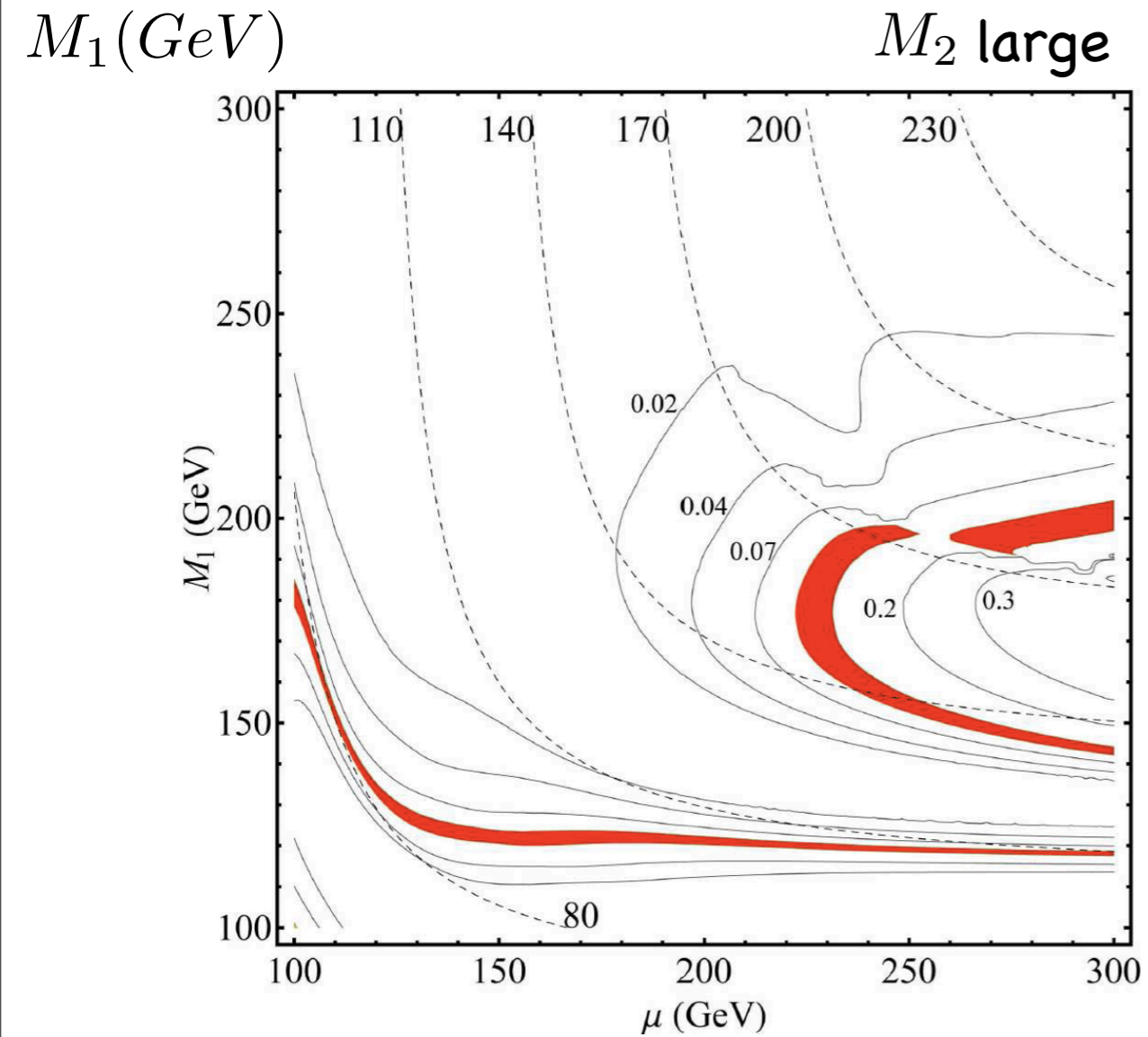
$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \mathcal{O}/\Lambda^2$$

	operator \mathcal{O}	affects	constraint on Λ
	$\frac{1}{2}(\bar{L}\gamma_\mu\tau^a L)^2$	μ -decay	10 TeV
	$\frac{1}{2}(\bar{L}\gamma_\mu L)^2$	LEP 2	5 TeV
T \rightarrow	$ H^\dagger D_\mu H ^2$	θ_W in M_W/M_Z	5 TeV
S \rightarrow	$(H^\dagger \tau^a H)W_{\mu\nu}^a B_{\mu\nu}$	θ_W in Z couplings	8 TeV
	$i(H^\dagger D_\mu \tau^a H)(\bar{L}\gamma_\mu \tau^a L)$	Z couplings	10 TeV
	$i(H^\dagger D_\mu H)(\bar{L}\gamma_\mu L)$	Z couplings	8 TeV
\Rightarrow	$H^\dagger (\bar{D}\lambda_D \lambda_U \lambda_U^\dagger \gamma_{\mu\nu} Q) F^{\mu\nu}$	$b \rightarrow s\gamma$	10 TeV
\Rightarrow	$\frac{1}{2}(\bar{Q}\lambda_U \lambda_U^\dagger \gamma_\mu Q)^2$	B mixing	10 TeV

1 σ -bounds \oplus a light Higgs

More conservatively: $\Lambda > \sim 5$ TeV

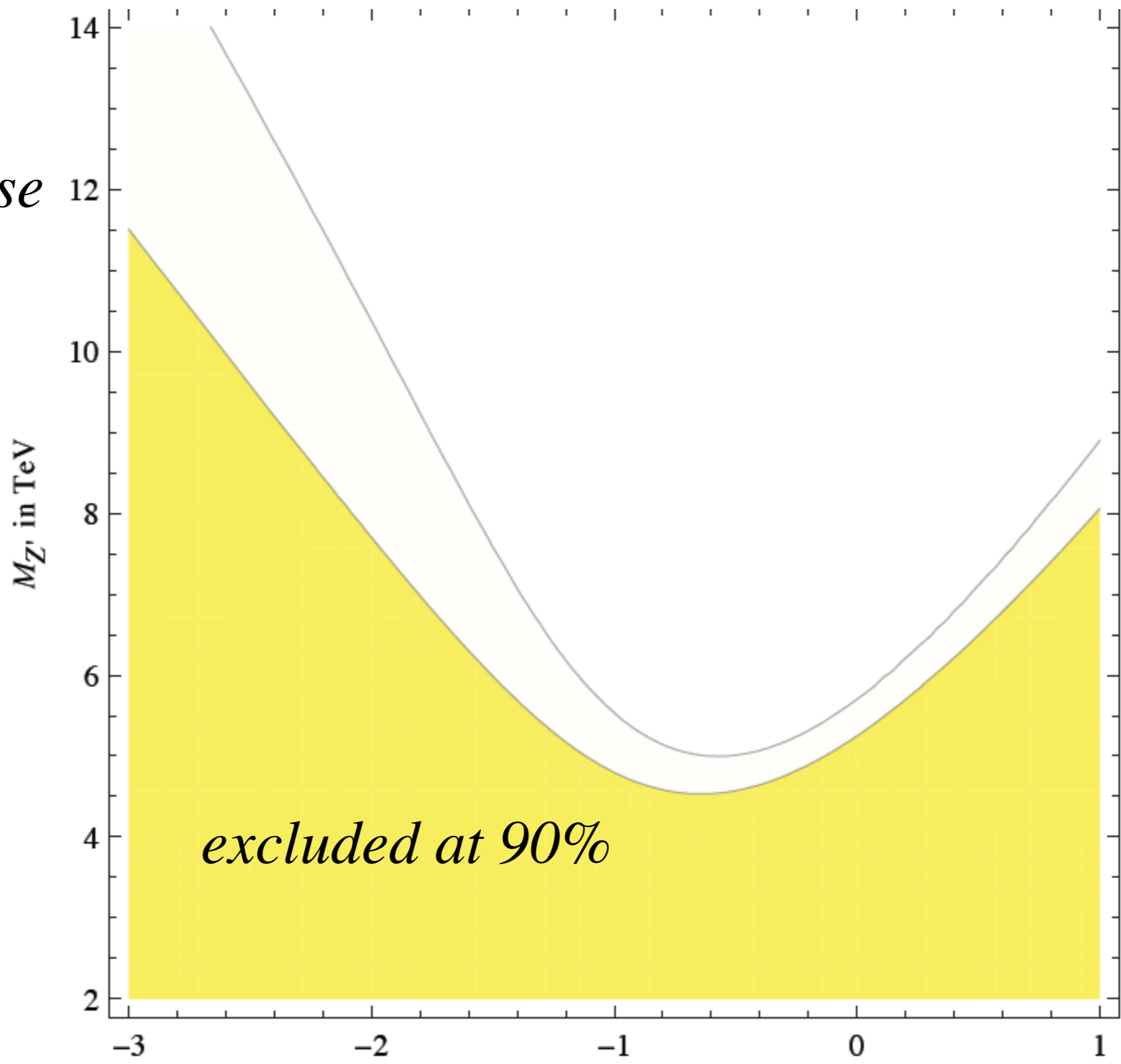
4.3 Dark Matter: relic abundance and detection



λ Susy: $m_h = 250$ GeV

dark blu: CDMS now
light blu: "XENON100"

extra U(1) case



EWSB: "weak" or "strong"?

"weak"

a relatively light Higgs boson exists
perturbativity extended \rightarrow high E (M_{GUT}, M_{Pl})
perhaps (probably) embedded in susy
gauge couplings unify

"strong"

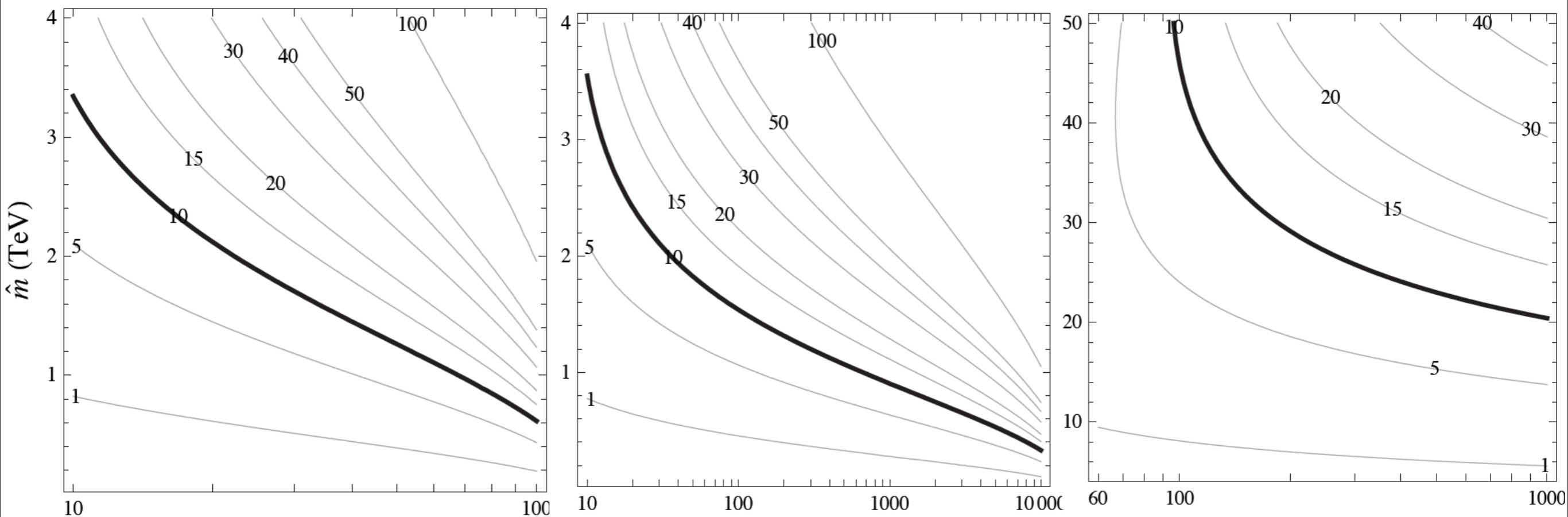
EWSB related to new forces, new degrees of freedom
or even new dimensions opening up in the TeVs
perturbativity lost in the multi-TeV range
high E extrapolation highly uncertain

Naturalness bounds

U(1) $m_h^{max} = 180 \text{ GeV}$

SU(2) $m_h^{max} = 250 \text{ GeV}$

λ Susy $m_h^{max} = 250 \text{ GeV}$



M_{susy}/TeV

$$\frac{\partial m_h^2}{\partial t} \approx \frac{\alpha_X^2}{16\pi^2} \tilde{m}_{1,2}^2$$

\hat{m} is $m_{\tilde{f}_{1,2}}$ with vertical degeneracy among \tilde{f} 's at M_{susy}

$\Rightarrow m_{\tilde{f}_{1,2}} \gtrsim 20 \text{ TeV}$ OK in λ Susy at $M = 100 \div 1000 \text{ TeV}$

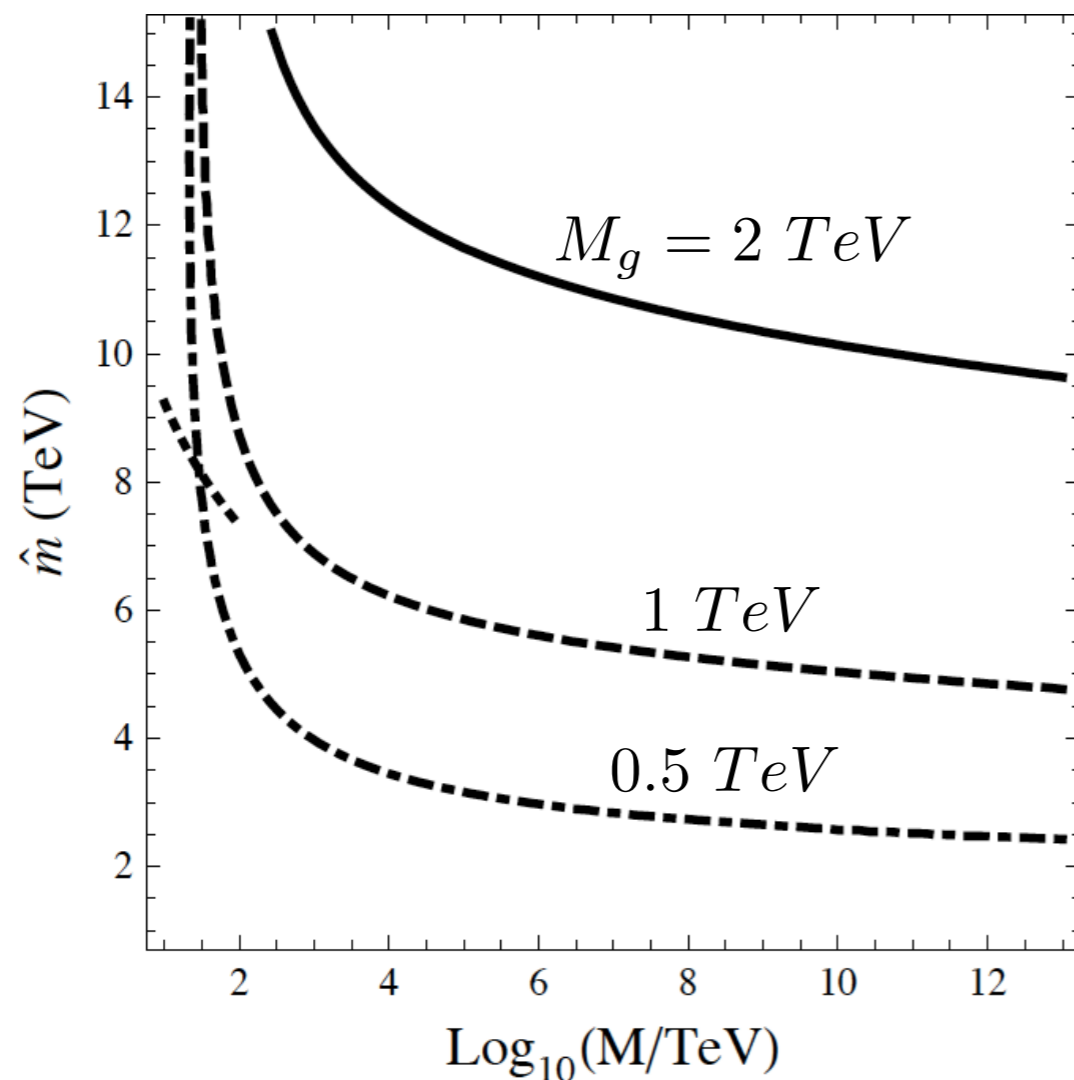
Colour/em conservation

Arkani-Hamed, Murayama

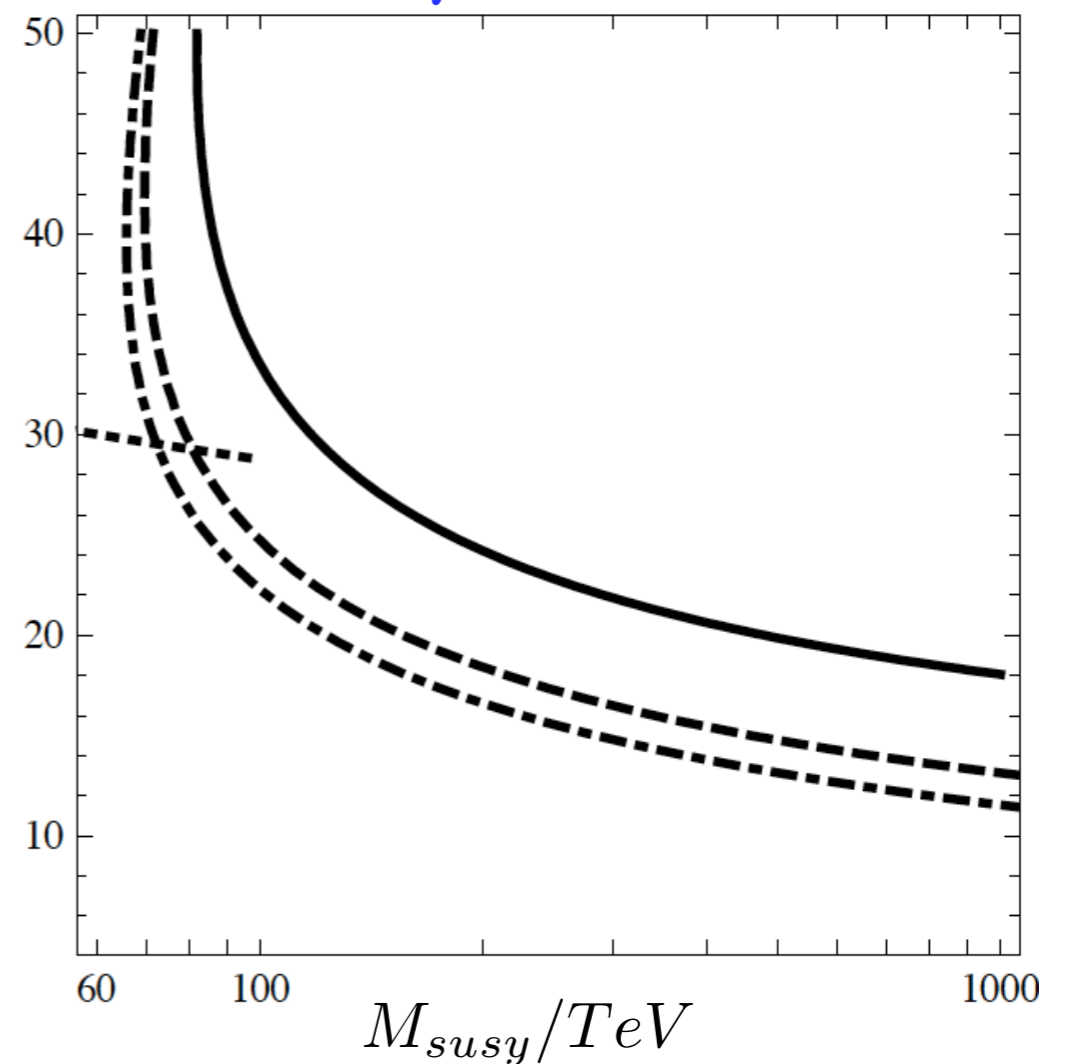
$$\frac{dm_{\tilde{Q}_3}^2}{d \log \mu} \approx -\frac{\alpha_S}{4\pi} M_g^2 + \frac{\alpha_S^2}{16\pi^2} \hat{m}_{1,2}^2$$

Require $m_{\tilde{Q}_3}^2 > 0$ for natural $m_{\tilde{Q}_3}^2(M)$

MSSM $m_h^{max} = 90 \text{ GeV}$



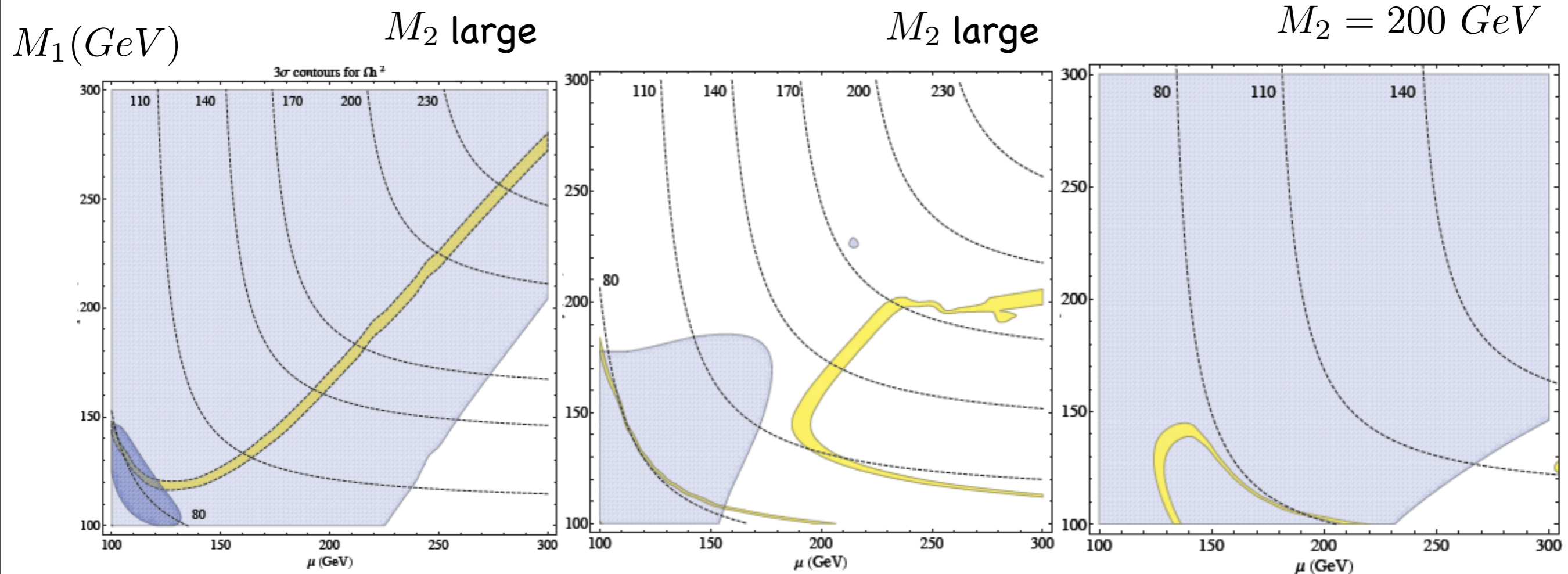
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4.3 Dark Matter: relic abundance and detection

Relic abundance:

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 No need of "well-temperament"



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