Supersymmetry: a very basic, biased and completely incomplete introduction

Michael Krämer (RWTH Aachen)

- ► The supersymmetric harmonic oscillator
- ► Motivation for SUSY: Symmetry & the hierarchy problem
- ► The MSSM
- ► SUSY searches

References

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The supersymmetric harmonic oscillator

Recall raising and lowering operators in quantum mechanics

$$\begin{array}{lll} b^+|n_B\rangle &=& \sqrt{n_B+1}\,|n_B+1\rangle \\ b^-|n_B\rangle &=& \sqrt{n_B}\,|n_B-1\rangle \end{array}$$

where $b^-|0
angle = 0$ and $[b^-, b^+] = 1; [b^-, b^-] = [b^+, b^+] = 0$

 $\rightarrow b^+/b^-$ creates/annihilates bosons

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Analogously for fermions

$$f^+|n_F\rangle = \sqrt{n_F+1}|n_F+1
angle$$

 $f^-|n_F
angle = \sqrt{n_F}|n_F-1
angle$

But fermions obey Pauli exclusion principle

 \rightarrow only two states $|0\rangle$ and $f^+|0\rangle=|1\rangle$

So for fermions

$$f^+|0
angle=|1
angle, f^-|1
angle=|0
angle$$
 and $f^-|0
angle=f^+|1
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For fermions

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Matrix representation:

with
$$|0\rangle \equiv \begin{pmatrix} 1\\0 \end{pmatrix}$$
 and $|1\rangle \equiv \begin{pmatrix} 0\\1 \end{pmatrix}$
one has $f^+ = \begin{pmatrix} 0&0\\1&0 \end{pmatrix}$ and $f^- = \begin{pmatrix} 0&1\\0&0 \end{pmatrix}$

and
$$\{f^-,f^+\}=1; \{f^-,f^-\}=\{f^+,f^+\}=0\,.$$

For fermions

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and
$$\{f^-, f^+\} = 1; \{f^-, f^-\} = \{f^+, f^+\} = 0.$$

Thus, bosonic and fermionic Hamilton operators take the form

$$H_B = \omega_B \left(b^+ b^- + \frac{1}{2} \right)$$
$$H_F = \omega_F \left(f^+ f^- - \frac{1}{2} \right)$$

SUSY transformations

SUSY operators act on product space

 $|n_B\rangle|n_F\rangle\equiv|n_Bn_F\rangle$ where $n_B=0,1,\ldots,\infty;$ $n_F=0,1$

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Need to construct operators with

so that

 $\begin{array}{ll} Q_+|{\rm boson}\rangle\propto |{\rm fermion}\rangle & & Q_+|{\rm fermion}\rangle=0\\ Q_-|{\rm fermion}\rangle\propto |{\rm boson}\rangle & & Q_-|{\rm boson}\rangle=0\,. \end{array}$

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angle & Q_+ |\mathrm{fermion}
angle = 0 \ Q_- |\mathrm{fermion}
angle \propto |\mathrm{boson}
angle & Q_- |\mathrm{boson}
angle = 0 \,. \end{aligned}$$

A simple choice is $Q_+ = b^- f^+$ $Q_- = b^+ f^-$

where $(f^+)^2 = (f^-)^2 = 0 \quad \Rightarrow \quad Q_+^2 = Q_-^2 = 0$.

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$$H_{\mathrm{SUSY}} = \{Q_+, Q_-\}$$

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 $[\mathsf{Check \ e.g.} \ [H_{\mathrm{SUSY}}, Q_+] = Q_+Q_-Q_+ + Q_-Q_+Q_+ - Q_+Q_+Q_- - Q_+Q_-Q_+ = 0\,.]$

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 $[\mathsf{Check e.g. } [H_{\mathrm{SUSY}}, Q_{+}] = Q_{+}Q_{-}Q_{+} + Q_{-}Q_{+}Q_{+} - Q_{+}Q_{+}Q_{-} - Q_{+}Q_{-}Q_{+} = 0\,.]$

Now recall
$$Q_+ = \sqrt{\omega} \ b^- f^+$$

 $Q_- = \sqrt{\omega} \ b^+ f^-$

so that $H_{SUSY} = \omega \{ b^- f^+, b^+ f^- \}$ $= \omega (b^- f^+ b^+ f^- + b^+ f^- b^- f^+)$ $= \omega ((1 + b^+ b^-) f^+ f^- + b^+ b^- (1 - f^+ f^-))$ $= \omega (f^+ f^- + b^+ b^-)$ $= H_B + H_E$

provided we set $\omega_B = \omega_F = \omega$.

The energy spectrum of the SUSY oscillator has remarkable features

$$H_{\rm SUSY}|n_B n_F\rangle = \omega (N_B + N_F)|n_B n_F\rangle$$

 $\rightarrow E = \omega (n_B + n_F)$

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The spectrum of the SUSY oscillator:



Summary of the SUSY oscillator

 If we start with a bosonic system we need to introduce fermions (and vice versa)

• We need identical couplings: $\omega_F = \omega_B$

The spectrum consists of pairs of states (bosonic/fermionic) with the same energy

The energy of the ground state is zero

Summary of the SUSY oscillator

- If we start with a bosonic system we need to introduce fermions (and vice versa)
 - \rightarrow for a SUSY extension of the SM we will have to introduce SUSY partners for all SM particles
- ► We need identical couplings: $\omega_F = \omega_B$ \rightarrow SUSY extensions of the SM do not introduce new couplings
- The spectrum consists of pairs of states (bosonic/fermionic) with the same energy
 - \rightarrow SM particles and SUSY partners have the same mass (and internal quantum numbers)
- ► The energy of the ground state is zero → SUSY QFTs have less divergences

- ► The supersymmetric harmonic oscillator
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Why supersymmetric quantum field theory?

SUSY is a symmetry which relates fermions and bosons:

 $egin{array}{rcl} Q|\mathrm{fermion}
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Example: electron $(\psi_e)_L(s = 1/2) \leftrightarrow \phi_{\tilde{e}_L}(s = 0)$ (scalar electron \tilde{e}_L) $(\psi_e)_R(s = 1/2) \leftrightarrow \phi_{\tilde{e}_R}(s = 0)$ (scalar electron \tilde{e}_R)

Note: $\tilde{e}_{L/R}$ are called "left/right-handed" selectron to indicate SUSY partner (scalar particle has no helicity).

How do we characterize a particle?

Consider Lorentz group (rotations & boosts) with invariants

$$P_{\mu}P^{\mu}=m^2 \ \ \, ext{and} \ \ \, W_{\mu}W^{\mu}=-m^2s(s+1)\,.$$

 P_{μ} : energy momentum operator $W_{\mu} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} P_{\nu} M_{\rho\sigma}$: Pauli-Lubanski spin vector where $M_{\mu\nu}$ = angular momentum tensor = $x^{\mu}P^{n}u - x^{\nu}P^{\mu} + \frac{1}{2}\Sigma^{\mu\nu}$

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The
$$\left\{ \begin{array}{c} \text{Lorentz} \\ \text{Gauge} \end{array} \right\}$$
 symmetry is an $\left\{ \begin{array}{c} \text{external} \\ \text{internal} \end{array} \right\}$ symmetry.

- $\rightarrow\,$ invariants of gauge symmetries ("charges") do not change in space and time
- → the generators of the gauge group T^a commute with the generators of the Lorentz group $[T^a, P^\mu] = 0$ and $[T^a, M^{\mu\nu}] = 0$

Coleman & Mandula, "*All Possible Symmetries of the S Matrix*", PRD 159 (1967):

The only possible conserved quantities that transform as tensors under the Lorentz group are the generators of the Lorentz group (P_{μ} , $M_{\mu\nu}$) and Lorentz scalars (internal symmetries).

According to Coleman & Mandula, if we add to the Lorentz symmetry any further external symmetry, whose generators are tensors, then the scattering process must be trivial, i.e. there is no scattering at all.

Let us work this out in an example...

We consider



 $2 \rightarrow 2$ spinless scattering

and take, for simplicity, $p_i^2 = m_i^2 = m^2$.

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Now let us postulate an additional external symmetry, e.g. a conserved tensor $R_{\mu\nu} = p_{\mu}p_{\nu} - \frac{1}{4}g_{\mu\nu}m^2$.

If $R_{\mu\nu}$ is conserved, then

$$\begin{aligned} R^1_{\mu\nu} + R^2_{\mu\nu} &= R^3_{\mu\nu} + R^4_{\mu\nu} \\ \text{and thus} \quad p^1_{\mu} p^1_{\nu} + p^2_{\mu} p^2_{\nu} &= p^3_{\mu} p^3_{\nu} + p^4_{\mu} p^4_{\nu} \end{aligned}$$

Specifically, in the center-of-mass frame we have

$$p_{1} = (E, 0, 0, p)$$

$$p_{2} = (E, 0, 0, -p)$$

$$p_{3} = (E, 0, p \sin \theta, p \cos \theta)$$

$$p_{4} = (E, 0, -p \sin \theta, -p \cos \theta)$$

Let us look at e.g. $\mu = \nu = 4$. We find

$$2p^2 = 2p^2\cos\theta$$

 $\Rightarrow \theta = 0$, i.e. no scattering

Tensors $a_{\mu_1\cdots\mu_N}$ are combinations of Lorentz vector indices, which each transform like a vector:

$$a'_{\mu_1\cdots\mu_N} = \Lambda_{\mu_1}^{\nu_1}\cdots\Lambda_{\mu_N}^{\nu_N}a_{\mu_1\cdots\mu_N}$$

 \rightarrow tensors are bosons

This points to the loop-hole in the Coleman-Mandula "no-go" theorem: The argument of Coleman-Mandula does not apply to conserved charges transforming as spinors. Tensors $a_{\mu_1\cdots\mu_N}$ are combinations of Lorentz vector indices, which each transform like a vector:

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How could nature have ignored this last possible external symmetry?

What is the algebra of the SUSY generators Q_{α} ?

One can work out that

$$\begin{array}{lll} \left[P^{\mu}, Q_{\alpha} \right] &=& 0 \\ \left[M^{\mu\nu}, Q_{\alpha} \right] &=& -i (\sigma^{\mu\nu})^{\beta}_{\alpha} Q_{\beta} \\ \left\{ Q_{\alpha}, Q_{\beta} \right\} &=& 0 \\ \left\{ Q_{\alpha}, Q^{\dagger}_{\beta} \right\} &=& 2 (\sigma^{\mu})_{\alpha\beta} P_{\mu} \end{array}$$

where $\sigma^{\mu} = (1, \sigma^{i})$, $\bar{\sigma}^{\mu} = (1, \sigma^{i})$, $\sigma^{\mu\nu} = (\sigma^{\mu}\bar{\sigma}^{\nu} - \sigma^{\nu}\bar{\sigma}^{\mu})/4$.

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Q raises by spin 1/2, Q^\dagger lowers by spin 1/2

$$c_{c}(s, \sigma) \xrightarrow{\qquad Q^{+}} \mathcal{R}_{c}(s, \tau)$$

What are the immediate consequences of SUSY invariance?

$$[P^{\mu},Q]=0 \quad \Rightarrow \quad [m^2,Q]=[P_{\mu}P^{\mu},Q]=0$$

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But we have not seen a 511 keV = $m_{\tilde{e}}$ charged ([Q, T^a] = 0) scalar

 \rightarrow SUSY must be broken

At what scale?

What is the mass of the supersymmetric particles?
The hierarchy problem and the scale of SUSY breaking

Let us first look at electrodynamics:

The Coulomb field of the electron is $E_{\text{self}} = \frac{3}{5} \frac{e^2}{r_e}$.

This can be interpreted as a contribution to the electron mass:

$$m_e c^2 = m_{e,0} c^2 + E_{\rm self} \,.$$

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However, with $r_e \lesssim 10^{-17}$ cm (exp. bound on point-like nature) one has

$$m_e c^2 = 511 \,\mathrm{keV} = (-9999.489 + 10000.000) \,\mathrm{keV}$$

 \rightarrow fine-tuning!

Coulomb self-energy in time-ordered perturbation theory:



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But also have positron e^+ with $Q(e^+) = -Q(e^-)$ and $m(e^+) = m(e^-)$ \rightarrow new diagram

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$$\rightarrow m_e c^2 = m_{e,0} c^2 \left(1 + \frac{3\alpha}{4\pi} \ln \left(\frac{\hbar}{m_e c r_e} \right) \right)$$

We found that $m_e c^2 = m_{e,0} c^2 \left(1 + \frac{3\alpha}{4\pi} \ln \left(\frac{\hbar}{m_e c r_e} \right) \right).$

So even if $r_e=1/M_{\rm Planck}=1.6\times 10^{-33}\,{\rm cm},$ the corrections to the electron mass are small

$$m_e c^2 \approx m_{e,0} c^2 \left(1 + 0.1\right)$$
 .

Also, if $m_{e,0} = 0$ then $m_e = 0$ to all orders:

the mass is protected by a (chiral) symmetry

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Recall 't Hooft's naturalness argument

A dimensionless number x is allowed to be very small iff The value x = 0 would imply an exact symmetry Now let us look at the scalar (=Higgs) self-energy:



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$$\Rightarrow \Delta m_{\phi}^2 = 2N(f) \lambda_f^2 \int \frac{d^4k}{(2\pi)^4} \left(\frac{1}{k^2 - m_f^2} + \frac{2m_f^2}{(k^2 - m_f^2)^2}\right)$$

The integral is divergent, so we introduce a momentum cut-off. [Recall that $d^4k \sim k^3 dk \rightarrow \int^{\Lambda} dk k^3 / (k^2 - m_f^2) \sim \Lambda^2$ and $\int^{\Lambda} dk k^3 / (k^2 - m_f^2)^2 \sim \ln \Lambda$.] Now let us look at the scalar (=Higgs) self-energy:

$$\Rightarrow \Delta m_{\phi}^{2} = 2N(f) \lambda_{f}^{2} \int \frac{d^{4}k}{(2\pi)^{4}} \left(\frac{1}{k^{2} - m_{f}^{2}} + \frac{2m_{f}^{2}}{(k^{2} - m_{f}^{2})^{2}}\right)$$

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Straightforward calculation gives

$$\Delta m_{\phi}^2 = \frac{N(f)\,\lambda_f^2}{8\pi^2} \left(\Lambda^2 + 3m_f^2 \ln\left(\frac{\Lambda^2 + m_f^2}{m_f^2}\right) + 2m_f^2 \frac{\Lambda^2}{\Lambda^2 + m_f^2}\right)$$

Because of the quadratic divergence we find

$$\Delta m_\phi^2(\Lambda=M_{
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and so

$$m_\phi^2 \lesssim 1\,{
m TeV}^2 = m_{\phi,0}^2 + \Delta m_\phi^2$$

implies a huge fine-tuning:

Comment: it is essential that $\Lambda < \infty$, i.e. we assume that new physics sets in at $E \sim \Lambda$. Is this a tautology? No: we assume new physics at some very high scale Λ and find that the standard model needs new physics well below Λ .

The natural mass scale of a scalar field is the highest scale in nature.

The SUSY solution to the hierarchy problem

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Let us increase the particle content (as for the e^- self-energy)

Before we had
$$\overset{\psi}{---}$$

Now we include in addition two scalars \tilde{f}_L, \tilde{f}_R with couplings

$$\mathcal{L}_{\phi\tilde{f}} = -\frac{\tilde{\lambda}_{f}^{2}}{2}\phi^{2}\left(|\tilde{f}_{L}|^{2} + |\tilde{f}_{R}|^{2}\right) - v\tilde{\lambda}_{f}^{2}\phi\left(|\tilde{f}_{L}|^{2} + |\tilde{f}_{R}|^{2}\right) + \left(\frac{\lambda_{f}}{\sqrt{2}}A_{f}\phi\tilde{f}_{L}\tilde{f}_{R}^{*} + \text{h.c.}\right)$$

which lead to additional contributions to the self-energy:



The additional contributions to the Higgs mass are:

$$\begin{split} \Delta m_{\phi}^2 &= \tilde{\lambda}_f^2 \, N(\tilde{f}) \, \int \! \frac{d^4 k}{(2\pi)^4} \left(\frac{1}{k^2 - m_{\tilde{f}_L}^2} + \frac{1}{k^2 - m_{\tilde{f}_R}^2} \right) \\ &+ (\tilde{\lambda}_f^2 v)^2 \, N(\tilde{f}) \int \! \frac{d^4 k}{(2\pi)^4} \left(\frac{1}{(k^2 - m_{\tilde{f}_L}^2)^2} + \frac{1}{(k^2 - m_{\tilde{f}_R}^2)^2} \right) \\ &+ (\lambda_f A_f)^2 \, N(\tilde{f}) \int \! \frac{d^4 k}{(2\pi)^4} \frac{1}{(k^2 - m_{\tilde{f}_L}^2)(k^2 - m_{\tilde{f}_R}^2)} \end{split}$$

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The first term cancels the SM $\Lambda^2\text{-contribution}$ if

$$\tilde{\lambda}_f = \lambda_f$$
 and $N(\tilde{f}) = N(f)$

as required in SUSY.

The cancellation happens because of spin-statistics:



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Note:

- ▶ the cancellation of quadratic divergences is independent of $m_{\tilde{f}_L}$, $m_{\tilde{f}_R}$, A_f .
- ▶ the term $\propto A_f \phi \tilde{f}_L \tilde{f}_R^*$ breaks SUSY but does not lead to Λ^2 divergences
 - \rightarrow "soft" SUSY breaking

Let us look at the finite SM + SUSY contributions:

$$\begin{split} \Delta m_{\phi}^2 &= \frac{\lambda_f^2 \mathcal{N}(f)}{16\pi^2} \left(-2m_f^2 \left(1 - \ln \frac{m_f^2}{\mu^2} \right) + 4m_f^2 \ln \frac{m_f^2}{\mu^2} \right. \\ &+ 2m_{\tilde{f}}^2 \left(1 - \ln \frac{m_{\tilde{f}}^2}{\mu^2} \right) - 4m_{\tilde{f}}^2 \ln \frac{m_{\tilde{f}}^2}{\mu^2} - |A_f|^2 \ln \frac{m_{\tilde{f}}^2}{\mu^2} \right) \,, \end{split}$$

where we have assumed $m_{\tilde{f}_L} = m_{\tilde{f}_R} = m_{\tilde{f}}$.

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where we have assumed $m_{\tilde{f}_L} = m_{\tilde{f}_R} = m_{\tilde{f}}$. One has

$$\Delta m_{\phi}^2 = 0$$
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But SUSY is broken, i.e. $m_{\tilde{f}}^2 = m_f^2 + \delta^2$. Thus

$$\Delta m_{\phi}^2 = \frac{\lambda_f^2 \mathcal{N}(f)}{8\pi^2} \,\delta^2 \,\left(2 + \ln \frac{m_f^2}{\mu^2}\right) + \mathcal{O}(\delta^4)$$

To have Δm_ϕ^2 small, we thus need $m_{\widetilde{f}}^2 = m_f^2 + \delta^2 = \mathcal{O}(1\,\mathrm{TeV}^2)$

SUSY is great!

Must have been tired yesterday...

A Priori:

- ► SUSY is the unique maximal external symmetry in Nature.
- ► Weak-scale SUSY provides a solution to the hierarchy problem.

A Posteriori:

- ► SUSY allows for unification of Standard Model gauge interactions.
- SUSY provides dark matter candidates.
- ► SUSY QFT's allow for precision calculations.
- ► SUSY provides a rich phenomenology and is testable at the LHC.

- ► The supersymmetric harmonic oscillator
- ▶ Motivation for SUSY: Symmetry & the hierarchy problem

► The MSSM

► SUSY searches

The Minimal Supersymmetric extension of the SM

- ► external symmetries: Poincare symmetry & supersymmetry
- ▶ internal symmetries: $SU(3) \otimes SU(2) \otimes U(1)$ gauge symmetries
- minimal particle content

Gauge Bosons $S=1$	Gauginos $S = 1/2$
$gluon, W^\pm, Z, \gamma$	gluino, $\widetilde{W}, \widetilde{Z}, \widetilde{\gamma}$
Fermions $S = 1/2$	Sfermions $S = 0$
${u_L \choose d_L} { u_L \choose e_L}$	$ig(\widetilde{u}_L \ \widetilde{d}_L ig) ig(\widetilde{ u}_L^e \ \widetilde{e}_L ig)$
u_R, d_R, e_R	$\widetilde{u}_R, \widetilde{d}_R, \widetilde{e}_R$
Higgs	Higgsinos
$\binom{H_2^0}{H_2^-}\binom{H_1^+}{H_1^0}$	${{\widetilde{H}_2^0}\choose{\widetilde{H}_2^-}}{{\widetilde{H}_1^+}\choose{\widetilde{H}_1^0}}$

In QFT the gauge couplings "run":

$$\frac{d\alpha_i(\mu)}{d\ln\mu^2} = \beta_i(\alpha_i(\mu))$$

The beta-functions β_i depend on the gauge group and on the matter multiplets to which the gauge bosons couple. Only particles with mass $< \mu$ contribute to the β_i and to the evolution of the coupling at any given mass scale μ .

The Standard Model couplings evolve with μ according to

$$\begin{array}{rcl} \mathrm{SU}(3) & : & \beta_{3,0} & = & (33 - 4n_g)/(12\pi) \\ \mathrm{SU}(2) & : & \beta_{2,0} & = & (22 - 4n_g - n_h/2)/(12\pi) \\ \mathrm{U}(1) & : & \beta_{1,0} & = & (-4n_g - 3n_h/10)/(12\pi) \end{array}$$

where $n_g = 3$ is the number of quark and lepton generations and $n_h = 1$ is the number of Higgs doublet fields in the Standard Model.

Loop contributions of superpartners change the beta-functions. In the MSSM one finds:

Gauge coupling unification

Loop contributions of superpartners change the beta-functions. In the MSSM one finds:



R-parity

- ▶ In the SM baryon and lepton number are accidental symmetries
- The most general superpotential of the SUSY-SM contains baryon and lepton number violating terms:

$$W \in \underbrace{\lambda_{ijk} L_i L_j \overline{E}_k + \lambda'_{ijk} L_i Q_j \overline{D}_k + \kappa_i L_i H_2}_{\lambda_{ijk} \overline{U}_i \overline{D}_j \overline{D}_k} + \underbrace{\lambda_{ijk}'' \overline{U}_i \overline{D}_j \overline{D}_k}_{\lambda_{ijk} \overline{U}_i \overline{D}_j \overline{D}_k}$$

lepton number violating

baryon number violating

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LQD and UDD couplings lead to rapid proton decay



 \rightarrow impose discrete symmetry: *R*-parity $R = (-1)^{3B+L+2S}$

$$ightarrow {\it R}_{
m SM} = +$$
 and ${\it R}_{
m SUSY} = -$

R-parity conservation has dramatic phenomenological consequences:

- ► lightest SUSY particle (LSP) is absolutely stable → dark matter candidate if also electrically neutral
- ▶ in collider experiments SUSY particles can only be produced in pairs
- in many models SUSY collider events contain missing E_T

SUSY breaking

Supersymmetry: $mass(e^-) = mass(\tilde{e}^-_{L,R})$

 \rightarrow SUSY must be broken

No agreed model of supersymmetry breaking

 \rightarrow phenomenological ansatz

Must preserve solution to hierarchy problem

 \rightarrow "soft" SUSY breaking

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 \rightarrow "soft" SUSY breaking

Introduce

- ► gaugino masses $M_{1/2}\chi\chi$: $M_1\tilde{B}\tilde{B}$, $M_2\tilde{W}\tilde{W}$, $M_3\tilde{g}\tilde{g}$
- ► squark and slepton masses $M_0^2 \phi^{\dagger} \phi$: $m_{\tilde{e}_L}^2 \tilde{e}_L^{\dagger} \tilde{e}_L$, $m_{\tilde{e}_R}^2 \tilde{e}_R^{\dagger} \tilde{e}_R$, $m_{\tilde{u}_L}^2 \tilde{u}_L^{\dagger} \tilde{u}_L$, $m_{\tilde{u}_R}^2 \tilde{u}_R^{\dagger} \tilde{u}_R$ etc.
- ► trilinear couplings $A_{ijk}\phi_i\phi_j\phi_k$: $A^e_{ij}\begin{pmatrix}\tilde{\nu}_i\\\tilde{e}_j\end{pmatrix}_L h_1\tilde{e}_{jR}$ etc.

• Higgs mass terms $B_{ij}\phi_i\phi_j$: Bh_1h_2 etc.

SUSY breaking

MSSM w/o breaking: two additional parameters from Higgs sector

Soft SUSY breaking

- $\blacktriangleright \ A^e_{ij}, A^d_{ij}, A^u_{ij} \qquad \qquad \rightarrow 27 \ {\sf real} + 27 \ {\sf phases}$
- $\blacktriangleright \ M^2_{\tilde{Q}}, \ M^2_{\tilde{U}}, \ M^2_{\tilde{D}}, \ M^2_{\tilde{L}}, \ M^2_{\tilde{E}} \ \rightarrow 30 \ {\rm real} \, + \, 15 \ {\rm phases}$
- $\blacktriangleright \ M_1, \ M_2, \ M_3 \qquad \qquad \rightarrow 3 \ {\sf real} + 1 \ {\sf phase}$

\rightarrow 124 parameters in the MSSM!

(but strong constraints from FCNS's, flavour mixing and CP violation)
SUSY breaking

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Simple framework constrained MSSM:

breaking is universal at GUT scale

- ▶ universal scalar masses: $M^2_{\tilde{Q}}$, $M^2_{\tilde{U}}$, $M^2_{\tilde{D}}$, $M^2_{\tilde{L}}$, $M^2_{\tilde{E}} \rightarrow M^2_0$ at $M_{\rm GUT}$
- \blacktriangleright universal gaugino masses: $\mathit{M}_{1}, \, \mathit{M}_{2}, \, \mathit{M}_{3} \rightarrow \mathit{M}_{1/2}$ at $\mathit{M}_{\rm GUT}$
- ▶ universal trilinear couplings $A^e_{ij}, A^d_{ij}, A^u_{ij} \rightarrow A \cdot h^e_{ij}, A \cdot h^d_{ij}, A \cdot h^u_{ij}$ at M_{GUT}
- \rightarrow 6 additional parameters: M_0 , $M_{1/2}$, A, B, μ , tan(β)

In QFT the (s)particle masses "run": $\frac{dM_i(\mu)}{d \ln \mu^2} = \gamma_i M_i$

SUSY mass spectrum

In QFT the (s)particle masses "run": $\frac{dM_i(\mu)}{d \ln \mu^2} = \gamma_i M_i$



In QFT the (s)particle masses "run": $\frac{dM_i(\mu)}{d \ln \mu^2} = \gamma_i M_i$



- ▶ RGE drives $(\mu^2 + m_{H_{\mu}^2})$ negative \rightarrow EWK symmetry breaking
- Masses of W and Z bosons fix B and $|\mu|$
- ▶ cMSSM has 4 1/2 parameters:

 M_0 , $M_{1/2}$, A, $tan(\beta)$ and $sign(\mu)$

After $SU(2)_L \times U(1)_Y$ breaking, mixing will occur between any two or more fields which have the same color, charge and spin

- $(\tilde{W}^{\pm}, \tilde{H}^{\pm}) \rightarrow \tilde{\chi}_{i=1,2}^{\pm}$: charginos
- $(\tilde{B}, \tilde{W}^3, \tilde{H}^0_{1,2}) \rightarrow \tilde{\chi}^0_{i=1,2,3,4}$: neutralinos
- $(\tilde{t}_L, \tilde{t}_R) \rightarrow \tilde{t}_{1,2}$ etc.: sfermion mass eigenstates

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: charginos

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: neutralinos

▶ $(\tilde{t}_L, \tilde{t}_R) \rightarrow \tilde{t}_{1,2}$ etc.: sfermion mass eigenstates

Note:

mixing involves various SUSY parameters

 \rightarrow cross sections and branching ratios become model dependent

• sfermion mixing $\propto m_f$

 \rightarrow large only for 3rd generation $(\tilde{t}_{1,2}, \tilde{\tau}_{1,2})$

- ▶ The supersymmetric harmonic oscillator
- ► Motivation for SUSY: Symmetry & the hierarchy problem
- ► The MSSM
- ► SUSY searches

Summary of SUSY searches so far...



Summary of SUSY searches so far...



... but let's see what to expect in 2011 & 2012...

- ► The supersymmetric harmonic oscillator
- ► Motivation for SUSY: Symmetry & the hierarchy problem
- ► The MSSM
- ► SUSY searches
 - indirect searches through quantum fluctuations
 - direct searches at colliders

Indirect SUSY searches

Wealth of precision measurements

from B/K physics, (g-2), astrophysics (DM) and collider limits

 $\rightarrow\,$ constraints on certain SUSY masses

e.g. through anomalous magnetic moment (g - 2)



Hamiltonian for interaction of μ -spin with external magnetic field

$$\mathcal{H}=g_{\mu}rac{e}{2m_{\mu}}ec{S}_{\mu}\cdotec{B}$$

with $g_{\mu} = 2$ in leading order

Loop-corrections modify the interaction of the $\boldsymbol{\mu}$ with the electromagnetic field

$$\Rightarrow \left(\frac{g-2}{2}\right)_{\text{QED}} = \frac{\alpha}{2\pi} = 0.00116114$$

There are additional diagrams in supersymmetric QED, e.g.

which is given by

$$I = \int \frac{d^4k}{(2\pi)^4} (ie\sqrt{2}) P_R \frac{1}{\not{k} - M_{\tilde{\gamma}}} P_L (ie\sqrt{2}) \frac{i}{(p'-k)^2 - m_{\tilde{\mu}_L}^2} \times (ie)(p'+p-2k)^{\nu} \frac{i}{(p-k)^2 - m_{\tilde{\mu}_L}^2}$$

After a short calculation (using standard QED techniques) one finds

$$\left(\frac{g-2}{2}\right)_{\rm SQED} = -\frac{m_{\mu}^2 e^2}{8\pi^2} \int_0^1 dx \frac{x^2(1-x)}{m_{\mu}^2 x^2 + (m_{\tilde{\mu}_L}^2 - M_{\tilde{\gamma}}^2 - m_{\mu}^2)x + M_{\tilde{\gamma}}^2}$$



In the limit $m_{ ilde{\mu}_L} \gg M_{ ilde{\gamma}}, m_\mu$ we find

$$\left(\frac{g-2}{2}\right)_{\rm SQED} = -\frac{\alpha}{6\pi} \frac{m_{\mu}^2}{m_{\tilde{\mu}_L}^2}$$

- SUSY contribution decouples rapidly for $m_{\tilde{\mu}_L} \gg m_{\mu}$
- ▶ SUSY contribution $\propto m_f \rightarrow$ effects in $(g-2)_e$ suppressed

Including mixing:

 \rightarrow dependence on further SUSY parameters (A and tan β)

Indirect SUSY searches

ightarrow CMSSM fit to B, K and EWK observables, $(g-2)_{\mu}$ and $\Omega_{
m DM}$

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- global fits point to light sparticle spectrum with $\tilde{m} < 1$ TeV
- current data cannot constrain more general SUSY models

Indirect SUSY searches

ightarrow CMSSM fit without $(g-2)_{\mu}$ and Ω_{DM}



• prediction of light SUSY spectrum rests on $(g - 2)_{\mu}$ and $\Omega_{\rm DM}$

SUSY particle production at the LHC

SUSY particles would be produced at the LHC via QCD processes



SUSY particle production at the LHC

SUSY particles would be produced at the LHC via QCD processes



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SUSY searches at hadron colliders

 \rightarrow Powerful MSSM signature at the LHC: cascade decays with $E_{\rm T,miss}$



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Generic signature for many new physics models which address

- the hierarchy problem
- the origin of dark matter
- → predict spectrum of new particles at the TeV-scale with weakly interacting & stable particle (← discrete parity)

Atlas limits (165 pb^{-1})



 $ightarrow m_{ ilde{q}} pprox m_{ ilde{g}} \gtrsim 950 \; {
m GeV}$

The LHC is probing the preferred region of SUSY parameter space



But what if we do not see any SUSY signal at the LHC?



We have considered the SUSY search in the 4 jets + $E_{T,miss}$ signature with $M_{eff} = \sum_{i} p_{T,i} + E_{T,miss}$



► The simulation of M_{eff} is based on Herwig++, Delphes and NLO+NLL K-factors.



• The 4 jets $+E_{T,\text{miss}}$ signature is rather independent of tan β and A_0



• Low-energy observables, DM and LHC exclusions with 2 fb $^{-1}$



▶ Low-energy observables, DM and LHC exclusions with 2 fb⁻¹



▶ Low-energy observables, DM and LHC exclusions with 7 fb⁻¹



• what happens if we take out $(g-2)_{\mu}$ and $\Omega_{\rm DM}$?

• what happens if we take out $(g - 2)_{\mu}$ and $\Omega_{\rm DM}$?



▶ LHC mass limits on squarks are rather model independent


Global SUSY fits with projected LHC exclusions: is there a tension?

- \rightarrow LEOs prefer low mass scales (for non-coloured sector)
- \rightarrow LHC prefers high mass scales (for coloured sector)
- Is there a tension building up?

Global SUSY fits with projected LHC exclusions: is there a tension?

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Is there a tension building up?

Let us look at the best fit points:

	M_0	$M_{1/2}$	A_0	aneta	χ^2/ndf
no LHC	77^{+114}_{-31}	333^{+89}_{-87}	426^{+70}_{-735}	$13\substack{+10\\-8}$	19/20
$35 \ \mathrm{pb}^{-1}$	$126\substack{+189 \\ -54}$	400^{+109}_{-40}	724_{-780}^{+722}	$17\substack{+14\\-9}$	20/21
$1~{ m fb}^{-1}$	235^{+389}_{-103}	601^{+148}_{-63}	627^{+1249}_{-717}	31^{+19}_{-18}	24/21
$2 \ \mathrm{fb}^{-1}$	254^{+456}_{-128}	647^{+157}_{-74}	771^{+1254}_{-879}	30^{+20}_{-19}	24/21
$7 \ \mathrm{fb}^{-1}$	403^{+436}_{-281}	744^{+142}_{-150}	781^{+1474}_{-918}	43^{+11}_{-33}	25/21

\rightarrow even the CMSSM would "survive" the 2011/2012 LHC run

[Note: $a_{\mu}^{\rm SUSY} \sim {
m sgn}(\mu) \tan\beta M_{\rm SUSY}^{-2}$ and $\Omega_{\rm DM}$ require larger $\tan\beta$]

Comparison of global CMSSM fits with and without LHC exclusions

There has been a lot of activity recently, see e.g.

Allanach, arXiv:1102.3149 [hep-ph], Buchmueller et al., arXiv:1102.4585 [hep-ph], Bechtle et al., arXiv:1102.4693 [hep-ph], Allanach et al., arXiv:1103.0969 [hep-ph]



 \rightarrow the analyses differ in detail, but there is good agreement overall

SUSY searches: Summary & Conclusions

- CMSSM fits to *B*, *K* and EWK observables, $(g 2)_{\mu}$ and $\Omega_{\rm DM}$
 - point to light sparticle spectrum with ${\tilde m} < 1~{
 m TeV}$
 - cannot constrain more general SUSY models
 - upper limits on sparticle masses rest on $(g-2)_{\mu}$ and $\Omega_{
 m DM}$

SUSY searches: Summary & Conclusions

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 - ▶ point to light sparticle spectrum with $\tilde{m} < 1$ TeV
 - cannot constrain more general SUSY models
 - upper limits on sparticle masses rest on $(g-2)_{\mu}$ and $\Omega_{
 m DM}$
- The LHC is now probing the SUSY parameter space favoured by low-energy observables and DM
 - It is possible to reconcile LE measurements with a possible non-discovery of SUSY in the 7 TeV run, even in very constrained models like the CMSSM.
 - LHC searches mostly constrain the coloured sparticle sector and can push squark and gluino mass limits up to about 1.5 TeV in 2011/2012.