



EDIT 2011

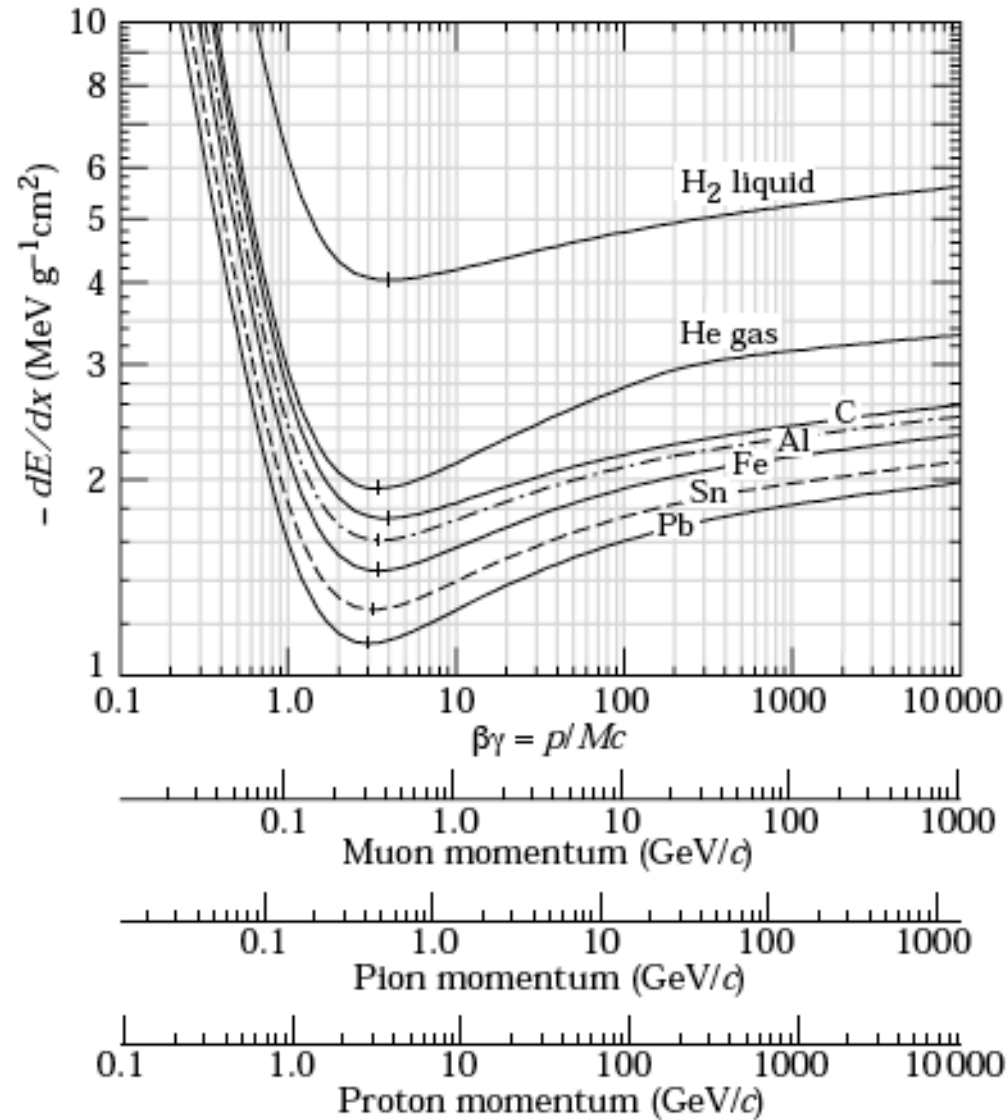
**Excellence in Detectors and Instrumentation Technologies
CERN, Geneva, Switzerland - 31 January - 10 February 2011**

GASEOUS DETECTORS FUNDAMENTS

Fabio Sauli
TERA Foundation and CERN

ENERGY LOSS OF CHARGED PARTICLES

DIFFERENTIAL ENERGY LOSS AS A FUNCTION OF VELOCITY



Reduced units:

$$\chi(\text{g cm}^{-2}) = \rho(\text{g cm}^{-3}) l(\text{cm})$$

$$\frac{dE}{d\chi} = \frac{1}{\rho} \frac{dE}{dx} \quad \rho : \text{density}$$

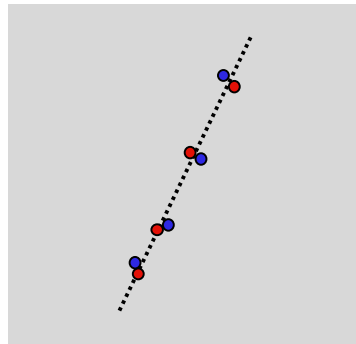
Expressed in $\text{MeV g}^{-1} \text{cm}^2$, the differential energy loss is equal within a factor of two for all materials (except H_2)

IONIZATION ENERGY LOSS OF CHARGED PARTICLES IN GASES

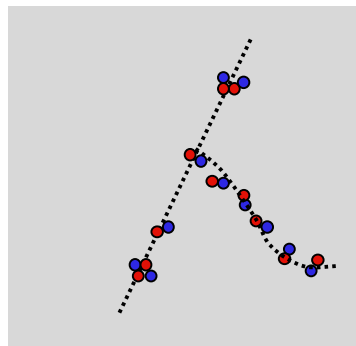
MAIN PARAMETERS:

Gas	Density, mg cm ⁻³	E_x eV	E_I eV	W_I eV	$dE/dx _{\min}$ keV cm ⁻¹	N_P cm ⁻¹	N_T cm ⁻¹
Ne	0.839	16.7	21.6	30	1.45	13	50
Ar	1.66	11.6	15.7	25	2.53	25	106
Xe	5.495	8.4	12.1	22	6.87	41	312
CH ₄	0.667	8.8	12.6	30	1.61	37	54
C ₂ H ₆	1.26	8.2	11.5	26	2.91	48	112
iC ₄ H ₁₀	2.49	6.5	10.6	26	5.67	90	220
CO ₂	1.84	7.0	13.8	34	3.35	35	100
CF ₄	3.78	10.0	16.0	54	6.38	63	120

PRIMARY IONIZATION:



TOTAL IONIZATION:



REVIEW OF PARTICLE PROPERTIES

<http://pdg.lbl.gov/>

Minimum ionizing particles in Argon NTP:

$$dE/dx: 2.5 \text{ keV/cm} \quad n_p: 25 \text{ ion pairs/cm}$$

Detection efficiency: $\varepsilon = 1 - P_0^n = 1 - e^{-n}$

Thickness: s (mm)	ε (%)
1	91.8
2	99.3

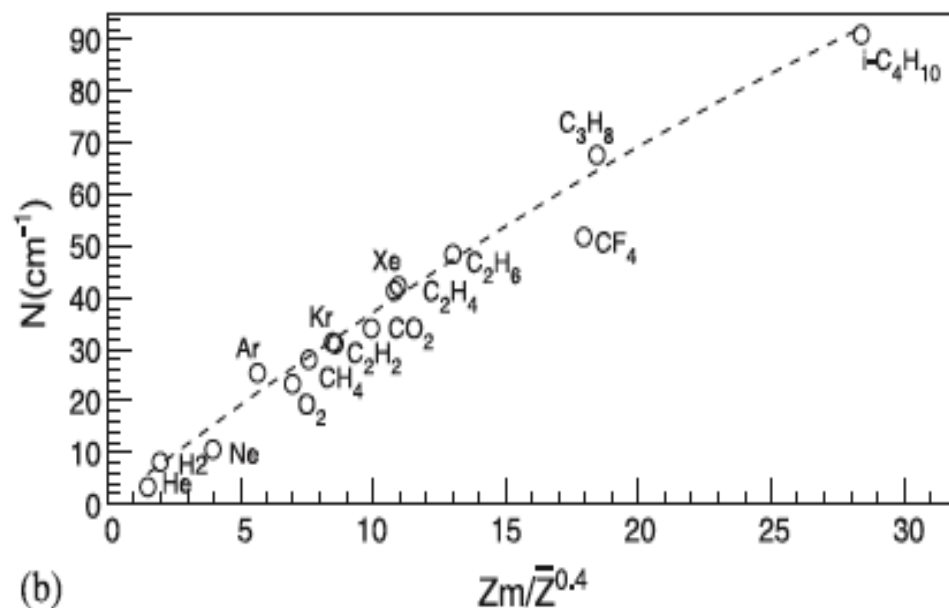
Total number of ion pairs: $n_T = \frac{\Delta E}{W_i}$

$$\Delta E = 2.5 \text{ keV/cm} \quad w_i = 25 \text{ eV} \quad n_T \approx 100 \text{ ip/cm}$$

$$\frac{n_T}{n_P} \approx 4$$

PRIMARY INTERACTIONS AND CLUSTERS

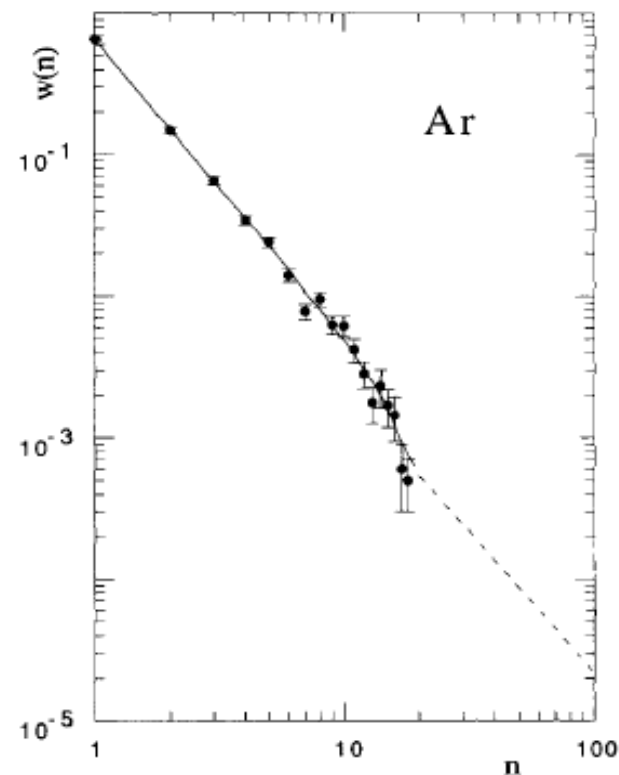
PROGRAM HEED:
NUMBER OF PRIMARY INTERACTIONS
(CLUSTERS) IN GASES AT STP



I. B. Smirnov, Nucl. Instr. and Meth. A554(2005)474

<http://consult.cern.ch/writeup/heed/>

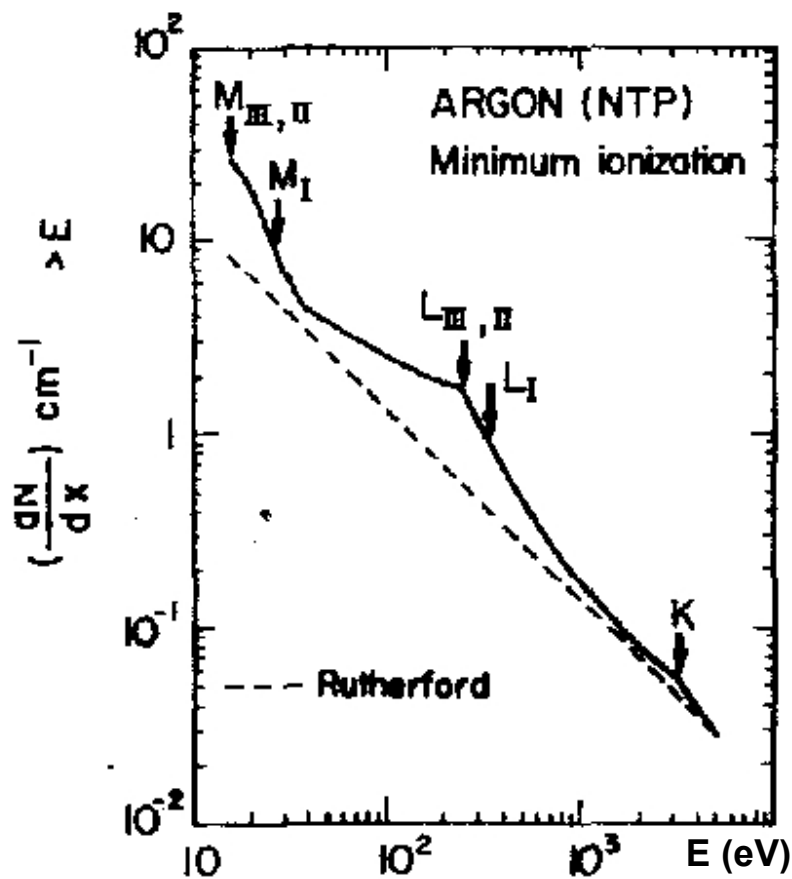
EXPERIMENTAL CLUSTER SIZE
PROBABILITY:



H. Fischle et al, Nucl. Instr. and Meth. A301 (1991) 202

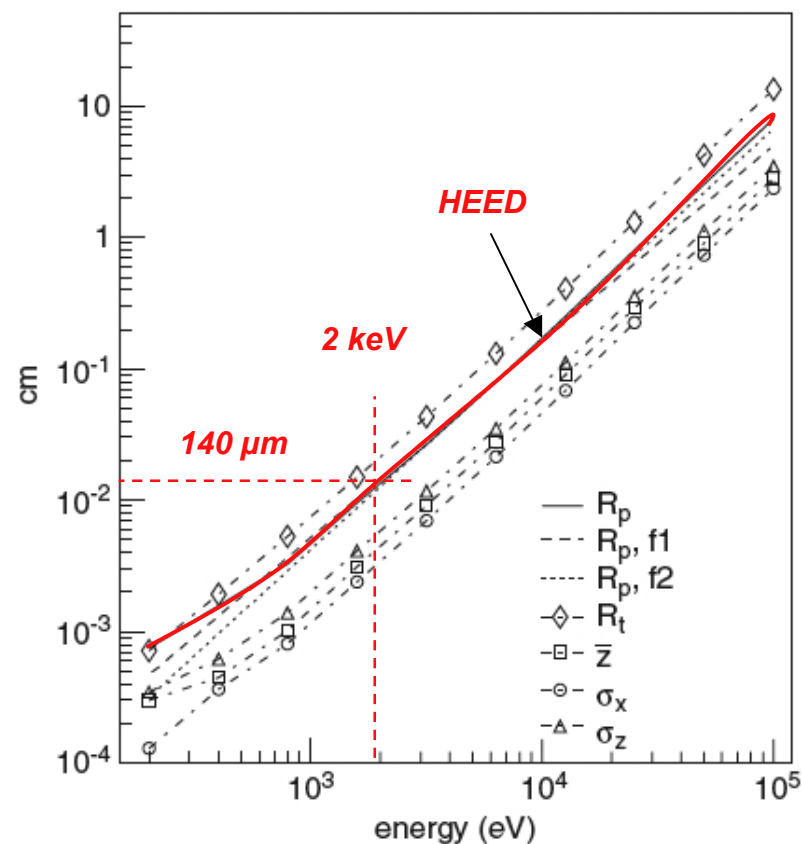
PROBABILITY AND RANGE OF DELTA ELECTRONS

PROBABILITY FOR AN ELECTRON OF ENERGY $> E$:



*F. Lapique and F. Piuz,
Nucl. instr. and Meth. 175(1980)297*

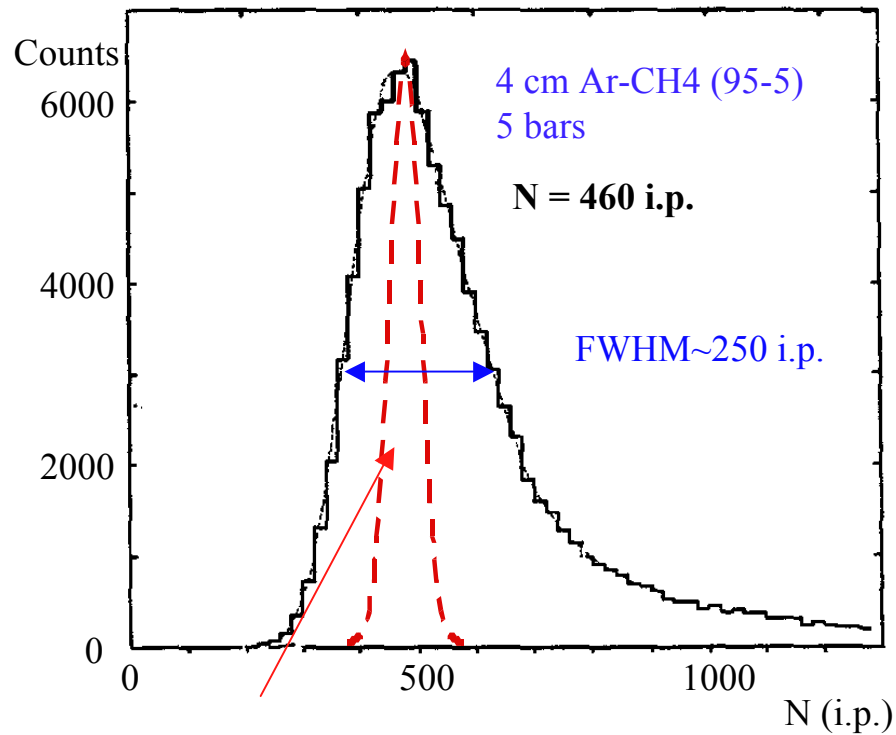
ELECTRON RANGE IN ARGON STP:



*I. B. Smirnov,
Nucl. Instr. and Meth. A554(2005)474*

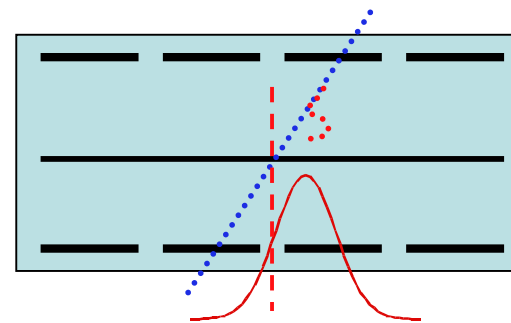
CONSEQUENCES OF IONIZATION STATISTICS

LANDAU DISTRIBUTION OF ENERGY LOSS:
POOR ENERGY LOSS RESOLUTION

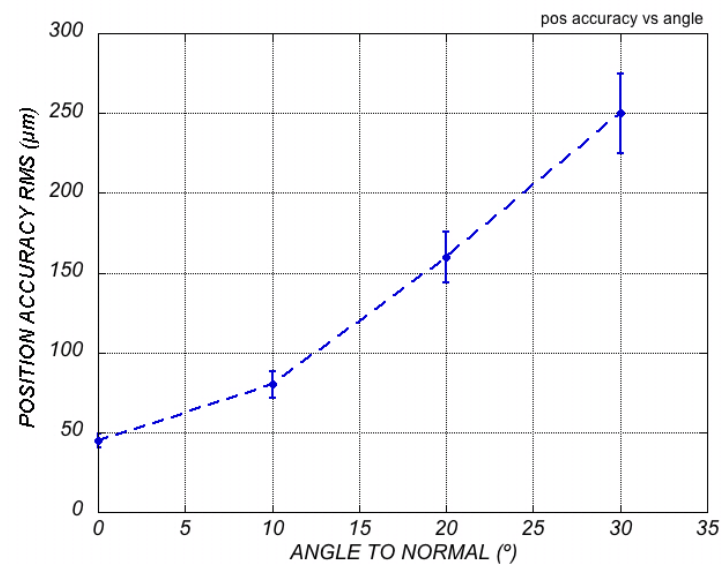


For a Gaussian distribution:
 $\sigma_N \sim 21$ i.p. FWHM ~ 50 i.p.

STRONG ANGULAR DEPENDENCE
OF POSITION ACCURACY



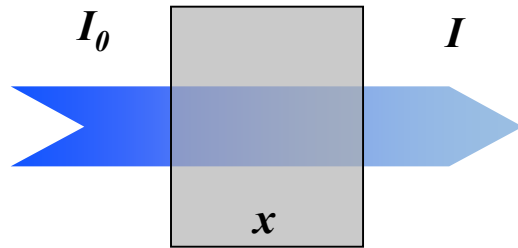
CENTER OF GRAVITY OF INDUCED CHARGE



G. Charpak et al, Nucl. Instr. and Meth. 167 (1979) 455

DETECTION OF PHOTONS

PHOTON ABSORPTION



$$I = I_0 e^{-\frac{x}{l}} \quad l : \text{absorption length}$$

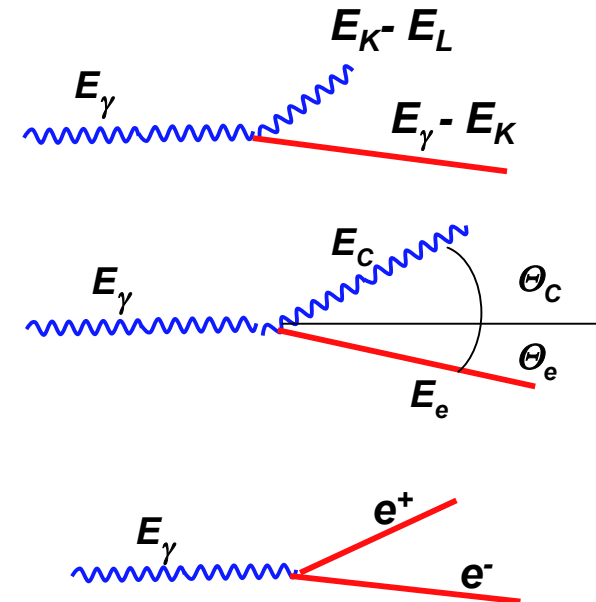
Conversion efficiency:

$$\varepsilon = \frac{I_0 - I}{I_0} = 1 - e^{-\frac{x}{l}}$$

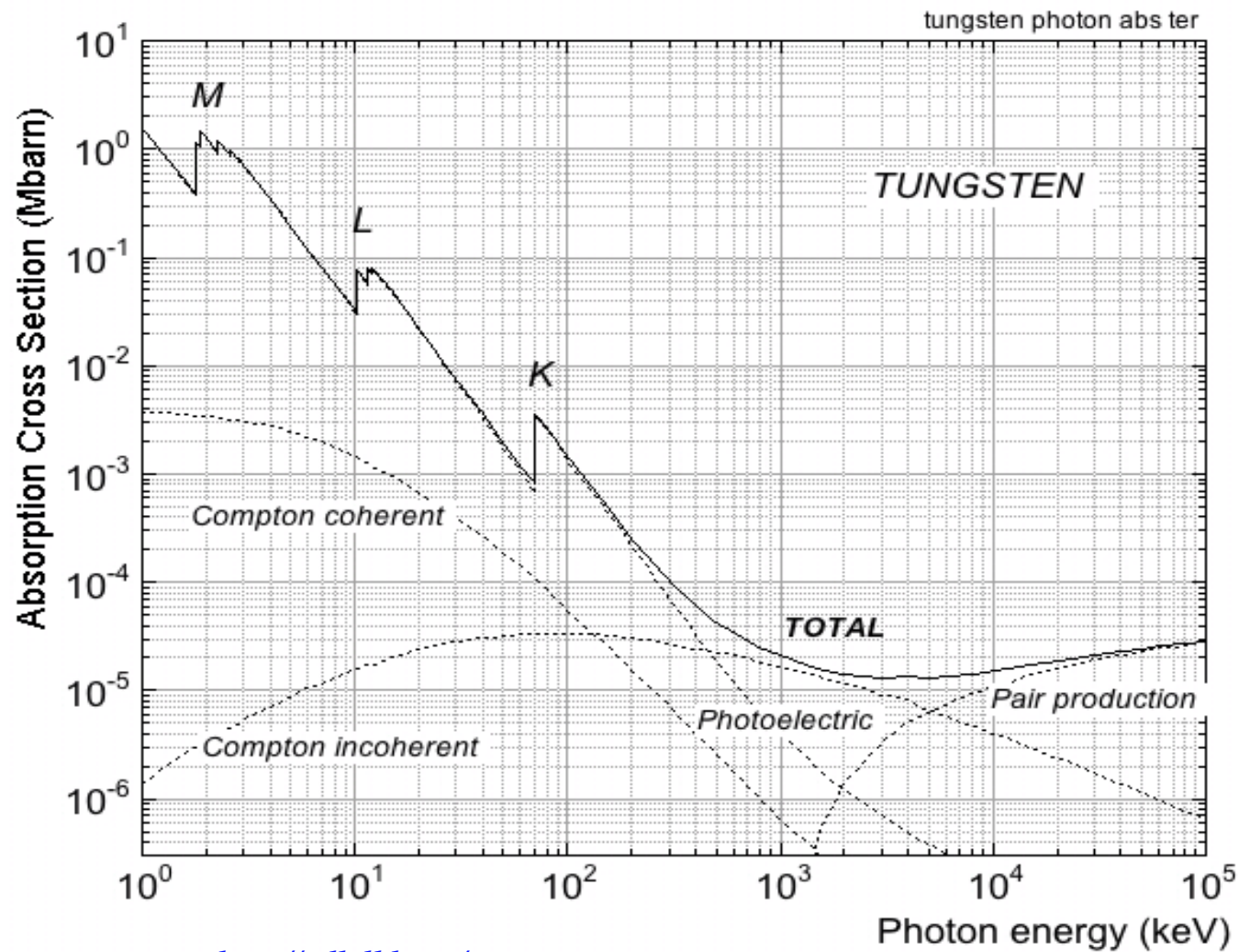
PHOTOELECTRIC: Interaction with an electronic shell with emission of a photoelectron. The excited atom/molecule returns to ground state through fluorescence or radiation-less (Auger) process.

COMPTON: Scattering of the photon by quasi-free electrons; can be coherent or incoherent

PAIR PRODUCTION: Conversion in a e^+e^- pair in the field of the atom/molecule. Possible for $E_\gamma > 2 m_e = 1.022 \text{ MeV}$



DETECTION OF PHOTONS



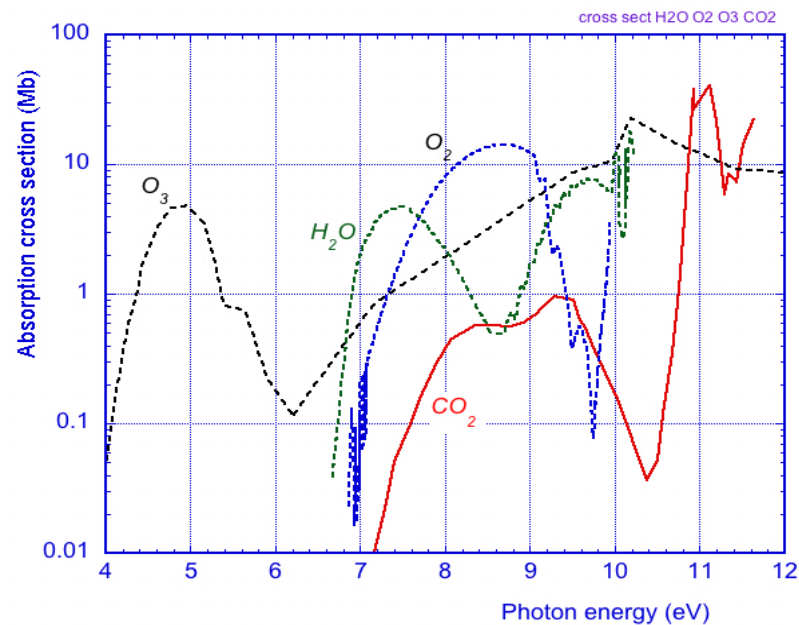
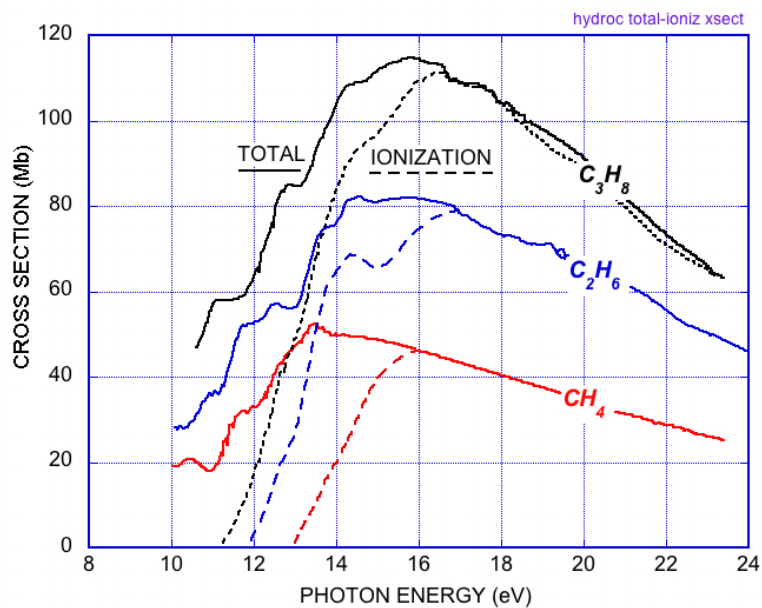
<http://xdb.lbl.gov/>

http://henke.lbl.gov/optical_constants/

<http://physics.nist.gov/PhysRefData/FFast/html/form.html>

PHOTON ABSORPTION: VISIBLE TO ULTRAVIOLET

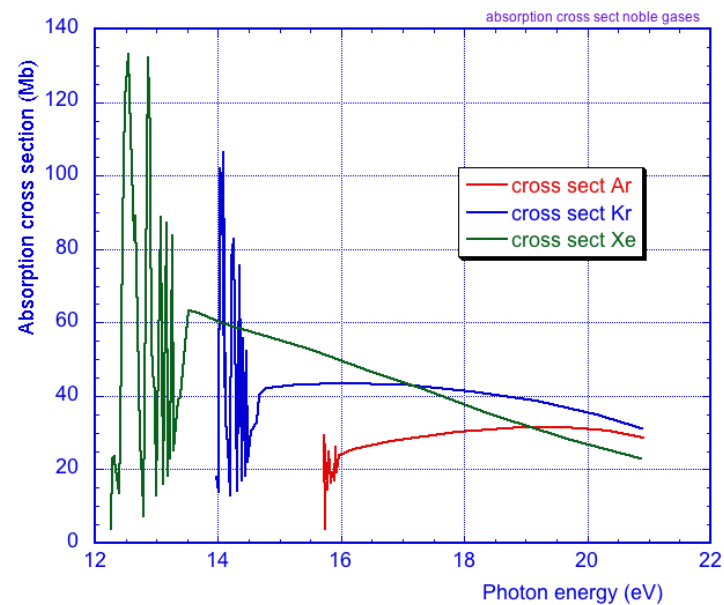
MOLECULAR GASES: ABSORPTION CROSS SECTIONS



NOBLE GASES: PHOTOIONIZATION ABOVE THRESHOLD

H. S. W. Massey, Electronic and Ionic impact Phenomena (Oxford Press 1969)

G. Marr, Photoionization Processes in Gases (Academic Press NY 1967)

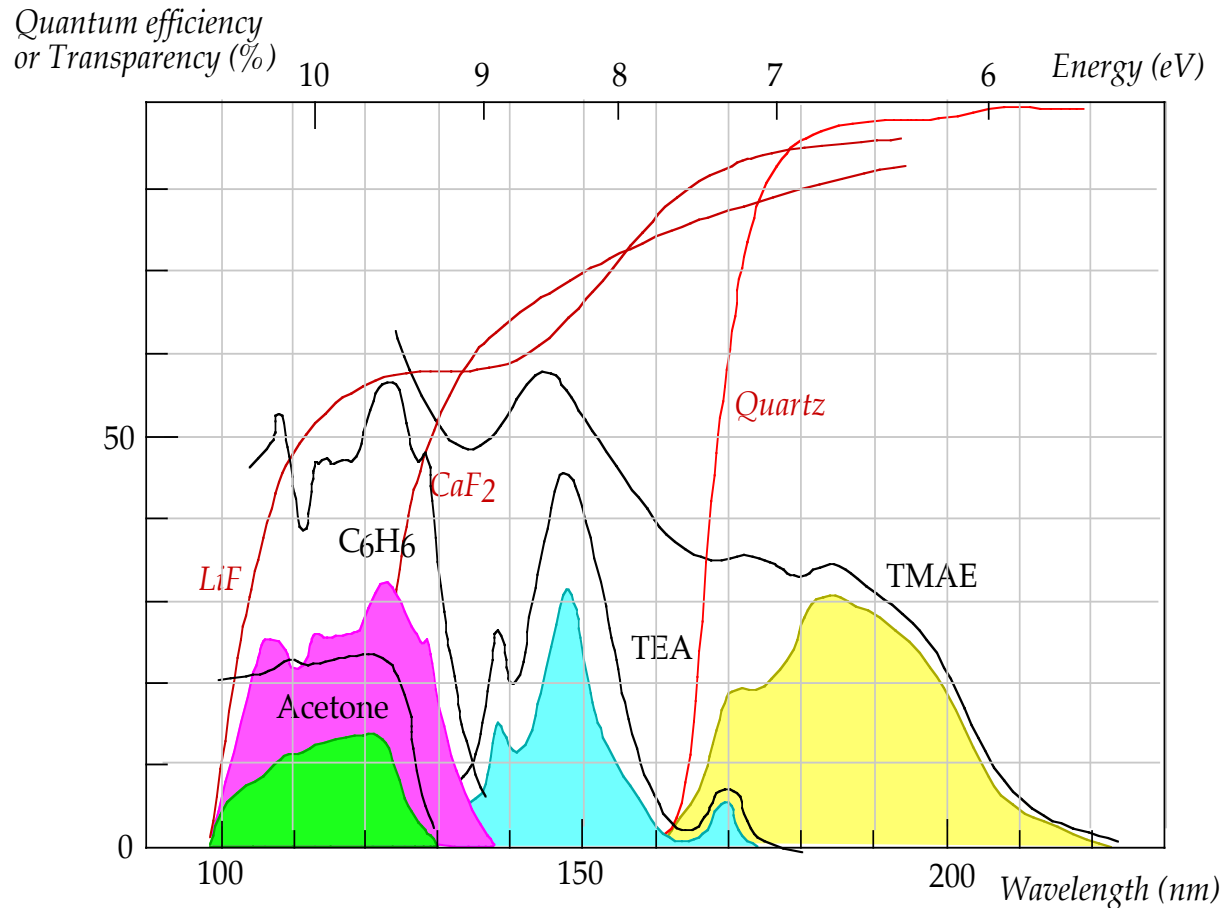


PHOTOIONIZATION

PHOTOSENSITIVE VAPOURS:

TEA (Triethylamine, $(C_2H_5)_3N$) $E_i=7.5$ eV

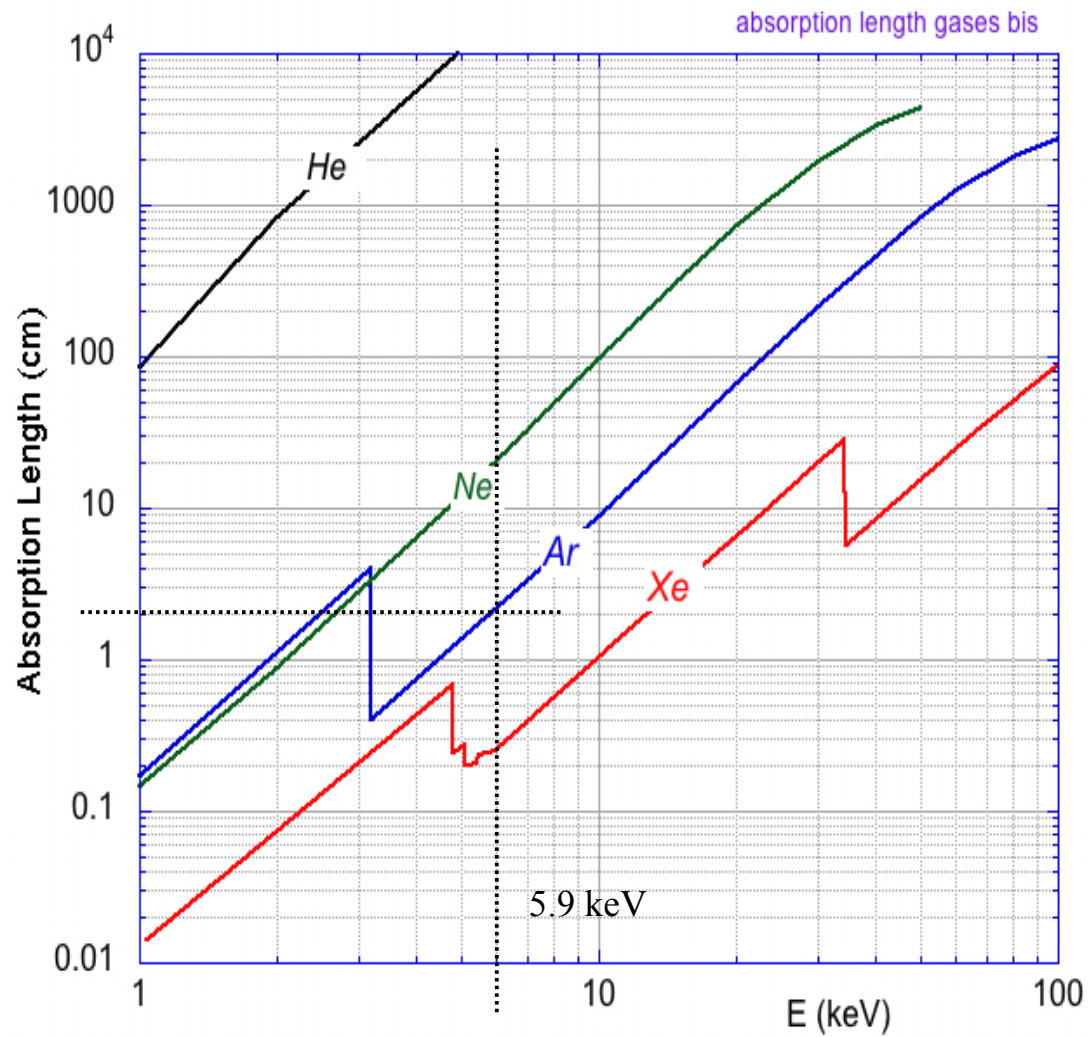
TMAE (Tetrakis (dimethylamine) ethylene, $[(CH_3)_2N]_2C$) $E_i=5.6$ eV



CHERENKOV RING IMAGING

SOFT X-RAYS

ABSORPTION LENGTH IN GASES (STP) VS PHOTON ENERGY

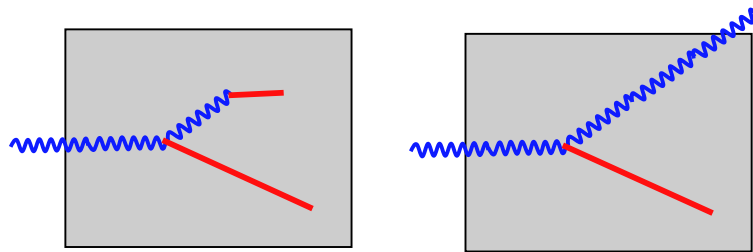


e.g.:
 ^{55}Fe 5.9 keV X-rays in Argon
 $l = 2$ cm

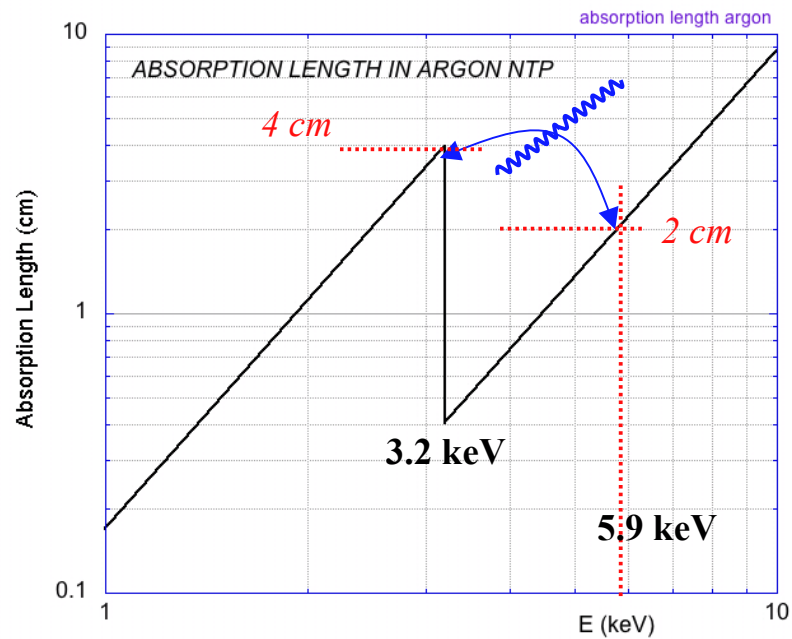
In a 1 cm thick counter:
 $\epsilon \sim 0.4$

SOFT X-RAYS: FLUORESCENCE YIELD

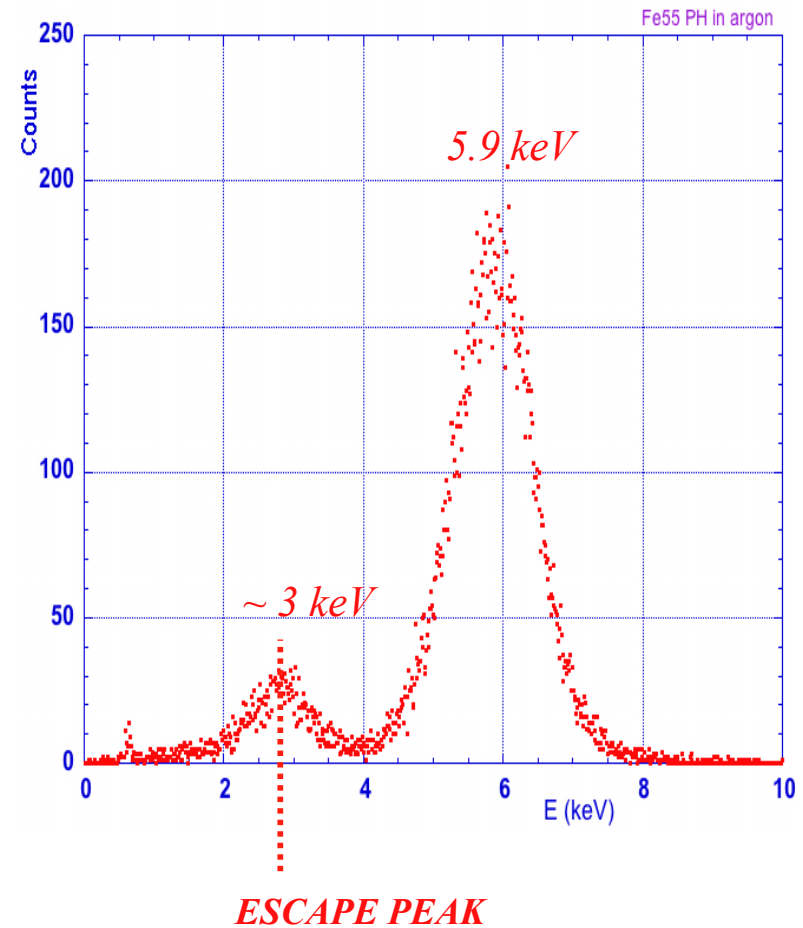
Fluorescence photons can convert far from the primary interaction, or escape from the sensitive volume (escape peak):



^{55}Fe 5.9 keV:

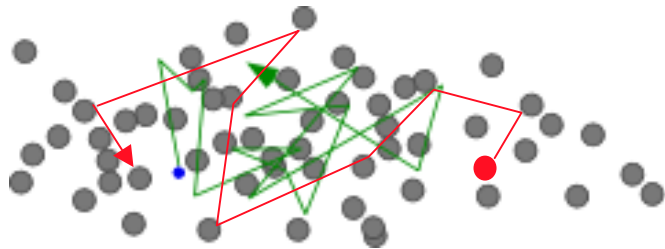


X-RAY ABSORPTION SPECTRUM
 ^{55}Fe X-Rays (5.9 keV) in Argon:

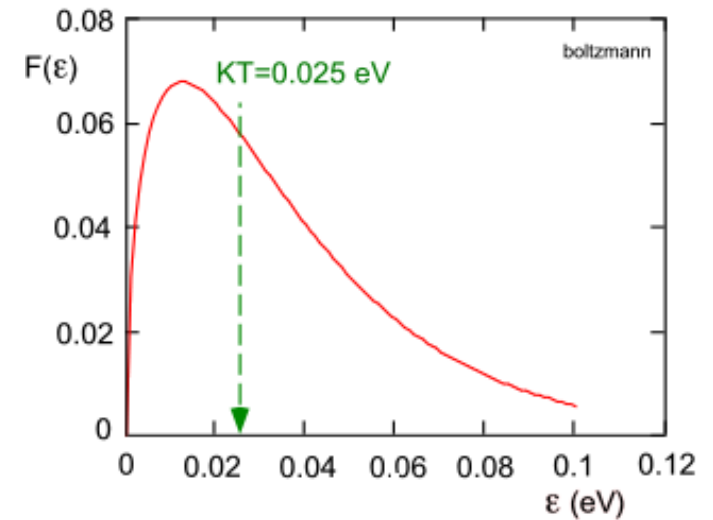


DRIFT AND DIFFUSION OF CHARGES IN GASES

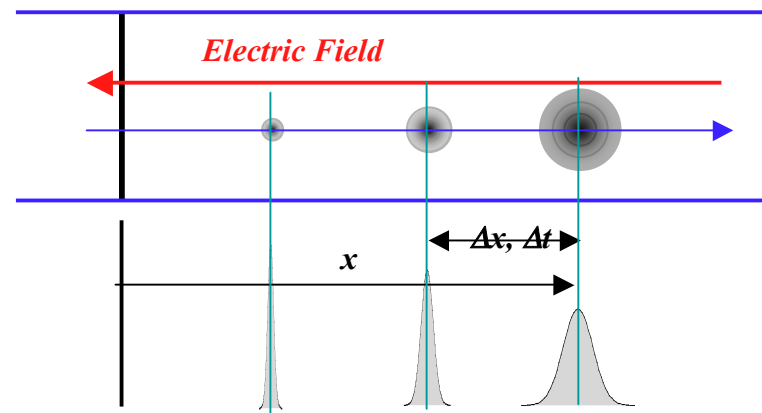
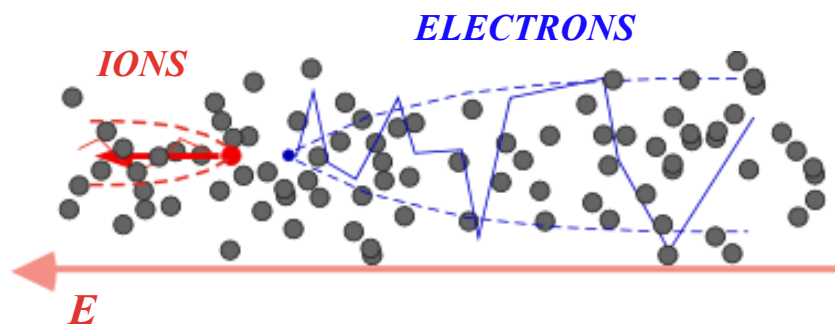
$E = 0$: THERMAL DIFFUSION (Ions and electrons):



Maxwell energy distribution: $F(\epsilon) = C\sqrt{\epsilon} e^{-\frac{\epsilon}{KT}}$



$E > 0$: CHARGE TRANSPORT AND DIFFUSION



Drift velocity: $w = \frac{\Delta x}{\Delta t}$

Diffusion: $\sigma = \sqrt{2Dt} = \sqrt{2D \frac{x}{w}}$

DRIFT OF IONS

MOBILITY: RATIO OF VELOCITY AND FIELD

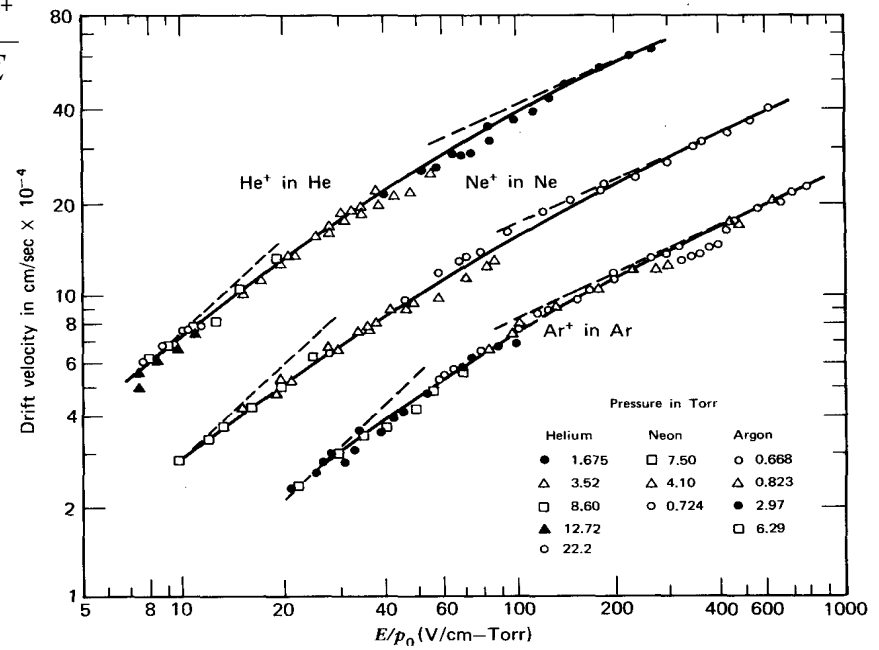
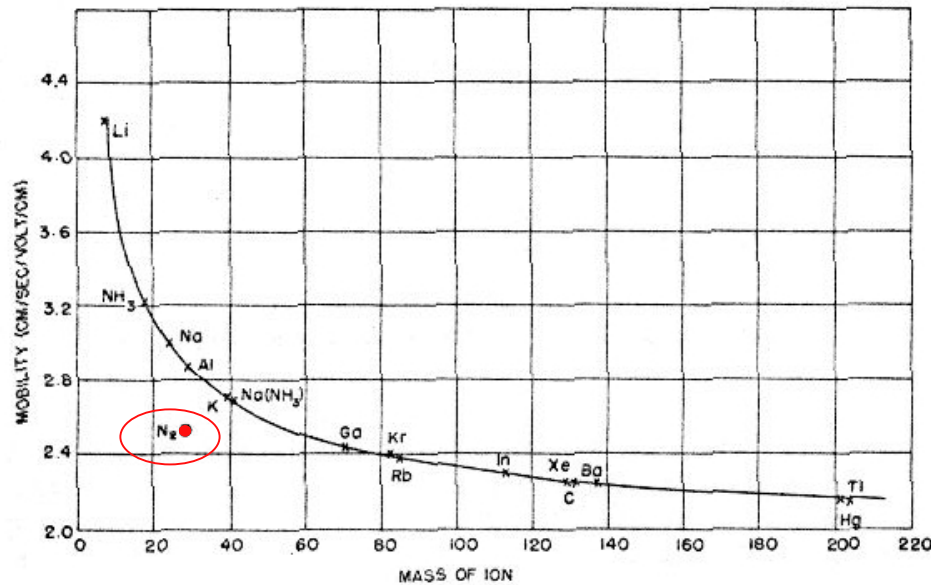
$$\mu^+ = \frac{w^+}{E}$$

IONS MOBILITY (NTP: 300 K, 760 mm Hg)

GAS	ION	$\mu^+(\text{cm}^2\text{s}^{-1}\text{V}^{-1})$
He	He ⁺	10.2
Ar	Ar ⁺	1.7
CH ₄	CH ₄ ⁺	2.26
Ar	CH ₄ ⁺	1.87
CO ₂	CO ₂ ⁺	1.09

Ar-CH₄, E=1kV cm⁻¹ w⁺= 1.87 cm ms⁻¹

IONS MOBILITY IN NITROGEN:

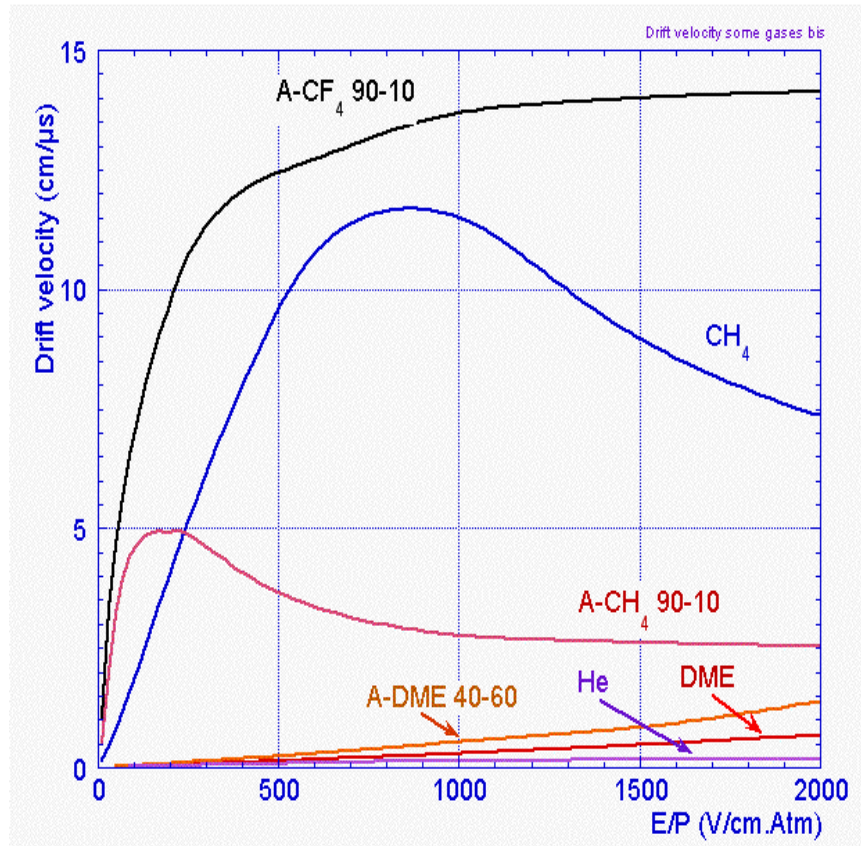


S. C. Brown

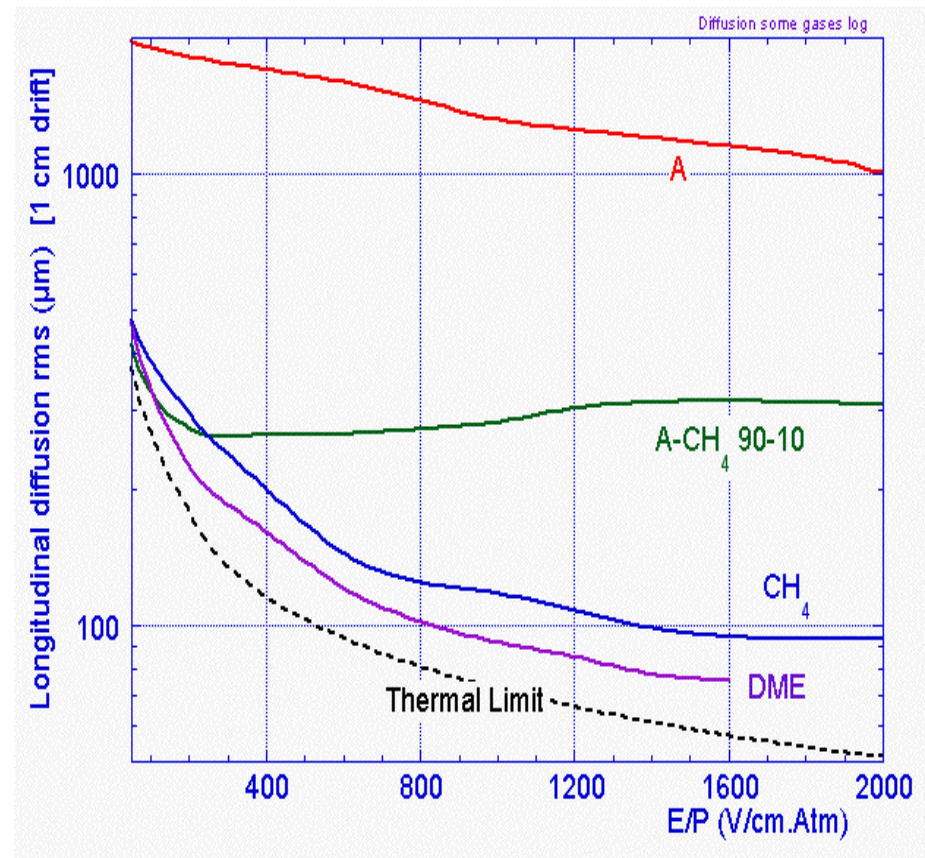
Basic Data in Plasma Physics (Wiley, New York 1959)

ELECTRONS DRIFT VELOCITY

DRIFT VELOCITY:



DIFFUSION:



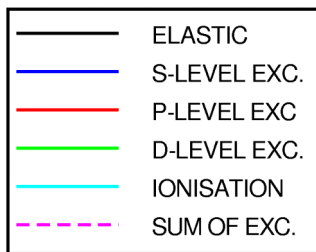
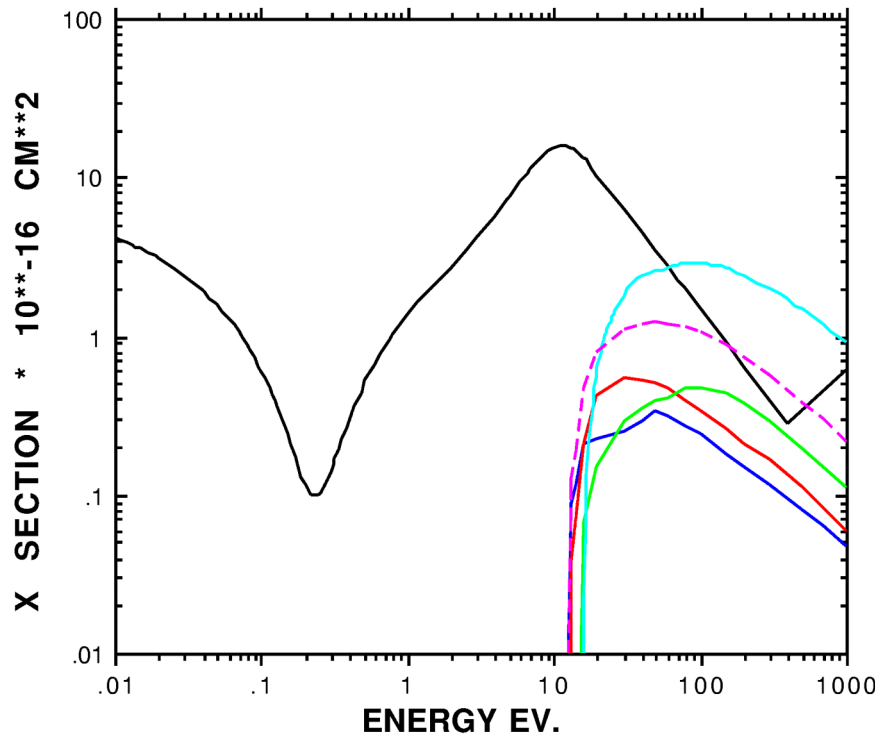
A. Peisert and F. Sauli, Drift and Diffusion of Electrons in Gases: a compilation CERN 84-08 (1984)

MAGBOLTZ

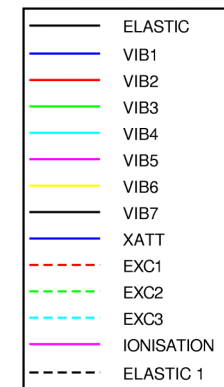
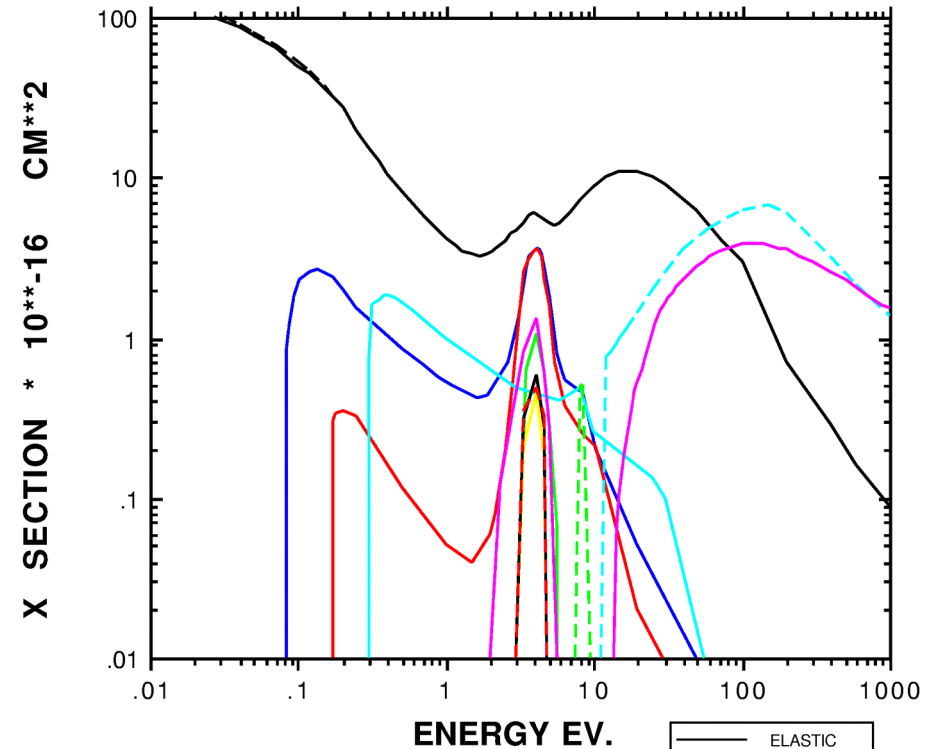
ELECTRON-MOLECULE CROSS SECTION

Charge transport processes are determined by the various electron-molecule cross sections:

ARGON (1997)



CO2 (NAKAMURA)



MAGBOLTZ:

Montecarlo program to compute electron drift and diffusion

S. Biagi, Nucl. Instr. and Meth. A421(1999)234

<http://rjd.web.cern.ch/rjd/cgi-bin/cross>

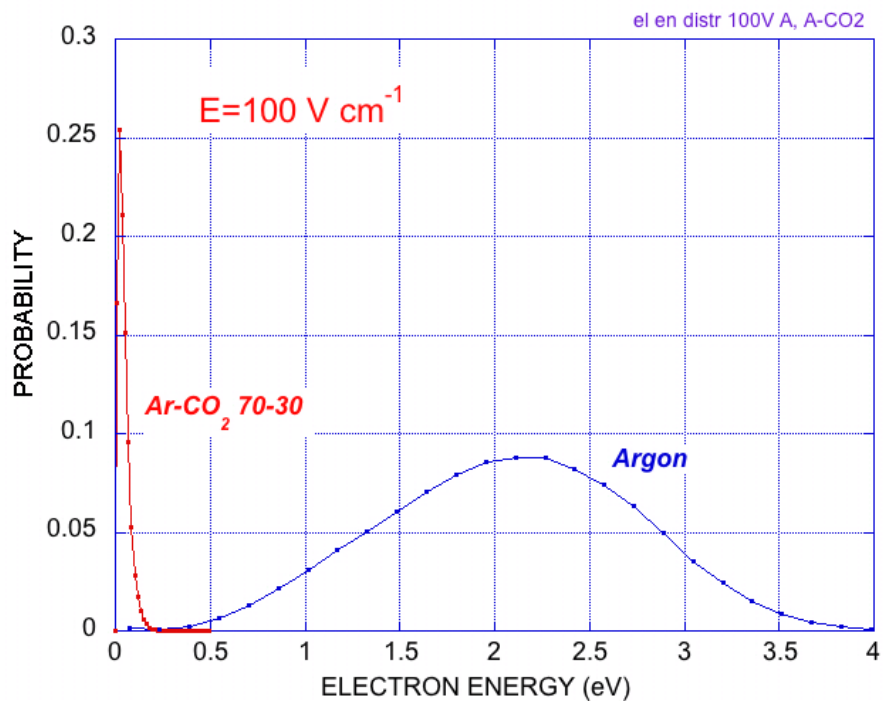


Stephen Biagi

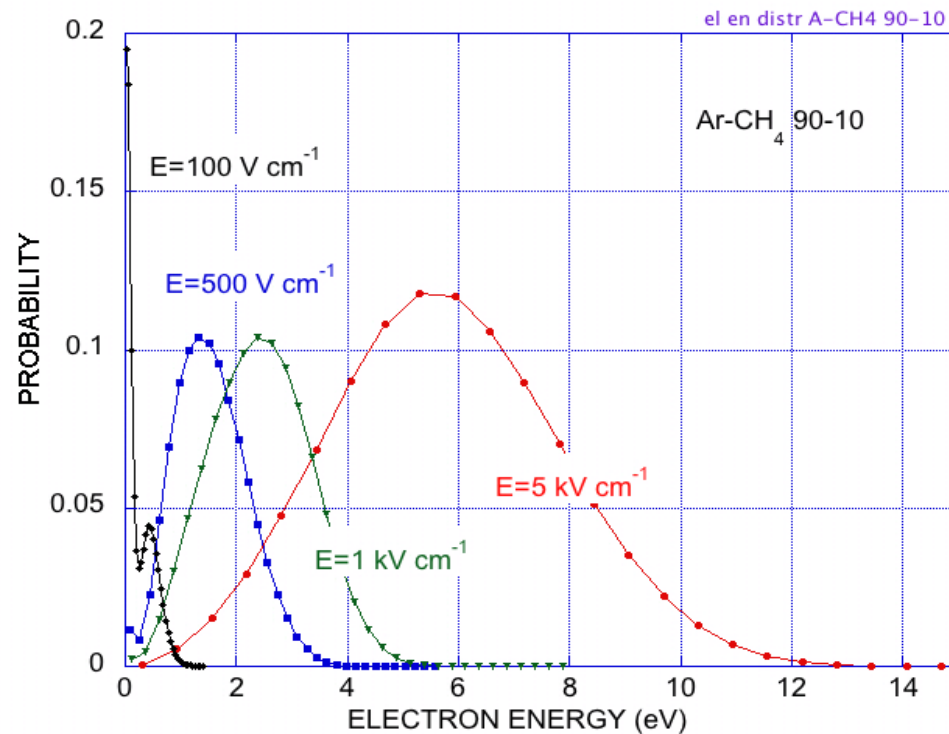
ELECTRONS ENERGY

ENERGY DISTRIBUTION AT INCREASING FIELDS:

EQUAL FIELD, DIFFERENT GAS:

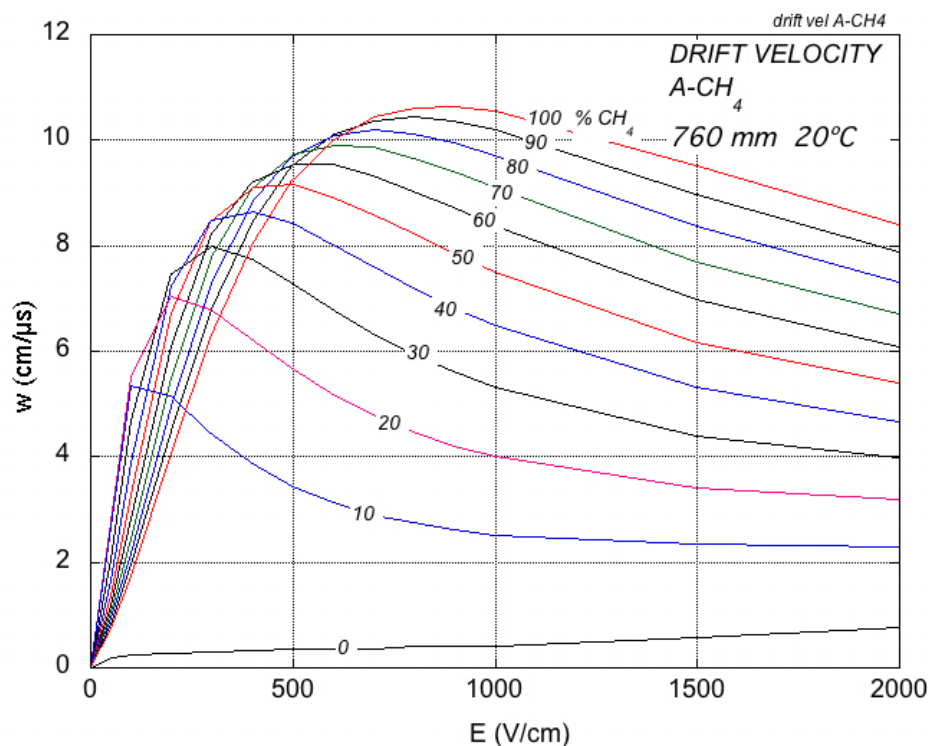


SAME GAS, INCREASING FIELD:



ELECTRONS DRIFT AND DIFFUSION

DRIFT VELOCITY IN ARGON-METHANE MIXTURES



EXAMPLE: Ar-CH₄ 90-10), STP, E=1kVcm⁻¹

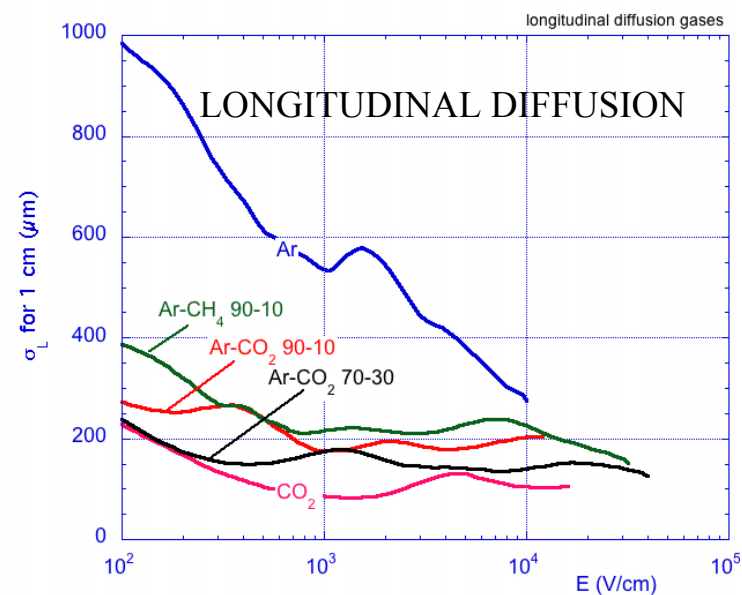
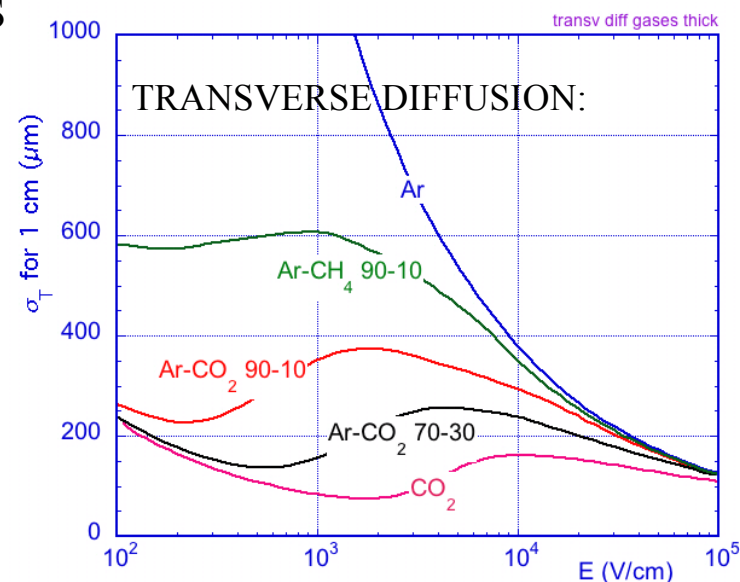
$$w^- = 2.5 \text{ cm } \mu\text{s}^{-1}$$

$$\sigma_T = 600 \text{ } \mu\text{m}$$

$$\sigma_L = 200 \text{ } \mu\text{m}$$

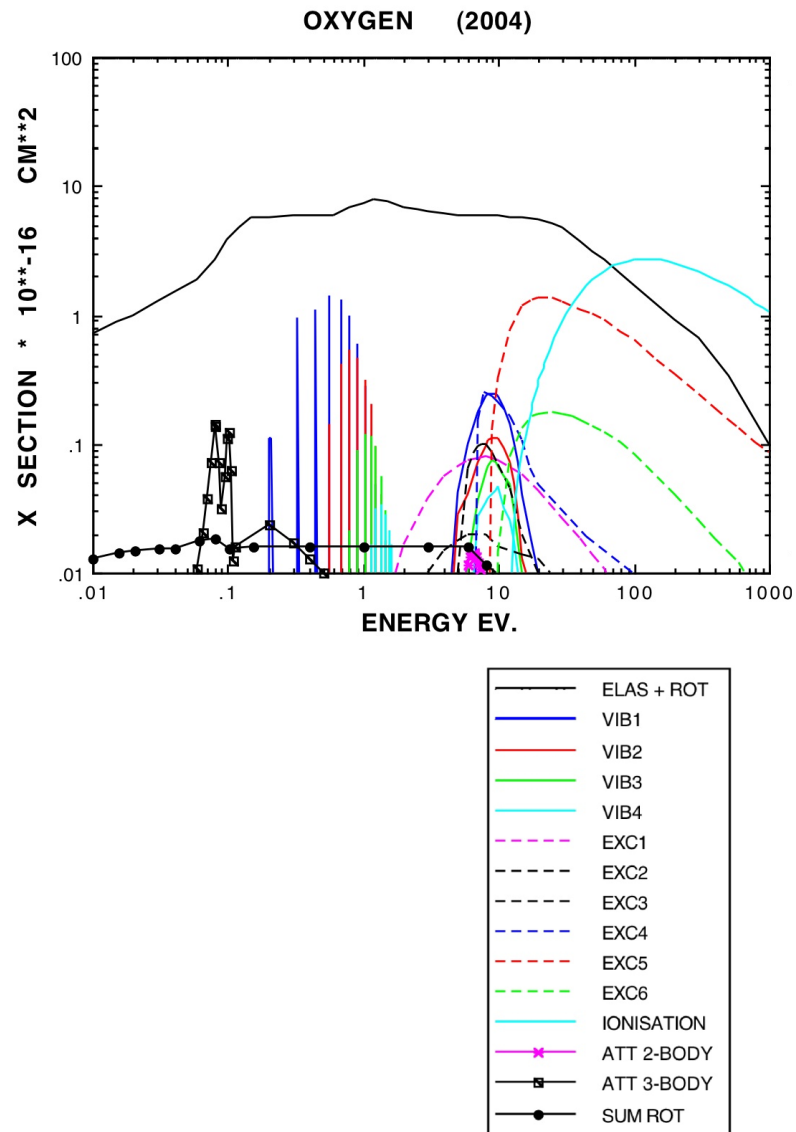
$$\frac{w^-}{w^+} \cong 10^3$$

Computed with MAGBOLTZ

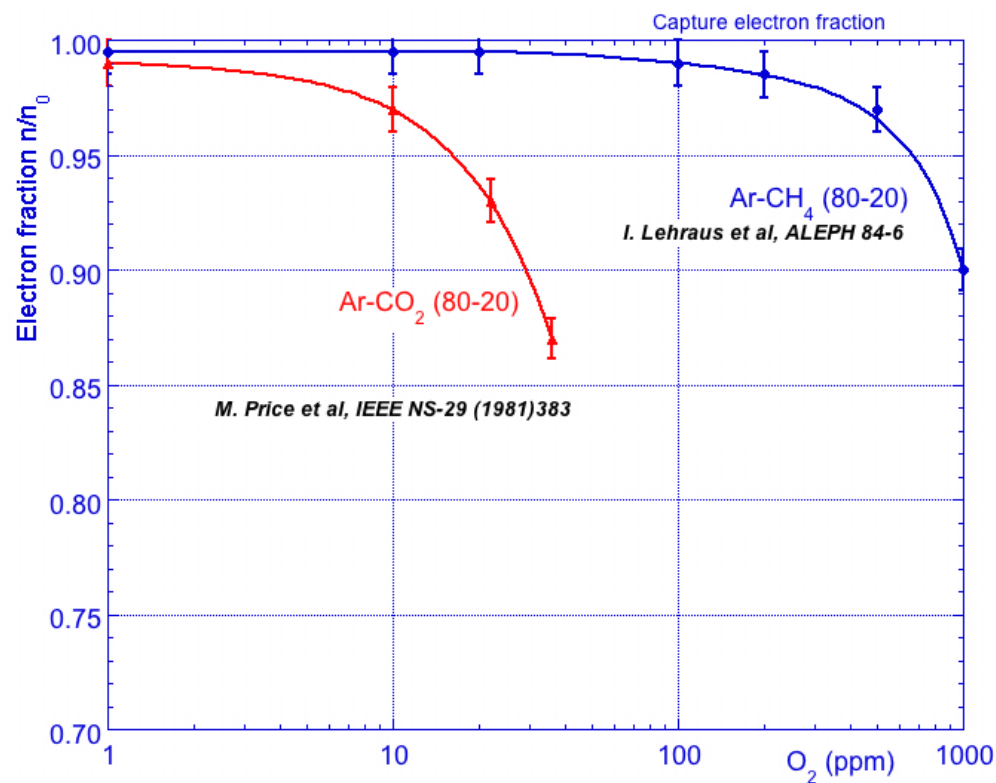


ELECTRON CAPTURE

ATTACHMENT CROSS SECTION OF OXYGEN:

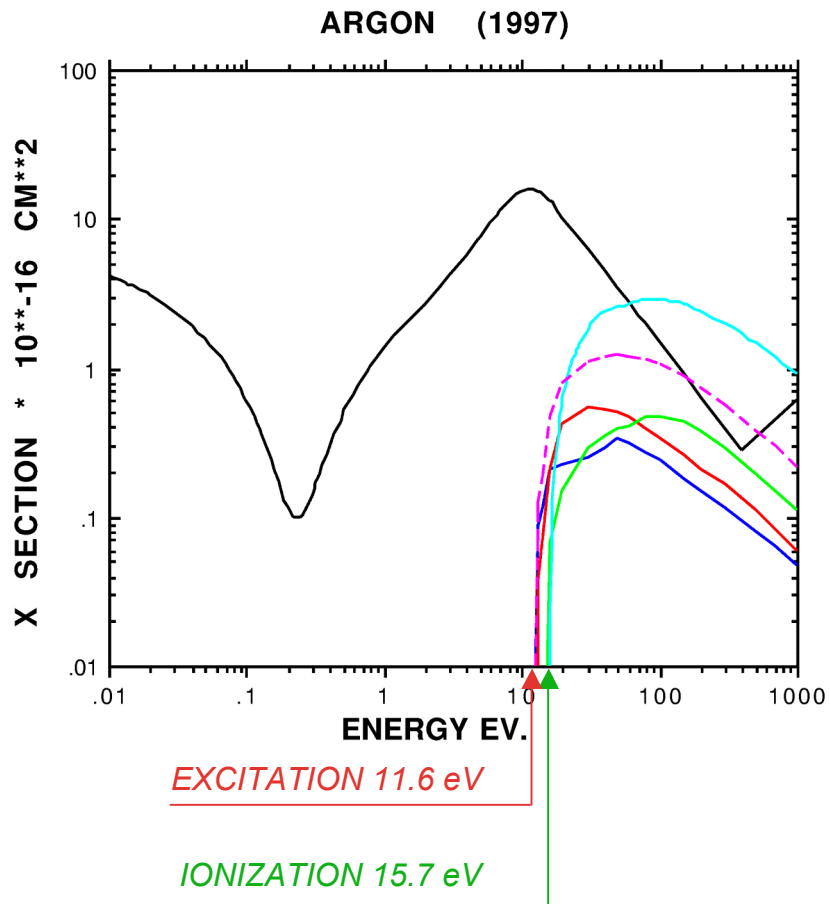


ELECTRONS SURVIVING AFTER 20 CM DRIFT (E = 200 V/cm):

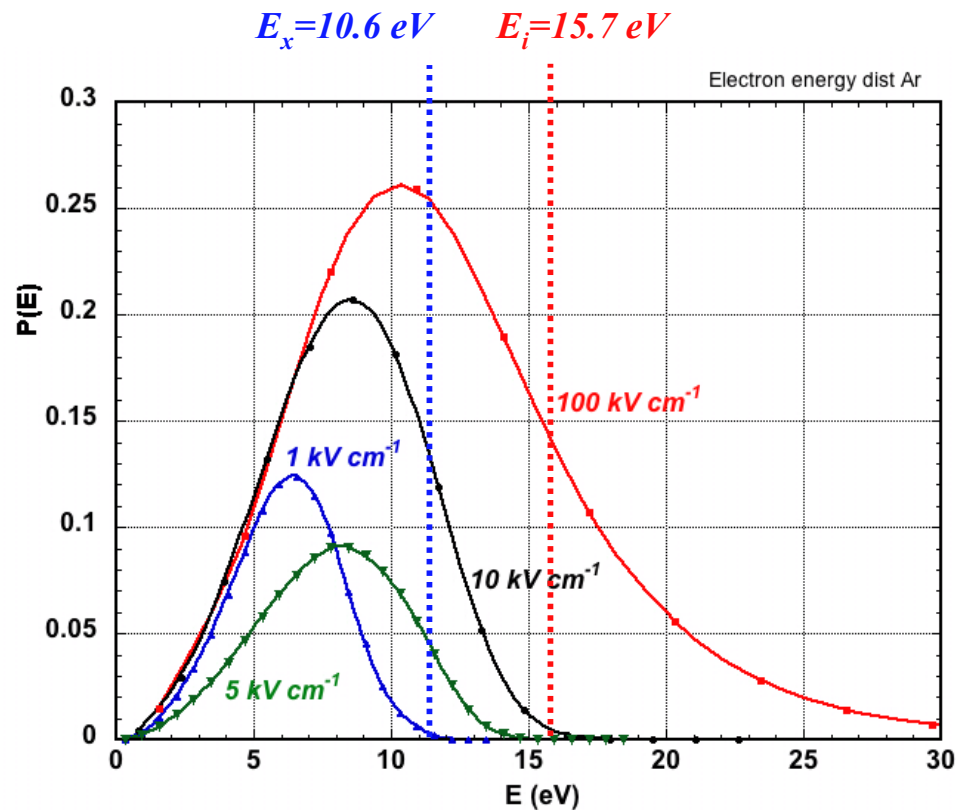


HIGH FIELD-INELASTIC COLLISIONS

ELECTRON CROSS SECTIONS IN ARGON:



ELECTRONS ENERGY DISTRIBUTION IN ARGON AT INCREASING FIELDS:



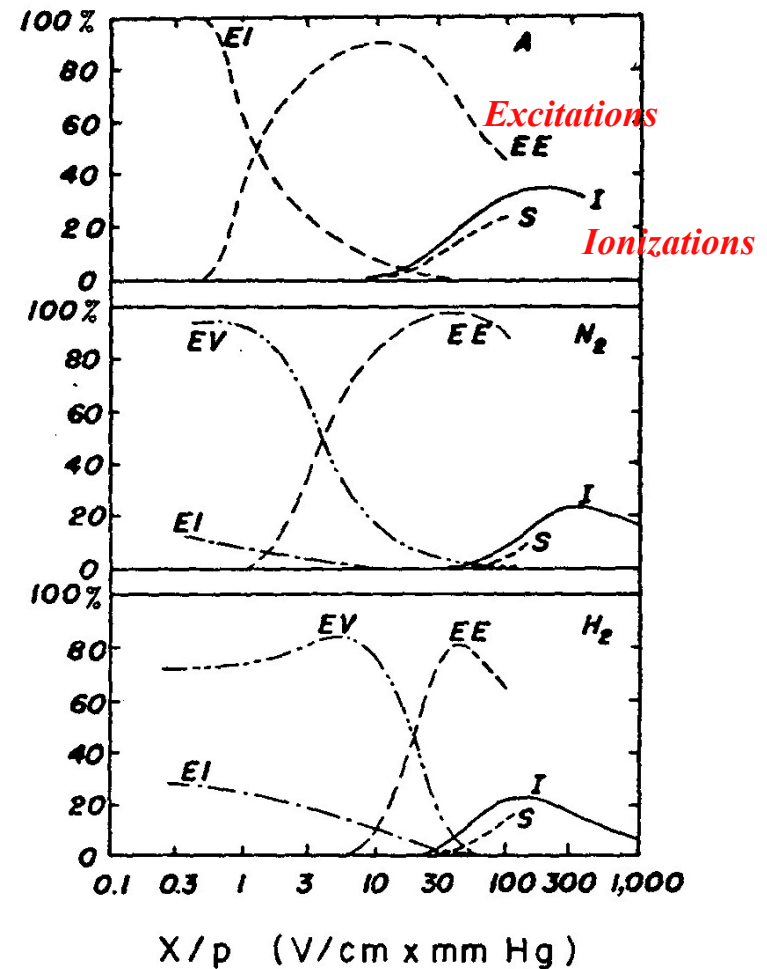
HIGH FIELD-INELASTIC COLLISIONS

MAIN ELECTRON-MOLECULE INELASTIC PROCESSES:

1) $A+e \Rightarrow A^++e+e$	Ionisation by electronic impact.
2) $A+e \Rightarrow A^++e$	Excitation by electronic impact.
3) $A^++e \Rightarrow A+e$	Deexcitation by electronic collision.
4) $A+h\nu \Rightarrow A^*$	Photo-excitation (absorption of light).
5) $A^* \Rightarrow A+h\nu$	Photo-emission (radiative deexcitation).
6) $A+h\nu \Rightarrow A^++e$	Photoionisation.
7) $A^++e \Rightarrow A+h\nu$	Radiative recombination.
8) $A^++B+e \Rightarrow A+B$	Three body recombination.
9) $A^++B \Rightarrow A+B^*$	Collisional deexcitation.
10) $A^++B \Rightarrow A+B^++e$	Penning effect.
11) $A^++B \Rightarrow A+B^+$	Charge exchange.
12) $A^++B \Rightarrow A^++B^++e$	Ionisation by ionic impact.
13) $A+B \Rightarrow A^++B$	Excitation by atomic impact.
14) $A+B \Rightarrow A^++B+e$	Ionisation by atomic impact.
15) $A+e \Rightarrow A^-$	Formation of negative ions.
16) $A^- \Rightarrow A+e$	Electrons release by negative ions.
17) $A^{**}+A \Rightarrow A_2^++e$	Associative ionisation.
18) $A^++2A \Rightarrow A_2^++A$	Molecular ion formation.
19) $A^++A+A \Rightarrow A_2^++A$	Excimer formation.
20) $A_2^* \Rightarrow A+A+h\nu$	Radiative excimer dissociation.
21) $(XY)^* \Rightarrow X+Y^*$	Dissociation.
22) $(XY)^++e \Rightarrow X+Y^*$	Recombinational dissociation.

J. Meek and J. D. Cragg, Electrical Breakdown of Gases (Clarendon Press, Oxford 1953)

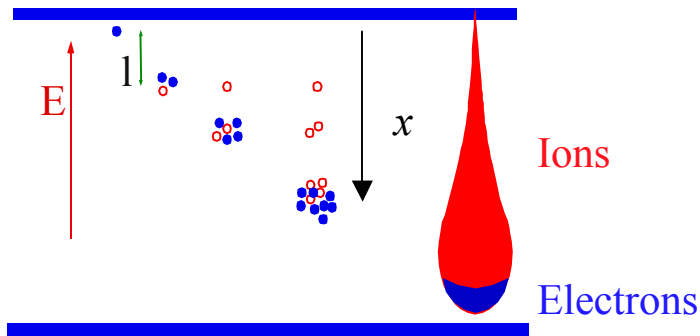
ENERGY SHARING BETWEEN COLLISION PROCESSES:



L. B. Loeb, Basic Processes of Gaseous Electronics (UC Berkeley Press, 1961)

CHARGE MULTIPLICATION

CHARGE MULTIPLICATION IN UNIFORM FIELD

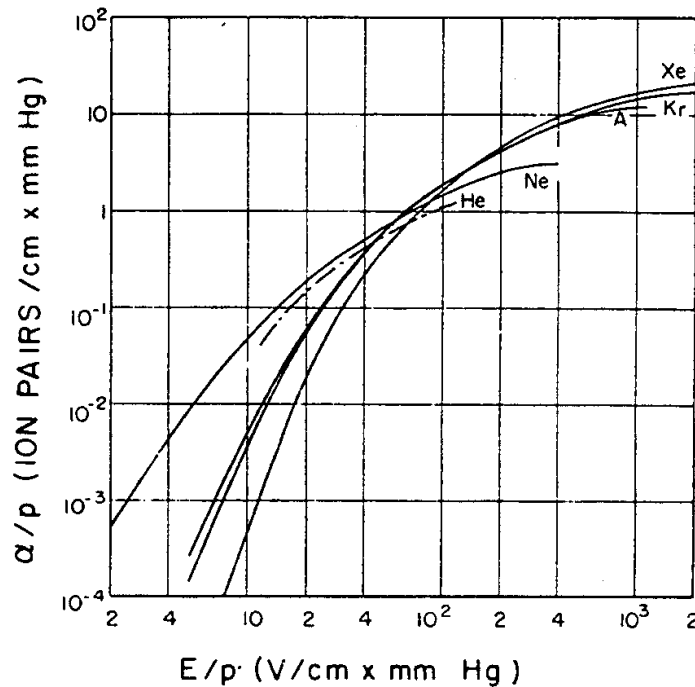


Mean free path for ionization:

$$\lambda = \frac{1}{N\sigma} \quad N: \text{molecules/cm}^3$$

Townsend coefficient:

$$\alpha = \frac{1}{\lambda} \quad \text{Ionizing collisions/cm} \quad \frac{\alpha}{P} = f\left(\frac{E}{P}\right)$$



Incremental increase of the number of electrons in the avalanche:

$$dn = n \alpha dx$$

Multiplication factor (Gain): $M(x) = \frac{n}{n_0} = e^{\alpha x}$

Maximum Avalanche size before discharge (Raether limit):

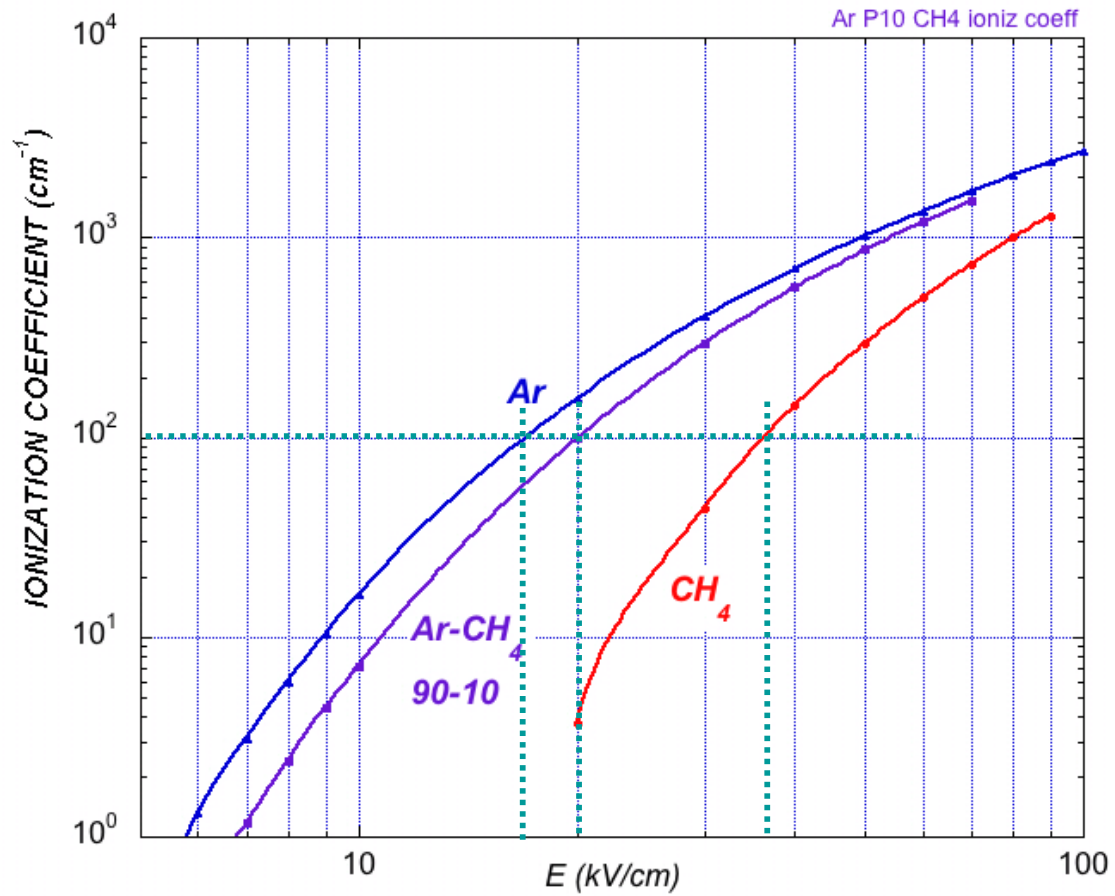
$$Q_{\text{MAX}} \approx 10^7 e$$

H. Raether, Electron Avalanches and Breakdown in Gases (Butterworth 1964)

S.C. Brown, Basic Data of Plasma Physics (MIT Press, 1959)

TOWNSEND COEFFICIENT

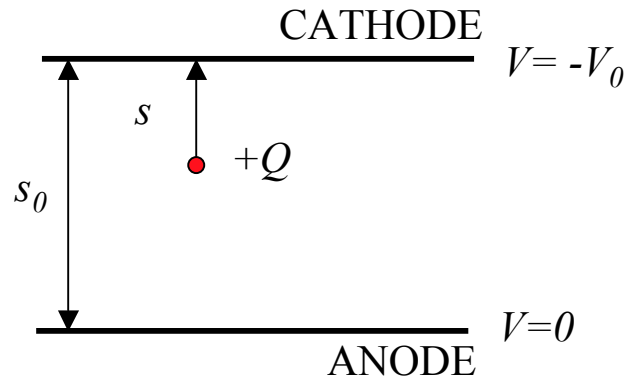
TOWNSEND COEFFICIENT FOR Ar, CH₄ and Ar-CH₄:



(COMPUTED WITH MAGBOLTZ)

CHARGE INDUCTION - IONIZATION CHAMBER

SIGNAL DEVELOPMENT BY A MOVING CHARGE +Q



Charge induced on each electrode by +Q moving through the difference of potential dV:

$$dq = Q \frac{dV}{V_0} = Q \frac{ds}{s_0}$$

Integrating over s (or time t):

$$q(s) = \frac{Q}{s_0} s \quad q(t) = \frac{Q}{s_0} wt \quad i(t) = \frac{dq}{dt} = \frac{Q}{s_0} w$$

Electrons- ion pair (-Q and +Q) released at the same distance s from the cathode :

$$q(t) = Q \left(\frac{w^- t}{s_0} + \frac{w^+ t}{s_0} \right) \quad 0 \leq t \leq T^-$$

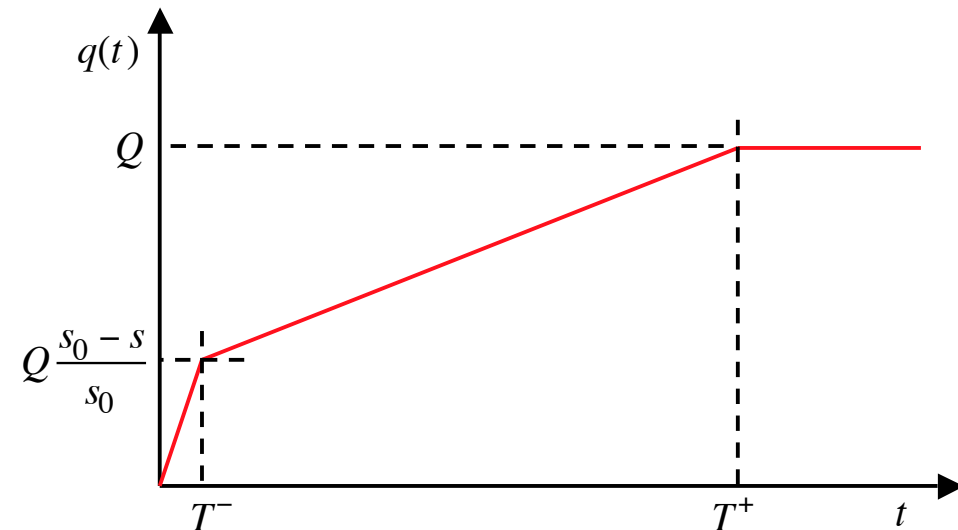
$$q(t) = Q \left(\frac{s - s_0}{s_0} + \frac{w^+ t}{s_0} \right) \quad T^- \leq t \leq T^+$$

$$q(T^+) = Q$$

w^- (w^+) : electron (ion) drift velocity

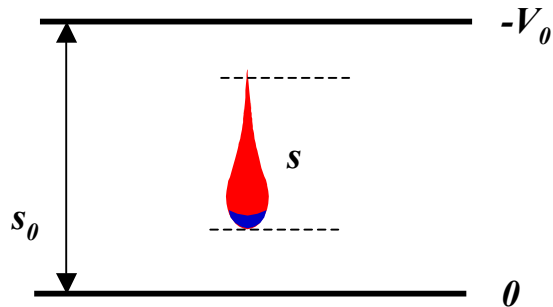
T^- (T^+) : total electron (ion) drift time

(+Q on cathode , -Q on anode)



CHARGE INDUCTION - AVALANCHE MULTIPLICATION

PARALLEL PLATE COUNTERS:



Increase in the number of charges after a path ds :

$$dn = n\alpha ds \quad n = n_0 e^{\alpha s}$$

Charge induced by electrons: $dq^- = -en_0 e^{\alpha s} \frac{ds}{s_0}$

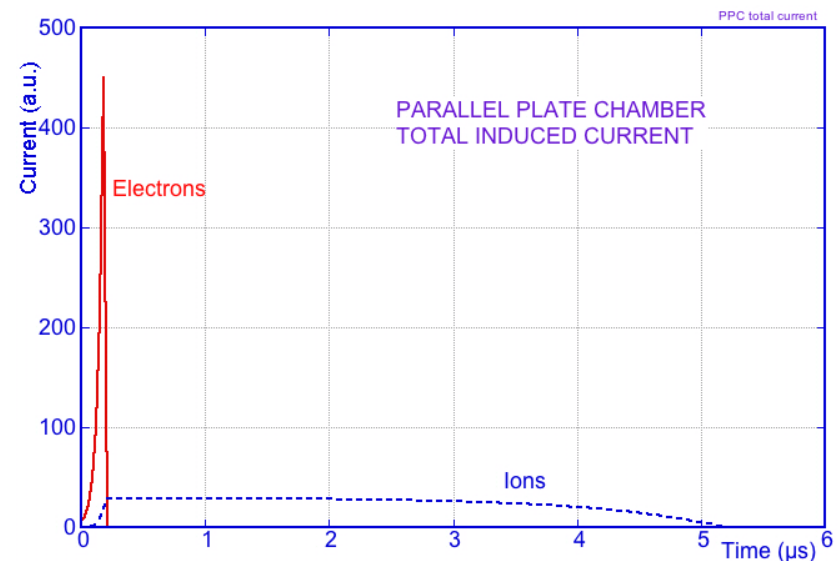
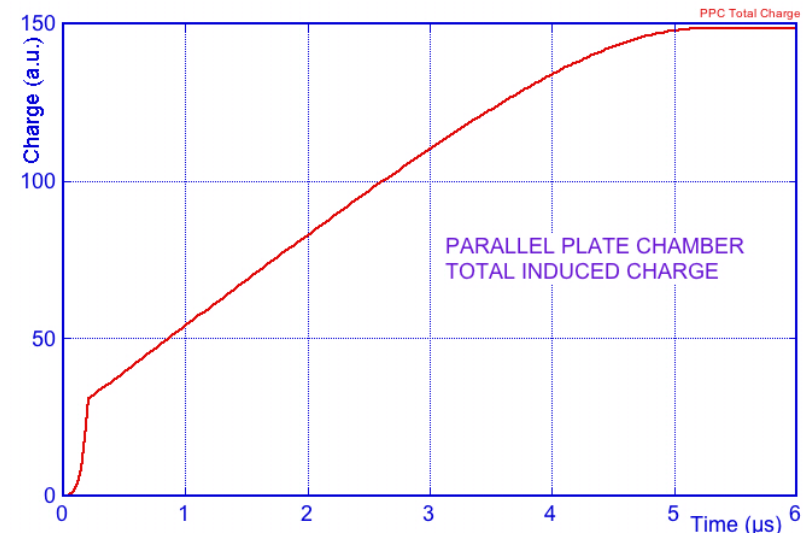
$$q^-(s) = \frac{en_0}{\alpha s_0} (e^{\alpha s} - 1) \approx \frac{en_0}{\alpha s_0} e^{\alpha s} = \frac{en_0}{\alpha s_0} e^{\alpha w^- t}$$

$$i^-(t) = \frac{dq^-}{dt} = \frac{en_0 w^-}{s_0} e^{\alpha w^- t} = \frac{en_0}{T^-} e^{\alpha w^- t}$$

Current signal induced by ions:

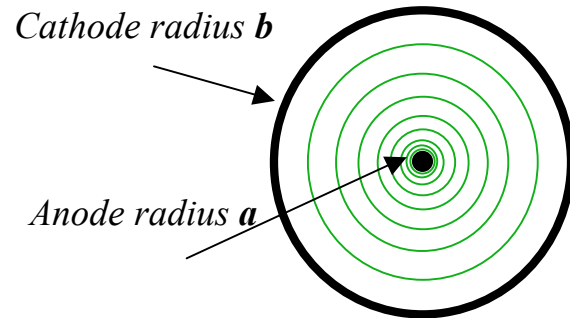
$$i^+(t) = \frac{en_0}{T^+} (e^{\alpha w^- t} - e^{\alpha w^+ t}) \quad 0 \leq t \leq T^-$$

$$i^+(t) = \frac{en_0}{T^+} (e^{\alpha s} - e^{\alpha w^+ t}) \quad T^- \leq t \leq T^+ \quad \frac{1}{w^*} = \frac{1}{w^+} + \frac{1}{w^-}$$



PROPORTIONAL COUNTER

THIN ANODE WIRE

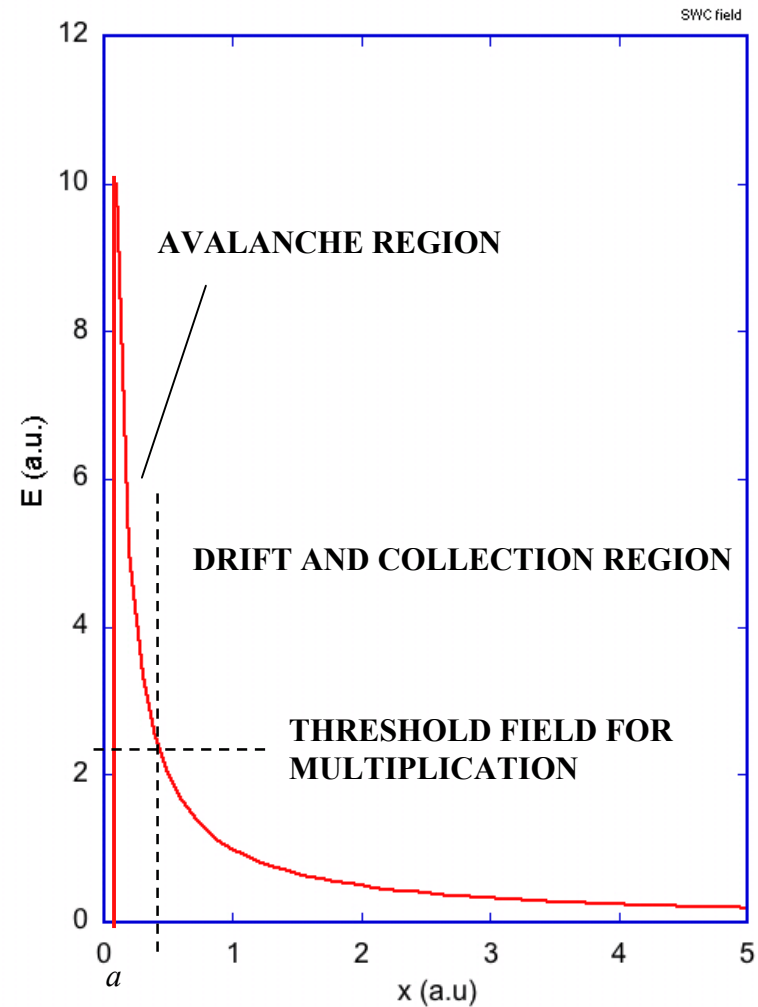


ELECTRIC FIELD AND POTENTIAL:

$$E(r) = \frac{CV_0}{2\pi\epsilon_0} \frac{1}{r}$$

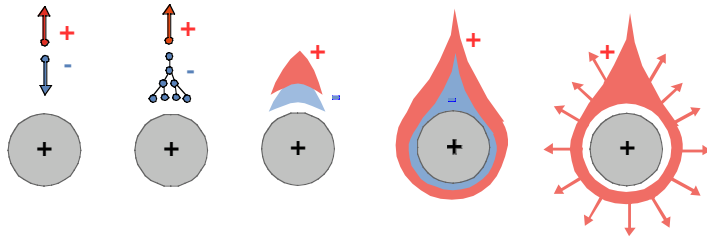
$$V(r) = \frac{CV_0}{2\pi\epsilon_0} \ln \frac{r}{a}$$

$$C = \frac{2\pi\epsilon_0}{\ln(b/a)} \quad \text{capacitance per unit length}$$



PROPORTIONAL COUNTER

AVALANCHE DEVELOPMENT:



CHARGE SIGNAL INDUCTION:

$$q^- = \frac{Q}{V_0} \int_a^{a+\lambda} \frac{dV}{dr} dr = -\frac{QC}{2\pi\epsilon_0} \ln \frac{a+\lambda}{a}$$

$$q^+ = \frac{Q}{V_0} \int_{a+\lambda}^b \frac{dV}{dr} dr = -\frac{QC}{2\pi\epsilon_0} \ln \frac{b}{a+\lambda}$$

$$q = q^- + q^+ = -\frac{QC}{2\pi\epsilon_0} \ln \frac{b}{a} = -Q$$

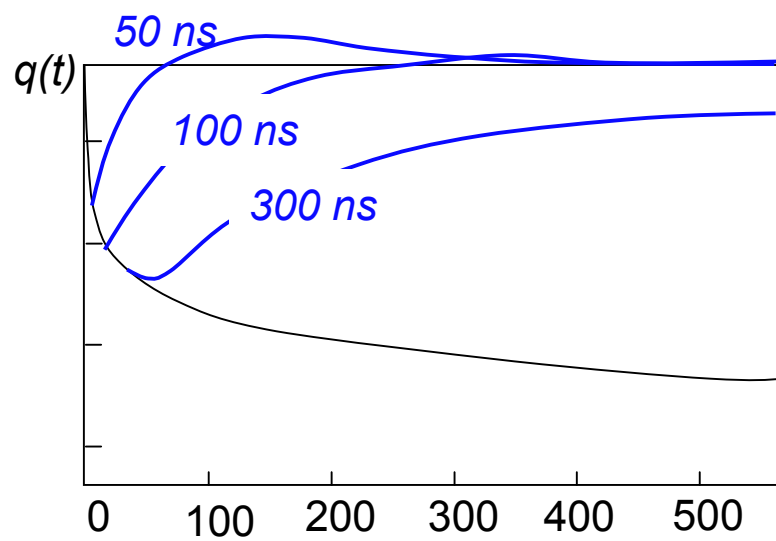
λ : distance of avalanche start

$$\frac{q^-}{q^+} = \frac{\ln(a+\lambda) - \ln a}{\ln b - \ln(a+\lambda)} \approx 0.01 \quad \text{99\% of signal due to positive ions}$$

$$q(t) = -\frac{QC}{2\pi\epsilon_0} \ln \left(1 + \frac{\mu^+ C V_0}{2\pi\epsilon_0 a^2} t \right) = -\frac{QC}{2\pi\epsilon_0} \ln \left(1 + \frac{t}{t_0} \right)$$

CHARGE SIGNAL: POSITIVE ION TAIL

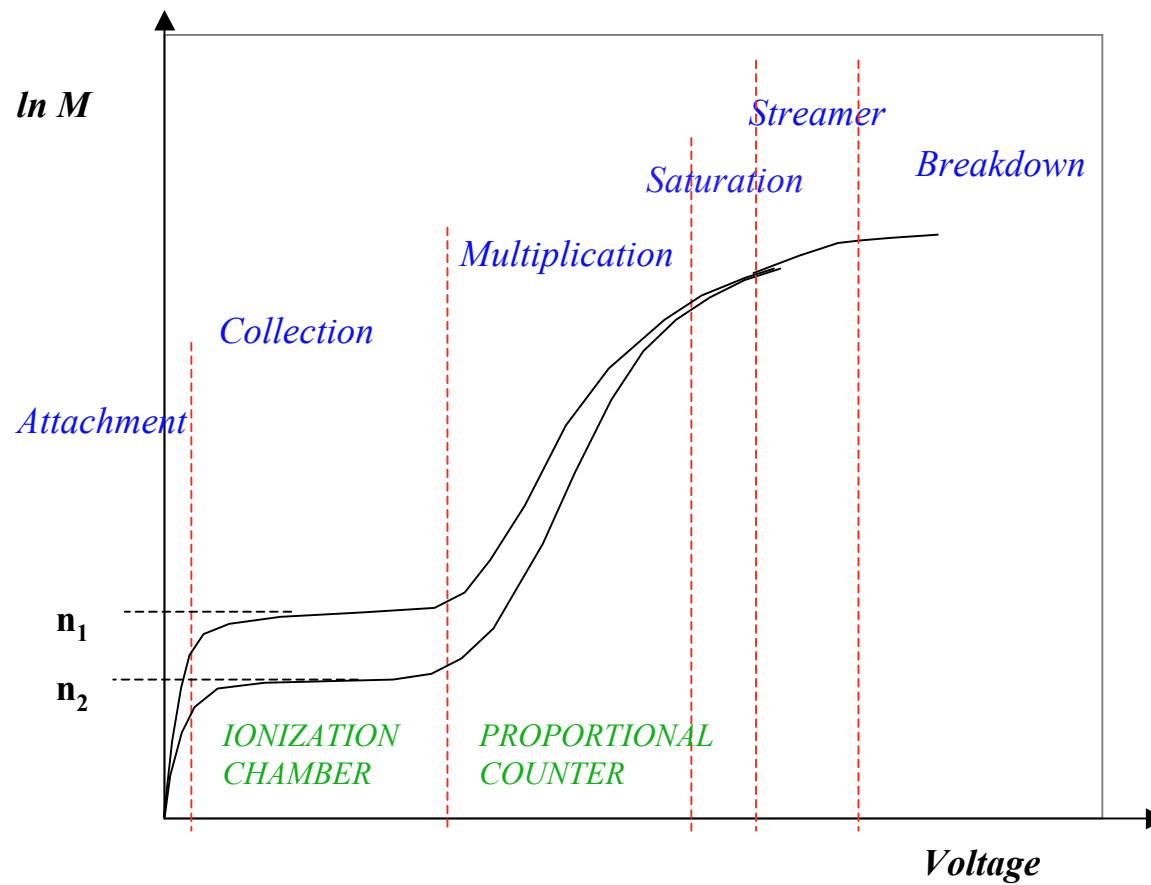
RC differentiation for faster response



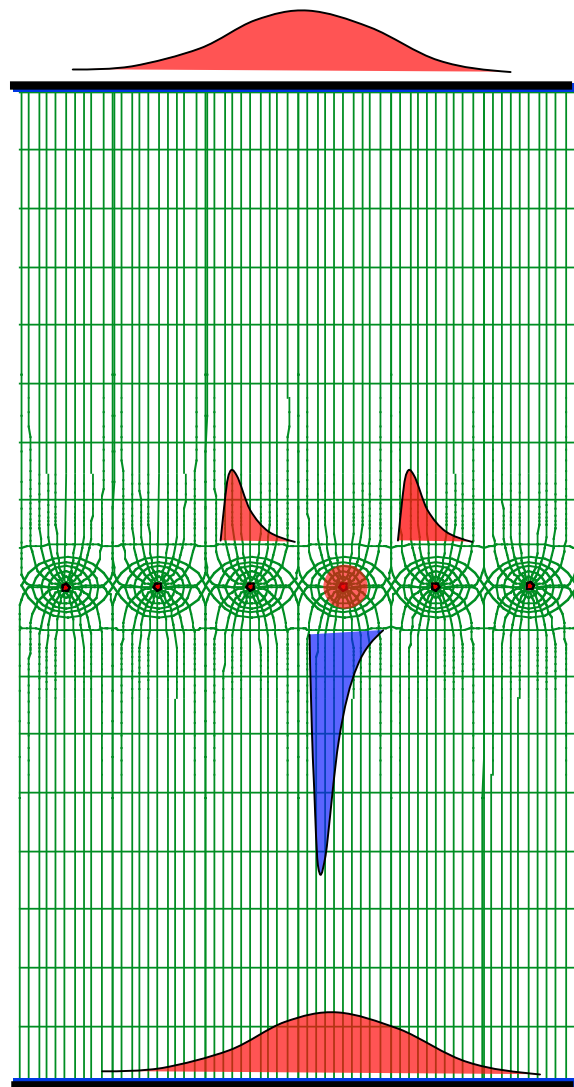
S. C. Curran and J. D. Craggs, Counting Tubes (Butterworth 1949)

F. Sauli, Principles of Operation of Multiwire Proportional and Drift Chambers (CERN 77-09)

PROPORTIONAL COUNTERS: OPERATING REGIMES



MULTIWIRE PROPRTIONAL CHAMBER



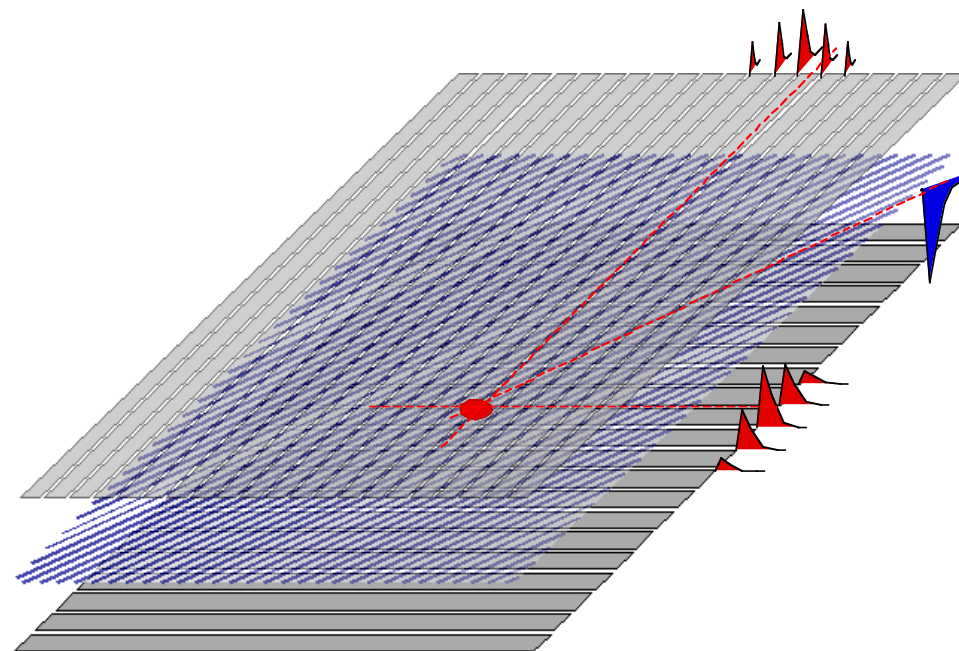
$-V_0$

TWO-DIMENSIONAL COORDINATE READOUT
Center of gravity of induced signals on cathodes

$$X = \sum \frac{X_i A_i(X)}{A(X)} \quad Y = \sum \frac{Y_i A_i(Y)}{A(Y)}$$

GND

$-V_0$

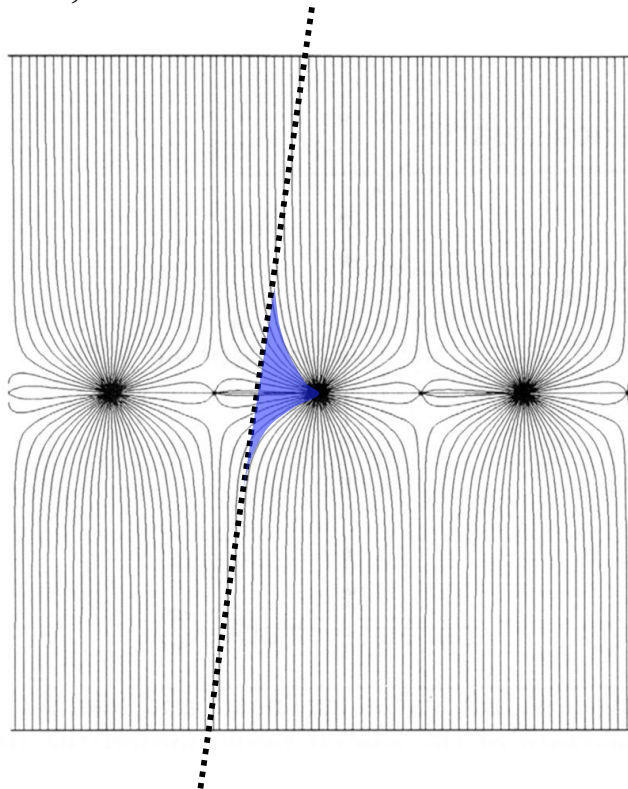


*G. Charpak et al,
Nucl. Instr. and Meth. 62(1968)235*

*G. Charpak and F. Sauli,
Nucl. Instr. and Methods 113(1973)381*

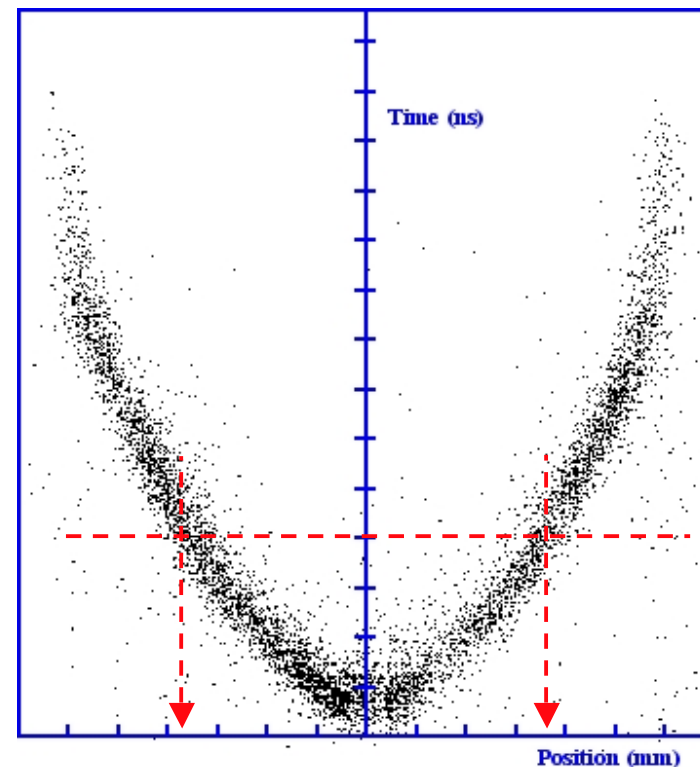
DRIFT CHAMBER

MWPC WITH A FIELD-SHAPING WIRE BETWEEN ANODES, TO AVOID LOW-FIELD REGIONS



*A. H. Walenta, J. Heintze and B. Scürlein,
Nucl. Instr. and Meth. 92(1971)373*

SPACE-TIME CORRELATION
(RIGHT-LEFT AMBIGUITY):



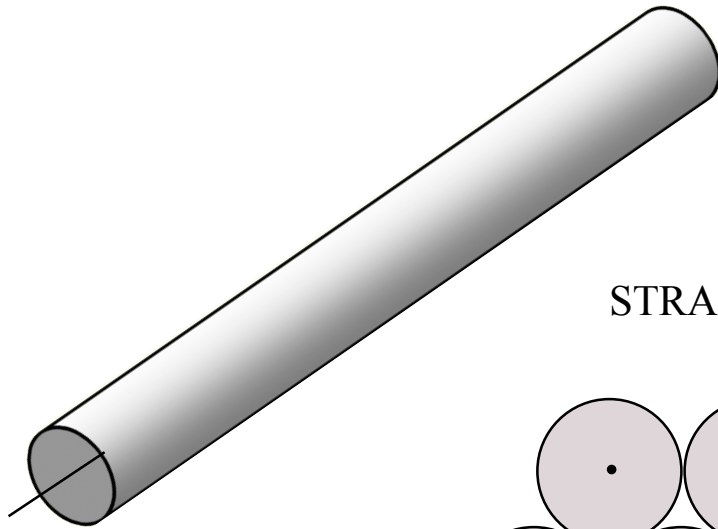
ELECTRIC FIELD AND DRIFT PROPERTIES CALCULATIONS: GARFIELD



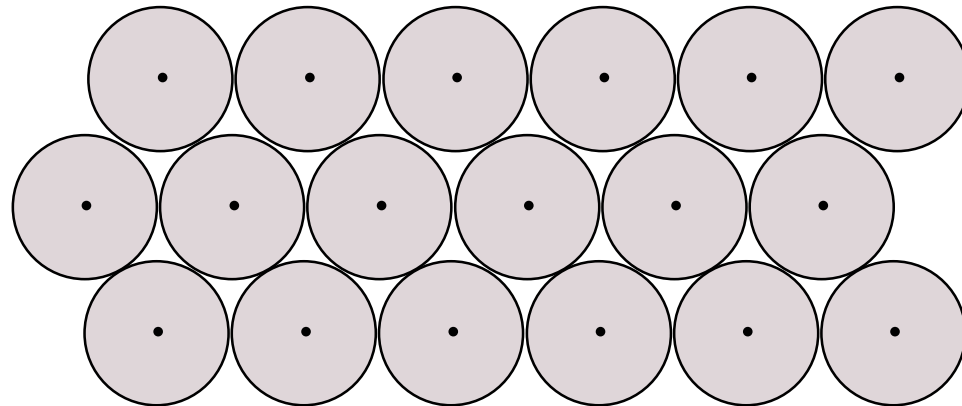
Rob Veenhof

LABORATORY: STRAWS AND DRIFT TUBES

SINGLE WIRE PROPORTIONAL COUNTERS



STRAWS ARRAYS:



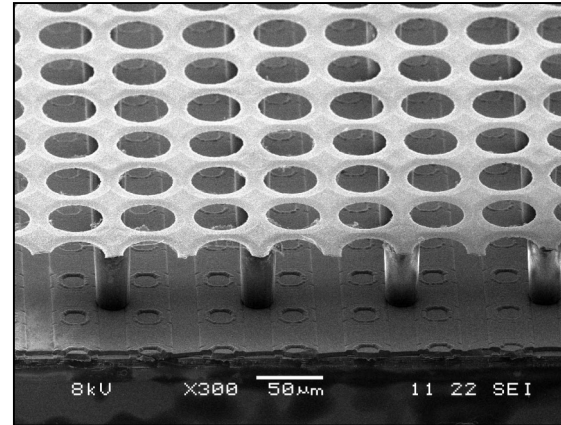
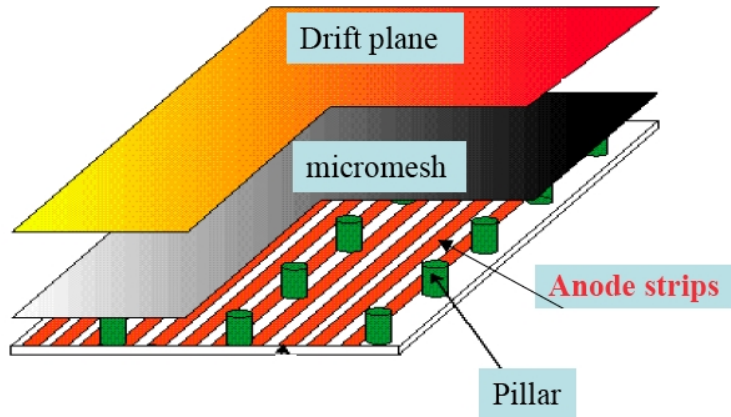
Anatoli Romaniouk: ATLAS Transition Radiation Tracker (TRT)

Hans Danielsson: NA62 Straw Detectors

Joerg Dubbert: ATLAS Monitored Drift Tubes (MDT)

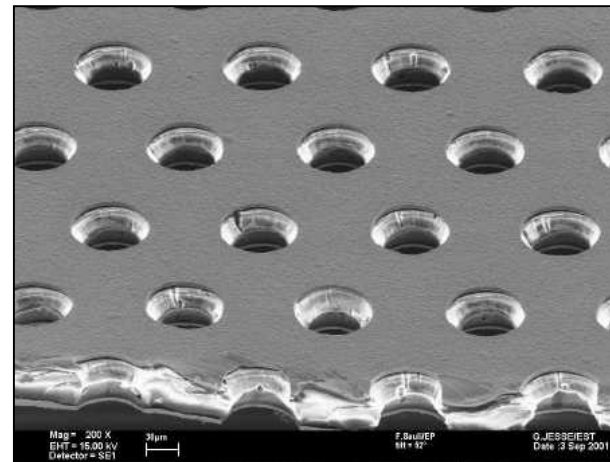
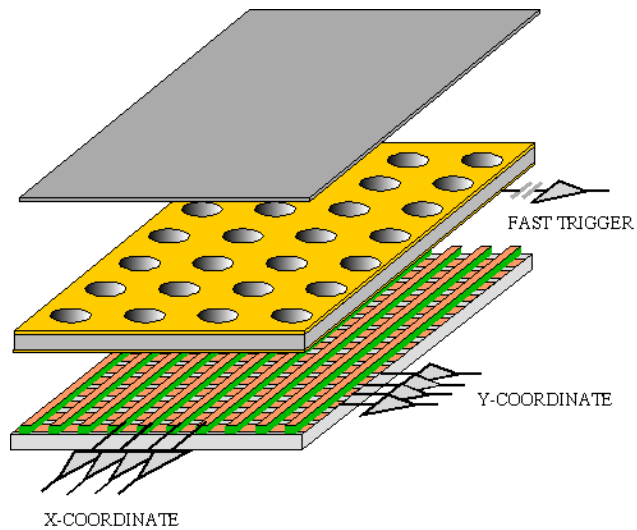
LABORATORY: MICROPATTERN GAS DETECTORS

MICROMEGAS and GRIDPIX



*Paul Colas
Harry van der Graaf*

GAS ELECTRON MULTIPLIER (GEM)



Gianni Bencivenni

AND NOW, PUT YOUR HANDS ON (CAREFULLY)!

