

Effective Lagrangian for a Strongly-Interacting Light Higgs

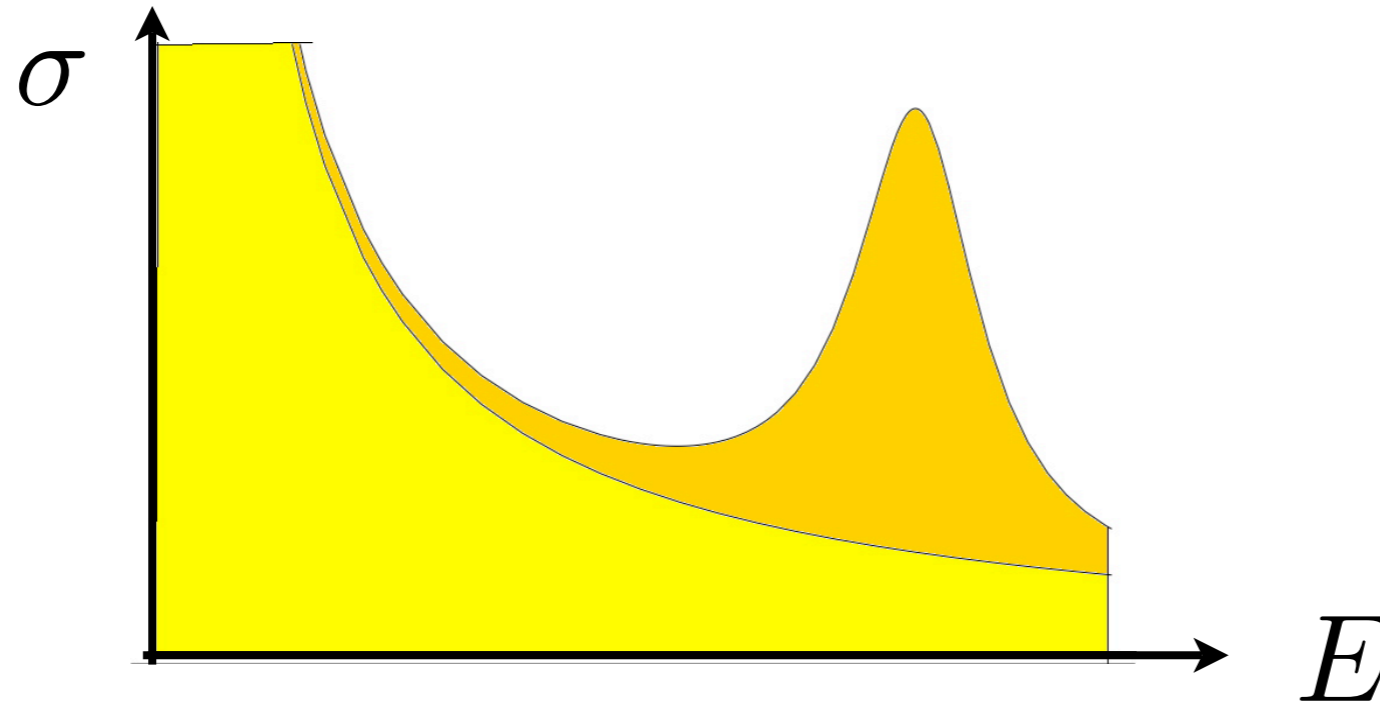
Giudice, Grojean, Pomarol, Rattazzi [hep-ph/0703164](#)

Riccardo Rattazzi



ÉCOLE POLYTECHNIQUE
FÉDÉRALE DE LAUSANNE

Two modes for New Physics discovery: resonances & tails



Ex. : dim = 6 operators from physics at scale m_ρ and coupling g_ρ

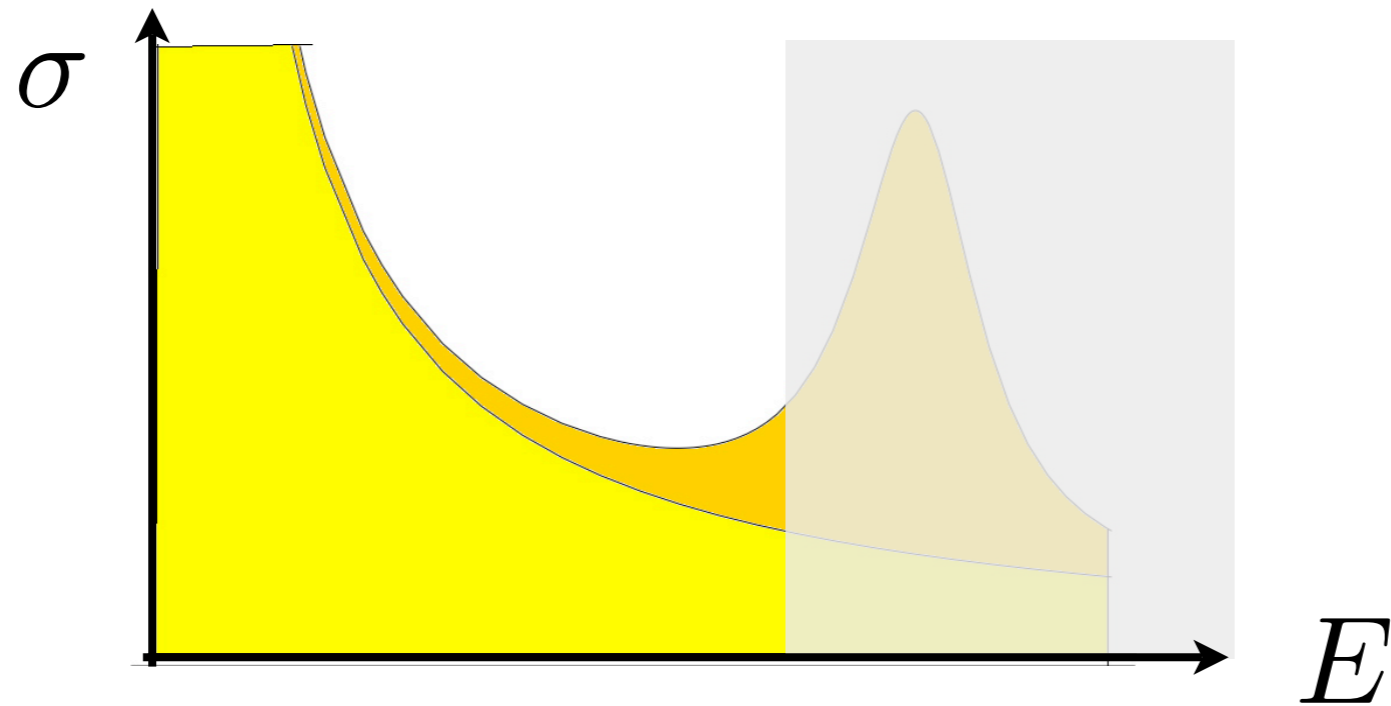
$$\mathcal{L}_{eff} = \frac{g_\rho^2}{m_\rho^2} \mathcal{O}_{d=6}$$

$$m_\rho > E_{beam}$$

Tails are important in the limit

$$g_\rho \text{ large}$$

Two modes for New Physics discovery: resonances & tails



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$g_\rho \sim 4\pi$: compositeness bounds

LEP + Tevatron

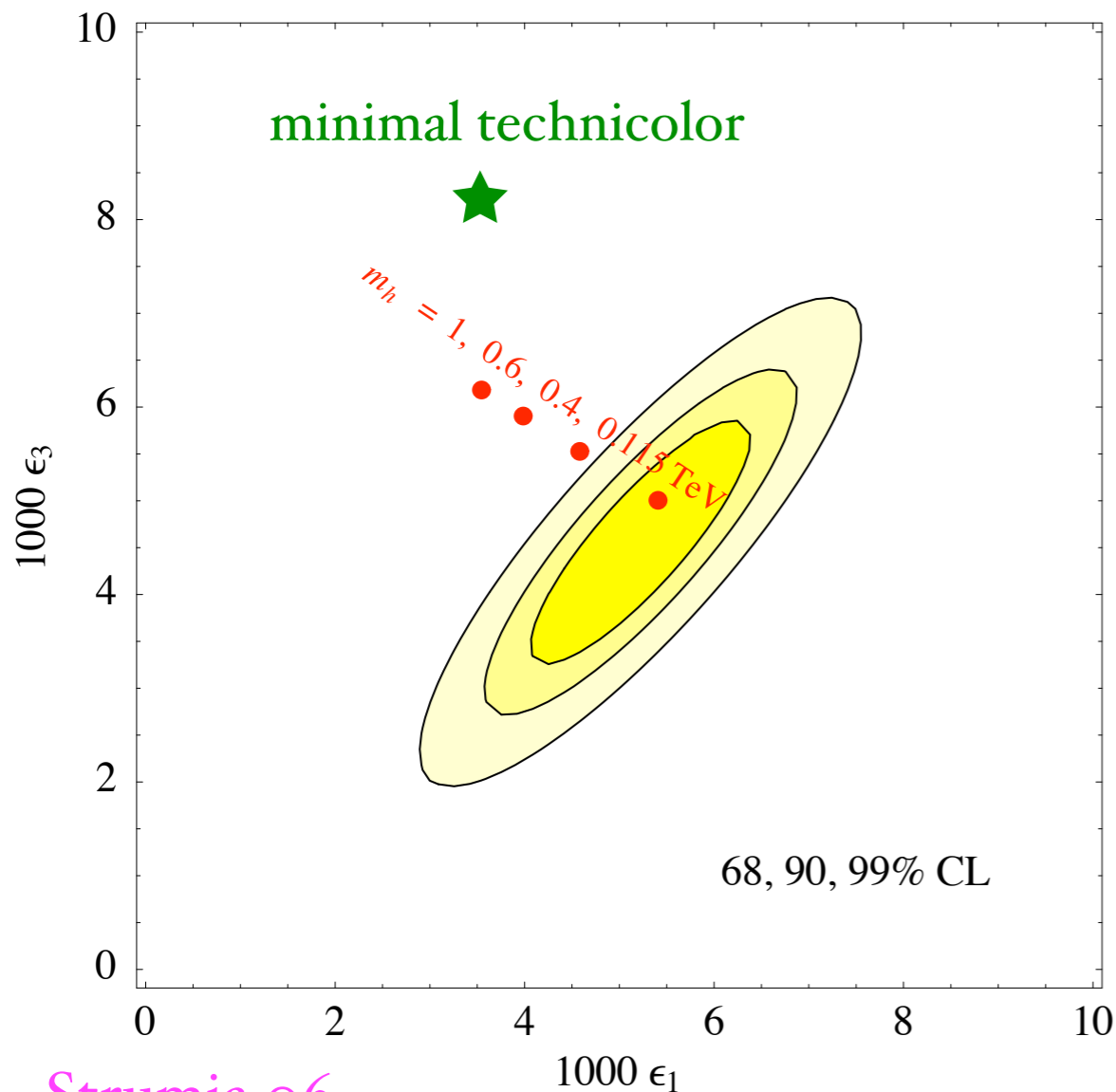
$\mathcal{L}_{4f} = \frac{(4\pi)^2}{\Lambda_c^2} (\bar{e}_L \gamma_\mu e_L) (\bar{e}_L \gamma^\mu e_L)$		$\Lambda_c > 30 \text{ TeV}$
quarks $(\bar{q} \gamma_\mu q)^2$		$\Lambda_c > 9 \text{ TeV}$
quarks & leptons $(\bar{q} \gamma_\mu q)(e \gamma^\mu e)$		$\Lambda_c > 20 \text{ TeV}$
transverse vector bosons:		$\Lambda_c \gtrsim 10 \text{ TeV}$

What about the electroweak breaking sector (eaten Goldstones + ...)?

hierarchy problem better motivates compositeness in this sector

Technicolor: simplest possibility

but most dramatic in that there is not even a narrow Higgs resonance



$$\Delta\epsilon_3 \equiv \hat{S} = \hat{S}_{UV} + \frac{g^2}{96\pi^2} \ln(m_h/m_Z)$$

$$\hat{S}_{UV} \sim \frac{g^2}{96\pi^2} N_{TF} N_{TC}$$

Peskin, Takeuchi '89

$$\Delta\epsilon_1 \equiv \hat{T} = \hat{T}_{UV} + \frac{3g^2 \tan^2 \theta_W}{32\pi^2} \ln(m_h/m_Z)$$

Minimal TC has no parameter to play with in order to reduce \hat{S}



a light pseudo-Goldstone Higgs helps in possibly two ways

Georgi, Kaplan '84
Dimopoulos, Preskill '82
Banks '84

● it screens IR contribution to \hat{S}, \hat{T}

$$\hat{S}_{UV} \simeq \frac{g^2 N}{96\pi^2} \times \frac{v^2}{f^2} \quad \left\{ \begin{array}{l} \langle H \rangle \equiv v \\ f = \text{pseudo-Goldstone decay const.} \end{array} \right.$$

$\frac{v^2}{f^2}$ depends on extra parameters \rightarrow can in principle be tuned to be a little bit smaller than 1

Compositeness scale $4\pi f$ could still be as low as a few TeV

Strong sector
 $H = \mathcal{G}/\mathcal{H}$

(proto)-Yukawas
 \longleftrightarrow
 gauge coupl.

quarks, leptons
 &
 gauge bosons

★ Simplest case:
 '80's

- Strong mass scale = m_ρ
 - NDA coupling $g_\rho \sim 4\pi$
- $$f = \frac{m_\rho}{g_\rho} \sim \frac{m_\rho}{4\pi}$$

★ 'Weakly' coupled version: g_ρ is a free parameter

5D models

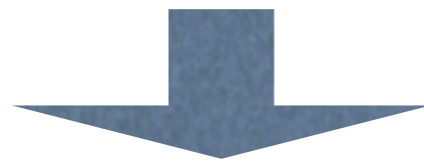
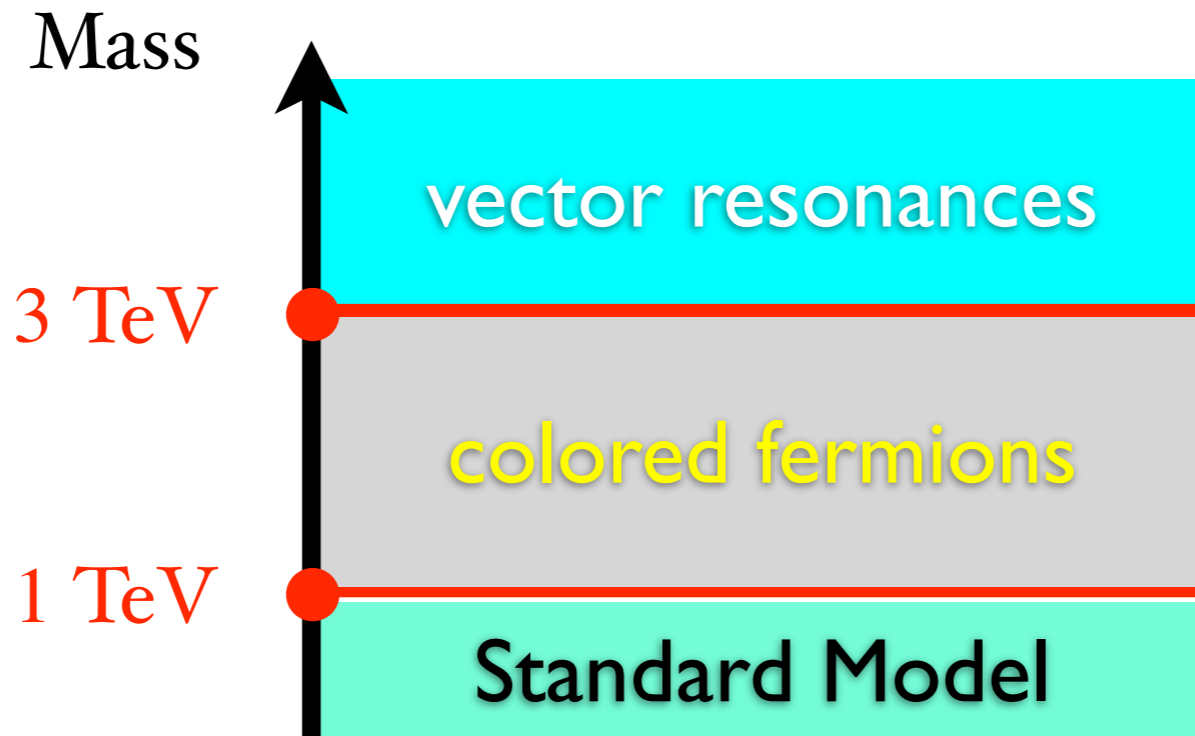
$$m_\rho \sim m_{KK}$$

$$g_\rho \sim g_{KK}$$

Little Higgs

(m_ρ, g_ρ)
 mass and coupling
 of 'regulators'

If



Low-energy effective lagrangian for a composite light Higgs
is a useful tool

$$\mathcal{G}/\mathcal{H} = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix} + \text{no other fields}$$



$$SO(5)/SO(4)$$

$$SU(3)/SU(2) \times U(1)$$

● Agashe, Contino, Pomarol '04: 5D example

● Chang '03: $SO(9)/SO(5) \times SO(4)$ LH model with 'strongish' extra gauge groups

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Custodial Symmetry

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★ Derive (m_ρ, g_ρ) dependence of dim = 6 effective low-energy lagrangian

$$U = e^{iH/f} \quad f = \frac{m_\rho}{g_\rho}$$

$$\mathcal{L}_{strong} = \frac{m_\rho^4}{g_\rho^2} \left[\mathcal{L}^{(0)}(U, \partial/m_\rho) + \frac{g_\rho^2}{(4\pi)^2} \mathcal{L}^{(1)}(U, \partial/m_\rho) + \dots \right] + \mathcal{L}_{break}(U, \Phi_{SM})$$

● each extra H leg costs $\frac{g_\rho}{m_\rho}$

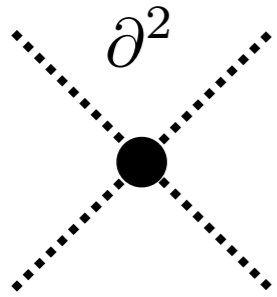
Basic
rules

● each extra ∂_μ costs $\frac{1}{m_\rho}$

$$\partial_\mu \rightarrow \partial_\mu + iA_\mu$$
$$\frac{\partial^2}{m_\rho^2} \rightarrow \frac{F_{\mu\nu}}{m_\rho^2}$$

'Higgs field insertions'

1)



$$\frac{g_\rho^2 \partial^2}{m_\rho^2} = \frac{\partial^2}{f^2}$$

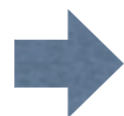
$$\frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{c_T}{2f^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \left(H^\dagger \overleftrightarrow{D}_\mu H \right)$$

$$\left\{ \begin{array}{l} \frac{1}{f^2} H^\dagger H |D_\mu H|^2 \sim \frac{1}{f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \text{non-derivative terms} \\ \text{by field redefinition} \quad H^\alpha \rightarrow H^\alpha + (H^\dagger H) H^\alpha / f^2 \end{array} \right.$$

$$2) \quad \lambda_H (H^\dagger H)^2 \rightarrow \mathcal{O}_6 = c_6 \frac{\lambda_H}{f^2} (H^\dagger H)^3$$

$$3) \quad y_{ij} \bar{\psi}_i H \psi_j \rightarrow \mathcal{O}_y = c_y y_{ij} \bar{\psi}_i H \psi_j \frac{H^\dagger H}{f^2}$$

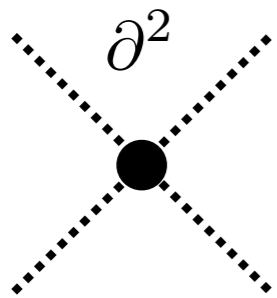
minimal flavor violation



just one universal operator

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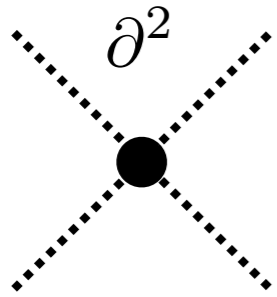
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minimal flavor violation



just one universal operator

2 Higgses & 4 covariant derivatives (CP conserving)

$$\mathbf{1)} \quad O_W = i \frac{c_W}{m_\rho^2} \left(H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i \quad O_B = i \frac{c_B}{m_\rho^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu})$$

- generated at tree level by massive vector exchange

$$\bullet \quad \widehat{S} = (c_W + c_B) \frac{m_W^2}{m_\rho^2} \quad m_\rho \gtrsim (c_W + c_B)^{1/2} 2.5 \text{ TeV} \quad \text{at } 95\% \text{ CL}$$

$$\frac{v^2}{f^2} \lesssim \frac{1.5}{c_W + c_B} \left(\frac{g_\rho}{4\pi} \right)^2$$

In a maximally strongly coupled theory f could well be quite low

$$\widehat{S} \sim \frac{g^2}{16\pi^2} \times \frac{16\pi^2}{g_\rho^2} \times \frac{v^2}{f^2}$$

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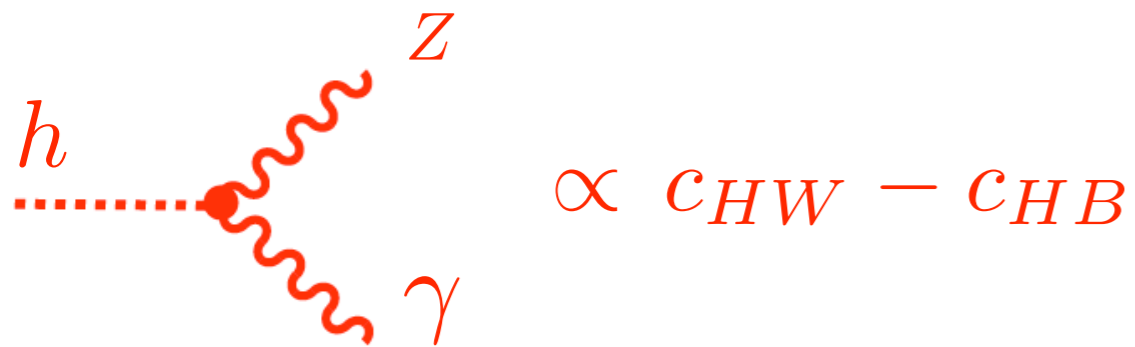
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$$\widehat{S} \sim \frac{g^2}{16\pi^2} \times N \times \frac{v^2}{f^2}$$

$$2) O_{HW} = i \frac{c_{HW}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i$$

$$O_{HB} = i \frac{c_{HB}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$



$$(g - 2)_W \propto c_{HW} + c_{HB}$$

one does not expect these effects by integrating out heavy modes at tree level in a minimally coupled gauge theory \longrightarrow 1-loop suppression

$$3) \frac{c_\gamma}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \left(\frac{g}{g_\rho} \right)^p H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

minimal coupling

Goldstone shift symmetry

the gauging of $U(1)_{EM}$ preserves the shift symmetry of neutral Higgs

$$\frac{c_\gamma}{m_\rho^2} \frac{g^2}{16\pi^2} H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\frac{c_g}{m_\rho^2} \frac{\lambda_t^2}{16\pi^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}$$

- analogous results apply for Higgs coupling to gluons
- gauging color is consistent with the whole Higgs multiplet being exactly a Goldstone

◆ ‘New Couplings’

$$\mathcal{L}_{NC} = \frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) - \frac{c_6 \lambda}{f^2} (H^\dagger H)^3 + \left(\frac{c_y y}{f^2} H^\dagger H \bar{\psi}_L H \psi_R + \text{h.c.} \right)$$

$$\frac{\delta \mathcal{A}}{\mathcal{A}_{SM}} \sim \frac{v^2}{f^2}$$

◆ ‘Form Factors’

$$\mathcal{L}_{FF} = \frac{ic_W}{2m_\rho^2} \left(H^\dagger \sigma^i \overleftrightarrow{D}^{\vec{\mu}} H \right) (D^\nu W_{\mu\nu})^i + \frac{ic_B}{2m_\rho^2} \left(H^\dagger \overleftrightarrow{D}^{\vec{\mu}} H \right) (\partial^\nu B_{\mu\nu}) + \frac{c_\gamma g^2}{16\pi^2 m_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g y_t^2}{16\pi^2 m_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}$$

$$\frac{\delta \mathcal{A}}{\mathcal{A}_{SM}} \sim \frac{E^2}{m_\rho^2}$$

◆ ‘Special Form Factors’

$$\frac{i c_{HW}}{16\pi^2 f^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{i c_{HB}}{16\pi^2 f^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

in principle they test
the strong dynamics

$$\frac{\delta\Gamma(h \rightarrow \gamma Z)}{\Gamma(h \rightarrow \gamma Z)_{SM}} \sim (c_{HW} - c_{HB}) \frac{v^2}{f^2}$$

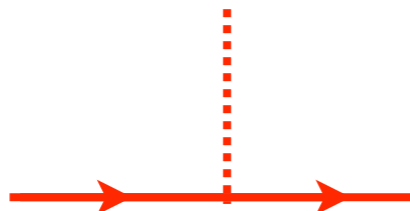
however this process is hard to measure and the well measured
observables are affected as

$$\frac{\delta\mathcal{A}}{\mathcal{A}_{SM}} \sim \frac{E^2}{m_\rho^2} \frac{g_\rho^2}{16\pi^2}$$

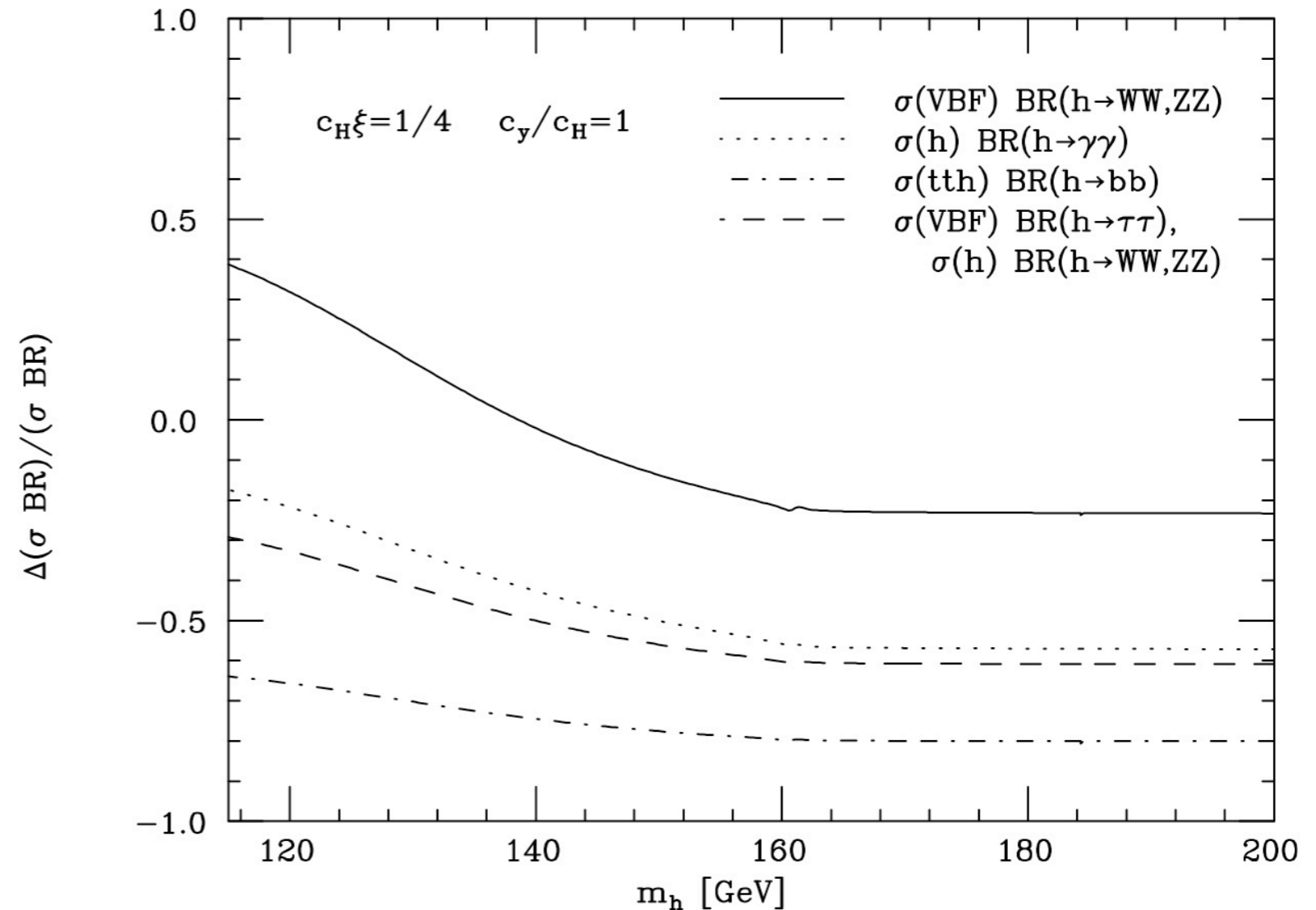
Effects in Higgs production & decay

all couplings rescaled by

$$c_H \longrightarrow \mathcal{L}_{kin} = \frac{1}{2} \left(1 + c_H \frac{v^2}{f^2} \right) \partial_\mu h \partial^\mu h \quad \frac{1}{\sqrt{1 + c_H \frac{v^2}{f^2}}} \simeq 1 - c_H \frac{v^2}{2f^2}$$

$$c_y \longrightarrow \frac{m_\psi}{v} \left(1 - c_y \frac{v^2}{f^2} \right)$$


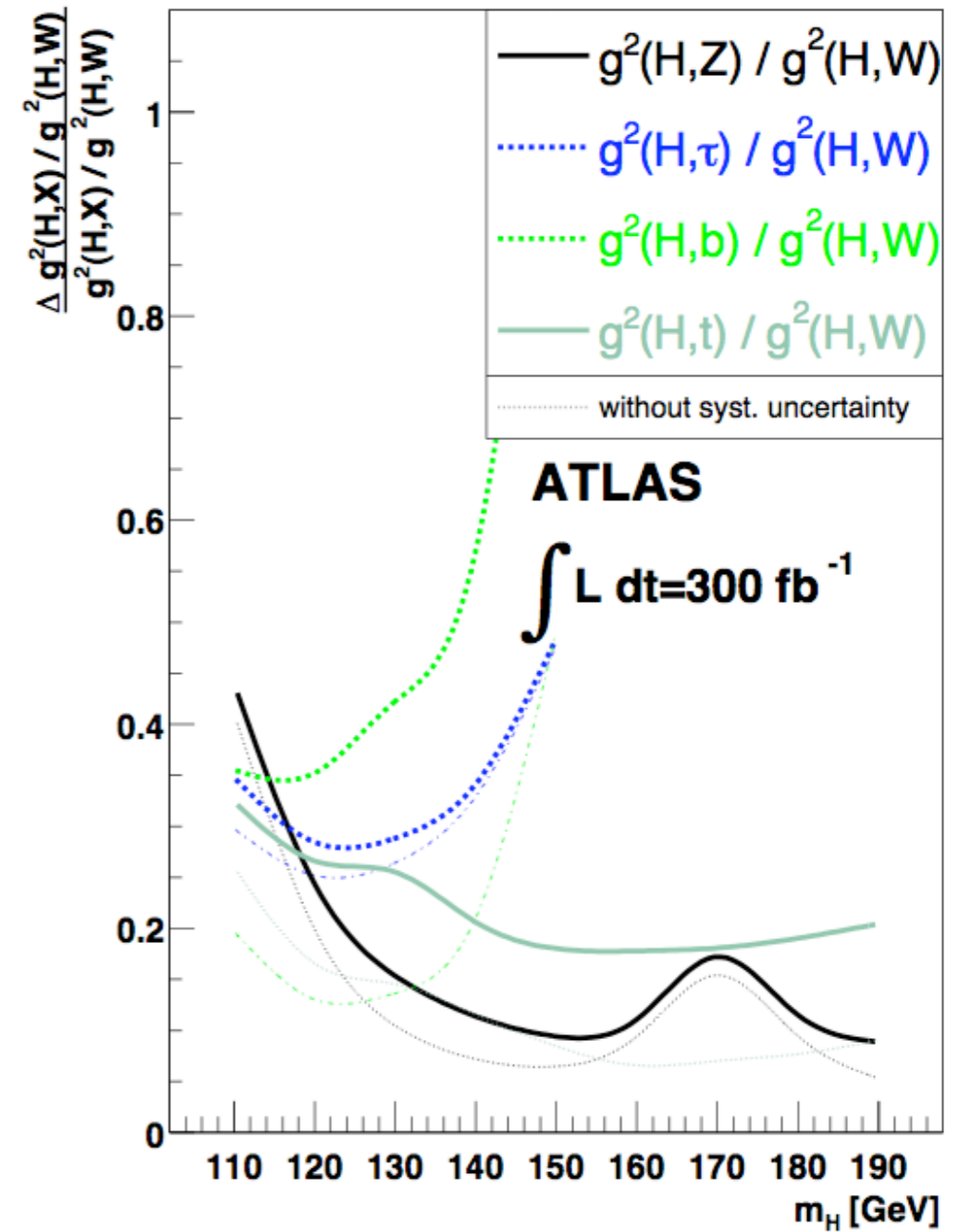
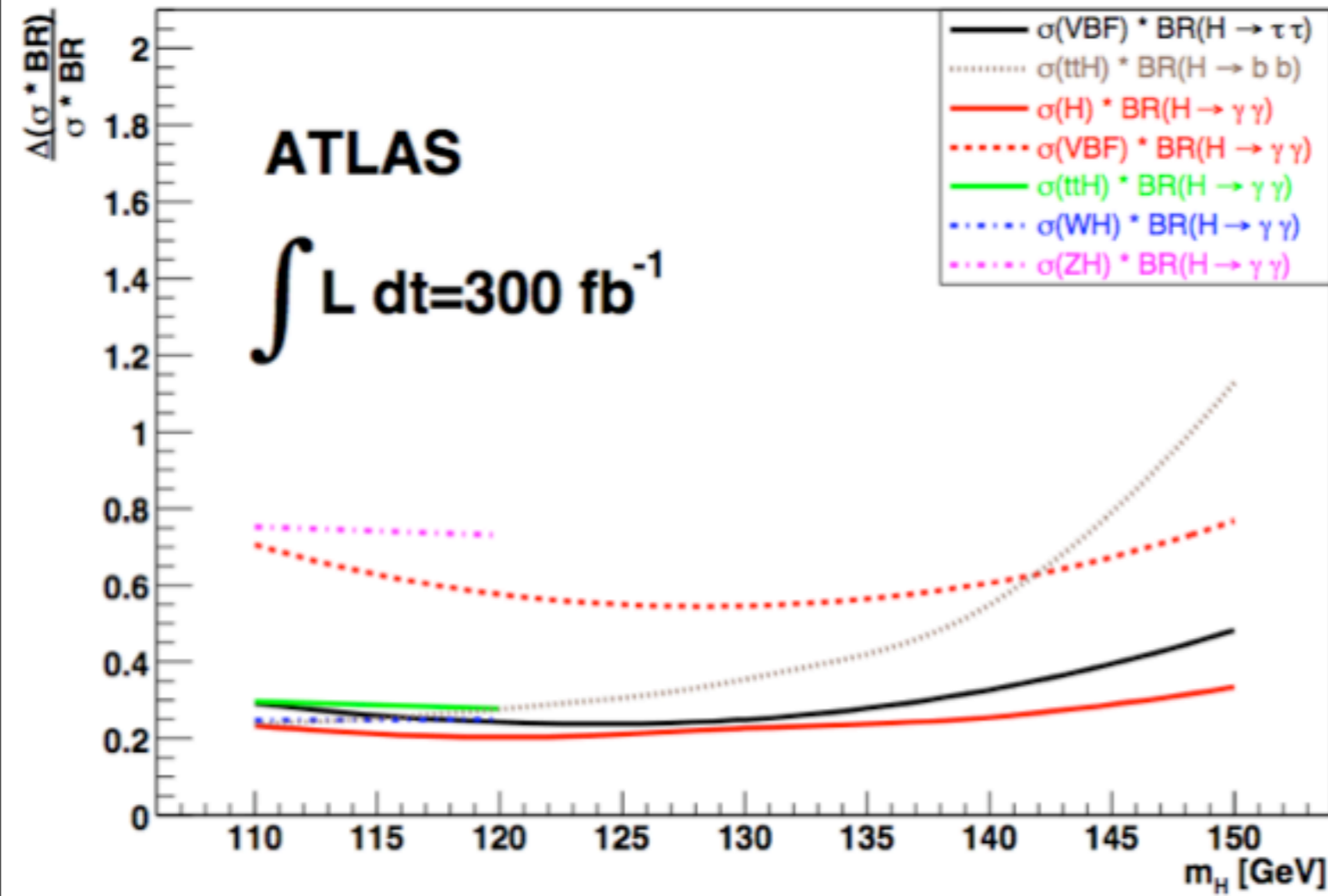
$$\frac{\Delta(\sigma(\text{prod}) \times \text{Br})}{(\sigma(\text{prod}) \times \text{Br})_{SM}} = \#c_H \frac{v^2}{f^2} + \#c_y \frac{v^2}{f^2}$$





at LHC can measure $c_y \frac{v^2}{f^2}, c_H \frac{v^2}{f^2}$ up to 20-40 %

Duhrssen 03



A sizeable deviation from SM in the absence of new light states would be indirect evidence for the composite nature of the Higgs

- At ILC one would test $\frac{v^2}{f^2}$ at % level

Barger, Han, Langacker,
McElrath, Zerwas 03

J.A. Aguilar Saavedra et al.
[ECFA/DESY LC Physics WG]

Coupling	$M_H = 120 \text{ GeV}$	140 GeV
g_{HWW}	± 0.012	± 0.020
g_{HZZ}	± 0.012	± 0.013
g_{Htt}	± 0.030	± 0.061
g_{Hbb}	± 0.022	± 0.022
g_{Hcc}	± 0.037	± 0.102
$g_{H\tau\tau}$	± 0.033	± 0.048
g_{HWW}/g_{HZZ}	± 0.017	± 0.024
g_{Htt}/g_{HWW}	± 0.029	± 0.052
g_{Hbb}/g_{HWW}	± 0.012	± 0.022
$g_{H\tau\tau}/g_{HWW}$	± 0.033	± 0.041
g_{Htt}/g_{Hbb}	± 0.026	± 0.057
g_{Hcc}/g_{Hbb}	± 0.041	± 0.100
$g_{H\tau\tau}/g_{Hbb}$	± 0.027	± 0.042

- Also test deviation from SM in Higgs potential $\frac{c_6 \lambda}{f^2} (H^\dagger H)^3$

$$c_6 \frac{v^2}{f^2} < 20\%$$

ILC can rule out Higgs compositeness scale $4\pi f$ below 30 TeV

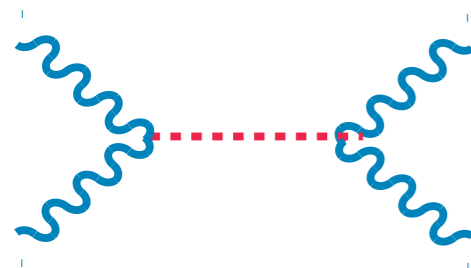
Direct signal of Higgs compositeness

$$\frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H)$$


 equivalence theorem

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow W_L^+ W_L^-) = \mathcal{A}(W_L^+ W_L^- \rightarrow Z_L^0 Z_L^0) = -\mathcal{A}(W_L^\pm W_L^\pm \rightarrow W_L^\pm W_L^\pm) = \frac{c_H s}{f^2}$$

$$\mathcal{A}(W^\pm Z_L^0 \rightarrow W^\pm Z_L^0) = \frac{c_H t}{f^2}, \quad \mathcal{A}(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) = \frac{c_H (s+t)}{f^2}$$


 $\propto 1 - c_H \frac{v^2}{f^2}$ fails to unitarize the amplitude

$$\sigma(pp \rightarrow V_L V_L' X)_{c_H} = \left(c_H \frac{v^2}{f^2} \right)^2 \sigma(pp \rightarrow V_L V_L' X)_H$$

leptonic and semileptonic
vector decay channels
with 300 fb^{-1}

sensitivity \longrightarrow

$$c_H \frac{v^2}{f^2} = 0.5 - 0.7$$

Bagger et al., '95
Butterworth et al., '02

$O(4)$ symmetry: Higgs is approximately a 4th (uneaten) Goldstone

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow hh) = \mathcal{A}(W_L^+ W_L^- \rightarrow hh) = \frac{c_H s}{f^2}$$

↓ sum rule

$$2\sigma_{\Delta\eta}(pp \rightarrow hhX)_{c_H} = \sigma_{\Delta\eta}(pp \rightarrow W_L^+ W_L^- X)_{c_H} + \frac{1}{6} \left(9 - \tanh^2 \frac{\Delta\eta}{2}\right) \sigma_{\Delta\eta}(pp \rightarrow Z_L^0 Z_L^0 X)_{c_H}$$

$$= O(\text{fb}) \times \left(c_H \frac{v^2}{f^2}\right)^2 \quad \text{for } m_{hh} > 1 \text{ TeV}$$

◆ $hh \rightarrow bbbb$ tough QCD background, but worth a try

- high p_T of b jets
- signal rather clean from minijets
- can use forward jet tag
- can use jet structure

Butterworth, Cox, Forshaw 02

Baur, Plehn, Rainwater 03

Pierce, Thaler, Wang 06

◆ $hh \rightarrow 4W \rightarrow \ell^\pm \ell^\pm \nu\nu jets$ more promising

Trilinear vector boson couplings

$$\mathcal{L}_V = -ig \cos \theta_W g_1^Z Z^\mu (W^{+\nu} W_{\mu\nu}^- - W^{-\nu} W_{\mu\nu}^+) \\ -ig (\cos \theta_W \kappa_Z Z^{\mu\nu} + \sin \theta_W \kappa_\gamma A^{\mu\nu}) W_\mu^+ W_\nu^-$$

$$g_1^Z = \frac{m_Z^2}{m_\rho^2} \left[c_W + \left(\frac{g_\rho}{4\pi} \right)^2 c_{HW} \right]$$

$$\kappa_\gamma = \frac{m_W^2}{m_\rho^2} \left(\frac{g_\rho}{4\pi} \right)^2 (c_{HW} + c_{HB}), \quad \kappa_Z = g_1^Z - \tan^2 \theta_W \kappa_\gamma$$

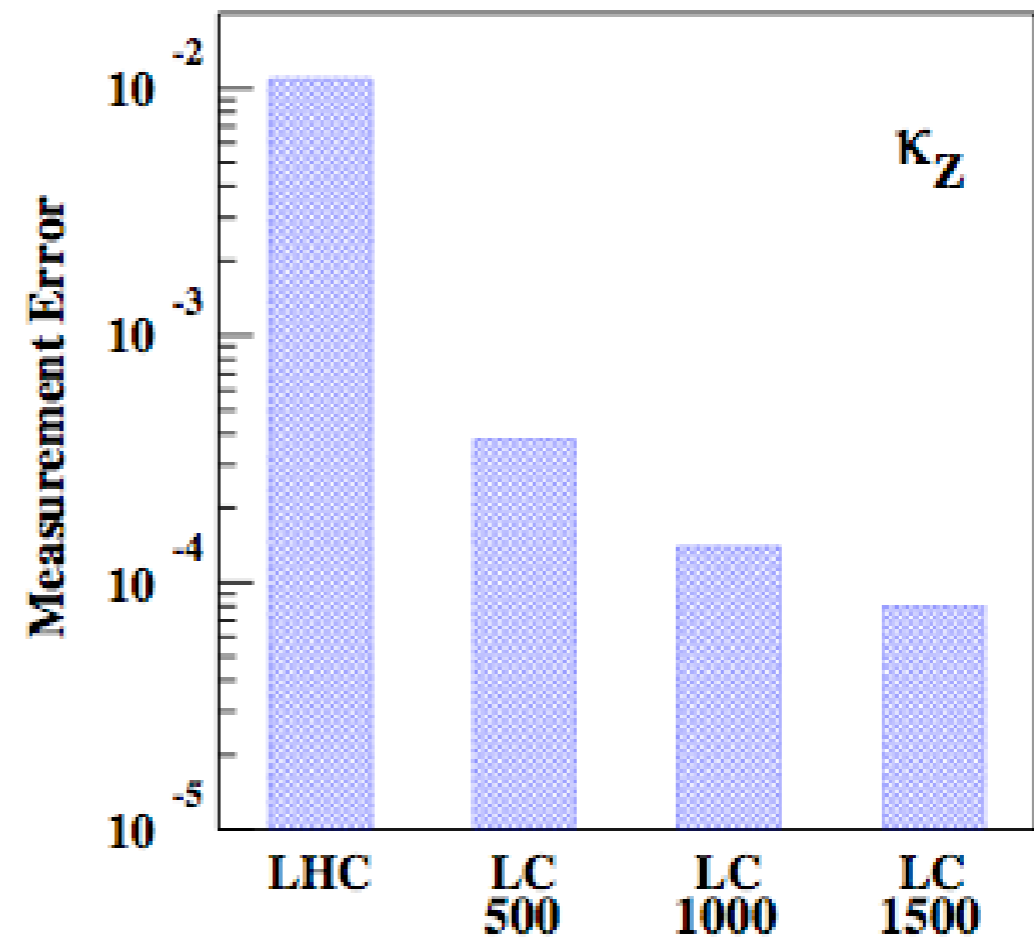
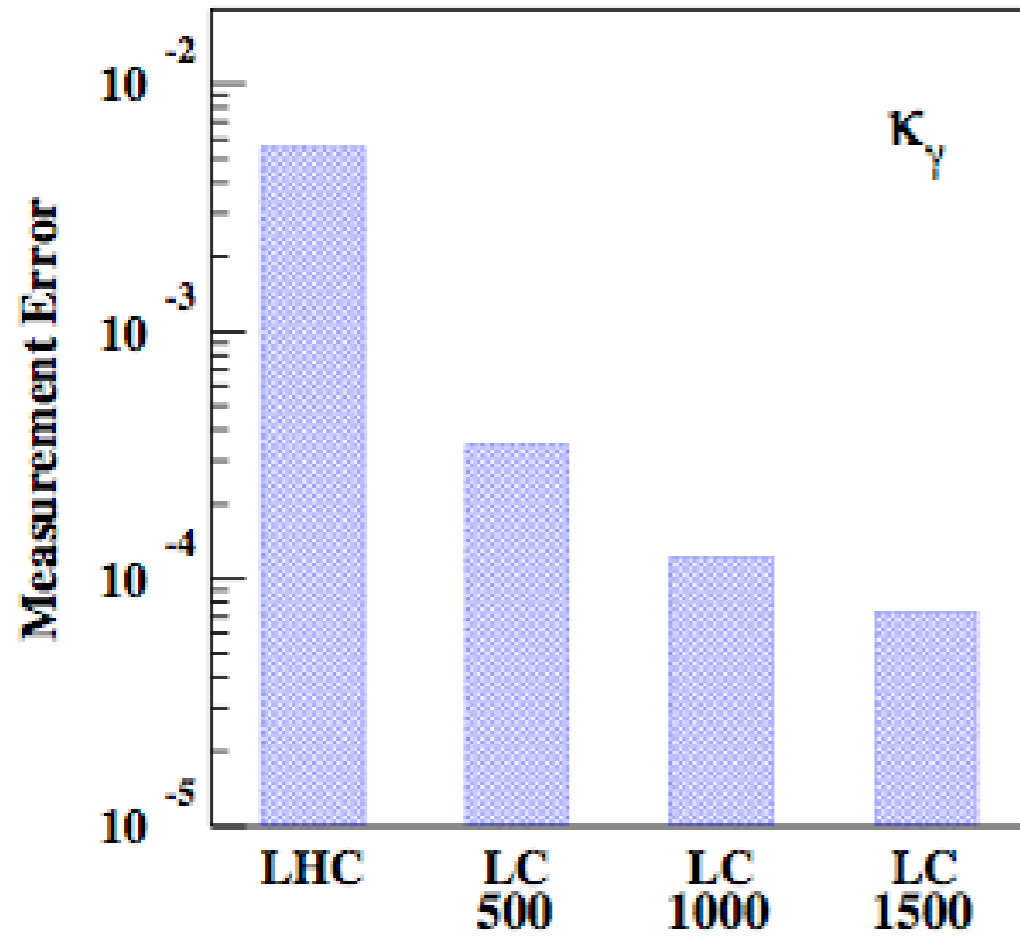
other trilinears $\lambda_{Z,\gamma} \sim \frac{\alpha_W}{4\pi} k_{Z,\gamma} \longrightarrow$ negligible

LHC with 100 fb^{-1} can test down to $g_1^Z = 1\%$, $k_{Z,\gamma} = 5\%$

weaker sensitivity on m_ρ than from direct production of heavy states

or than LEP bound $\hat{S} < 2 \times 10^{-3}$

Trilinears at ILC



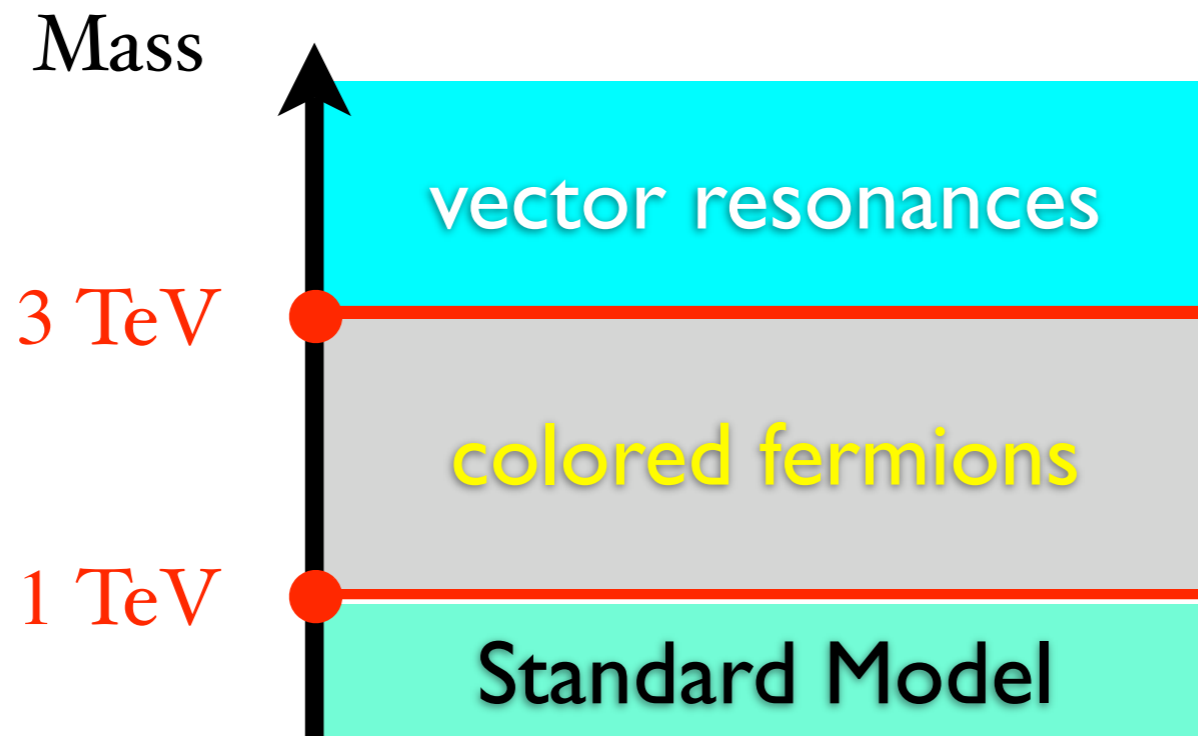
T.Abe et al., [American Linear Collider Working Group]
Snowmass 2001.

indirect reach

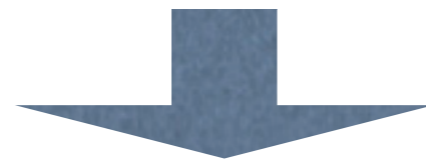
$$m_\rho = 6 - 8 \text{ TeV}$$

in NDA limit $g_\rho = 4\pi$

If

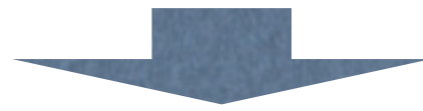


A 'precision' study of Higgs properties would help understanding the origin of the weak scale



Low-energy effective lagrangian description for a composite light Higgs

Custodial & Goldstone Symmetry + Minimal Flavor Violation



3 leading operators

$$\frac{c_H}{2f^2} [\partial_\mu (H^\dagger H)]^2$$

$$\frac{c_6 \lambda}{f^2} (H^\dagger H)^3$$

$$\frac{c_y y_{ij}}{f^2} H^\dagger H \bar{\psi}_L^i H \psi_R^j$$

Most analyses focus instead on $H^\dagger H F_{\mu\nu} F^{\mu\nu}$

Manohar, Wise 06

◆ Single Higgs production with 300 fb^{-1} $\longrightarrow \frac{v^2}{f^2} \lesssim 0.2$

◆ $W_L W_L$ scattering emerges as a relevant process to study even in the presence of a light Higgs

◆ $W_L W_L \rightarrow hh$

◆ ILC, with 500 fb^{-1} and $\sqrt{s} = 500 \text{ GeV}$ $\longrightarrow \frac{v^2}{f^2} \lesssim 10^{-2}$

$$4\pi f \gtrsim 30 \text{ TeV}$$

Drell-Yan production of heavy resonances



$$\sigma(pp \rightarrow \rho_H^\pm + X) = \left(\frac{4\pi}{g_\rho}\right)^2 \left(\frac{3 \text{ TeV}}{m_\rho}\right)^6 0.5 \text{ fb}$$

at fixed $f = \frac{m_\rho}{g_\rho}$ resonances are increasingly harder to see as $g_\rho \rightarrow 4\pi$

- broad & heavy
- couple weakly to SM fermions