



ULTIMATE POLARIZATION FOR ILC

Alexander Mikhailichenko

Cornell University, LEPP, Ithaca, NY 14853

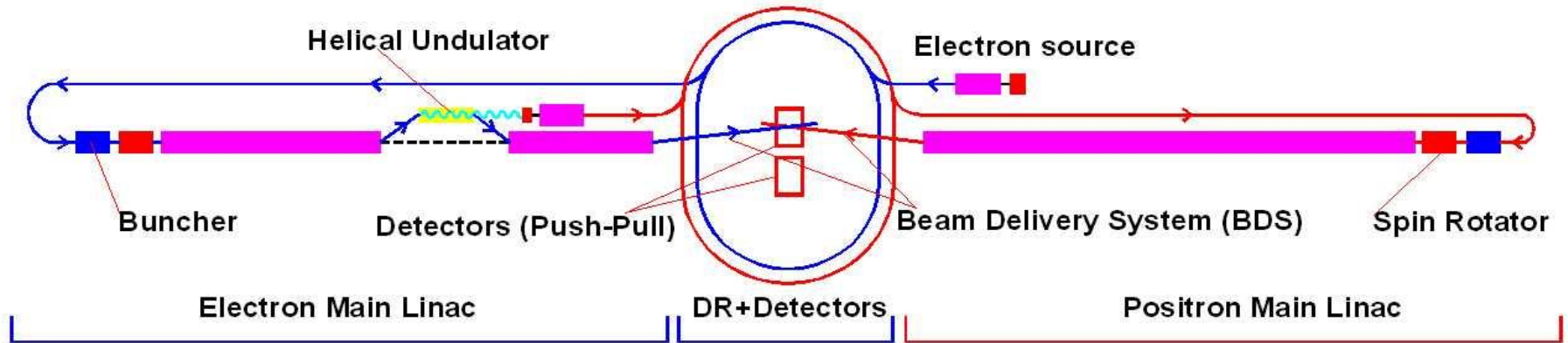
Workshop on High Precision Measurements of Luminosity at Future Linear Colliders and Polarization of Lepton Beams

October 3-5, 2010

Tel-Aviv University, Tel-Aviv, Israel

POSITRON SOURCE FOR ILC

The undulator scheme of positron production has been chosen as a baseline for ILC

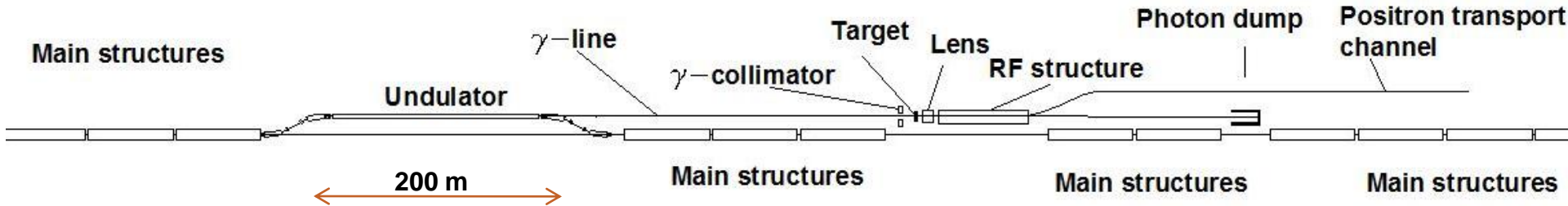


Main advantage of this scheme is that it allows **POLARIZED** positron production

In principle, positrons could be generated by positrons, so the linacs become independent

Positron source is a complex system which includes a lot of different components and each of these components could be a subject of a separate talk

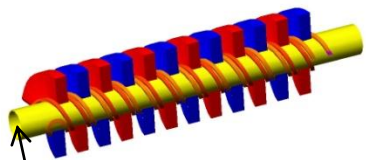
MORE DETAILED VIEW



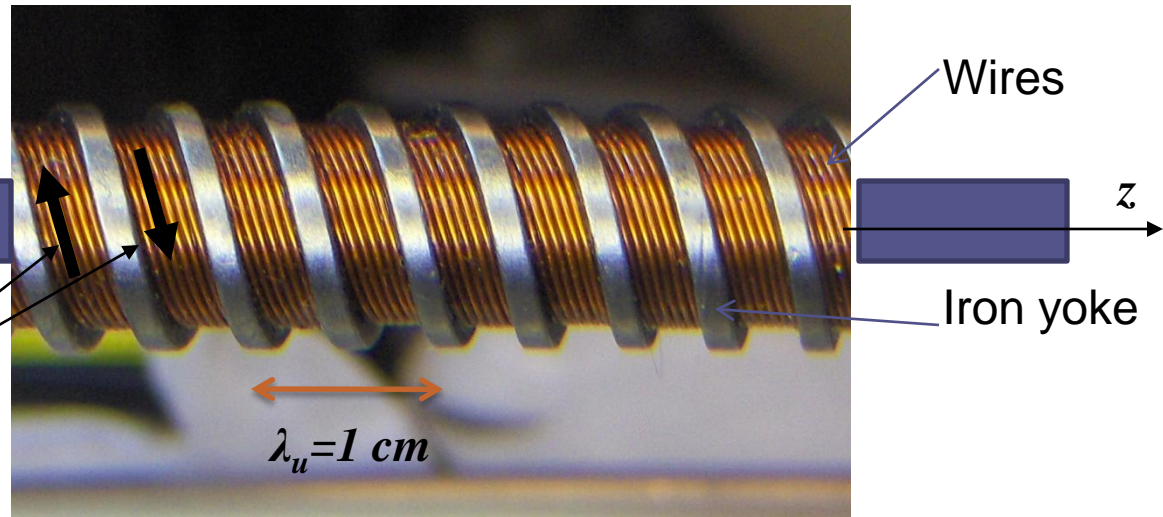
Helical undulator is a device for generation magnetic field of a type

$$\vec{H}_\perp(z) = \vec{e}_x H_{xm} \cos \frac{2\pi z}{\lambda_u} + \vec{e}_y H_{ym} \sin \frac{2\pi z}{\lambda_u}$$

Radius of particle's helix $a \cong eH_\perp \lambda_u^2 / mc^2 \gamma$



Vacuum tube inside



Direction of currents

$$\lambda_u = 1 \text{ cm}$$

Fragment from publication of Balakin-Mikhailichenko, Budker INP 79-85, Sept. 13, 1979.

Circularly polarized photons are produced in helical fields of minimal period. Much more interesting is to obtain such fields with the help of the usual helical static fields and the electromagnetic waves. It may well be that the method of gamma production in helical crystals can be useful in future.

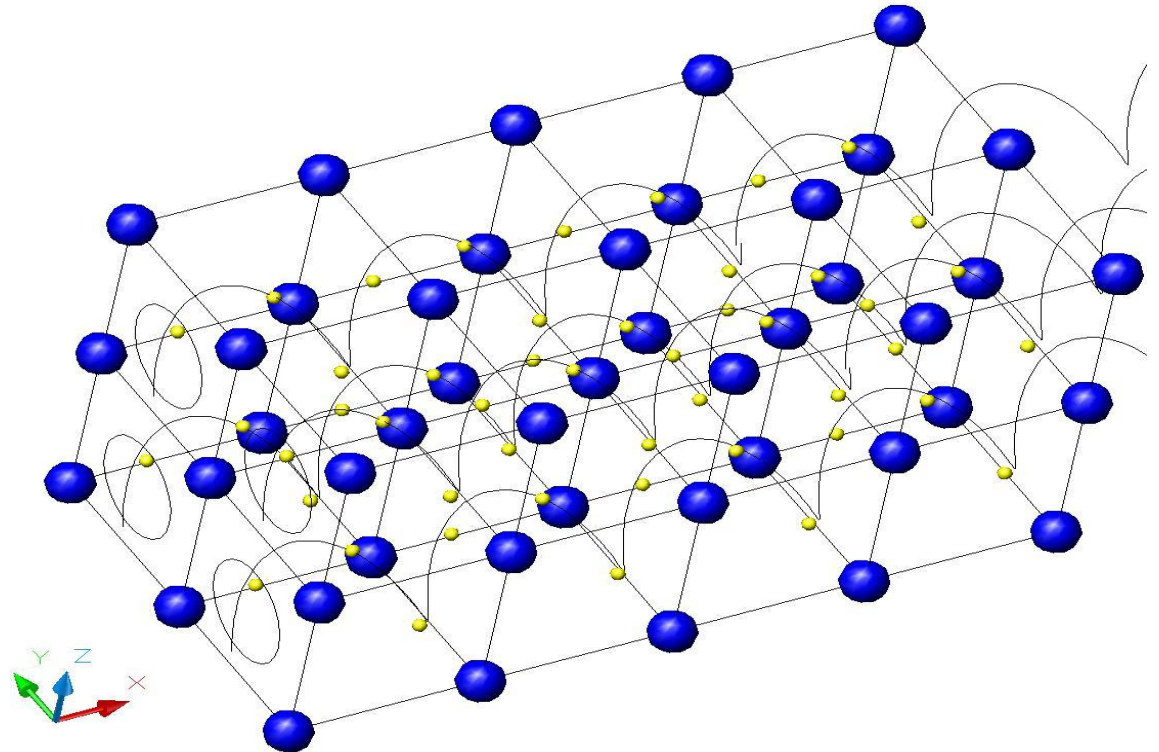
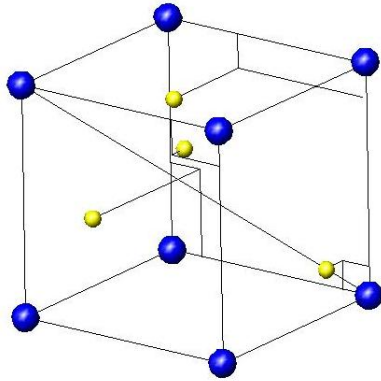
Scattering on the Laser radiation is the same process as the scattering on the electromagnetic wave.

One comment about helical crystals first .

Helical (chiral) crystals

Crystal structure MnSi and FeGe

P.Bak, M.H.Jensen, J.Phys.C: Solid St.Physics, 13,(1980) L881-5



Helical structure demonstrates CsCuCl_3 , FeGe , MgSi , $\text{Ba}_2\text{CuGe}_2\text{O}_7$, MnS_2

Laser bunch as an undulator

The number of the quantas radiated by an electron by scattering on photons (real from the laser or virtual from the undulator) can be described as the following

$$K = eH \lambda_u / 2\pi mc^2 \cong 0.934 \cdot H [T] \cdot \lambda_u [cm] \quad K = \beta_{\perp} \gamma$$

$$N_{\gamma} \cong 4\pi\alpha \frac{L}{\lambda_u} \frac{K^2}{1 + K^2} = 4\pi \frac{e^2}{\hbar c} \frac{L}{\lambda_u} \left(\frac{eH \lambda_u}{2\pi mc^2} \right)^2 \approx \left(\frac{e^2}{mc^2} \right)^2 \frac{L \lambda_u}{2\pi \hbar c} H^2 \cong r_0^2 L \frac{H^2}{\hbar \Omega} \cong \sigma_{\gamma} n_{\gamma} L$$

Formation length in
undulator $l_f \cong \lambda_u$

L - length of
undulator

$$\sigma_{\gamma} \cong \pi r_0^2 \quad n_{\gamma} \cong H^2 / \hbar \Omega \quad \Omega = 2\pi c / \lambda_u$$

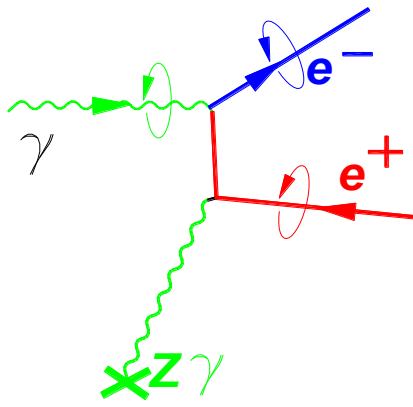
$$l_{\gamma} \cong 1 / \sigma_{\gamma} n_{\gamma} \quad \text{– Length of interaction}$$

Written in this form it is clear that the photon back scattering (especially with 90° crossing angle) is a full equivalent of radiation in an undulator (as soon as the photon energy is much less, than the energy of particle).

$$E_{\gamma n} \cong \frac{n \cdot 2.48 \cdot (\gamma / 10^5)^2}{\lambda_u [cm] (1 + K^2 + \gamma^2 \mathcal{G}^2)} [MeV]$$

That is why undulator installed at >100 GeV line, where $E_{\gamma} > 10$ MeV

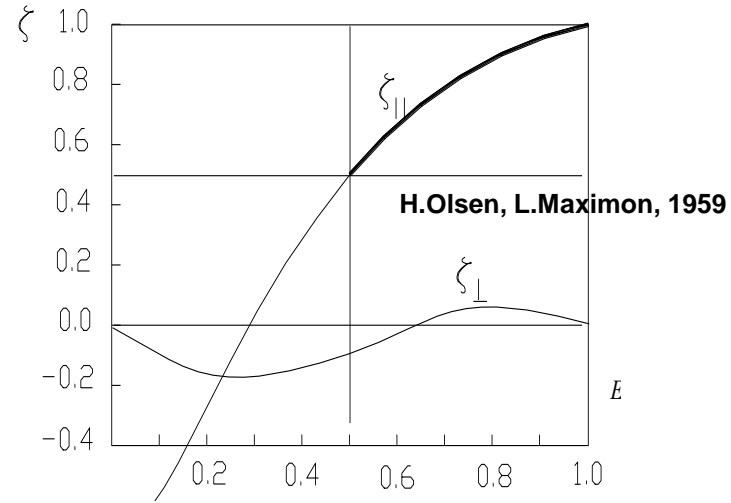
(POLARIZED) POSITRON PRODUCTION



+cross diagram

Only gamma quanta can create positron (with electron)

Longitudinal polarization as function of particle's fractional energy $E_+/(E_\gamma - 2mc^2)$



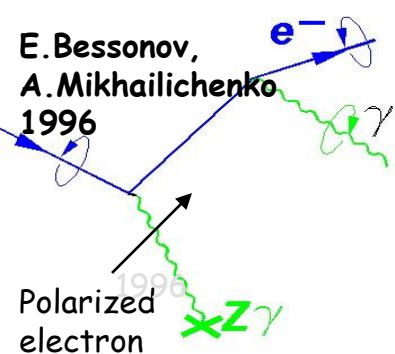
Photon polarization

$$\vec{\zeta} = \xi_2 \cdot \left[f(E_+, E_-) \cdot \vec{n}_\parallel + g(E_+, E_-) \cdot \vec{n}_\perp \right] = \vec{\zeta}_\parallel + \vec{\zeta}_\perp$$

Polarization is a result of selection positrons by their energy

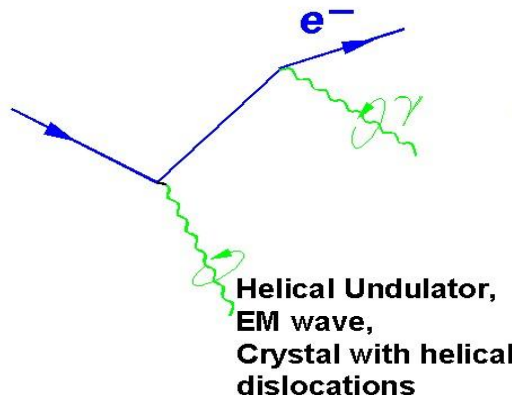
The ways to create circularly polarized photons in practical amounts

V.Balakin, A. Mikhailichenko, 1979

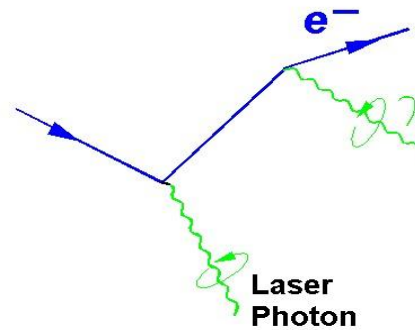


E. Bessonov, A. Mikhailichenko 1996

Polarized electron



Helical Undulator, EM wave, Crystal with helical dislocations



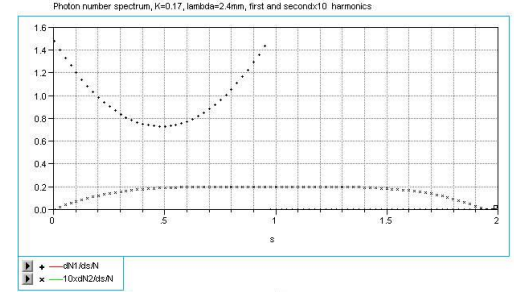
E. Bessonov 1992

Laser Photon

Analytical calculations are possible

Spectral density of radiation

$$\frac{dN_\gamma}{dE_\gamma} = \sum_n \frac{dN_\gamma}{dE_\gamma} = \frac{\alpha K^2 L}{2\gamma^2} \sum_{n=1}^{\infty} F_n(K, s)$$



where $s = E_\gamma / E_{\gamma \max}$ $E_{\gamma \max}$ is the energy of photon radiated straightforward

$$F_n(K, s) = J_n'^2(n\kappa) + \frac{1 + K^2}{4K^2} \frac{(2s - 1)^2}{s(1 - s)} J_n^2(n\kappa) \quad \kappa = 2K \sqrt{s(1 - s) / (1 + K^2)}$$

The number of positrons generated by a single photon in the target becomes

$$\frac{dN_+}{dE_+ d\tau} \cong 0.4 \frac{\alpha K^2 L}{\gamma^2 \hbar c} \frac{7}{9} (1 - E/E_{\gamma 1}) (1 - e^{-7\tau/9})$$

For $E_0=150$ GeV, $L=150$ m,
 $K^2=0.1$, $\tau=0.5$ (rad units)

$$\frac{1}{N_{tot}} \frac{dN_+}{dE_+} \cong 0.2 [1/MeV]$$

Analytical formula taking into account finite length of undulator and finite diameter of target

E.Bessonov, A.Mikhailichenko, 1992

$$\Delta N_{+1} \cong 2 \cdot 10^{-2} \chi^2 \frac{L}{\lambda u} \delta \frac{K^2}{1 + K^2} \frac{z_f}{z_i} \eta$$

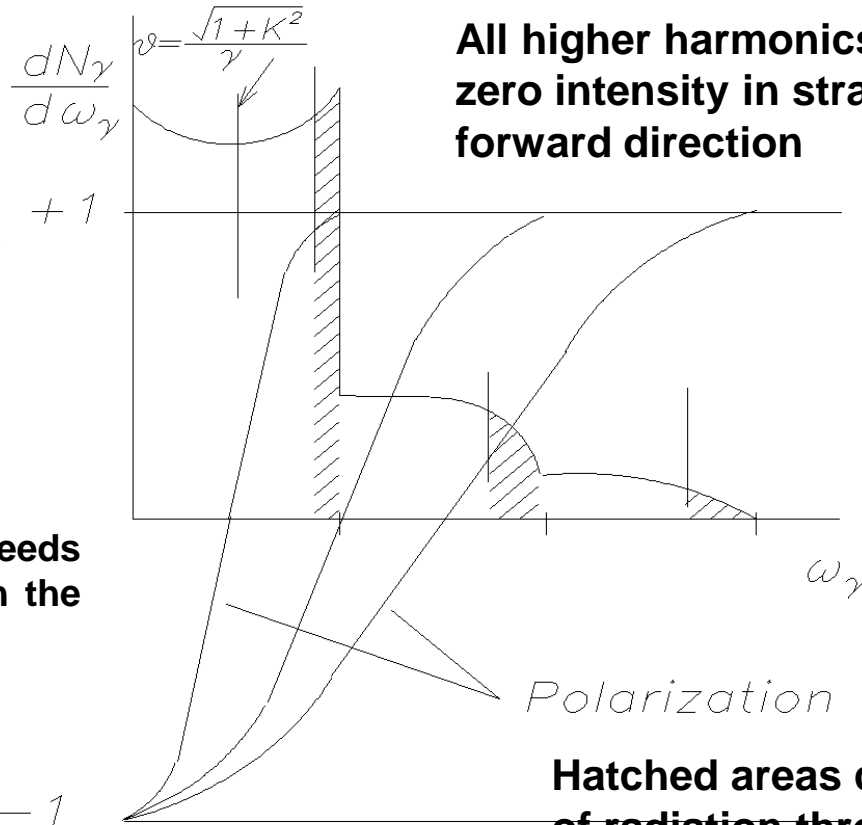
For $\chi = 1/2$, $L=200$ m, $\lambda_u=1$ cm $\delta=0.5$, $K=0.35$, $\eta=0.3$

$$\Delta N_{+1} \cong 3$$

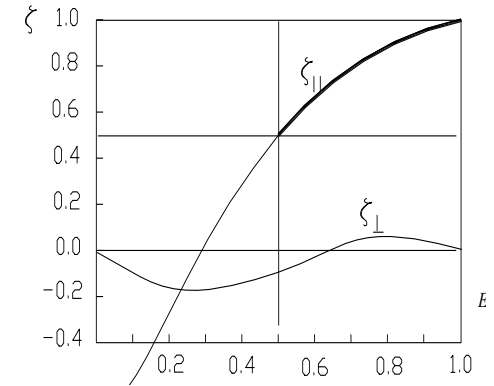
$Z_{f,i}$ - are the coordinates of undulator end and beginning calculated from the target position;

χ is a fraction of what is the target radius in respect to the size of the gamma spot at the target distance

Spectral distribution and polarization schematics



All higher harmonics have zero intensity in straight forward direction



This curve applied to each harmonics

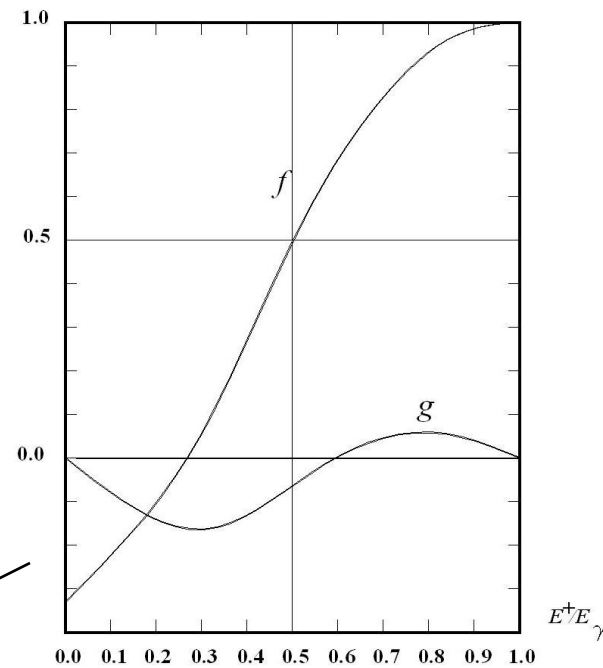
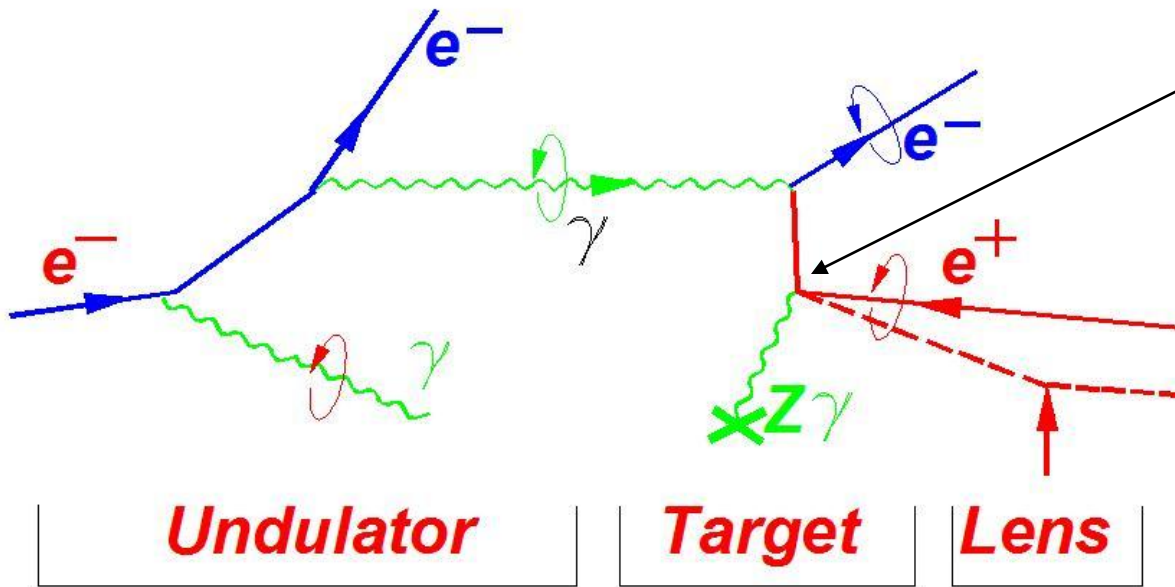
Hatched areas correspond to a passage of radiation through the collimator

Angle to observer (radiation) and the energy of the photon are not independent

Polarization curve needs to be convolved with the photon density

Diaphragm helps to enhance integrated photon polarization as each harmonics carries the photon polarization as a factor

KONN –interactive code for positron production with undulator



Monte-Carlo

POLARIZATION CURVE APPROXIMATION

EP=POSITRON ENERGY/ $E_{\gamma} - 2mc^2$

$$EP4 = EP - 0.4$$

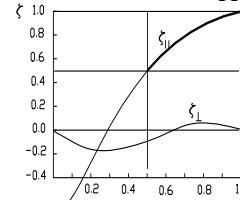
$$EP6 = EP - 0.6$$

$$PP = 0.305 + 2.15 * EP4$$

$$IF(EP.LT.0.4) PP = PP - 0.05 * EP4 - 2.5 * EP4^{**3}$$

$$IF(EP.GT.0.6) PP = PP - 0.55 * EP6 - 2.65 * EP6^{**2} + 0.7 * EP6^{**3} \quad ! PP = PP - 0.55 * EP6 - 2.6 * EP6^{**2}$$

$$IF(PP.GT.1.) PP = 1. \quad \text{Sentinel}$$



Depolarization occurs due to spin flip in act of radiation of quanta having energy $0 < \hbar\omega_{\gamma} \leq E_1$ where E_1 stands for initial energy of positron. Depolarization after one single act

$$D = 1 - \left| \frac{d\sigma_{\gamma e}(\zeta_1, \zeta_1) - d\sigma_{\gamma e}(\zeta_1, -\zeta_1)}{d\sigma_{\gamma e}} \right|$$

Where $d\sigma_{\gamma e}(\zeta_1, \zeta_1)$ stands for bremsstrahlung cross section without spin flip, $d\sigma_{\gamma e}(\zeta_1, -\zeta_1)$ –the cross section with spin flip and $d\sigma_{\gamma e}$ is total cross section.

$$D = \frac{\hbar^2 \omega_{\gamma}^2 \cdot [1 - \frac{1}{3} \zeta_{1\parallel}^2]}{E_1^2 + E_2^2 - \frac{2}{3} E_1 E_2} \quad \text{Energy after radiation}$$

$$L_{dep} \cong \frac{1}{n \int D(\vec{p}_1, \zeta_1) d\sigma} \quad \longrightarrow \quad L_{dep} \cong \frac{2X_0}{1 - \frac{1}{3} \zeta_{\parallel}^2} \cong 3X_0 \quad \text{Rad. length}$$

Depolarization ~5%

PROGRAM KONN

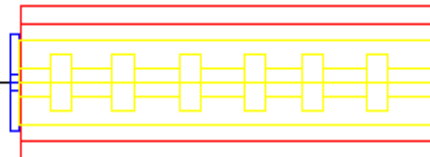
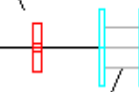
T.A.Vsevolozhskaya, A.A.Mikhailichenko

Monte-Carlo simulation of positron conversion

Energy of the beam;
Length of undulator;
Undulator period $M=L/\lambda_u$;
K-factor;
Emittance;
Beta-function;
Number of harmonics (four);
Number of positrons to be generated;

Target:
Distance to the undulator
Thickness;
Diameter of target;
Material;
Diameter of hole at center;
Step of calculation

Acceleration:
Distance to the lens;
Length of structure;
Gradient;
Diameter of collimator at the entrance;
Diameter of trices;
External solenoidal field;
Further phase volume captured;



CALCULATES at every stage:
Efficiency in given phase volume;
Polarization in given phase volume;
Beam dimensions;
Phase-space distributions;
Beam lengthening;
Energy spread within phase space;

Lithium Lens:
Distance to the target;
Length;
Diameter;
Thickness of flanges;
Material of flanges;
Gradient;
Step of calculations;

Interactive code, now is ~3000 lines

```

c:\AMSDEV\Projects\POSITRON CONVERSION\CONVERSION.exe
CONVERSION          - C
FOCUSING            - F
ACCELERATION       - A
WHAT TO DO?        -

D0 = .300  AL = .400  DW0 = .100  GG = .070

*** PARAMETERS OF ACCELERATION ***
DISTANCE TO RF STRUCTURE cm = 2.0000  ==
RADIUS OF DIAPHRAGM      cm = 3.0000  ==
LENGTH OF RF STRUCTURE  cm =100.0000  ==
GRADIENT                 MeU/cm      ==
LONGITUDINAL FIELD MGs  = .0400     ==
INNER RADIUS OF DIPHRAGM cm = 3.0000  ==
FURTHER ACCEPTANCE      MeUxcm      ==

POSITRONS PASSED= 4051  POSITRONS ACCEPTED = 4011
WW = 2.065  WWP = .958
F0 = .553  BETA = .384  DE/DT = -1.19  EFF = 2.065

      PV0      AL0      ALMB      R      EPS      BT      RTG      GG
150000.0    17500.0    1.00    .350    .000001    40000.0    .50    .070

RMS = .915  AMS = .040  DEM = 136.344  EM = 58.225  D7 =18000.00
PTM = 2.383  PZM = 58.176  DPZ = 5.001  PRM = -.017  PUG = 19.071
TM = 100.685  DTM = .620  WW = 2.065  WP = .464  N0 = 2400
RF = 3.00  AL/Xo = .40  H0 = .040  EPSF = 10.00 MeUxcm

      EFF<EX,CT>
.0065 .0141 .0286 .0379 .0354 .1444
.0602 .1703 .1959 .1583 .1233 .1462
.0715 .1733 .1486 .1049 .0557 .0126
.0248 .0843 .0700 .0255 .0106 .0007
.0158 .0315 .0211 .0106 .0032 .0006

      EFP<EX,CT>
.0372 -.0222 .0644 .0730 -.0607 .0555
.4200 .4642 .4093 .4150 .3323 .2957
.7056 .6618 .6318 .6424 .6403 .5375
.5951 .6645 .6523 .5436 .5939 .3507
.6141 .6423 .6217 .6786 .6096 .7789

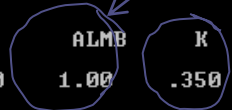
      EFF = 1.610  EFP= 47.420 %

```

Example

Period

K-factor



Efficiency and polarization

Code has ~3000 rows;

Possibility for the file exchange with graphical and statistical Codes (JMP);

Possibility for the file exchange with PARMELA;

Few seconds for any new variant

Before representing results of calculation let us demonstrate how different elements of conversion system look like

UNDULATOR (Cornell design)

Complete design done;
Diameter of cryostat -100mm

System for magnetic
measurement designed;

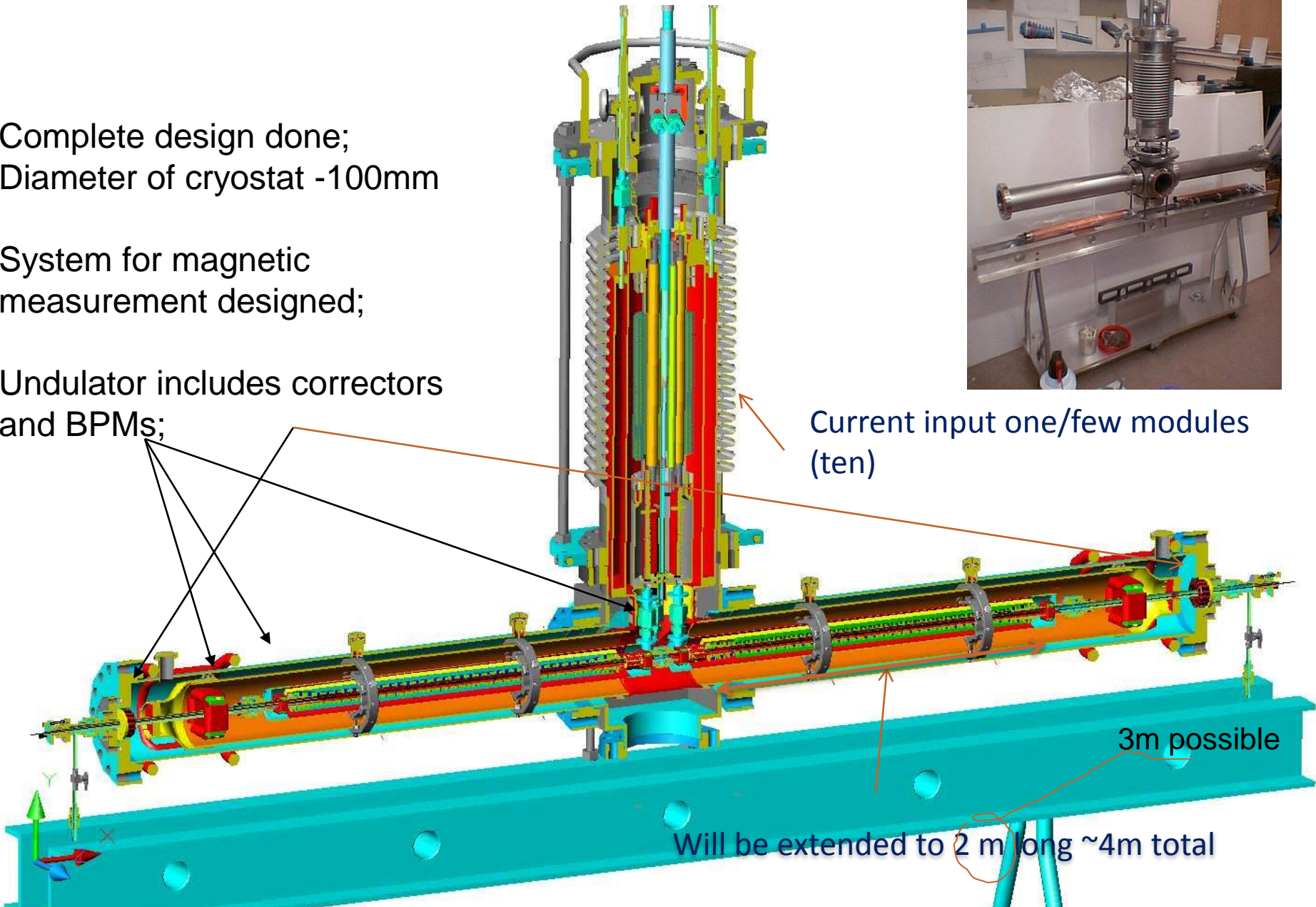
Undulator includes correctors
and BPMs;



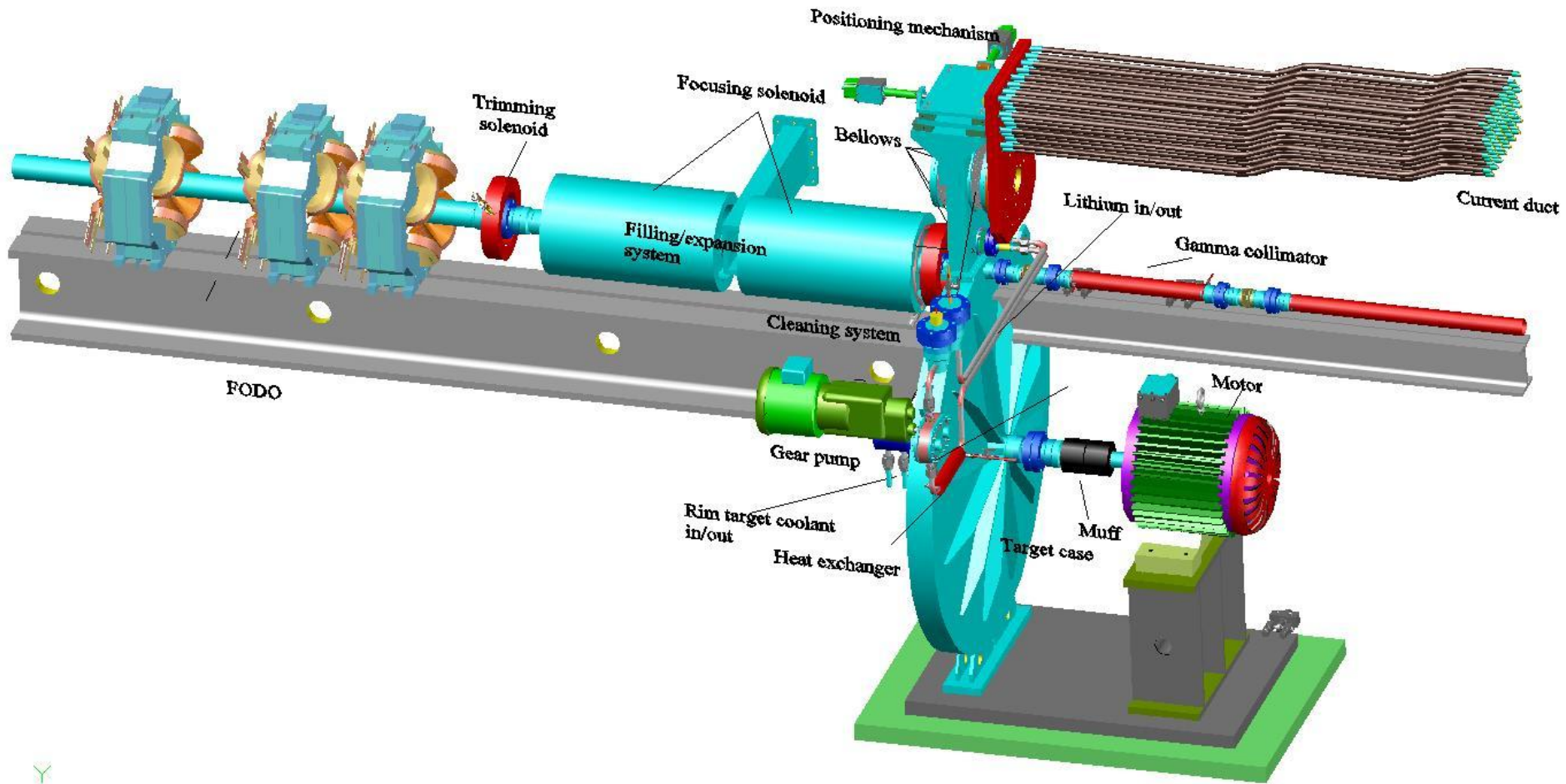
Current input one/few modules
(ten)

3m possible

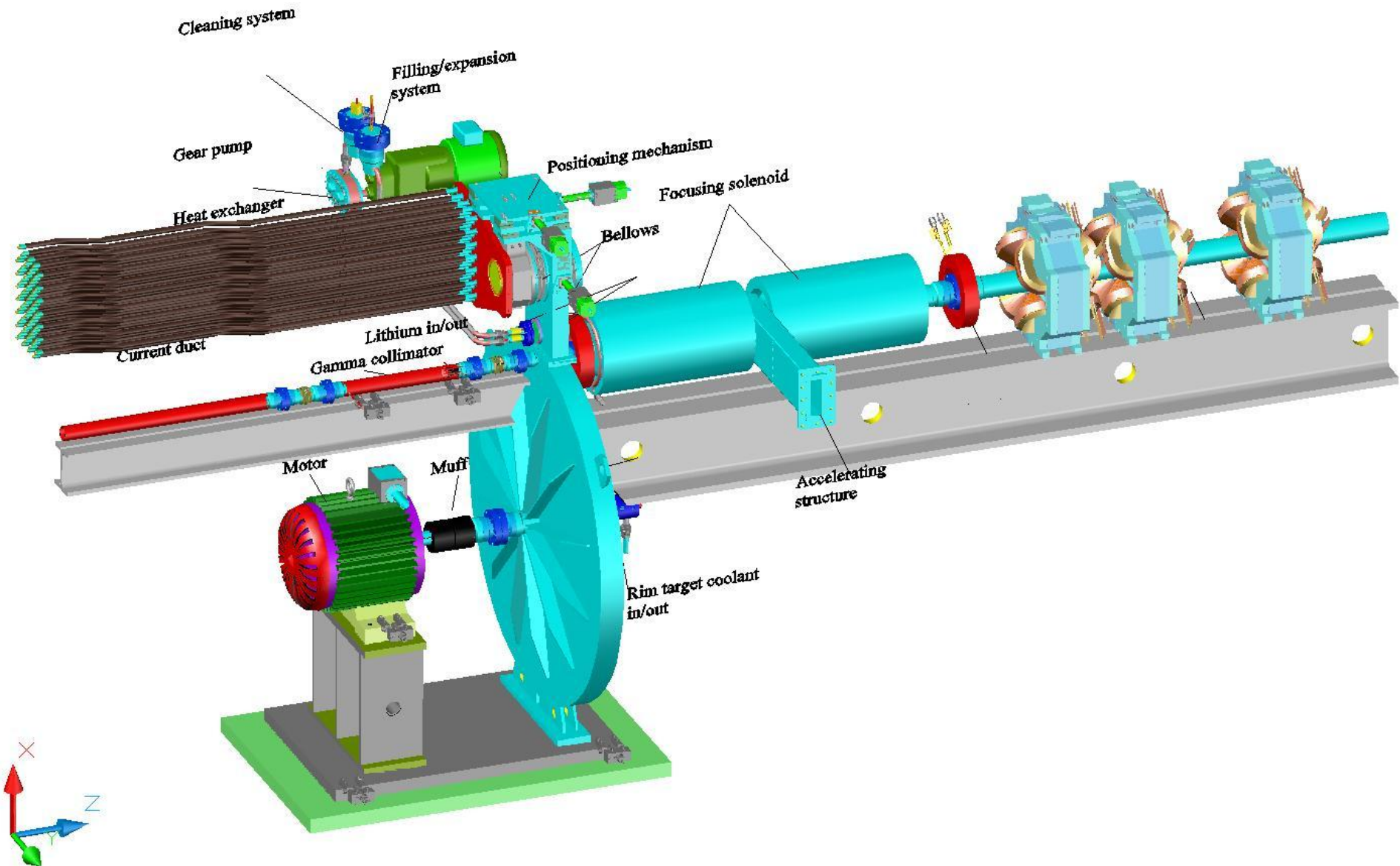
Will be extended to 2 m long ~4m total



TARGET STATION FOR ILC



TARGET STATION



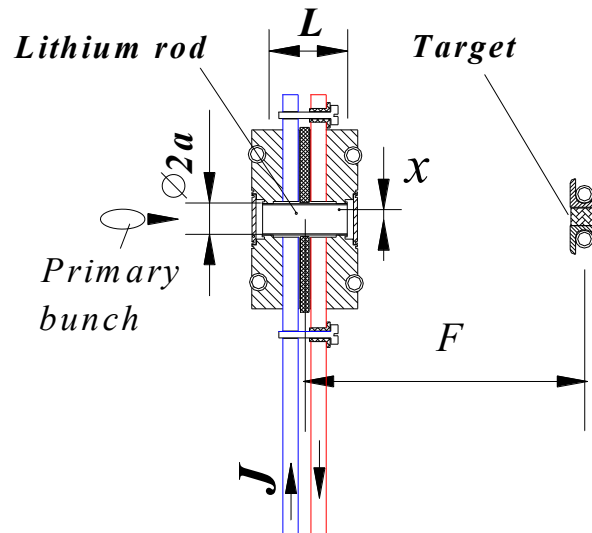
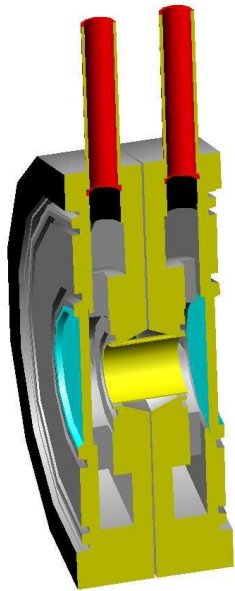
LITHIUM LENS

If steady current I runs through the round conductor having radius a , its azimuthal magnetic field inside the rod could be described as

$$H_{\theta}(r) = \frac{0.4\pi I r}{2\pi a^2}$$

where magnetic field is measured in Gs, a –in cm , I –in Amperes. Current density comes to $j_s = I / \pi a^2$ The particle, passed through the rod, will get the transverse kick

$$\alpha \cong \frac{H(x) \cdot L}{(HR)} \cong \frac{0.2ILx}{a^2 \cdot (HR)}$$



This picture drawn for the focusing of electron beam to the target

So the focal distance could be defined as the following

$$F \cong \frac{a^2 \cdot (HR)}{0.2IL}$$

Li lens resume

Utilization of Lithium lens allows Tungsten survival under condition required by ILC with $N_e \sim 2 \times 10^{10}$ with moderate $K \sim 0.3-0.4$ and do not require big-size spinning rim (or disc). Thin W target allows better functioning of collection optics (less depth of focusing).

Lithium lens (and x-lens) is well developed technique.

Usage of Li lens allows drastic increase in accumulation rate, low K-factor.

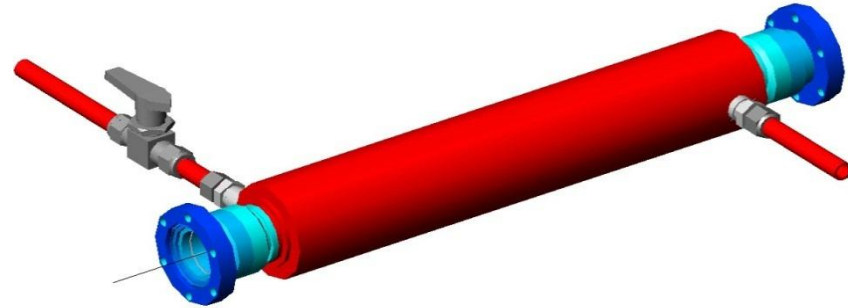
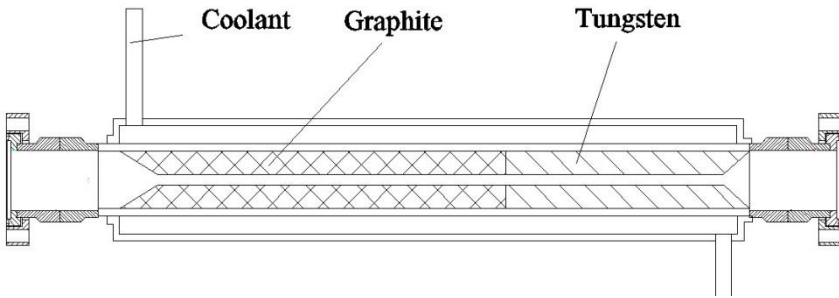
Field is strictly limited by the surface of the lens from the target side.

Liquid targets such as Pb/Bi or Hg allow further increase of positron yield.

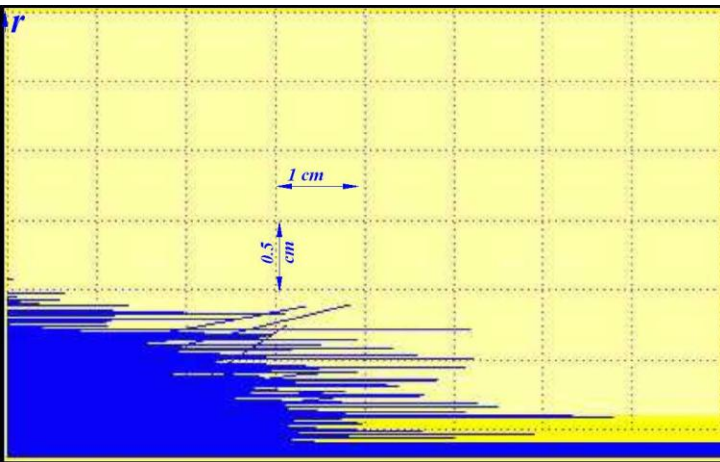
Plan is to repeat optimization for cone-shape Lithium rod.

Collimator for gammas

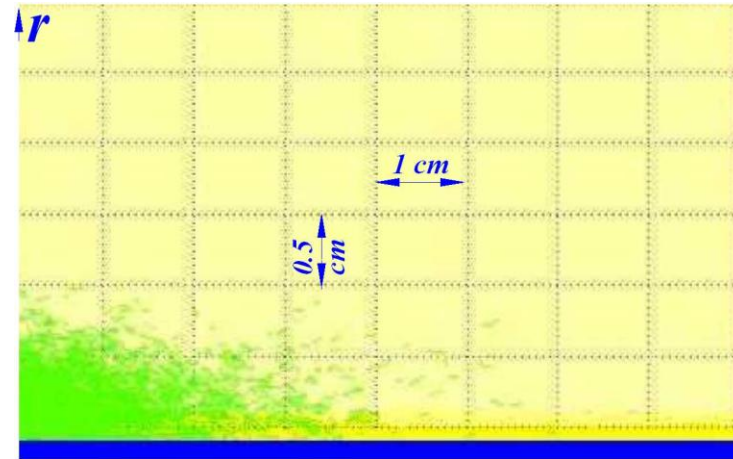
Pyrolytic Graphite (PG) is used here. The purpose of it is to increase the beam diameter, before entering to the W part. Vacuum outgassing is negligible for this material. Heat conductivity $\sim 300 \text{ W/m}\cdot\text{oK}$ is comparable with meals. *Beryllium* is also possible here, depending on task.



Transverse dimensions defined by Moliere radius



Gamma-beam. $s_g = 0.5\text{cm}$, diameter of the hole (blue strip at the bottom) $d=2 \text{ mm}$. Energy of gamma-beam coming from the left is 20 MeV .



Positron component of cascade

PERTURBATION OF POLARIZATION

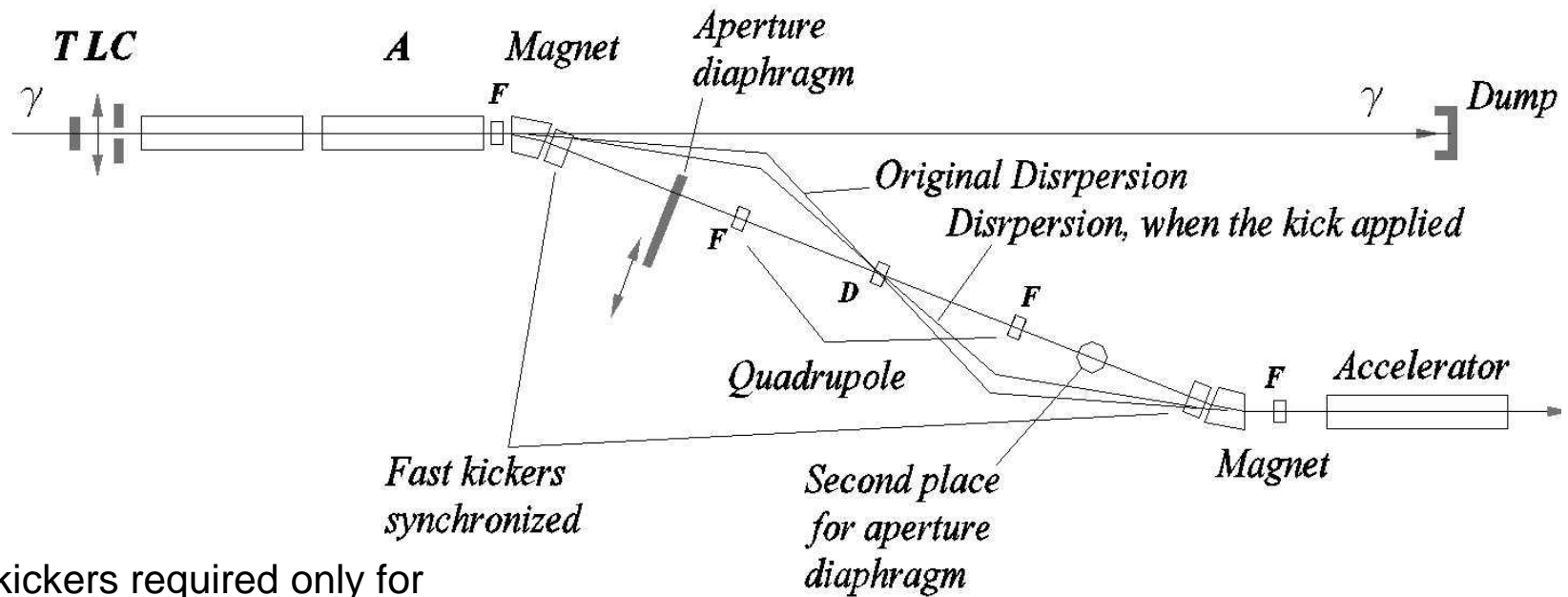
Perturbation due to multiple scattering	- absent
Spin flip in a target	~5%
Spin flip in an undulator	- hardly mentionable effect
Depolarization at IP	~5%
Cinematic depolarization in undulator	-absent

CONCLUSIONS ABOUT POLARIZATION

Perturbation of spin is within 10% total (from creation).

This number could be reduced by increasing the length of undulator, making target thinner (two targets) and beams more flat at IP.

SCHEME FOR PARTICLES SELECTION BY ENERGY



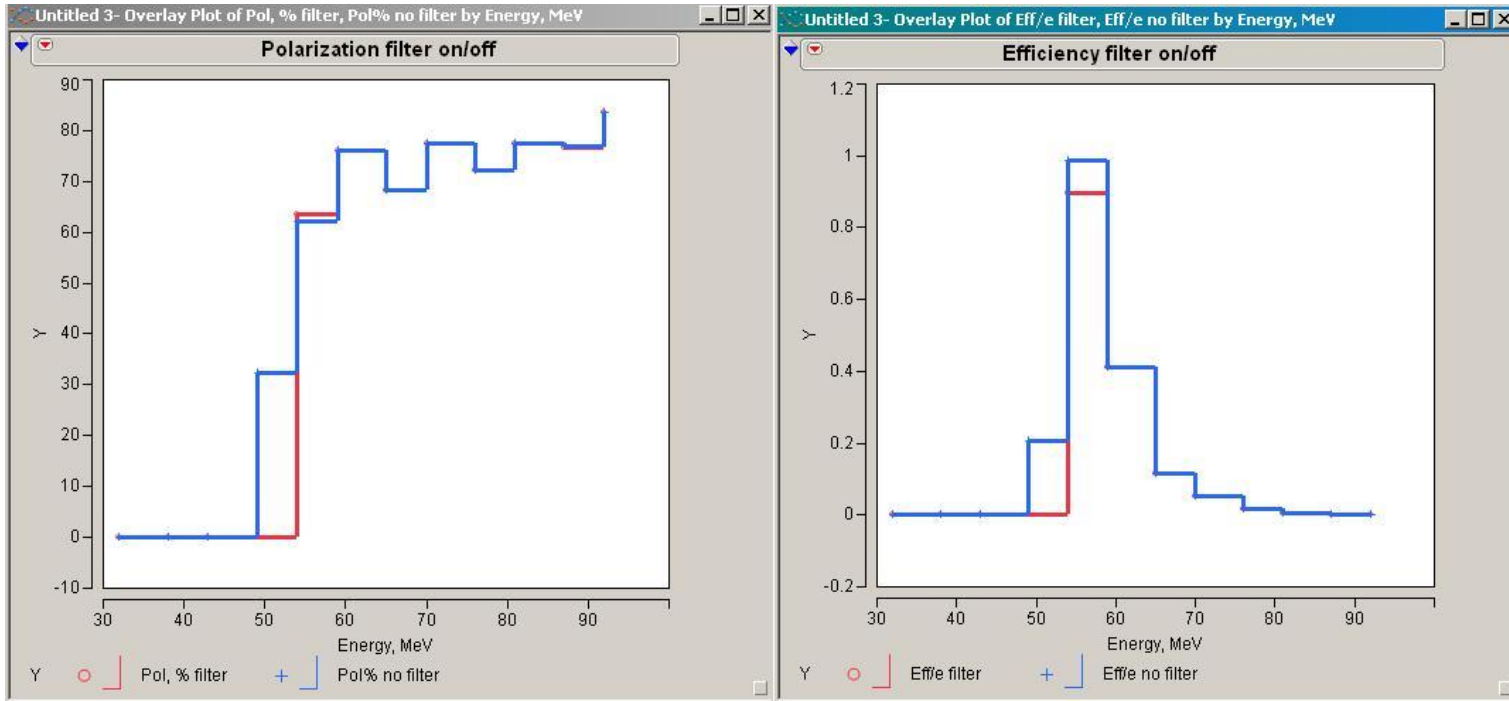
*Fast kickers
synchronized*

*Second place
for aperture
diaphragm*

Fast kickers required only for independent positron wing operation

Achromatic bend with aperture diaphragm. *T*—is a target, *L*—is a short focusing lens, *C*—stands for collimator. *F* and *D* stand for focusing and defocusing lenses respectively. *A* stands for RF accelerator structure.

ONE EXAMPLE



Average polarization
Filter on: 68.15%
Filter off: 62.78%

Efficiency
Filter on: 1.49
Filter off: 1.796

Resulting efficiency and polarization calculated with KONN

*radius of target is an equivalent of the radius of collimator

Beam energy, GeV	150	250	350	500
Length of undulator, m	170	200	200	200
K factor	0.44	0.44	0.35	0.28
Period of undulator, cm	1.0	1.0	1.0	1.0
Distance to the target, m	150	150	150	150
Radius of target*, cm	0.049	0.03	0.02	0.02
Emittance, $cm\cdot rad$	1e-9	1e-9	1e-9	1e-9
Bunch length, cm	0.05	0.05	0.05	0.05
Beta-function, m	400	400	400	400
Length of target/ X_0	0.57	0.6	0.65	0.65
Distance to the length, cm	0.5	0.5	0.5	0.5
Radius of the length, cm	0.7	0.7	0.7	0.7
Length of the length, cm	0.5	0.5	0.5	0.5
Gradient, MG/cm	0.065	0.065	0.08	0.1
Wavelength of RF, cm	23.06	23.06	23.06	23.06
Phase shift of crest, rad	-0.29	-0.29	-0.29	-0.29
Distance to RF str., cm	2.0	2.0	2.0	2.0
Radius of collimator, cm	2.0	2.0	2.0	2.0
Length of RF str., cm	500	500	500	500
Gradient, MeV/cm	0.1	0.1	0.1	0.1
Longitudinal field, MG	0.045	0.045	0.045	0.045
Inner rad. of irises, cm	3.0	3.0	3.0	3.0
Acceptance, $MeV\cdot cm$	5.0	5.0	5.0	5.0
Energy filter, $E > -MeV$	54	74	92	114
Energy filter, $E < -MeV$	110	222	222	222
Efficiency, e^+/e^-	1.5	1.8	1.5	1.5
Polarization, %	70	80	75	70

One another way to increase the polarization associated with installation of a second target.

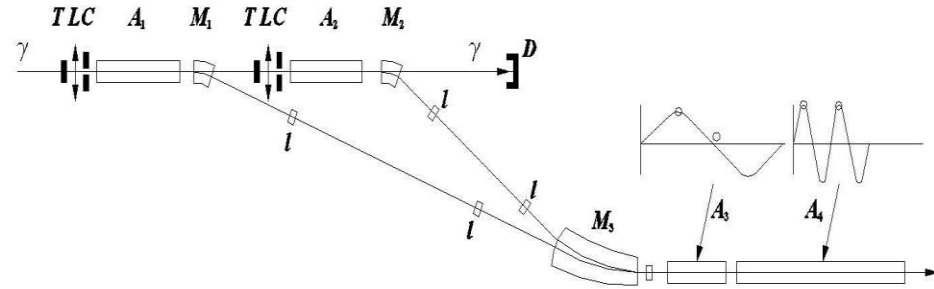
This is possible as the gamma beam loses its intensity after the first target ~13% only

Collection of positrons in the longitudinal phase space is possible with combining scheme

COMBINING SCHEME

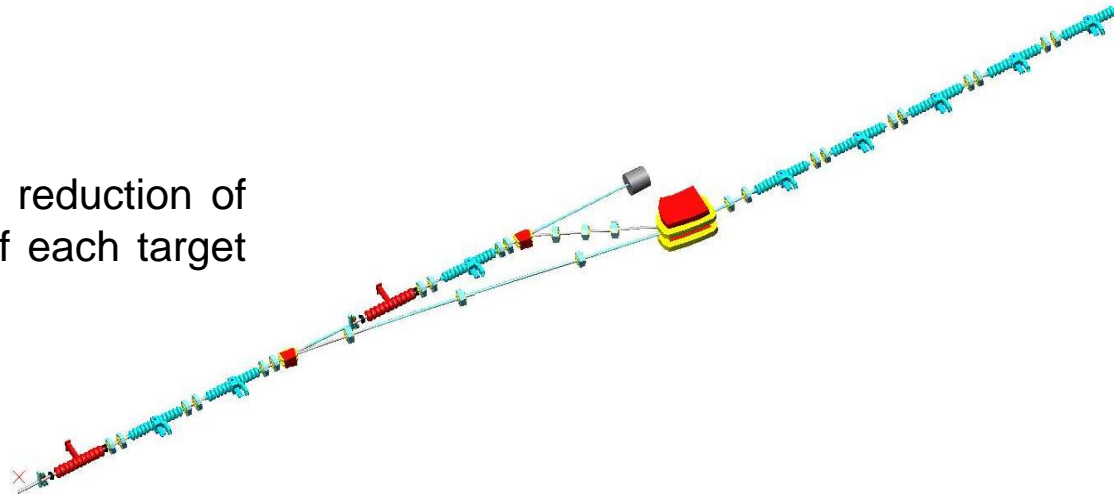
Combining in longitudinal phase space could be arranged easily in the same RF separatrix in damping ring.

Additional feed back system will be required for fast dump of coherent motion.



Energy provided by acceleration structures A_1 and A_2 are slightly different, $A_1 > A_2$.

This combining can help in reduction of power deposition in target if each target made thinner, than optimal.



Combining scheme doubles the positron yield and cuts in half the length of undulator → increase of polarization

One another way to reconsider maximal polarization and luminosity achievable at IP

It is associated with the spin-spin interaction of particles in the same bunch while the bunch is moving towards IP

Minimal emittance

Fundamental restriction to the minimal emittance achievable in the electron/positron beam is

$$(\gamma \varepsilon_x)(\gamma \varepsilon_y)(\gamma \varepsilon_s) = (\gamma \varepsilon_x)(\gamma \varepsilon_y)(\gamma l_b (\Delta p / p_0)) \geq \frac{1}{2} (2\pi \tilde{\lambda}_c)^3 N$$

A.A. Mikhailichenko, *On the physical limitations to the Lowest Emittance (Toward Colliding Electron-Positron Crystalline Beams)*, 7th-Advanced Accelerator Concepts Workshop, 12-18 October 1996, Lake Tahoe, CA, AIP 398 Proceedings, p.294. See also CLNS 96/1436, Cornell, 1996, and in *To the Quantum Limitations in Beam Physics*, CLNS 99/1608, PAC99, New York, March 29- April 2 1999, Proceedings, p.2814.

This formula can be obtained from counting the number of states in the phase space of a Fermi gas :

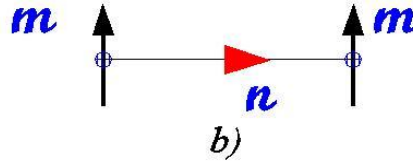
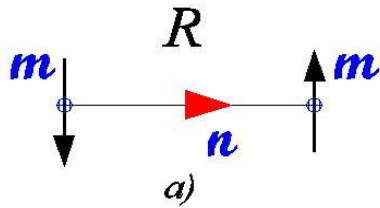
$$dn \cong 2 \frac{dp_x dp_y dp_s \cdot V}{(2\pi\hbar)^3} \longrightarrow N = \int dn \cong 2 \frac{p_x p_y \Delta p_{\parallel} S_{\perp} l_b \gamma}{(2\pi\hbar)^3} \cong 2 \frac{\gamma \varepsilon_x \gamma \varepsilon_y \gamma l_b (\Delta p / p_0)}{(2\pi\tilde{\lambda}_c)^3} = 2 \frac{\gamma \varepsilon_x \gamma \varepsilon_y \gamma \varepsilon_z}{(2\pi\tilde{\lambda}_c)^3}$$

The problem is that in the fully degenerated state polarization of beam is zero

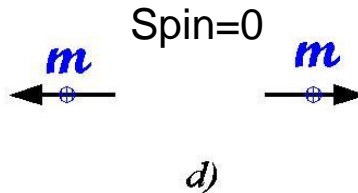
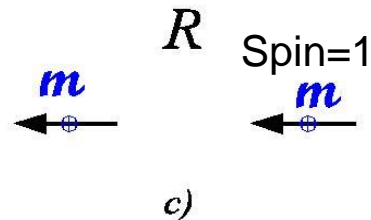
SUPERCONDENSATION of ELECTRON GAS

Magnetic dipole \vec{m} defines magnetic field around as

$$\vec{H} = \frac{3\vec{n} \cdot (\vec{m} \cdot \vec{n}) - \vec{m}}{R^3}$$



In case a) and c) there is attraction by magnetic force.



In case b) and d) there is additional repulsion

Balancing attraction by magnetic force and repulsion by the same sign of charge, one can obtain

$$\frac{3(\vec{m} \cdot \vec{n})^2 - m^2}{4R^4} \cong \frac{e^2}{R^2} \longrightarrow R \cong \frac{(2)\hbar}{4mc} = \frac{(2)}{4} \cdot \tilde{\lambda}_c$$

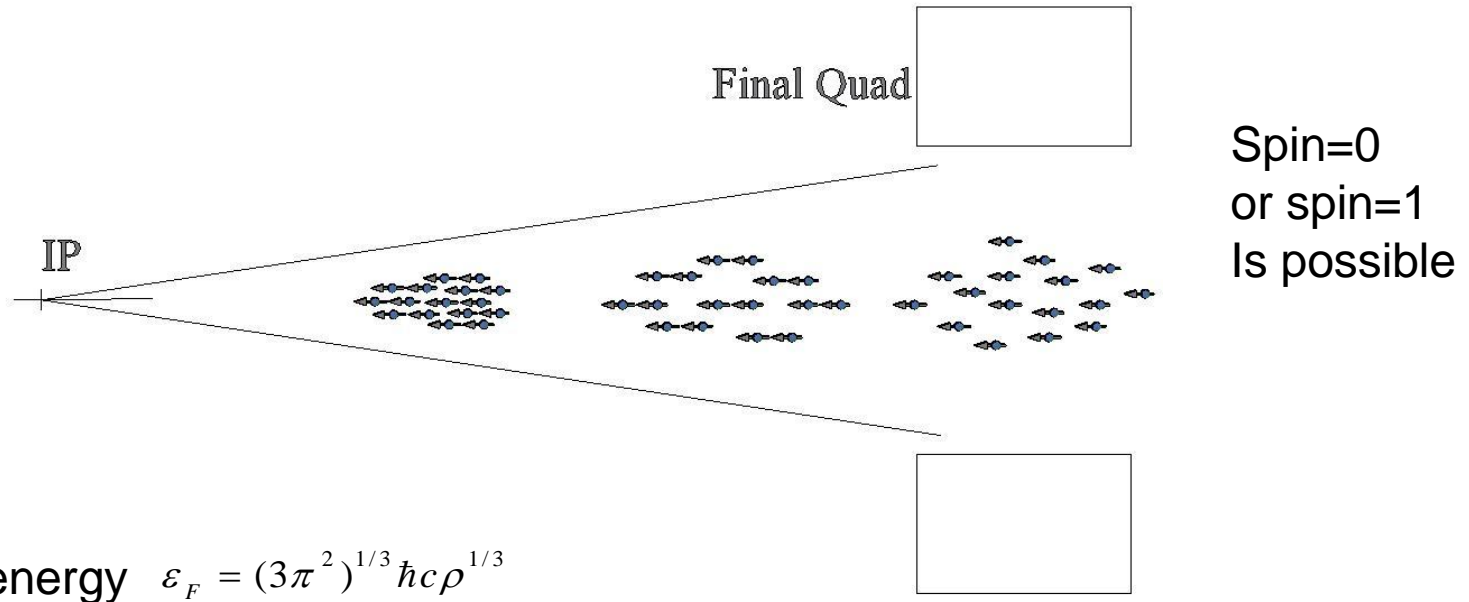
Energy required bringing two electrons to the distance of Compton wavelength is

$$\frac{e^2}{\tilde{\lambda}_c} \cong \frac{e^2}{r_0} \cdot \alpha \cong \alpha \cdot mc^2$$

i.e. pretty small compared with energy of transverse motion at IP especially

SUPERCONDENSATION AT IP – A WAY TO SUPER LUMINOSITY

While beam in running to IP its density increases



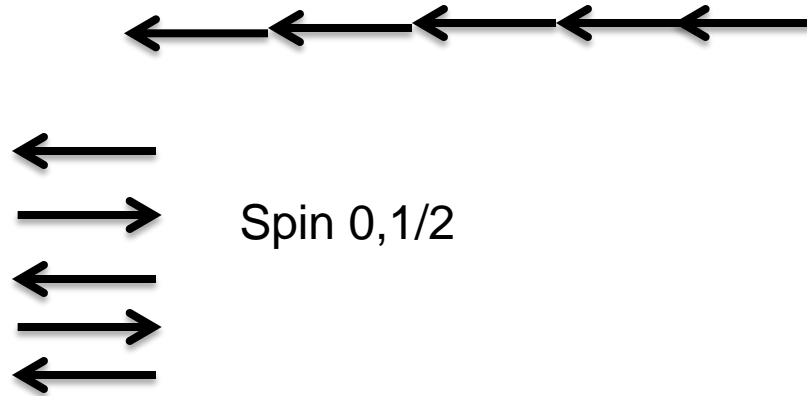
The condition for degeneration $k_B T \leq (3\pi^2)^{1/3} \hbar c \rho^{1/3}$

Fermi gas becomes more degenerative while its density increased.

These conditions realizing better and better while beam traveling to IP.

Taking into account interaction through magnetic momentum, it will possible to condense beam below Fermi-limit (couple of fermions behaves as a boson).

What is the limit for the number of electrons in a cluster



The topic of super-condensation requires theoretical investigations

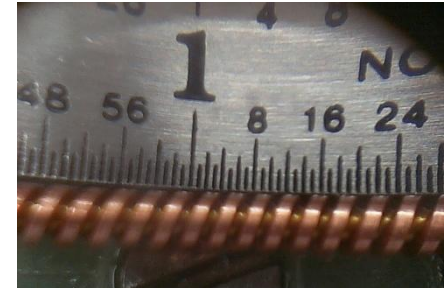
E-166 experiment at SLAC

First suggested in 1992

Experimental test of polarized positron production

With gammas generated by high energy beam in undulator

Beam chamber
0.8 mm in dia



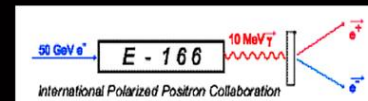
Stretched wire to check
the straightness

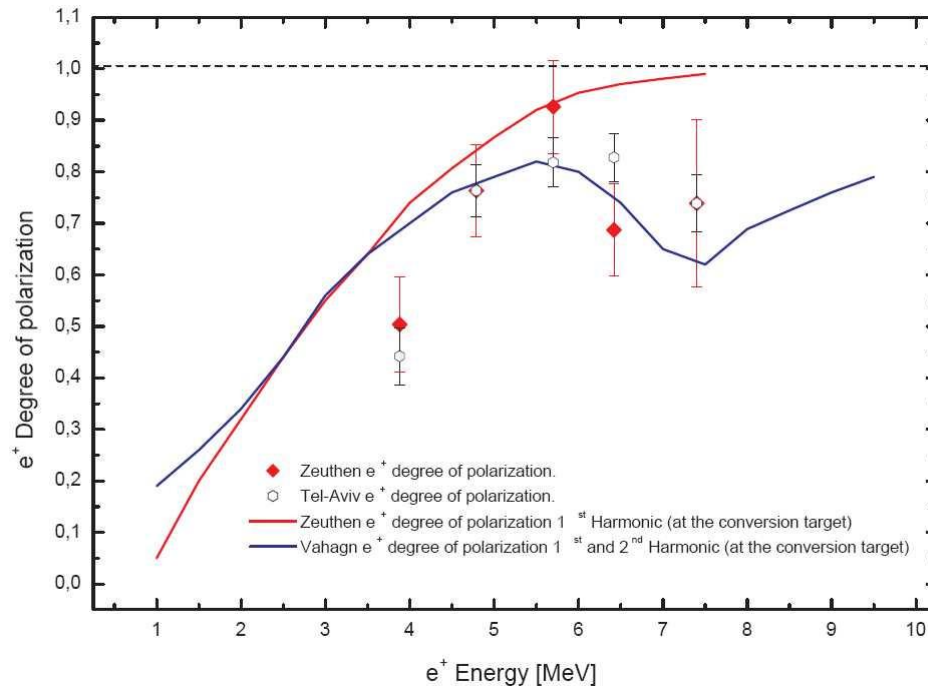
$$E_{\gamma n} \cong \frac{n \cdot 2.48 \cdot (\gamma / 10^5)^2}{\lambda_u [cm] (1 + K^2 + \gamma^2 \theta^2)} [MeV]$$

→ Goes to 2.54 mm period for 50 GeV beam



E166 collaboration
Helical Undulator based polarized positron source for the ILC





Degree of longitudinal polarization for positrons and electrons as measured by the E166 experiment (preliminary).

Results published in PRL, NIM

CONCLUSIONS

Maximal polarization can be achieved not only by collimation of gammas, but with selection of positrons by energy after the target.

Separation of secondary particles (positrons or electrons) by energy is a key procedure in polarization gain.

Generation of polarized electrons is possible in this method as well

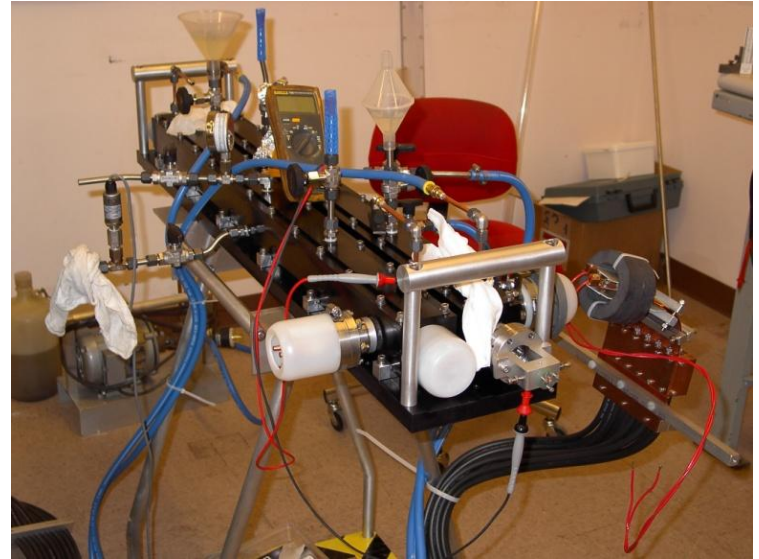
State with minimal emittance has zero overall polarization

More detailed calculation required for process of squeezing the polarized beam to IP while spin-spin interaction taken into account

E-166 diffused any doubts about undulator-based positron production for ILC

Back-up slides

Helical undulator (cornell)



Modeling of E-166 experiment with KONN

Phase space right after the target

```

C:\MSDEV\Projects\POSITRON CONVERSION\Debug\POSITRON CONVERSION.exe
WHAT TO DO?

*** SYSTEM PARAMETERS ***

INITIAL MOMENTA ,MeV      =150000.0  :=49000
LENGTH OF UNDULATOR,cm  = 17500.0  :=100
K FACTOR                  =    .350  :=.17
PERIOD OF ONDULATOR, cm =  1.000  :=.254
DISTANCE TO THE TARGET   = 18000.0  :=3200
RADIUS OF TARGET, cm     =   .500  :=.15
RADIUS OF HOLE            =    .000  :=
EMITTANCE, cmxrad        =  1.000E-06:=
BETTA-FUNCTION, cm       =  40000.0  :=4000
LENGTH OF TARGET/%o      =   .400  :=.5
STEP OF CALCULATION      =    .100  :=
HARMONICS INDEX          =  0; <5   =  0   :=
NUMB.OF PART ON 1 H     = 2400    :=

TOTAL NUMBER OF PHOTONS  =  1.014
MAX ENERGY OF QUANTA   =  8.741 MeU
GAMMA                   =  95890.4

POSITRONS ACCEPTED = 5000    POSITRONS GENERATED = 30820

ENERGY OF QUANTA = 8.741  BETA = 1.274  EFF = .003  PUG = 49000.0
LENGTH OF UNDUL. = 100.0  PERIOD = .25  PT2 = .03  EPT = .0000010
BT = 4000.0  RTG = .15  F0 = -.091  RMS = 1.138  AMS = .894
XU = .072  NUMBER OF PARTICLES BY FIRST HARMONIC = 2400
PHOTONS/e = 1.014  GAMMA= 95890.4

          EFF<EX,CT>
.0000 .0000 .0000 .0001 .0001 .0001
.0001 .0001 .0002 .0002 .0002 .0003
.0000 .0001 .0001 .0002 .0002 .0004
.0000 .0000 .0000 .0000 .0001 .0002
.0000 .0000 .0000 .0000 .0000 .0000

          EFF<EX,CT>
-.0336 -.0927 .0143 -.0414 -.0172 -.0734
.4099 .4170 .4039 .3911 .3971 .2796
.7835 .7675 .7085 .7309 .7255 .6872
.8858 .8004 .8221 .8011 .8528 .8420
.6790 .6925 .7001 .6678 .7615 .7450

```

Dependence of polarization seen in experiment

ILC Beam parameters important for conversion system

$g_{e_x} = 8 \cdot 10^{-6}$ m rad -high edge

$g_{e_y} = 8 \cdot 10^{-8}$ m rad –high edge

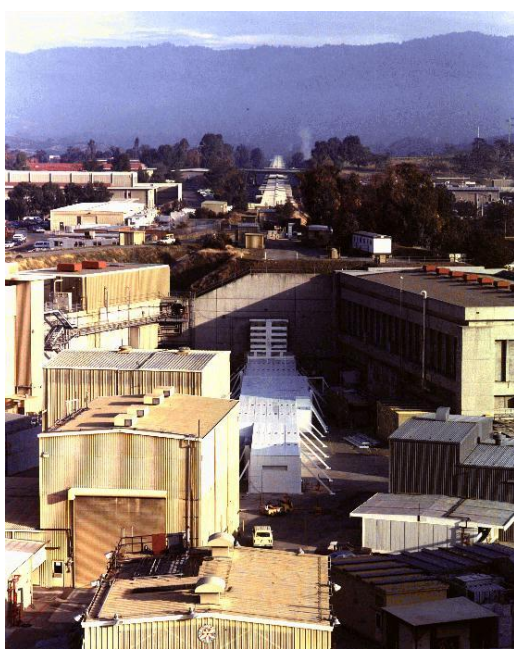
$b_x \sim 200$ m in undulator

Angular spread in radiation	$\alpha \sim \sqrt{1 + K^2} / \gamma$	$3 \cdot 10^{-6}$ ($K=1$)
Angular spread in beam, vert.	$y' \cong \pm \sqrt{\gamma \varepsilon_z / \beta \gamma}$	$3.5 \cdot 10^{-8}$
Angular spread in beam, rad.	$y' \cong \pm \sqrt{\gamma \varepsilon_z / \beta \gamma}$	$3.5 \cdot 10^{-7}$
Radius of helix	$a \cong \hat{\lambda}_u K / \gamma$	$5 \cdot 10^{-7}$ cm ($K=1$)
Beam size, vertical	$\sqrt{\langle y^2 \rangle} \cong 2 \times \sqrt{\gamma \varepsilon_y \beta / \gamma}$	$1.4 \cdot 10^{-3}$ cm
Beam size, radial	$\sqrt{\langle x^2 \rangle} \cong 2 \times \sqrt{\gamma \varepsilon_x \beta / \gamma}$	$1.4 \cdot 10^{-2}$ cm

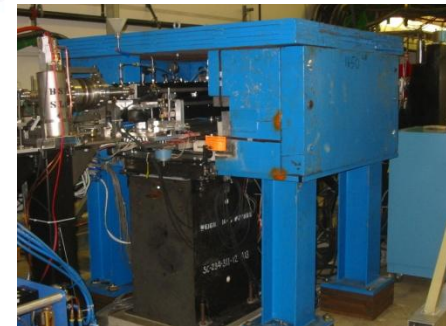
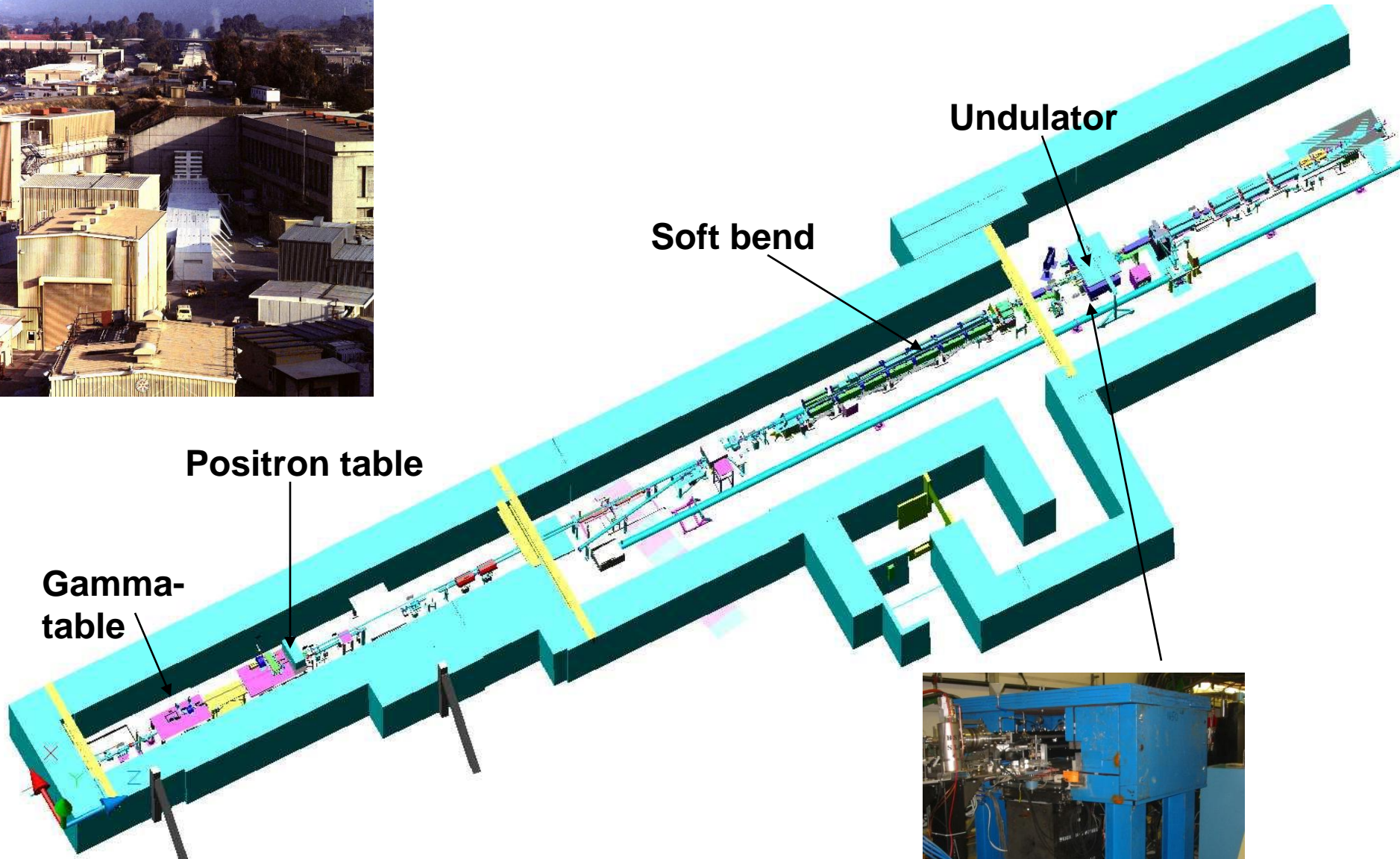
50 sigma ~ 7 mm ; At the beginning of operation one can expect emittance degradation

At Cornell the undulators having aperture $\emptyset = 8$ mm tested so far; 6.35 (1/4 in) designed.

Daresbury deals with aperture $\emptyset = 5.23$ mm

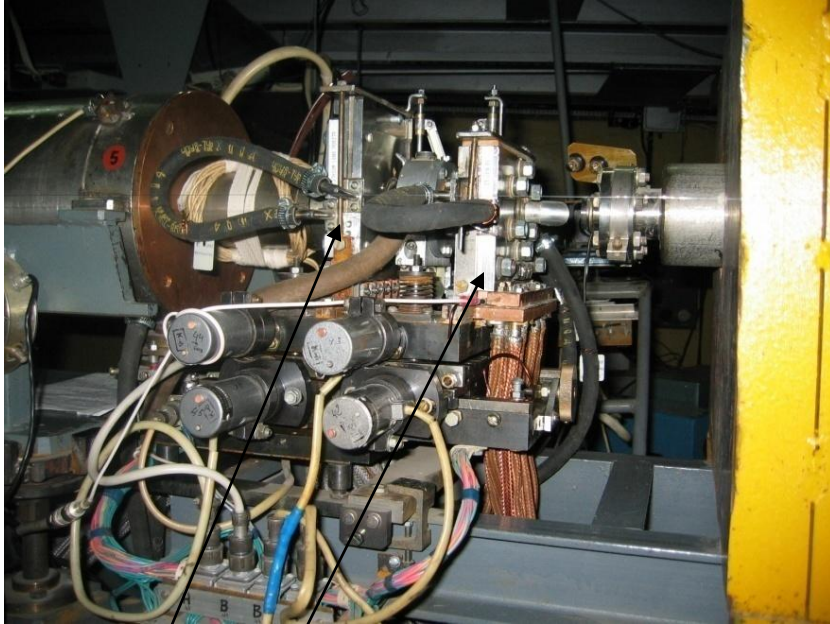


3D scope of E-166



Doublet of Lithium lenses in Novosibirsk BINP

Photo- courtesy of Yu Shatunov



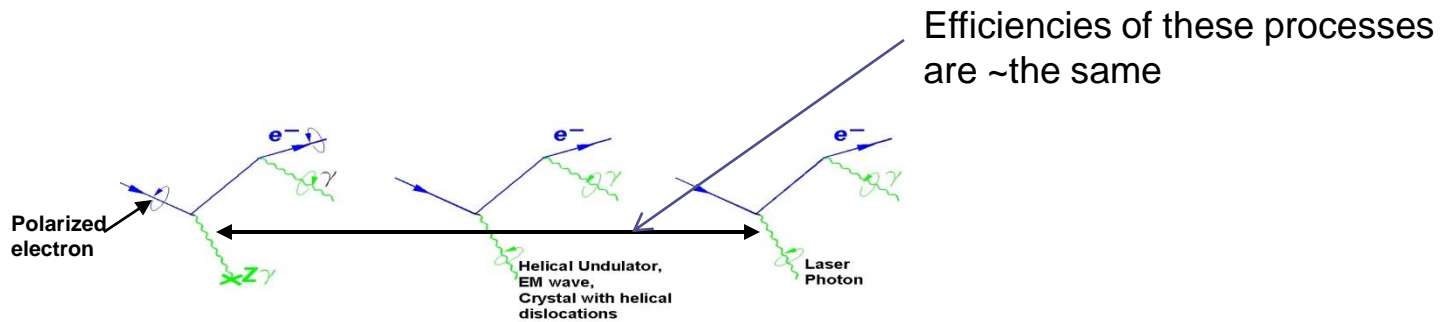
First lens is used for focusing of primary 250 MeV electron beam onto the W target,
Second lens installed after the target and collects positrons at ~150MeV

Number of primary electrons per pulse $\sim 2 \cdot 10^{11}$; ~ 0.7 Hz operation (defined by the beam cooling in Damping Ring)

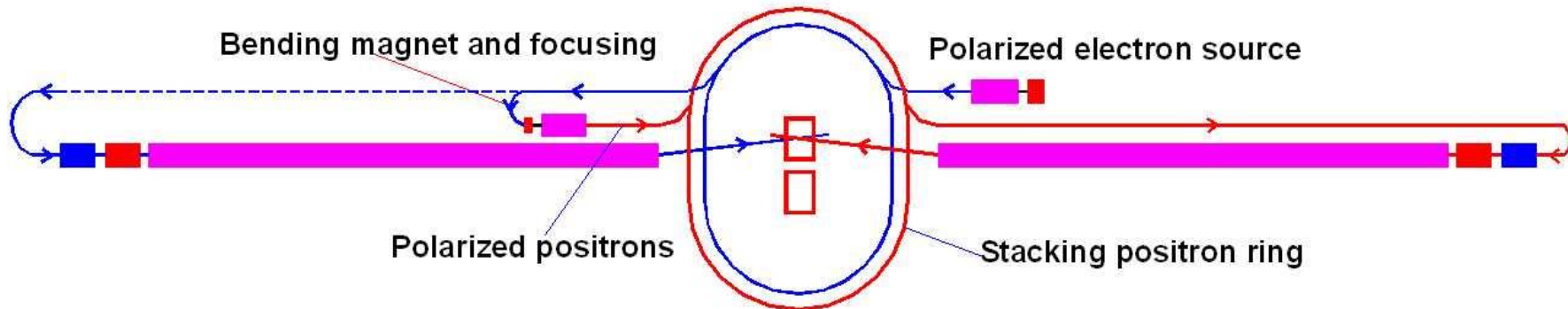
Lenses shown served ~ 30 Years without serious problem (!)

POLARIZED POSITRON PRODUCTION WITH STACKING IN DR

If stacking in DR is allowed, then there is one additional way to generate polarized positrons. Calculations show that efficiency $\sim 1.5\%$ is possible for the first process with polarization $\sim 75\%$



Realization of this method



No lasers !

However, the Undulator-based scheme remains more advantageous

Depolarization at IP

- Depolarization arises as the spin changes its direction in coherent magnetic field of incoming beam. Again, here the deviation does not depend on energy, however it depends on location of particle in the bunch: central particles are not perturbed at all. Absolute value of angular rotation has opposite sign for particles symmetrically located around collision axes.
- This topic was investigated immediately after the scheme for polarized positron production was invented. This effect is not associated with polarized positron production exclusively because this effect tolerates the polarization of electrons at IP as well. Later many authors also considered this topic in detail. General conclusion here is that depolarization remains at the level $\sim 5\%$

E.A. Kushnirenko, A. A. Likhoded, M.V. Shevlyagin, “*Depolarization Effects for Collisions of Polarized beams*”, IHEP 93-131, SW 9430, Protvino 1993.

Spin flip in undulator

Positron or electron may flip its spin direction while radiating in magnetic field. Probability:

$$\frac{1}{\tau} [\text{sec}^{-1}] = w_{flip} = \frac{5\sqrt{3}}{16} \frac{r_0^2}{\alpha} \frac{\omega_0^3}{c^2} \gamma^5 \left(1 - \frac{2}{9} \zeta_{\parallel}^2 - \frac{8\sqrt{3}}{15} \frac{e}{|e|} \zeta_{\perp} \right)$$

Probability of radiation:

$$w_{rad} \cong \frac{I}{\hbar \omega_0 2\gamma^2} = \frac{2}{3} \frac{e^4 H^2 \gamma^2}{m^2 c^3} \frac{1}{\hbar \omega_0 2\gamma^2} = \frac{1}{3} \alpha \gamma^2 \omega_0$$

$$\lambda_c = r_0 / \alpha = e^2 / mc^2 / \alpha \cong 3.8616 \cdot 10^{-11}$$

The ratio

$$\frac{w_{flip}}{w_{rad}} = \frac{15\sqrt{3}}{16} \frac{\lambda_c^2}{\lambda_u^2} \gamma^3 \left(1 - \frac{2}{9} \zeta_{\parallel}^2 - \frac{8\sqrt{3}}{15} \frac{e}{|e|} \zeta_{\perp} \right) \quad (\text{K} \sim 1)$$

Effect of spin flip still small (i.e. radiation is dominating).

KINEMATIC PERTURBATION OF POLARIZATION

Kinematical perturbations due to multiple scattering in a target

Let us consider the possible effect of *kinematical* depolarization associated with rotation of spin vector while particle experience multiple scattering in media of target before leaving. Typically polarized positron carries out $\sim(0.5-1)\hbar\omega$ -energy of gamma quanta. As positrons/electrons created have longitudinal polarization, it is good to have assurance that during scattering in material of target polarization is not lost. Each act of scattering is Coulomb scattering in field of nuclei. So BMT equation describing the spin $\vec{\zeta}$ motion in electrical field of nuclei looks like

$$\frac{d\vec{\zeta}}{dt} = \frac{e}{mc^2\gamma} \left\{ G\gamma + \frac{\gamma}{\gamma+1} \right\} \cdot \vec{\zeta} \times (\vec{E} \times \vec{v}), \quad (A16)$$

where $\vec{E} \sim Ze\vec{r}/r^3$ stands for repulsive (for positrons) electrical field of nuclei, factor $G = \frac{g-2}{2} \cong 1.1596 \times 10^{-3} \approx \frac{\alpha}{2\pi}$. Deviation of momentum is simply $d\vec{p}/dt = e\vec{E}$.

So the spin equation becomes

$$\frac{d\vec{\zeta}}{dt} = \frac{1}{mc^2\gamma} \left\{ G\gamma + \frac{\gamma}{\gamma+1} \right\} \cdot \vec{\zeta} \times \left(\frac{d\vec{p}}{dt} \times \vec{v} \right). \quad (A17)$$

We neglected variation of energy of particle during the act of scattering, so $\frac{d\vec{p}}{dt} \cong m\gamma \frac{d\vec{v}}{dt}$ and vector \vec{p} just changes its direction. Introducing normalized velocity as usual $\vec{\beta} = \vec{v}/c$, equation of spin motion finally comes to the following

$$\frac{d\vec{\zeta}}{dt} = \left\{ G\gamma + \frac{\gamma}{\gamma+1} \right\} \cdot \vec{\zeta} \times (\vec{\beta} \times \dot{\vec{\beta}}) = \left\{ G\gamma + \frac{\gamma}{\gamma+1} \right\} \cdot \vec{\zeta} \times \frac{d\vec{\varphi}}{dt}, \quad (A18)$$

where φ stands for the scattering angle and the vector $d\vec{\varphi}/dt$ directed normally to the scattering plane. For intermediate energy of our interest $\gamma \sim 40$, so the term in bracket ~ 1 and, finally

$$\frac{d\vec{\zeta}}{dt} \cong \vec{\zeta} \times \frac{d\vec{\varphi}}{dt}. \quad (A19)$$

The last equation means that spin rotates to the same angle as the scattering one, i.e. spin follows the particle trajectory.

- See A.Mikhailichenko, CBN 06-1, Cornell LEPP, 2006.

Fragment from CBN 06-1

Filling positron ring from electron source

