

What is “Discovering SUSY” ?

- E.g. – what makes Supersymmetry different to Universal Extra Dimensional models with Kaluza-Klein particles.
- One part of the answer:

SPIN



QUACK !



QUACK !

Not all things that quack are ducks!

We will see two important themes:

- Mass measurements will precede^(*) spin determinations
- “Spin measurement”^(**) should not be confused with “sensitivity to spin”

(*) or will at best be simultaneous with

(**) Here “spin measurement” means “determining unambiguously the correct nature (scalar, fermion, vector) of one or more particles in a decay chain or model”

(more info at)

A REVIEW OF SPIN DETERMINATION AT THE LHC

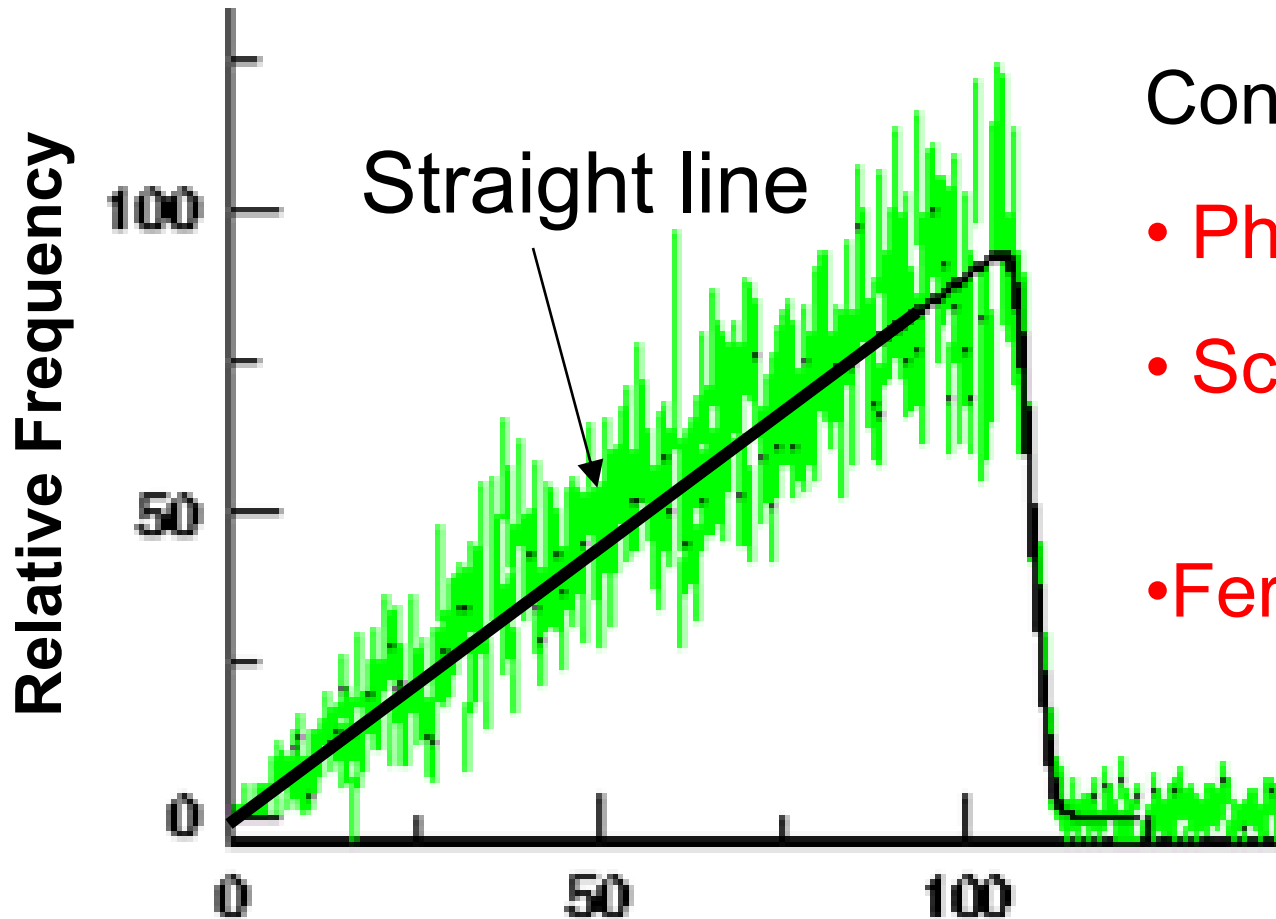
Lian-Tao Wang and Itay Yavin

[arXiv:0802:2726](https://arxiv.org/abs/0802.2726)

Spin determination topics

- Consistency checks
- Spins in “QLL chain”
 - A.Barr hep-ph/0405052
 - Smillie et al hep-ph/0605286
 - Florida etc [arXiv:0808.2472](https://arxiv.org/abs/0808.2472)
 - Biglietti et al ATL-PHYS-PUB-2007-004
- Slepton Spin (production)
 - A.Barr hep-ph/0511115
- MAOS method
 - Cho, Kong, Kim, Park arXiv:0810.4853
- Gluino chain spin
 - Alvez, Eboli, Plehn hep-ph/0605067
- Spins in chains with charginos
 - Wang and Yavin hep-ph/0605296
 - Smillie hep-ph/0609296
- Spins in chains radiating photons
 - Ehrenfeld et al arXiv:0904.1293

Spin Consistency Check

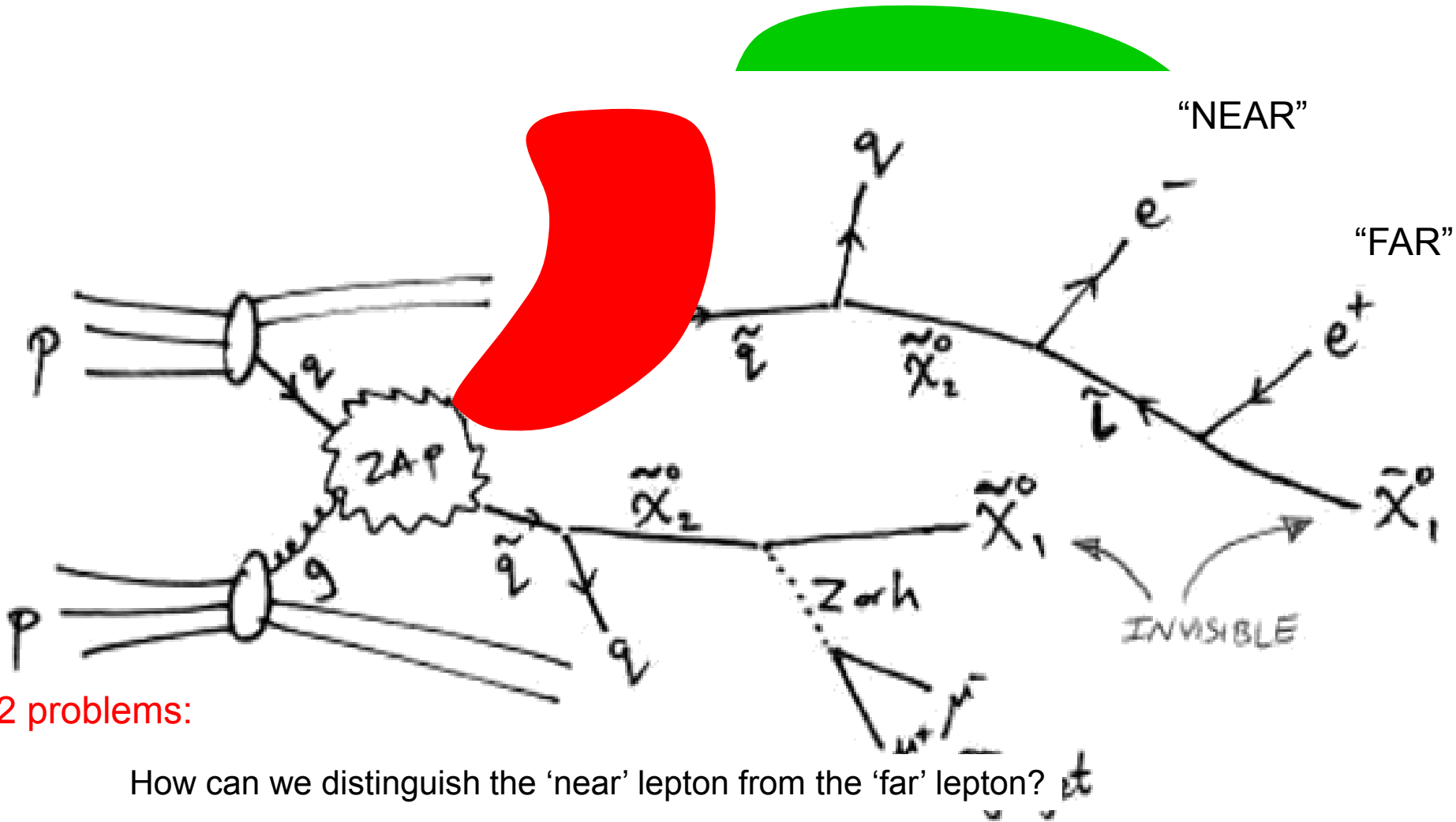


Consistent with:

- Phase-space
- Scalar slepton (SFSF)
- Fermion KK lepton (FVFFV)

Di-Lepton Invariant Mass (GeV)

QL Spin Determination (A.Barr)



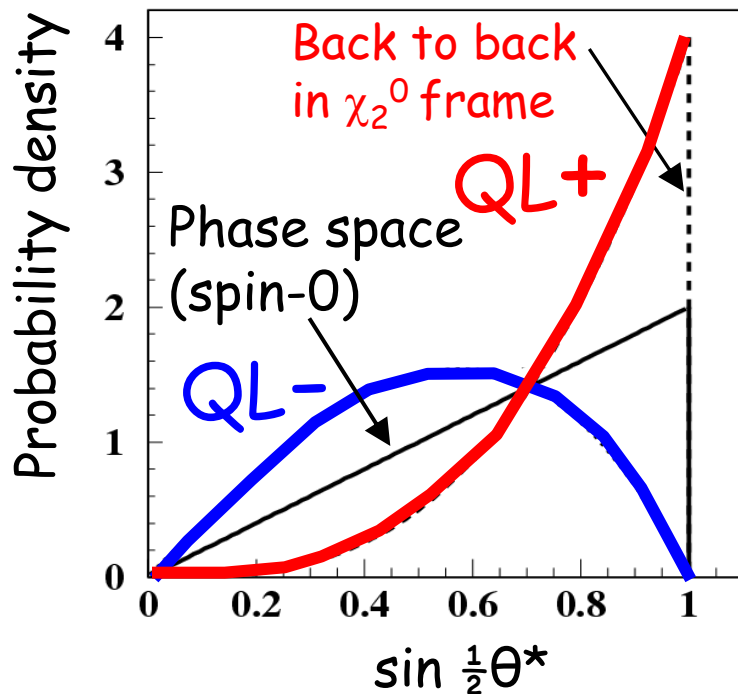
2 problems:

How can we distinguish the ‘near’ lepton from the ‘far’ lepton?

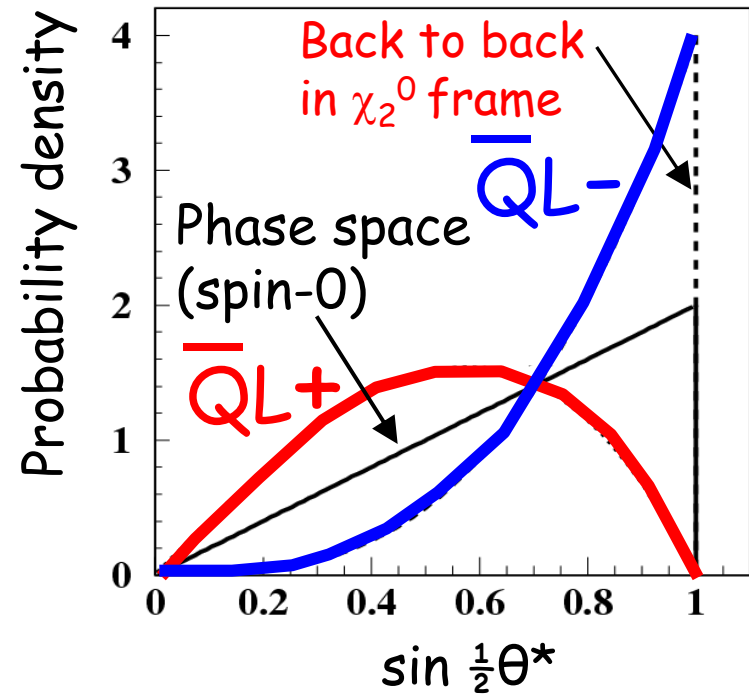
How can we tell $l^+ q$ from $l^+ \bar{q}$?

Quark+NearLepton invariant mass distributions for:

L+ **L-** and
QUARKS



L+ **L-** and
ANTI-QUARKS

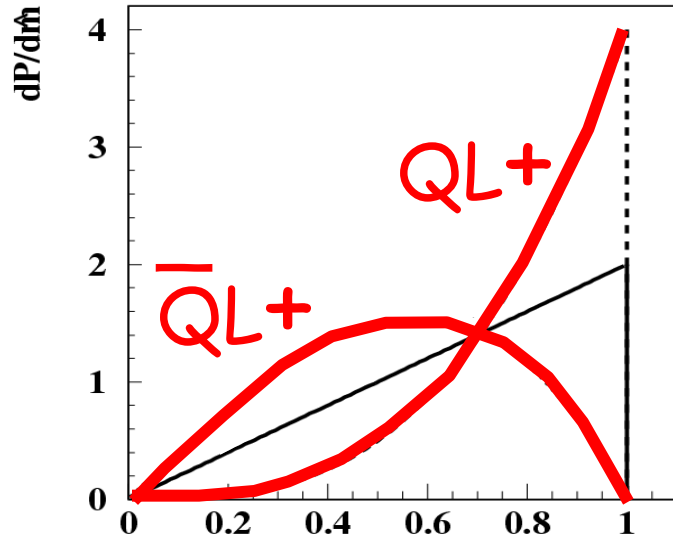


Experimental problem

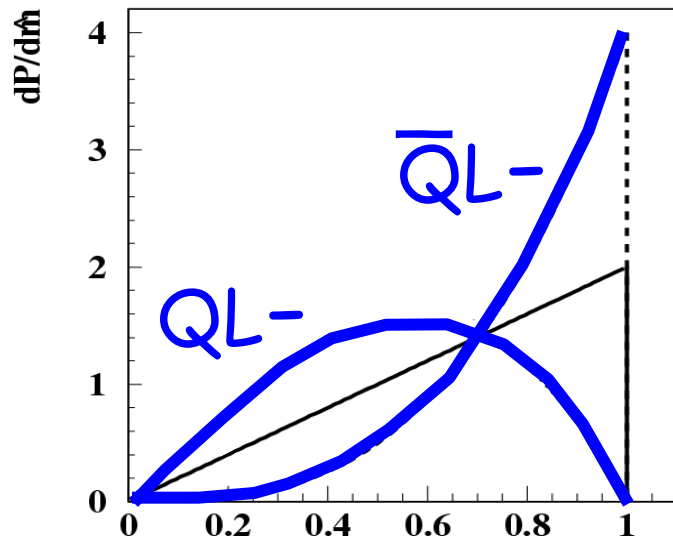
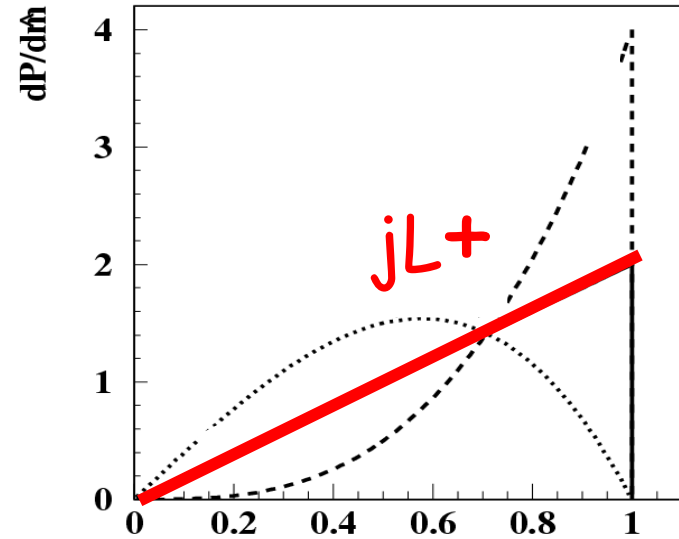
- Cannot reliably distinguish **QUARKs** from **ANTI-QUARKs**

Can only distinguish lepton charge
RED(Q_L^+ , \bar{Q}_L^+) from **BLUE**(Q_L^- , \bar{Q}_L^-)

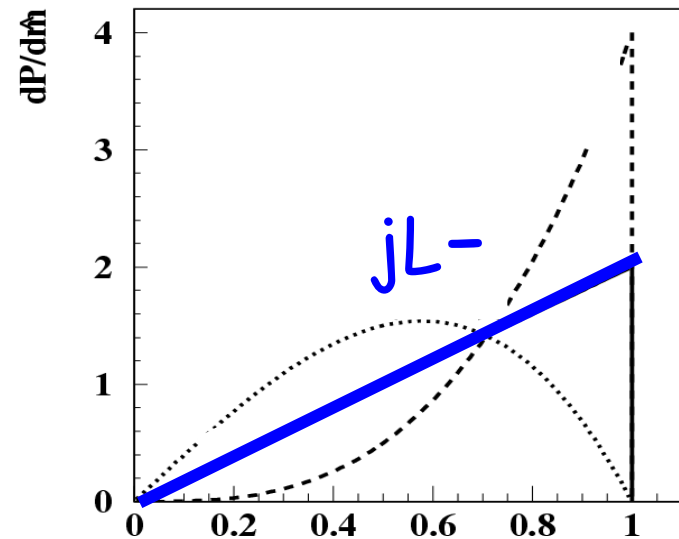
Expect QUARK and ANTI-QUARK contributions to cancel:



SUM \rightarrow

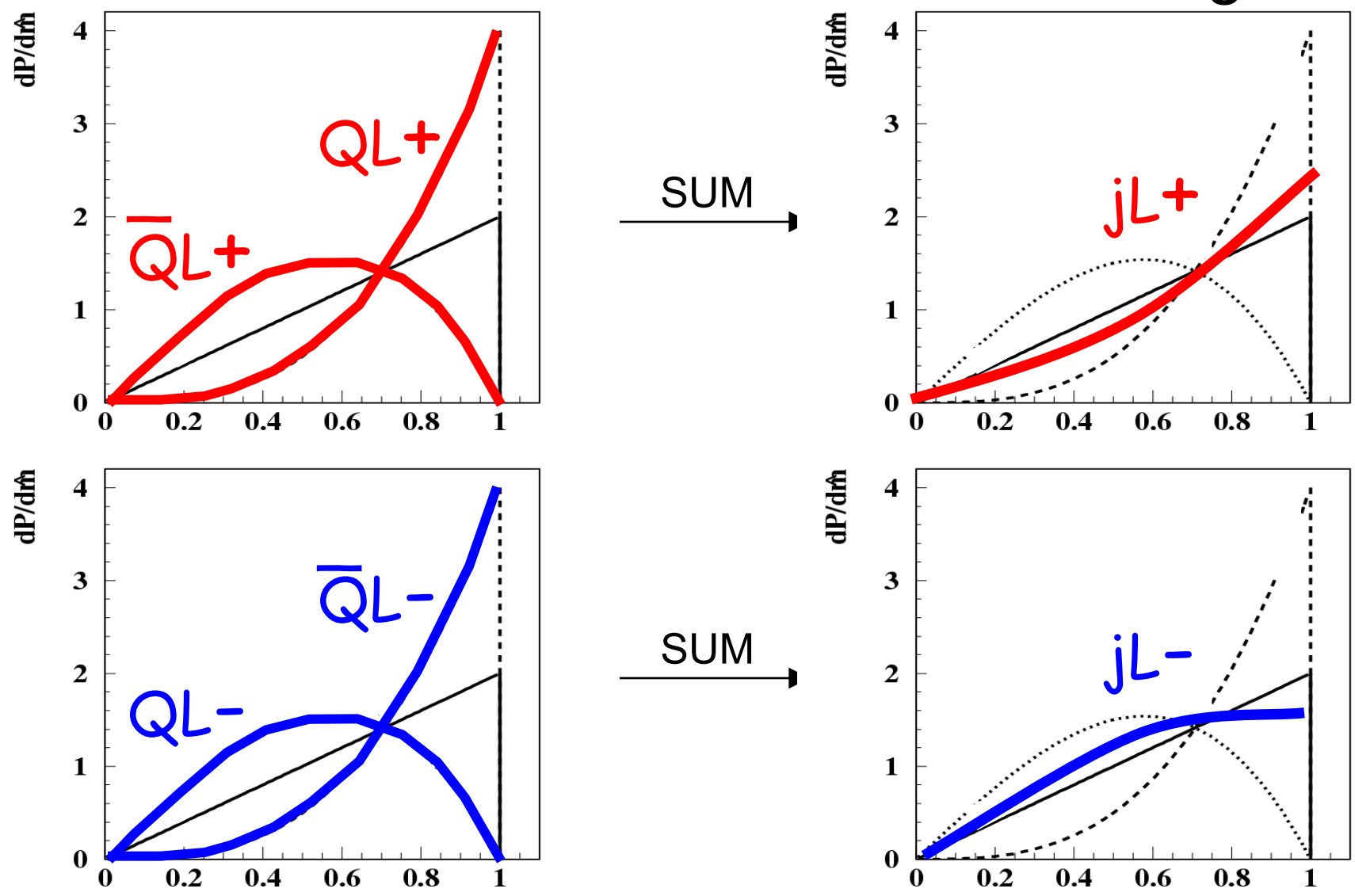


SUM \rightarrow



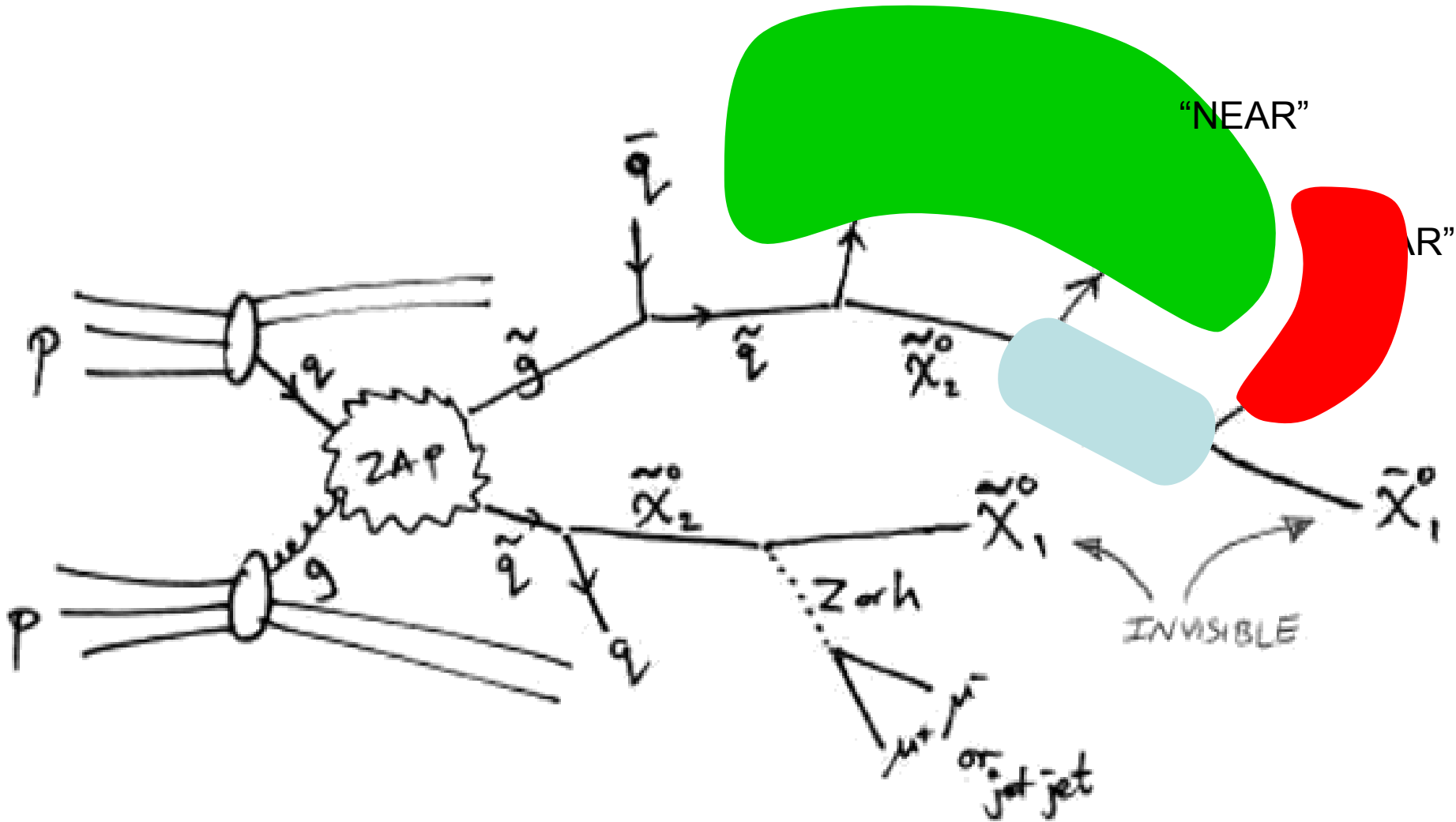
But LHC is Proton-Proton machine

- More Quarks than Anti-Quarks! So get:

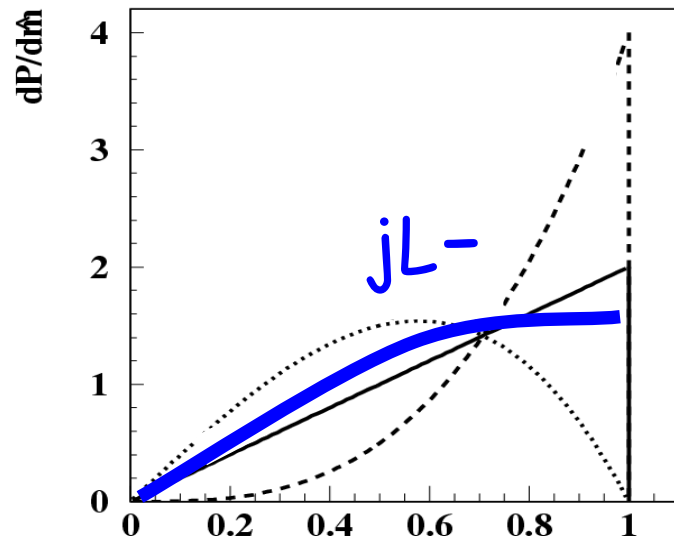
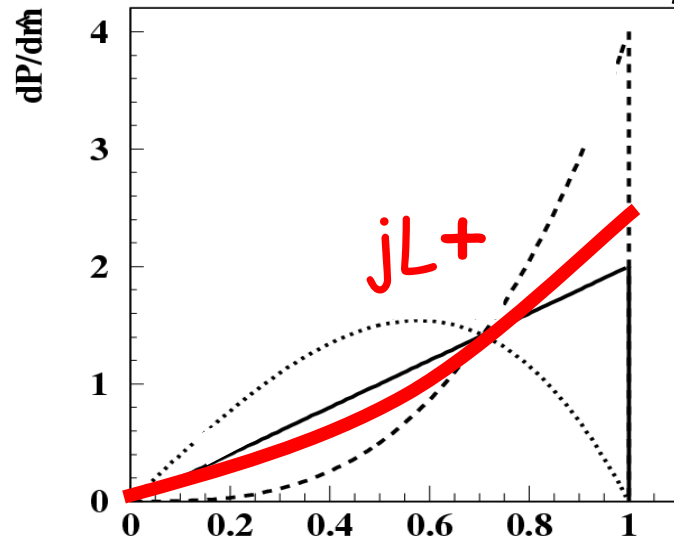


Asymmetry!

“Far” Lepton washout?

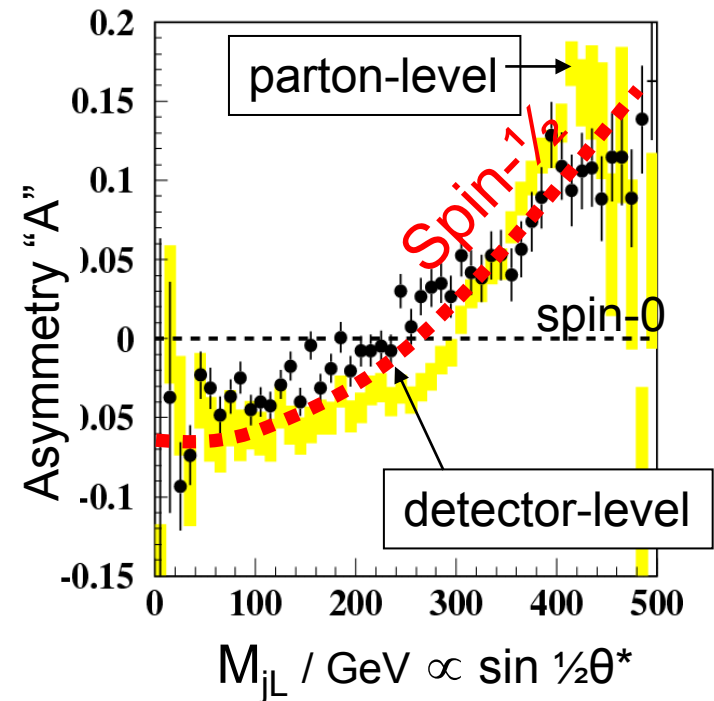


So define m_{jL^+} , m_{jL^-} asymmetry



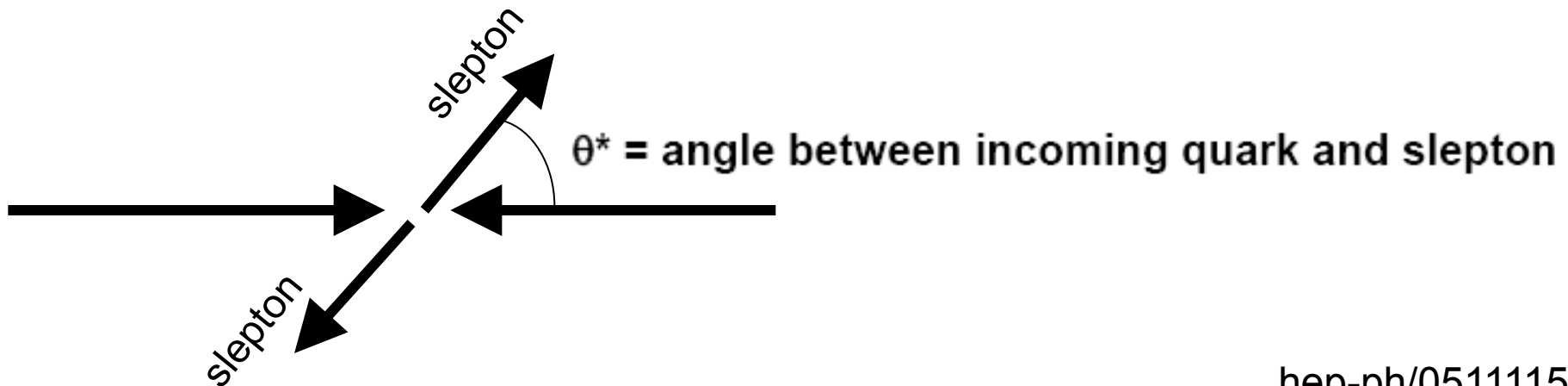
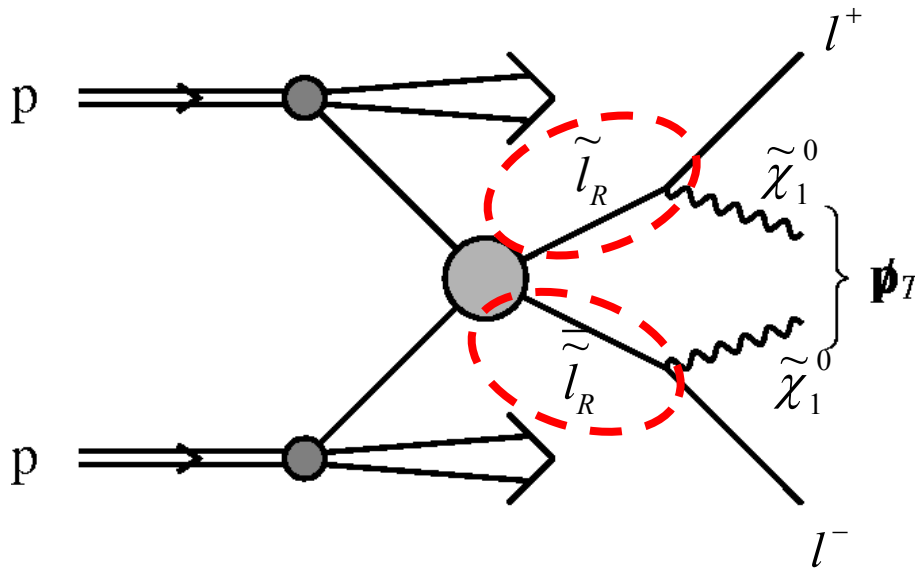
$$A = \frac{s^+ - s^-}{s^+ + s^-}$$

where $s^\pm = \frac{d\sigma}{dm_{jL^\pm}}$



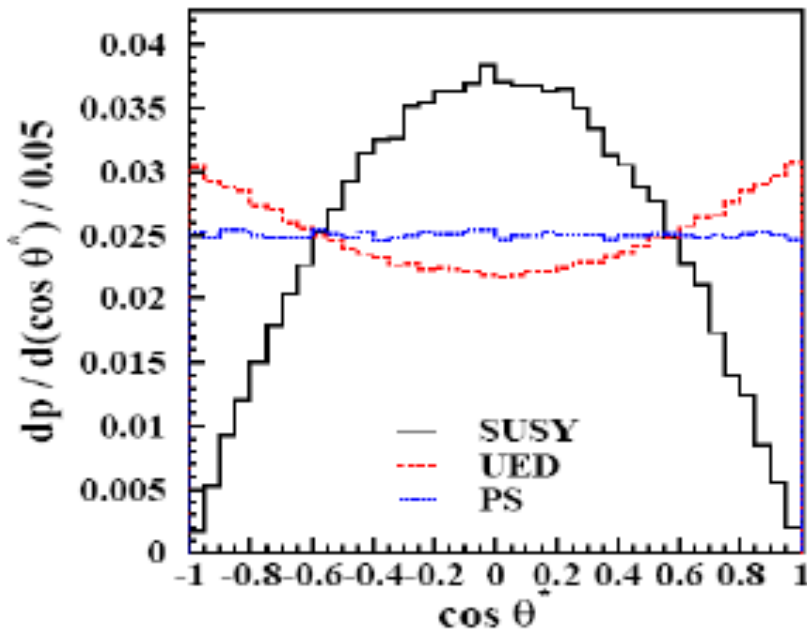
Different method altogether

Direct slepton spin detection: $qq \rightarrow Z\gamma^* \rightarrow \text{slepton slepton}$



Look at slepton production angle in c.o.m.

- θ^* = angle between incoming quark and slepton



$$\left(\frac{d\sigma}{d \cos \theta^*} \right)_{\text{SUSY}} \propto 1 - \cos^2 \theta^* \quad \text{SUSY = LHC point 5}$$

$$\left(\frac{d\sigma}{d \cos \theta^*} \right)_{\text{PS}} \propto \text{constant}$$

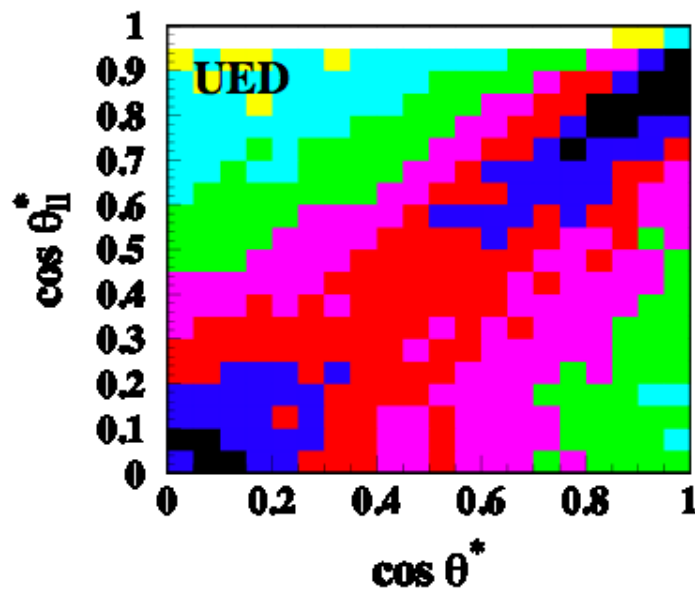
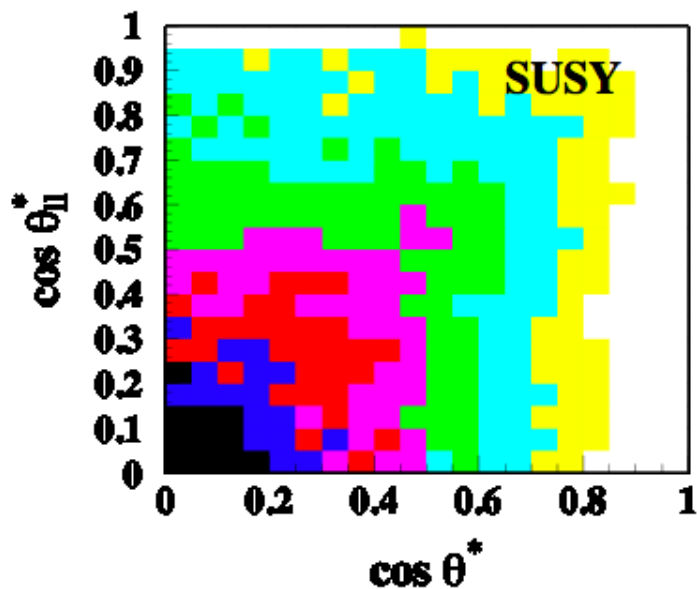
$$\left(\frac{d\sigma}{d \cos \theta^*} \right)_{\text{UED}} \propto 1 + \left(\frac{E_{\ell_1}^2 - M_{\ell_1}^2}{E_{\ell_1}^2 + M_{\ell_1}^2} \right) \cos^2 \theta^*$$

Sensitive to spin, but can we measure θ^* ?

Define: $\cos \theta_u^* \equiv \cos \left(2 \tan^{-1} \exp(\Delta\eta_{e^+e^-}/2) \right) = \tanh(\Delta\eta_{e^+e^-}/2)$

Have some access to desired angle

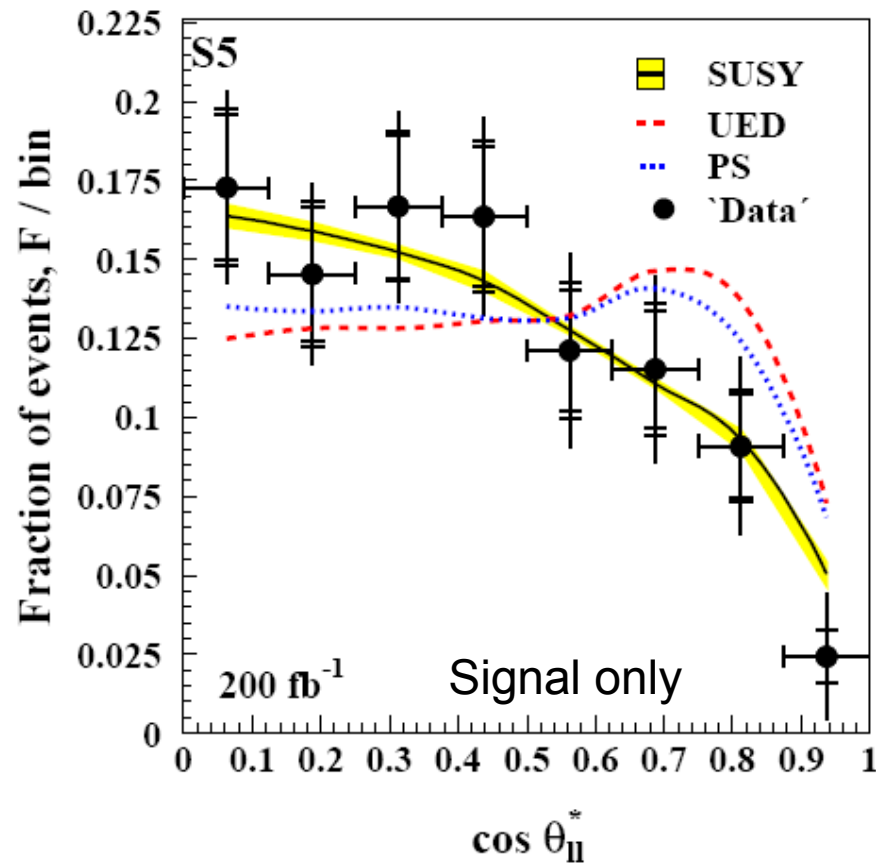
Distribution of $\cos \theta_{ll}^* \equiv \tanh(\Delta\eta_{\ell+\ell^-}/2)$
is correlated with Z^0/γ decay angle θ^*



Direct slepton spin (A.Barr)

hep-ph/0511115

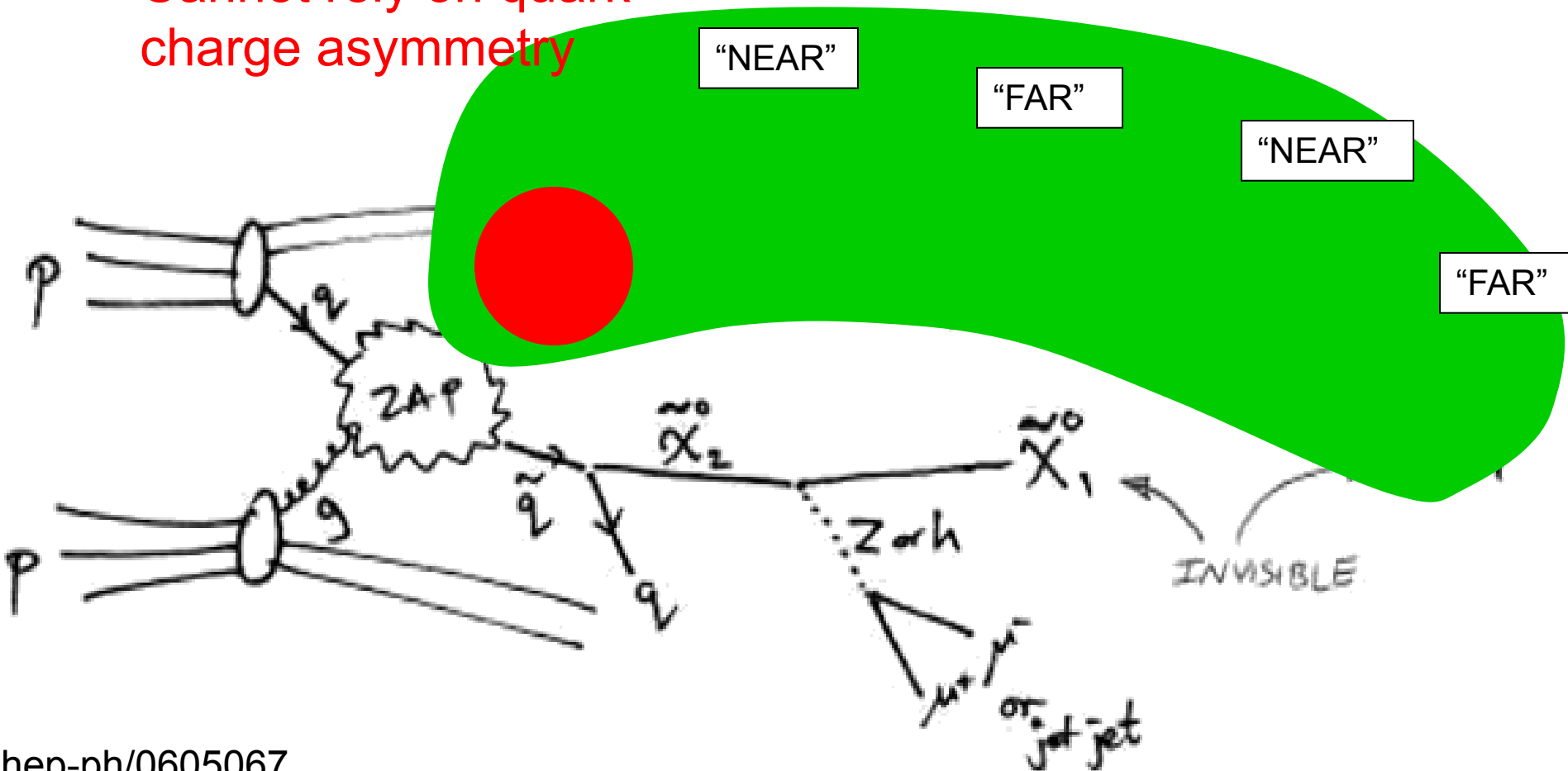
2 years high luminosity?



Different again

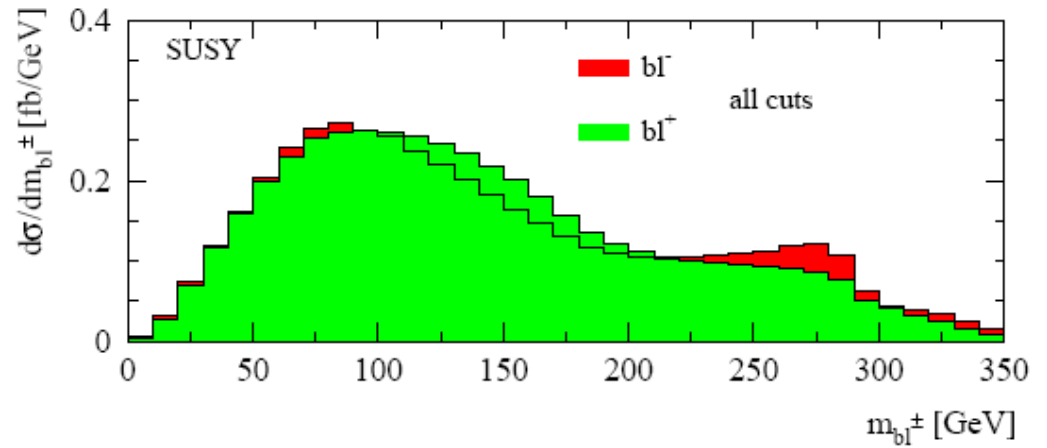
Spin Determination (T.Plehn et.al.)

- What if we **want to investigate chain from gluino?**
- Crucial to test gluino nature
- **Cannot rely on quark charge asymmetry**

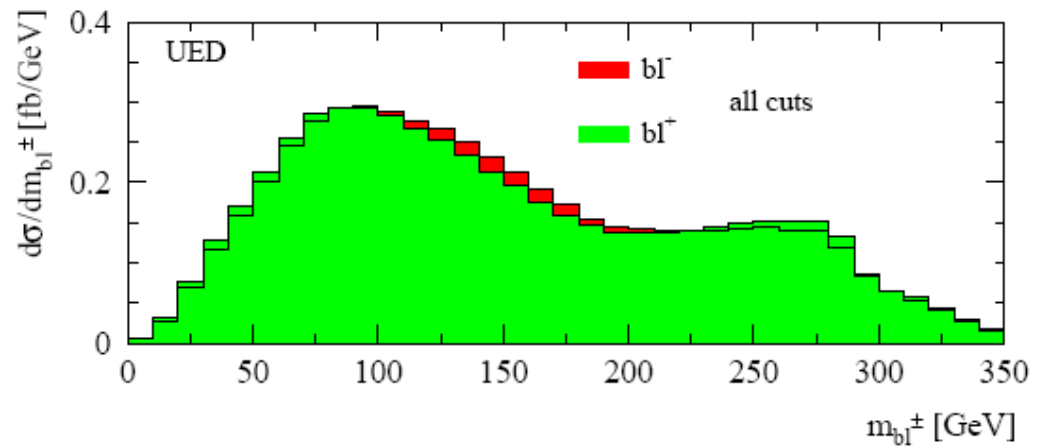


M_{BL}^+ and M_{BL}^- distributions

SUSY



UED



Room for an asymmetry!

So define asymmetry

$$A^\pm(m_{bl}) = \frac{d\sigma/dm_{bl+} - d\sigma/dm_{bl-}}{d\sigma/dm_{bl+} + d\sigma/dm_{bl-}}$$

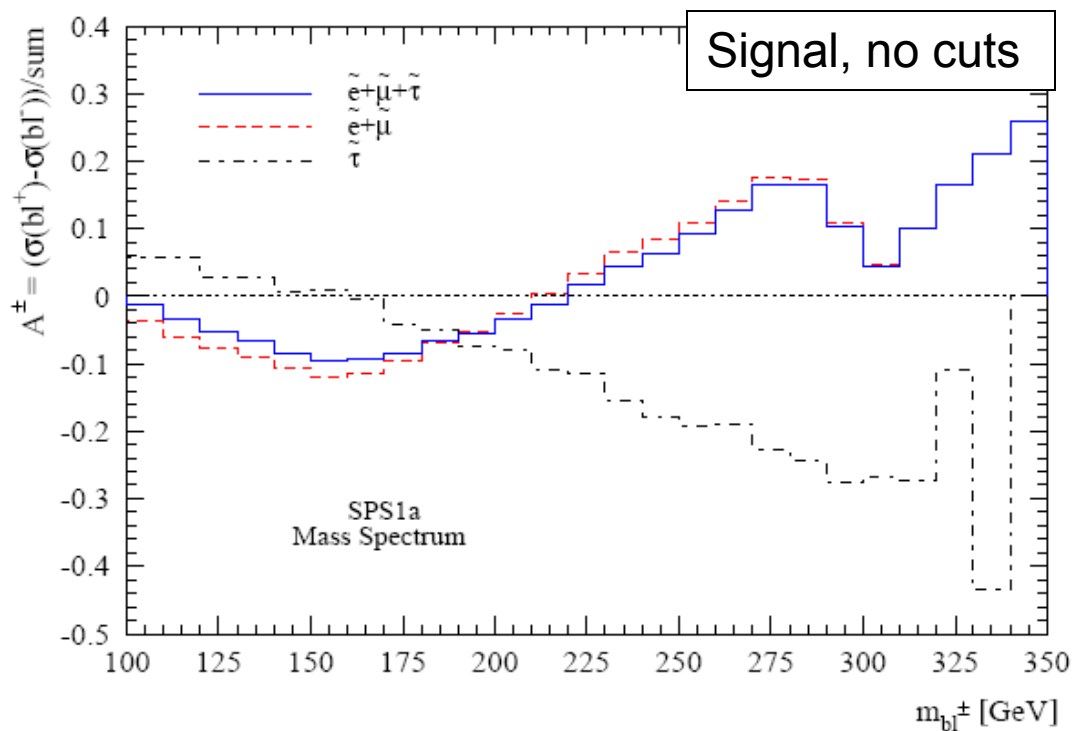
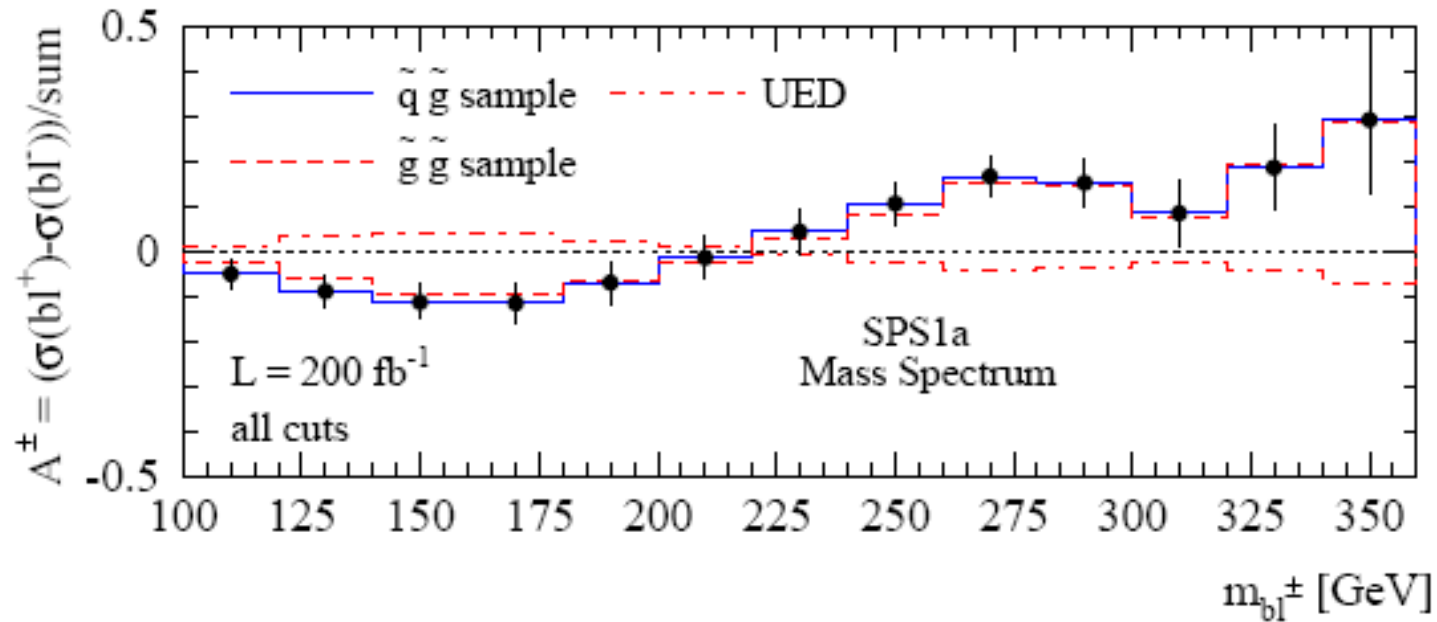


Figure 3: Bottom-lepton asymmetry for the SUSY signal only. The curves shown are for the first and second generation sleptons and for leptons coming from an intermediate $\tilde{\tau}$.

After realistic cuts, SPS1A, 200 fb⁻¹

Asymmetry
still
observable



Acceptance cuts:

$$\begin{aligned}
 p_{T,b} &> 50 \text{ GeV} & p_{T,\ell} &> 10 \text{ GeV} \\
 p_{T,j}^{\min} &> 40 \text{ GeV} & p_{T,j}^{\max} &> 150 \text{ GeV} \\
 |\eta_i| &< 2.4 & \Delta R_{ik} &> 0.4 \quad (i, k = b, j, \ell)
 \end{aligned}$$

Cuts to reject Standard Model

$$m_{\ell\ell} < 80 \text{ GeV} \quad M_{\text{eff}} > 450 \text{ GeV} \quad m_{jj} < 300 \text{ GeV}$$

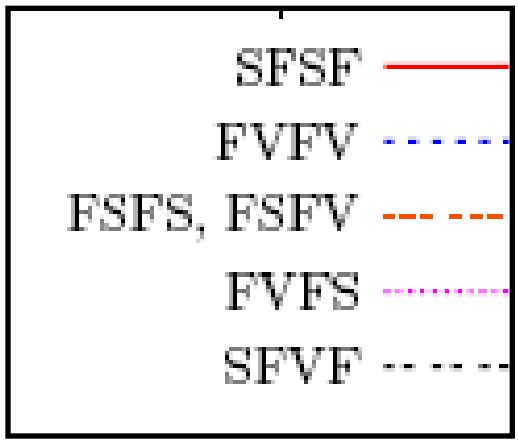
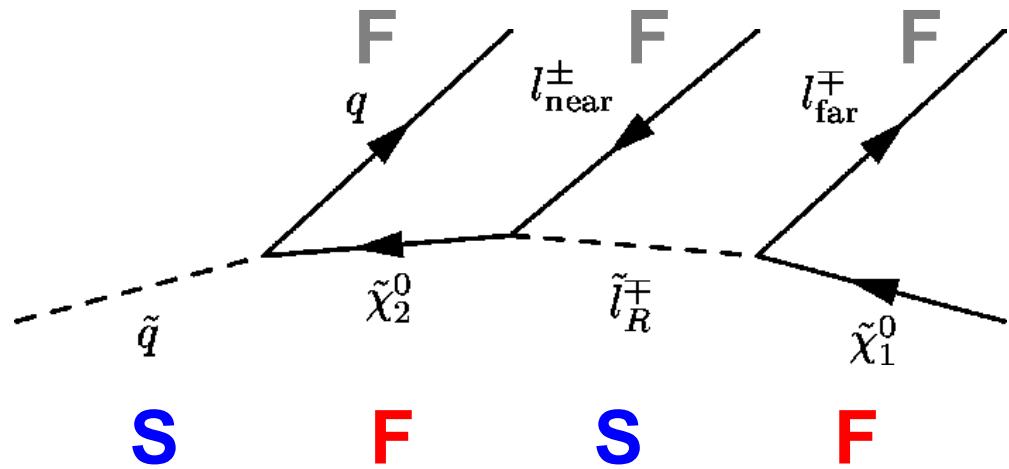
For a quantitative study we choose the (collider friendly) parameter point SPS1a. The masses in the gluino decay cascade are $m_{\tilde{g}} = 608 \text{ GeV}$, $m_{\tilde{b}_1} = 517 \text{ GeV}$, $m_{\tilde{b}_2} = 547 \text{ GeV}$, $m_{\tilde{\chi}_2^0} = 181 \text{ GeV}$, $m_{\tilde{\ell}_1} = 145 \text{ GeV}$, $m_{\tilde{\ell}_2} = 202 \text{ GeV}$, $m_{\tilde{\tau}_1} = 136 \text{ GeV}$, $m_{\tilde{\tau}_2} = 208 \text{ GeV}$, and $m_{\tilde{\chi}_1^0} = 97 \text{ GeV}$. The NLO production cross sections are 7.96 pb for $\tilde{g}\tilde{g}$, 8.02 pb for $\tilde{q}\tilde{q}^*$, 26.6 pb for $\tilde{q}\tilde{g}$, and 7.51 pb for $\tilde{q}\tilde{q}$. For the SPS1a parameter choice the lighter of the

Back to long chains

Spin sensitivity elsewhere in the llq chain (Smillie et.al.)

Later more general follow-up (Matchev, Kong, et al)

$$\bar{\Psi}_F (g_L P_L + g_R P_R) \Psi_f \Phi + h.c.$$



Scalar	Fermion	Scalar	Fermion
Fermion	Vector	Fermion	Vector
Fermion	Scalar	Fermion	Scalar
Fermion	Vector	Fermion	Scalar
Fermion	Scalar	Fermion	Vector
Scalar	Fermion	Vector	Fermion

Cannot distinguish:
 {FSFS, FSFV} and {FVFS, FVFV}

But masses matter

SPS1a mass spectrum: (GeV)

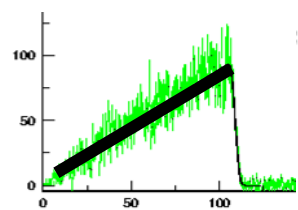
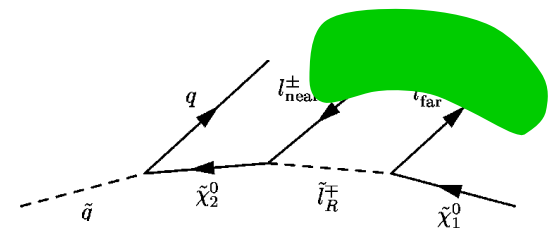
A	B	C	D
$\tilde{\chi}_1^0$	\tilde{e}_R	$\tilde{\chi}_2^0$	\tilde{u}_L
96	143	177	537

UED-type mass spectrum: (GeV)

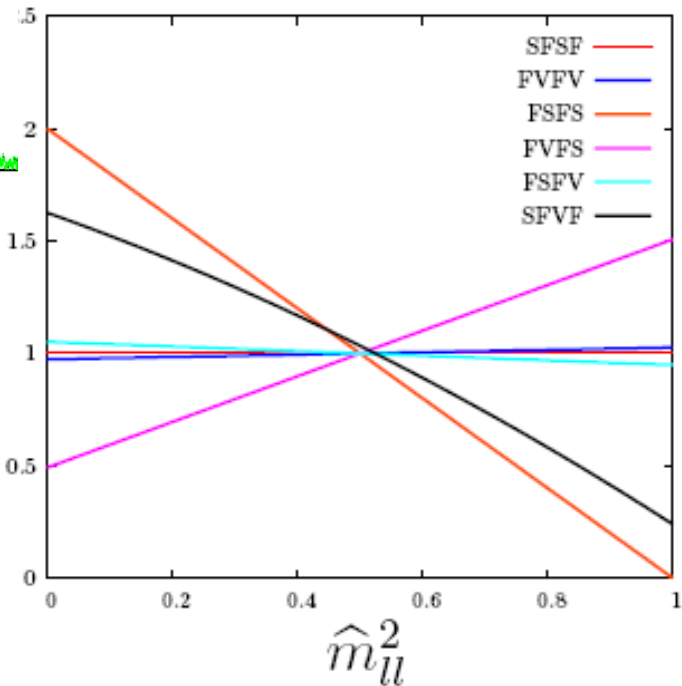
($R^{-1} \sim 800$ GeV)

A	B	C	D
γ^*	l_L^*	Z^*	q_L^*
800	824	851	956

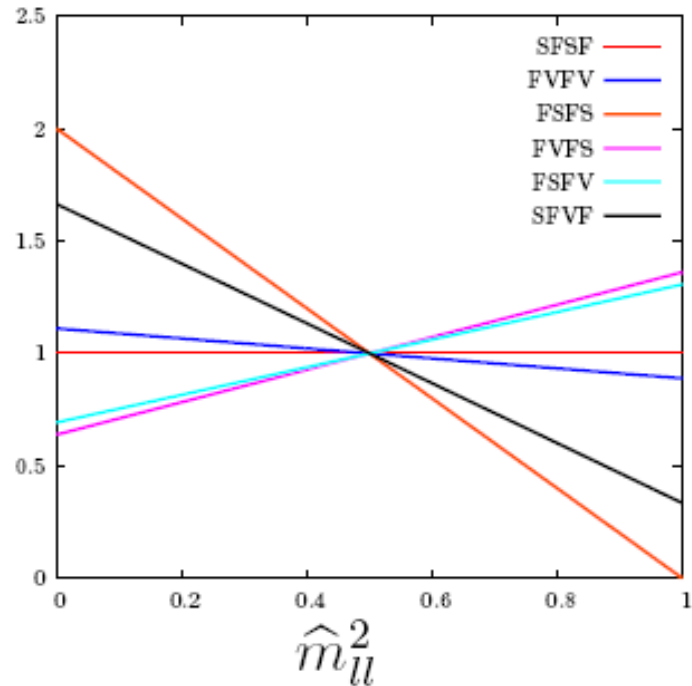
Maybe masses are not too important for m_{ll} distribution



$$\frac{dP}{d\hat{m}_{ll}^2}$$



SPS1a masses



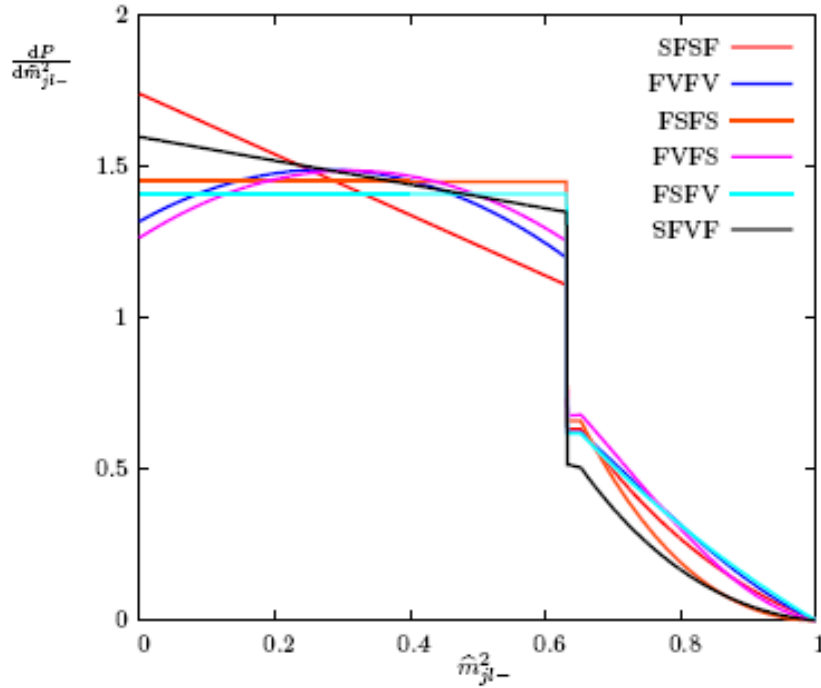
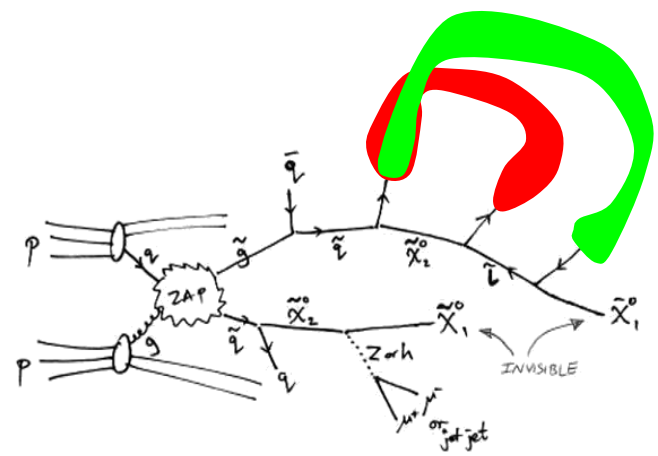
UED type masses

hep-ph/0605286

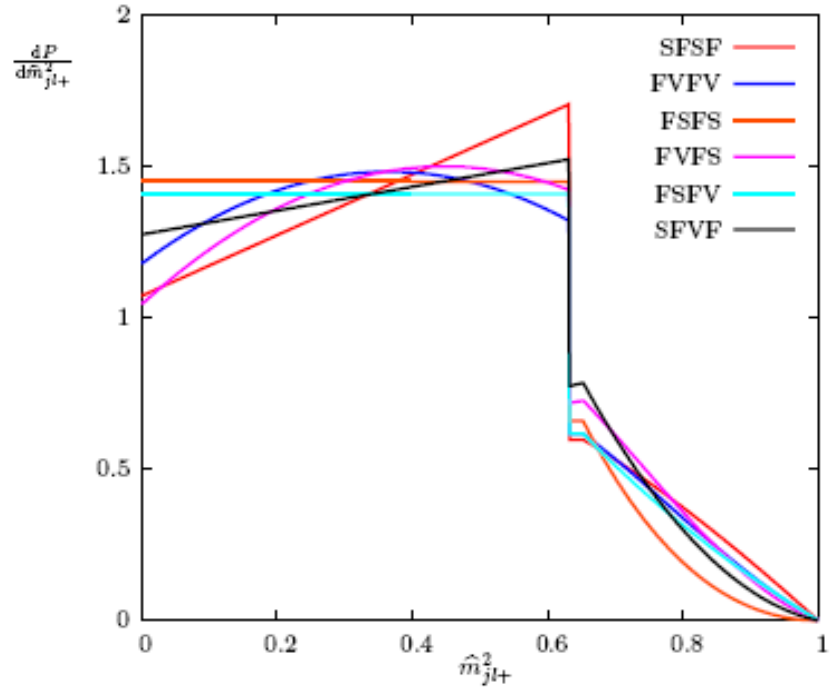
... but this fun

jet + l^\pm

At SPS 1a:

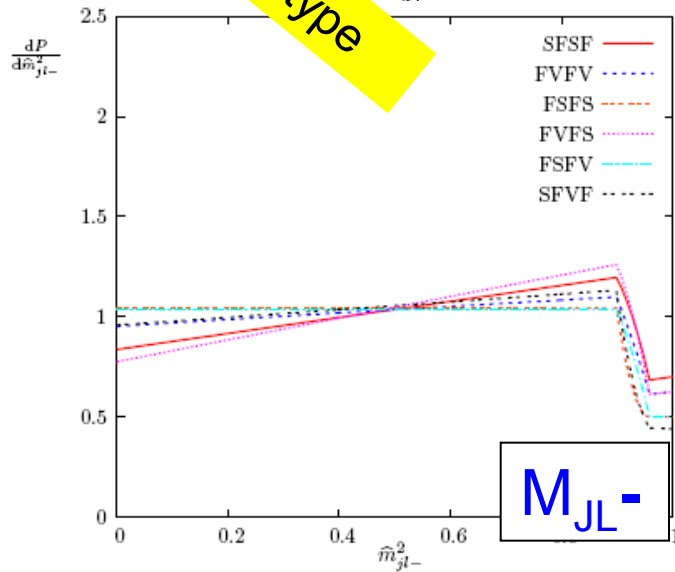
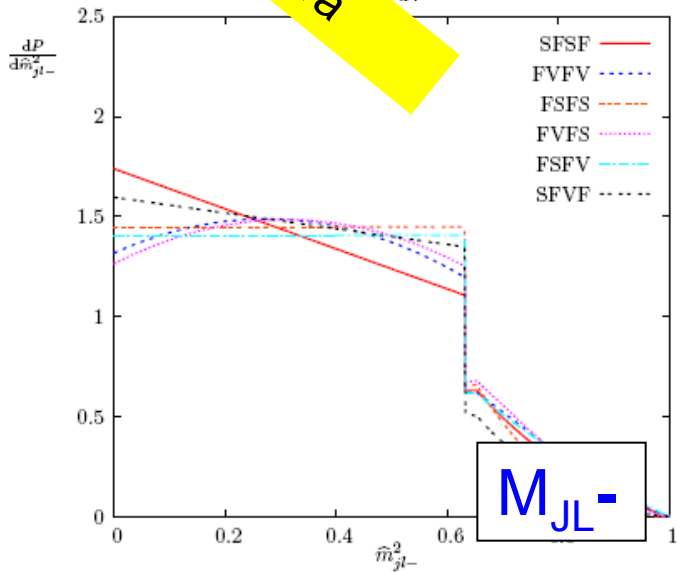
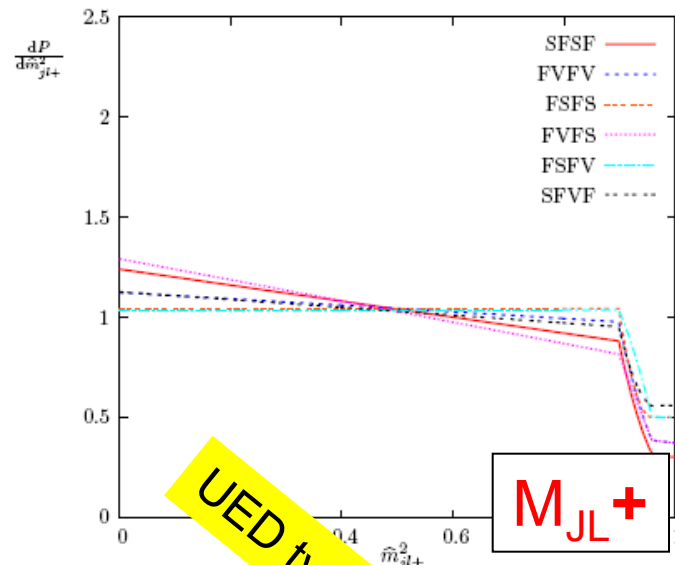
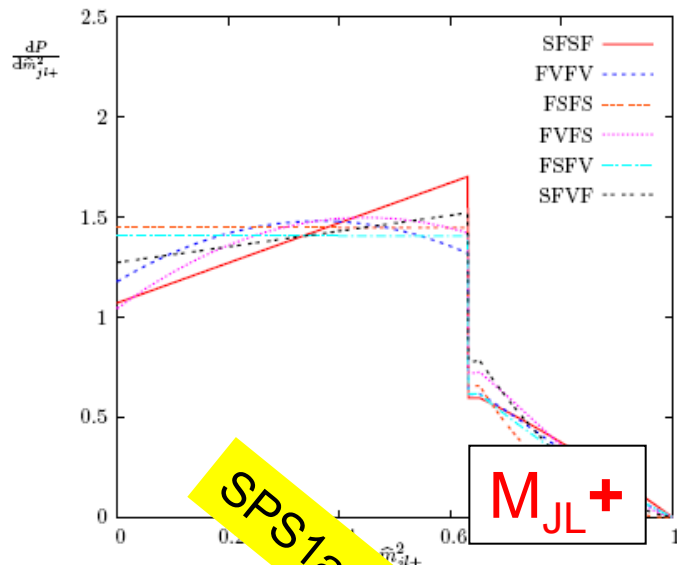


jet + l^-



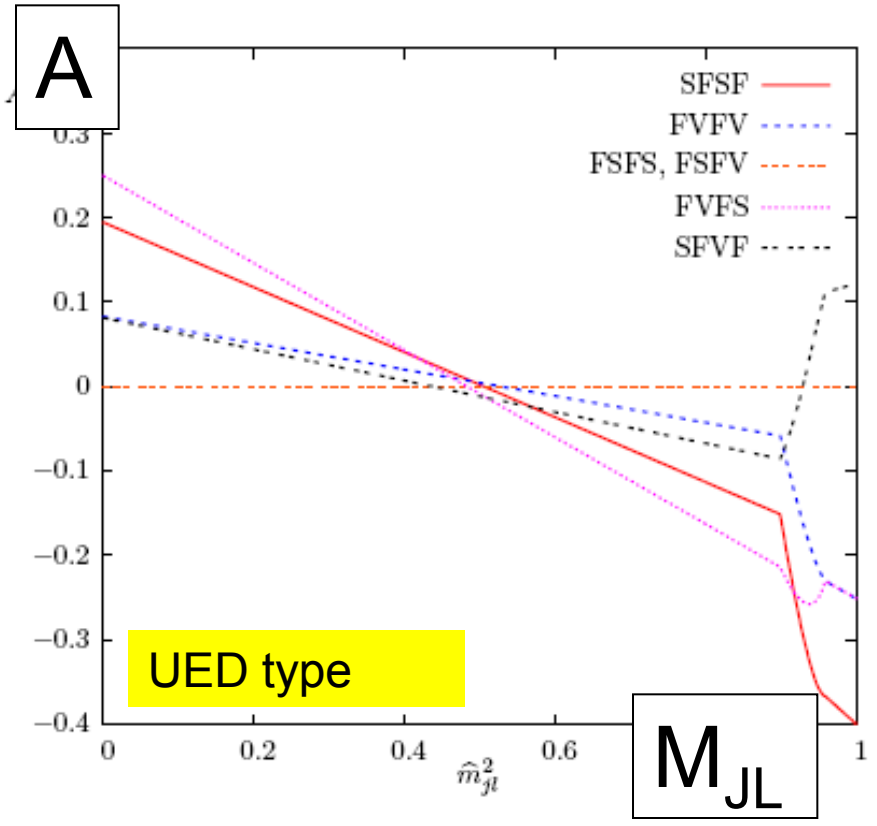
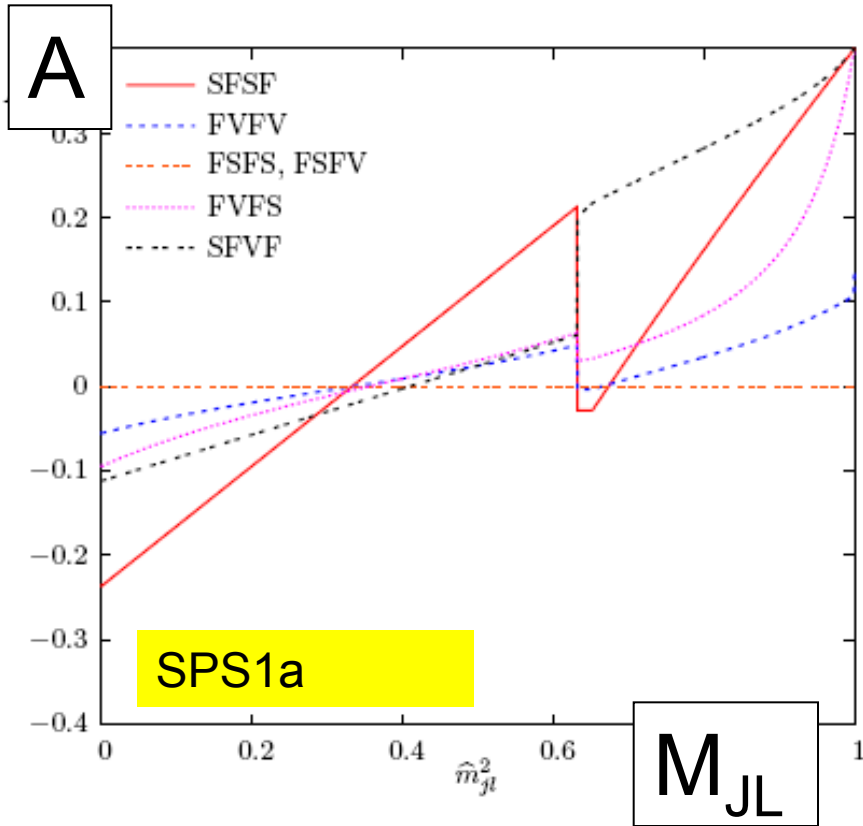
jet + l^+

.... is spoiled. ☹️



Example asymmetries:

(a big mix of spin and mass spectrum) ☹️



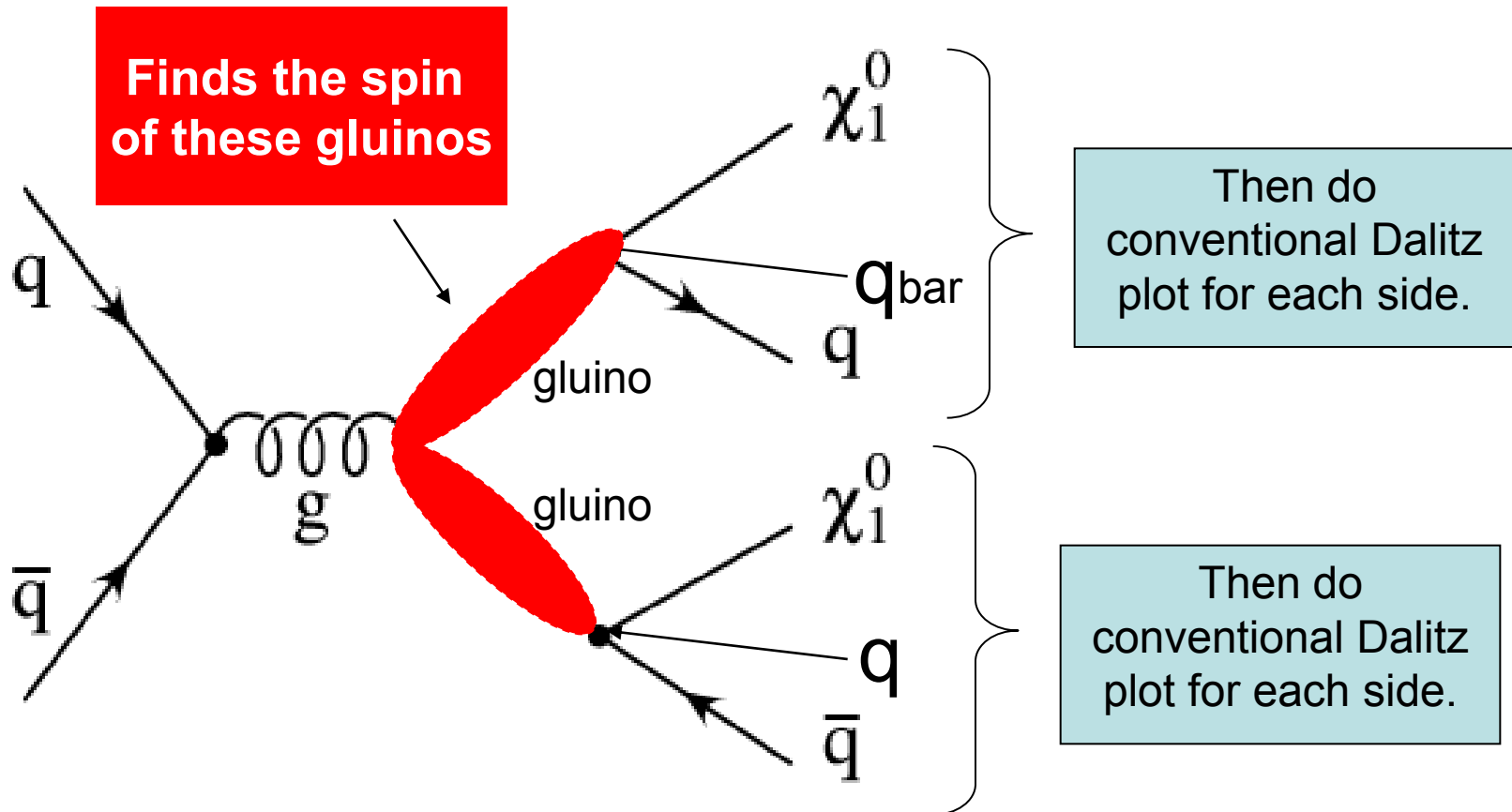
$$A = \frac{\text{Red Box} - \text{Blue Box}}{\text{Red Box} + \text{Blue Box}}$$

Yet another game one can play

M_{T2} -assisted (MAOS) spin determination

$$pp \rightarrow Y(1) + \bar{Y}(2) \rightarrow V(p_1)\chi(k_1) + V(p_2)\chi(k_2), \quad Y \rightarrow q(p_q)\bar{q}(p_{\bar{q}})\chi(k).$$

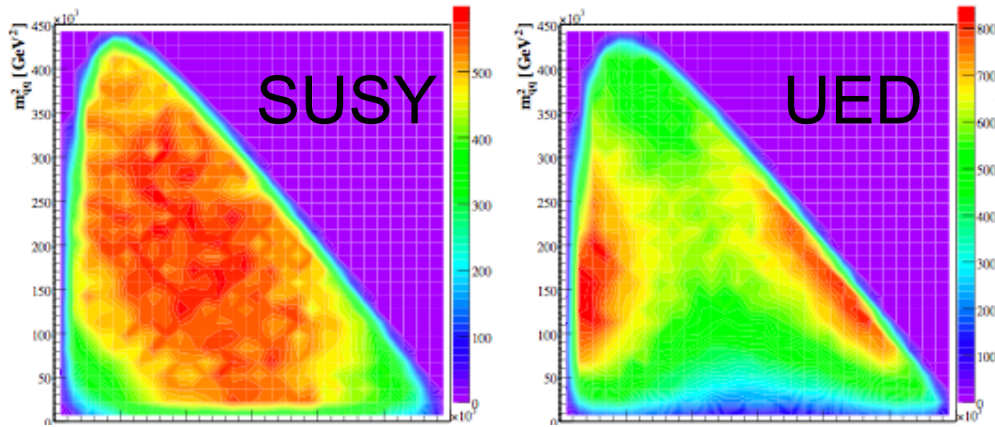
Use splitting for which leads to M_{T2} solution to assign 4-momenta to invisible particles:



M_{T2} -assisted (MAOS) spin determination

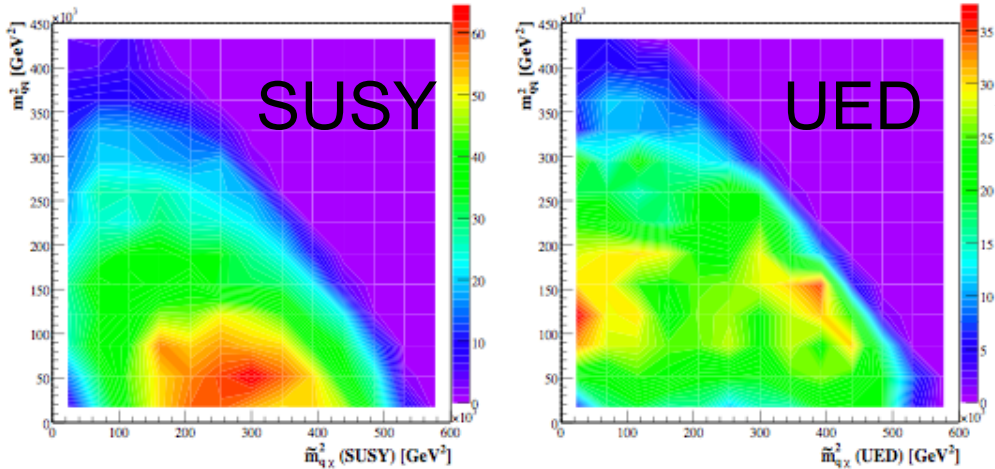
$$pp \rightarrow Y(1) + \bar{Y}(2) \rightarrow V(p_1)\chi(k_1) + V(p_2)\chi(k_2), \quad Y \rightarrow q(p_q)\bar{q}(p_{\bar{q}})\chi(k):$$

$$M_{T2}(p_i, m_\chi) \equiv \min_{\mathbf{k}_{1T} + \mathbf{k}_{2T} = \mathbf{p}_T^{\text{miss}}} \left[\max\{M_T^{(1)}, M_T^{(2)}\} \right] \rightarrow \text{assign 4-momenta}$$



$$m_{\chi, Y} = m_{\chi, Y}^{\text{true}}$$

$$\mathcal{L} = \infty$$

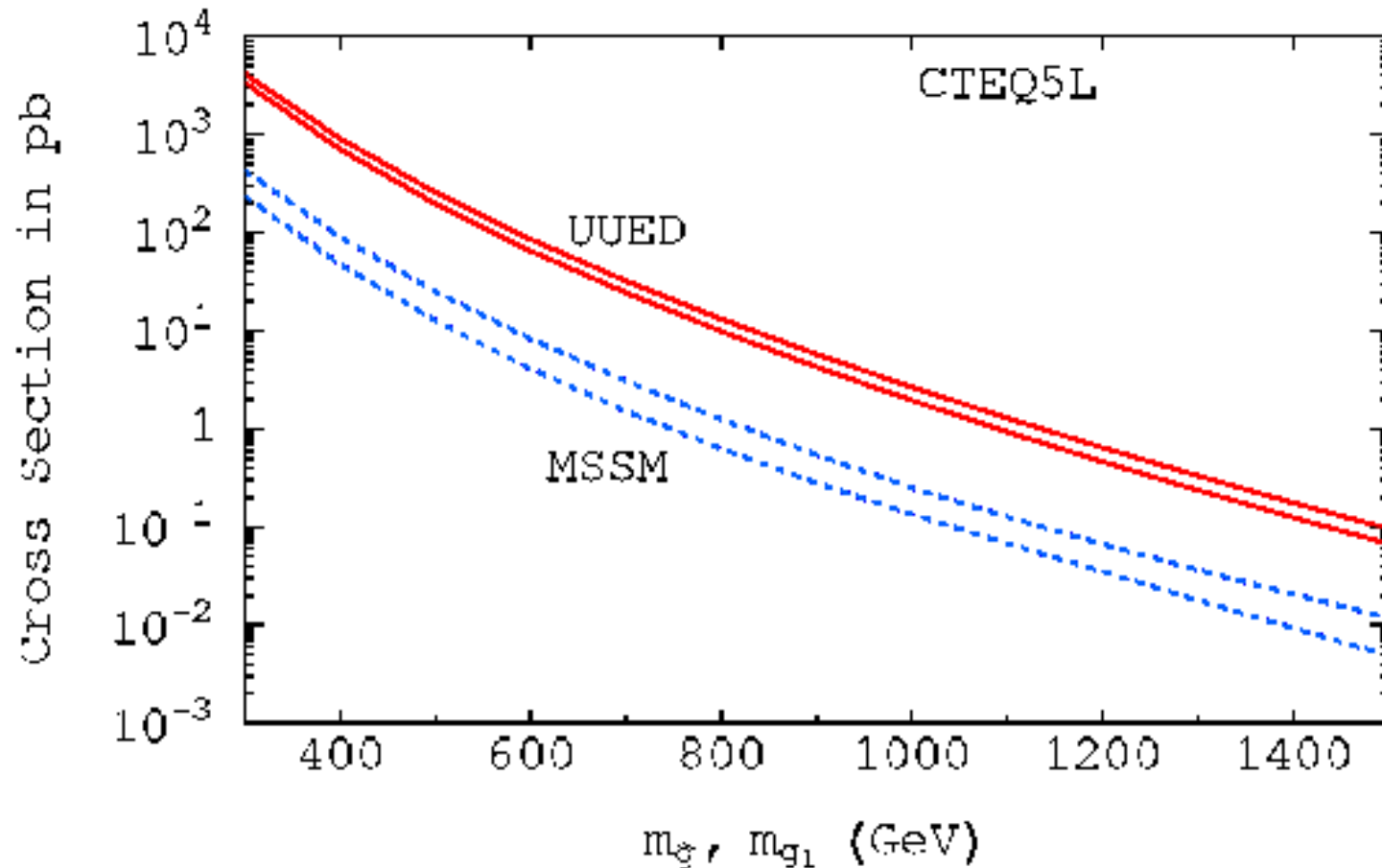


$$m_\chi = 0, m_Y = M_{T2}^{\text{max}}(m_\chi = 0)$$

$$\mathcal{L} = 300 \text{ fb}^{-1}$$

Cho, Choi, Kim, Park, 0810.4853

Reminder: cross sections reveal spins



➔ Higher spins mean higher cross sections
(for given masses)

End Notes

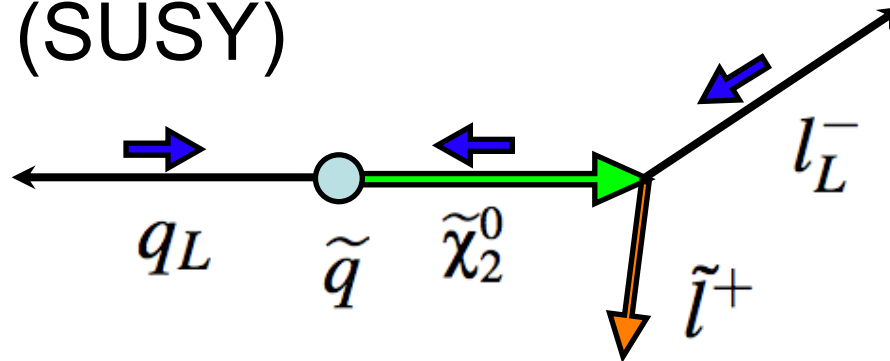
- QLL chain
 - Some spin “sensitivity” – but no strong UED/SUSY separation
 - Reduced discriminatory power when considering general couplings (Matchev/Kong).
- Di-slepton production
 - Better chance of separating UED/SUSY
 - Still model dependent
- Both require large cross sections
- Masses inextricably intertwined.



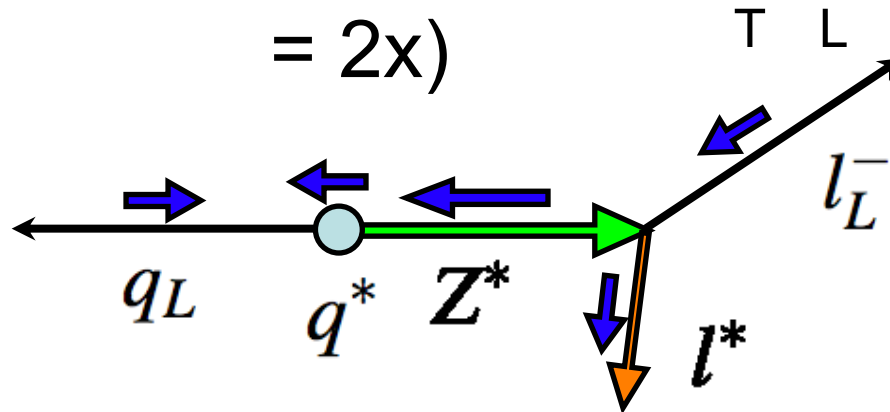
Backup slides

Helicity dependence

○ Process 1 (SUSY)



○ Process 1 (UED, transverse Z^* : $P/P = 2x$)



⇒ Both prefer high $(ql^-)^{near}$ invariant mass