

# Optics measurements of TOTEM

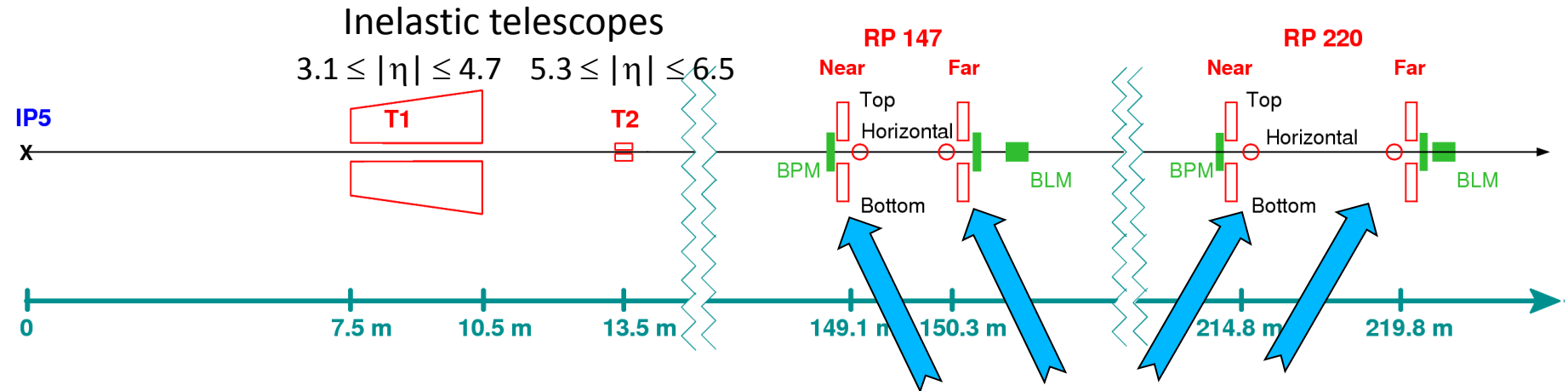
7 sigma runs ( $\beta^*=3.5\text{m}$ ) on 30/10/2010

Hubert Niewiadowski

Optics Measurements, Corrections and Modelling for High-  
Performance Storage Rings workshop (OMCM)

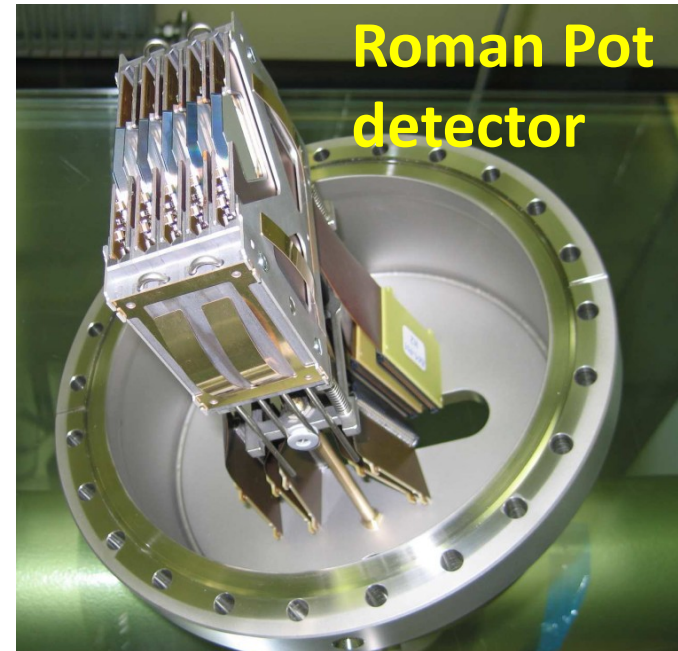
CERN, 20-23.06.2011

# TOTEM Roman Pots in the LHC



## TOTEM Roman Pots

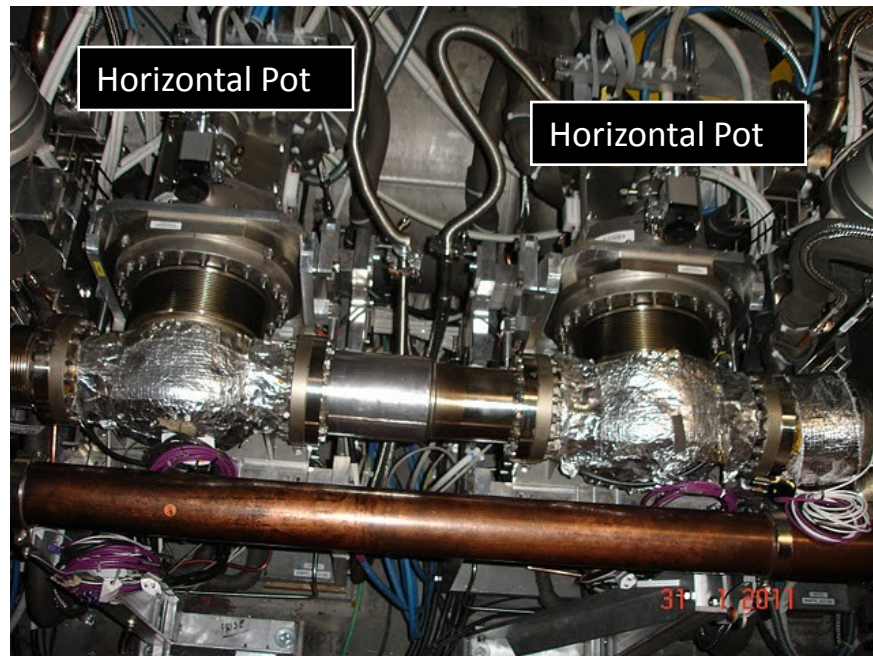
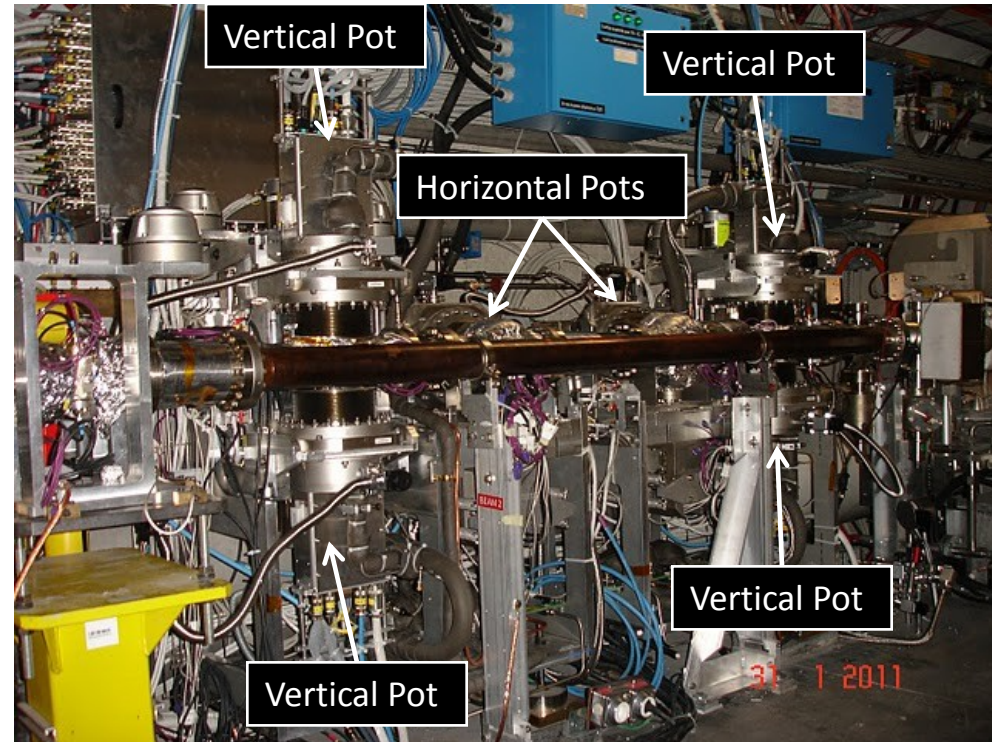
- 4 stations @  $s \approx \pm 147$  and  $s \approx \pm 220$  m
  - 6 Roman Pots per station (4 vertical + 2 horizontal)
- A total of 24 Roman Pots



# Roman Pot station outlook

- **High spatial resolution of track reconstruction**

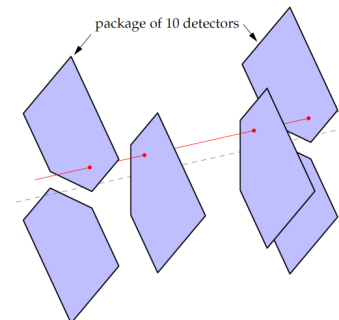
- $\sigma(x)=\sigma(y)\approx 13\mu\text{m}$
- $\sigma(\theta_x)=\sigma(\theta_y)\approx 3.7\mu\text{rad}$



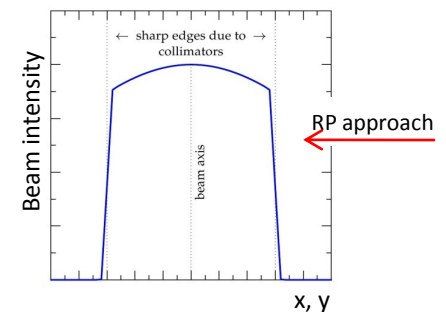
( $s\sim 147\text{m}$  from IP5)

## Precise detector alignment

Track based alignment:  $\sim 5\mu\text{m}$

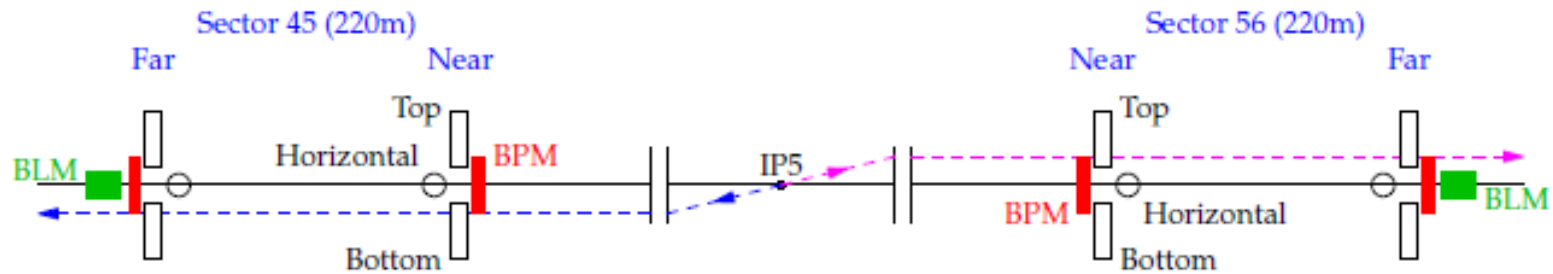


Beam touching alignment:  $\sim 20\mu\text{m}$



# Elastic protons for optics diagnosis

7 sigma runs on 30/10/2010



## Transport IP5→RP220

$$\left. \begin{array}{l} \text{Measured} \\ \text{in Roman} \\ \text{Pots} \end{array} \right\} \begin{pmatrix} x \\ \Theta_x \\ y \\ \Theta_y \\ \Delta p/p \end{pmatrix}_{\text{RP}} = \begin{pmatrix} v_x & L_x & 0 & 0 & D_x \\ v'_x & L'_x & 0 & 0 & D'_x \\ 0 & 0 & v_y & L_y & 0 \\ 0 & 0 & v'_y & L'_y & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x^* \\ \Theta_x^* \\ y^* \\ \Theta_y^* \\ \Delta p/p \end{pmatrix}_{\text{IP5}} \right\} \text{Reconstructed}$$

- **Elastically scattered protons:**

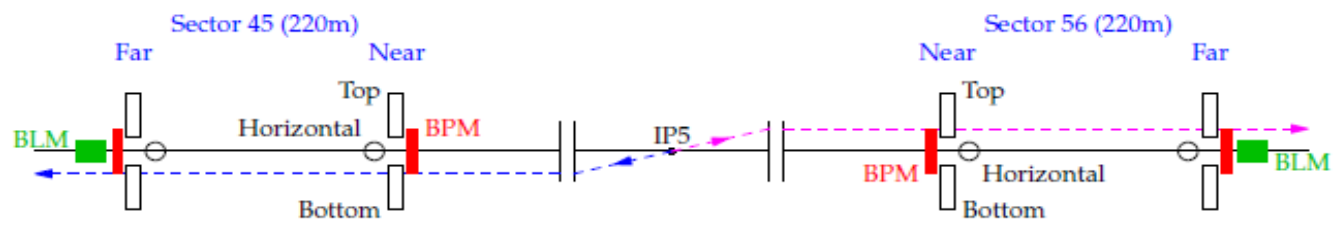
- Can be easily tagged
- Pair of collinear protons:  $\Theta_{\text{left}}^* = \Theta_{\text{right}}^*$  (within beam divergence)
- No momentum loss:  $\xi = \Delta p / p = 0$  (within beam momentum spread)
  - Dispersion and tune change eliminated

- **$\beta^*=3.5\text{m}$  optics:**

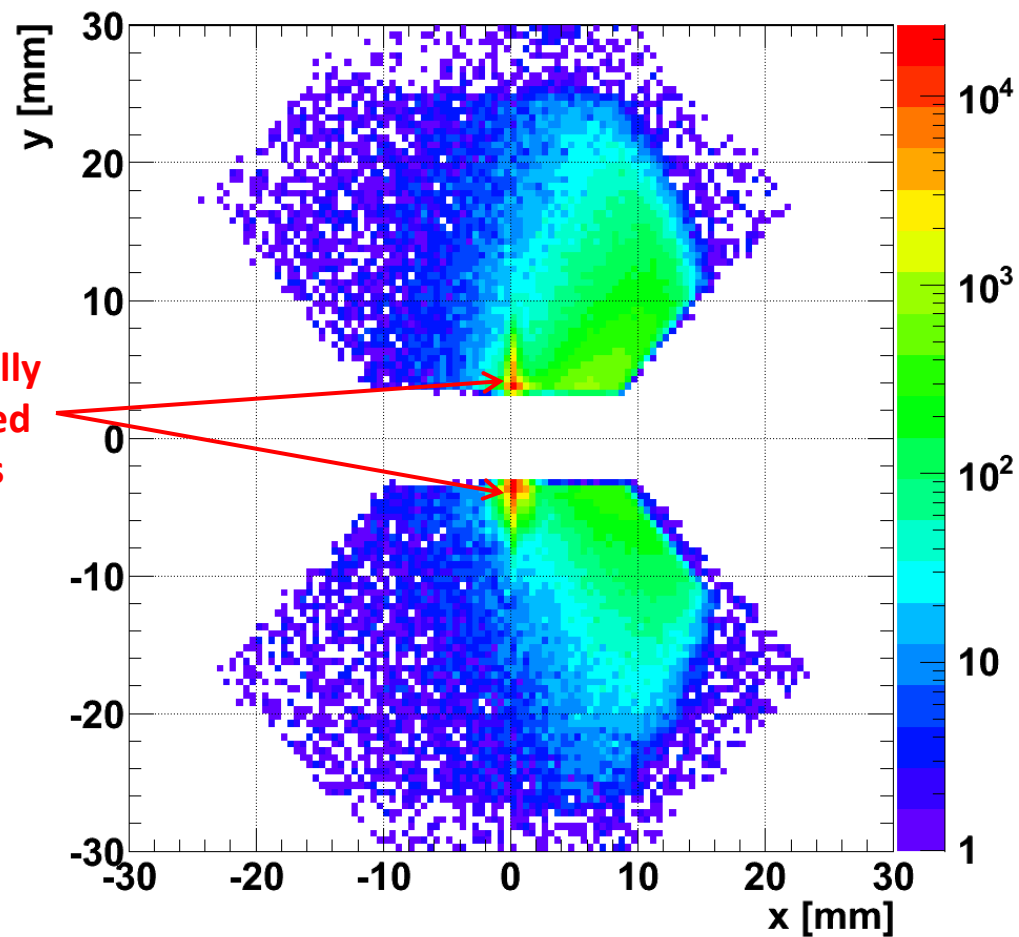
- Beam size @ IP5:  $59\mu\text{m}$ , its impact eliminated by antisymmetric event topology
- @  $s=220\text{m}$  :  $L_x \approx 0$ ,  $L_y \approx 20\text{m}$

# Proton tracks of a single diagonal

(left-right coincidences)



Sector 56



Elastically scattered protons

Sector 45

$$t = -p^2 \theta^2$$

$$\xi = \Delta p/p$$

$$y = L_y \Theta_y$$

$$x = L_x \Theta_x + \xi D$$

$$L_x \sim 0$$

For details on elastic proton selection see backup slides

# Elastic proton reconstruction

- Elastic proton reconstruction:

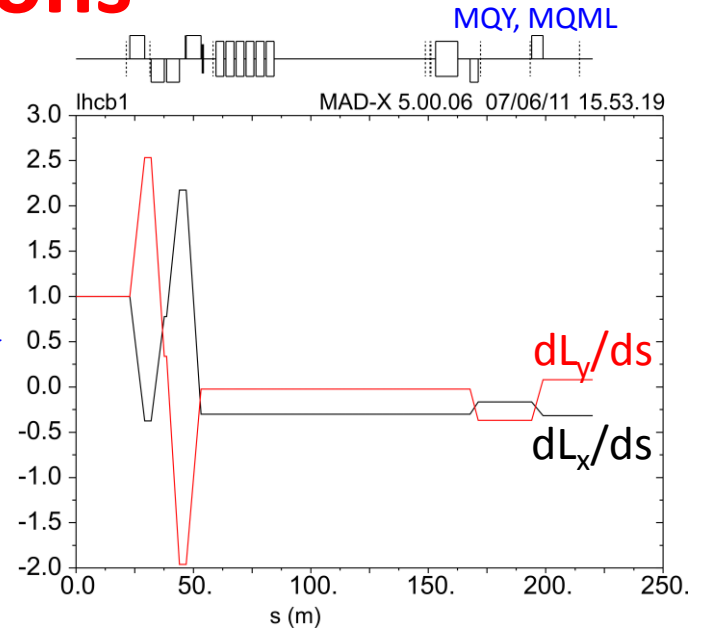
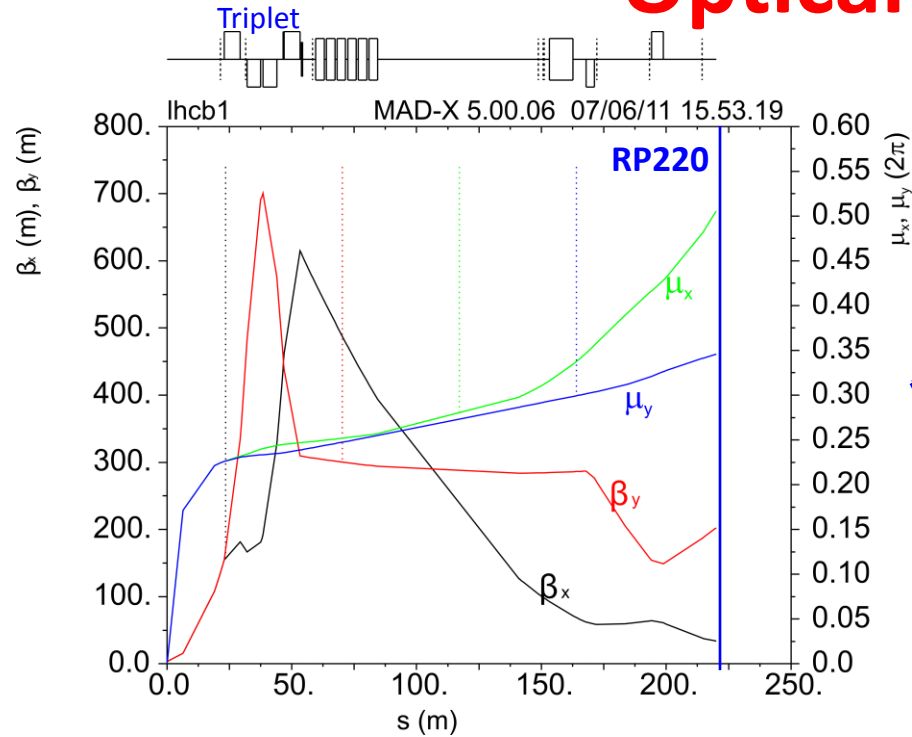
$$\text{Per arm: } \left\{ \begin{array}{l} \Theta_{x,\text{arm}}^* = \Theta_{x,\text{arm},\text{RP220}} / \frac{dL_{x,\text{arm}}}{ds} \\ \Theta_{y,\text{arm}}^* = y_{\text{arm},\text{RP220}} / L_{y,\text{arm}} \end{array} \right.$$

$$\text{Arms averaged: } \left\{ \begin{array}{l} \Theta_x^* = (\Theta_{x,45}^* + \Theta_{x,56}^*) / 2 \\ \Theta_y^* = (\Theta_{y,45}^* + \Theta_{y,56}^*) / 2 \end{array} \right.$$

$$\text{Finally: } t = -p^2 (\Theta_x^{*2} + \Theta_y^{*2})$$

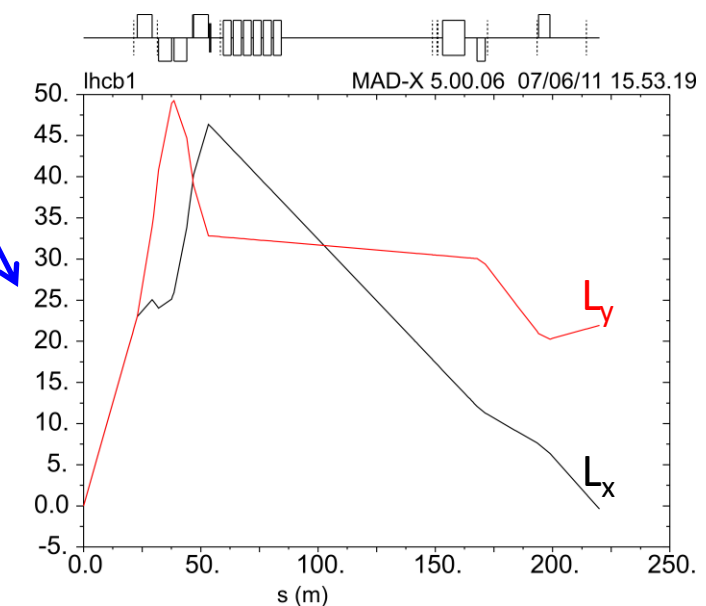
- Precise values of  $dL_x/ds$  and  $L_y$  @ RP locations needed!
  - enough to have the values, sources of errors of less importance for TOTEM
  - $\beta$ -measurement based estimations give the error of 5–10%
- Can we measure them with the proton tracks?
- What are the sources of optics imperfections in the range of interest?

# Optical functions



Inner triplet determines  $dL_x/ds$  and  $dL_y/ds$  for  $s=50..220$ m

$$\begin{cases} L_{x,y}(s) = \int_0^s \frac{dL_{x,y}(\hat{s})}{d\hat{s}} d\hat{s} + C_1 \\ \frac{dL_{x,y}(s)}{ds} = \int_0^s L_{x,y}(\hat{s}) k(\hat{s}) d\hat{s} + C_2 \end{cases}, \text{ with } \begin{cases} L_{x,y}(0) = 0 \\ \frac{dL_{x,y}}{ds}(0) = 1 \end{cases}$$



# Optics perturbation in IP5

k change by 0.1% (expected limit for the TF error)

Perturbed magnets BEAM 1	BETX	BETY	MUX	MUY	$v_x$	$v_y$	$L_x$	$L_y$	$dL_x/ds$	$dL_y/ds$	$s : L_x=0$	$\Delta s : L_x=0$ [m]
Nom. MADX solution (TIMBER Oct 30 2010)	33.7m	208m	0.502 $\cdot 2\pi$	0.344 $\cdot 2\pi$	3.10	4.28	-0.132m	22.4m	-0.321	0.086	220m	
MQXA.1R5	0.29%	1.24%	0.31%	-0.25%	0.13%	-0.20%	<b>79.59%</b>	0.98%	-0.46%	3.20%	-0.15%	-0.331
MQXB.A2R5	-0.14%	-2.83%	-0.25%	0.57%	-0.07%	0.37%	<b>-64.86%</b>	<b>-2.24%</b>	0.33%	-7.46%	0.12%	0.268
MQXB.B2R5	-0.13%	-3.08%	-0.37%	0.60%	-0.06%	0.36%	<b>-96.49%</b>	<b>-2.42%</b>	0.45%	-8.13%	0.18%	0.398
MQXA.3R5	0.33%	1.91%	1.00%	-0.34%	0.08%	-0.18%	<b>259.35%</b>	1.45%	<b>-1.14%</b>	4.95%	-0.49%	<b>-1,086</b>
MQY.4R5.B1	0.07%	-0.17%	-0.01%	0.01%	0.03%	-0.05%	<b>-3.83%</b>	-0.10%	-0.02%	-0.64%	0.01%	0.016
MQML.5R5.B1	-0.12%	0.09%	0.01%	0.00%	-0.06%	0.04%	<b>2.80%</b>	0.05%	0.05%	0.54%	-0.01%	-0.011

t-reconstruction

- Only inner triplet really important
- MQY, MQML not really important
- Roman Pot measurements can be used for optics matching



# Optics determination

## Measurements with Roman Pots:

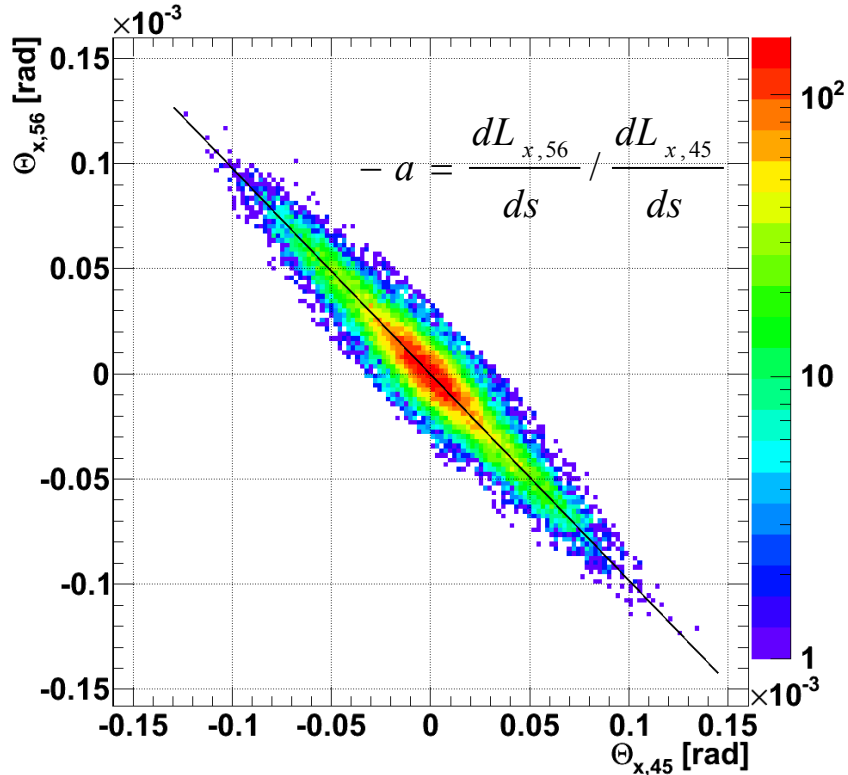
- $\frac{dL_{x,56}}{ds} / \frac{dL_{x,45}}{ds}$
  - $L_{y,56} / L_{y,45}$
  - $\frac{dL_y}{ds} / L_y \Big|_{s=\pm 220}$
  - $s : L_x(s) = 0 \Big|_{s \approx \pm 220}$
  - $x \leftrightarrow y$  coupling  $\Big|_{s=\pm 214, \pm 220} (re_{14} / L_y, re_{14} = \frac{x_{RP220}}{\Theta_y^*})$
- } Constrains between the 2 IP5 triplets (2 sides of IP5)  
 } Independent constraints per triplet

## Strategy:

1. Magnet settings from TIMBER/LSA
2. MADX (PTC Twiss) optics model
3. Insertion of the Roman Pots and data taking
4. Elastically scattered protons selection
5. Determination of optics constraints with RP proton tracks
6. Matching of the optics (determination of the transport matrix)

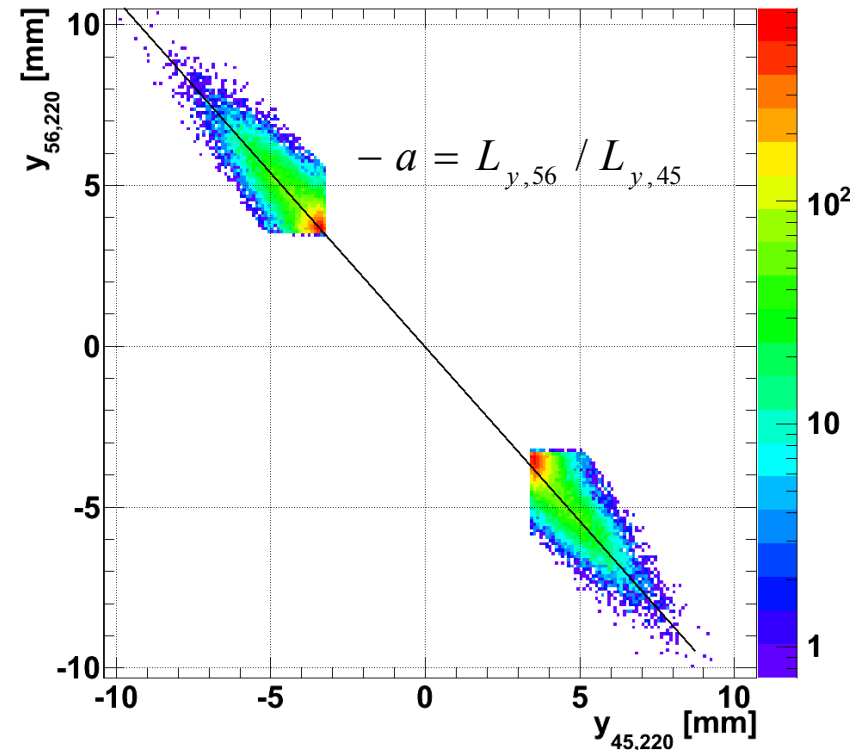
# $(dL_x/ds_{45}) / (dL_x/ds_{56})$ and $L_{y,45} / L_{y,56}$ determination beam 1 & 2 together

$$\Theta_{x,56} = \frac{dL_{x,56}}{ds} \Theta_{x,45}^* + \frac{dv_x}{ds} x_{56}^*$$



$$\Theta_{x,45} = \frac{dL_{x,45}}{ds} \Theta_{x,45}^* + \frac{dv_x}{ds} x_{45}^*$$

$$y_{56} = L_{y,56} \Theta_{y,56}^* + v_y y_{56}^*$$



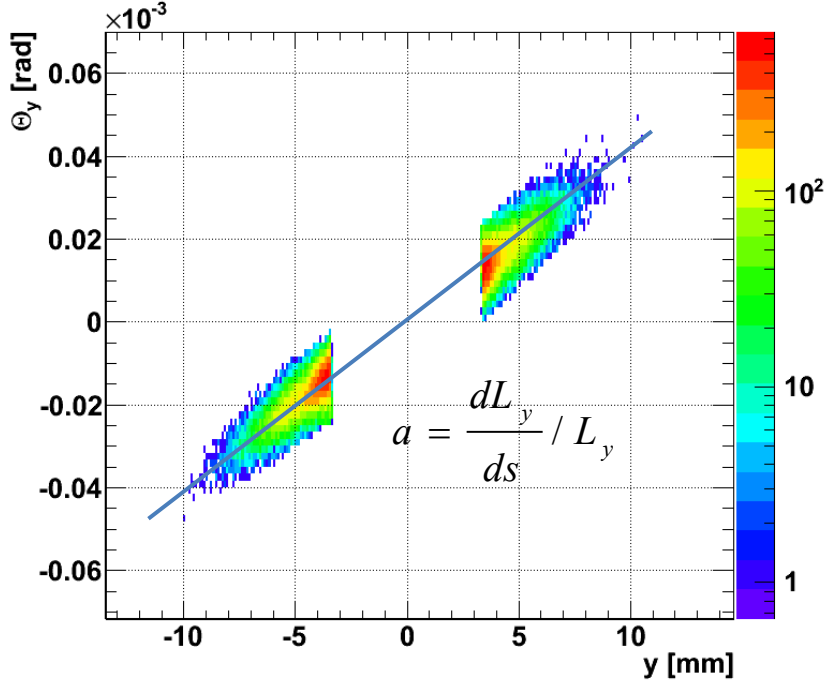
$$y_{45} = L_{y,45} \Theta_{x,45}^* + v_y y_{45}^*$$

Constraints for triplet strengths matching

# (dL<sub>y</sub>/ds)/L<sub>y</sub> and coupling determination

beam 1 & beam 2 separately

$$\Theta_{y,56} = \frac{dL_{y,56}}{ds} \Theta_{y,45}^* + \frac{dv_y}{ds} y_{56}^*$$

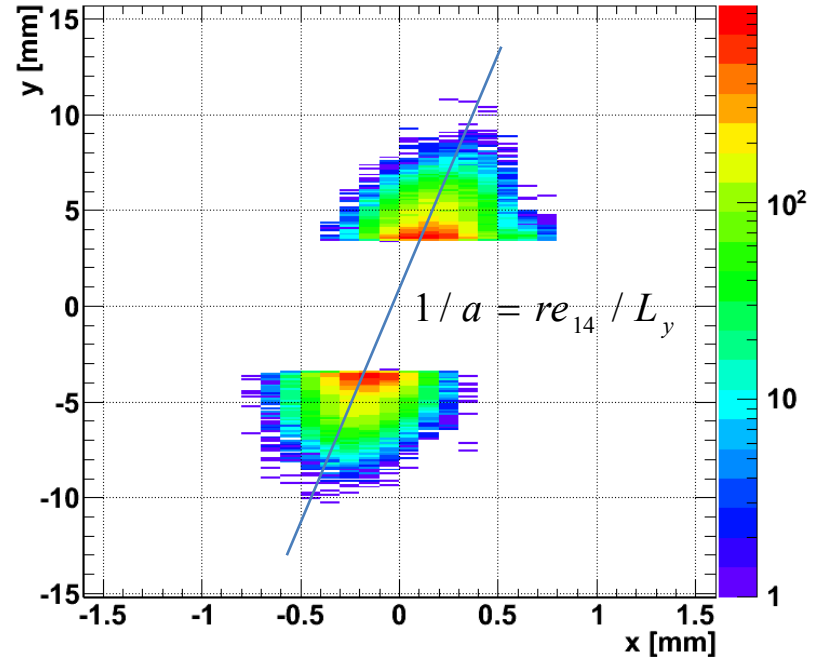


$$y_{56} = L_{y,56} \Theta_{y,56}^* + v_y y_{56}^*$$

(dL<sub>y</sub>/ds) / L<sub>y</sub> near =  $3.92 \cdot 10^{-3} \text{ m}^{-1}$   
 Nominally:  $2.7 \cdot 10^{-3} \text{ m}^{-1}$

Constraint for triplet strengths matching

$$y_{56} = L_{y,56} \Theta_{y,56}^* + v_y y_{56}^*$$



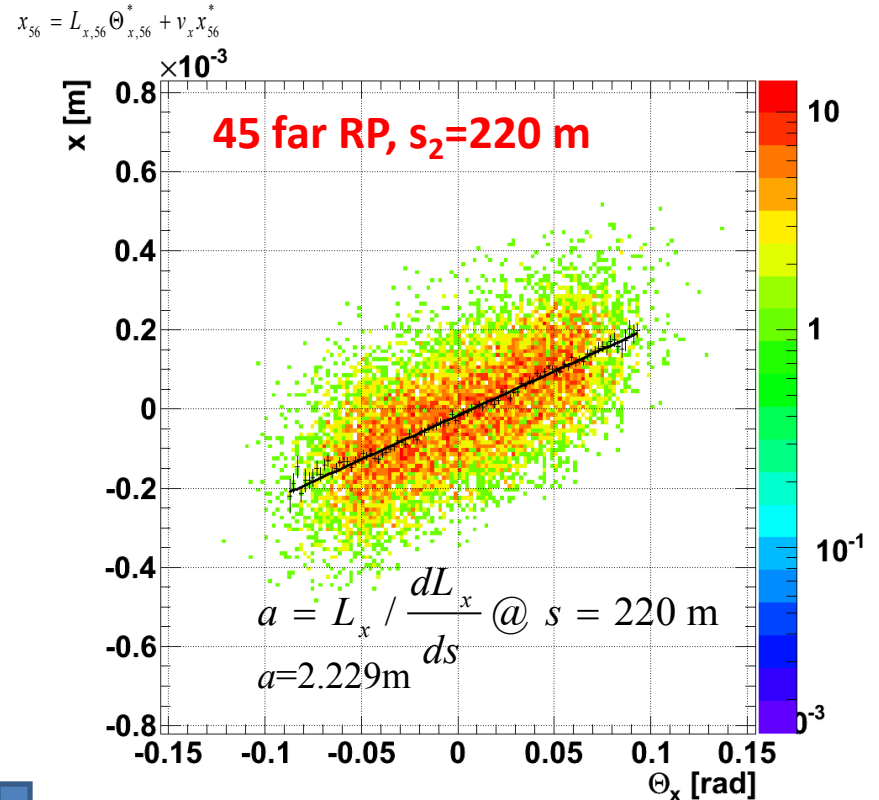
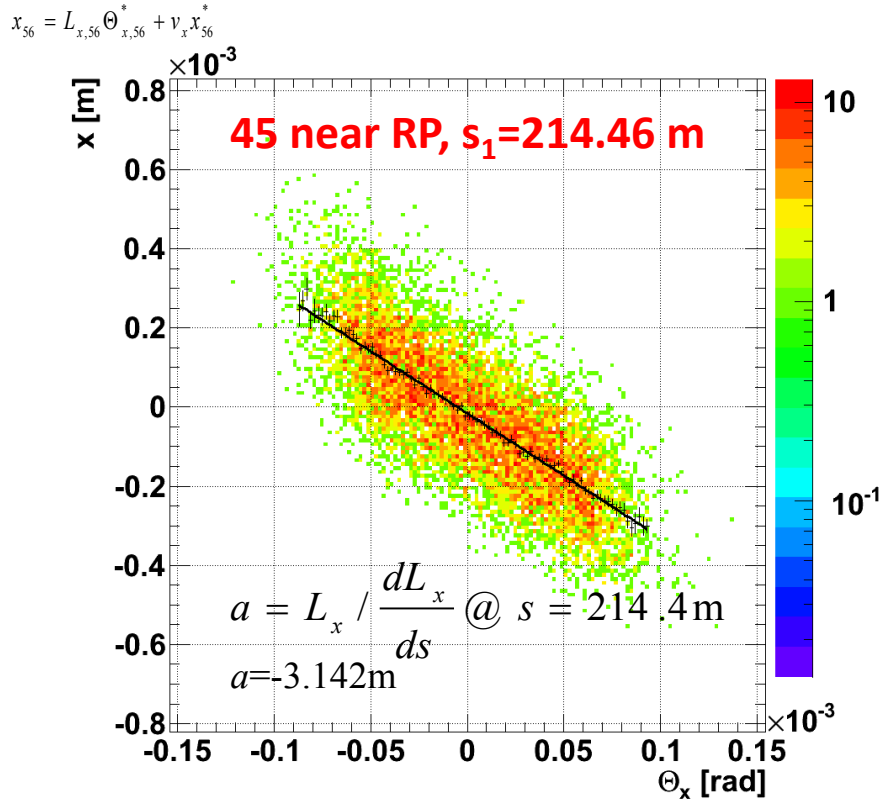
$$x_{56} = L_{x,56} \Theta_{x,56}^* + v_x x_{56}^* + re_{14} \Theta_{y,56}^*$$

re<sub>14</sub>/L<sub>y</sub> far = 36 mrad  
 Nominally: 0

Constraint for triplet rotation matching

# s: $L_x(s)=0$ determination

beam 1 & beam 2 separately



$\Theta_{x,56} = \frac{dL_{x,56}}{ds} \Theta_{x,45}^* + \frac{dv_x}{ds} x_{56}^*$

$\frac{dL_x}{ds} = \text{const with } \Theta_{x,45}^* \text{ in RP station, } L_x(s_2) = \int_{s_1}^{s_2} \frac{dL_x(\hat{s})}{d\hat{s}} d\hat{s} + L_x(s_1)$

**Interpolation:  $L_{x,45}(s) = 0 : s = 217.77$  m**

# Matched parameters

- Influence of all magnet parameters in  $\pm 220\text{m}$  range analysed...
  - ~30 parameters per beam
  - Magnet positions, rotations, k
  - Beam momentum, displacement, crossing angle, harmonics...
- Most significant parameters selected for matching
  - 6 strengths per beam (MQXA, MQXB, MQXB, MQXA, MQY, MQML)
  - 6 corresponding rotations about the beam
  - Mean  $\Delta p/p$  per beam
  - Total of 26 fitted parameters

# Constraints

- Measured elastic scattering kinematics constraints between arms (a total of 2):
  - Ratio of  $L_{y56} / L_{y45}$  (0.5 % precision)
  - Ratio of  $(dL_x/ds_{56}) / (dL_x/ds_{45})$  (0.5 % precision)
- Measured constraints of individual arms (a total of 8):
  - $(dL_y/ds)/L_y$  (0.5%)
  - near unit coupling, far unit coupling (3%)
  - $s: L_x=0$  (1 m)
- LHC design constraints (a total of 26):
  - $\sigma(k)/k = 0.1\%$
  - $\sigma(\text{rot}) = 1\text{mrad}$
  - $\sigma(\xi)/\xi = 10^{-3}$

**TOTAL of 36 constraints**

# Matching solution

## Full 4x4 transport matrix IP5→RP220 obtained per beam

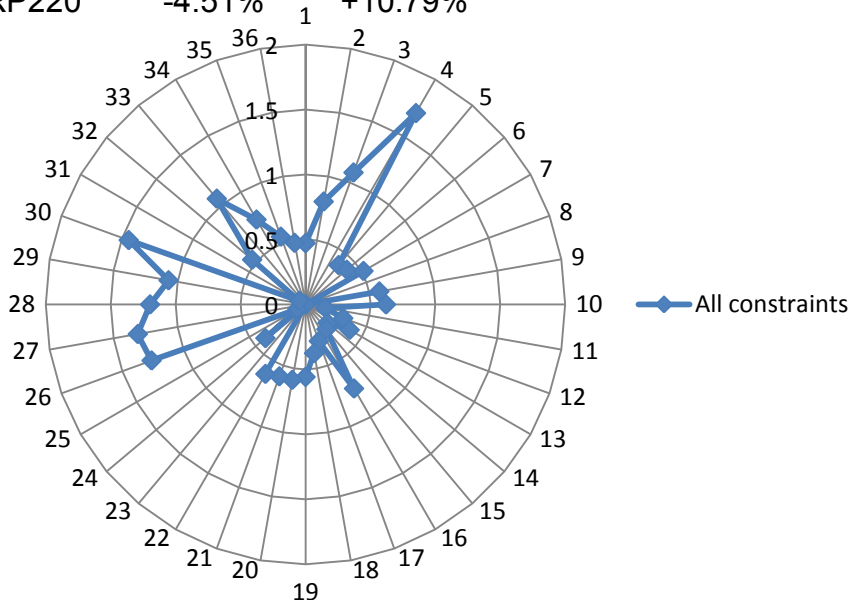
<u>Beam 1</u>	<u>dL<sub>x</sub>/ds</u>	<u>L<sub>y</sub> [m]</u>	<u>rot [mrad]</u>
RP215	-0.311962	22.15	0.0432
RP220	-0.311962	22.62	0.0396
Δ RP215	-2.84%	+0.78%	
Δ RP220	-2.84%	+0.81%	

Strong correlations between fitted parameters

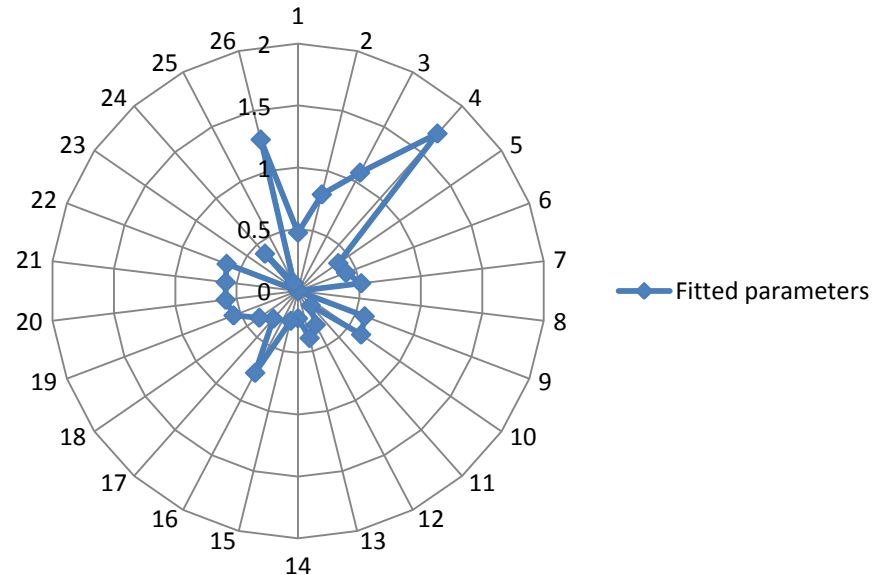
PCA should ideally be applied

<u>Beam 2</u>	<u>dL<sub>x</sub>/ds</u>	<u>L<sub>y</sub> [m]</u>	<u>rot [mrad]</u>
RP215	-0.314508	20.3883272	0.0400268
RP220	-0.314508	20.6709463	0.0372828
Δ RP215	-4.51%	+10.19%	
Δ RP220	-4.51%	+10.79%	

$\chi^2/\text{NDF} = 25.8/(36-26)=2.6$   
(would be lower in correlations are eliminated)



Abs(Pulls) of constraints



Abs(Pulls) of fitted parameters

# Complete solution

## Beam 1

	BETX	BETY	MUX	MUY
nominal	3.37E+01	2.08E+02	5.13E-01	3.43E-01
obtained	3.41E+01	2.10E+02	5.02E-01	3.44E-01
difference	0.96%	1.07%	2.24%	-0.20%

Obtained transport matrix

$$\begin{pmatrix} x \\ \Theta_x \\ y \\ \Theta_y \end{pmatrix} = \begin{pmatrix} -3.11E+00 & -9.18E-01 & 2.35E-02 & 8.89E-01 \\ 3.11E-02 & \mathbf{-3.12E-01} & -2.23E-04 & -1.13E-02 \\ 3.09E-02 & 1.40E+00 & -4.27E+00 & \mathbf{2.26E+01} \\ 4.49E-04 & 1.82E-02 & -6.08E-02 & 8.79E-02 \end{pmatrix} \cdot \begin{pmatrix} x^* \\ \Theta_x^* \\ y^* \\ \Theta_y^* \end{pmatrix}$$

Obtained changes

$$\begin{pmatrix} 0.31\% & 85.59\% & 114.70\% & 100.02\% \\ 0.38\% & \mathbf{-2.84\%} & 115.46\% & 96.83\% \\ 84.59\% & 101.79\% & -0.15\% & \mathbf{0.81\%} \\ 84.88\% & 100.53\% & -0.28\% & 2.13\% \end{pmatrix}$$

## Beam 2

	BETX	BETY	MUX	MUY
nominal	3.40E+01	1.60E+02	4.90E-01	3.58E-01
obtained	3.39E+01	1.81E+02	5.08E-01	3.47E-01
difference	-0.41%	11.93%	3.51%	-3.04%

Obtained transport matrix

$$\begin{pmatrix} x \\ \Theta_x \\ y \\ \Theta_y \end{pmatrix} = \begin{pmatrix} -3.12E+00 & -5.39E-01 & 2.42E-02 & 6.87E-01 \\ 3.33E-02 & \mathbf{-3.15E-01} & -2.33E-04 & -8.42E-03 \\ 1.32E-02 & 1.07E+00 & -4.16E+00 & \mathbf{2.07E+01} \\ 2.05E-04 & 1.33E-02 & -5.90E-02 & 5.26E-02 \end{pmatrix} \cdot \begin{pmatrix} x^* \\ \Theta_x^* \\ y^* \\ \Theta_y^* \end{pmatrix}$$

Obtained changes

$$\begin{pmatrix} 0.38\% & 226.67\% & 85.69\% & 100.11\% \\ 0.70\% & \mathbf{-4.51\%} & 84.17\% & 104.35\% \\ 135.55\% & 98.09\% & -1.44\% & \mathbf{10.79\%} \\ 132.41\% & 99.80\% & -1.23\% & 54.60\% \end{pmatrix}$$



# Error estimation

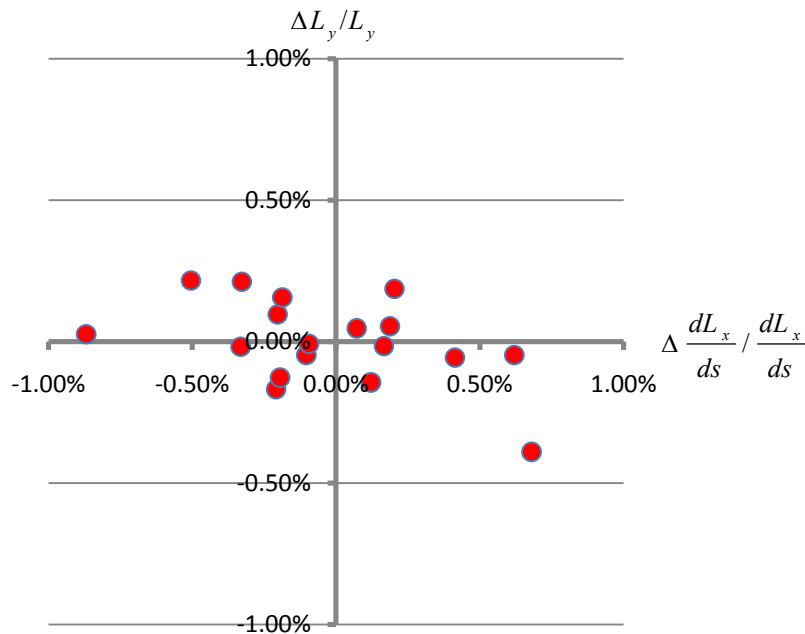
- **All the measurements provoke magnet corrections in the same direction**
  - Observed optics imperfections in x and y per beam provoke identical needs for strengths corrections
  - Independent corrections of beam 1 and beam 2 lead to the observed ratios of  $(dL_x/ds_{45}) / (dL_x/ds_{56})$  and  $L_{y,45} / L_{y,56}$
- **Which part of the triplet is precisely responsible? Difficult to say**
  - main source of systematic error of corrected optics
- Optics error estimation
  - Required corrections of up to 10% of the nominal optics values of  $L_y$  and  $dL_x/ds$
  - Values of corrections of  $L_y$  and  $dL_x/ds$  change by up to 10% depending on the quadrupole of the triplet to which the error is attributed
  - The error of the optics estimation is therefore  $\sim 10\% \cdot 10\% = 1\%$

# MC error verification

(in progress)

## Verification procedure

- 1) Randomly perturbate the initial optics within magnet tolerances
- 2) Measure optics parameters with RPs
- 3) Match the optics
- 4) Compare matched optics to the initial perturbed conditions

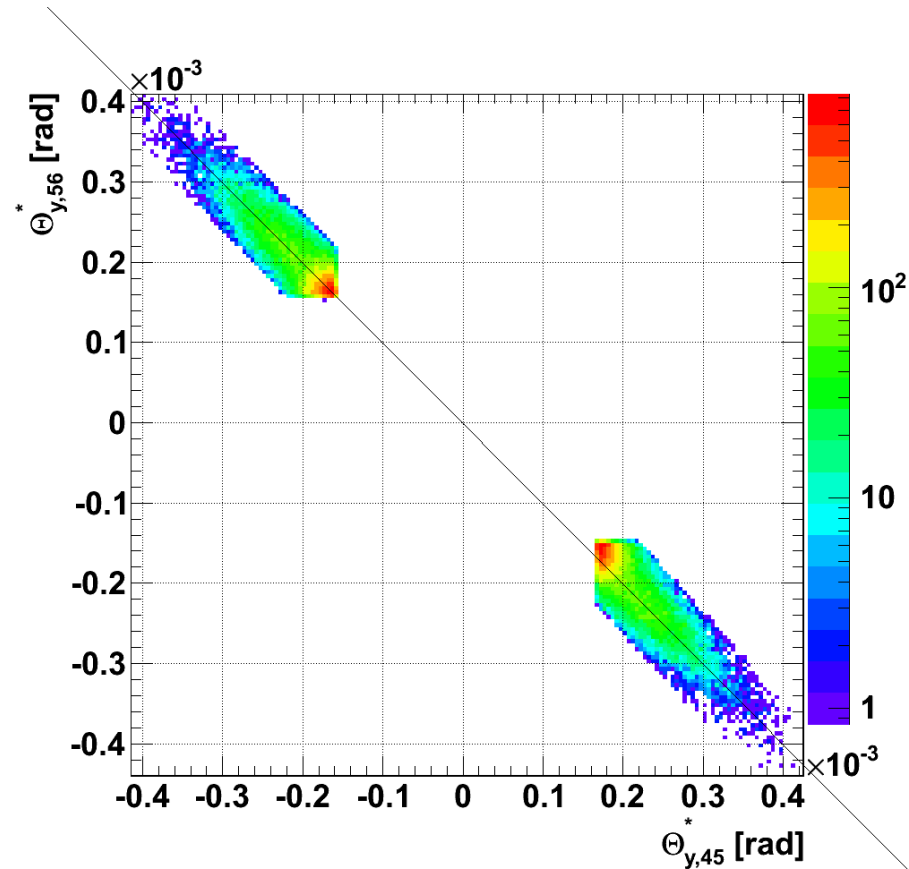
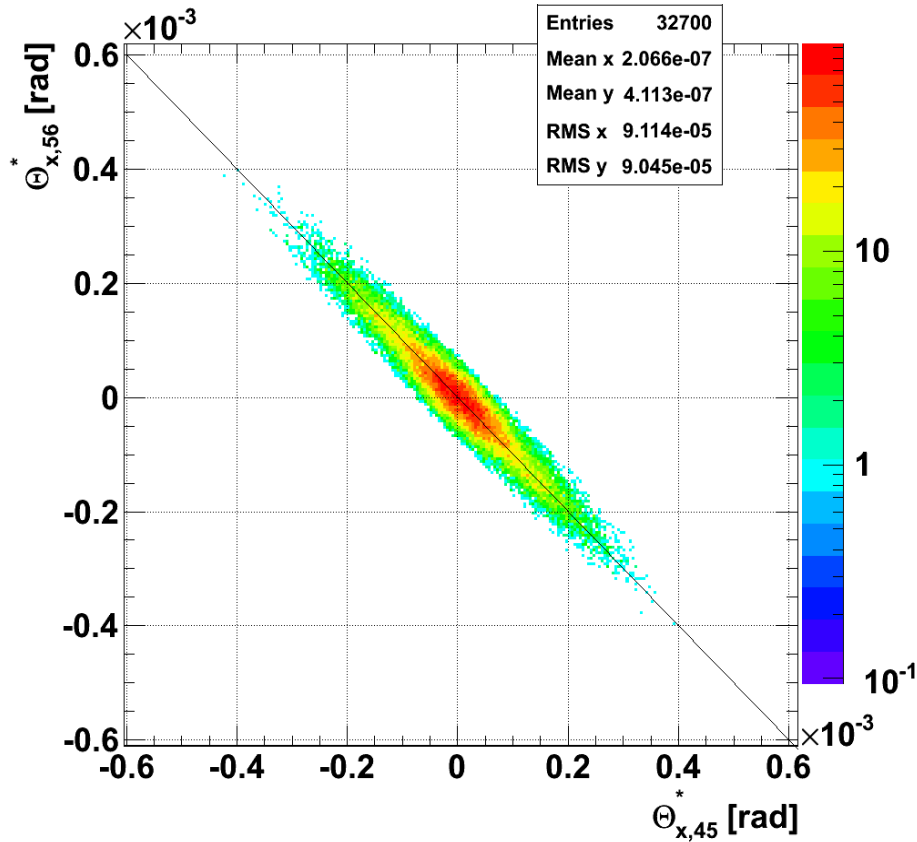


Obtained errors:

$$\sigma \left( \Delta \frac{dL_x}{ds} / \frac{dL_x}{ds} \right) = 0.4\%$$

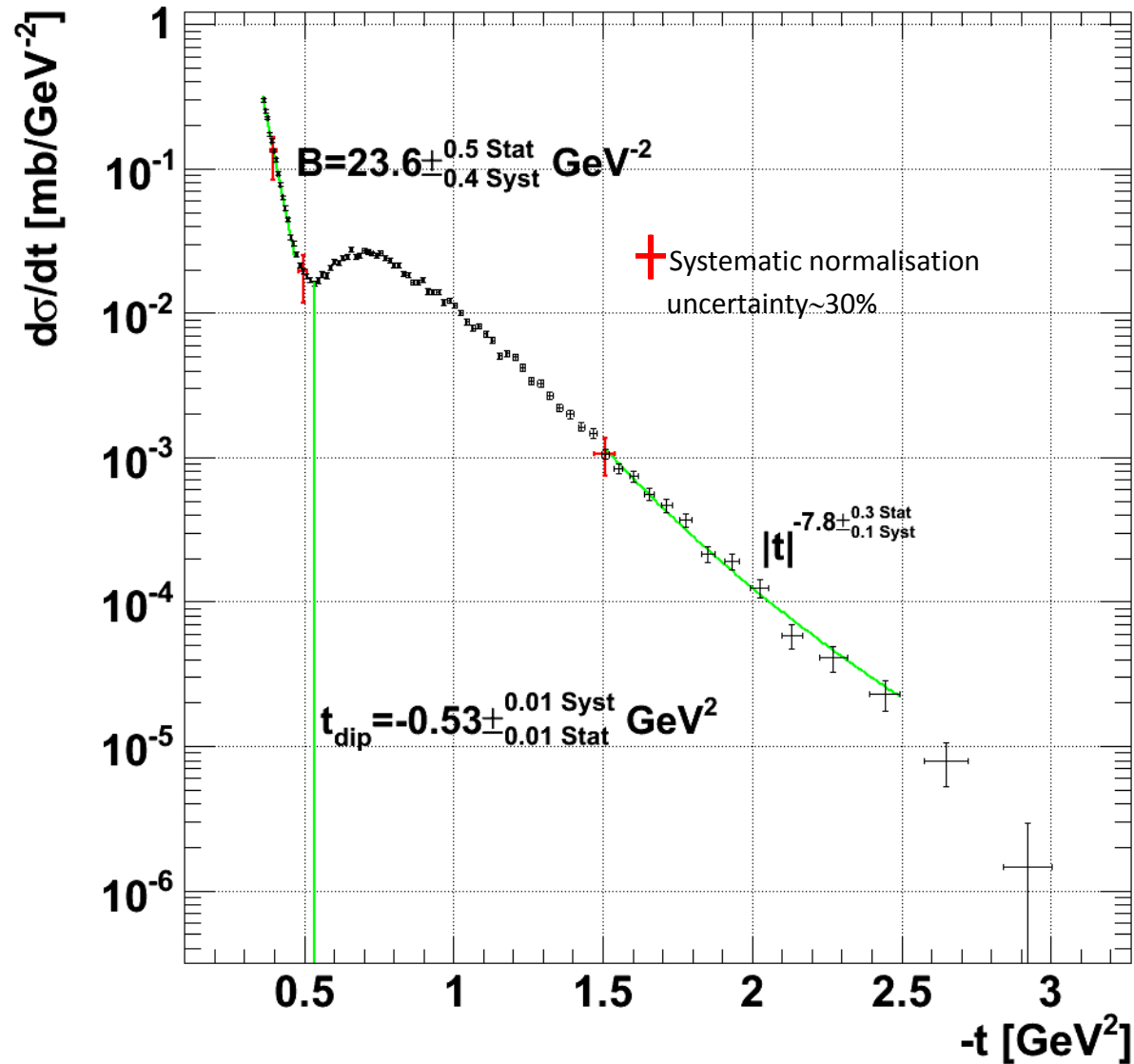
$$\sigma (\Delta L_y/L_y) = 0.2\%$$

# After matching, reconstructed protons



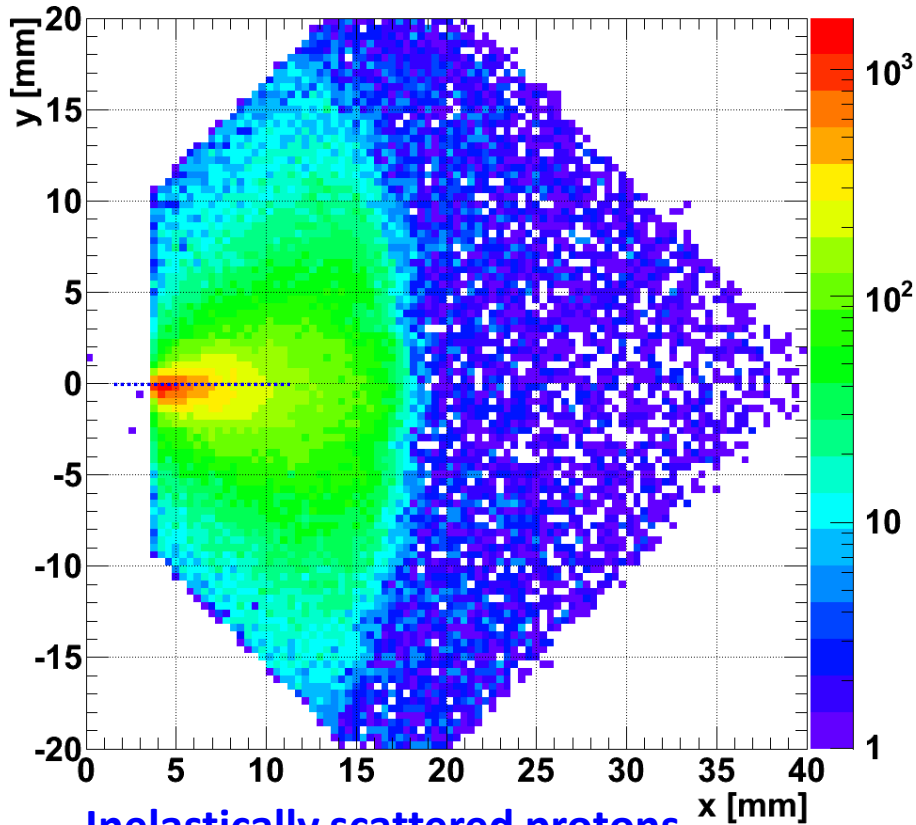
Arms and diagonals in perfect agreement

# Final result: unfolded el. scat. distribution

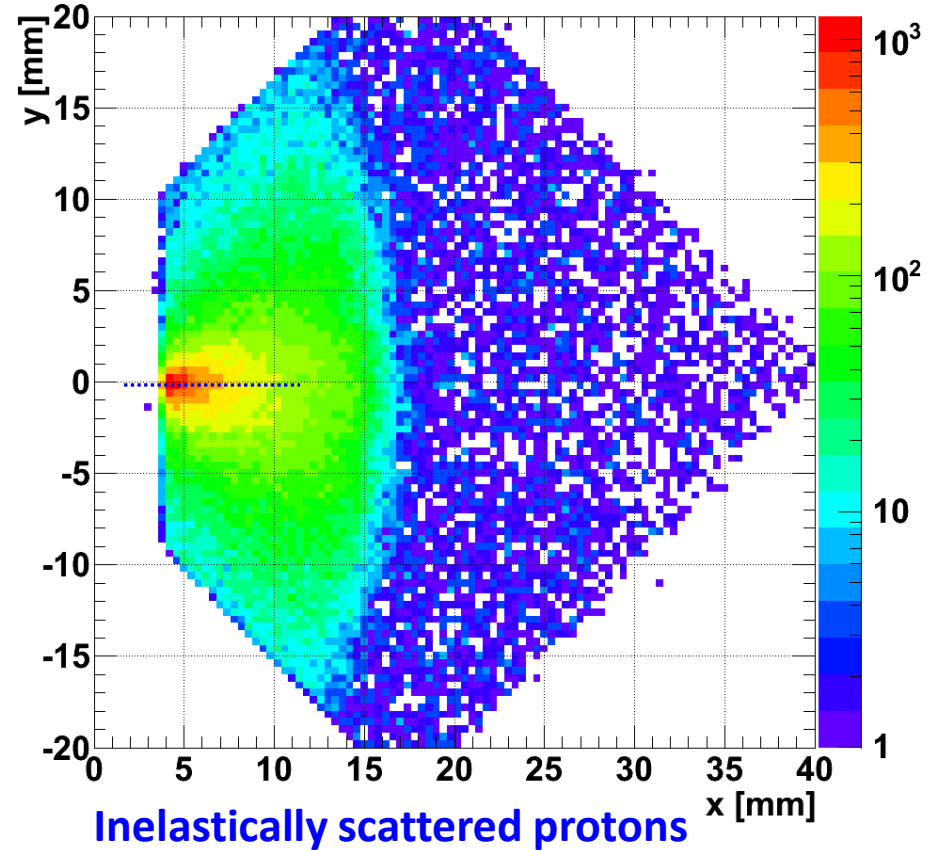


# Further steps: inelastic protons, $D_y$

Horizontal s=215m, beam 2



Horizontal s=220m, beam 2

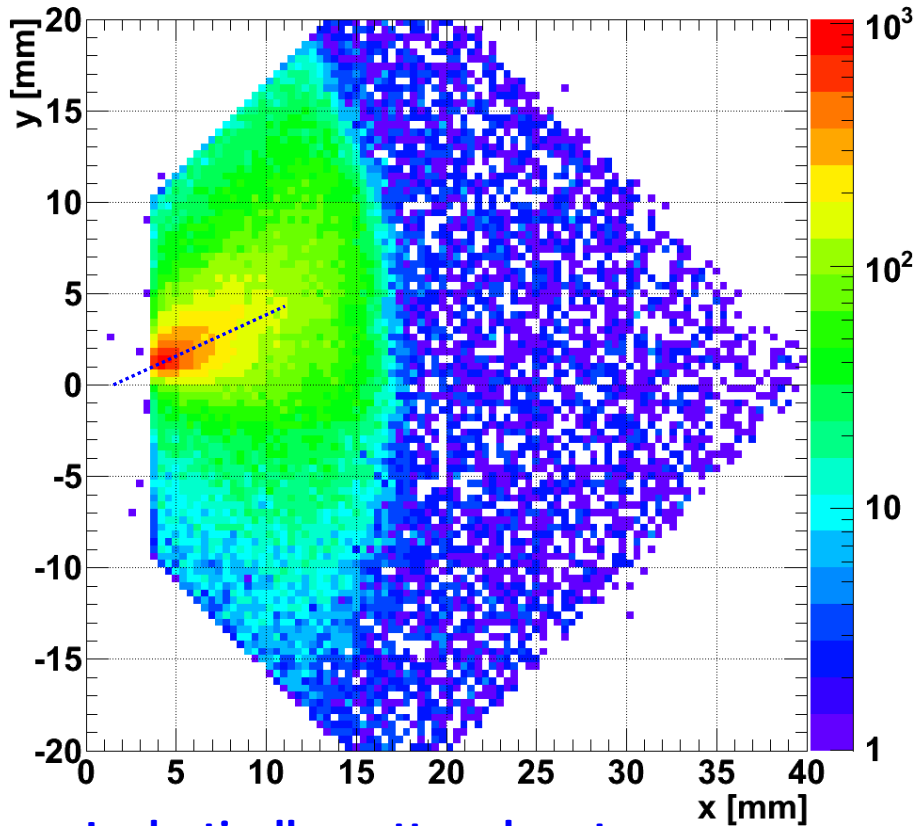


$$\begin{cases} x(s) = v_x(s) \cdot x^* + L_x(s) \cdot \Theta_x^* + D_x(s) \cdot \xi \\ y(s) = v_y(s) \cdot y^* + L_y(s) \cdot \Theta_y^* + D_y(s) \cdot \xi \end{cases} \quad \xi = \frac{\Delta p}{p} \neq 0$$

Beam 2 :  $D_y \approx 0$

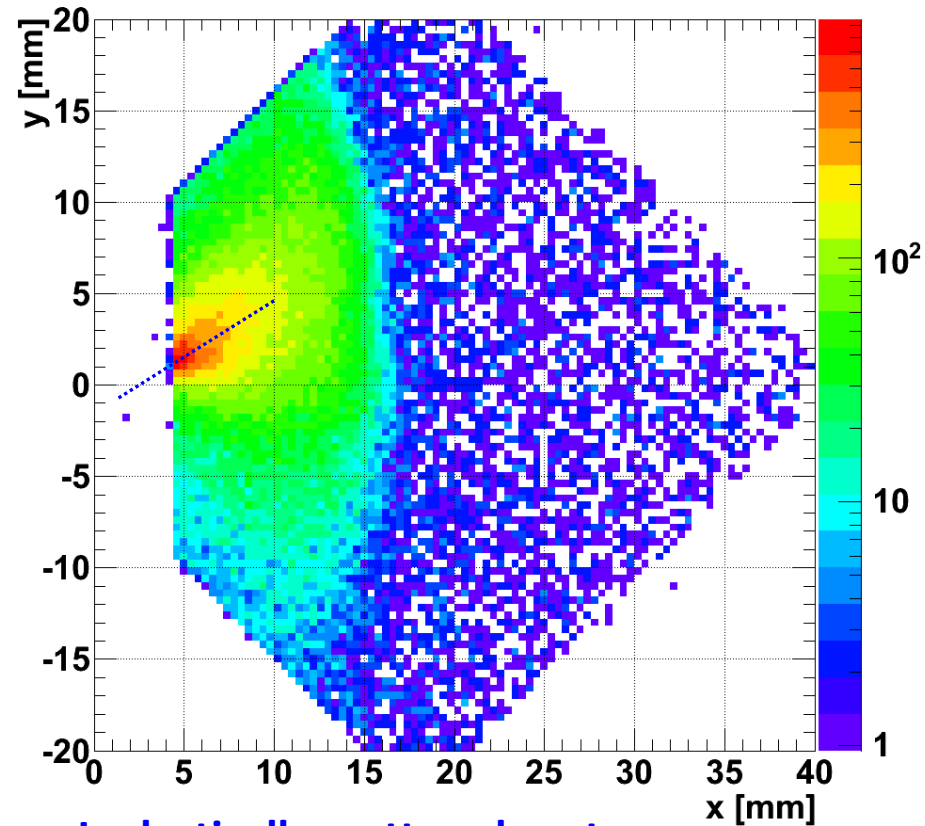
# Further steps: inelastic protons, $D_y$

Horizontal s=215m, beam 1



Inelastically scattered protons

Horizontal s=220m, beam 1



Inelastically scattered protons

$$\begin{cases} x(s) = v_x(s) \cdot x^* + L_x(s) \cdot \Theta_x^* + D_x(s) \cdot \xi \\ y(s) = v_y(s) \cdot y^* + L_y(s) \cdot \Theta_y^* + D_y(s) \cdot \xi \end{cases} \quad \xi = \frac{\Delta p}{p} \neq 0$$

Beam 1:  $D_y \neq 0$ , is of the order of  $D_x$

# Further steps

- Analysis of the results on the basis of different 2010 runs at different RP distances from the beam
- Analysis of the dispersion for inelastic proton reconstruction
- Analysis of optics for/from future 2011 TOTEM runs ( $\beta^*=1.5\text{m}$ , 90m)

We would like to thank you for all your help

Massimo Giovannozzi, Helmut Burkhardt, Ralph Assmann, Rogelio Garcia, Ezio Todesco, Marek Strzelczyk, Gabriel Mueller, Frank Schmidt, Carmen Alabau Pons, ...

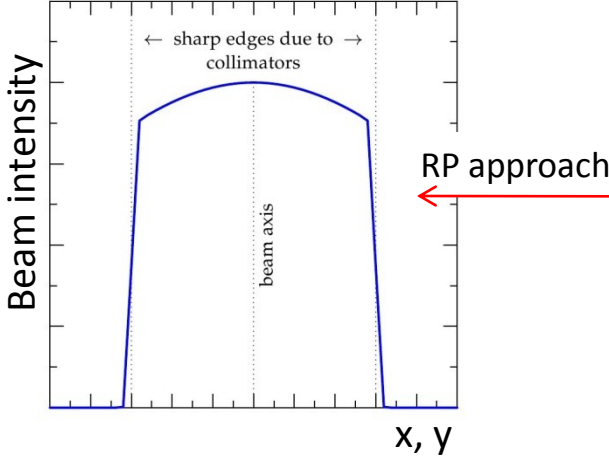
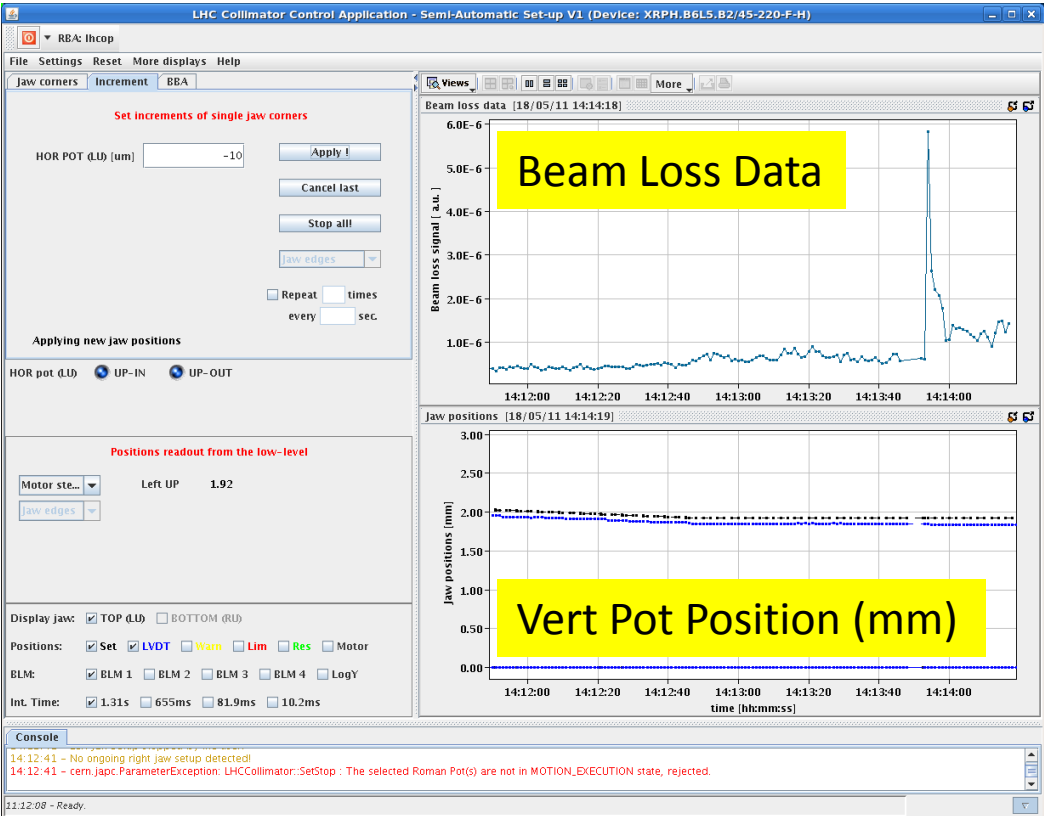
Thank you!

**BACKUP**



# Beam based alignment of RPs @220m and data taking (T1,T2,RP220m) (18 May 2011)

Scraping exercise:  
RP220 approached the low intensity beam in 10  $\mu\text{m}$  steps  
RP220 now ready for routine insertions in 2011



Data taking with RPs @ 220 close to the beams

- vertical RPs @  $5\sigma = 2.2 \text{ mm}$
- horizontal RPs @  $7\sigma = 1 \text{ mm}$
- low pile-up

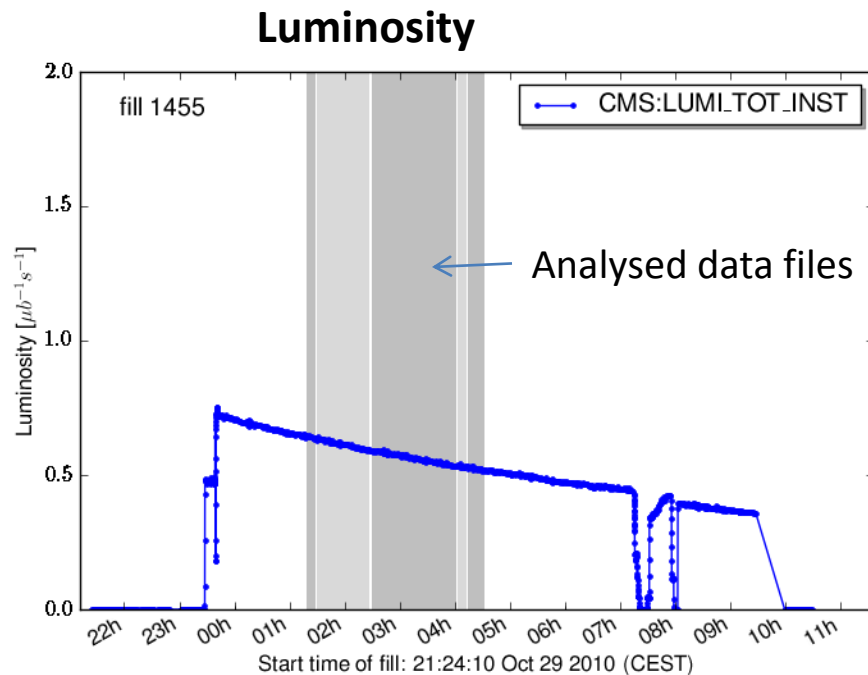
Alignment of RP147 planned in August

**ELASTIC pp SCATTERING**

**t-range: 0.36 – 3 GeV<sup>2</sup>**

# Elastic pp scattering

- Several runs were taken during 2010 with different distances of the Roman pots to the beam center
- The  $7\sigma$  runs were analyzed
- The  $18\sigma$  runs with a total luminosity of  $\sim 5.8\text{ pb}^{-1}$  will follow



RP dist.      Integrated  
                 luminosity

$25\sigma$	$1.5\text{ nb}^{-1}$
$20\sigma$	$185\text{ nb}^{-1}$
$18\sigma$	$5800\text{ nb}^{-1}$
$7\sigma$	$9.5\text{ nb}^{-1}$

important for  
large  $t$

# Proton reconstruction

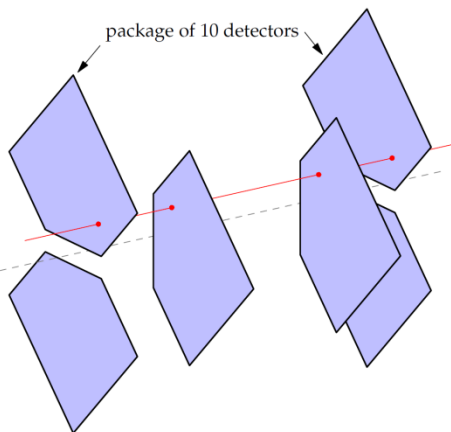
- Both angle projections reconstructed:  $\Theta_x^*$  and  $\Theta_y^*$ 
  - $\Theta_x^*$  from  $\Theta_x$  @ RP220 (through  $dL_x/ds$ )       $\Theta_x = dL_x/ds \Theta_x^*$
  - $\Theta_y^*$  from  $y$  @ RP220 (through  $L_y$ )       $y = L_y \Theta_y^*$

## → Excellent optics understanding

- Magnet currents measured
- Measurements of optics parameters with elastic scatt.
  - $\Theta_{\text{left}}^* = \Theta_{\text{right}}^*$  (proton pair collinearity)
  - Proton position  $\leftrightarrow$  angle correlations
  - $L_x=0$  determination, coupling corrections

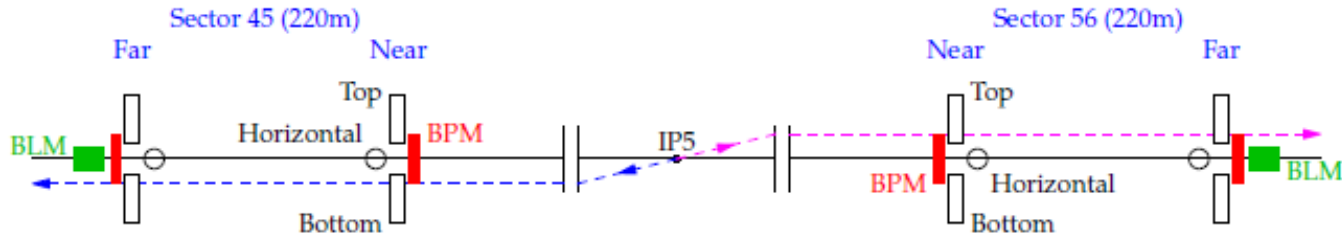
## → Fine alignment

- Alignment between pots with overlapping tracks ( $\sim 1\mu\text{m}$ )
- Alignment with respect to the beam – scraping exercise ( $\sim 20\mu\text{m}$ )
- Mechanical constraints between top and bottom pots ( $\sim 10\mu\text{m}$ )



Track based alignment

# Cuts and data reduction



- Topology
  - near and far units
  - diagonals
- Low  $|\xi|$  selection ( $3\sigma$ )
  - $|x_{RP,45}| < 3\sigma_x @ L_{x,45}=0$
  - $|x_{RP,56}| < 3\sigma_x @ L_{x,56}=0$
  - corr.  $y_{RP216,45} \leftrightarrow y_{RP220,45}$
  - corr.  $y_{RP216,56} \leftrightarrow y_{RP220,56}$
- Elastic collinearity ( $3\sigma$ )
  - $\theta_{x,45}^* \leftrightarrow \theta_{x,56}^*$
  - $\theta_{y,45}^* \leftrightarrow \theta_{y,56}^*$

Integrated luminosity :  $6.2 \text{ nbarn}^{-1}$

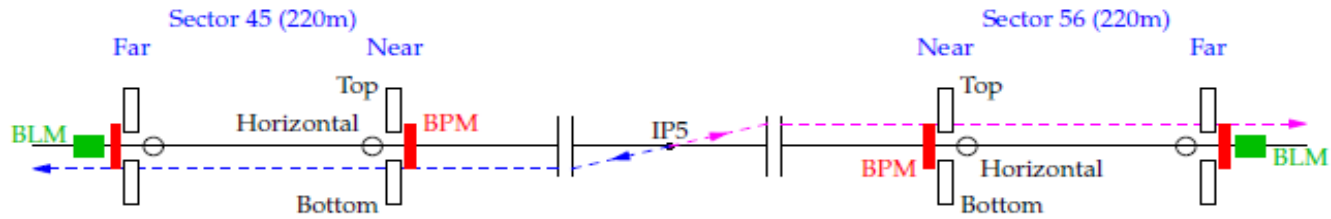
Total triggers	5.28M
Reconstructed tracks & elastic topology	293k
Low $ \xi $ selection	70.2k
Collinearity cuts	66.0k

↑ showers ↓

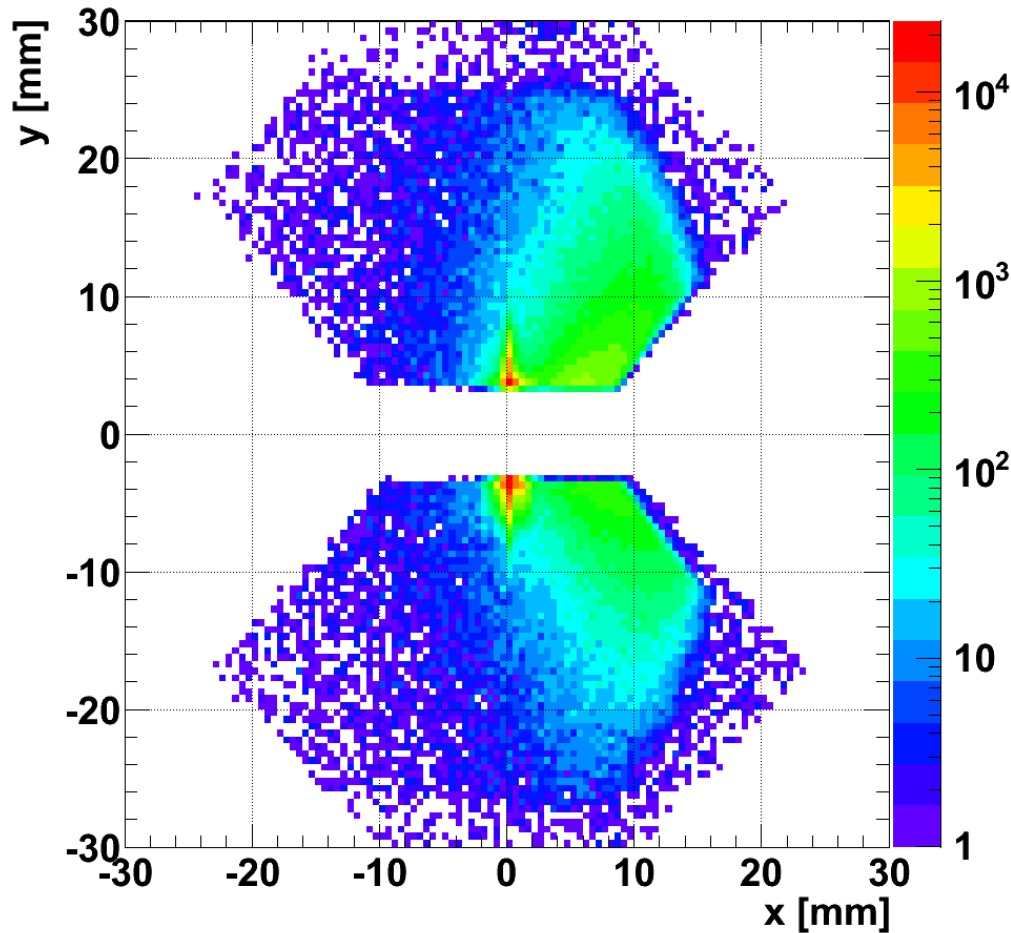
Diagonals analysed independently

# Proton tracks of a single diagonal

(left-right coincidences)



Sector 56



Sector 45

$$t = -p^2 \theta^2$$

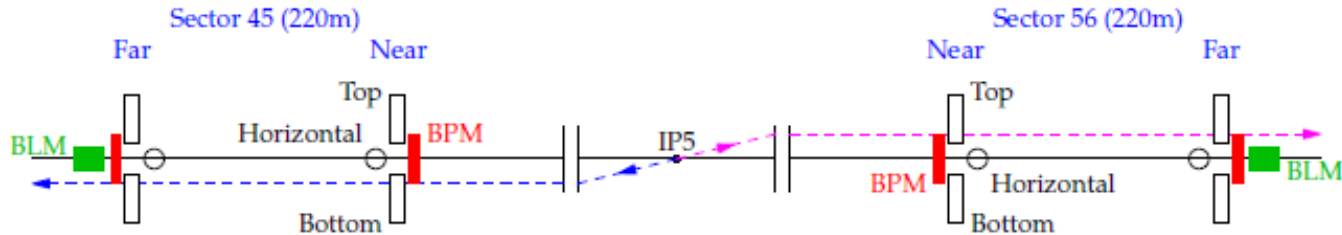
$$\xi = \Delta p/p$$

$$y = L_y \Theta_y$$

$$x = L_x \Theta_x + \xi D$$

$$L_x \sim 0$$

# Cuts and data reduction



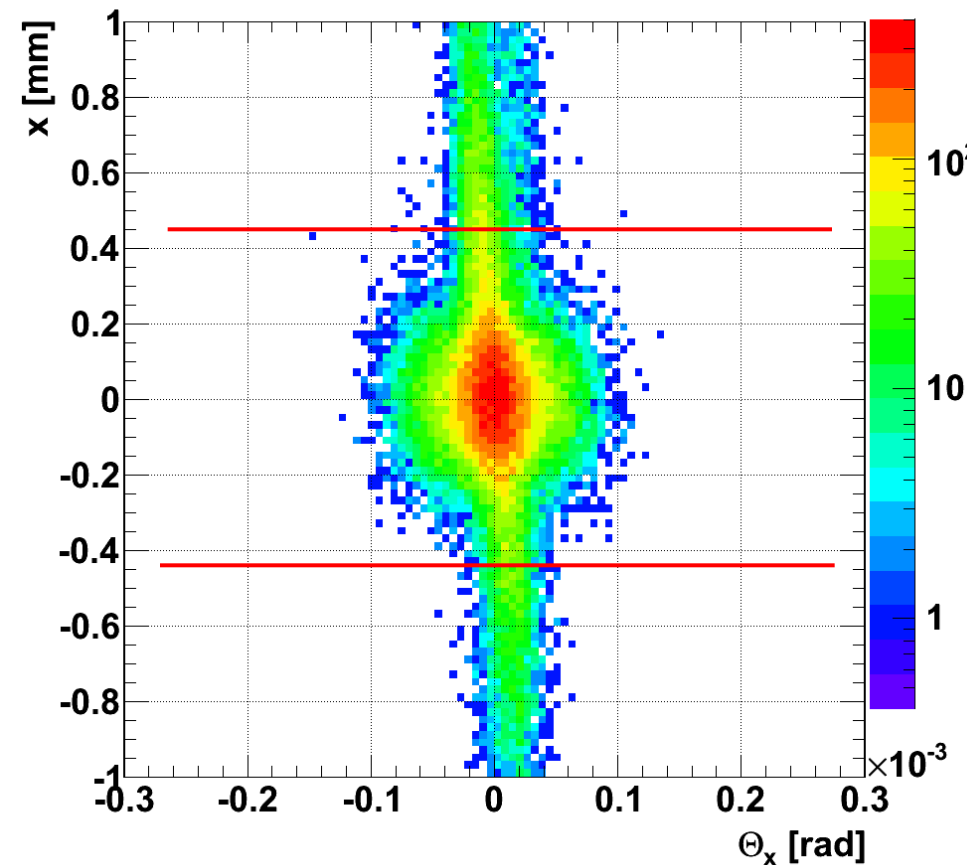
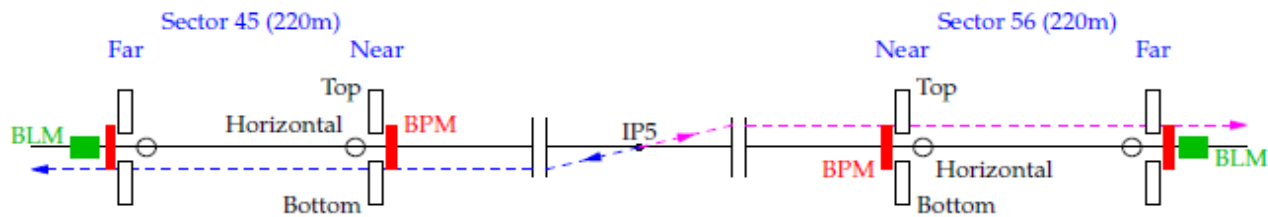
Integrated luminosity :  $6.2 \text{ nbarn}^{-1}$

- Topology
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- Low  $|\xi|$  selection ( $3\sigma$ )
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  - corr.  $y_{RP216,56} \leftrightarrow y_{RP220,56}$
- Elastic collinearity ( $3\sigma$ )
  - $\theta_{x,45}^* \leftrightarrow \theta_{x,56}^*$
  - $\theta_{y,45}^* \leftrightarrow \theta_{y,56}^*$

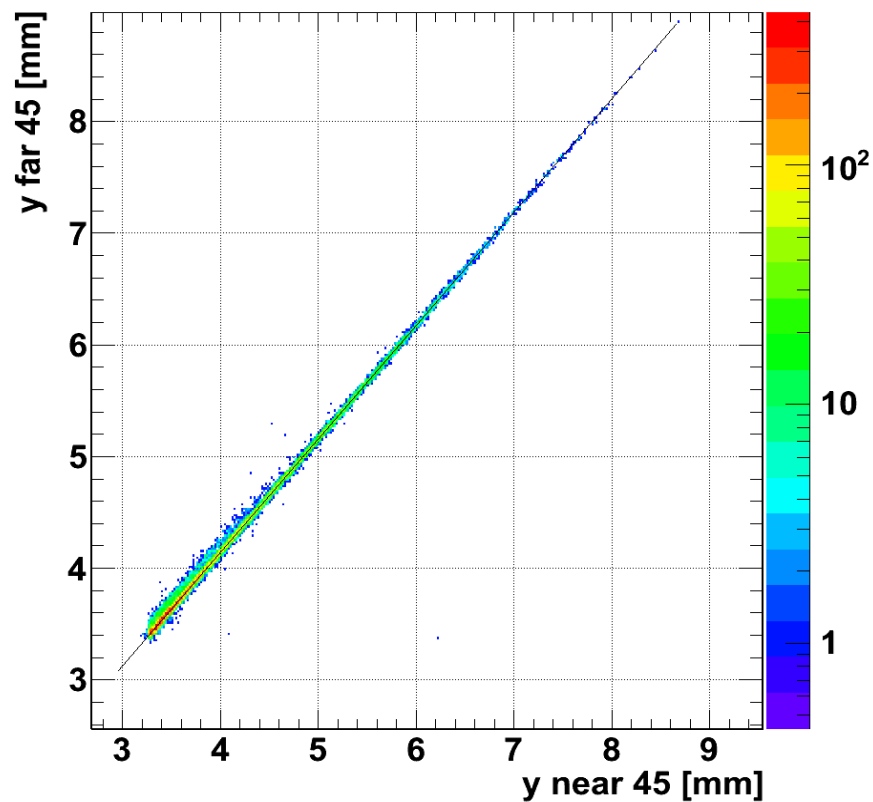
Total triggers	5.28M
Reconstructed tracks & elastic topology	293k
Low $ \xi $ selection	70.2k
Collinearity cuts	66.0k

↑ showers

# Low $\xi = \Delta p/p$ cuts



$$|x| < 3\sigma_x @ L_x = 0$$

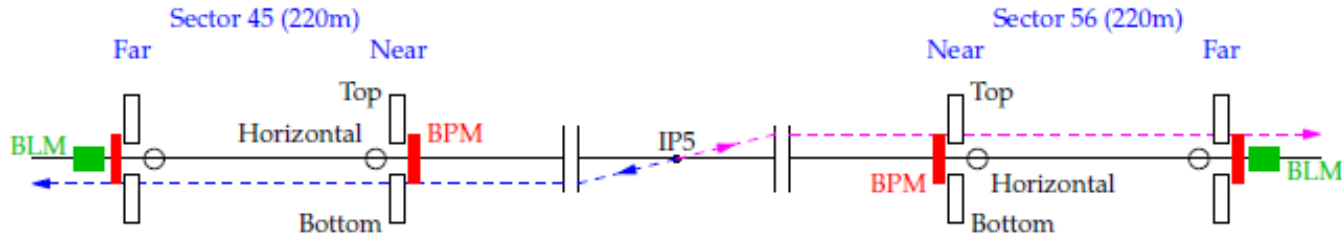


$$Y_{RP \text{ near},45} \leftrightarrow Y_{RP \text{ far},45}$$

( $dL_y/ds \approx 0$ )



# Cuts and data reduction



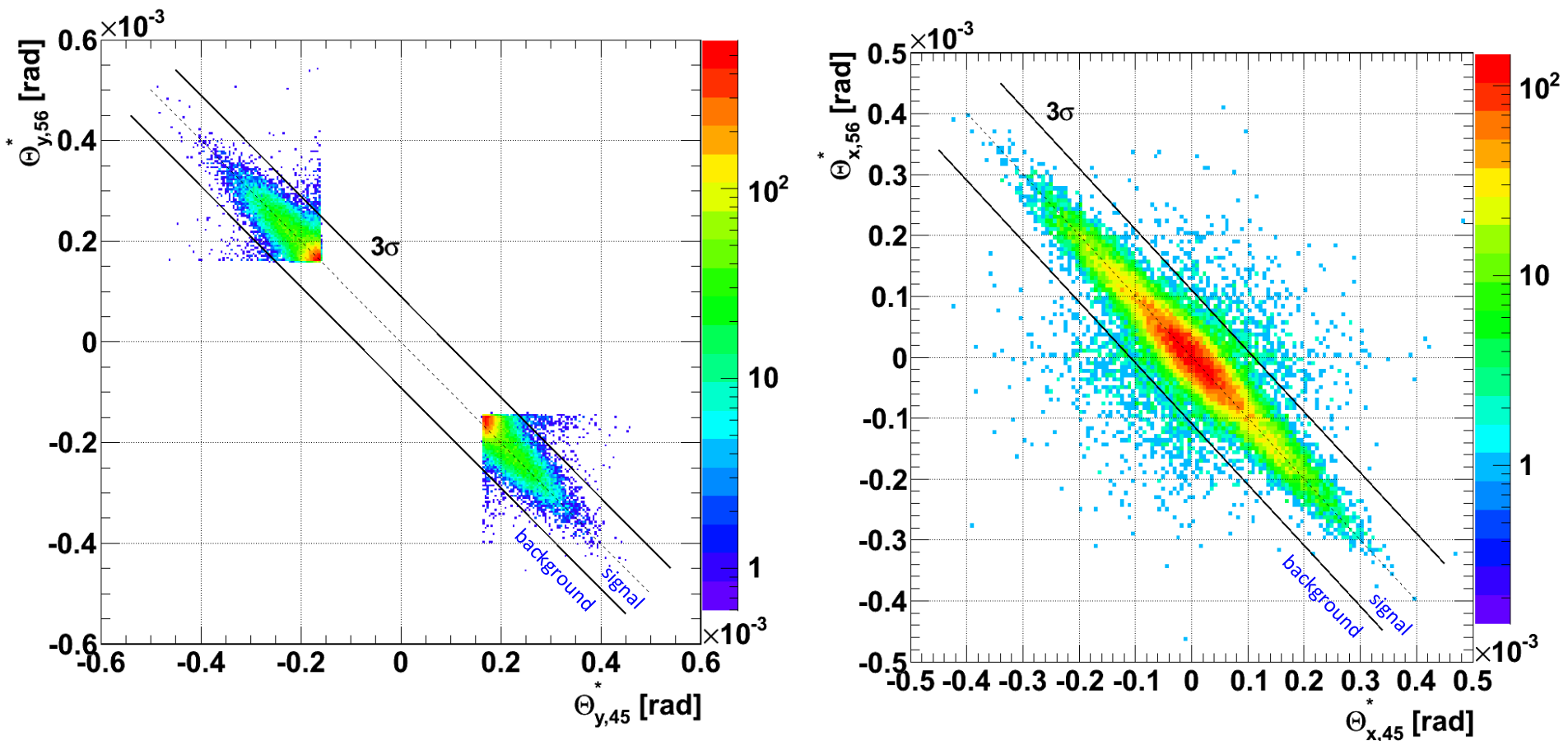
Integrated luminosity : 6.2 nbarn<sup>-1</sup>

- Topology
  - near and far units
  - diagonals
- Low  $|\xi|$  selection ( $3\sigma$ )
  - $|x_{RP,45}| < 3\sigma_x @ L_{x,45}=0$
  - $|x_{RP,56}| < 3\sigma_x @ L_{x,56}=0$
  - corr.  $y_{RP216,45} \leftrightarrow y_{RP220,45}$
  - corr.  $y_{RP216,56} \leftrightarrow y_{RP220,56}$
- Elastic collinearity ( $3\sigma$ )
  - $\theta_{x,45}^* \leftrightarrow \theta_{x,56}^*$
  - $\theta_{y,45}^* \leftrightarrow \theta_{y,56}^*$

Total triggers	5.28M
Reconstructed tracks & elastic topology	293k
Low $ \xi $ selection	70.2k
Collinearity cuts	66.0k

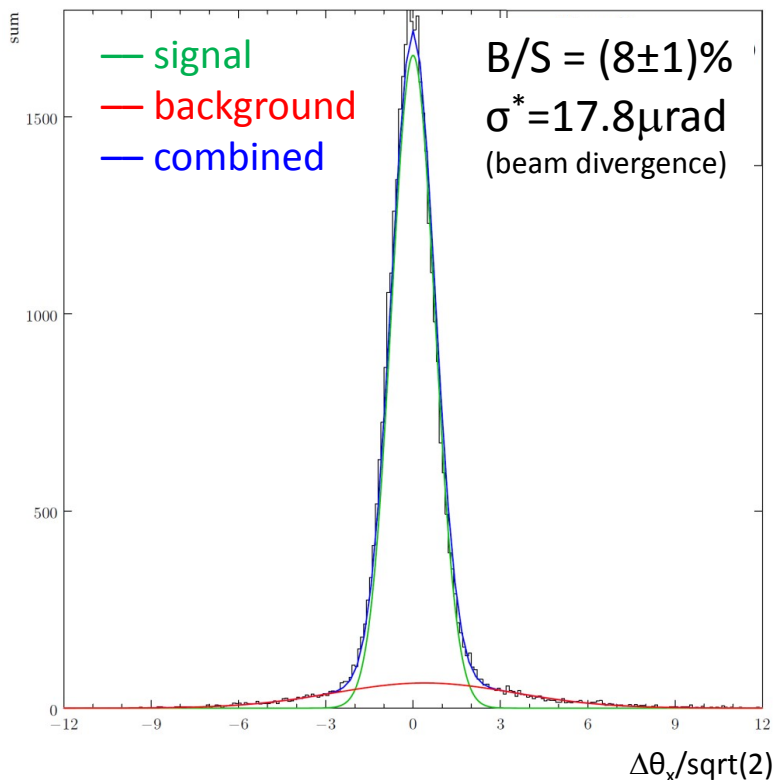
↑ showers

# Elastic collinearity cuts



Data outside the  $3\sigma$  cuts used for background estimation

# Background and resolution determination

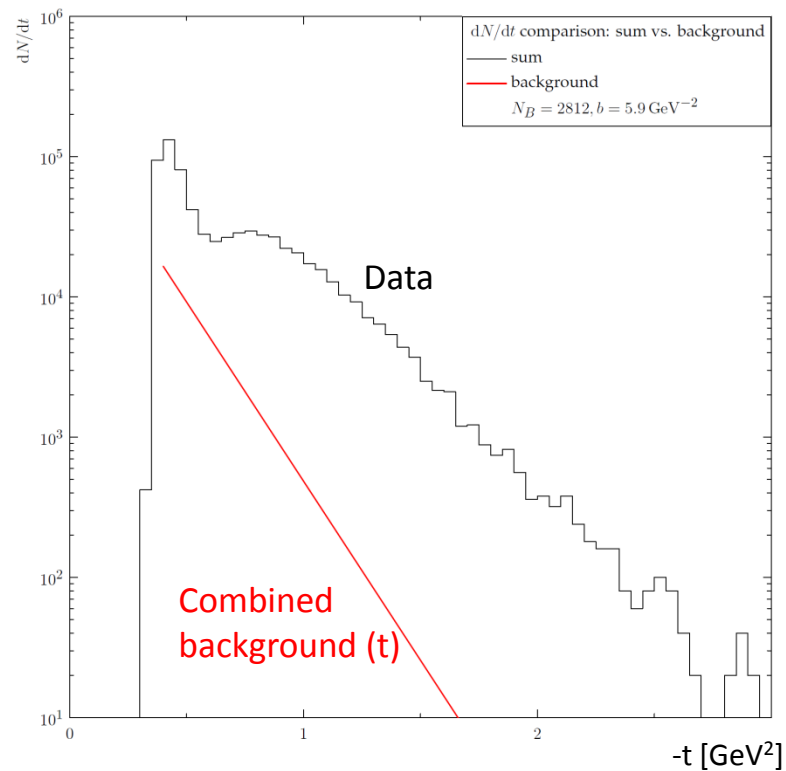


**Signal to background normalisation**  
(also as a function of  $\Delta\theta_y$ )

$\sigma^* \rightarrow$  **t-reconstruction resolution:**

$$\frac{\sigma(t)}{t} = \frac{\sqrt{2} p \sigma^*}{\sqrt{t}}$$

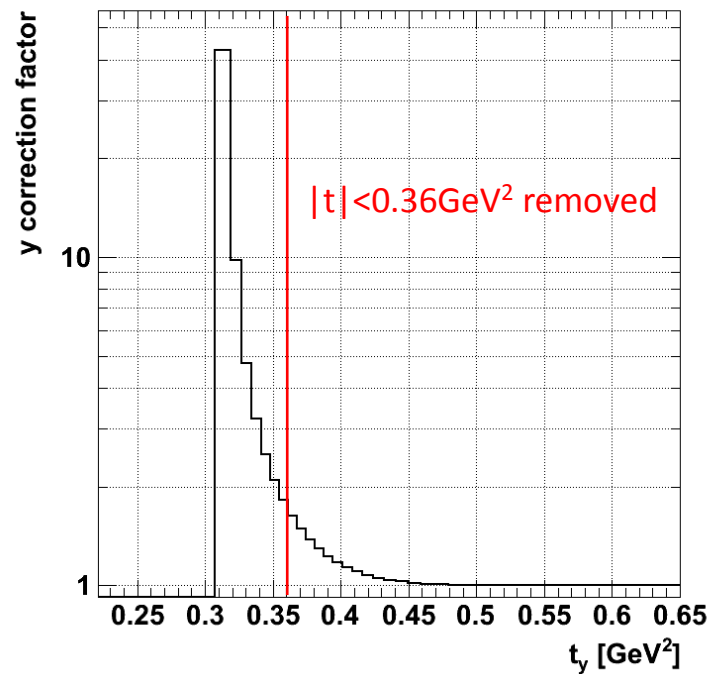
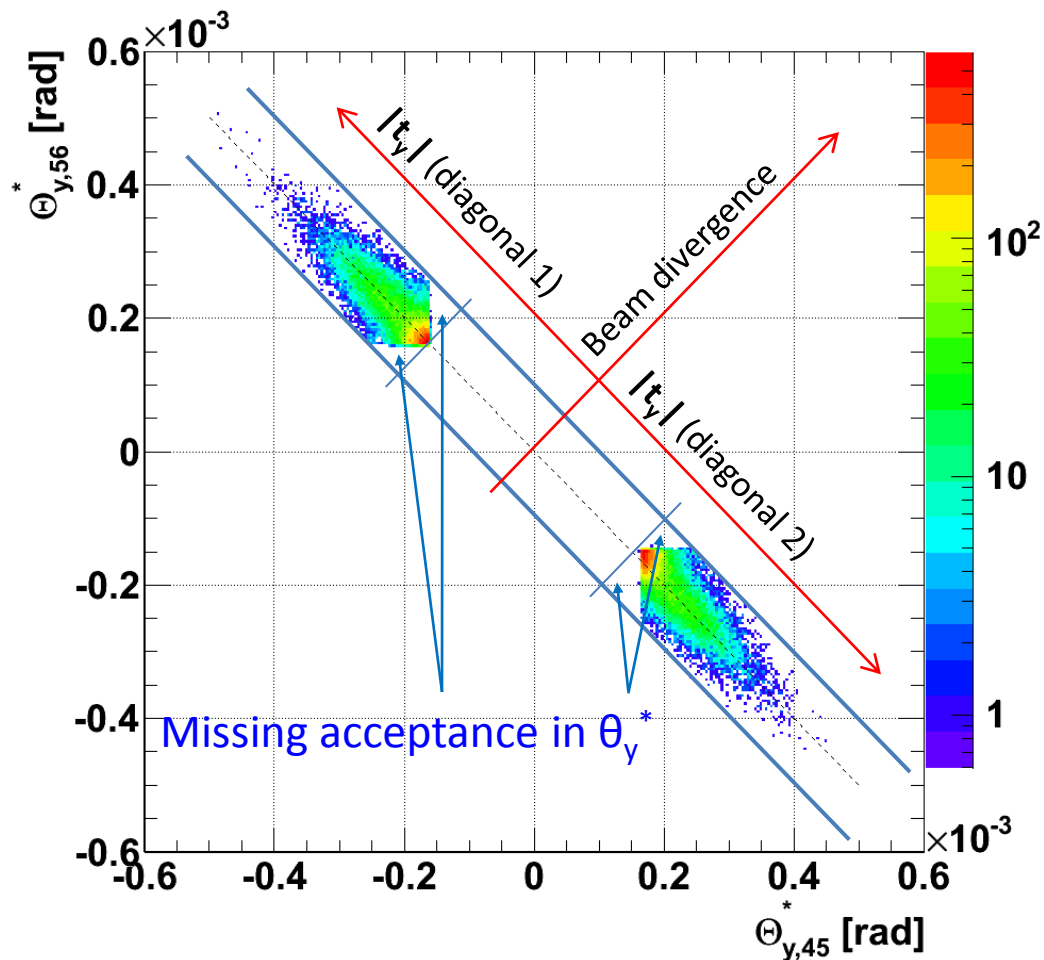
0.4 GeV<sup>2</sup> : 14%  
1 GeV<sup>2</sup> : 8.8%  
3 GeV<sup>2</sup> : 5.1%



**Signal vs. background (t)**

$|t|=0.4 \text{ GeV}^2$ :  $B/S = (11 \pm 2)\%$   
 $|t|=0.5 \text{ GeV}^2$ :  $B/S = (19 \pm 3)\%$   
 $|t|=1.5 \text{ GeV}^2$ :  $B/S = (0.8 \pm 0.3)\%$

# $t_y$ -acceptance corrections



**Correction error ( $t_y$ ):**

0.31 GeV $^2$  : 30%

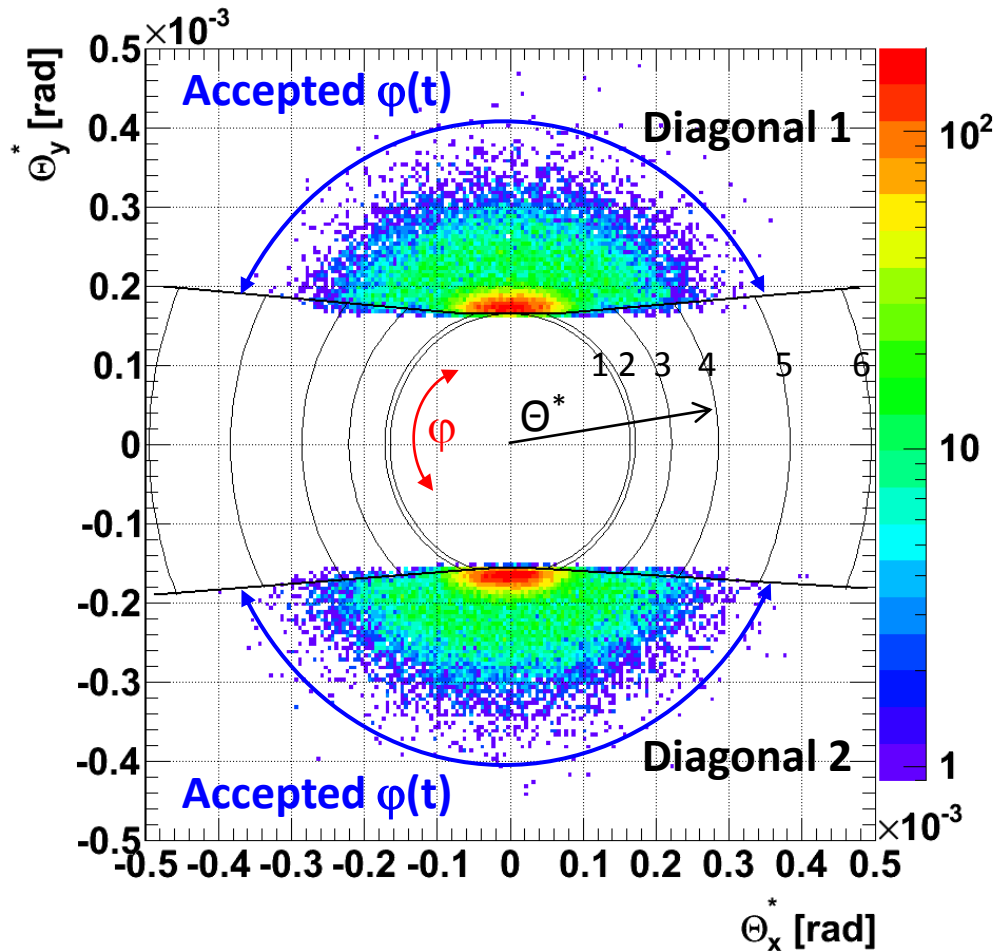
0.33 GeV $^2$  : 11%

0.35 GeV $^2$  : 2%

0.4 GeV $^2$  : 0.8%

0.5 GeV $^2$  : 0.1%

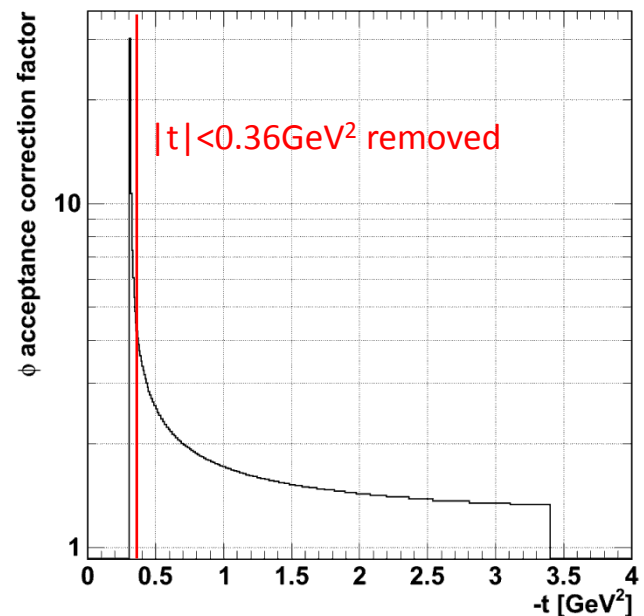
# $\phi$ -acceptance correction



Critical at low  $t$ -acceptance limit

## Total $\phi$ -acceptance correction

No.	$t$ [GeV <sup>2</sup> ]	$\Theta^*$ [rad]	Accepted $\phi$ (2 diag.) [°]	$\phi$ accept. correct. factor
1	0.33	1.65E-04	38.6	$9.3 \pm 4.7\%$
2	0.36	1.71E-04	76.4	$4.7 \pm 1.8\%$
3	0.60	2.21E-04	162.5	$2.2 \pm 0.3\%$
4	1.00	2.86E-04	209.8	$1.7 \pm 0.1\%$
5	1.80	3.83E-04	246.3	1.5
6	3.00	4.95E-04	269.0	1.3



# Final unfolded distribution

