

# **FCNC Processes in the LHC Era**

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**CERN, 28th of March, 2007**

# **TH-Finale: Allegro Vivace**

# Overture

# Standard Model of Strong and Electroweak Interactions

Low Energy Effective Quantum Field Theory  
based on

$$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \xrightarrow[\text{broken}]{\text{spontaneously}} SU(3)_C \otimes U(1)_{\text{QED}}$$

which describes low energy phenomena in terms  
of 28 Parameters that have to be determined from  
experiment.

2	+	4	+	6	+	6	+	4	+	6	=	28
QCD ( $\alpha_{\text{QCD}}$ , $\theta_{\text{QCD}}$ )		Electroweak Gauge Boson and Higgs Sector		Quark Masses		Lepton Masses		$V_{\text{CKM}}$		$V_{\text{PMNS}}$		
				22	in the	Flavour Sector		★				



# Impressive Success of the CKM Picture of Flavour Changing Interactions

(GIM)

(Once quark masses determined : only 4 parameters)

- 1.** All leading decays of  $K$ ,  $D$ ,  $B_s^0$ ,  $B_d^0$  mesons correctly described
- 2.** Suppressed transitions :  $K^0 - \bar{K}^0$ ,  $B_d^0 - \bar{B}_d^0$ ,  $B_s^0 - \bar{B}_s^0$   
Mixings found at suppressed level
- 3.** CP-violating Data ( $K$ ,  $B_d$ ) correctly described
- 4.**  $B \rightarrow X_s \gamma$ ,  $B \rightarrow X_s l^+ l^-$  OK

$\cancel{CP}$  in  $B_s$ ?

**5.** Very very highly suppressed transitions also consistent with experiment: (not seen)

**Standard Model**

**Exp Upper Bound**

$$\text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-) \cong 3 \cdot 10^{-9}$$

$$\sim 10^{-7}$$

$$\text{Br}(\mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu}) \cong 3 \cdot 10^{-11}$$

$$\sim 10^{-7}$$

$$\text{Br}(\mathbf{K}_L \rightarrow \mu e) \cong 10^{-40}$$

$$\sim 10^{-12}$$

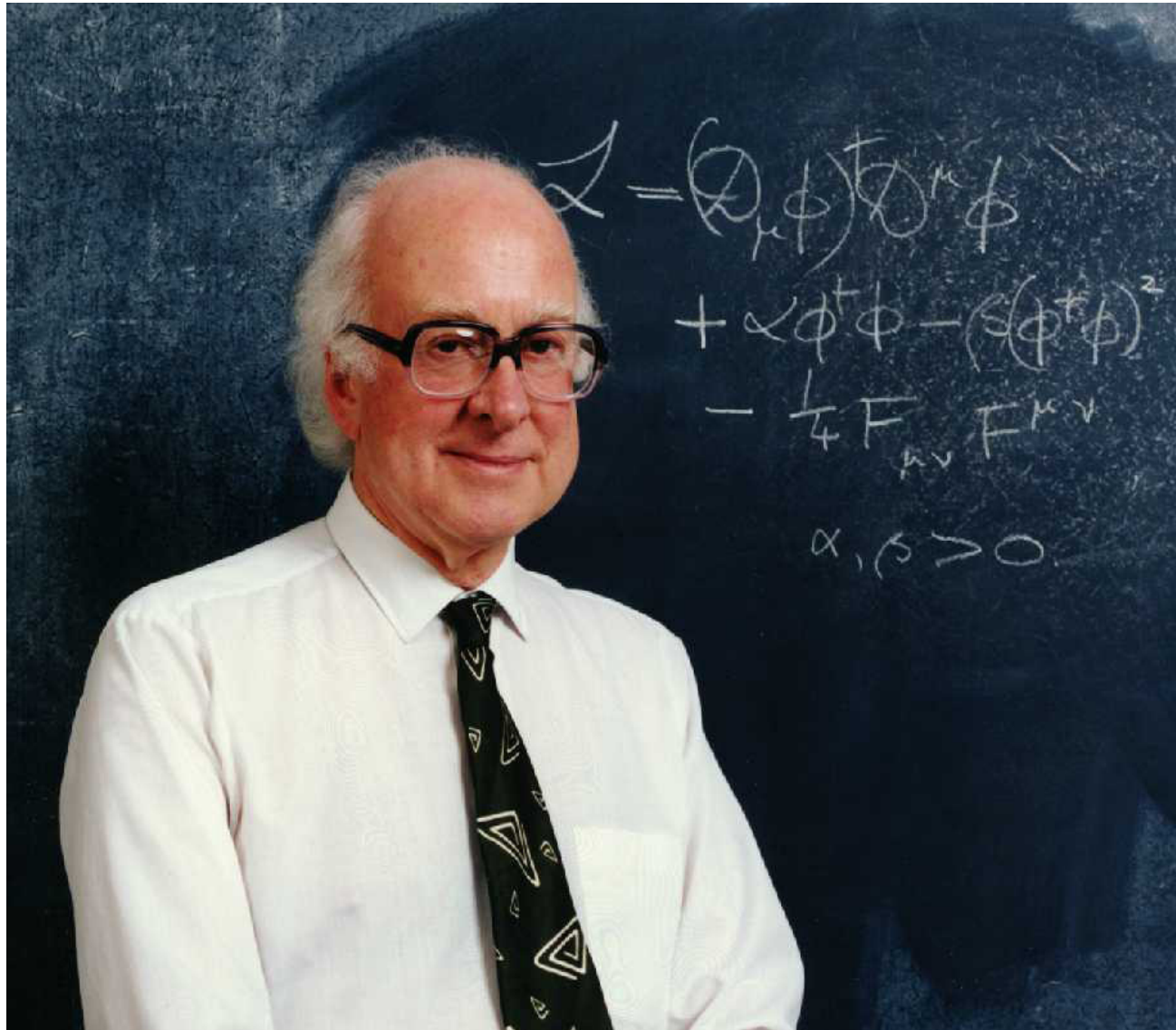
$$\text{Br}(\mu \rightarrow e \gamma) \approx 10^{-54}$$

$$\sim 10^{-11}$$

$$\mathbf{d}_n \approx 10^{-32} \text{ ecm}$$

$$\sim 10^{-26} \text{ ecm}$$

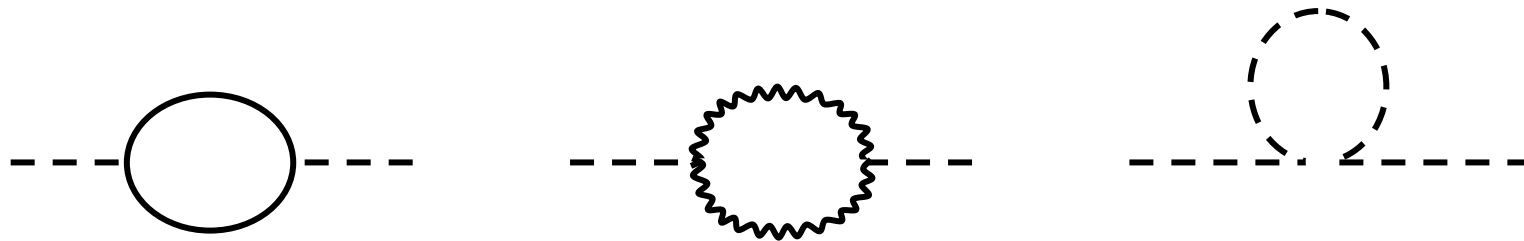
# The only Higgs found : Peter Higgs



# Hierarchy (Naturalness) Problem

(Quadratic divergences in the Higgs mass)

$$m_H^2 \sim \Lambda_{\text{cut-off}}^2 \quad \text{through radiative effects}$$



Disaster for  $\Lambda_{\text{cut-off}} \gg 1 \text{ TeV}$

$$\Lambda_{\text{cut-off}} \approx \Lambda_{\text{Planck}}$$

Must fine tune parameters to 34 decimal places to keep  $m_H \approx 0$  ( $v_{\text{SM}}$ )

or postulate New Physics at scales  $\mathbf{0}$  (1 TeV)

# Most popular Approaches to address the Hierarchy Problems

- 1. Supersymmetry** Cancellation of divergences with the help of new particles of different spin-statistic } Perturbative up to GUT scales
- 2. Little Higgs** Cancellation of divergences with the help of new particles of the same spin-statistic } Perturbative up to 10 – 20 TeV  
(Higgs = Pseudogoldstone Boson of a new spontaneously broken global symmetry) (New strong force at 10 – 20 TeV)
- 3. Technicolour** Higgs = Bound State of Techniquarks } (New strong force at 1 TeV)
- 4. Extra Dimensions** (Gauge-Higgs-Unification) Higgs = 5th component of a Gauge Field in  $D = 5$  dimensions (+ many other ideas) (Higgsless models)

# Collider Signatures of these Proposals

New Particles with masses 500 – 2000 GeV

**1.**

**Supersymmetry**

(R-Parity)



(Dark matter candidate)

Superpartners: squarks, sleptons, gluinos, charginos, neutralinos

**2.**

**Little Higgs**

(T-Parity)



New heavy Gauge Bosons:  $W_H, Z_H, A_H$

New heavy Fermions: Mirror Fermions

(Dark matter candidate)

(Scalars)

**3.**

**Technicolour**

New Resonances

Pseudogoldstone Bosons (Scalars)



Analogy to QCD

**4.**

**Extra Dimensions**

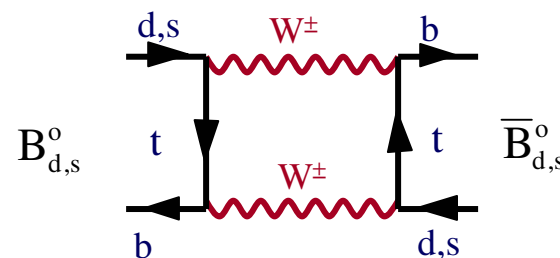
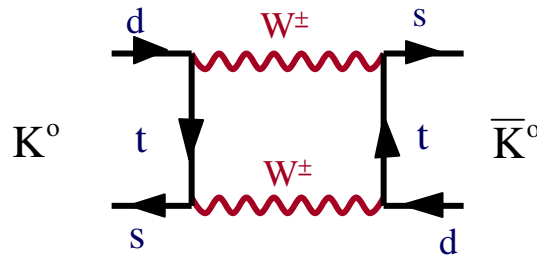
Kaluza-Klein Particles

(KK-Parity)



(Dark matter candidate)

# Impact through Quantum Fluctuations



★  $\cancel{CP}$   $\epsilon_K$ -Parameter  
 $\Delta M (K_L - K_S)$

$B_d^0 - \bar{B}_d^0$  Mixing ★  $(\Delta M_d)$

$B_s^0 - \bar{B}_s^0$  Mixing ★ ★  $(\Delta M_s)$

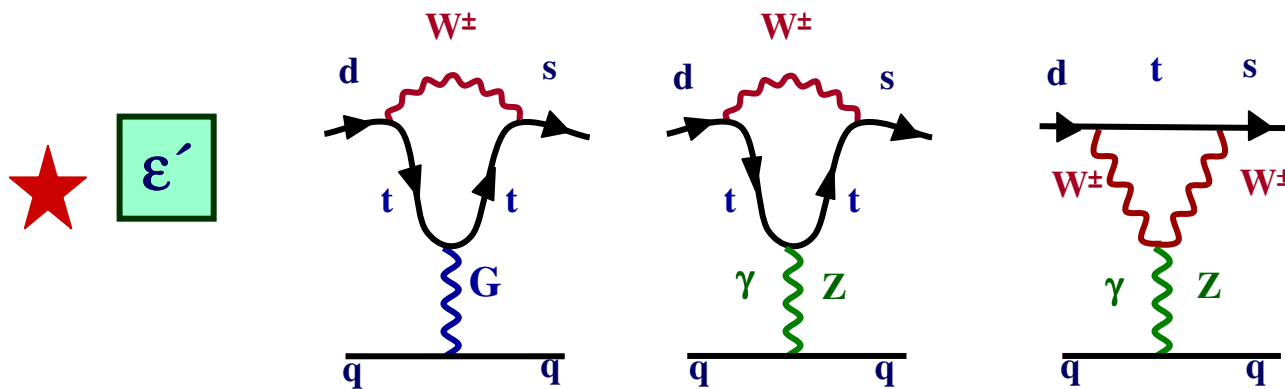
(CDF, DØ)

## CP-Asymmetries

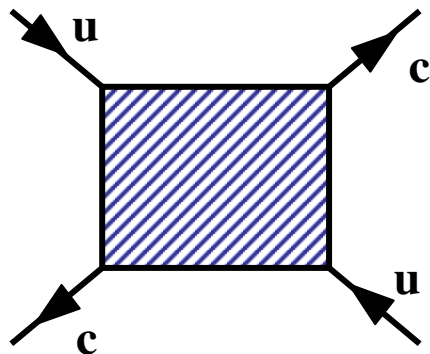
$$S_{\psi K_s} = \sin(2\beta + 2\phi_d^{\text{new}}) \quad (\text{Babar, Belle})$$

$$S_{\psi\phi} = \sin(2|\beta_s| - 2\phi_s^{\text{new}}) \quad (\text{LHC})$$

# Impact through Quantum Fluctuations



(NA48, KTeV)



$D^0 - \bar{D}^0$  Mixing  $\star$

(BaBar, Belle)



# Impact through Quantum Fluctuations



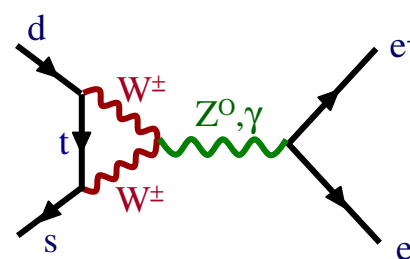
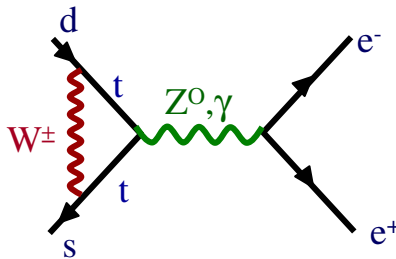
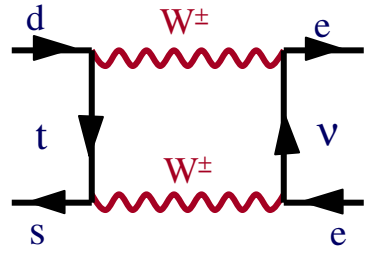
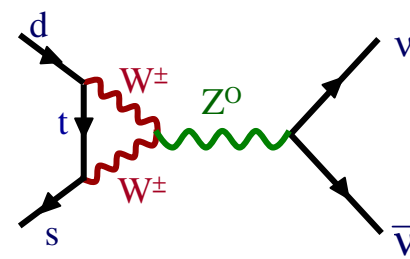
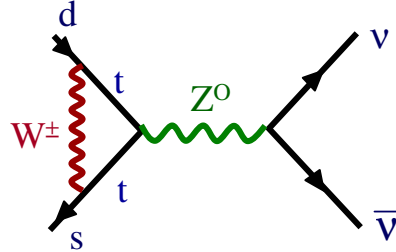
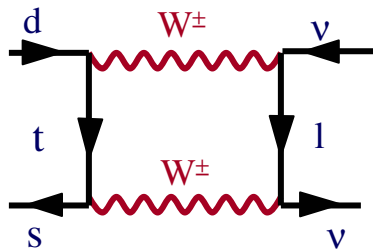
$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

$$K_L \rightarrow \pi^0 \nu \bar{\nu}$$



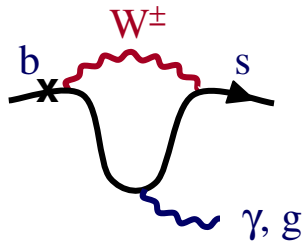
$$K_L \rightarrow \mu \bar{\mu}$$

$$B \rightarrow \mu \bar{\mu}, \quad B \rightarrow X_s \nu \bar{\nu}$$



$$K_L \rightarrow \pi^0 e^+ e^-$$

$$B \rightarrow X_s e^+ e^-, X_s \mu \bar{\mu}$$



$$B \rightarrow X_s \gamma \quad B \rightarrow K^* \gamma$$



$$B \rightarrow X_d \gamma \quad b \rightarrow s \text{ gluon}$$

# Little Hierarchy Problem

**Stabilization of the Higgs mass requires  
New Physics at scales  $\sim$  (1 TeV)**

**but**

**Electroweak Precision Tests and Flavour  
Physics Experiments imply that New Physics  
shifted to scales  $\sim$  (10 TeV) or higher**

**Solution :**

**Protective Symmetries that suppress  
NP effects in EWP-tests and Flavour  
Physics in spite of NP Scales  $\sim$  (1 TeV)**

**Custodial Symmetry; GIM Mechanism; T-Parity**

**Minimal Flavour  
Violation (MFV)**

# Different Roles of EWP-Tests and Flavour Physics

**EWPT**

:

Possible signals of NP in EWP-observables have to be very small (1%). Experiments (LEP, SLC) reached already high precision. Can be used mainly to bound parameters of a given extension of SM.

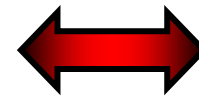
**Flavour Physics  
(Quarks  
and  
Leptons)**

:

Many observables (decays) not measured yet or measured poorly. Flavour Physics only now enters the precision era.



**Spectacular  
Deviations from SM  
still possible**



Interplay

**Direct searches  
at Tevatron, LHC,  
ILC**

## Goals for the Next 37 Min

- 1. Theoretical Framework**
- 2. Puzzles in Flavour Physics (SM)**
- 3. CMFV and MFV**
- 4. Going beyond MFV**
- 5. Finals**

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**Main Goal**

:

**Collection of 31 Goals for the LHC Era**

**1.**

# Theoretical Framework

**Starting Point**

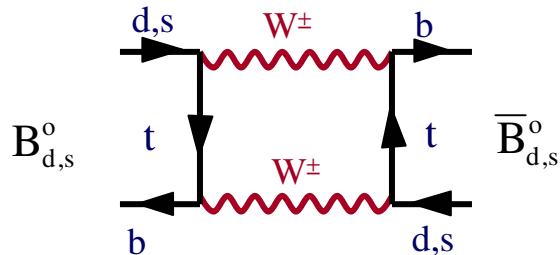
$$\mathcal{L} = \mathcal{L}_{\text{SM}}(g_i, m_i, V_{\text{CKM}}^i) + \mathcal{L}_{\text{NP}}(g_i^{\text{NP}}, m_i^{\text{NP}}, V_{\text{NP}}^i)$$

**Goal**

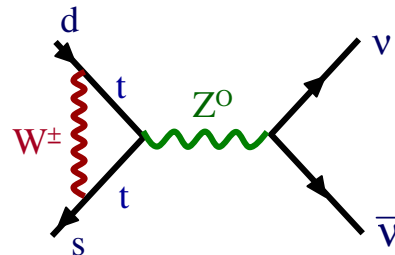
Identify the effects of  $\mathcal{L}_{\text{NP}}$  in weak decays in the presence of the background from  $\mathcal{L}_{\text{SM}}$

**First Implication from  $\mathcal{L}$**

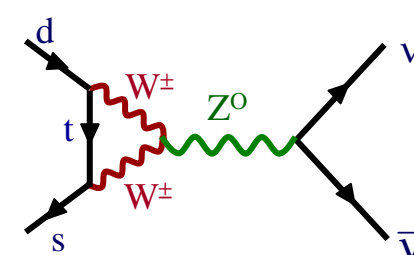
: Feynman Diagrams



$B_d^0 - \bar{B}_d^0$  Mixing



$K^+ \rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu}$



+ NP

## Two challenges :

1. Theory formulated in terms of quarks but experiments involve their bound states (K, B, D)
2. NP takes place at very short distance scales ( $10^{-19}$ - $10^{-18}$ m), while K, B, D live at  $10^{-16}$ - $10^{-15}$ m.

## Solution

: Effective Theories, OPE, Renormalization Group



Separation of SD from LD  
+ Summation of large  $\log(\mu_{SD} / \mu_{LD})$



# Master Formula for Weak Decays

AJB (2001)  
 hep-ph/0101336  
 hep-ph/0109197

Non-Perturbative  
 Factors in the SM

QCD RG  
 Factors

Short Distance Loop  
 Functions (Penguins, Boxes)

New Flavour-  
 Changing Parameters

Represent different  
 Dirac and Colour  
 Structures

$$A(\text{Decay}) = B_i \eta_{\text{QCD}}^i V_{\text{CKM}}^i \left[ F_{\text{SM}}^i + F_{\text{New}}^i \right] + B_i^{\text{New}} \left[ \eta_{\text{QCD}}^i \right]^{\text{New}} V_{\text{New}}^i \left[ G_{\text{New}}^i \right]$$

(Summation over i)

New  $\equiv$  NP

Non-Perturbative  
 Factors beyond SM

Short Distance Loop  
 Functions Penguins, Boxes

$F_{\text{SM}}^i, F_{\text{New}}^i, G_{\text{New}}^i$

: Fully calculable in  
 Perturbation Theory

$\eta_{\text{QCD}}^i, \left[ \eta_{\text{QCD}}^i \right]^{\text{New}}$

: Fully calculable in RG  
 improved Perturbation Theory

$B_i, B_i^{\text{New}}$

: Require Non-Perturbative Methods or  
 can be extracted from leading decays

(represent  $\langle Q_i \rangle$ )

Fully  
 calculable  
 in the SM

## Possible Dirac Structures in

$$K^0 - \bar{K}^0 \text{ and } B_{d,s}^0 - \bar{B}_{d,s}^0$$

**SM:**

$$\gamma_\mu (1 - \gamma_5) \otimes \gamma^\mu (1 - \gamma_5)$$

**Beyond SM:**

$$\gamma_\mu (1 - \gamma_5) \otimes \gamma^\mu (1 + \gamma_5)$$

$$(1 - \gamma_5) \otimes (1 + \gamma_5)$$

$$(1 - \gamma_5) \otimes (1 - \gamma_5)$$

$$\sigma_{\mu\nu} (1 - \gamma_5) \otimes \sigma^{\mu\nu} (1 - \gamma_5)$$

**MSSM with large  $\tan\beta$**

**General Supersymmetric Models**

**Models with complicated Higgs System**

NLO  $[\eta_{\text{QCD}}^i]^{\text{New}}$  : Ciuchini, Franco, Lubicz,  
Martinelli, Scimemi, Silvestrini

AJB, Misiak, Urban, Jäger

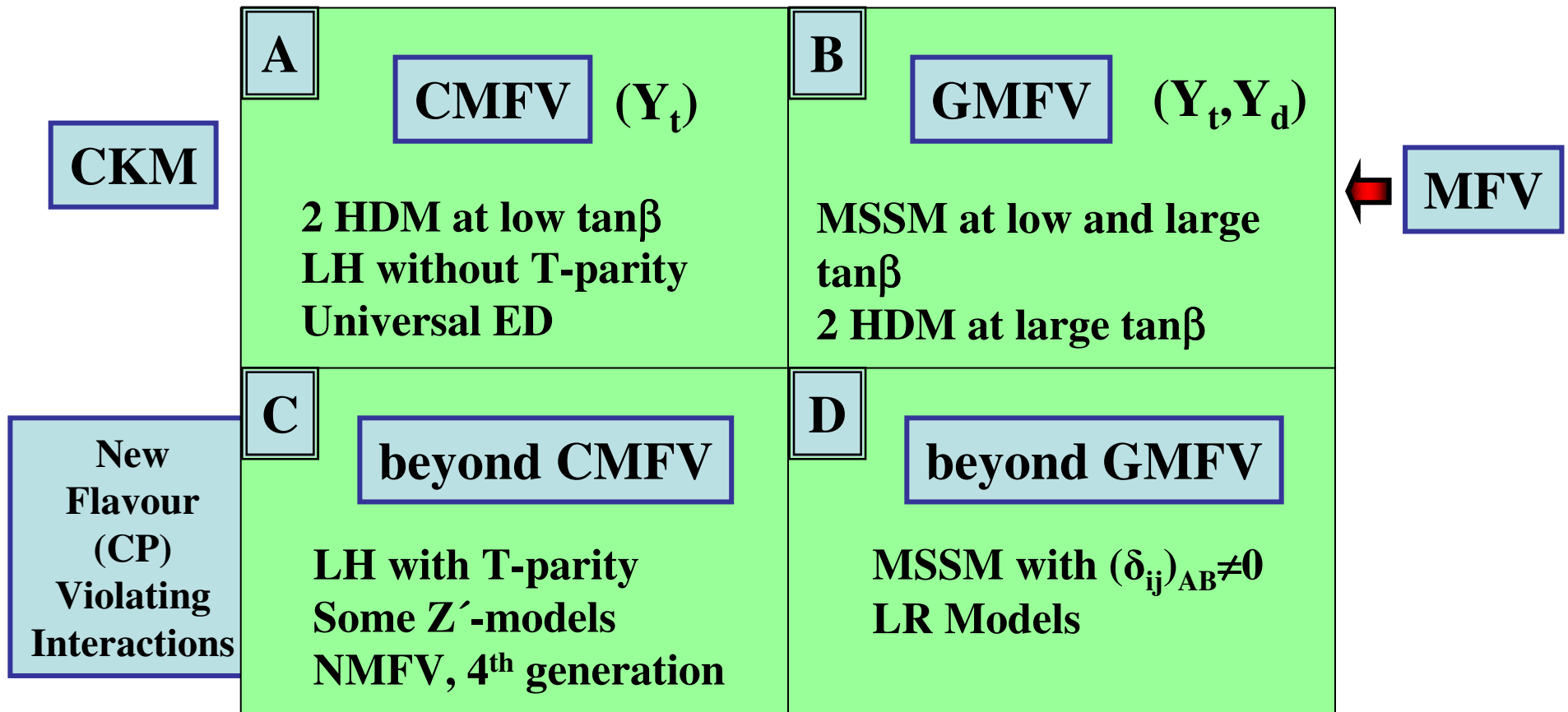


# 2 x 2 Flavour Matrix of Basic NP Scenarios

(AJB, hep-ph/0101336, Erice)

SM Operators

+ Additional Operators



# More on the 2 x 2 Flavour Matrix

**(1,1)** = CMFV ( $Y_t$ ) } 
 Gabrielli, Giudice  
 AJB, Gambino, Gorbahn, Jäger, Silvestrini  
 Ali, London; Laplace, Ligeti, Nir, Perez  
 Blanke, AJB, Guadagnoli, Tarantino

**(1,1) + (1,2)**  $\equiv$  MFV ( $Y_t, Y_d$ ) } D`Ambrosio, Giudice, Isidori, Strumia  
(Spurions and Flavour Symmetries)

**(2,1)** = New Phases in CMFV

Enhanced $Z^0$ -penguins (Munich + Rome, BFRS) NMFV (Agashe, Papucci, Perez, Pirjol) $Z'$ (Promberger, Schatt, Schwab)	}	New Physics coupling dominantly to third generation
--	---	--

LHT (Hubisz et al; Blanke et al)	}	New Sector of FV-Interactions (Mirror Fermions)
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**(2,1) + (2,2)**  $\equiv$  nMFV ( $Y_t, Y_d, Y_R, Z_L, \dots$ ) ("Spurion-Symphony")  
 (Feldmann + Mannel)

# Essential Ingredients in the Master Formula

**1.**

**Hadronic Matrix Elements ( $\hat{B}_i$ )**

(Progress still has to be made)

**2.**

**QCD and QED RG-Effects for  $\mu < m_t$  ( $\eta_i^{\text{QCD}}$ )**

1990's - era of NLO calculations

2000's - era of NNLO calculations

★  $B \rightarrow X_s l^+ l^-$  (Greub et al; Isidori et al, Beneke et al)

★  $B \rightarrow X_s \gamma$  (Misiak et al)

★  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  (AJB, Gorbahn, Haisch, Nierste)

★ Non - Leptonic  
+ Semi - Leptonic (Gorbahn, Haisch)

3 Loop  $\hat{\gamma}_{\text{anom}}$

## Magnificent 17

**M. Misiak, H.M. Asatrian, K. Bieri, M. Czakon,  
A. Czarnecki, T. Ewerth, A. Ferroglia,  
P. Gambino, M. Gorbahn, C. Greub, U. Haisch,  
A.Hovhannisyan, T. Hurth, A. Mitov,  
B.V. Poghosyan, M. Ślusarczyk, M. Steinhauser**

**$B \rightarrow X_s \gamma$  at NNLO**

## Magnificent 17

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**$B \rightarrow X_s \gamma$  at NNLO**

**Mount Everest Expedition**

# 3.

## Calculation of short distance loop functions

Best studied:

SM

MSSM

UED

LH

LHT

Z'-Models



# 2.

## Puzzles in Flavour Physics (SM)

## **UTfit Collaboration**

**Thank You !**

**M. Bona, M. Ciuchini, E. Franco, V. Lubicz  
G. Martinelli, F. Parodi, M. Pierini, P. Roudeau  
C. Schiavi, L. Silvestrini, V. Sordini, A. Stocchi  
V. Vangoni**

## **CKMfit Collaboration**

**Thank You !**

**T. Charles, A. Höcker, H. Lacker,  
F.R. Le Diberder, S. T'Jampens**

# 10 important Goals around the SM

1.

Precise measurement of  $|V_{ub}|$  and  $\gamma$  from tree-level decays



Reference UT (RUT)

$|V_{us}|, |V_{cb}|$

CKM Matrix without NP pollution

2.

Resolution of the first "sin2 $\beta$ -Problem"



$UUT \stackrel{?}{\neq} RUT$

$\varphi_{B_d}^{new} \stackrel{?}{\neq} 0$

$(\sin 2\beta)_{\psi K_s} < (\sin 2\beta)_{RUT}$

3.

Resolution of the second "sin2 $\beta$ -Problem"



$(\sin 2\beta)_{eff} < (\sin 2\beta)_{\psi K_s}$

# Reference Unitarity Triangle and UUT (CMFV)

$$(R_b)_{\text{CMFV}} = 0.363 \pm 0.016$$

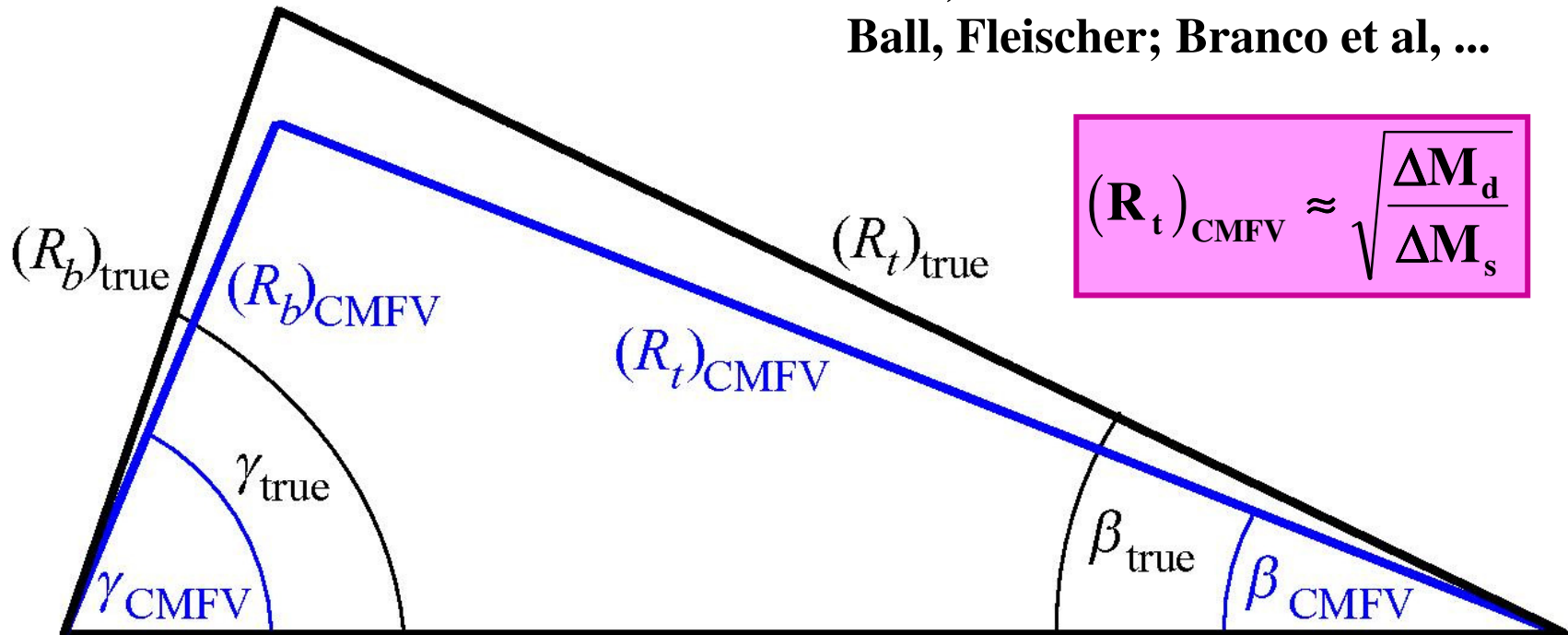
$$(R_b)_{\text{true}} = 0.428 \pm 0.027$$

$$\gamma_{\text{true}} = (82 \pm 20)^\circ$$

$$\sin 2\beta_{\text{CMFV}} = 0.675 \pm 0.026$$

$$\sin 2\beta_{\text{true}} = 0.749 \pm 0.063 \quad \text{"true" = RUT}$$

Blanke, AJB, Guadagnoli, Tarantino  
 Ufit, CKMfit  
 Ball, Fleischer; Branco et al, ...



$$(R_t)_{\text{CMFV}} \approx \sqrt{\frac{\Delta M_d}{\Delta M_s}}$$

$$\beta_{\text{CMFV}} = \beta_{\psi K_s}$$

# First Sign of a new Phase $\varphi_{B_d}$ in $B_d^0 - \bar{B}_d^0$ ?

$S_{\psi K_s}$

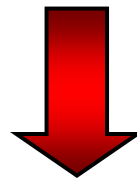
$$\begin{aligned} (\sin 2\beta)_{\text{true}} &= 0.749 \pm 0.063 \\ (\sin 2\beta)_{\psi K_s} &= 0.675 \pm 0.026 \end{aligned}$$

$$0.759 \pm 0.037$$

↑ (Ufit)

sides added

$$\gamma_{\text{true}} = (80 \pm 20)^\circ$$



$$S_{\psi K_s} = \sin(2\beta_{\text{true}} + 2\varphi_{B_d})$$

"sin 2 $\beta$  Problem"

Is this a  $|V_{ub}|$  Problem?

$$\varphi_{B_d} = -(2.9 \pm 3.3)^\circ \quad (\text{pure tree})$$

$$\varphi_{B_d} = -(3.5 \pm 1.9)^\circ \quad \text{sides added}$$

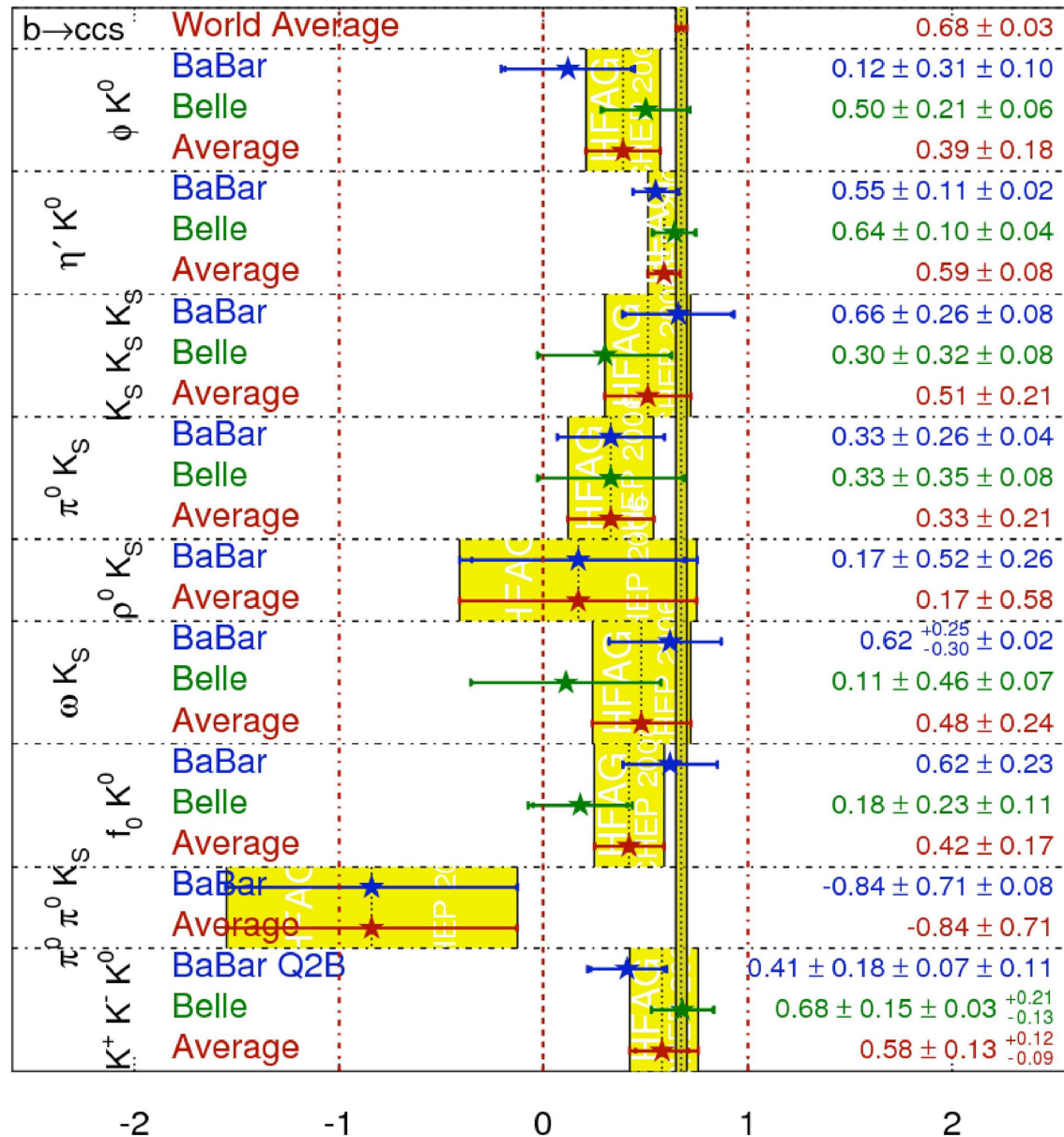
# Preliminary

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$



second

"sin2β Problem"



**4.**

Precise calculations of  
 $\hat{\mathbf{B}}_d \mathbf{F}_{B_d}^2, \hat{\mathbf{B}}_s \mathbf{F}_{B_s}^2, \xi$



**?**

$(\Delta M_{d,s})_{\text{exp}} = (\Delta M_{d,s})_{\text{SM}}$   
Important for CMFV,  
MSSM and LHT

**5.**

Precise calculation of  
 $\hat{\mathbf{B}}_K$



Does the SM  
really describe  
 $(\epsilon)_{\text{exp}}$  ?

(indirect  $\not\mathcal{P}$ )

**6.**

Precise calculation of  
 $B_6$  and  $B_8$   
(hadronic matrix elements  
in  $\Delta S = 1$  Hamiltonian)



Does the SM  
really describe  
 $(\epsilon'/\epsilon)_{\text{exp}}$   $\left[ \begin{array}{c} \text{direct} \\ \not\mathcal{P} \end{array} \right]$  ?

**7.**

Resolution of the  
 $B \rightarrow X_s \gamma$  problem

$$(B \rightarrow X_s \gamma)_{SM} < (B \rightarrow X_s \gamma)_{exp}$$

**8.**

Resolution of the  
 $(g-2)_\mu$  problem

$$[(g-2)_\mu]_{SM} \neq [(g-2)_\mu]_{exp}$$

**9.**

$B \rightarrow \pi K, \pi^+ \pi^-$   
Puzzles

Some "Puzzles" softened  
Other remained (CP-asymmetries)  
Are new phases necessary to fit  
the two body data ?

**10.**

Did we see  
direct CP in  $B_d^0 \rightarrow \pi^+ \pi^-$  ?

$$\begin{aligned} [A_{CP}^{dir}(\pi^+ \pi^-)]_{Belle} &= -0.55 \pm 0.08 \pm 0.05 \\ [A_{CP}^{dir}(\pi^+ \pi^-)]_{Babar} &= -0.16 \pm 0.11 \pm 0.03 \end{aligned}$$



## **$B \rightarrow X_s \gamma$ Puzzle (2007)**

$$\text{Br}(B \rightarrow X_s \gamma)_{\text{exp}} = (3.55 \pm 0.24 \pm 0.10 \pm 0.03) \cdot 10^{-4}$$

(BaBar, Belle) (HFAG)

$$\text{Br}(B \rightarrow X_s \gamma)_{\text{SM}} = (2.98 \pm 0.26) \cdot 10^{-4}$$

(Misiak + 16 Magnificent) (Becher, Neubert)

1.4  $\sigma$  lower

Really not a puzzle but  
models with

$\text{Br}(B \rightarrow X_s \gamma) < \text{Br}(B \rightarrow X_s \gamma)_{\text{SM}}$   
disfavoured

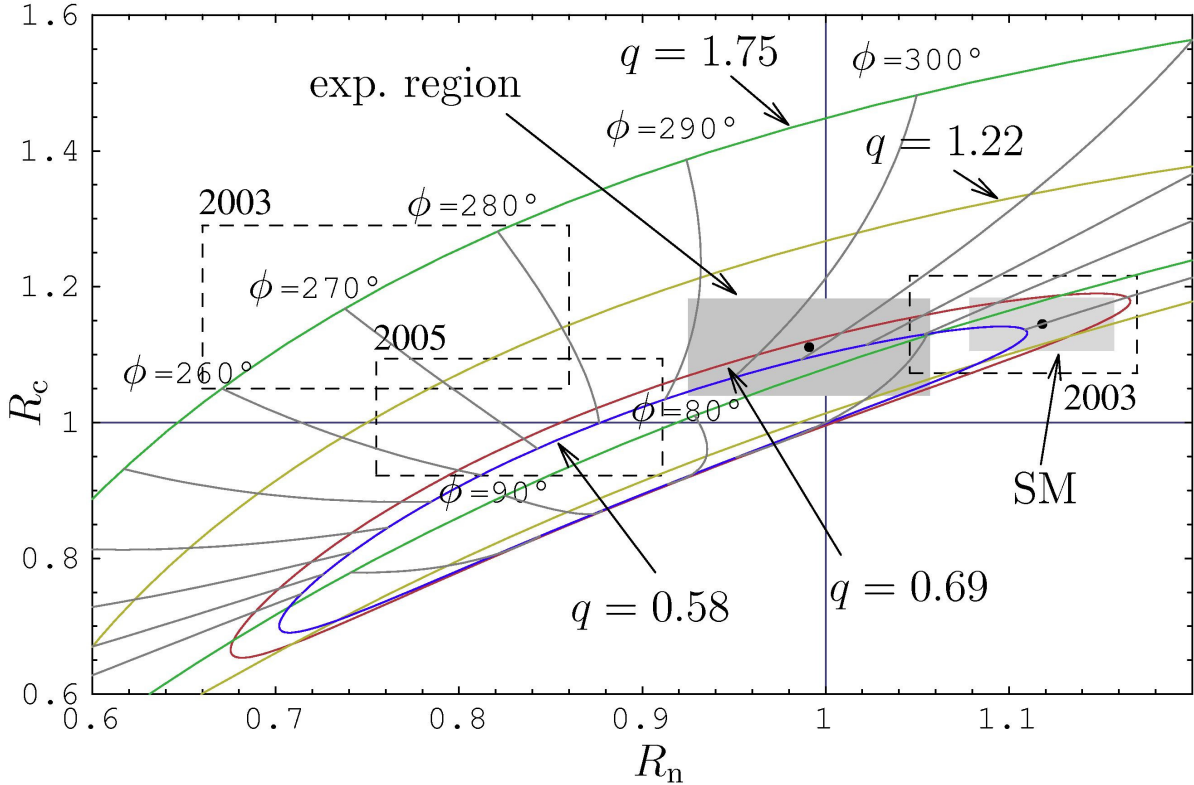
# B → ππ, πK Puzzles

(2007)

**AJB, Fleischer (2000)**  
**Yoshikawa (2003)**  
**Gronau, Rosner (2003)**  
**Beneke, Neubert (2003)**  
**BFRS (2003)**

**(EWP with new  
 complex phases  
 at work ?)**

**AJB  
 Fleischer  
 Recksiegel  
 Schwab**



**FRS  
 (0702275)**

# Messages from Fleischer, Recksiegel, Schwab

hep-ph 0702275

1.

**BFRS strategy**

$$+ \\ A_{\text{CP}}^{\text{dir}}(\text{B}_d \rightarrow \pi^\pm \text{K}^\pm) \\ (\text{Belle} + \text{BaBar})$$



$$A_{\text{CP}}^{\text{dir}}(\text{B}_d \rightarrow \pi^+ \pi^-) = -0.24 \pm 0.04$$

in favour of BaBar

2.

$R_n \neq R_c$  softened but  
CP-puzzle remains

$$A_{\text{CP}}^{\text{mix}}(\text{B}_d \rightarrow \pi^0 \text{K}_s)_{\text{SM}} = -0.81 \pm 0.03 \\ A_{\text{CP}}^{\text{mix}}(\text{B}_d \rightarrow \pi^0 \text{K}_s)_{\text{exp}} = -0.33 \pm 0.21$$

possibly related to  $(\sin 2\beta)_{\text{eff}} < (\sin 2\beta)_{\psi\text{K}_s}$

3.

$$A_{\text{CP}}^{\text{dir}}(\text{B}^\pm \rightarrow \pi^0 \text{K}^\pm) - A_{\text{CP}}^{\text{dir}}(\text{B}_d \rightarrow \pi^\mp \text{K}^\pm) \stackrel{\text{exp}}{=} -0.140 \pm 0.030$$

likely generated through hadronic effects

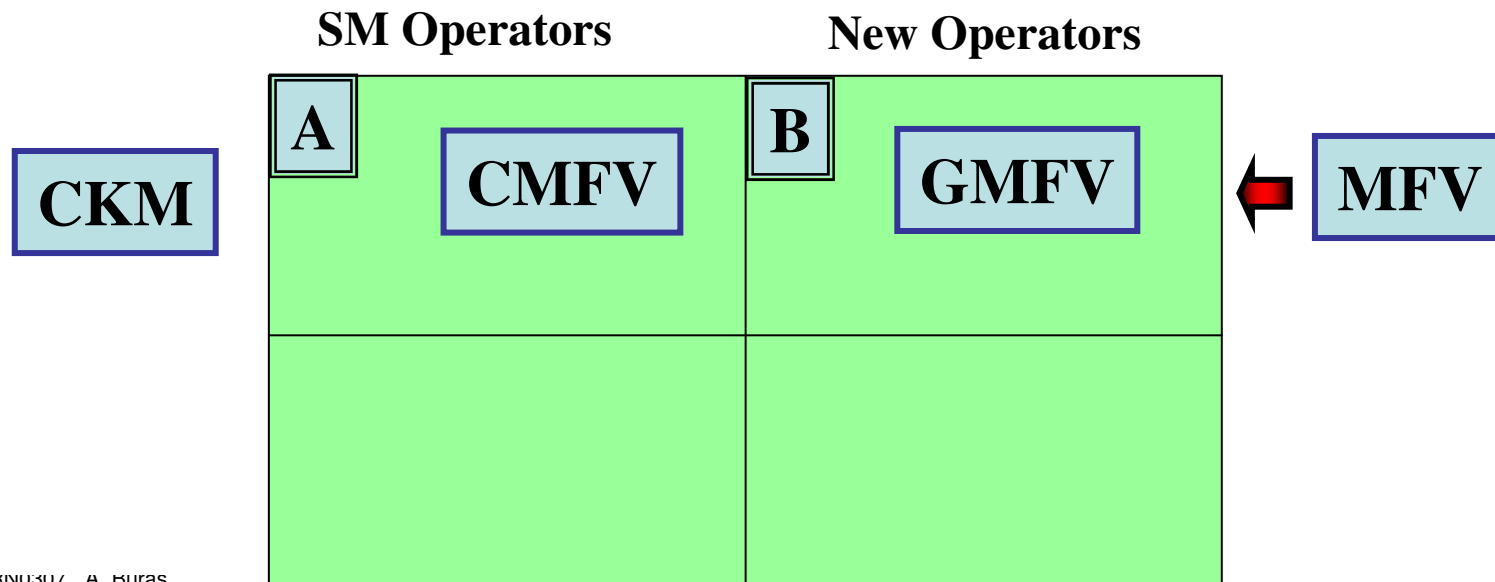
4.

$$\gamma = \left( 70.0^{+3.8}_{-4.3} \right)^{\circ} \pm \text{TH}$$

in agreement with UT-fits

# 3.

## CMFV and MFV



# Upper Bounds on Rare K and B Decays from CMFV

Bobeth, Bona, AJB, Ewerth, Pierini, Silvestrini, Weiler hep-ph/0505110

Branching Ratios	CMFV (95%)	SM (95%)	SM (68%)	Exp
$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) \cdot 10^{11}$	$<11.9$	$<10.9$	$8.3 \pm 1.2$	$14.7^{+13.0}_{-8.9}$
$\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu}) \cdot 10^{11}$	$<4.6$	$<4.2$	$3.1 \pm 0.6$	$<5.9 \cdot 10^4$
$\text{Br}(\text{B} \rightarrow X_s \nu \bar{\nu}) \cdot 10^5$	$<5.2$	$<4.1$	$3.7 \pm 0.2$	$<64$
$\text{Br}(\text{B}_s \rightarrow \mu^+ \mu^-) \cdot 10^9$	$<7.4$	$<5.9$	$3.7 \pm 1.0$	$<5.0 \cdot 10^2$
$\text{Br}(\text{B}_d \rightarrow \mu^+ \mu^-) \cdot 10^{10}$	$<2.2$	$<1.8$	$1.1 \pm 0.4$	$<1.6 \cdot 10^3$

Improved  
Bounds  
(2007)

Including Impact from  $R_b^0$ ,  $A_b$ ,  $A_{FB}^{0,b}$

Haisch  
Weiler  
(2007)

The sign of Z-penguin Amplitude in CMFV is SM like

Branching Ratios	CMFV (95%)	SM (95%)	Exp
$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \cdot 10^{11}$	3.9-10.7	5.5-9.5	$14.7^{+13.0}_{-8.9}$
$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \cdot 10^{11}$	1.2-4.5	2.3-3.6	$<2.1 \cdot 10^4$
$\text{Br}(B \rightarrow X_s \nu \bar{\nu}) \cdot 10^5$	1.5-4.7	3.0-3.6	$<64$
$\text{Br}(B_s \rightarrow \mu^+ \mu^-) \cdot 10^9$	0.8-6.1	2.9-4.2	$<1.0 \cdot 10^2$
$\text{Br}(B_d \rightarrow \mu^+ \mu^-) \cdot 10^{10}$	0.2-1.5	0.9-1.3	$<3.0 \cdot 10^2$

## Golden Relations of CMFV and MFV:

AJB (03)

$$\frac{Br(B_s \rightarrow \mu^+ \mu^-)}{Br(B_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{B}_{B_d}}{\hat{B}_{B_s}} \frac{\tau(B_s)}{\tau(B_d)} \frac{\Delta M_s}{\Delta M_d} r$$

**(CMFV)**  
r = 1

Buchalla, AJB (94)  
AJB, Fleischer (01)

$$(\sin 2\beta)_{B \rightarrow \psi K_S} = (\sin 2\beta)_{K \rightarrow \pi \nu \bar{\nu}}$$

**(MFV)**

The **violation** of these model independent **MFV (CMFV)** relations would **signal new flavour and CP-violating interactions (and/or new operators)**

$$\Delta M_{s,d} \text{ (2007)}$$

$$(\Delta M_s) = (17.77 \pm 0.10 \pm 0.07) / \text{ps} \quad (\text{CDF, D}\emptyset)$$

$$(\Delta M_s)_{\text{UTfit}}^{\text{SM}} = (21.5 \pm 2.6) / \text{ps}$$

$$(\Delta M_s)_{\text{CKMfitter}}^{\text{SM}} = \left( 21.7 \pm \begin{matrix} 5.9 \\ 4.2 \end{matrix} \right) / \text{ps}$$

(before measurements)

$$(\Delta M_s)_{\text{UTfit}}^{\text{SM}} = (18.4 \pm 2.2) / \text{ps}$$

$$(\Delta M_s)_{\text{CKMfitter}}^{\text{SM}} = \left( 18.9 \pm \begin{matrix} 5.7 \\ 2.8 \end{matrix} \right) / \text{ps}$$

(2007)



BBGT  
(2006)

## Implications of $\Delta M_s$ Measurement for Rare Decays

(Model independent “magic numbers” of CMFV)

$$\frac{\text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-)}{\text{Br}(\mathbf{B}_d \rightarrow \mu^+ \mu^-)} = 33.0 \pm 1.9$$

$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.210 \pm 0.010$$

$$\frac{\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_s \nu \bar{\nu})}{\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_d \nu \bar{\nu})} = 22.7 \pm 2.2$$

(Blanke, AJB,  
Guadagnoli, Tarantino)  
(update)

$$\begin{aligned} \text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-)_{\text{SM}} &= (3.37 \pm 0.31) \cdot 10^{-9} \\ \text{Br}(\mathbf{B}_d \rightarrow \mu^+ \mu^-)_{\text{SM}} &= (1.02 \pm 0.09) \cdot 10^{-10} \end{aligned}$$

$$> 1 \cdot 10^{-7}$$

$$> 3 \cdot 10^{-8}$$

CDF (95% C.L.)  
DØ

$$\text{Is } (\Delta M_s)_{\text{CMFV}} > (\Delta M_s)_{\text{SM}} ?$$

**M. Blanke, AJB (06) : (Diagrammatic analysis)**

**Indeed it is, with two possible exceptions:**

**Negative contributions from :**

- ★ **U(1) neutral gauge bosons in box diagrams (no tree)**
- ★ **Majorana Fermions in box diagrams (for certain values of the parameters of a given theory)**

**Could still be cancelled by other positive contributions in a given theory.**



# MSSM with MFV and low $\tan\beta$

Altmannshofer, AJB, Guadagnoli (07)

0703200

Explicit Execution of D'Ambrosio, Giudice, Isidori, Strumia (02)

Proposal :

Expression of all soft terms through Yukawa couplings  $Y_t$  and  $Y_d$

Very significant increase of predictivity



Correct MFV Limit of MSSM

Messages

1.

$$(\Delta M_s)_{\text{MSSM (low } \tan\beta)} > (\Delta M_s)_{\text{SM}}$$

Interesting interplay of charginos and gluinos

2.

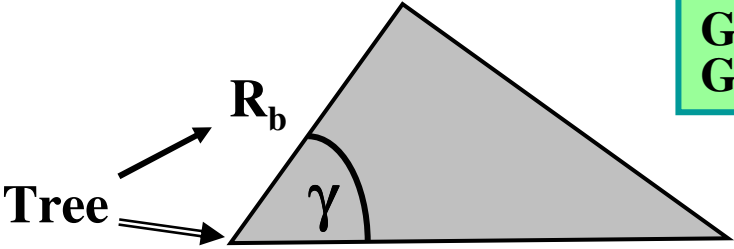
MSSM at low  $\tan\beta \neq \text{CMFV}$   
(mainly because of gluino contributions at large  $\mu$ , which imply **NEW OPERATORS**)



# Three Unitarity ( $B_d$ ) Triangles

Reference  
Unitarity  
Triangle

Goto, Kitazawa, Okada, Tanaka,  
Grossman, Nir, Worah

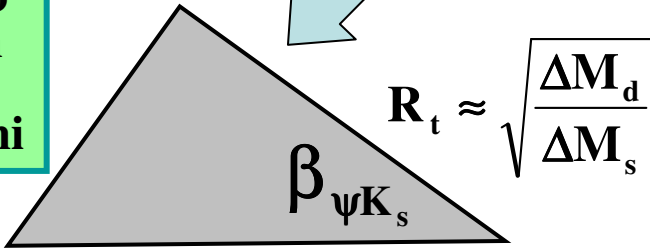


Useful for search of  
new operators and  
phases in  $B_d^0 - \bar{B}_d^0$

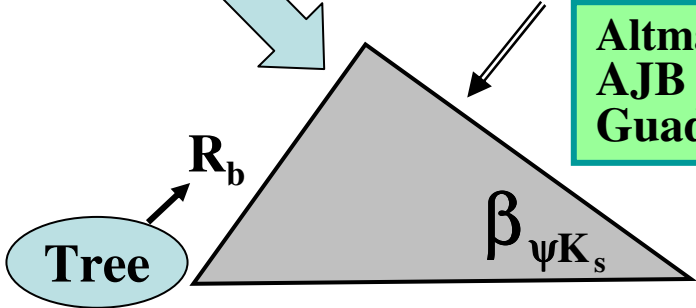
Useful for test  
of correlation  
 $R_b \leftrightarrow \gamma$  from MFV

$$R_t \approx \sqrt{\frac{\Delta M_d}{\Delta M_s}} r_{NP}$$

AJB  
Gambino  
Gorbahn  
Jäger  
Silvestrini



Altmannshofer  
AJB  
Guadagnoli



UUT in CMFV

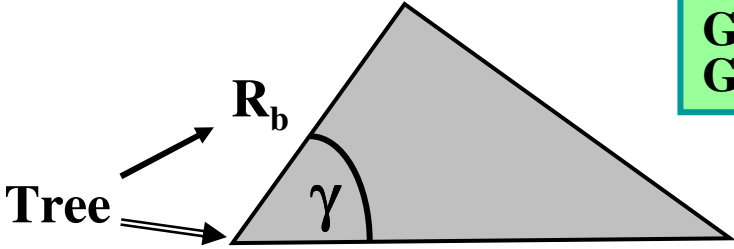
UT in MFV

Need improved Non-Pert. + SFF(SB) to distinguish them

# Three Unitarity ( $B_d$ ) Triangles

Reference  
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Goto, Kitazawa, Okada, Tanaka,  
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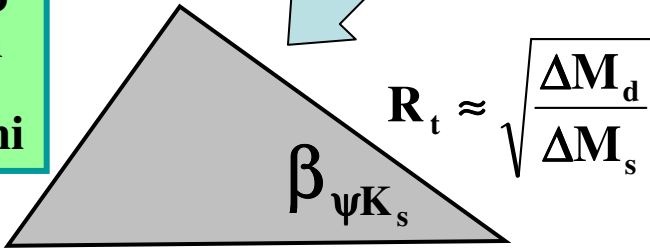


Useful for search of  
new operators and  
phases in  $B_d^0 - \bar{B}_d^0$

Useful for test  
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$$R_t \approx \sqrt{\frac{\Delta M_d}{\Delta M_s}} r_{NP}$$

AJB  
Gambino  
Gorbahn  
Jäger  
Silvestrini



Altmannshofer  
AJB  
Guadagnoli

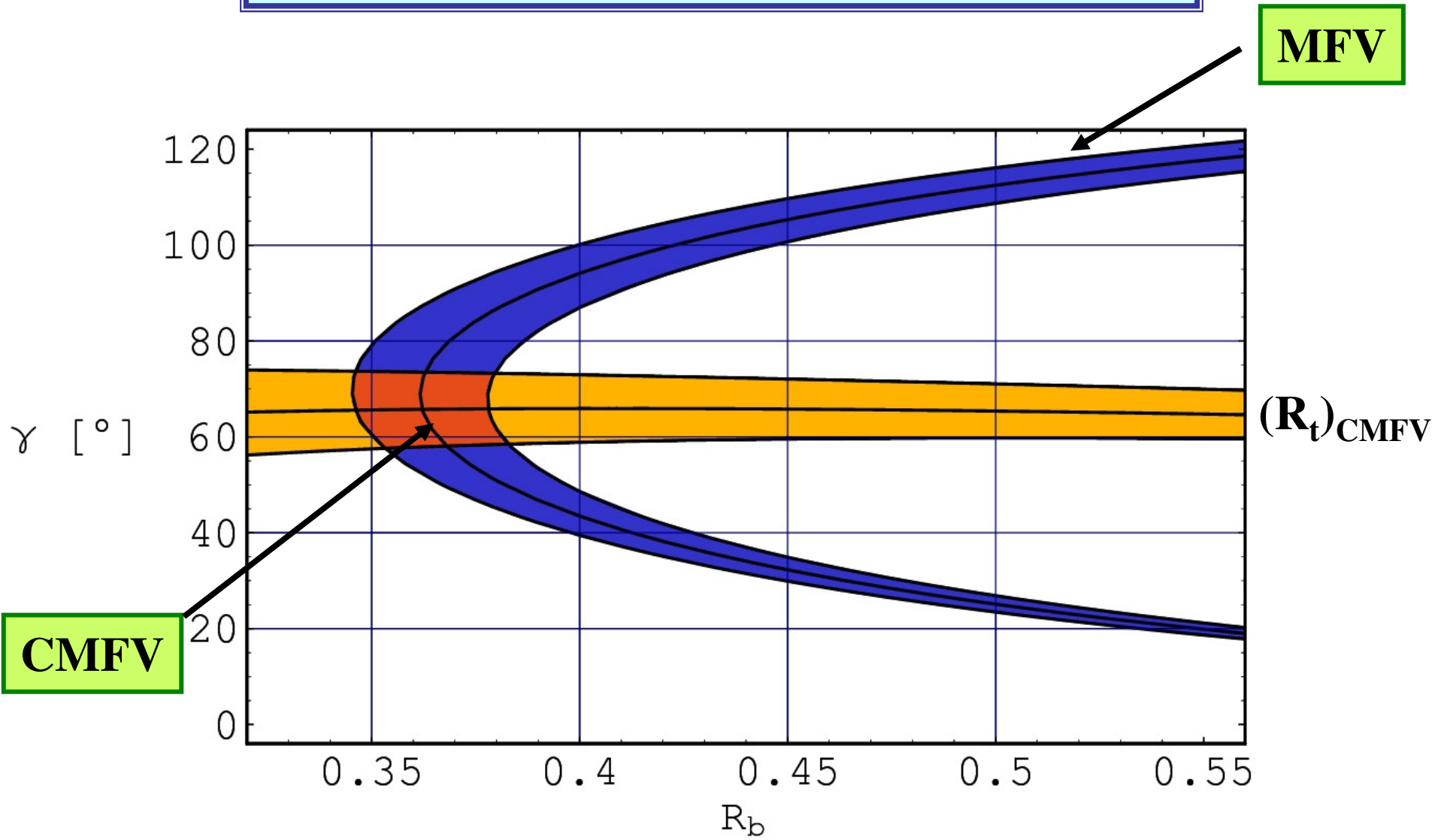


UUT in CMFV

UT in MFV

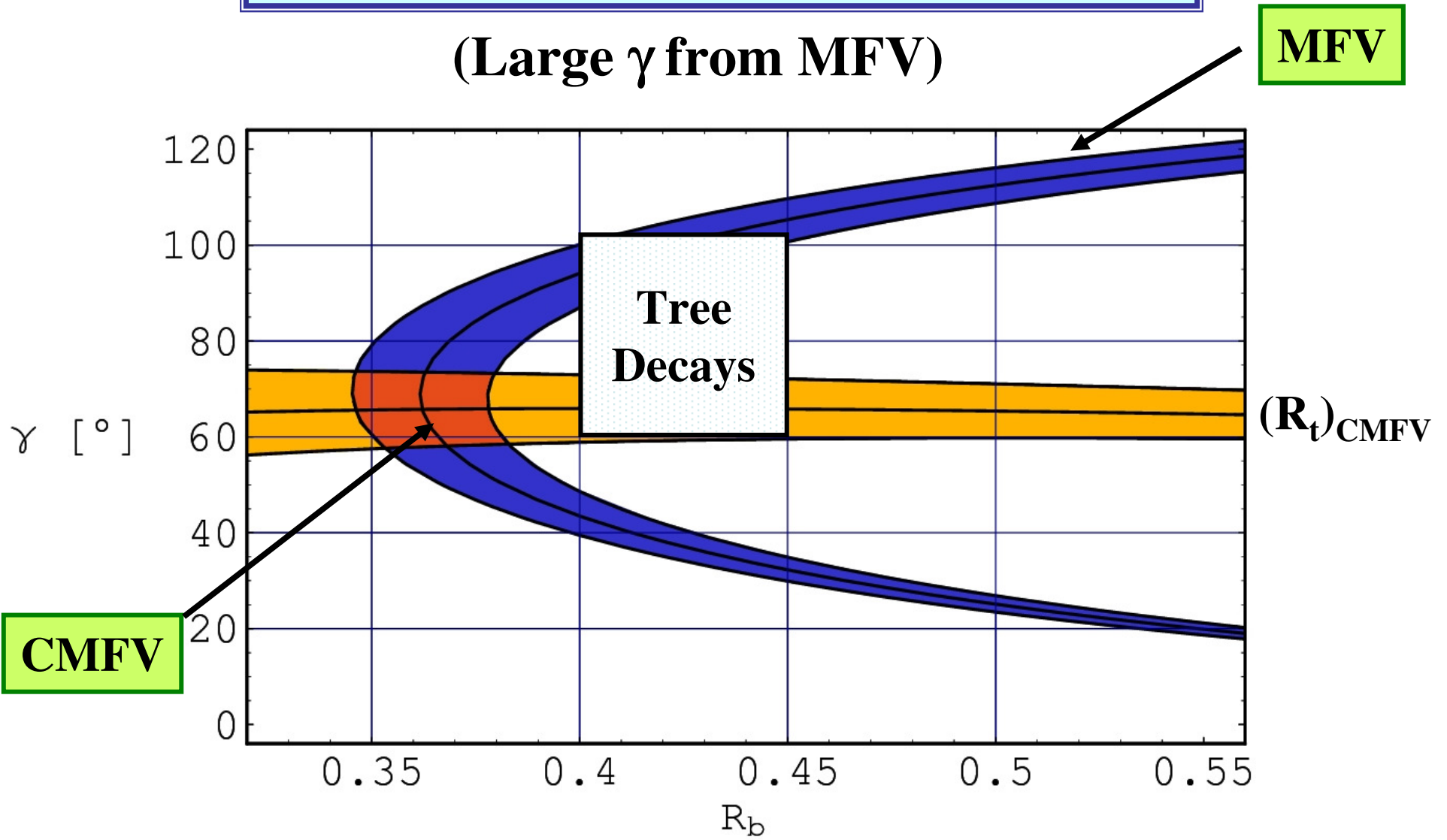
Need improved Non-Pert. + SFF(SB) to distinguish them

# A closer Look at CMFV and MFV : $R_b \leftrightarrow \gamma$ Correlation



# A closer Look at CMFV and MFV : $R_b \leftrightarrow \gamma$ Correlation

(Large  $\gamma$  from MFV)



**Conjecture**

**$|V_{ub}|_{incl}$  correct**

**( $R_b$ )**

**First "sin2 $\beta$  problem" is not a problem of MFV but a problem of CMFV**



**MFV**

$$\gamma_{true} \gtrsim 80^\circ$$

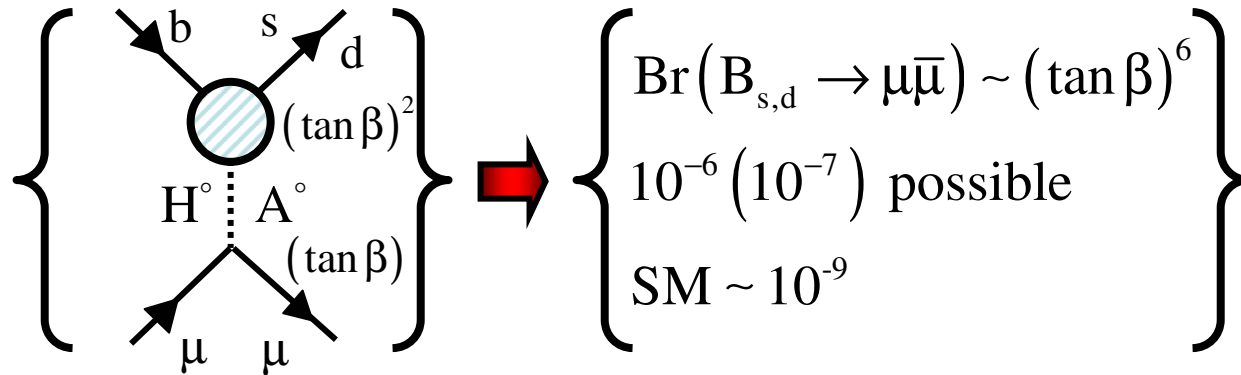
**Larger than SM UT-fits but could be OK in the presence of NP**



# $B_{s,d} \rightarrow \mu^+ \mu^-$ and MSSM with MFV at large $\tan\beta$

In MSSM at large  $\tan\beta$   
 (CKM still the only source of Flavour and CP Violation)

**Strong Enhancement**



- Babu, Kolda
- Chankowski, Slawianowska
- Bobeth, Ewerth, Krüger, Urban
- Huang, Liao, Yan, Zhu
- Isidori, Retico
- Dedes, Dreiner, Nierste
- Dedes, Pilaftis
- Chankowski, Rosiek
- Foster, Okumura, Roszkowski
- Carena et al.
- Isidori, Paradisi

**$\text{Br}(B_s \rightarrow \mu\bar{\mu}) < 1 \cdot 10^{-7}$**

95% C.L  
 (CDF, DØ)

**$\text{Br}(B_d \rightarrow \mu\bar{\mu}) < 3 \cdot 10^{-8}$**

95% C.L.

# $\Delta M_{s,d}$ in MSSM with MFV and large $\tan\beta$

Suppression

$$\left\{ \begin{array}{c} \text{Diagram with } b, s, H^0, A^0 \text{ and } (\tan\beta)^2 \text{ vertices} \end{array} \right\} \rightarrow \left\{ \Delta M_s \approx (\Delta M_s)^{\text{SM}} - c(\tan\beta)^4 \right\}$$

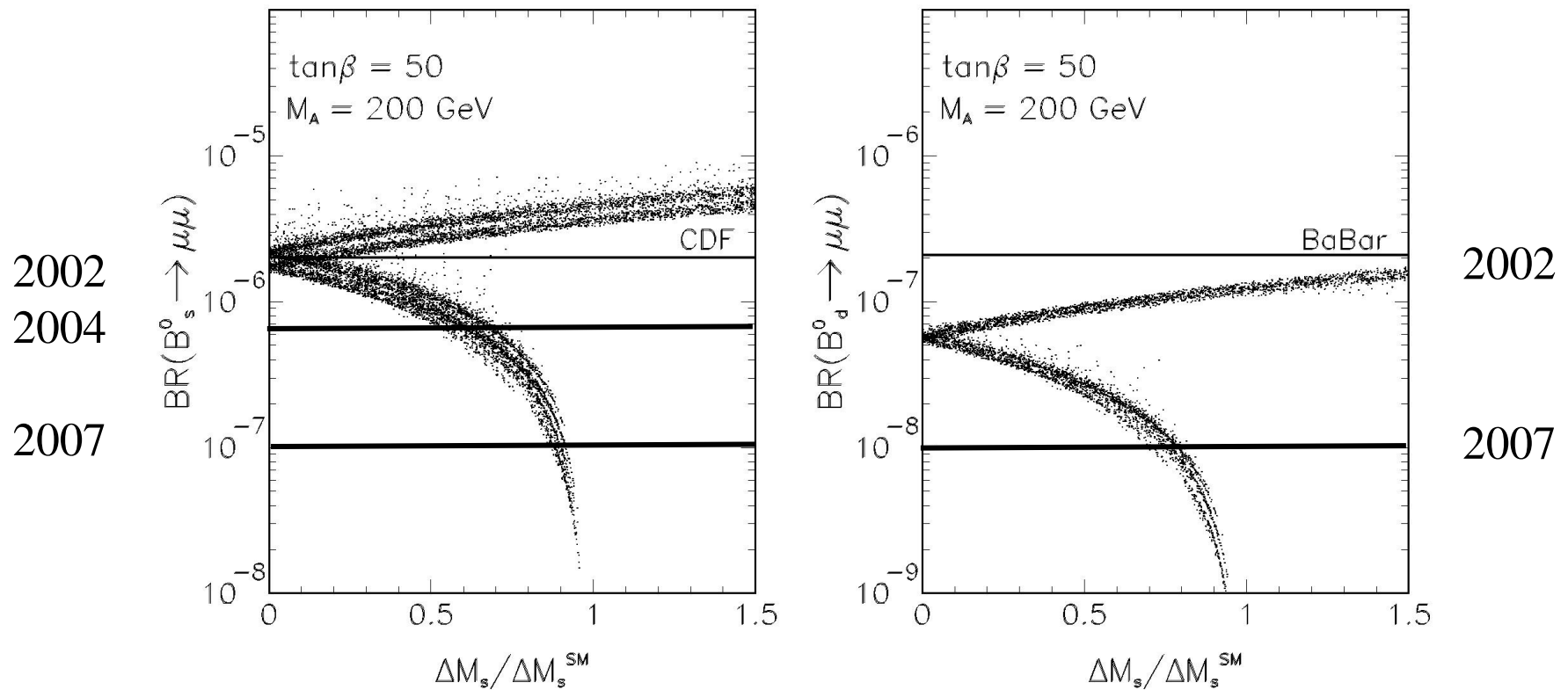
AJB, Chankowski, Rosiek  
Slawianowska (2001, 2002)

Correlation between  
SUSY effects in  
 $\text{Br}(B_{s,d} \rightarrow \mu\bar{\mu})$  and  $\Delta M_s$

Subsequent analyses: D'Ambrosio, Giudice, Isidori, Stumia  
Dedes, Pilaftis; Carena et al

# $\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)$ vs $(\Delta M_s)^{\text{exp}} / (\Delta M_s)^{\text{SM}}$ in SUSY at Large $\tan \beta$

AJB, Chankowski, Rosiek, Slawianowska, hep-ph/0207241



# The Virtue of $\Delta M_s$

$$(\Delta M_s)_{\text{CMFV}} > (\Delta M_s)_{\text{SM}}$$

$$(\Delta M_s)_{\text{MSSM}} > (\Delta M_s)_{\text{SM}} \\ \text{(Low } \tan\beta\text{)}$$

$$(\Delta M_s)_{\text{MSSM}} < (\Delta M_s)_{\text{SM}} \\ \text{(Large } \tan\beta\text{)}$$

**Answering**  
 $(\Delta M_s)_{\text{exp}} \leftrightarrow (\Delta M_s)_{\text{SM}}$   
**could rule out**  
**certain scenarios**  
**independently of**  
**specific parameters**  
**of a given model**

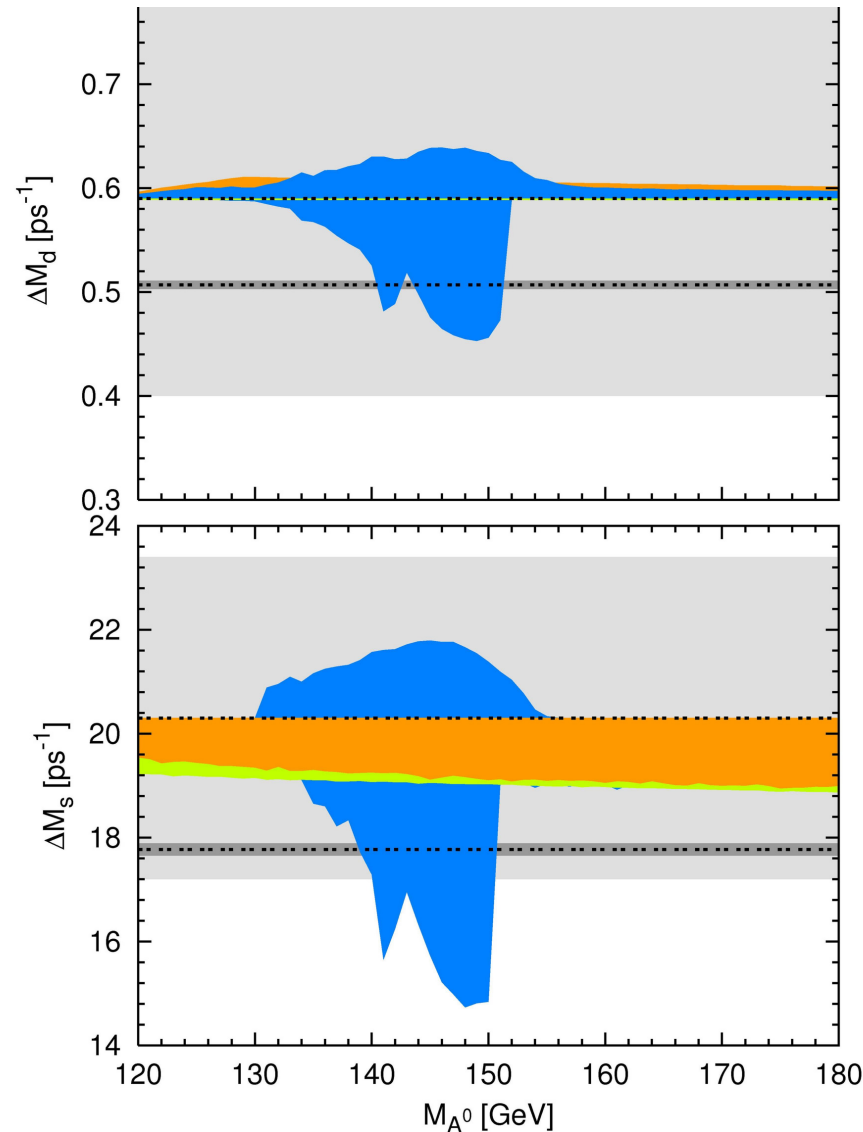
# New Analysis of $\Delta M_{s,d}$ at large $\tan\beta$

(MSSM)  
with

**MFV**

A. Freitas  
E. Gasser  
U. Haisch

(hep-ph/0702267)

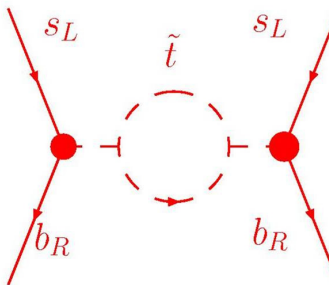
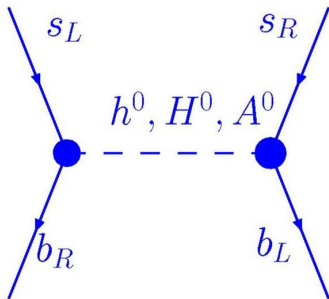
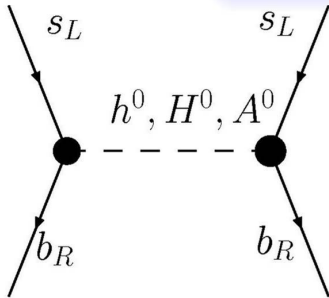


Inclusion of  
three loop  
corrections

$(\Delta M_s)_{\text{MSSM}} > (\Delta M)_{\text{SM}}$   
at large  $\tan\beta$

Possible (?)

## Message from Gorbahn, Jäger, Nierste, Trine 2007



- “Tree-level” contribution vanishes [Babu, Kolda '99]
- All subleading effects have to be studied:  
 $m_s/m_b$ , loops,  $1/\tan\beta$ ,  $v_{EW}/M_{SUSY}$
- $\mathcal{O}(\frac{m_s}{m_b})$ : Significantly suppress  $\Delta M_{B_s}$ .  
[AJB, Chankowski, Rosiek, Slawianowska '02]
- Loop induced Higgs interactions:  
Moderately enhance  $\Delta M_{B_s}$  and  $\Delta M_{B_d}$ .

Sparticle Loops and  $\mathcal{O}(m_s/m_b)$ :

$$(\Delta M_s)_{MSSM} < (\Delta M_s)_{SM}$$

$$(\Delta M_d)_{MSSM} > (\Delta M_d)_{SM}$$

Impact on UT fit

Large  $\tan\beta$

# Messages from Universal Extra Dimensions

ACD Model in D=5

CMFV

**1.**

$$\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_s \gamma)_{\text{UED}} < \text{Br}(\mathbf{B} \rightarrow \mathbf{X}_s \gamma)_{\text{SM}}$$

Agashe, Deshpande, Wu  
AJB, Poschenrieder,  
Spranger, Weiler

**2.**

$$(\hat{\mathcal{S}}_0)_{\text{UED}} < (\hat{\mathcal{S}}_0)_{\text{SM}}$$

$$A_{\text{FB}}(\mathbf{B} \rightarrow \mathbf{X}_s l^+ l^-)$$

BPSW

correlated with the suppression of  $\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_s \gamma)$

**3.**

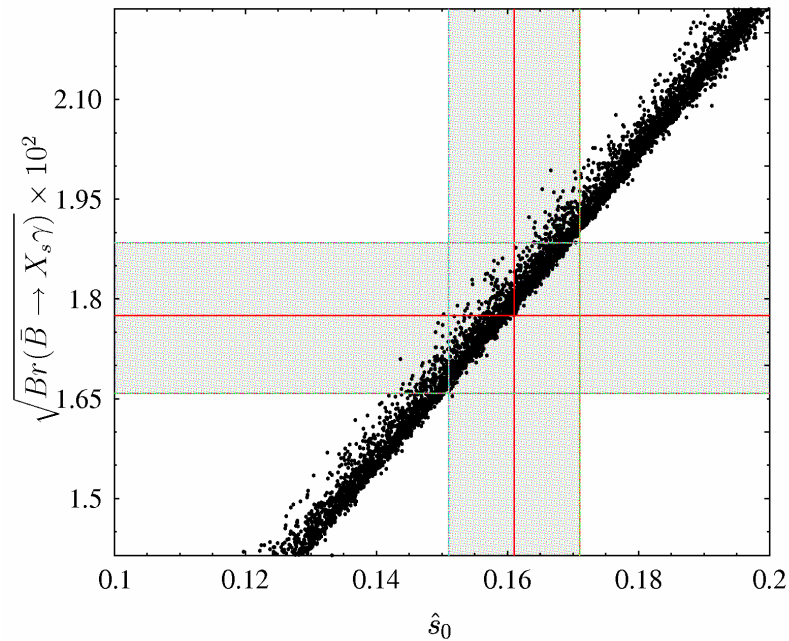
Similar suppression in  $A_{\text{FB}}(\mathbf{B} \rightarrow \mathbf{K}^* l^+ l^-)$

(Colangelo, De Fazio, Ferrandes, Pham)

Correlation:  $\text{Br}(B \rightarrow X_s \gamma) \leftrightarrow \hat{s}_0$  in  $A_{\text{FB}}(B \rightarrow X_s l^+ l^-)$

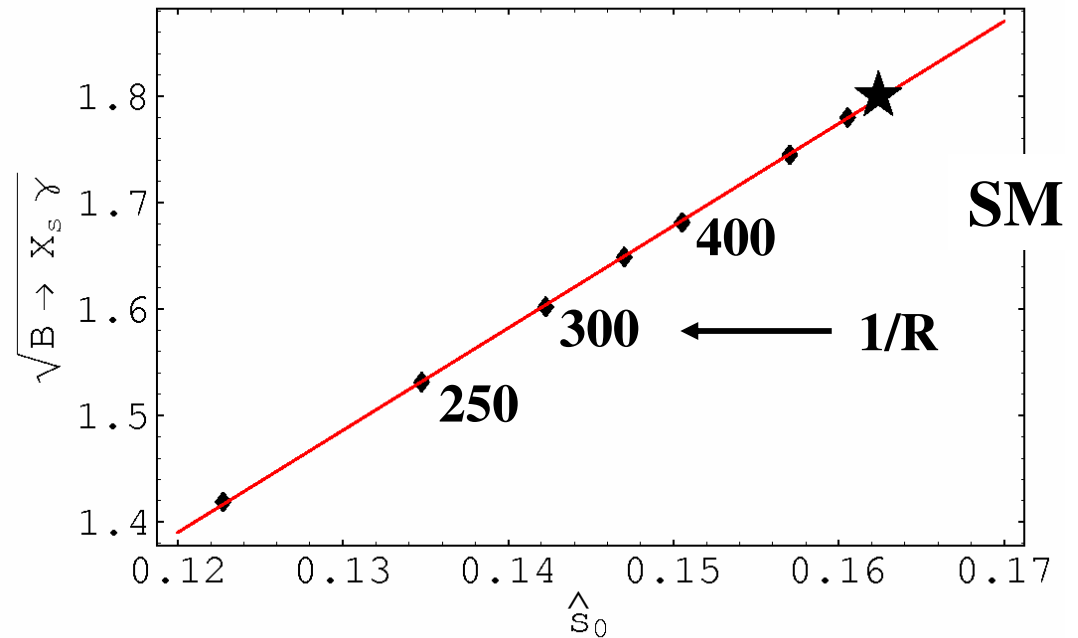
## MSSM (MFV)

(Bobeth, AJB, Ewerth)



## Universal Extra Dimensions

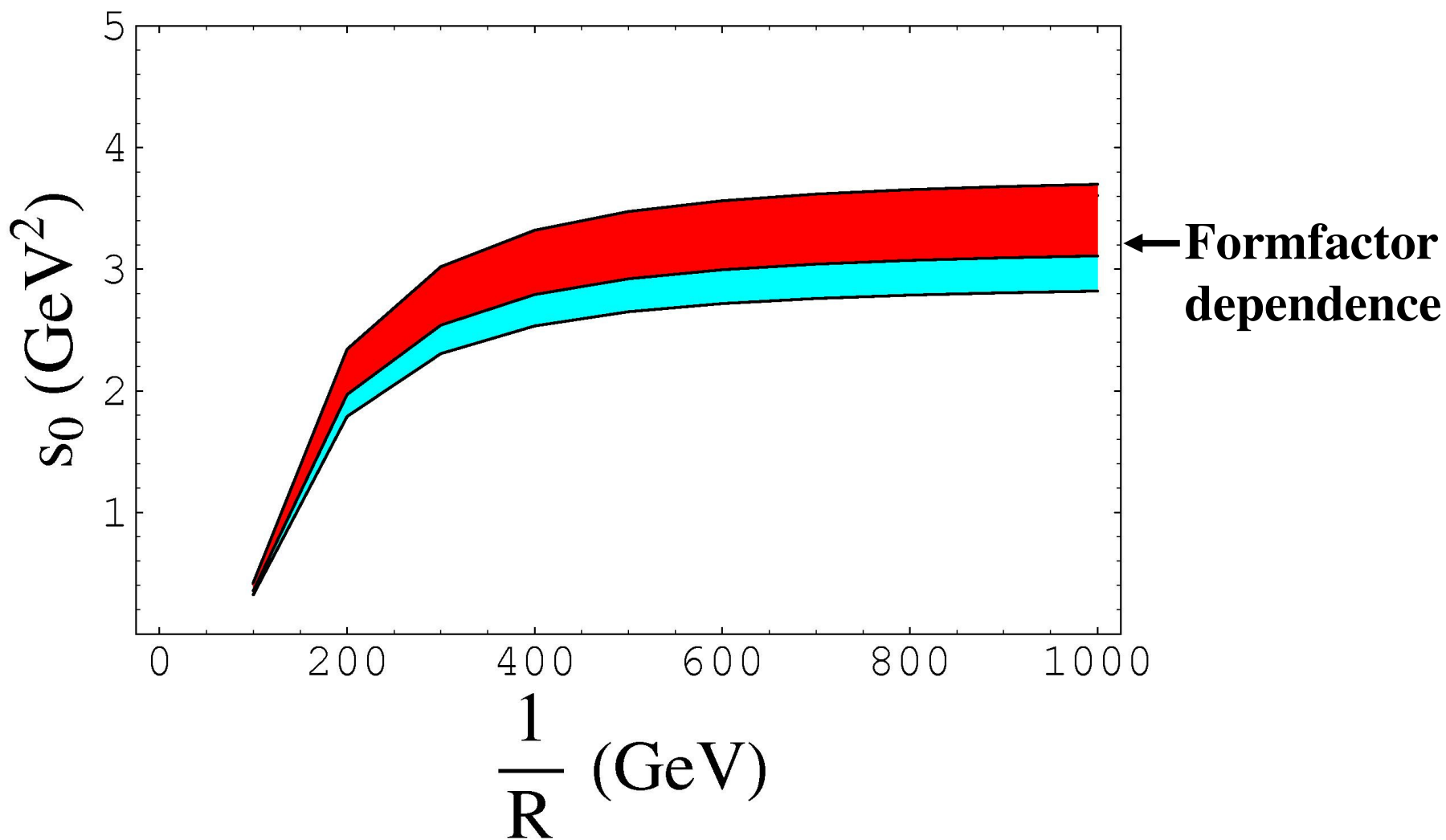
(AJB, Poschenrieder, Spranger, Weiler)





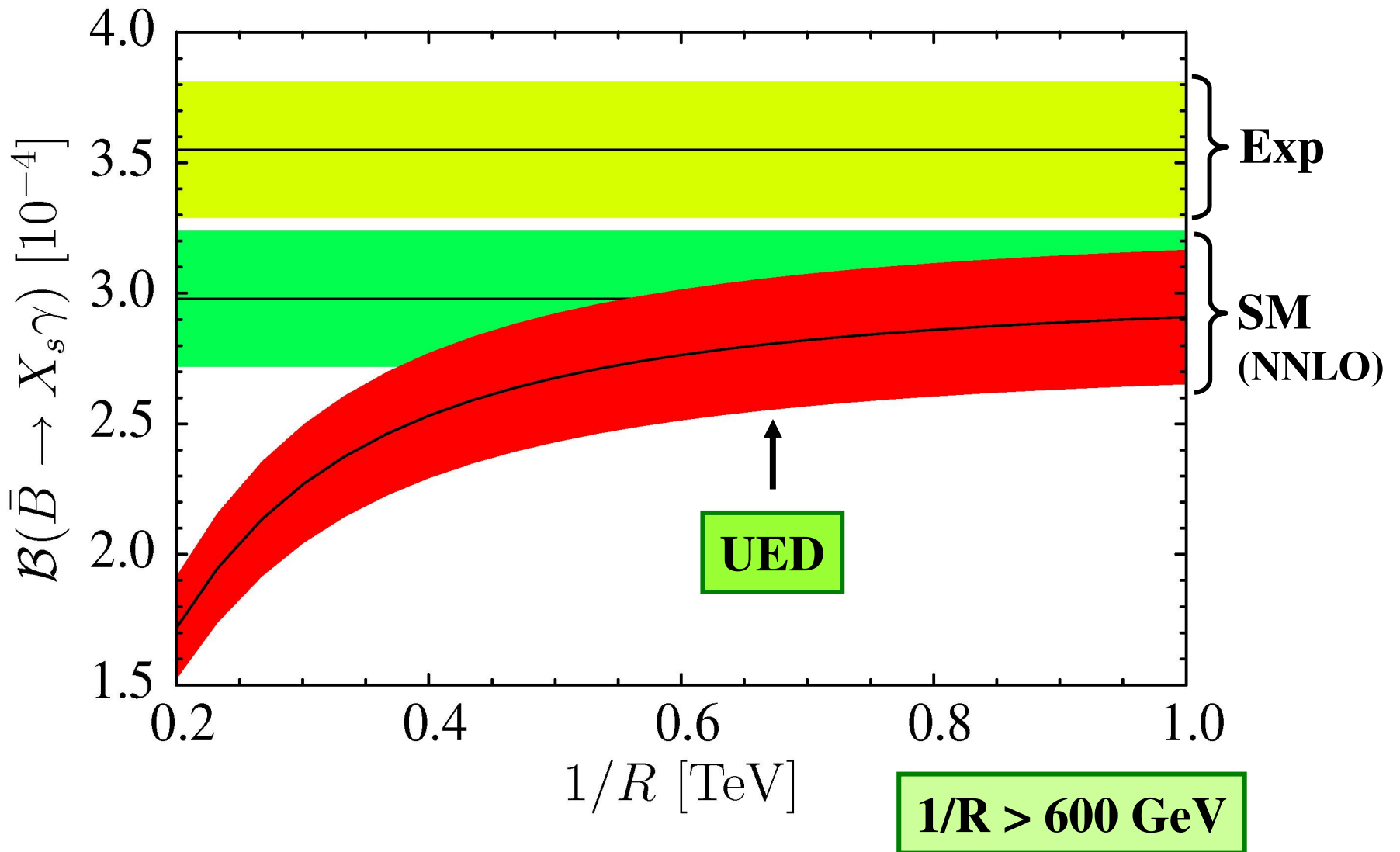
# UED and $B \rightarrow K^* l^+ l^-$

Colangelo  
De Fazio  
Ferrandes  
Pham



# $B \rightarrow X_s \gamma$ in Universal Extra Dimensions

Haisch, Weiler (2007)



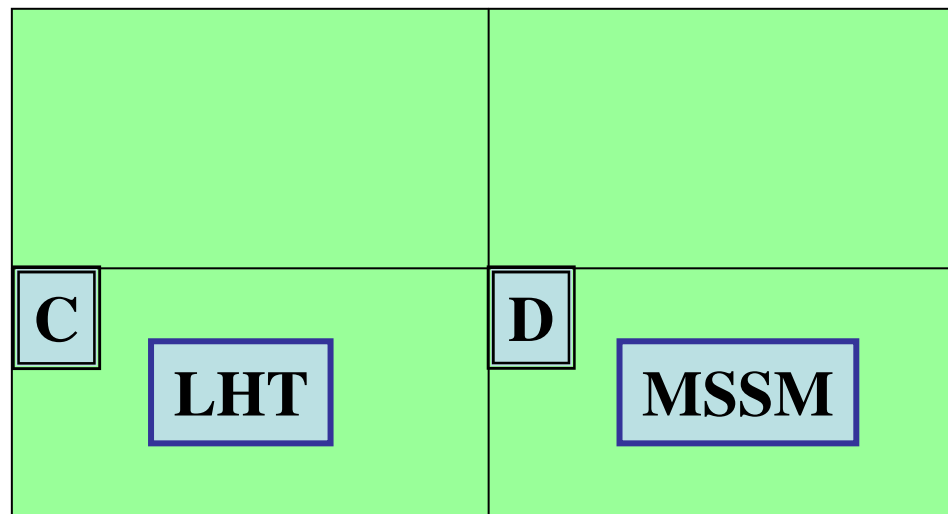
- 11.** Tests of CMFV bounds on rare decays and  $\Delta M_{d,s}$ . **In particular UED** ( $\hat{s}_0$ )
- 12.** Test of  **$\text{Br}(\text{B}_{s,d} \rightarrow \mu^+ \mu^-) \xleftrightarrow{\text{CMFV}} \Delta M_{d,s}$**
- 13.** Measurement of  $\beta$  through  $\text{K} \rightarrow \pi \nu \bar{\nu}$  system
- 14.** Test of MSSM correlation at large  $\tan\beta$
- $\text{Br}(\text{B}_{s,d} \rightarrow \mu^+ \mu^-) \xleftrightarrow{\text{MSSM MFV}} \Delta M_{d,s}$**
- 15.** **Exploration of the  $R_b \leftrightarrow \gamma$  Plot**

# 4.

## Beyond MFV

SM Operators

New Operators



New sources  
of Flavour (CP)  
Violation

# Next Hopes for new Phases : $B_s^0 - \bar{B}_s^0$ System

$$(S_{\psi\phi})_{SM} = \sin(2|\beta_s|) \approx 0.035$$

$$V_{ts} = -|V_{ts}|e^{-i\beta_s}$$

$$\beta_s = -1^\circ$$

But if there is a new phase  $\varphi_{B_s} \neq 0$

$$(S_{\psi\phi}) = \sin(2|\beta_s| - 2\varphi_{B_s}) \approx 0.30$$

$(\varphi_{B_s} \approx -8^\circ)$

One order  
of magnitude  
enhancement

Can be also tested in semi-leptonic CP-Asymmetry

$$A_{SL}^s = - \left| \operatorname{Re} \left( \frac{\Gamma_{12}}{M_{12}} \right)^{SM} \right| \frac{S_{\psi\phi}}{C_{B_s}}$$



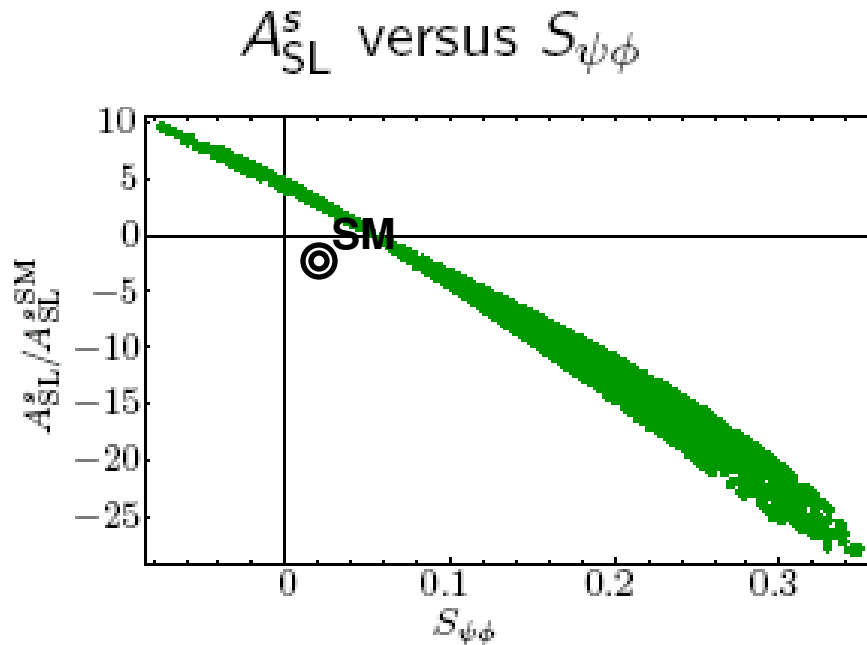
$$C_{B_s} = \frac{\Delta M_s}{(\Delta M_s)_{SM}}$$

could be measured  
this way (BBGT)

From Lattice (cleaner than  $\Delta M_s$ )

# Correlation $A_{SL}^s \leftrightarrow S_{\psi\phi}$

Ligeti  
Papucci  
Perez (06)



Example from LHT  
(Blanke et al)

- $A_{SL}^s$  enhanced by 10-20
- $S_{\psi\phi}$  can be as high as +0.3

# The Magnificent Six

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$



$$K_L \rightarrow \pi^0 \nu \bar{\nu}$$

$$K_L \rightarrow \pi^0 e^+ e^-$$

$$K_L \rightarrow \pi^0 \mu^+ \mu^-$$



$$B_s \rightarrow \mu^+ \mu^-$$

$$B_d \rightarrow \mu^+ \mu^-$$



sensitive to helicity suppressed operators (scalar operators)

## Golden Relations of CMFV and MFV:

AJB (03)

$$\frac{Br(B_s \rightarrow \mu^+ \mu^-)}{Br(B_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{B}_{B_d}}{\hat{B}_{B_s}} \frac{\tau(B_s)}{\tau(B_d)} \frac{\Delta M_s}{\Delta M_d} r$$

**(CMFV)**  
r = 1

Buchalla, AJB (94)  
AJB, Fleischer (01)

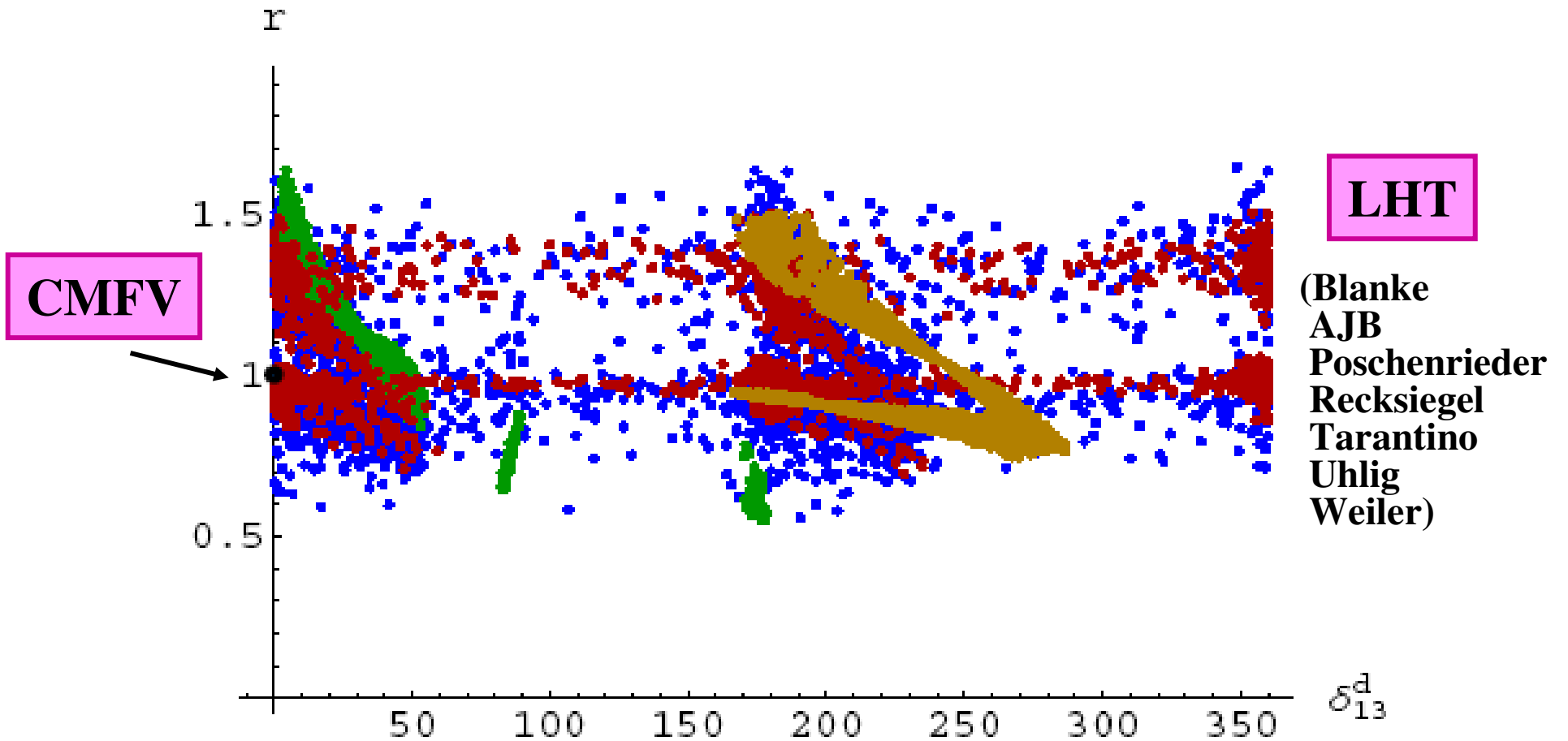
$$(\sin 2\beta)_{B \rightarrow \psi K_S} = (\sin 2\beta)_{K \rightarrow \pi \nu \bar{\nu}}$$

**(MFV)**

The **violation** of these model independent **MFV (CMFV)** relations would **signal new flavour and CP-violating interactions (and/or new operators)**



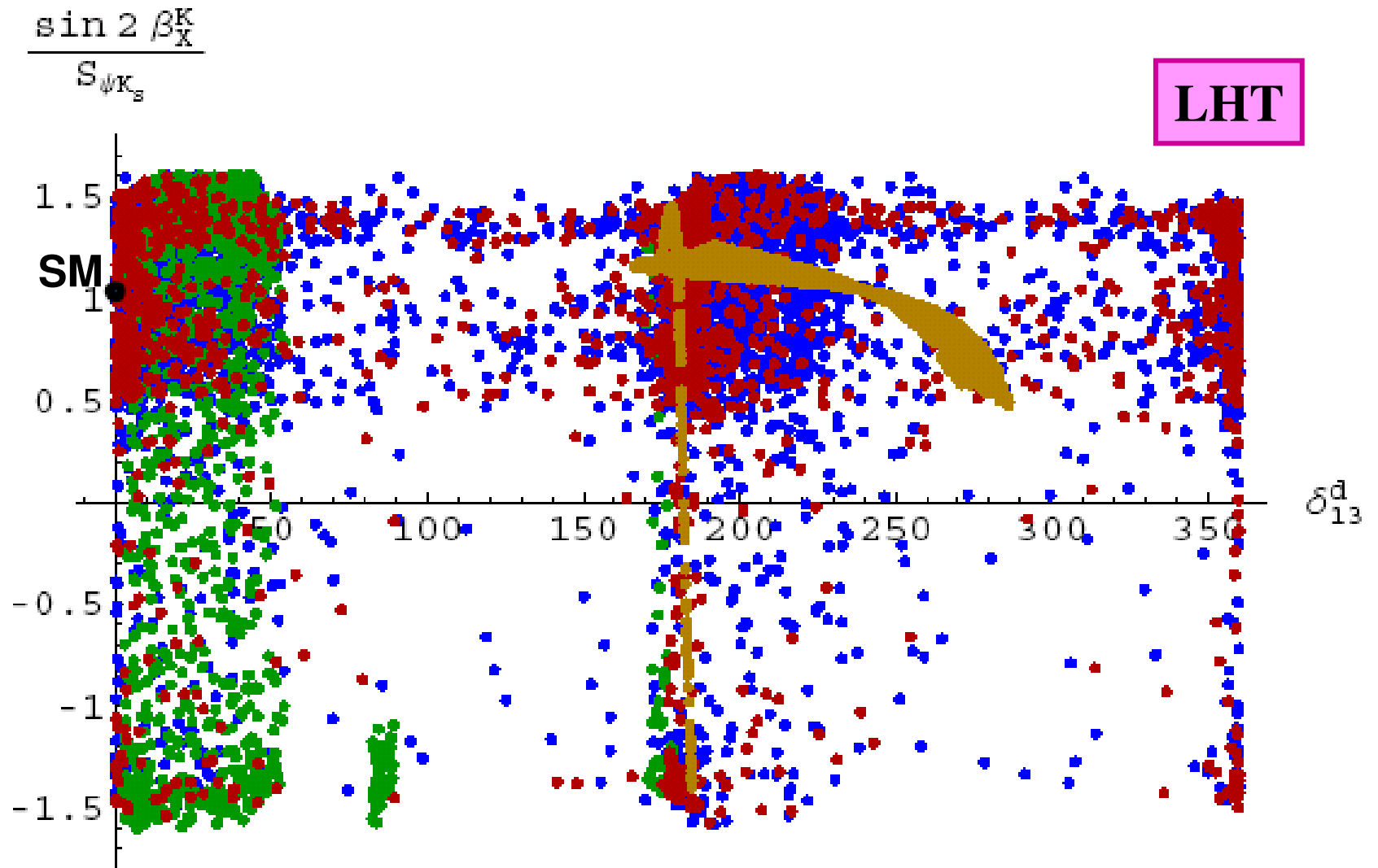
# Violation of the Golden Relation



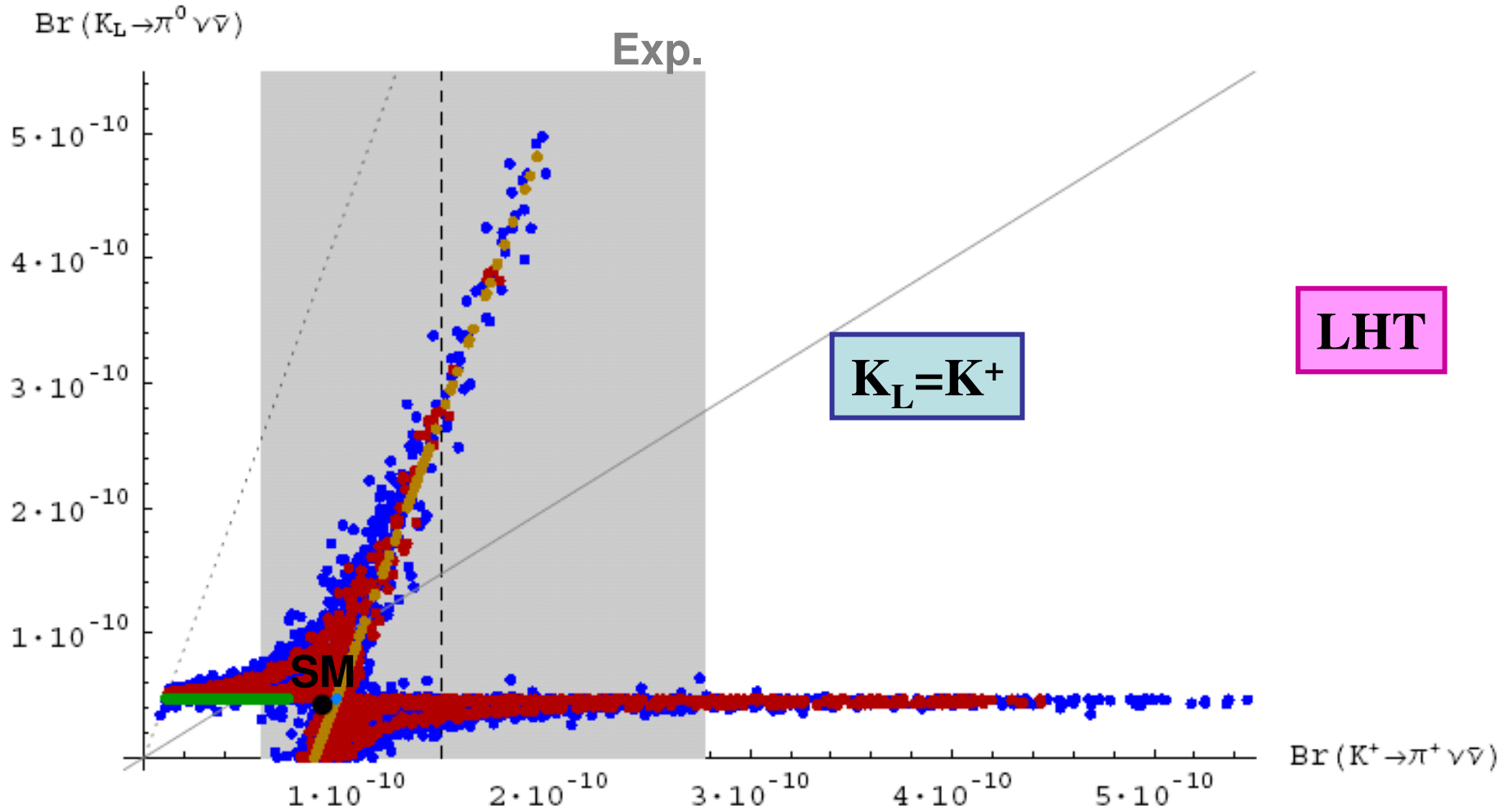
Similar in  $Z'$  models: Promberger, Schatt, Schwab (07)

An evident Consequence  
of Universality Breakdown

The MFV identity between  $\beta$   
from  $B \rightarrow \psi K_S$  and  $K_L \rightarrow \pi^0 \nu \bar{\nu}$   
can be strongly violated



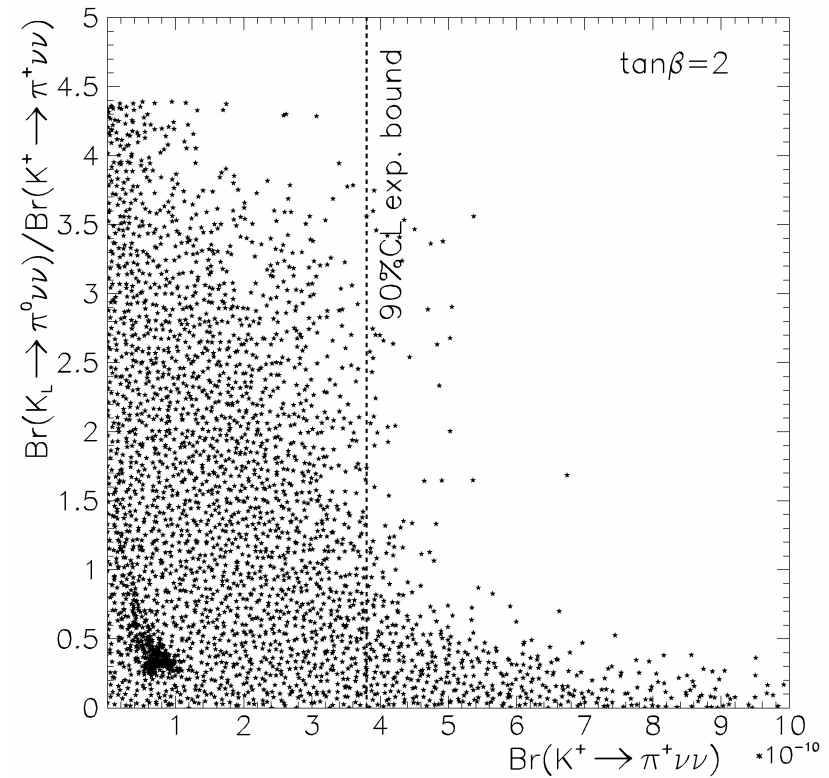
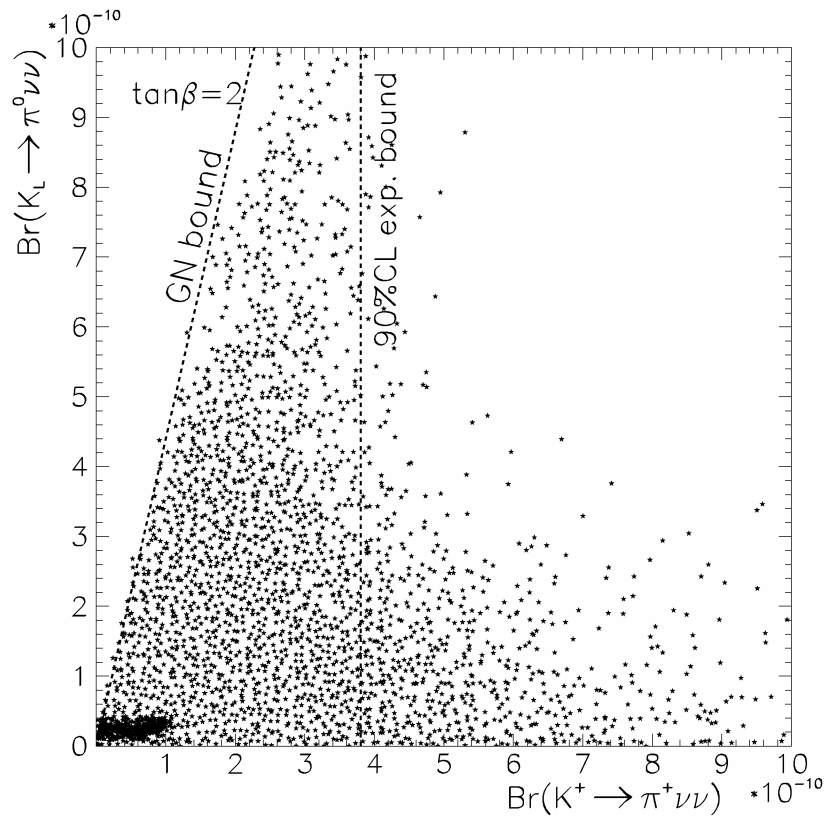
**K-system:  $K_L \rightarrow \pi^0 \nu \bar{\nu}$  vs  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$**



**Two distinguished branches appear!**  
 ~10 times enhancement in  $K_L \rightarrow \pi^0 \nu \bar{\nu}$   
 ~5 times enhancement in  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

# $K_L \rightarrow \pi^0 \nu \bar{\nu}$ and $K^+ \rightarrow \pi^0 \nu \bar{\nu}$ from a general MSSM

AJB, Ewerth, Jäger, Rosiek (04)

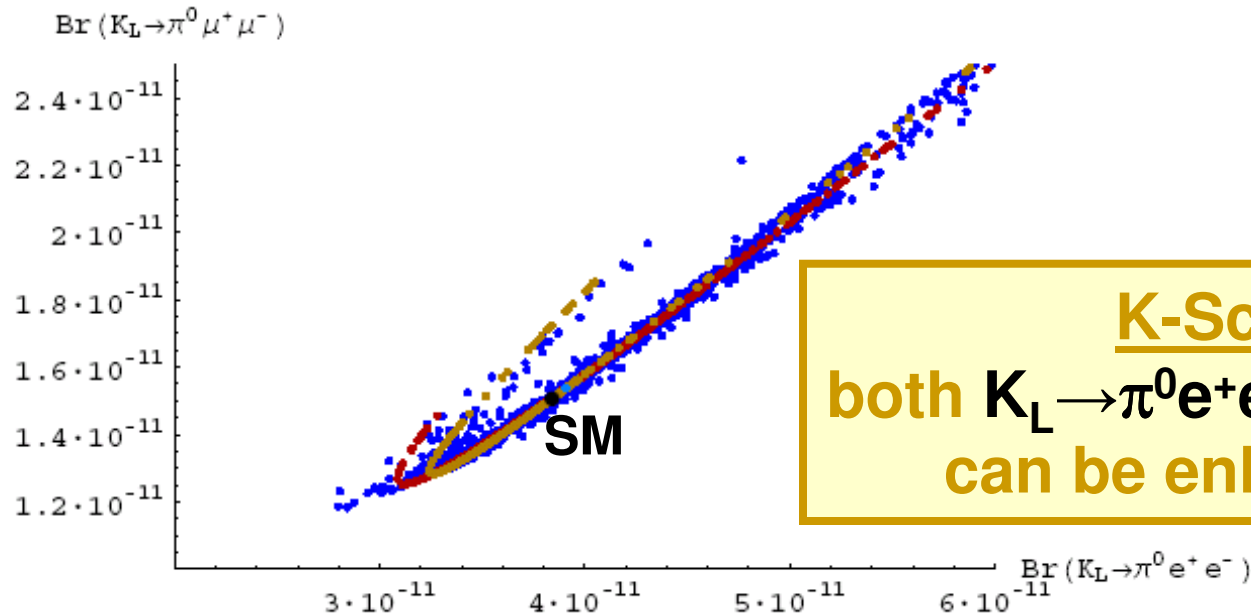


see also (Isidori, Mescia, Paradisi, Smith, Trine)

**K-system:  $K_L \rightarrow \pi^0 e^+ e^-$  and  $K_L \rightarrow \pi^0 \mu^+ \mu^-$**

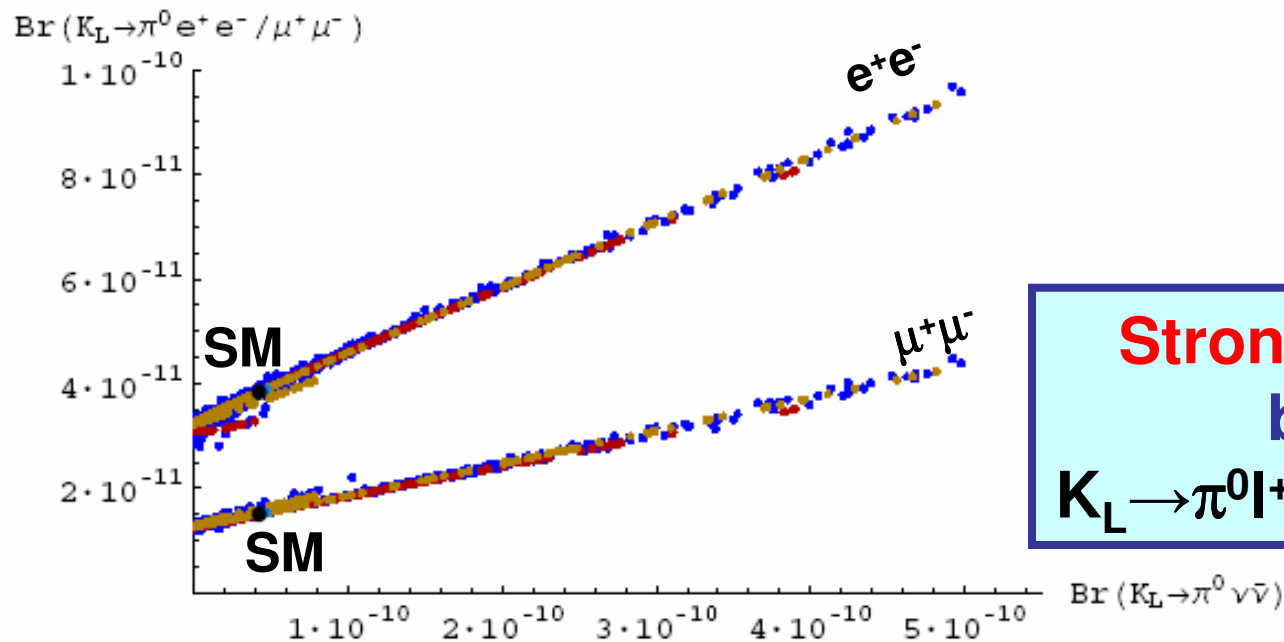
**(2,1)**

Friot, Greynat, de Rafael (04)  
 General correlation:  
 Isidori, Smith, Unterdorfer (04)  
 Mescia, Smith, Trine (06)



**K-Scenario:**  
 both  $K_L \rightarrow \pi^0 e^+ e^-$  and  $K_L \rightarrow \pi^0 \mu^+ \mu^-$   
 can be enhanced by  $\sim 2$

**LHT**

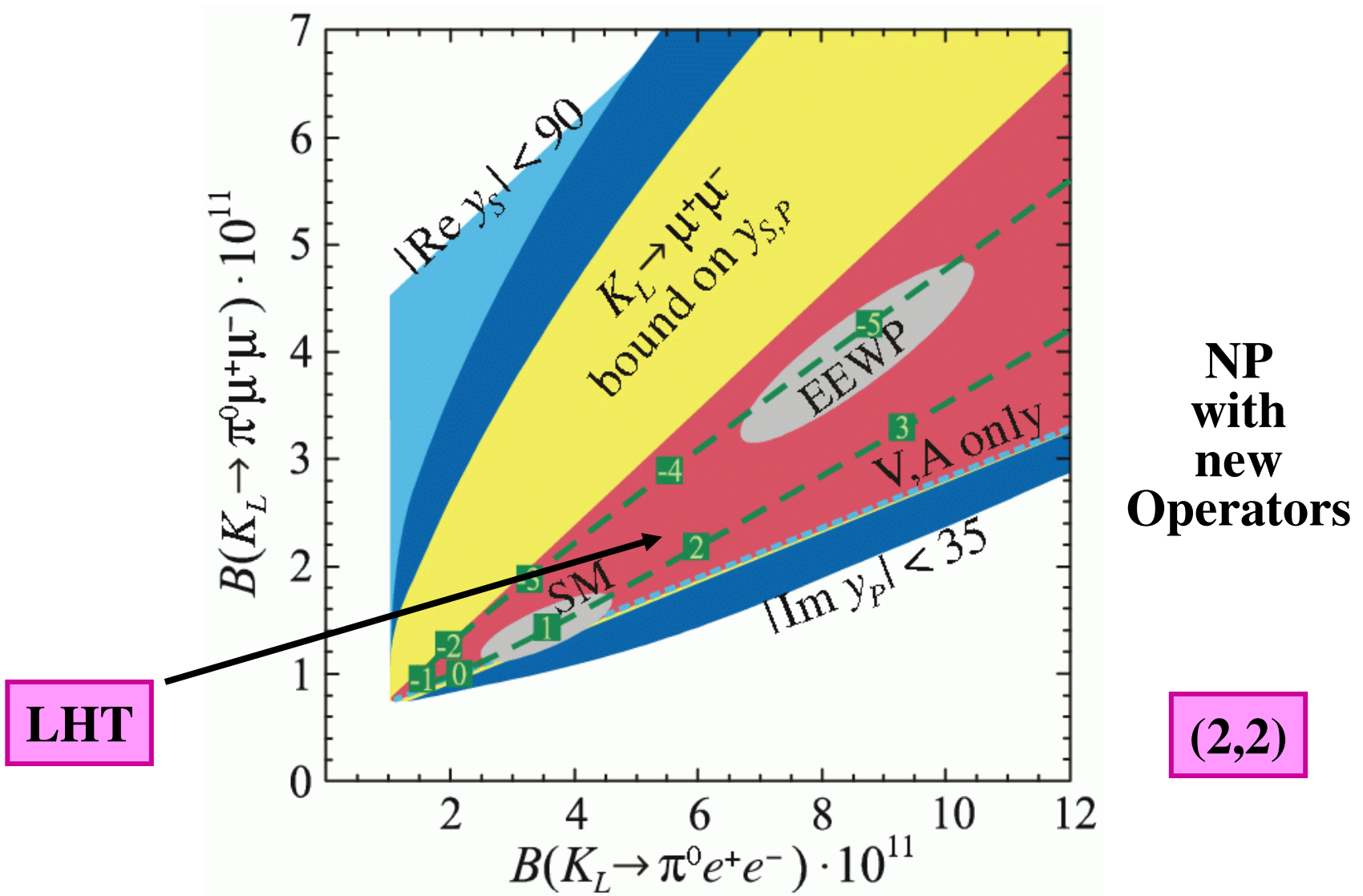


BBPRTUW (06)

**Strong correlation**  
 between  
 $K_L \rightarrow \pi^0 l^+ l^-$  and  $K_L \rightarrow \pi^0 \nu \bar{\nu}$

# Correlations in various NP Scenarios

Mescia, Smith, Trine (06)



## Important Constraint

$$\frac{\varepsilon'}{\varepsilon} = (16.7 \pm 1.6) \cdot 10^{-4} \quad \begin{array}{l} \text{(NA48)} \\ \text{(KTeV)} \end{array}$$

**AJB + Silvestrini (99)**

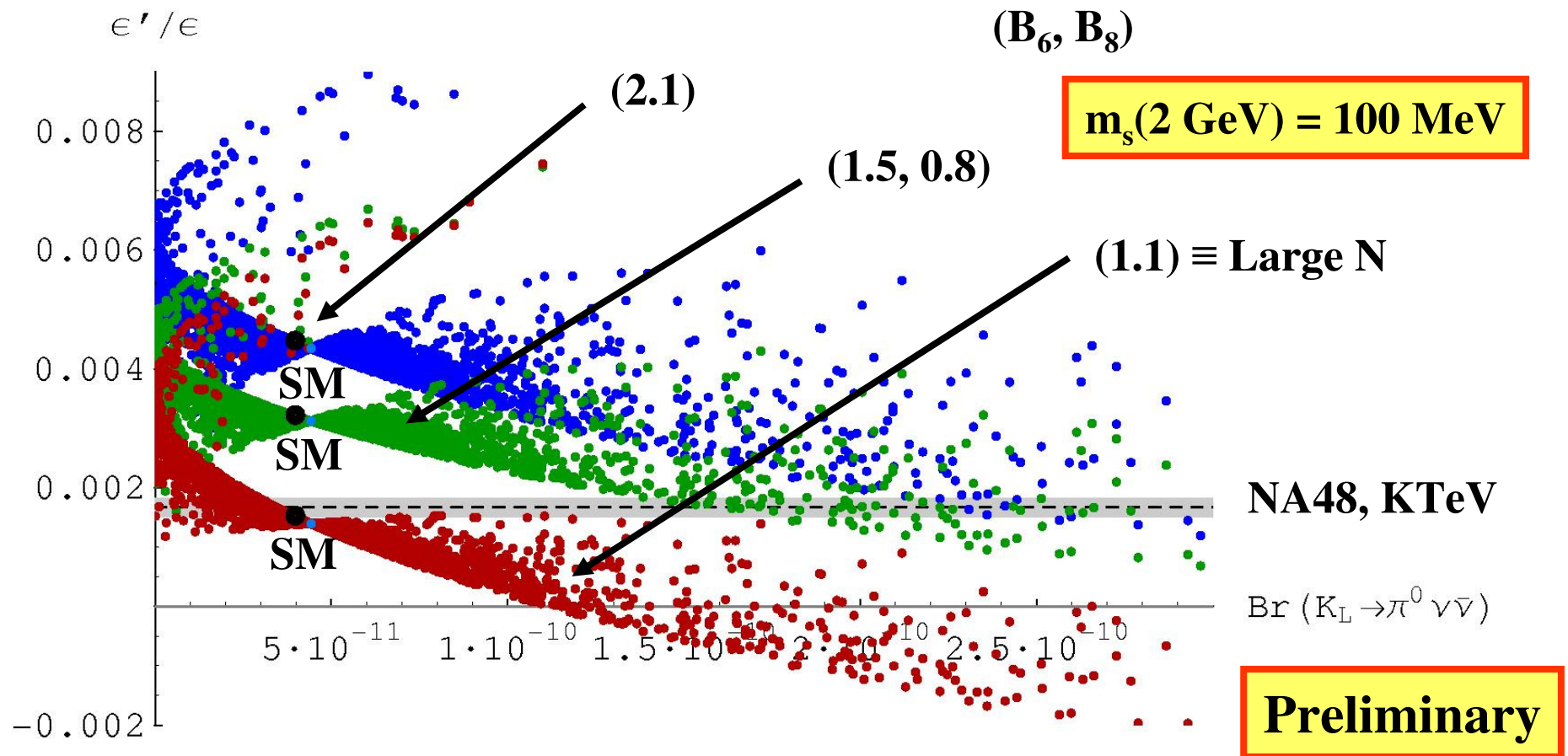
**AJB + Colangelo, Isidori, Romanino, Silvestrini (99)**

**Could have considerable impact on possible enhancements of rare K Decays provided hadronic matrix elements ( $B_6$ ,  $B_8$ ) under control.**

# Correlation between $\varepsilon'/\varepsilon$ and Rare K Decays

M. Blanke, AJB, S. Recksiegel, C. Tarantino, S. Uhlig (0704xxx)

LHT





## **D<sup>0</sup> – $\bar{D}^0$ Mixing (2007)**

$$\Delta M_D = (14.5 \pm 5.6) \cdot 10^{-3} / \text{ps}$$

**(BaBar)**  
**(Belle)**

**First implications:**

**Ciuchini, Franco, Guadagnoli, Lubicz  
Pierini, Porretti, Silvestrini**

**(Impact on MSSM)**

**(hep-ph/0703204)**

**see also Nir  
(0703235)**

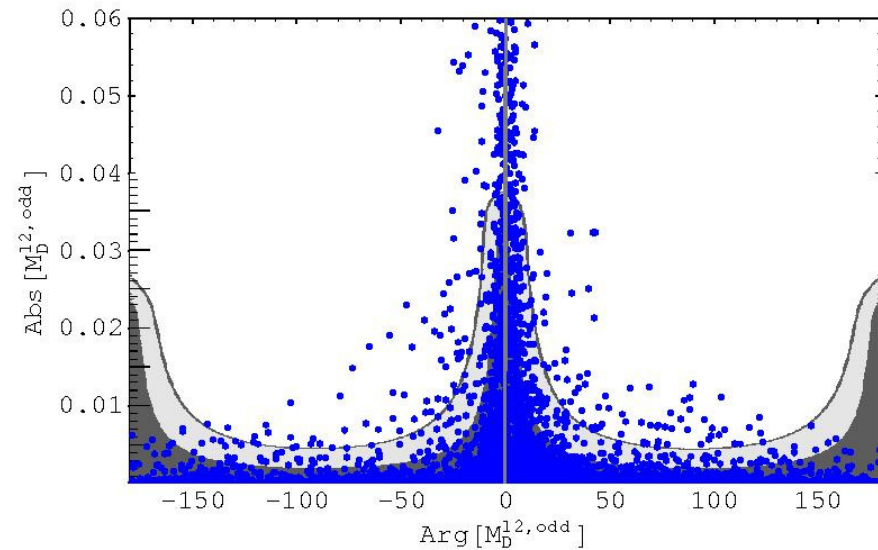
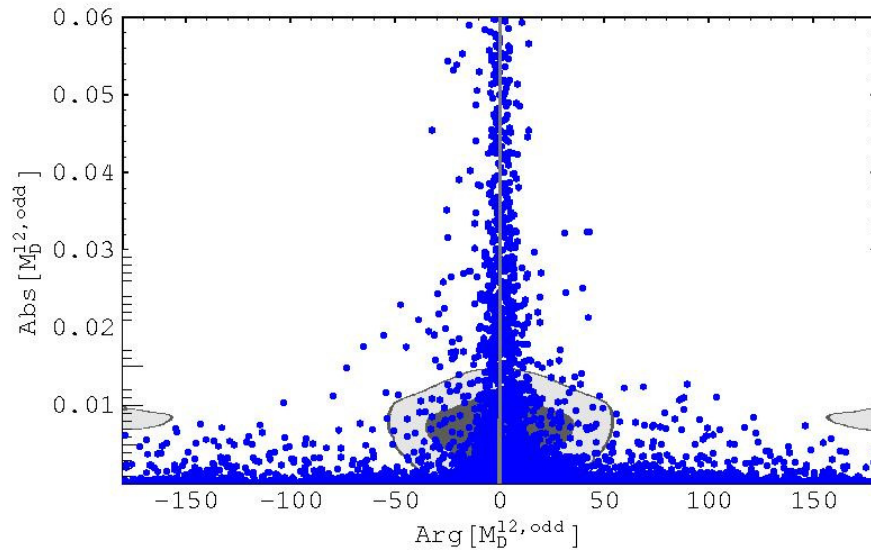
# LHT confronts new data on $D^0 - \bar{D}^0$ Mixing

M. Blanke, AJB, S. Recksiegel, C. Tarantino, S. Uhlig (0703254)

LHT

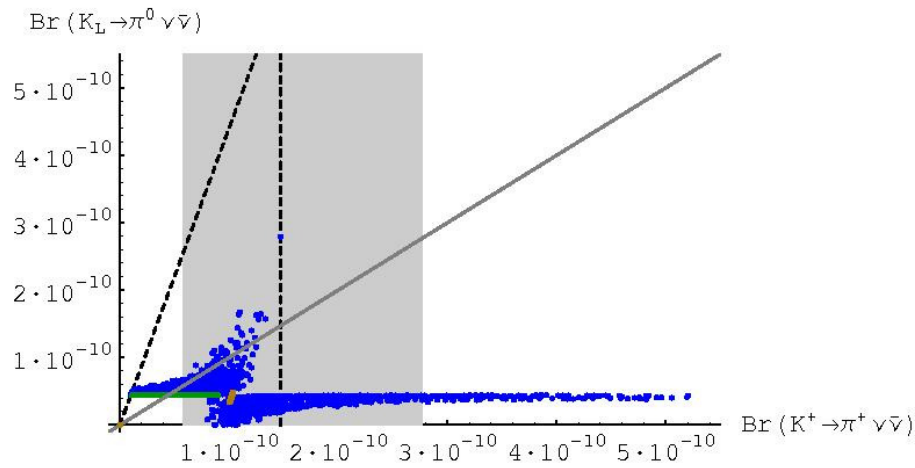
$$(\Delta M_D)^{\text{SM}} = 0$$

$$(\Delta M_D)^{\text{SM}} \neq 0$$

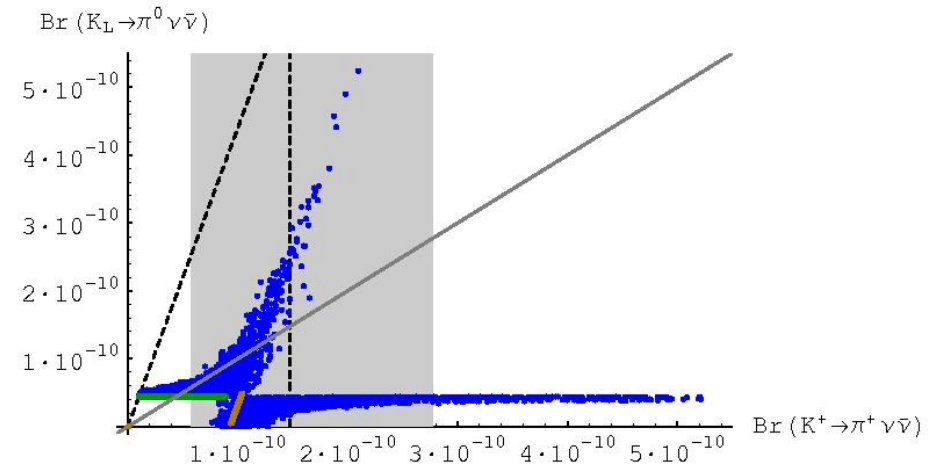


# Impact on $K \rightarrow \pi \nu \bar{\nu}$

$$(\Delta M_D)^{\text{SM}} = 0$$



$$(\Delta M_D)^{\text{SM}} \neq 0$$



- 16.** Measurements of  $S_{\psi\phi}$  and  $A_{SL}^{s,d}$
- 17.** Test of  $K_L \rightarrow \pi^0 \nu \bar{\nu} \leftrightarrow K^+ \rightarrow \pi^+ \nu \bar{\nu}$  correlation
- 18.** Test of  $K_L \rightarrow \pi^0 e^+ e^- \leftrightarrow K^+ \rightarrow \pi^0 \mu^+ \mu^-$  correlation
- 19.** Test of  $K_L \rightarrow \pi^0 \nu \bar{\nu} \leftrightarrow K_L \rightarrow \pi^0 l^+ l^-$  correlations
- 20.**  $D^0 - \bar{D}^0$  Mixing and  $\mathcal{CP}$
- 21.** Transverse muon polarisation in  $K^+ \rightarrow \pi^0 \mu^+ \nu$  (T)
- 22.**  $B \rightarrow X_{s,d} \nu \bar{\nu}$  and  $B \rightarrow K^*(\rho) \nu \bar{\nu}$

# What about Lepton Flavour Violation ?

## $\mu \rightarrow e\gamma$ : State of the Art

- ◆ **SM (+ Dirac  $\nu_R$ ):**

very much suppressed due to the smallness of  $m_\nu$

$$Br(\mu \rightarrow e\gamma)_{SM} \approx 10^{-54}$$

- ◆ **Experimental bound:**

[MEGA Collaboration]

$$Br(\mu \rightarrow e\gamma)_{\text{exp}} < 1.2 \cdot 10^{-11} \quad (90\% C.L.)$$

It will be improved to  $\sim 10^{-13}$  by MEG in 2007

- ◆ **MSSM and LHT could explain such high values.**

# Other interesting Processes

- ◆  $\mu^- \rightarrow e^- e^+ e^-$ : even more constrained than  $\mu \rightarrow e \gamma$

$$Br(\mu^- \rightarrow e^- e^+ e^-)_{\text{exp}} < 1.0 \cdot 10^{-12}$$

[SINDRUM Collaboration]

- ◆  $\tau \rightarrow \mu \gamma$  and  $\tau \rightarrow e \gamma$ : similar to  $\mu \rightarrow e \gamma$

$$Br(\tau \rightarrow \mu \gamma)_{\text{exp}} < 1.6 \cdot 10^{-8}$$

[Belle, BaBar]

$$Br(\tau \rightarrow e \gamma)_{\text{exp}} < 9.4 \cdot 10^{-8}$$

[BaBar, Belle]

- ◆  $\tau \rightarrow \mu \pi$ : semileptonic decay

$$Br(\tau \rightarrow \mu \pi)_{\text{exp}} < 5.8 \cdot 10^{-8}$$

[Belle, BaBar]

(Future:  
Super B)

- ◆  $\mu \rightarrow e$  conversion

$$R(\mu T_i \rightarrow e T_i) < 4.3 \cdot 10^{-12}$$

$10^{-18}$  (J-Parc)

- ◆  $K_L \rightarrow \mu e$ : flavour violating in both quark and lepton sectors

$$Br(K_L \rightarrow \mu e)_{\text{exp}} < 4.7 \cdot 10^{-12}$$

[BNL E871 Collaboration]

# Symphony of LFV Decays

$$\begin{aligned} \mu &\rightarrow e\gamma \\ \tau &\rightarrow \mu\gamma \\ \tau &\rightarrow e\gamma \end{aligned}$$

$$\begin{aligned} \mu^- &\rightarrow e^- e^+ e^- \\ \tau^- &\rightarrow \mu^- \mu^+ \mu^- \\ \tau^- &\rightarrow e^- e^+ e^- \end{aligned}$$

$$\begin{aligned} K_L &\rightarrow \mu e && \Delta L=1 \\ B_{d,s} &\rightarrow \mu e && \Delta S=1 \\ &&& (\Delta B=1) \\ B_{d,s} &\rightarrow \tau e \\ B_{d,s} &\rightarrow \tau \mu \end{aligned}$$

*$\mu - e$  Conversion  
in nuclei*

$$K_L \rightarrow \pi^0 \mu e$$

$$\begin{aligned} \tau^- &\rightarrow e^- \mu^+ e^- \\ \tau^- &\rightarrow \mu^- e^+ \mu^- \end{aligned}$$

$\Delta L=2$

$$\begin{aligned} \tau^- &\rightarrow \mu^- e^+ e^- \\ \tau^- &\rightarrow e^- \mu^+ \mu^- \end{aligned}$$

$(\Delta L=1, \Delta L=2)$

$$\tau^- \rightarrow \mu^- P$$

$$(g-2)_\mu$$

$$P = \pi, \eta, \eta'$$



# Correlations between LFV Processes

**MSSM**

: Dipole Operator Dominance  
(Ellis, Hisano, Raidal, Shimizu; Arganda, Herrero; Paradisi)  
(Brignole, Rossi)

$$\frac{\text{Br}(l_i^- \rightarrow l_j^- l_j^+ l_j^-)}{\text{Br}(l_i^- \rightarrow l_j^- \gamma)} \cong \frac{\alpha}{3\pi} \left( \log \frac{m_{l_i}^2}{m_{l_j}^2} - 2.7 \right)$$
$$\frac{\text{Br}(l_i^- \rightarrow l_j^- l_k^+ l_k^-)}{\text{Br}(l_i^- \rightarrow l_j^- \gamma)} \cong \frac{\alpha}{3\pi} \left( \log \frac{m_{l_i}^2}{m_{l_k}^2} - 2.7 \right)$$

**LHT**

: Dipole Operator Irrelevance (Z-penguins, Boxes dominate)  
(Blanke, AJB, Duling, Poschenrieder, Tarantino)

# Symphony of Correlations

MSSM

$$\frac{\text{Br}(\mu^- \rightarrow e^- e^+ e^-)}{\text{Br}(\mu^- \rightarrow e^- \gamma)} \approx \frac{1}{161}$$

LHT

0.4 – 2.5

$$\frac{\text{Br}(\tau^- \rightarrow e^- e^+ e^-)}{\text{Br}(\tau^- \rightarrow e^- \gamma)} \cong \frac{\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-)}{\text{Br}(\tau^- \rightarrow \mu^- \gamma)} \approx \frac{1}{95}$$

0.4 – 2.3

0.3 – 1.6

$$\frac{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{\text{Br}(\tau^- \rightarrow \mu^- \gamma)} \cong \frac{\text{Br}(\tau^- \rightarrow e^- \mu^+ \mu^-)}{\text{Br}(\tau^- \rightarrow e^- \gamma)} \approx \frac{1}{435}$$

0.4 – 2.3

0.3 – 1.6

$$\frac{\text{R}(\mu T_i \rightarrow e T_i)}{\text{Br}(\mu \rightarrow e \gamma)} \approx 5 \cdot 10^{-3}$$

$10^{-2} - 10^2$

# " $\mu \leftrightarrow e$ Symmetry" and its Violation

(BBDPT)

		$\mu \leftrightarrow e$ Symmetry	MSSM	LHT
$\frac{\text{Br}(\tau^- \rightarrow e^- e^+ e^-)}{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}$	$\frac{\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-)}{\text{Br}(\tau^- \rightarrow e^- \mu^+ \mu^-)}$	1	21	$1.0 \pm 0.2$
$\frac{\text{Br}(\tau^- \rightarrow e^- e^+ e^-)}{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}$	$\frac{\text{Br}(\tau^- \rightarrow \mu^- \gamma)}{\text{Br}(\tau^- \rightarrow e^- \gamma)}$	1	4.6	$1.0 \pm 0.2$
$\frac{\text{Br}(\tau^- \rightarrow e^- \mu^+ \mu^-)}{\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-)}$	$\frac{\text{Br}(\tau^- \rightarrow \mu^- \gamma)}{\text{Br}(\tau^- \rightarrow e^- \gamma)}$	1	0.2	$1.0 \pm 0.2$

**23.**  $\mathcal{CP}$  in neutrino oscillations

**24.**  $\theta_{13}$

**25.**  $\mu \rightarrow e\gamma, \tau \rightarrow e\gamma, \tau \rightarrow \mu\gamma$

**26.**  $\mu \rightarrow 3e, \tau \rightarrow 3e, \tau \rightarrow 3\mu, \mu \rightarrow e$  **Conversion**

**27.**  $\tau^- \rightarrow \mu^- e^+ e^-, \tau^- \rightarrow e^- \mu^+ \mu^-, \tau \rightarrow \mu(e)P$

**28.**  $K_L \rightarrow \mu e, K_L \rightarrow \pi^0 \mu e$

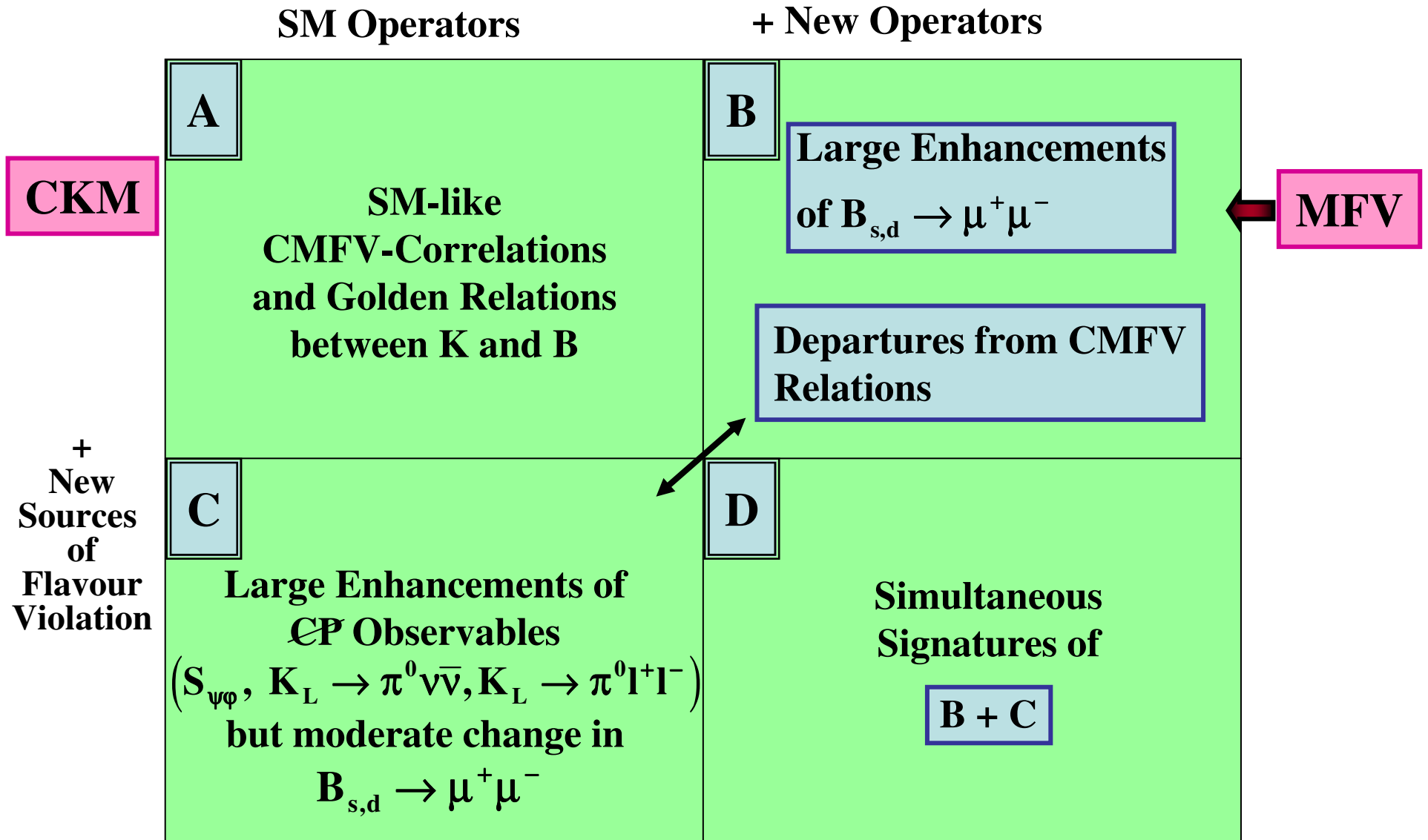
**29.**  $d_n, d_e, d_\mu$

**30.** **Leptogenesis**  $\Leftrightarrow$  **LFV**

**5.**

**Finals**  
**(Allegro Vivace)**

# 2 x 2 Flavour Matrix



# Comparison of MSSM with LHT

**Very large departures from SM in both models**

$S_{\psi\phi}, K_L \rightarrow \pi^0 \nu\bar{\nu}, K^+ \rightarrow \pi^+ \nu\bar{\nu}$   
 $K_L \rightarrow \pi^0 e^+ e^-, K_L \rightarrow \pi^0 \mu^+ \mu^-$   
**All LFV decays**

Pattern could distinguish MSSM from LHT

**Very large or significant departures only in MSSM**

$B_{s,d} \rightarrow \mu^+ \mu^-, (g-2)_\mu$   
 $d_n, d_e$

**Correlations in LFV very different in both models**

$\frac{\text{Br}(\mu^- \rightarrow e^- e^+ e^-)}{\text{Br}(\mu \rightarrow e \gamma)} \approx \begin{cases} 0(10^{-2}) & \text{MSSM} \\ 0(1) & \text{LHT} \end{cases}$   
**Approximate ~~MSSM~~**  
**" $\mu \leftrightarrow e$ " Symmetry **LHT****

# FCNC Goals for the LHC Era

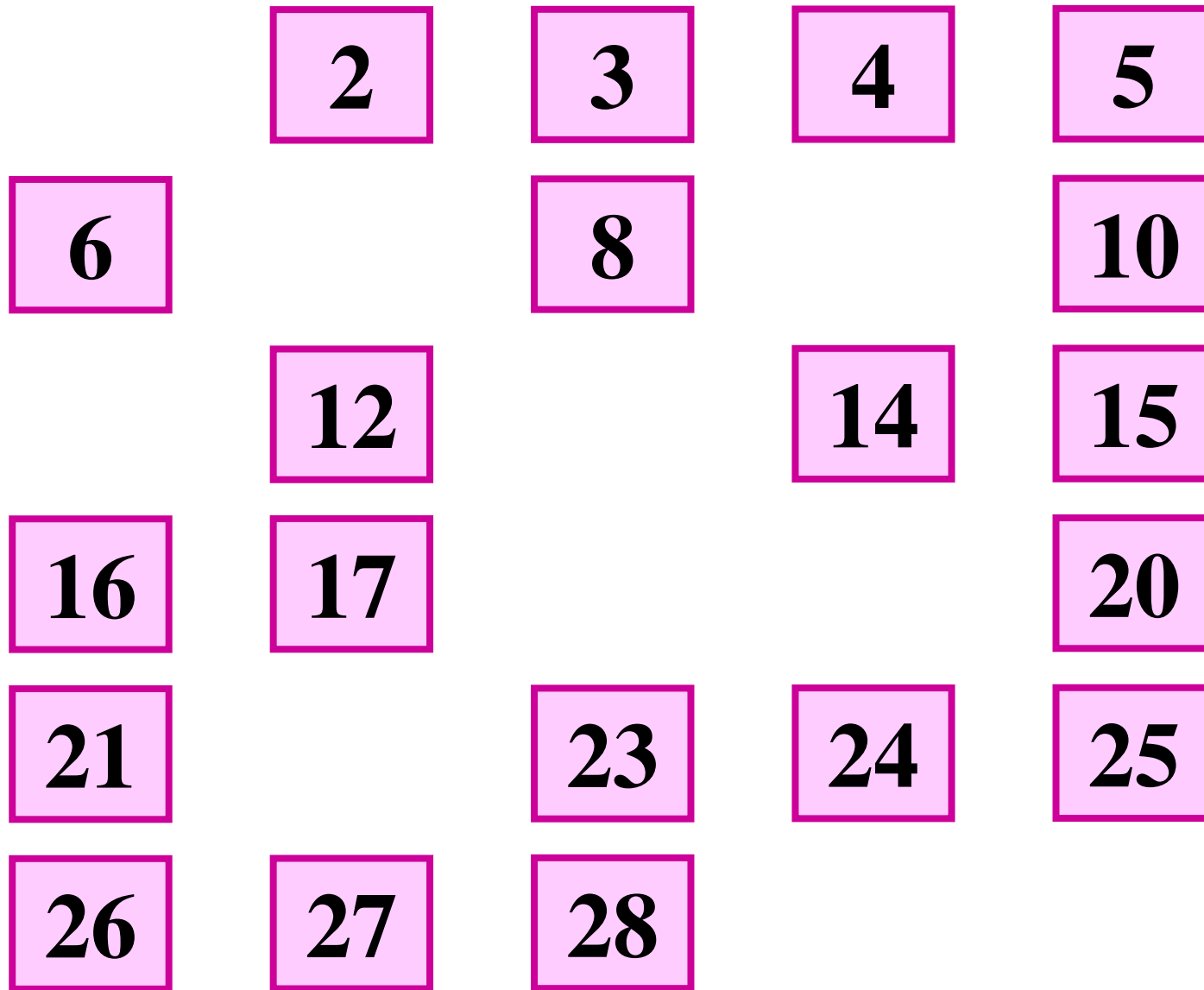
(2007)

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25
26	27	28	29	30



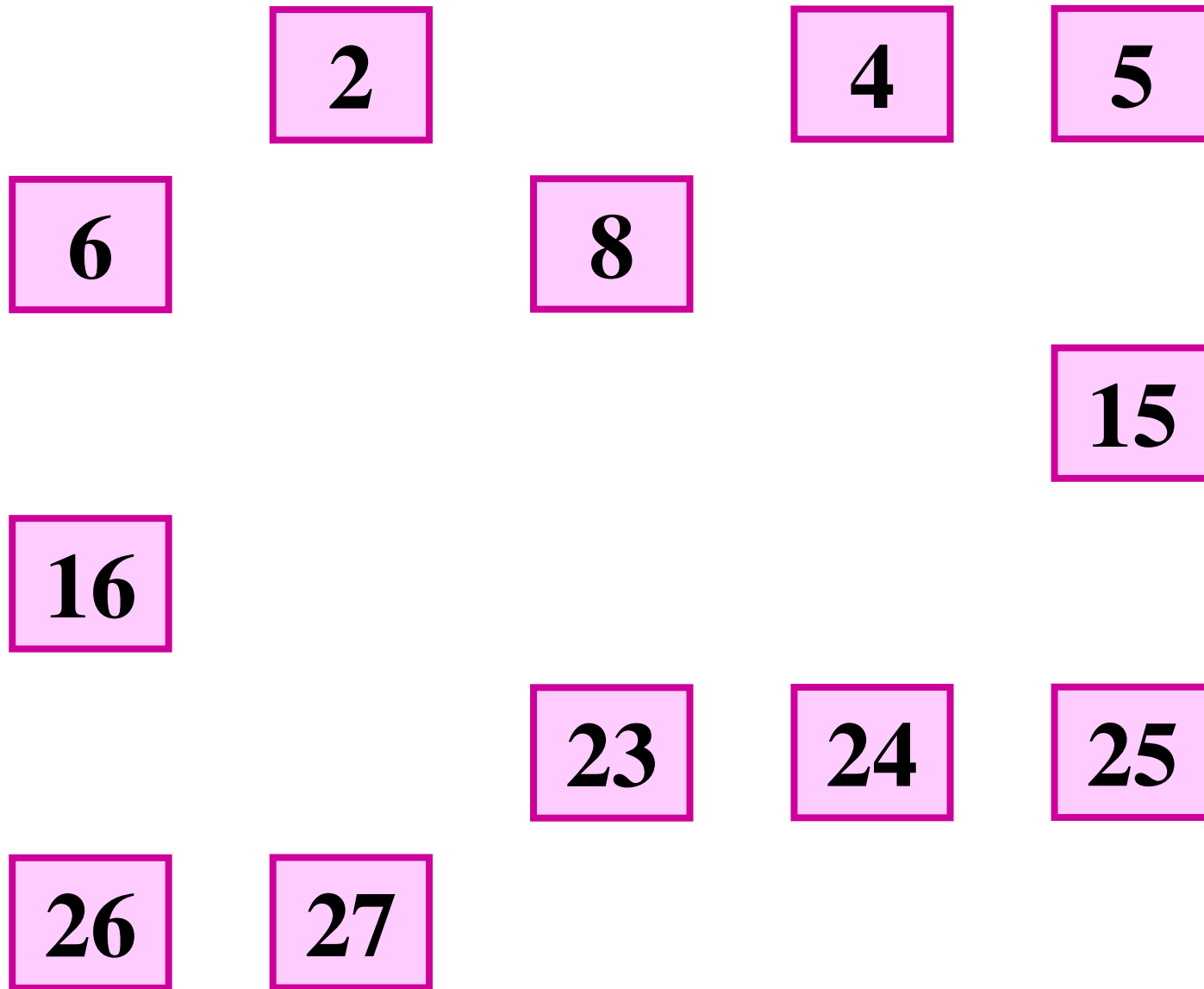
# FCNC Goals for the LHC Era

(2009)



# FCNC Goals for the LHC Era

(2011)



# FCNC Goals for the LHC Era

(2013)

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25
26	27	28	29	30

**31**

**A new very high energy  
collider (100 TeV)  
before**

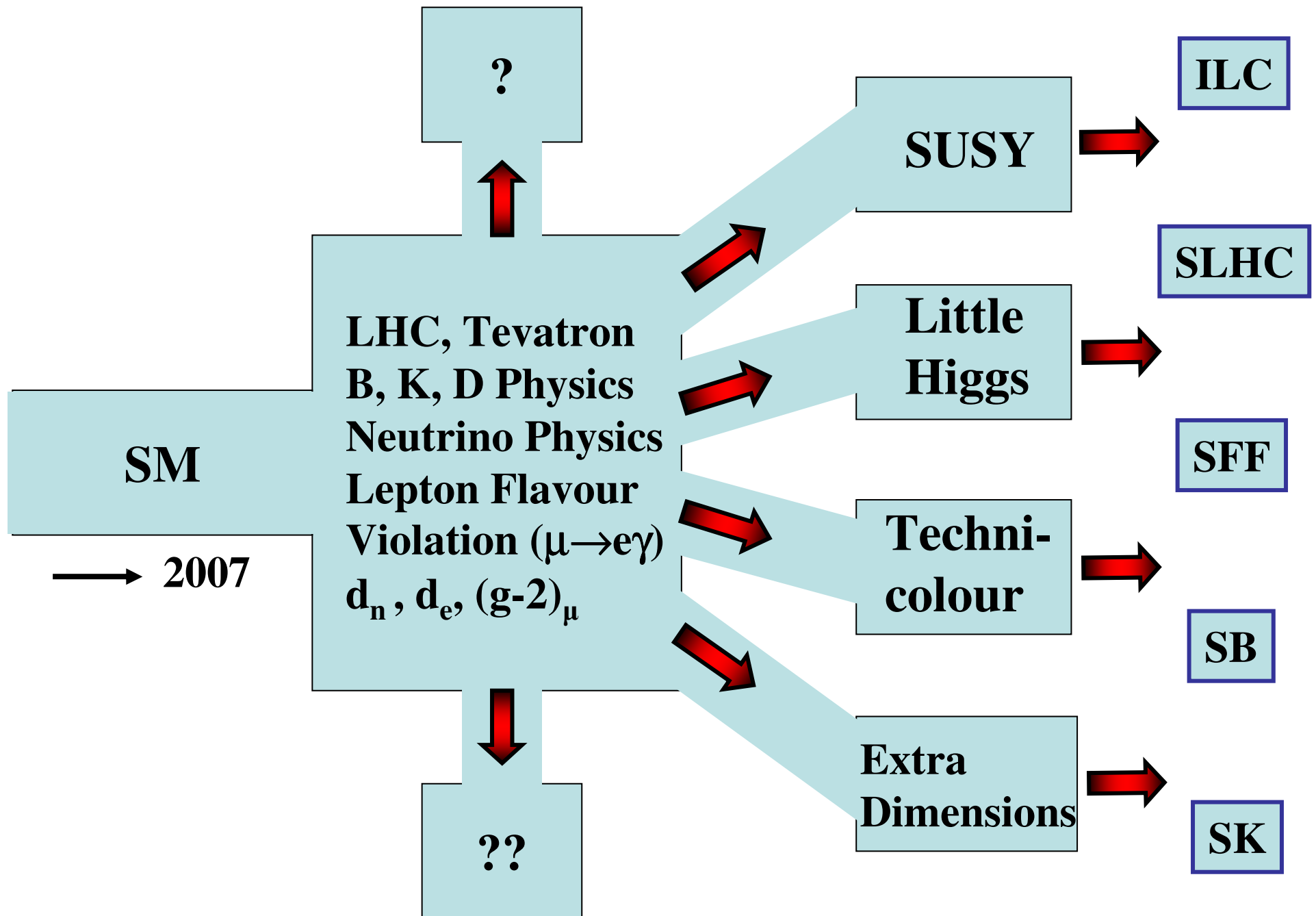
**2046**

**31**

**A new very high energy  
collider (100 TeV)  
before**

**2046**

**Very important for John Ellis and me !**

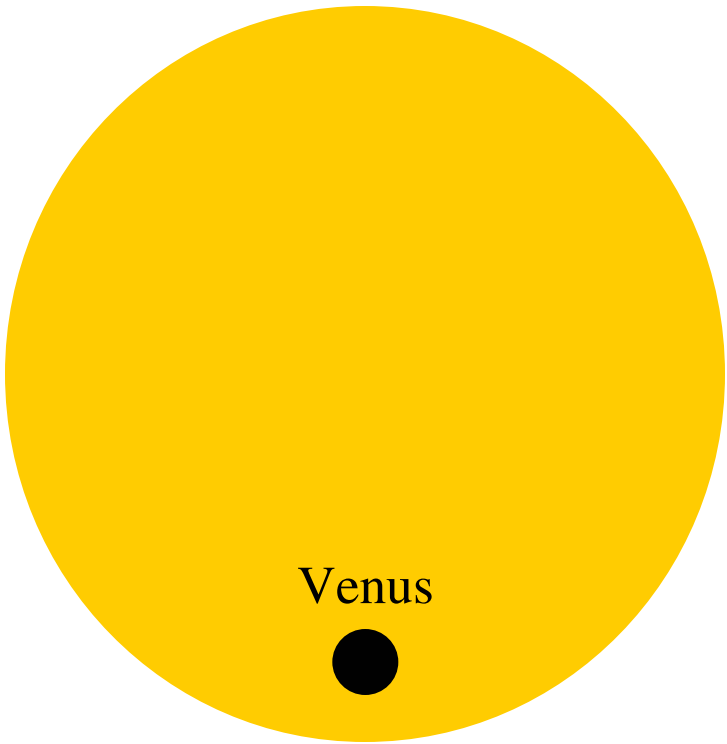


from

## **The European Strategy for Particle Physics**

CERN Courier, Sept. 2006

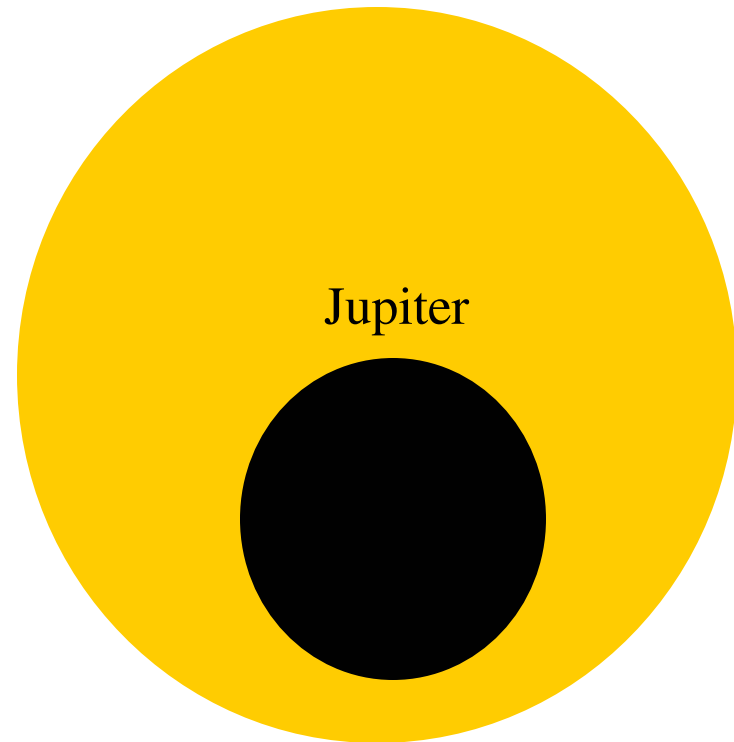
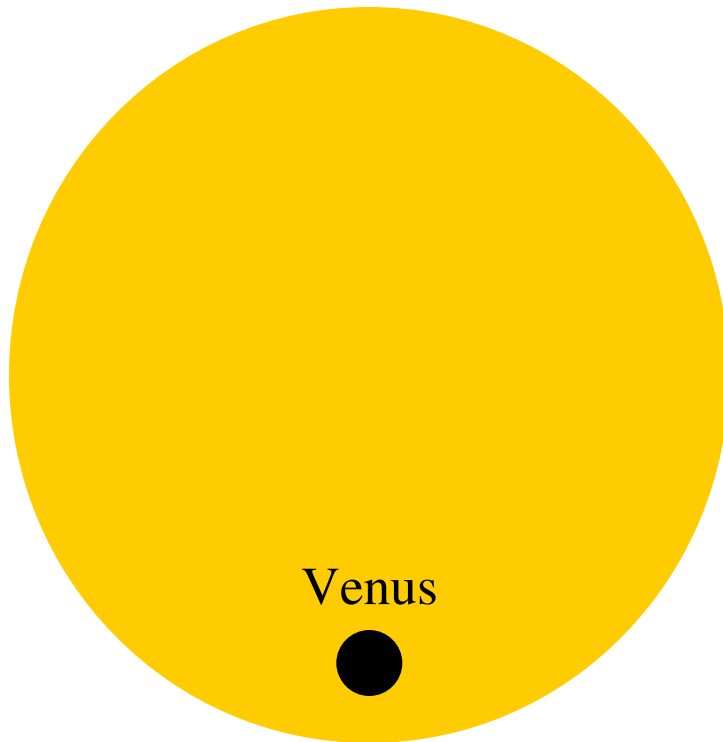
**"Particle Physics stands on the threshold of a new and exciting era of discovery. The next generation of experiments will explore new domains and probe the deep structure of space-time. They will measure the properties of the elementary constituents of matter and their interactions with unprecedented accuracy, and they will uncover new phenomena such as the Higgs boson or new forms of matter. Long-standing puzzles such as the origin of mass, the matter-antimatter asymmetry of the universe and the mysterious dark matter and energy that permeate the cosmos will soon benefit from the insights that new measurements will bring. Together, the results will have a profound impact on the way we see our universe."**



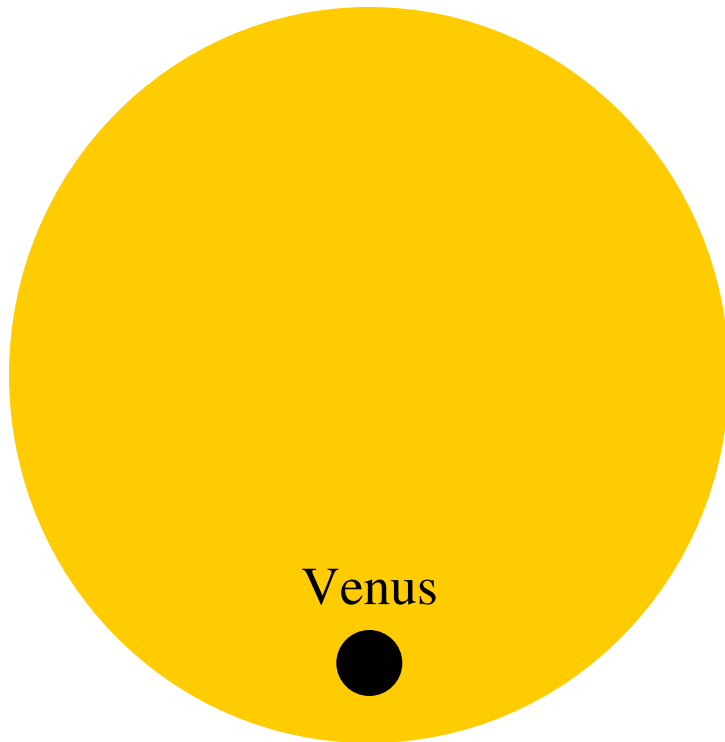
Venus



# Profound Impact on the Way we see our Universe



## Standard Model



## A clear Signal of New Physics

