

BSM Search Techniques (for the Large Hadron Collider)

Based on "A review of Mass Measurement Techniques proposed for the Large Hadron Collider", Barr and Lester, <u>arXiv:1004.2732</u>

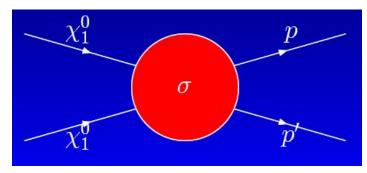
NExT-PhD Abingdon 2011

Christopher Lester University of Cambridge

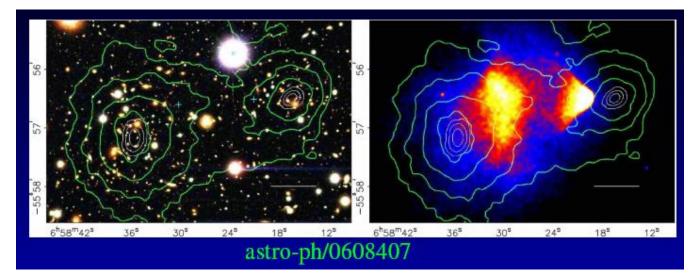


Recall 3 awkward problems ...

Aim was to fix some of these problems with the Standard Model



- Fine-tuning / "hierarchy problem" (technical) – Why are particles light?
- Does not explain Dark Matter
- No gauge coupling unification



What are common features of "solutions" to these problems?

- Big increase in particle content
- Longish decay chains
- Missing massive particles
- Large jet/lepton/photon multiplicity

At some point, 5000 people will shout:



... not a collider of large hadrons

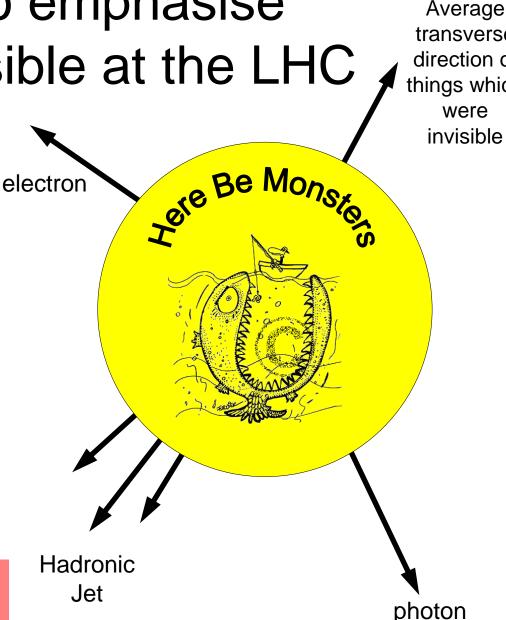
How hard is it to identify what was found?

Want to emphasise what is visible at the LHC

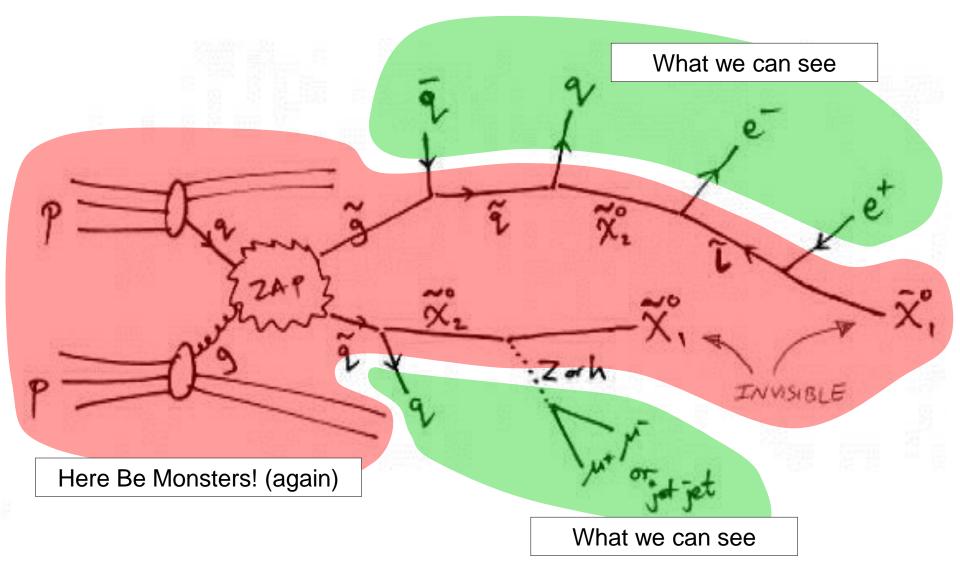
transverse direction of things which were invisible

- Distinguish the following from each other
 - Hadronic Jets,
 - B-jets (sometimes)
 - Electrons, Positrons, Muons, Anti-Muons
 - Tau leptons (sometimes)
 - Photons
- Measure Directions and Momenta of the above.
- Infer total transverse ٠ momentum of invisible particles. (eg neutrinos)

What do we NOT measure?

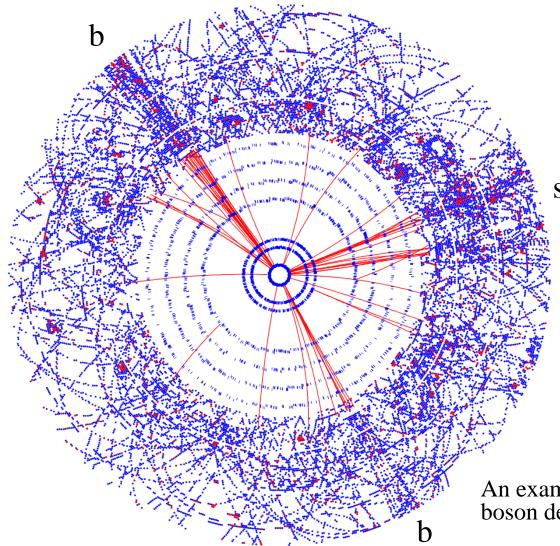


What might events look like?



This is the high energy physics of the 21st Century!

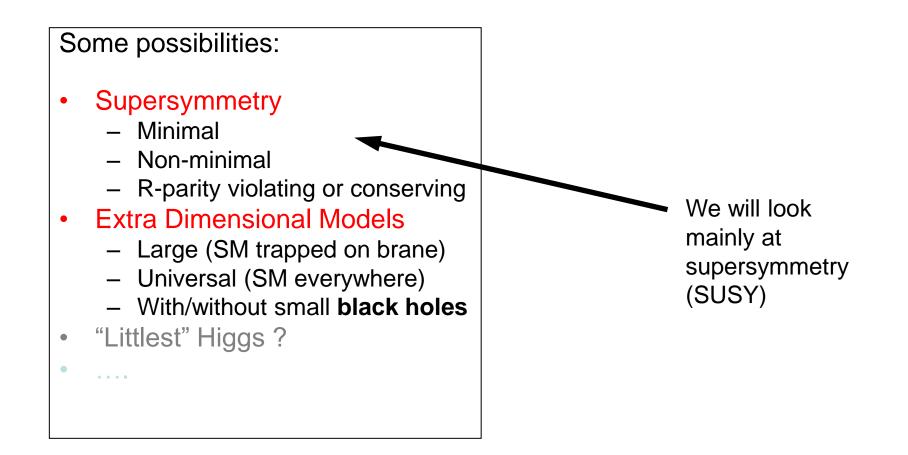
What events really look like scares me!



soft gluon radiation?

An example of an event where a higgs boson decayed to a pair of b-quarks/

Supersymmetry as Lingua Franca



Supersymmetry! CAUTION!

- It may exist
- It may not
- First look for deviations from Standard Model!



Experiment must lead theory.

Gamble:

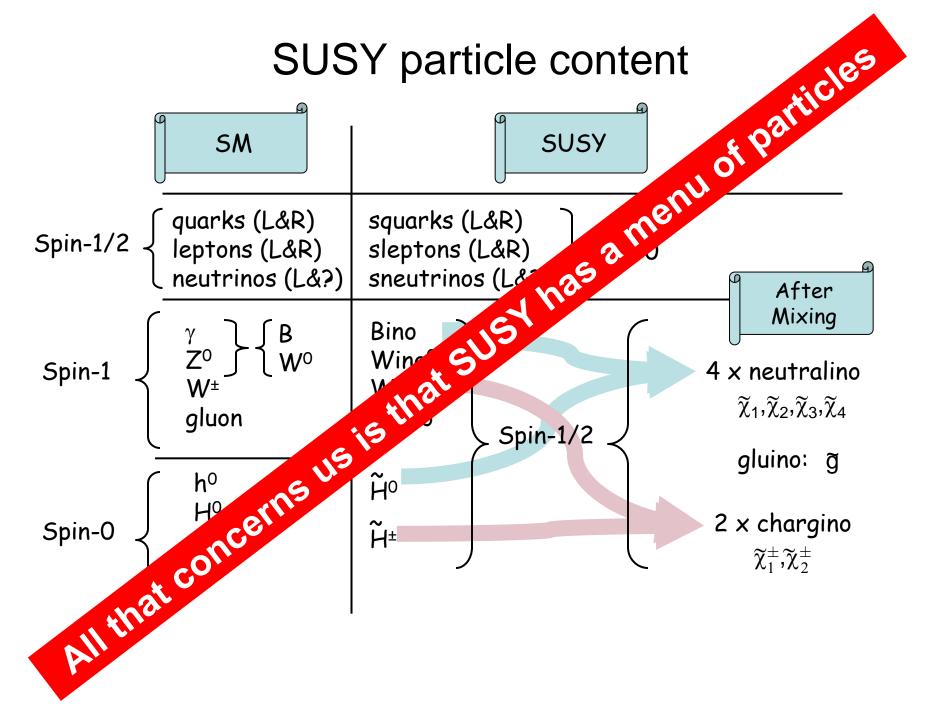
IF DEVIATIONS ARE SEEN:

- Old techniques won't work
- New physics not simple

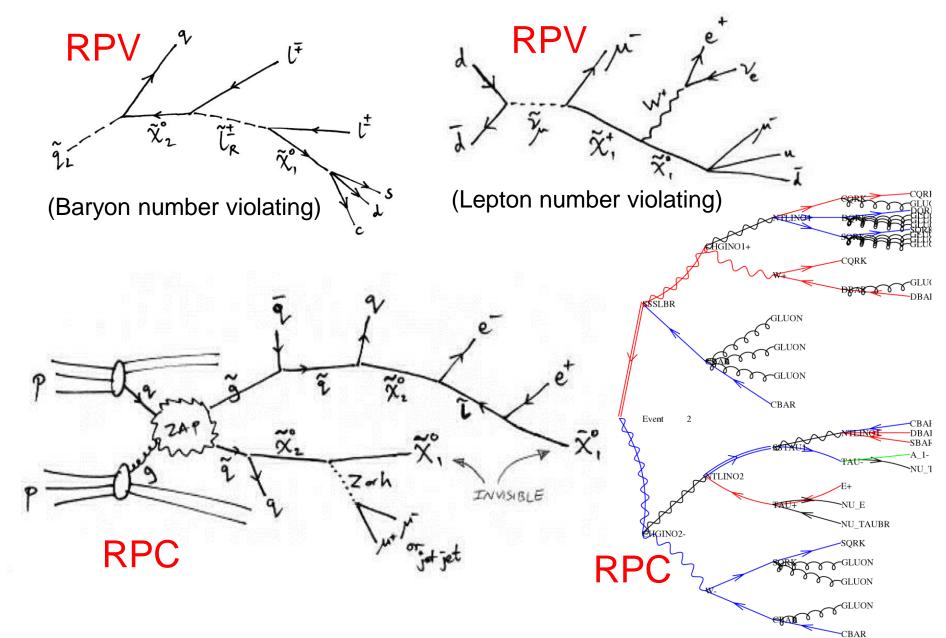
CAUTION

• Can new techniques in SUSY but can apply them elsewhere.





Even in SUSY many possibilities



Do we care about masses?

- Common Parameter in the Lagrangian
- Expedites discovery optimal selection
- Interpretation

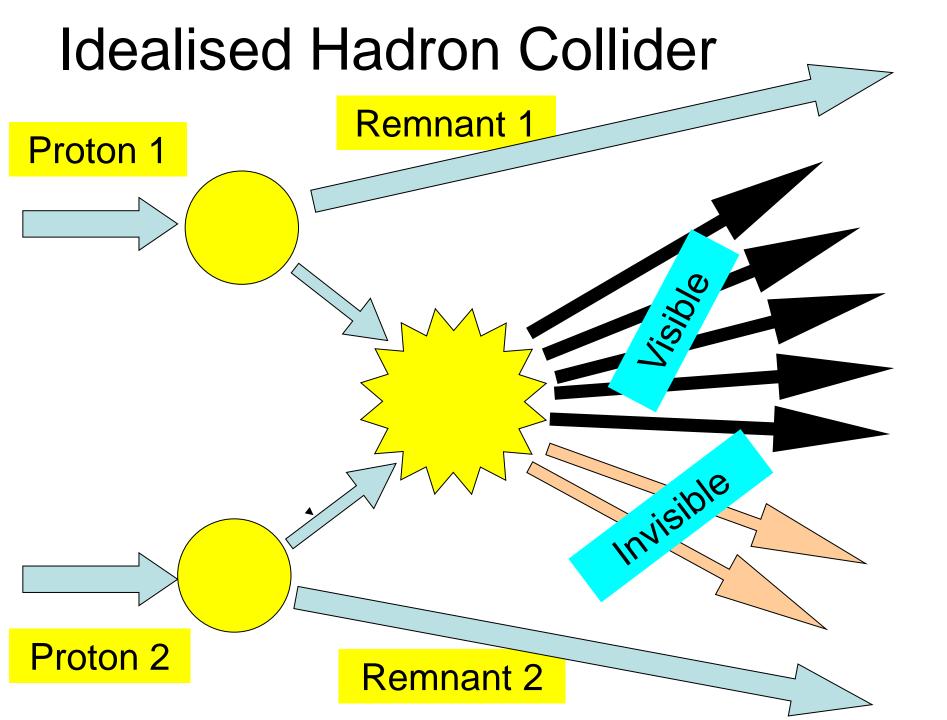
(SUSY breaking mechanism, Geometry of Extra Dimensions)

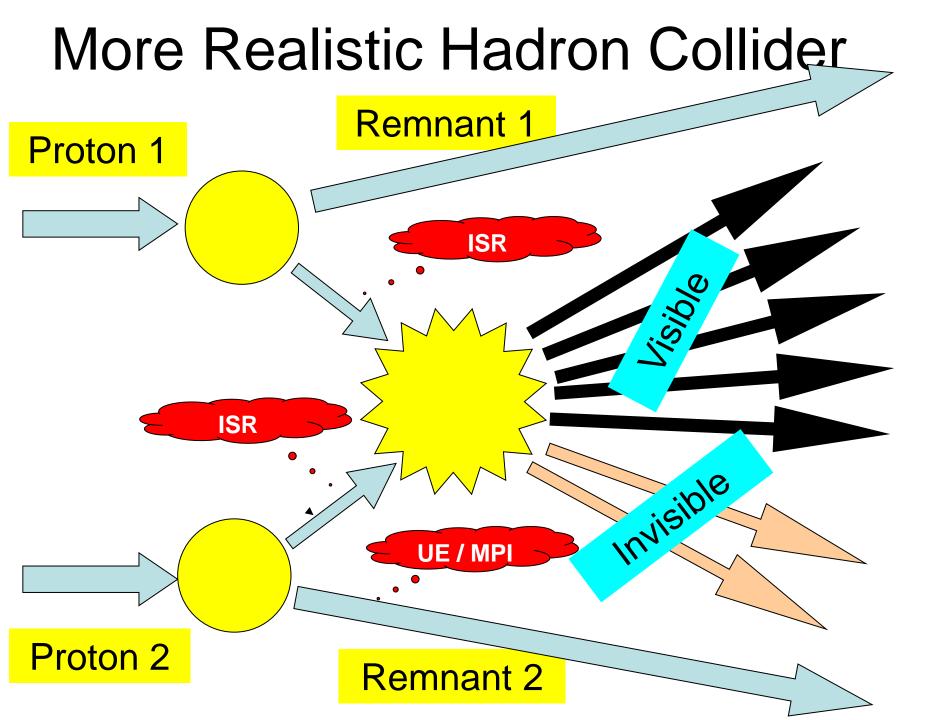
Prediction of new things
 Mass of W,Z → indirect top quark mass "measurement"

"mass measurement methods"

... short for ...

"parameter estimation and discovery techniques"

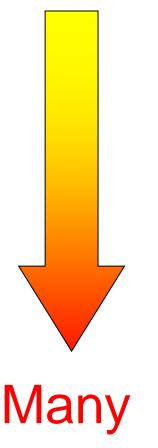




Types of Technique

Few

assumptions



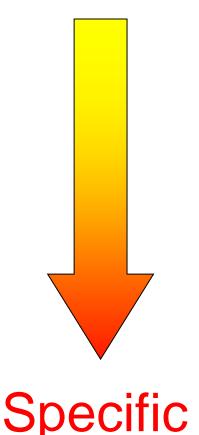
assumptions

- Missing transverse momentum
- M_eff, H_T
- s Hat Min
- M_T
- M_TGEN
- M_T2 / M_CT
- M_T2 (with "kinks")
- M_T2 / M_CT (parallel / perp)
- M_T2 / M_CT ("sub-system")
- "Polynomial" constraints
- Multi-event polynomial constraints
- Whole dataset variables
- Cross section
- Max Likelihood / Matrix Element

Types of Technique

Vague

conclusions



Missing transverse momentum

- M_eff, H_T
- s Hat Min
- M_T
- M_TGEN
- M_T2 / M_CT
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conclusions

Types of Technique

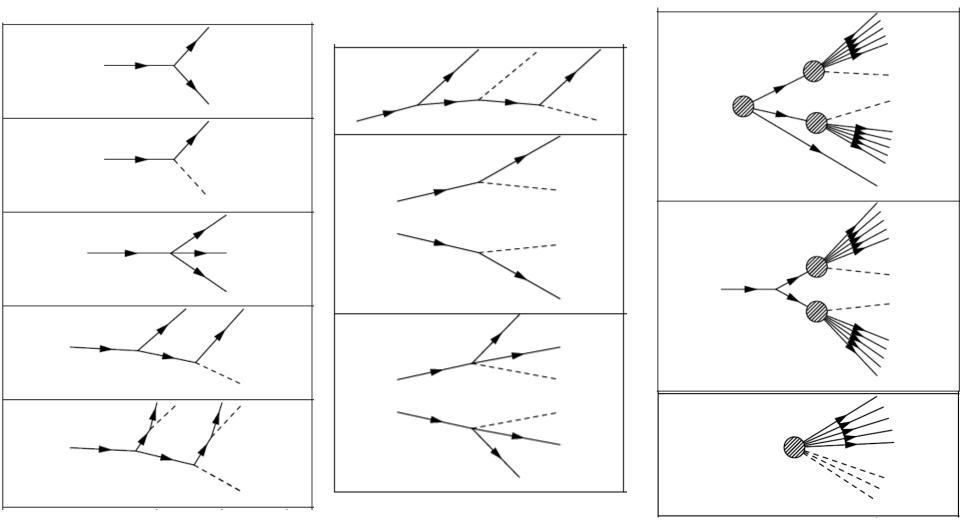
Robust

Fragile

- Missing transverse momentum
- M_eff, H_T
- s Hat Min
- M_T
- M_TGEN
- M_T2 / M_CT
- M_T2 (with "kinks")
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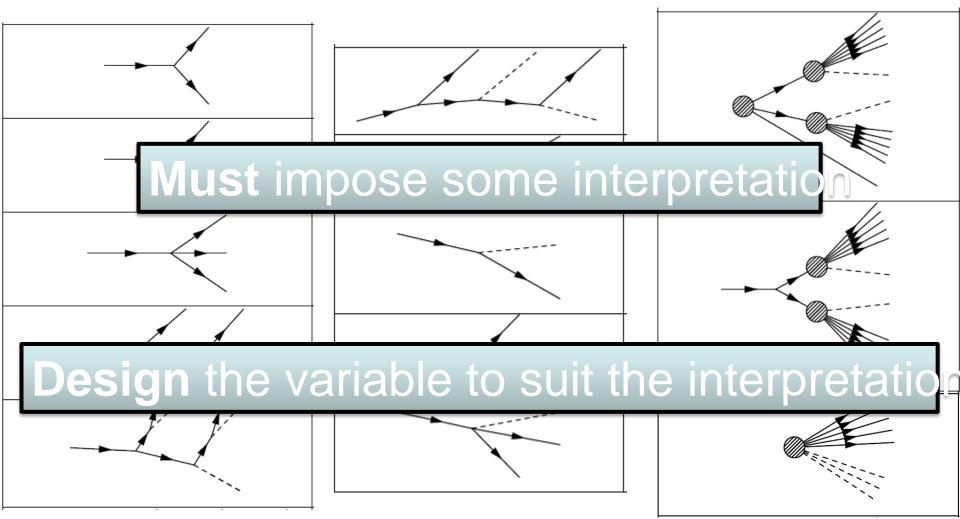
Interpretation : the balance of benefits Few Vague Robust conclusions assumptions **Specific** Many Fragile conclusions assumptions

Topology / hypothesis



Full index in arXiv:1004.2732

Topology / hypothesis

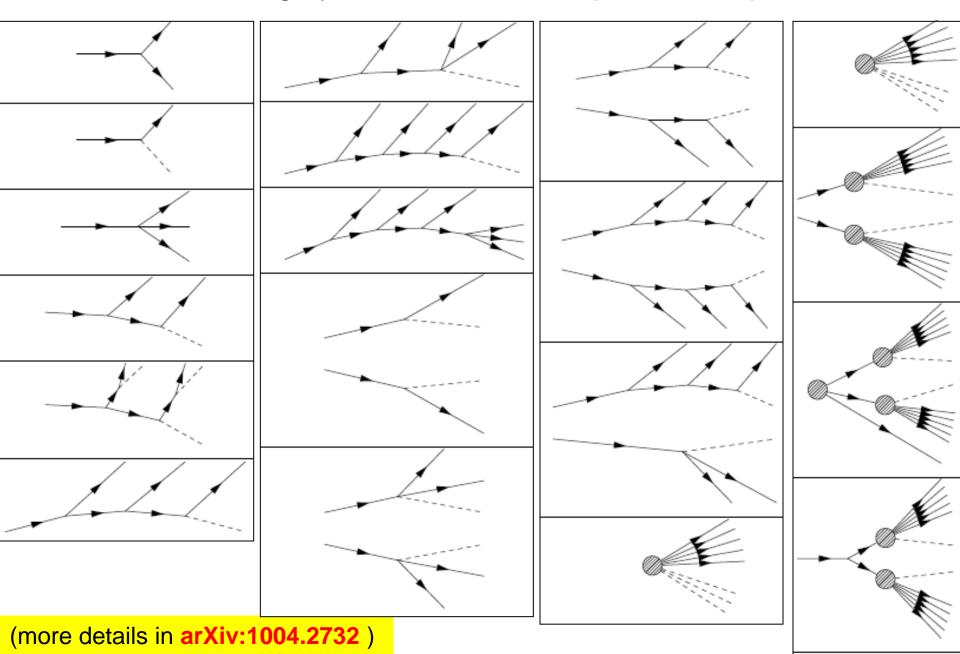


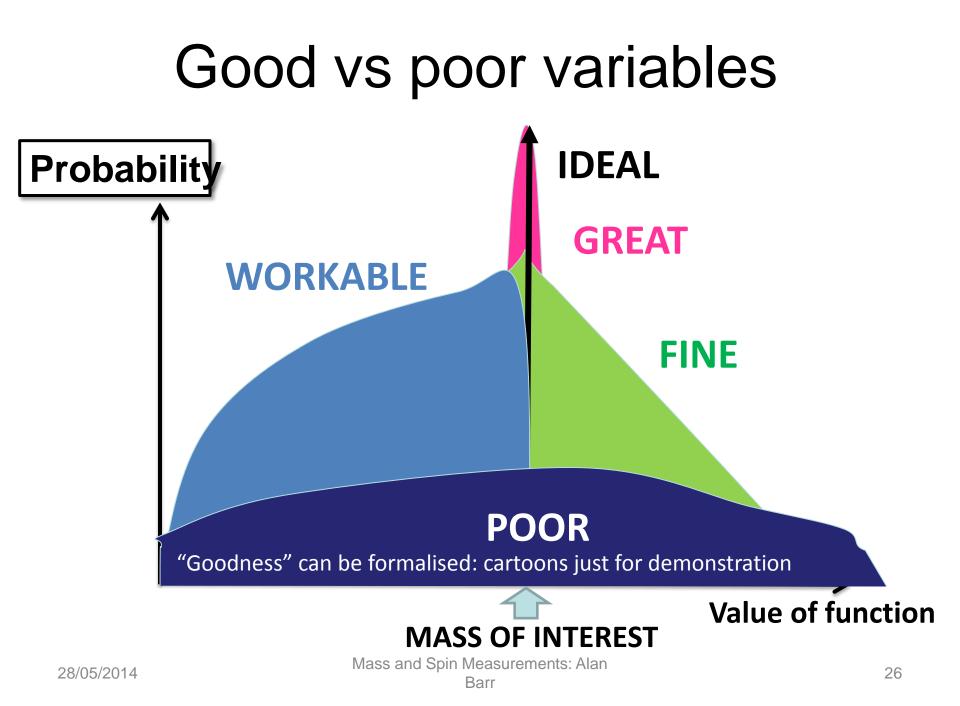
Full index in arXiv:1004.2732

Mass and Spin Measurements: Alan

28/05/2014

Lectures are roughly ordered from simple to complicated ...





[much of the talk based on material in]

arXiv:1004.2732

A Review of the Mass Measurement Techniques proposed for the Large Hadron Collider

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Keble Road, Oxford OX1 3RH, United Kingdom

Christopher G Lester[†]

Department of Physics, Cavendish Laboratory,

JJ Thomson Avenue, Cambridge, CB3 0HE, United Kingdom

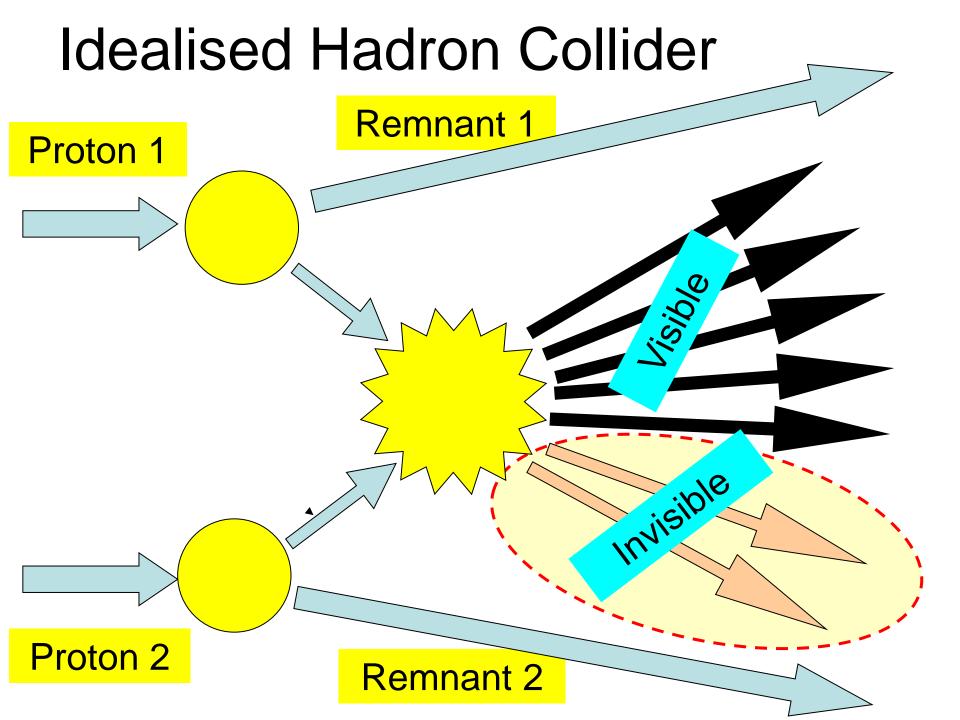
We review the methods which have been proposed for measuring masses of new particles at the Large Hadron Collider paying particular attention to the kinematical techniques suitable for extracting mass information when invisible particles are expected.

Scope and disclaimers

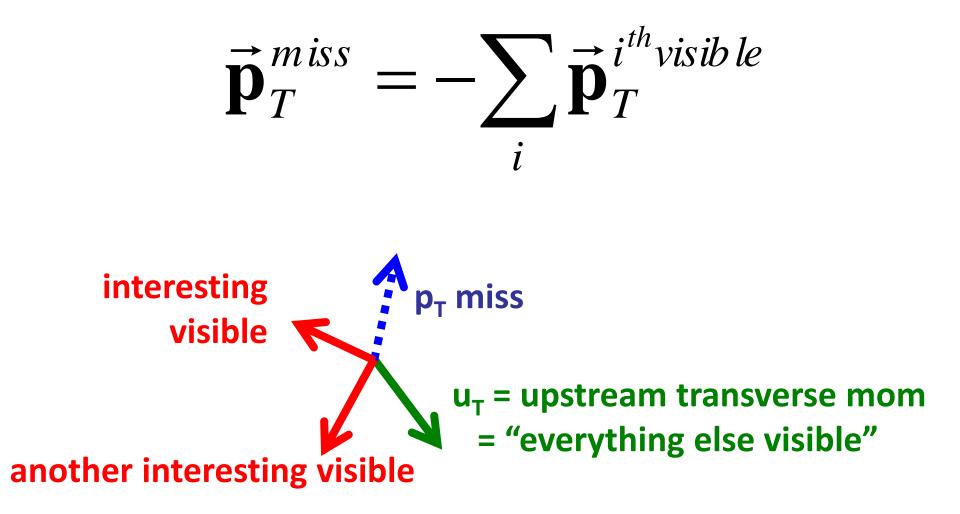
- will not spend much time on fully visible final states as standard mass reconstruction techniques apply
- will only consider new particles of unknown mass decaying to invisible particles of unknown mass (and other visible particles)
- selection bias more emphasis on things I've worked with
 - Transverse masses, MT2, kinks, kinematic methods.
 - (Not Matrix Element / likelihood methods / loops)
- not shameless promotion focus on faults!

Few assumptions, Vague Conclusions.

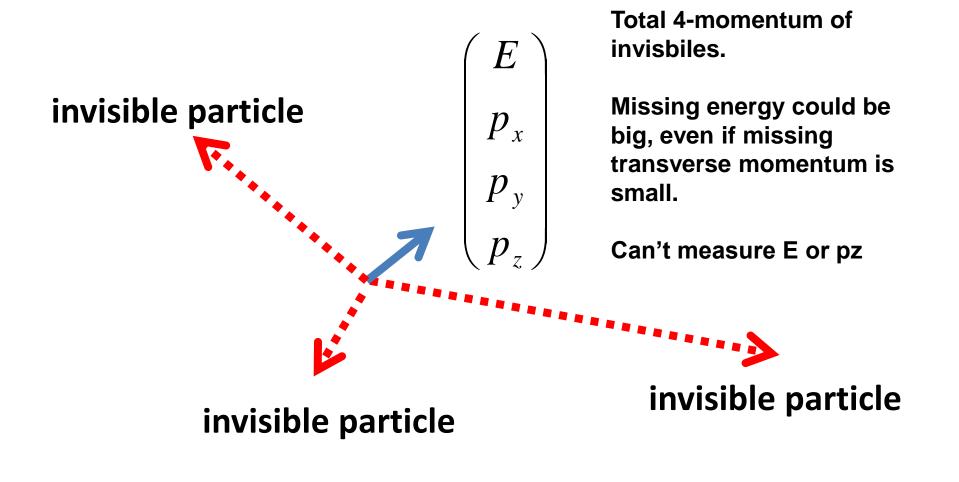
Anything with sensitivity to mass scales.



Missing transverse momentum



Events have missing energy too, and it's not missing momentum

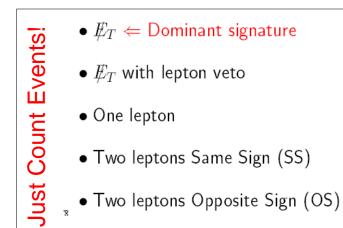


Rant about missing transverse momentum

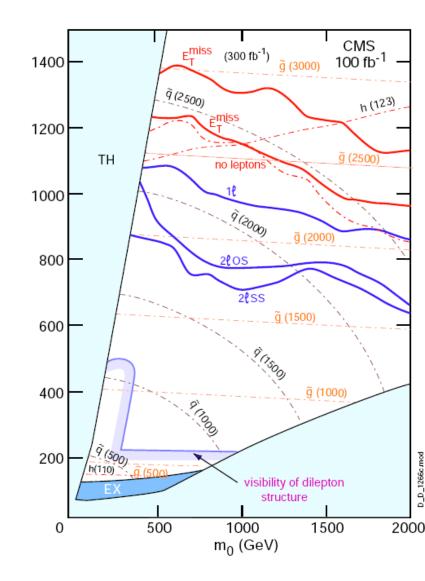
- eTmiss aaargh
- MET AAAARGH
- missing energy AAAAAARRGH
- Blame LEP?
- Calorimeter apologists?
- alphaT

Main EASY signatures are:

- Lots of missing pt
- Lots of leptons
- Lots of jets



Simply count events containing the above



Perhaps

simple = best ?

-- The End --



Am in great danger of appearing to sweep a great number of LHC analyses under here!

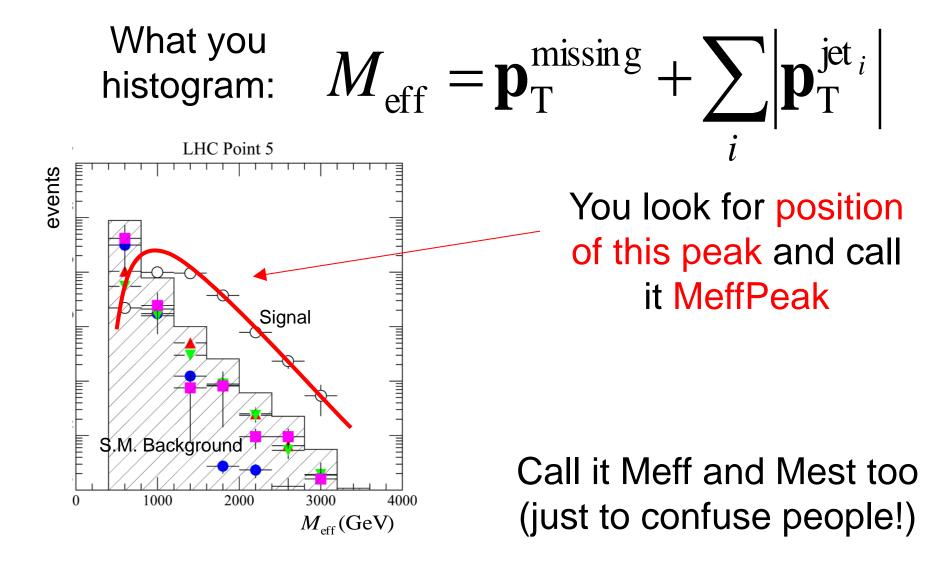
Not my intention at all!

Can attempt to spot susy by counting "strange" events ...

... but can we say anything concrete about a mass scale?

Next example still low-tech

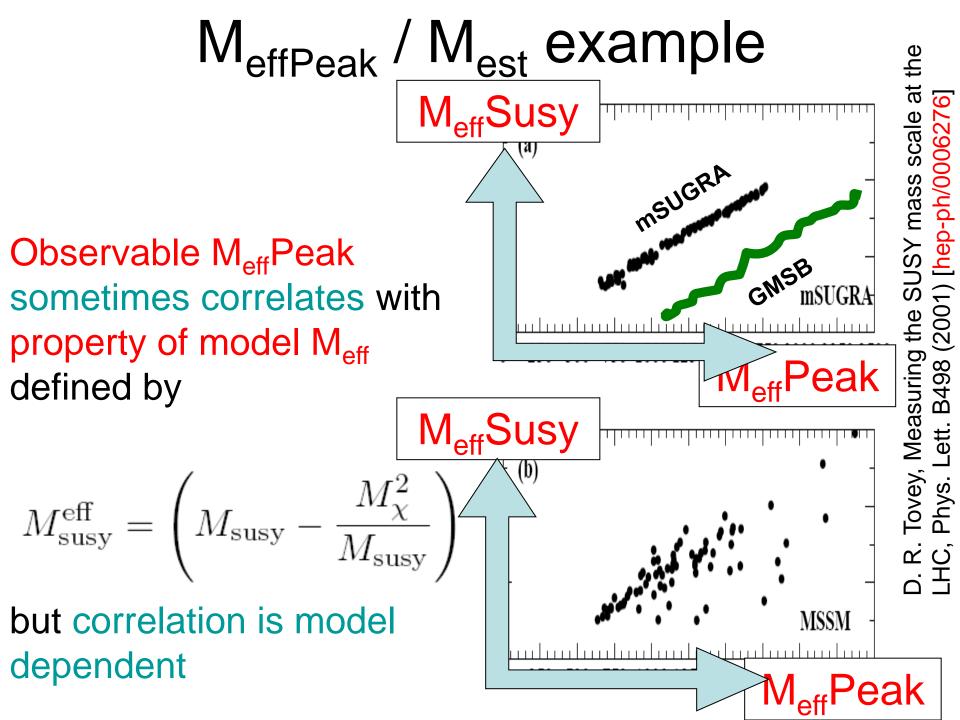
Effective mass



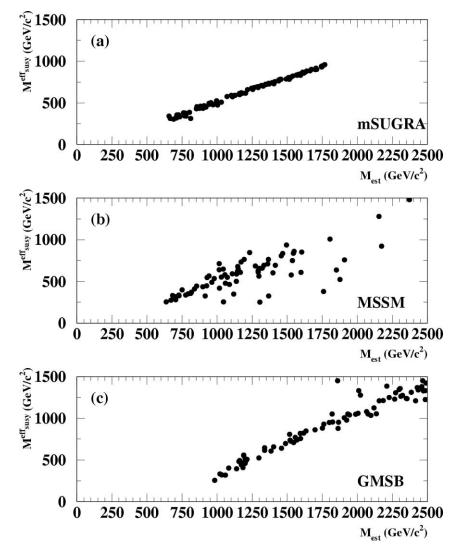
What might Meff peak position correlate with?

Define SUSY scale:

$$M_{\rm susy}^{\rm eff} = \left(M_{\rm susy} - \frac{M_{\chi}^2}{M_{\rm susy}}\right), \text{ with } M_{\rm SUSY} \equiv \frac{\sum_i M_i \sigma_i}{\sum_i \sigma_i}$$



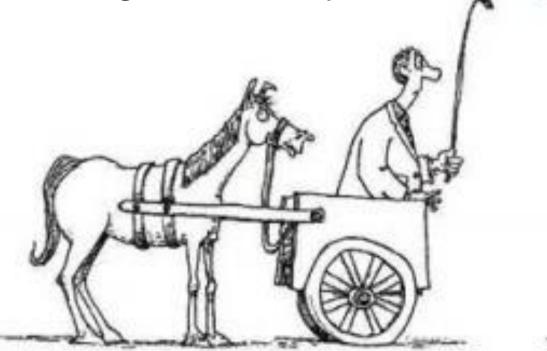
Correlations between MeffPeak position and MeffSusy



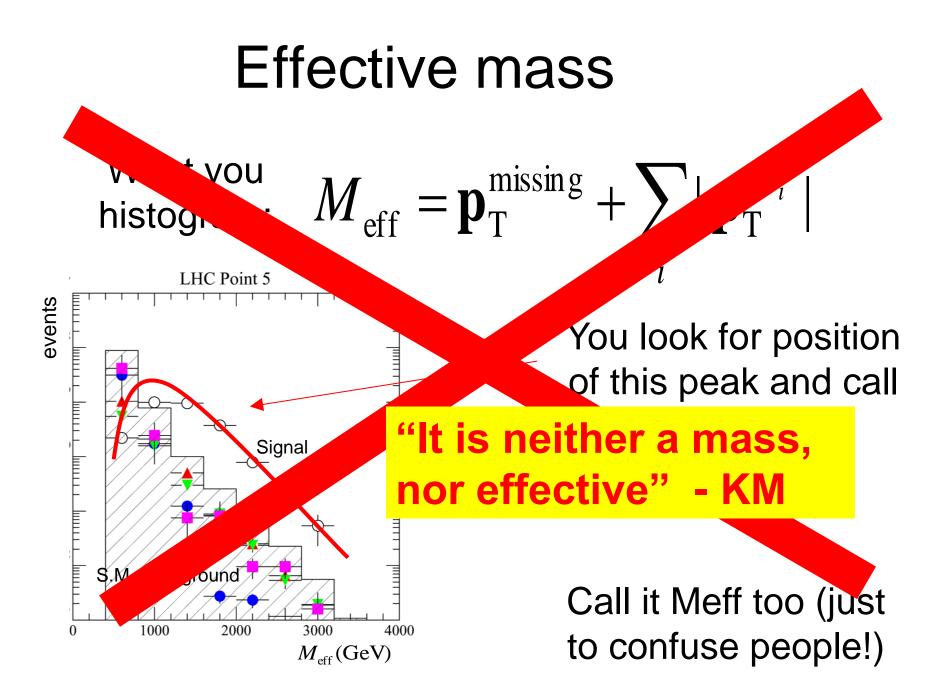
(Tovey)

M_Hotpants ..

• Can encourage tendency to



 Create your variable, then see what might be able to measure. Oops.



Meff is not alone ...

Murky underworld of hidden relatives known variously as HT ... same thing ... sometimes

$$H_T = E_{T(2)} + E_{T(3)} + E_{T(4)} + |\mathbf{p}_T|$$

 $E_T = E\sin\theta$

See arXiv:1105.2977 for why sinTheta brings on nightmares.

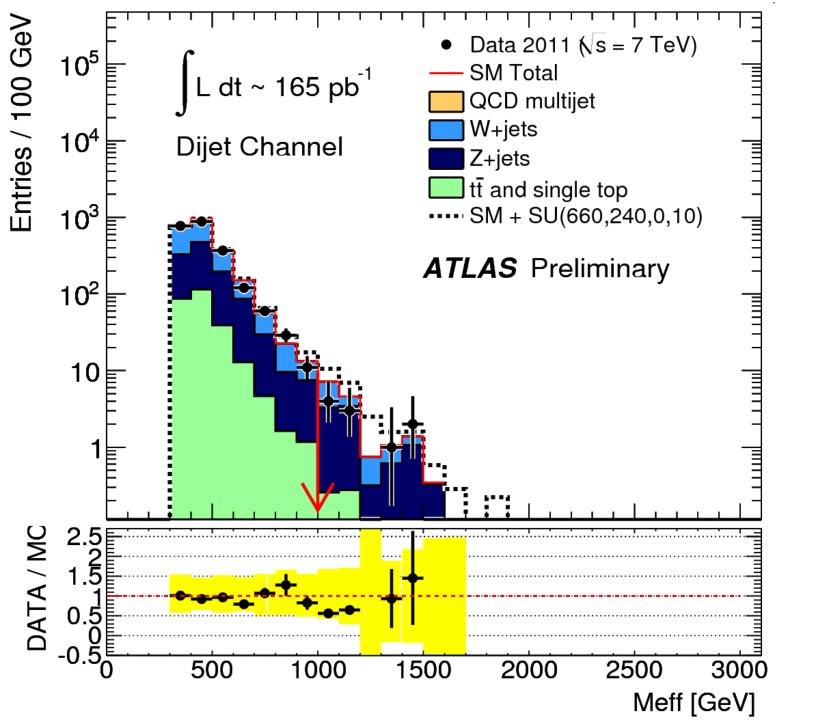
(There are **no standard definitions** of H_T or Meff. Authors differ in how many jets are used, whether PT miss should be added etc.)

All have *some* sensitivity to the overall mass scales involved, but interpretation requires a model and more assumptions.

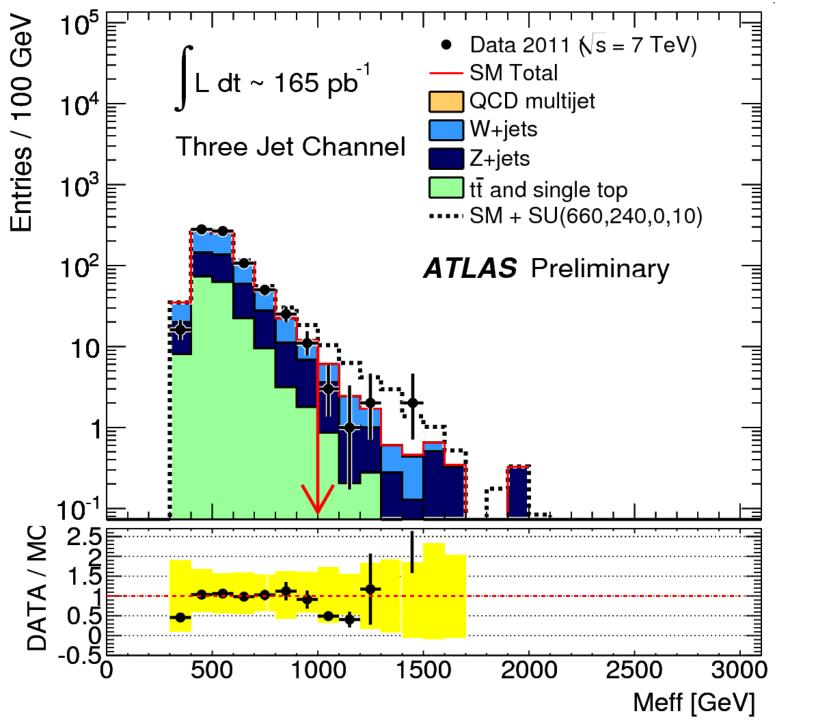
Why are we adding transverse momenta?

- Why not multiply? (or add logs)? $M_{happy} = \left(\prod_{i=1}^{n} \mathbf{p}_{T}^{i}\right)^{\frac{1}{n}}$
- Serious proposal to use Meff²- $(u_T)^2$ in arXiv:1105.2977
- Why are the signs the same? Why equal weights? Silly?
- How many years would it take ATLAS/CMS to discover the invariant mass for Z -> a b ?

$$\mathbf{M}^{2} = \left(\sqrt{m_{a}^{2} + a_{x}^{2} + a_{y}^{2} + a_{z}^{2}} + \sqrt{m_{b}^{2} + b_{x}^{2} + b_{y}^{2} + b_{z}^{2}}\right)^{2}$$
$$- \left(a_{x} + b_{x}\right)^{2} - \left(a_{y} + b_{y}\right)^{2} - \left(a_{z} + b_{z}\right)^{2}$$



atest AT transverse AS 0-lepton, momentum data. lets missing

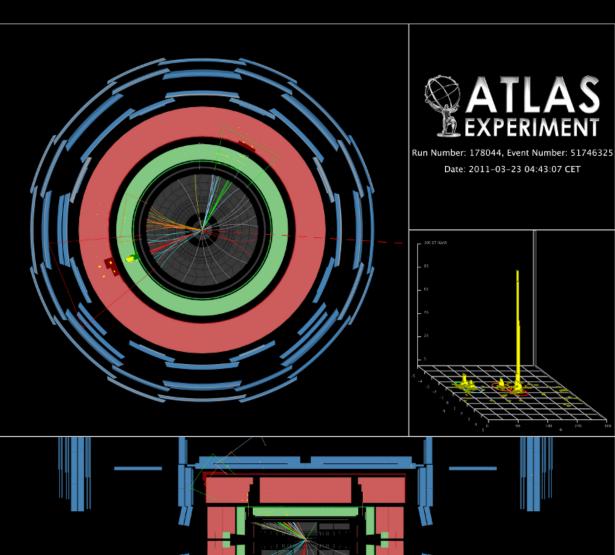


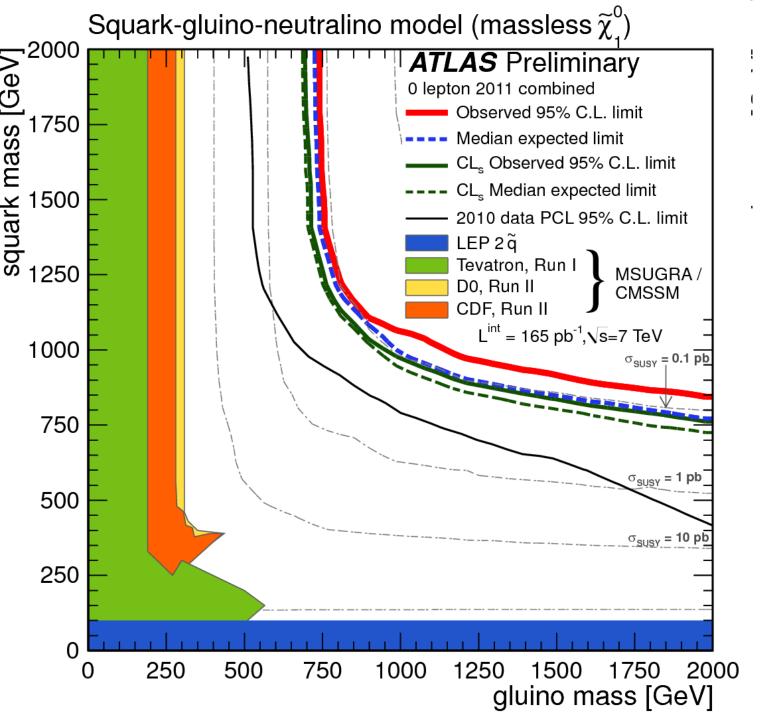
atest AT transverse AS 0-lepton, momentum data. lets missing

Highest Meff event so far

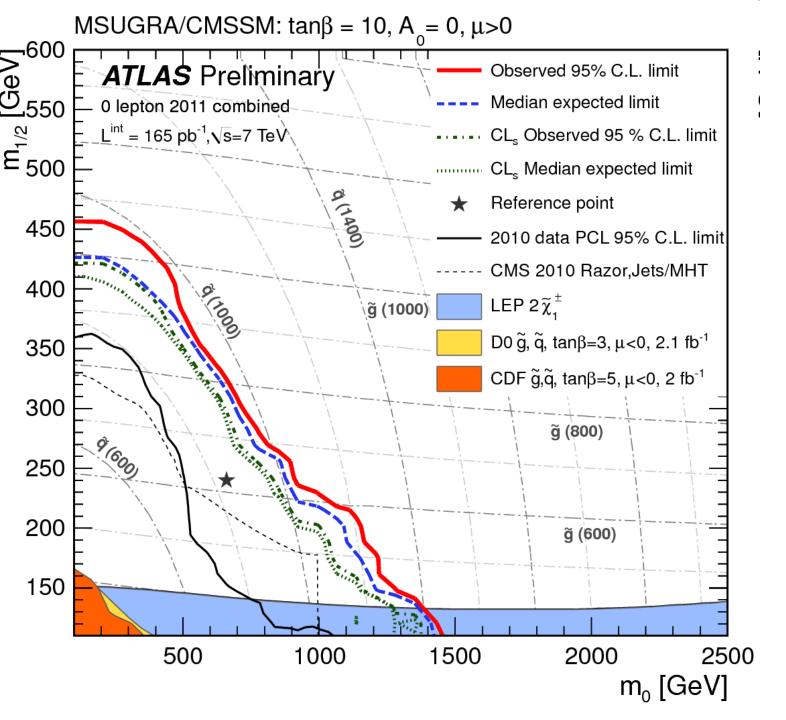
The highest Meff in any (supposedly "clean") ATLAS event is 1548 GeV

- calculated from four jets with pts:
 - 636 GeV
 - 189 GeV
 - 96 GeV
 - 81 GeV
- 547 GeV of missing transverse momentum.





atest A transverse AS S 0-lepton, momentum data. **ets** missing



atest AT transverse LAS 0-lepton, momentum data. **Jets** missing

Don't confuse simplicity with complexity ... can layer add many layers of interpretation

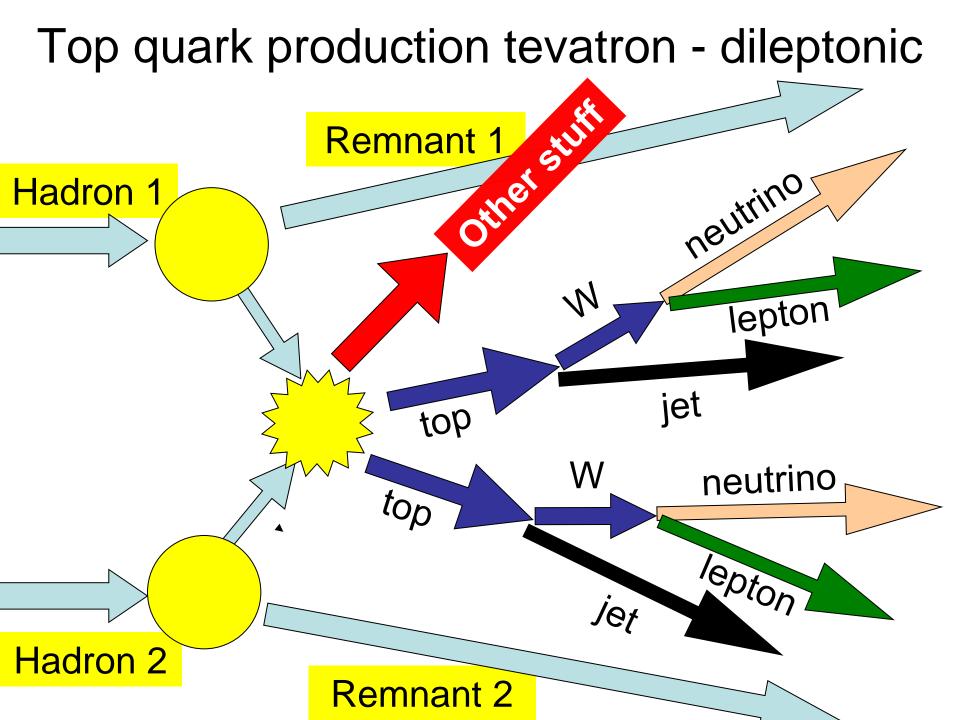
Measure top quark mass from mean lepton PT only!

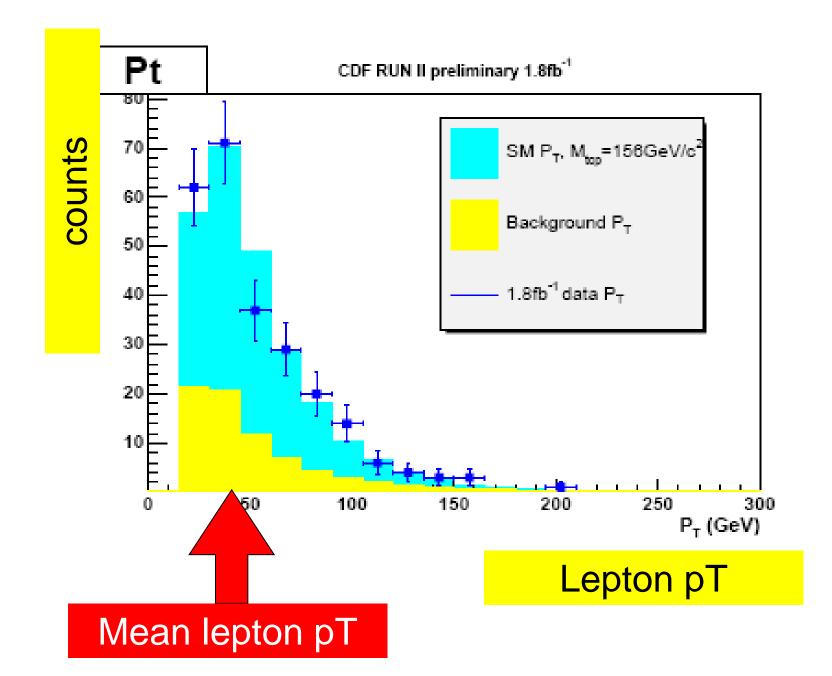


CDF note 8959

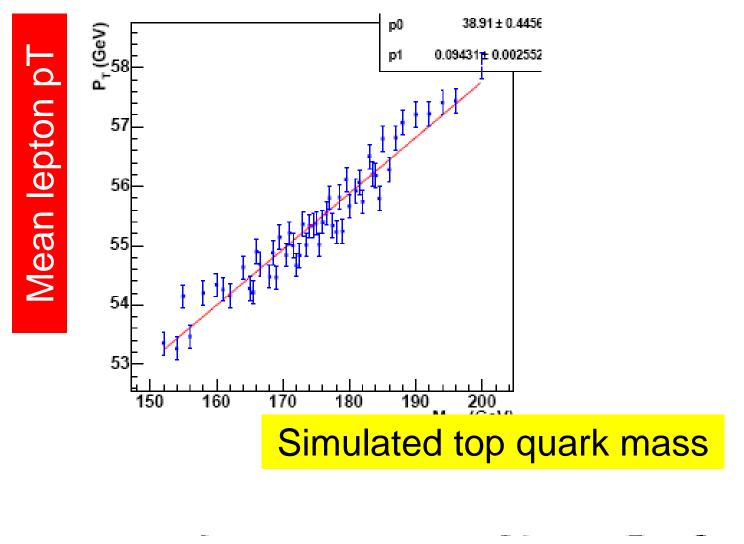
Measurement of the top quark mass from the lepton transverse momentum in the $t\overline{t} \rightarrow dilepton$ channel at the Tevatron

A new measurement of the top quark mass at 1.8 fb⁻¹ integrated luminosity, using leptons' P_T in the dilepton channel is presented. A top quark mass of $m_{top}=156\pm 20_{(stat)}\pm 4.6_{(syst)}GeV/c^2$ is obtained with the Likelihood method and of $149\pm 21_{(stat)}\pm 5(syst)GeV/c^2$ is obtained with the Straight Line method.





Frightening y-axis!



Result $m_{top} = 156 \pm 20_{(stat)} \pm 4.6_{(syst)} GeV_{\mu}$

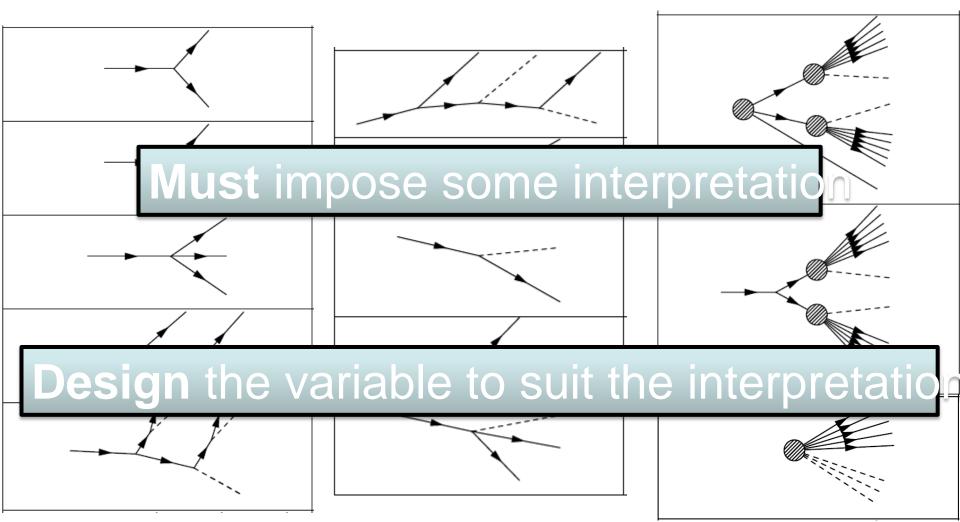
Moral

- You can monte-carlo anything.
 - example h->tau tau
- But do you trust it? Is it the best you can do?

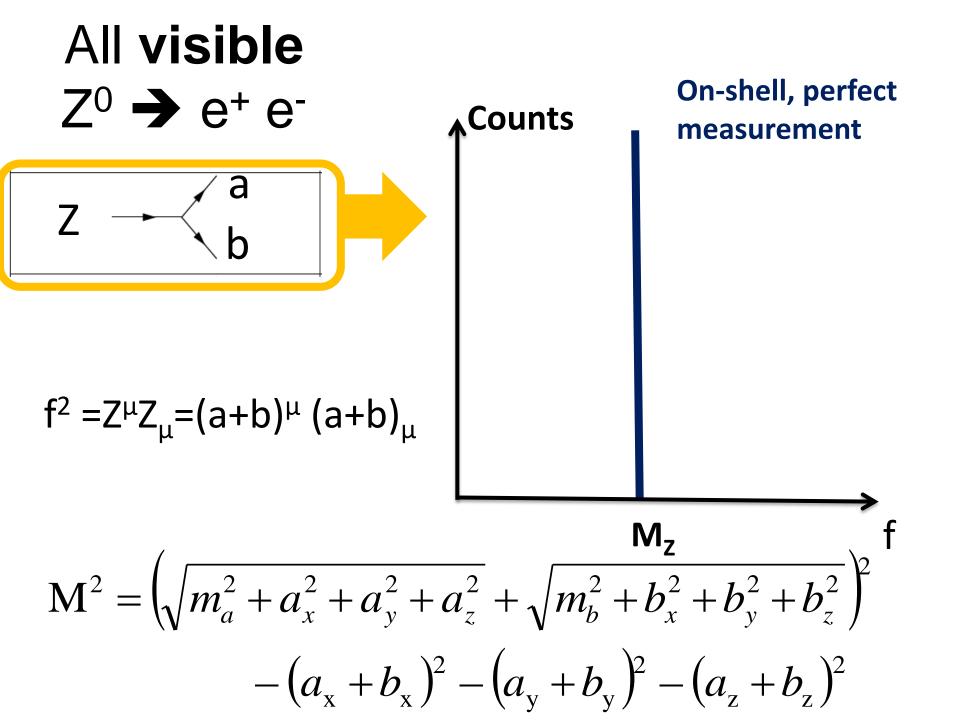
More assumptions Less Vague Conclusions

non-hotpants

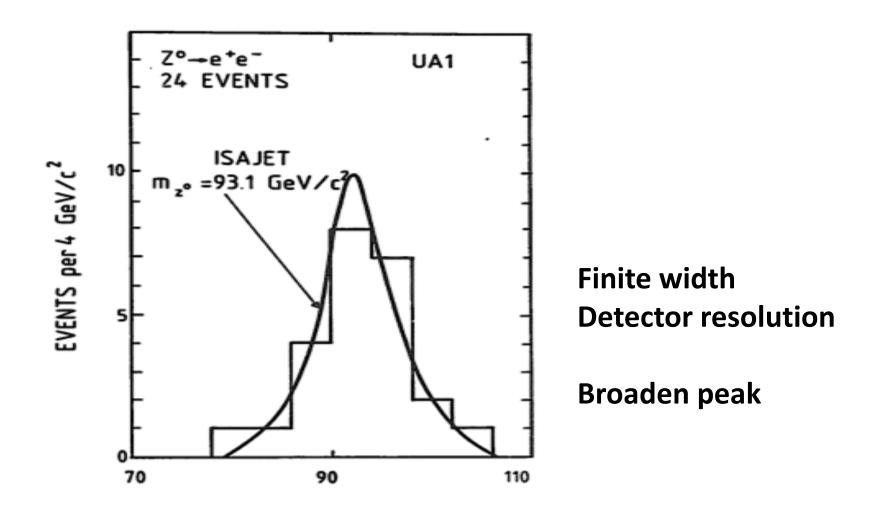
Topology / hypothesis



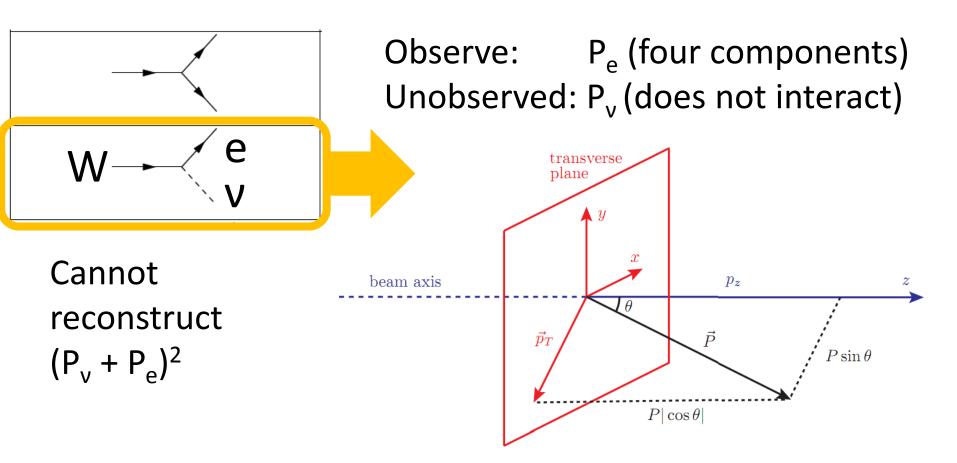
Full index in arXiv:1004.2732



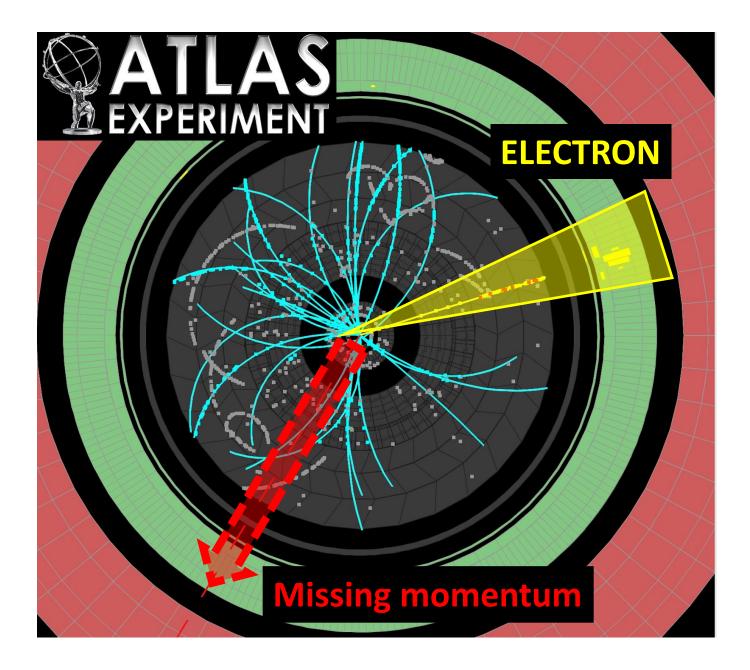
SPS – the Z boson Mass



Dealing with incomplete information



Unobserved, but not unconstrained...



Historical solution:
(full!) W transverse mass

$$m_T^2 = m_e^2 + m_v^2 + 2(e_e e_v - \mathbf{p}_e \cdot \mathbf{p}_v)$$

$$\mathbf{w} = \sqrt{m_e^2 + p_{Te}^2}$$

$$e_e = \sqrt{m_e^2 + p_{Te}^2}$$

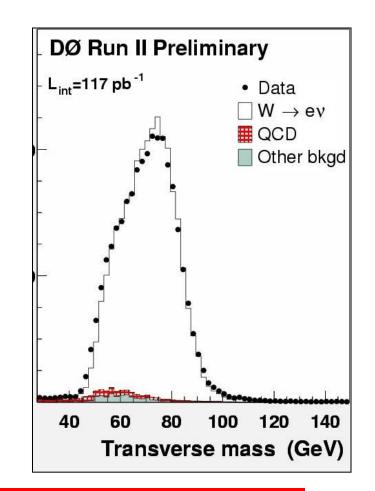
$$e_v = \sqrt{m_v^2 + p_{Tv}^2}$$
HOT THIS !!

$$m_T = \sqrt{2} |\vec{P}_{Te}| |\vec{P}_{Tv}| (1 - \cos \theta)$$

!! This is NOT the transverse mass !!

W transverse mass: nice properties

- In every event $m_T < m_W$ if the W is on shell
- There are events in which m_T can saturate the bound on m_W .
- motivate m_T in W discovery and mass measurements.



But where did these properties come from?

Re-examine invariant mass: $M \rightarrow a b$

$$M^{2} = \left(\sqrt{m_{a}^{2} + a_{x}^{2} + a_{y}^{2} + a_{z}^{2}} + \sqrt{m_{b}^{2} + b_{x}^{2} + b_{y}^{2} + b_{z}^{2}}\right)^{2}$$
$$- (a_{x} + b_{x})^{2} - (a_{y} + b_{y})^{2} - (a_{z} + b_{z})^{2}$$
$$= (E_{a} + E_{b})^{2} - (a_{x} + b_{x})^{2} - (a_{y} + b_{y})^{2} - (a_{z} + b_{z})^{2}$$
$$= m_{a}^{2} + m_{b}^{2} + 2(E_{a}E_{b} - a_{x}b_{x} - a_{y}b_{y} - a_{z}b_{z})$$
$$= m_{a}^{2} + m_{b}^{2} + 2(e_{a}e_{b}\cosh(\Delta\eta) - a_{x}b_{x} - a_{y}b_{y})$$

where

$$\begin{aligned} e_{a} &= \sqrt{m_{a}^{2} + a_{x}^{2} + a_{y}^{2}} \\ e_{b} &= \sqrt{m_{b}^{2} + a_{b}^{2} + a_{b}^{2}} \end{aligned} \quad \text{and} \quad \begin{aligned} \eta_{a} &= \frac{1}{2} \ln((E_{a} + a_{z})/(E_{a} - a_{z})) \\ \eta_{b} &= \frac{1}{2} \ln((E_{b} + b_{z})/(E_{b} - b_{z})) \\ \Delta \eta &= \eta_{a} - \eta_{b} \end{aligned}$$

Comparing invariant and transverse masses:

$$M^{2} = m_{a}^{2} + m_{b}^{2} + 2\left(e_{a}e_{b}\cosh(\Delta\eta) - a_{x}b_{x} - a_{y}b_{y}\right)$$
$$M_{T}^{2} = m_{a}^{2} + m_{b}^{2} + 2\left(e_{a}e_{b} - a_{x}b_{x} - a_{y}b_{y}\right)$$

Since $\cosh(\Delta \eta) \ge 1$ have $M_T \le M$ with equality when $\Delta \eta = 0$.

(Not same as throwing away z information!)

But have bound, and bound can be saturated.

Note that at this point we are assuming we know m_b.

W boson mass measurement

mw

Counts

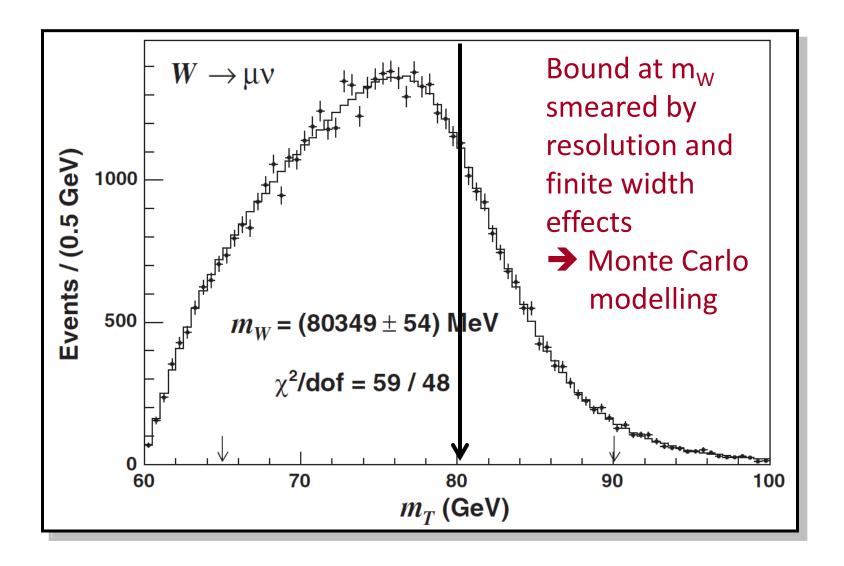
Plot m_T for each event

Each new event gives a new lower bound on m_w

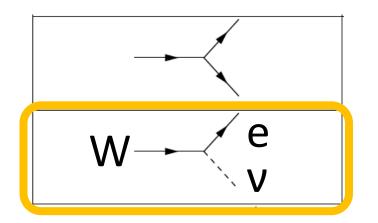
If bound is saturated (as it is in this example) the endpoint is m_w

Phys.Rev.D. 77, 112001 (2008)

In the data....



Alternative way of approaching the problem



Set out **INTENDING** to construct best lower **bound** on $(P_e+P_v)^2$ given the constraints

Constraints in this instance: $0 = (P_v)^2$ [massless neutrino] $0 = \Sigma \mathbf{p}_T = \mathbf{u}_T + \mathbf{p}_T(e) + \mathbf{p}_T(v)$

[momentum conservation in transverse plane]

Suggests general prescription...

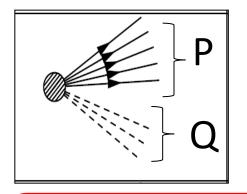
(1) Propose a decay topology
 (2) Write down your the Lorentz Invariant of choice
 (3) Write down the constraints
 (4) Calculate the bound (algebraically/numerically/mix)

(1)
$$P_{i}$$

(2)
$$\mathcal{M}_a \equiv \sqrt{g_{\mu\nu} \left(\mathbf{P}_a + \mathbf{Q}_a\right)^{\mu} \left(\mathbf{P}_a + \mathbf{Q}_a\right)^{\nu}}$$

(3)
$$\sum_{i=1}^{N_{\mathcal{I}}} \vec{q}_{iT} = \vec{p}_T \equiv -\vec{u}_T - \sum_{i=1}^{N_{\mathcal{V}}} \vec{p}_{iT}$$

Single parent ... multiple daughters



 $M_{\rm slash} = \sum \tilde{M}_i$

many visibles

many invisibles

$$M_{1T}^{2} = \left(\sqrt{M_{P}^{2} + \vec{\mathbf{p}}_{T}^{2}} + \sqrt{M_{\text{slash}}^{2} + \vec{\mathbf{q}}_{T\text{miss}}^{2}} \right)^{2} - u_{T}^{2}$$

Bound depends on GUESS masses of all invisible daughters Most conservative: set to zero [more later] Almost exactly same as transverse mass – one small generalization

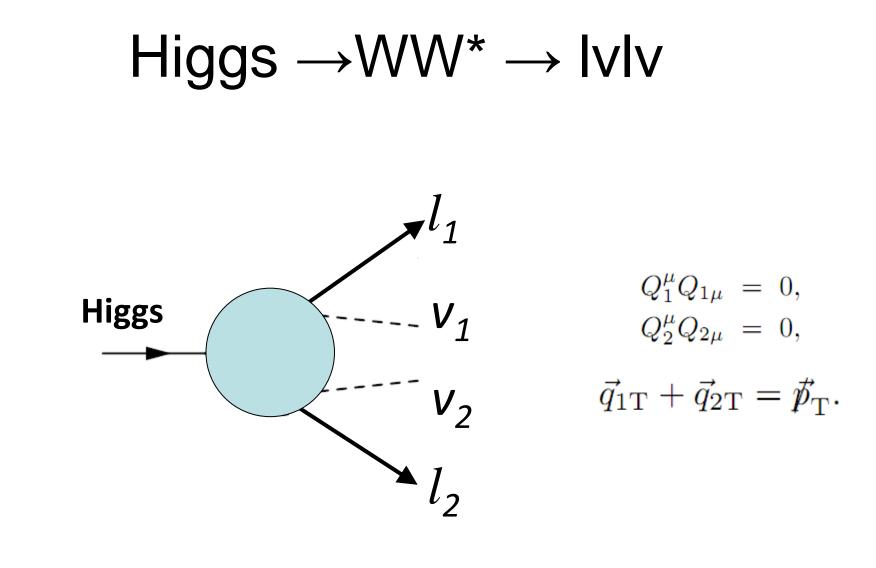
$$M_{1T}^{2} = \left(\sqrt{M_{P}^{2} + \vec{\mathbf{p}}_{T}^{2}} + \sqrt{M_{\text{slash}}^{2}} + \vec{\mathbf{q}}_{T\text{miss}}^{2}\right)^{2} - u_{T}^{2}$$
$$M_{T}^{2} = \left(\sqrt{M_{P}^{2} + \vec{\mathbf{p}}_{T}^{2}} + \sqrt{M_{Q}^{2}} + \vec{\mathbf{q}}_{T\text{miss}}^{2}\right)^{2} - u_{T}^{2}$$

The "invisible mass" has become a parameter rather than the actual visible mass.

We will come back to this many times.

Suggests we should think about non-physical parameters a bit more

Applications of M_{1T} ?



Written up in http://arxiv.org/abs/1106.2322

 $Higgs \rightarrow WW^* \rightarrow IvIv$

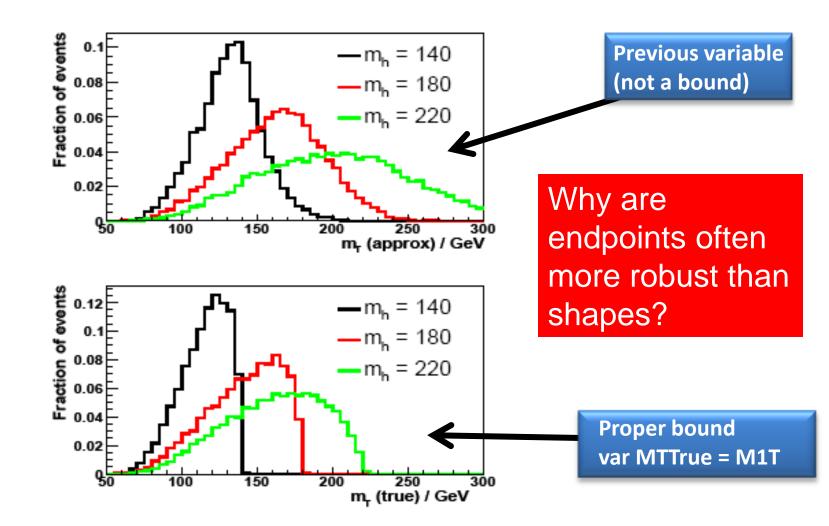
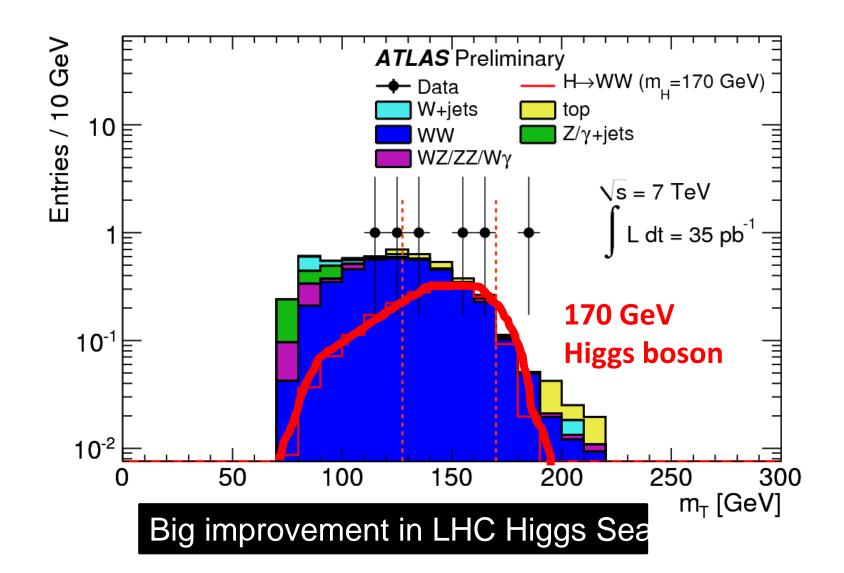
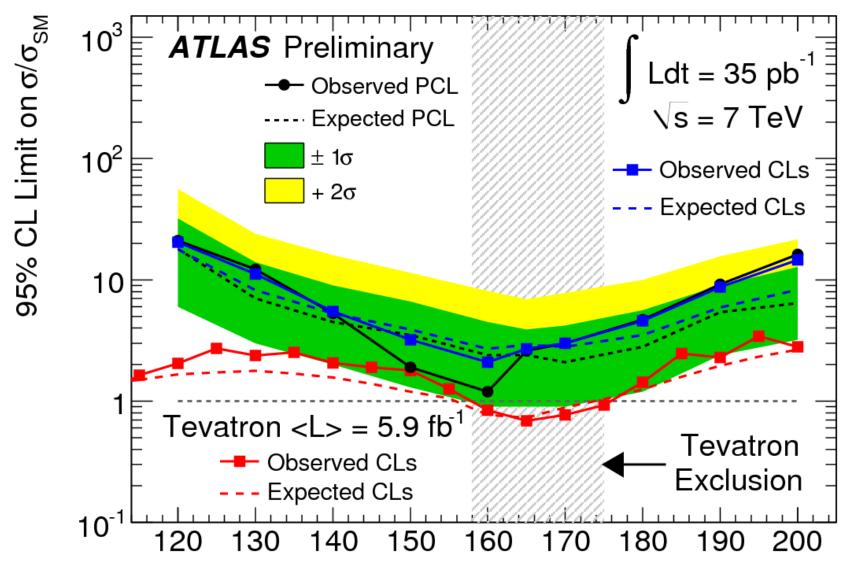


FIG. 1: Signal-only distributions of m_T^{approx} (top) and m_T^{true} (bottom) for various values of m_h (in GeV). No cuts on $\Delta \phi_{\ell\ell}^{\text{max}}$ and p_{TWW}^{min} have been applied.

Against the 2010 LHC data...



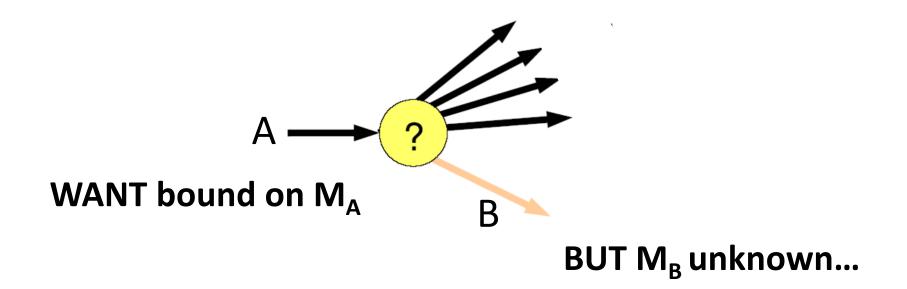
ATLAS 35/pb: $H \rightarrow WW \rightarrow IvIv$



m_H [GeV]

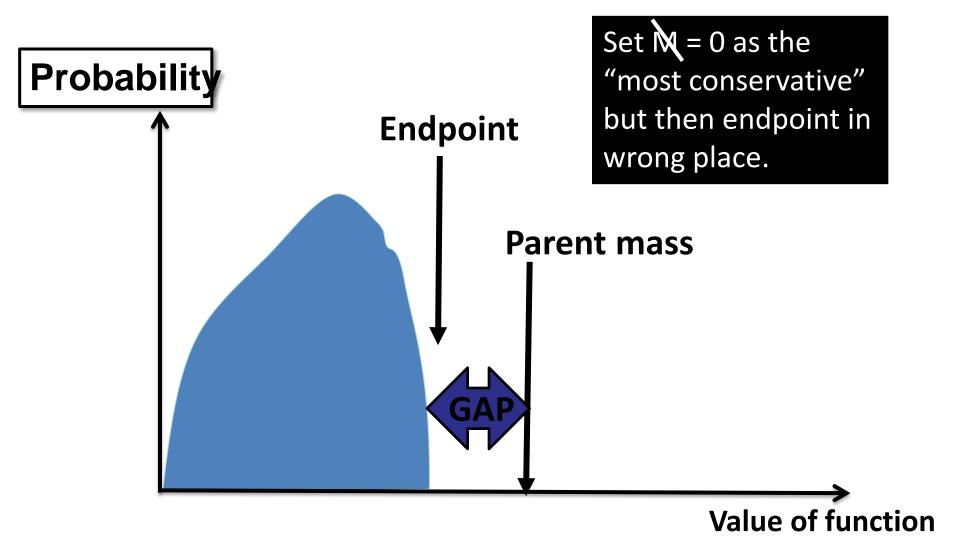
change of topic – moving closer to BSM

What if we don't know the masses of the invisible particle(s)?



Can we construct a maximal lower bound on M_A that depends on a hypothesis for M_B ?

Hmm "wrong M_B " not what M_T was designed for.

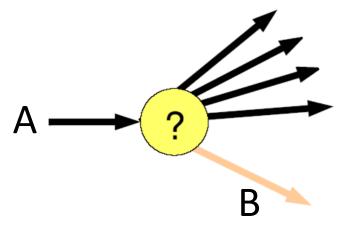


Let's go back to the (full) transverse mass again for a closer look!

In next few slides:

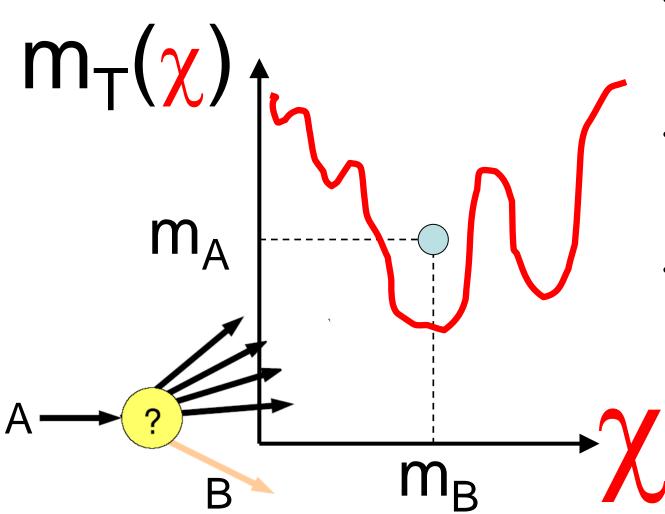
 $\chi =$

Guess (i.e. hypothesis) for mass of the invisible daughter



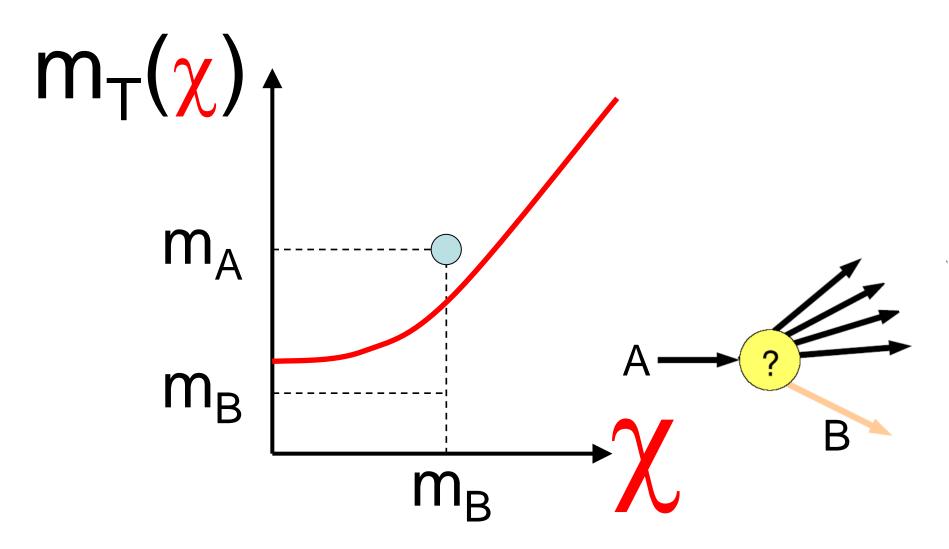
In other words, we will use χ in all the places we previously used M_B.

Schematically, all we have guaranteed so far is the picture below:



- Since "x" can now be "wrong", some of the properties of the transverse mass can "break":
- $m_T(\chi)$ max is no longer invariant under transverse boosts! (except when $\chi=m_B$)
- $m_T(\chi) < m_A$ may no longer hold! (however we always retain: $m_T(m_B) < m_A$)

Actual dependence on invisible mass guess χ more like this:



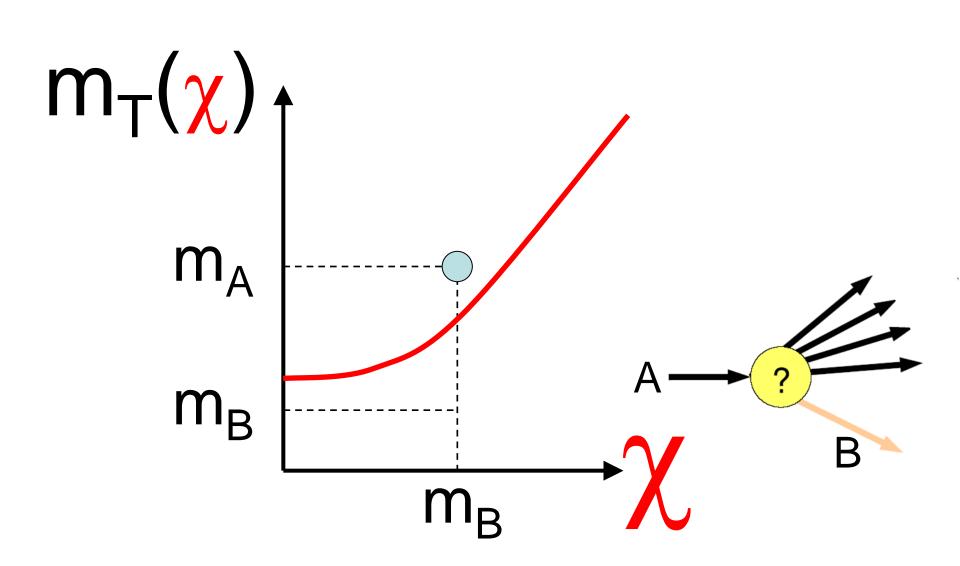
In fact, we get this very nice result:

</h

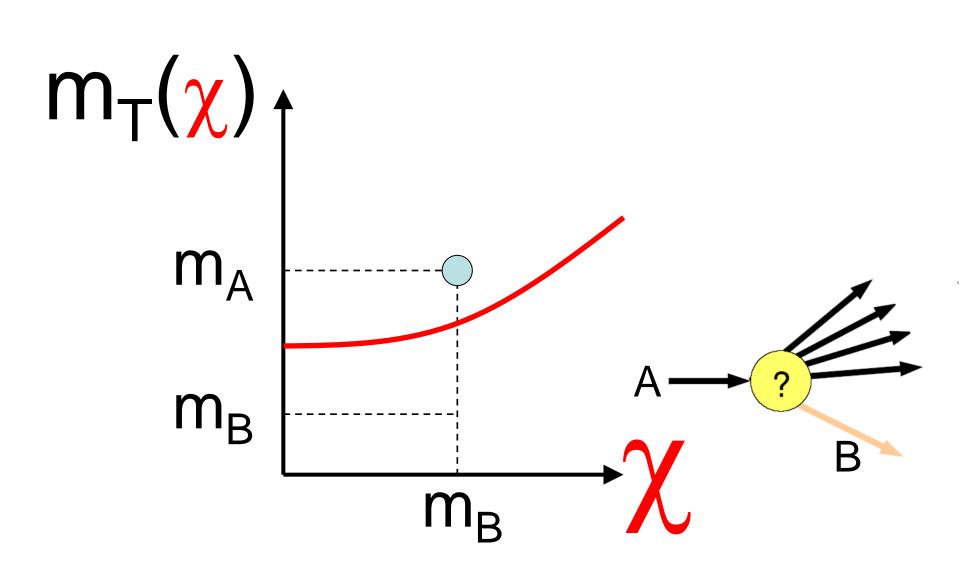
The "full" transverse mass curve is the boundary of the region of (mother,daughter) masses consistent with the observed event!

Minimal Kinematic Constraints and m(T2), Hsin-Chia Cheng and Zhenyu Han (UCD) e-Print: <u>arXiv:0810.5178 [hep-ph]</u> and "Transverse masses and kinematic constraints, from the Boundary to the Crease" <u>arXiv:0908.3779</u>

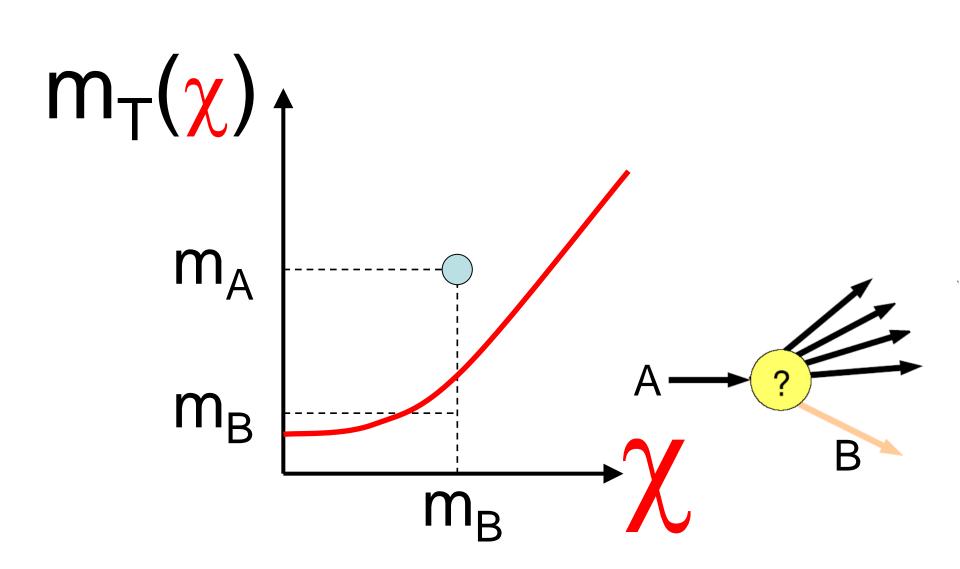
Event 1 of 8



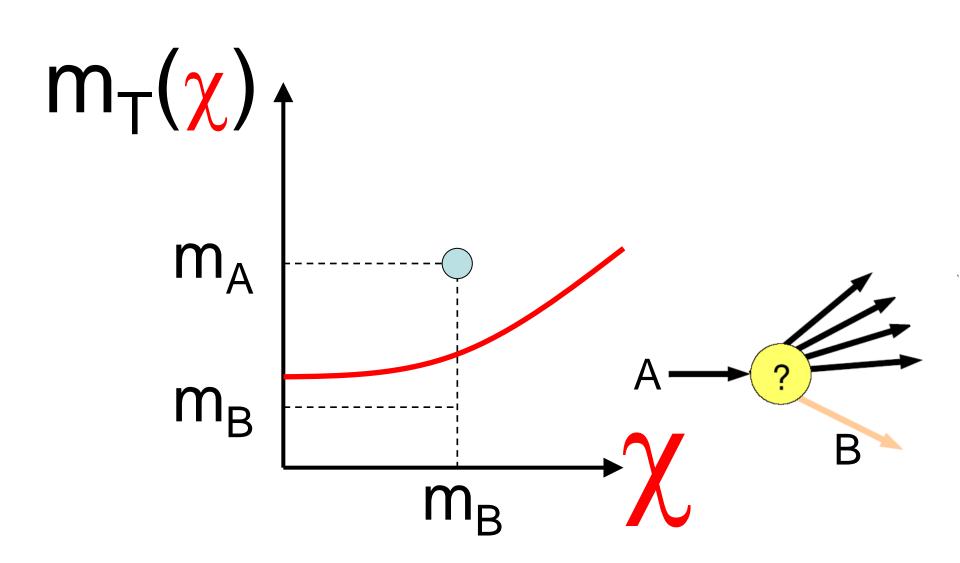
Event 2 of 8



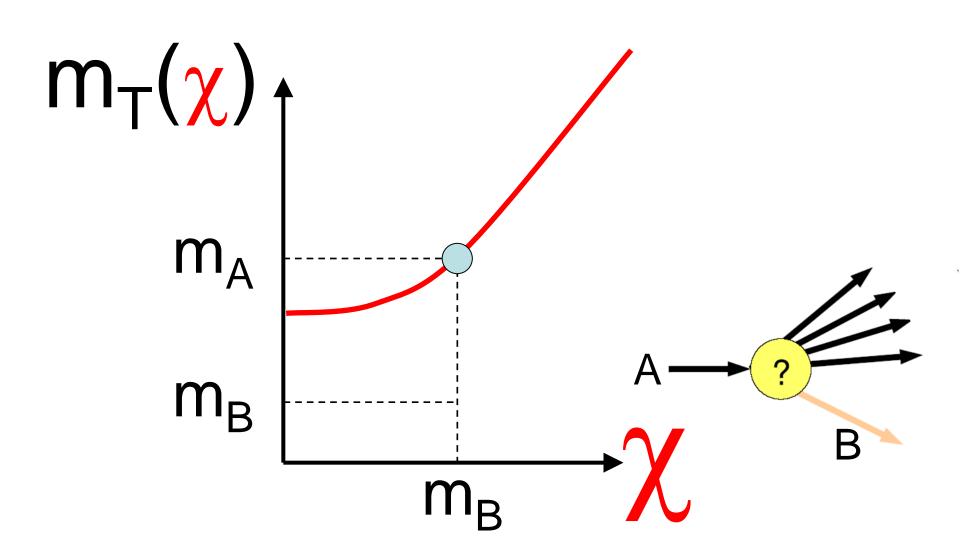
Event 3 of 8



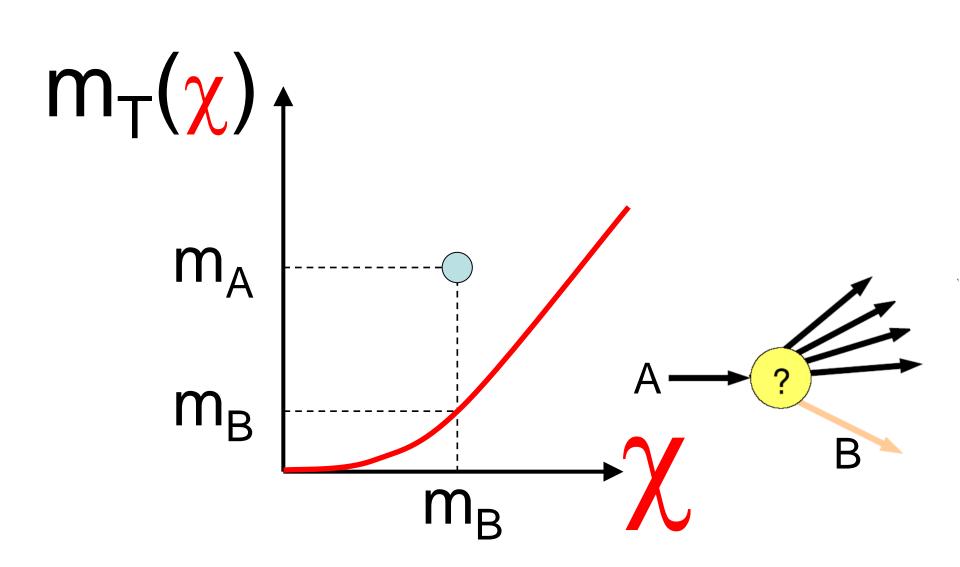
Event 4 of 8



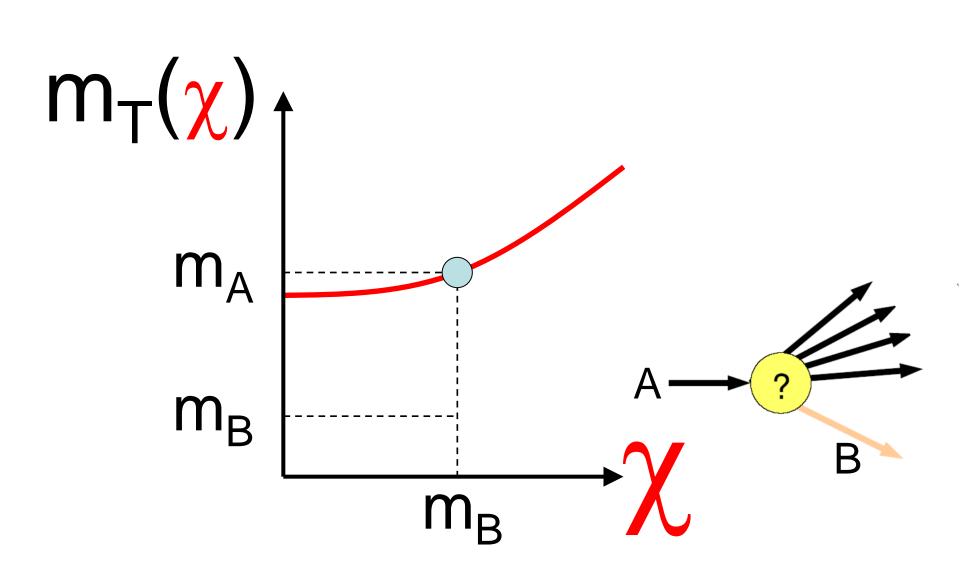
Event 5 of 8



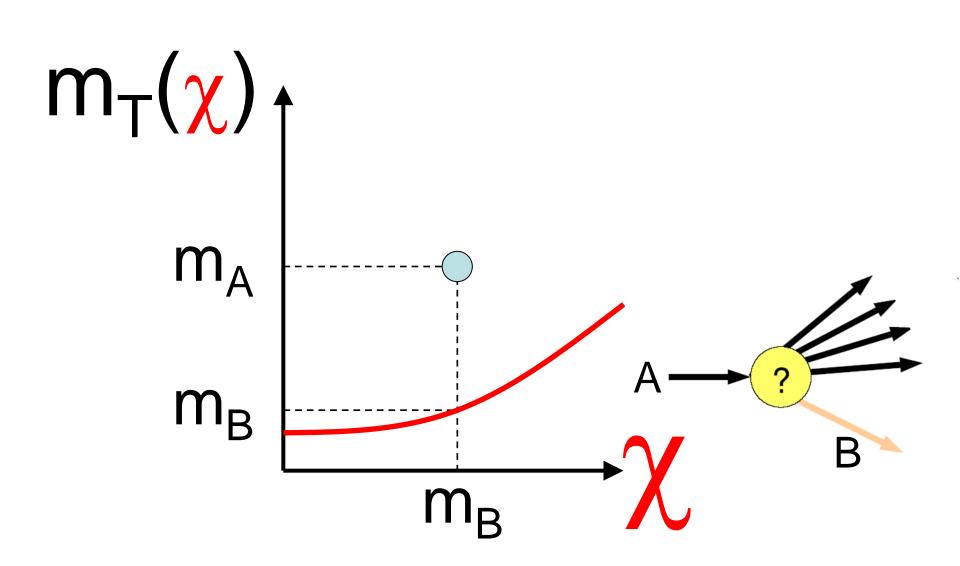
Event 6 of 8



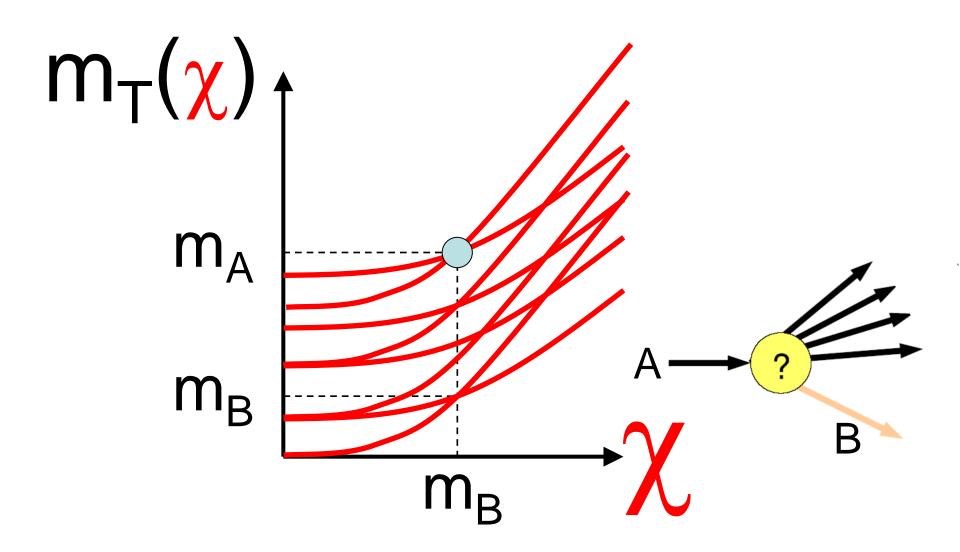
Event 7 of 8



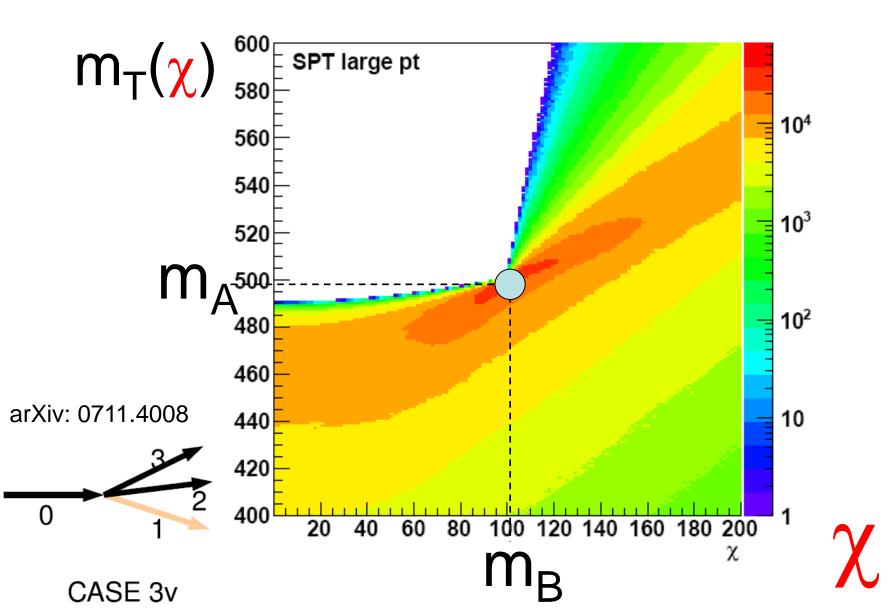
Event 8 of 8



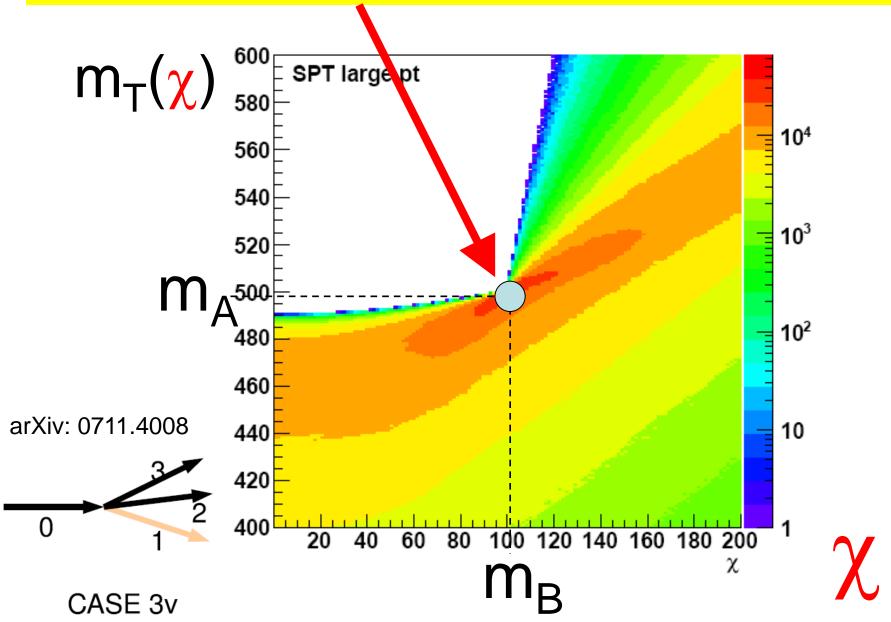
Overlay all 8 events



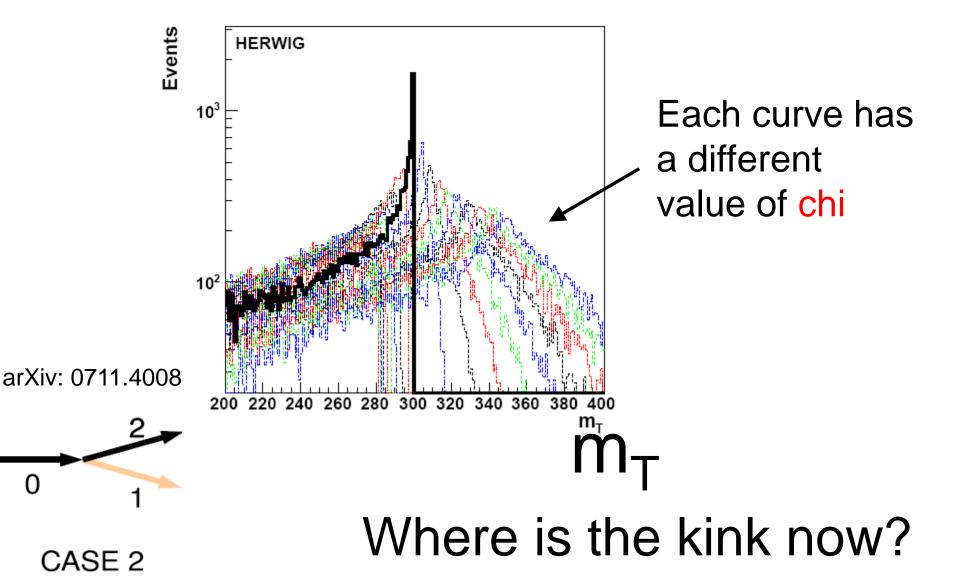
Overlay many events



Here is a transverse mass "KINK"



Alternatively, look at M_T distributions for a variety of values of chi.



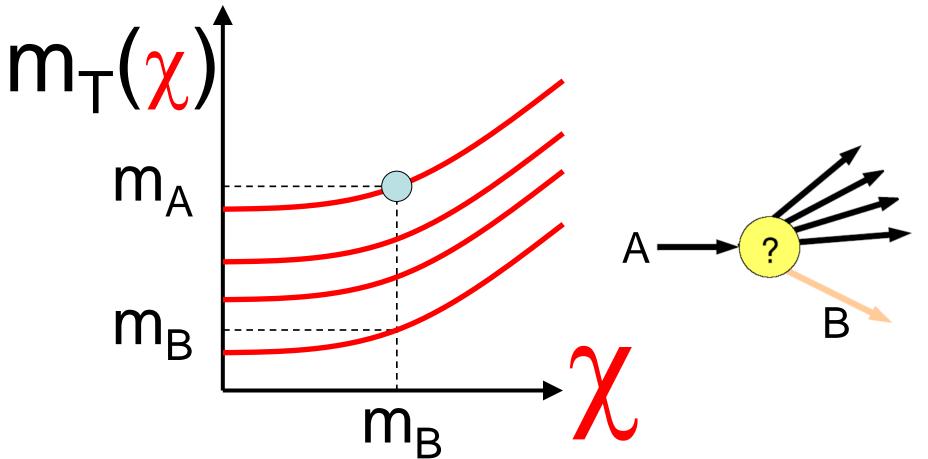
0

What causes the kink?

- Two entirely independent things can cause the kink:
 - -(1) Variability in the "visible mass"
 - (2) Recoil of the "interesting things" against Upstream Transverse Momentum
- Which is the dominant cause depends on the particular situation ... let us look at each separately:

Kink cause 1: Variability in visible mass

- $m_{\mbox{Vis}}$ can change from event to event
- Gradient of $m_T(\chi)$ curve depends on m_{Vis}
- Curves with low m_{Vis} tend to be "flatter"



Kink cause 1: Variability in visible mass

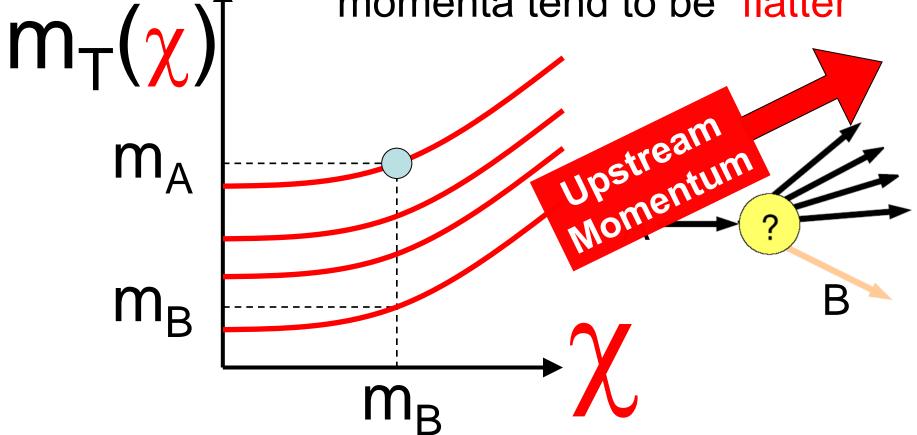
- m_{Vis} can change from event to event
- Gradient of $m_T(\chi)$ curve depends on m_{Vis}
- Curves with high m_{Vis} tend to be "steeper" $m_T(\chi)$ **m**_A m_R

Upstream Momentum Visible Invisible Kink cause 2: **Recoil against Upstream Momentum**

Kink cause 2: Recoil against UTM

- UTM can change from event to event
- Gradient of $m_{\tau}(\chi)$ curve depends on UTM
- Curves with UTM parallel to visible

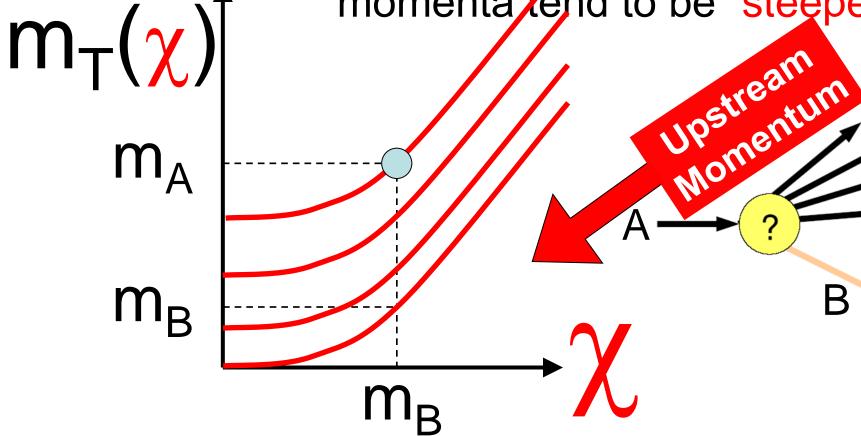
momenta tend to be "flatter"



Kink cause 2: Recoil against UTM

- UTM can change from event to event
- Gradient of $m_{\tau}(\chi)$ curve depends on UTM
- Curves with UTM opposite to visible







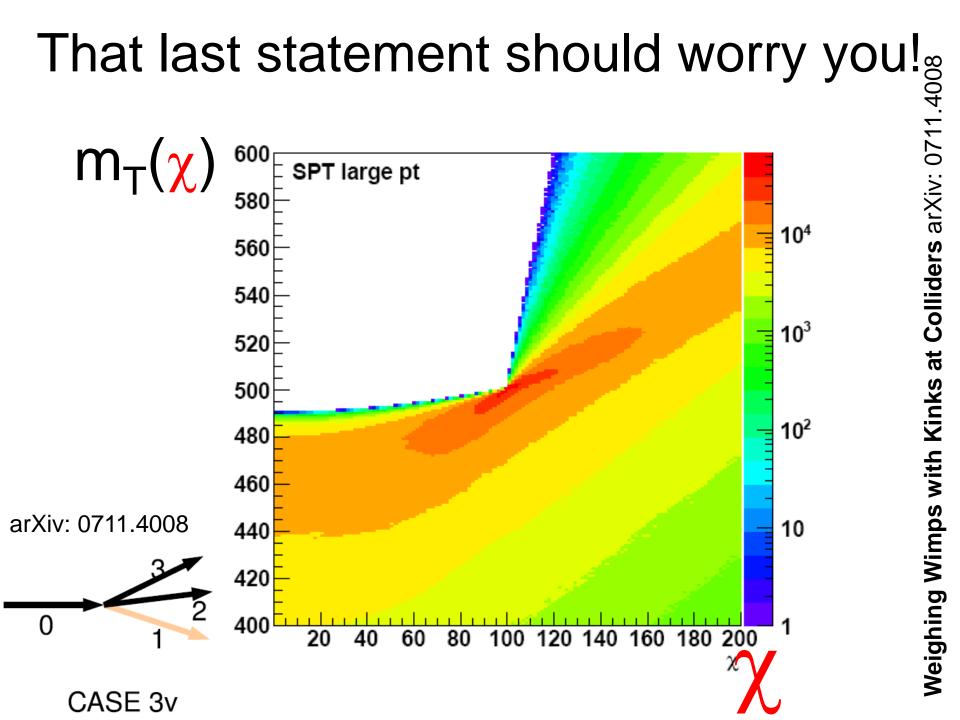
Health warning!

(for those of you interested in LHC dark matter constraints)



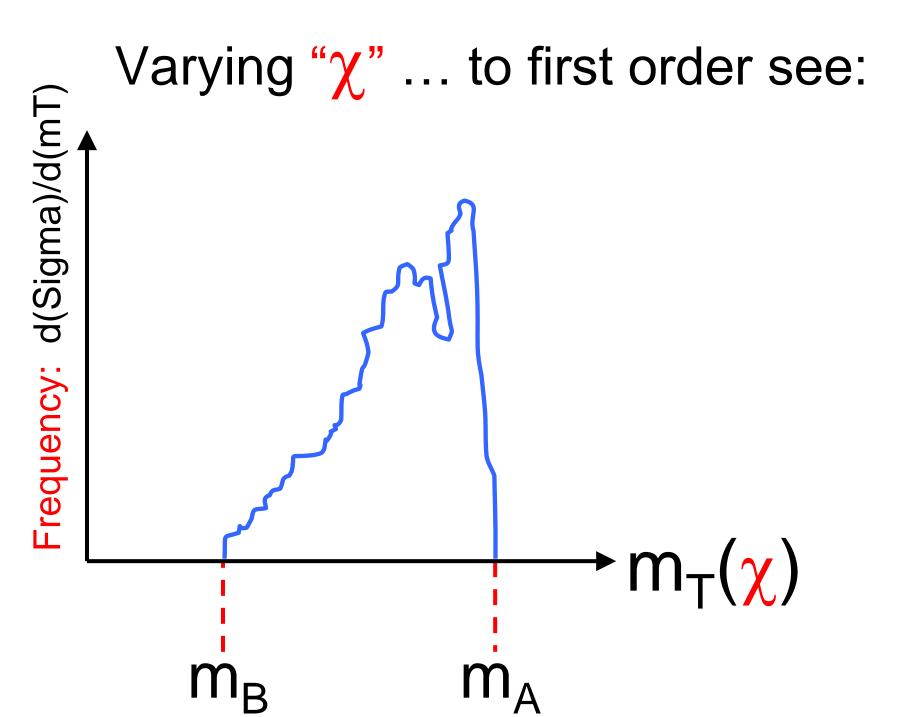
Rather worryingly, M_T kinks are at present the only known kinematic methods which (at least in principle) allow determination of the mass of the invisible particle in short chains at hadron colliders!

[We will see a dynamical method that works for single three+ body decays shortly. Likelihood methods can determine masses in pair decays too, though at cost of model dependence and CPU. See Alwall.]



Spot the kink





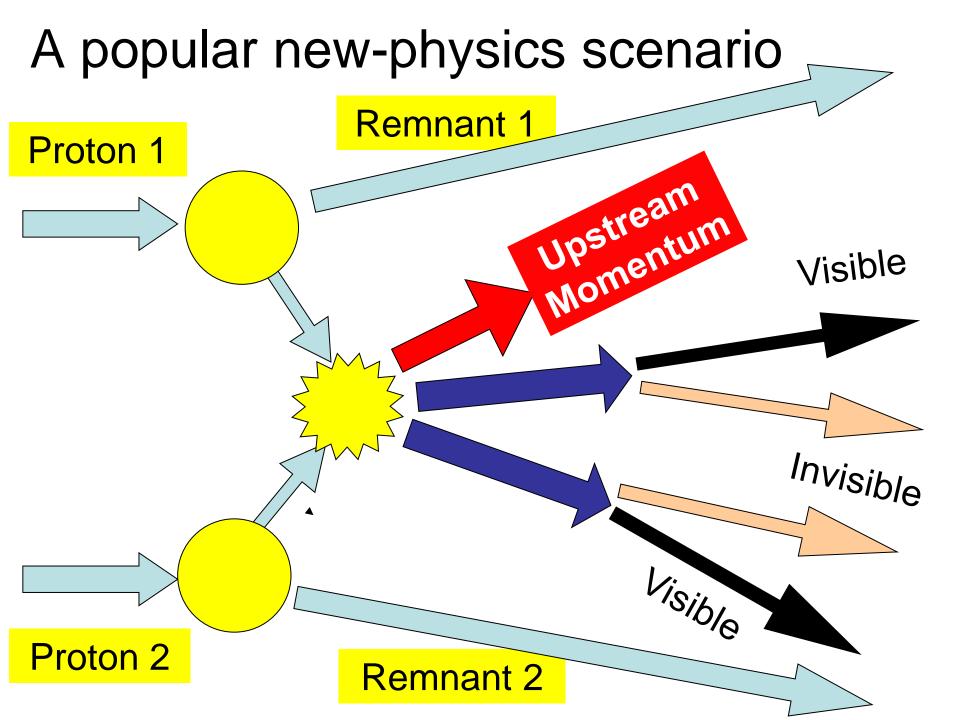
Take home messages for MT

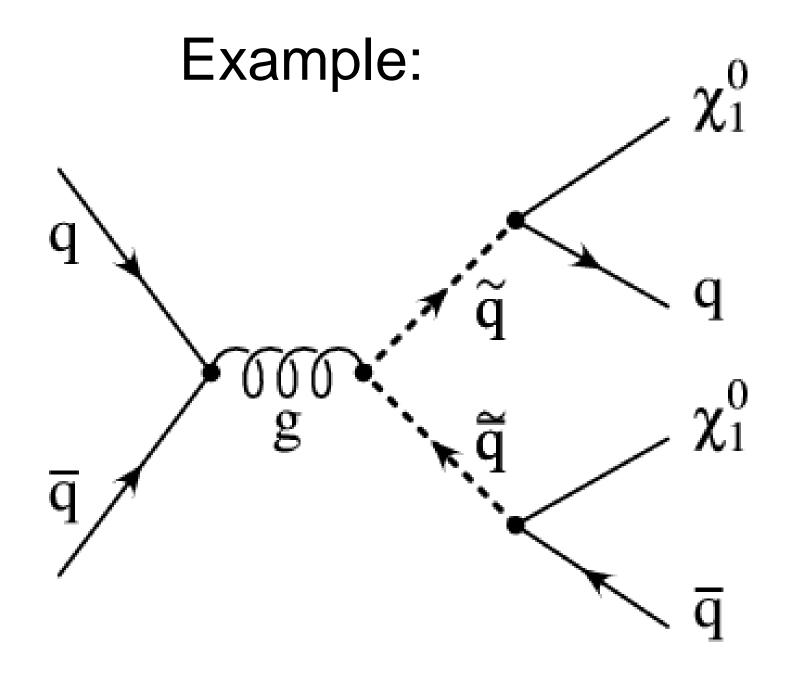
- EASY to get MASS DIFFERENCE
- We have two independent kinematical opportunities to measure invisible daughter mass in single particle decays:
 - "Upstream boost induced" MT kink
 - from ISR alone, useless, from real UTM, possible
 - "Variable visible mass induced" MT kink
 - impossible in 2-body decay, otherwise possible

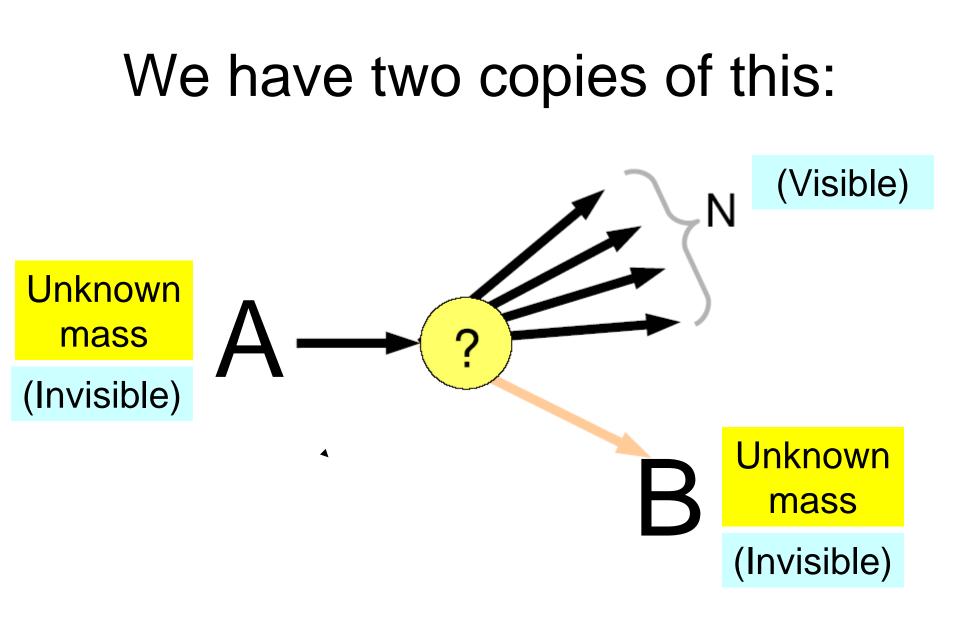
-HARD to set absolute mass scale

• We used pT-miss information – so only works with one invisible (so far ...)

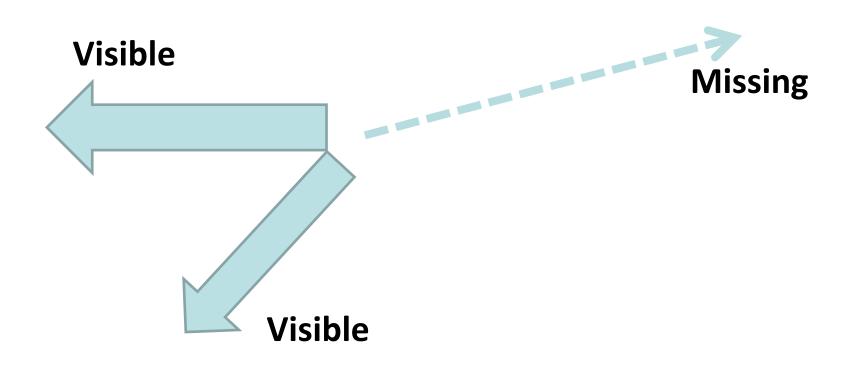
Change of topic: How do we measure masses when there is **Pair Production**?

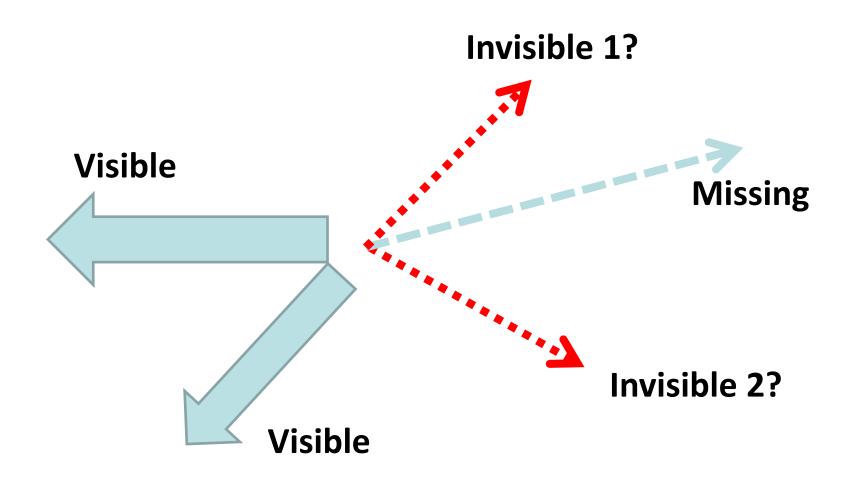




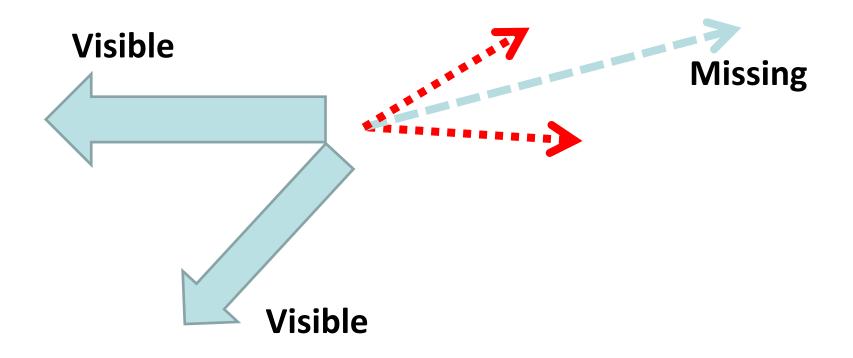


But don't know p_T of B this time! \bigotimes

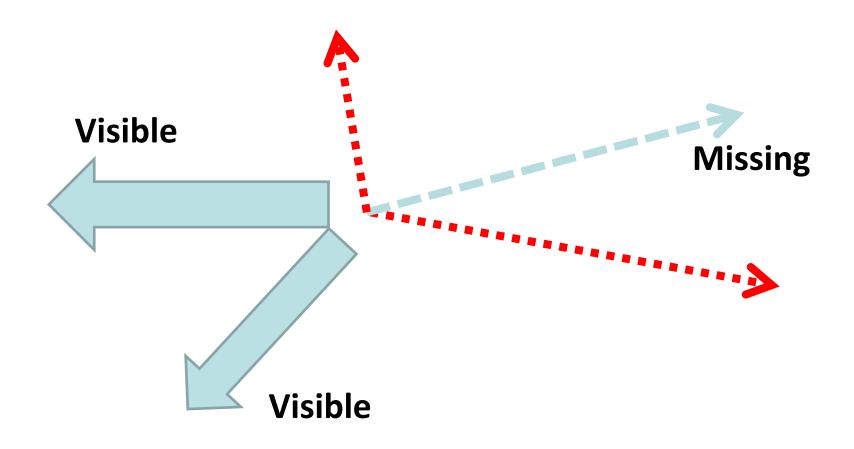




a possible "splitting"

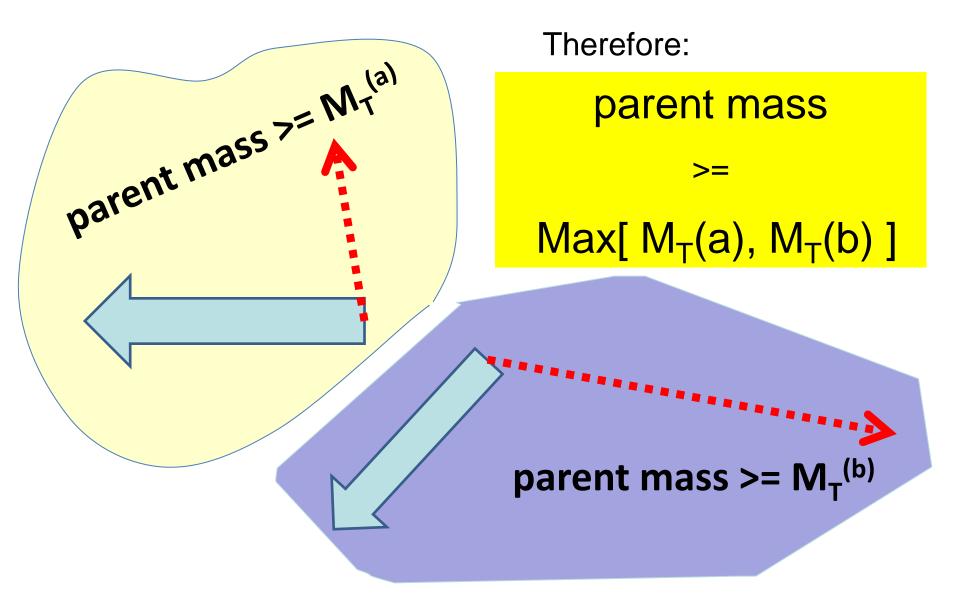


another possible "splitting"

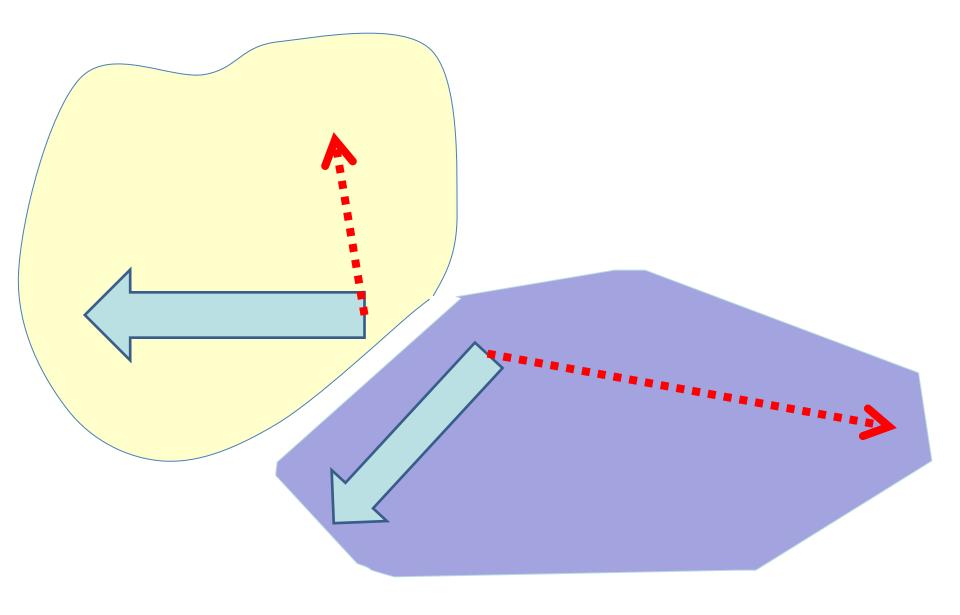


another possible "splitting"

If this splitting is "correct":



But this splitting might be wrong!



But can say that:

Lester and Summers (hep-ph/9906349)

This is m_{T2} the "Stransverse Mass"

$$m_{T2}(v_1, v_2, \mathbf{p}_T, m_i^{(1)}, m_i^{(2)}) \equiv \min_{\sum \mathbf{q}_T = \mathbf{p}_T} \left\{ \max\left(m_T^{(1)}, m_T^{(2)}\right) \right\}$$

The most conservative partition consistent with the constraint

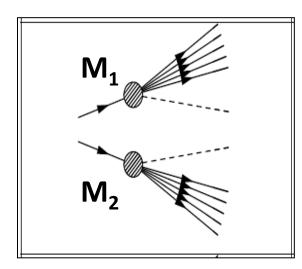
Take the better of the two lower bounds

It is the <u>generalisation of transverse mass to pair production</u>. Clear how to generalise it to any other types of production.

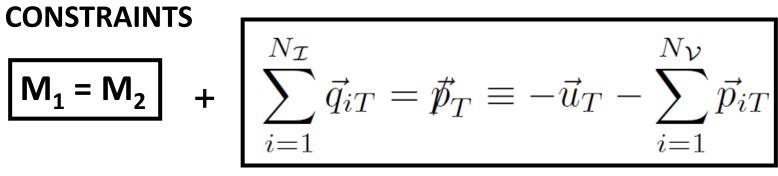
[Received six comments about "mis-spelling" of transverse in ATLAS editorial board!]

Note MT2 def is part of the four-step procedure:

[(1) select topology, (2) parent mass, (3) constraints, (4) find maximal lower bound] described earlier.



Note, other approaches: MCT, Rogan, etc.



Momentum conservation in transverse plane

In other words:

If your event is signal ...

and if MT2 is "350 GeV" ... then the squark mass is \geq 350 GeV.

Indeed, can show MT2 is, by construction, the best possible lower bound on the squark mass.

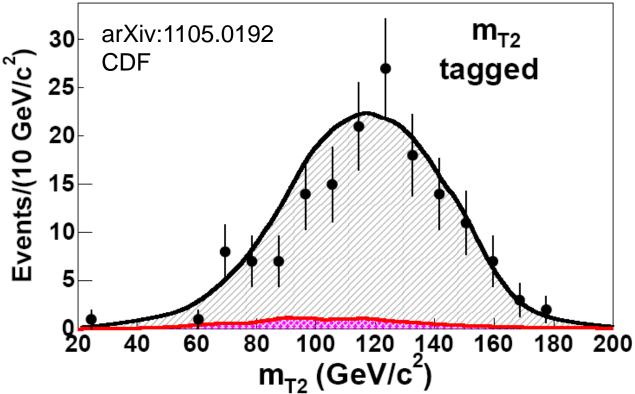
q

000 g χ_1^0

q

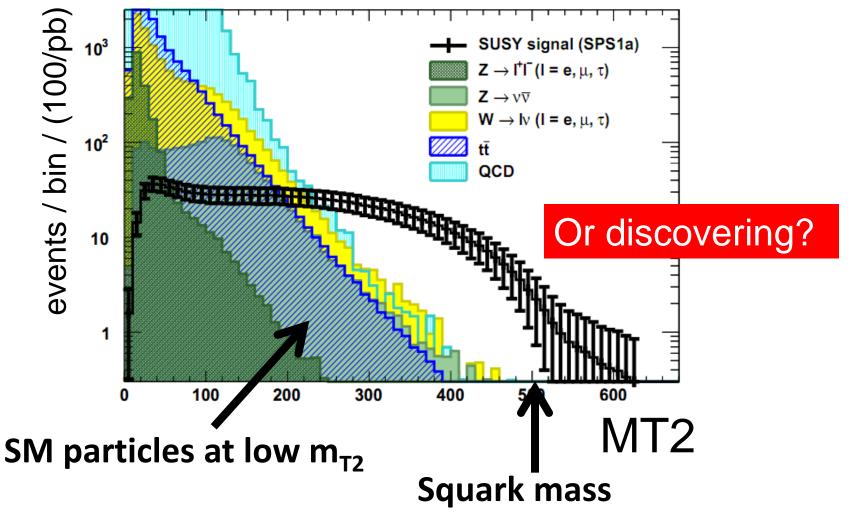
MT2 example in real data

 "Top Quark Mass Measurement using mT2 in the Dilepton Channel at CDF" (arXiv:0911.2956 and arXiv:1105.0192) reports that they "achieve the single most precise measurement of m_{top} in [the dilepton] channel to date". Also under study by ATLAS.

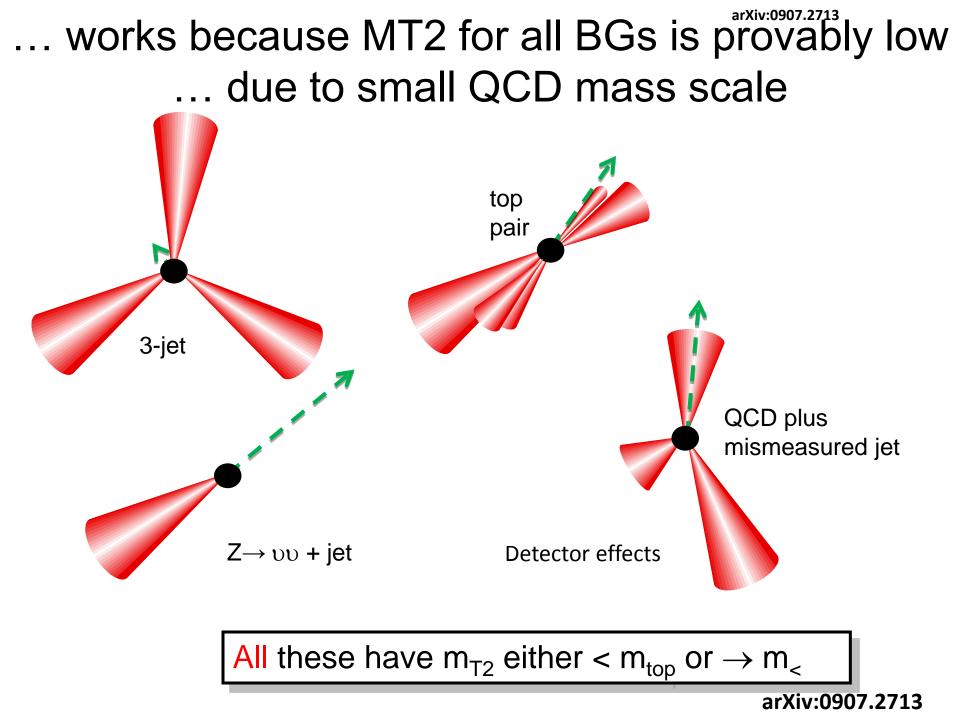


Top-quark physics is an important testing ground for mT2 methods, both at the LHC and at the Tevatron. If it can't work there, its not going to work elsewhere.

Example MT2 distribution ?weighing? 500 GeV squarks

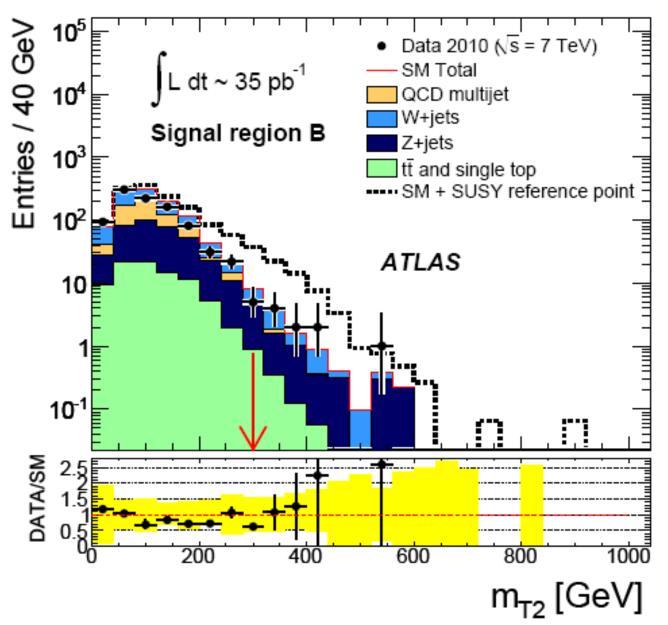


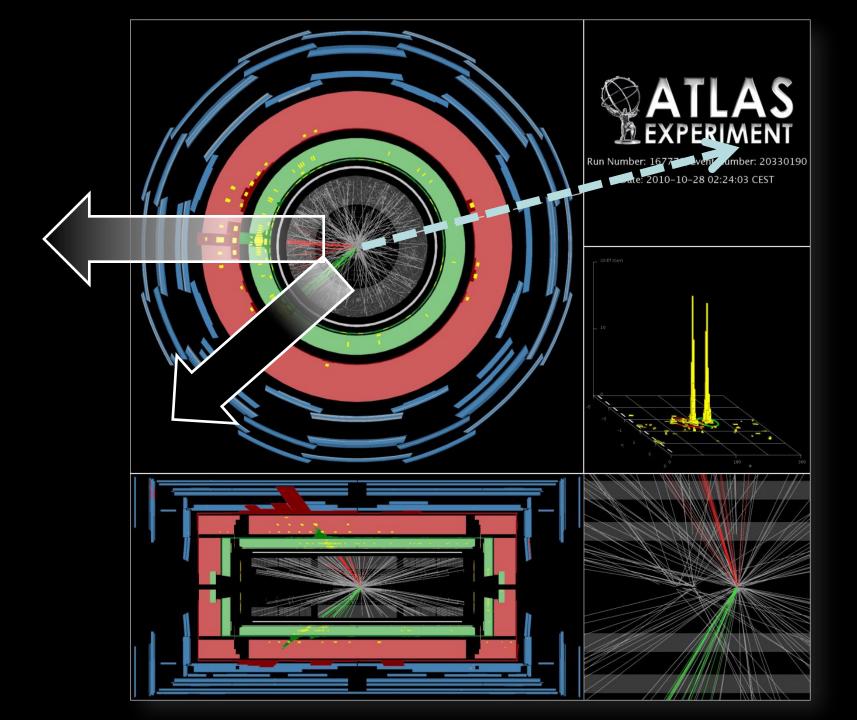
arXiv:0907.2713



Process	$m_{T2}(v_1, v_2, p_T, 0, 0)$	Comments
QCD di-jet \rightarrow hadrons	$= \max m_j$ by Lemmas 1.4	5?
QCD multi jets \rightarrow hadrons	$= \max m_j$ by Lemma 4	lepto!
$t\bar{t}$ production	$= \max m_j$ by Lemma 4	fully hadronie di ⁵ s
	$\leq m_t$ by Lemmas 1.7	fully hadronian distributions? fully hadronian distributions fully hadronic decays fully hadronic decays ful
Single top / tW	$= \max m_j$ by Lemma 4	fully big onc decays
	$\leq m_t$ by Lemmas 2.7	a nal conic decays
Multi jets: "fake" $p \hspace{-1.5mm} /_T$	$= \max m_j$ by Lemma 5	sig_{gle}^{9} mismeasured jet ^a
	$= \max m_j$ by Lemp u^{cllo}	two mismeasured $jets^a$
Multi jets: "real" $p\!\!\!/_T$	$= \max m_j$ by $\prod_{j \in \mathcal{O}} \int \int \frac{1}{2} dx_j dx_j dx_j dx_j dx_j dx_j dx_j dx_j$	single jet with leptonic $b \operatorname{decay}^a$
	$= \max m_j \sum_{i=1}^{2} p^{2i}$ inma 6	two jets with leptonic b decays ^{<i>a</i>}
$Z ightarrow u ar{ u}$	= 0 by 0 is 0	
$Zj ightarrow u ar{ u}j$	$=$ $n^{1/1}$ Lemma 3	one ISR jet^a
$W ightarrow \ell u^{-b}$	We by Lemma 3	
$W j \rightarrow \ell \nu j^{b}$	$\leq m_W$ by Lemma 2	one ISR jet^a
$WW ightarrow \ell u \ell u ightarrow {}^{b}$	$\leq m_W$ by Lemma 1	
$ZZ \rightarrow \nu \bar{\nu} \nu \bar{\nu}$	= 0 by Lemma 3	also = m_j for one ISR jet ^a
$LQ\overline{LQ} ightarrow q uar{q}ar{ u}$	$\leq m_{LQ}$)
$ ilde{q}ar{ ilde{q}} o q ilde{\chi}^0_1ar{q} ilde{\chi}^0_1$	$\leq m_{ ilde{q}}$	★ i.e. can take large values
$q_1, ar q_1 o q \gamma_1, ar q \gamma_1$	$\leq m_{q_1}$	·

Putting it to work for discovery







Health warning!

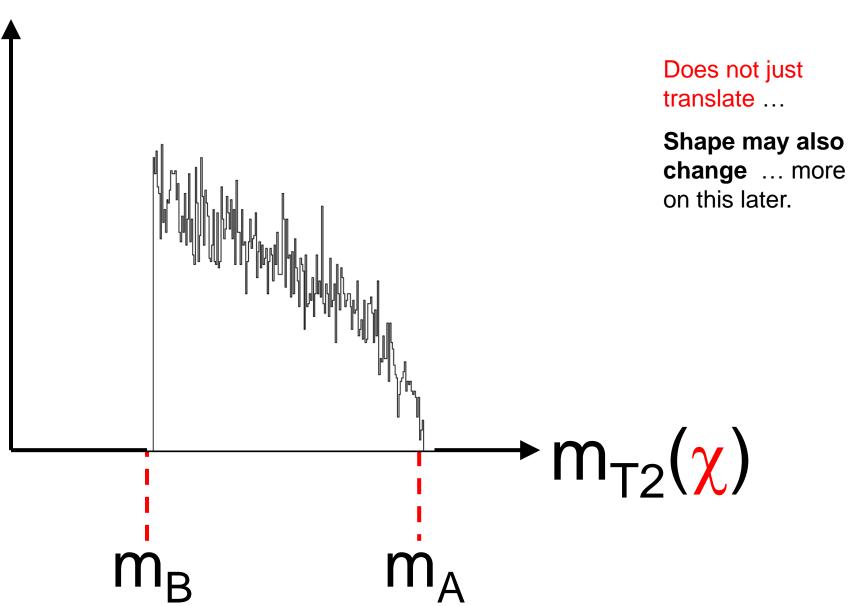


But note: high multiplicity environment already proving to be a challenge for mT2 (post 35/pb) and di-squark search in most recent data is being conducted with Meff. Problem is diagnosing the di-jet system.

Have dodged question of mass of invisible daughters.

What if we don't know their masses?

Varying " χ " ... to first order



MT2 inherits mass-space boundary from MT

KIA

The MT2(chi) curve is the **boundary** of the region of (mother, daughter) mass-space consistent with the observed event!

Minimal Kinematic Constraints and m(T2), Hsin-Chia Cheng and Zhenyu Han (UCD) e-Print: <u>arXiv:0810.5178 [hep-ph]</u>

 $\begin{array}{c} 2 \\ 0 \\ 5 \\ 8 \end{array}$

MT2 is defined in terms of MT

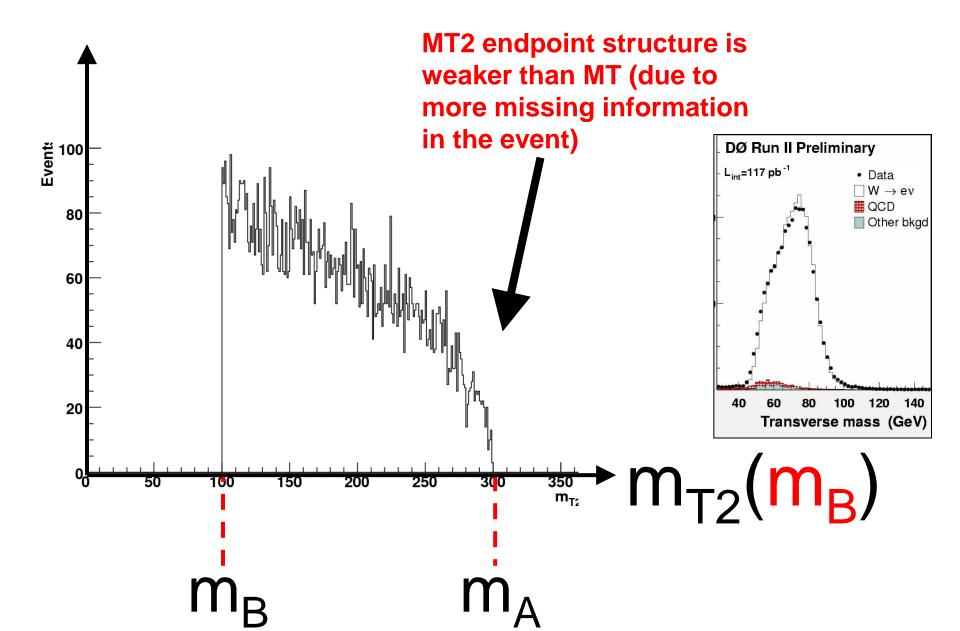
- Consequently, MT2 inherits the "kink structure" of MT and can (in principle) be used to:
 - EASILY measure the parent-daughter mass difference,
 - might PERHAPS measure the absolute mass scale using <u>utm boosts kinks</u> or <u>variable visible mass kinks</u> (HARD)

Are MT2 kinks observable ?

Expect KINK only from UTM Recoil (perhaps only from ISR!) Expect stronger KINK due to both UTM recoil, AND variability in the visible masses.

arXiv: 0711.4008

Perhaps: MT2's endpoint structure is weaker than MT's.





Caveat Mensor!

(for those of you interested in LHC dark matter constraints)

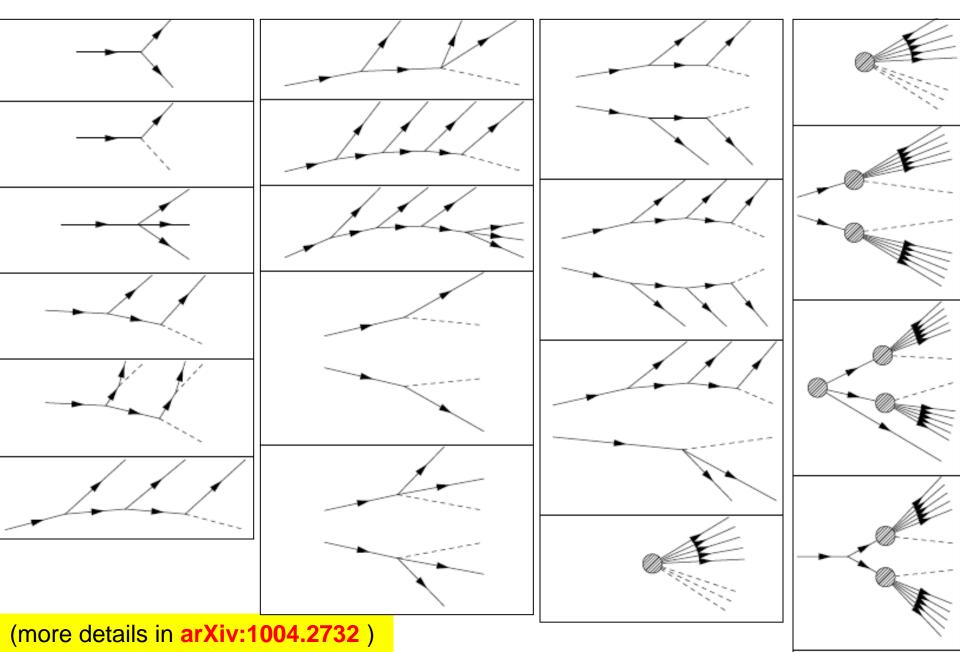


Disappointingly, M_{T2} kinks, are the only known kinematic methods which (at least in principle) allow determination of the mass of the invisible daughters of pair produced particles in short chains.

[We will see a dynamical method that works for three+ body decays shortly. Likelihood methods can determine masses in pair decays too, though at cost of model dependence and CPU. See Alwall.]

change of topic!

Not all proposed new-physics chains are short!



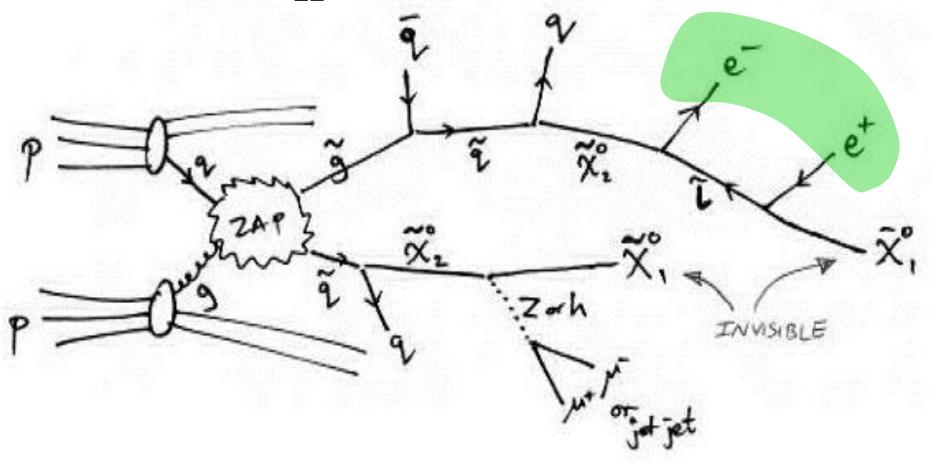
If chains a longer use "edges" or "Kinematic endpoints"

Plot distributions of the invariant masses of what you can see

INVISIBIE

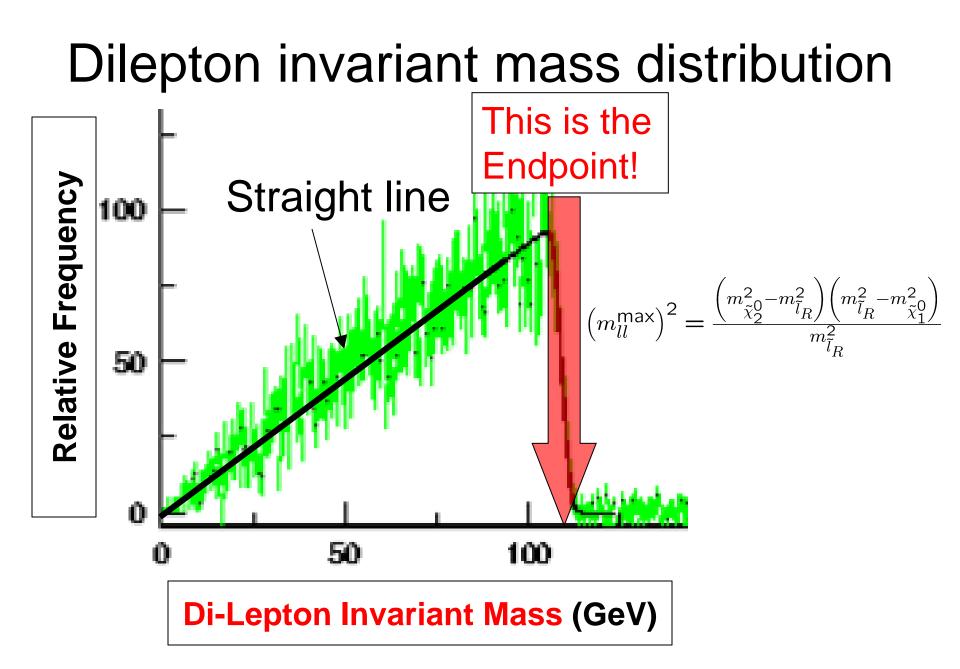
What is a kinematic endpoint?

Consider M_{LL}



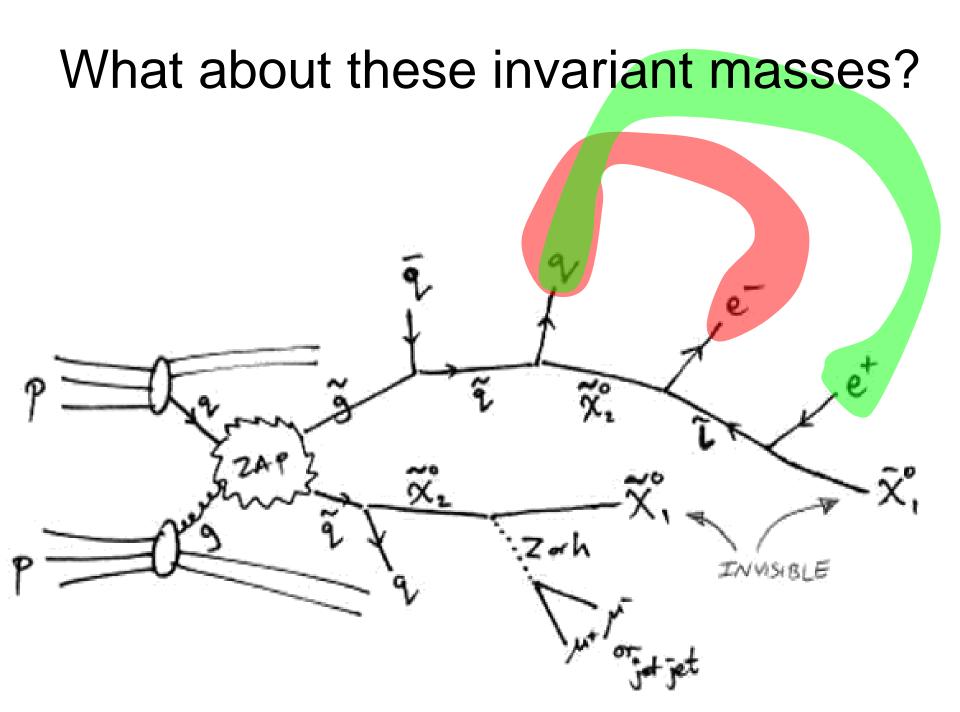
What is a kinematic endpoint?

 $l_{\rm near}^{\pm}$ $l_{\rm far}^{\mp}$ Zoom in on di-leptons to calculate m₁₁ \tilde{l}_R^{\mp} $ilde{\chi}_2^0$ $ilde{\chi}^0_1$ In slepton rest-frame θ Chi2 Slepton L+ $m_{ll}^2 = (m_{ll}^{\text{max}})^2 (1 - \cos \theta)/2$ Chi1

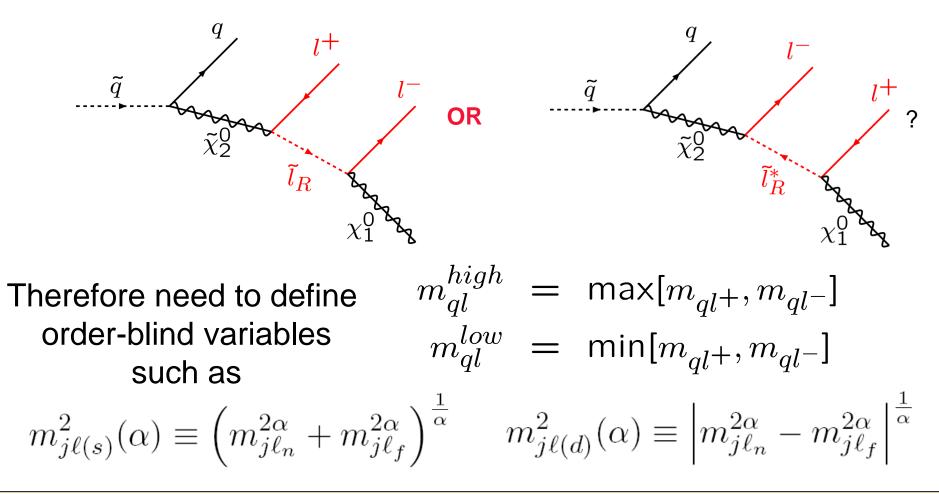


Note key difference to bounding vars

- With the bounding vars you place a bound on a property/parameter/invariant of the hypothesis or model by construction.
- With the kinematic edges and enpoints, you look for a kinematic strucure in a distribution, and use it to constrain one or more parameters of the hypothesis or model.

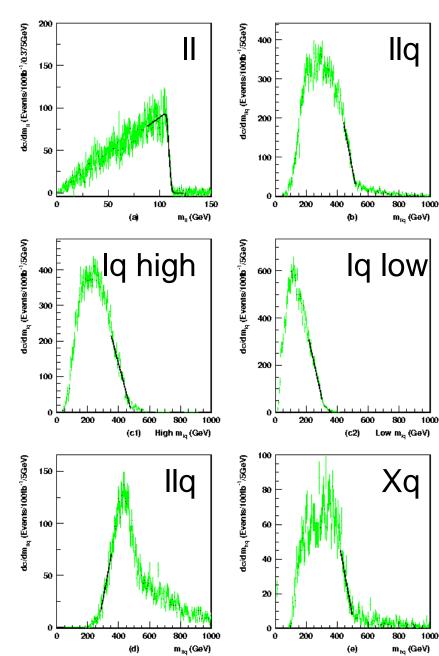


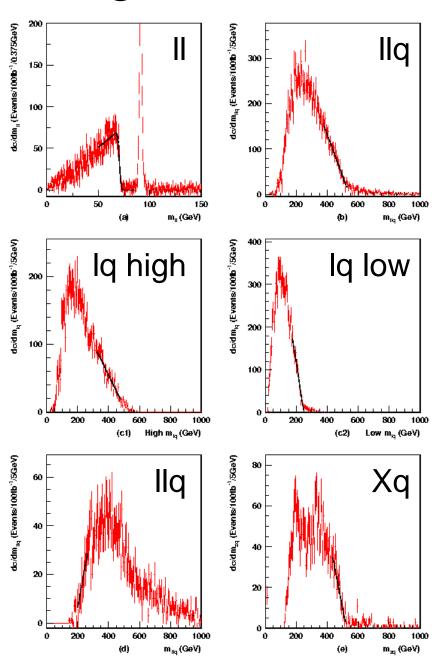
Some extra difficulties – may not know order particles were emitted



There are many other possibilities for resolving problems due to position ambiguity. Compare hep-ph/0007009 and hep-ph/0510356 with arXiv:0906.2417

Measure Kinematic Edge Positions





		Related edge	Kinematic endpoint		
epend on	masses	l^+l^- edge	$(m_{ll}^{ ext{max}})^2 = (ilde{\xi} - ilde{l})(ilde{l} - ilde{\chi})/ ilde{l}$		
		l^+l^-q edge	$(m_{\tilde{l}lq}^{\max})^2 = egin{cases} \max\left[rac{(ilde{q}- ilde{\xi})(ilde{\xi}- ilde{\chi})}{ ilde{\xi}}, rac{(ilde{q}- ilde{l})(ilde{l}- ilde{\chi})}{ ilde{l}}, rac{(ilde{q} ilde{l}- ilde{\xi} ilde{\chi})(ilde{\xi}- ilde{l})}{ ilde{\xi}^2} ight] \\ ext{except for the special case in which } ilde{l}^2 < ilde{q} ilde{\chi} < \\ ilde{\xi}^2 ilde{\chi} < ilde{q} ilde{l}^2 \text{ where one must use } (m_{ ilde{q}} - m_{ ilde{\chi}_1^0})^2. \end{cases}$	$\langle { ilde \xi}^2 $ อเ	nd
		Xq edge	$(m_{Xq}^{\max})^2 = X + (ilde{q} - ilde{\xi}) \left[ilde{\xi} + X - ilde{\chi} + \sqrt{(ilde{\xi} - X - ilde{\chi})^2 - 4X} ight]$	$\left[\tilde{\chi}\right]/(2$	$2 ilde{\xi})$
		l^+l^-q threshold	$(m_{llq}^{\min})^2 = \begin{cases} [2\tilde{l}(\tilde{q} - \tilde{\xi})(\tilde{\xi} - \tilde{\chi}) + (\tilde{q} + \tilde{\xi})(\tilde{\xi} - \tilde{l})(\tilde{l} - \tilde{\chi}) \\ -(\tilde{q} - \tilde{\xi})\sqrt{(\tilde{\xi} + \tilde{l})^2(\tilde{l} + \tilde{\chi})^2 - 16\tilde{\xi}\tilde{l}^2\tilde{\chi}} \end{bmatrix} / (4\tilde{l}\tilde{\xi})$		updated version at <u>arXiv:1004.2732</u>
σ	Φ	$l^{\pm}_{\mathrm{near}}q~\mathrm{edge}$	$(m^{ ext{max}}_{l_{ ext{near}}q})^2 = (ilde{q} - ilde{\xi})(ilde{\xi} - ilde{l})/ ilde{\xi}$	6	Xiv:10
SC	rticl	$l^\pm_{{f far}} q { m edge}$	$(m^{ ext{max}}_{l_{ ext{far}}q})^2 = (ilde{q} - ilde{\xi})(ilde{l} - ilde{\chi})/ ilde{l}$	0070	at <u>ar)</u>
Ō	art	$l^{\pm}q$ high-edge	$(m_{lq(\mathrm{high})}^{\mathrm{max}})^2 = \max\left[(m_{l_{\mathrm{near}q}}^{\mathrm{max}})^2, (m_{l_{\mathrm{far}q}}^{\mathrm{max}})^2 ight]$	hep-ph/0007009	ersion
Sit	spa	$l^{\pm}q$ low-edge	$(m^{\max}_{lq(\mathrm{low})})^2 = \min\left[(m^{\max}_{l_{\mathrm{near}}q})^2, (ilde{q} - ilde{\xi})(ilde{l} - ilde{\chi})/(2 ilde{l} - ilde{\chi}) ight]$	lq-qe	ated ve
oositions	S	$M_{T2} \mathrm{edge}$	$\Delta M = m_{ ilde{l}} - m_{ ilde{\chi}_1^0}$	ž	pdn
			l		

Determine how edge

Table 4: The absolute kinematic endpoints of invariant mass quantities formed from decay chains of the types mentioned in the text for known particle masses. The following shorthand notation has been used: $\tilde{\chi} = m_{\tilde{\chi}_1^0}^2$, $\tilde{l} = m_{\tilde{\chi}_2^0}^2$, $\tilde{\xi} = m_{\tilde{\chi}_2^0}^2$, $\tilde{q} = m_{\tilde{q}}^2$ and X is m_h^2 or m_Z^2 depending on which particle participates in the "branched" decay.

So now we have:

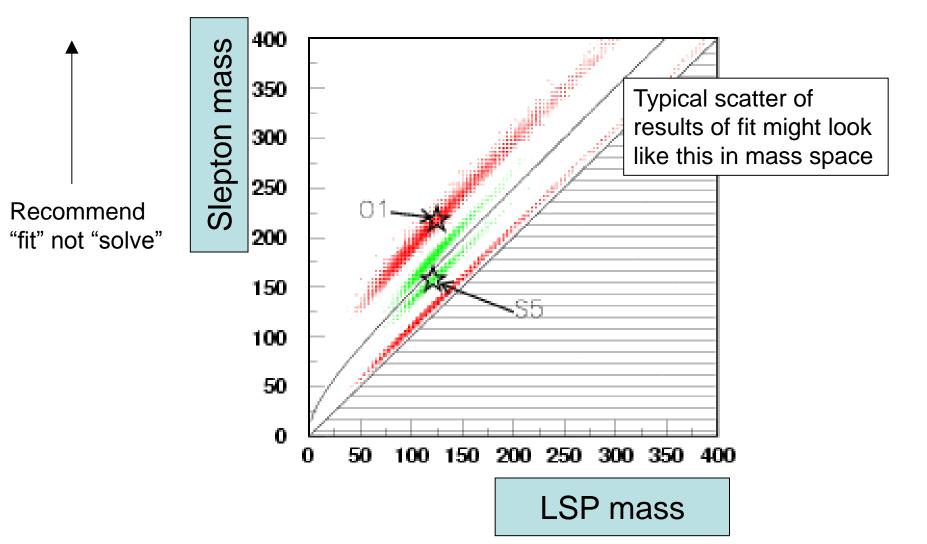
Large set of	f measurements
--------------	----------------

S5	
Fit	Fit error
109.10	0.13
532.1	3.2
483.5	1.8
321.5	2.3
266.0	6.4
514.1	6.6
	Fit 109.10 532.1 483.5 321.5 266.0

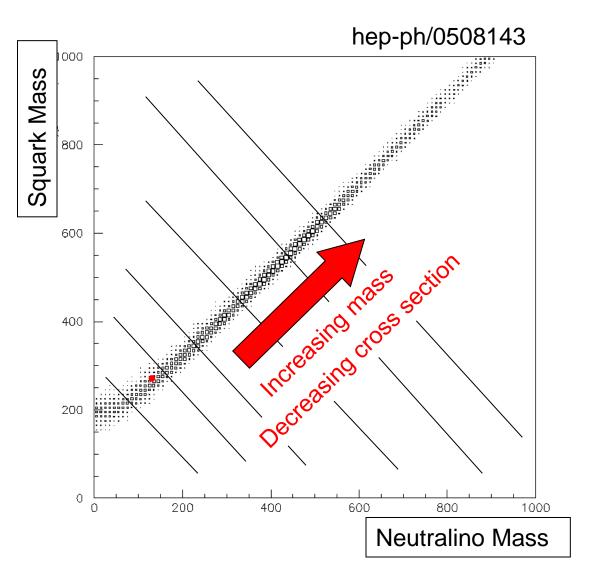
Theoretical expressions for edge positions in terms of masses

Related edge	Kinematic endpoint		
l^+l^- edge	$(m_{ll}^{\max})^2 = (ilde{\xi} - ilde{l})(ilde{l} - ilde{\chi})/ ilde{l}$		
l^+l^-q edge	$(m_{llq}^{\max})^2 = \begin{cases} \max\left[\frac{(\bar{q}-\bar{\xi})(\bar{\xi}-\bar{\chi})}{\bar{\xi}}, \frac{(\bar{q}-\bar{l})(\bar{l}-\bar{\chi})}{\bar{\ell}}, \frac{(\bar{q}\bar{l}-\bar{\xi}\bar{\chi})(\bar{\xi}-\bar{l})}{\bar{\xi}\bar{l}}\right] \\ \text{except for the special case in which } \tilde{l}^2 < \bar{q}\bar{\chi} < \bar{\xi}^2 \text{ and} \\ \bar{\xi}^2\bar{\chi} < \bar{q}\tilde{l}^2 \text{ where one must use } (m_{\bar{q}} - m_{\bar{\chi}_1^0})^2. \end{cases}$		
Xq edge	$(m_{Xq}^{\max})^2 = X + (\tilde{q} - \tilde{\xi}) \left[\tilde{\xi} + X - \tilde{\chi} + \sqrt{(\tilde{\xi} - X - \tilde{\chi})^2 - 4X\tilde{\chi}} \right] / (2\tilde{\xi})$		
l^+l^-q threshold	$(m_{llq}^{\min})^2 = \begin{cases} [2\tilde{l}(\tilde{q} - \tilde{\xi})(\tilde{\xi} - \tilde{\chi}) + (\tilde{q} + \tilde{\xi})(\tilde{\xi} - \tilde{l})(\tilde{l} - \tilde{\chi}) \\ -(\tilde{q} - \tilde{\xi})\sqrt{(\tilde{\xi} + \tilde{l})^2(\tilde{l} + \tilde{\chi})^2 - 16\tilde{\xi}\tilde{l}^2\tilde{\chi}} \end{bmatrix} / (4\tilde{l}\tilde{\xi}) \end{cases}$		
$l^{\pm}_{\mathrm{near}}q$ edge	$(m^{ m max}_{l_{ness}q})^2 = (ilde{q} - ilde{\xi})(ilde{\xi} - ilde{l})/ ilde{\xi}$		
$l_{\mathbf{far}}^{\pm}q$ edge	$(m^{\max}_{l_{tax}q})^2 = (ilde q - ilde \xi) (ilde l - ilde \chi) / ilde l$		
$l^{\pm}q$ high-edge	$(m_{l_q(\mathrm{high})}^{\mathrm{max}})^2 = \max\left[(m_{l_{nearq}}^{\mathrm{max}})^2,(m_{l_{txr}q}^{\mathrm{max}})^2 ight]$		
$l^\pm q$ low-edge	$(m^{ ext{max}}_{liq(ext{low})})^2 = \min\left[(m^{ ext{max}}_{ligenref})^2, (ilde{q} - ilde{\xi})(ilde{l} - ilde{\chi})/(2 ilde{l} - ilde{\chi}) ight]$		
M_{T2} edge	$\Delta M = m_{ ilde{l}} - m_{ ilde{\chi}_1^0}$		

Fit all edge position for masses! ...mainly constrain mass differences

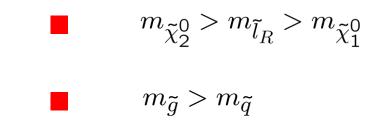


Cross section information is orthogonal to mass differences



How applicable are these long chain techniques ?

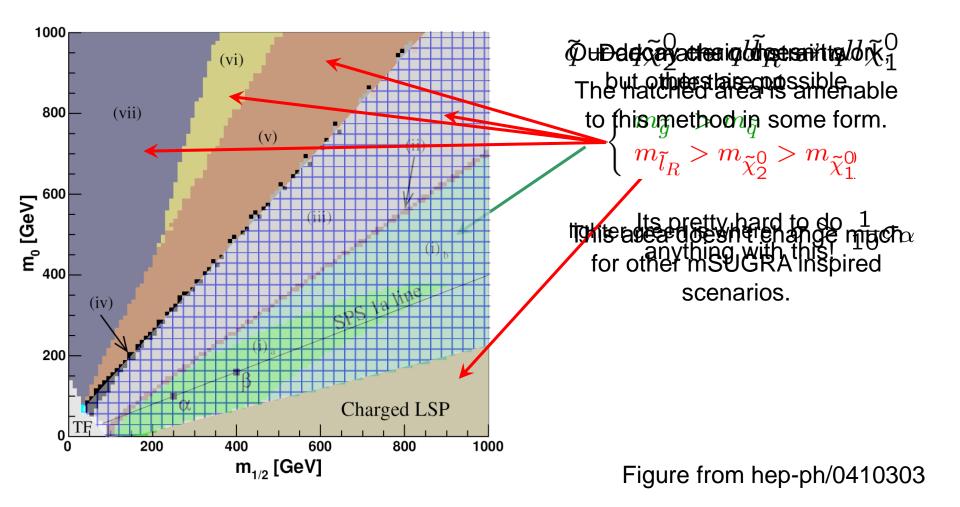
For the chain $\tilde{q} \rightarrow q \tilde{\chi}_2^0 \rightarrow q l \tilde{l}_R \rightarrow q l l \tilde{\chi}_1^0$ we need:

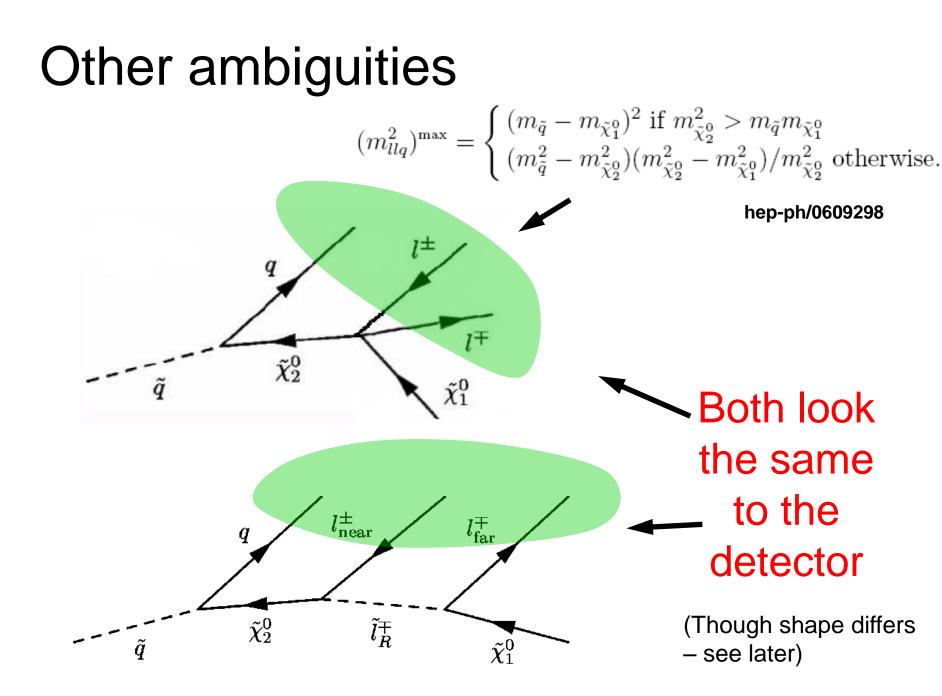


This is possible over a wide range of parameter space.

If this chain is not open, the method is still valid, but we need to look at other decay chains. Example mSUGRA inspired scenario: $-A_0 = m_0$, $\tan \beta = 10$, $\mu > 0$

[See Allanach et al, Eur.Phys.J.C25 (2002) 113, hep-ph/0202233]





Endpoints are not always linearly independent

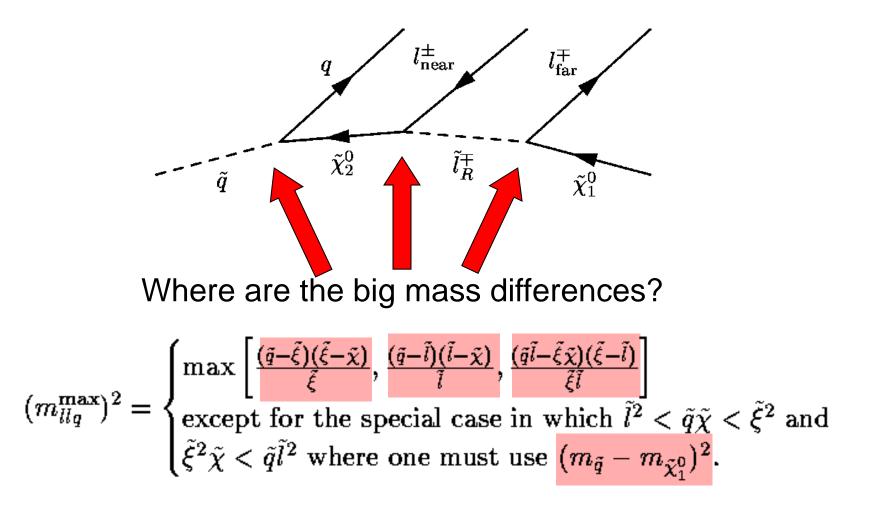
e.g. if
$$m_{\tilde{q}_L} > m_{\tilde{\chi}_2^0}^2 / m_{\tilde{\chi}_1^0}$$
 and $m_{\tilde{\chi}_1^0}^2 + m_{\tilde{\chi}_2^0}^2 > 2m_{\tilde{\chi}_1^0} m_{\tilde{\chi}_2^0} > 2m_{\tilde{q}_L}^2$

then the endpoints are

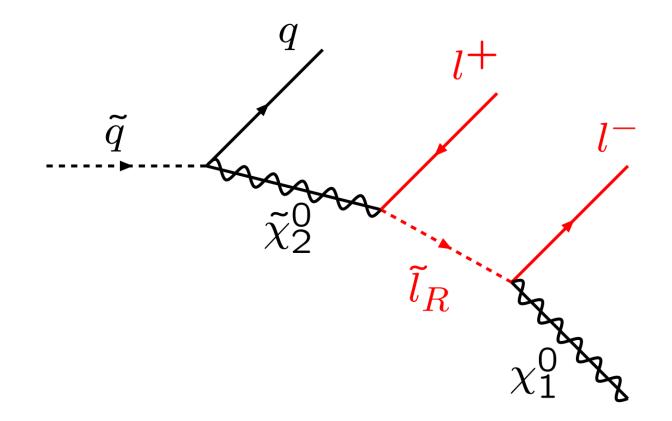
$$\begin{pmatrix} m_{ll}^{\max} \end{pmatrix}^2 = (m_{\tilde{\chi}_2}^2 - m_{\tilde{l}_R}^2)(m_{\tilde{l}_R}^2 - m_{\tilde{\chi}_1}^2)/m_{\tilde{l}_R}^2 \\ (m_{qll}^{\max})^2 = (m_{\tilde{q}_L}^2 - m_{\tilde{l}_R}^2)(m_{\tilde{l}_R}^2 - m_{\tilde{\chi}_1}^2)/m_{\tilde{l}_R}^2 \\ (m_{ql_n}^{\max})^2 = (m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2}^2)(m_{\tilde{\chi}_2}^2 - m_{\tilde{l}_R}^2)/m_{\tilde{\chi}_2}^2 \\ (m_{ql_f}^{\max})^2 = (m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2}^2)(m_{\tilde{l}_R}^2 - m_{\tilde{\chi}_1}^2)/m_{\tilde{l}_R}^2 \\ \Rightarrow (m_{qll}^{\max})^2 = (m_{ll}^{\max})^2 + (m_{ql_f}^{\max})^2$$
Four endpoints not always sufficient to find the masses
Introduce new distribution $m_{qll\,\theta>\pi/2}$ identical to m_{qll} except require $\theta>\pi/2$
It is the minimum of this distribution which is interesting

Slide from David Miller

Different parts of model space behave differently: m_{QLL}^{max}



Which parts of (m²_{qlnear},m²_{qlfar},m²_{II})-space are populated by these events:



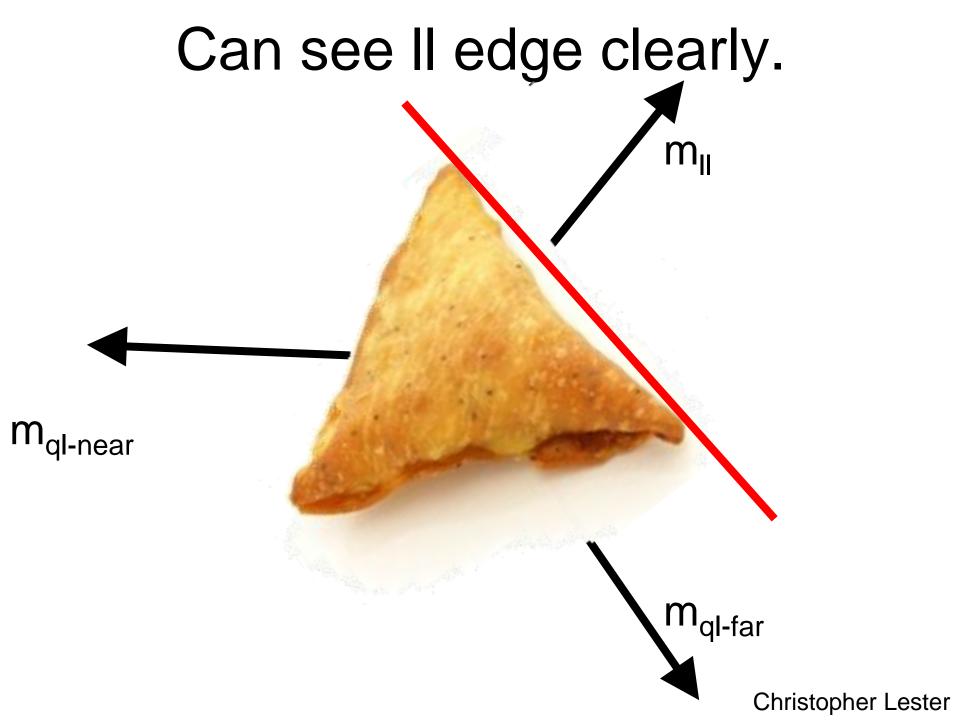


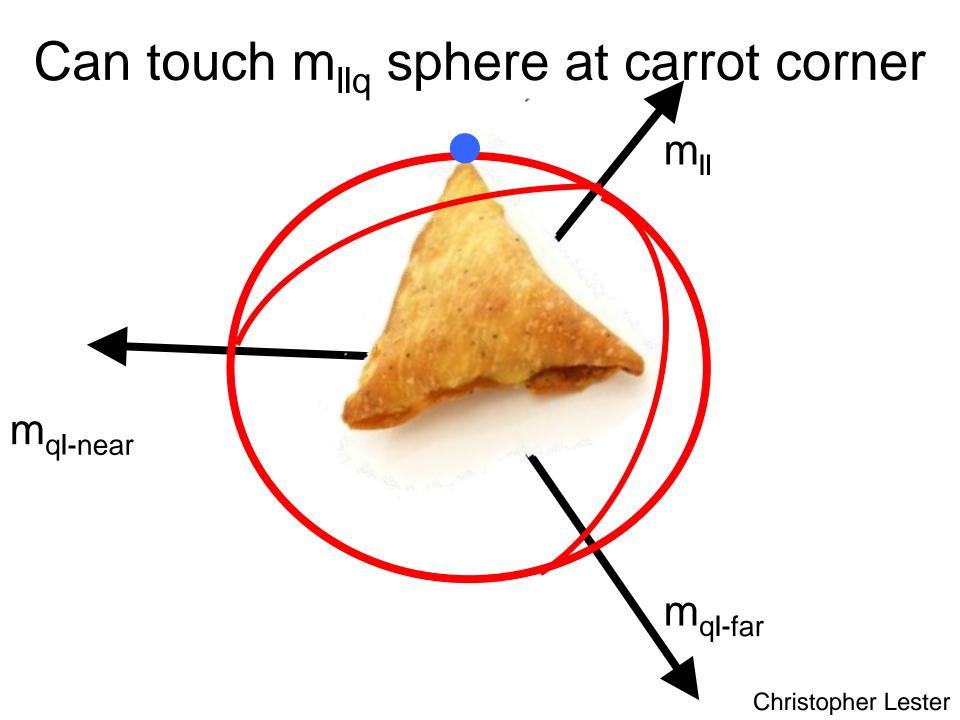
Answer: The Vegetable Samosa

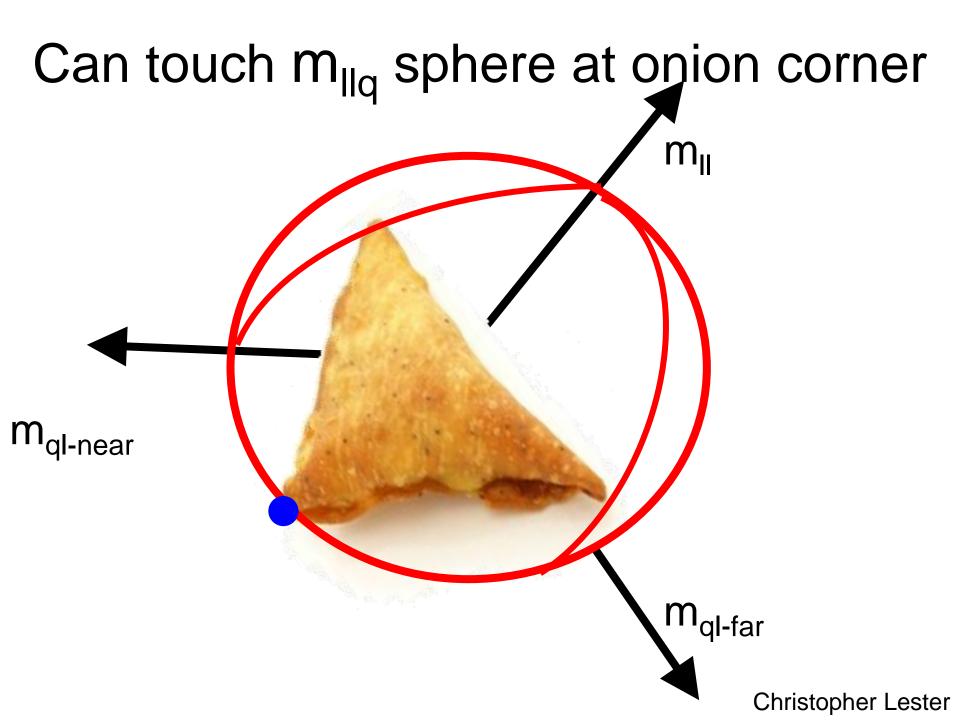
m_{ql-near}

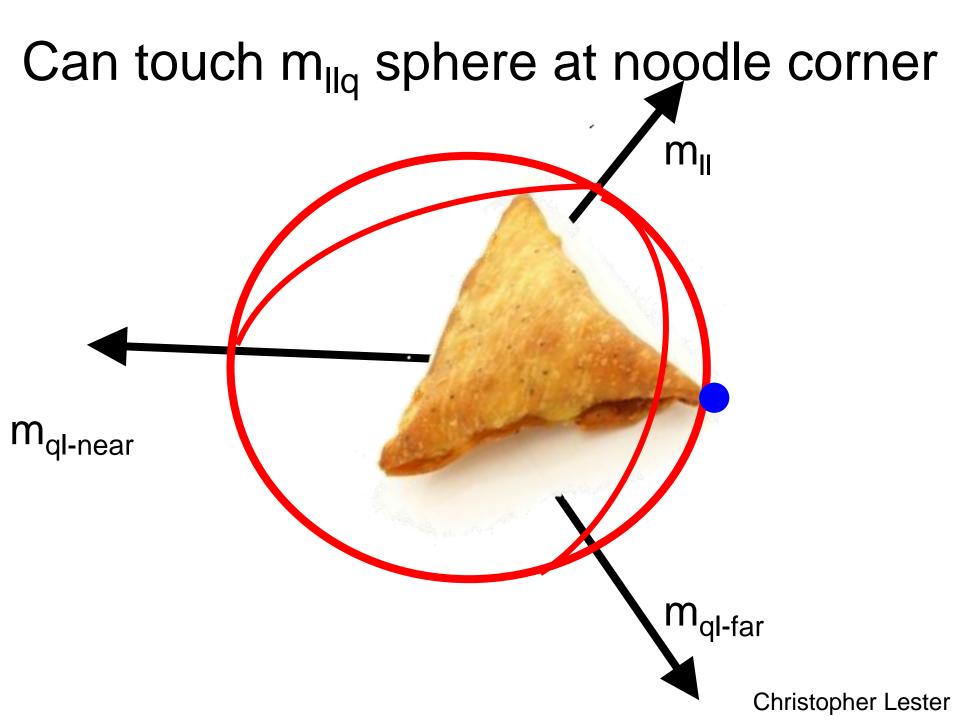


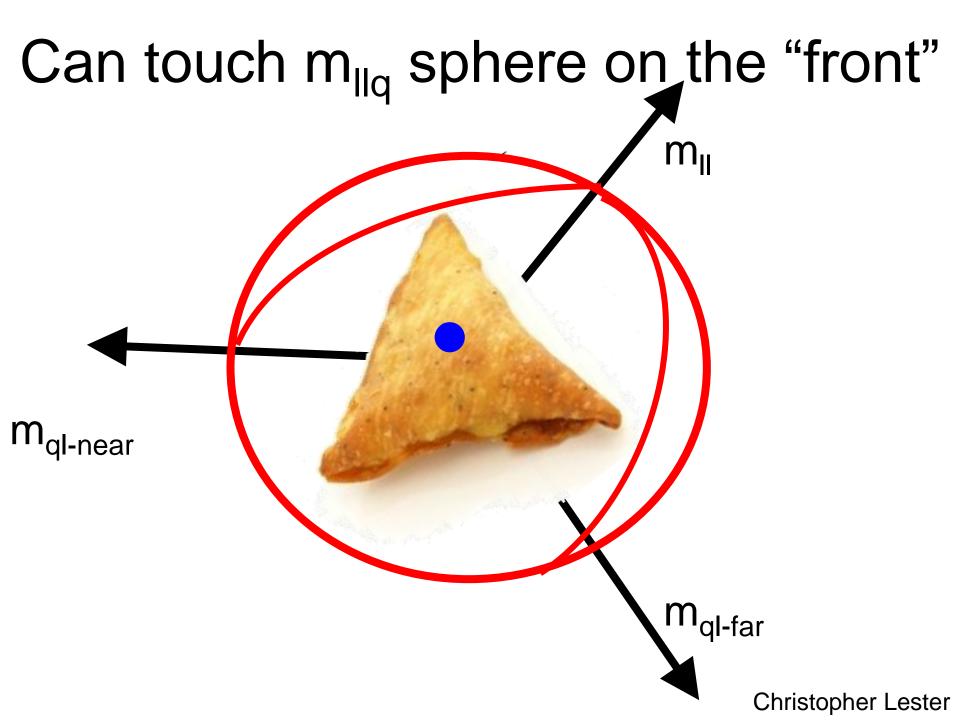
m_{ql-far}

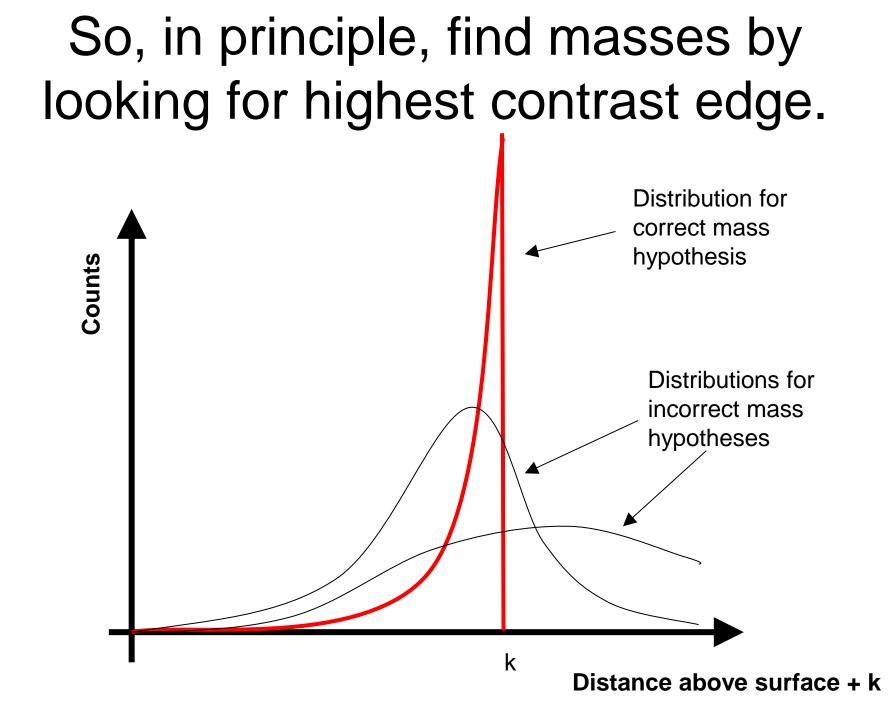












The "shadow" (projection) of the samosa is useful for origami too

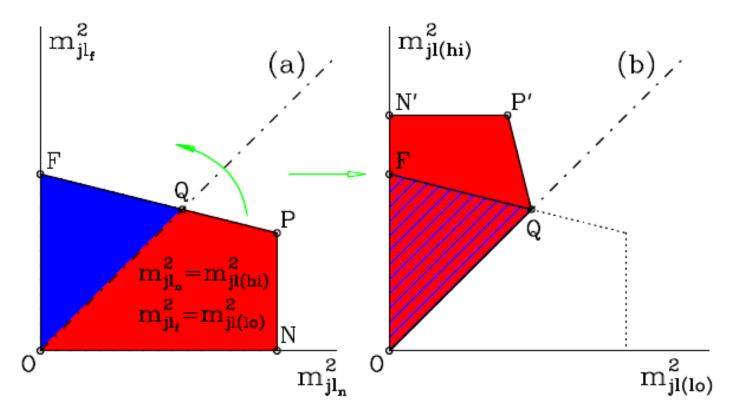
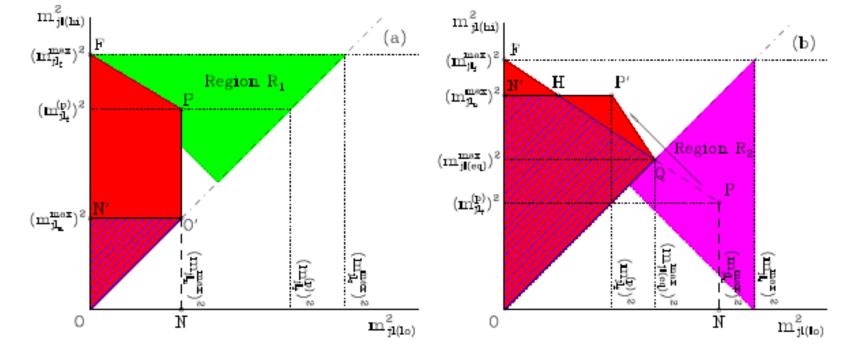
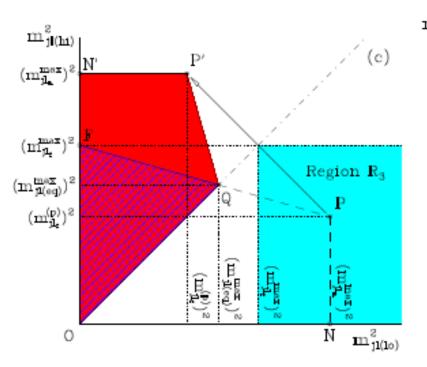
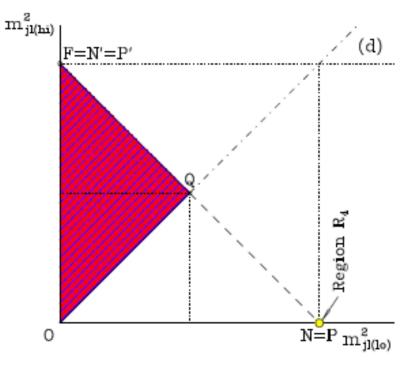


Figure 7: Obtaining the shape of the $m_{jl(lo)}^2$ versus $m_{jl(hi)}^2$ bivariate distribution by folding the $m_{jl_n}^2$ versus $m_{jl_f}^2$ distribution across the line $m_{jl_n}^2 = m_{jl_f}^2$. This particular example applies to region \mathcal{R}_3 . For the other three regions, refer to Figs. 8(a), 8(b) and 8(d).

arXiv:0903.4371







arXiv:0903.4371

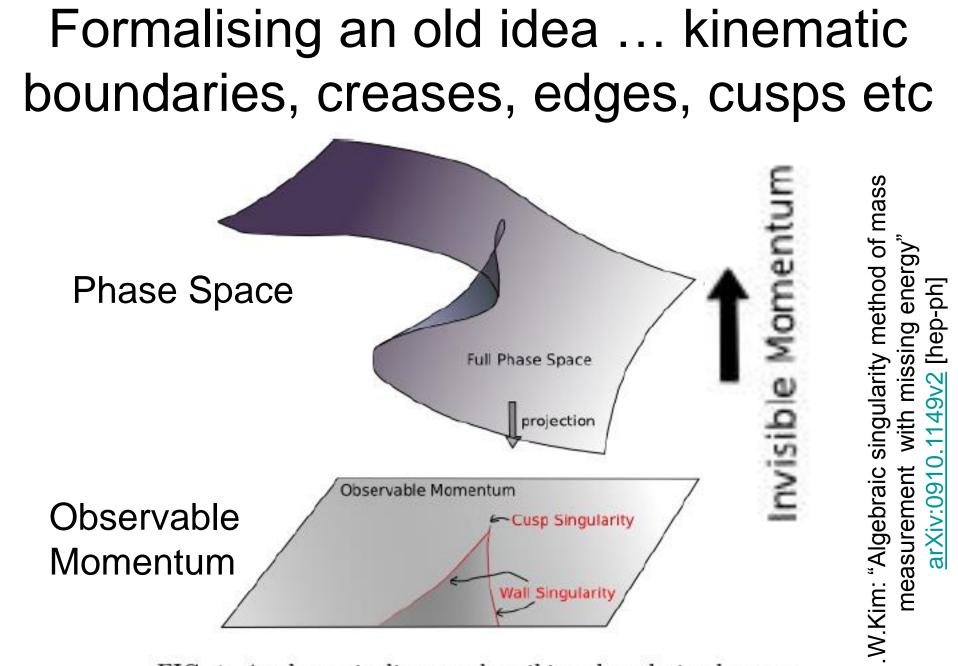
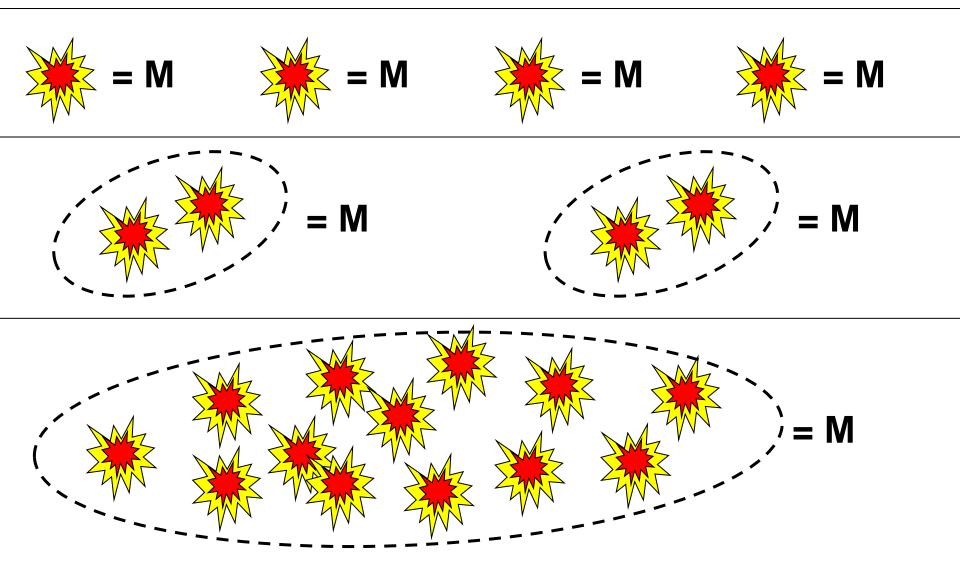


FIG. 1: A schematic diagram describing the relation between the full phase space and the projected observable phase space.

Adding even more assumptions ...

Let's consider what happens when we allow ourselves to look at more than one event



See sections X and IX of hep-ph/0402295

• In D space-time dimensions

- D+(N+1) unknowns: comprising
 - D unknown momentum-components for final "missing particle"

N successive 2-body decays

- (N+1) unknown backbone-particle masses
- N+1 constraints:
 - Invariant masses of the backbone-<u>momenta</u> must match the "unknown" masses
- UNKNOWNS CONSTRAINTS = D > 0

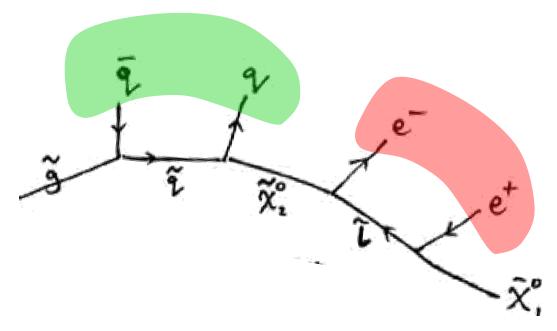
− Cannot solve for unknowns! ⊗

Why not look at K events?

- K events, each (N successive 2-body decays)
- KD+(N+1) unknowns: comprising
 - KD unknown momentum-components for final "missing particle"
 - (N+1) unknown backbone-particle masses
- K(N+1) constraints:
 - Invariant masses of the backbone-<u>momenta</u> must match the "unknown" masses
- UNKNOWNS CONSTRAINTS = K(D (N + 1)) + (N + 1)
- System solvable for $K \geq \frac{N+1}{N+1-D}$ provided $_{N+1 > D \text{ i.e. } N \geq 4.}$

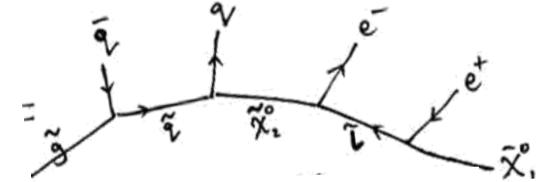
Ambiguities

- Which jet is which?
- Which lepton is which?



 So will need more events than the last calculation suggests ~ x4 ?

"Mass relation" method: summary



- Can:
 - reconstruct complete decay kinematics
 - Measure all sparticle masses
- provided that:
 - Chain has $N \ge 4$ successive two-body decays
 - One simultaneously examines at least

$$\frac{N+1}{N+1-D} = \frac{N+1}{N-3}$$

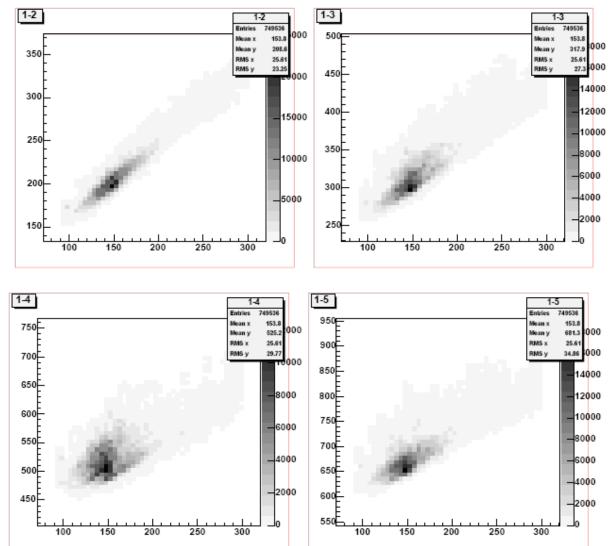
$$N+1-D$$
 $N-3$

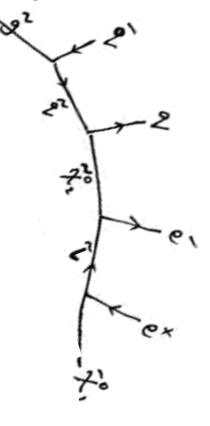
events sharing the same sparticles.

See sections X and IX of hep-ph/0402295

Some example reconstructed masses

(100 events, toy MC)





Caveats:

Though see Miller hep-ph/0501033

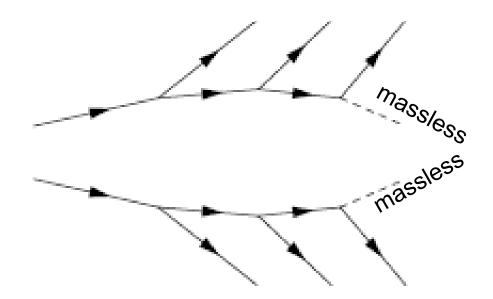
Nobody has shown that this will work for real data. Sample purity. Bias. Heavily model dependent?

Dependence on reconstruction resolution.

- N=4 two-body decays
- Fewer than 5 events
 Under constrained, cannot solve
- 5 events
 - Can solve in principle (ignoring ambiguities)
 - Can treat events as "ideal"
- More than 5 events
 - Over constrained. Potential for inconsistency.
 - Reconstructed events will not "make sense" until resolutions are taken into account.

Another sort of "just"-constrained event

- get constraint from other "side"

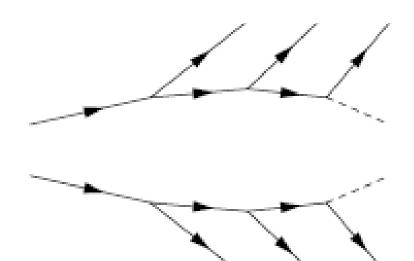


Left: case considered in hep-ph/9812233

- Even if there are invisible decay products, events can often be fully reconstructed if decay chains are long enough.
- (mass-shell constraints must be >= unknown momenta)
- Since we can use ptmiss constraint, chains can be shorter than N=4 now.

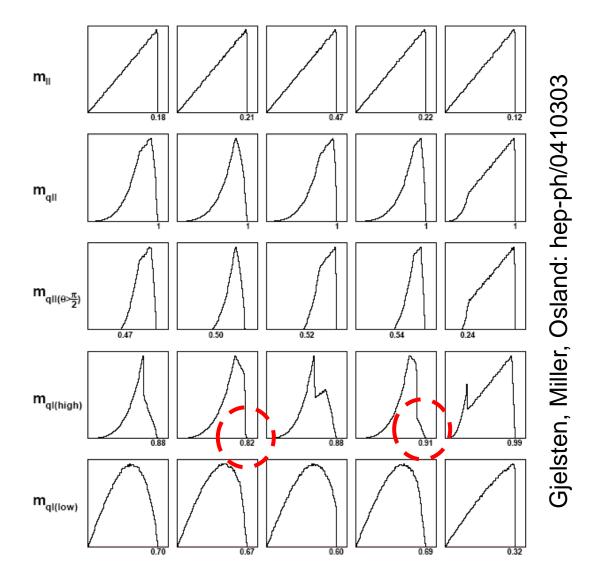
Or do both at once – pairs of double events!

 Pairs of events of the form:

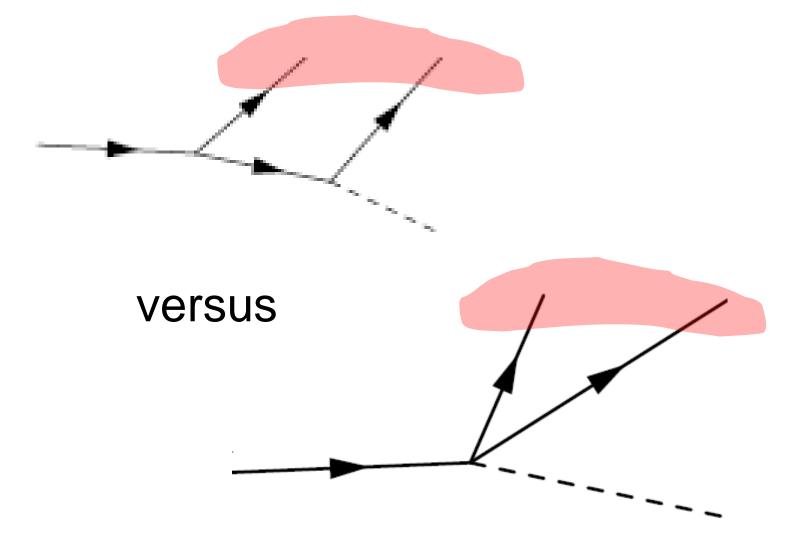


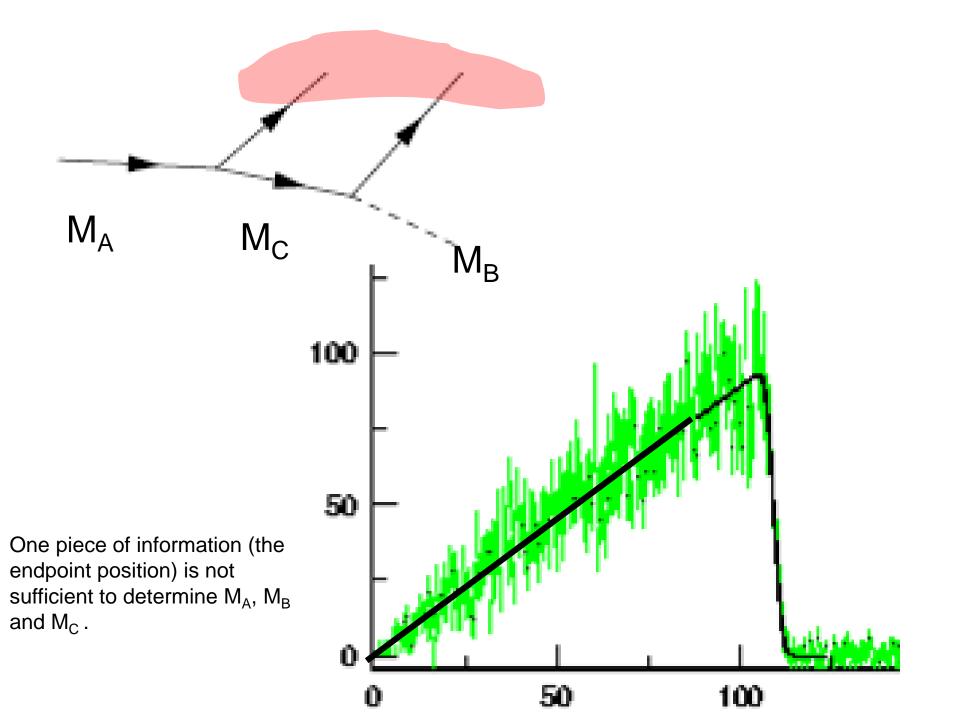
are exactly constrained. (arXiv:0905.1344)

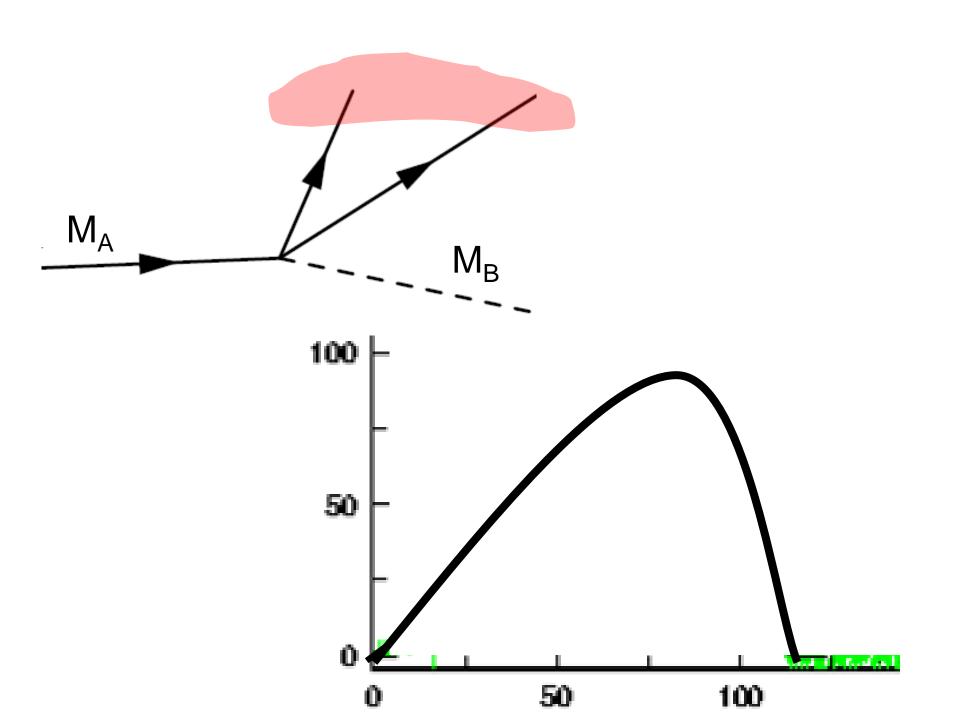
What about shapes of distributions?

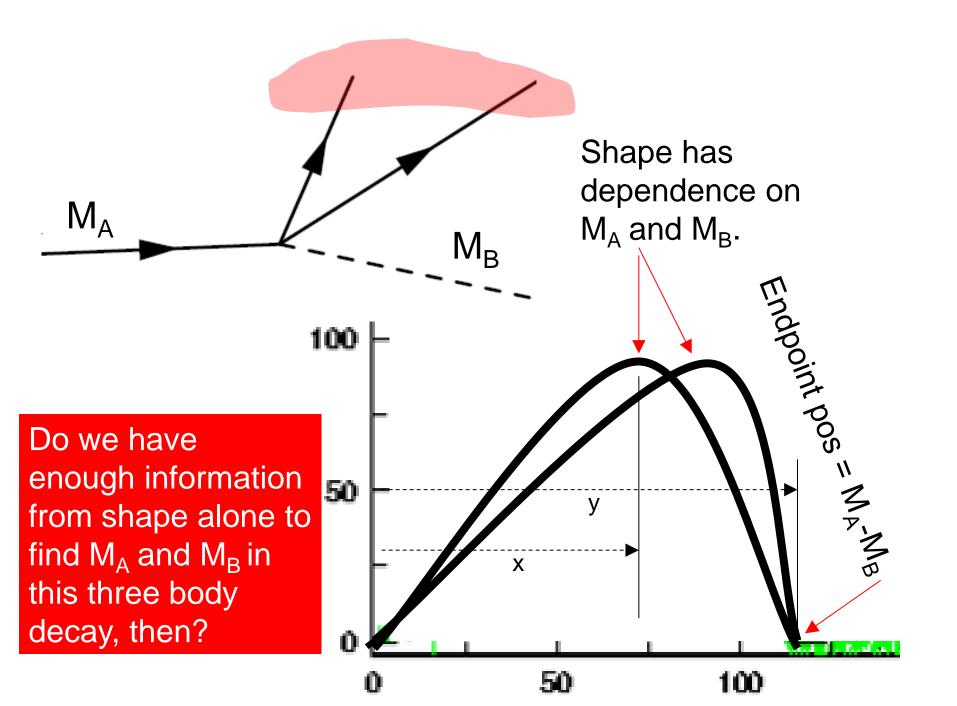


Compare shapes of invariant mass distributions for the highlighted pairs of visible massless momenta:







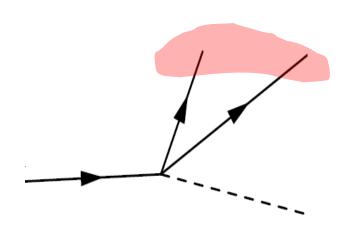


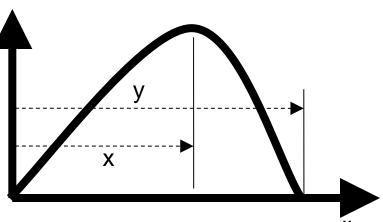
Yes and no ..

- Putting aside experimental fears concerning efficiency and acceptance corrections ...
- ... huge errors in the fit, and very poor sensitivity to absolute mass scale. See next exercises.
- This is why endpoints, edges and resonances are good, but shapes less so

Exercises

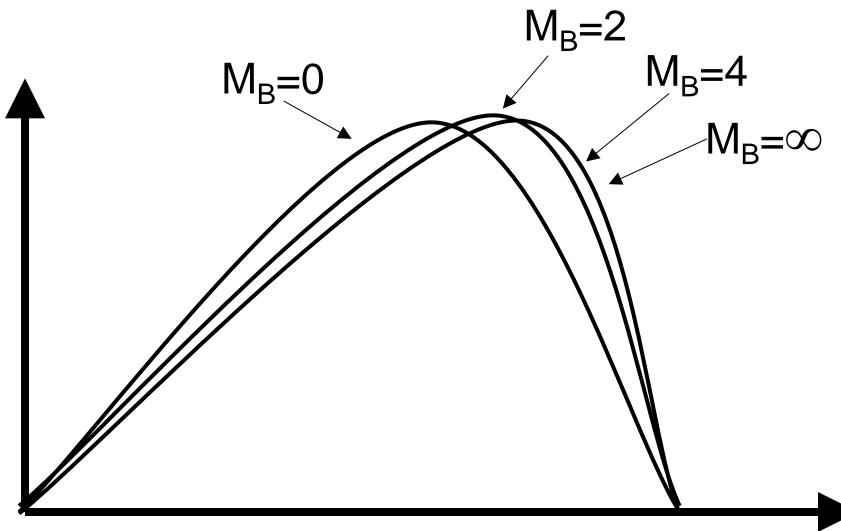
- (12) Determine the shape of the phase space distribution dσ/d(mll) (up to an arbitrary normalizing constant) for the three-body decay shown below. Assume massless visibles, and arbitrary masses for the parent and invisible.
- (13) Prove that r=x/y must lie in the range 1/√3 ≤ r ≤ 1/√2. (Note this means r can only move by ±0.06 ... not far!)
- (14) Estimate how many events (approximately) would be needed to distinguish two r values differing by 0.012 (i.e. ~1/10th of allowed range)





m

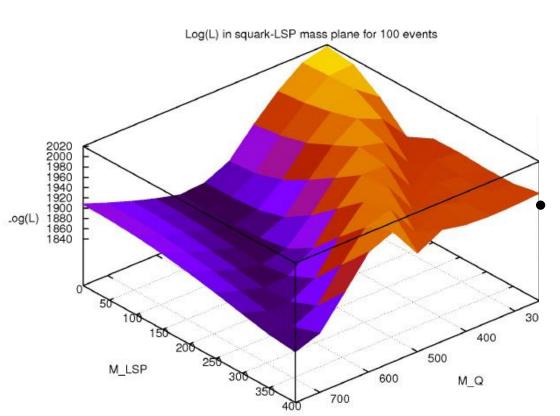
At fixed M_A - M_B you should find

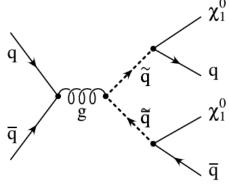




The most detailed "shape" of all is the complete likelihood of the data

 Alwall et.al. (arXiv:0910.2522, arXiv:1010.2263) applied matrix element method to:

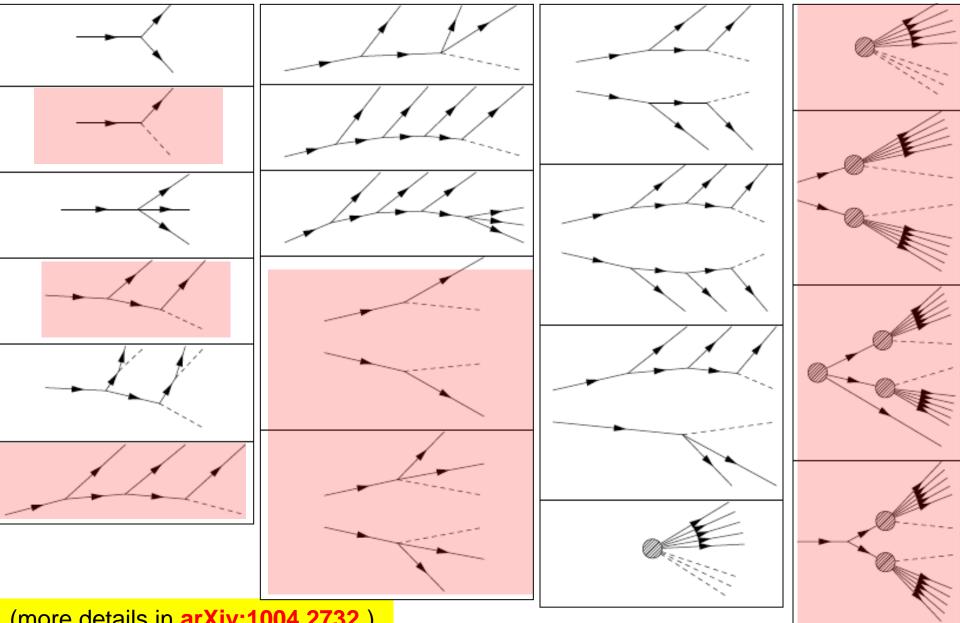




For ~ 100 events get valley in likelihood surface with same shape as boundary of MT2 distribution

That's probably enough on mass measurement techniques!

Have only begun to scrape the surface.



(more details in arXiv:1004.2732)

Not time to talk about many things

- Parallel and perpendicular MT2 and MCT
- Subsystem MT2 and MCT methods
- Solution counting methods (eg arXiv:0707.0030)
- Hybrid Variables
- Phase space boundaries (arXiv:0903.4371)
- Cusps and Singularity Variables (Ian-Woo Kim)
- Why wrong solutions are often near right ones (arXiv:1103.3438)
- Razors
- and many more!

I have only scratched the surface of the variables that have been discussed. Even the review of mass measurement methods arXiv:1004.2732 makes only a small dent in 70+ pages. However it provides at least an index ...

Take home messages

- Lots of approaches to kinematic mass measurement
 - some very general, some very specific.
 - very little of the "detailed stuff" is tested in anger.
 Experimentalists not universally convinced of utility!
 - very often BGs present serious impediment.
 - theorists and experimenters should pay close attention to zone of applicability
- BUT
 - Finding sensible variables buys more than just mass measurements - e.g. signal sensitivity

Extras if time ...

Notes:

- At TASI 2010: 75 mins per lecture:
- Lec1: 1-73 (73 slides)
- Lec2: 74-183 (110 slides)
- Lec3: 184-224 (41 slides) on masses

- then segue into spins for another 40

Other MT2 related variables (1/3)

- MCT ("Contralinear-Transverse Mass") (arXiv:0802.2879)
 - Is equivalent to MT2 in the special case that there is no missing momentum (and that the visible particles are massless).
 - Proposes an interesting multi-stage method for measuring additional masses
 - Can be calculated fast enough to use in ATLAS trigger.

Other MT2 related variables (2/3)

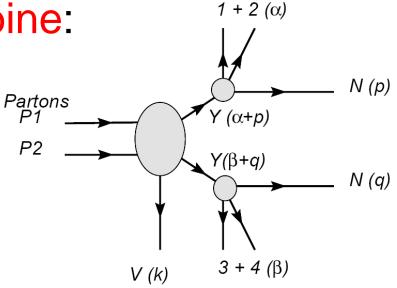
- MTGEN ("MT for GENeral number of final state particles") (arXiv:0708.1028)
 - Used when
 - each "side" of the event decays to MANY visible particles (and one invisible particle) and
 - it is not possible to determine which decay product is from which side ... all possibilities are tried
- Inclusive or Hemispheric MT2 (Nojirir + Shimizu) (arXiv:0802.2412)
 - Similar to MTGEN but based on an assignment of decay product to sides via hemisphere algorithm.
 - Guaranteed to be >= MTGEN

Other MT2 related variables (3/3)

- M2C ("MT2 Constrained") arXiv:0712.0943 (wait for v3 ... there are some problems with the v1 and v2 drafts)
- M2CUB ("MT2 Constrained Upper Bound") arXiv:0806.3224
- There is a sense in which these two variables are really two sides of the same coin.
 - if we could re-write history we might name them more symmetrically
 - I will call them m_{Small} and m_{Big} in this talk.

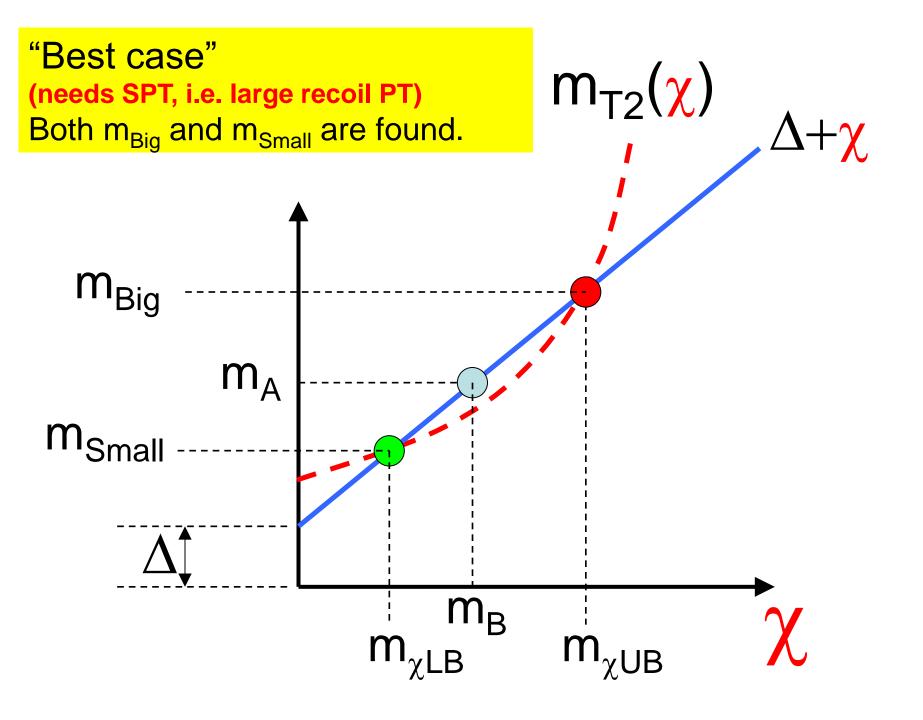
m_{Small} and m_{Big}

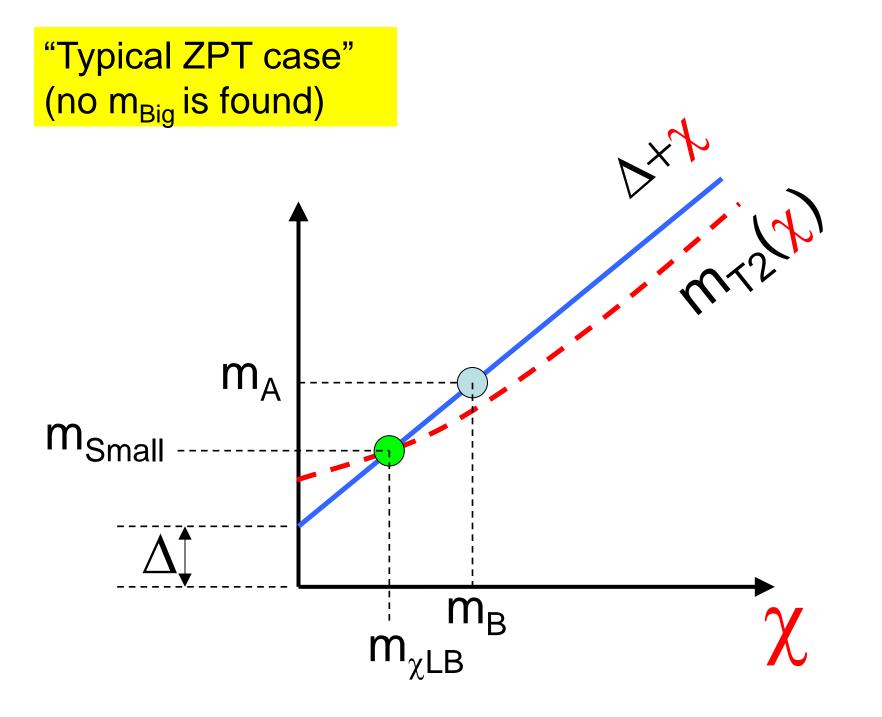
- Basic idea is to combine:
 - -MT2

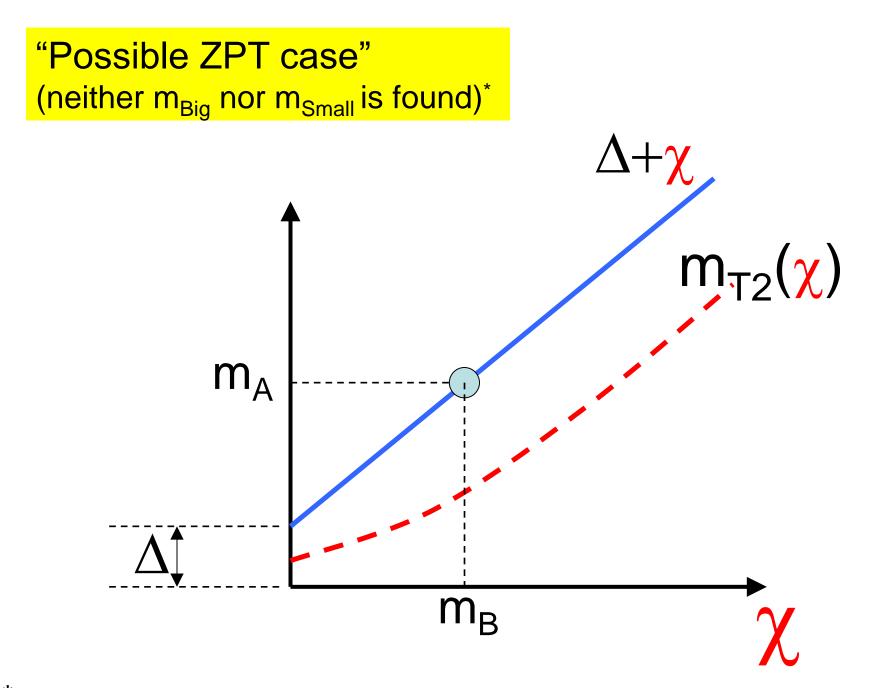


- with
 - a di-lepton invariant mass endpoint measurement (or similar) providing:

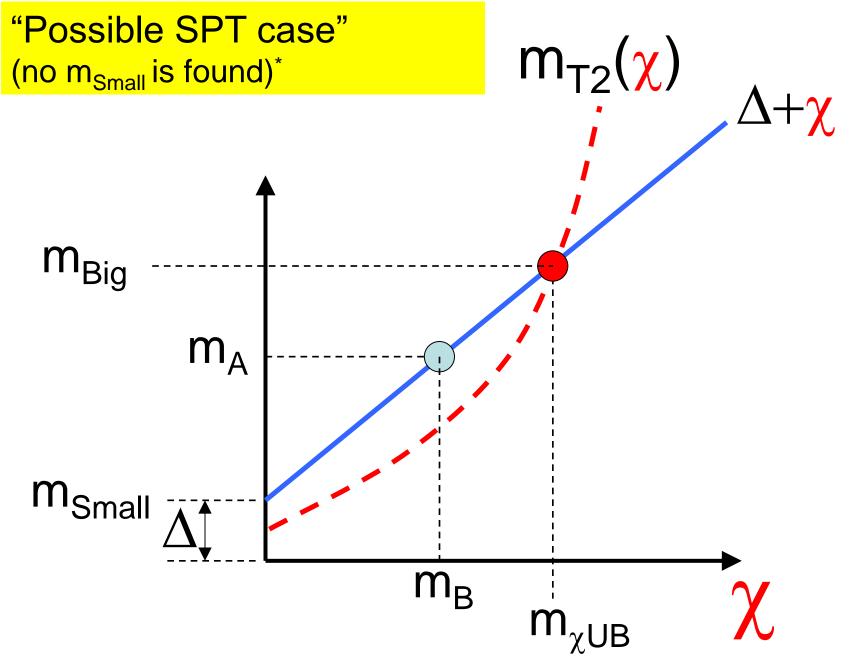
 $\Delta = M_A - M_B$ (or M_Y - M_N in the notation of their figure above)





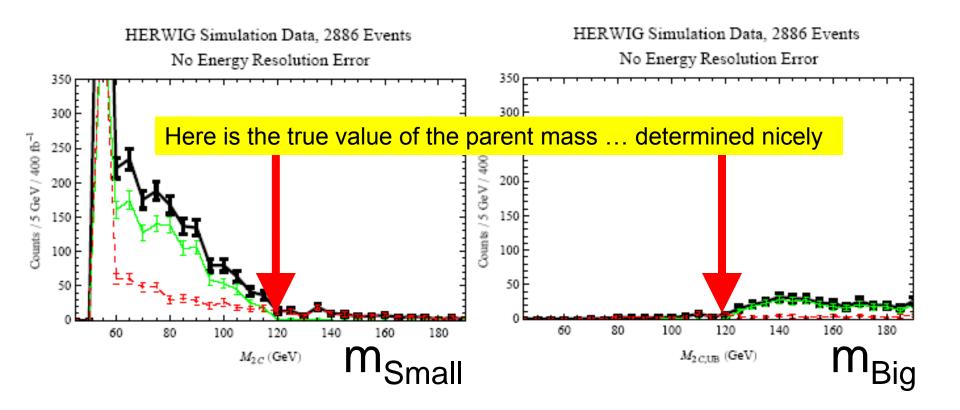


* Except for conventional definition of m_{Small} to be Δ in this case.



* Except for conventional definition of m_{Small} to be Δ in this case.

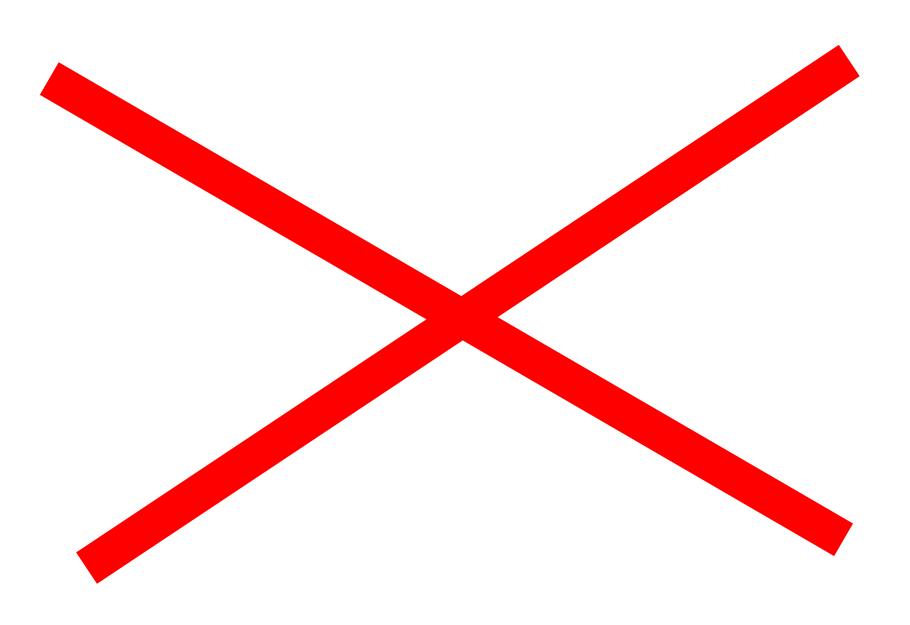
What m_{Small} and m_{Big} look like, and how they determine the parent mass



arXiv:0806.3224

Outcome:

- m_{Big} provides the first potentially-useful eventby-event upper bound for m_A
 - (and a corresponding event-by-event upper bound for m_{B} called $m_{\chi UB})$
- m_{Small} provides a new kind of event-by-event lower bound for m_A which incorporates consistency information with the dilepton edge
- m_{Big} is always reliant on SPT (large recoil of interesting system against "up-stream momentum") – cannot ignore recoil here!



LHC Specific problems

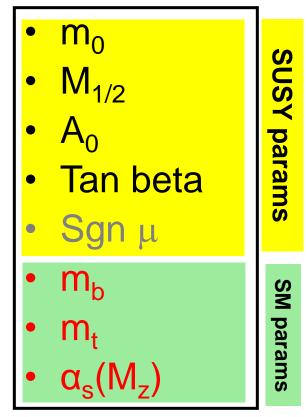
- Hadron Collider z-boost of COM unknown
- Pile up, multiple interactions
- Production of many new particles at once?

• Multiple massive stable invisible particles?

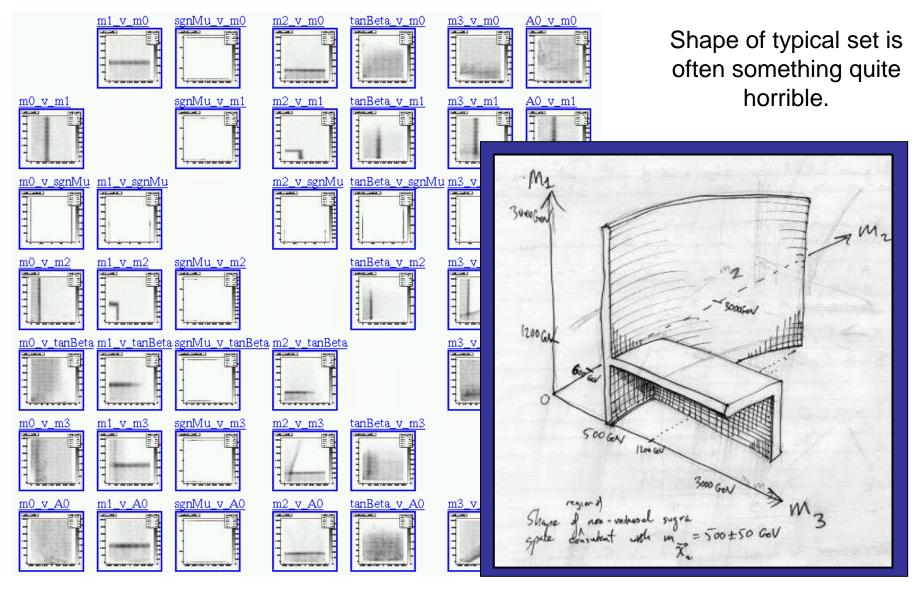
What sort of parameter spaces?

- High dimensional
- At the very least, 8 dims
- More like ~100 dims

 No really compelling reasons to believe in any particular simple model



Unusual parameter spaces!



Contrast with UA1/UA2

- Glashow Wienberg Salam: Phys Rev Lett 19, 1264 (1967)
 - Predictions in terms of (then) unknown θ_W :

- $\rm M_Z > 75~GeV/c^2,~M_W > 35~GeV/c^2$

- By 1982 θ_W much constrained, giving: - $M_z \approx 92 \pm 2 \text{ GeV/c}^2$, $M_W \approx 82 \pm 2 \text{ GeV/c}^2$
- CERN able to build UA1+UA2 (~1980) knowing the above.
- In 1983 UA1+UA2 observe W and Z at expected masses:

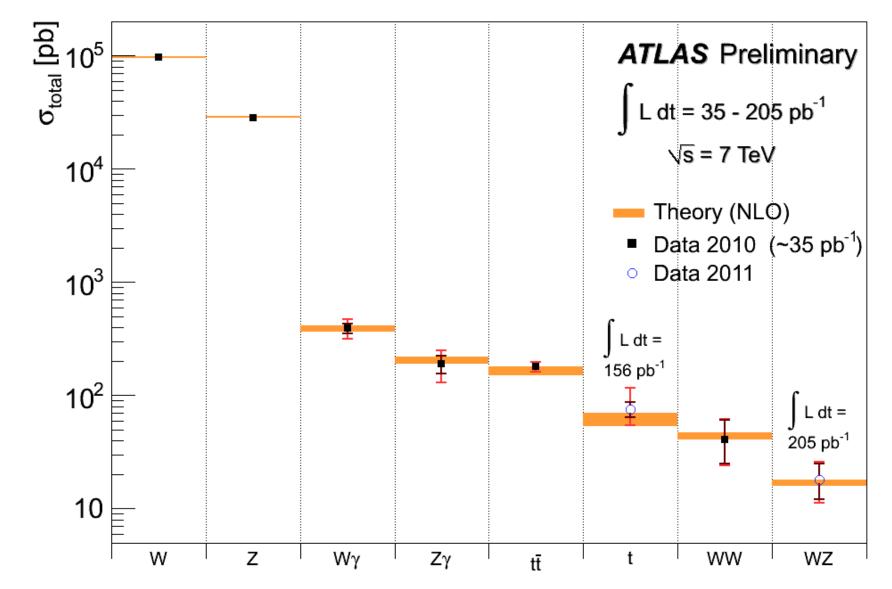
- $M_Z{\approx}$ 95±3 GeV/c², $M_W{\approx}81{\pm}5$ GeV/c²

A personal view of some of the recent ATLAS results

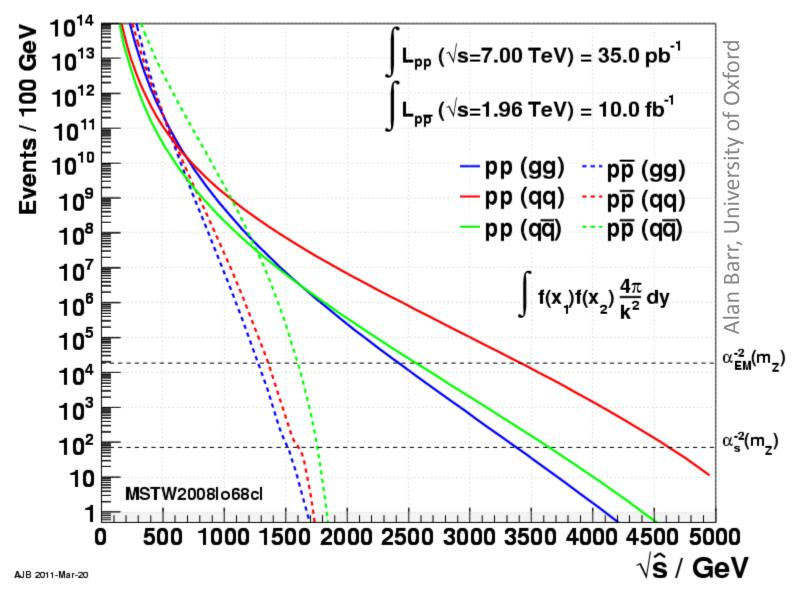
(unashamed focus on new physics searches)

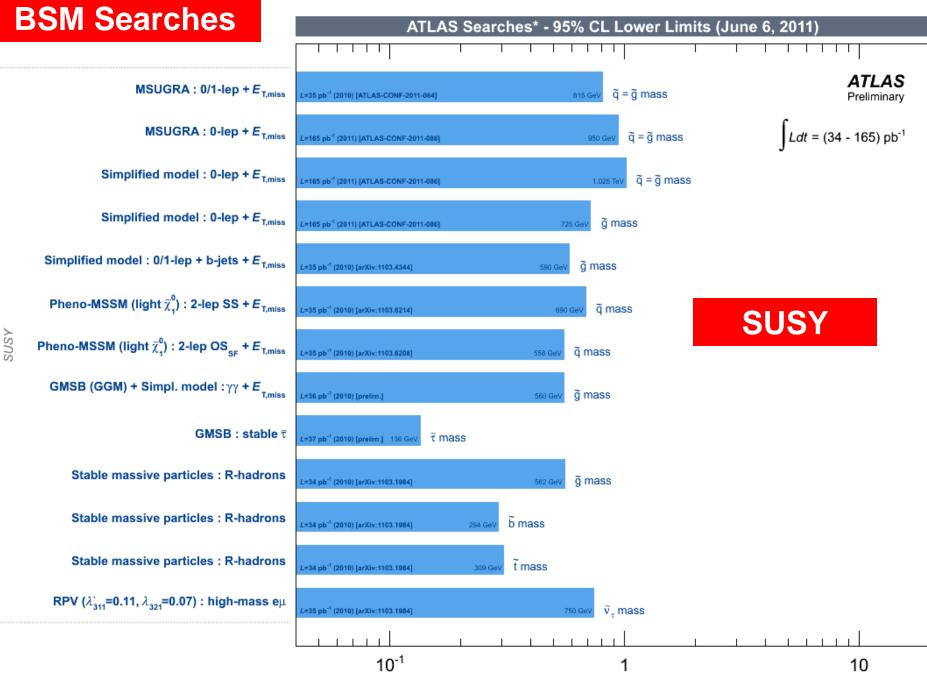
Christopher Lester

Inclusive weak boson and top quark cross section measurements by ATLAS



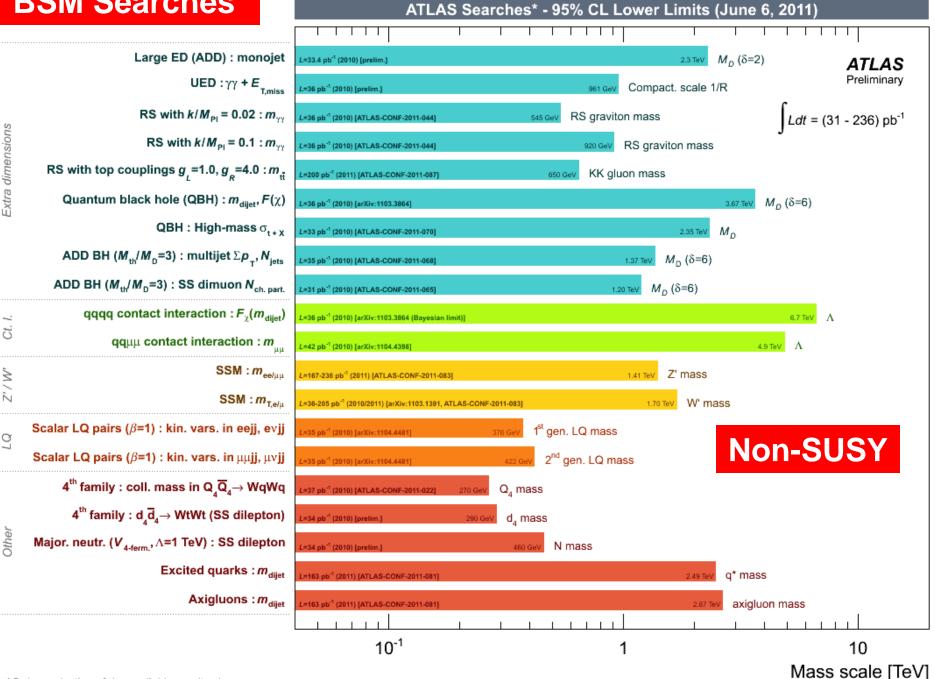
Parton-parton luminosity



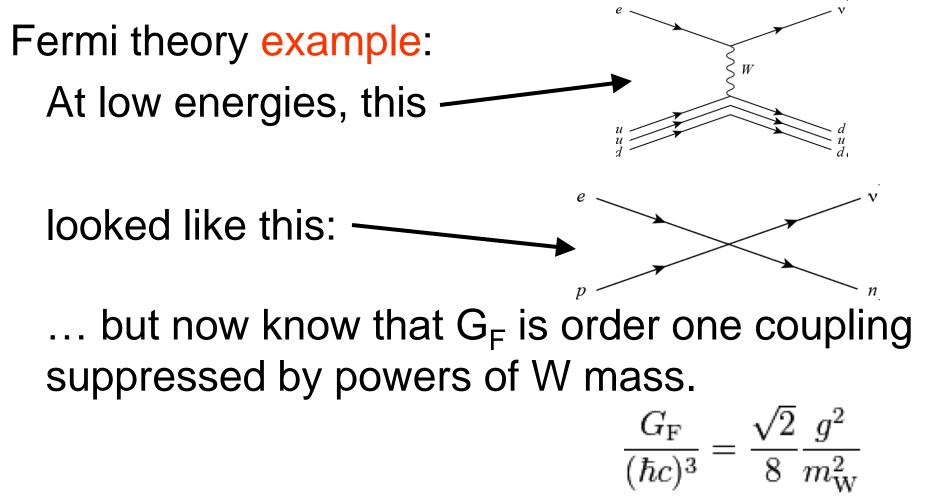


Mass scale [TeV]

BSM Searches

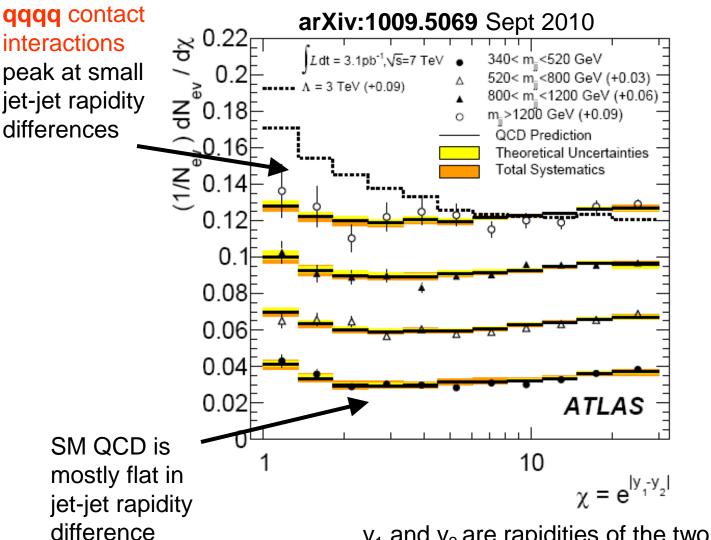


Contact interactions



Can do the same sort of thing for "four quark vertex" to constrain new mass scale.

3.4 TeV contact interactions were excluded by 3/pb of data (95% CL)

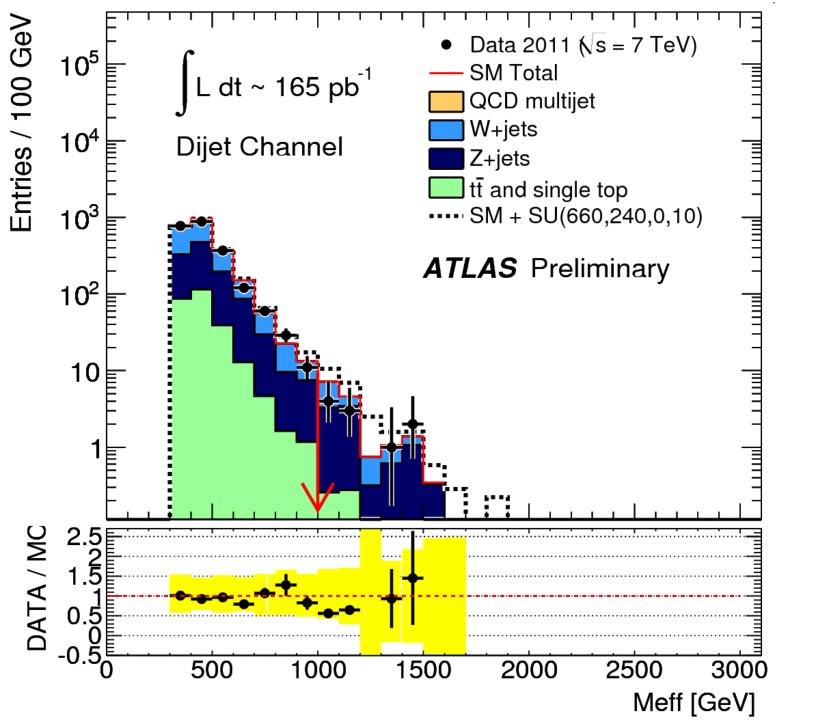


qqqq limit increases to 9.5 TeV with 36/pb (Mar 2011: arXiv:1103.3864)

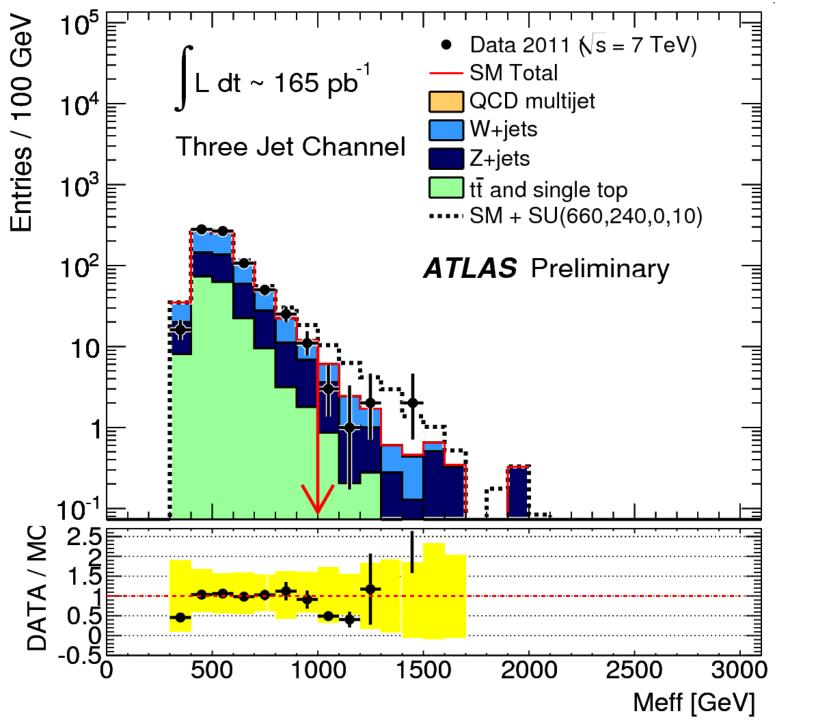
and

qquu limit is at 4.5 TeV with 42/pb (April 2011: arXiv:1104.4398)

 y_1 and y_2 are rapidities of the two jets.



atest AT transverse AS 0-lepton, momentum data. lets missing

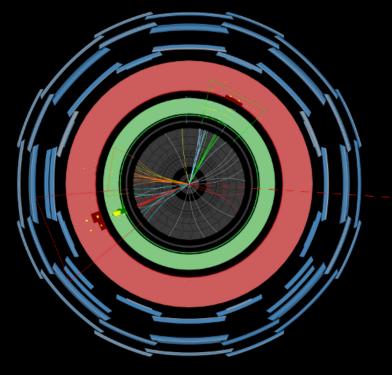


atest AT transverse AS 0-lepton, momentum data. lets missing

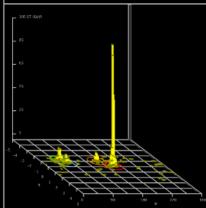
Highest Meff event so far ...

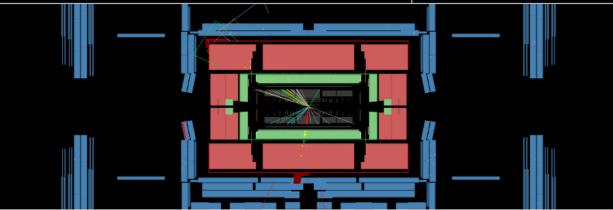
The highest Meff in any (supposedly "clean") ATLAS event is 1548 GeV

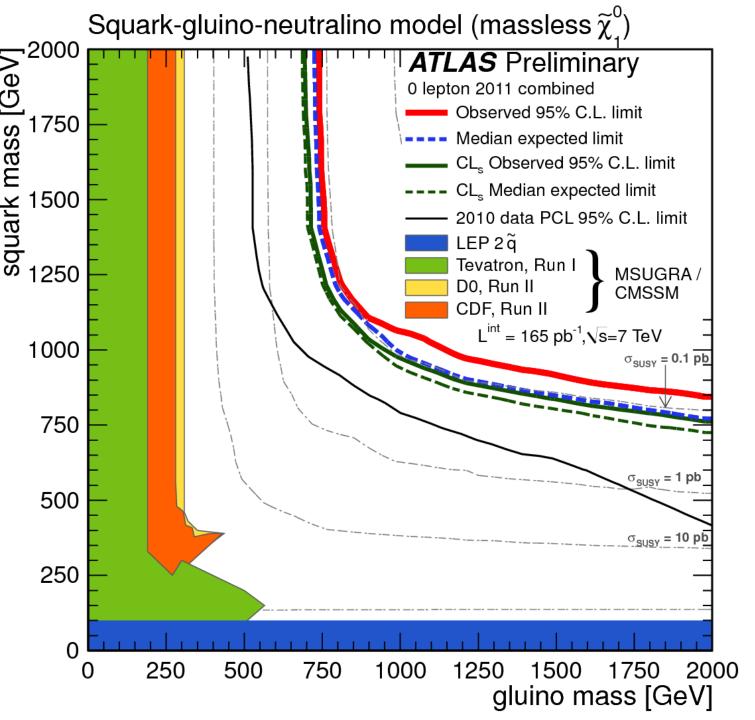
- calculated from four jets with pts:
 - 636 GeV
 - 189 GeV
 - 96 GeV
 - 81 GeV
- 547 GeV of missing transverse momentum.



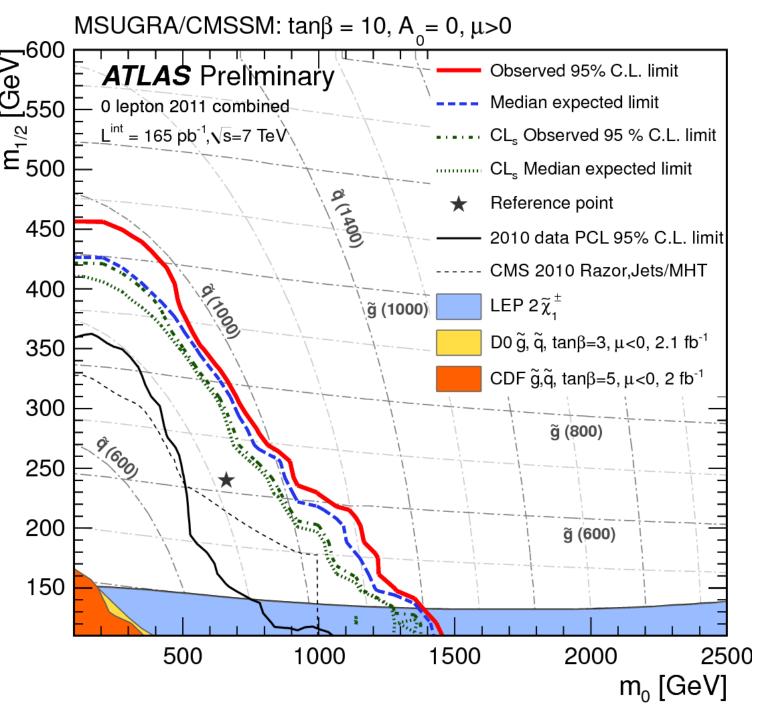








atest A transverse AS S 0-lepton, momentum data. **Jets** missing

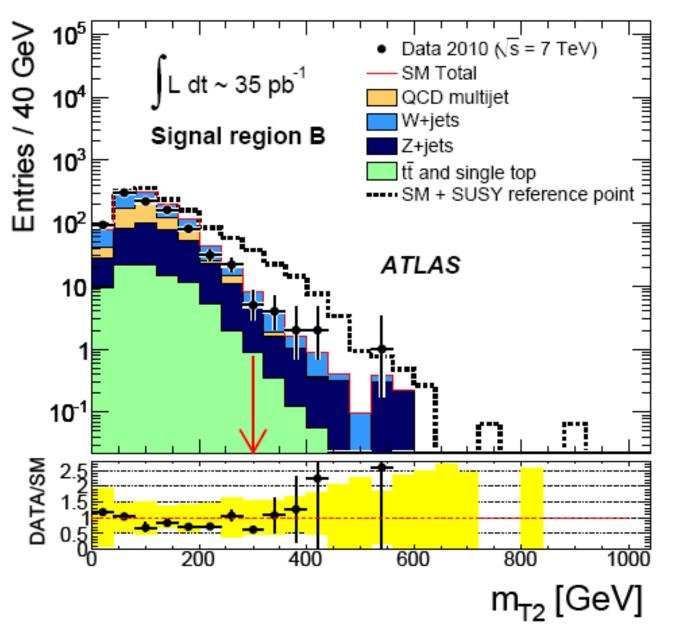


atest AT transverse LAS 0-lepton, jets, momentum data. missing

Less well tested areas

- neutralino mass close to squark or gluino mass
- signatures with not many jets

So far MT2 only competitive at 35/pb

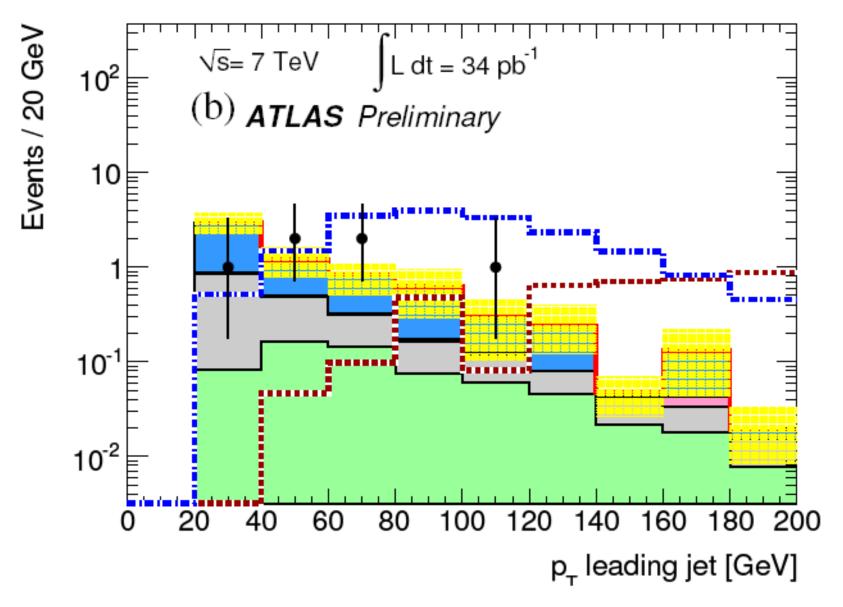


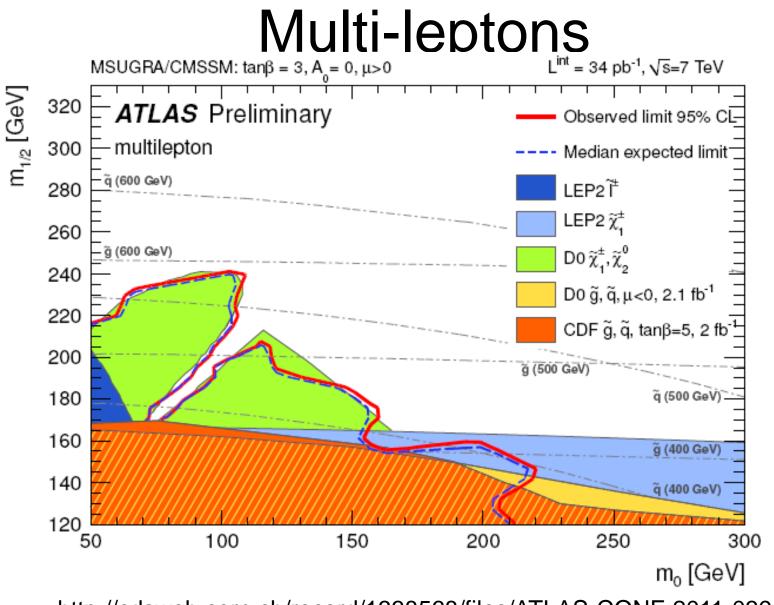
Multi-leptons (with jets and MPT)

- Require 3 leptons (any flavour and charge combos)
 - 20 GeV electron/muon
 - 20 GeV electron/muon
 - 20 GeV electron / 10 GeV muon
- Require 2 jets > 50 GeV and MPT > 50 GeV to suppress ttbar and Z+jets
 - so not sensitive to direct multilepton production.

http://cdsweb.cern.ch/record/1338568/files/ATLAS-CONF-2011-039.pdf

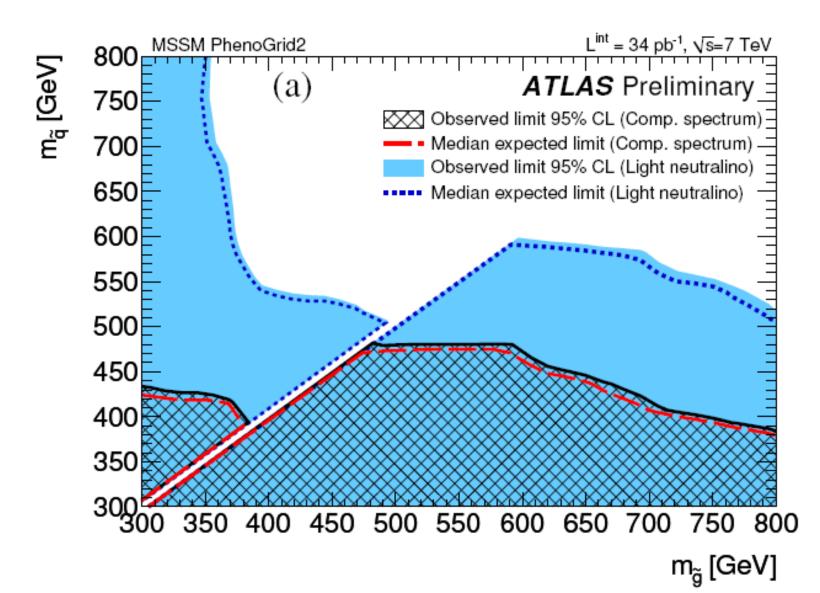
Multi-leptons





http://cdsweb.cern.ch/record/1338568/files/ATLAS-CONF-2011-039.pdf

Multi-leptons



 Your favourite multi-lepton producing model is probably not ruled yet, unless you know it makes lots of jets too ... Excesses in e+e- or mu+mu- over e+mu- and e-mu+?

 Can we focus on flavour-conserving BSM signals, and reduce sensitivity to BG modelling?

$$S = \frac{N(e^{\pm}e^{\mp})}{\beta(1 - (1 - \tau_e)^2)} - \frac{N(e^{\pm}\mu^{\mp})}{1 - (1 - \tau_e)(1 - \tau_{\mu})} + \frac{\beta N(\mu^{\pm}\mu^{\mp})}{(1 - (1 - \tau_{\mu})^2)}$$

http://arxiv.org/abs/1103.6208

	$e^{\pm}e^{\mp}$	$e^{\pm}\mu^{\mp}$	$\mu^{\pm}\mu^{\mp}$
Data	4	13	13
Z/γ^*+ jets	$0.40{\pm}0.46$	0.36 ± 0.20	0.91 ± 0.67
Dibosons	$0.30{\pm}0.11$	$0.36 {\pm} 0.10$	$0.61 {\pm} 0.10$
$t\bar{t}$	$2.50{\pm}1.02$	6.61 ± 2.68	4.71 ± 1.91
Single top	0.13 ± 0.09	$0.76 {\pm} 0.25$	$0.67 {\pm} 0.33$
Fakes	0.31 ± 0.21	-0.15 ± 0.08	$0.01 {\pm} 0.01$
Total SM	$3.64{\pm}1.24$	8.08 ± 2.78	6.91 ± 2.20
	Z/γ^*+ jets Dibosons $t\bar{t}$ Single top Fakes	$\begin{array}{c c} \hline \text{Data} & 4 \\ \hline Z/\gamma^* + \text{jets} & 0.40 \pm 0.46 \\ \hline \text{Dibosons} & 0.30 \pm 0.11 \\ \hline t\bar{t} & 2.50 \pm 1.02 \\ \hline \text{Single top} & 0.13 \pm 0.09 \\ \hline \text{Fakes} & 0.31 \pm 0.21 \\ \end{array}$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $

2lepton flavour subtraction :

If the assumption is made that the branching fractions for $e^{\pm}e^{\mp}$ and $\mu^{\pm}\mu^{\mp}$ final states in new physics events are identical, and the branching fraction for $e^{\pm}\mu^{\mp}$ final states is zero, a limit $\bar{S}_s < 8.8$ is set at 95% confidence level. Al-

i.e. lepton flavour conserving limit of order 10 events for order 35 events/pb indicates limit for cross section for lepton flavour conserving production is about ~0.3 pb

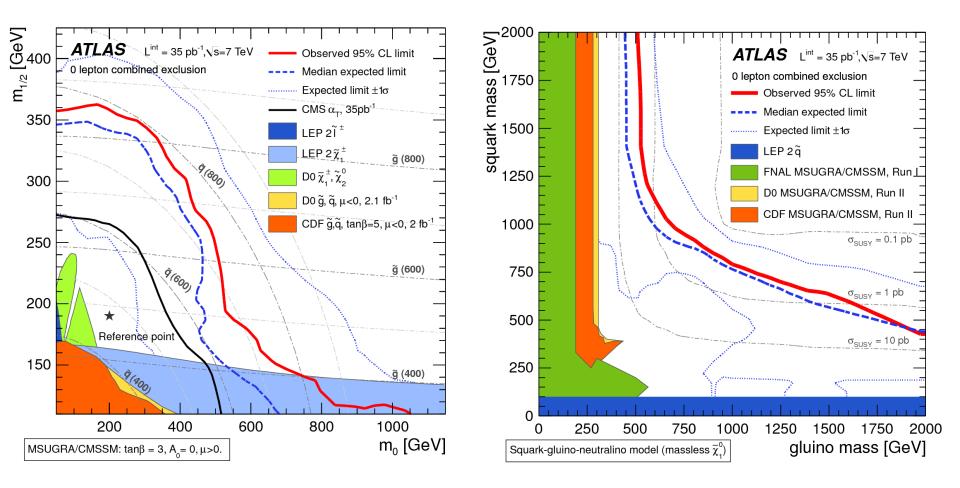
fairly model independent

http://arxiv.org/abs/1103.6208

competitive with results from the jets+mpt analysis:

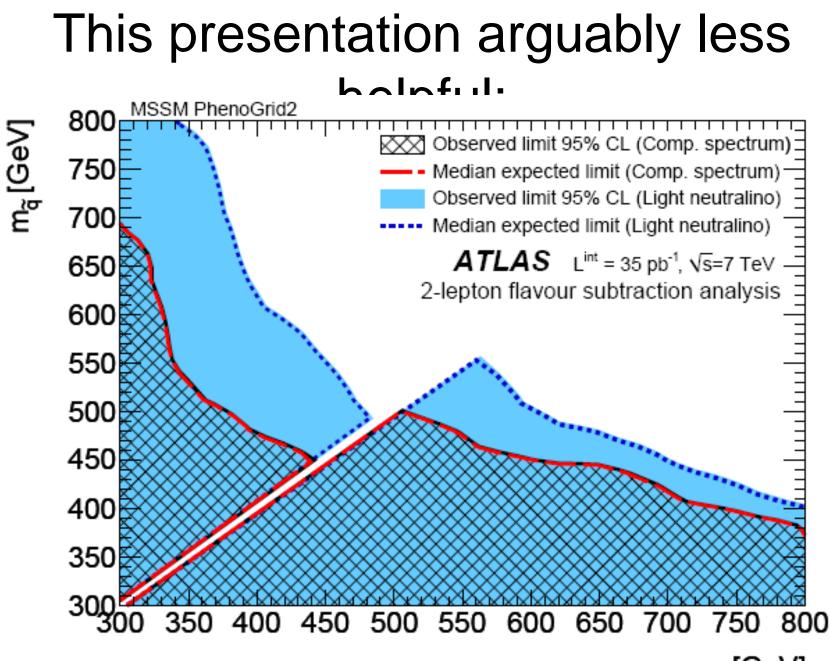
Exclude non-SM effective cross sections (σ x BR x Acc x Eff): A: 1.3 pb B: 0.35 pb C: 1.1 pb D: 0.11 pb https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PAPERS/susy-Olepton_01/

.. competitive with 35/pb limits on strong BSM production



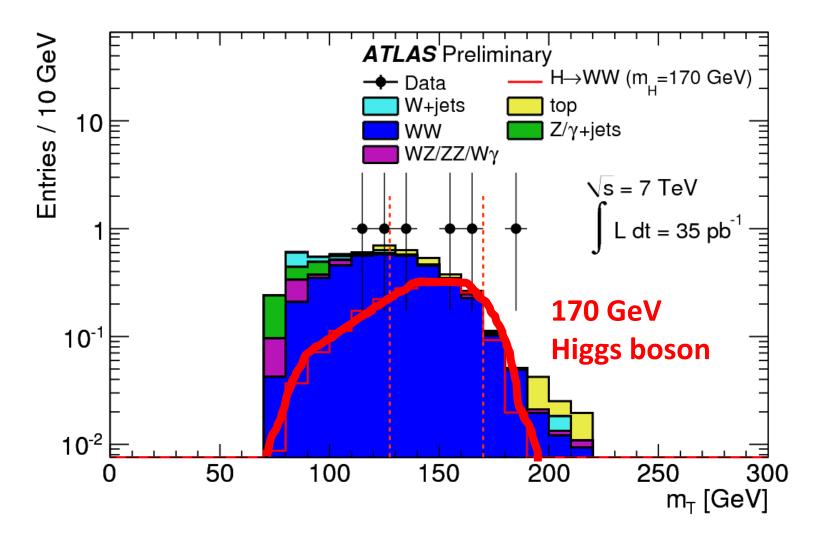
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https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PAPERS/susy-Olepton_01/

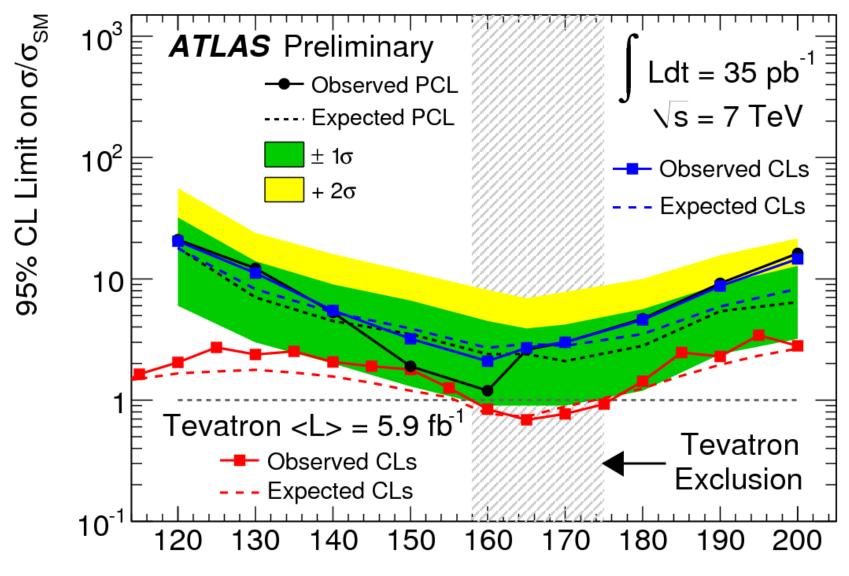


m_ã [GeV]

Against the 2010 LHC data...



ATLAS 35/pb: $H \rightarrow WW \rightarrow$



m_H [GeV]