



Optics Measurements, Corrections and  
Modeling for High-Performance Storage Rings



# Low $\gamma_t$ optics in the SPS

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# Acknowledgements



G. Arduini, T. Argyropoulos, E. Benedetto, C. Bhat, T. Bohl, S. Cettour Cave, K. Cornelis, J. Esteban Muller, F. Follin, A. Guerrero, W. Hofle, D. Jacquet, K. Li, B. Mikulek, A. Rey, G. Rumolo, B. Salvant, E. Shaposhnikova, R. Tomas, G. Vanbavinckhove, J. Wenninger

# Outline



- The background
  - Benefits for reducing transition energy in the SPS, as LHC injector
  - Methods for reducing the transition energy
- New optics based on “resonant arcs”
- Machine studies
  - Optics and non-linear model
  - Tune scans for resonance identification
  - Emittance vs. intensity, beam loss and space-charge limit
- Summary and perspectives

# SPS as LHC injector



- ❑ LHC upgrade considerations require high bunch intensities ( $\geq 1.8 \times 10^{11}$  p/b) with small transverse emittances to be extracted from the SPS
- ❑ Known intensity limitations for LHC proton beams in SPS at present
  - ❑ Instabilities leading to emittance blow up and/or beam loss
    - ❑ TMCI (transverse mode coupling instability) due to transverse impedance  $N_{th} \propto \eta$
    - ❑ Longitudinal instability due to loss of Landau damping,  $N_{th} \propto \eta \epsilon_l^2 \tau$  (stationary bucket)
    - ❑ Longitudinal coupled bunch instabilities due to longitudinal impedance,  $N_{th} \propto \eta \epsilon_l^2 / \tau$
    - ❑ Electron cloud instability (E. Shaposhnikova, Chamonix 2011)
  - ❑ Other limitations
    - ❑ Beam loss (resonances, injection mismatch?)
    - ❑ Beam loading in the RF systems
    - ❑ Heating and out-gassing of machine elements
    - ❑ Space charge
- ❑ Increase in instability thresholds can be expected for the same bunch parameters for higher slippage factor due to faster synchrotron motion ( $\Omega_s \propto \sqrt{|\eta| V_{RF}}$ ) and damping of instabilities

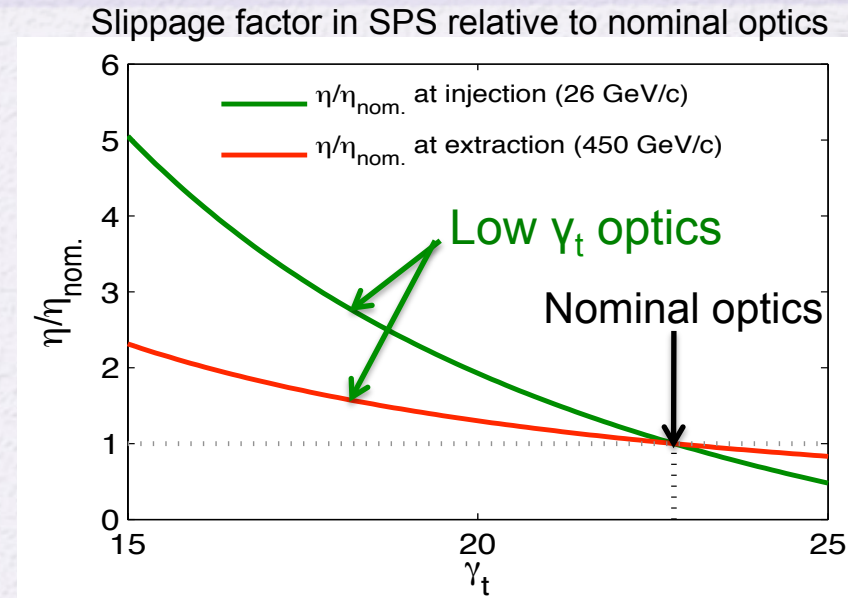
$N_{th}$  ... Instability threshold  
 $\epsilon_l$  ... longitudinal emittance  
 $\tau$  ... bunch length  
 $\eta$  ... slippage factor

# Increasing the slippage factor – lowering transition energy

- Transition energy of “nominal” SPS optics for LHC beams is 22.8 – tunes of (26.13,26.18) through the cycle
- Above transition, slippage factor increases by reducing transition energy (increasing momentum compaction factor)

$$\eta = \frac{1}{\gamma_t^2} - \frac{1}{\gamma^2}$$

- Higher effect @ **injection** (26GeV)
- Smaller but appreciable effect @ **extraction** (450GeV)
- For keeping constant longitudinal emittance, RF-voltage has to be increased accordingly  $V \propto \eta$  (already presently limited for applying controlled longitudinal emittance blow-up at high energies)
- Only partially solved by RF system upgrade



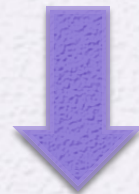
# Transition energy manipulation



- Transition energy (or momentum compaction factor) is defined as

$$\frac{1}{\gamma_t^2} = \alpha_p = \frac{1}{C} \oint \frac{D(s)}{\rho(s)} ds$$

- The higher the dispersion oscillation in the bends, the lower the transition energy



## Quadrupoles

- Note also that, for FODO cells (SPS lattice),  $\gamma_t \approx Q_x$  meaning that lowering the transition energy implies **lowering the horizontal tune**

# Transition energy change in the SPS



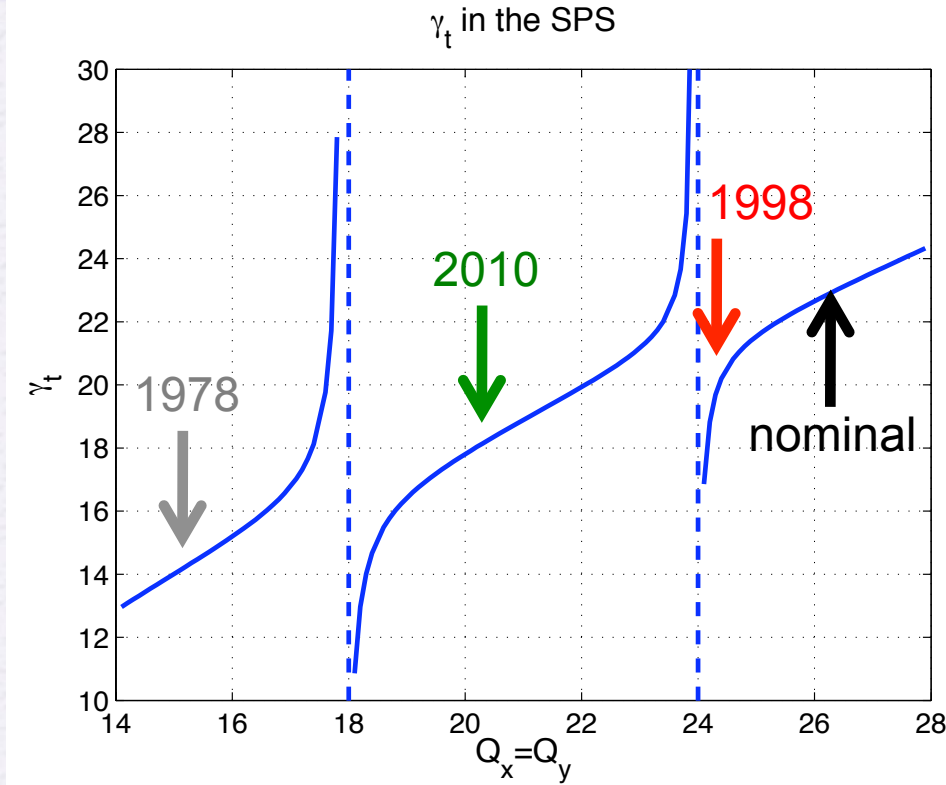
## □ In the past

- Install 2 new quadrupole families in phase advance of  $\mu_x = (2k+1)\pi$  for inducing dispersion waves (K. Cornelis, Chamonix 1999)
  - Tests with “resonant integer tune” of 24 in 1998 demonstrated change of transition energy from 23 to  $\sim 20$ ) (G. Arduini et al. 1998)
  - Reduction of unstable mode amplitudes due to microwave instability (T. Bohl et al., 1998)
  - “Difficult” beam conditions...

## □ New optics studies in 2010

- Flipping quadrupole polarity (from FODOFODO to FODODOFO) for moderate increase in beta functions and notable change in  $\gamma_+$  (requires bipolar power supplies)
- Individually powering central quadrupole of 2 consecutive FODO cells allows to induce dispersion wave for obtaining imaginary  $\gamma_+$  (requires additional power supplies and increased magnet strength)
- For keeping dispersion low in the straights, phase advance of the arcs of the SPS can be reduced to a lower multiple of  $2\pi$  (“resonant arcs”) → increase of dispersion in the arcs (no hardware limitation)

# Transition energy versus SPS working point



Resonant oscillation of dispersion function close to the “Resonant integer tunes” (multiples of super-periodicity 6)  $\rightarrow$  asymptotic behavior of  $\gamma_t$ , (difficult for routine operation)

$\gamma_t$  is linear function of horizontal tune  $Q_x$  elsewhere

- D. Boussard et al., SPS improvement note No 147, 1978; Injection above transition as TT10 was not ready for 26 GeV/c ( $\gamma_t \sim 14$ )
- Low  $\gamma_t$ , 2010 - “Resonant arc” with small dispersion in long straight sections ( $\gamma_t \sim 18$ )
- G. Arduini et al., CERN/SL-Note 98-001, 1998; “Resonant tune” ( $\gamma_t \sim 20$ )
- Nominal SPS working point for LHC proton beams ( $\gamma_t \sim 23$ )

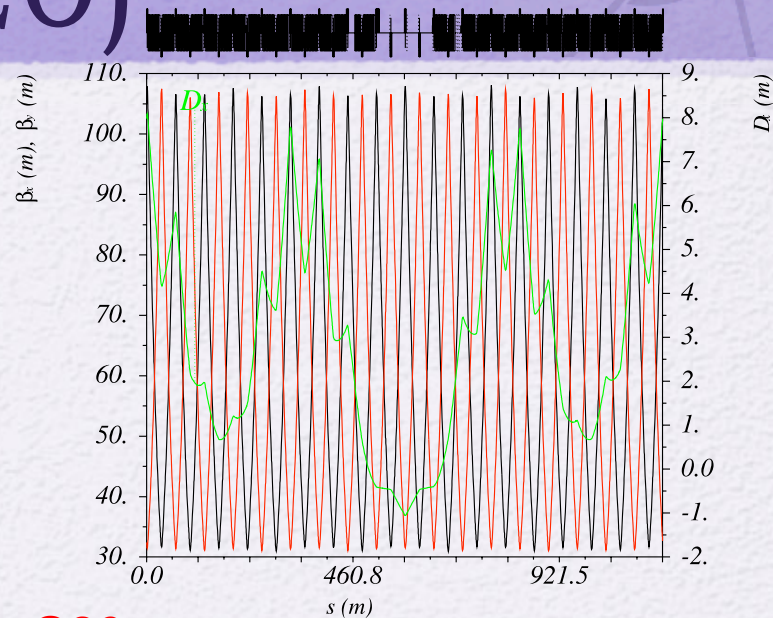




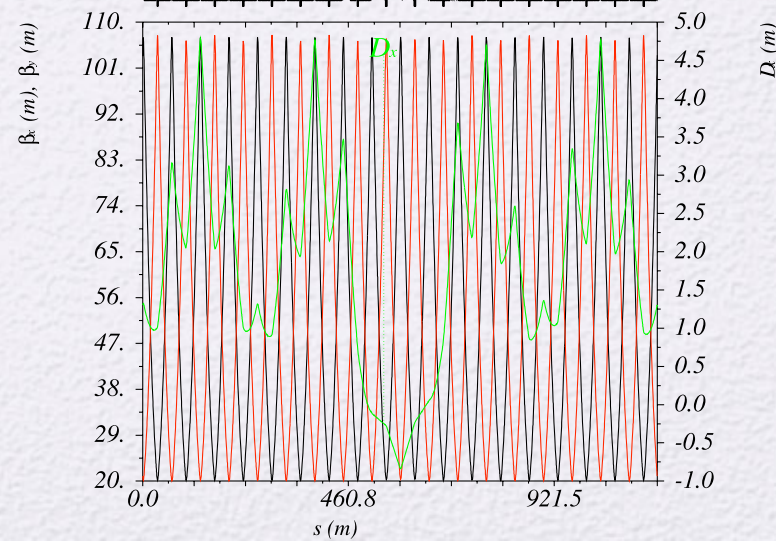
# Low transition energy optics (Q20)

- New optics "Q20" vs. nominal optics "Q26"
  - No increase in maximum  $\beta$ -functions but minimum  $\beta$ -functions increased by 50%
  - Notable reduction in  $\gamma_+$  allows significant increase of  $\eta$  (factor of 2.85 @injection, 1.6 @extraction)!
  - 6 integer tune units below nominal optics  $\rightarrow$  same resonance diagram for systematic resonances (super periodicity of 6)!
  - Comfortable aperture for LHC beams although maximum dispersion almost doubled
  - Slightly increased dispersion in straight section (only small impact on injection/extraction)

Q20:



Q26:



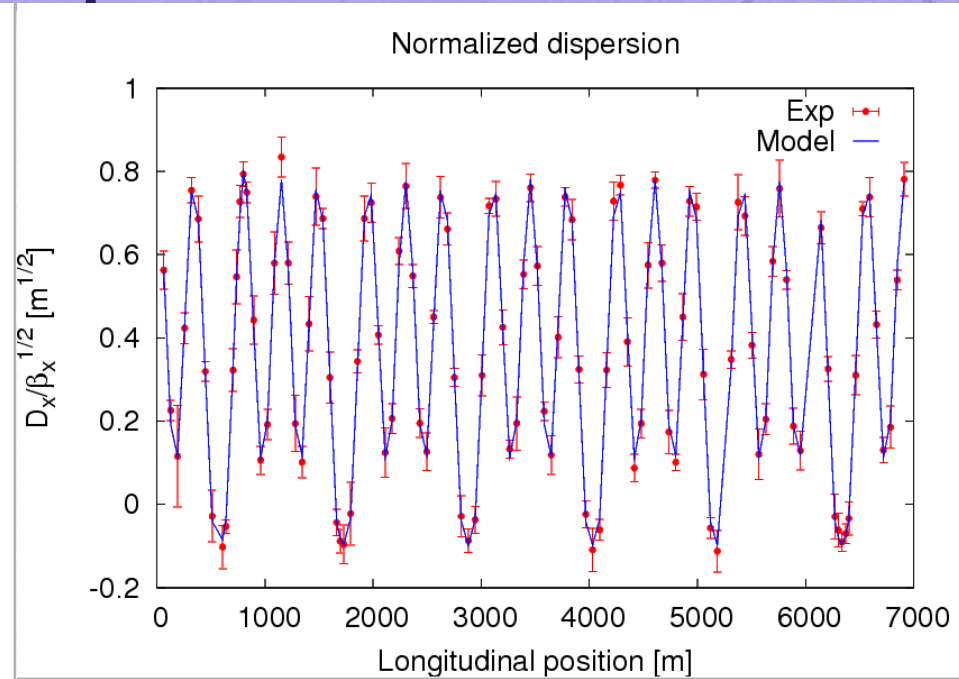
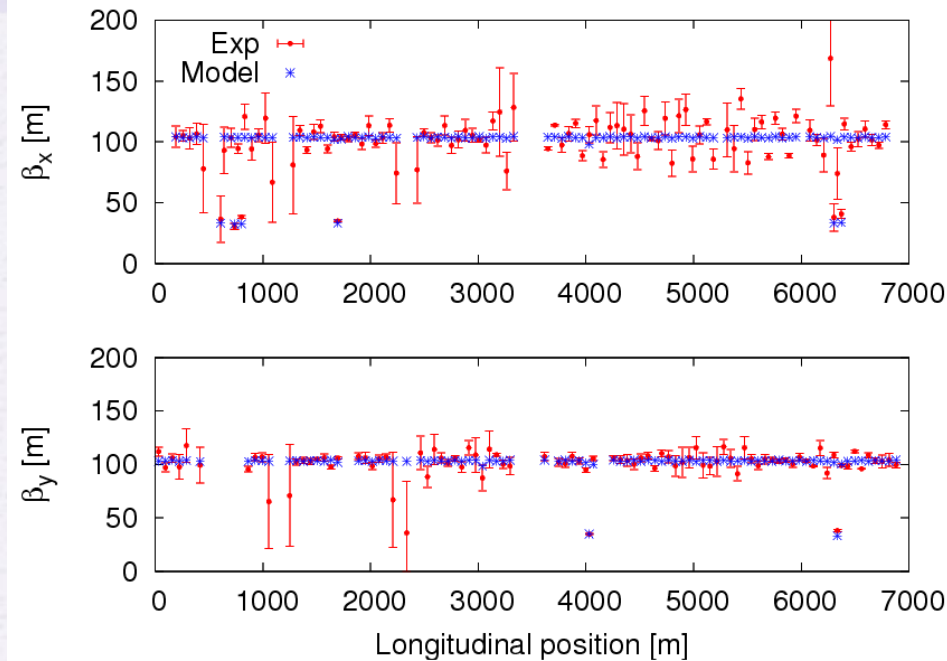
Optics	Q20 (low $\gamma_+$ )	Q26 (nominal)
Working point	(20.13, 20.18)	(26.13, 26.18)
Max. Dispersion	8 m	4.5 m
Max. $\beta$ -functions	105 m	105 m
Min. $\beta$ -functions	30 m	20 m
$\gamma t$	18	22.8
$\eta$ @ 26 GeV/c	1.8E-3	0.63E-3
$\eta$ @ 450 GeV/c	3.1E-3	1.9E-3
Phase advance/cell	$3 * 2\pi / 16$	$4 * 2\pi / 16$

# Machine studies on low transition energy optics



- ❑ Prepared several "Q20" cycles with new optics
  - ❑ Long flat bottom of about 3.7 s before beam is dumped
  - ❑ Short flat bottom of 60 ms and fast acceleration up to 450 GeV
  - ❑ Long flat bottom and slow ramp up to 450 GeV of about 10s each
- ❑ Status
  - ❑ Machine model with integer tunes of 20 entered into the SPS database
  - ❑ New "zero-chromaticity" values for sextupoles and knob parameters defined
  - ❑ RF program slightly adapted from Q26 cycle
  - ❑ Most of the machine controls can be used
  - ❑ Tunes corrected along the ramp for all Q20 cycles
  - ❑ TT2-TT10 transfer-line re-matched but no significant impact yet
  - ❑ Extraction optics and TI2 transfer-line matched and ready for tests

# Experimental confirmation of the new optics



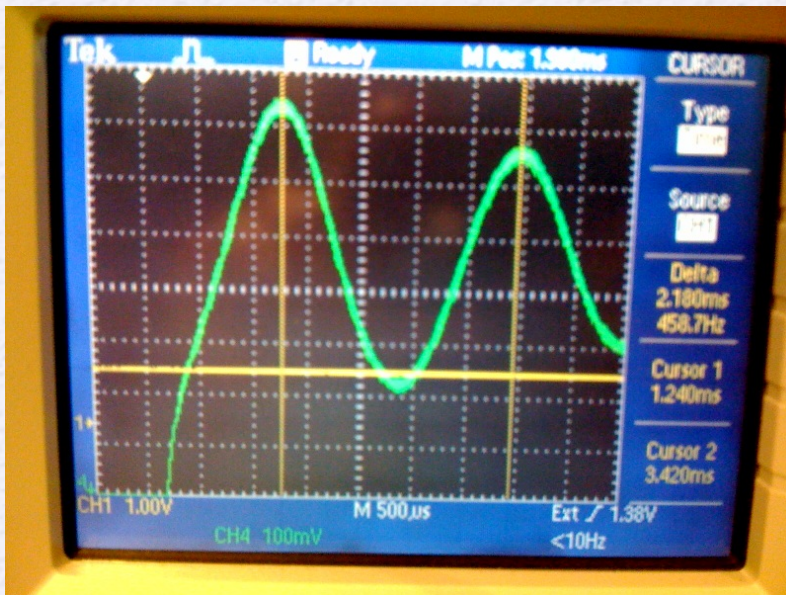
measured by R. Tomas and G. Vanbavinckhove

- Measurement of the optics functions of the new lattice
- Beta beating around 20% in horizontal and 10% in vertical plane
- Normalized dispersion in striking agreement with the model

# Synchrotron frequency

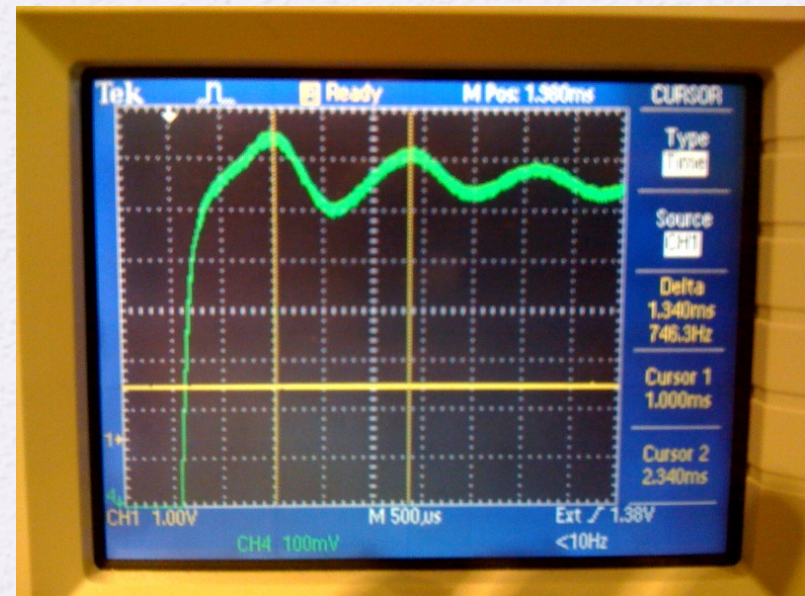


- ❑ Measured synchrotron frequency from “quadrupole” oscillations at injection
  - ❑ Same RF-voltage for both optics
  - ❑ “Over-focusing” RF-bucket in both cases
- ❑ Ratio of Synchrotron frequencies  $\sim 1.63$  corresponds to an **increase in slippage factor  $\eta$  by factor 2.65** (MADX prediction: 2.86)



Q26:

$$F_s = 458/2 = 229\text{Hz}, \quad Q_s = 0.0106/2 = 0.0053$$



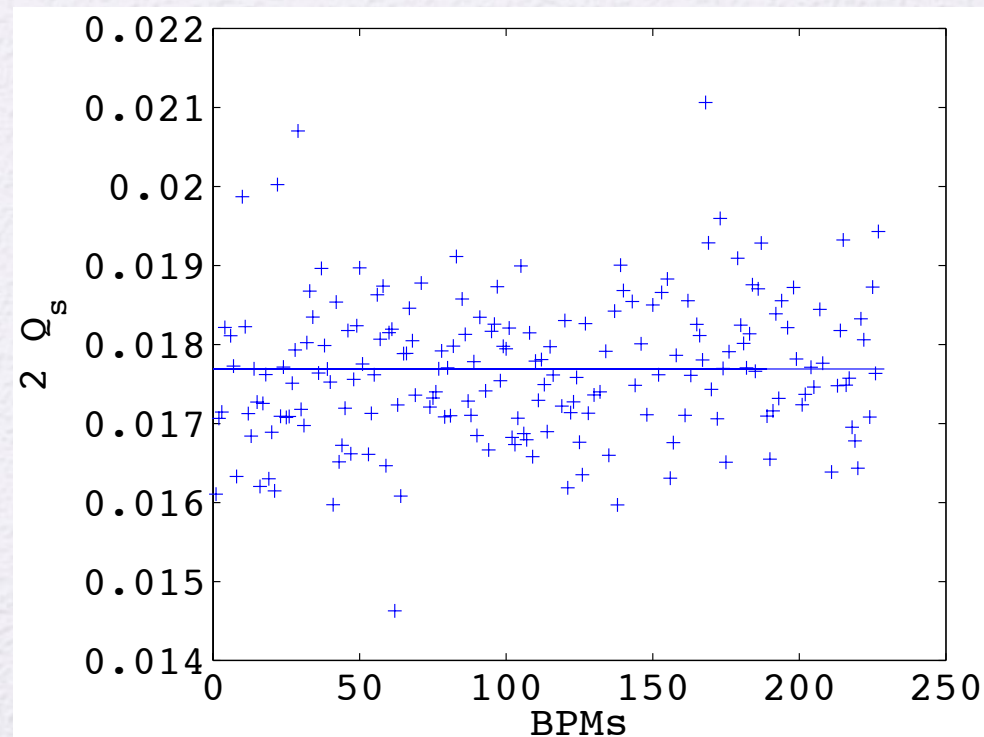
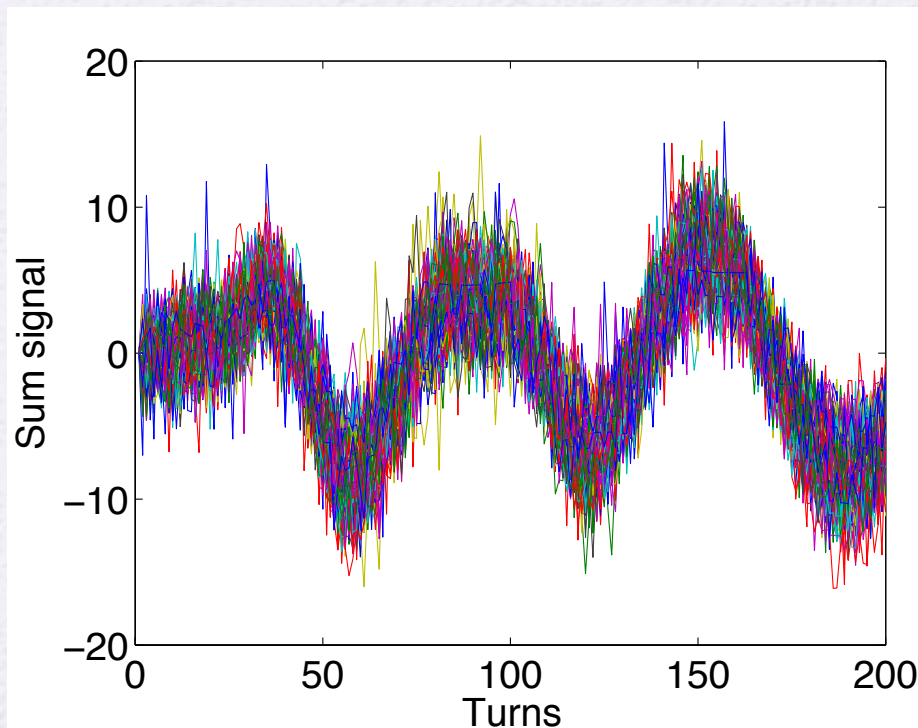
Q20:

$$F_s = 746/2 = 373\text{Hz}, \quad Q_s = 0.0172/2 = 0.0086$$

# Synchrotron frequency: an alternative method



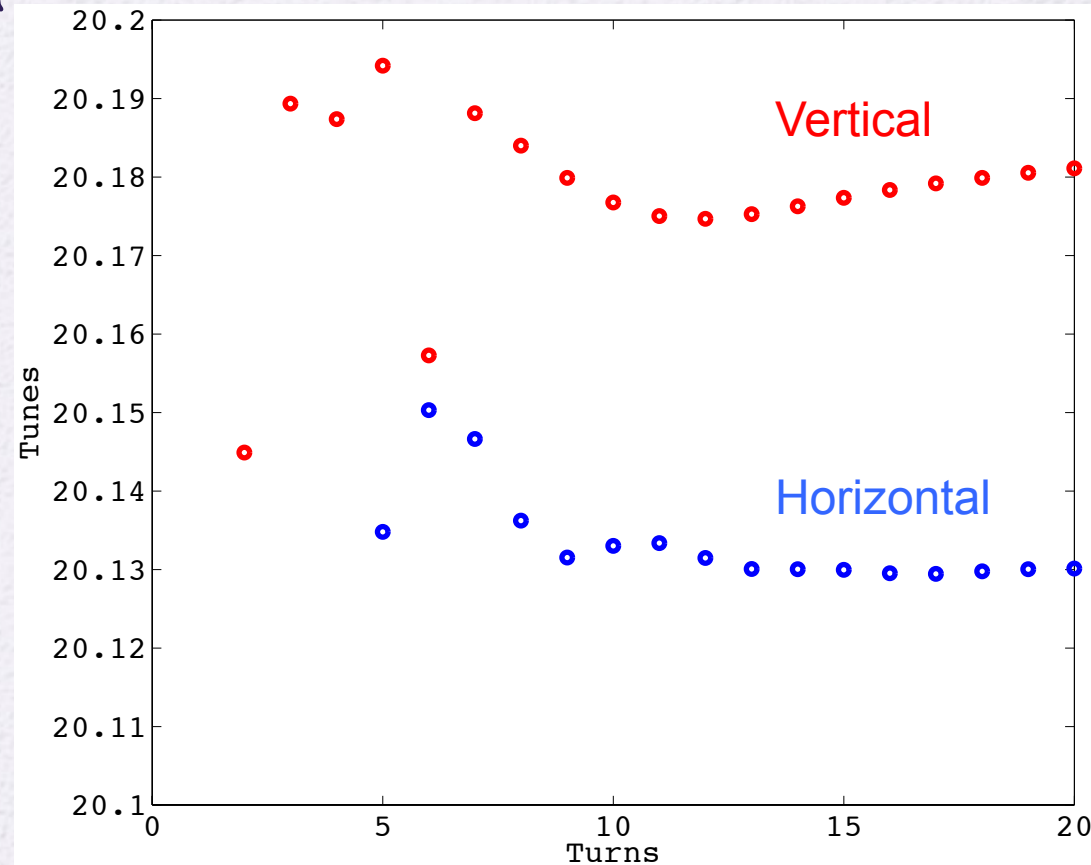
- Recording sum signal from turn-by-turn BPM system @ injection
- Estimating synchrotron tune by refined Fourier analysis (NAFF)
- Average of  $2Q_s = 0.0176 \pm 0.0009$



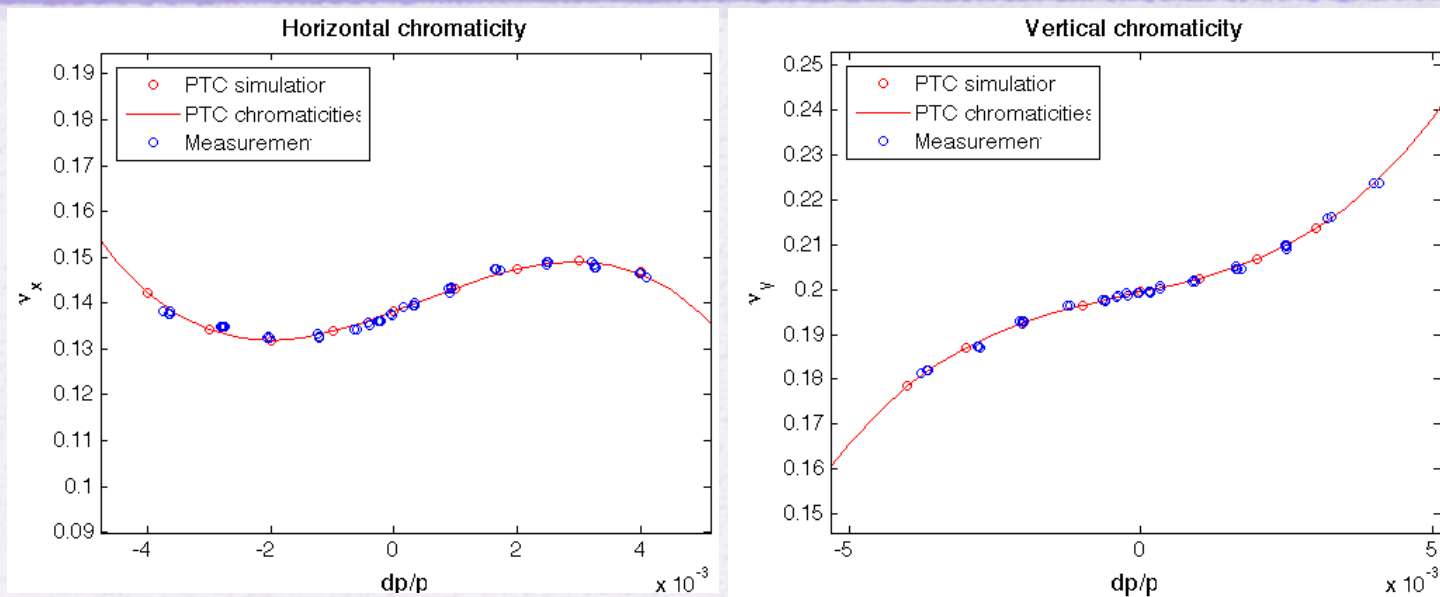


# Fast tune determination

- Combining turn-by-turn positions for all BPMs within a turn
- Analyzing all data for a number of turns with NAFF
- Convergence to the tune (including the integer!) in 15-20 turns, even for 20% of the BPMs failing
- Completely model independent
- Overcome decoherence (or evaluate the tune dependence on it)
- A rapid way to measure tune-shift with amplitude or chromaticity



# Nonlinear chromaticity in the new lattice



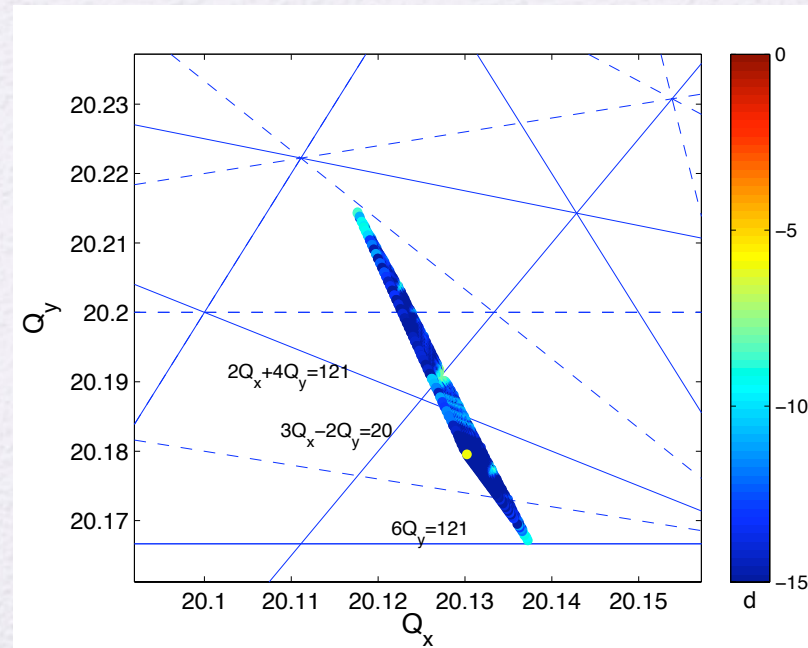
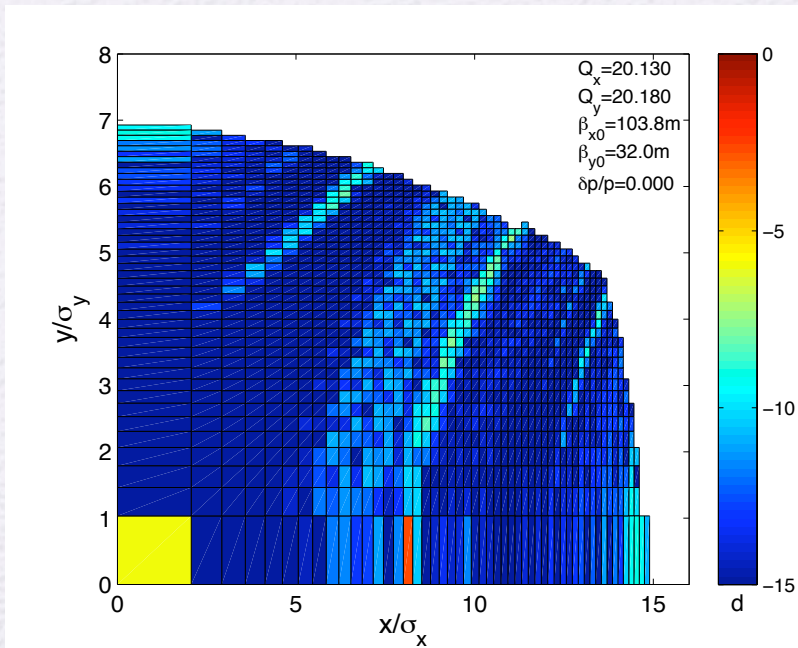
(see previous work  
G. Arduini et al.  
PAC2005)

- ❑ Sextupole strengths set with new chromaticity knobs; measurement with low intensity bunch
- ❑ MADX-PTC nonlinear model of SPS adapted/fitted to the measurements on new optics and compared with measurements on nominal optics
  - ❑ Sextupole components in dipoles in rough agreement between Q20 and Q26
  - ❑ Octupole components (assumed to be located in quadrupoles) change sign from Q20 to Q26 model!
  - ❑ Decapole components in dipoles in rough agreement between Q20 and Q26
- ❑ Chromaticity sextupole strengths needed are much smaller (1/3) in Q20 optics due to: smaller natural chromaticity, much bigger dispersion function at sextupole locations, partial compensation of chromaticity due to sextupole components of main dipoles
- ❑ On-going studies including tune-shift with amplitude and higher order chromaticity term measurements as additional nonlinear fit parameters

# Nonlinear dynamics simulations



- Nonlinear model as obtained from the measurement of nonlinear chromaticity
  - Assumed misalignments, random errors in the main components and random errors in the multipole components such that the measured nonlinear chromaticity is reproduced (rms orbit  $\approx 2\text{mm}$ ,  $\beta$ -beat  $\approx 10\%$ )
  - Dynamic aperture much bigger than physical aperture
- Frequency map analysis allows to visualize the tune-shift with amplitude and to identify resonances
  - Tracking particles with PTC in 5D with initial conditions in configuration space evenly spaced in action
  - Aperture model included in the simulation
  - Color-code indicates the tune diffusion coefficient  $d$  in logarithmic scale,  $d = \sqrt{(\nu_{x,1} - \nu_{x,2})^2 + (\nu_{y,1} - \nu_{y,2})^2}$
  - Big diffusion coefficient  $d$  means chaotic motion in phase space
  - $\sigma$  (beam size) is calculated for on-momentum particles with normalized emittance  $\varepsilon_x = \varepsilon_y = 3 \mu\text{m}$

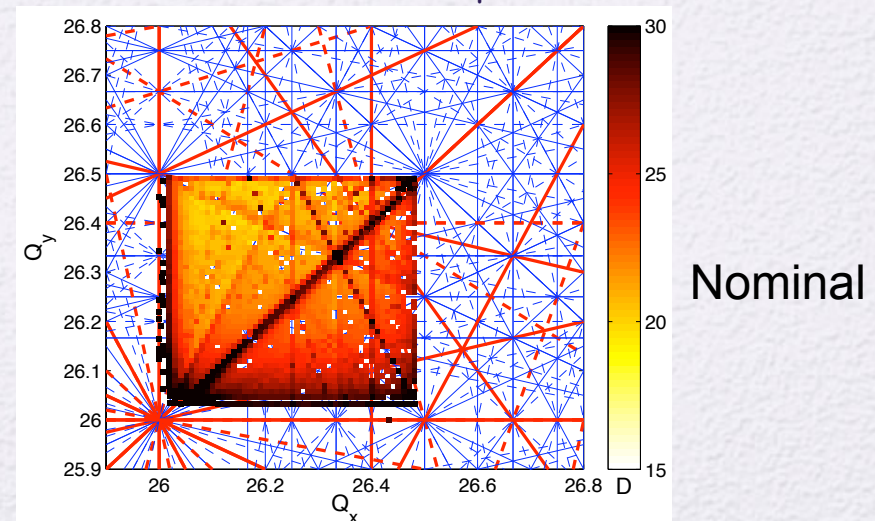
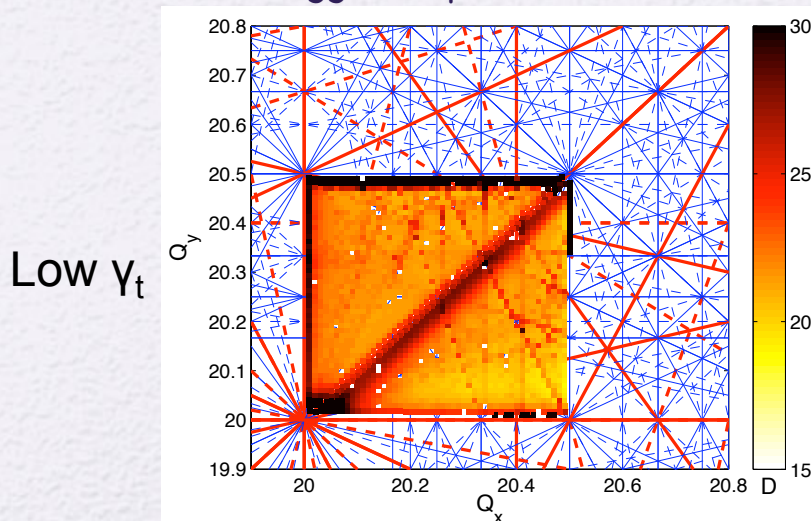




# Nonlinear dynamics simulations (cont.)



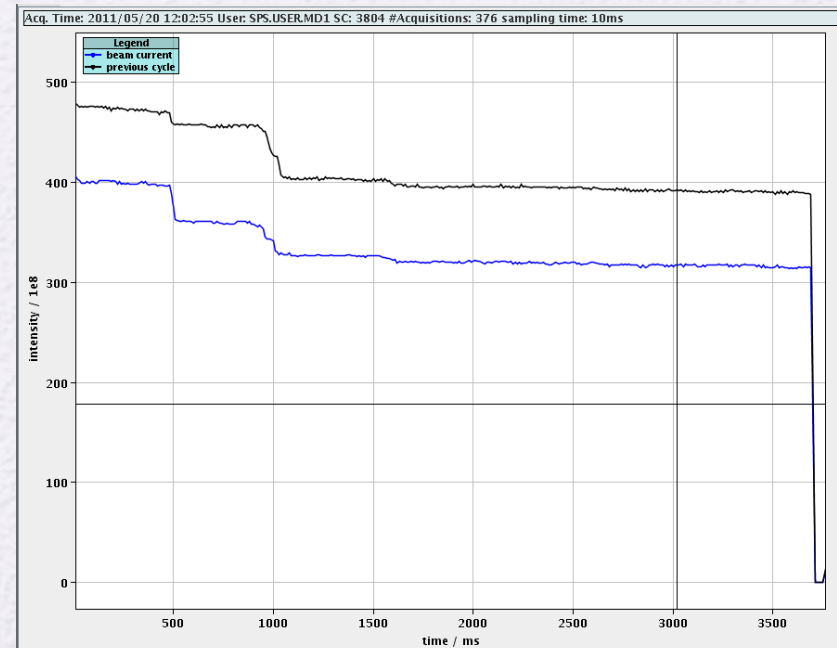
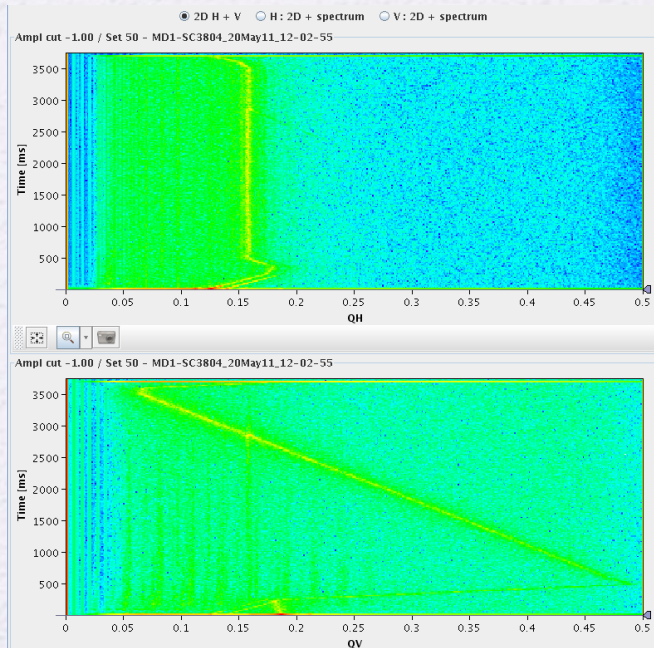
- Tune-scan for a global picture of machine resonances
  - Frequency Map produced for each working point and diffusion coefficients' sum for all particles (D) is computed
  - For direct comparison, same nonlinear model (Q20) assumed for both optics variants
  - Orbit corrected (rms orbit  $\approx 2\text{mm}$ ,  $\beta$ -beat  $\approx 10\%$ ) before changing the tune
  - Chromaticity corrected to  $\xi_x = \xi_y = 0.1$  using sextupole "knobs" of the corresponding case
  - Coupling not corrected, octupoles are always switched off
- Observations
  - Same resonances can be identified in both cases
  - Resonances appear to be stronger in the nominal optics, especially the third order ones  $\rightarrow$  Modified phase advance between chromatic sextupole families in low  $\gamma_t$  optics seems not to be an issue
  - Note the bigger stop-band widths for the integer resonances in the nominal optics





# Experimental Tune scans – Method\*

- ❑ Study the resonance behavior around working points of nominal and low  $\gamma_+$  (Q20) optics @ injection
- ❑ **Strength of individual resonance lines can be identified from the beam loss rate**, i.e. the derivative of the beam intensity at the moment of **crossing the resonance**
- ❑ Vertical tune is scanned from about 0.45 down to 0.05 during a period of 3s along the flat bottom
- ❑ Low intensity 4-5e10 p/b single bunches with  $\varepsilon \sim 1.2 \mu\text{m}$  (“single particle behaviour”) injected at nominal tunes
- ❑ Horizontal tune is constant during the same period within a super-cycle (scanned from cycle to cycle)
- ❑ Tunes are continuously monitored using the BBQ (tune post-processed with NAFF) and the beam intensity is recorded with BCT



\* See also method from G. Franchetti et al. in the PS

# Tune Scans - Results



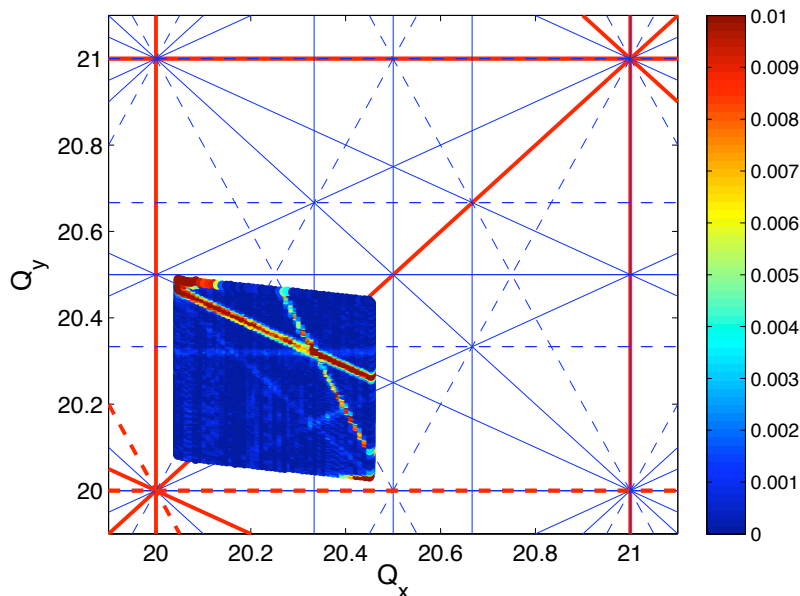
## Resonances in the low $\gamma_+$ optics

- Normal sextupole  $Q_x+2Q_y$  is the strongest
- Skew sextupole  $2Q_x+Q_y$  quite strong !!??
- Normal sextupole  $Q_x-2Q_y$ , skew sextupole at  $3Q_y$  and  $2Q_x+2Q_y$  fourth order visible

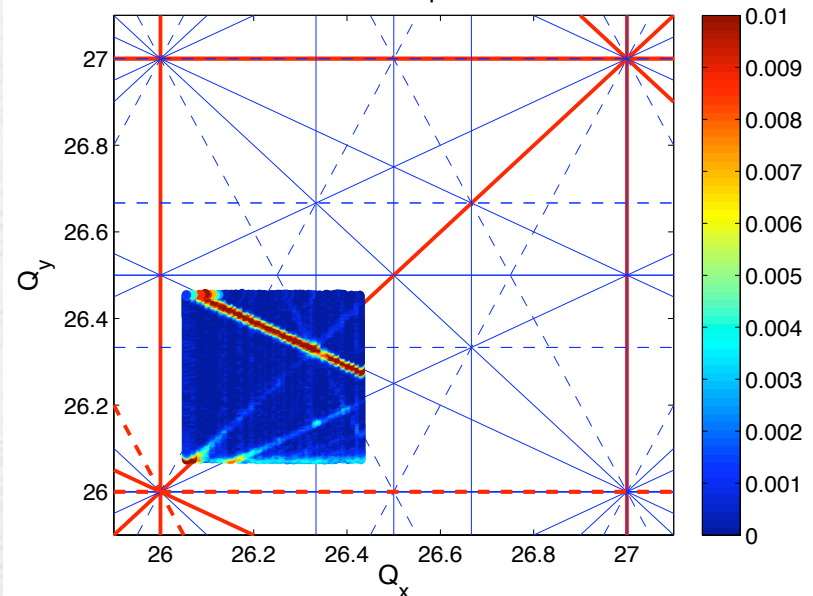
## Resonances in the nominal optics

- Normal sextupole resonance  $Q_x+2Q_y$  is the strongest
- Coupling resonance (diagonal, either  $Q_x-Q_y$  or some higher order of this),  $Q_x-2Q_y$  normal sextupole
- skew sextupole resonance  $2Q_x+Q_y$  weak compared to Q20 case
- Stop-band width of the vertical integer is stronger than in Q20 optics, as predicted by simulations

Low  $\gamma_t$  optics



Nominal Optics

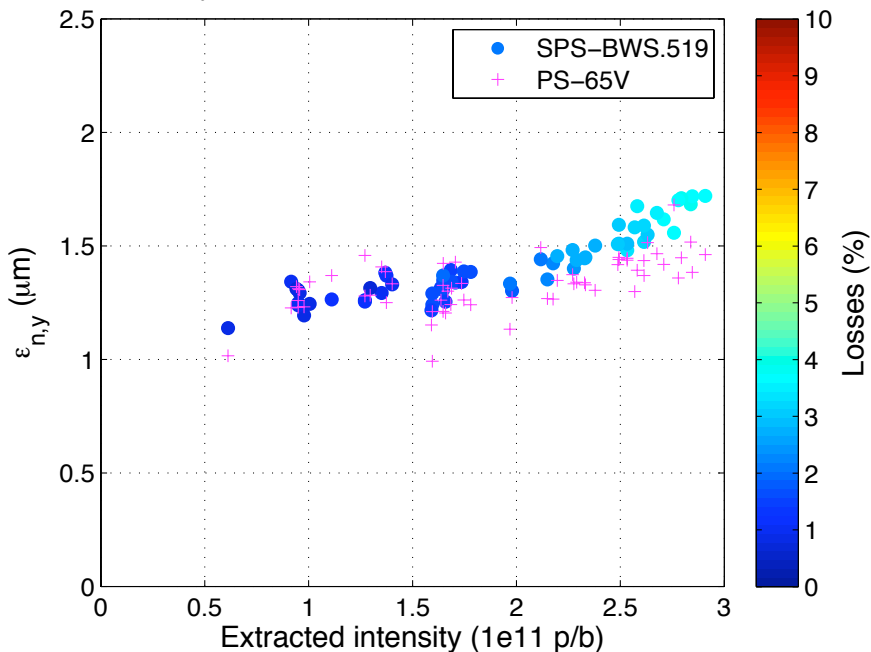




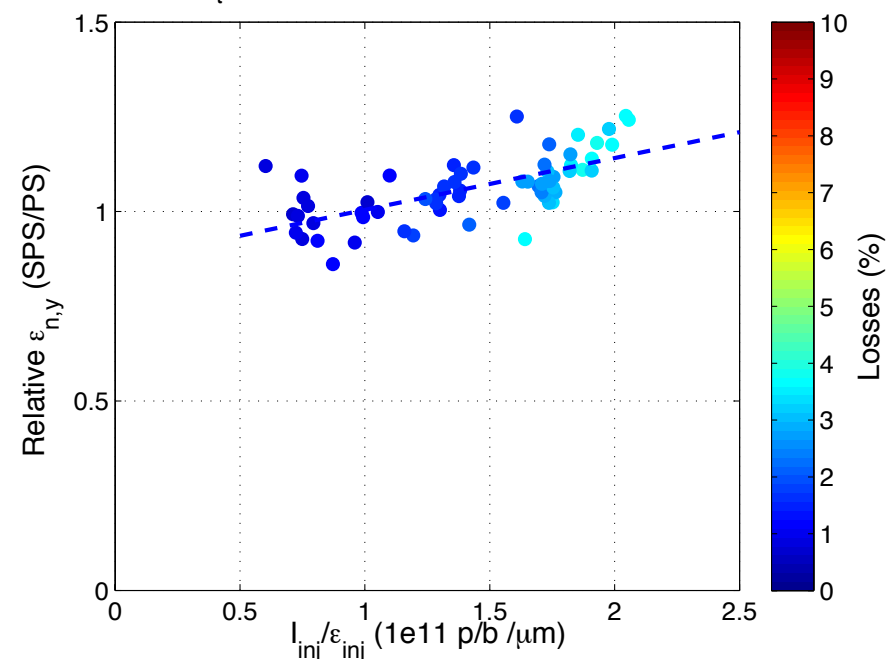
# Emittance vs intensity

- Beams injected and accelerated in single and multi-bunch mode up to top energy without any significant emittance degradation or losses
- Large effort to quantify SPS emittance blow-up for high-intensity single bunches
- Simultaneous measurements of vertical emittance in PS and SPS
  - At extraction (just before bunch rotation) in PS and end of flat bottom in SPS
- Emittance blow-up for intensities  $>1.5e11$  p/b with peak values of 25% at  $3e11$  p/b

Low  $\gamma_t$  optics – end of flat bottom (26 GeV/c)



Low  $\gamma_t$  optics – end of flat bottom (26 GeV/c)



# Beam loss @ flat bottom



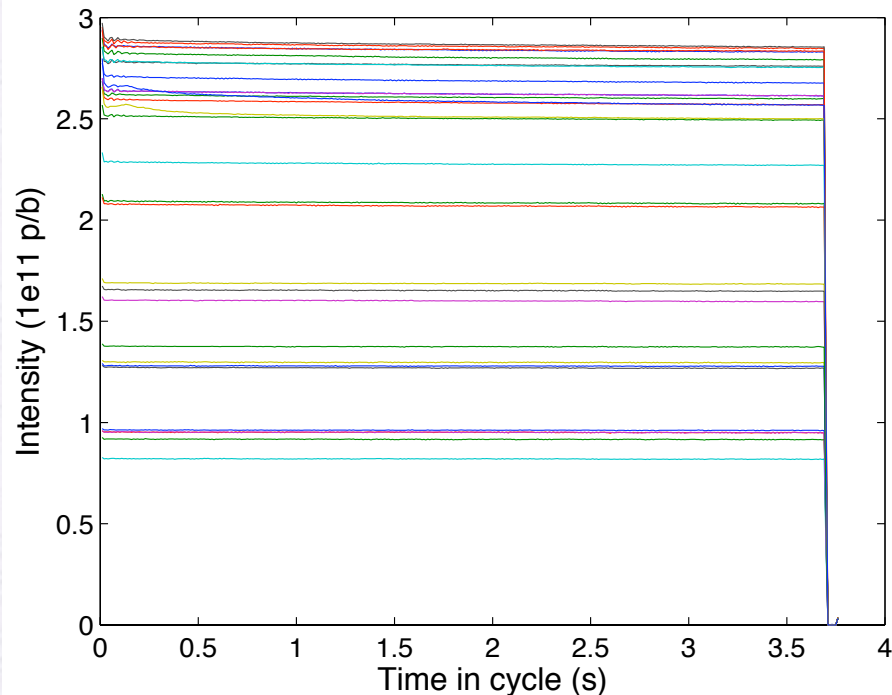
## Low $\gamma_t$ optics

- Low losses (up to 4% for 3e11 p/b) from injection to end of flat bottom
- Flat intensity profiles even for high intensity but injection losses increase

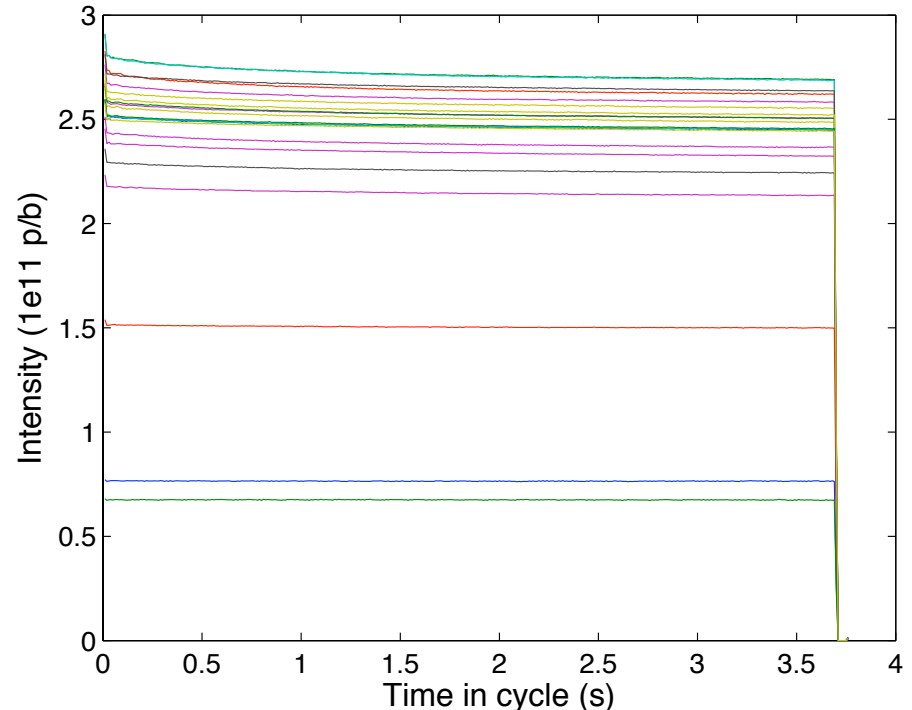
## Nominal optics

- Significantly increasing losses for intensities above 2.5e11 p/b up to 10%
- Losses at injection and along the flat bottom for high intensities

Intensity profiles – low  $\gamma_t$  optics



Intensity profiles – Nominal optics

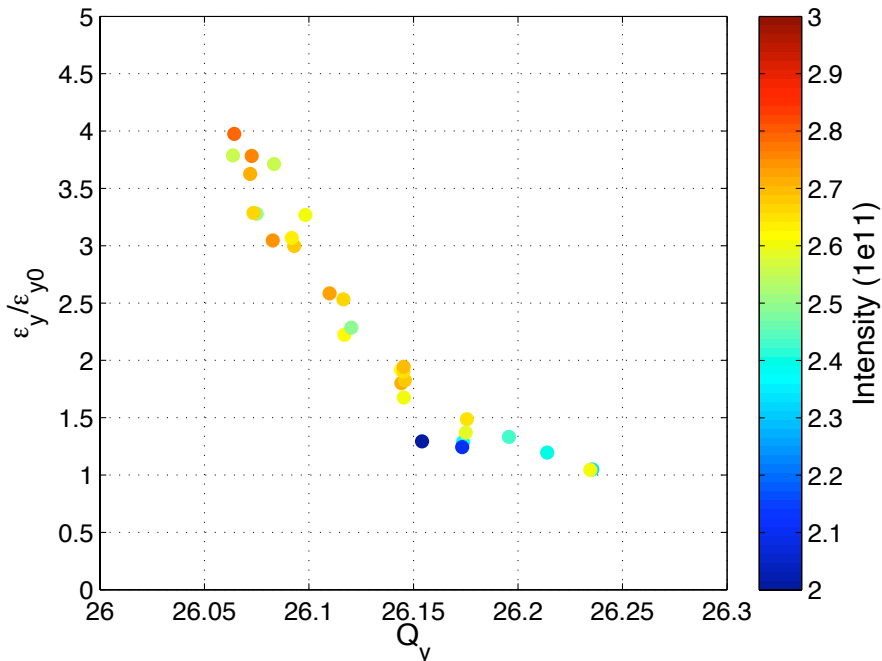


# High intensity tune scan

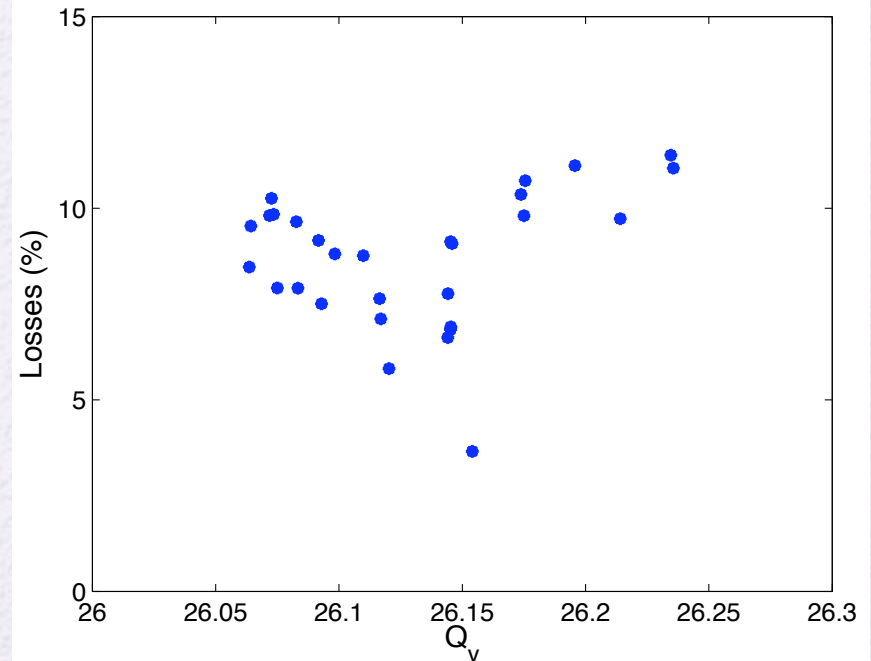


- Tune scan with high intensity small emittance single bunches
  - “Space charge” tune scan with intensities of  $\sim 2.5\text{--}3e11$  p/b and injected norm. emittances of  $1.3\text{--}1.5\ \mu\text{m}$
  - Measuring emittance at flat bottom end as function of injected emittance and total losses
  - First scan of vertical tune with fixed horizontal tune of  $Q_x \sim 26.18$
  - To be completed with further scans for different horizontal tune settings

Scan of vertical tune ( $Q_x=26.18$ ) – Nominal optics



Losses for vertical tunescan ( $Q_x=26.18$ ) – Nominal optics



# Summary and perspectives



- ❑ New low transition energy optics proposed and implemented in SPS for machine studies during 2010–2011, showing promising results
  - ❑ Single bunches injected and accelerated successfully **with intensities up to  $3.3 \times 10^{11}$  p/b**
  - ❑ **No clear triggering of TMCI instability** even for low chromaticity settings with only small emittance blow-up
  - ❑ **Transverse emittances below  $2.5 \mu\text{m}$**  at the end of a long cycle for single bunches with intensities of  $3 \times 10^{11}$  p/b with moderate losses
  - ❑ **Multi-bunch injection (12 bunches)** and acceleration for nominal LHC transverse characteristics
  - ❑ Yet another attempt to build a **non-linear machine model** for SPS and working point optimization for high intensity
- ❑ Ongoing studies and questions
  - ❑ Emittance blow-up for high intensity single bunches in both optics (“space charge limit”)
  - ❑ Setup of extraction for new optics to LHC
  - ❑ Large simulation effort for qualifying the impact on instabilities, e-cloud, space charge
  - ❑ **Reaching acceptable LHC beam parameters with the available RF-voltage?**
  - ❑ **Experimental confirmation of expected stability improvement for multi-bunch beams (LHC bunch trains)?**