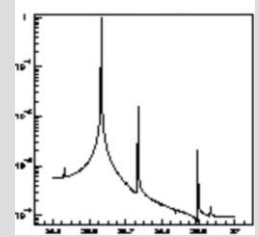
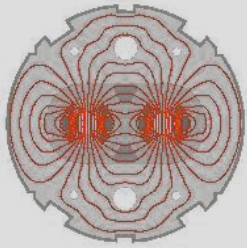


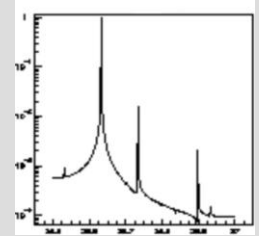
# Non-linear (Effective) Modeling of Accelerators



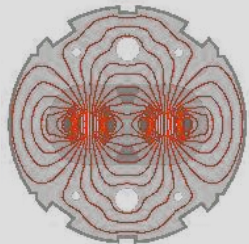
- Definition: **Effective Model** of an Accelerator
- **Effective Model** of the **LHC** (schematic)
- Optic Code Advancements
- **Effective Modeling** for the **LHC**
- Tools for n.l. Analysis and Measurements
- References



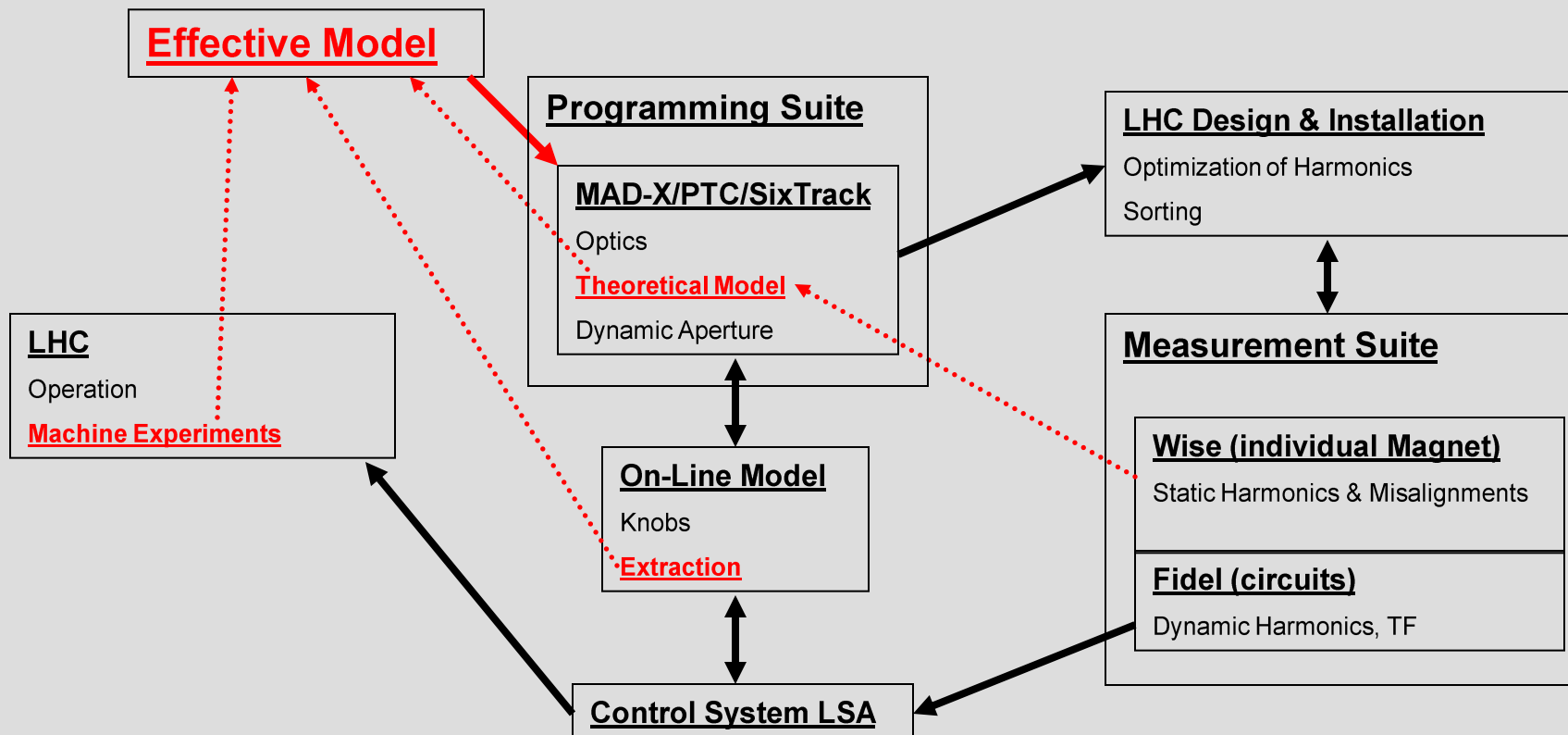
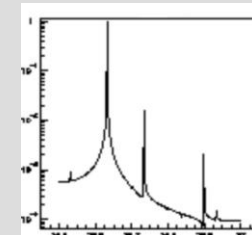
# Definition of Effective Modeling of an Accelerators

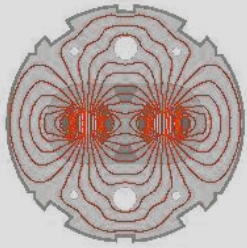


- Starting point is a good knowledge of the **harmonics** and **misalignments** of the accelerator.
- Equally important is an optics code with a **solid physics description** of the accelerator elements and a **flexible toolkit**.
- This allows the construction of the best **theoretical** n.l. model of the machine.
- The remaining difference to the **“real”** machine is **that what cannot be known** which includes errors in the measurements.
- The next step is to measure the missing linear and non-linear components directly from the machine.
- The **“effective”** model is then constructed by fitting the relevant components to the measured values.
- Lastly, one can attempt to adjust the theoretical model, in particular when additional **measurements at the magnets** can confirm the experimental findings.

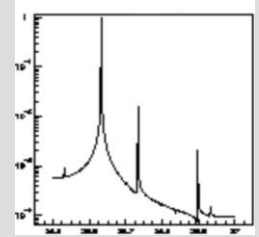


# Effective Model of the LHC (schematic)

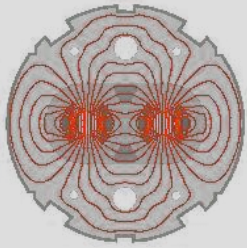




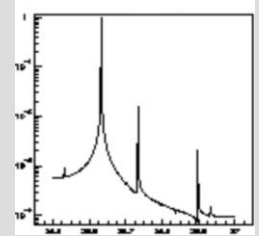
# Optics Code Advancement



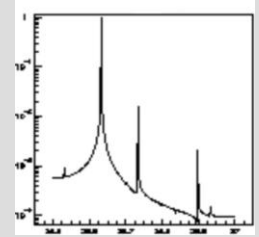
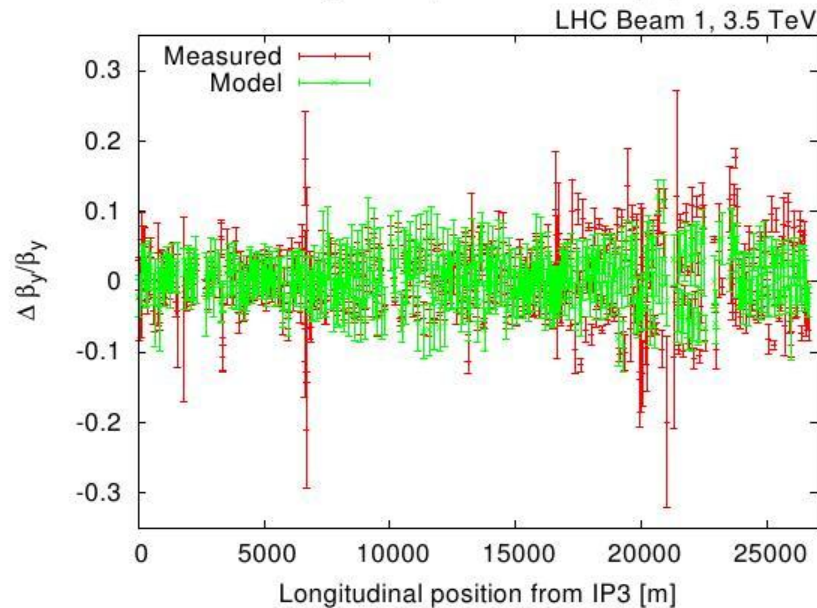
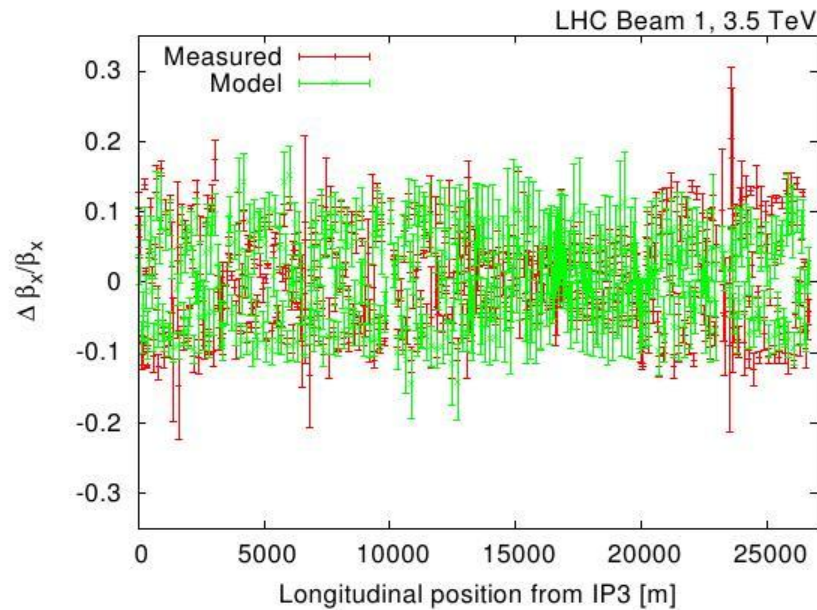
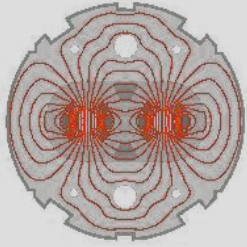
- **MAD-X** has been operational for the entire design phase and the commissioning of the **LHC**.
- Its main advantage is its **input flexibility** and the **many tools** like matching, error assignment etc.
- **MAD-X** transforms the **LHC** optics including harmonics and misalignment into **SixTrack**. All dynamic aperture studies have been performed with **SixTrack** on large computing clusters.
- The main upgrade item has been the inclusion of the **PTC** module with more sophisticated physics models to overcome certain known limitations of **MAD-X**.
- The **PTC** approach allows for a modern design approach which is being applied for the **LHC**.
- **Definitely we have to go further in that direction for future design studies!**



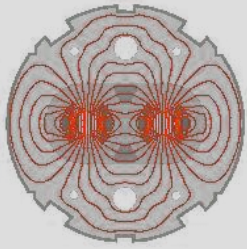
# Second Best Theoretical Model for the LHC



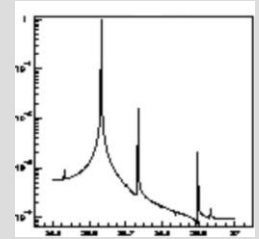
- We are presently preparing the **“second”** best model of the **LHC**. By that I mean that we are operating entirely within the **MAD-X PTC** framework.
- Starting point is the latest optics version of the LHC.
- However we **DO NOT split** its elements to include thin-lens multipole kicks that we have been doing since decades for the dynamic aperture studies.
- Instead we are using **PTC** facilities to apply the harmonics to thick elements.
- We are applying the measured misalignments to all elements. (A reminder: harmonics and misalignments are provided by **Wise**.)
- The measured **LHC** closed-orbit is taking into account which represents the first **“effective”** component of the model.
- We cannot expect that we can reproduce the machine parameters like **closed-orbit, tunes, coupling and chromaticities** and therefore perform **PTC** based matching.
- The first goal is to reproduce the measured beta-beating but n.l. will be next!



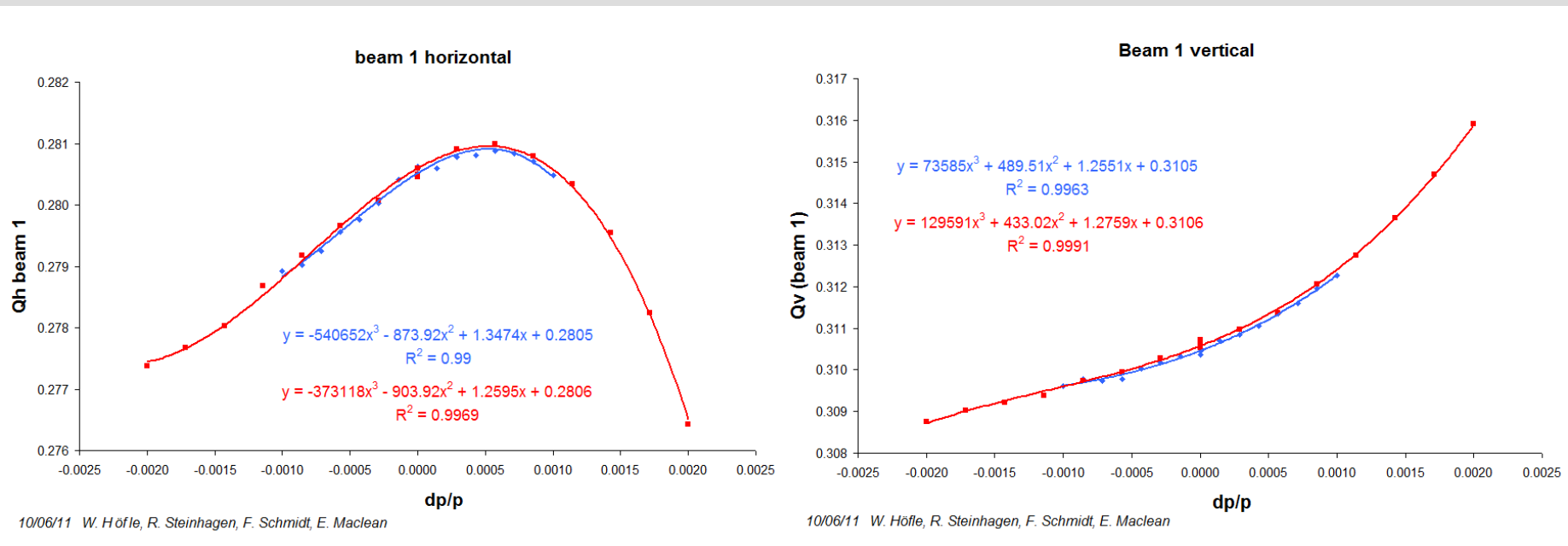
# Effective Modelling of the Beta-beating of the LHC at 3.5 TeV

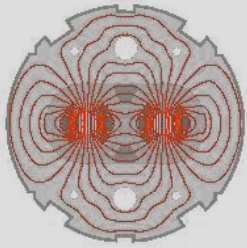


# N.L. Chromaticity Measurements

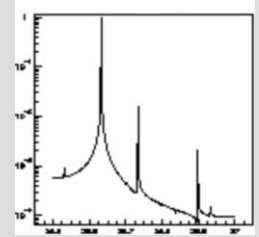


PhD student Ewen Maclean student is presently looking at this in great detail!





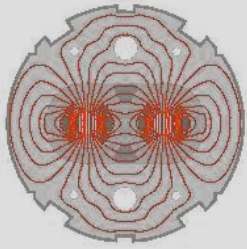
# PTC standalone Model for the LHC



- **PTC** has more powerful features that can presently not be steered by **MAD-X\***.
- The standard **MAD-X** thick lattices of **Beam1** and **Beam2** are used and transferred into **PTC** format.
- Harmonics and misalignment are taken from **WISE** except that the misalignment of both elements and the assemblies will be used separately.
- In a first step the 2 rings are properly separated in the arcs and oriented in **3D** space according to **SURVEY** data. Special care has to be taken in the regions where the arcs join into the common areas.
- Then all assemblies are bound into “**GIRDERS**” and **2-in-1** magnets are linked as “**SIAMESE**” and the misalignments are put into place for both elements and assemblies.
- All harmonics are read-in.
- After attaching the transfer lines in **3D** the **whole super structure** is track-able in both directions.

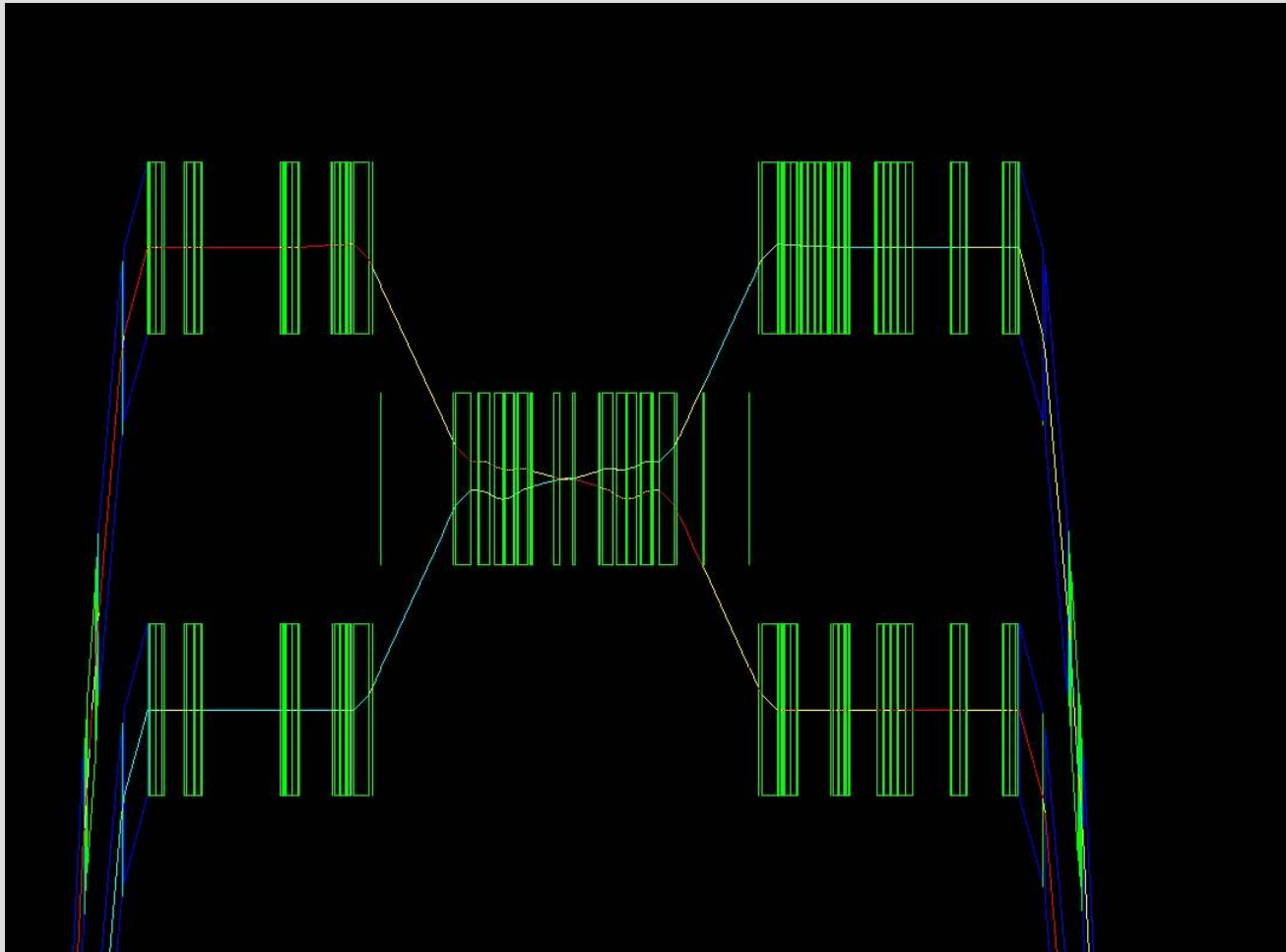
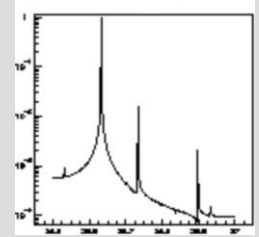
(\* Hans Grote in collaboration with Etienne Forest and myself are planning a MAD-X extension to overcome this problem.)

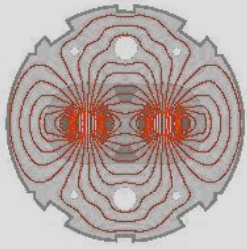




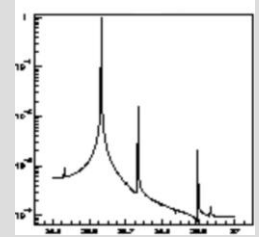
# IR5 of LHC in PTC Stand-alone

PhD student Ewen Maclean student will look into this in more detail!





# Tools for N.L. Analysis and Measurements



- The classical non-linear measurement are:
  - Detuning with Amplitude
  - Resonance Driving-Term Analysis
  - Tune Scan
  - Dynamic Aperture
- The **driving-term analysis** has been advanced in the last **23 years** due to the availability of high resolution **1000 turn BPM** systems.
- This **driving-terms** can be identified at each **BPM** via a harmonic analysis. It allows for a direct comparison with what the **effective model** predicts for the accelerator.
- A simple example of **PSB** shows a driving term correction in practice.
- All that will now be tested for the **LHC**!

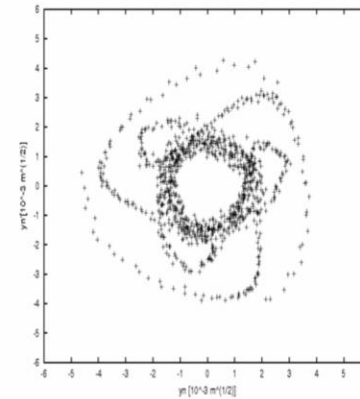
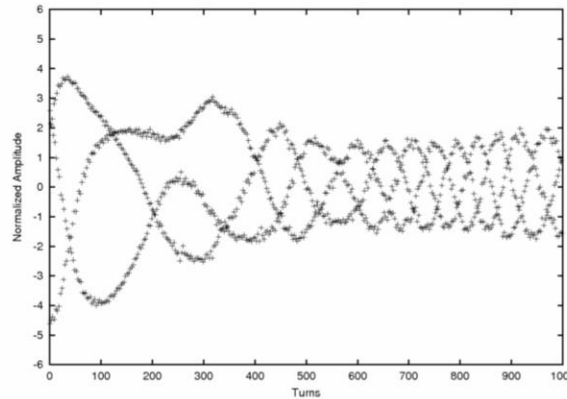
# Results 2003 – systematic $3Q_y=16$

Situation for the bare machine.

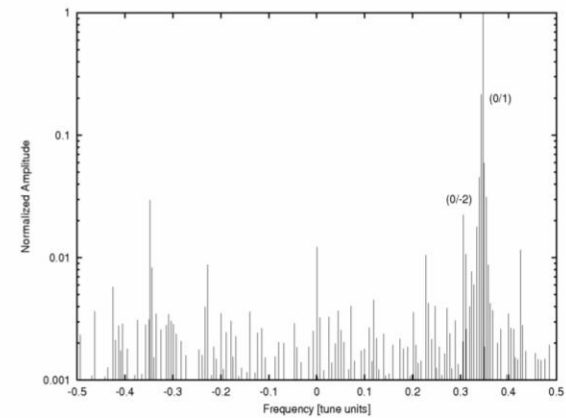
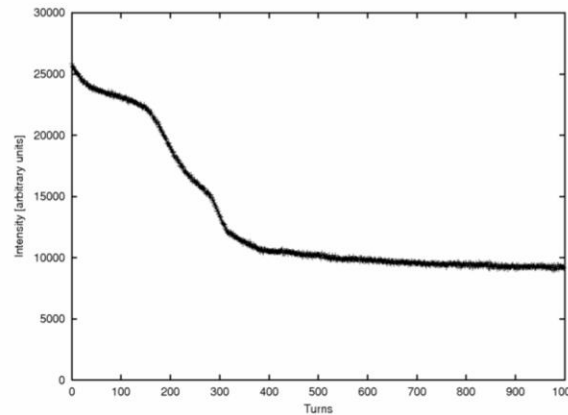
$$|h_{0030}| = 9.0 \pm 0.6^*$$

$$10^{-3} \text{ mm}^{-1/2}$$

$$\psi_{0030} = -21.4^\circ \pm 13.9^\circ$$



Vertical beam position and phase space



Intensity curve and Fourier spectrum (res. line: (0/-2))

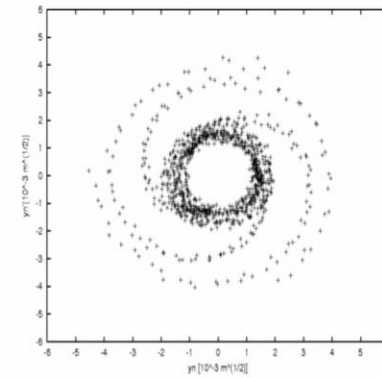
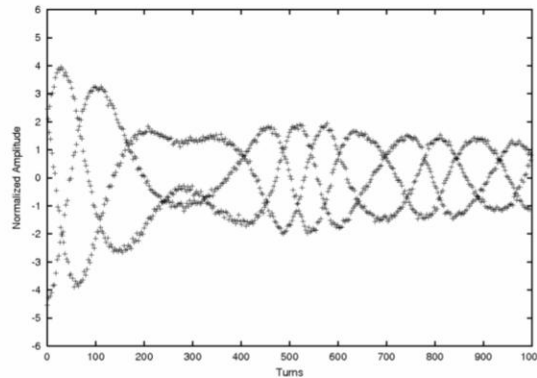
# Results 2003 – $3Q_y=16$

Resonance  
compensated with  
the calculated  
currents:

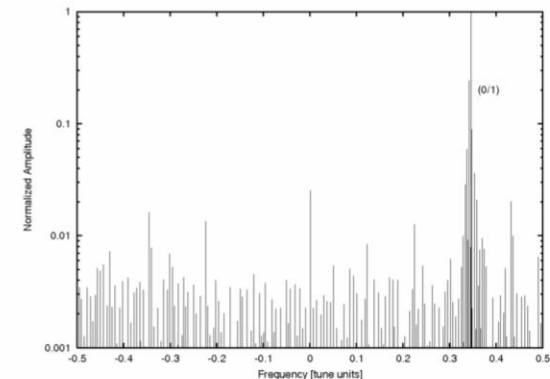
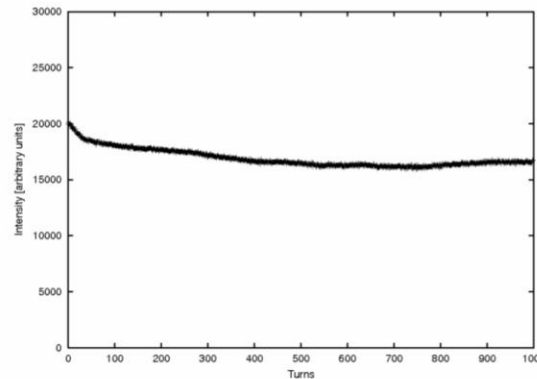
$$I_{\text{XSK2L4}} = -12.3\text{A},$$

$$I_{\text{XSK9L1}} = +15.3\text{A}$$

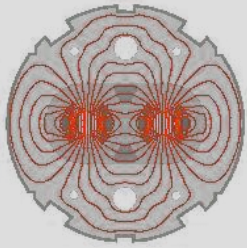
(XSK...skew  
sextupoles)



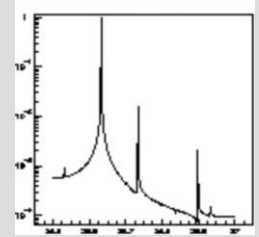
Vertical beam position and phase space



Intensity curve and Fourier spectrum

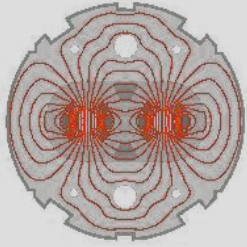


# References I

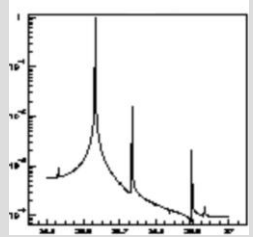


I have collected relevant papers and provide them at: <http://frs.web.cern.ch/frs/Source/OMCM/>

- Fidel working group
  - E. Todesco, <http://fidel.web.cern.ch/fidel/>
  - L. Bottura et al., "FIRST FIELD TEST OF FIDEL THE MAGNETIC FIELD DESCRIPTION FOR THE LHC", in the proceedings of PAC09, Vancouver, BC, Canada.
- Wise team
  - P. Hagen et al., "WISE: A SIMULATION OF THE LHC OPTIC INCLUDING MAGNET GEOMETRICAL DATA", in the Proceedings of 10th European Particle Accelerator Conference (EPAC 06), Edinburgh.
- LSA
  - G. Kruk et al., "LHC SOFTWARE ARCHITECTURE [LSA] – EVOLUTION TOWARD LHC BEAM COMMISSIONING", in the proceedings of ICALEPCS07, Knoxville, Tennessee, USA.
- BBQ
  - M. Gasior et al., "An overview of the LHC Transverse Diagnostics Systems", Proceedings fo BIW'08, CERN BE-2009-002, 2009.
  - R.J. Steinhagen et al., "Advancements in the Base-Band-Tune and Chromaticity Instrumentation [..]", DIPAC'11, 2011.



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- Drivingterm Measurements
  - A. Schoch, “Theory of linear and non-linear perturbations of betatron oscillations in alternating gradient synchrotrons”, CERN Yellow Report 57-21.
  - J. Bengtsson, “NON-LINEAR TRANSVERSE DYNAMICS FOR STORAGE RINGS WITH APPLICATIONS TO THE LOW-ENERGY ANTIPROTON (LEAR) AT CERN”, CERN 88-05, 1988.
  - R. Bartolini and F. Schmidt, “Normal Form via Tracking or Beam Data”, LHC Project Report 132, 1997.
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  - P. Urschütz, “Measurement and Compensation of Betatron Resonances at the CERN PS Booster Synchrotron”, CERN-THESIS-2004-043, Vienna Univ., 2004.