

PROBING FLAVOUR WITH NEUTRINOS

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OUTLINE

Introduction:

The Parameters of the New Minimal Standard Model

Update on ν Masses and Mixing from Global 3 ν Mixing Analysis

Near Future Expectations and Far Future Challenges

And what about LSND?

Beyond Masses and Mixing

Flavour Tests of Fundamental Symmetries (LI, WEP, CPT), NSNI ...

Summary

ν in the SM

- The SM is a gauge theory based on the symmetry group

$$SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow SU(3)_C \times U(1)_{EM}$$

$(1, 2)_{-\frac{1}{2}}$	$(3, 2)_{\frac{1}{6}}$	$(1, 1)_{-1}$	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$
$\begin{pmatrix} e \\ \nu_e \end{pmatrix}_L$	$\begin{pmatrix} u^i \\ d^i \end{pmatrix}_L$	e_R	u^i_R	d^i_R
$\begin{pmatrix} \mu \\ \nu_\mu \end{pmatrix}_L$	$\begin{pmatrix} c^i \\ s^i \end{pmatrix}_L$	μ_R	c^i_R	s^i_R
$\begin{pmatrix} \tau \\ \nu_\tau \end{pmatrix}_L$	$\begin{pmatrix} t^i \\ b^i \end{pmatrix}_L$	τ_R	t^i_R	n^i_R

There is no ν_R

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\Rightarrow Accidental global symmetry:
 $B \times L_e \times L_\mu \times L_\tau$

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\Rightarrow **There is no ν_R**
 \Rightarrow **Accidental global symmetry:**
 $B \times L_e \times L_\mu \times L_\tau$

\Rightarrow **ν strictly massless**

- We have learned:

- * Atmospheric ν_μ disappear ($> 15\sigma$) most likely to ν_τ
- * K2K: accelerator ν_μ disappear at $L \sim 250$ Km with E -distortion ($\sim 2.5\text{--}4\sigma$)
- * MINOS: accelerator ν_μ disappear at $L \sim 735$ Km with E -distortion ($\sim 5\sigma$)
- * Solar ν_e convert to ν_μ or ν_τ ($> 7\sigma$)
- * KamLAND: reactor $\bar{\nu}_e$ disappear at $L \sim 200$ Km with E -distortion ($\gtrsim 3\sigma$ CL)
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- The *important* question:

What is the underlying physics?

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All this implies that neutrinos are massive

- The *important* question:

What is the underlying physics?

- The *difficult* path:

Detailed determination of the new LE parameters

- Minimal Extensions to give Mass to the Neutrino:

- * Introduce ν_R AND impose L conservation \Rightarrow Dirac ν :

$$\mathcal{L} = \mathcal{L}_{SM} - M_\nu \overline{\nu}_L \nu_R + h.c.$$

- * NOT impose L conservation \Rightarrow Majorana ν

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{2} M_\nu \overline{\nu}_L \nu_L^C + h.c.$$

Effects of ν Mass

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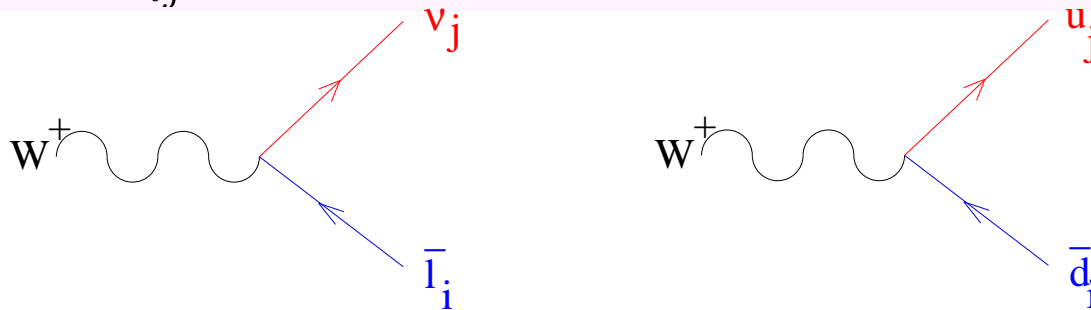
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- The charged current interactions of leptons are not diagonal

$$\frac{g}{\sqrt{2}} W_\mu^+ \sum_{ij} (U_{LEP}^{ij} \bar{\ell}^i \gamma^\mu L \nu^j + U_{CKM}^{ij} \bar{U}^i \gamma^\mu L D^j) + h.c.$$



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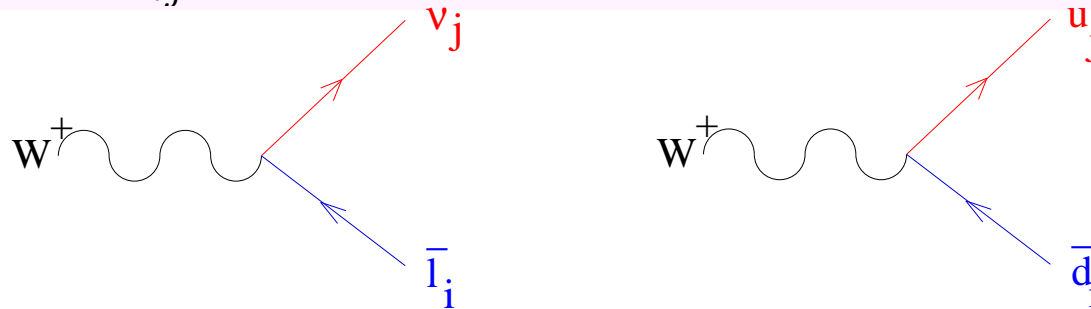
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- In general for $N = 3 + m$ massive neutrinos U_{LEP} is $3 \times N$ matrix

$$U_{LEP} U_{LEP}^\dagger = I_{3 \times 3} \quad \text{but in general} \quad U_{LEP}^\dagger U_{LEP} \neq I_{N \times N}$$

- U_{LEP} : $3(N - 2)$ angles + $2N - 5$ Dirac phases + $N - 1$ Majorana phases

Effects of ν Mass: Oscillations

- If neutrinos have mass, a weak eigenstate $|\nu_\alpha\rangle$ produced in $l_\alpha + N \rightarrow \nu_\alpha + N'$

is a linear combination of the mass eigenstates ($|\nu_i\rangle$): $|\nu_\alpha\rangle = \sum_{i=1}^n U_{\alpha i} |\nu_i\rangle$

- After a distance L it can be detected with flavour β with probability

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{j \neq i}^n \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\frac{\Delta_{ij}}{2} \right) + 2 \sum_{j \neq i} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin(\Delta_{ij})$$

$$\frac{\Delta_{ij}}{2} = \frac{(E_i - E_j)L}{2} = 1.27 \frac{(m_i^2 - m_j^2)}{\text{eV}^2} \frac{L/E}{\text{Km/GeV}}$$

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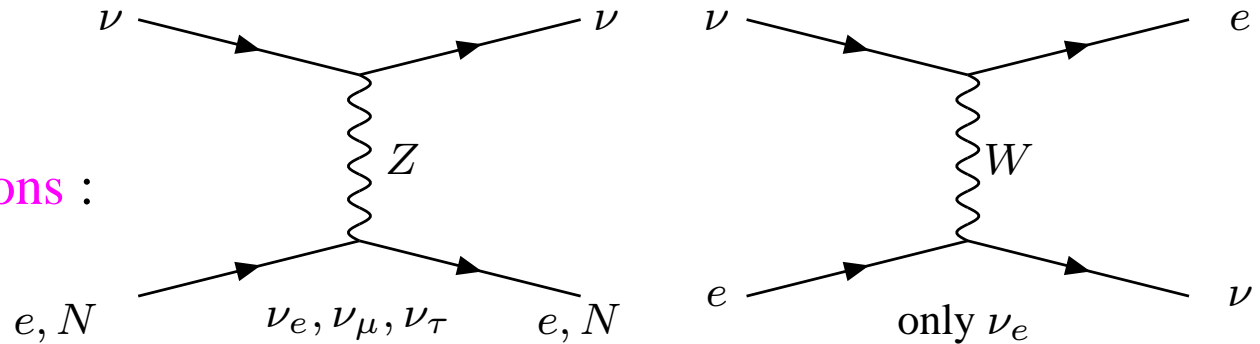
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No information on mass scale nor Majorana versus Dirac ν nature

Matter Effects

- If ν cross **matter** regions (Sun, Earth...) it interacts *coherently*

– But **Different flavours** have **different interactions** :



– To include this effect: **potential in the evolution equation: $V_e \neq V_\mu$**

\Rightarrow Modification of mixing angle and oscillation wavelength

- The mixing angle in matter

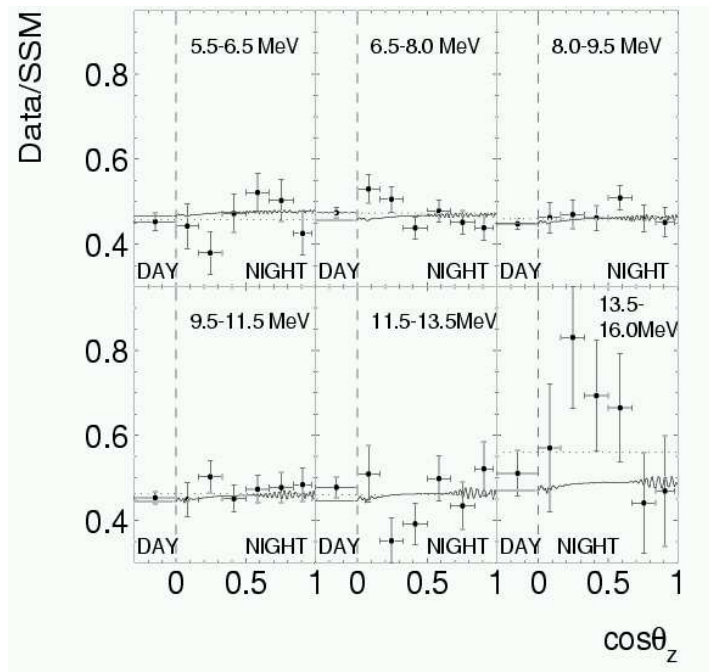
$$\sin(2\theta_m) = \frac{\Delta m^2 \sin(2\theta)}{\sqrt{(\Delta m^2 \cos(2\theta) - A)^2 + (\Delta m^2 \sin(2\theta))^2}} \quad A = 2E(V_\alpha - V_\beta)$$

– When $\Delta m^2 \cos(2\theta) \sim A \Rightarrow$ **Enhancement of Oscillation (MSW Effect)**

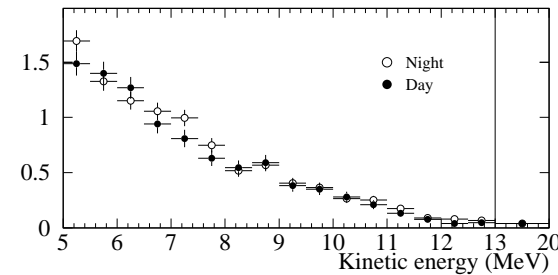
* $\Sigma(\text{Cl}) = 2.56 \pm 0.23$ (SNU)

* $\Sigma(\text{Ga}) = 68.1 \pm 3.75$ (SNU)

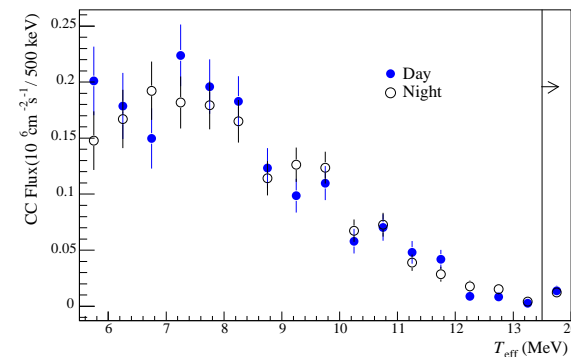
* SK Zenith spectrum (44 Data points)



* SNO Ph-I D-N Spectrum (34 Points)



* SNO Ph-II CC D-N Spec (34 Points)



* SNO Ph-II ES, NC D&N Fluxes (4)

$\phi_{\text{ES,D}}^{\text{SNO}} = 2.17 \pm 0.34 \pm 0.14$

$\phi_{\text{ES,N}}^{\text{SNO}} = 2.52 \pm 0.32 \pm 0.16$

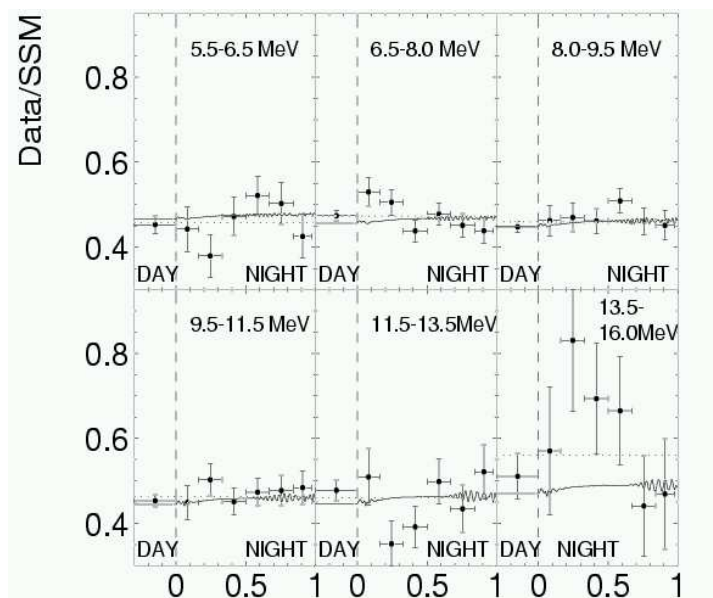
$\phi_{\text{NC,D}}^{\text{SNO}} = 4.81 \pm 0.31 \pm 0.39$

$\phi_{\text{NC,N}}^{\text{SNO}} = 5.02 \pm 0.29 \pm 0.16$

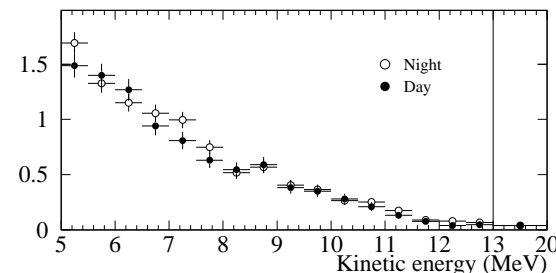
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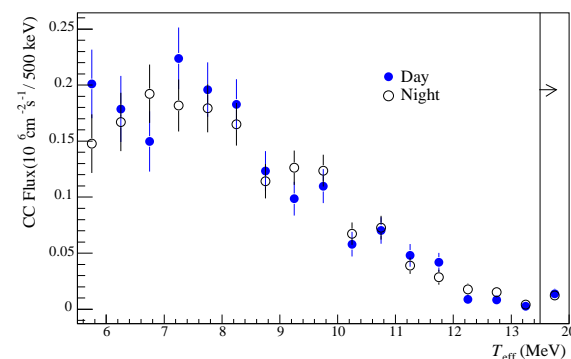
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All experiments measuring mostly ν_e observed a deficit

Deficit is energy dependent for $E_\nu \lesssim 5 \text{ MeV}$

Deficit disappears in NC

Seasonal Variation \Rightarrow Nothing beyond $1/R^2$

Very small Day-Night Variation \Rightarrow No Earth Matter Effect

CC D&N Fluxes (4)

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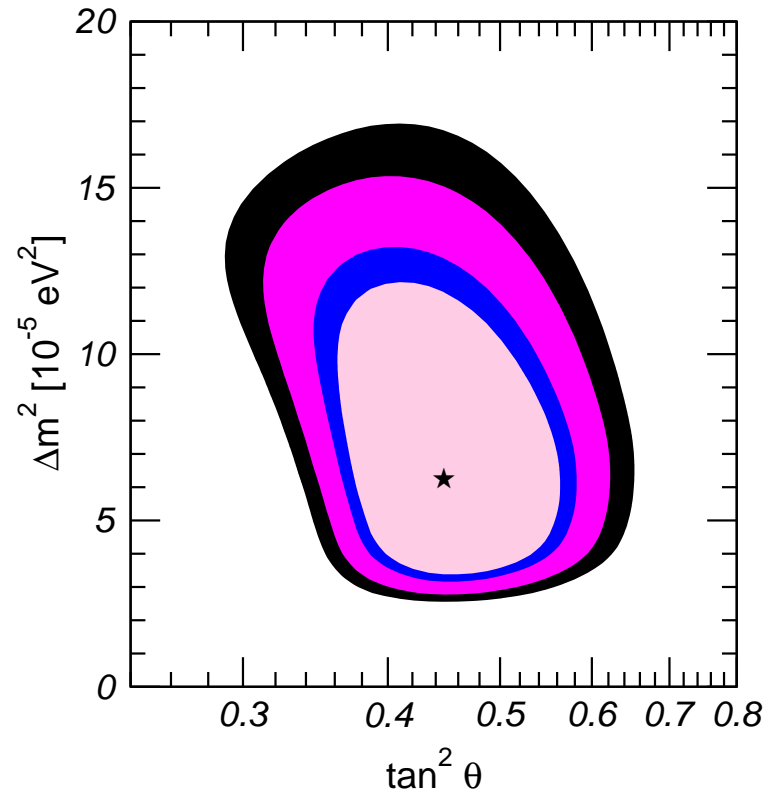
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Solar Neutrinos: Oscillation Solutions

- $\nu_e \rightarrow \nu_\mu, \nu_\tau$:



CL

3 σ

99

95

90

Best fit

$$\Delta m^2 = 6.3 \times 10^{-5} \text{ eV}^2$$

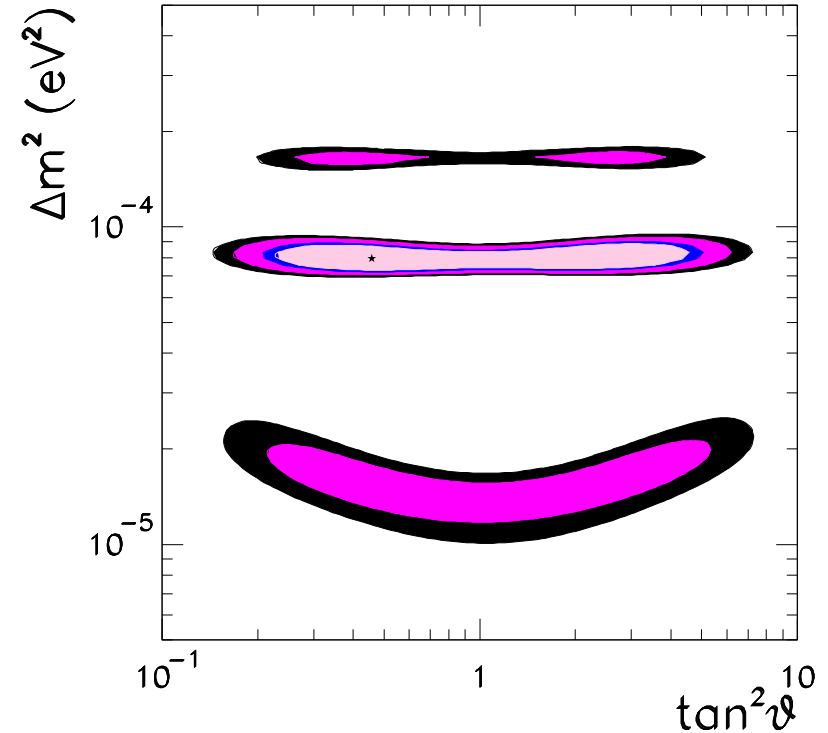
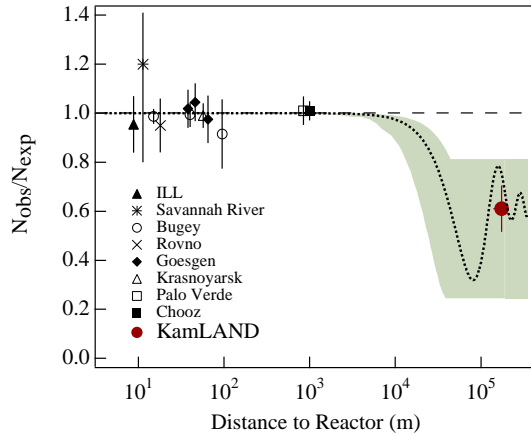
$$\tan^2 \theta = 0.44$$

Terrestrial Test of LMA: KamLAND

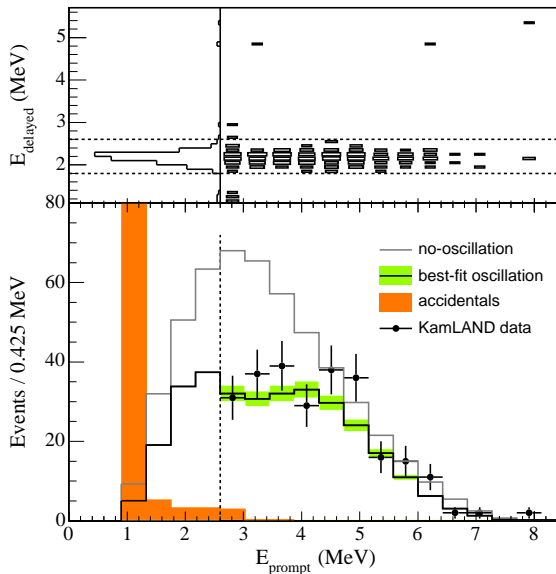
- Search on $\bar{\nu}_e$ at $L \sim 180$ km reactors, $E_{\bar{\nu}} \sim$ few MeV: $\bar{\nu}_e + p \rightarrow n + e^+$

2002: Deficit $R_{\text{KamLAND}} = 0.611 \pm 0.094$

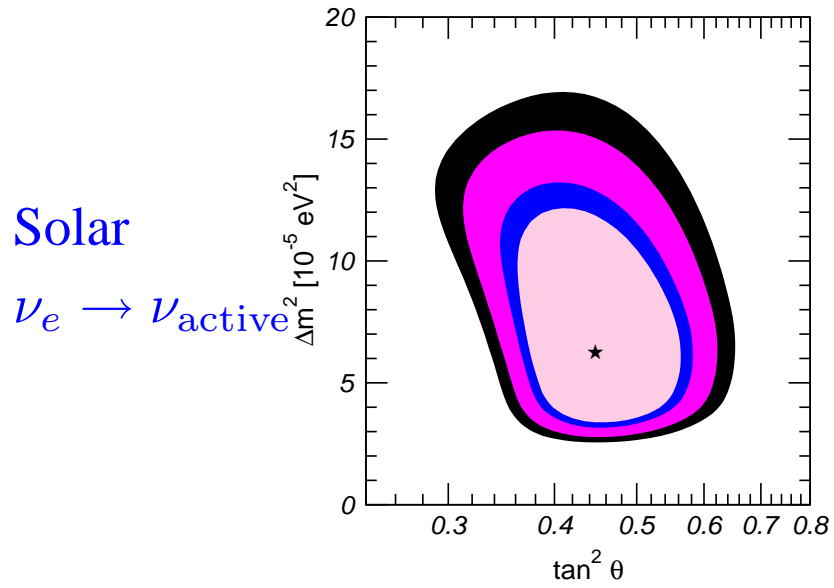
Oscillation Analysis



2004: Significant Energy Distortion

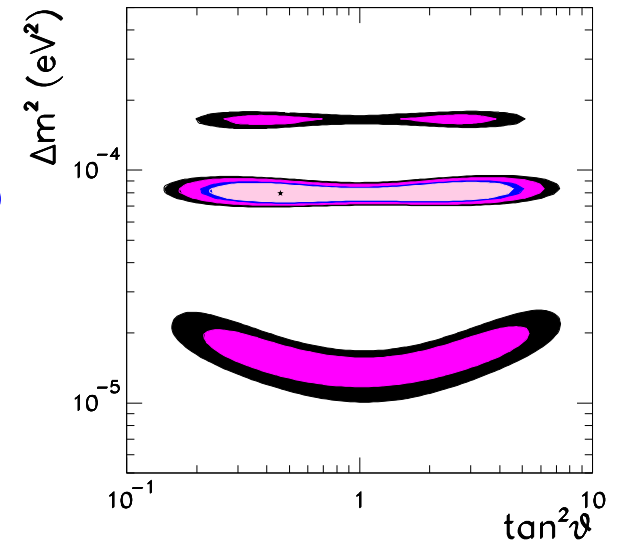


Best Fit
 $\Delta m^2 = 7.9 \times 10^{-5} \text{ eV}^2$
 $\tan^2 \theta = 0.46 \quad (2.2)$



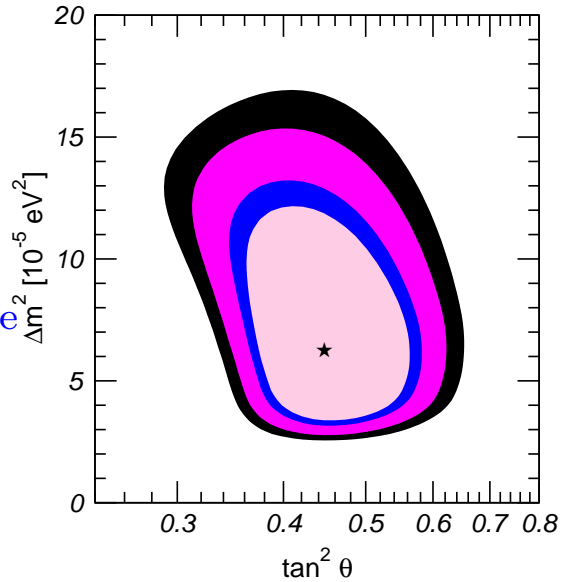
+ KamLAND

$\bar{\nu}_e \rightarrow \bar{\nu}_e$



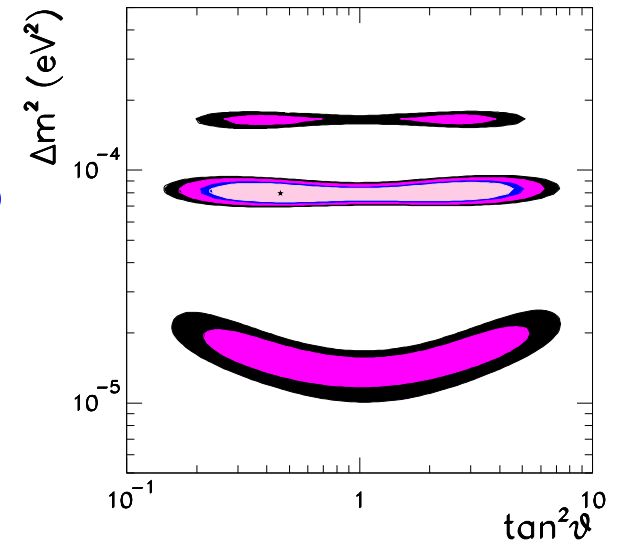
Solar

$\nu_e \rightarrow \nu_{\text{active}}$

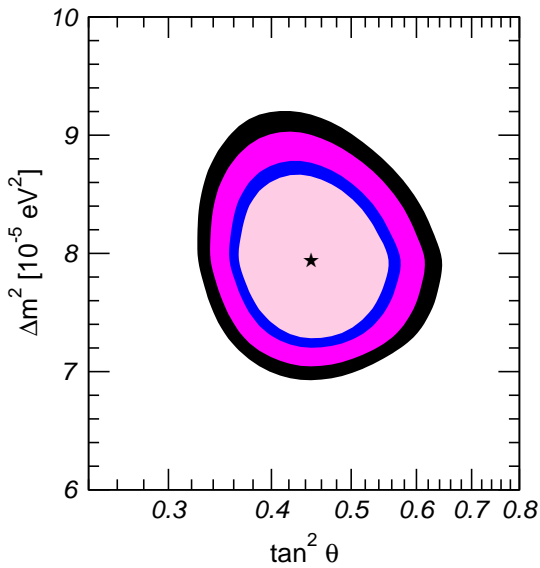


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$\bar{\nu}_e \nrightarrow \bar{\nu}_e$



ν_e oscillation parameters compatible with $\bar{\nu}_e$: *Sensible to assume CPT: $P_{ee} = P_{\bar{e}\bar{e}}$*

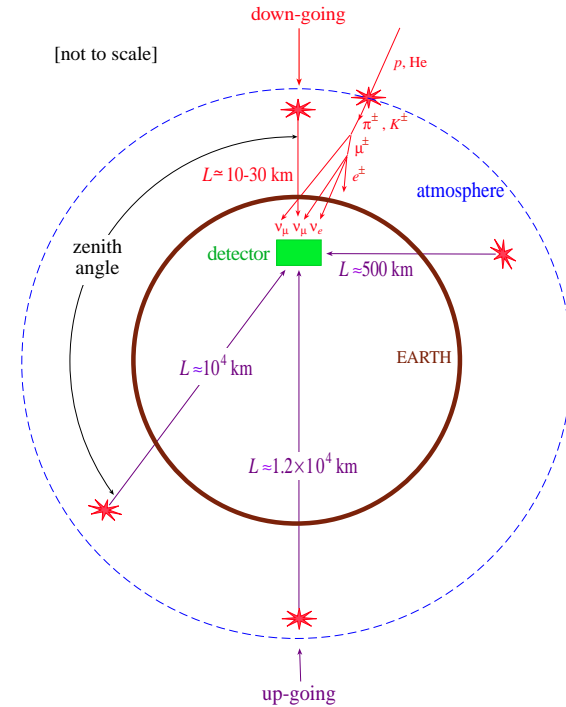
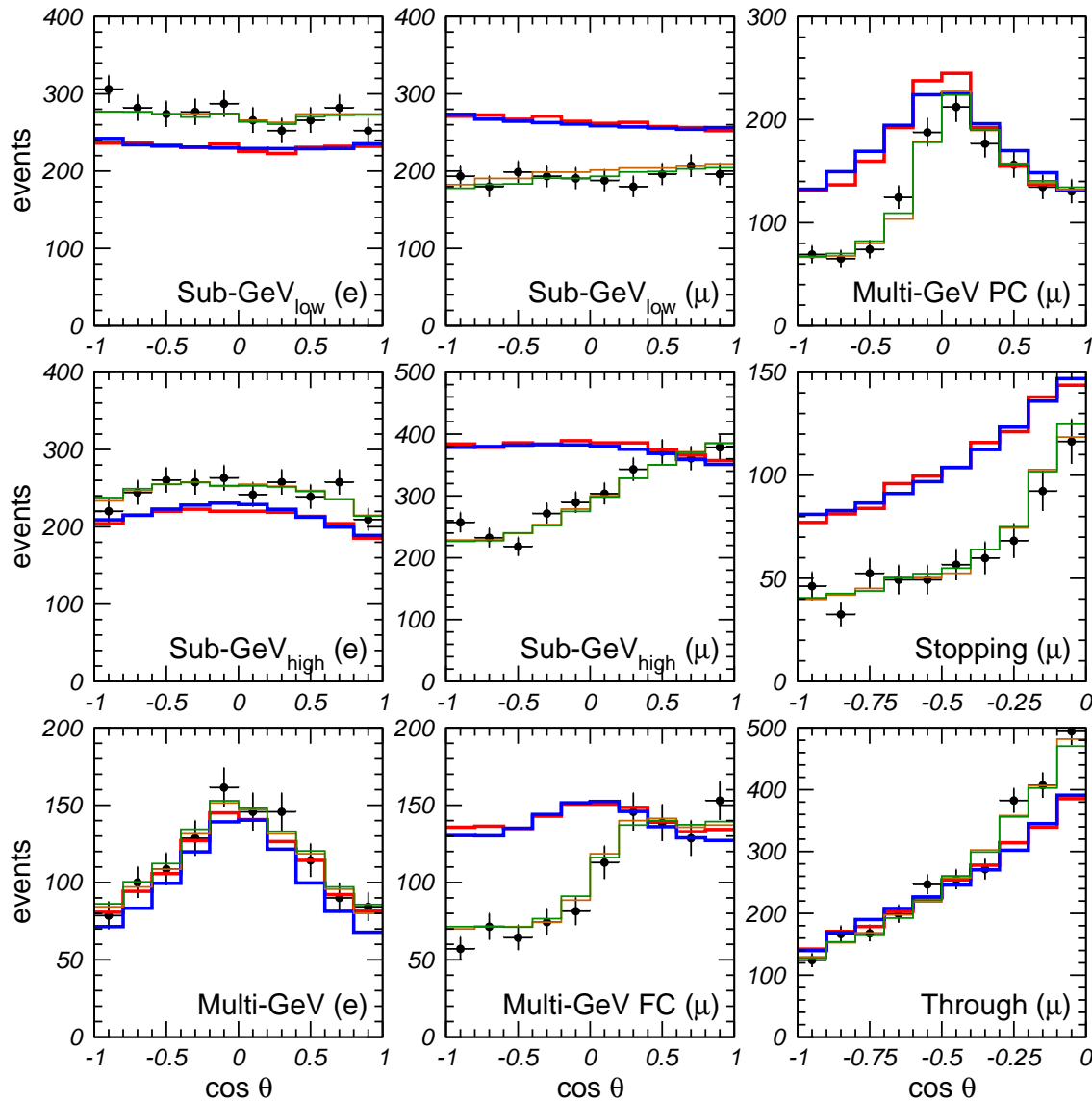


$$\Delta m^2 = (7.9^{+0.27}_{-0.28}) \times 10^{-5} \text{ eV}^2 \quad (1\sigma)$$

$$\tan^2 \theta = 0.44^{+0.045}_{-0.042}$$

Atmospheric Neutrinos

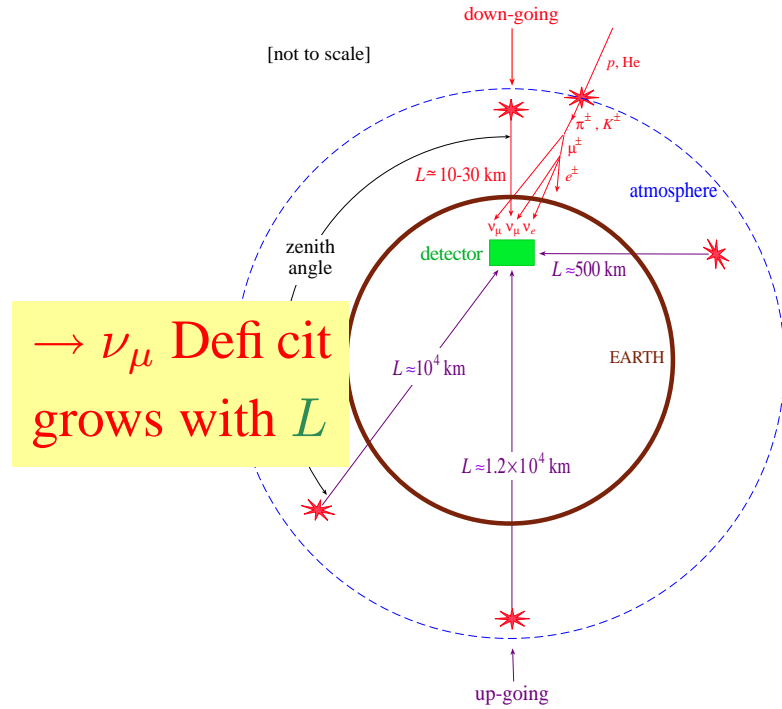
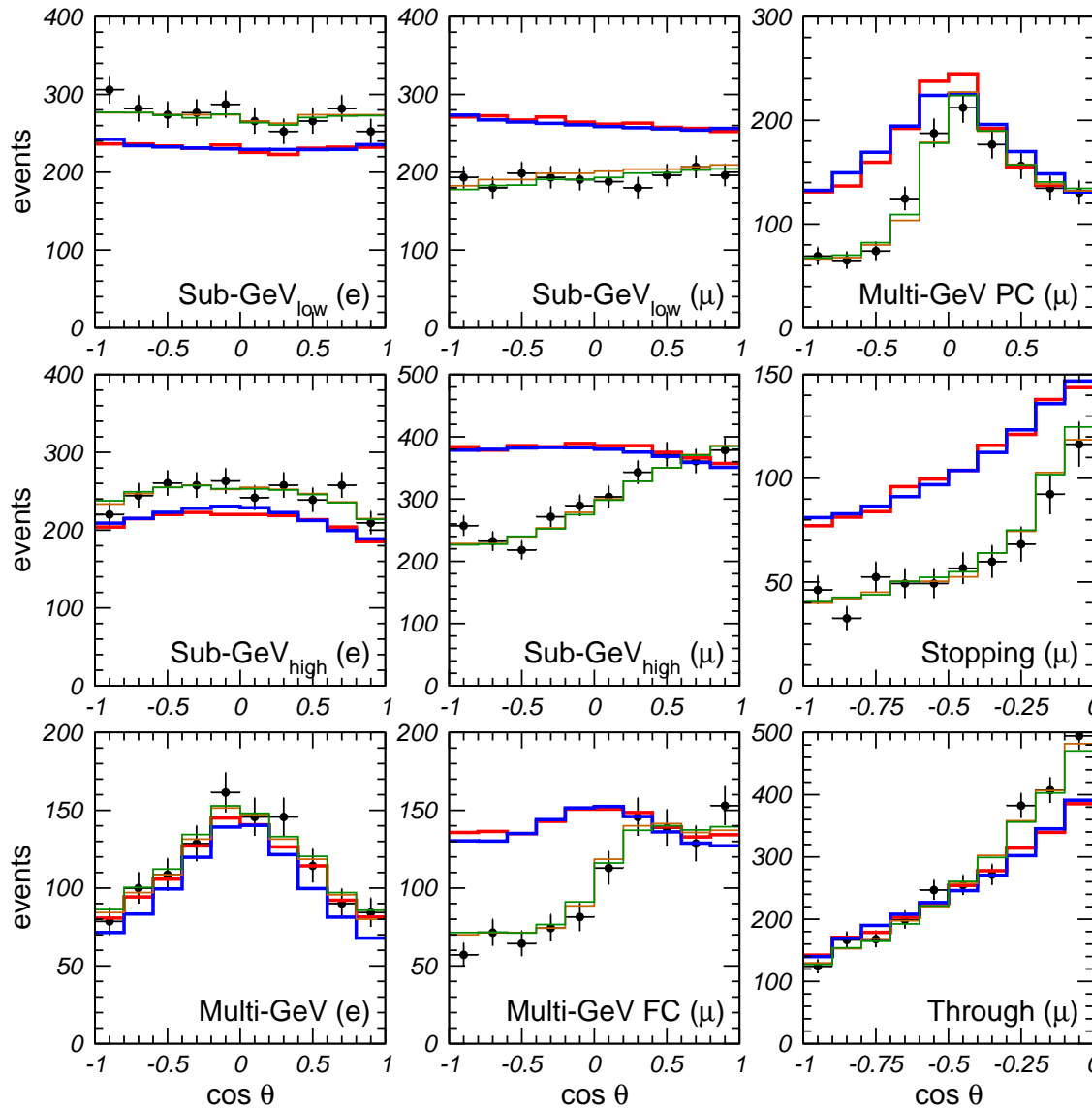
● Complete SKI+II data:



Atmospheric Neutrinos

• Complete SKI+II data:

ν_e in agreement with SM

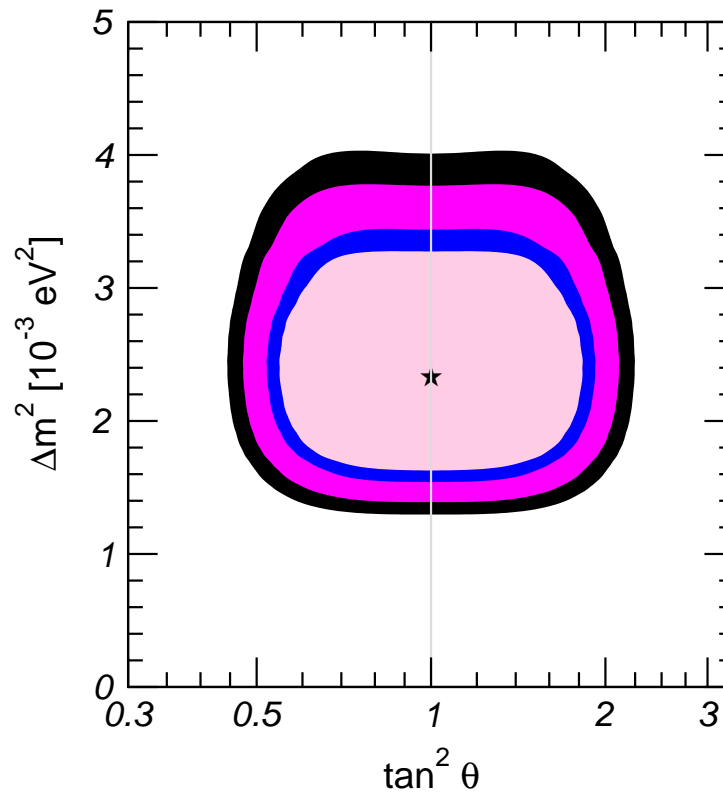


$\rightarrow \nu_\mu$ Deficit grows with L

$\rightarrow \nu_\mu$ Deficit decreases with E

Atmospheric Neutrinos: Oscillation Solutions

- $\nu_\mu \rightarrow \nu_\tau$: best channel



Best fit

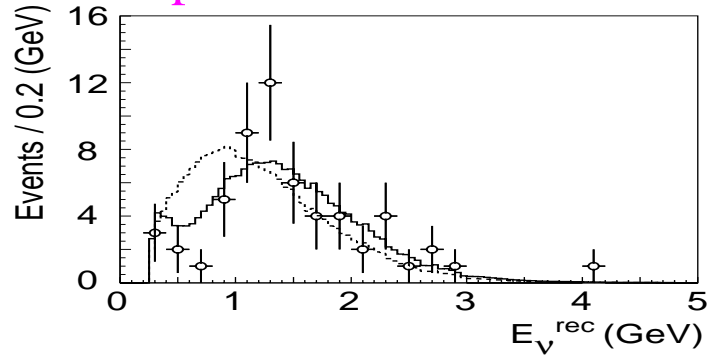
$$\Delta m^2 = 2.15 \times 10^{-3} \text{ eV}^2$$

$$\tan^2 \theta = 1$$

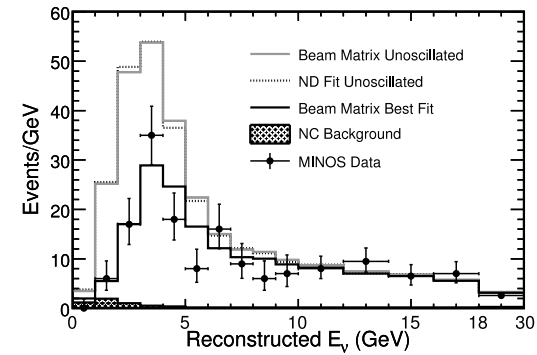
ATM Test at Long Baseline Experiments

K2K	ν_μ at KEK	SK	L=250 km
MINOS	ν_μ at Fermilab	Soundan	L=735 km
Opera	ν_μ at CERN	Gran Sasso	L=740 km

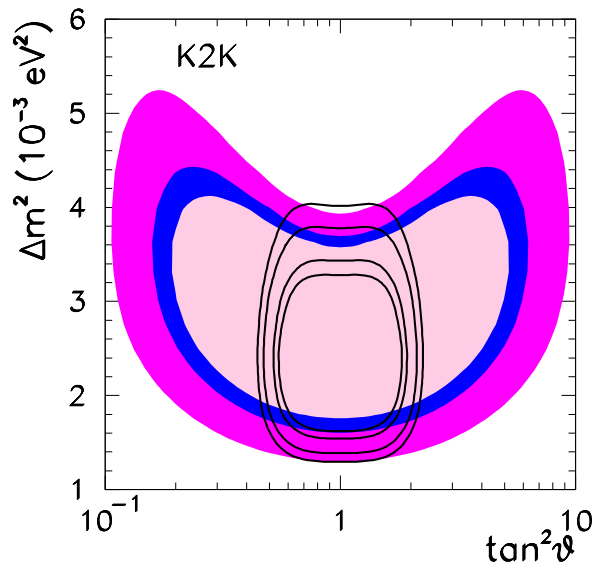
K2K 2004: spectral distortion



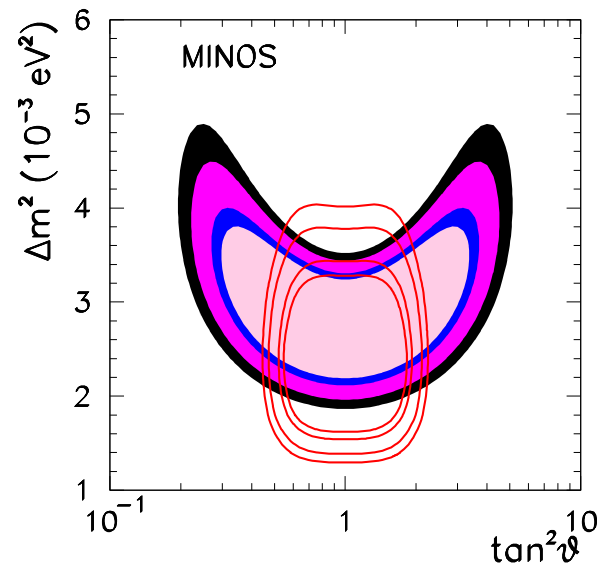
MINOS 2006: spectral distortion



Confirmation of ATM oscillations



Confirmation of ATM oscillations

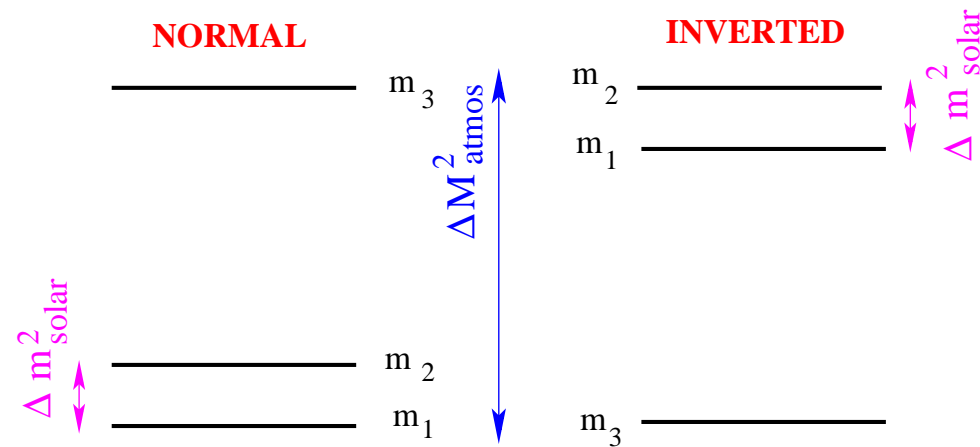


Solar+Atmospheric+Reactor+LBL 3ν Oscillations

U : 3 angles, 1 CP-phase
+ (2 Majorana phases)

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Two mass schemes

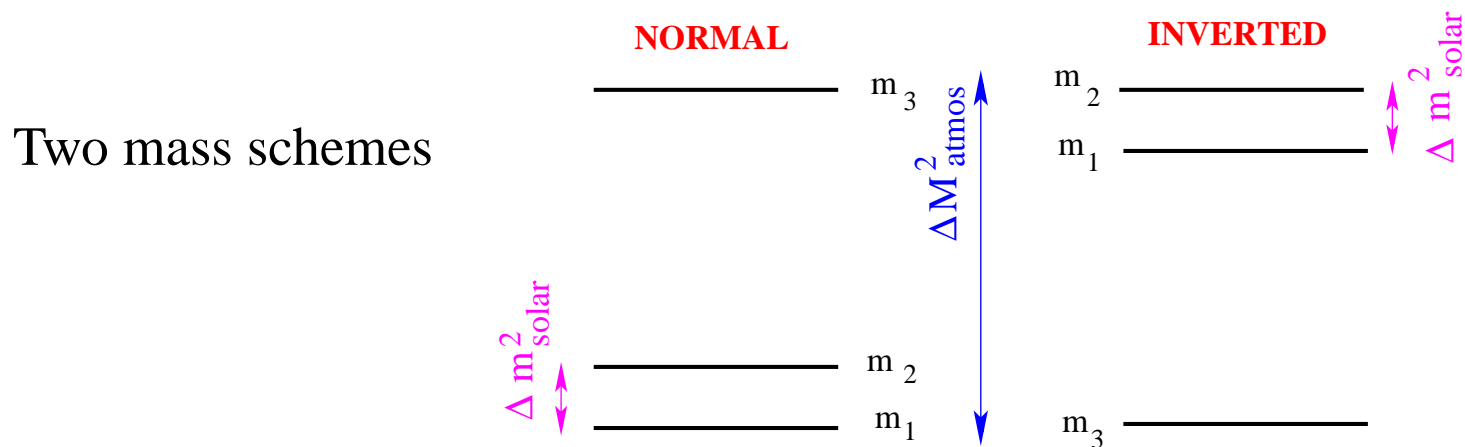


2ν oscillation analysis $\Rightarrow \Delta m_{21}^2 = \Delta m_{\odot}^2 \ll \Delta M_{atm}^2 \simeq \pm \Delta m_{32}^2 \simeq \pm \Delta m_{31}^2$

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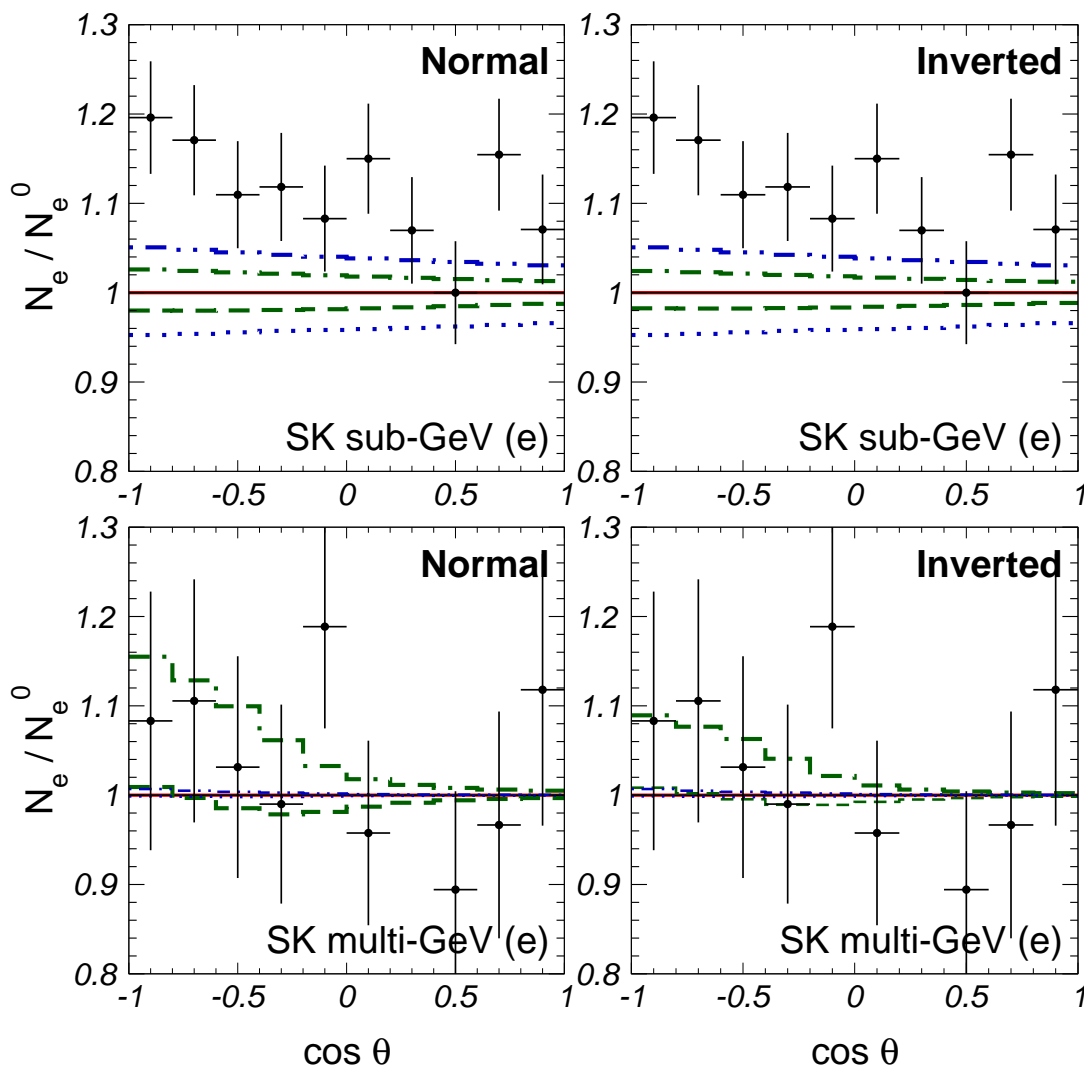
Generic 3ν mixing effects:

- Effects due to θ_{13}
- Difference between **Inverted** and **Normal**
- Interference of **two wavelength** oscillations
- **CP violation** due to phase δ

Beyond Hierarchical: Δm_{21}^2 effects in ATM Data

Smirnov, Peres 99,01; Fogli, Lisi, Marrone 01; MC G-G, Maltoni 02; MCG-G, Maltoni, Smirnov 04

Best at electron samples



- $s_{13}^2=0.04, s_{23}^2=0.35, \Delta m_{21}^2=0$
- .-. $s_{13}^2=0.04, s_{23}^2=0.65, \Delta m_{21}^2=0$
- $s_{13}^2=0.00, s_{23}^2=0.35, \Delta m_{21}^2=10^{-4} \text{ eV}^2$
- $s_{13}^2=0.00, s_{23}^2=0.65, \Delta m_{21}^2=10^{-4} \text{ eV}^2$

- For $\Delta m_{21}^2 \neq 0$ and $\theta_{13} = 0$:

$$\frac{N_e}{N_{e0}} - 1 \sim \left(c_{23}^2 - \frac{1}{\bar{r}} \right)$$

$$\left[\bar{r} = \frac{N_{\mu 0}}{N_{e0}} \simeq 2 \right]$$

⇒ Sensitivity to Octant of θ_{23} !!!

Most important for Sub-GeV e

- For $\Delta m_{21}^2 = 0$ and $\theta_{13} \neq 0$ the opposite:

$$\frac{N_e}{N_{e0}} - 1 \sim \left(s_{23}^2 - \frac{1}{\bar{r}} \right)$$

Most important for Multi-GeV e

Beyond Hierarchical: Effect $\theta_{13} \times \Delta m_{21}^2$ in ATM

Smirnov, Peres 01,03, MC G-G, Maltoni 02

For sub-GeV energies

$$\frac{N_e}{N_e^0} - 1 \simeq \overline{P_{e2}} \overline{r} (c_{23}^2 - \frac{1}{\overline{r}}) + 2 \tilde{s}_{13}^2 \overline{r} (s_{23}^2 - \frac{1}{\overline{r}}) - \overline{r} \tilde{s}_{13} \tilde{c}_{13}^2 \sin 2\theta_{23} (\cos \delta_{CP} \overline{R_2} - \sin \delta_{CP} \overline{I_2})$$

$$P_{e2} = \sin^2 2\theta_{12,m} \sin^2 \frac{\phi_m}{2}$$

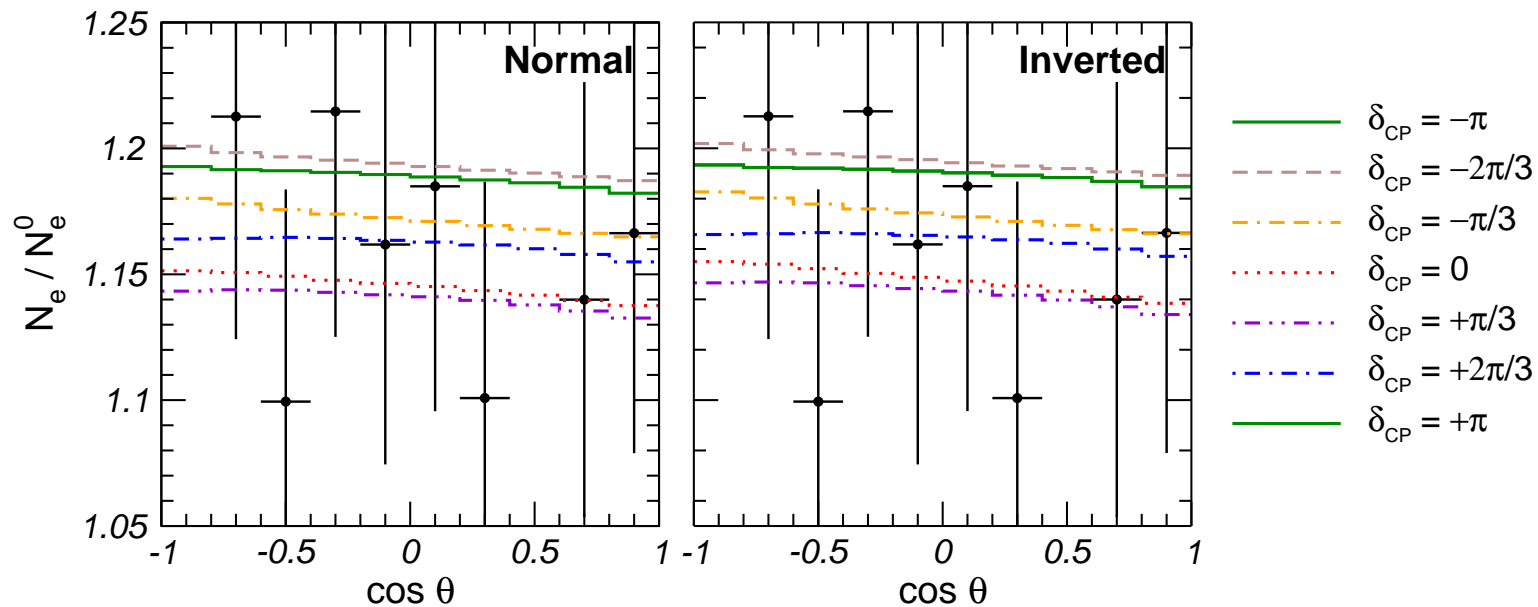
$$\sin 2\theta_{12,m} = \frac{\sin 2\theta_{12}}{\sqrt{(\cos 2\theta_{12} \mp \frac{2E_\nu V_e}{\Delta m_{21}^2})^2 + \sin^2 2\theta_{12}}}$$

$$R_2 = -\sin 2\theta_{12,m} \cos 2\theta_{12,m} \sin^2 \frac{\phi_m}{2}$$

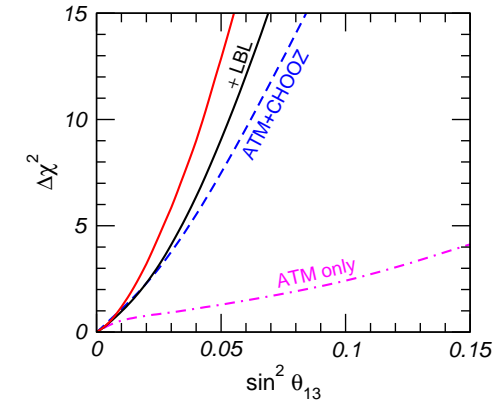
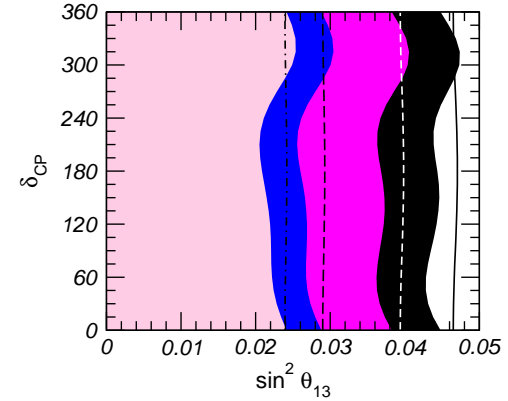
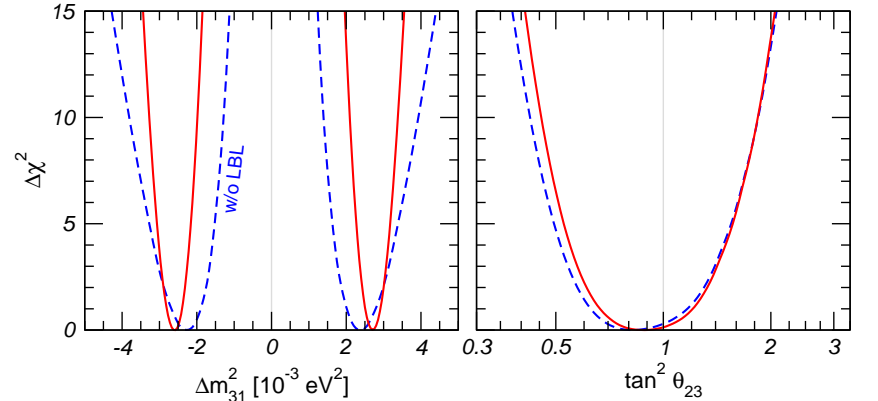
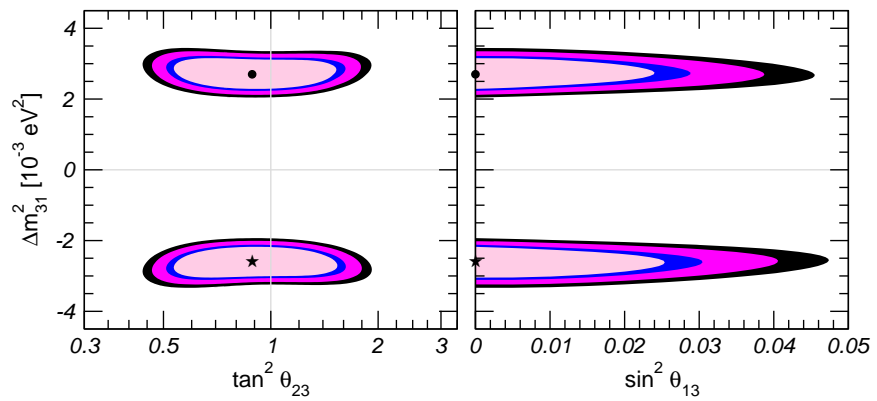
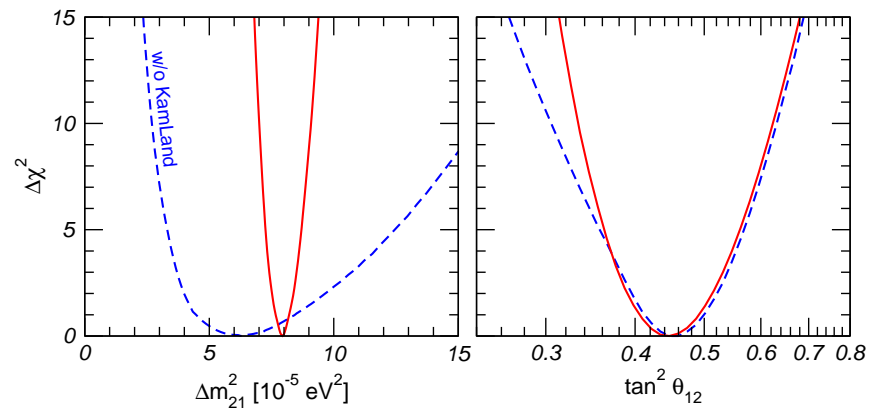
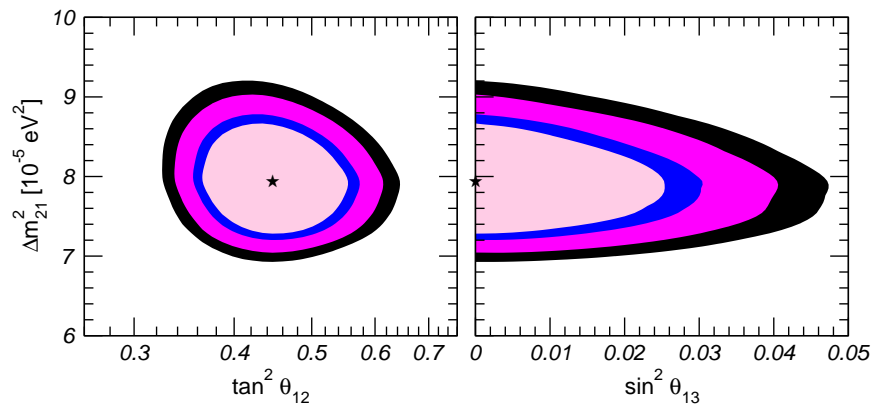
$$I_2 = -\frac{1}{2} \sin 2\theta_{12,m} \sin \phi_m$$

$$\tilde{\theta}_{13} \approx \theta_{13} \left(1 + \frac{2E_\nu V_e}{\Delta m_{31}^2} \right)$$

$$\phi \approx (\Delta m_{31}^2 + s_{12}^2 \Delta m_{21}^2) \frac{L}{2E_\nu}$$



Global Analysis: Three Neutrino Oscillations



Global Analysis: Three Neutrino Oscillations

The derived ranges for the six parameters at 1σ (3σ) are:

$$\begin{aligned} \Delta m_{21}^2 &= 7.9_{-0.28}^{+0.27} \left({}_{-0.89}^{+1.1} \right) \times 10^{-5} \text{ eV}^2 & |\Delta m_{31}^2| &= 2.6 \pm 0.2 \left(0.6 \right) \times 10^{-3} \text{ eV}^2 \\ \theta_{12} &= 33.7 \pm 1.3 \left({}_{-3.5}^{+4.3} \right) & \theta_{23} &= 43.3_{-3.8}^{+4.3} \left({}_{-8.8}^{+9.8} \right) \\ \theta_{13} &= 0_{-0.0}^{+5.2} \left({}_{-0.0}^{+11.5} \right) & \delta_{\text{CP}} &\in [0, 360] \end{aligned}$$

$$|U|_{3\sigma} = \begin{pmatrix} 0.79 \rightarrow 0.86 & 0.50 \rightarrow 0.61 & 0.00 \rightarrow 0.20 \\ 0.25 \rightarrow 0.53 & 0.47 \rightarrow 0.73 & 0.56 \rightarrow 0.79 \\ 0.21 \rightarrow 0.51 & 0.42 \rightarrow 0.69 & 0.61 \rightarrow 0.83 \end{pmatrix}$$

$$\sim \begin{pmatrix} \frac{1}{\sqrt{2}}(1 + \lambda) & \frac{1}{\sqrt{2}}(1 - \lambda) & \epsilon \\ \frac{1}{2}(1 - \lambda + \Delta + \epsilon \cos \delta) & \frac{1}{2}(1 + \lambda + \Delta - \epsilon \cos \delta) & \frac{1}{\sqrt{2}}(1 - \Delta) \\ \frac{1}{2}(1 - \lambda - \Delta - \epsilon \cos \delta) & \frac{1}{2}(1 + \lambda - \Delta + \epsilon \cos \delta) & \frac{1}{\sqrt{2}}(1 + \Delta) \end{pmatrix}$$

With 1σ ranges

$$\lambda \simeq 0.18 \pm 0.02 \quad \Delta \simeq 0.03 \pm 0.07 \quad \epsilon \leq 0.09 \quad -1 \leq \cos \delta \leq 1$$

Open Questions

We still ignore:

- (1) Is $\theta_{13} \neq 0$? How small?
- (2) Is $\theta_{23} = \frac{\pi}{4}$? If not, is it $>$ or $<$?
- (3) Is there CP violation in the leptons (is $\delta \neq 0, \pi$)?
- (4) What is the ordering of the neutrino states?
- (5) Are neutrino masses:
 - hierarchical: $m_i - m_j \sim m_i + m_j$?
 - degenerated: $m_i - m_j \ll m_i + m_j$?
- (6) Dirac or Majorana?

Neutrino Mass Scale: Tritium β Decay

- Fermi proposed a kinematic search of ν_e mass from beta spectra in ${}^3\text{H}$ beta decay



- For “allowed” nuclear transitions, the electron spectrum is given by phase space alone

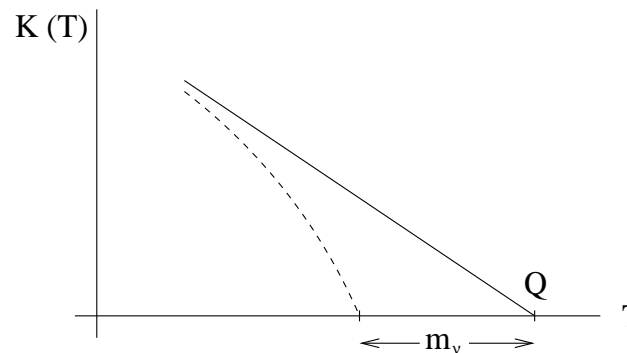
$$K(T) \equiv \sqrt{\frac{dN}{dT} \frac{1}{C_p E F(E)}} \propto \sqrt{(Q - T) \sqrt{(Q - T)^2 - m_\nu^2}}$$

$T = E_e - m_e$, $Q =$ maximum kinetic energy, (for ${}^3\text{H}$ beta decay $Q = 18.6$ KeV)

- $m_\nu \neq 0 \Rightarrow$ distortion from the straight-line at the end point of the spectrum

$$m_\nu = 0 \Rightarrow T_{\text{max}} = Q$$

$$m_\nu \neq 0 \Rightarrow T_{\text{max}} = Q - m_\nu$$



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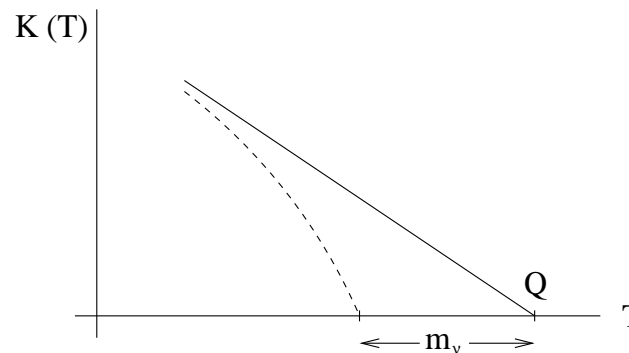
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- At present only a bound:

$$m_{\nu_e}^{eff} \equiv \sqrt{\sum m_j^2 |U_{ej}|^2} < 2.2 \text{ eV (at 95 \% CL)} \\ \text{(Mainz \& Troisk experiments)}$$

- Katrin proposed to improve present sensitivity to $m_{eff}^\beta \sim 0.3 \text{ eV}$

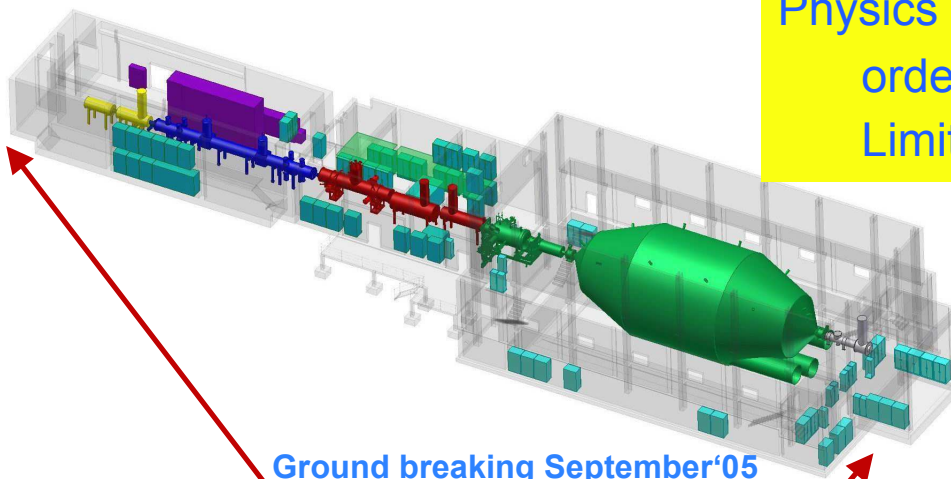
m_ν "Near" Future: Katrin

KARlsruhe TRITium Neutrino experiment - KATRIN

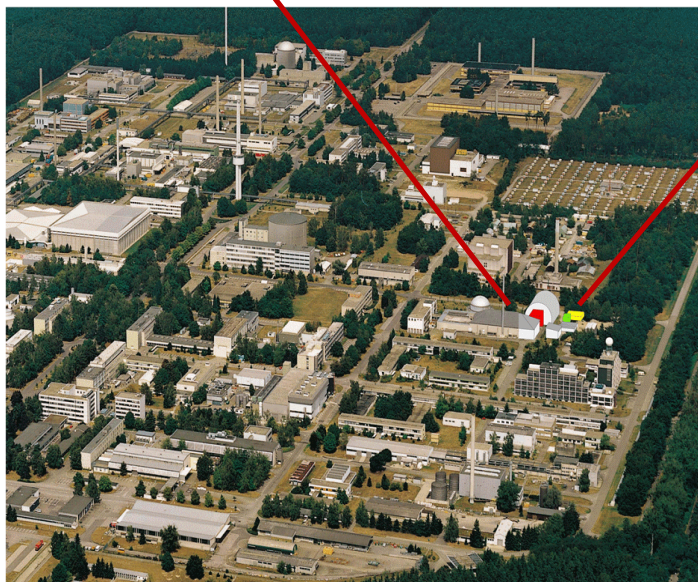


Physics Goal:

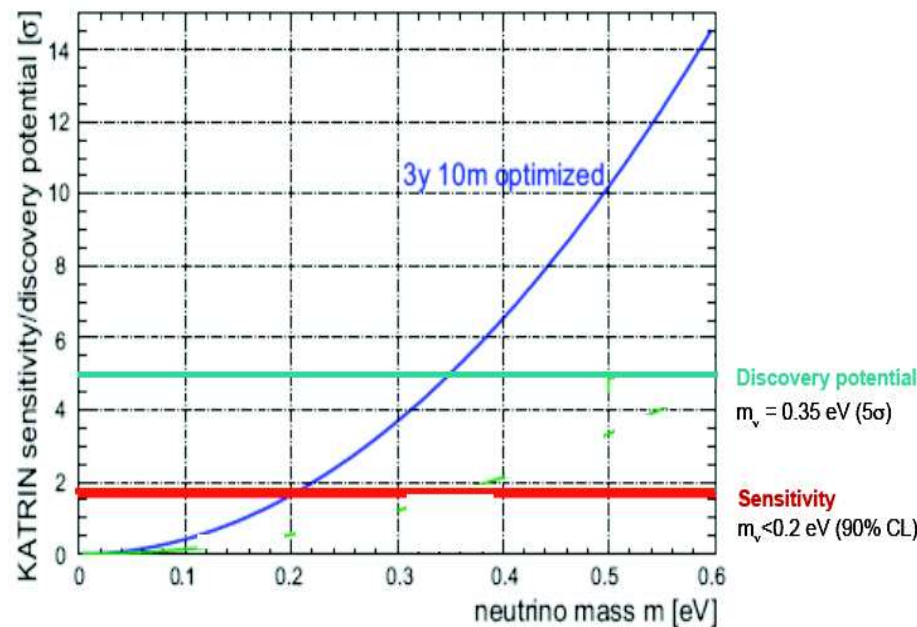
order of magnitude improvement in m_ν
 Limit m_ν 2.2 eV \rightarrow 0.2 eV



Ground breaking September'05



Expect after 3 full beam years $\sigma_{\text{sys}} \approx \sigma_{\text{stat}}$
 (~ 5 calendar years)

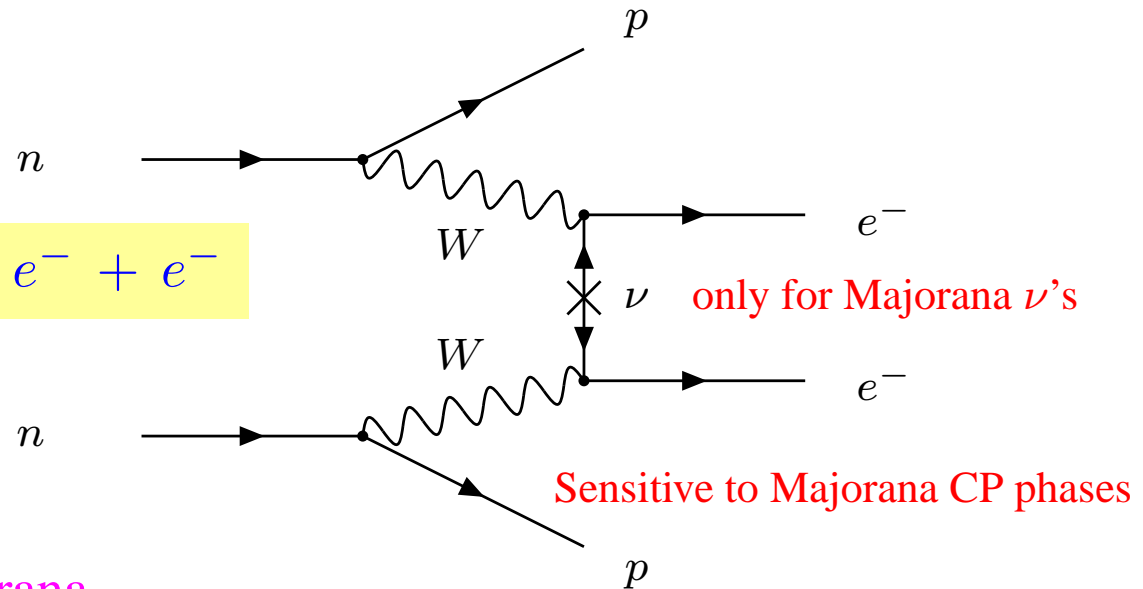


First data Fall 2009

Full sensitivity 2015

Neutrino Mass Scale: ν -less Double- β Decay

$$(A, Z) \rightarrow (A, Z + 2) + e^- + e^-$$

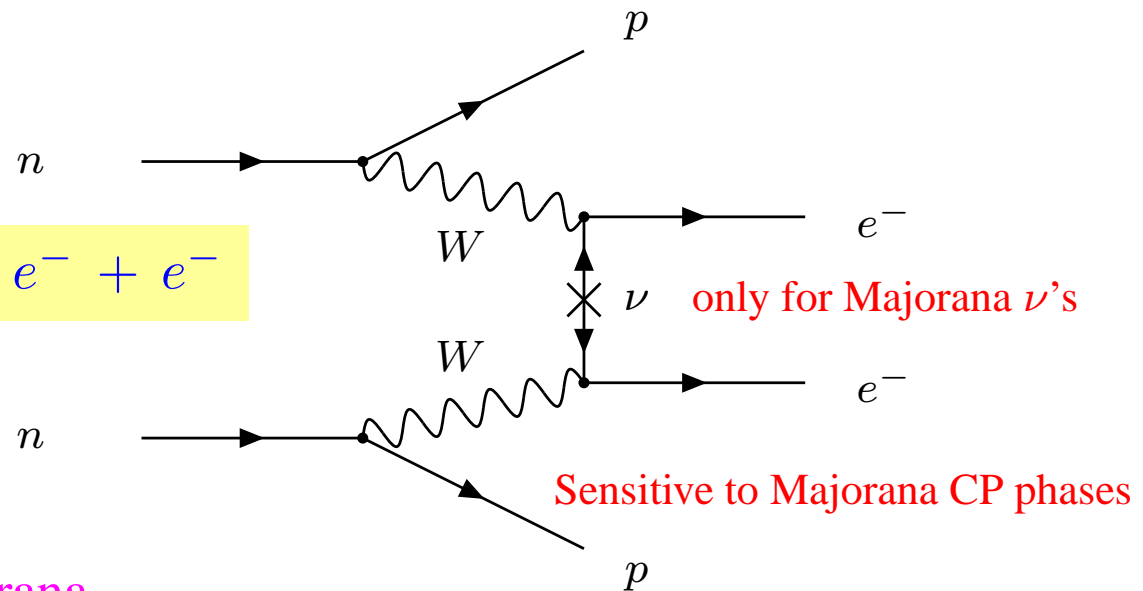


- ν -less- $\beta\beta \Leftrightarrow \nu$ is Majorana
- But Majorana m_ν maybe not unique source of L breaking
- If only Majorana $m_\nu \Rightarrow (T_{1/2}^{0\nu})^{-1} = \frac{1}{m_e^2} G^{0\nu} |M^{0\nu}|^2 \langle m_{ee} \rangle^2$ with

$$\langle m_{ee} \rangle = \left| \sum U_{ej}^2 m_j \right|$$

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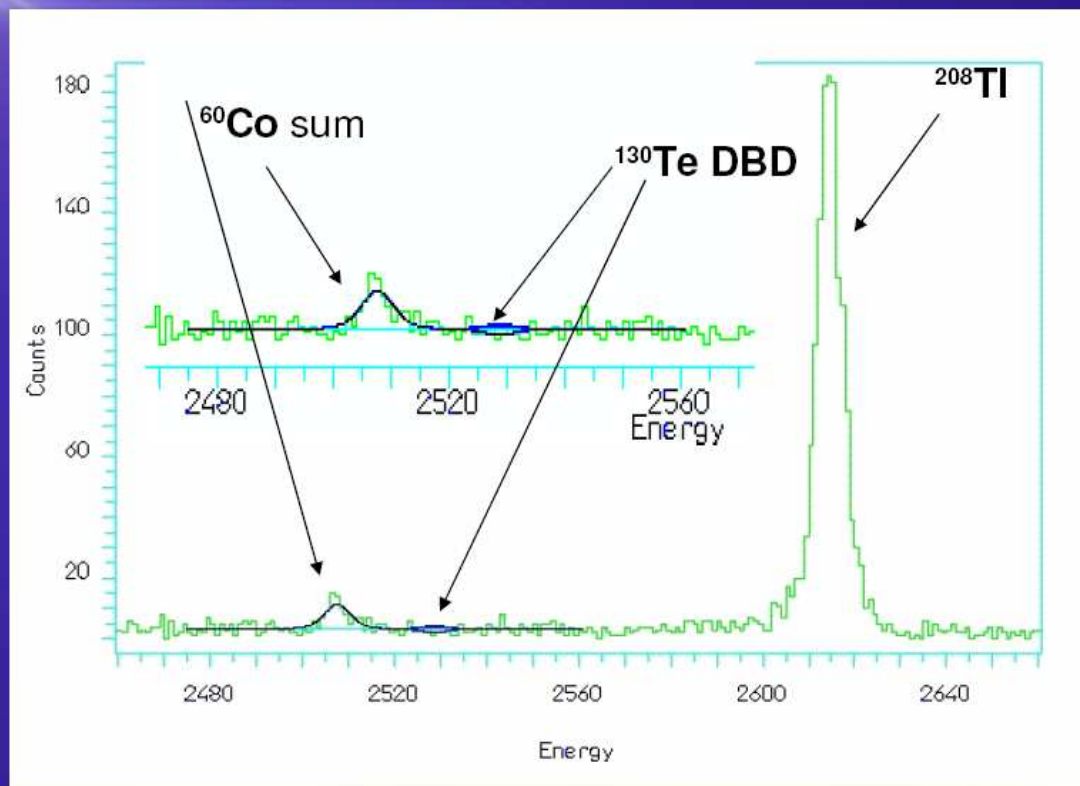
– Present bound: $|\langle m_{ee} \rangle| < 0.35 \text{ eV}$ +theor. uncert. $< 1.05 \text{ eV}$ (90% CL)

(Heidelberg-Moscow and IGEX experiments)

ν -less Double- β : Present

- Two experiments: **Cuorecino** and NemoIII running
- Less sensitive than present bounds
- But able to partially test masses in range of claimed evidence

CUORICINO - Results



about 40 kg running

$T_{1/2} > 1.8 \times 10^{24}$ yrs
(90% CL)

$m < 0.2-1.1$ eV

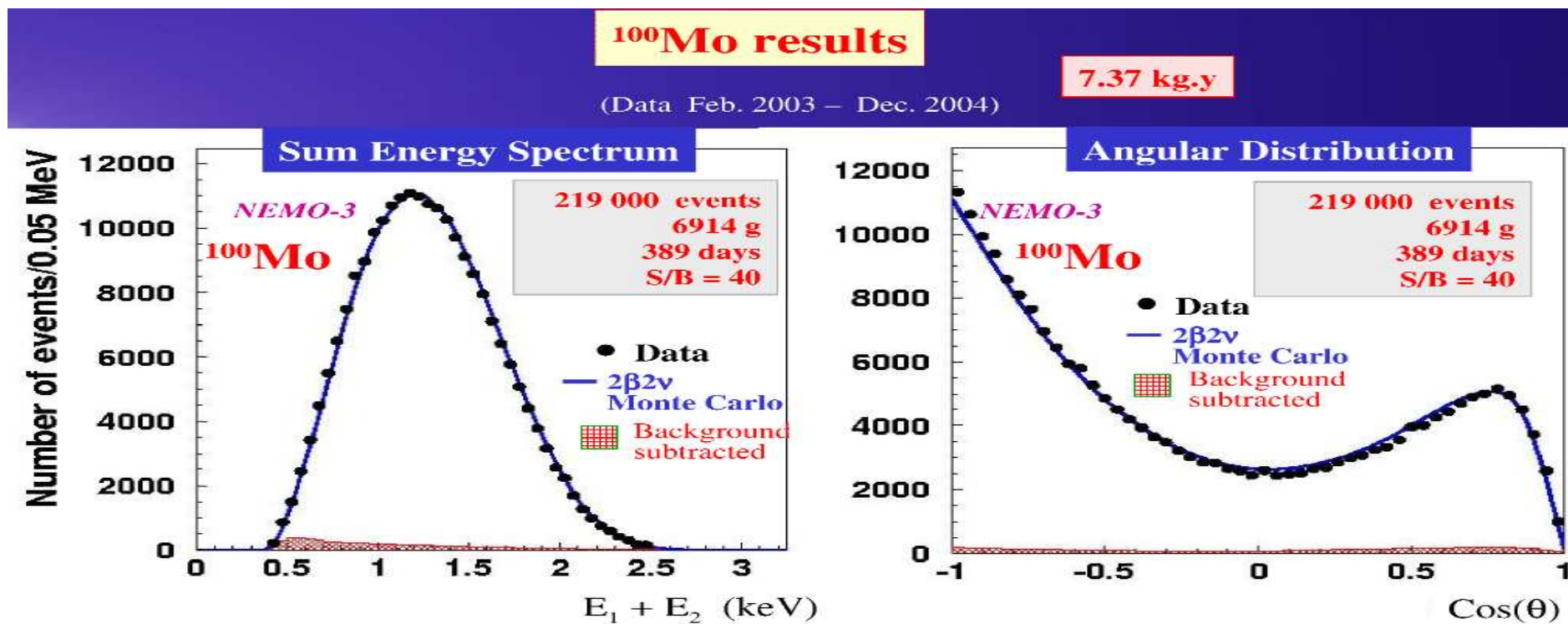
C.Arnaboldi et al, hep-ex0501034,
Phys. Rev. Lett. 2005

Idea:
CUORE (750 kg)
approved by INFN

ν -less Double- β : Present

- Two experiments: Cuorecino and **NemoIII** running
- Less sensitive than present bounds
- But able to partially test claimed evidence

Talk By K. Zuber at Epiphany Conf 06



$2\nu\beta\beta$: $T_{1/2} = 7.14 \pm 0.02 \text{ (stat)} \pm 0.54 \text{ (syst)} \times 10^{18} \text{ y}$

$0\nu\beta\beta$: $T_{1/2} > 3.1 \times 10^{23} \text{ yrs (90\% CL)}$
 $m_\nu < 0.7 - 2.8 \text{ eV}$

R. Arnold et al, hep-ex/0507083
Idea: Super-NEMO (100 kg)

ν -less Double- β : Future

- Many Proposals to reach $m_{ee} \sim 0.05$ eV

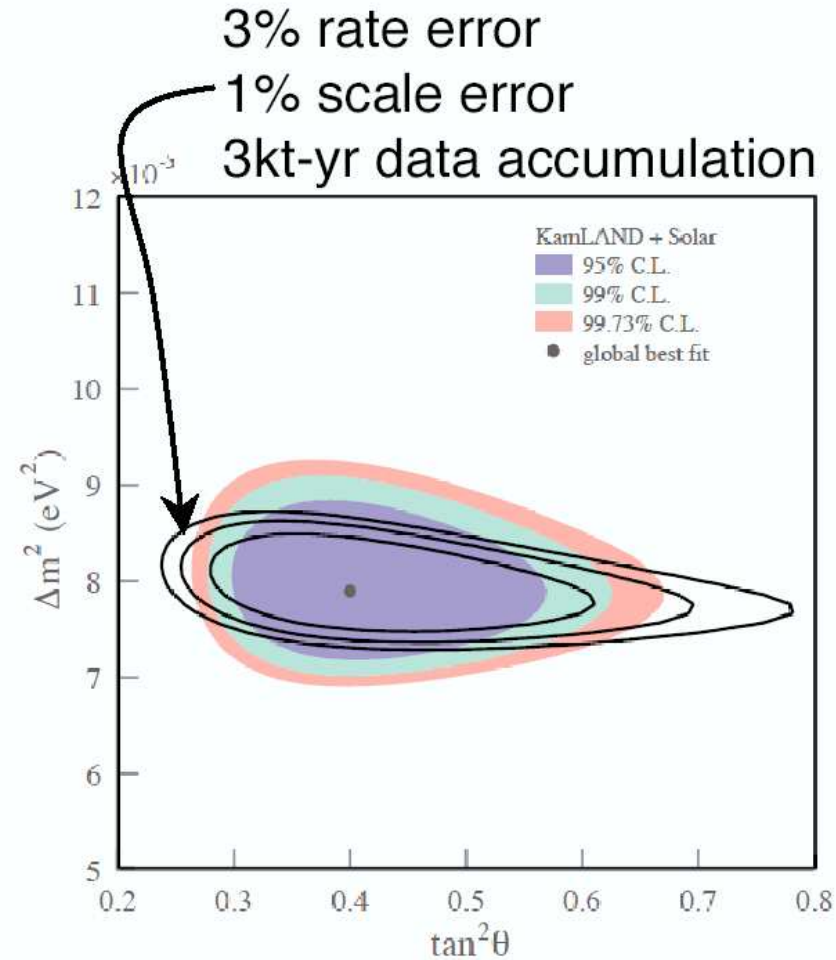
CARVEL	Ca-48	100 kg $^{48}\text{CaWO}_4$ crystal scintillators
COBRA	Te-130	10 kg CdTe semiconductors
DCBA	Nd-150	20 kg Nd layers between tracking chambers
NEMO	Mo-100, Various	10 kg of $\beta\beta$ isotopes (7 kg of Mo), expand to superNEMO
CAMEO	Cd-114	1 t CdWO_4 crystals
CANDLES	Ca-48	Several tons CaF_2 crystals in liquid scint.
CUORE	Te-130	750 kg TeO_2 bolometers
EXO	Xe-136	1 ton Xe TPC (gas or liquid)
GEM	Ge-76	1 ton Ge diodes in liquid nitrogen
GENIUS	Ge-76	1 ton Ge diodes in liquid nitrogen
GERDA	Ge-76	~ 30 -40 kg Ge diodes in LN, expand to larger masses
GSO	Gd-160	2 t $\text{Gd}_2\text{SiO}_5:\text{Ce}$ crystal scint. in liquid scint.
Majorana	Ge-76	~ 180 kg Ge diodes, expand to larger masses
MOON	Mo-100	Mo sheets between plastic scint., or liq. scint.
Xe	Xe-136	1.56 t of Xe in liq. Scint.
XMASS	Xe-136	10 t of liquid Xe

Present and Future of Neutrino Parameters

3- ν parameter	Present knowledge ($\sim 3\sigma$ C. L.)	Near and Not so Near Future
θ_{12}	$0.34 \leq \tan^2 \theta_{12} \leq 0.61$	KamLAND, Future LE Solar
θ_{23}	$0.47 \leq \tan^2 \theta_{23} \leq 1.8$	$P(\nu_\mu \rightarrow \nu_\mu)$ MINOS, OPERA
θ_{13}	$\sin^2 \theta_{13} \leq 0.04$	$P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$ Reactor, $P(\nu_\mu \rightarrow \nu_e)$ LBL
$ \Delta m_{21}^2 $	$7.0 \leq \Delta m_{21}^2 / 10^{-5} \text{eV}^2 \leq 9.0$	$P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$ KamLAND
$ \Delta m_{31}^2 $	$2.4 \leq \Delta m_{31}^2 / 10^{-3} \text{eV}^2 \leq 3.2$	$P(\nu_\mu \rightarrow \nu_\mu)$ MINOS, OPERA LBL
$\text{sgn}(\Delta m_{31}^2)$	unknown	$P(\nu_\mu \rightarrow \nu_e), P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$ LBL
δ	unknown	$P(\nu_\mu \rightarrow \nu_e)$ versus $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$ LBL
Majorana	unknown	$0\nu\beta\beta$
m_ν	$\sum m_\nu < \mathcal{O}(1) \text{eV}$	β -decay, $0\nu\beta\beta$

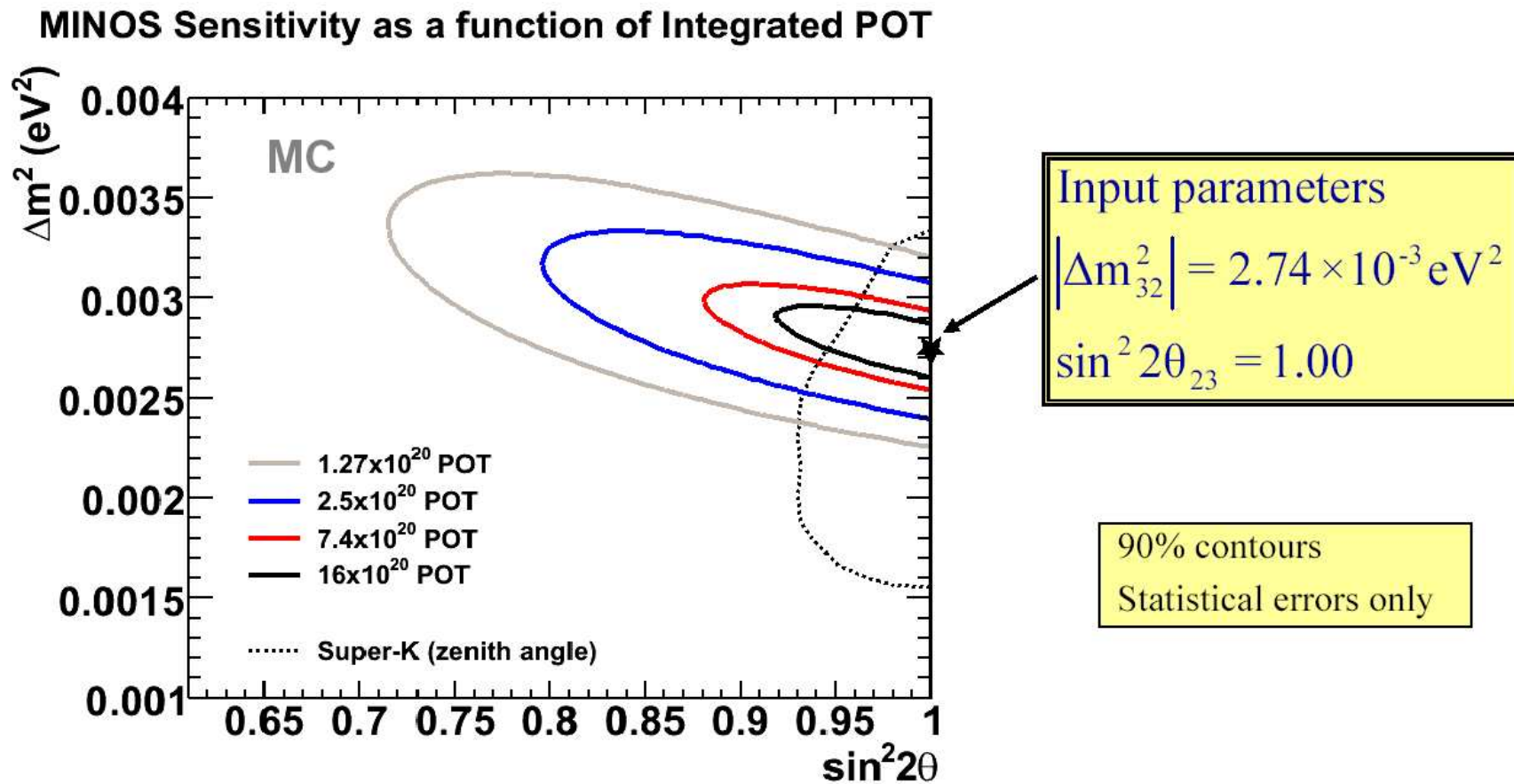
12 Near Future: Expected KamLAND Sensitivity

From T. Mitsui, Talk at ν 2006



- No improvement on θ_{12}
- $\sigma(\Delta m_{21}^2)/\Delta m_{21}^2 \gtrsim \pm 3\%$ (1dof)

23 Near Future: Expected Minos Sensitivity



<http://www-numi.fnal.gov>

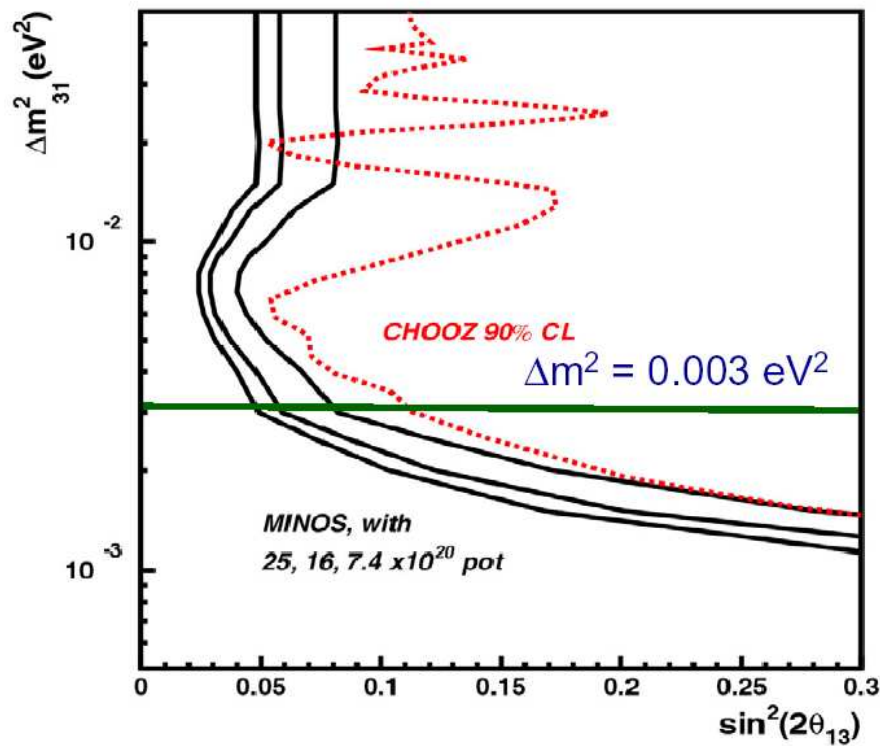
- No improvement on θ_{23}
- $\sigma(\Delta m_{31}^2) / \Delta m_{31}^2 \gtrsim \pm 5\%$ (1dof)

θ_{13} Near Future: MINOS and OPERA

MINOS

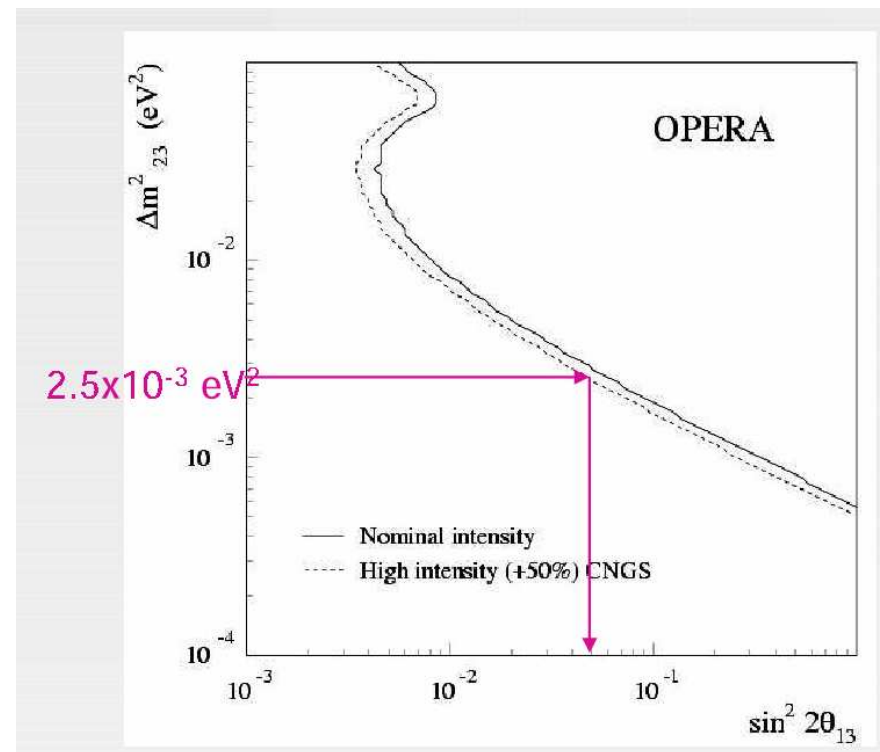
$$\nu_{\mu} \rightarrow \nu_e$$

3 σ Contours



OPERA 5 Years (2.2×10^{20} pot)

$$\sin^2 2\theta_{13} \leq 0.06 \quad 90\% \text{ CL}$$



C. Sirignano, talk at ν -2006

<http://www-numi.fnal.gov>

Neutrino Parameters: Future Strategies

- Oscillation Probabilities in Earth: $\Delta_{ij} = \frac{\Delta m_{ij}^2}{2E_\nu}$ $B_\pm = \Delta_{31} \pm V_E$ ($V_E \sim 10^{-13}$ eV)
 $\tilde{J} = c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$

$$\begin{aligned}
 P_{\nu_e \nu_\mu (\bar{\nu}_e \bar{\nu}_\mu)} &\simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{B_\mp} \right)^2 \sin^2 \left(\frac{B_\mp L}{2} \right) \\
 &+ \tilde{J} \frac{\Delta_{12}}{V_E} \frac{\Delta_{31}}{B_\mp} \sin \left(\frac{V_E L}{2} \right) \sin \left(\frac{B_\mp L}{2} \right) \cos \delta \cos \left(\frac{\Delta_{31} L}{2} \right) \\
 &\pm \tilde{J} \frac{\Delta_{12}}{V_E} \frac{\Delta_{31}}{B_\mp} \sin \left(\frac{V_E L}{2} \right) \sin \left(\frac{B_\mp L}{2} \right) \sin \delta \sin \left(\frac{\Delta_{31} L}{2} \right) + \dots
 \end{aligned}$$

$$P(\nu_\mu \rightarrow \nu_\mu) \simeq 1 - c_{13}^2 \sin^2 2\theta_{23} \sin^2 \left(\frac{\Delta_{31} L}{2} \right) + \mathcal{O}(\Delta_{12}, s_{13}^2)$$

$$P(\nu_e \rightarrow \nu_e) \simeq 1 - \sin^2 2\theta_{31} \sin^2 \left(\frac{\Delta_{31} L}{2} \right) - c_{31}^4 \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta_{21} L}{2} \right)$$

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– θ_{13} : Very intense ν_μ or ν_e beam + low background and/or small systematics

Neutrino Parameters: Future Strategies

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- $\text{sgn}(\Delta m_{31}^2)$: Need of matter effects \Rightarrow very long L

Neutrino Parameters: Future Strategies

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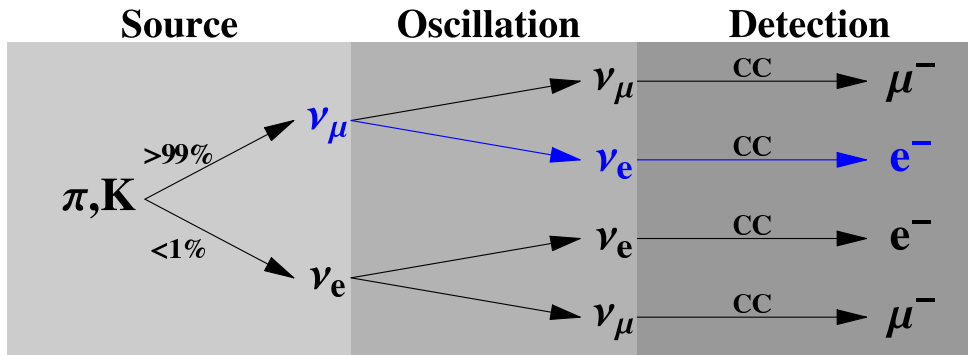
– $\text{sgn}(\Delta m_{31}^2)$: Need of matter effects \Rightarrow very long L

– \mathcal{CP} : All angles and Δm^2 non vanishing $\Rightarrow \theta_{13}$ not too small

Intense beams best with exchangeable initial state ($\nu/\bar{\nu}$)

Experimental Set-ups

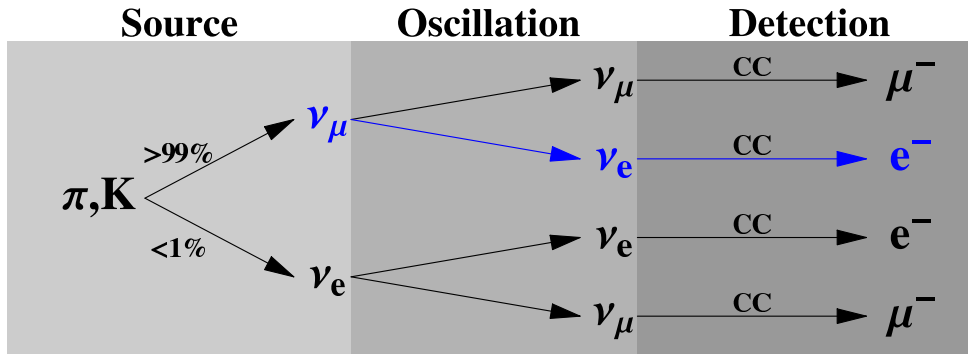
- Conventional (=from π decay) Superbeams



	Exp	L	$\langle E \rangle$
Off-Axis	T2K (Japan)	295 km	0.76 GeV
	Nova (Fermilab)	812 km	2.22 GeV

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- Conventional (=from π decay) Superbeams



	Exp	L	$\langle E \rangle$
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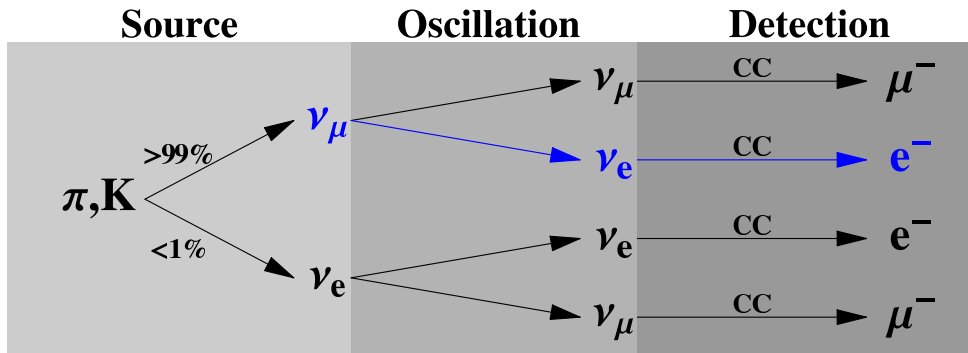
- Reactor Experiment with 2 Detectors [only θ_{13}]

$$P(\nu_e \rightarrow \nu_e) \simeq 1 - \sin^2 2\theta_{31} \sin^2 \left(\frac{\Delta_{31} L}{2} \right)$$

CHOOZII (France), Many proposals
 $\langle E \rangle \sim 4$ MeV $L \sim 1-2$ km

Experimental Set-ups

- Conventional (=from π decay) Superbeams



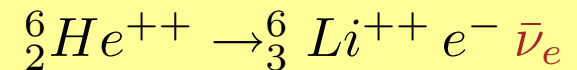
	Exp	L	$\langle E \rangle$
Off-Axis	T2K (Japan)	295 km	0.76 GeV
	Nuova (Fermilab)	812 km	2.22 GeV

- Reactor Experiment with 2 Detectors [only θ_{13}]

$$P(\nu_e \rightarrow \nu_e) \simeq 1 - \sin^2 2\theta_{31} \sin^2 \left(\frac{\Delta_{31} L}{2} \right)$$

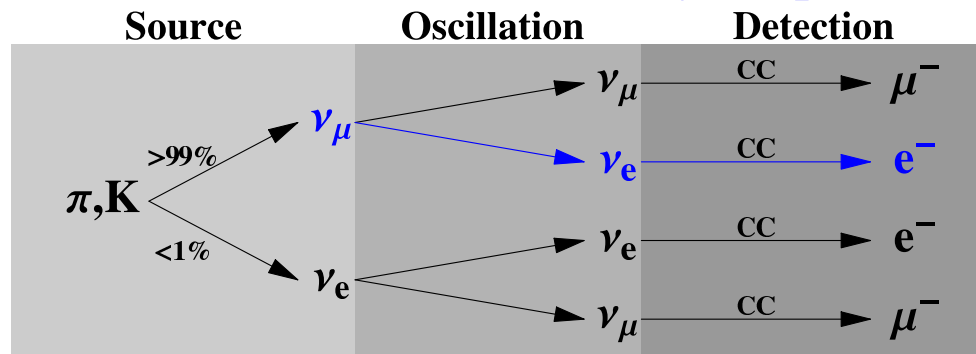
CHOOZII (France), Many proposals
 $\langle E \rangle \sim 4 \text{ MeV}$ $L \sim 1-2 \text{ km}$

- β -beam : Beam of pure ν_e or $\bar{\nu}_e$ from radioactive ion decay:



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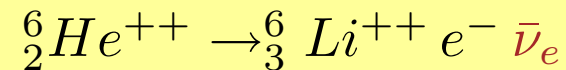
Off-Axis

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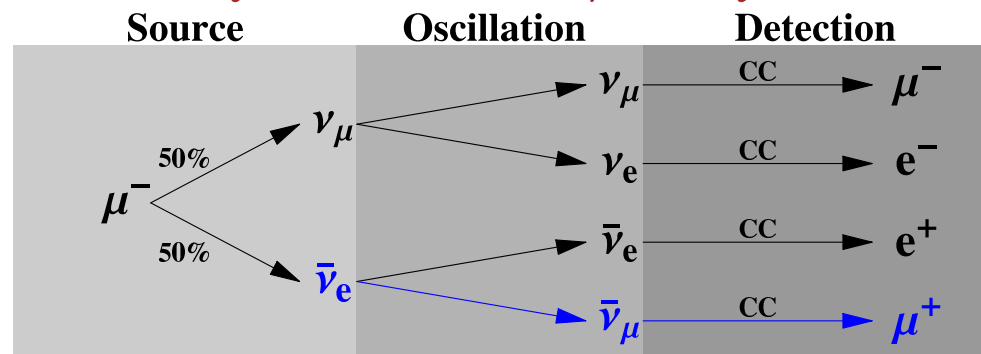
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CHOOZII (France), Many proposals
 $\langle E \rangle \sim 4$ MeV $L \sim 1-2$ km

- β -beam : Beam of pure ν_e or $\bar{\nu}_e$ from radioactive ion decay:



- ν -factory: ν beam from μ decay



$$\langle E \rangle \sim 20-50 \text{ GeV}$$

$$L \sim 700-7000 \text{ km}$$

World of Proposed Reactor Neutrino Experiments



Prospects for a Reactor Measurement of $\sin^2 2\theta_{13}$

Angra, Brazil

$$\sin^2 2\theta_{13} < 0.005$$

- R&D on reactor monitoring. Proposal for θ_{13} measurement after Double Chooz.

Daya Bay, China

$$\sin^2 2\theta_{13} < 0.01$$

- Approved by the Chinese Academy of Science for 50M RMB.
- Other Chinese agencies are expected to contribute ~ 100 M RMB.
- US DOE has provided 0.8M\$ for R&D for FY06. Working towards US project start in FY08.
- Plan to start near-mid data taking in 2009, and begin full operation in 2010.

Double-CHOOZ, France

$$\sin^2 2\theta_{13} < 0.03$$

- Funding commitment in France and Germany.
- Begin running far detector in 2008.
- Complete near detector in 2009.

RENO, Korea

$$\sin^2 2\theta_{13} < 0.02$$

- Approved by Ministry of Science and Technology for US \$9M. R&D program starting.
- Plan to begin data taking in 2009/2010.

KASKA, Japan

$$\sin^2 2\theta_{13} < 0.025$$

- R&D program in progress. If funded, plan to begin data taking in 2009/2010.

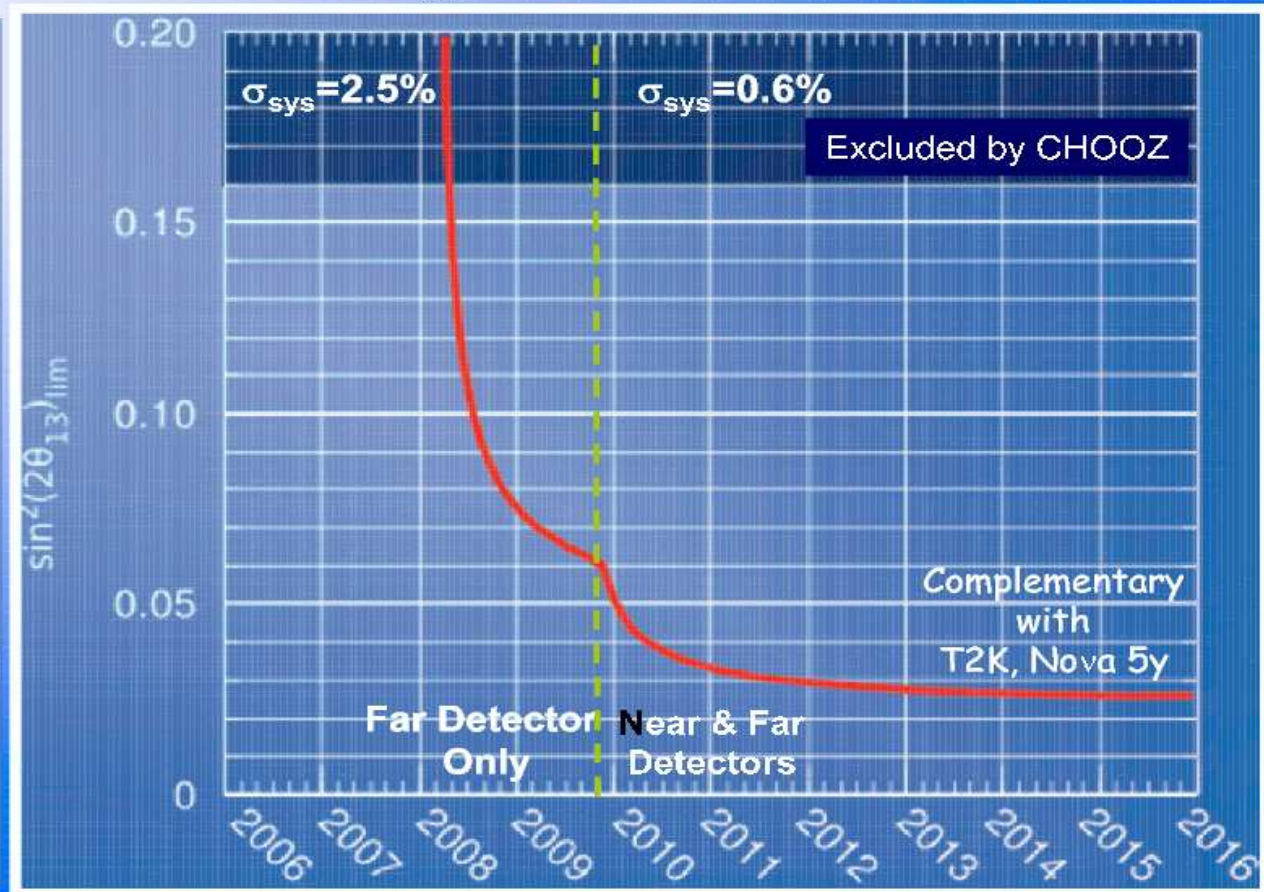
Expectations at Double Chooz



Expected Milestones

Limit @ 90% C.L. for $\sin^2(2\theta)=0$
 $\Delta m^2_{\text{atm}} = 2.5 \cdot 10^{-3} \text{ eV}^2$ (with 20% uncertainty)

- 2007: assembly of far detector on site
- 2008: data taking with far detector
 - Start of Near lab building
- 2009: assembly of near detector
- 2010: data taking with 2 detectors



Expectations at T2K-I

- JPARC to SuperKamiokande:

$L = 295 \text{ Km}$, 10^{21} pot/yr , Off-Axis 2-2.5 deg, $\langle E \rangle \sim .75 \text{ GeV}$

Starting data taking 2009

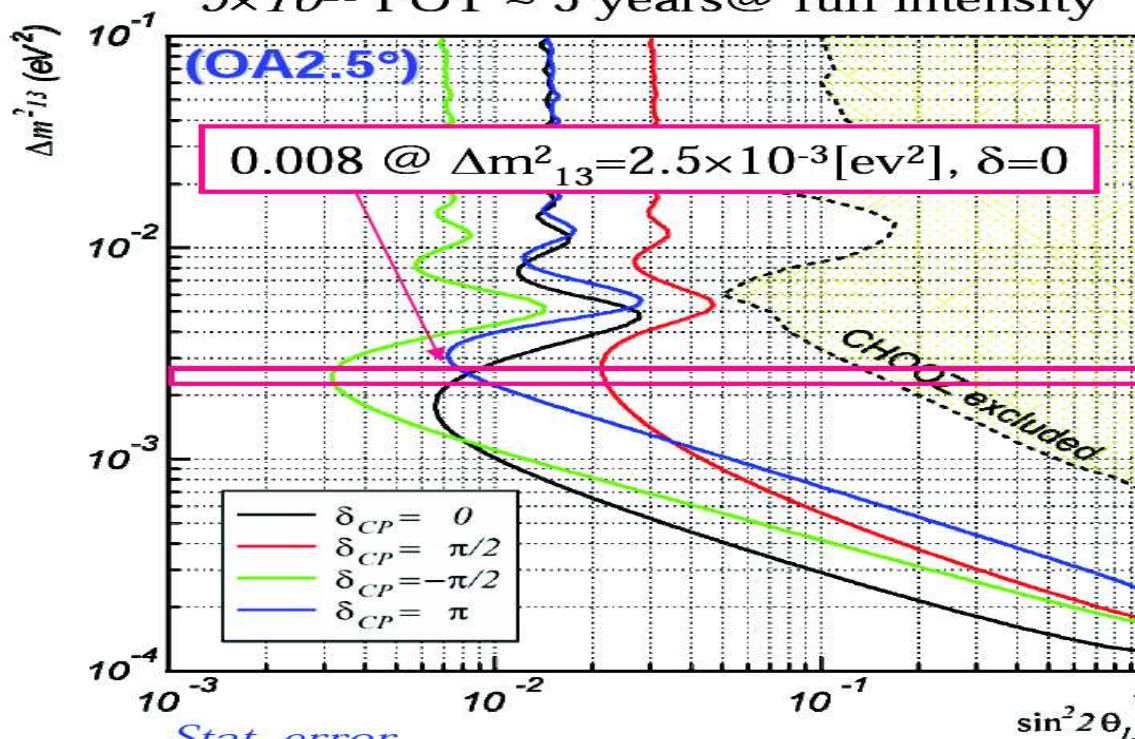
- In $\nu_\mu \rightarrow \nu_\mu$: Goal $\delta(\sin^2 2\theta_{23}) \sim 0.01$ and $\delta(\Delta m_{31}^2) \sim 10^{-4} \text{ eV}^2$

- In $\nu_\mu \rightarrow \nu_e$:

T2K 90%CL sensitivity

$\sin^2 2\theta_{23} = 1.0$ is assumed.

$5 \times 10^{21} \text{ POT} \sim 5 \text{ years@ full intensity}$



Talk by T. Nakadaira at ν -2006

Stat. error
+ Syst. error for BG subtraction (10%)

Challenges at Future LBL: Parameter Degeneracies

$$\begin{aligned}
 P_{\nu_e \nu_\mu}(\bar{\nu}_e \bar{\nu}_\mu) &\simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{B_\mp} \right)^2 \sin^2 \left(\frac{B_\mp L}{2} \right) \\
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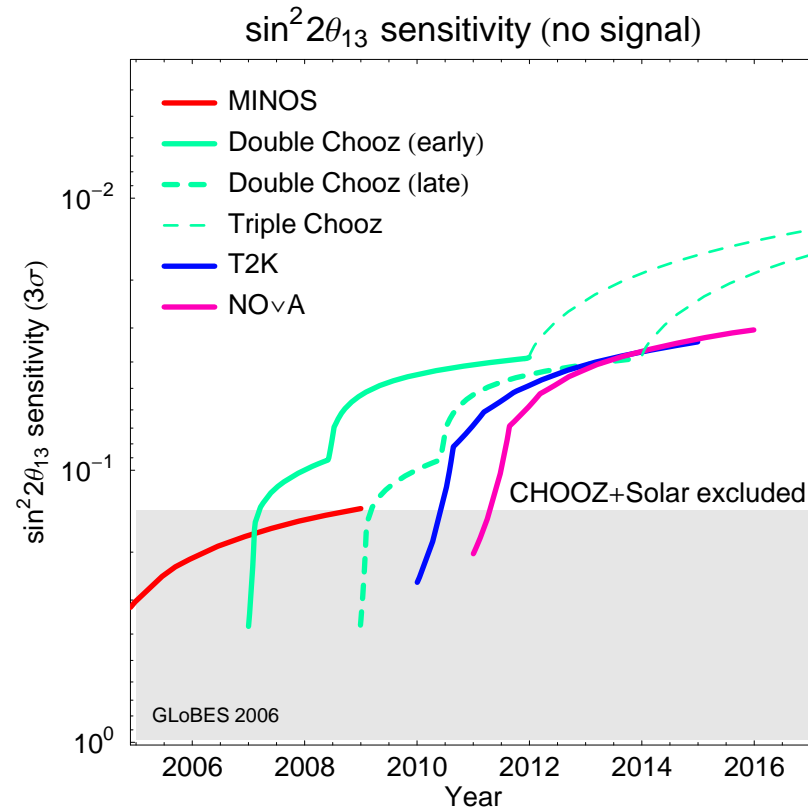
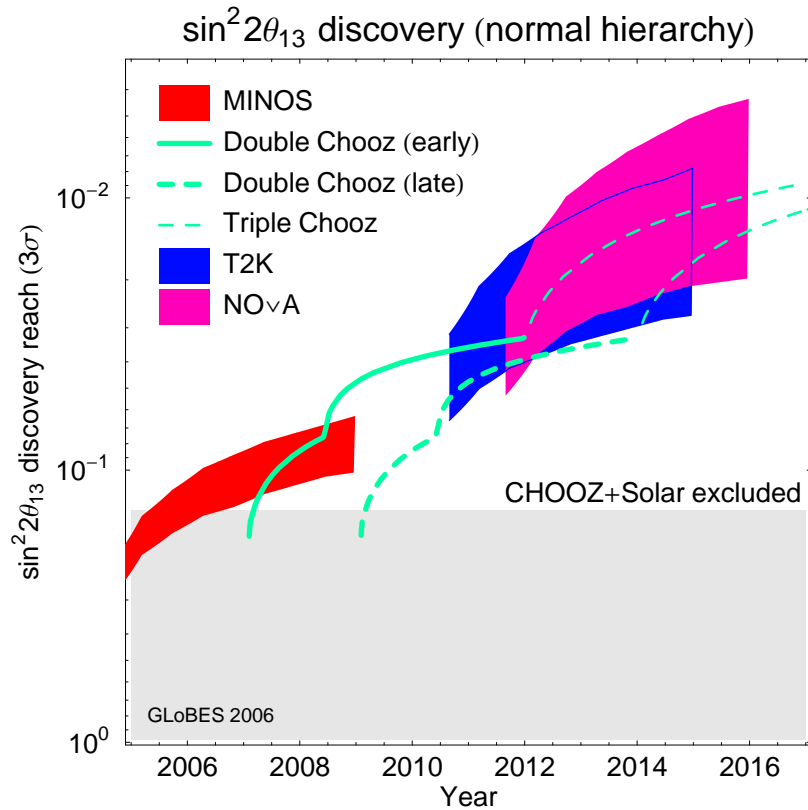
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If only total number of $\nu_e, \nu_\mu, \bar{\nu}_e$ and $\bar{\nu}_\mu$ at given L are measured \Rightarrow 8-fold degeneracy

Possible Time Scale in Sensitivity to θ_{13}



From Huber, Kopp, Lindner, Rolinec and Winter 06

Future LBL: Cures of Degeneracies

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At $L = \frac{2\pi}{V_e} \sim 8000 \text{ km} \Rightarrow$ Only first term survives

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(θ_{13}, δ) ambiguity broken **but others remain**

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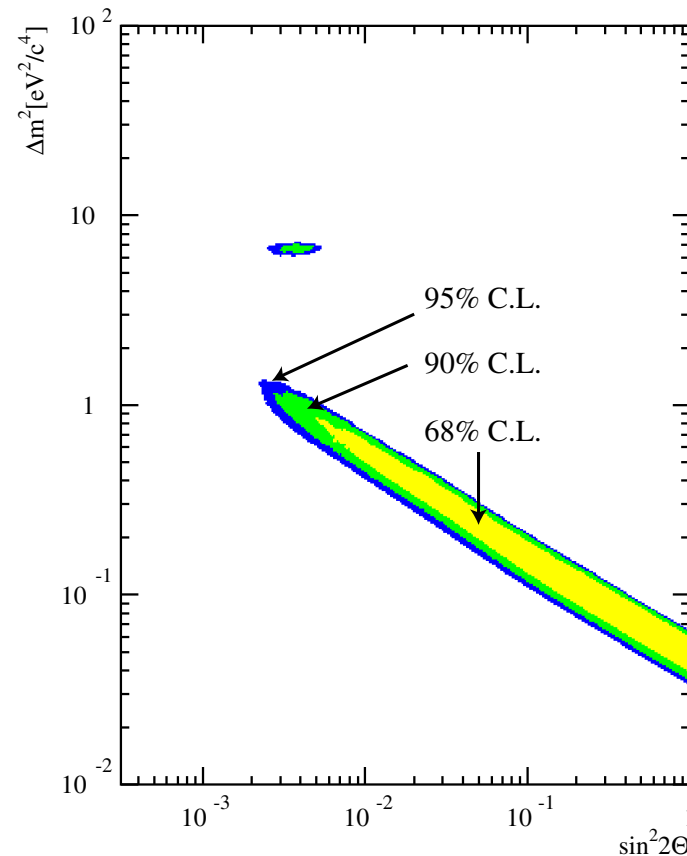
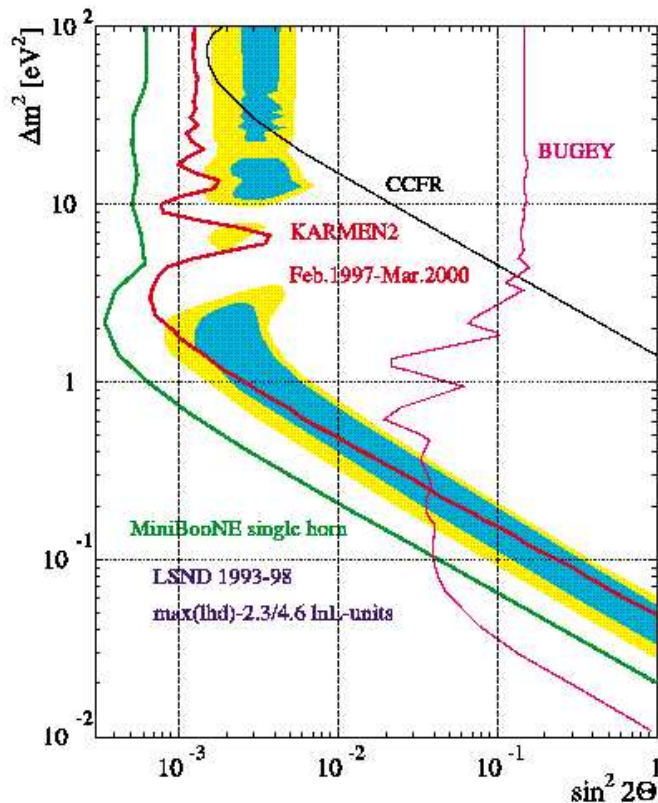
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 Burget-Castell *etal* 02; Huber, Lindner, Winter 03, Minakata, Nunokawa, Parke 03; etc ...
- Use “silver” oscillation channels $\nu_e \rightarrow \nu_\tau$ and $\nu_\mu \rightarrow \nu_\tau$
 Need higher beam energy and high resolution detector
 Donini, Meloni, Migliozzi, 02...
- Combine with atmospheric ν data
 Huber, Maltoni, Schwetz 05...
- Wide-band superbeam allowing for spectrum measurements $N_\nu(E_\nu)$
 M. Diwan *etal* 03

LSND

- The only short distance signal for oscillation: $L = 30$ m with $\langle E_\nu \rangle \sim 30$ MeV
- Observed $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ with probability $\langle P_{e\mu} \rangle = (0.26 \pm 0.07 \pm 0.05)\%$
- *Karmen* searched for the same signal and did not observe oscillations

LSND+Karmen Combined Analysis



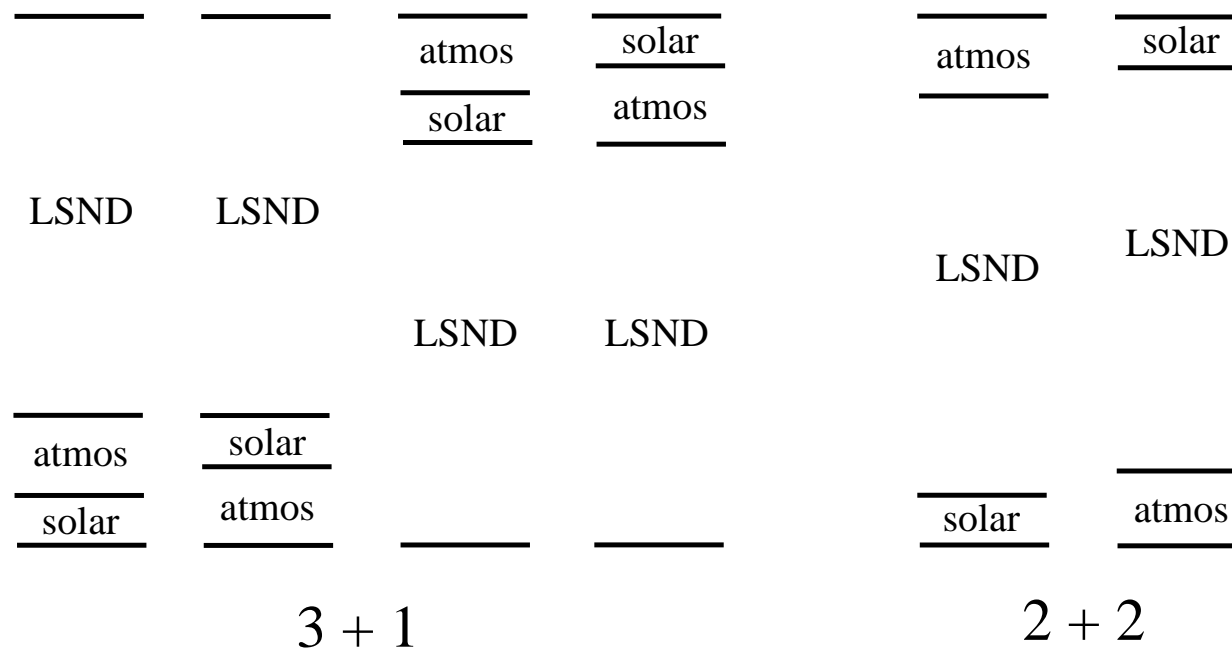
- *MiniBoone* in Fermilab is expected to clarify this **SOON!!**.

LSND Try I: Sterile Neutrinos and 4ν Mixing

- Motivation: To explain LSND

$$\Delta m_{\text{LSND}}^2 \gg \Delta m_{\text{atm}}^2 \gg \Delta m_{\odot}^2$$

- To fit solar, atmospheric and LSND $\Rightarrow 3 \Delta m^2 \Rightarrow$ 4th sterile ν
- U : 6 mixing angles and 3 CP Dirac phases and 3 Majorana phases
- 6 mass spectra of two type:



LSND Try I: Sterile Neutrinos and 4ν Mixing

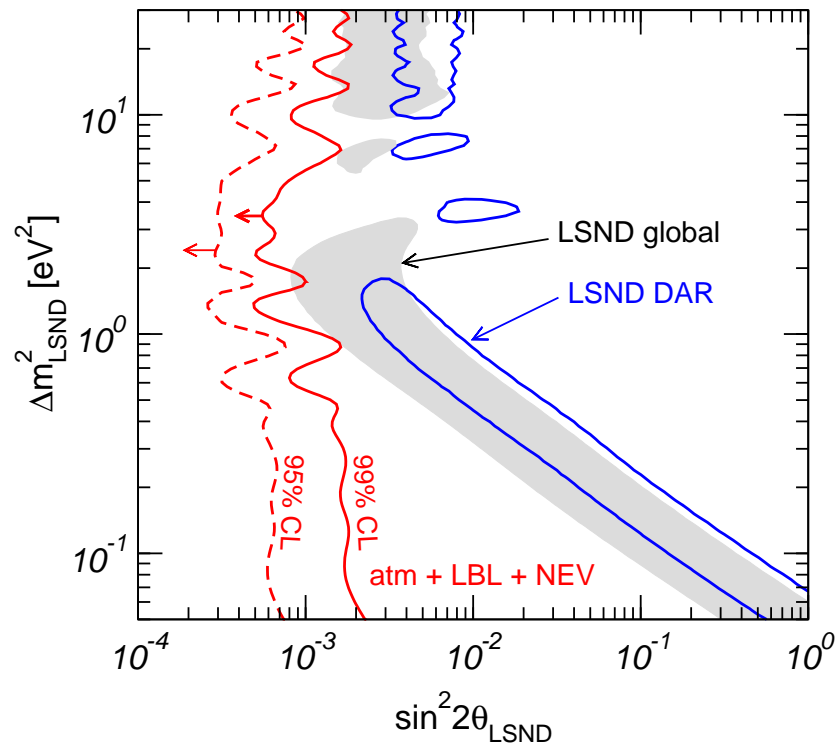
3 + 1

$$\sin^2 2\theta_{\text{LSND}} = 4|U_{e4}|^2|U_{\mu4}|^2$$

$|U_{e4}|^2$ constrained by Bugey

$|U_{\mu4}|^2$ constrained by CDHSW+ATM

Maltoni et al 05, Updated Maltoni, MCG-G 07

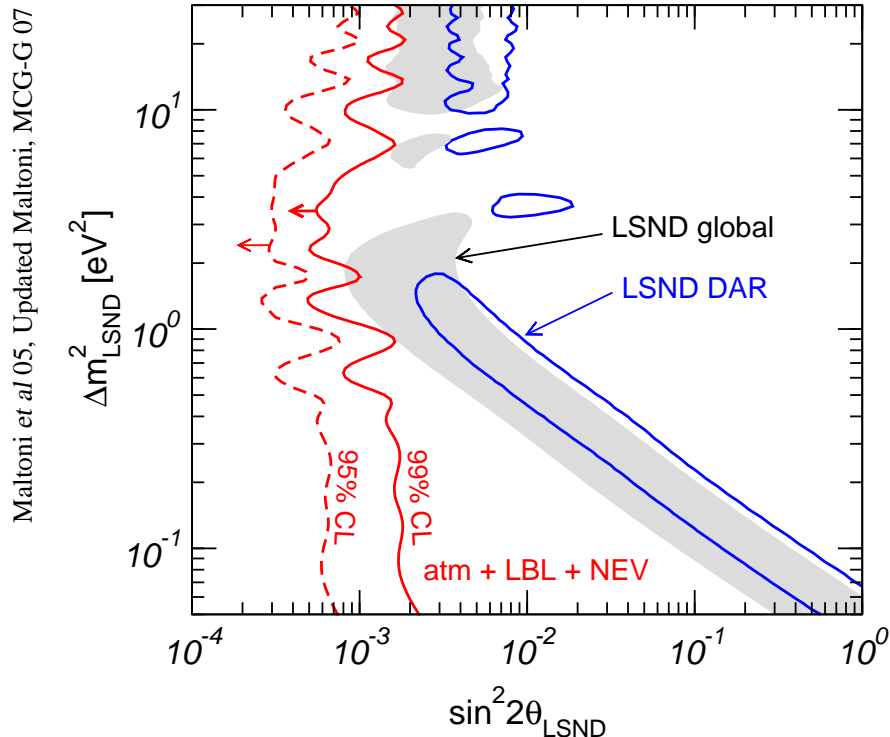


Only tiny regions at 99% CL

LSND Try I: Sterile Neutrinos and 4ν Mixing

3 + 1

$\sin^2 2\theta_{\text{LSND}} = 4|U_{e4}|^2|U_{\mu4}|^2$
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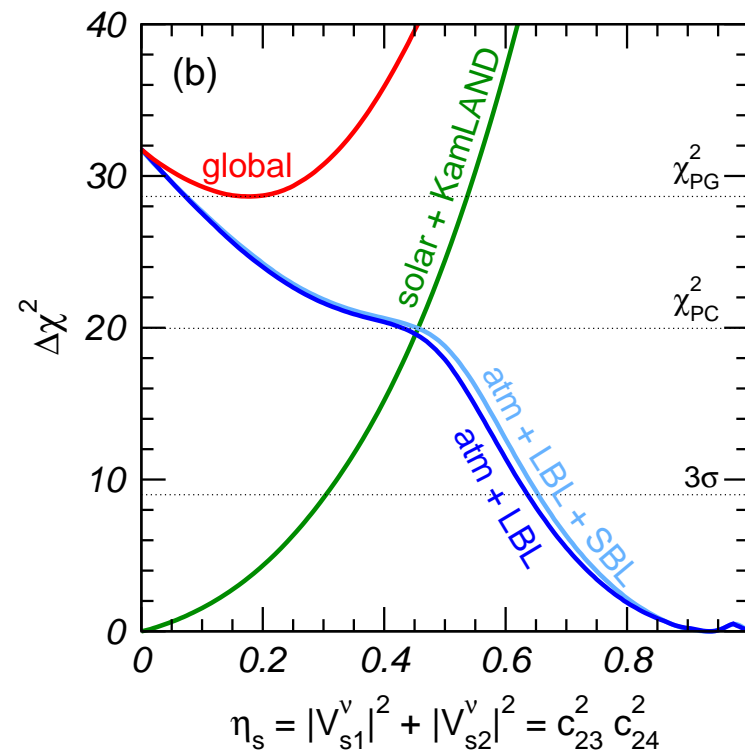
Only tiny regions at 99% CL

2 + 2

Mixed active-sterile oscillations

Naively: Solar: $\nu_e \rightarrow \cos \eta \nu_s + \sin \eta \nu_\tau$

Atm: $\nu_\mu \rightarrow \sin \eta \nu_s - \cos \eta \nu_\tau$



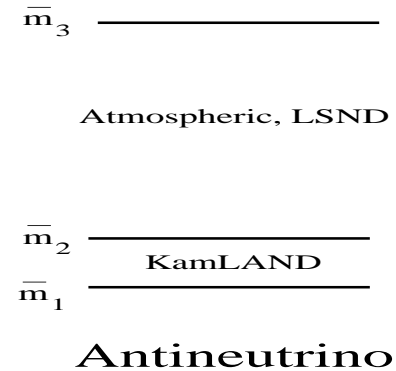
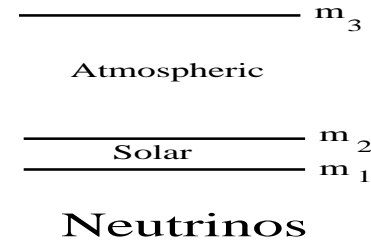
Disagreement at more than 4σ

LSND Try II : CPT Violation

MCG-G, Maltoni, Schwetz 04, MCG-G, Maltoni 07

CPT violation:

- ⇒ ν 's and $\bar{\nu}$'s can have different masses
- ⇒ Possibility of accommodating LSND?



LSND Try II : CPT Violation

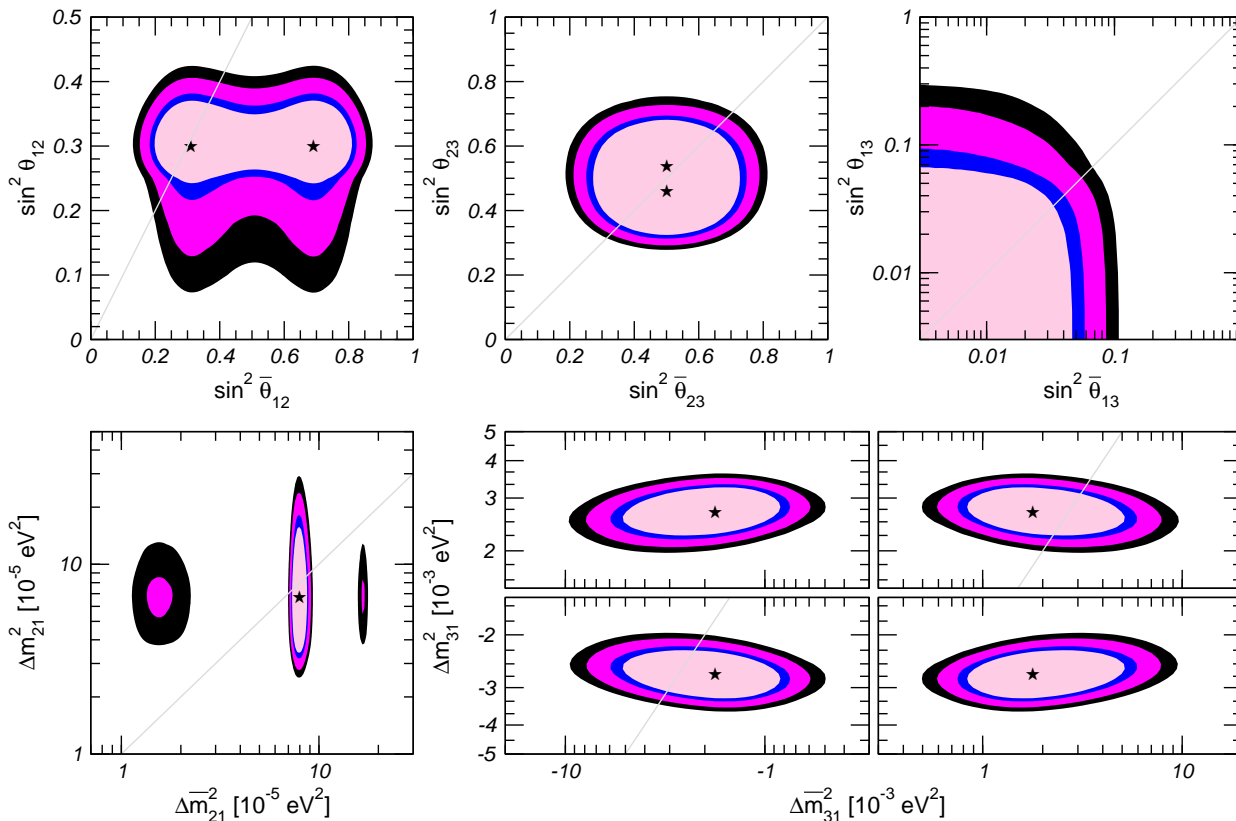
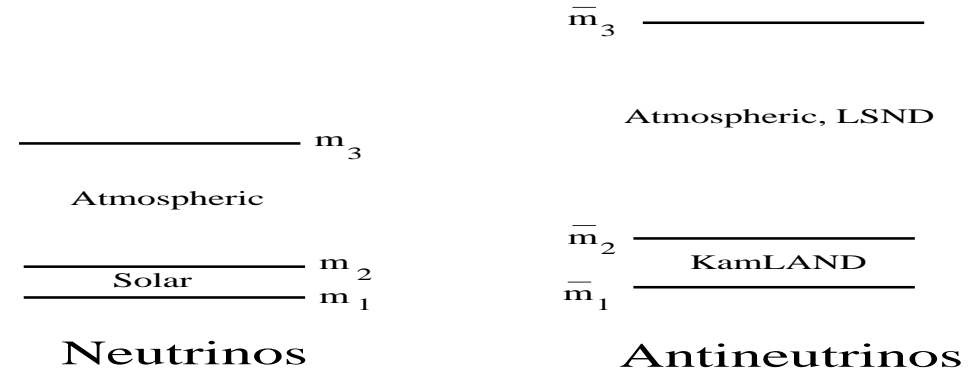
MCG-G, Maltoni, Schwetz 04, MCG-G, Maltoni 07

CPT violation:

- ⇒ ν 's and $\bar{\nu}$'s can have different masses
- ⇒ Possibility of accommodating LSND?

But Data does not support this:

- ATM ⇒ ν_μ and $\bar{\nu}_\mu$'s similar wavelength
- Solar ν_e and KamLAND $\bar{\nu}_e$ similar Δm^2



Best fit near
CPT conservation

LSND Try II : CPT Violation

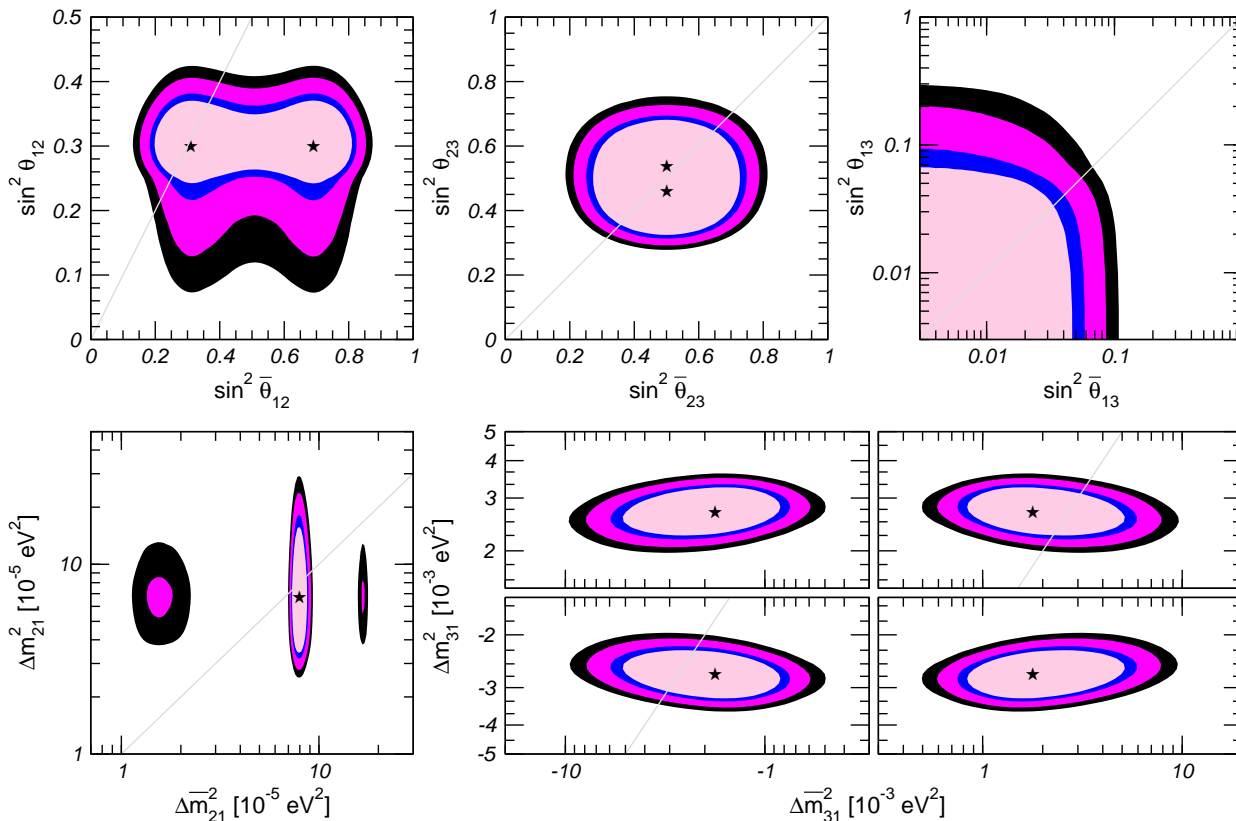
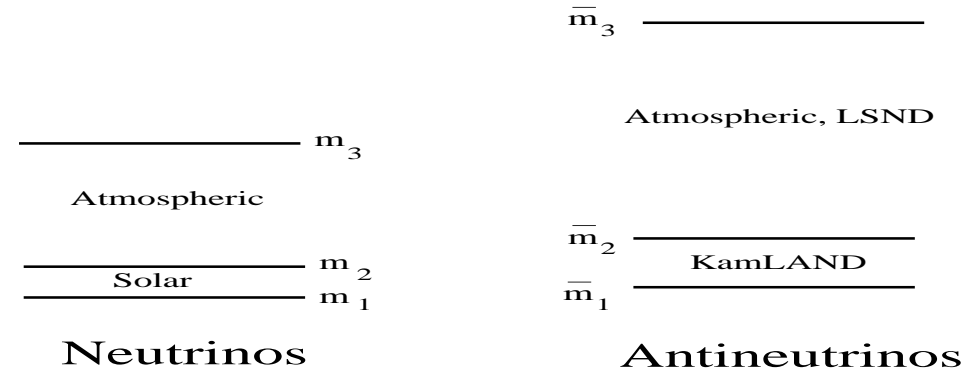
MCG-G, Maltoni, Schwetz 04, MCG-G, Maltoni 07

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Best fit near
CPT conservation

Ruled out at $\gtrsim 4\sigma$

LSND III: What it is Claimed to Work

- 3 active plus 2 light sterile neutrino mixing

Sorel, Conrad and Shaevitz, hep-ph/0305255

- 3 active plus 1 light sterile neutrino mixing plus CPT violation

Barger, Marfatia and Whisnant hep-ph/0308299

- 3 active plus 1 light sterile neutrino mixing plus MaVaN's interactions

Barger, Marfatia and Whisnant hep-ph/0509163

- 3 active plus 1 light sterile neutrino mixing plus decay

Ma, Rajasekaran and Stancu hep-ph/9908489

Palomares-Ruis, Pascoli and Schewtz, hep-ph/0505216

- 3 active plus 1 light sterile neutrino with extra dimensions

Pas, Pakvasa and Weiler, hep-ph/0504096

- 3 active plus quantum decoherence (and CPT violation)

Baremboim, Mavromatos hep-ph/0404014

Baremboim, Mavromatos, Sarkar and Waldron-Lauda, hep-ph/0603028

Some New Physics in ATM ν -Oscillations

- Oscillations are due to:

- Misalignment between CC-int and propagation states: **Mixing** \Rightarrow **Amplitude**

- Difference phases of propagation states \Rightarrow **Wavelength.**

For Δm^2 -OSC $\lambda = \frac{4\pi E}{\Delta m^2}$

- ν masses are not the only mechanism for oscillations

Violation of Equivalence Principle (VEP): Gasperini 88, Halprin, Leung 01

Non universal coupling of neutrinos $\gamma_1 \neq \gamma_2$ to gravitational potential ϕ

$$\lambda = \frac{\pi}{E|\phi|\delta\gamma}$$

Violation of Lorentz Invariance (VLI): Coleman, Glashow 97

Non universal asymptotic velocity of neutrinos $c_1 \neq c_2 \Rightarrow E_i = \frac{m_i^2}{2p} + c_i p$

$$\lambda = \frac{2\pi}{E\Delta c}$$

Interactions with space-time torsion: Sabbata, Gasperini 81

Non universal couplings of neutrinos $k_1 \neq k_2$ to torsion strength Q

$$\lambda = \frac{2\pi}{Q\Delta k}$$

Violation of Lorentz Invariance (VLI) Colladay, Kostelecky 97; Coleman, Glashow 99

due to CPT violating terms: $\bar{\nu}_L^\alpha b_\mu^{\alpha\beta} \gamma_\mu \nu_L^\beta \Rightarrow E_i = \frac{m_i^2}{2p} \pm b_i$

$$\lambda = \pm \frac{2\pi}{\Delta b}$$

Non-standard ν interactions in matter: Wolfenstein 78

$$G_F \epsilon_{\alpha\beta} (\bar{\nu}_\alpha \gamma^\mu \nu_\beta) (\bar{f} \gamma_\mu f)$$

$$\lambda = \frac{2\pi}{2\sqrt{2}G_f N_f \sqrt{\epsilon_{\alpha\beta}^2 + (\epsilon_{\alpha\alpha} - \epsilon_{\beta\beta})^2/4}}$$

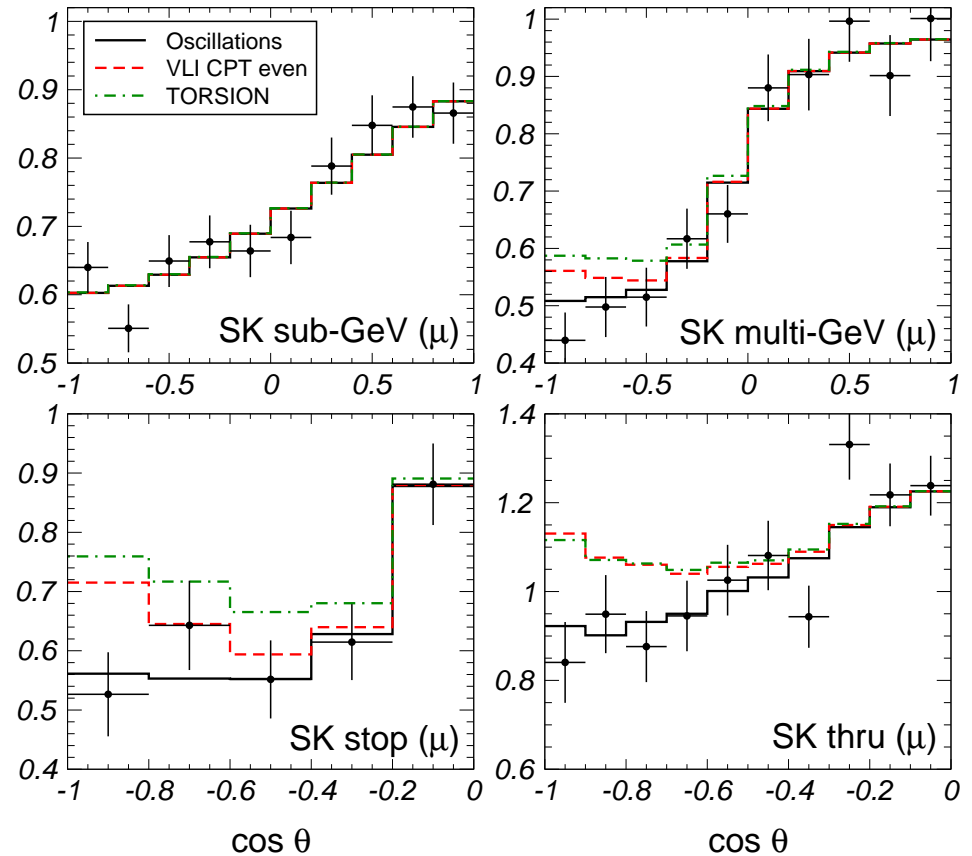
ATM ν 's: Subdominant NP Effects

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \sin^2 2\Theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \mathcal{R} \right)$$

$$\mathcal{R} \cos 2\Theta = \cos 2\theta + \sum_n R_n \cos 2\xi_n$$

$$\mathcal{R} \sin 2\Theta = \sin 2\theta + \sum_n R_n \sin 2\xi_n e^{i\eta_n}$$

$$R_n = \sigma_n^+ \frac{\Delta \delta_n E^n}{2} \frac{4E}{\Delta m^2}$$

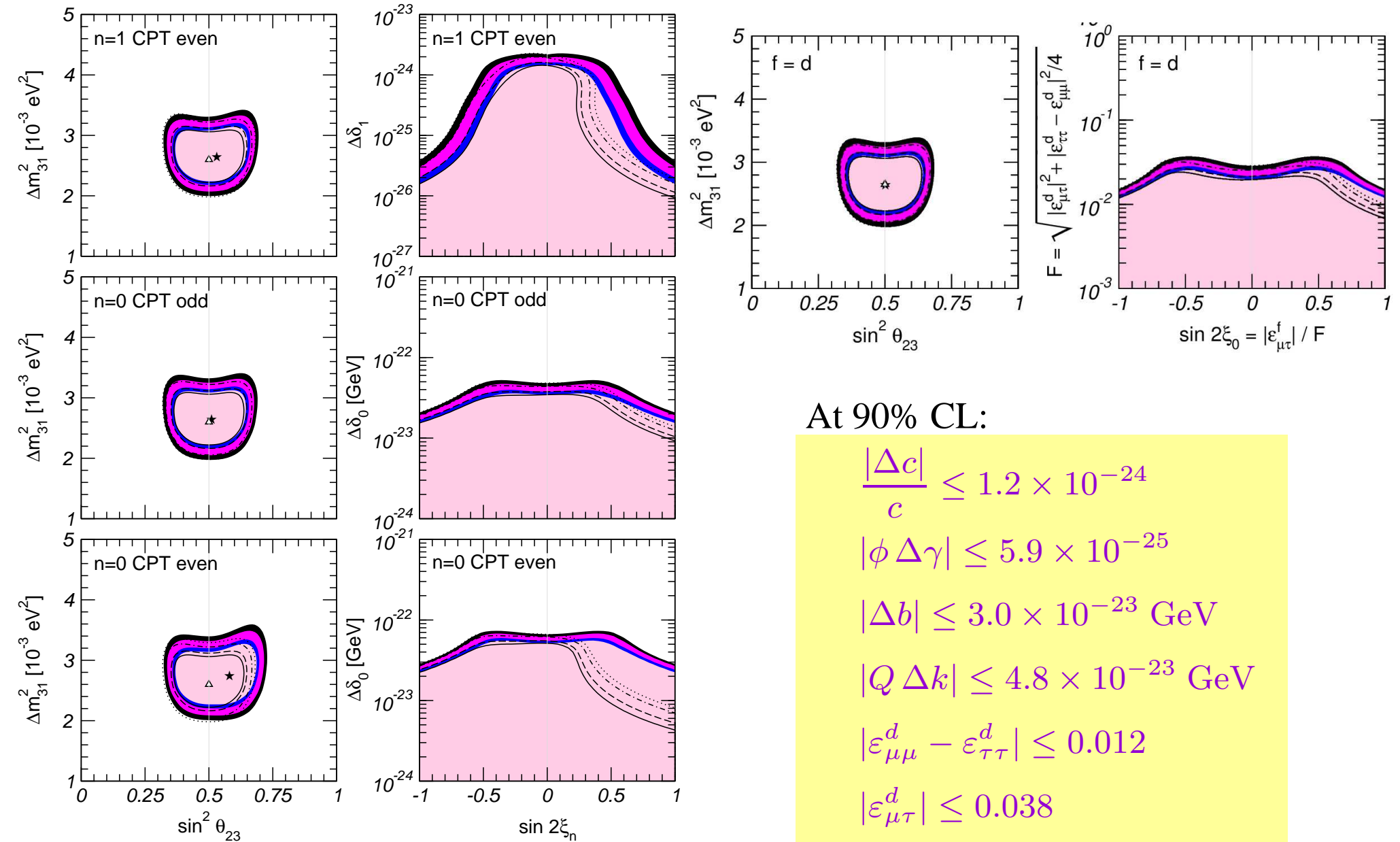


• Questions:

- Do these effects affect our determination of oscillation parameters?
- Can we limit these effects?

ATM ν 's: Subdominant NP Effects

MCG-G, M. Maltoni 04,07



At 90% CL:

$$\frac{|\Delta c|}{c} \leq 1.2 \times 10^{-24}$$

$$|\phi \Delta \gamma| \leq 5.9 \times 10^{-25}$$

$$|\Delta b| \leq 3.0 \times 10^{-23} \text{ GeV}$$

$$|Q \Delta k| \leq 4.8 \times 10^{-23} \text{ GeV}$$

$$|\epsilon_{\mu\mu}^d - \epsilon_{\tau\tau}^d| \leq 0.012$$

$$|\epsilon_{\mu\tau}^d| \leq 0.038$$

Future Bounds on New Physics: ν Telescopes

At ν Telescopes (Amanda, Antares, IceCube)

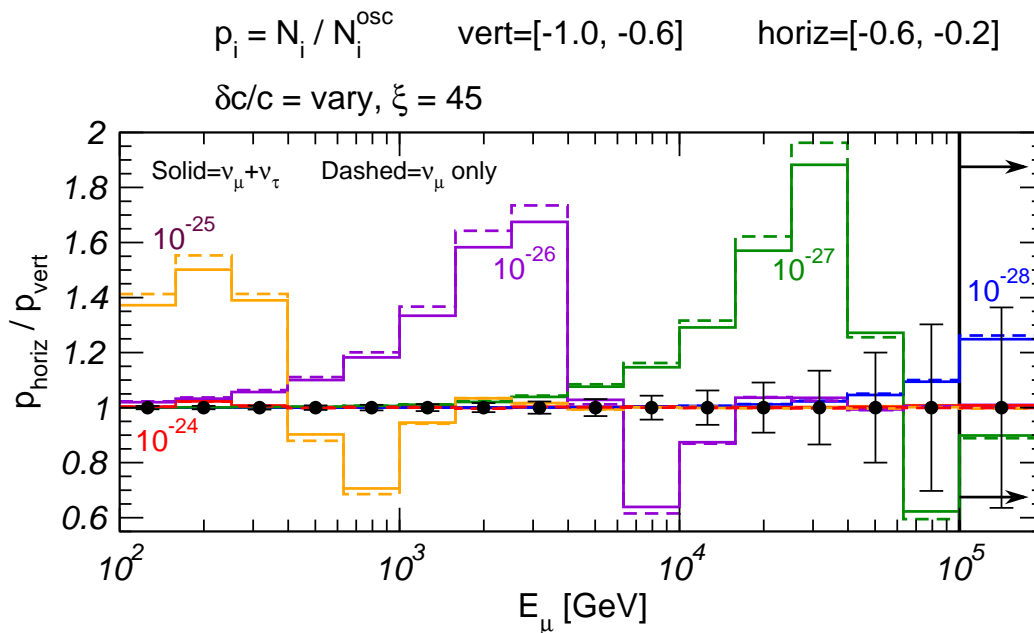
$E_{\nu,thres} \gtrsim 100 \text{ GeV}$

Large # ATM ν 's

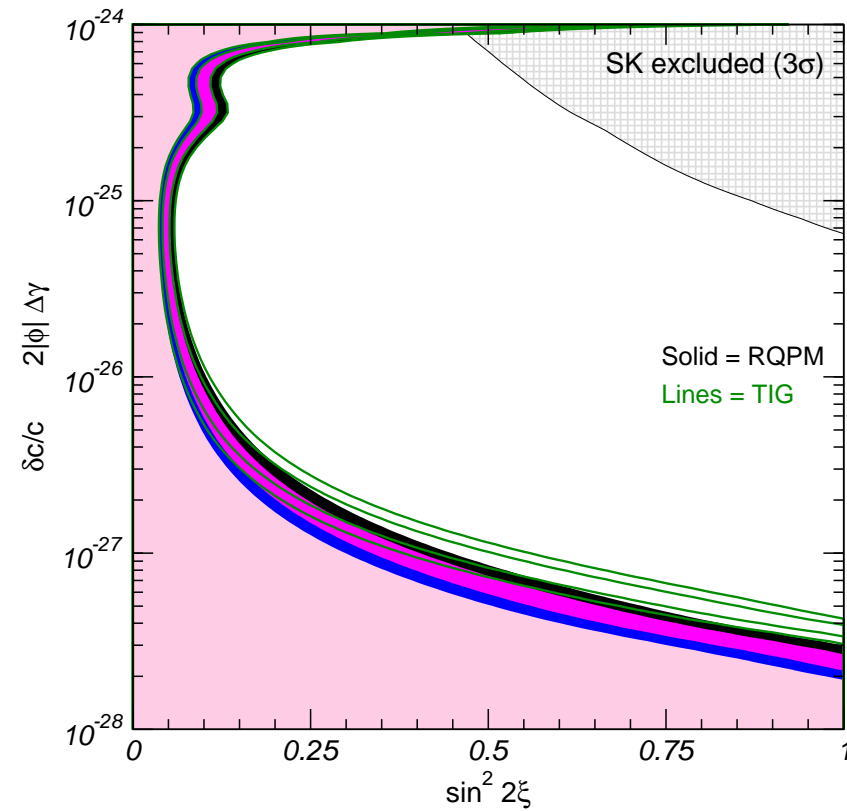
($\sim 10^5 \nu_{\mu}$ events/yr at ICECUBE)

\Rightarrow Standard oscillations suppressed

\Rightarrow Better sensitivity to Oscillations due to NP



Expected Sensitivity at IceCube



MCG-G, Halzen, Maltoni, 05

Summary

- **Big experimental effort** has been devoted to proof ν oscillations beyond doubt
- Solar and atmospheric signals are being **confirmed with** “**man-made**” **neutrino beams** from reactor and accelerators.
- **Solar, Reactor, Atmospheric and LBL data: Perfect in 3ν -oscillations**
- Ambitious experimental program and intense activity of phenomenologists to optimize the path to answer **open questions**:
 - What is the value of θ_{13} ?
 - Is there **CP violation** in the leptons
 - What is the **ordering of the states**
 - The absolute **scale of neutrino mass**
 - Are neutrinos **Dirac or Majorana** particles?
- **Accommodating LSND: A problem**
- ν oscillation data already provides interesting constraints on:
 - Fundamental symmetries: LI, WEP, CPT**
 - ν models for Dark Energy**
 - Solar Physics ...**