

# *Broken symmetry*

*I. Mass and interaction range*

*II. Spontaneous breaking of a global symmetry*

*III. The BEH mechanism*

*IV. The quest for unified laws of nature*

*24 February 2011, CERN*

# *I. Mass and interaction range*

## *Relativity: massive and massless particles*

*$c$  is the maximal causal velocity*

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*The mass  $m$  of a particle of rest mass  $m_0$  increases with its velocity  $v$*

# I. Mass and interaction range

## Relativity: massive and massless particles

$c$  is the maximal causal velocity



The mass  $m$  of a particle of rest mass  $m_0$  increases with its velocity  $v$

$$E = mc^2 = \frac{m_0 c^2}{\sqrt{1 - \frac{v^2}{c^2}}}$$



$$m_0 \neq 0$$

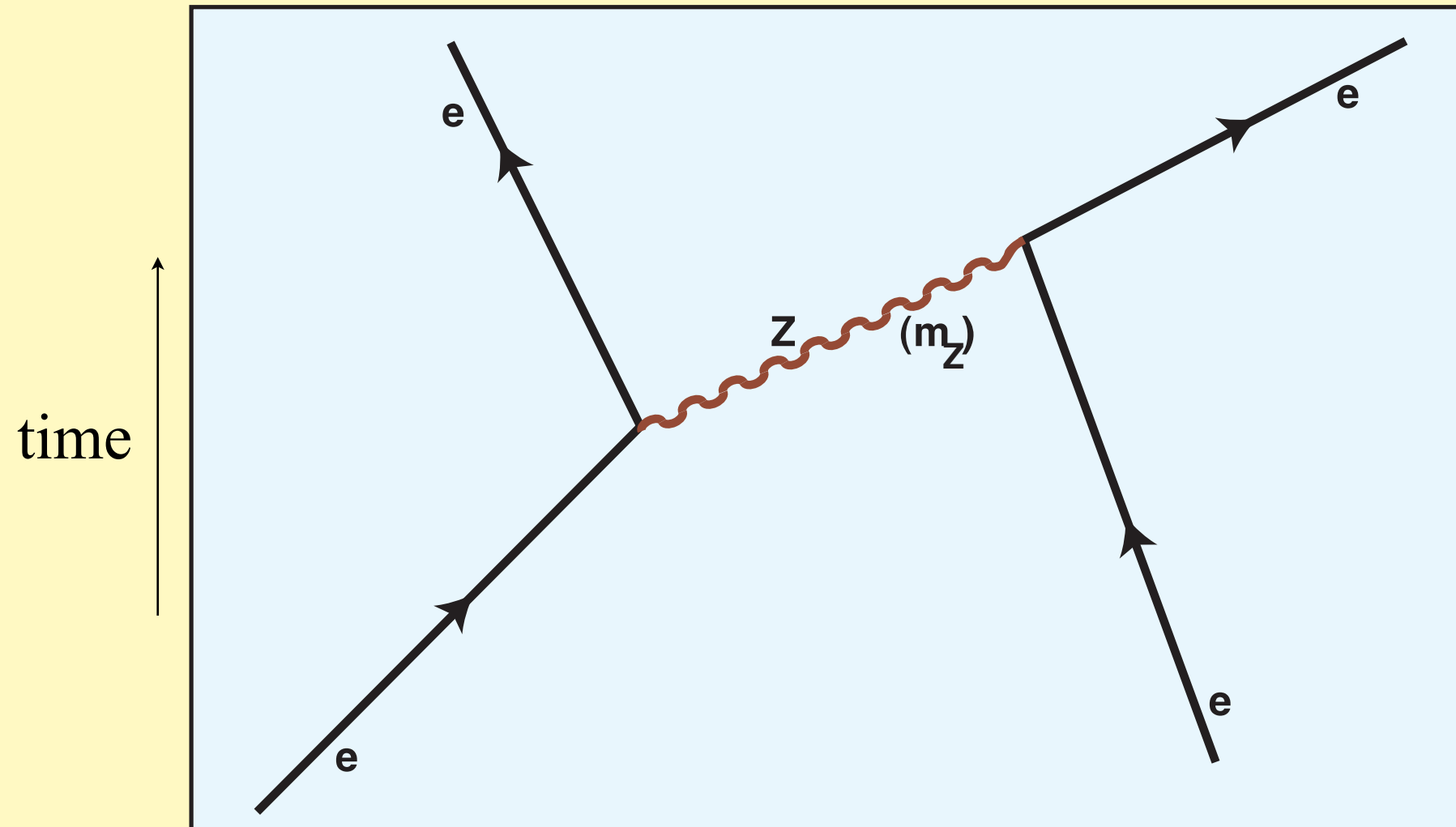
$$m_0 = 0$$



The particle never reaches the velocity  $c$  | The particle always moves with velocity  $c$

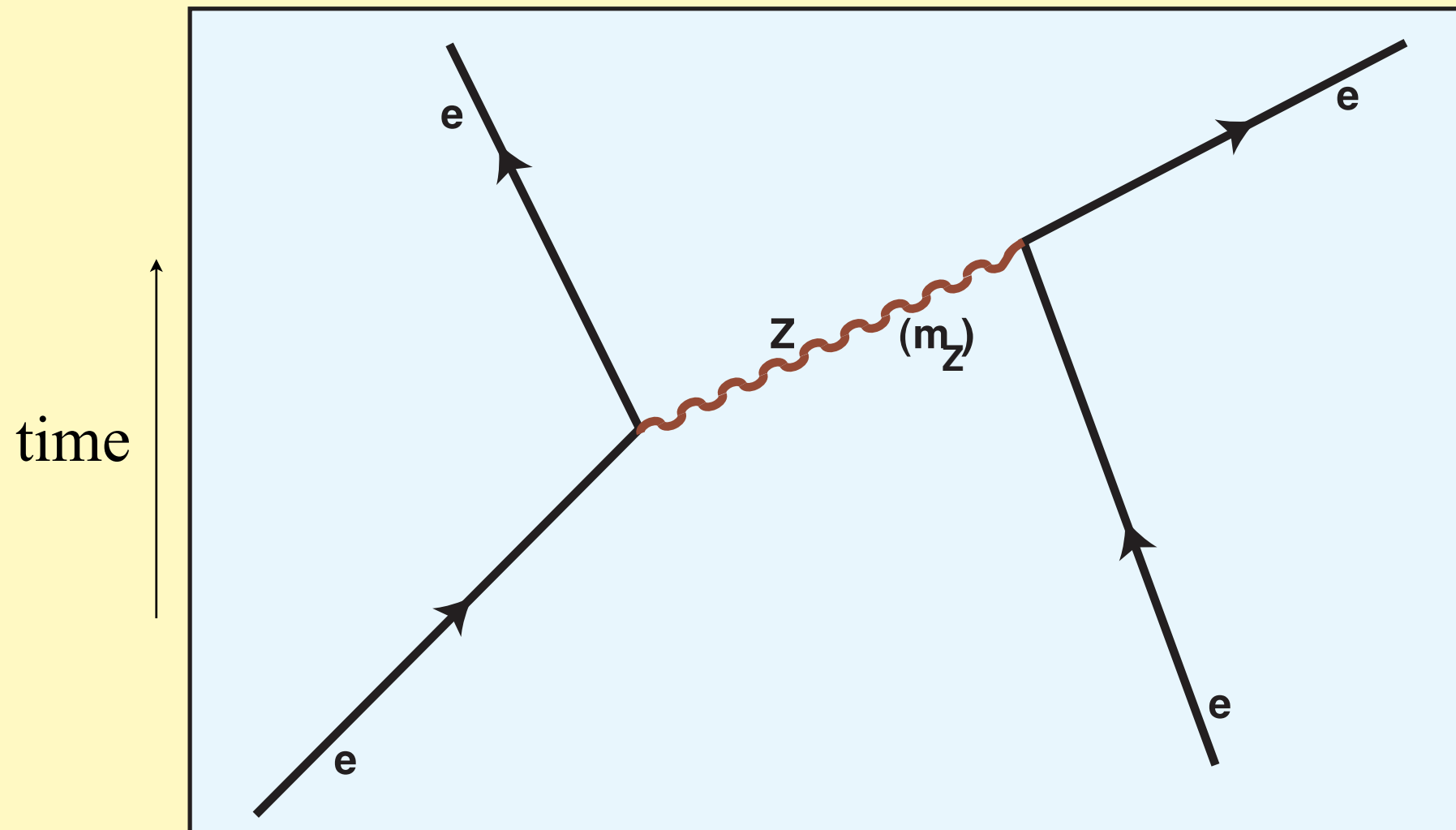
# *Quantum mechanics: long and short range forces*

*Interactions between particles are described by particle exchange*



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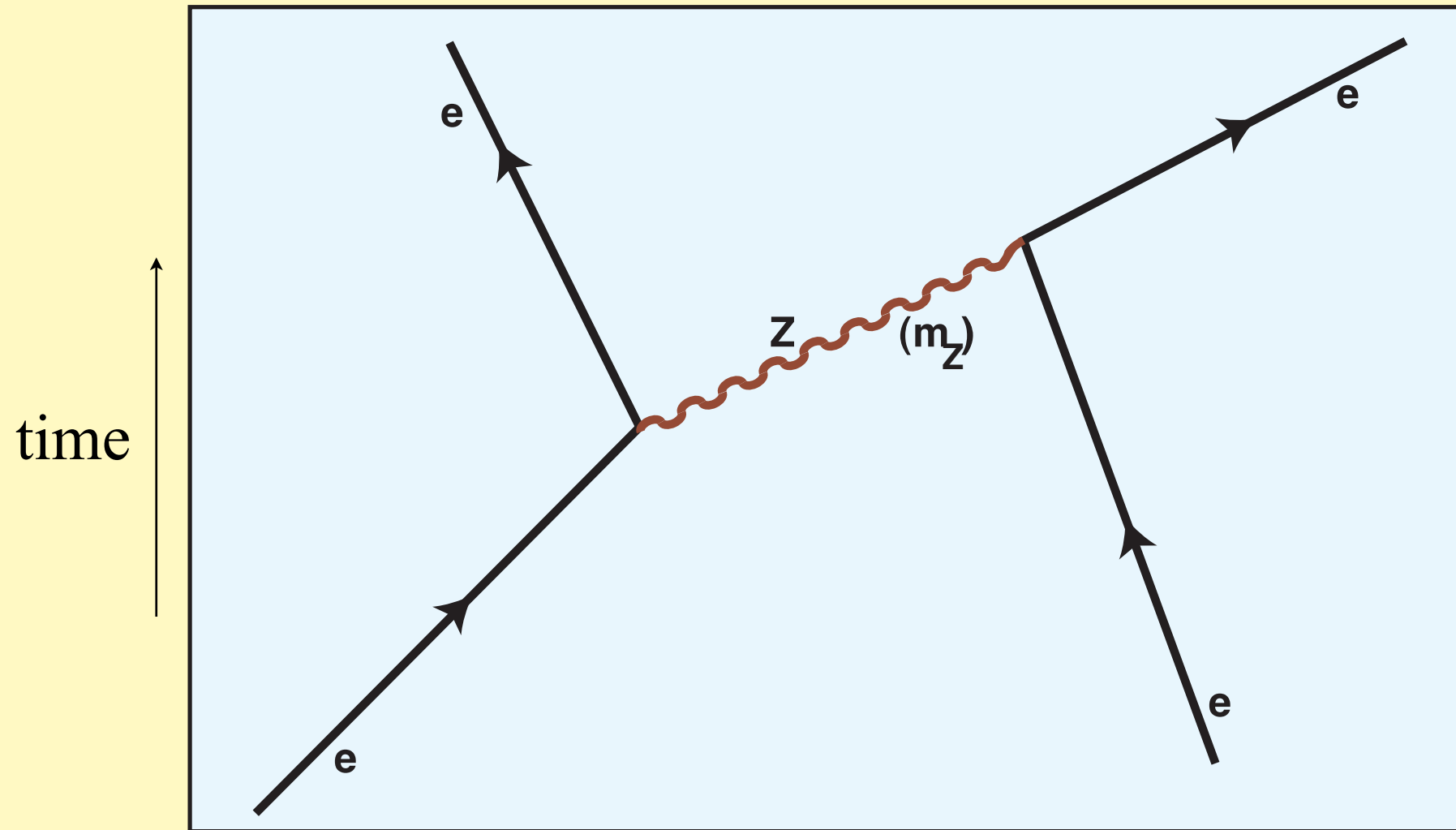
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*Energy is conserved in the limit of large time intervals*

# *Quantum mechanics: long and short range forces*

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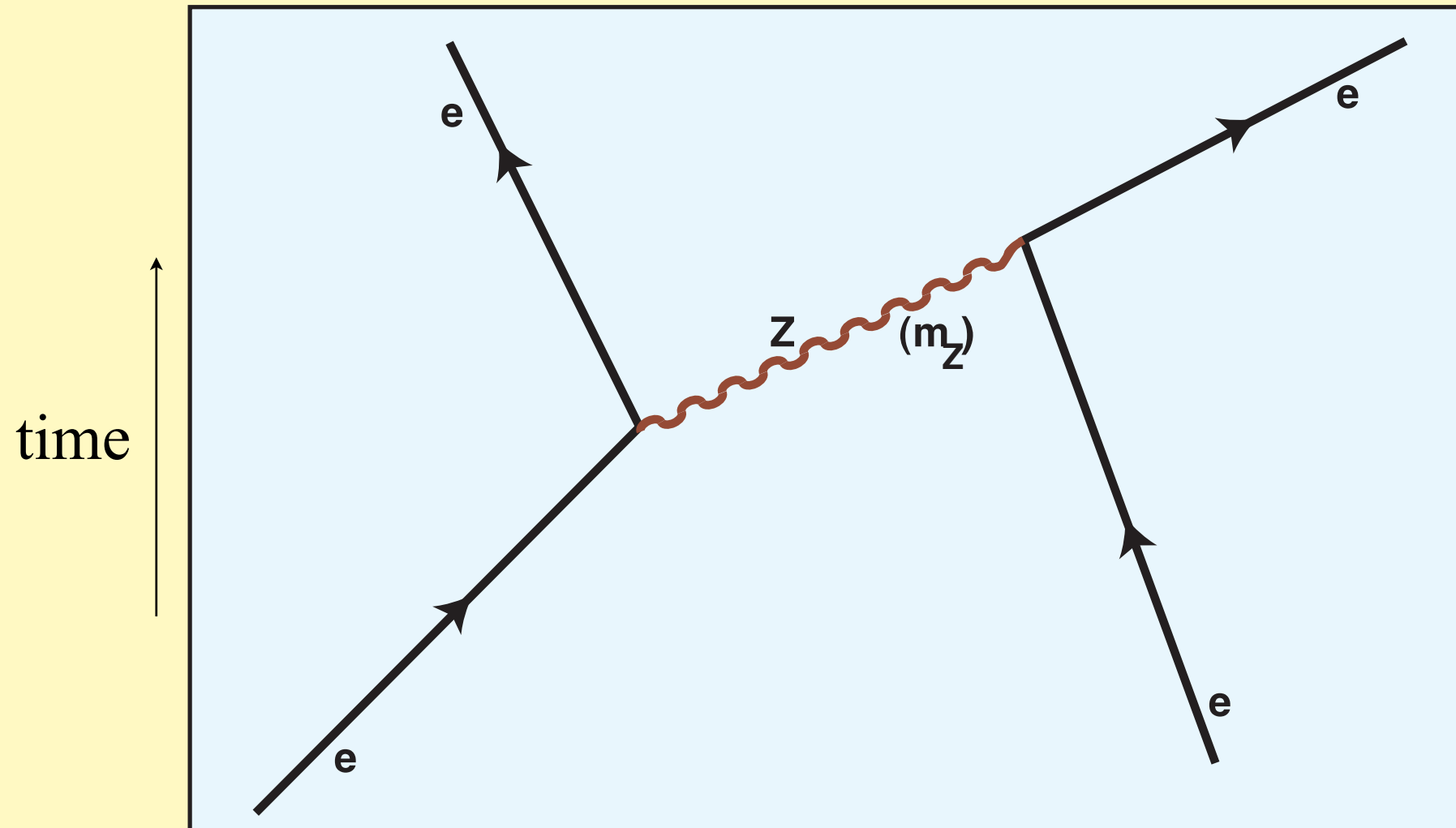
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# *Quantum mechanics: long and short range forces*

*Interactions between particles are described by particle exchange*



*Energy is conserved in the limit of large time intervals*



*The range of the interaction increases when the Z mass decreases*

*Massless particle exchange generates long range forces*

*Massive particle exchange generates short range forces*



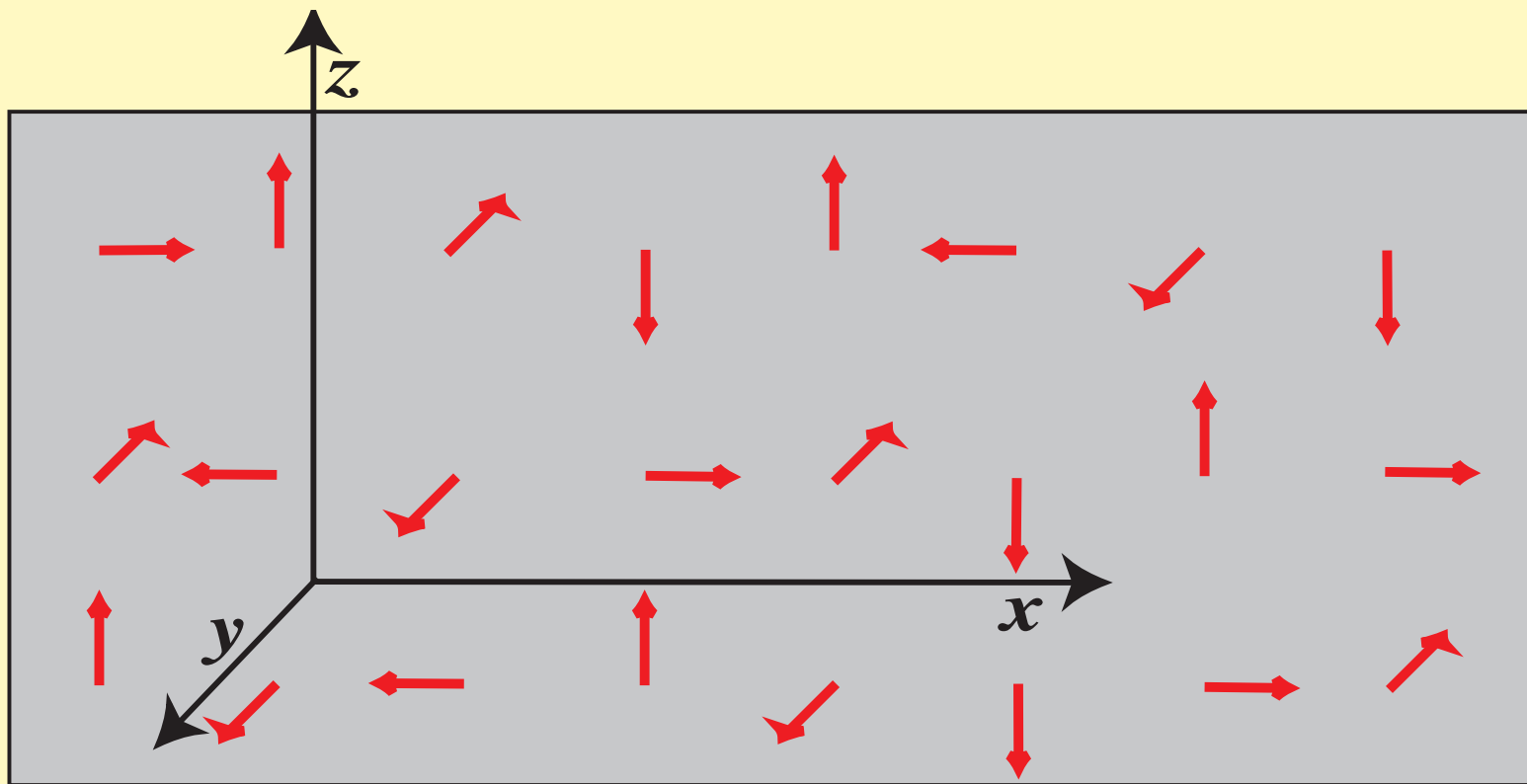
## *II. Spontaneous breaking of a global symmetry*



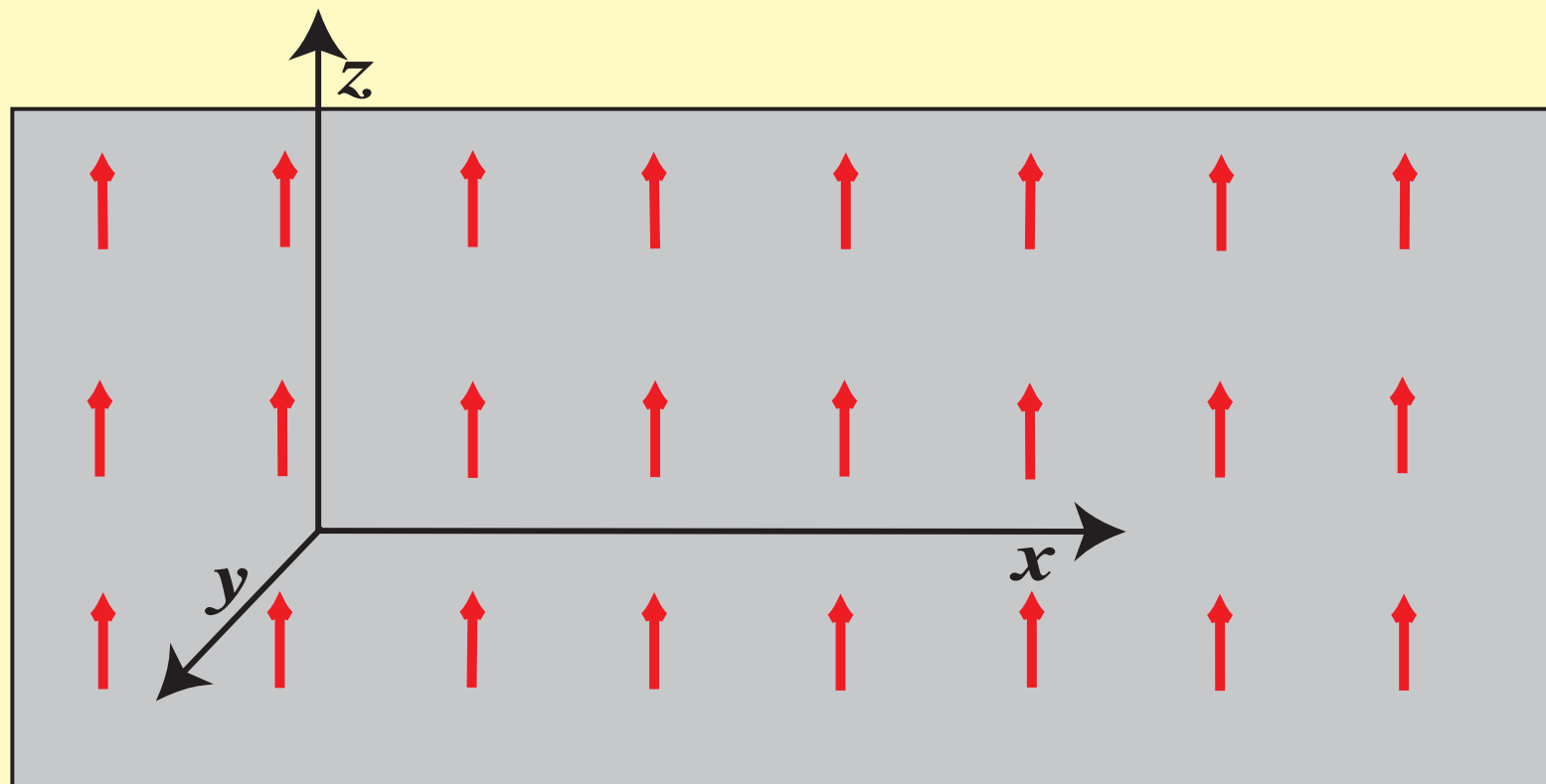
# 1. Spontaneous symmetry breaking in phase transitions

L.D. Landau, Phys. Z. Sowjet. 11 (1937) 26 [JETP 7 (1937) 19].

## Ferromagnetism : the phase transition

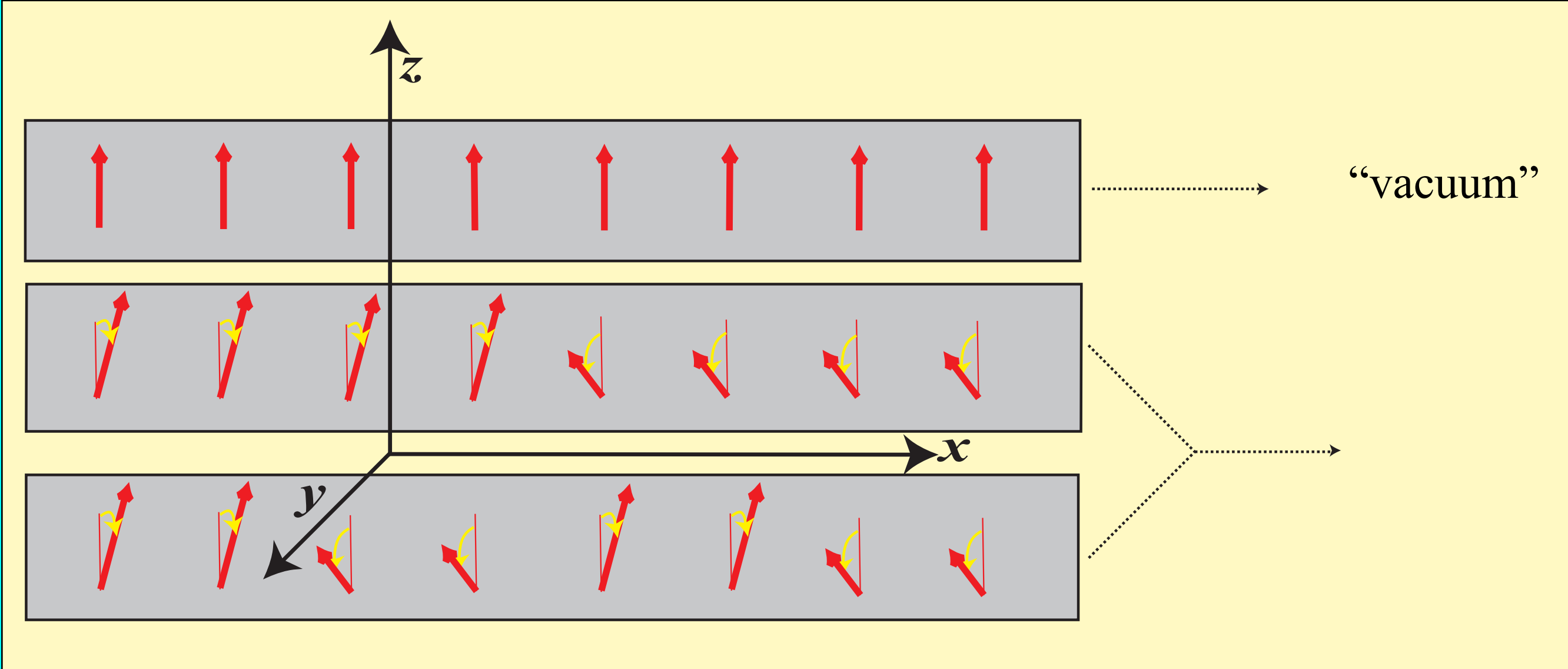


Disordered phase at high temperature

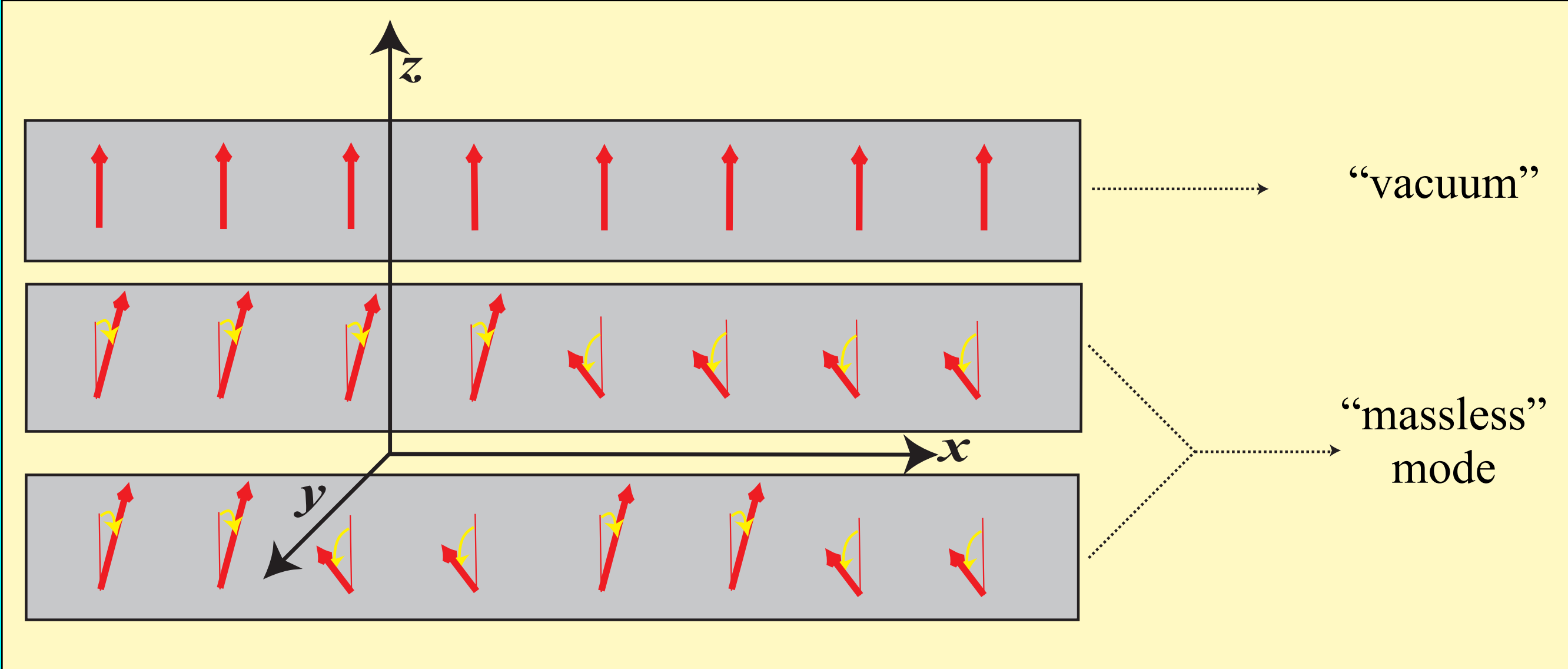


Ordered phase at low temperature

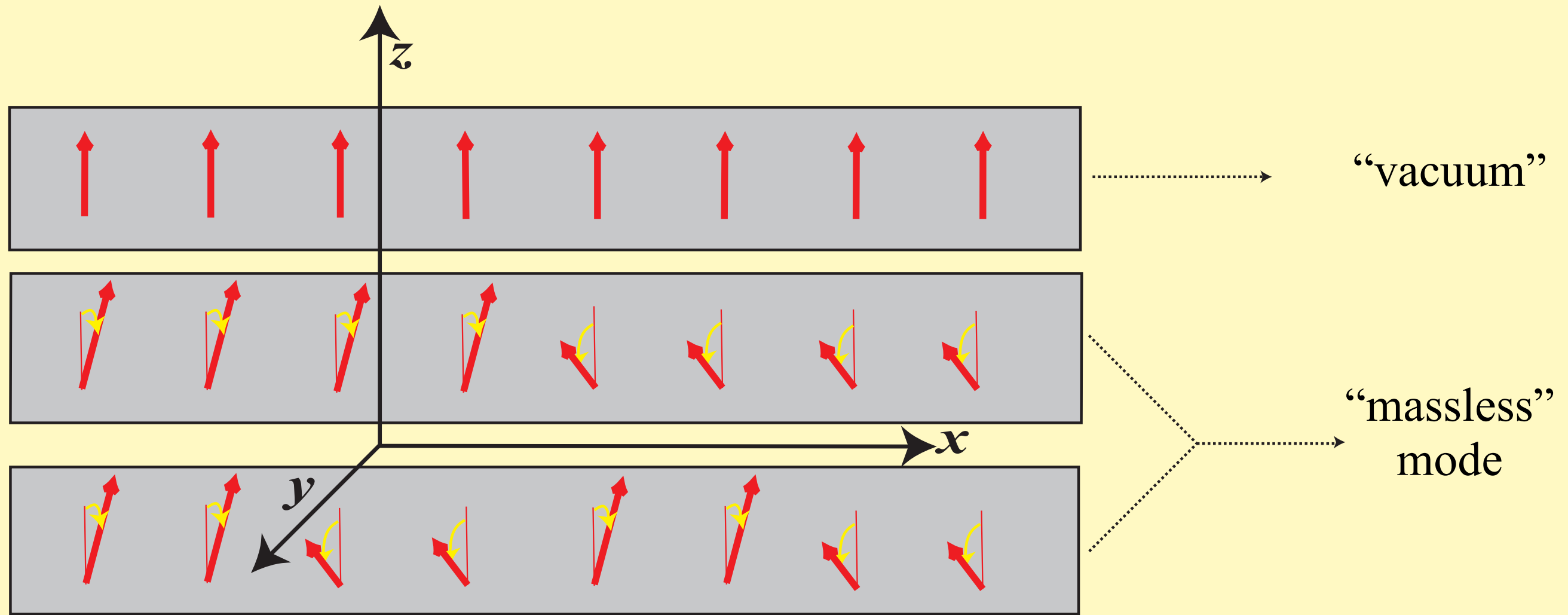
# *Ferromagnetism : the “massless” boson*



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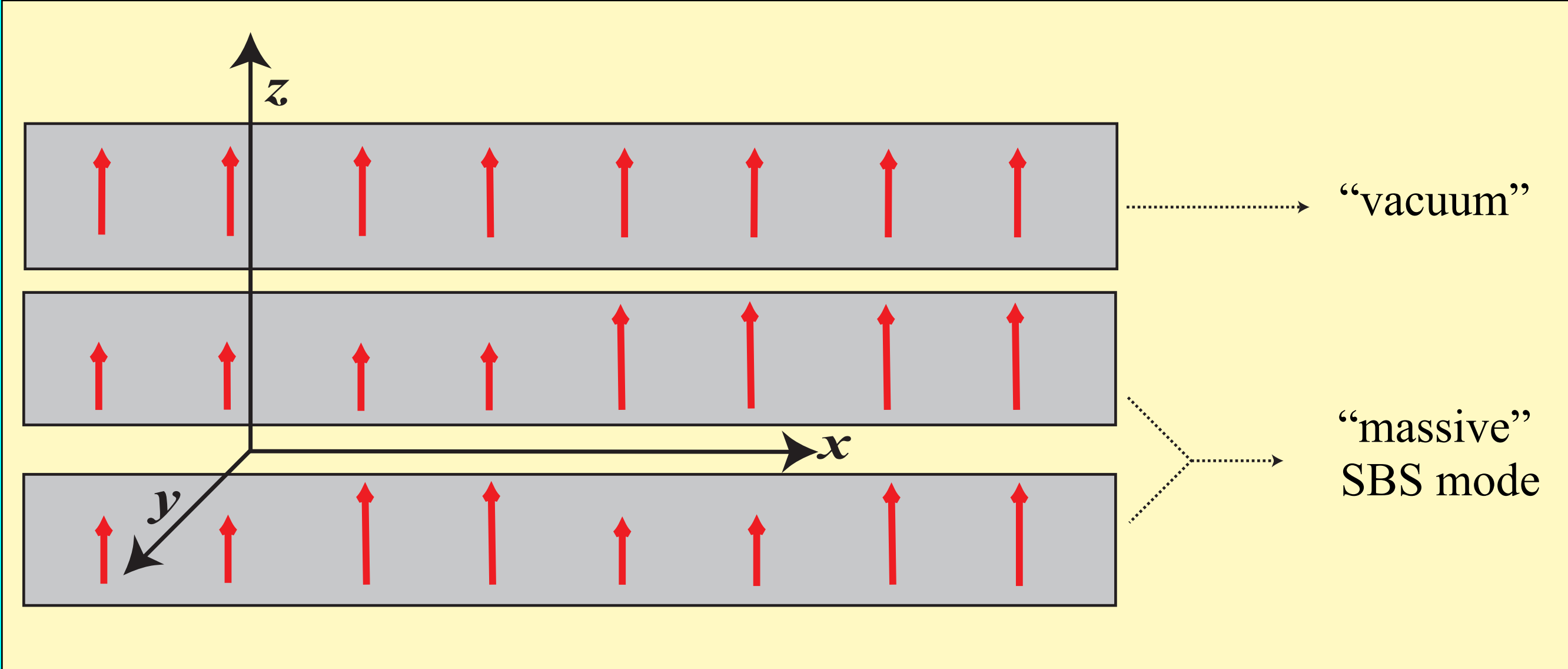


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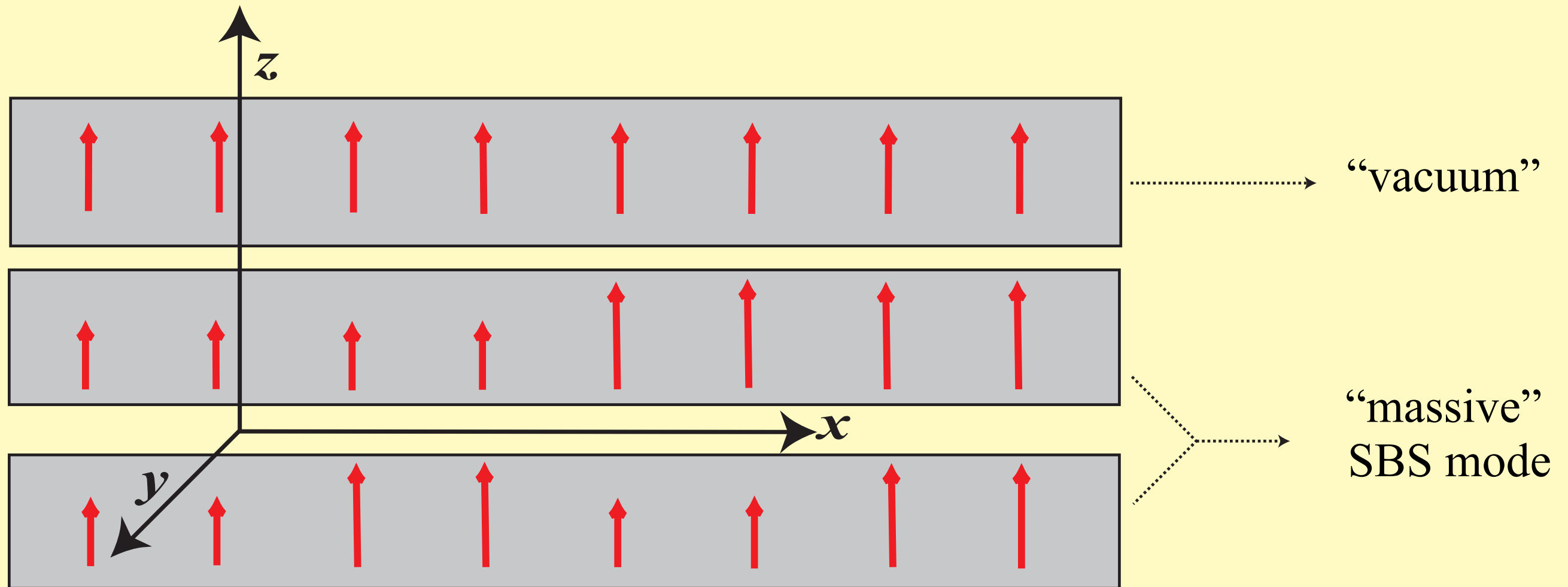


*The “massless” mode characterizes a **continuous** SBS  
It is the ancestor of the massless Nambu-Goldstone boson*

# *Ferromagnetism : the “massive” SBS boson*



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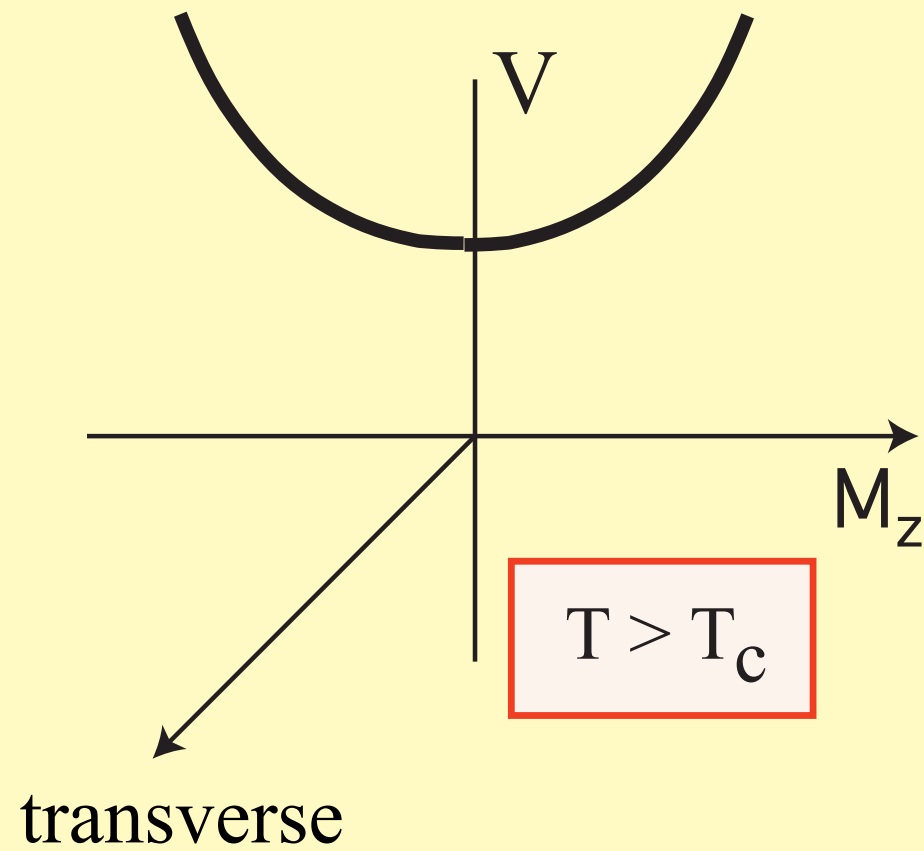


*The “massive” SBS mode measures the rigidity of the SBS phase*

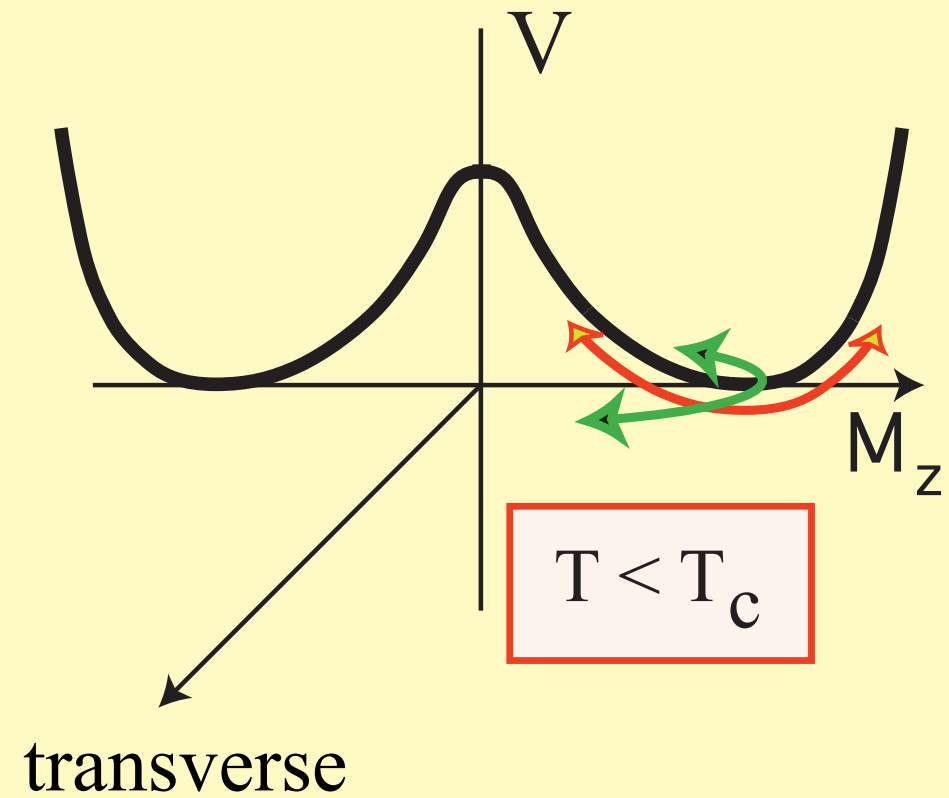
*It is the ancestor of the massive SBS scalar boson*

# Ferromagnetism : the quantitative description

$$V = \lim_{N \rightarrow \infty} G / N$$



$$\vec{M} = 0$$

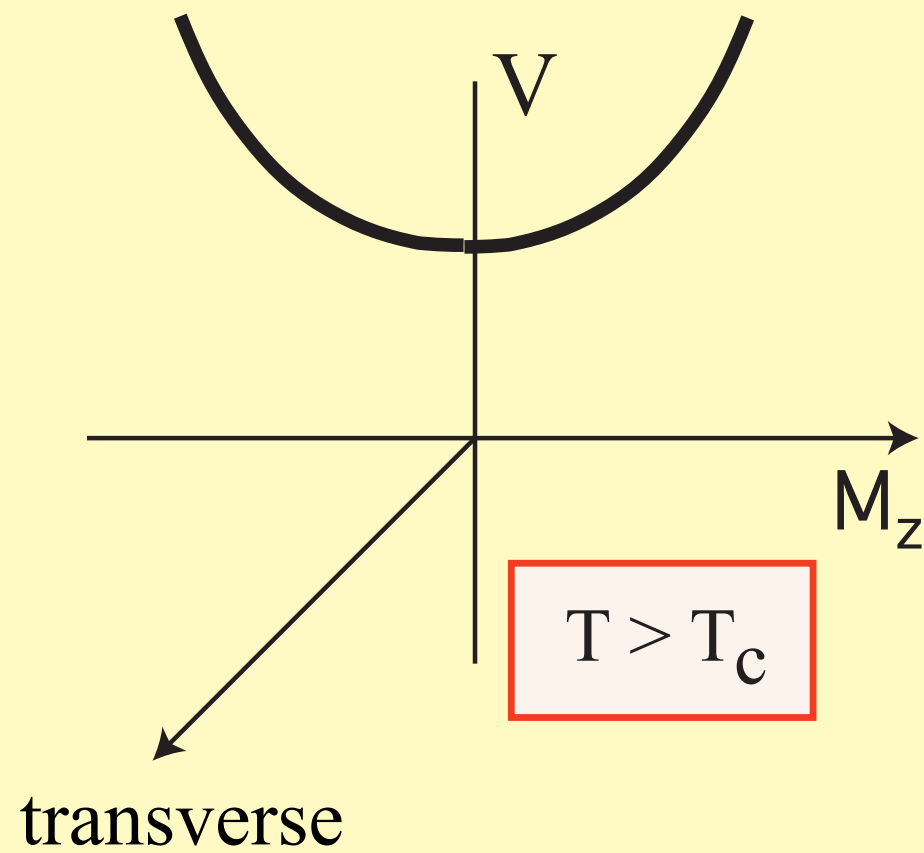


$\vec{M} \neq 0$   
"massless" mode      "massive" mode

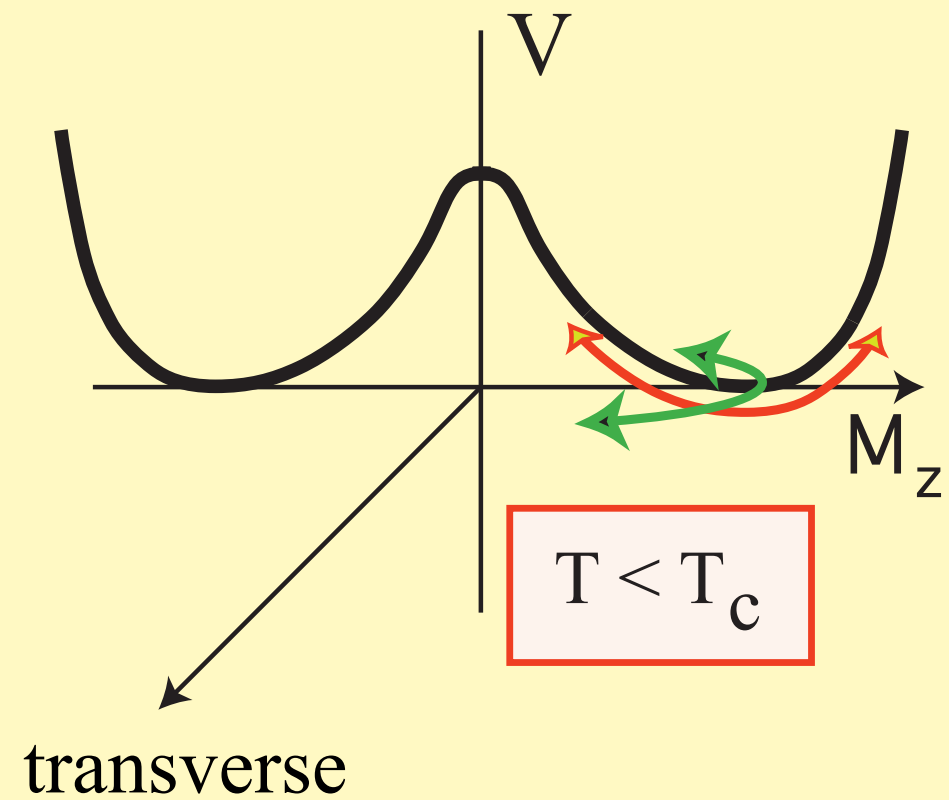


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“massless” mode

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## Superconductivity ?

P.W. Anderson, Phys. Rev. **112** (1958) 1900; Y. Nambu, Phys.Rev. **117** (1960) 648.

## 2. *Spontaneous symmetry breaking of the vacuum*

Y. Nambu, Phys. Rev. Lett. **4** (1960) 380; Y. Nambu and G. Jona-Lasinio, Phys. Rev. **122** (1961) 345, Phys. Rev. **124** (1961) 246;  
J. Goldstone, Il Nuovo Cimento **19** (1961) 154; J. Goldstone, A. Salam and S. Weinberg, Phys. Rev. **127** (1962) 965.

### *Chiral symmetry breaking*

*Massless fermions*  $\equiv \{ \nu_R \ \nu_L \} \longrightarrow$  (chiral)  $U(1)$  invariance

*Chiral invariant interactions preserve masslessness*

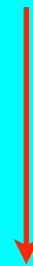
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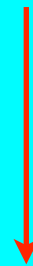
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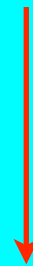
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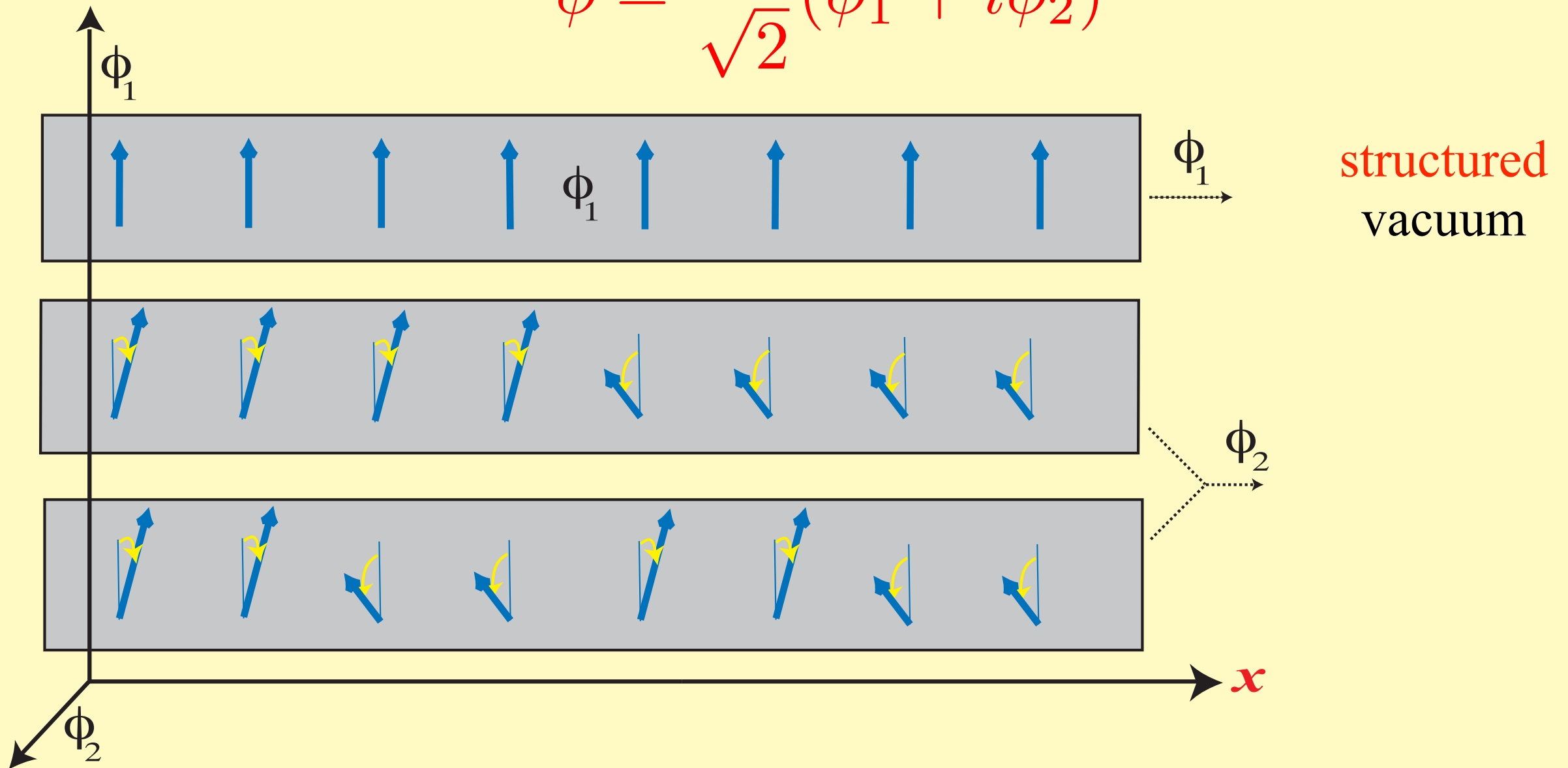
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*massive SBS scalar boson*

# A simple model : the Nambu-Goldstone boson

$U(1)$  symmetry  $\phi \rightarrow e^{i\alpha} \phi$  of a complex scalar is broken by  $|\phi| \neq 0$

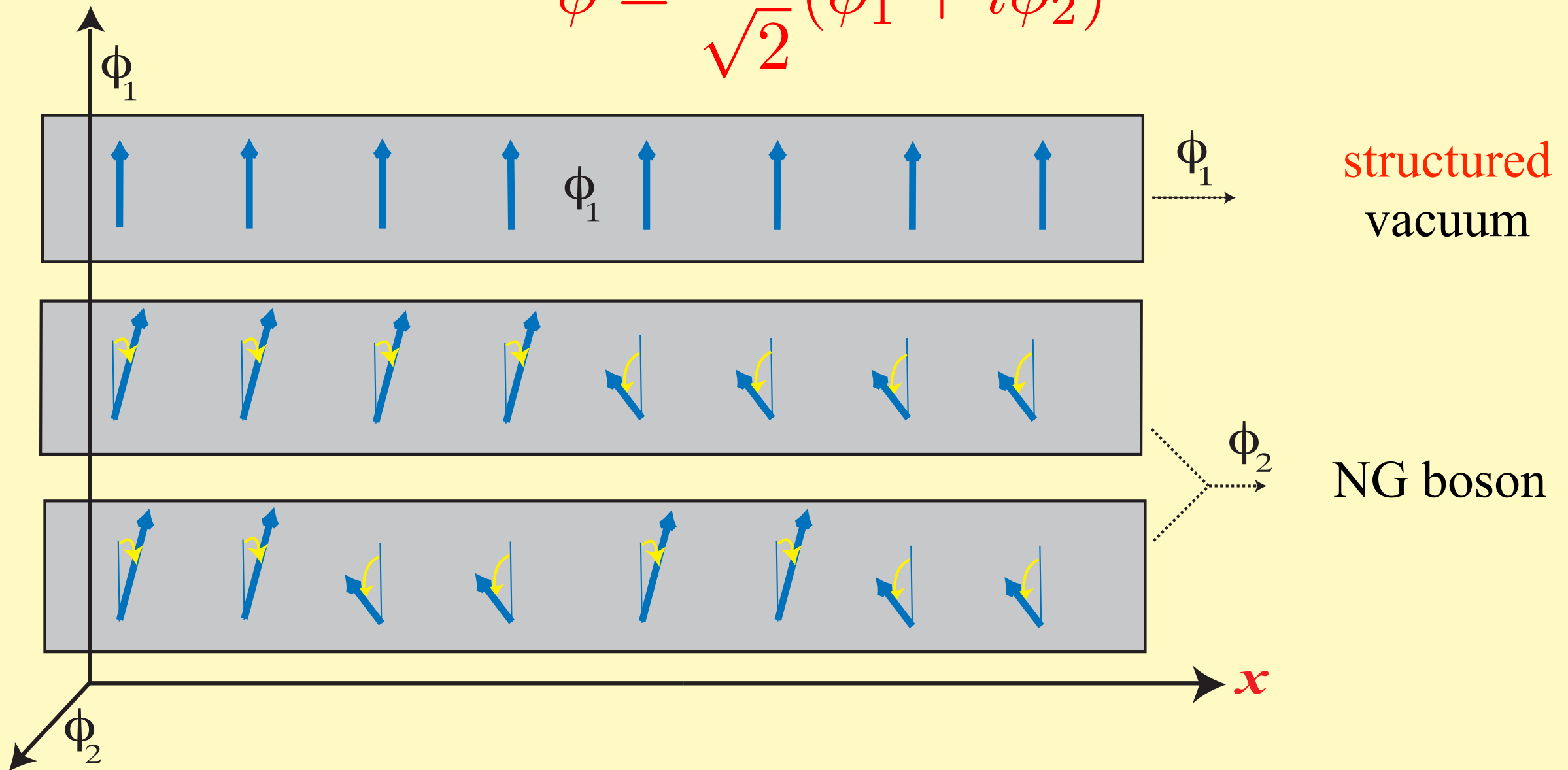
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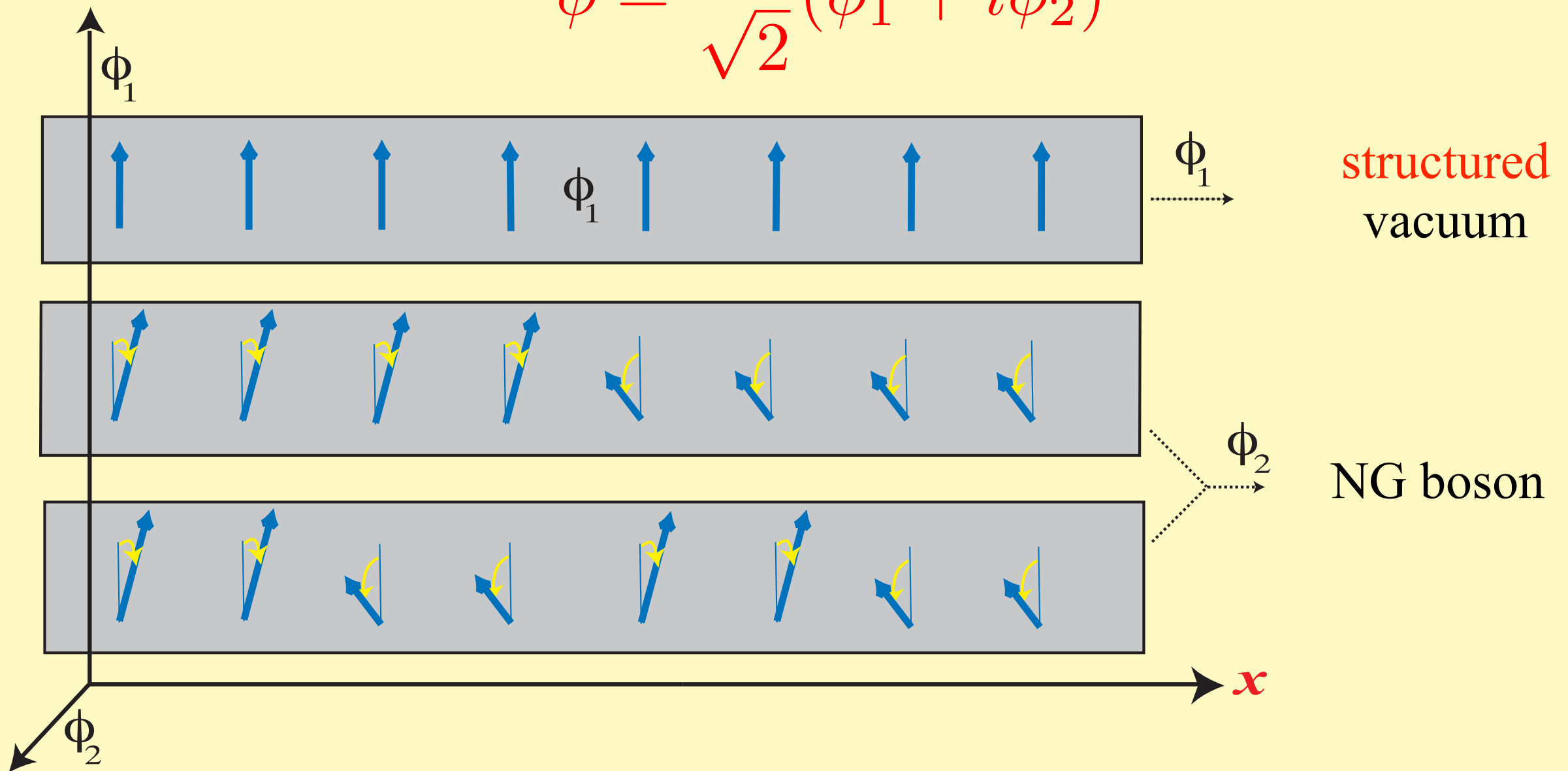
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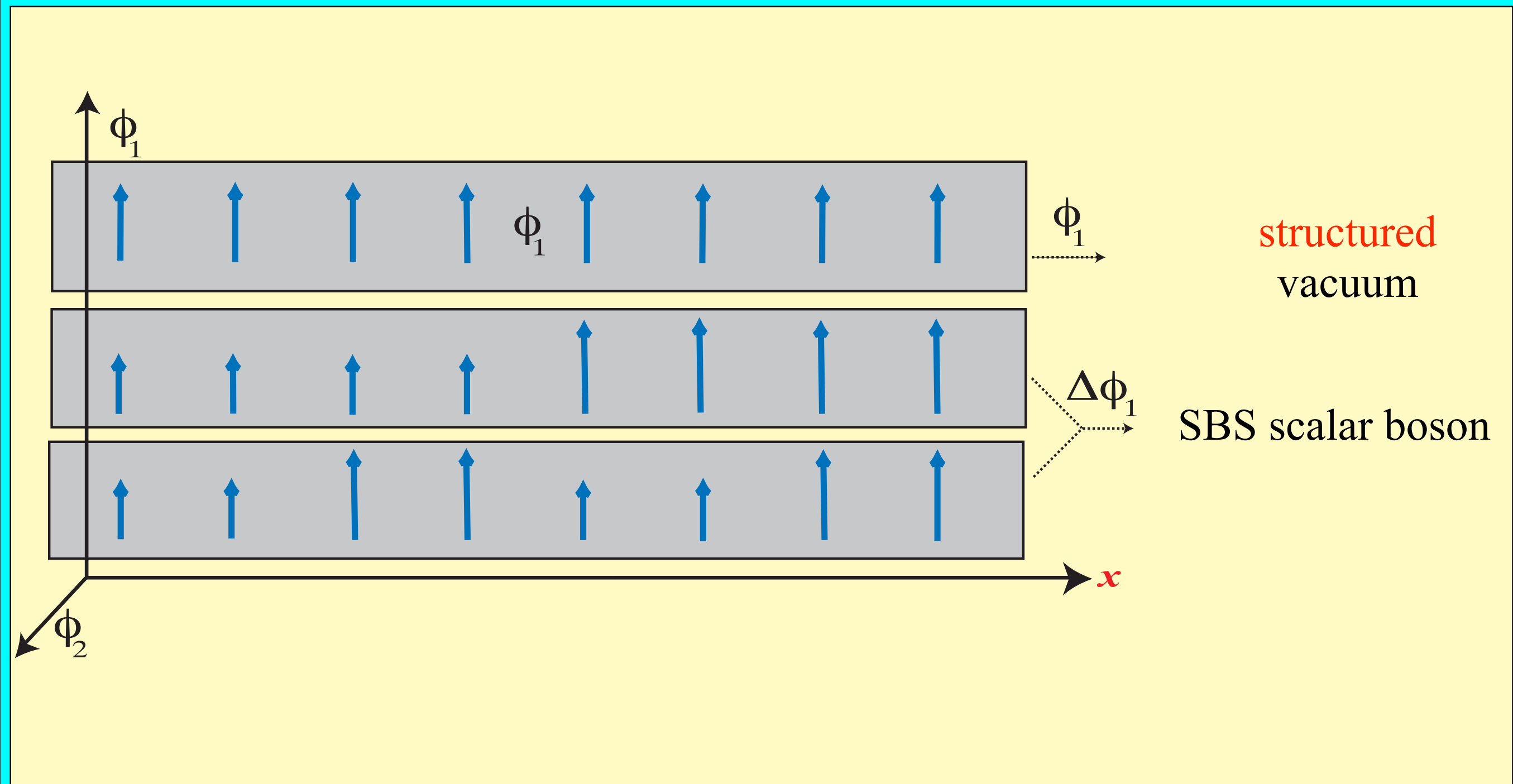
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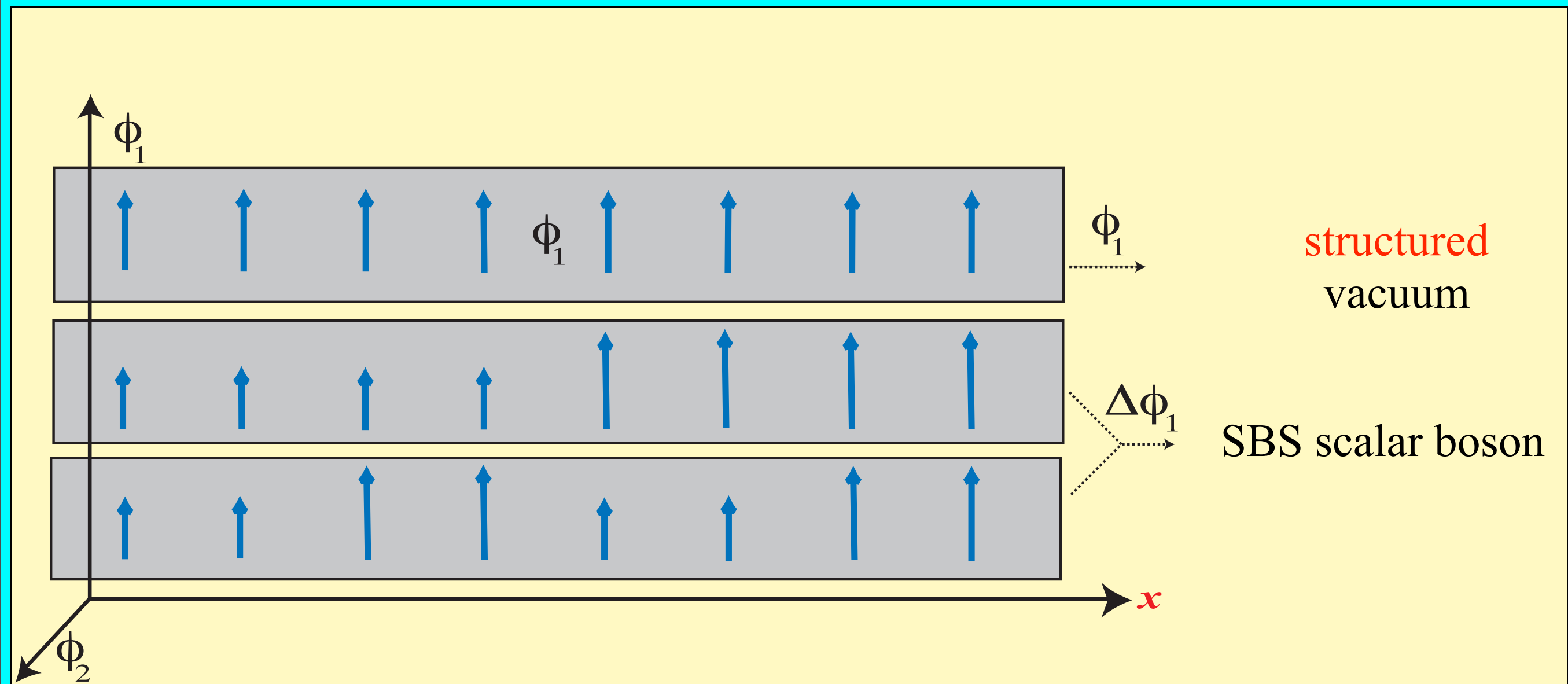
The massless NG boson characterizes a *continuous* SBS



# *A simple model : the SBS scalar boson*



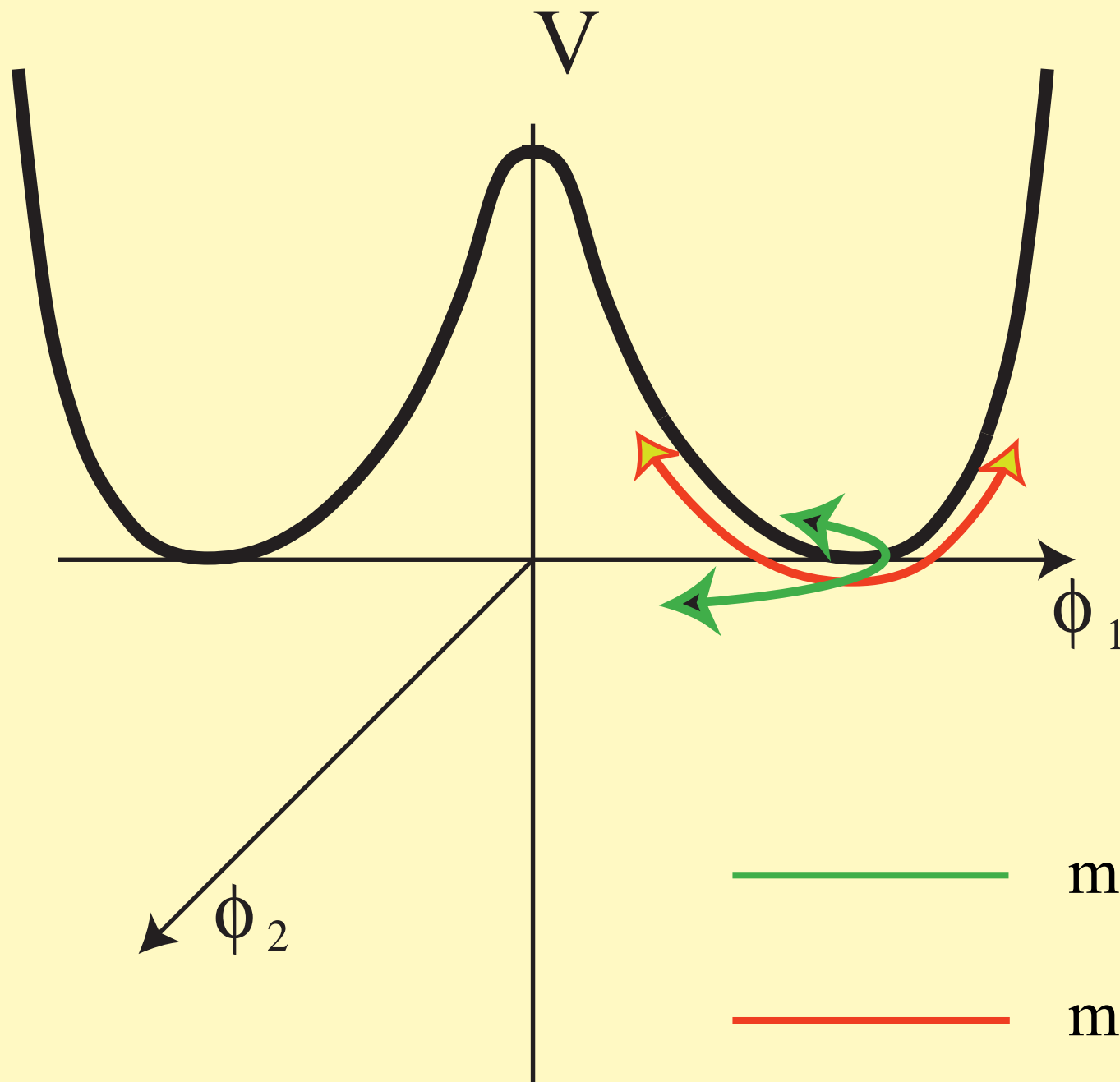
# *A simple model : the SBS scalar boson*



*The massive SBS scalar boson measures the rigidity of the vacuum*

# *A simple model : the quantitative description*

$$\mathcal{L} = \partial^\mu \phi^* \partial_\mu \phi - V(\phi^* \phi) \quad V(\phi^* \phi) = -\mu^2 \phi^* \phi + \lambda(\phi^* \phi)^2$$



$$\langle \phi_2 \rangle = 0$$

$$\langle \phi_1 \rangle \neq 0$$

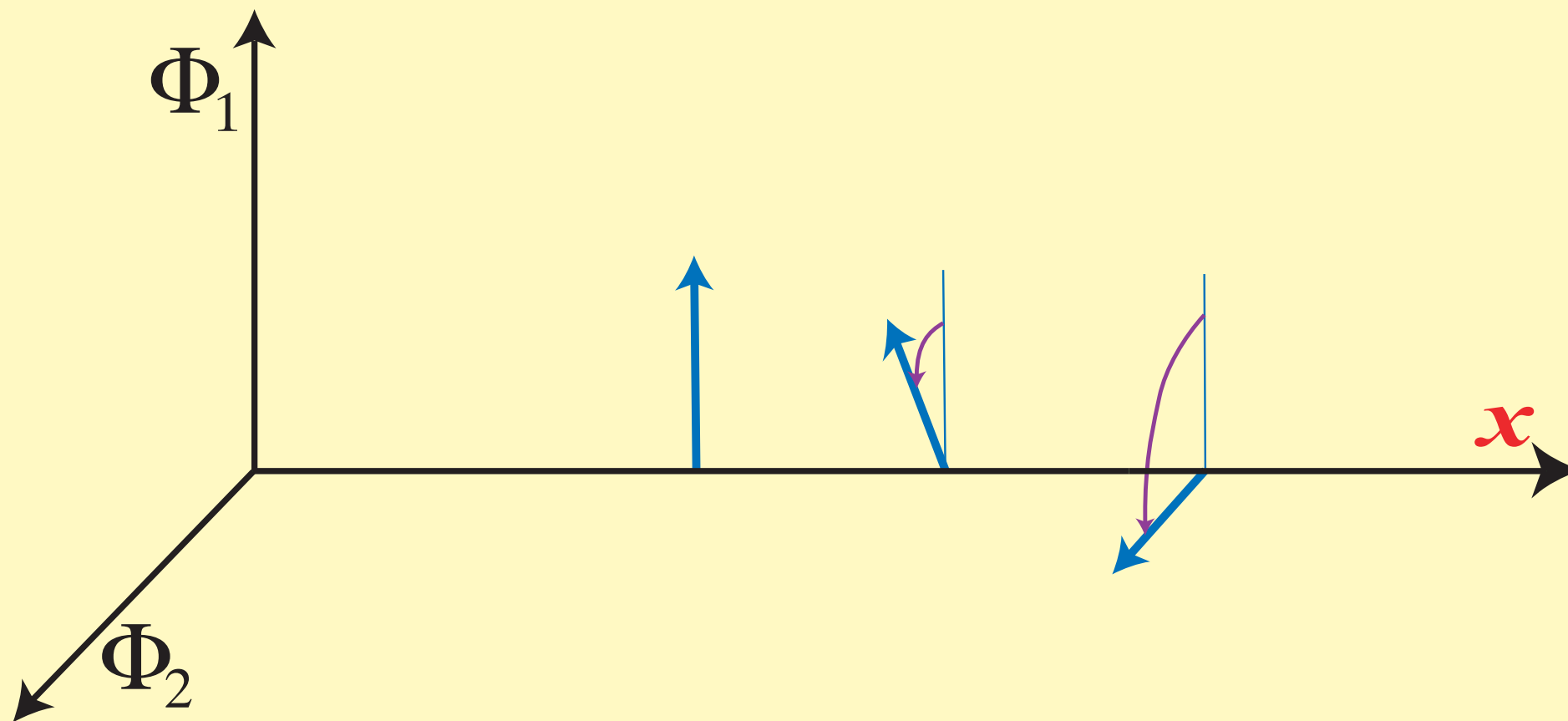
— massless NG boson

— massive SBS boson

### *III. The BEH mechanism*

#### *1. From global to local symmetry*

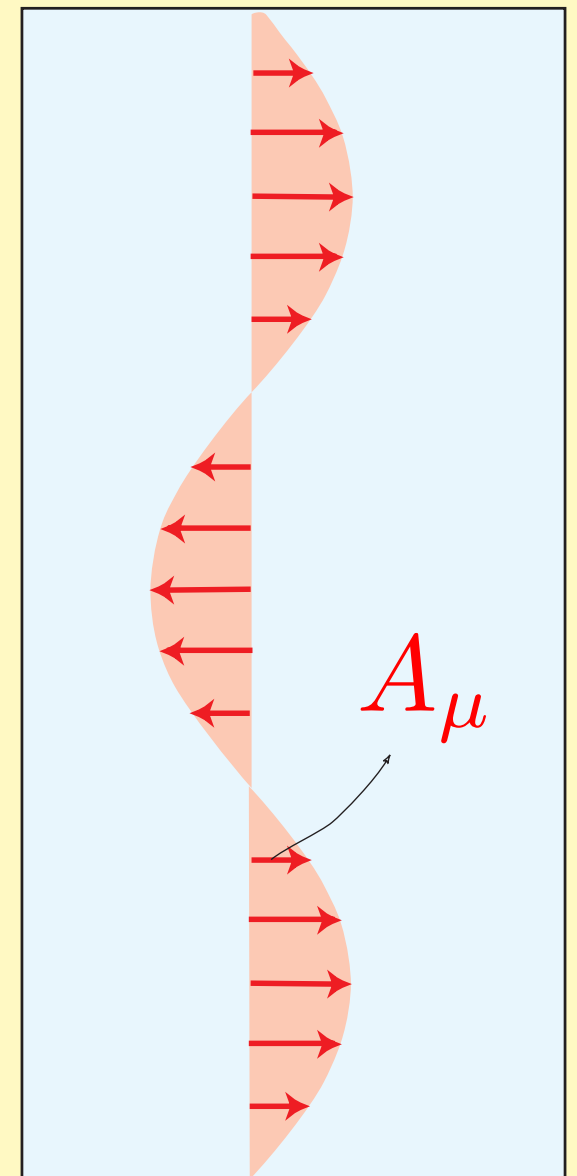
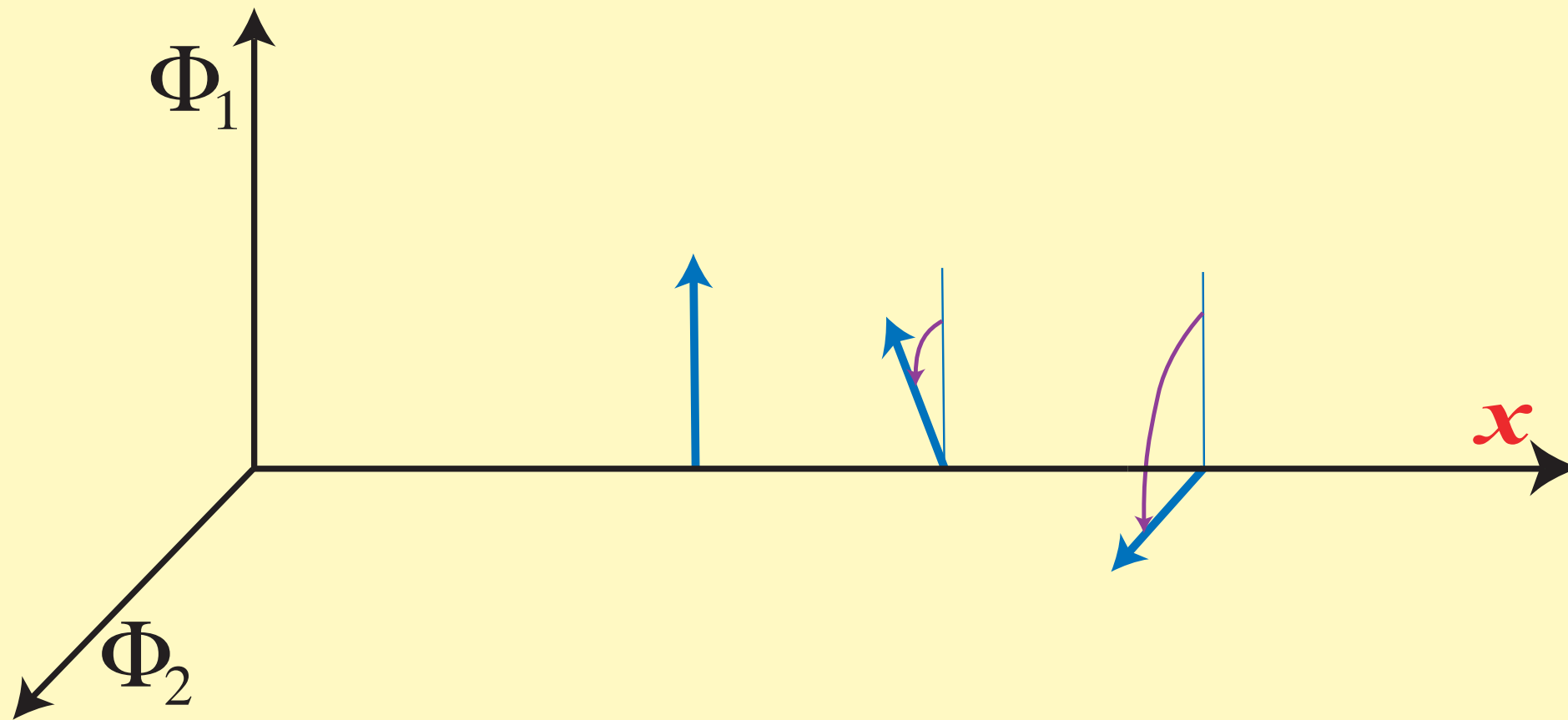
*Example: “abelian” local symmetry*



### III. The BEH mechanism

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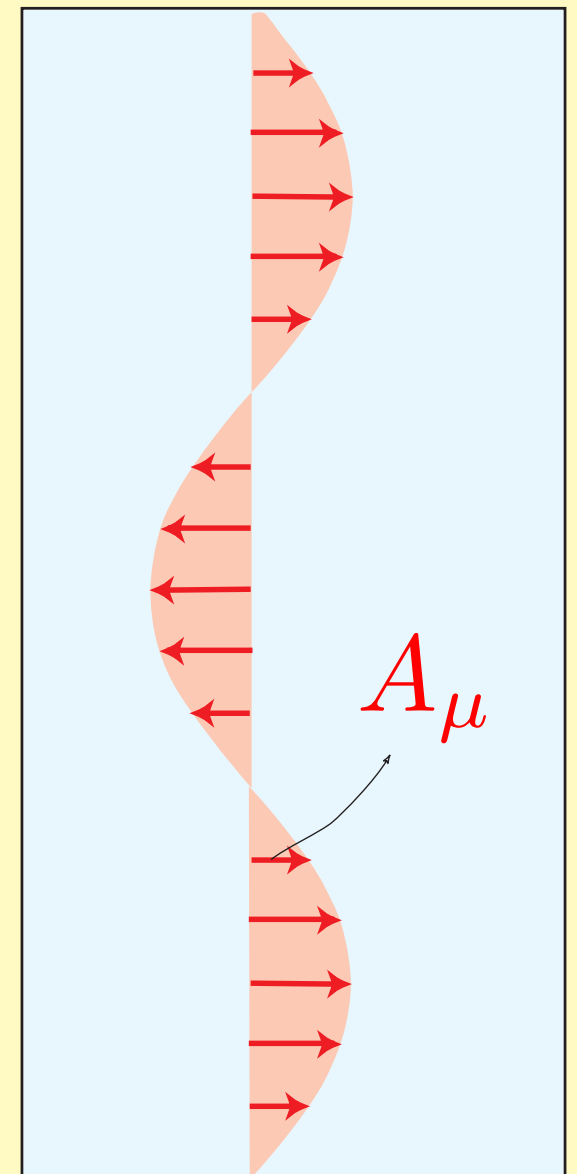
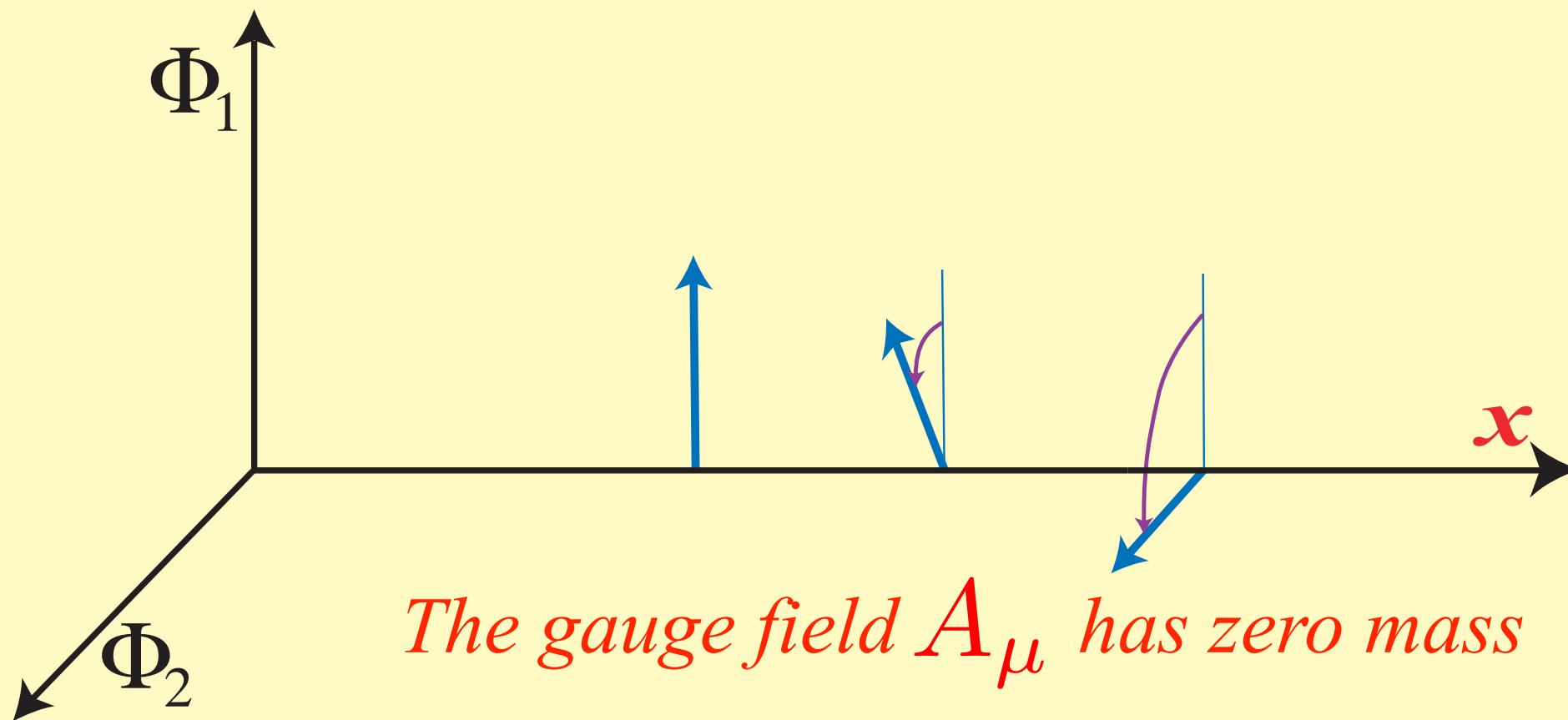
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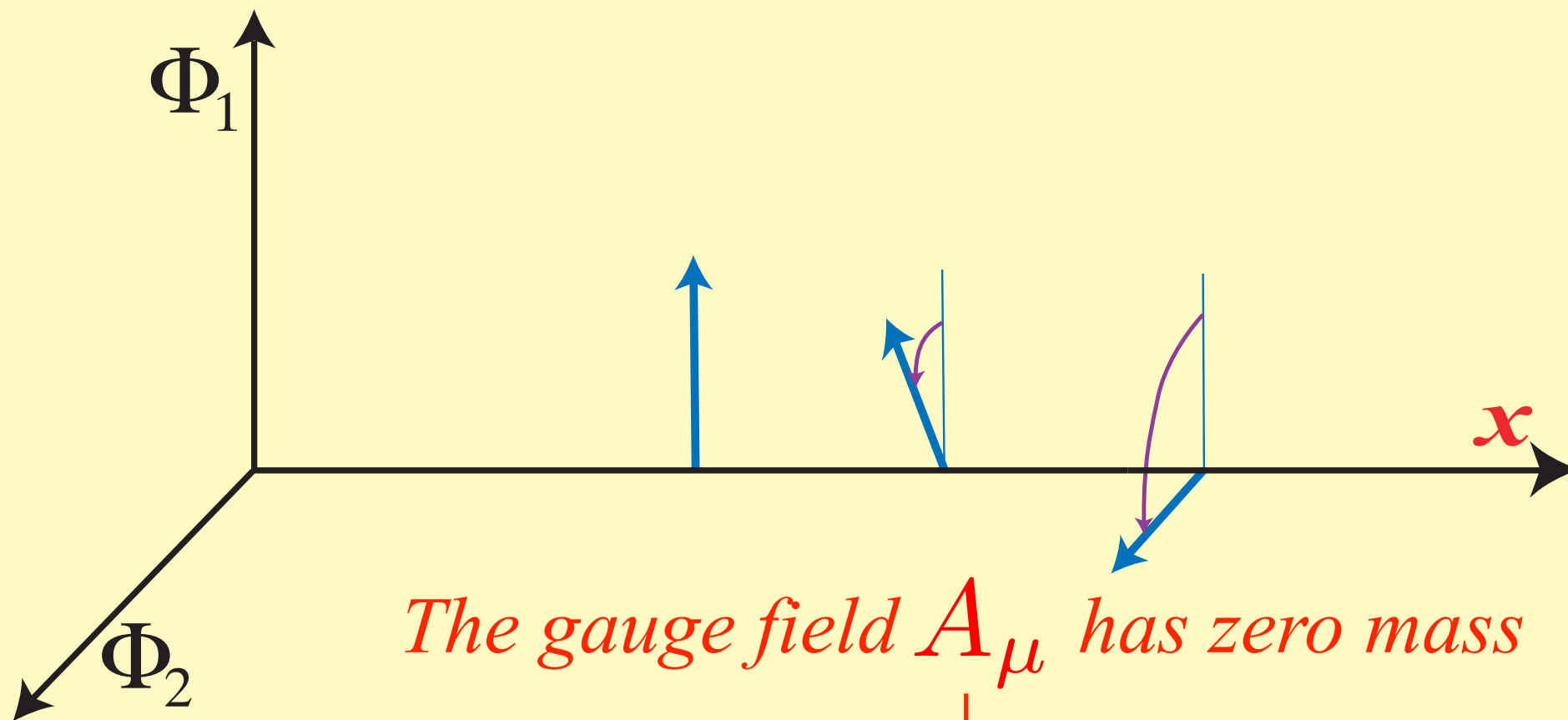
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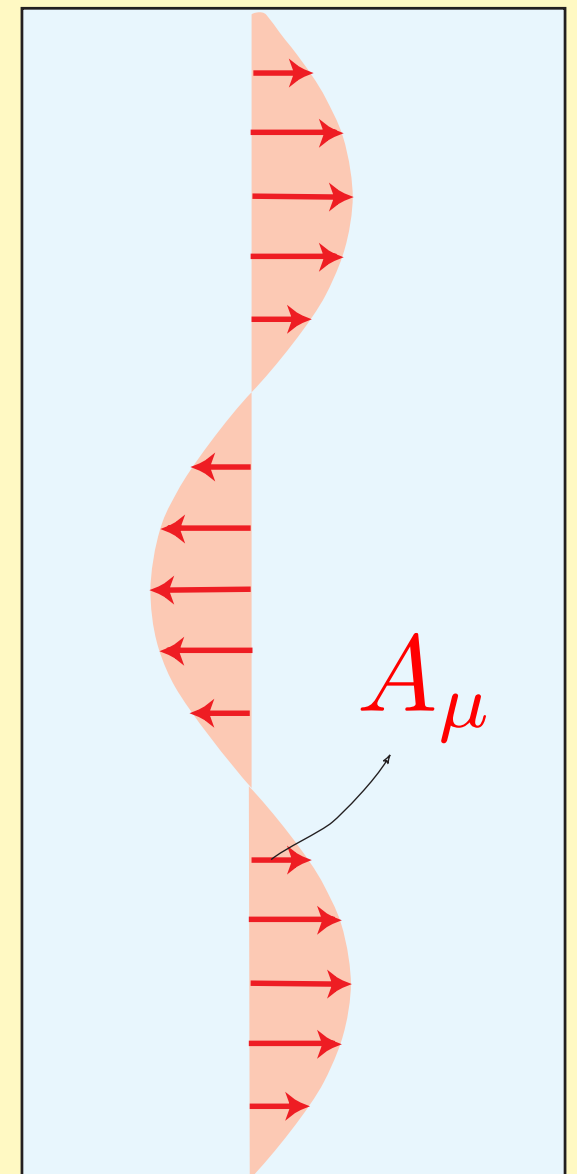
#### 1. From global to local symmetry

*Example: “abelian” local symmetry*



*The gauge field  $A_\mu$  has zero mass*

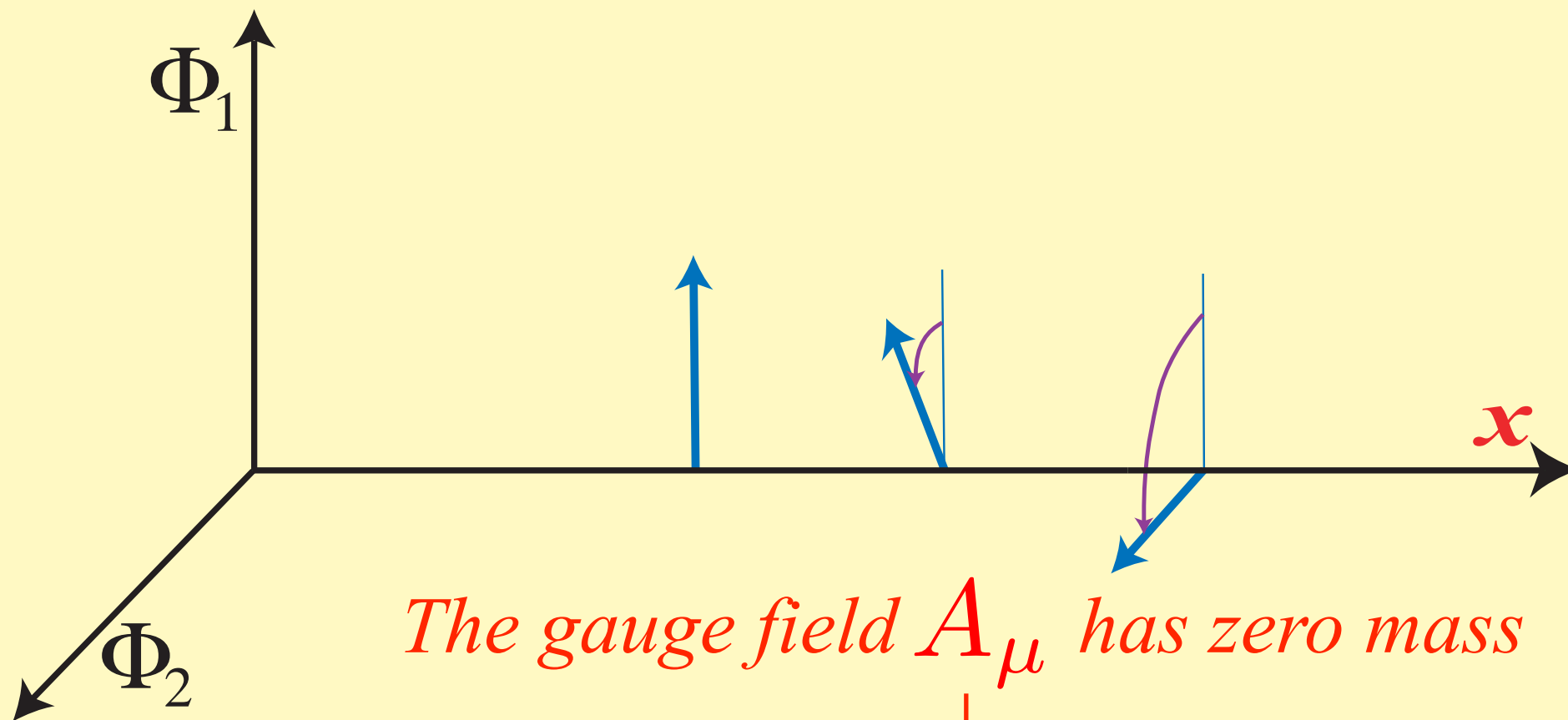
*2 polarizations*



### III. The BEH mechanism

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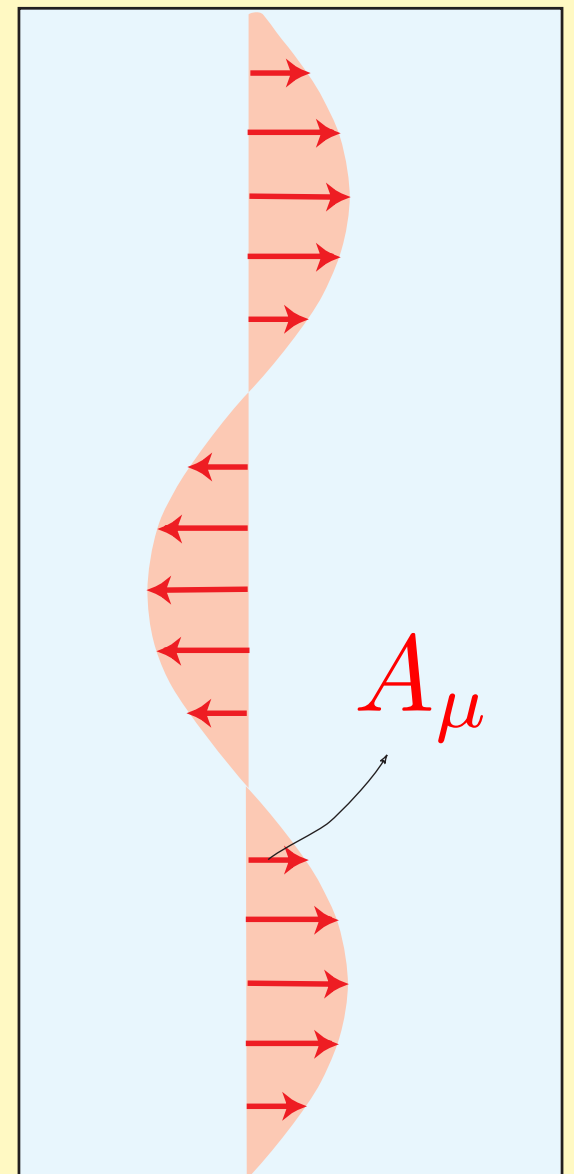
Example: “abelian” local symmetry



The gauge field  $A_\mu$  has zero mass

2 polarizations

This is electromagnetism!



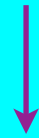


## *Global abelian symmetry*

$$\phi \rightarrow e^{i\alpha} \phi \quad \mathcal{L} = \partial^\mu \phi^* \partial_\mu \phi - V(\phi^* \phi)$$

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## *Local abelian symmetry*

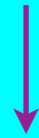
$$\phi \rightarrow e^{i\alpha(x)} \phi \quad A_\mu \rightarrow A_\mu + \partial_\mu \alpha$$

$$\mathcal{L} = D^\mu \phi^* D_\mu \phi - V(\phi^* \phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$D_\mu \phi = \partial_\mu \phi - ieA_\mu \phi \quad F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

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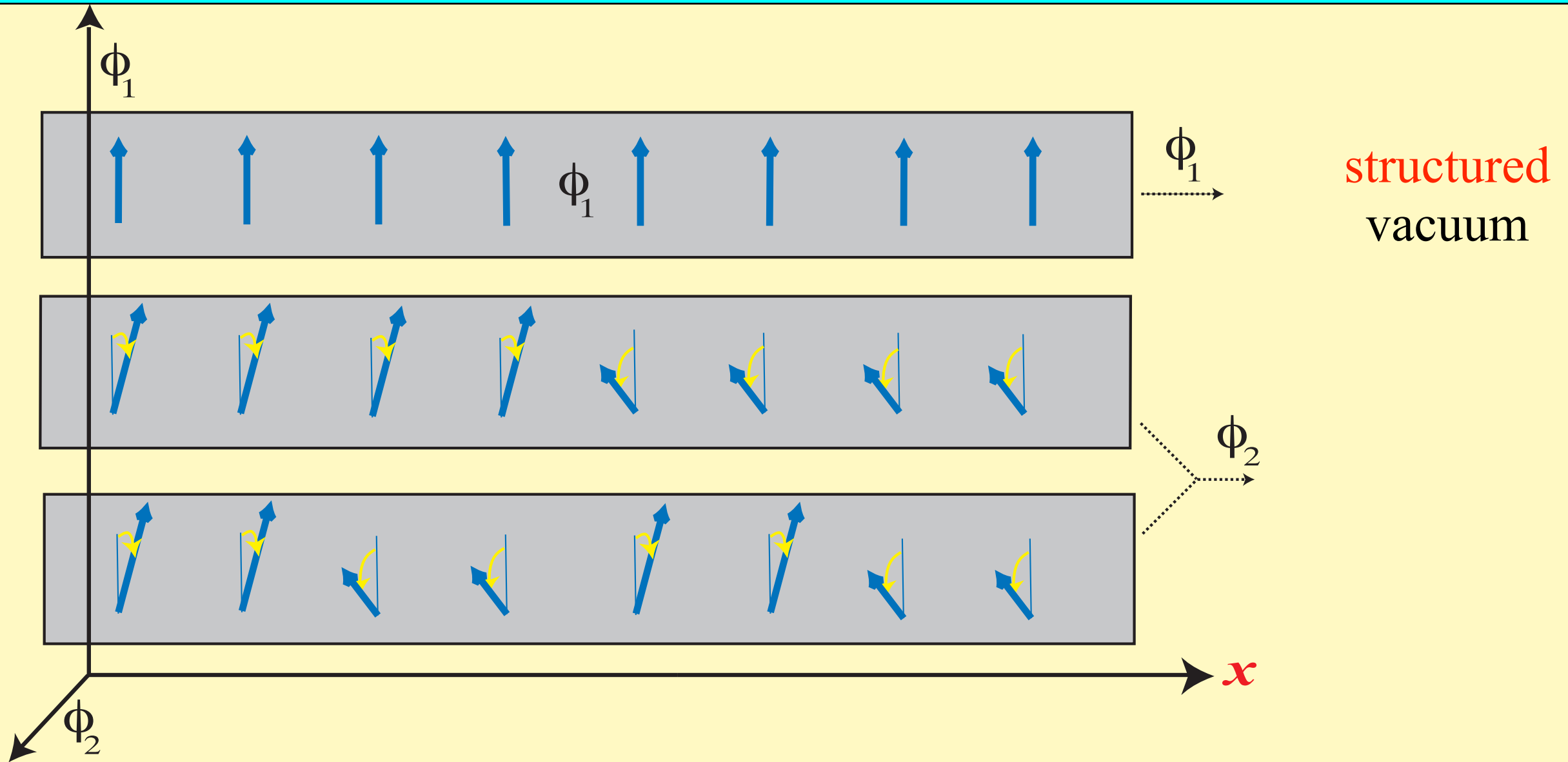
## *Local non-abelian symmetry*

$$(D_\mu \phi)^A = \partial_\mu \phi^A - eA_\mu^a T^a{}^{AB} \phi^B$$

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + ef^{abc} A_\mu^b A_\nu^c$$

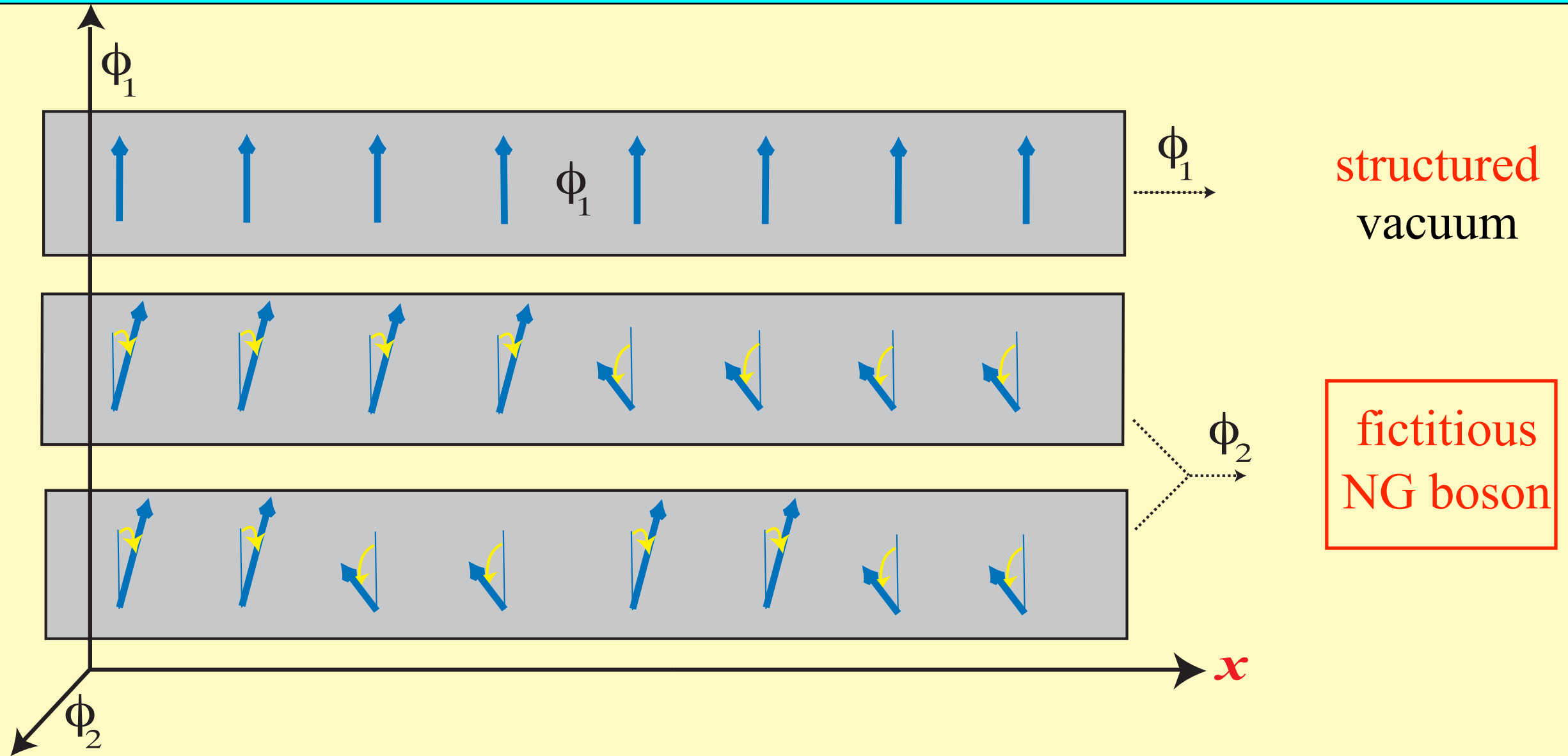
## 2. Conceptual issues in SBS for local symmetries

### The fate of the Nambu-Goldstone boson (a simple model)



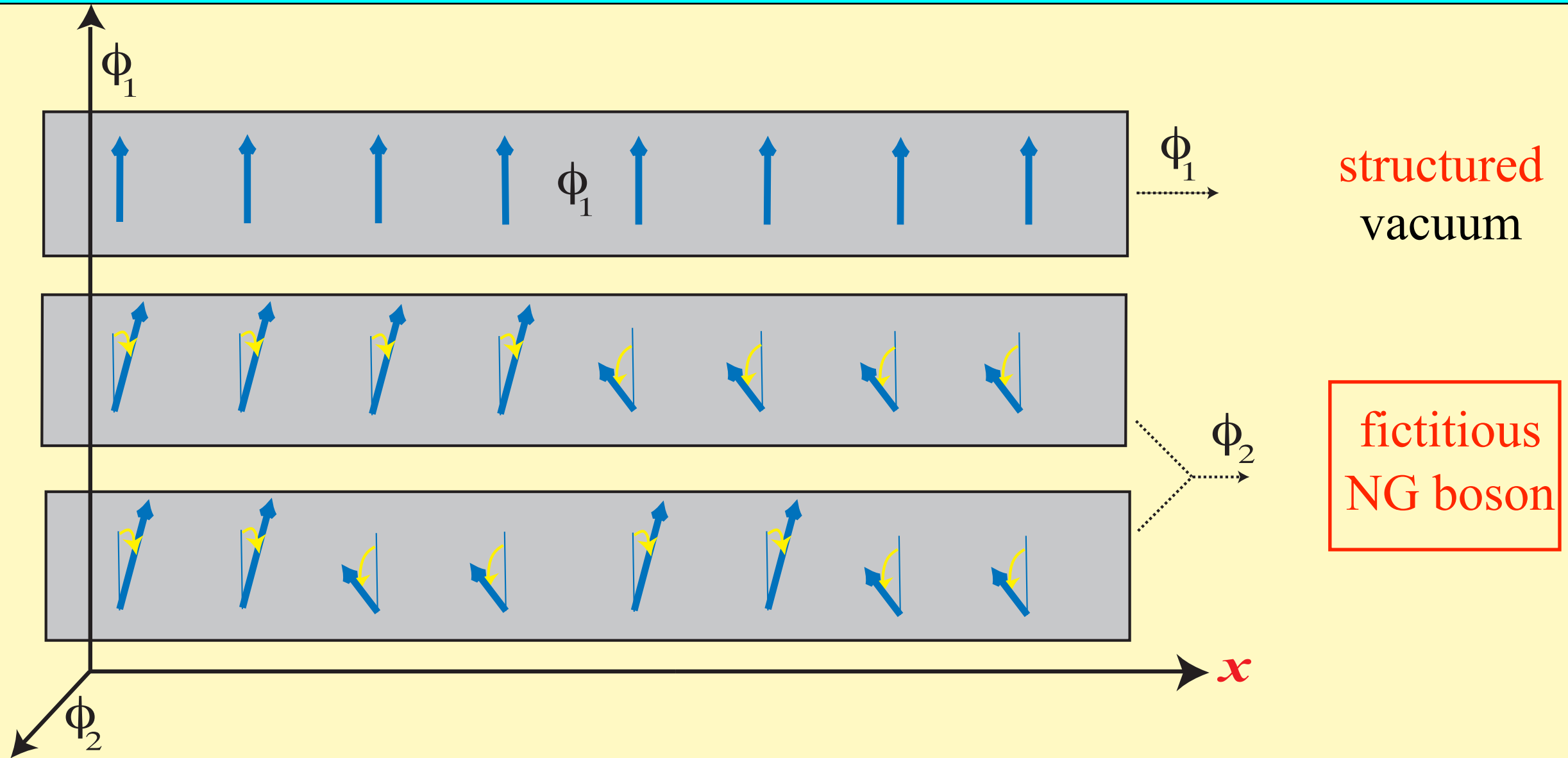
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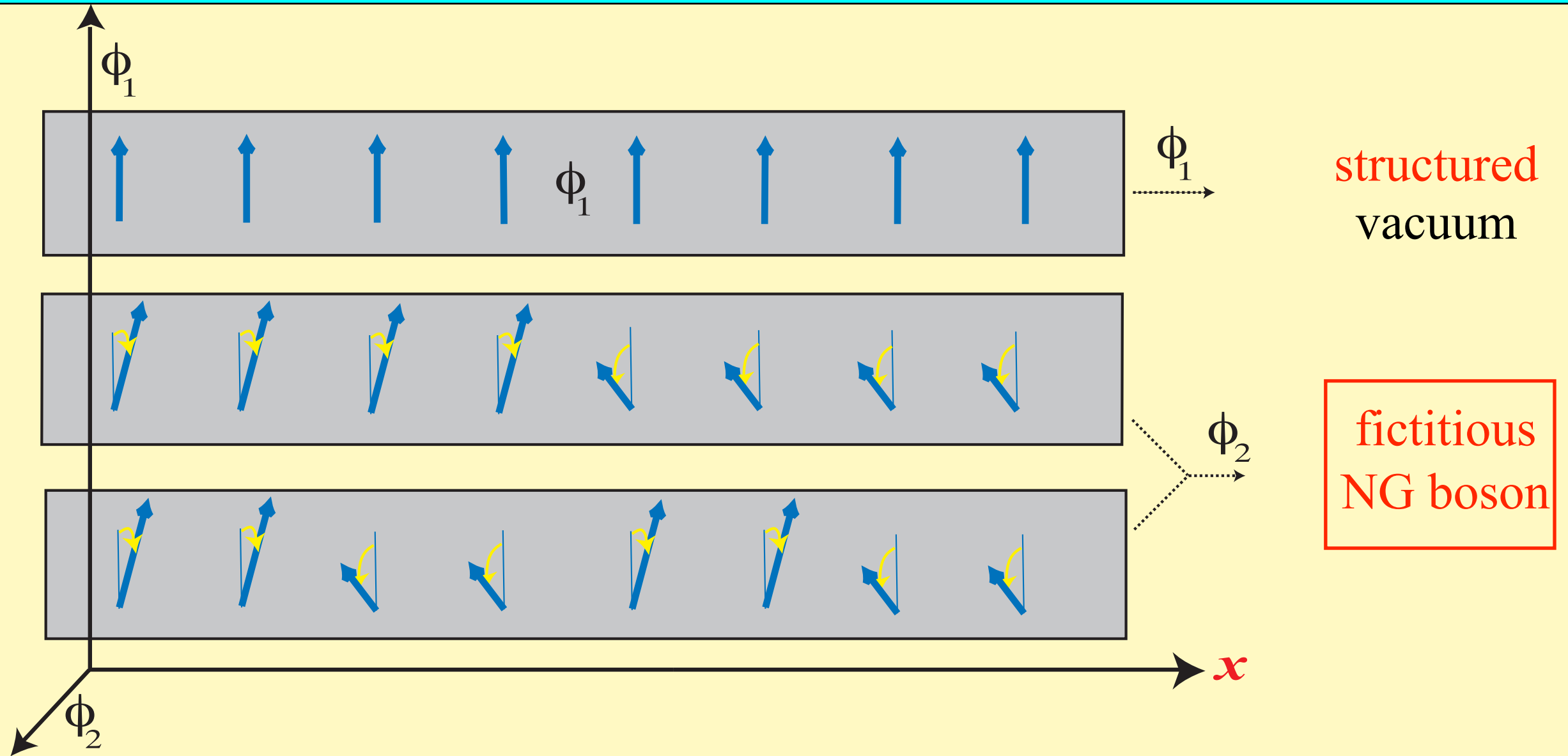
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cf. P.W. Higgs, Phys. Letters **12** (1964) 132; G.S. Guralnik, C.R. Hagen and T.W. Kibble, Phys;Rev.Lett. **13** (1964) 585.

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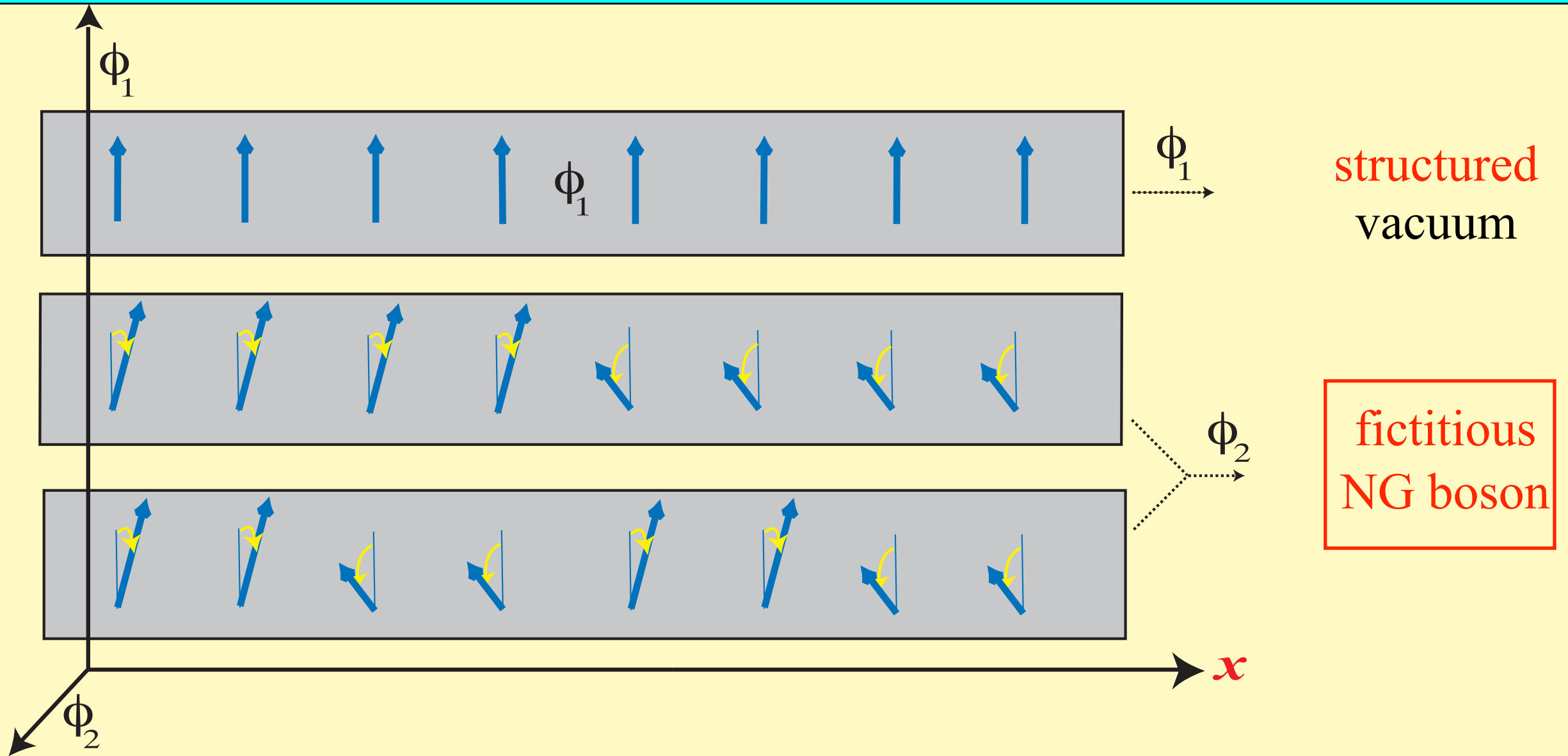
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- The local symmetry is *unbroken* !  
Apparent breaking is with respect to a *preferred orientation*

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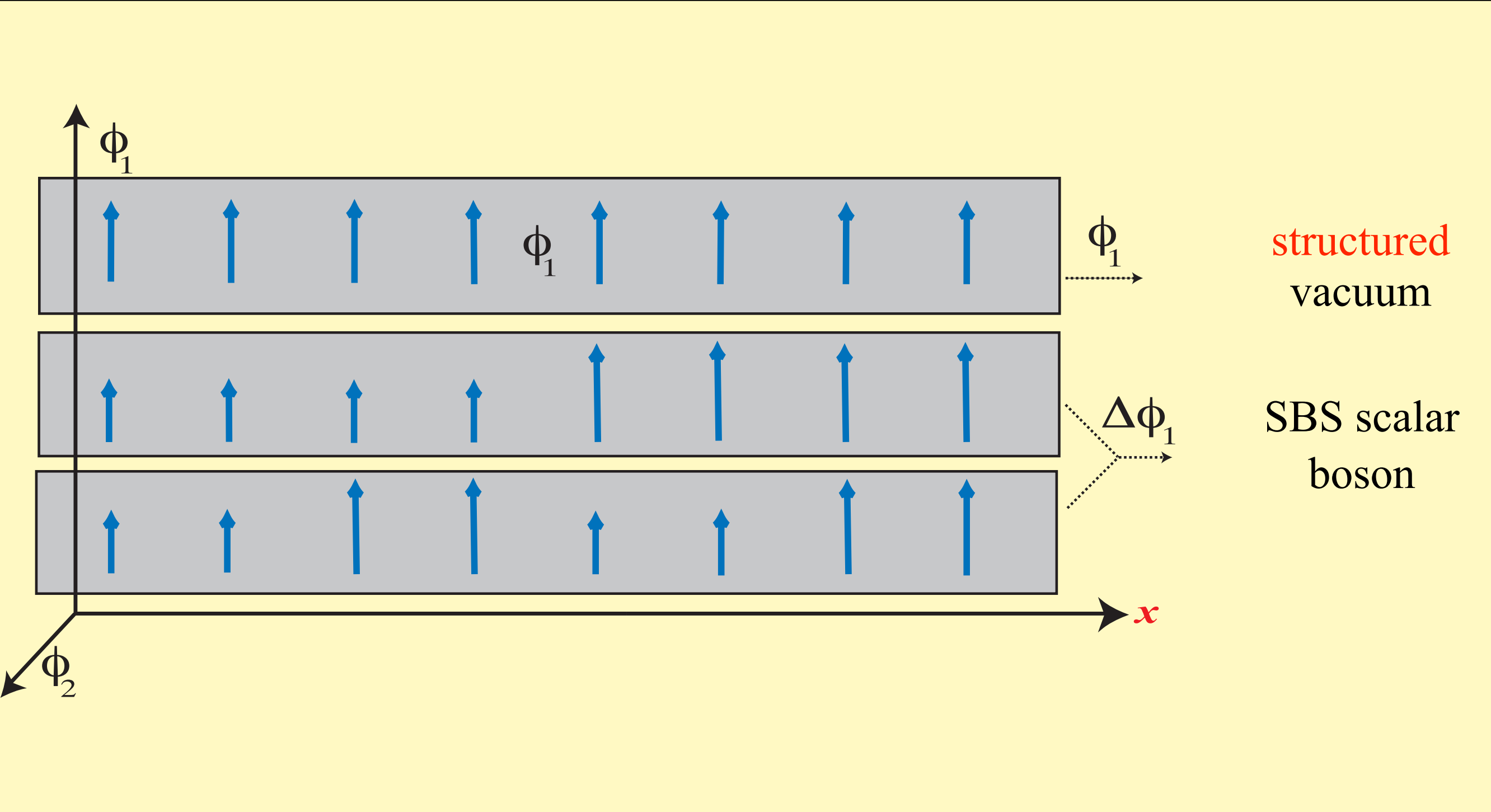
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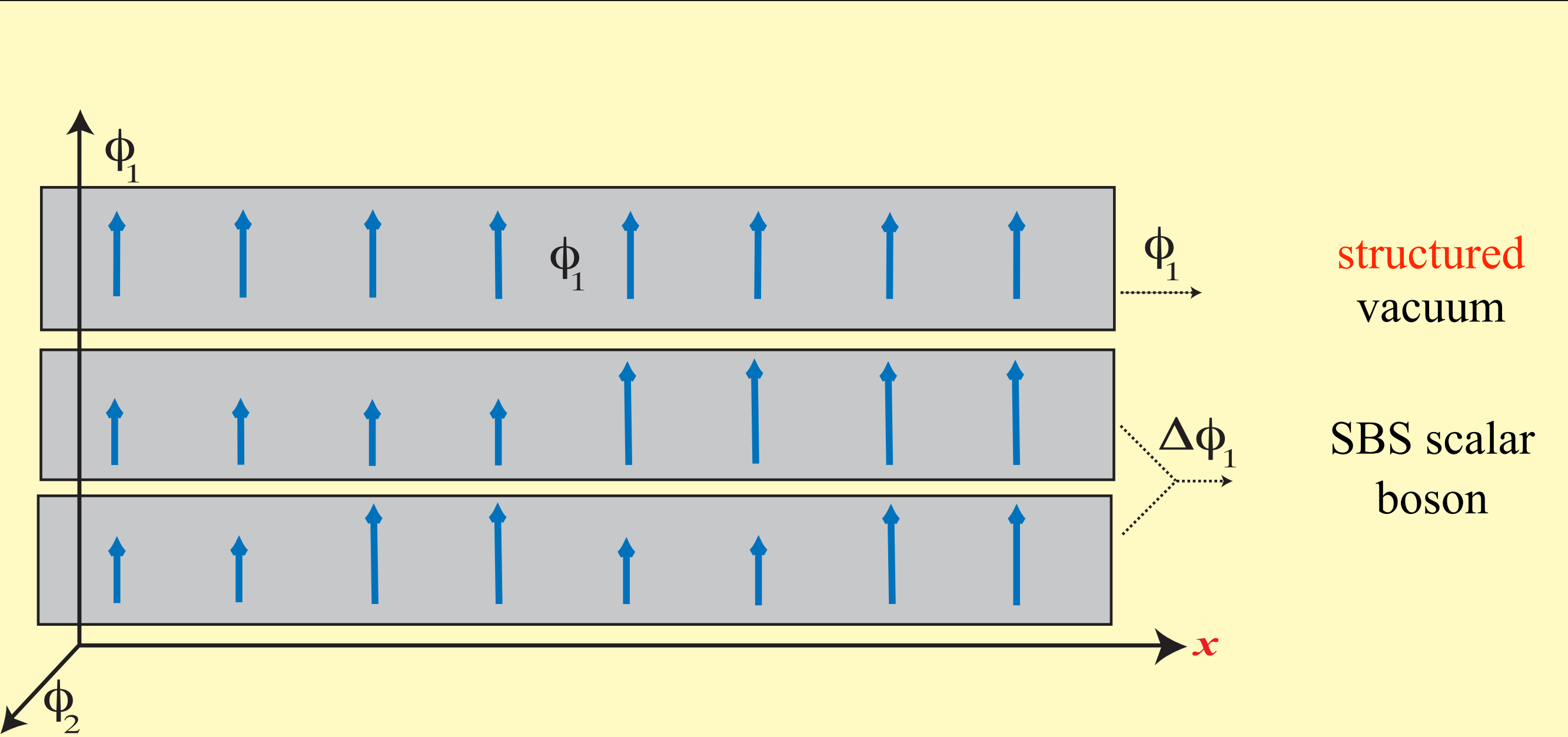
- The local symmetry is *unbroken* !
- Apparent breaking is with respect to a *preferred* orientation
- The NG boson  $\rightarrow$  the third polarization of a *massive* gauge boson



# The fate of the SBS scalar boson (a simple model)



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*The SBS scalar boson is not affected by the gauging*

### 3. *The field-theoretic approach*

F. Englert and R. Brout, Phys. Rev. Lett. 13 (1964) 321.

## *Breaking by scalar fields: the abelian case*

*time* →




gauge field

$$D_{\mu\nu}^0 = \frac{g_{\mu\nu}}{q^2}$$

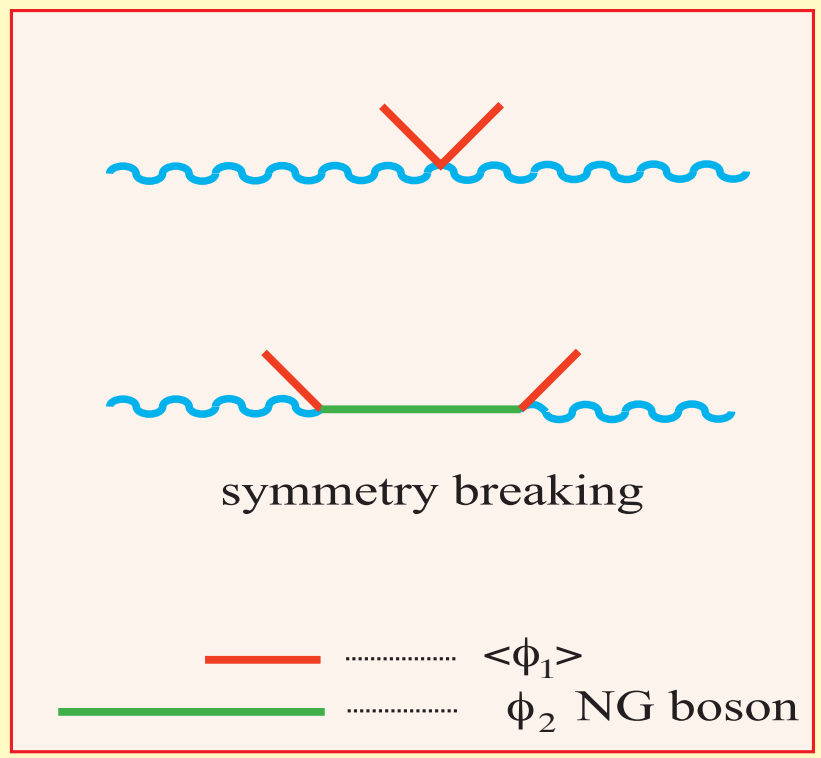
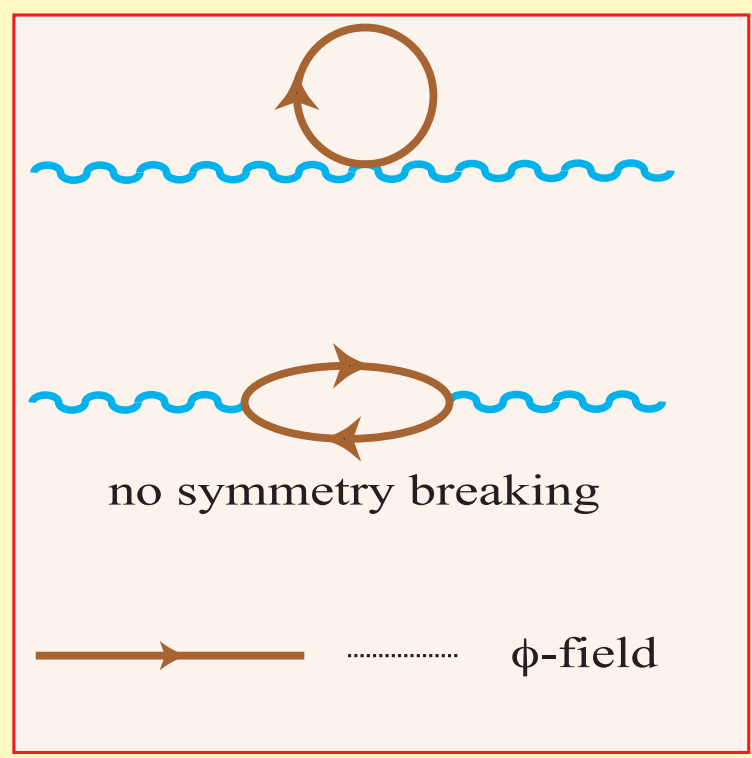
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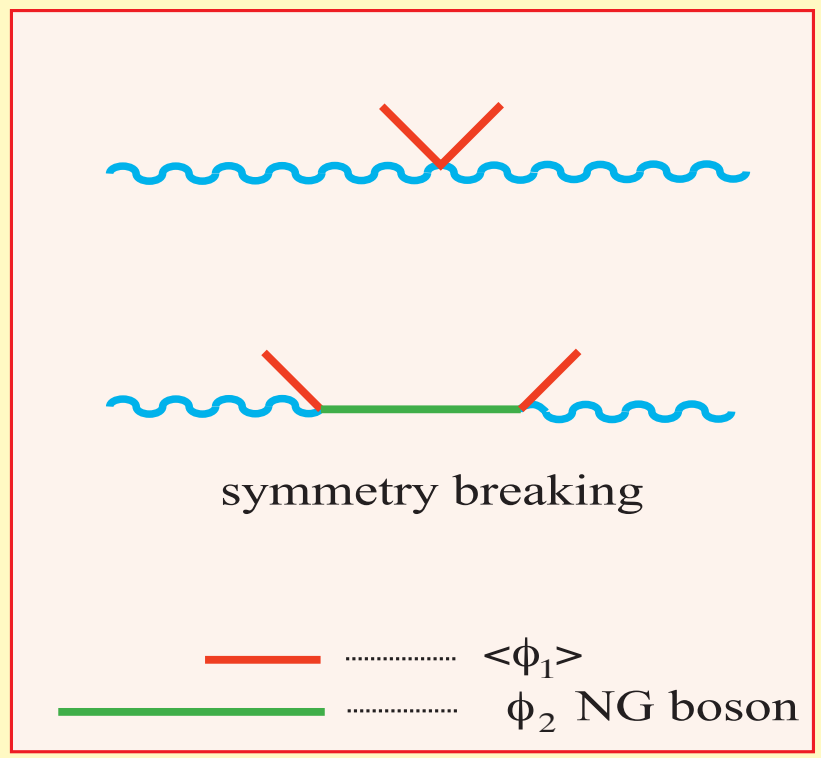
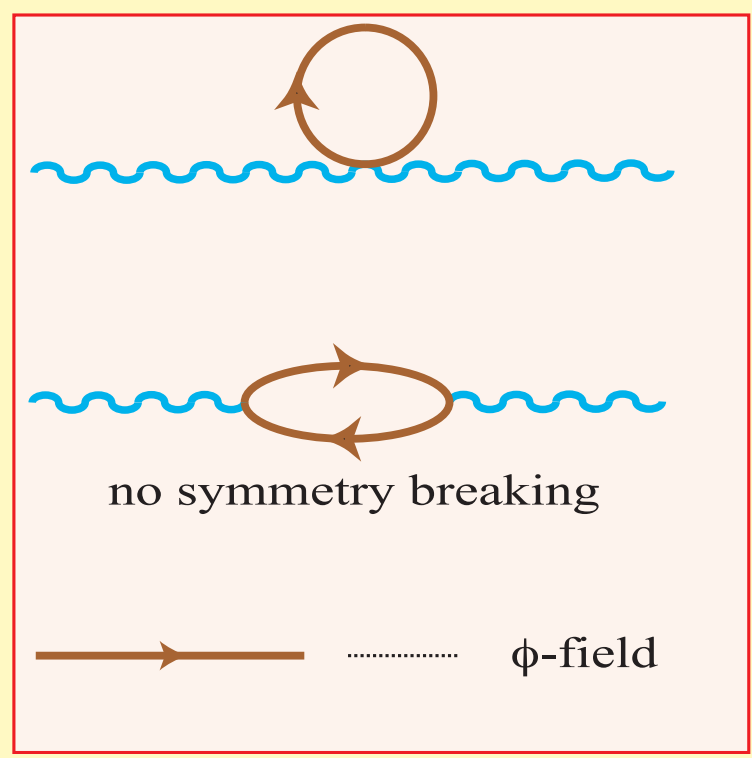
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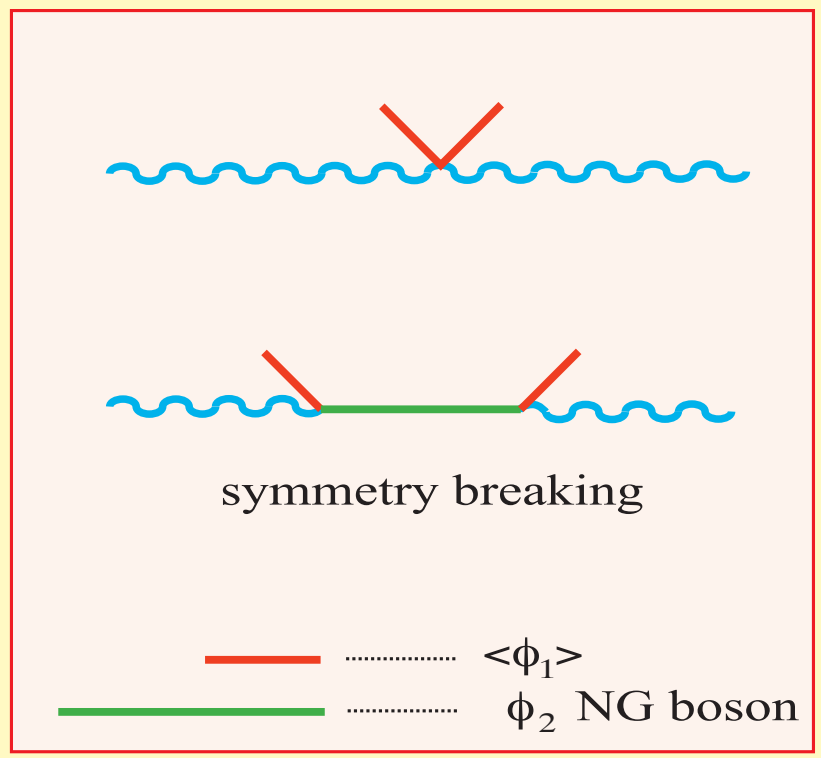
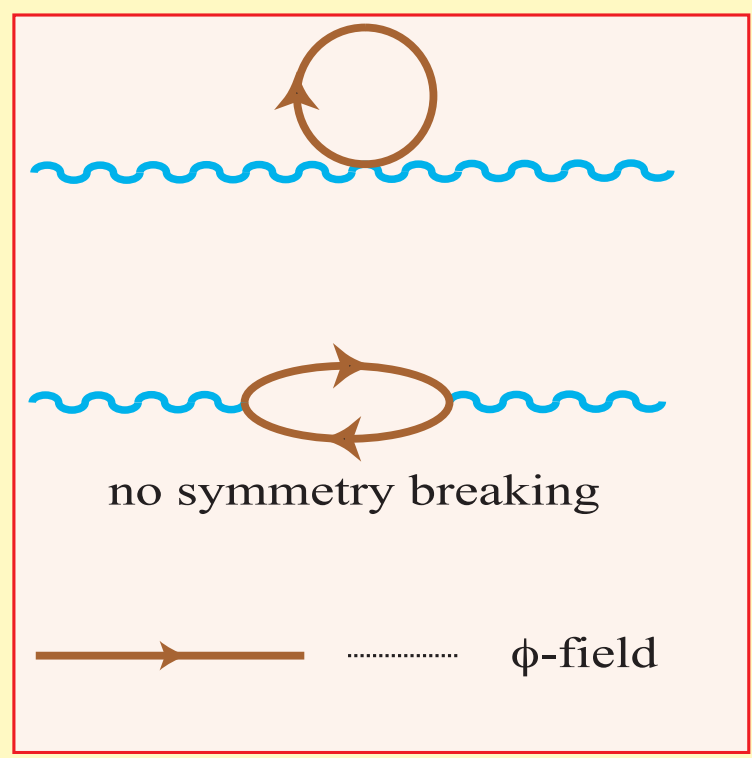
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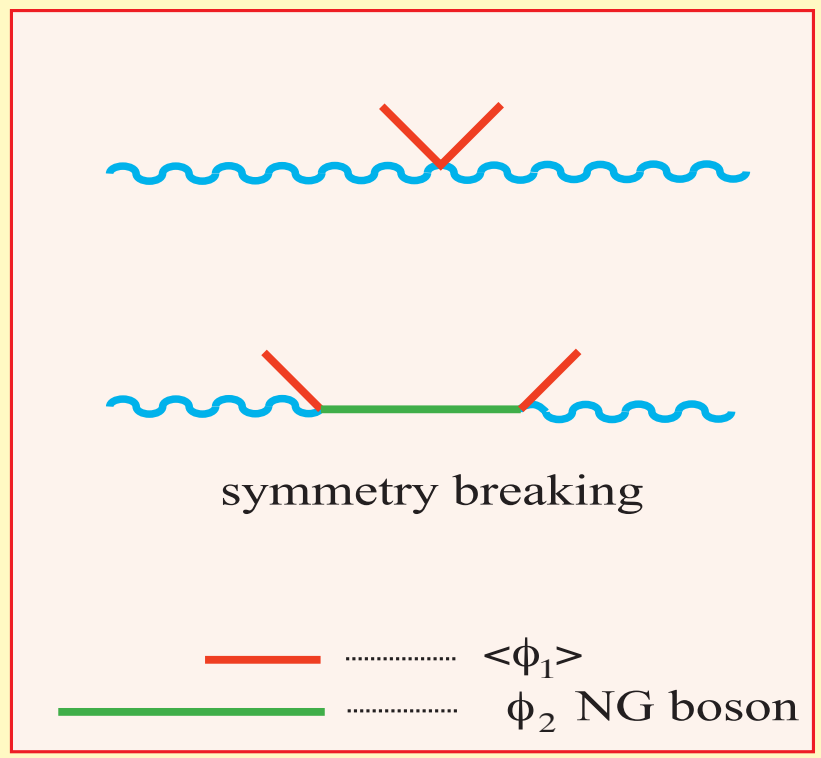
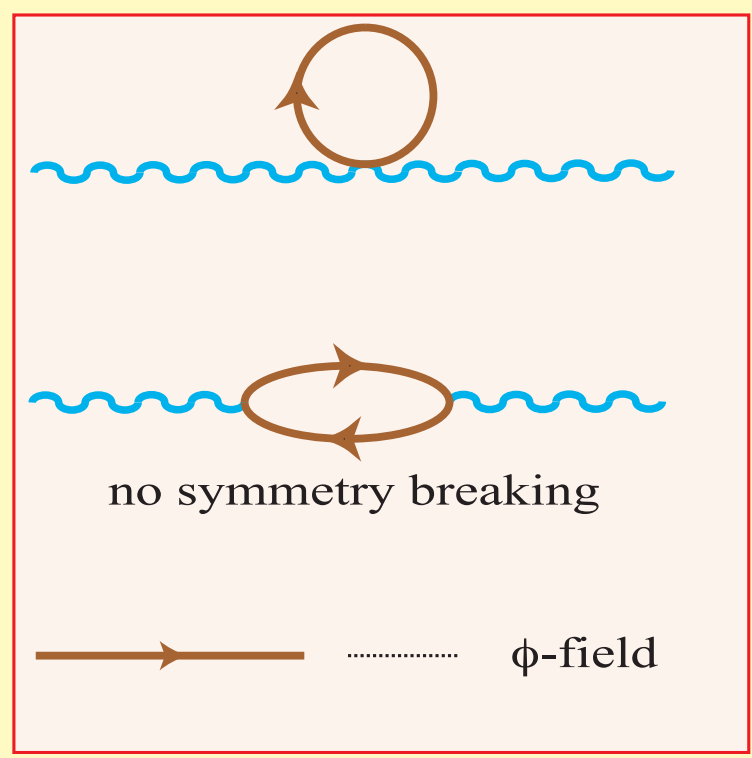
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$$D_{\mu\nu}^0 = \frac{g_{\mu\nu}}{q^2}$$

$$\Pi(q^2) = \frac{e^2 \langle \phi_1 \rangle^2}{q^2}$$


$$D_{\mu\nu} = \frac{g_{\mu\nu} - q_\mu q_\nu / q^2}{q^2 - e^2 \langle \phi_1 \rangle^2}$$

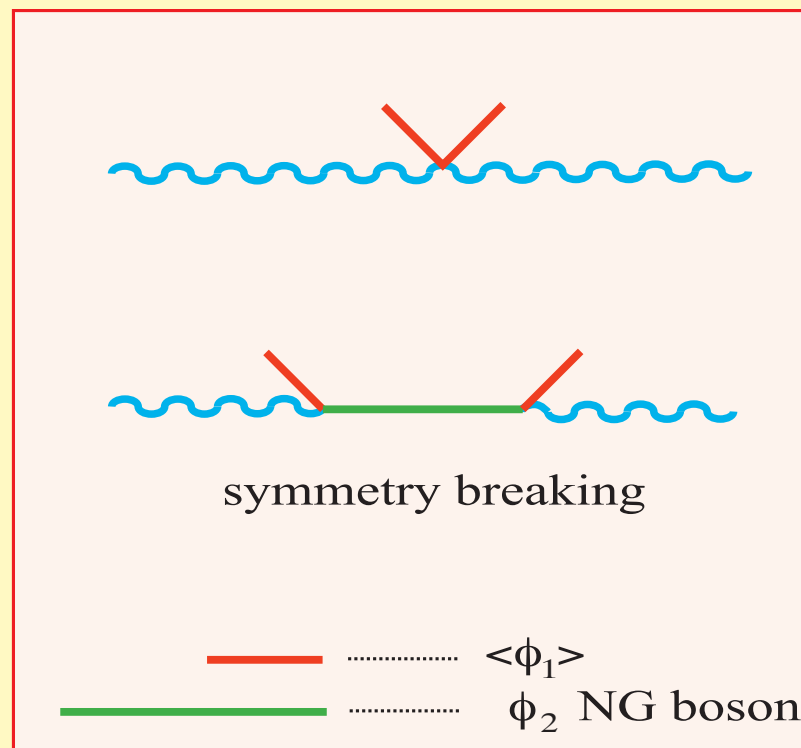
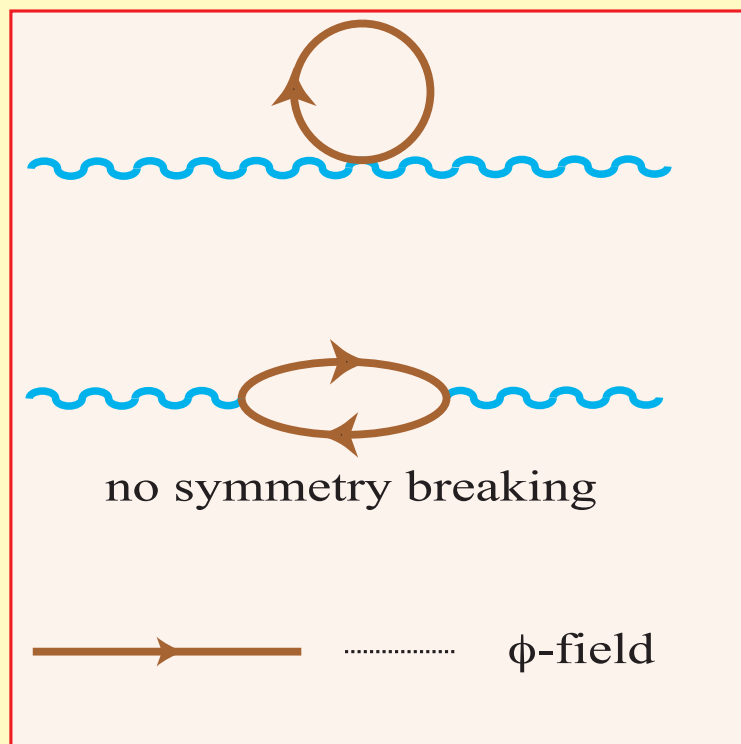
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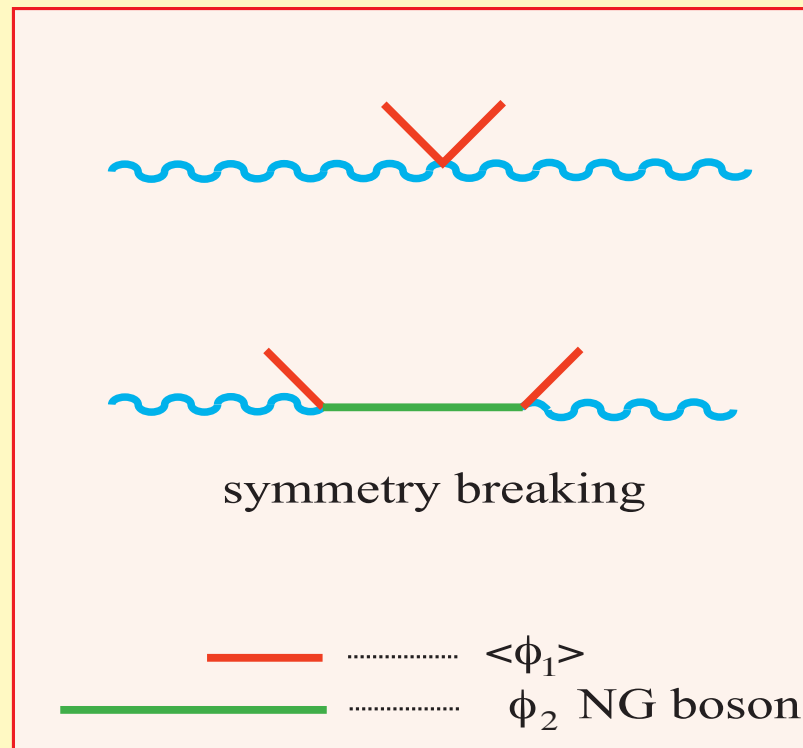
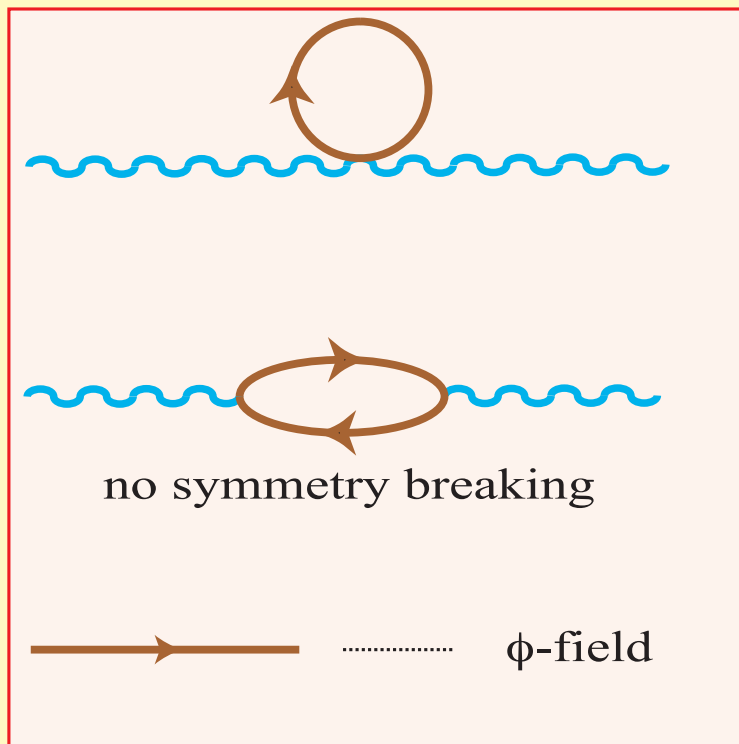


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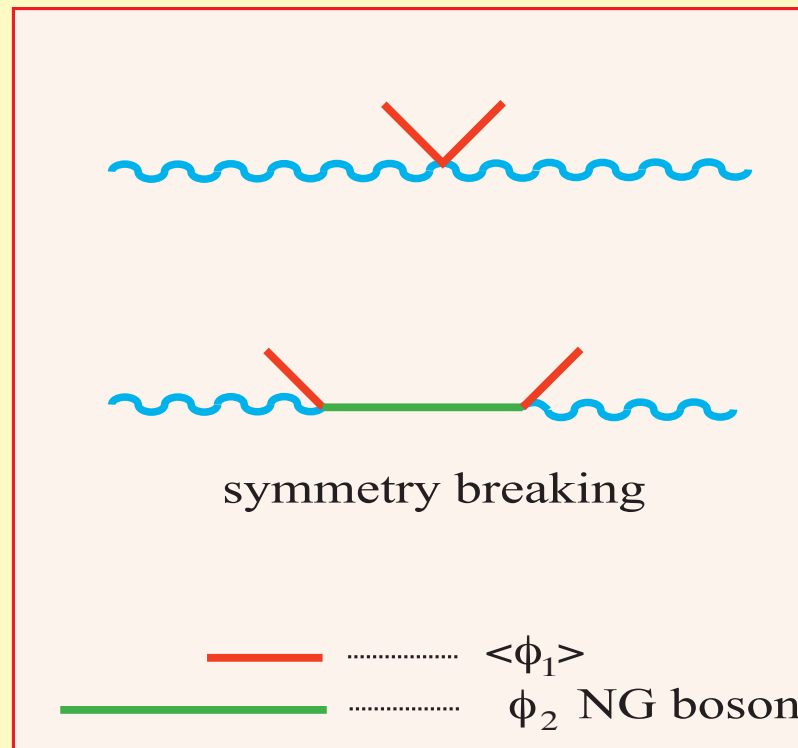
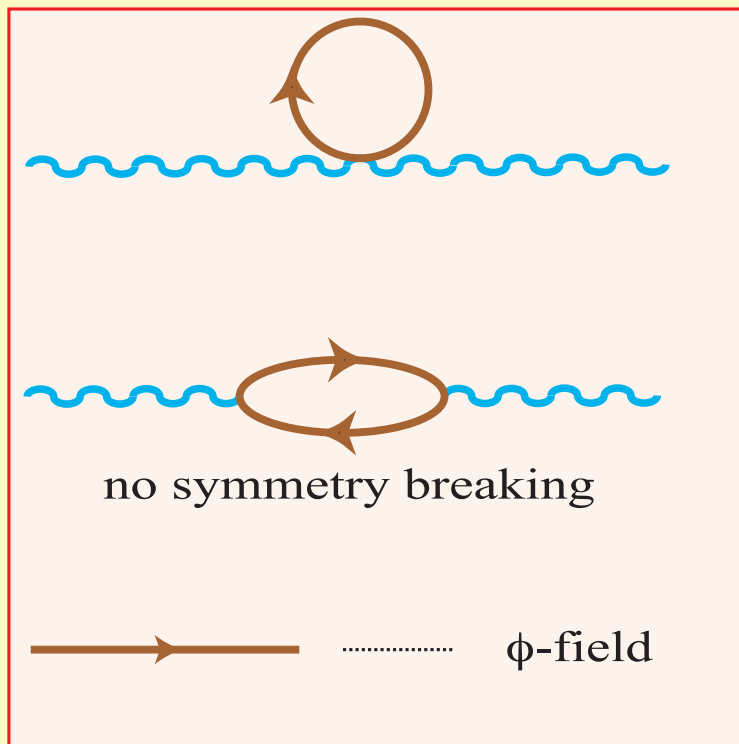
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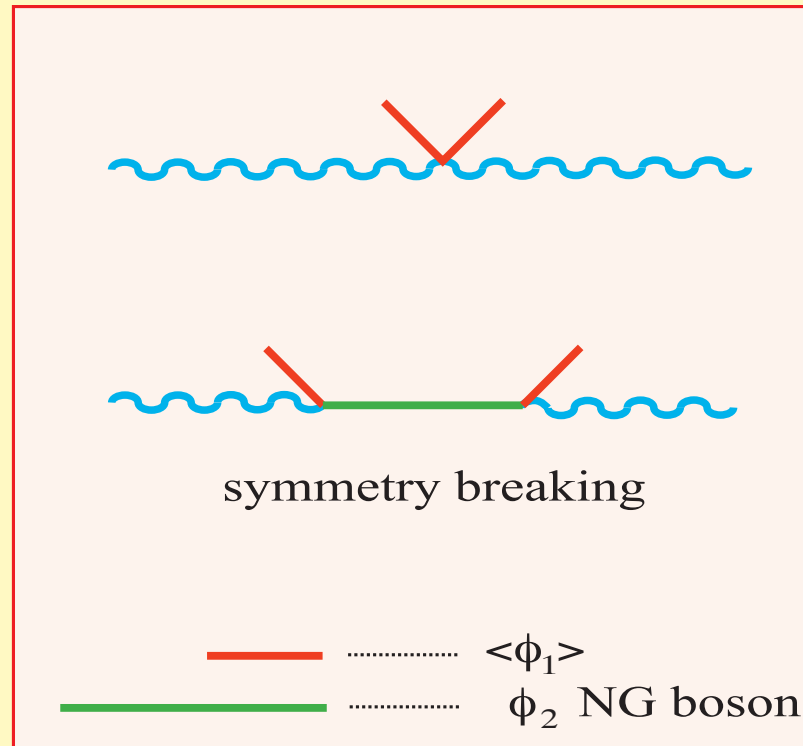
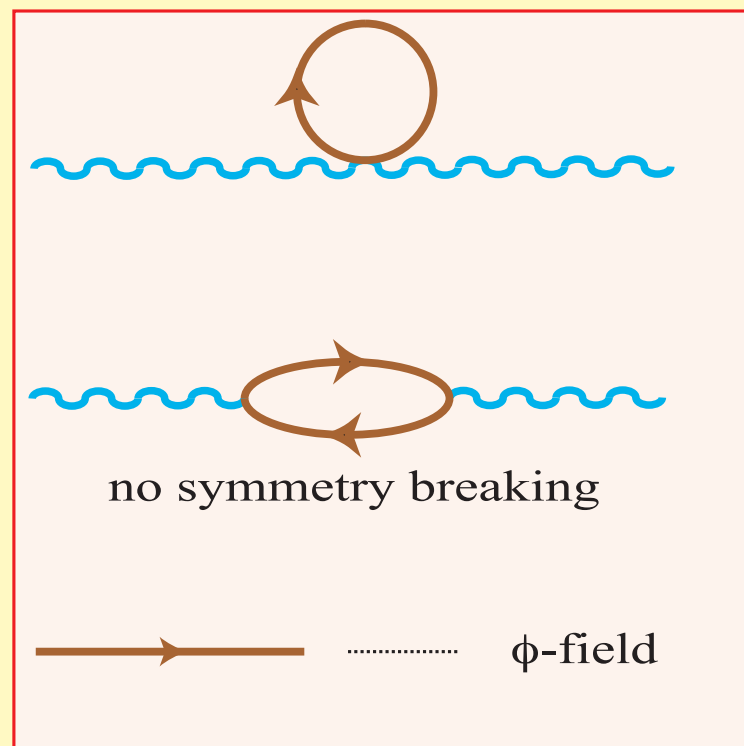
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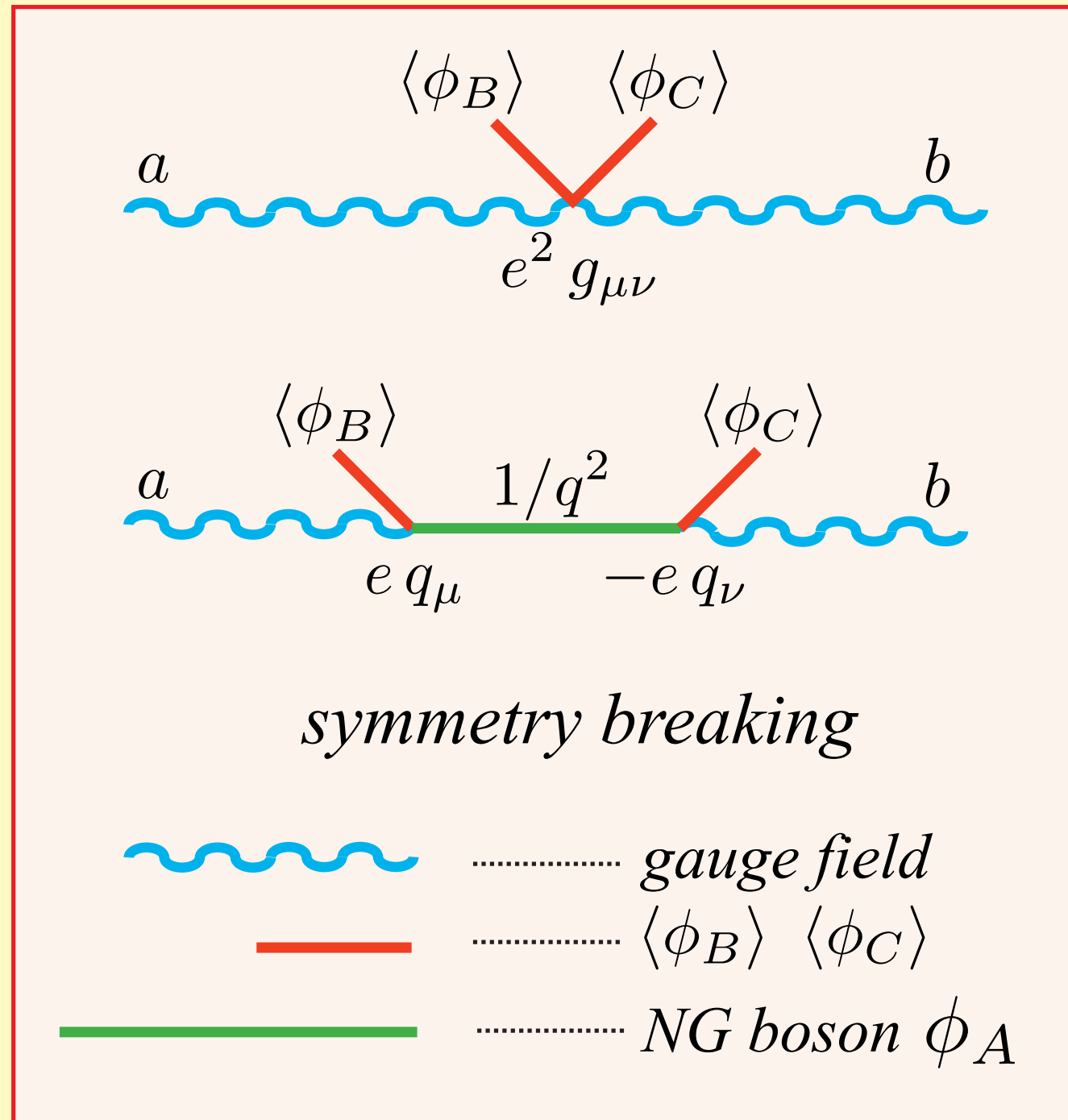
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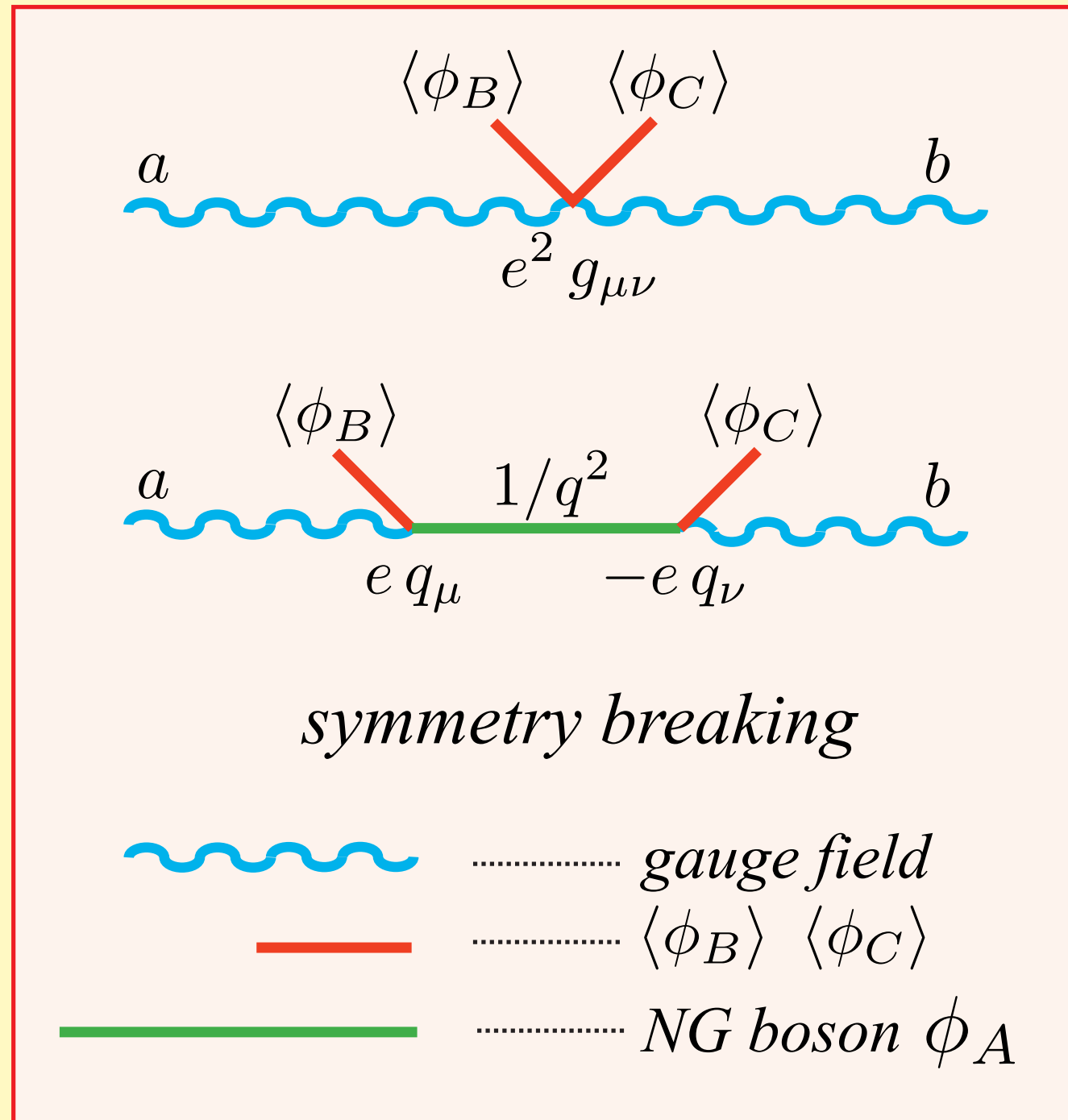
The SBS scalar boson decouples from  $D_{\mu\nu}$

# Breaking by scalar fields: the “non-abelian” generalization



$$(\mu^2)^{ab} = -e^2 \langle\phi_B\rangle T^{aBA} T^{bAC} \langle\phi_C\rangle$$

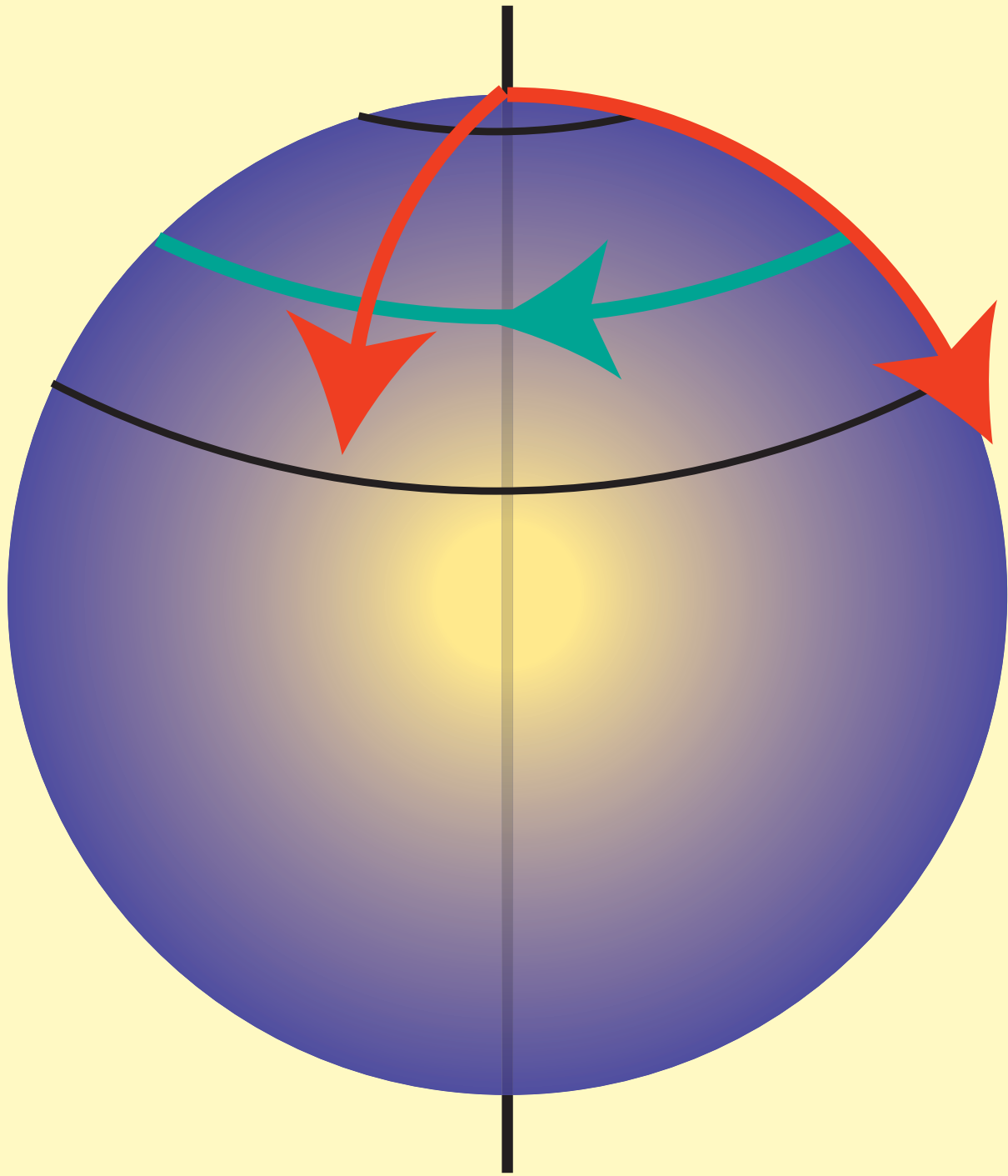
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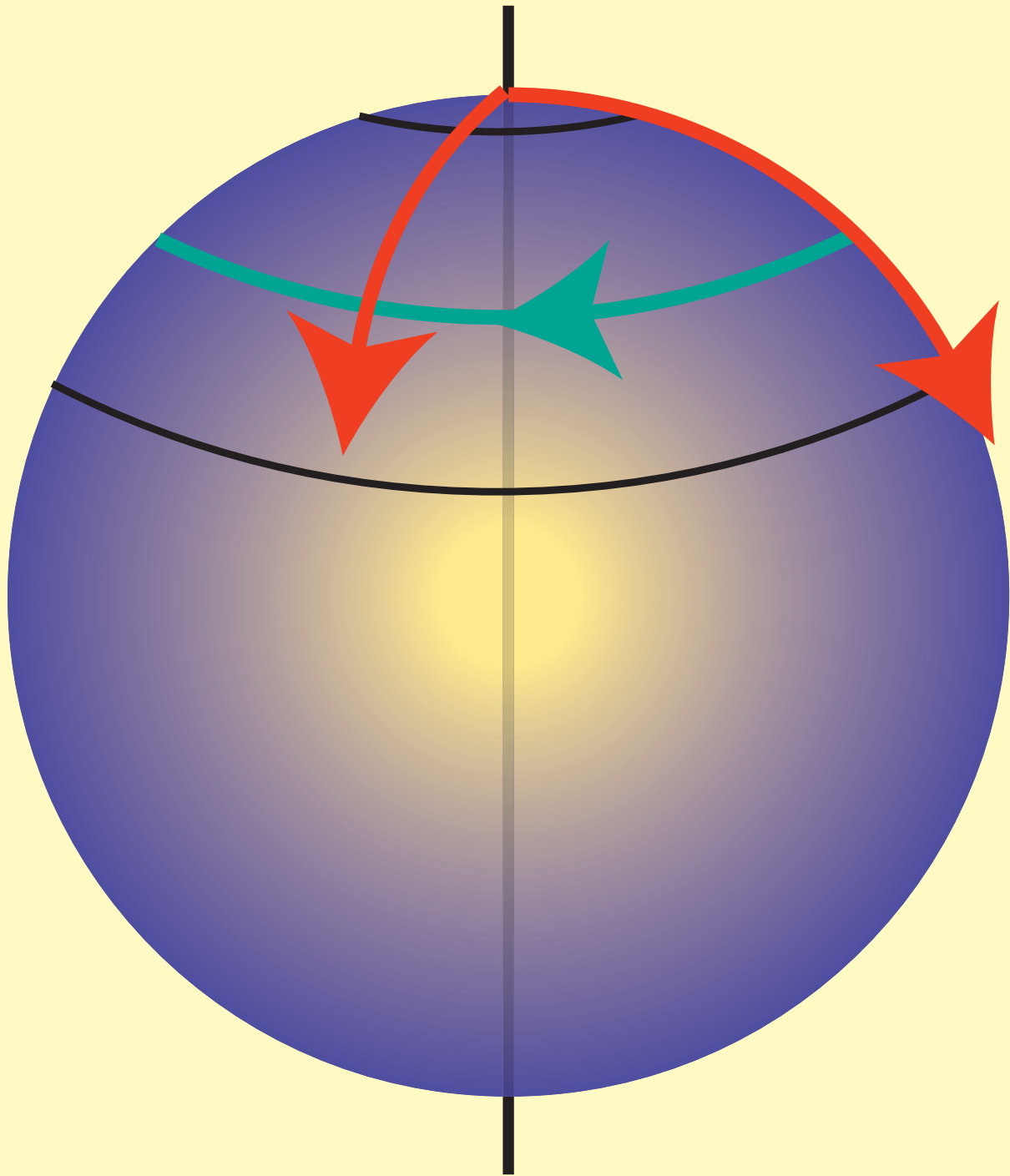
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*Each fictitious NG boson yields a massive gauge field*

*Example  $SO(3)/U(1)$*

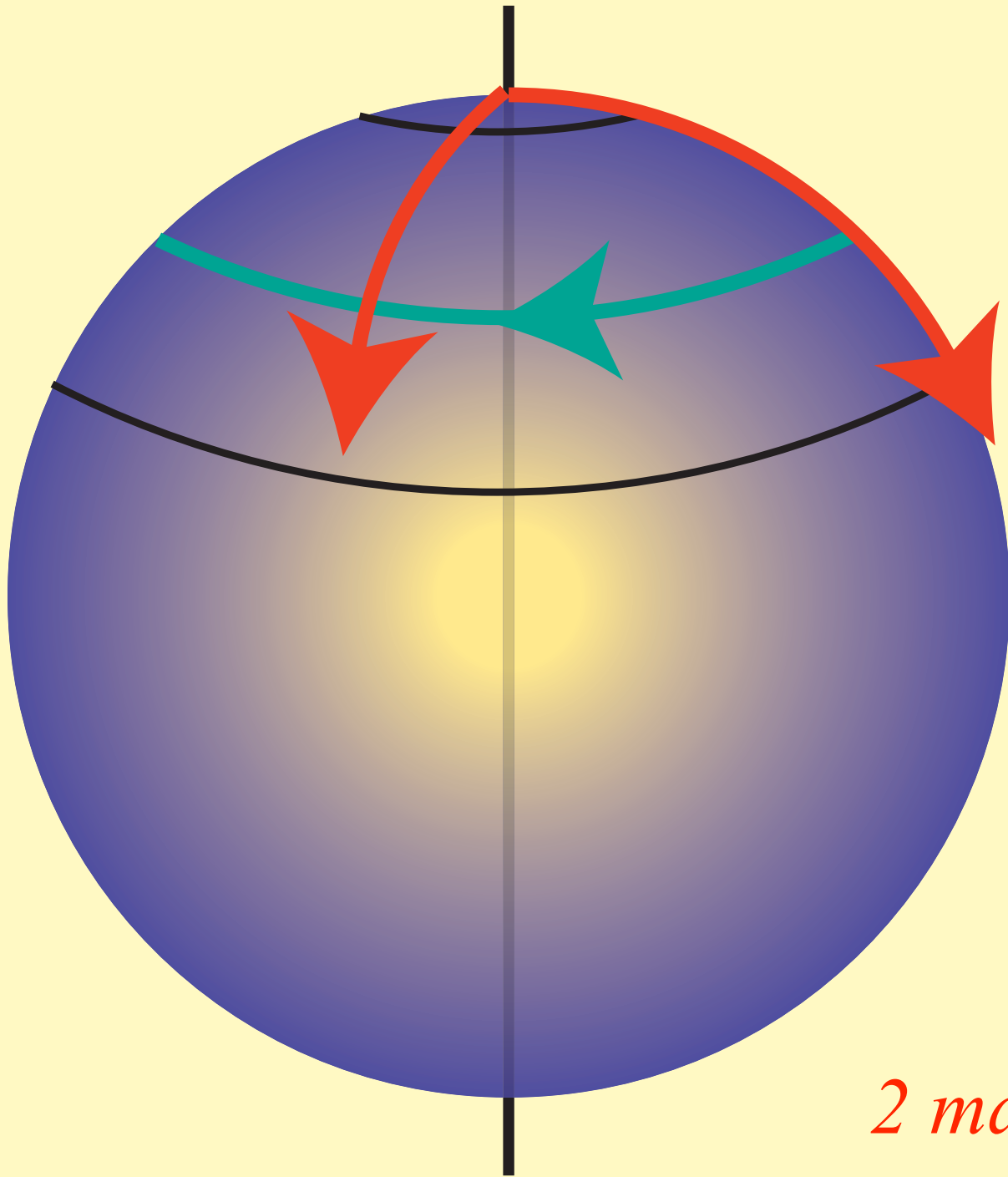


*Example  $SO(3)/U(1)$*



*2 fictitious NG bosons*

*Example  $SO(3)/U(1)$*



*2 fictitious NG bosons*



*2 massive and 1 massless gauge boson*



# *Dynamical symmetry breaking*

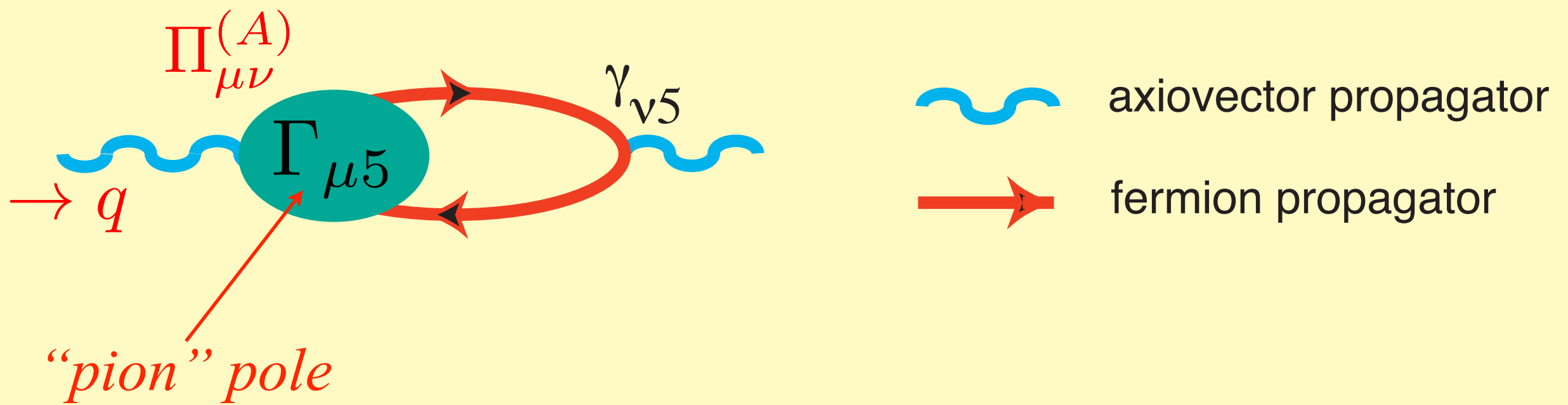
$$U(1) \times U(1)$$

$$\mathcal{L} = \mathcal{L}_0^F - e_V \bar{\psi} \gamma_\mu \psi V_\mu - e_A \bar{\psi} \gamma_\mu \gamma_5 \psi A_\mu - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} (V) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} (A)$$

# Dynamical symmetry breaking

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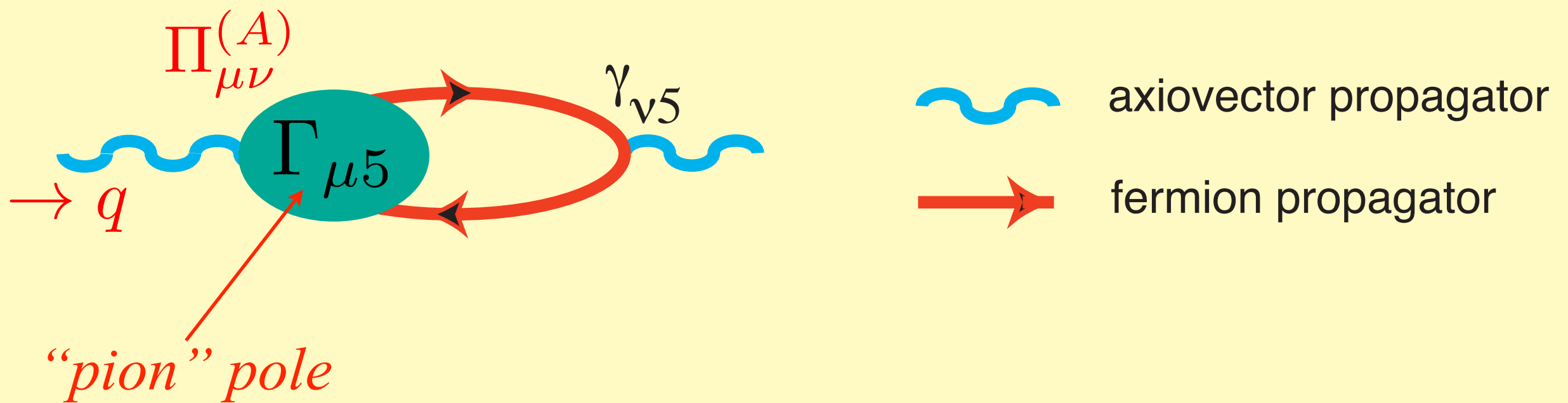
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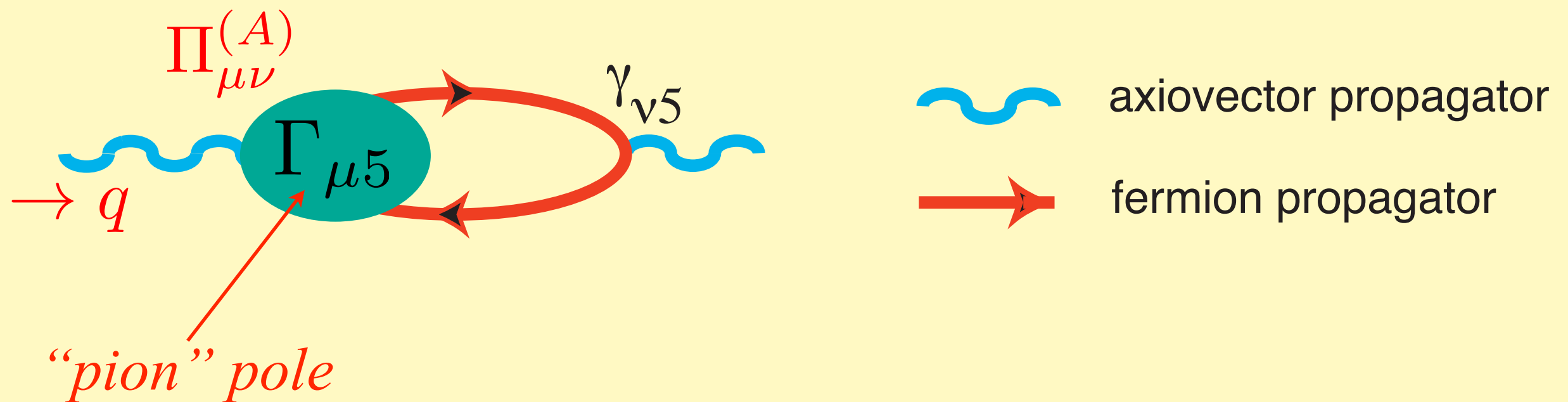


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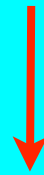
*Mass arises from the absorption of the NG boson*

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P.W. Higgs, Phys. Rev. Lett. **13** (1964) 508.

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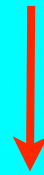
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*renormalizable gauge*

(Brout - Englert)

R. Brout, F. Englert and M.F. Thiry, *Il Nuovo Cimento* **43A** (1966) 244.

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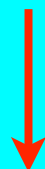
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*Precision measurements*

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	Article	Reception date	Publication date
<i>1</i>	F. Englert and R. Brout Phys. Rev. Letters 13 (1964) 321	26/06/1964	31/08/1964
<i>2</i>	P.W. Higgs Phys. Letters 12 (1964) 132	27/07/1964	15/09/1964
<i>3</i>	P.W. Higgs Phys. Rev. Letters 13 (1964) 508	31/08/1964	19/10/1964
<i>4</i>	G.S. Guralnik, C.R. Hagen and T.W.B. Kibble Phys. Rev. Letters 13 (1964) 585	12/10/1964	16/11/1964

# IV. The quest for unified laws of nature

## 1. The electroweak theory

S.L. Glashow, Nucl. Phys. **22** (1961) 579; S. Weinberg, Phys. Rev. Lett. **19** (1967)1264;  
A. Salam, Proceedings of the 8th Nobel Symposium, p 367.

Local internal symmetry with **four** massless gauge fields  $SU(2) \times U(1)/U'(1)$

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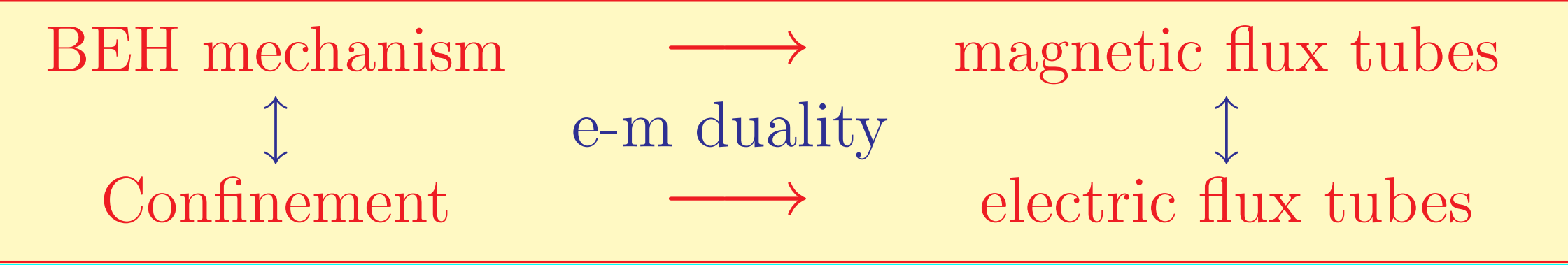
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S. Mandelstam, Phys. Rep. **23C** (1976) 245; C. Montonen and D.I. Olive, Phys. Lett. **B72** (1977)177 ; F. Englert and P. Windey, Nucl.Phys. **B135** (1978) 529; G 't Hooft, Nucl. Phys. **B138** (1978) 1.

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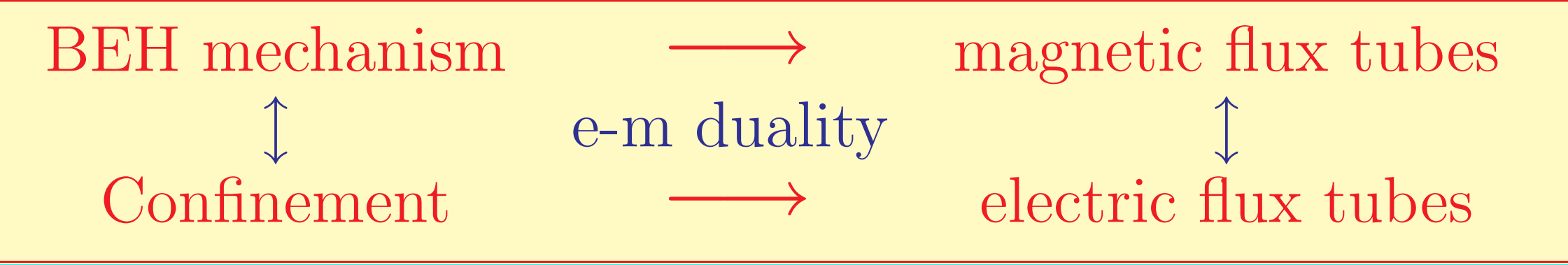
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## 3. Grand unification

H. Georgi, H.R. Quinn and S. Weinberg, Phys. Rev. Lett. **33** (1974) 451.



# 4. *The unification paradigm*

<b>electromagnetism</b>	<b>weak interactions</b>	<b>strong interactions</b>	<b>?</b>	<b>gravity</b>
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## *4. The unification paradigm*

### **Spontaneous symmetry breaking**

**electromagnetism**

**weak interactions**

**strong interactions**

**?**

**gravity**

## 4. *The unification paradigm*

### Spontaneous symmetry breaking

electromagnetism

weak interactions

strong interactions

?

gravity

*electroweak theory*

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graph TD; A[electromagnetism] --> C[electroweak theory]; B[weak interactions] --> C;
```

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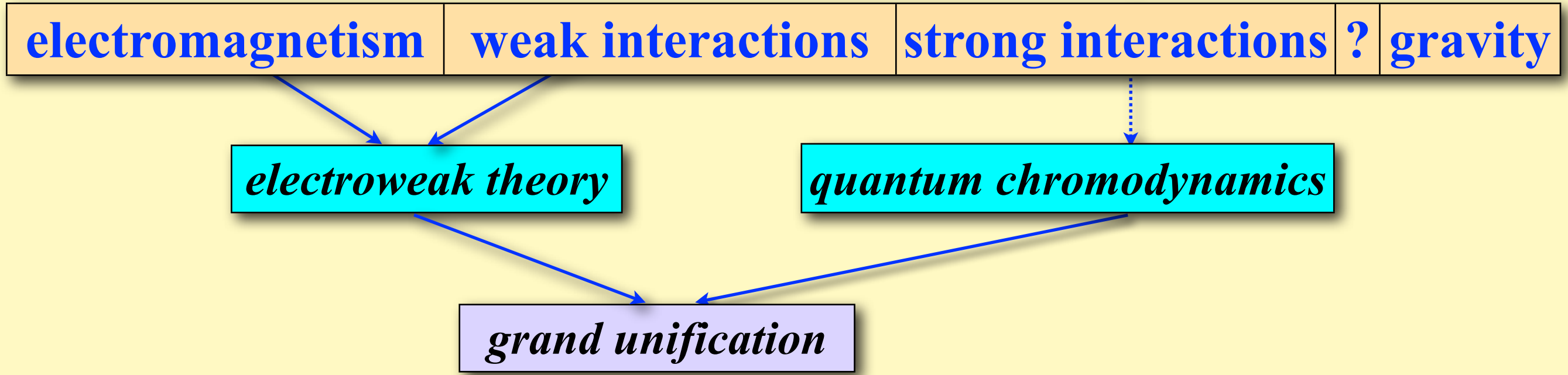
electromagnetism	weak interactions	strong interactions	?	gravity
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*electroweak theory*

*quantum chromodynamics*

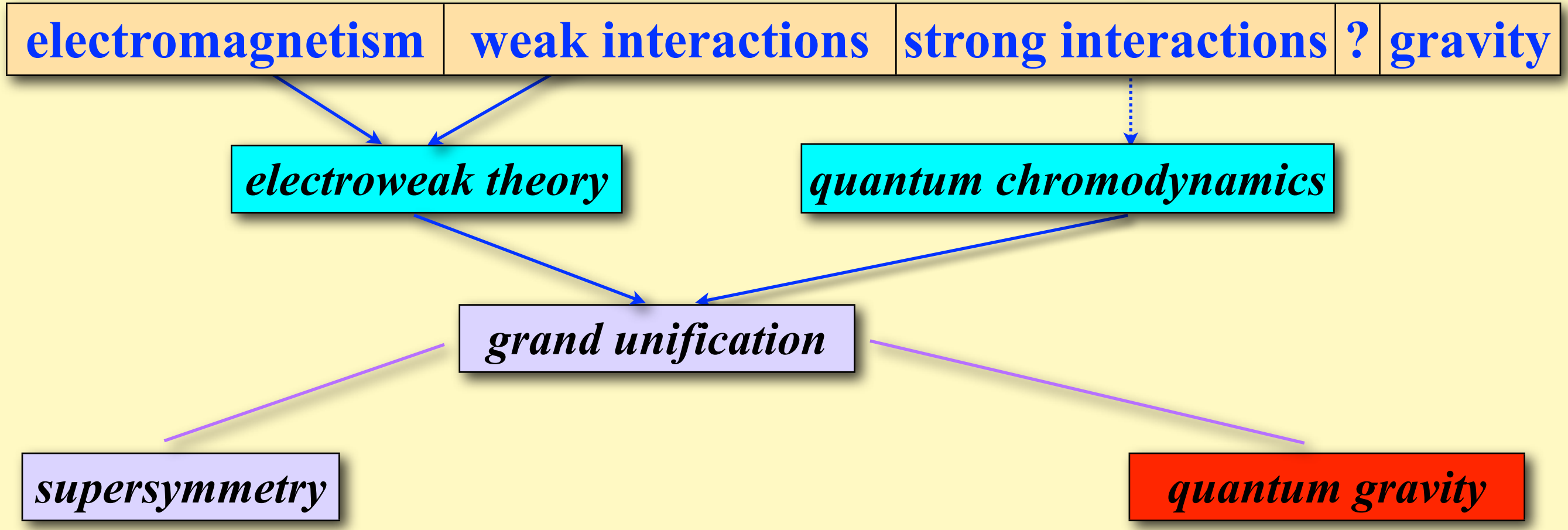
# 4. The unification paradigm

## Spontaneous symmetry breaking



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*electroweak theory*

*quantum chromodynamics*

*grand unification*

*supersymmetry*

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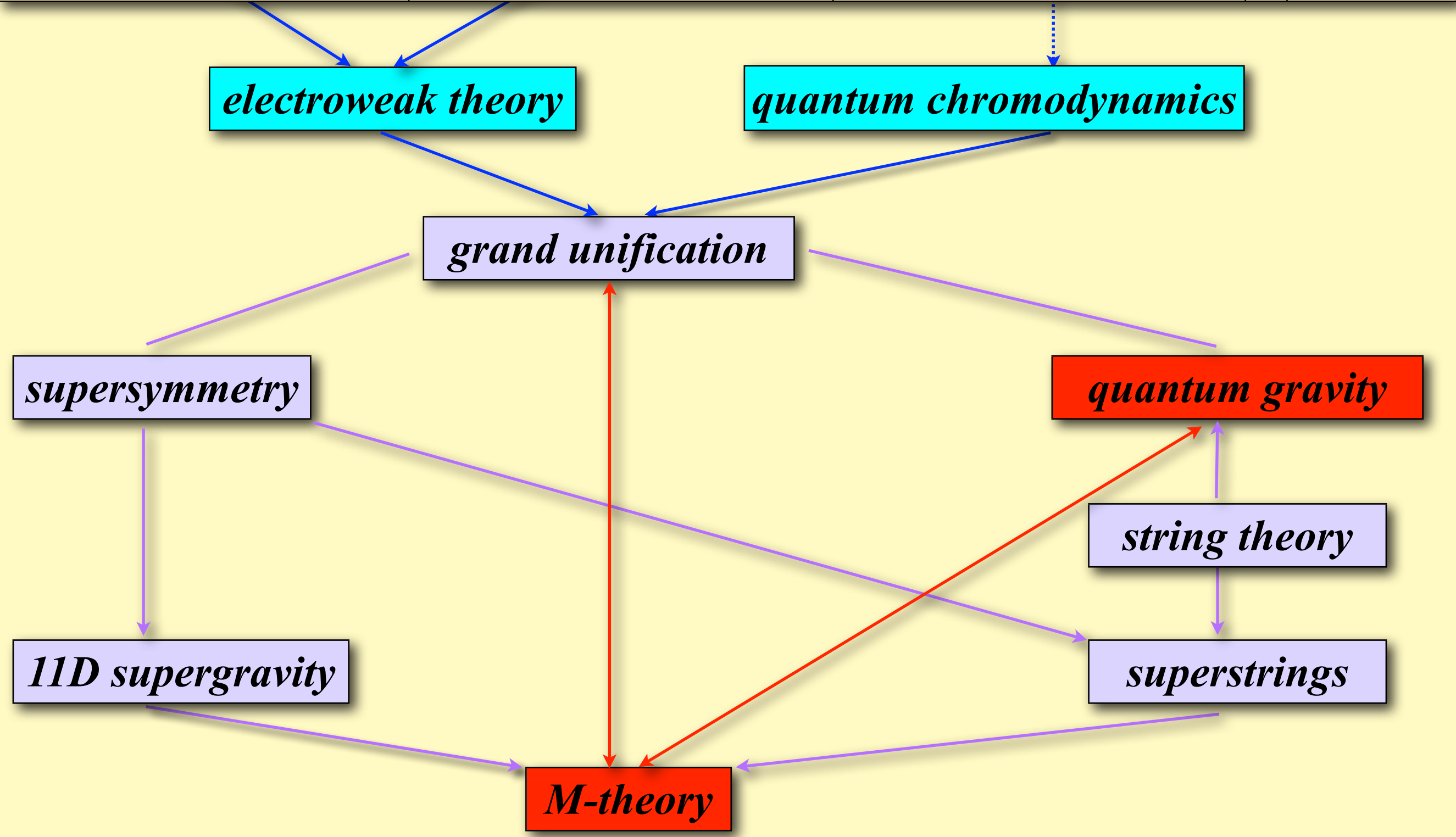
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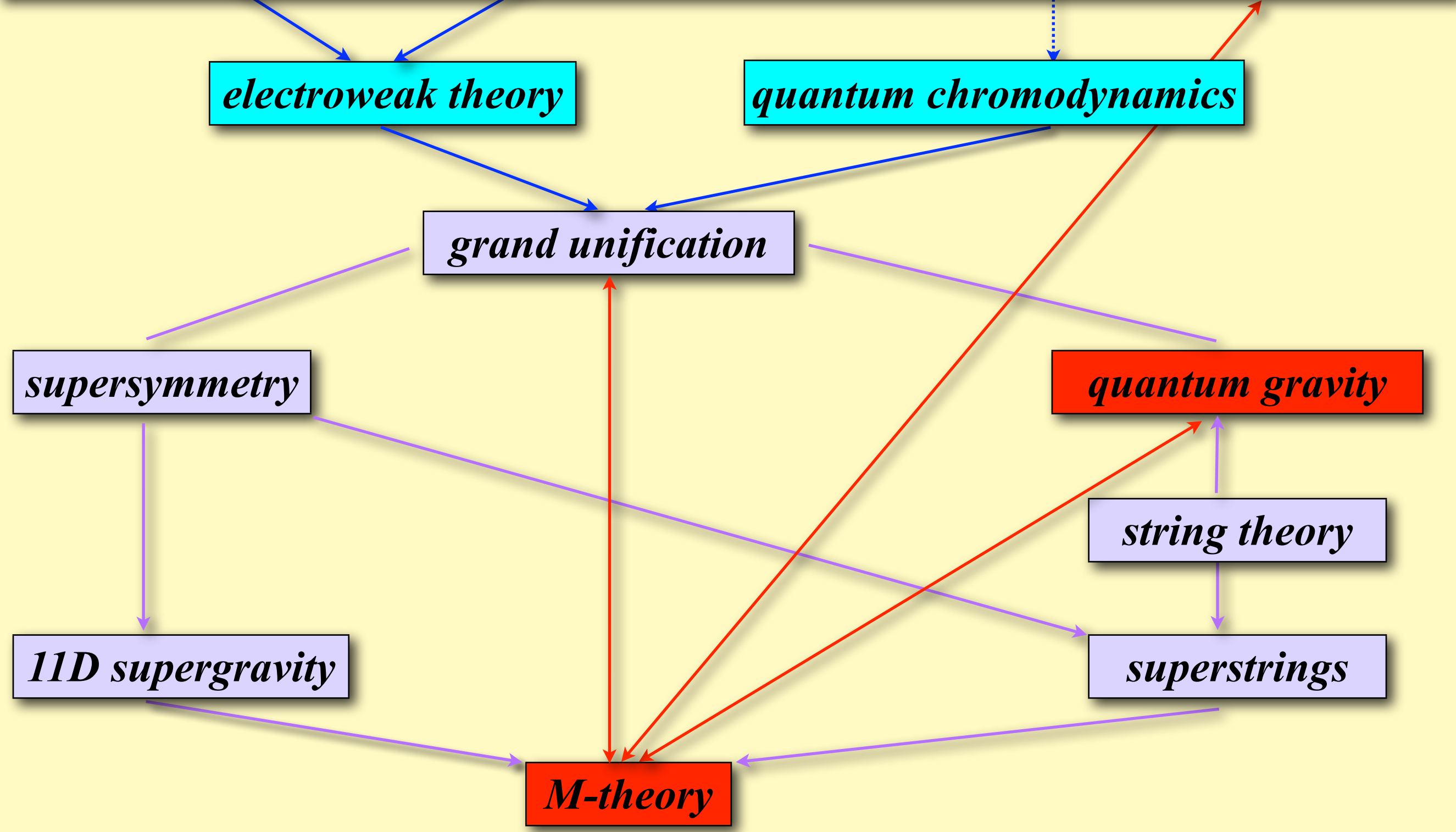
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## 4. *The unification paradigm*

### Spontaneous symmetry breaking

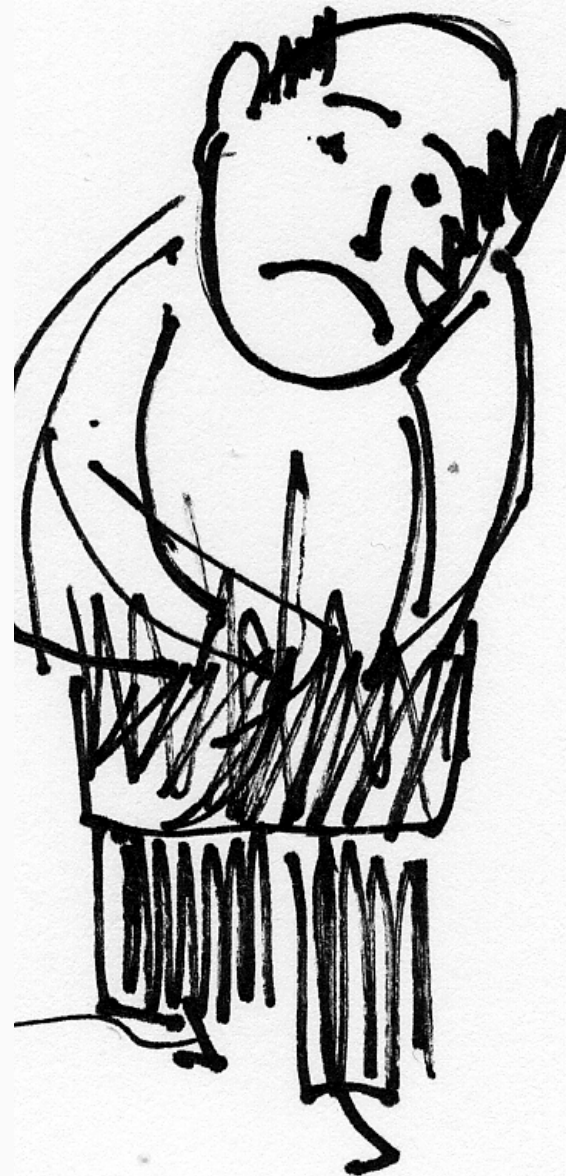
electromagnetism

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TOE

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