Composite Dynamics

Francesco Sannino

CP³ - Origins

Particle Physics & Origin of Mass

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CP3- Origins: 2009-20

Cp3-Origins

Discovering Technicolor

First Black Report

2011

Particle Physics & Origin of Mass

Composite Higgs physics @ LHC

A RUE

Conformal Dynamics for TeV Physics and Cosmology

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Abstract We introduce the topic of dynamical breaking of the electroweak symmetry and its link to unparticle physics and cosmology. The knowledge of the phase diagram of strongly coupled theories plays a fundamental role when trying to construct viable extensions of the standard model (SM). Therefore we present the state-of-the-art of the phase diagram for SU, Sp and SO gauge theories with fermionic matter transforming according to arbitrary representations of the underlying gauge group. We summarize several analytic methods used recently to acquire information about these gauge theories. We also provide new results for the phase diagram of the generalized Bars-Yankielowicz and Georgi-Glashow chiral gauge theories. These theories have been used for constructing grand unified models and have been th template for models of extended technicolor interactions. To gain information the phase diagram of chiral gauge theories we will introduce a novel all orders function for chiral gauge theories. This permits the first unified study of a supersymmetric gauge theories with fermionic matter representation bo and non-chiral. To the best of our knowledge the phase diagram of these models appears here for the first time. We will introduce recent exten SM featuring minimal conformal gauge theories known as minimal y els. Finally we will discuss the electroweak phase transition at nonzi for models of dynamical electroweak symmetry breaking.

* Lectures presented at the 49th Cracow School of Theoretical P



Standard Model











RXTE PUFFED ACCRETION DISK VERSION 2 WITH NO WOBBLE



ANIMATION BY DANA BERRY SKYWORKS DIGITAL ANIMATION 310-441-1735

Mystery of Mass



Riddles



Standard Model





WW Scattering



S-wave amplitude:

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$$A_{0} = \frac{G_{F}}{8\pi\sqrt{2}} \qquad G_{F} = \frac{g^{2}}{4\sqrt{2}M_{W}^{2}}$$
$$\simeq 1.14 \times 10^{-5} \text{GeV}^{-2}$$

Unitarity:

$$\Re \left[A_0 \right] \le \frac{1}{2} \quad \longrightarrow \quad s \le 4\pi \sqrt{2}/G_F \sim (1.2 \text{ TeV})^2$$



WW Scattering





$$A_0' = -\frac{G_F}{8\pi\sqrt{2}} \ s$$

Theorem:

Unitarity requires the existence of a weakly coupled Higgs particle or New Physics around the Terascale!





$$H = \frac{1}{\sqrt{2}} \left(\begin{array}{c} \pi_2 + i \, \pi_1 \\ \sigma - i \, \pi_3 \end{array} \right)$$

$[i\tau_2 H^*, H] = \frac{1}{\sqrt{2}} \left(\sigma + i\vec{\tau} \cdot \vec{\pi}\right) \equiv M$

$SU_L(2) \times SU_R(2)$

 $g_{L/R} \in SU_{L/R}(2) \qquad \qquad M \to g_L M g_R^{\dagger}$

 $m^2 < 0$





 $\sigma = v + h$



Gauge Boson-Masses

$$\frac{1}{2} \operatorname{Tr} \left[D_{\mu} M^{\dagger} D^{\mu} M \right] \longrightarrow M_{W} = gv/2 = M_{z} \cos \theta_{w}$$

$$\downarrow$$

$$SU_{L}(2) \times SU_{R}(2) \to SU_{V}(2)$$

$$e = g \sin \theta_{w} \quad \cos \theta_{w} = g/\sqrt{g^{2} + {g'}^{2}}$$

Quark-Masses

$$-\lambda_d \bar{Q}_L \cdot H d_R \longrightarrow m_d = \lambda_d v / \sqrt{2}$$

Higgs mechanism in Nature

Superconductivity

Macroscopic-Screening Non-Relativistic

SM-Screening Relativistic

0

 $T < T_c$

 $n_s = \text{Density SC electrons}$

$$|\psi|^2 = n_C = \frac{n_s}{2} \qquad |H|^2 = \frac{v^2}{2}$$

Superconductivity

Meissner-Mass Static Vector Potential

$$M^2 = q^2 n_s / 2m$$

$$m = 2m_e \quad q = -2e$$

$$n_s \sim 4 \times 10^{28} m^{-3}$$

Weak-GB-Mass

$$M_W^2 = g^2 v^2 / 4$$

 $M_W \sim 80 \ GeV$

 $\xi = 1/M \sim 10^{-6} cm$

Hidden structure

$$\xi_W = 1/M_W \sim 10^{-15} cm$$

????

Fermi Scale

 $v = 1/\sqrt{\sqrt{2}G_F} \approx 246 \text{ GeV}$

 $M_H^2 = 2\lambda v^2$



SM - Geometry



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Many Models



Technicolor - Geometry



Dynamical EW Breaking

$$L(H) \to -\frac{1}{4} F^{a\mu\nu} F^a_{\mu\nu} + i \bar{Q} \gamma^\mu D_\mu Q + \cdots$$

Dots are partially fixed by Anomalies as well as other principles

$\cdots \longrightarrow L(\text{New SM Fermions})$



New Strong Interactions at ~ 250 GeV [Weinberg, Susskind]

Natural to use QCD-like dynamics.

 $SU(N)_{TC} \times SU(3)_C \times SU_L(2) \times U_Y(1)$

$$\langle Q^f \tilde{Q}_{f'} \rangle = \Lambda_{TC}^3 \qquad \qquad \Lambda_{TC} \simeq 1 \text{ TeV}$$





$$\Pi_{XY}^{\mu\nu}(q^2) = \Pi_{XY}(q^2)g^{\mu\nu} + \cdots$$

Kennedy-Lynn, Peskin-Takeuchi, Altarelli-Barbieri, Bertolini- Sirlin, Marciano-Rosner

S & T

S-measures the left - right type current correlator

$$S = -16\pi \frac{\Pi_{3Y}(m_Z^2) - \Pi_{3Y}(0)}{m_Z^2}$$

T-measures deviations from

$$m_{\rm W}^2 = \cos^2 \theta_{\rm W} \, m_{\rm Z}^2$$

$$T = 4\pi \frac{\Pi_{11}(0) - \Pi_{33}(0)}{s_W^2 c_W^2 m_Z^2}$$

Need novel dynamics

Large & Positive S from QCD-like Technicolor



SM Fermion Masses

Extending Technicolor



Different Approaches

Scalar-less New Gauge Interactions (Extended TC)

Marry SUSY and Technicolor

....

Add New Scalars in the Flavor Sector

Extended Technicolor





Need to go beyond QCD

Near Conformal



Why walking helps?

$$\left\langle \bar{Q}Q_{ETC} \right\rangle = \exp\left(\int_{\Lambda_{TC}}^{\Lambda_{ETC}} d\ln(\mu) \ \gamma_m(\alpha(\mu))\right) \left\langle \bar{Q}Q_{TC} \right\rangle$$

<u>QCD-Like</u>

$$\exp\left(\int_{\Lambda_{TC}}^{\Lambda_{ETC}} d\ln(\mu) \ \gamma_m(\alpha(\mu))\right) \sim (\ln(\Lambda_{ETC}/\Lambda_{TC}))^{\gamma_m}$$

Near the conformal window

$$\exp\left(\int_{\Lambda_{TC}}^{\Lambda_{ETC}} d\ln(\mu) \ \gamma_m(\alpha(\mu))\right) \sim \left(\left(\Lambda_{ETC}/\Lambda_{TC}\right)^{\gamma_m(\alpha^{\star})}\right)$$
$$m_{\rm f} \approx \frac{g_{ETC}^2}{\Lambda_{ETC}^2} < \bar{Q}Q >_{ETC} = \frac{g_{ETC}^2}{\Lambda_{ETC}^2} \left(\frac{\Lambda_{ETC}}{\Lambda_{TC}}\right)^{\gamma_m(\alpha^*)} < \bar{Q}Q >_{TC}$$

If large anomalous dimension, around $\gamma_m(\alpha^*) \sim 1.7$

Fermion Mass Enhancement & FCNC decoupling

Selecting Nature's Next Force





Gauge Theories

Gauge Group

Matter



Xtreme-conditions











Free Electric



Coulomb







 $V \propto \sigma r$

Asymptotic safety



Knobs



Gauge Group, i.e. SU, SO, SP

Matter Representation

of Flavors per Representation



A novel phase @ large Nf

Interesting structure at large Nf

Pica & Sannino 10

Entire series at large Nf is known



Universal Picture

SU(N) Phase Diagram



What is the use?





Ideal?



Walking is highly fine tuned

Anomalous dimensions are small

Ideal walking

Fukano & Sannino 10

$$L(H) \rightarrow -\frac{1}{4} F^{a\mu\nu} F^a_{\mu\nu} + i \bar{Q} \gamma^\mu D_\mu Q + \cdots$$

$$(\alpha_{ab} \frac{\bar{Q} T^a Q \bar{Q} T^b Q}{\Lambda_{ETC}^2} + \beta_{ab} \frac{\bar{Q}_L T^a Q_R \bar{\psi}_R T^b \psi_L}{\Lambda_{ETC}^2} + \gamma_{ab} \frac{\bar{\psi}_L T^a \psi_R \bar{\psi}_R T^b \psi_L}{\Lambda_{ETC}^2} + \dots$$

Gauged Nambu Jona-Lasinio

- * As if the number of flavors is continuous
- Anomalous dimensions increase



- Phenomenologically viable
- Being tested!



S in Gauge Theories

$$i\Pi^{a,b}_{\mu\nu}(q) \equiv \int d^4x \, e^{-iqx} \left[\langle J^a_{\mu,V}(x) J^b_{\nu,V}(0) \rangle - \langle J^a_{\mu,A}(x) J^b_{\nu,A}(0) \rangle \right]$$

$$\Pi^{a,b}_{\mu\nu}(q) = \left(q_{\mu}q_{\nu} - g_{\mu\nu}q^{2}\right)\,\delta^{ab}\Pi(q^{2})$$

$$S[q^2] = -16\pi \frac{\Pi(q^2) - \Pi(0)}{q^2}$$

• This is not automatically the phenomenological S-parameter

• Unambiguous

• It is the definition to use in lattice simulations

Open Questions



• Does S vanish as we approach the conformal window ?

• What happens at the lower boundary ?

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• What is its value inside the conformal window ?

Perturbative Conformal S



One - loop

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Conformal limit

$$\lim_{\frac{m^2}{q^2} \to 0} \Re[S] = x \frac{\sharp}{\pi} \left[2 + \log(x)\right] + \mathcal{O}(x^2)$$



$$\sharp = N_D \, d[r] \qquad x = \frac{m^2}{q^2}$$



• Real and Imaginary part vanish

Sannino 1006.0207

One - loop S-ummary



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Di Chiara, Pica, Sannino 10

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CP³ - Origins Particle Physics & Origin of Mass Conformal S @ 2 loops



N

CP³ - Origins Particle Physics & Origin of Mass Conformal S O 2 LOOPS















Sannino PRL, 10



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S - conjecture

Sannino 1006.0207

$$\lim_{\frac{q^2}{m^2} \to 0} \frac{6\pi S}{N_D d[r]} = S_{\text{norm}} \ge 1$$

S increases as Nf decreases
S counts relevant degrees of freedom
S tests weak-strong gauge duality

Sannino 1007.0254

Tested to higher loops: Di Chiara, Pica, Sannino 10

Strong constraints for old models!

In fact ...

 $S = S_{(W)TC} + S_{NS}$

Offset the first term

Rule:

Find WT minimizing the lower bound for S

Minimal Working TC

• Minimal WT $SU(2)_{TC}$ \square $\begin{bmatrix} U & N \\ D & E \end{bmatrix}$

Sannino & Tuominen 04 Dietrich, Sannino, Tuominen 05 Frandsen, Masina, Sannino 09

•Next to MWT

 $SU(3)_{TC} \square \begin{bmatrix} \mathbf{U} \\ \mathbf{D} \end{bmatrix}$

Sannino, Tuominen 04 Dietrich, Sannino, Tuominen 05

•Orthogonal $SO(4)_{TC} \square \begin{matrix} \mathbf{U} \\ \mathbf{D} \end{matrix}$

Frandsen, Sannino 09

•Ultra MT $SU(2)_{TC}$ \Box $\begin{bmatrix} \mathbf{U} \\ \mathbf{D} \end{bmatrix}$ Ryth

Ryttov & Sannino 08

Vanilla TC & Scooby -Doo



Minimal Walking Technicolor



U and **D**: Adj of SU(2)


 $S = S_{(W)TC} + S_{NS}$

Offset the first term

New Leptons

Fermions :
$$\psi_L = \begin{pmatrix} \psi_{1L} \\ \psi_{2L} \end{pmatrix}$$
, ψ_{1R} , ψ_{2R}
Hypercharge : Y , $Y + \frac{1}{2}$, $Y - \frac{1}{2}$

$$S_{\text{Leptons}} = \frac{1}{6\pi} \left[1 - 2Y \ln\left(\frac{M_1}{M_2}\right)^2 + \frac{1 + 8Y}{20} \left(\frac{m_Z}{M_1}\right)^2 + \frac{1 - 8Y}{20} \left(\frac{m_Z}{M_2}\right)^2 + O\left(\frac{m_Z^4}{M_i^4}\right) \right]$$

$$M_{1,2}^2 \gg m_Z^2$$

New Leptons & Precision Data



Exotic Leptonic hypercharge Y=-3/2

Standard Model Leptonic hypercharge

MWT Features

- The most economical WT theory
- Compatible with precision measurements
- Possible DM candidates and Unification
- Can support 1st order Electroweak Phase Transition
- Features a light composite Higgs Dietrich, F.S., Tuominen 05.
 Da Silva, Doff, Natale 08, 09.
- Lattice studies have begun

MWT Effective Lagrangian

 $\mathcal{L}(\text{Composites}) + \mathcal{L}(\text{Mixing with SM}) + \mathcal{L}(\text{New Leptons}) + \mathcal{L}(\text{SM} - \text{Higgs})$

Composite Higgs

Composite Axial - Vector States



Heavy Electron

2 Heavy Majoranas



Hapola, Masina, Sannino 11

Frandsen, Masina, Sannino 09

Constraining MWT



Belyaev, Foad, Frandsen, Jarvinen, Pukhov, Sannino 08 M_A (TeV)



- Implement technibaryon sector of MWT in CalCHEP MadGraph
- Composite fermions in MWT
- Topological terms (in progress)
- Orthogonal technicolor
- Implement Ultra Minimal Walking Technicolor
- Supersymmetric extension of Minimal Walking Technicolor

New life in Technicolor



Not the Coldplay album



Dark Matter



 $\frac{\Omega_{DM}}{\Omega_B}\sim 5$

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First evidence for DM



- # 1953 F. Zwicky found the first evidence for DM
- Welocity dispersion of the galaxies in the COMA cluster
- Dark Matter was dubbed then!

Cluster Evidence Today

- From X-ray emission: Stronger evidences
- Temperature of the cluster gas too high!
- Factor 5 higher than the one from baryonic matter



Bullet Cluster



Self interactions

From bullet cluster one deduces:

Markevitch et al. 03

$$\sigma \le 1.7 \times 10^{-24} \mathrm{cm}^2 \sim 10^9 \mathrm{pb}$$

- Stronger constraints requiring large cores of clusters.
 Yoshida, Springer & White 00
- Sphericity of halos.

Galactic Scales

Stars in the outer part of galaxies rotate faster than expected!



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Galactic Scales



- Density is uncertain in the internal regions of galaxies
- Data & numerical simulations: Isothermal, NFW, Moore, Kratsov, Einasto, etc...

$$\rho(r) = \frac{\rho_0}{\left(\frac{r}{R}\right)^{\gamma} \left[1 + \left(\frac{r}{R}\right)^{\alpha}\right]^{\frac{\beta - \gamma}{\alpha}}}$$

Large structure formation

V. Springel, MPA Munich

Yoshida et al. 03

Eugenio Del Nobile

DM Properties

- Interacts gravitationally
- Electrically neutral and decoupled from primordial plasma
- Lead to correct density profile for galaxy rotation curves
- Cold DM: Must cluster & lead to structure formation
- Either stable or very long lived

DM candidates in SM?

LSS constrain also

 $m_{\nu} \le 0.27 - 1 \text{eV} \implies \Omega_{\nu} \ll \Omega_{DM}$

Charged

- Decaying too soon/
 Charged
- Baryonic / Charged
- Massless like graviton
- For thermal neutrinos

$$\Omega_{\nu}h^2 \sim \frac{\sum_i m_{\nu i}}{93 \text{eV}} \le 0.07$$

 $m_{\nu} \leq 2 \text{eV} \text{ (Tritium } \beta \text{ decay)}$

What makes DM?

DM candidates

- Minimal Supersymmetric Standard Model
- Axion
- # Just another particle with no links to SM

New strong force with new quarks (technibaryon, meson, ...)

Un-baryons

貒

Incomplete list

DM asymmetry

A particle similar to the nucleon

- Electrically neutral
- At most EW-type cross sections
- Great if connected to EW (Observable at LHC)

(Un)TC Interact. Massive Particle (u)TIMP

TIMPs	Masses	Annih.	Asymm	Symm	Models
TC-Baryon	(I - 3)TeV	_	Х	-	Complex-Rep Traditional TC
TC-PGB	5 GeV5 TeV	Х	Х	Х	(Pseudo)-Real (UMT, MWT, OT)
Unbaryon	(- 0) GeV	X	X	X	Techni-unparticle

Nussinov, 86 Barr - Chivukula - Farhi 90 Sarkar 96 Gudnason - Kouvaris - F.S. 06 Foadi, Frandsen, Sannino 09 Nardi, Sannino., Strumia, 08. Sannino, 10

TC-Baryon

TC-PGB

Gudnason - Kouvaris - Sannino. 06 Ryttov - Sannino 08 Frandsen & Sannino. 09 Unbaryon

D.B. Kaplan 92 Sannino, Zwicky 09 Frandsen, Sarkar, 10

Related

Kouvaris 06,07,10 Kainulainen, Virkajarvi, Tuominen 06,09,10

Mixed TIMP DM

Belyaev, Frandsen, Sannino, Sarkar 10

DM and GUTs

Nardi, FS, Strumia, 08.

Del Nobile, Kouvaris, Sannino II

Interfering Composite ADM

CoGeNT and DAMA

Del Nobile, Kouvaris, Sannino II

• DEWSB can naturally occur at the LHC

• Phase Diagram of strongly interacting theories

• Minimal models of technicolor are near conformal

• Composite Dark Matter

• Composite inflation... to discuss another time.