

UT angles and sides measurement at BaBar

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*On behalf of **BaBar** Collaboration*



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Outline



- Introduction
- UT sides measurements
 - $|V_{cb}|$
 - $|V_{ub}|$
 - $|V_{td}/V_{ts}|$ \longrightarrow See D. Monorchio's talk
- UT angles measurements
 - β
 - γ
 - α
- Conclusions



Introduction



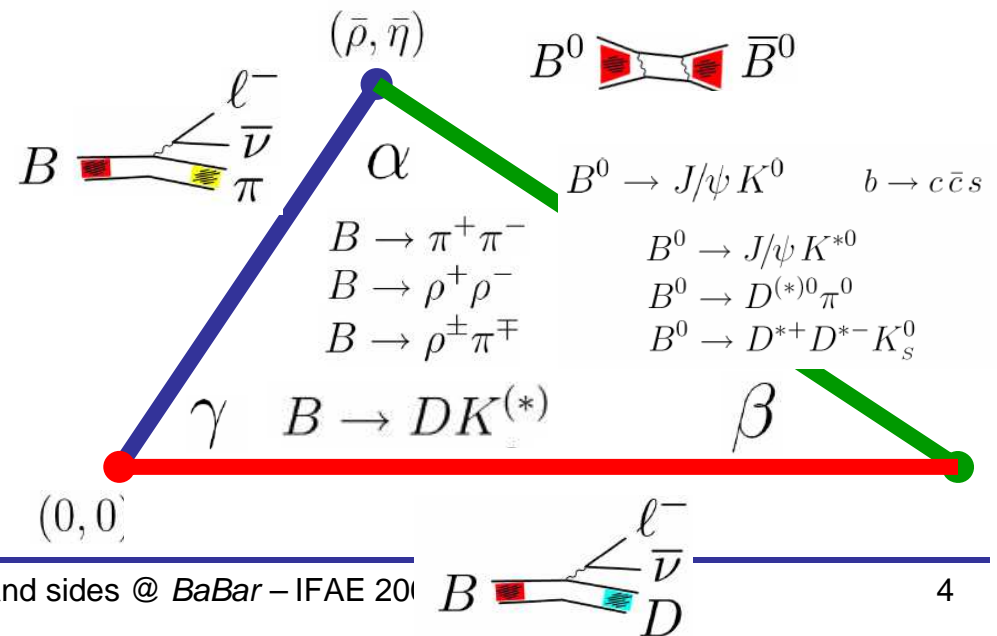
Quark mixing matrix

- weak and mass eigenstates of the quarks are not the same
- changes in base are described by unitarity transformations

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$V_{td}V_{tb}^* + V_{cd}V_{cb}^* + V_{ud}V_{ub}^* = 0$$

- Cabibbo Kobayashi Maskawa (CKM) matrix
- with 3 quark families there is an irreducible complex phase in the matrix, responsible of CP Violation in Standard Model (SM)

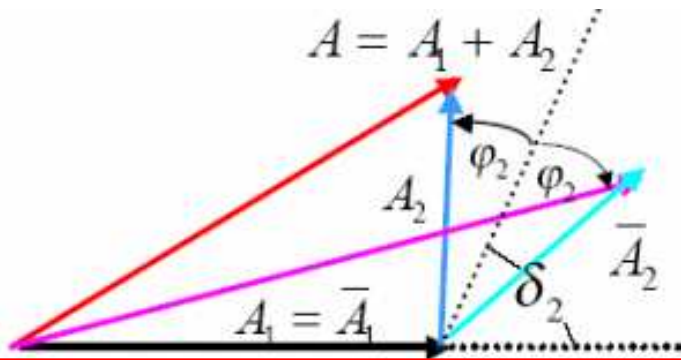




CP Violation: three types

1. Direct CP violation in the decay

$$\left| \langle f | B^0 \rangle \right|^2 \neq \left| \langle \bar{f} | \bar{B}^0 \rangle \right|^2$$



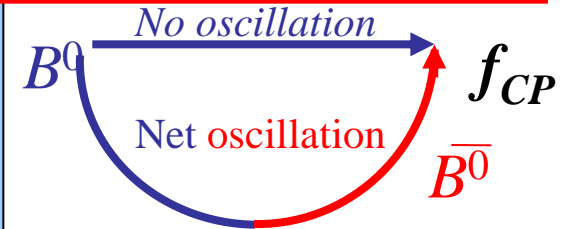
2. CP violation in mixing

$$\left| \langle f | B^0 \rangle \right| \neq \left| \langle \bar{f} | \bar{B}^0 \rangle \right|$$

$$\left| \frac{q}{p} \right| = \sqrt{\frac{(M_{12}^* - i \frac{\Gamma_{12}^*}{2})}{(M_{12} - i \frac{\Gamma_{12}}{2})}} \neq 1$$

SM predicts: $\left| \frac{q}{p} \right| - 1 \approx 4\pi \frac{m_c^2}{m_t^2} \sin \beta \approx 5 \times 10^{-4}$

3. Interference between mixing & decay



$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}$$

$$S_{f_{CP}} = \frac{-2 \text{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}$$

$$\lambda_{f_{CP}} = \frac{q}{p} \frac{\bar{A}}{A}$$

$$A_{f_{CP}}(t) = \frac{\Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP}) - \Gamma(B_{phys}^0(t) \rightarrow f_{CP})}{\Gamma(B_{phys}^0(t) \rightarrow f_{CP}) + \Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP})}$$

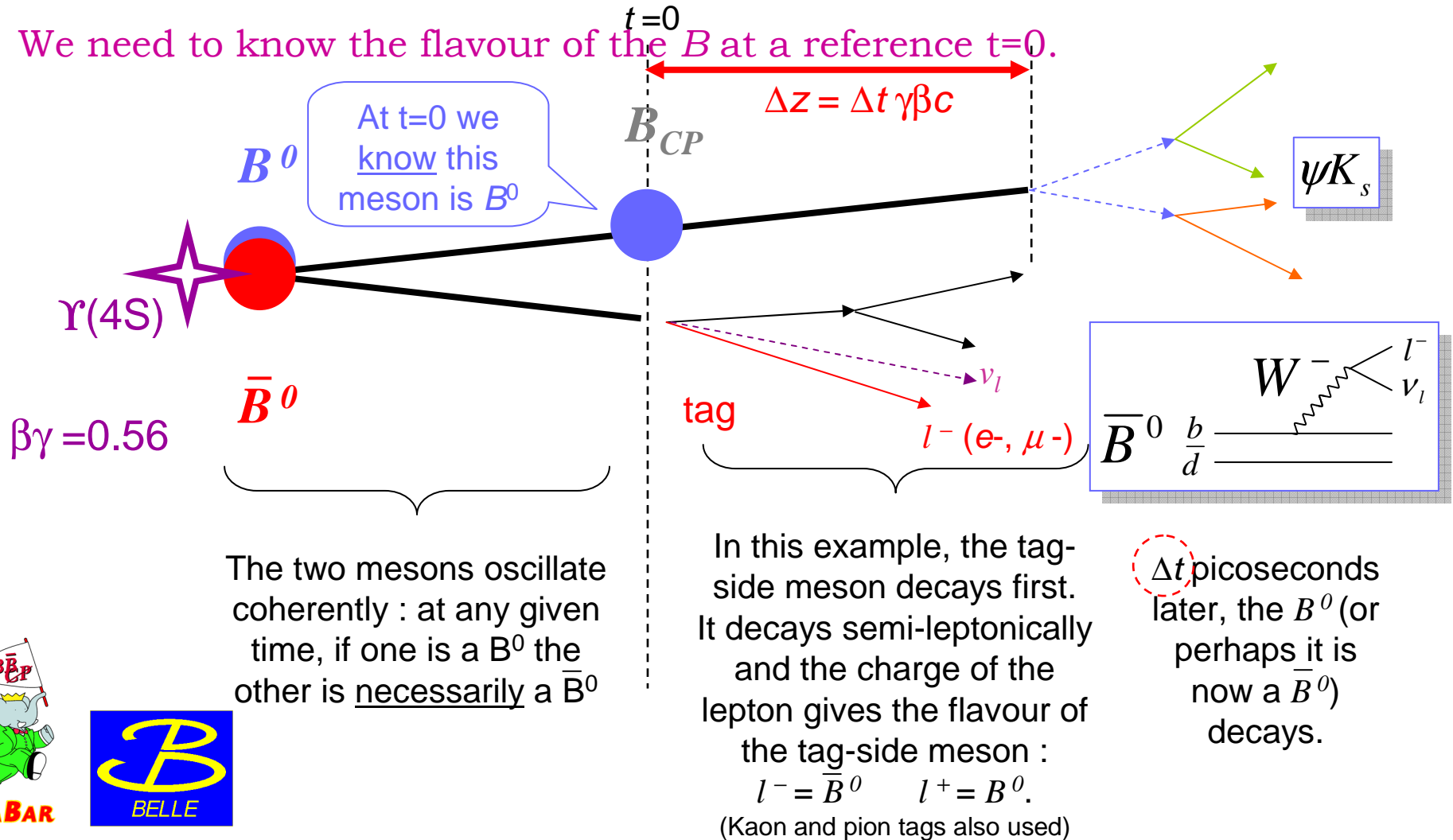
$$A_{f_{CP}} = -C_{f_{CP}} \cos(\Delta m t) + S_{f_{CP}} \sin(\Delta m t)$$



CPV measurements at B-factories



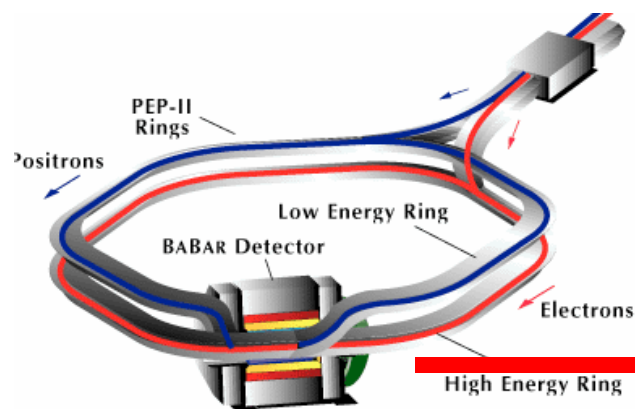
We need to know the flavour of the B at a reference $t=0$.





BaBar Experiment

PEP-II at SLAC

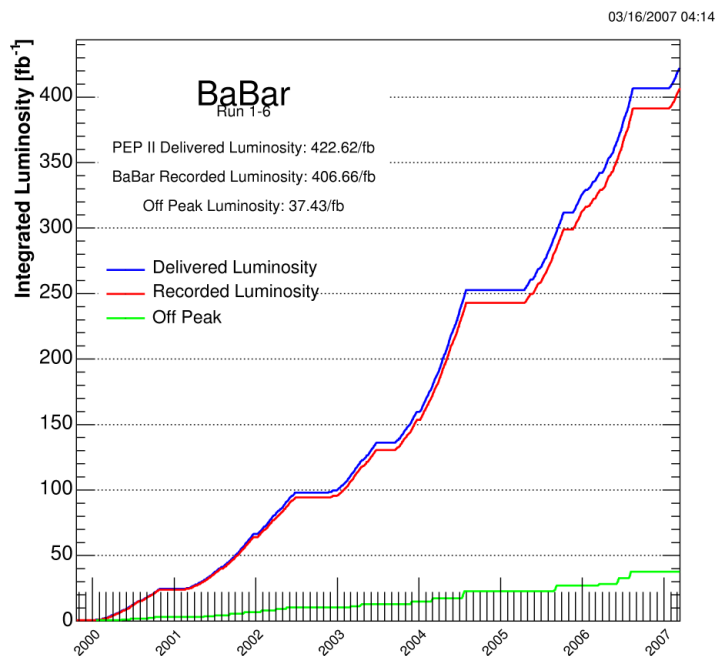
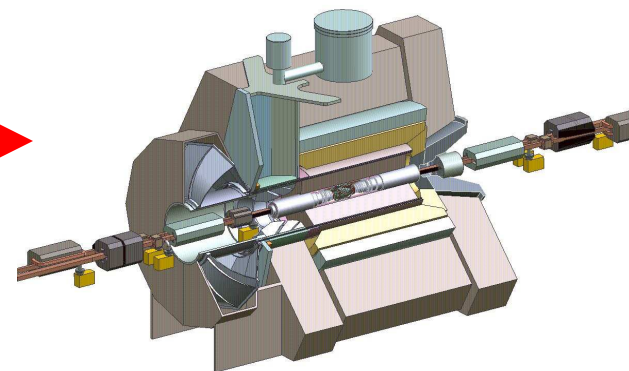


9 GeV (e^-) \times 3.1 GeV (e^+)
 peak luminosity:
 $1.2 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$



11 nations,
 77 institutes,
 ~600 persons

BaBar



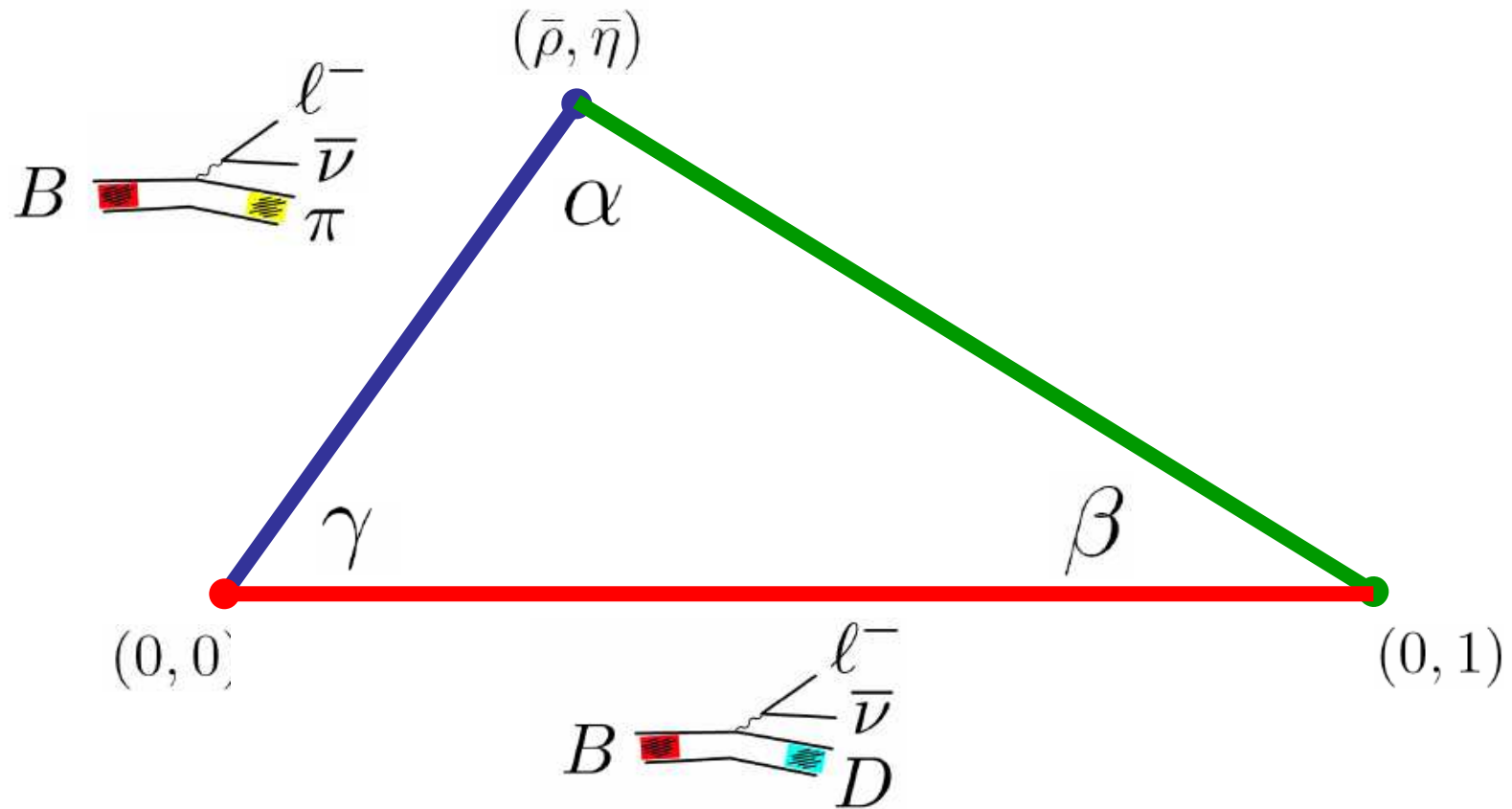
More than 400 fb⁻¹



UT sides measurements



$|V_{cb}|$ & $|V_{ub}|$





$|V_{cb}|$ & $|V_{ub}|$: howto

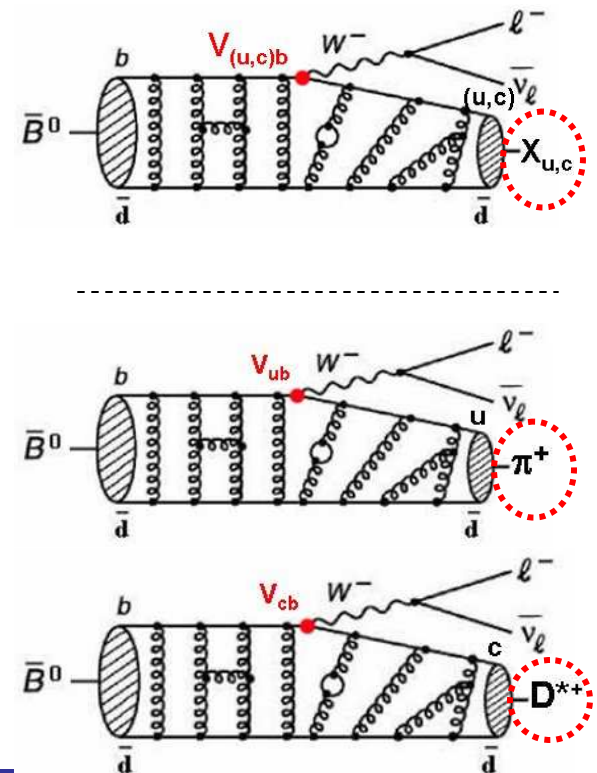
- $|V_{ub}|$ and $|V_{cb}|$ are measured with semileptonic $b \rightarrow ulv$ and $b \rightarrow clv$ decays.
- Complementary approaches: **inclusive** Vs **exclusive**

Inclusive:

- calculate $b \rightarrow xlv$, measure $B \rightarrow Xlv$ for **any** X hadron
- unknown b-quark parameters obtained from measurements of $B \rightarrow X_c lv$ and $B \rightarrow X_s \gamma$ decays

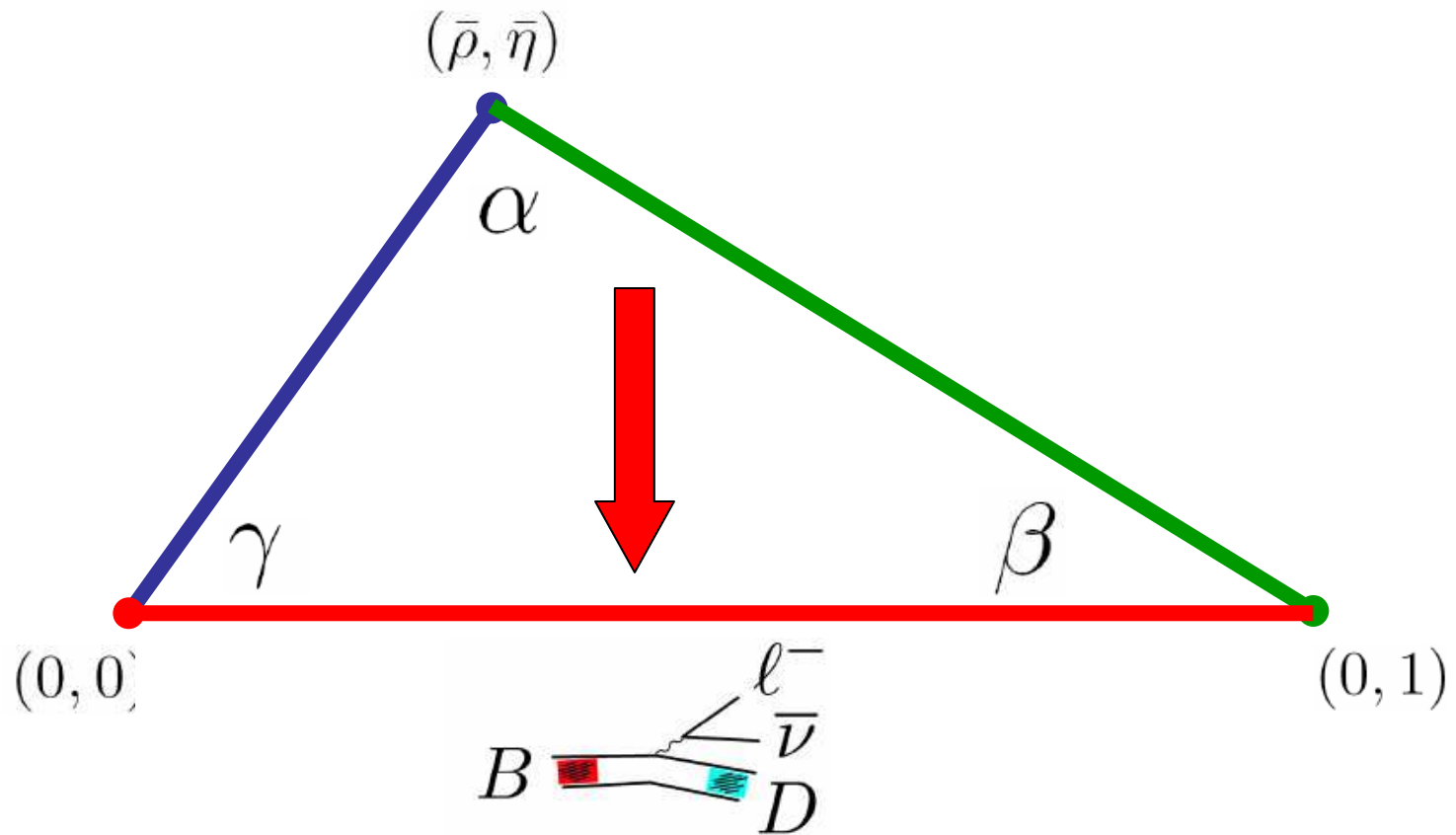
Exclusive:

- calculate and measure $B \rightarrow Xlv$, for **one** hadron
- rely on form factor calculations (which are improving):
 - “unquenched” lattice QCD (HPQCD, Fermilab, ...)
 - Light-Cone Sum Rules (Ball & Zwicky, ...)
 - quark models (ISGW2, HQET, ...)





$$|V_{cb}|$$

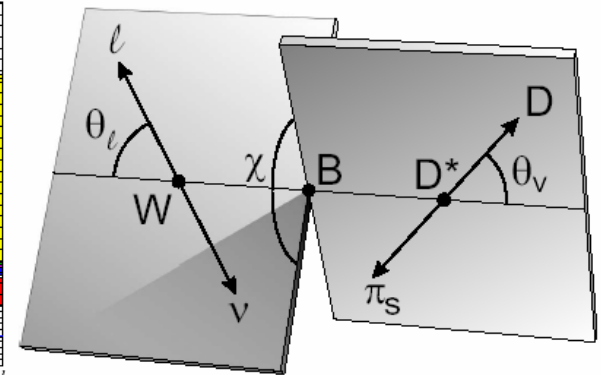
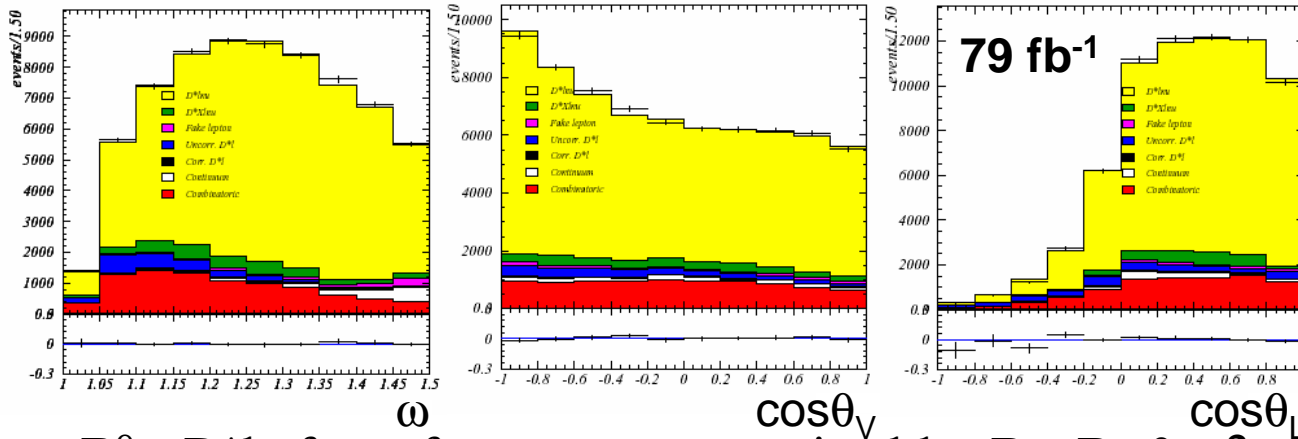




Exclusive $|V_{cb}|$

- Simultaneous measurement of $|V_{cb}|$ and the $B^0 \rightarrow D^* l \nu$ form factors

hep-ex/0607076



- $B^0 \rightarrow D^* l \nu$ form factors parametrized by R_1 , R_2 & ρ^2
- $\mathcal{F}(1)|V_{cb}|$ & form factors given by fit of ω , $\cos\theta_V$ & $\cos\theta_L$ spectra

Preliminary

Form factors 5 times more precise than former CLEO results

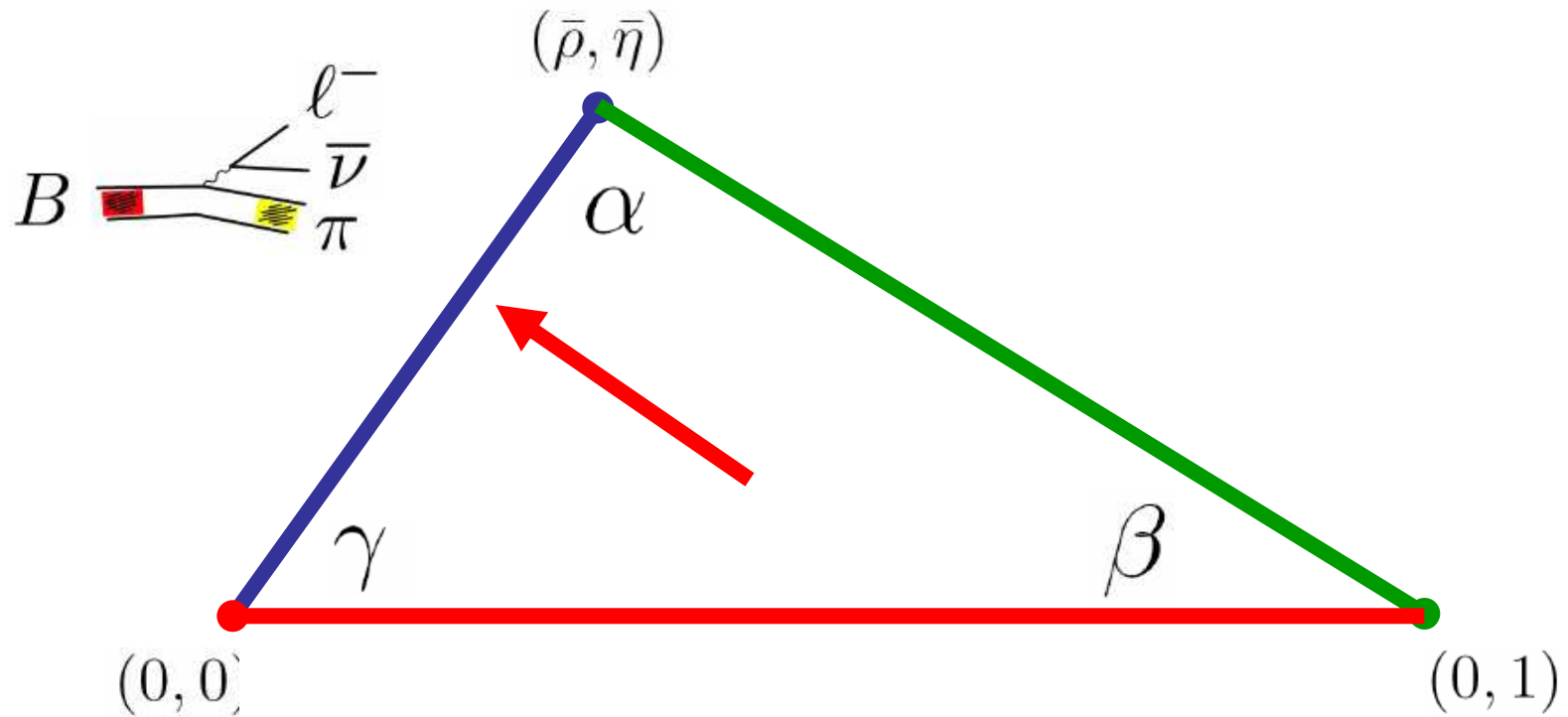
$\mathcal{F}(1) V_{cb} $	$= (34.68 \pm 0.32 \pm 1.15) \times 10^{-3}$
ρ^2	$= 1.179 \pm 0.048 \pm 0.028$
R_1	$= 1.417 \pm 0.061 \pm 0.044$
R_2	$= 0.836 \pm 0.037 \pm 0.022$

$|V_{cb}| = (37.6 \pm 0.3 \pm 1.3 (+1.5, -1.3)) \times 10^{-3}$

* ρ^2 , R_1 , R_2 averaged with BaBar's Phys.Rev.**D74**, 092004 (2006) *lBar* – IFAE 2007, Napoli

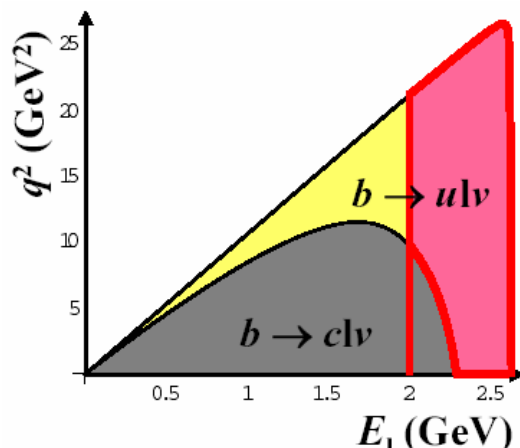


$|V_{ub}|$

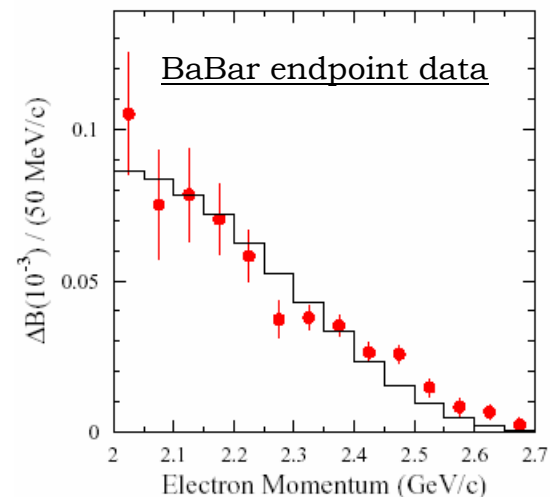
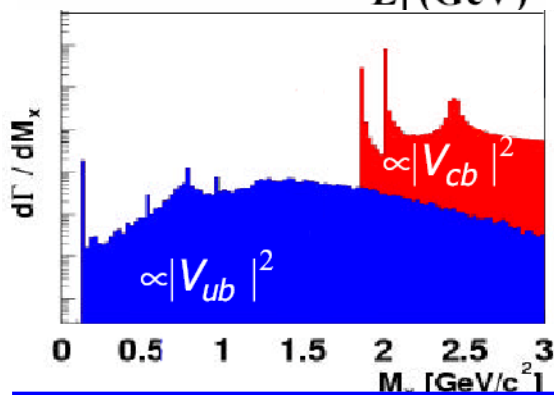




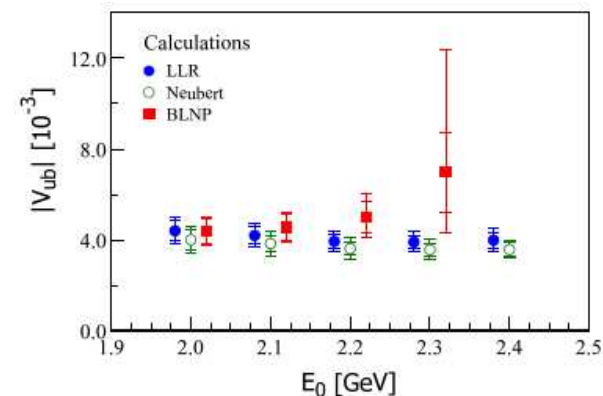
Inclusive $|V_{ub}|$



- Problem: $B \rightarrow X_c lv$ bkg rate $\sim 50x$ higher than $B \rightarrow X_u lv$ signal...
- Solution: select $b \rightarrow ulv$ events with **low M_x** , **high E_{lep}** and/or **high q^2** .



New interpretation of BaBar endpoint: **hep-ph/0702072**



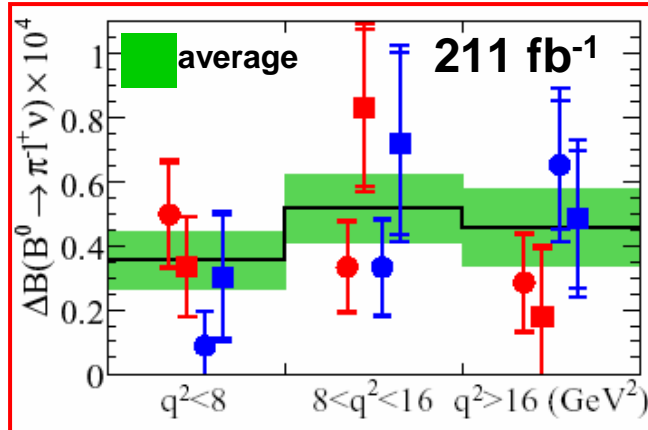
Four BaBar measurements using $\sim 82 \text{ fb}^{-1}$ so far:

- Tagged "SF free" (M_x): PRL **96**, 221801 (2006)
- Untagged endpoint: Phys. Rev. **D73**, 012006 (2006)
- Untagged E_e - q^2 : PRL **97**, 019903 (2006)
- Tagged M_x - q^2 : hep-ex/0507017

$$|V_{ub}| = (4.40 \pm 0.30 \pm 0.41 \pm 0.23) \times 10^{-3} \text{ (BLNP)}$$



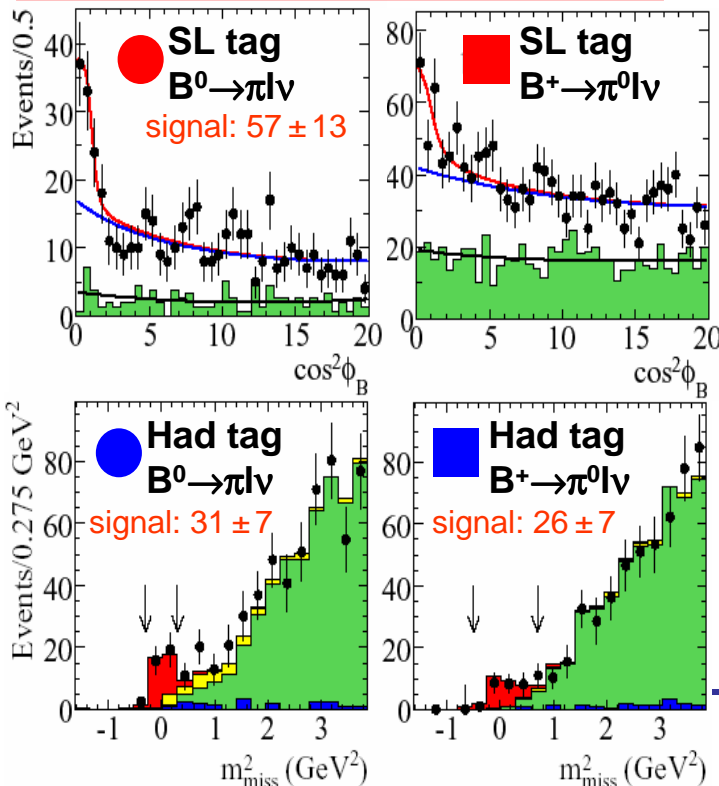
Exclusive $|V_{ub}|$ (tagged)



Measurement of $|V_{ub}|$ from tagged $B \rightarrow \pi \ell \nu$ decays

Phys. Rev. Lett. **97**, 211801 (2006)

- Tagged $B \rightarrow \pi \ell \nu$ reconstruction in 3 q^2 bins
- Combination of **semileptonic** and **hadronic** tags



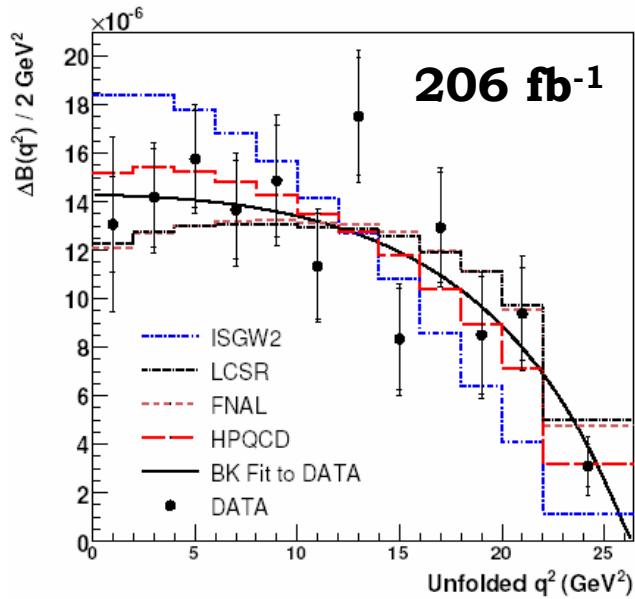
$$BF(B^0 \rightarrow \pi \ell \nu) = (1.33 \pm 0.17_{stat} \pm 0.11_{syst}) \times 10^{-4}$$

$$|V_{ub}| = (4.5 \pm 0.5_{stat} \pm 0.7_{syst} \pm 0.5_{FF}) \times 10^{-3} \quad (\text{HPQCD})$$

- **Statistically limited!!!**
- **Very promising with increasing BaBar dataset!!!**



Exclusive $|V_{ub}|$ (untagged)



Measurement of $|V_{ub}|$ and $B^0 \rightarrow \pi \ell \nu$ form-factor shape with a loose neutrino reconstruction technique

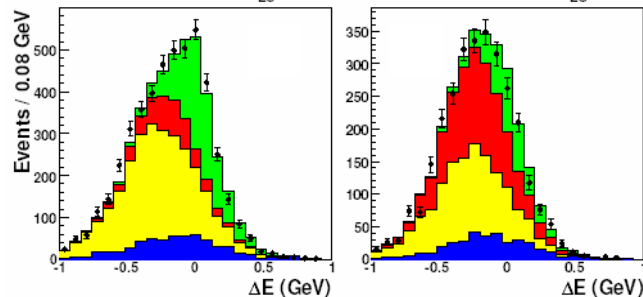
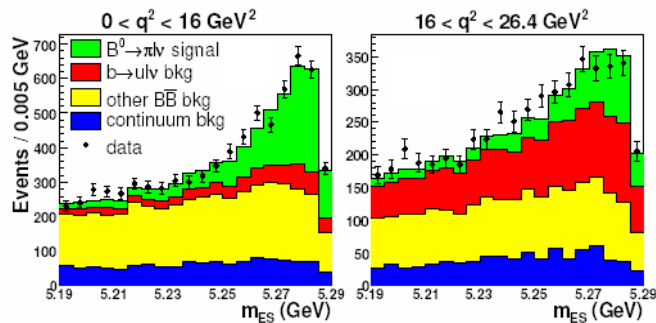
hep-ex/0612020 (accepted by Phys. Rev. Lett.)

- Reconstruct ~ 5000 signal events
- Signal & bkgd yields by a multi-parameter fit
- **test QCD calculations:**
 - **LQCD & LCSR compatible**
 - **ISGW2 incompatible**

$$BF(B^0 \rightarrow \pi \ell \nu) = (1.46 \pm 0.07_{stat} \pm 0.08_{syst}) \times 10^{-4}$$

$$|V_{ub} f_+(0)| = (9.6 \pm 0.3_{stat} \pm 0.2_{syst}) \times 10^{-4}$$

$$|V_{ub}| = (4.1 \pm 0.2_{stat} \pm 0.2_{syst}^{+0.6}_{-0.4 FF}) \times 10^{-3} \quad (\text{HPQCD})$$



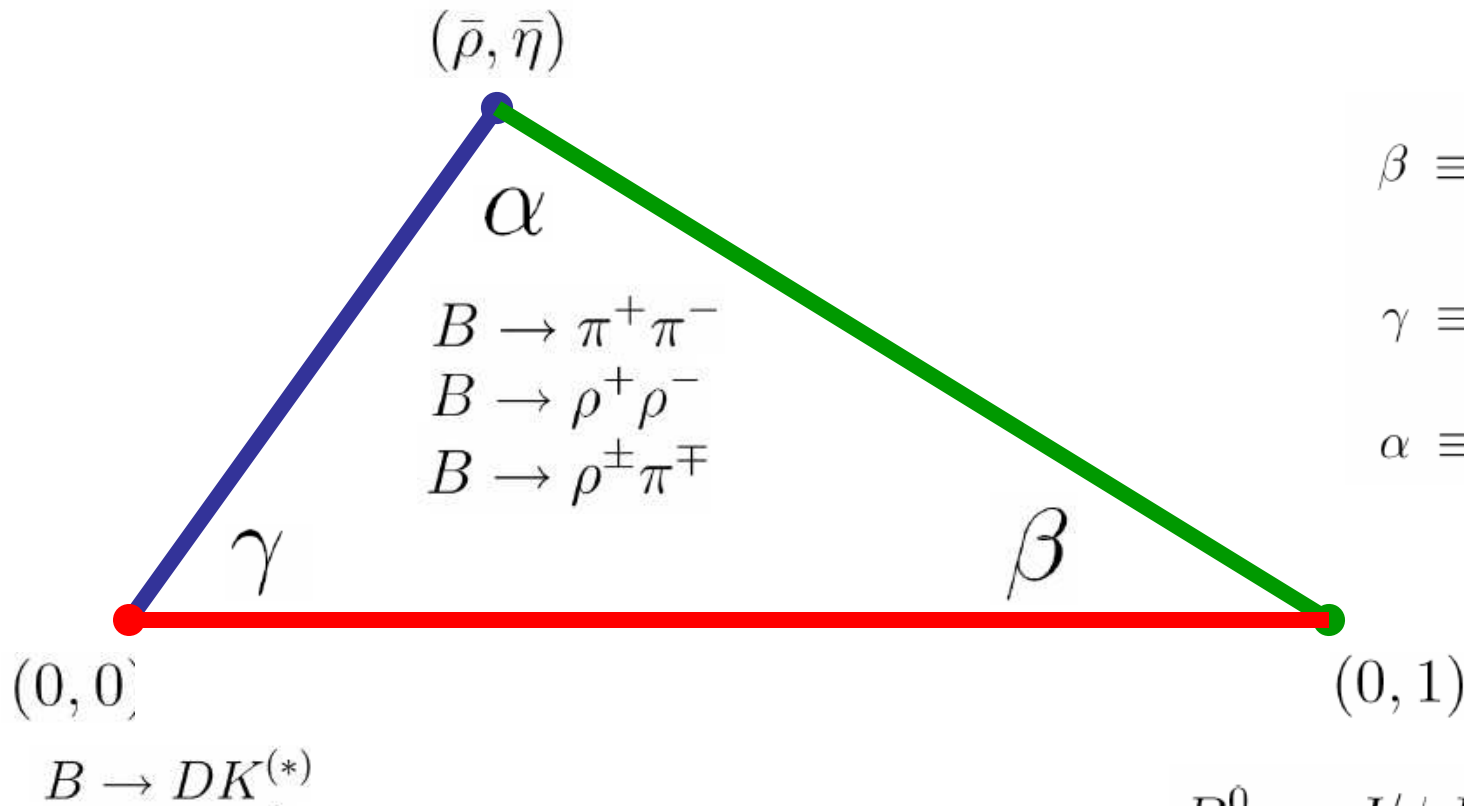
Smallest statistical & systematic uncertainties of all individual $B \rightarrow \pi \ell \nu$ measurements to date!!!



UT angles measurements



α, β & γ



$$\beta \equiv \arg \left[-\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right]$$

$$\gamma \equiv \arg \left[-\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right]$$

$$\alpha \equiv \pi - \beta - \gamma$$

$$B^0 \rightarrow J/\psi K^0 \quad b \rightarrow c \bar{c} s$$

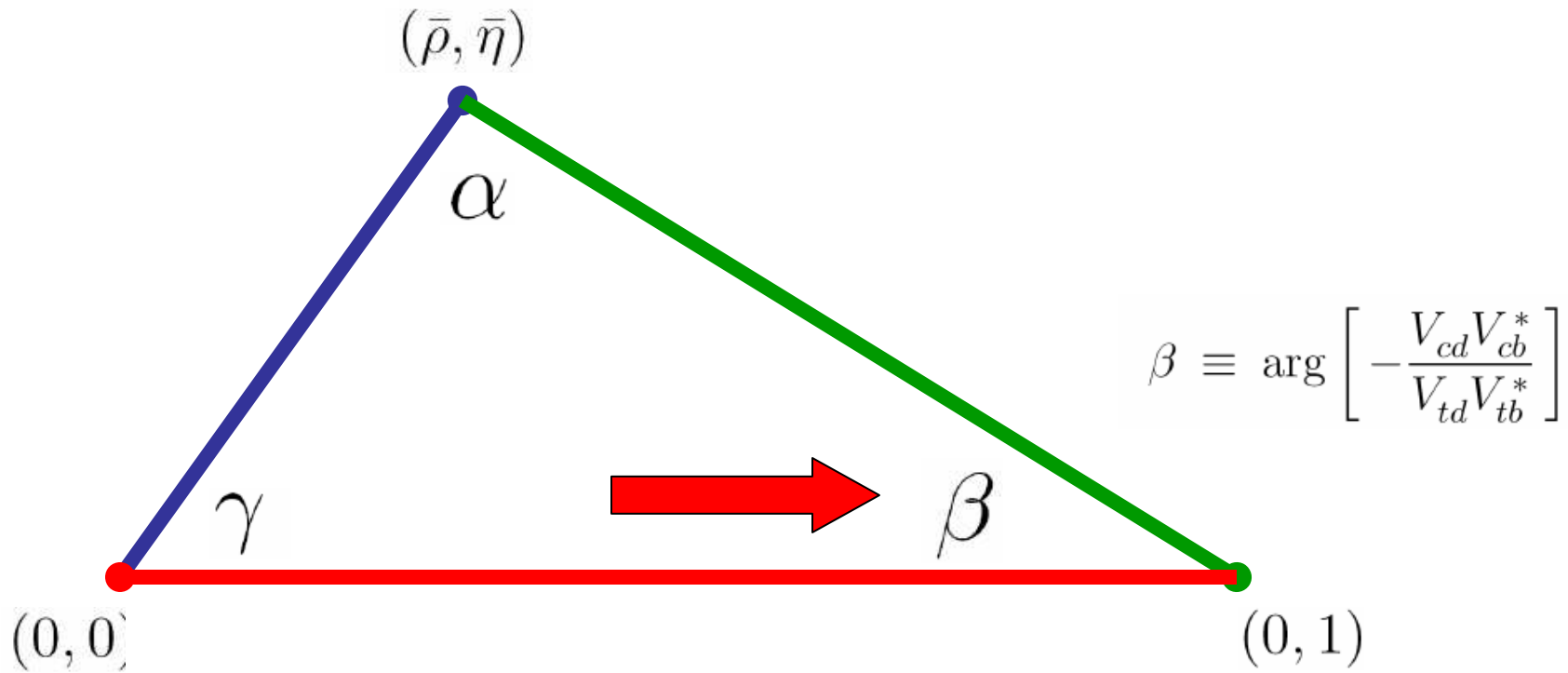
$$B^0 \rightarrow J/\psi K^{*0}$$

$$B^0 \rightarrow D^{(*)0} \pi^0$$

$$B^0 \rightarrow D^{*+} D^{*-} K_S^0$$



β



$$B^0 \rightarrow J/\psi K^0 \quad b \rightarrow c \bar{c} s$$

$$B^0 \rightarrow J/\psi K^{*0}$$

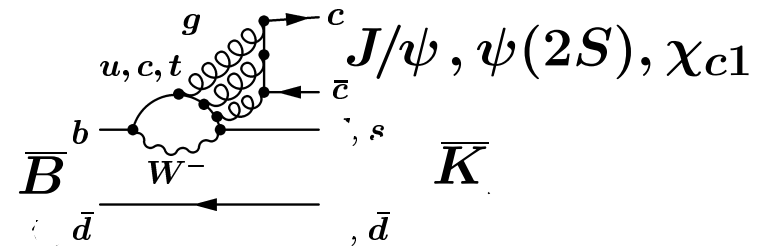
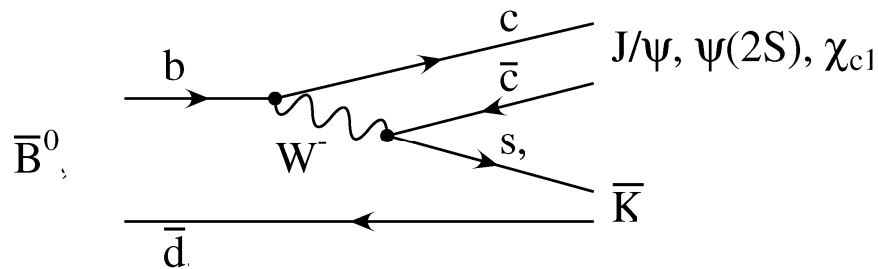
$$B^0 \rightarrow D^{(*)0} \pi^0$$

$$B^0 \rightarrow D^{*+} D^{*-} K_S^0$$



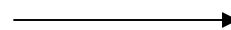
Charmonium K^0 modes

“Golden” modes: tree diagrams dominate; the t -quark penguin has the same weak phase as the tree, so the measured SM quantity is $\sin 2\beta$



$$SM \text{ prediction: } C_f=0 \rightarrow A_{CP}(\Delta t) = S_f \sin(\Delta m \Delta t)$$

Experimentally very clean!
Many accessible decay modes
with (relatively) large BF's



- $B \rightarrow J/\psi K^0 \sim 8.5 \times 10^{-4}$
- $B \rightarrow J/\psi K^{*0} \sim 1.3 \times 10^{-3}$
- $B \rightarrow \psi(2S) K^0 \sim 6.2 \times 10^{-4}$
- $B \rightarrow \chi_{c1} K^0 \sim 4 \times 10^{-4}$
- $B \rightarrow \eta_c K^0 \sim 1.2 \times 10^{-3}$



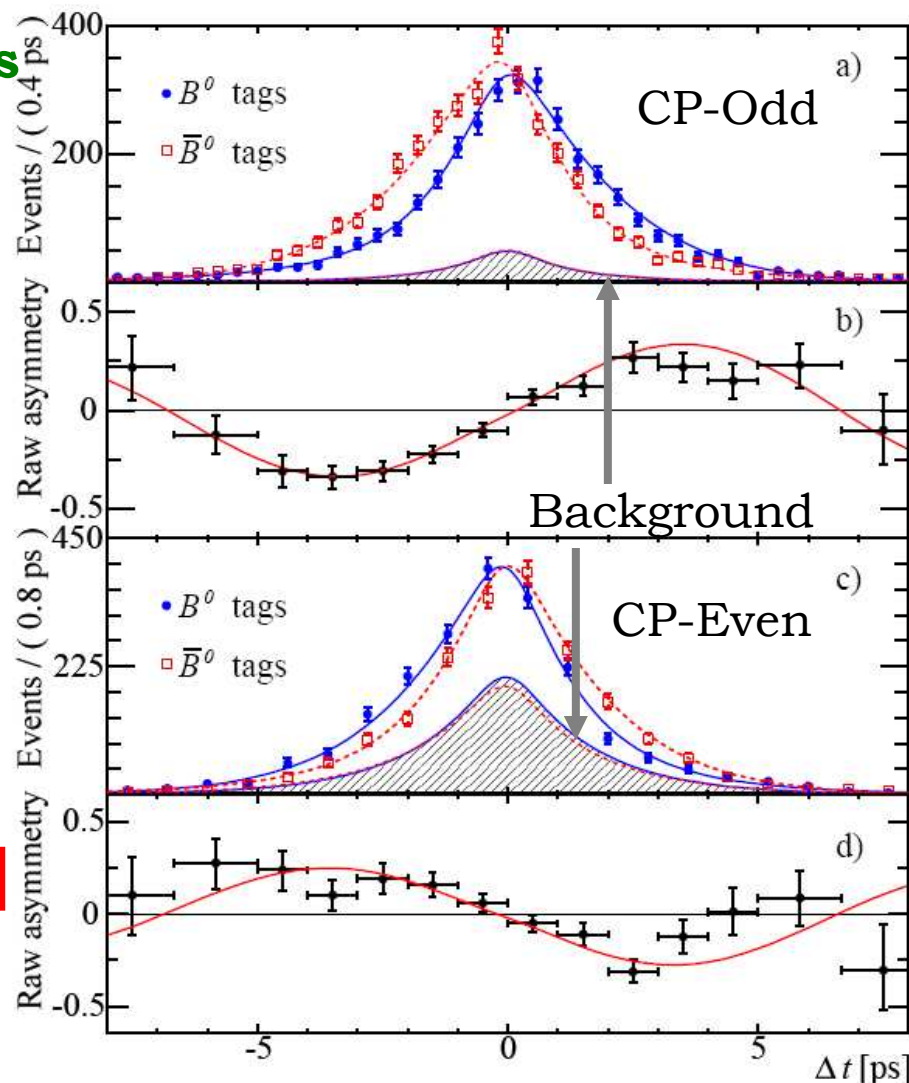
Charmonium K^0 modes

hep-ex/0703021, 384 M BB pairs submitted to PRL

Sample	N_{tag}	$P(\%)$	$\sin 2\beta$	$ \lambda $
Full CP sample	12677	75	0.714 ± 0.032	0.952 ± 0.022
$J/\psi K_S^0 (\pi^+ \pi^-)$	4459	96	0.702 ± 0.042	0.976 ± 0.030
$J/\psi K_S^0 (\pi^0 \pi^0)$	1086	88	0.617 ± 0.103	0.812 ± 0.058
$\psi(2S) K_S^0$	687	83	0.947 ± 0.112	0.867 ± 0.079
$\chi_{c1} K_S^0$	313	89	0.759 ± 0.170	0.804 ± 0.102
$\eta_c K_S^0$	328	69	0.778 ± 0.195	0.948 ± 0.141
$J/\psi K_L^0$	4748	55	0.734 ± 0.074	1.061 ± 0.063
$J/\psi K^{*0}$	1056	66	0.477 ± 0.271	0.954 ± 0.083
$J/\psi K^0$	10275	76	0.697 ± 0.035	0.966 ± 0.025
$J/\psi K_S^0$	5547	94	0.686 ± 0.039	0.950 ± 0.027
$\eta_f = -1$	6873	92	0.711 ± 0.036	0.935 ± 0.024
1999-2002 data	3084	79	0.735 ± 0.063	0.987 ± 0.045
2003-2004 data	4850	77	0.728 ± 0.052	0.940 ± 0.035
2005-2006 data	4725	74	0.681 ± 0.054	0.940 ± 0.037

$$\sin 2\beta = 0.714 \pm 0.032 \text{ (stat)} \pm 0.018 \text{ (syst)}$$

$$|\lambda| = 0.952 \pm 0.022 \text{ (stat)} \pm 0.017 \text{ (syst)}$$

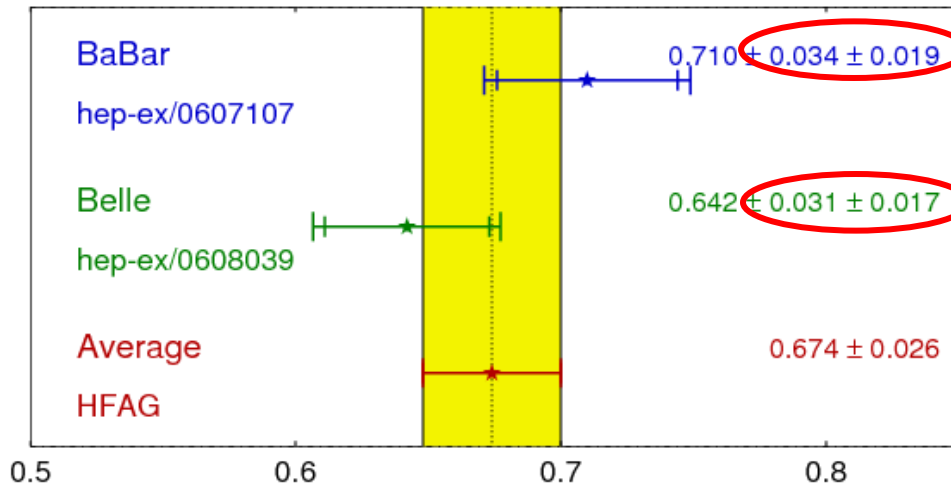




Sin2β averages

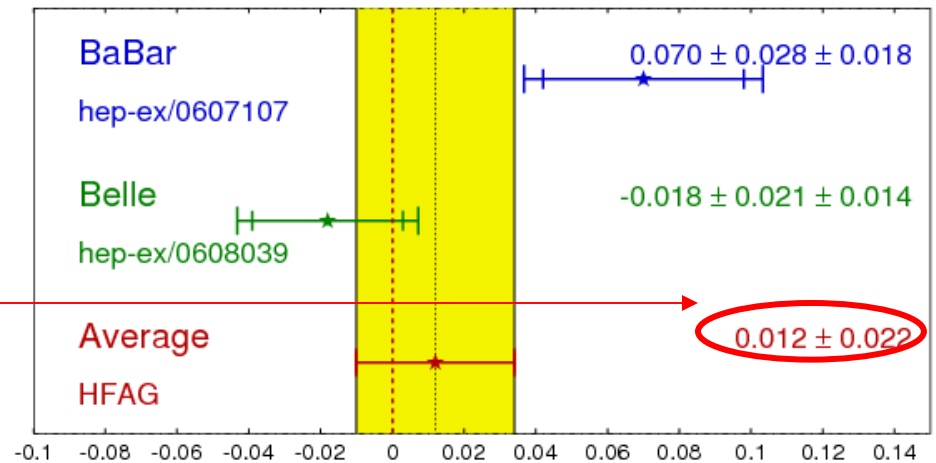
$\sin(2\beta) \equiv \sin(2\phi_1)$ **HFAG**
ICHEP 2006
PRELIMINARY

Heavy Flavors Averaging Group
E.Barberio et al., hep-ex/0603003



still statistically limited

$b \rightarrow ccs$ C_{CP} **HFAG**
ICHEP 2006
PRELIMINARY



Consistent with zero: no evidence for NP in tree decay

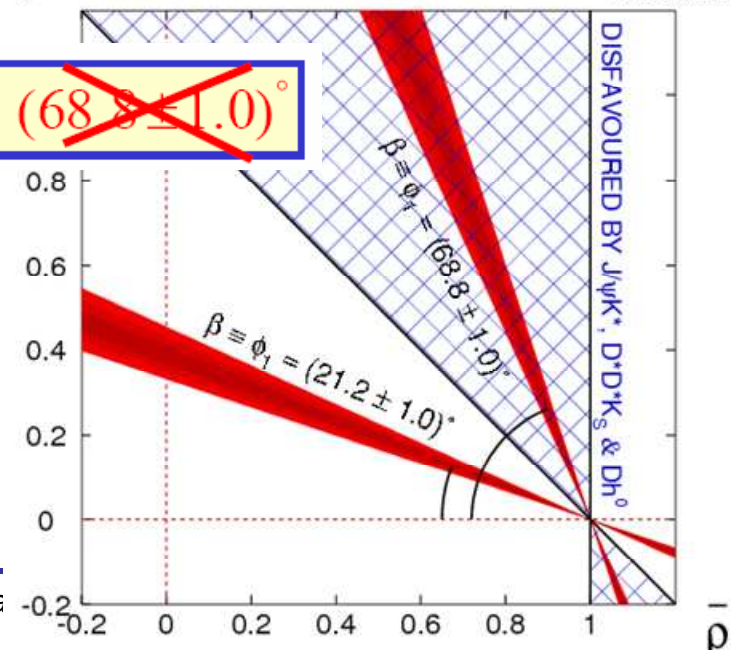


All the $\cos(2\beta)$ world

- Resolve the geometric ambiguity on β in the measurement of $\cos 2\beta$
 - TD analysis of $VV J/\Psi K^{*0}$ decays
 - TD Dalitz fit of $D \rightarrow K_S \pi^+ \pi^-$ in $B^0 \rightarrow D^0 h^0$
 - TD study of $B^0 \rightarrow D^* D^* K_S \bar{\eta}$ $\beta \equiv \phi_1$

HFAG
ICHEP 2006
PRELIMINARY

$\beta = (21.2 \pm 1.0)^\circ$ or ~~$(68.8 \pm 1.0)^\circ$~~



1. [Phys.Rev.D71 \(2005\) 032005](#)
2. [hep-ex/0607105](#)
3. [Phys.Rev. D74 \(2006\) 091101](#)



Colour suppressed decays

TD analysis of $D^0 \rightarrow CP$ in $B^0 \rightarrow D^{(*)0} h^0$ 348 fb⁻¹

$\eta_f = +1$ (CP even)			$\eta_f = -1$ (CP odd)		
Mode	D_{CP}	N_{signal}	Mode	D_{CP}	N_{signal}
$D_{K_S^0 \omega}^0$	-	26.2 ± 6.3	$D_{KK}^0 \pi^0$	+	104 ± 17
$D_{K_S^0 \pi^0 \omega}^0$	-	40.0 ± 8.0	$D_{KK}^0 \eta \gamma \gamma$	+	28.9 ± 6.5
$D_{K_S^0 \omega}^0$	-	23.2 ± 6.8	$D_{KK}^0 \eta 3\pi$	+	14.2 ± 4.7
$D_{KK}^{*0} \pi^0$	+	23.2 ± 6.3	$D_{KK}^0 \omega$	+	51.2 ± 8.5
$D_{KK}^0 \eta \gamma \gamma$	+	9.8 ± 3.5	$D_{K_S^0 \omega}^{*0} \pi^0$	-	5.5 ± 3.3
$D_{KK}^{*0} \eta 3\pi$	+	6.8 ± 2.9			
Combined		131 ± 16			209 ± 23
Total					340 ± 32

tree level dominated

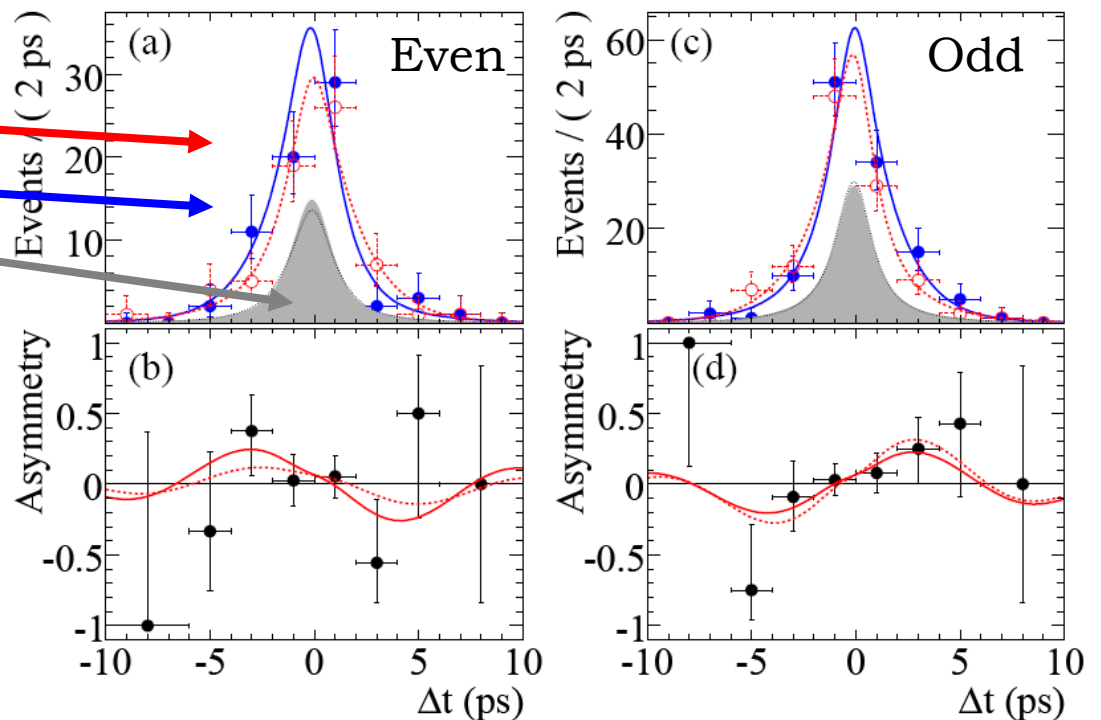
small SM uncertainty

Δt for \bar{B}^0 tag
 Δt for B^0 tag
 Background

$$\mathcal{S} = -0.56 \pm 0.23 \pm 0.05$$

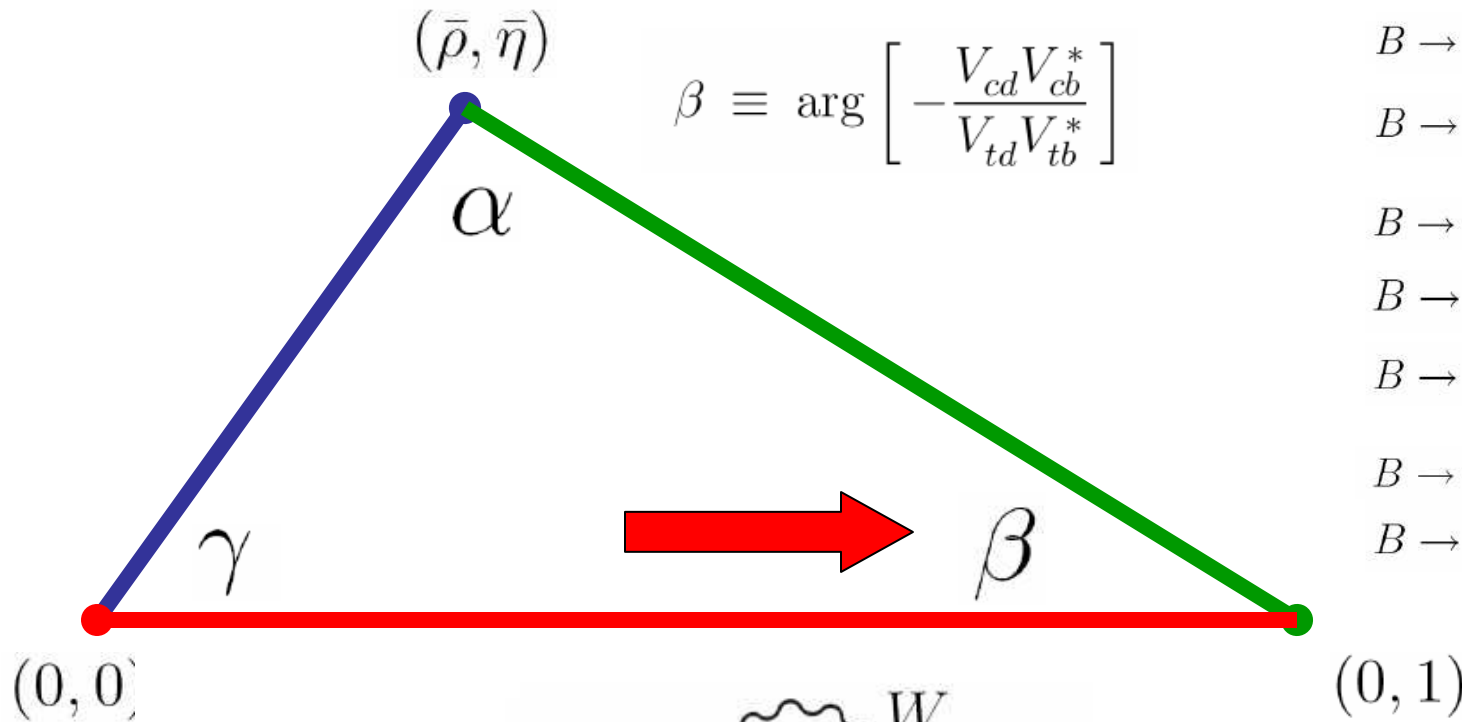
$$\mathcal{C} = -0.23 \pm 0.16 \pm 0.04$$

First measurement of $\sin 2\beta$ in these modes!

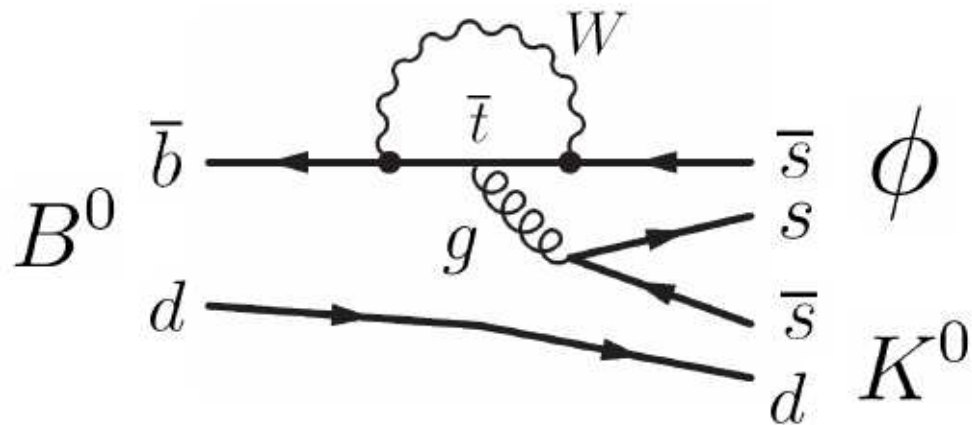




β : penguin modes

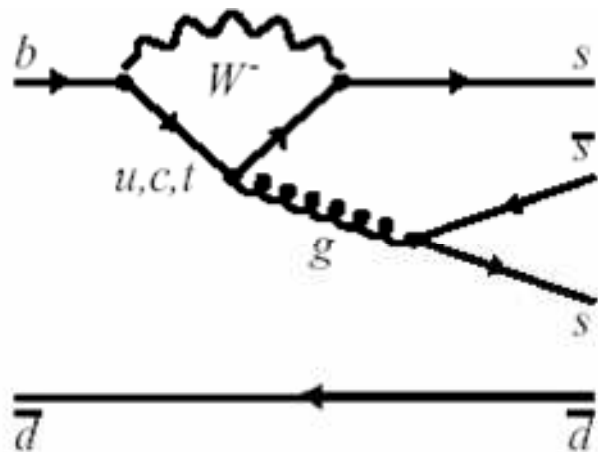


- $B \rightarrow \phi K_S^0$ $b \rightarrow s \bar{s} s$
- $B \rightarrow K_S^0 K_S^0 K_S^0$
- $B \rightarrow \eta' K_S^0$
- $B \rightarrow f_0 K_S^0$
- $B \rightarrow K K K_S^0$
- $B \rightarrow \pi^0 K_S^0$
- $B \rightarrow \omega K_S^0$ $b \rightarrow q \bar{q} s$

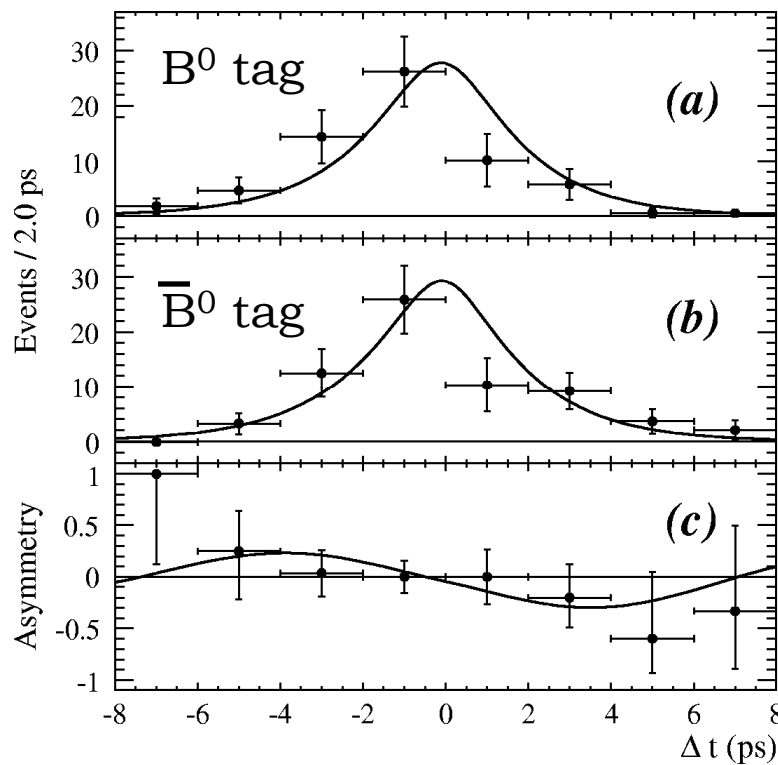




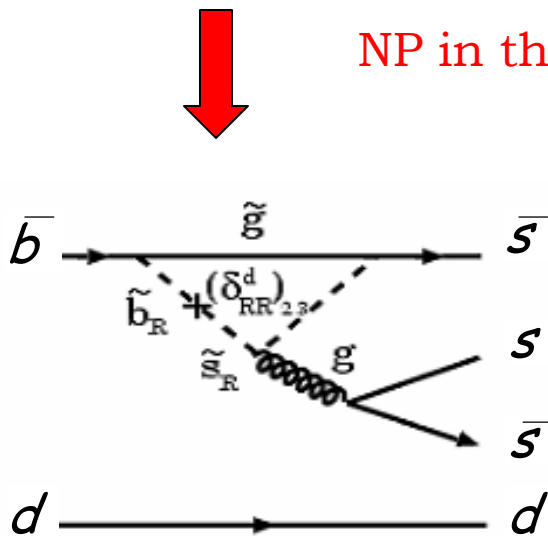
Sin2β with penguins



$B^0 \rightarrow K_S K_S K_S$ 384 M BB



NP in the loop?



$$S = +0.71 \pm 0.24 \pm 0.04$$

$$C = +0.02 \pm 0.21 \pm 0.05$$

hep-ex/0702046 (submitted to PRL)

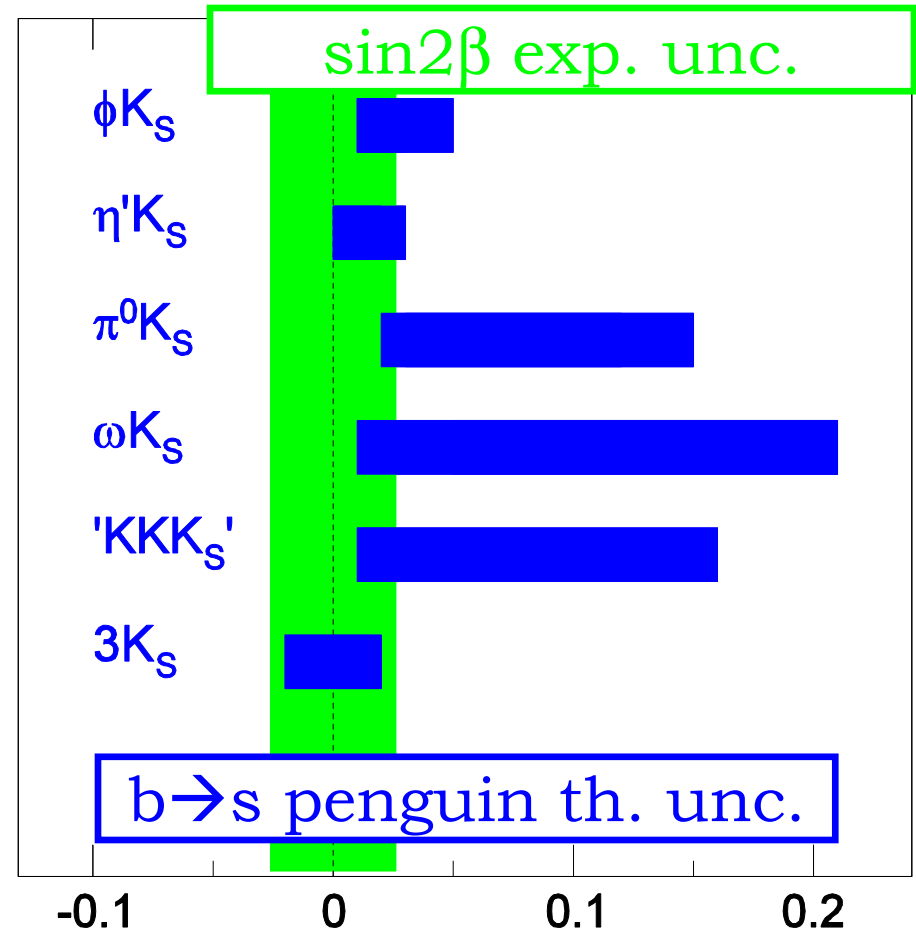
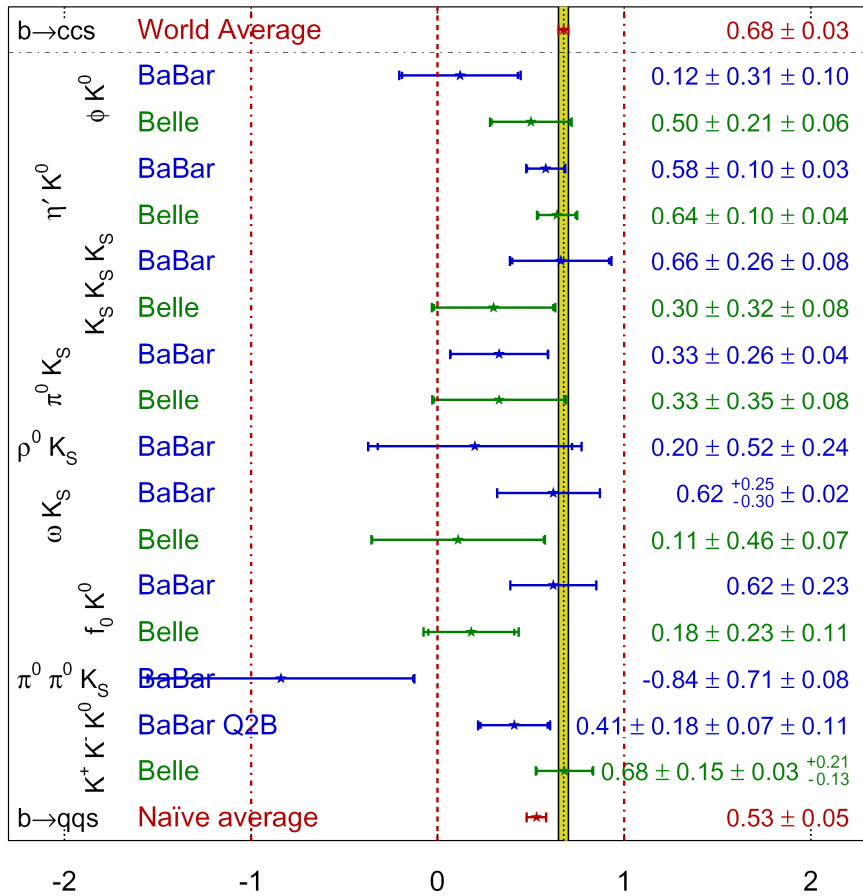


Sin2β with penguins

$\sin 2\beta_{\text{eff}}$ points towards values lower than $\sin 2\beta$

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

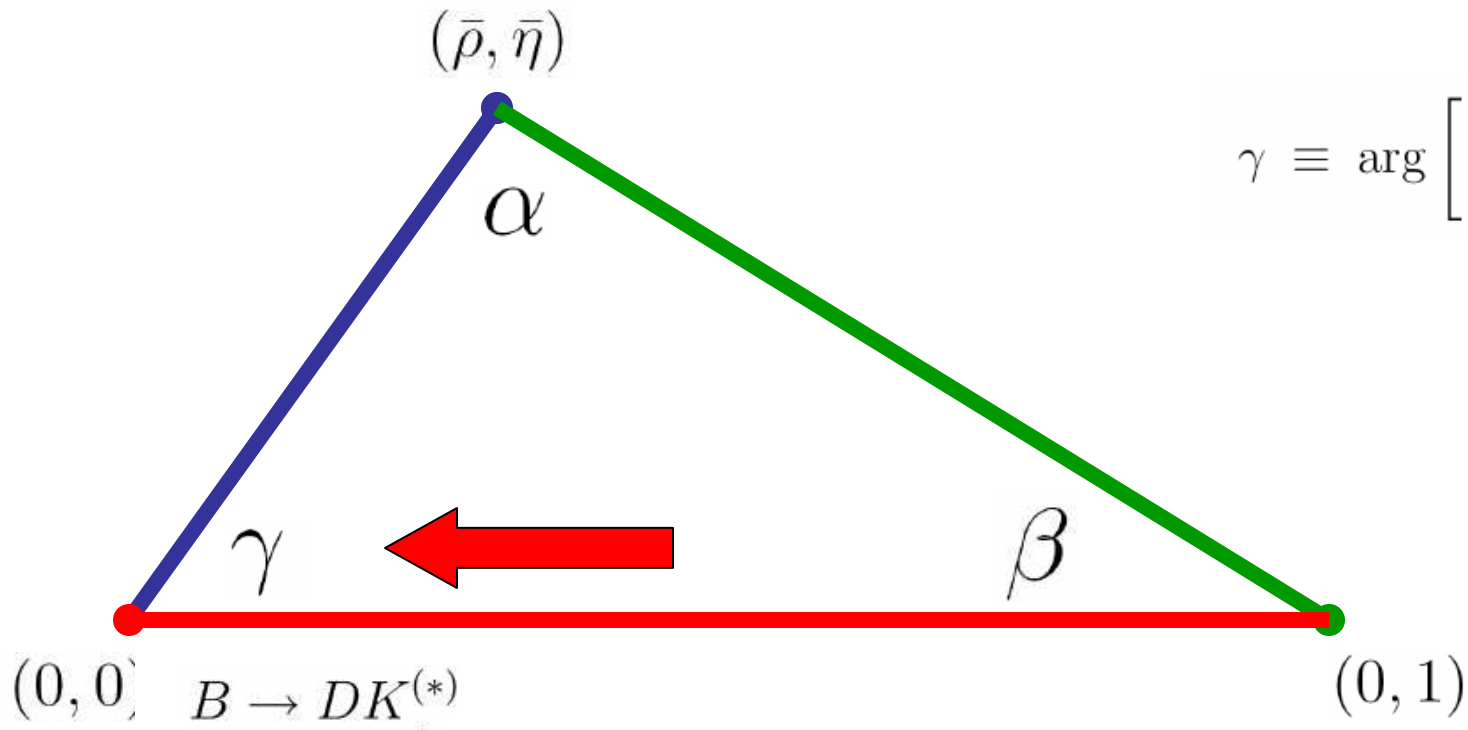
HFAG
DPF/JPS 2006
PRELIMINARY



$$\Delta \sin 2\beta = \sin 2\beta_{\text{eff}} - \sin 2\beta$$



γ



$$\gamma \equiv \arg \left[-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right]$$



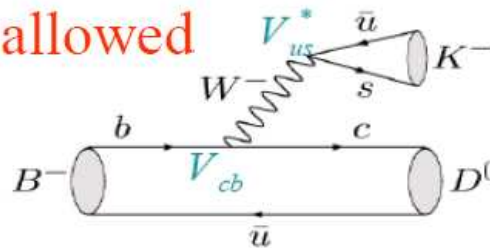
$$B^+ \rightarrow D^0 K^+$$



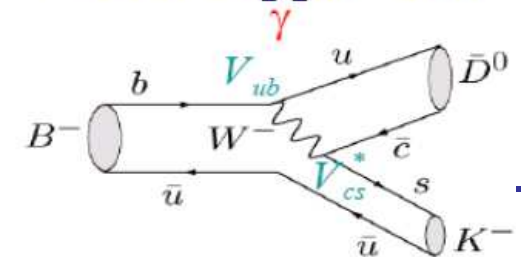
only tree diagrams: no issue with New Physics in loops

- Interference between:
 1. $(b \rightarrow c) B^+ \rightarrow \bar{D}^0 K^+$
 2. CKM- and color-suppressed $(b \rightarrow u) B^+ \rightarrow D^0 K^+$,
- D^0 and the \bar{D}^0 decay to a common final state f
 1. **GLW** : f is a CP eigenstate
 - $KK, \pi\pi, K_S\omega, K_S\phi, K_S\pi$
 2. **ADS** : f is doubly Cabibbo suppressed
 - $K\pi, K\pi\pi^0$
 3. **GGSZ** : f is a 3 body decay (Dalitz)
 - $K_S\pi\pi, \pi\pi\pi^0$

Color allowed



Color suppressed

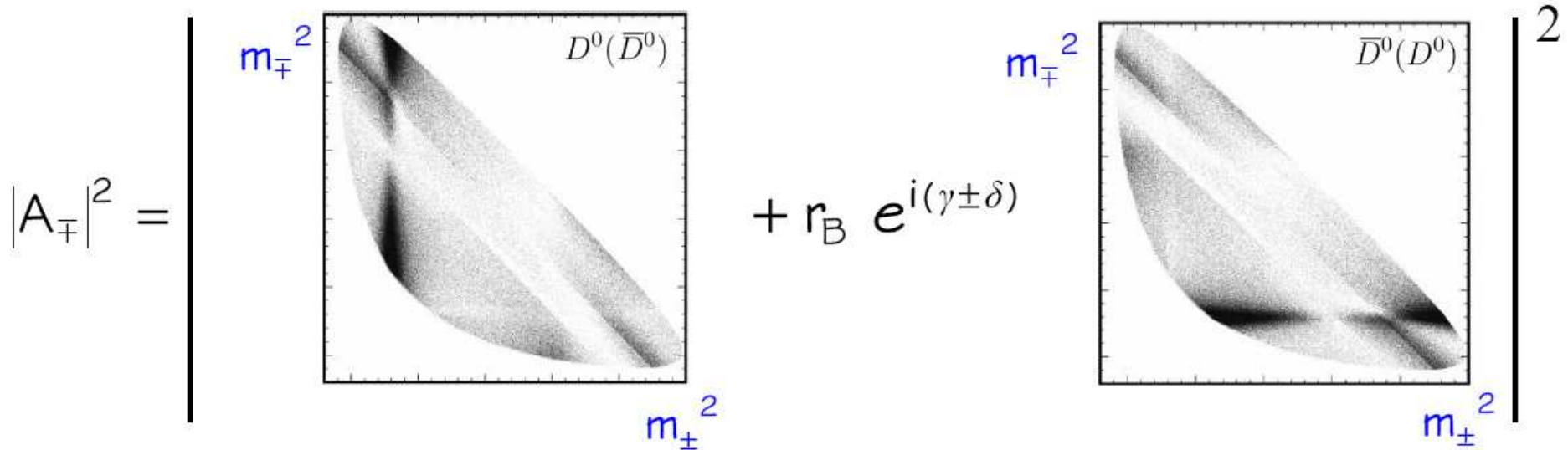




$B^+ \rightarrow D^{(*)0}[K_S\pi\pi] K^+ : \text{GGSZ (Dalitz)}$

$B \rightarrow D[K_S\pi\pi]K$

Idea: fit $K_S\pi\pi$ Dalitz structure



$$CP \begin{cases} \Gamma(B^-) \propto |f_-|^2 + r_b^2 |f_+|^2 + 2x_- \text{Re}(f_- f_+^*) + 2y_- \text{Im}(f_- f_+^*) \\ \Gamma(B^+) \propto |f_+|^2 + r_b^2 |f_-|^2 + 2x_+ \text{Re}(f_+ f_-^*) + 2y_+ \text{Im}(f_+ f_-^*) \end{cases} \quad f_{\mp} \equiv f(m_{\mp}^2, m_{\pm}^2)$$

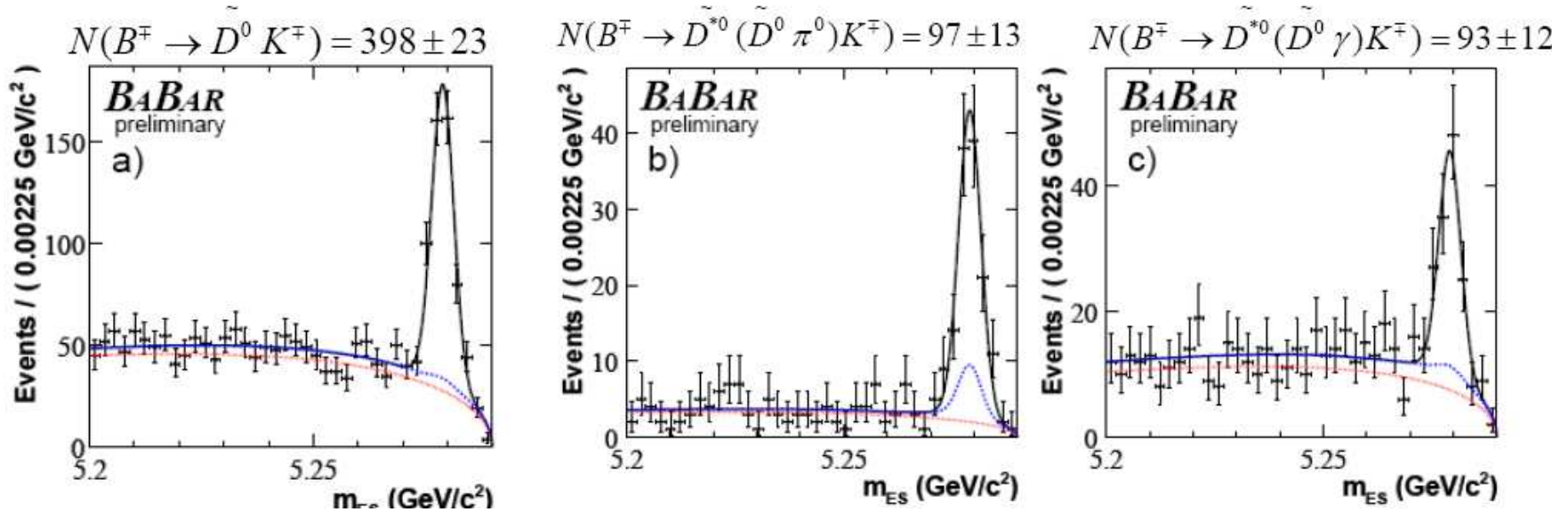
$$r_B = \left| \frac{A(b \rightarrow u)}{A(b \rightarrow c)} \right|$$

$$\begin{cases} x_{\mp} = r_b \cos(\delta_{\mp} + \gamma) \\ y_{\mp} = r_b \sin(\delta_{\mp} + \gamma) \end{cases}$$

From a large D^0 control sample



$B^+ \rightarrow D^{(*)0} K^+ : \text{GGSZ (Dalitz)}$



$$\gamma = (92 \pm 41 \pm 11 \pm 12)^{\circ}$$

(stat)
(syst)
(Dalitz)

$$\delta_B = (118 \pm 63 \pm 19 \pm 36)^{\circ}$$

$$\delta_B^* = (-62 \pm 59 \pm 18 \pm 10)^{\circ}$$

$$0.00 < r_B < 0.140$$

$$0.017 < r_B^* < 0.203$$

hep-ex/0607104

$347 \times 10^6 B\bar{B}$ pairs



$B^+ \rightarrow D^{(*)0}[\pi\pi\pi^0] K^+ : \text{GGSZ (Dalitz)}$

- First measurement of CP parameters with this channel
- Signal yield: 170 ± 29 on $\sim 324 \times 10^6$ $B\bar{B}$ pairs



hep-ex/0703037

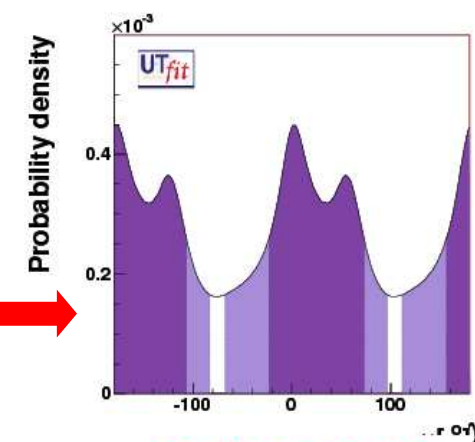
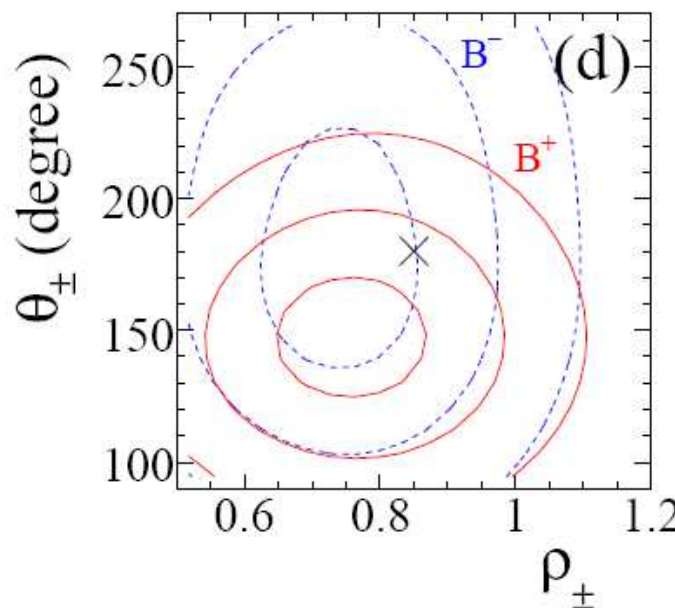
$$x_{\pm} = \rho_{\pm} \cos \vartheta_{\pm} + x^0$$

$$y_{\pm} = \rho_{\pm} \sin \vartheta_{\pm}$$

$$x_0 \equiv - \int \text{Re}(f(m_+^2, m_-^2), f^*(m_-^2, m_+^2)) dm_+^2 dm_-^2$$

f = D Dalitz amplitude

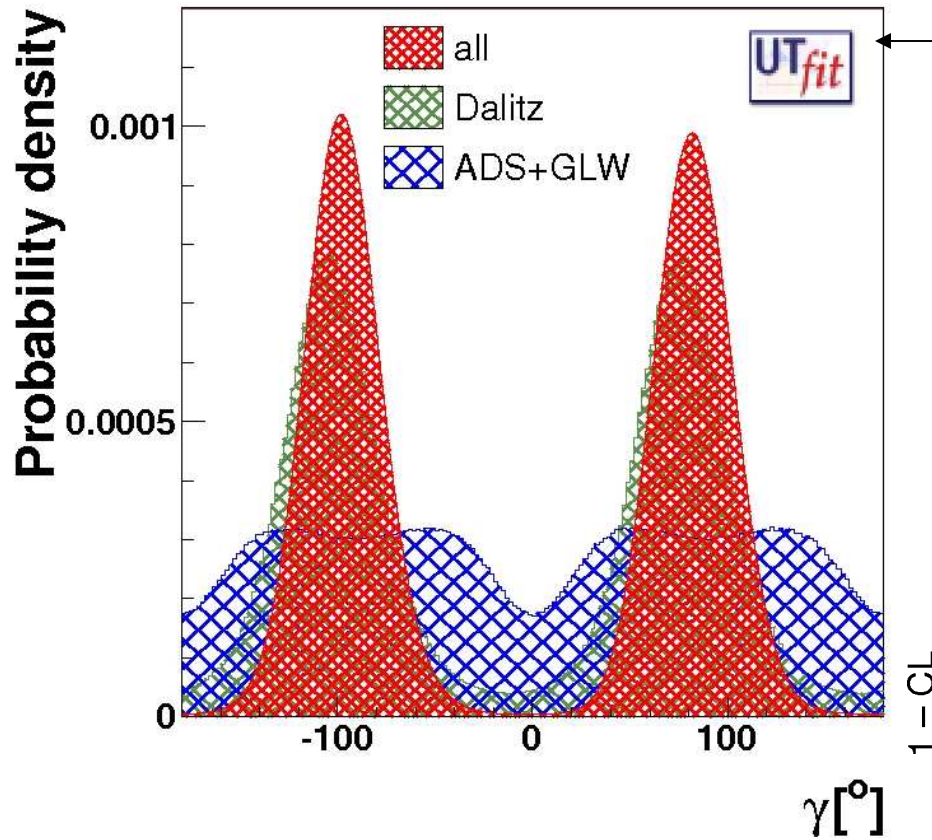
- $\rho^- = 0.72 \pm 0.11 \pm 0.06$
- $\vartheta^- = (173 \pm 42 \pm 19)^\circ$
- $\rho^+ = 0.75 \pm 0.11 \pm 0.06$
- $\vartheta^+ = (147 \pm 23 \pm 16)^\circ$



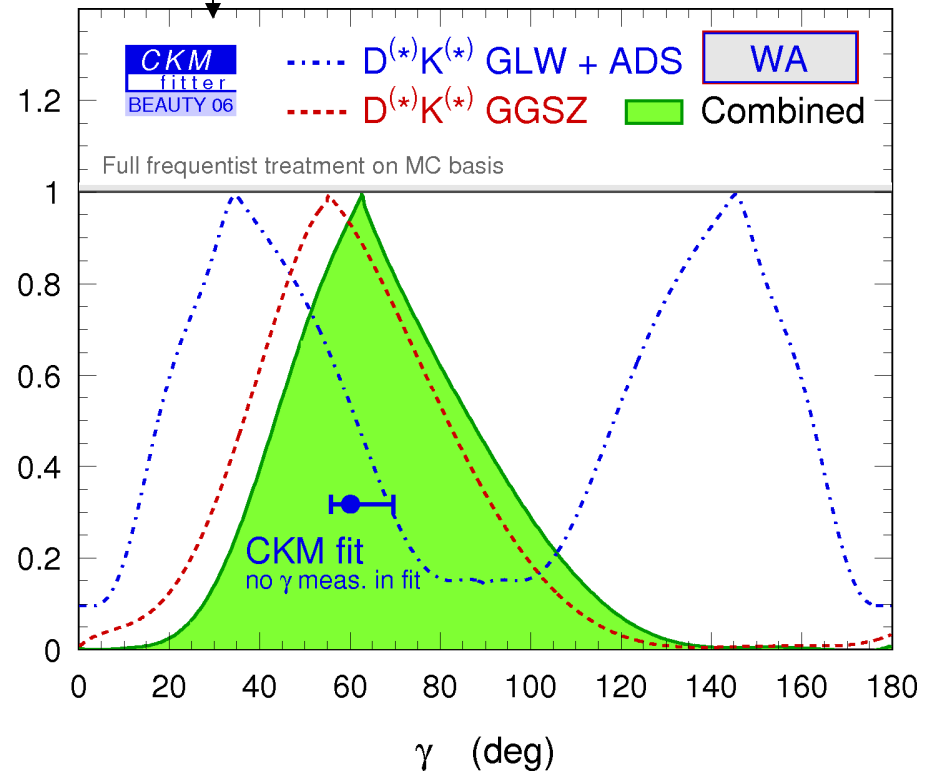
$\gamma = 25 \pm 48$ @ 68% CL
 $\gamma = [-67, 97]$ @ 90% CL



γ : results

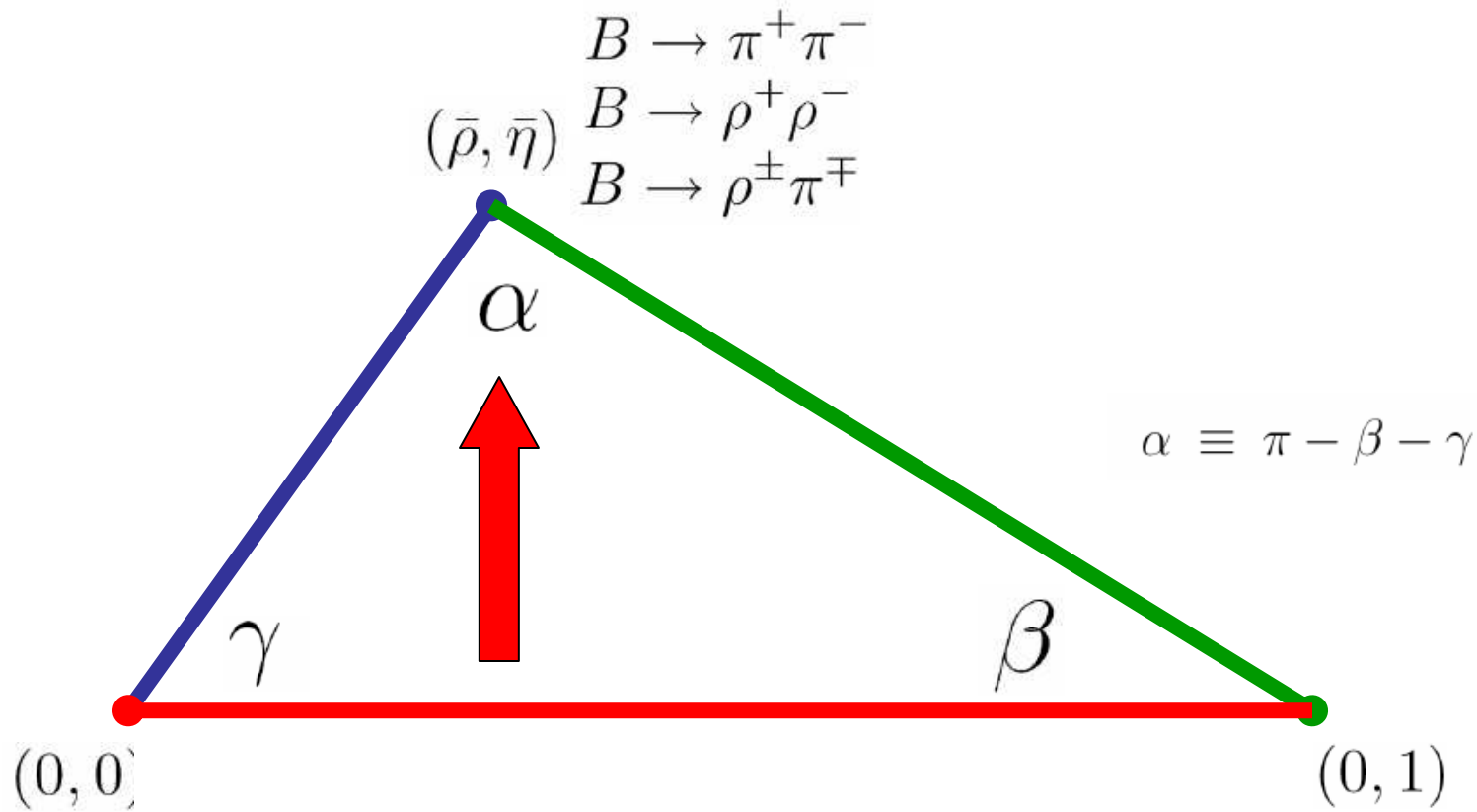


$UT_{fit} = (82 \pm 19)^\circ$
 $CKM_{fitter} = (62^{+38}_{-24})^\circ$





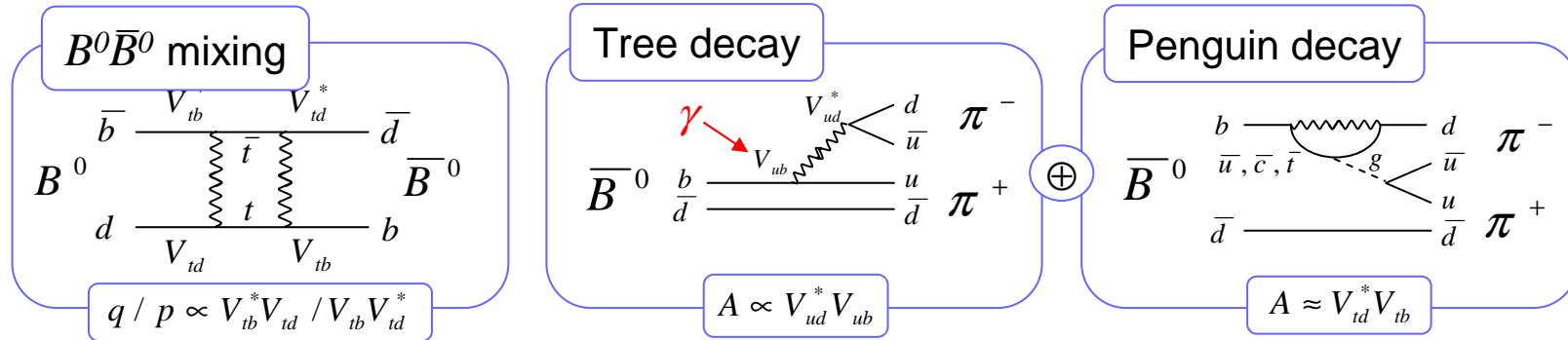
α





α: howto

- Access to α from the interference of a $b \rightarrow u$ decay (γ) with $B^0 \bar{B}^0$ mixing (β)



$$\lambda = \frac{q}{p} \frac{\bar{A}}{A} = e^{-i2\beta} e^{-i2\gamma} = e^{i2\alpha}$$

Inc. penguin contribution \rightarrow

$$\lambda = e^{i2\alpha} \frac{T + P e^{+i\gamma} e^{i\delta}}{T + P e^{-i\gamma} e^{i\delta}}$$

$$S = \sin(2\alpha)$$

$$C = 0$$

$$S = \sqrt{1 - C^2} \sin(2\alpha_{\text{eff}})$$

$$C \propto \sin \delta$$

How can we obtain α from α_{eff} ?

Time-dep. asymmetry : $A_{\pi\pi}(\Delta t) = S_{\pi\pi} \sin(\Delta m_d \Delta t) - C_{\pi\pi} \cos(\Delta m_d \Delta t)$

Use SU(2) to relate different hh final states

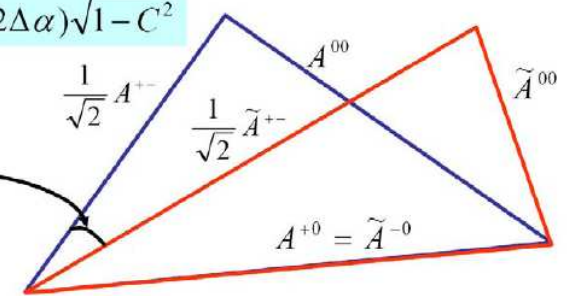
- $A^{+-} = A(B^0 \rightarrow \pi^+ \pi^-)$
- $\tilde{A}^{+-} = A(\bar{B}^0 \rightarrow \pi^+ \pi^-)$
- $A^{00} = A(B^0 \rightarrow \pi^0 \pi^0)$
- $\tilde{A}^{00} = A(\bar{B}^0 \rightarrow \pi^0 \pi^0)$
- $A^{+0} = A(B^+ \rightarrow \pi^+ \pi^0)$
- $\tilde{A}^{-0} = A(B^- \rightarrow \pi^- \pi^0)$

$$A_{hh} = e^{+i\gamma} T + e^{-i\beta} P$$

$$\tilde{A}_{hh} = e^{-i\gamma} T + e^{+i\beta} P$$

$$S = \sin(2\alpha + 2\Delta\alpha) \sqrt{1 - C^2}$$

2Δα



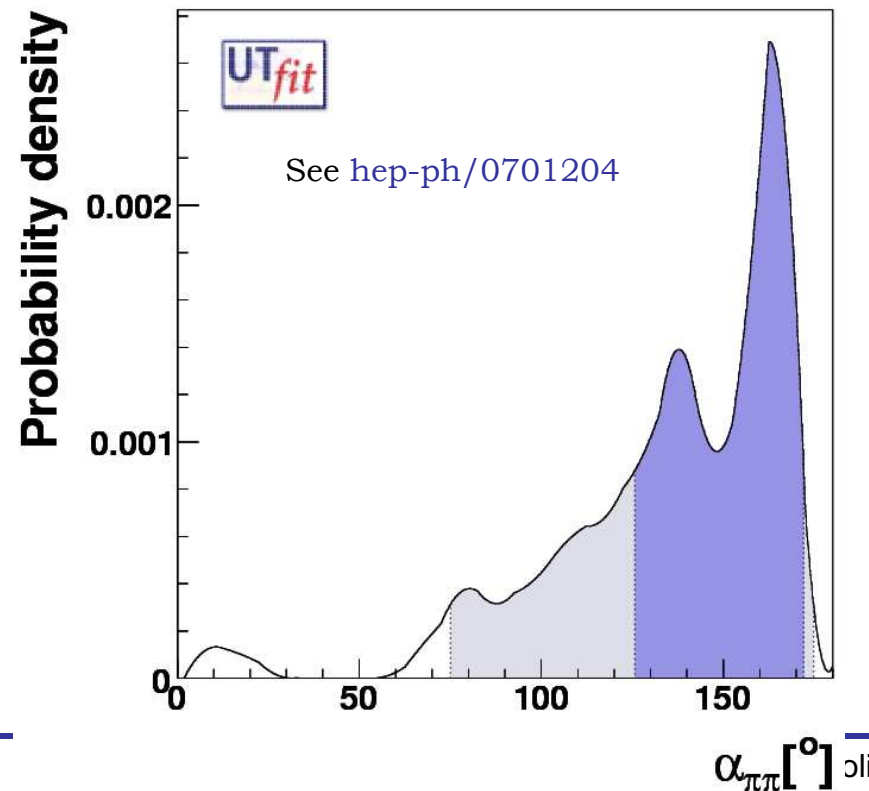


Using isospin relations

$$\text{BR}(B^0 \rightarrow \pi^+ \pi^-) = 5.2 \pm 0.2 \quad \text{HFAG } (10^{-6}) \quad -$$

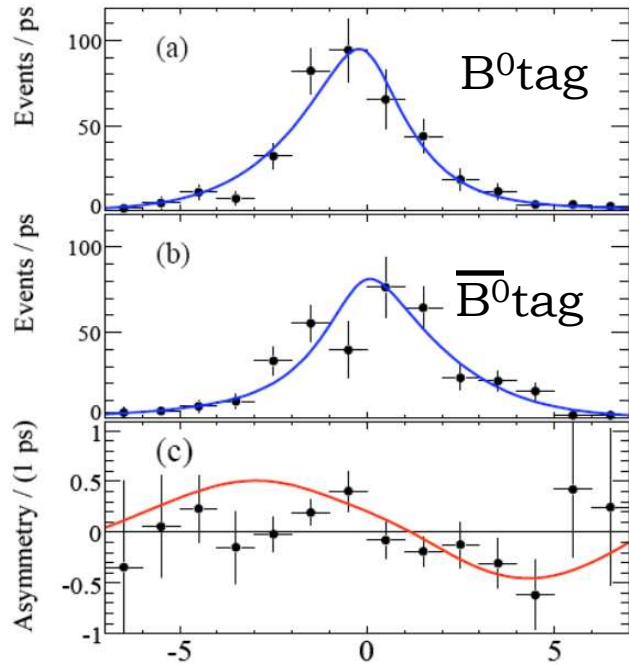
$$\text{BR}(B^+ \rightarrow \pi^+ \pi^0) = 5.7 \pm 0.4 \quad A_{\text{CP}}(B^+ \rightarrow \pi^+ \pi^0) = 0.04 \pm 0.05$$

$$\text{BR}(B^0 \rightarrow \pi^0 \pi^0) = 1.3 \pm 0.2 \quad A_{\text{CP}}(B^0 \rightarrow \pi^0 \pi^0) = 0.36^{+0.33}_{-0.31}$$

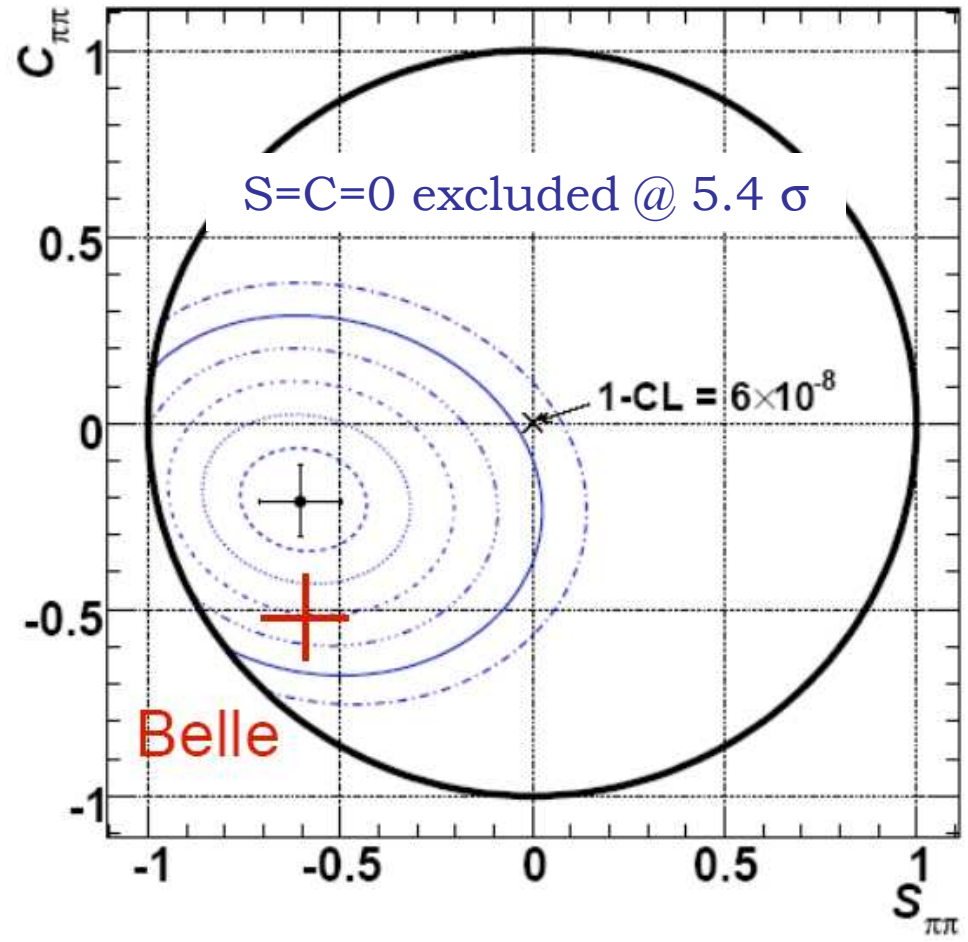




$B^0 \rightarrow \pi^+ \pi^-$ & $B^0 \rightarrow K^+ \pi^-$



383 M BB pairs; hep-ex/0703016



$$N_{\pi\pi} = 1139 \pm 49$$

$$N_{K\pi} = 4372 \pm 82$$

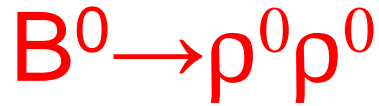
$$S_{\pi\pi} = -0.60 \pm 0.11 \pm 0.03 (5.2\sigma)$$

$$C_{\pi\pi} = -0.21 \pm 0.09 \pm 0.02 (2.2\sigma)$$

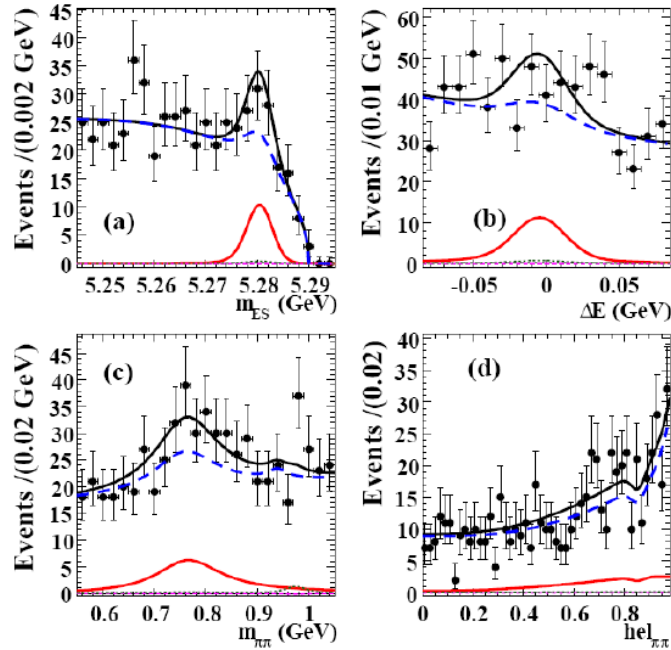
$$A_{K\pi} = -0.107 \pm 0.018^{+0.007}_{-0.004} (5.5\sigma)$$



hep-ex/0612021
PRL accepted



$384 \times 10^6 B\bar{B}$ pairs



$$N_{\rho^0 \rho^0} = 100 \pm 32 \pm 17$$

3.5 σ evidence for $B \rightarrow \rho^0 \rho^0$

$$f_L(B^0 \rightarrow \rho^0 \rho^0) = 0.87 \pm 0.13 \pm 0.04$$

$$Br(B^0 \rightarrow \rho^0 \rho^0) = (1.07 \pm 0.33 \pm 0.19) \cdot 10^{-6}$$

Small $\rho^0 \rho^0$ BF \Rightarrow small penguin pollution



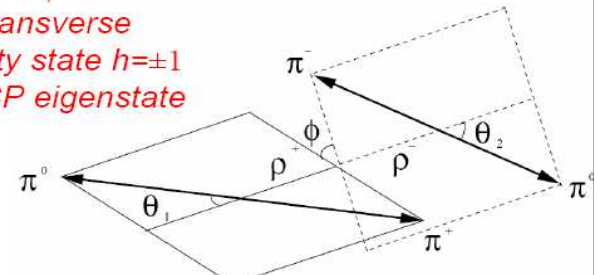
hep-ex/0607097

$347 \times 10^6 B\bar{B}$ pairs

April 11th 2007

$$\frac{d^2 N}{d \cos \theta_1 d \cos \theta_2} \propto \underbrace{f_L \cos^2 \theta_1 \cos^2 \theta_2}_{\text{Longitudinal Helicity state } h=0 \text{ CP+1 eigenstate}} + \underbrace{\frac{1}{4}(1-f_L) \sin^2 \theta_1 \sin^2 \theta_2}_{\text{Transverse Helicity state } h=\pm 1 \text{ non-CP eigenstate}}$$

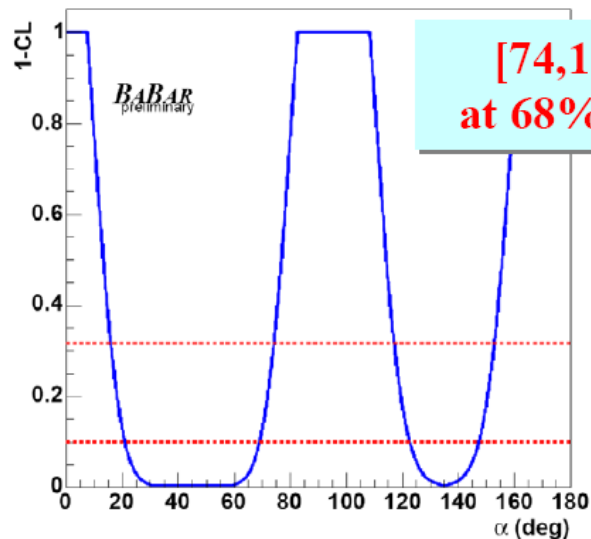
$$f_L = 0.977 \pm 0.024 \begin{matrix} +0.015 \\ -0.013 \end{matrix}$$





All $B \rightarrow \rho\rho$ together

- Isospin analysis of $\rho\rho$ as for $\pi\pi$

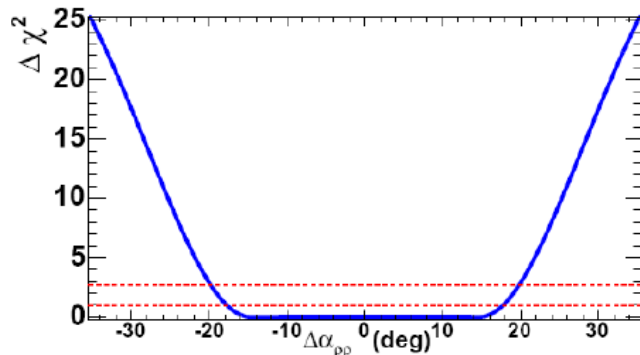


Constraint on α worse than previous result because of:

- smaller $\mathcal{B}(B^\pm \rightarrow \rho^\pm \rho^0)$
- larger $\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0)$

$$|\Delta\alpha| \equiv |\alpha - \alpha_{eff}| < 18^\circ @ 68\%CL$$
$$< 20^\circ @ 90\% CL$$

(previous result $11^\circ @ 68\% CL$)



Still most promising
decay to measure α



More α : $B \rightarrow \pi\pi\pi^0$ (Dalitz)

- describe the $\pi^+\pi^-\pi^0$ final state as sum of interfering $\rho^+\pi^-$, $\rho^-\pi^+$, $\rho^0\pi^0$
- measure the time-dependent and Dalitz Plot-dependent decay rate

Snyder & Quinn,
PRD48, 2139 (1993)

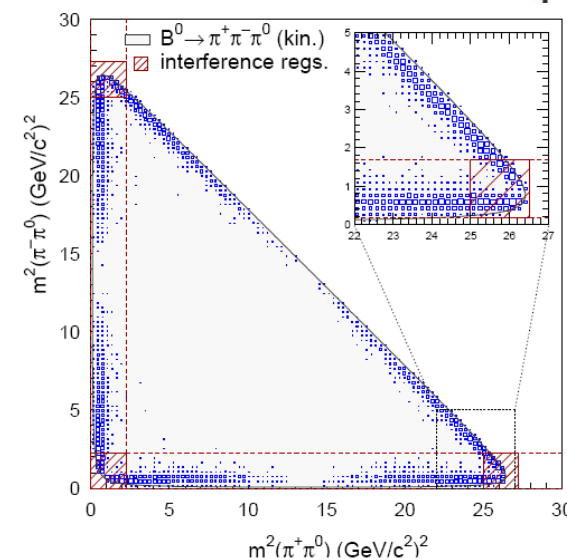
$$|\mathcal{A}_{3\pi}^{\pm}(\Delta t)|^2 = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left[|A_{3\pi}|^2 + |\bar{A}_{3\pi}|^2 \mp (|A_{3\pi}|^2 - |\bar{A}_{3\pi}|^2) \cos(\Delta m_d \Delta t) \pm 2\text{Im} [\bar{A}_{3\pi} A_{3\pi}^*] \sin(\Delta m_d \Delta t) \right]$$

$$A_{3\pi} = f_+ A^+ + f_- A^- + f_0 A^0 \quad \text{charge of } \rho$$

$$\bar{A}_{3\pi} = f_+ \bar{A}^+ + f_- \bar{A}^- + f_0 \bar{A}^0$$

Dalitz Model
 $f_i(m_{\pi^+\pi^0}^2, m_{\pi^-\pi^0}^2)$

strong and weak phases
 $A^\kappa = T^\kappa e^{-i\alpha} + P^\kappa$
 $\bar{A}^\kappa = T^{\bar{\kappa}} e^{+i\alpha} + P^{\bar{\kappa}}$





hep-ex/0703008

Extracting α from $B \rightarrow \pi\pi\pi^0$

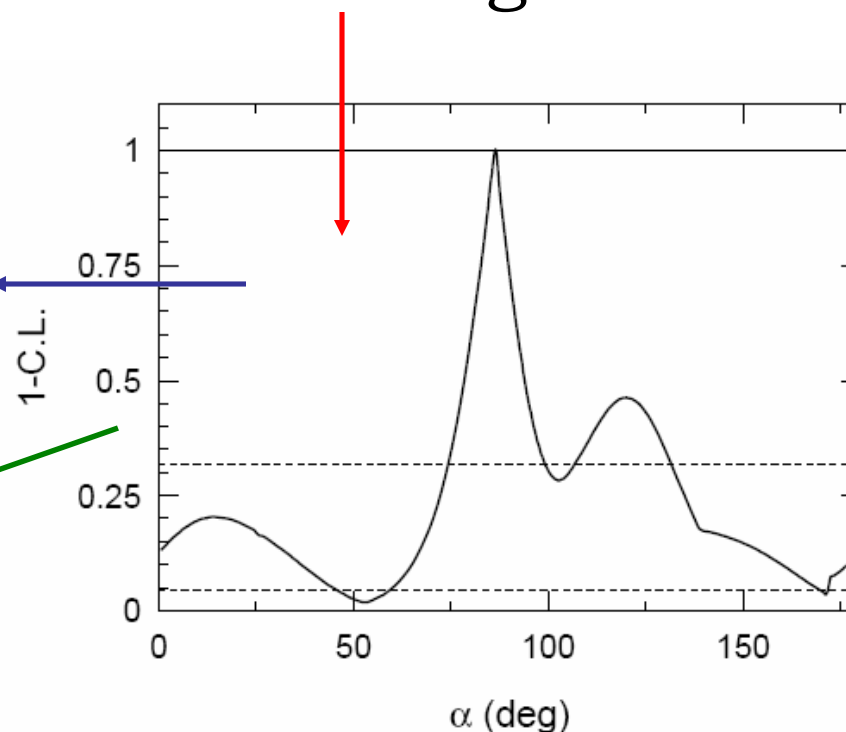
375M BB



- use frequentist procedure to extract a CL for α from the 26 parameters
 - The method extracts without ambiguities in $[0, 180]^\circ$

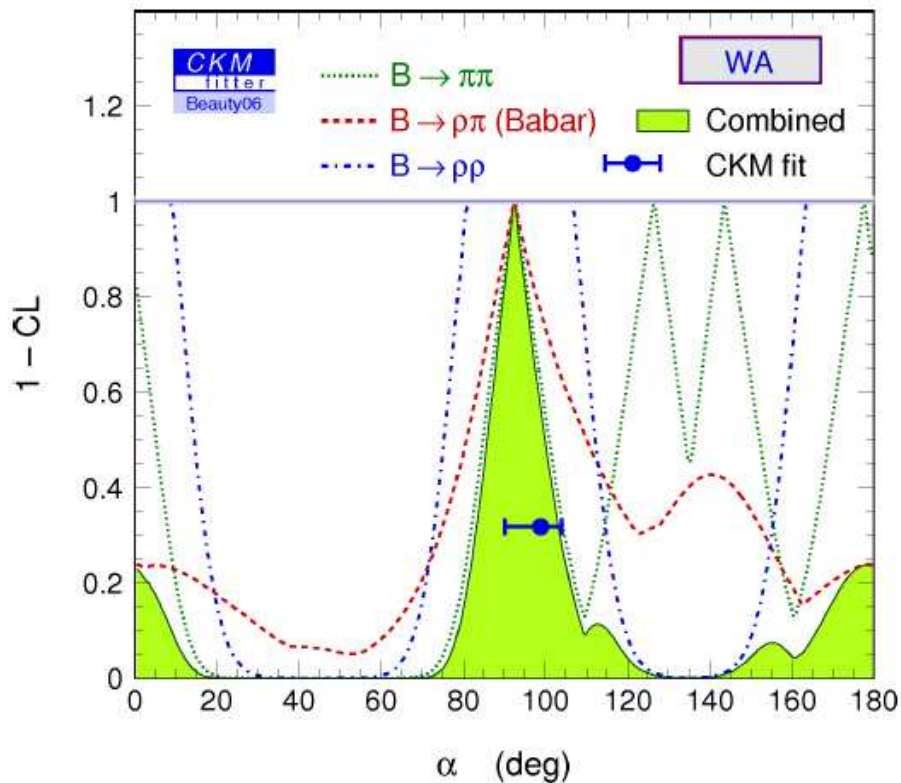
Result consistent with SM

Need more data to set a constraint at 90% C.L.

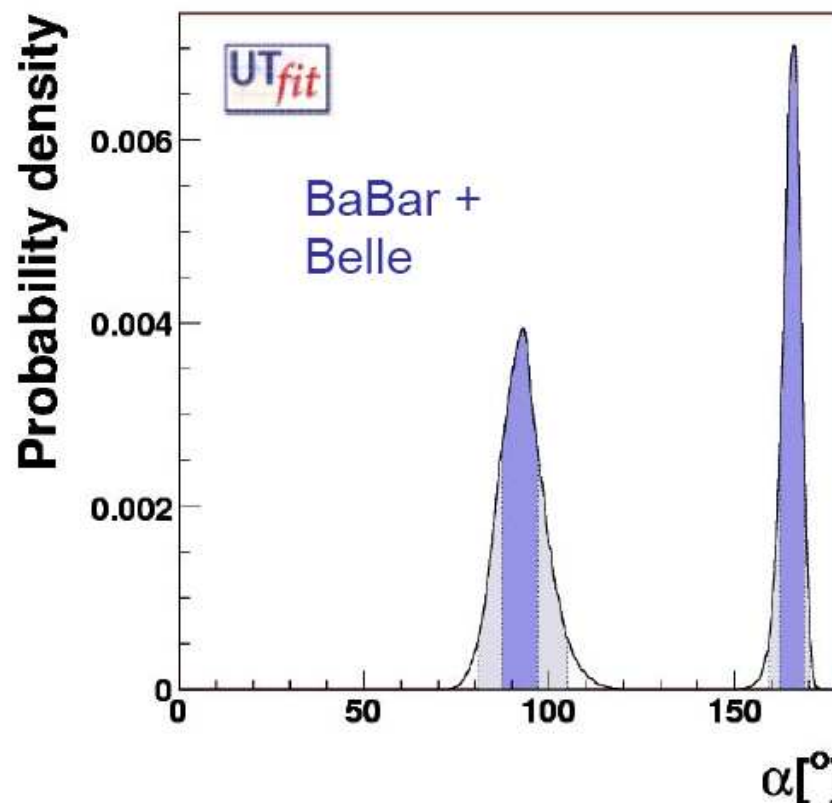




α : the whole picture



$$\alpha_{WA,CKMfitter} = (93_{-9}^{+11})^\circ$$



$$\alpha_{WA,UTfit} = [81,105]^\circ \cup [159,171]^\circ @95\%CL$$



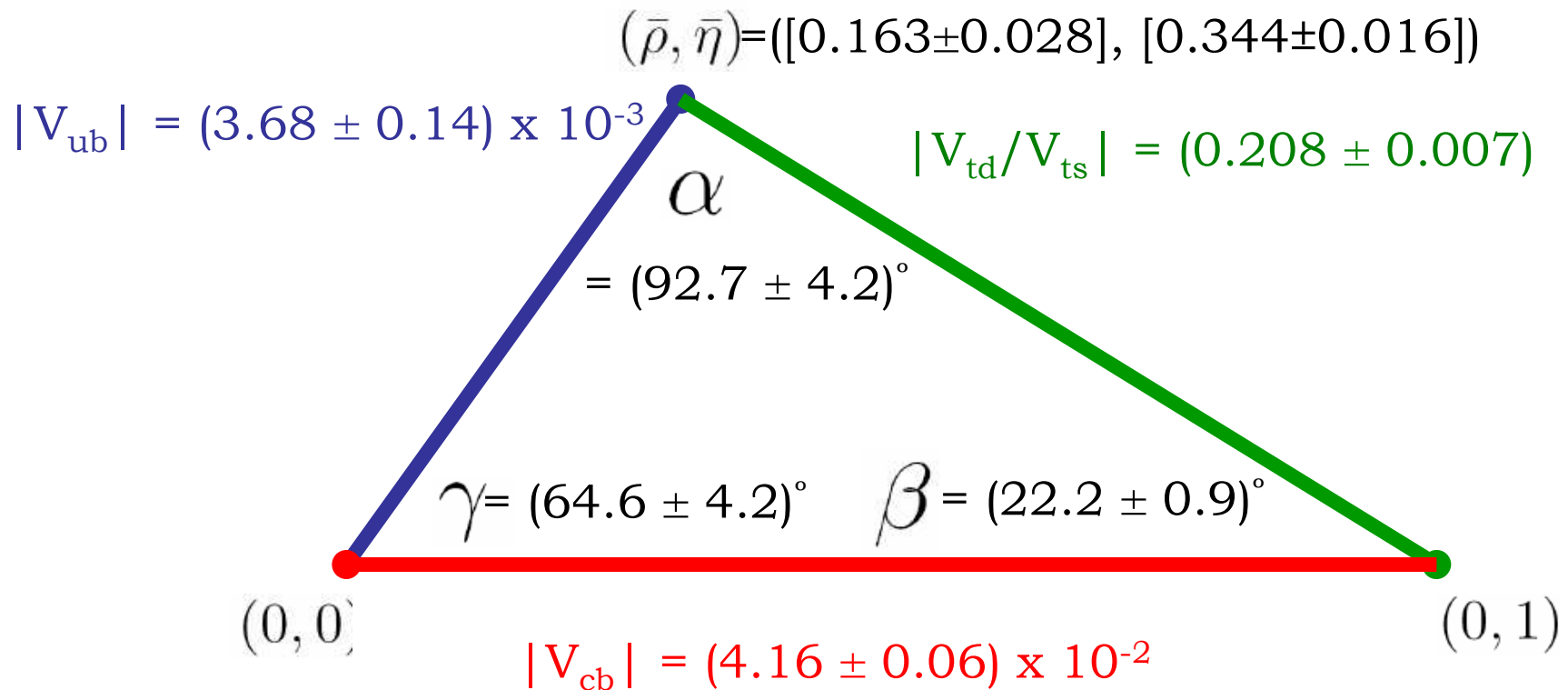
Conclusions



UTfit™ : global fit

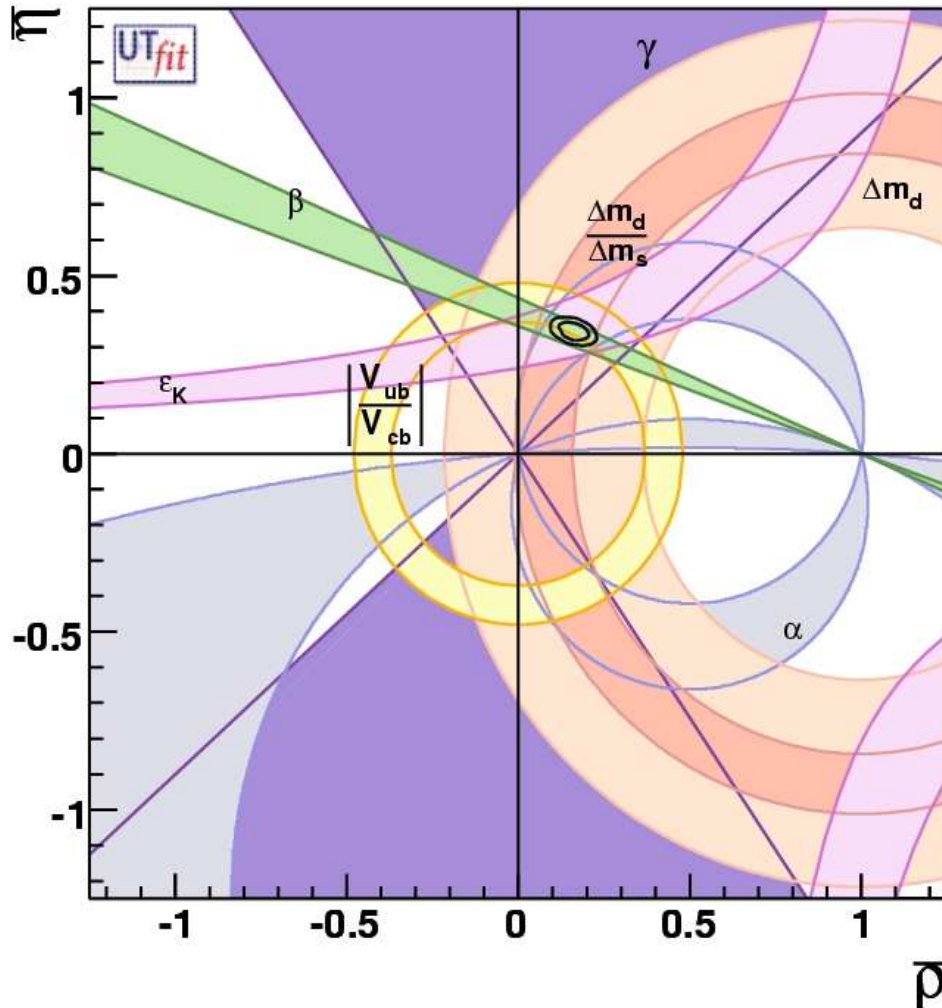


<http://utfit.roma1.infn.it>





CKM: it works!



•CKM is now a tested theory

•Great success for the Standard Model

$$\alpha = (93^{+11}_{-9})^\circ$$

$$\beta = (21.2 \pm 1.0)^\circ$$

$$\gamma = (62^{+38}_{-24})^\circ$$

$$|V_{cb}| = (4.15 \pm 0.07) \times 10^{-2}$$

$$|V_{ub}| = (4.09 \pm 0.26) \times 10^{-3}$$

$$|V_{td}/V_{ts}| = 0.202 \pm 0.021$$

BaBar massively contributed to this great success!!!



The end





Backup slides



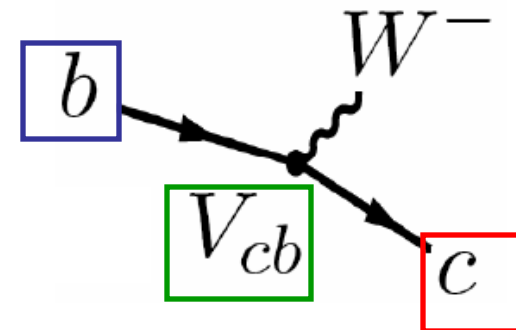


Quark mixing matrix

- weak and mass eigenstates of the quarks are not the same
- changes in base are described by unitarity transformations
- Cabibbo Kobayashi Maskawa (CKM) matrix
- with 3 quark families there is an irreducible complex phase in the matrix
- This is responsible of CP Violation in Standard Model (SM)

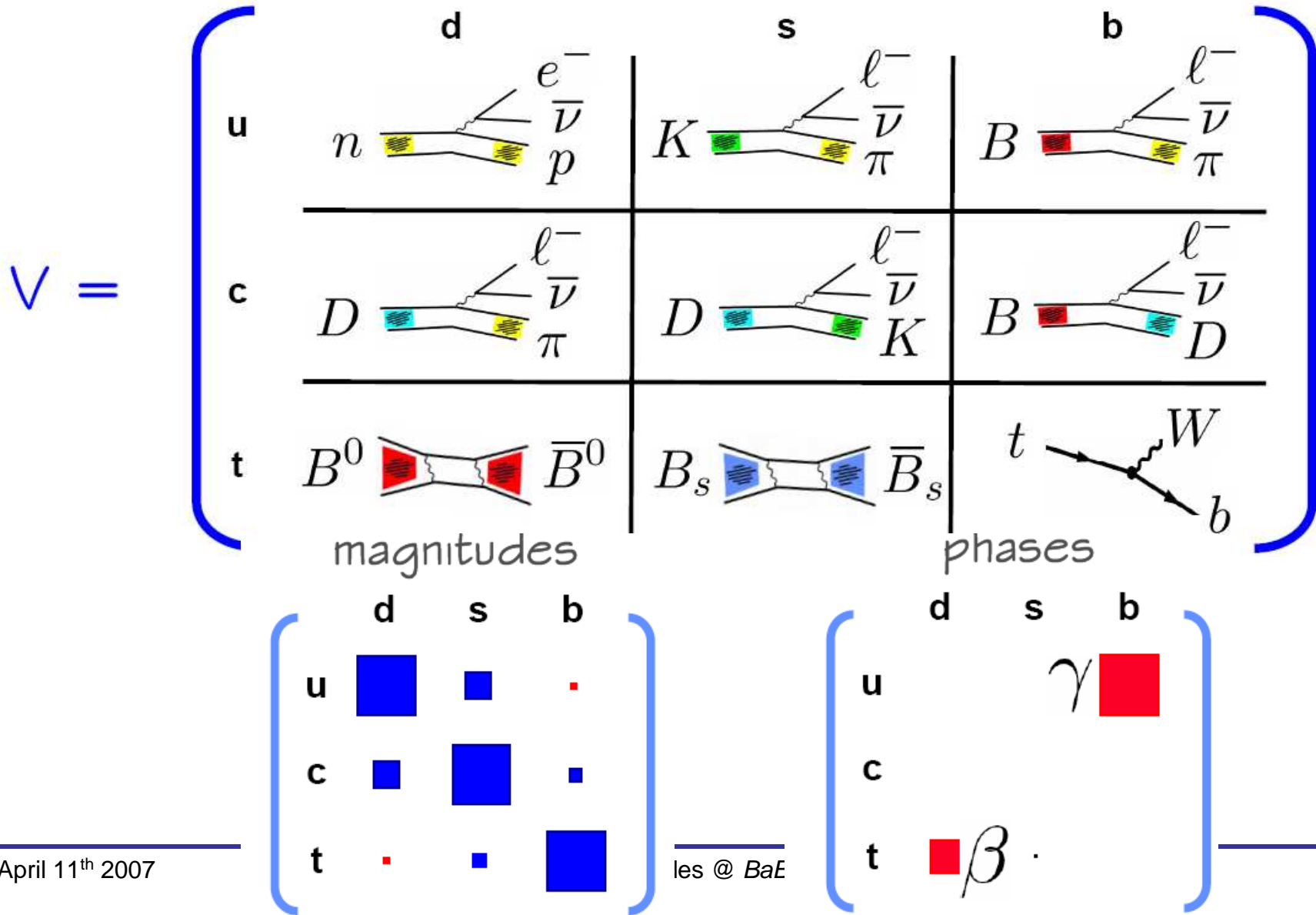
$$\mathbf{V} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

CKM elements:
“weak couplings”
between Down-type
and Up-type quarks





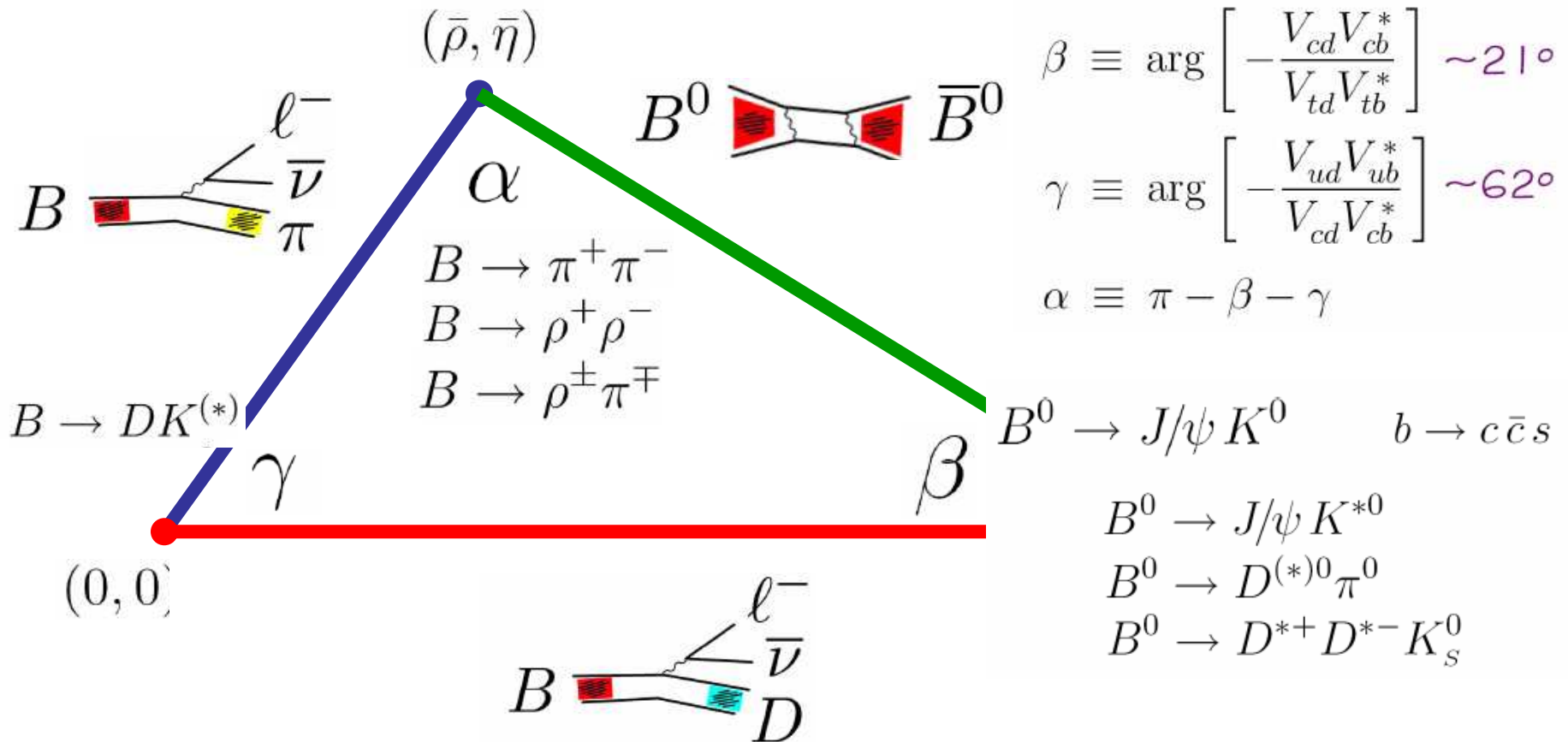
CKM matrix





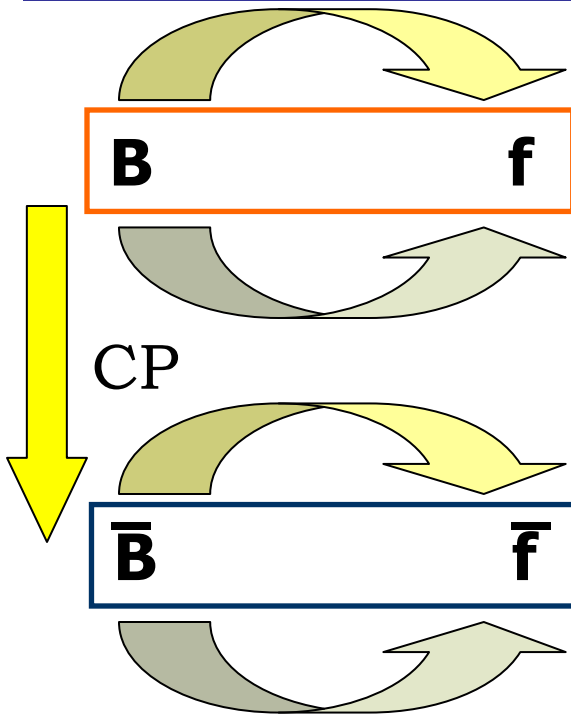
The Unitarity Triangle (UT)

$$V_{td}V_{tb}^* + V_{cd}V_{cb}^* + V_{ud}V_{ub}^* = 0$$





CP violation in B mesons (I)



$$A_1 = a_1 e^{i\phi_1} e^{i\delta_1}$$

$$A_2 = a_2 e^{i\phi_2} e^{i\delta_2}$$

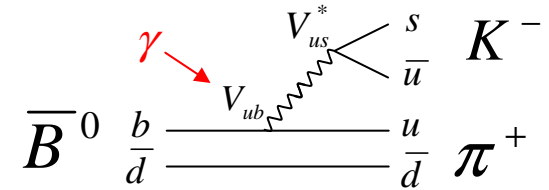
$$\bar{A}_1 = a_1 e^{-i\phi_1} e^{i\delta_1}$$

$$\bar{A}_2 = a_2 e^{-i\phi_2} e^{i\delta_2}$$

Interference $\rightarrow (A_1 + A_2)^2 \neq (\bar{A}_1 + \bar{A}_2)^2$

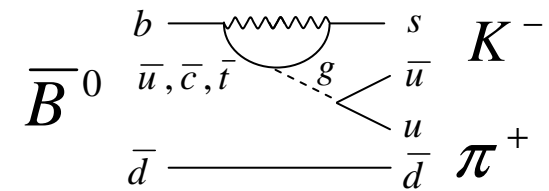
$$\text{Asymmetry} = \frac{\Gamma(\mathbf{B}) - \Gamma(\bar{\mathbf{B}})}{\Gamma(\mathbf{B}) + \Gamma(\bar{\mathbf{B}})} = \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} \sim 2 \sin(\phi_1 - \phi_2) \sin(\delta_1 - \delta_2)$$

Tree decay



$$A \propto V_{us}^* V_{ub}$$

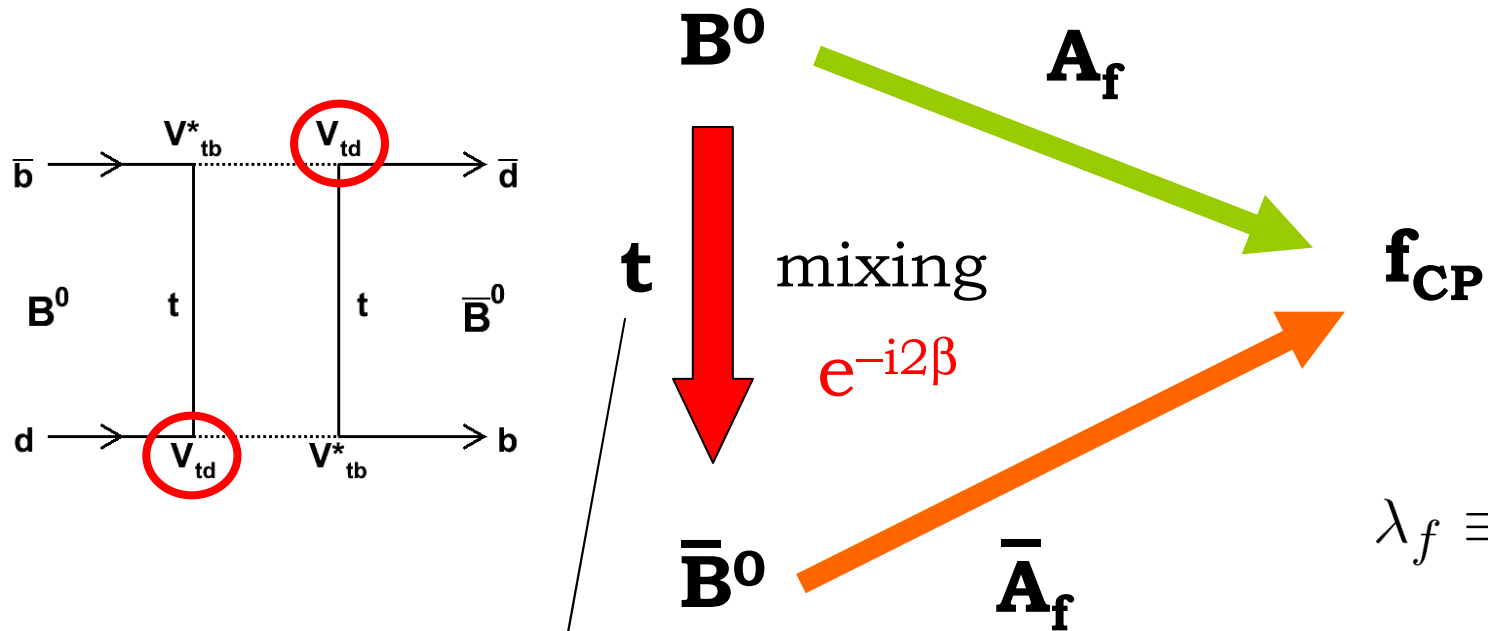
Penguin decay



$$A \approx V_{ts}^* V_{tb}$$



CP violation in B mesons (II)



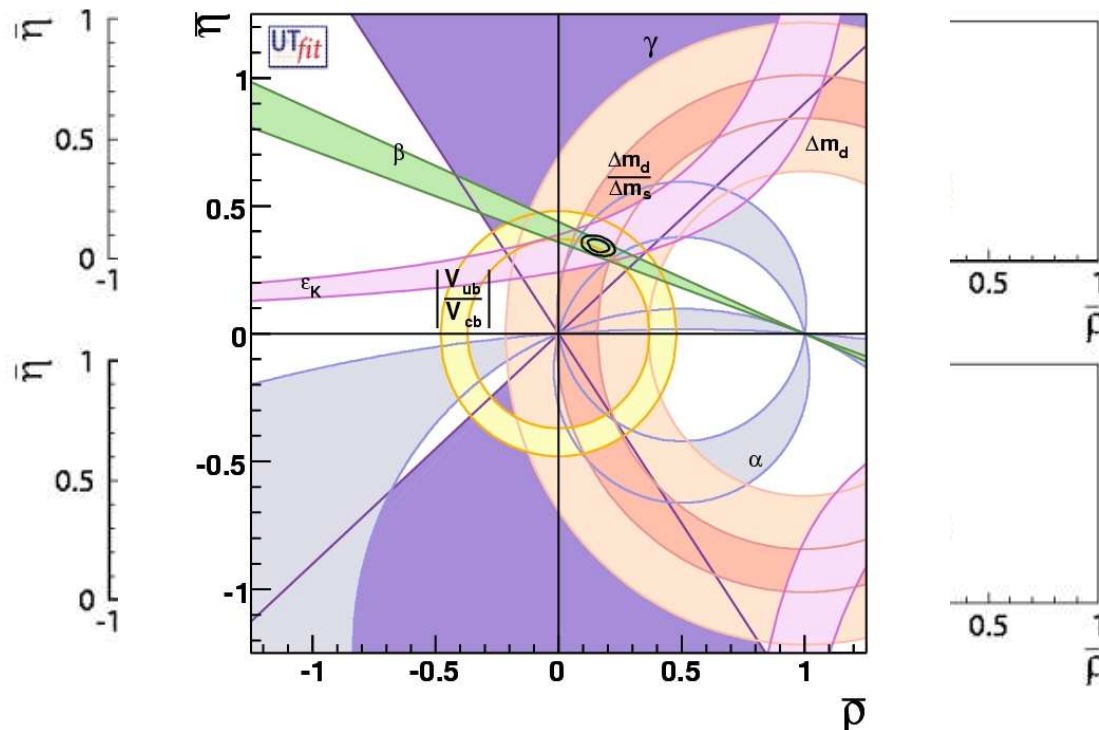
$$\lambda_f \equiv \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

$$A_{CP} = \frac{\Gamma(\bar{B}^0(t) \rightarrow f) - \Gamma(B^0(t) \rightarrow f)}{\Gamma(\bar{B}^0(t) \rightarrow f) + \Gamma(B^0(t) \rightarrow f)} = \underbrace{\frac{1 - |\lambda|^2}{1 + |\lambda|^2}}_C \cos(\Delta m \cdot t) + \underbrace{\frac{2 \text{Im}(\lambda)}{1 + |\lambda|^2}}_S \sin(\Delta m \cdot t)$$



Idea: overconstrain UT

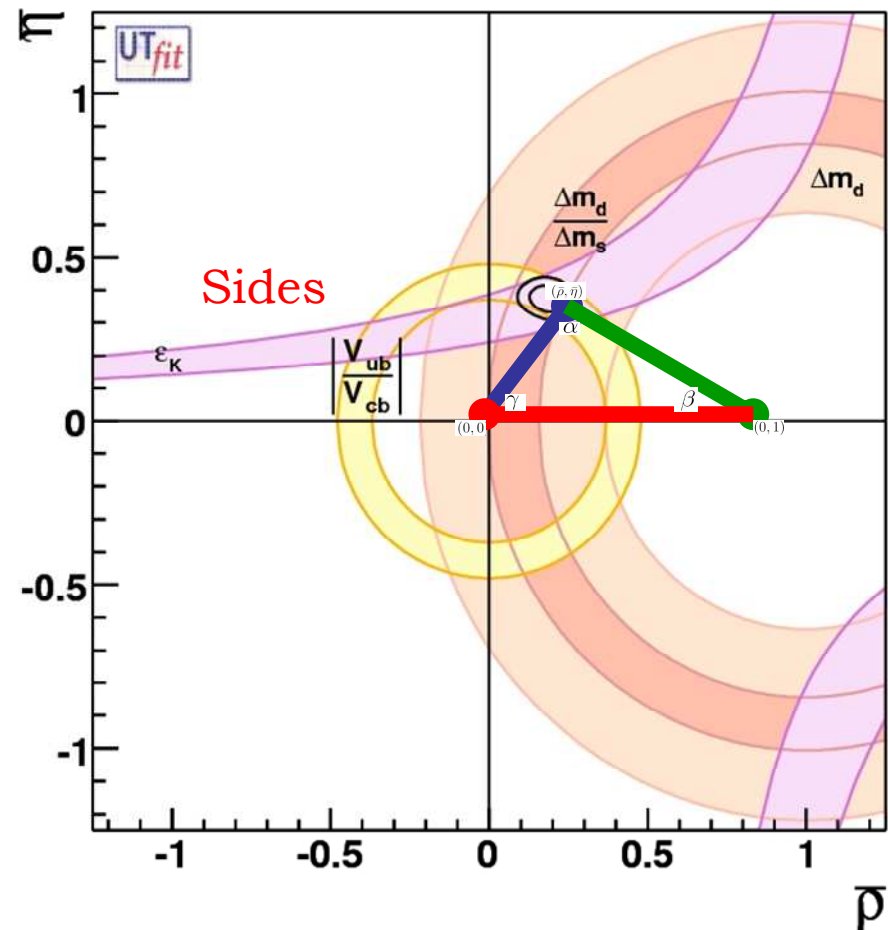
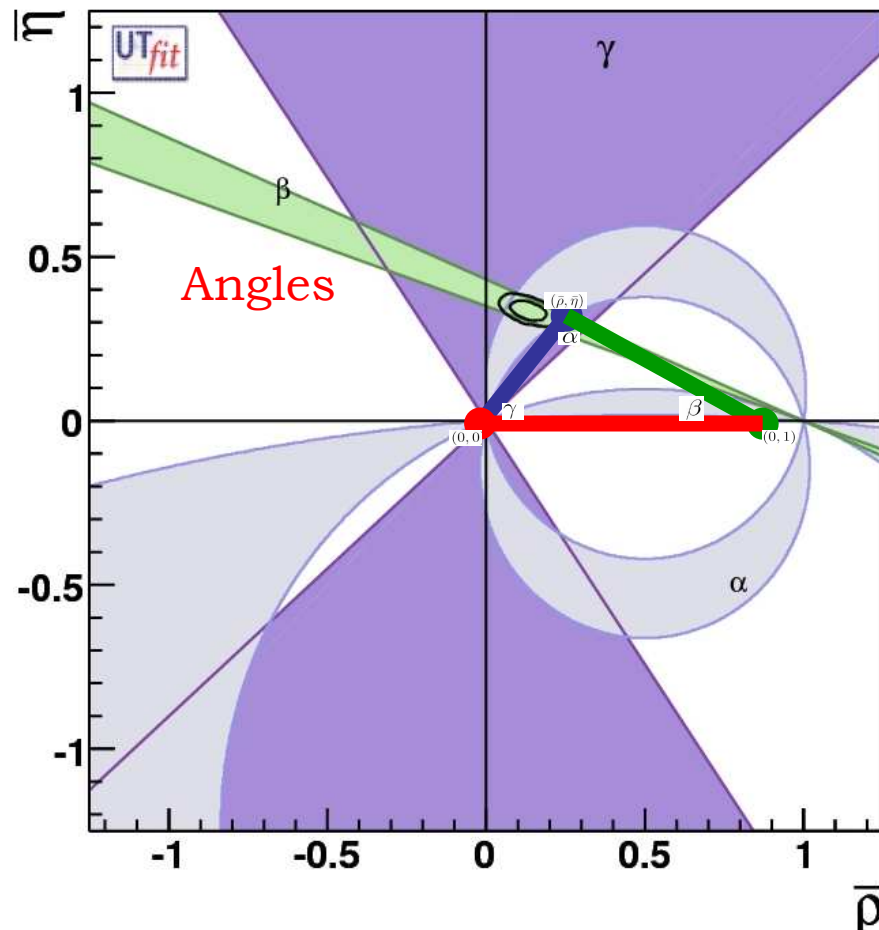
- Measuring different B decays, all UT parameters can be determined
- There are several independent constraints available





UT & CP violation

- UT area $\neq 0 \Leftrightarrow$ CP violation





Exclusive B decay reconstruction

- **Likelihood fits with discriminating variables:**

- **Kinematics:**

$$m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$

$$\Delta E = E_B^* - E_{beam}^*$$

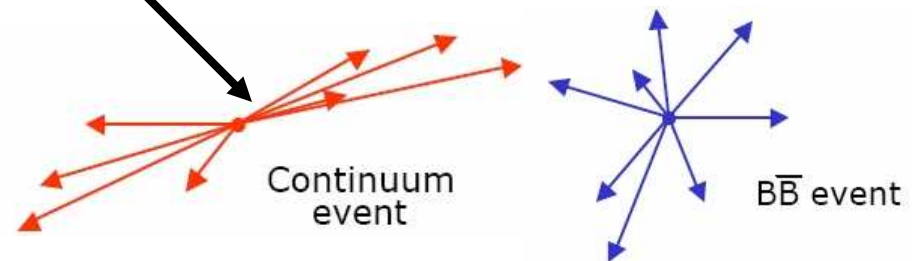
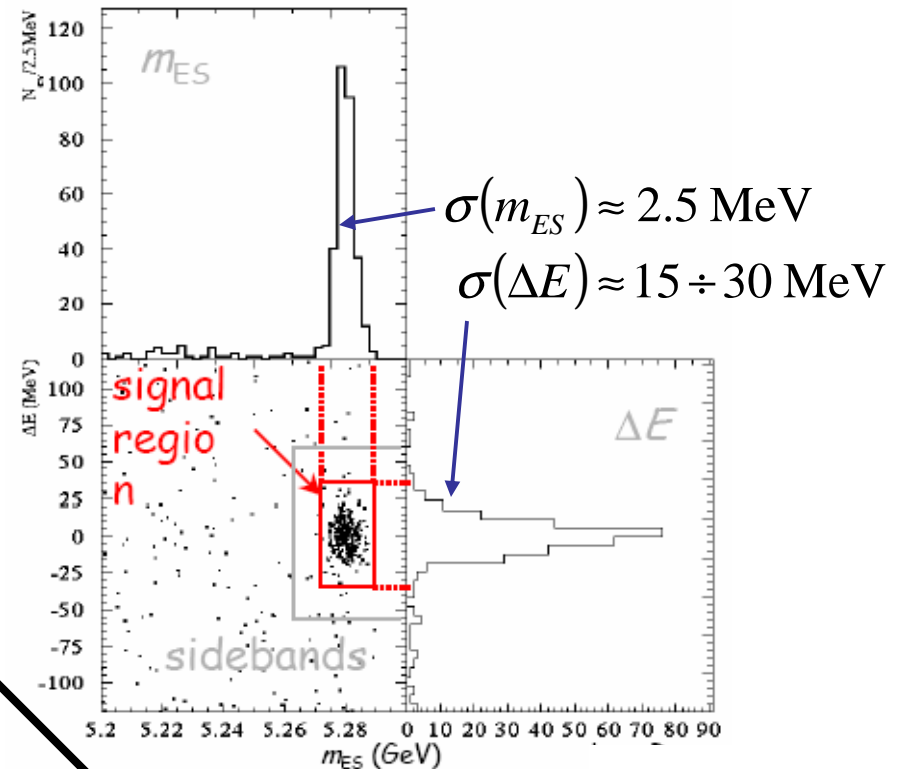
- **Particle ID: π , K , e , μ , ...**
- **Event shape variables, to separate the continuum bkgd (use “off-resonance” data as control sample!!!)**

- **Efficiency**

- Typically $\varepsilon \approx 15 \div 40\%$

- **Purity**

- Up to 97% (for $J/\psi K_S$)





Resolutions

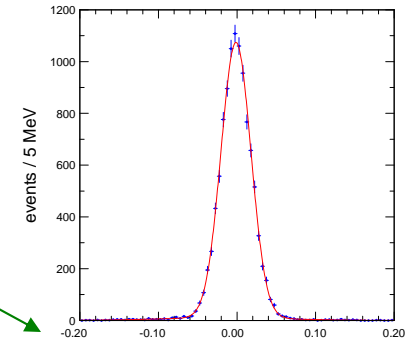
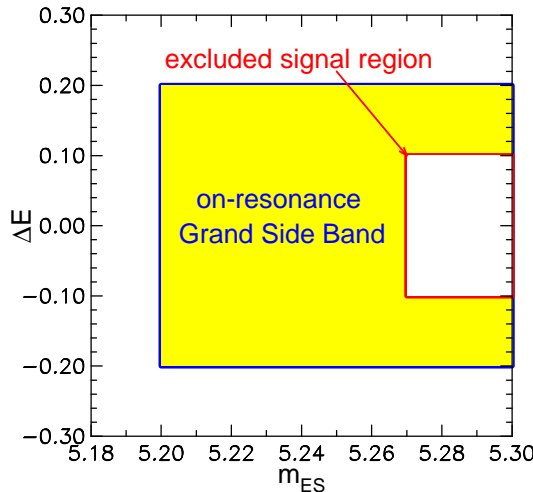
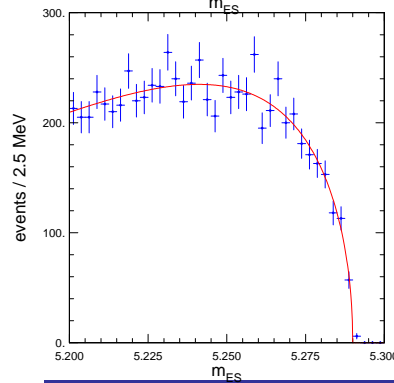
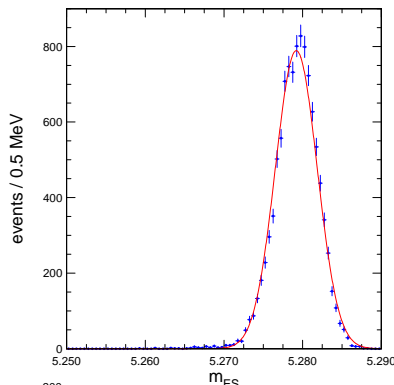
Variables that reflect energy and momentum conservation:
peaking for fully reconstructed B decays, smooth for combinatorial background

$$m_{ES} \equiv \sqrt{E_{CM\ beam}^2 - p_{CM\ B}^2} = m_B$$

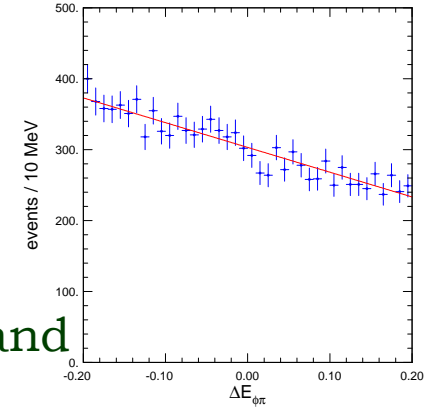
$$\Delta E \equiv E_{CM\ B} - E_{CM\ beam} = 0$$

resolution ~ 2.5 – 3.0 MeV

depending on
presence of neutrals
in the final state



resolution ~ 15 – 80 MeV



continuum background in the Grand Side Band



Tagging: efficiency and effects

The figure of merit for tagging is the effective tagging efficiency $Q \equiv \sum_i \varepsilon_i (1 - 2w_i)^2 = (30.4 \pm 0.3)\%$

Category	ε (%)	w (%)	Δw (%)	Q (%)
Lepton	8.67 ± 0.08	3.0 ± 0.3	-0.2 ± 0.6	7.67 ± 0.13
Kaon I	10.96 ± 0.09	5.3 ± 0.4	-0.6 ± 0.7	8.74 ± 0.16
Kaon II	17.21 ± 0.11	15.5 ± 0.4	-0.4 ± 0.7	8.21 ± 0.19
Kaon-Pion	13.77 ± 0.10	23.5 ± 0.5	-2.4 ± 0.8	3.87 ± 0.14
Pion	14.38 ± 0.10	33.0 ± 0.5	5.2 ± 0.8	1.67 ± 0.10
Other	9.61 ± 0.08	41.9 ± 0.6	4.6 ± 0.9	0.25 ± 0.04
All	74.60 ± 0.12			30.4 ± 0.3

$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left\{ (1 \mp \Delta\omega) \pm (1 - 2\omega) \times \left[\frac{2\text{Im}\lambda}{1 + |\lambda|^2} \sin(\Delta m_d \Delta t) - \frac{1 - |\lambda|^2}{1 + |\lambda|^2} \cos(\Delta m_d \Delta t) \right] \right\}$$



$|V_{ub}|$: untagged Vs tagged

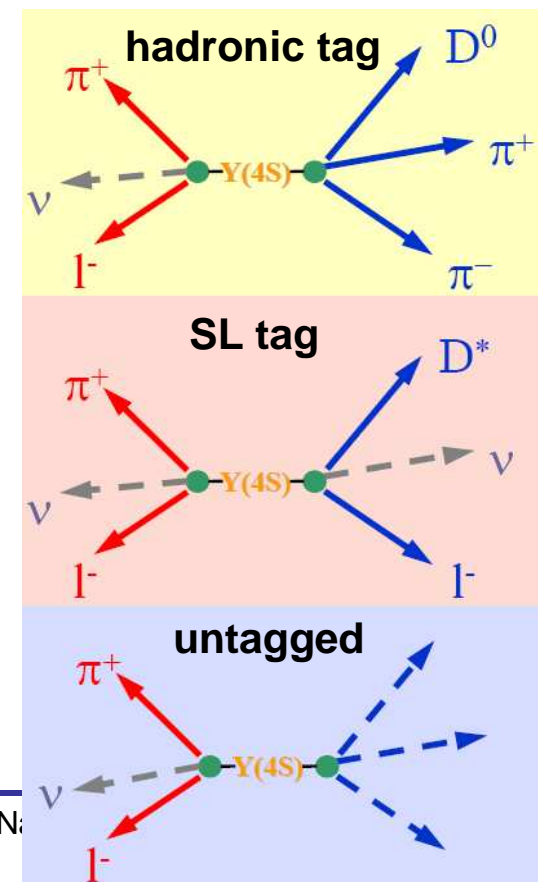
- Complementary experimental approaches
 - different systematic errors
 - statistically independent samples

Tagged:

- reconstruct non-signal B to select $Y(4S) \rightarrow B_{\text{tag}} B_{\text{sig}}$ events
- B_{tag} reconstructed via hadronic or semileptonic decays
- ✓ high signal purity for almost all phase space
- ✗ low signal efficiency

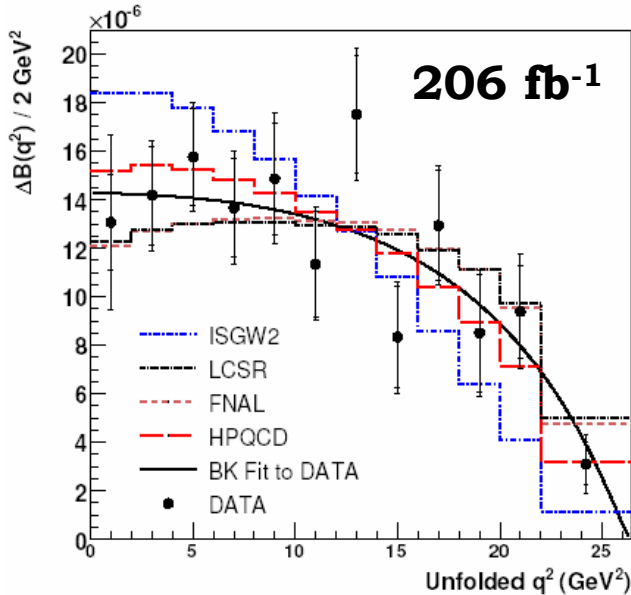
Untagged:

- reconstruct $B_{\text{sig}} \rightarrow Xlv$ only
- v reconstruction using event's P_{miss}
- ✗ lower signal purity and restricted phase space
- ✓ high signal efficiency





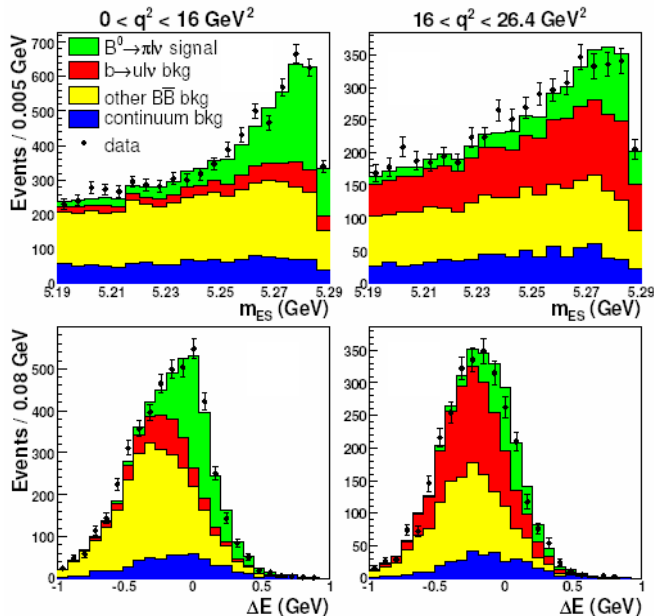
Exclusive $|V_{ub}|$ (untagged)



Measurement of $|V_{ub}|$ and $B^0 \rightarrow \pi \ell \nu$ form-factor shape with a loose neutrino reconstruction technique

hep-ex/0612020 (accepted by Phys. Rev. Lett.)

- Reconstruct ~ 5000 signal events, in 12 q^2 bins
- Signal & bkgd yields by a multi-parameter fit ($m_{ES}; \Delta E, q^2$)
- test QCD calculations:
 - LQCD and LCSR compatible with our data
 - ISGW2 quark-model incompatible (Prob < 0.06%).



$$BF(B^0 \rightarrow \pi \ell \nu) = (1.46 \pm 0.07_{stat} \pm 0.08_{syst}) \times 10^{-4}$$

$$|V_{ub} f_+(0)| = (9.6 \pm 0.3_{stat} \pm 0.2_{syst}) \times 10^{-4}$$

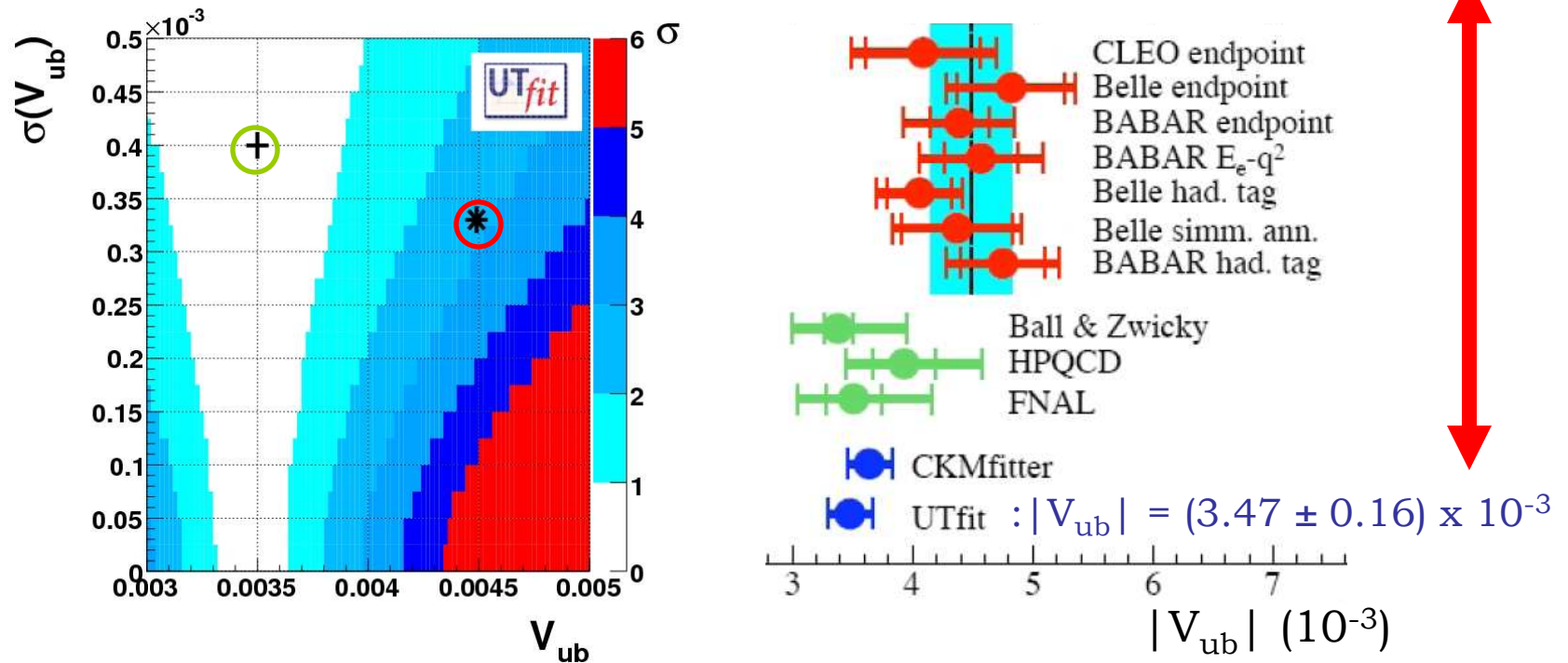
$$|V_{ub}| = (4.1 \pm 0.2_{stat} \pm 0.2_{syst}^{+0.6}_{-0.4 FF}) \times 10^{-3} \quad (\text{HPQCD})$$

Smallest statistical & systematic uncertainties of all individual $B \rightarrow \pi \ell \nu$ measurements to date!!!



The $|V_{ub}|$ puzzle

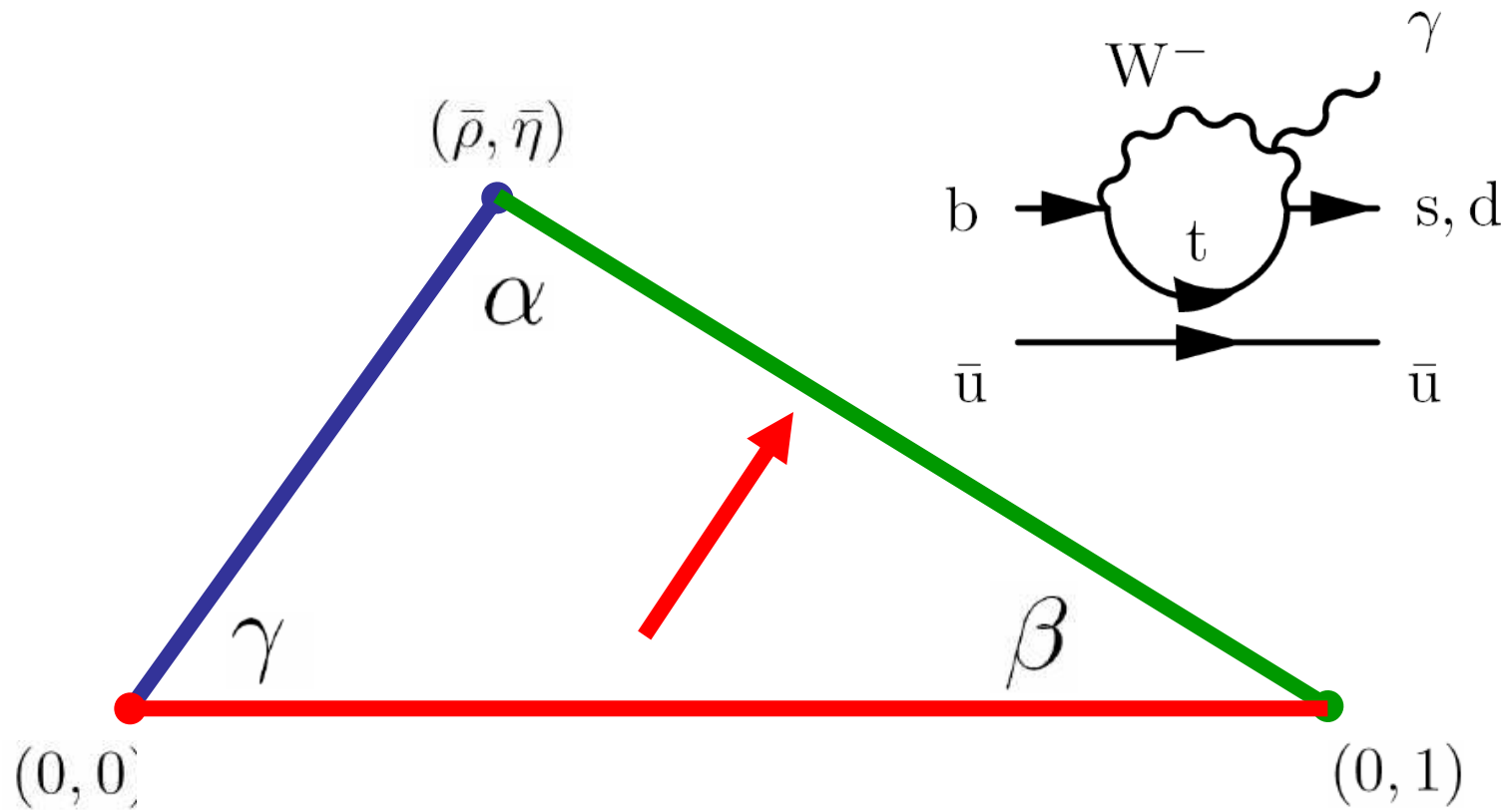
Direct measurement: $|V_{ub}| = (4.09 \pm 0.26) \times 10^{-3}$



- 2-3 sigmas difference between inclusive $|V_{ub}|$ measurements and global CKM fits
- exclusive $|V_{ub}|$ measurements seem to agree better...

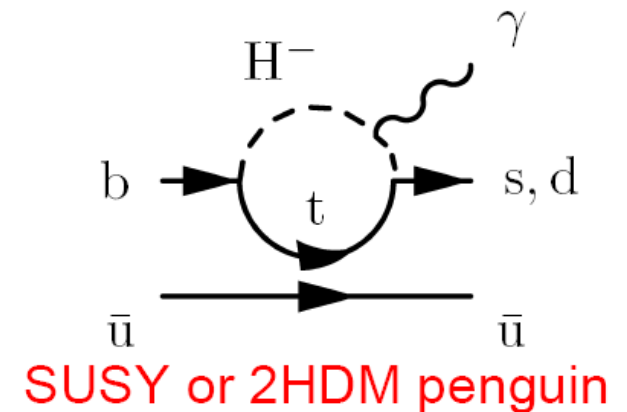
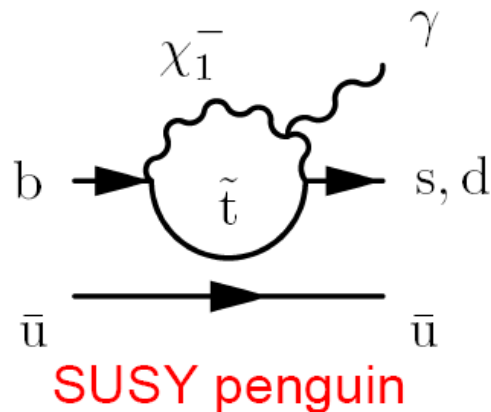
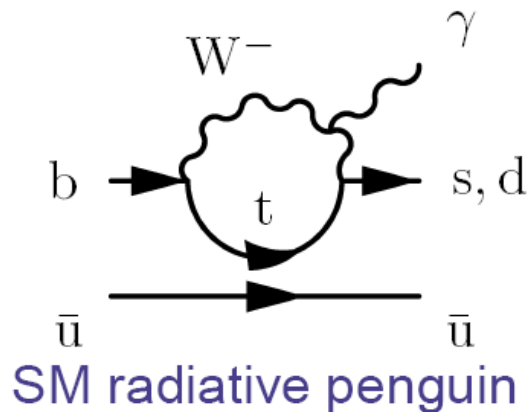


$$|V_{td}/V_{ts}|$$





$|V_{td}/V_{ts}|$: radiative penguins



- Possibility to measure $|V_{td}| / |V_{ts}|$ independently of $\Delta m_d / \Delta m_s$

$$\frac{\Gamma(B \rightarrow \rho\gamma)}{\Gamma(B \rightarrow K^*\gamma)} = \left| \frac{V_{td}}{V_{ts}} \right|^2 \frac{(m_B - m_\rho)^3}{(m_B - m_{K^*})^3} \left(\frac{T^\rho(0)}{T^{K^*}(0)} \right)^2 (1 + \Delta R)$$

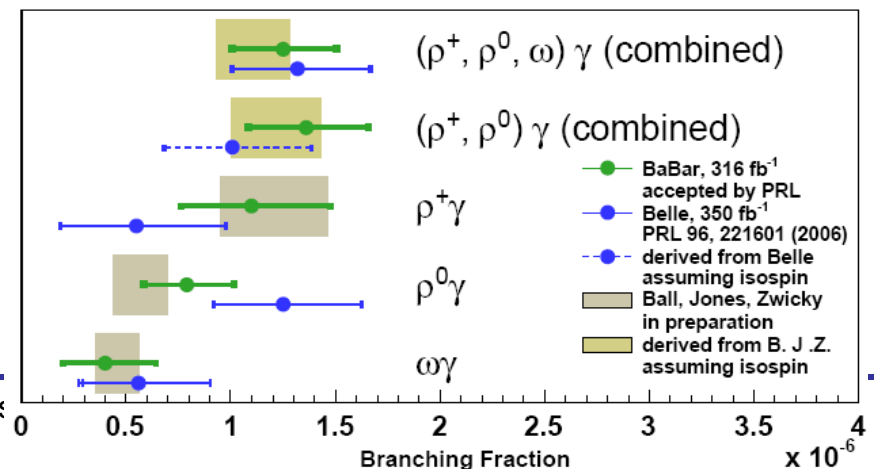
$\Delta R = 0.1 \pm 0.1$ **Ali, Lunghi, Parkhomenko, PLB595, 323 (2004),**

$\left(\frac{T^\rho(0)}{T^{K^*}(0)} \right)^{-1} = 1.17 \pm 0.09$ **Ball,Zwicky JHEP0604, 046 (2006), hep-ph/0603232**



$|V_{td}/V_{ts}|$: radiative penguins

- BaBar results (10^{-6}):
 - hep-ex/0612017, accepted by PRL
 - $(\rho^0\gamma)$: $0.79^{+0.22}_{-0.20} \pm 0.06$ (4.9σ)
 - $(\rho^\pm\gamma)$: $1.1^{+0.37}_{-0.33} \pm 0.09$ (3.8σ): 1st evidence!
 - $B(\omega\gamma)$: $0.40^{+0.24}_{-0.20} \pm 0.05$ (2.2σ)
 - $B((\rho/\omega)\gamma)$: $1.25^{+0.25}_{-0.24} \pm 0.09$ (6.4σ)





Measure $|V_{td}|/|V_{ts}|$ indep. of $\Delta m_d/\Delta m_s$

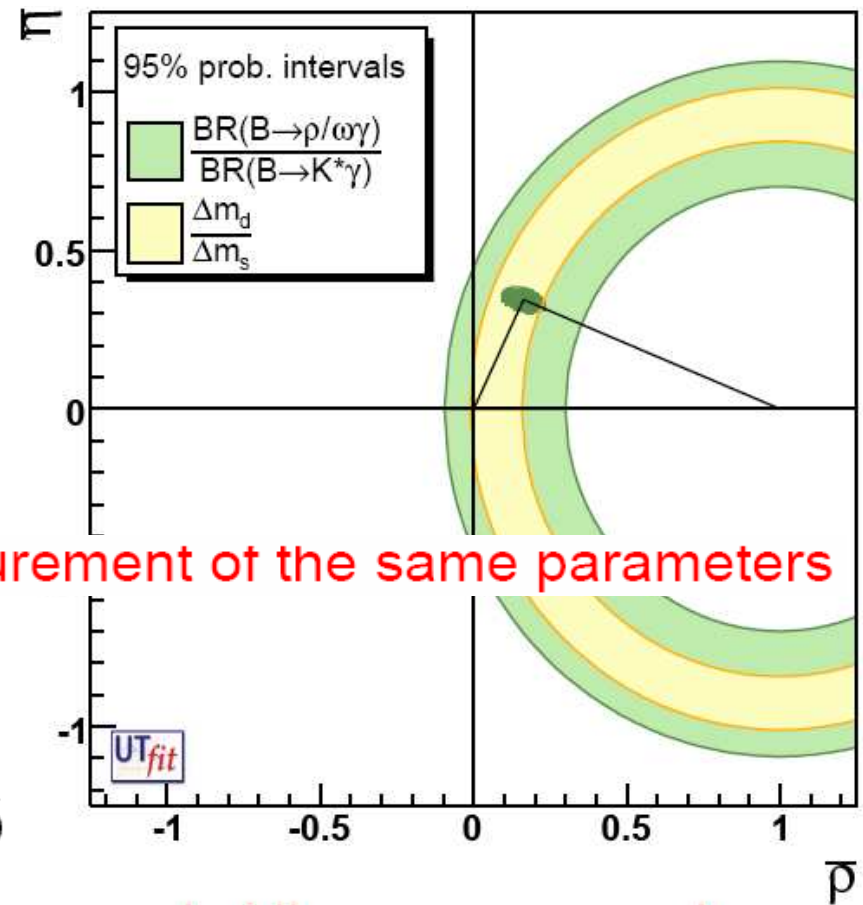


$$\mathcal{B}(B \rightarrow \rho/\omega\gamma)(10^{-6}) : \quad \underbrace{1.25^{+0.25}_{-0.24} \pm 0.09}_{\text{BaBar}} \quad \underbrace{1.32^{+0.34+0.10}_{-0.31-0.09}}_{\text{Belle}} \quad \underbrace{1.28^{+0.20}_{-0.19} \pm 0.06}_{\text{Average}}$$

$$\left| \frac{V_{td}}{V_{ts}} \right|_{\rho/\omega\gamma} = 0.202 \underbrace{^{+0.017}_{-0.016}}_{8.2\%} \pm \underbrace{0.015}_{7.4\%}$$

Ball, Jones, Zwicky hep-ph/0612081

Different diagrams: independent measurement of the same parameters



$$\left| \frac{V_{td}}{V_{ts}} \right|_{\Delta m_d/\Delta m_s} = 0.2060 \pm 0.0007 \underbrace{^{+0.0081}_{-0.0060}}$$



Charmonium K^0 : details



- B_{CP} sample
- $B \rightarrow J/\psi K^0$
 - $J/\psi \rightarrow e e, \mu \mu$
 - $K_S^0 \rightarrow \pi \pi$
 - K_L^0 : cluster
- $B \rightarrow \psi(2S) K^0$
 - $\psi(2S) \rightarrow e e, \mu \mu, J/\psi \gamma$
- $B \rightarrow x_{c1} K^0$
 - $x_{c1} \rightarrow J/\psi \gamma$
- $B \rightarrow \eta_c K^0$
 - $\eta_c \rightarrow K^0 K^+ \pi^-$

- B_{flav} sample
 - $B \rightarrow D^{*-} \pi^+$
 - $B \rightarrow D^{*-} \rho^+$
 - $B \rightarrow D^{*-} a_1^+$
 - $B \rightarrow D^- \pi^+$
 - $B \rightarrow J/\psi K^{*0} (K^{*0} \rightarrow K^+ \pi^-)$

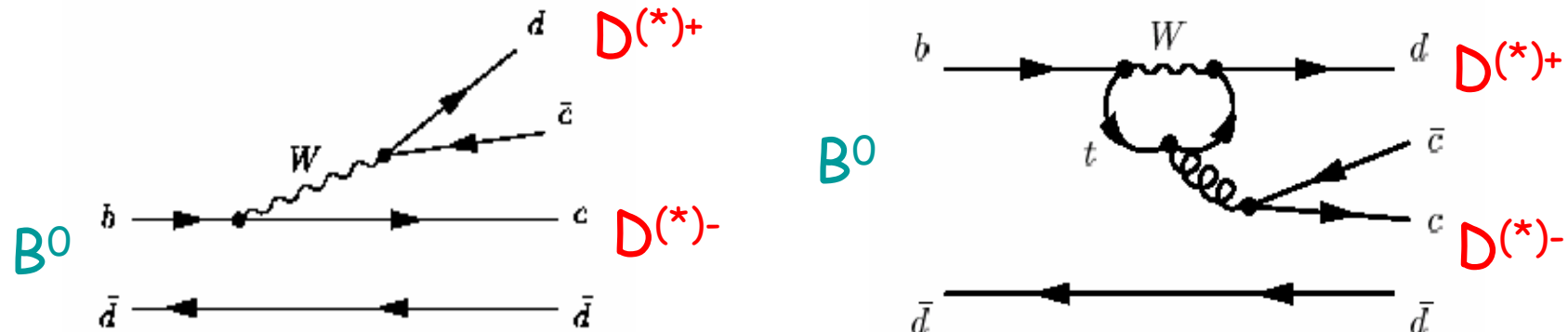
For tagging
performance
and
resolution
studies

- B^- sample
 - $B^- \rightarrow D^0 \pi^-$
 - $B^- \rightarrow D^{*0} \pi^-$
 - $B^- \rightarrow J/\psi K^-$
 - $B^- \rightarrow \psi(2S) K^-$
 - $B^- \rightarrow x_{c1} K^-$
 - $B^- \rightarrow J/\psi K^{*-} (K^{*-} \rightarrow K^- \pi^0)$

Control
sample



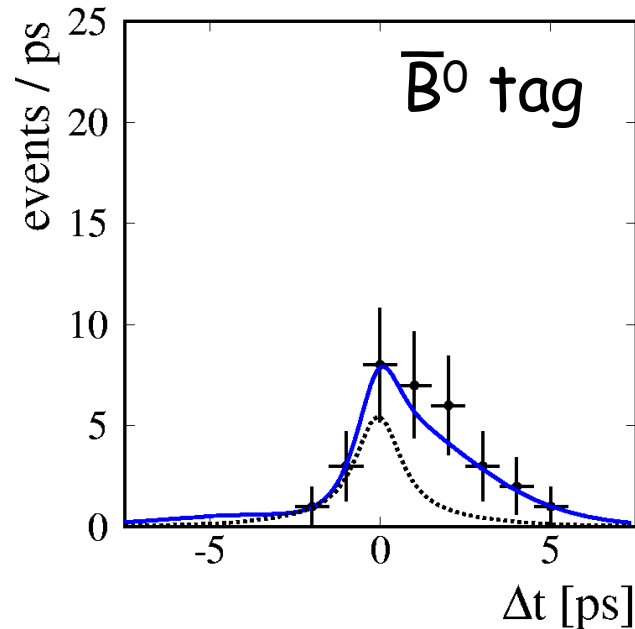
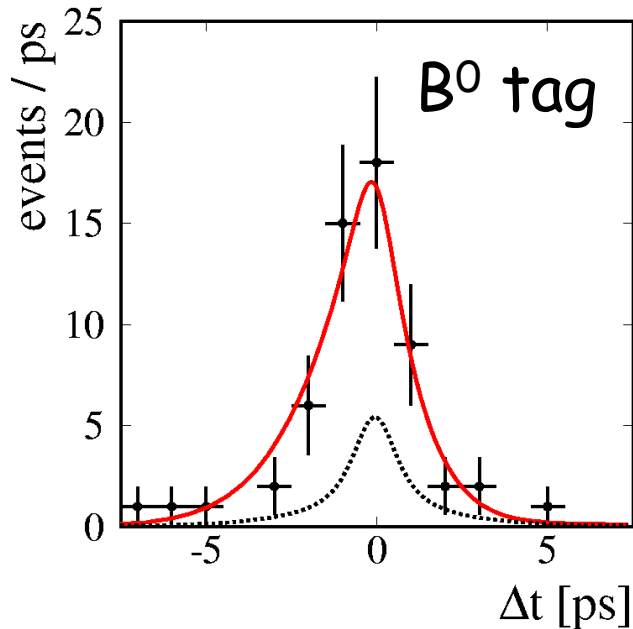
CP Violation in $B \rightarrow D^{(*)}D^{(*)}$ decays



- TD asymmetry $\sim \sin 2\beta$: $B \rightarrow D^+D^-$: $C=0$, $S=-\sin 2\beta$
- Penguin contribution expected to be minimal
 - 2-10% [Phys.Rev.D61:014010,2000]
- Sensitive to new physics in loops



Belle: Evidence for large CPV in $B \rightarrow D^+ D^-$



535 M BB

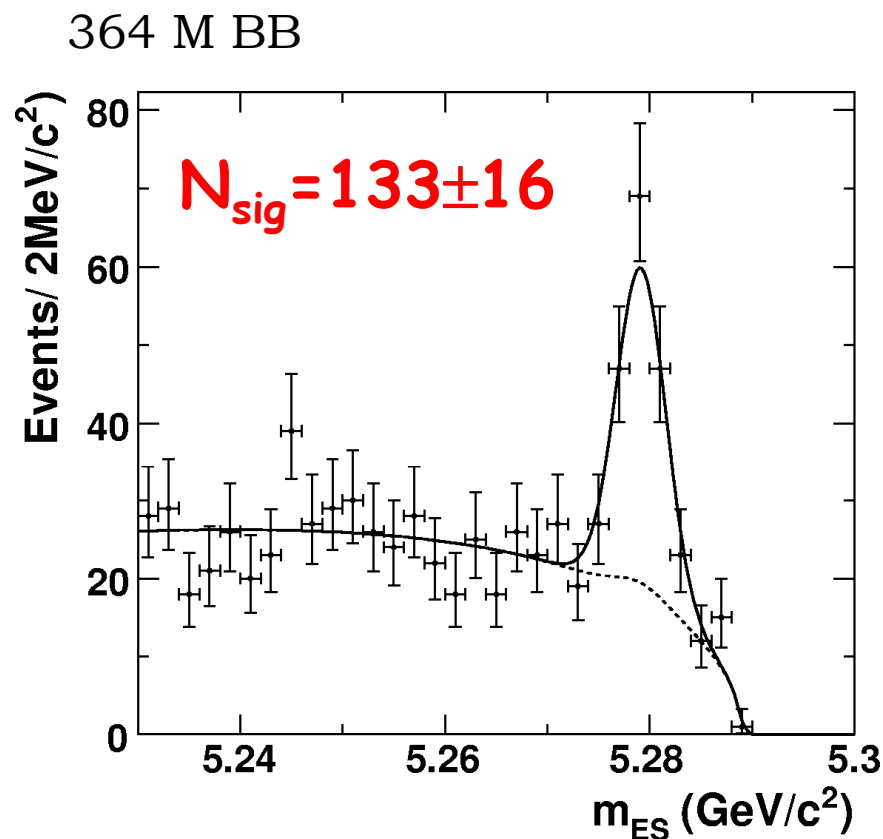
$$\begin{aligned} \sin 2\beta &= +1.13 \pm 0.37 \pm 0.09 \\ C &= -0.91 \pm 0.23 \pm 0.06 \end{aligned}$$

- $(\sin 2\beta, C) = (0, 0)$ point excluded at 4.1σ confidence

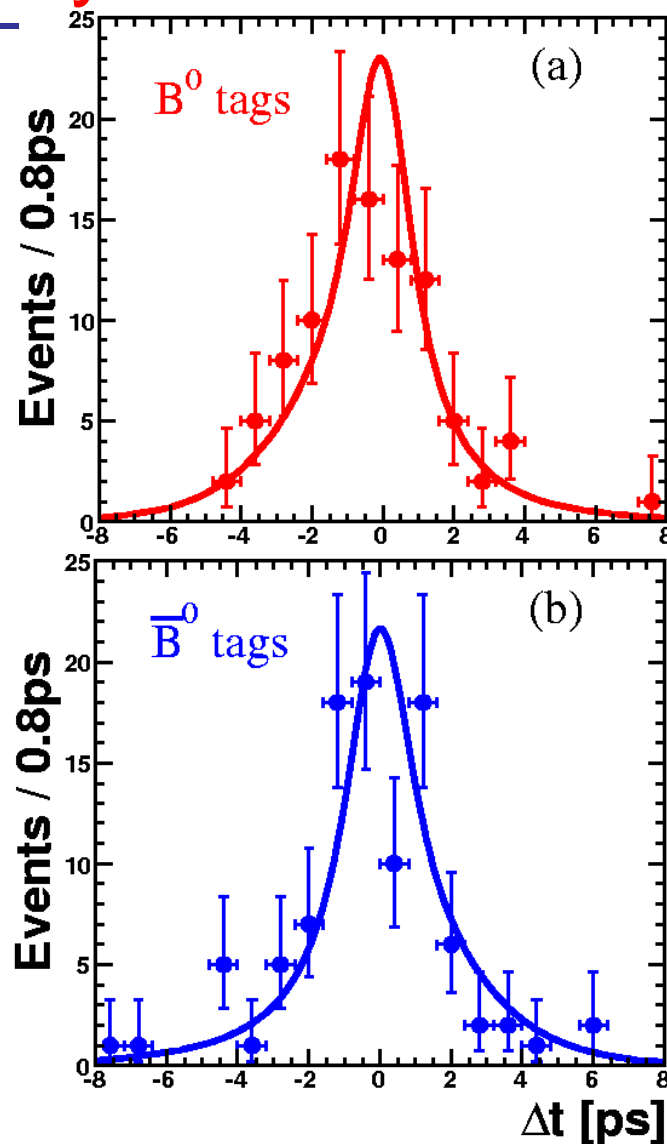
hep-ex/0702031, Submitted to PRL



BABAR does not confirm the large CP violation observed by Belle

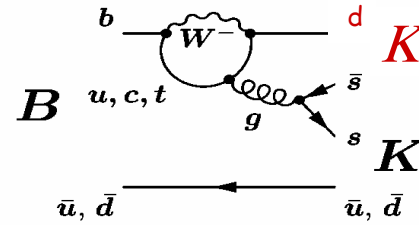


$$\sin\beta = +0.54 \pm 0.34 \pm 0.06$$
$$C = 0.11 \pm 0.22 \pm 0.07$$





B → K \bar{K} : Observation of b → dg Penguins

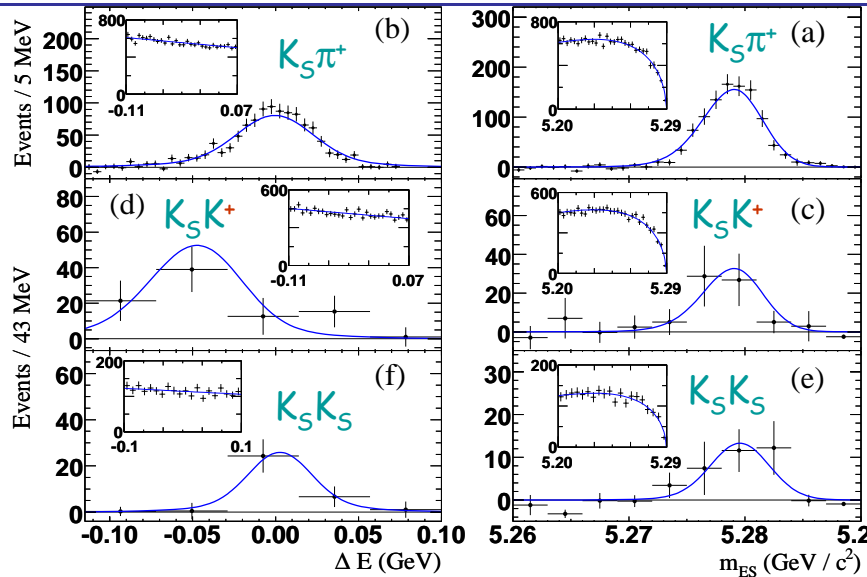


$$\frac{\Gamma(b \rightarrow d)}{\Gamma(b \rightarrow s)} \sim \frac{|V_{td}|^2}{|V_{ts}|^2} \sim 4\%$$

$$\begin{aligned} \text{Br}(B^0 \rightarrow K^0 \bar{K}^0) &= (1.08 \pm 0.28 \pm 0.11) \times 10^{-6} \quad (7.3\sigma) \\ \text{Br}(B^+ \rightarrow \bar{K}^0 K^+) &= (1.61 \pm 0.44 \pm 0.09) \times 10^{-6} \quad (5.3\sigma) \\ \text{Br}(B^0 \rightarrow K^+ K^-) &< 0.5 \times 10^{-6} \quad (90\% \text{ C.L.}) \end{aligned}$$

PRL 97: 171805, 2006

347 M BB

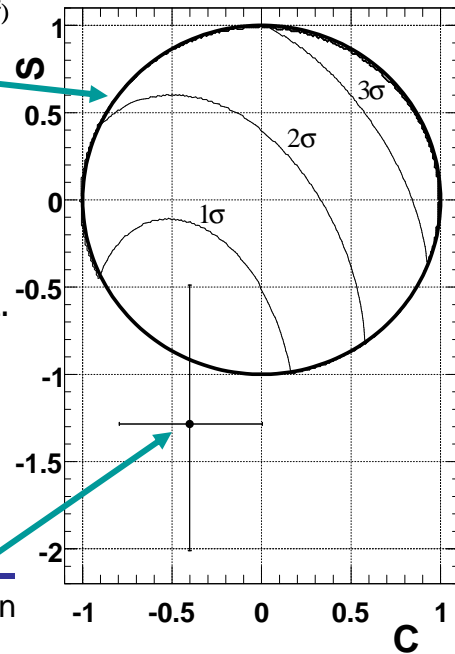


$$\begin{aligned} A_{CP} &\equiv \frac{\Gamma(\bar{B}^0 \rightarrow f_{CP}) - \Gamma(B^0 \rightarrow f_{CP})}{\Gamma(\bar{B}^0 \rightarrow f_{CP}) + \Gamma(B^0 \rightarrow f_{CP})} \\ &= \underbrace{S_{f_{CP}} \sin(\Delta m \Delta t)}_{\text{Indirect CPV}} - \underbrace{C_{f_{CP}} \cos(\Delta m \Delta t)}_{\text{Direct CPV}} \end{aligned}$$

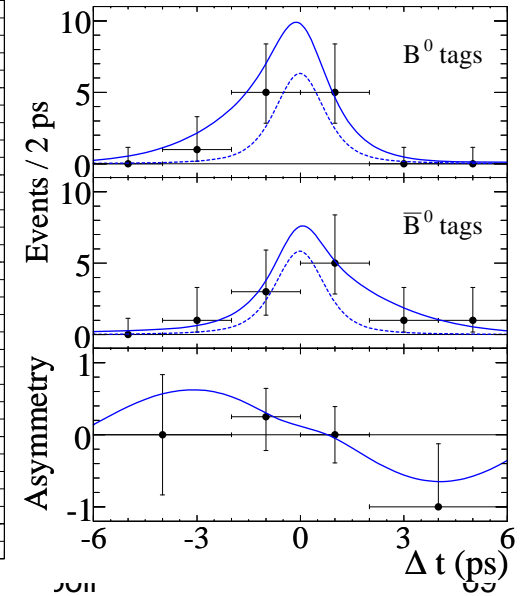
$$\begin{aligned} S(K_s^0 K_s^0) &= -1.28^{+0.80 \quad +0.11}_{-0.73 \quad -0.16} \\ C(K_s^0 K_s^0) &= -0.40 \pm 0.41 \pm 0.06 \\ A_{K_s^0 K_s^+} &= 0.10 \pm 0.26 \pm 0.03 \end{aligned}$$

physical region

- 1σ = 68% 2-D C.L.
- 2σ = 95% 2-D C.L.
- 3σ = 99.7% 2-D C.L.



fit result





$B^+ \rightarrow D^0 K^+ : \text{GLW}$

- $B \rightarrow D_{CP} K$

$$R_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{[\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)] / 2}$$

$$A_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}$$

$$R_{CP\pm} = 1 + r^2 \pm 2r \cos \delta \cos \gamma$$

$$A_{CP\pm} = \pm 2r \sin \delta \sin \gamma / R_{CP\pm}$$

$$x_{\pm} = \frac{R_{CP+}(1 \mp A_{CP+}) - R_{CP-}(1 \mp A_{CP-})}{4}$$

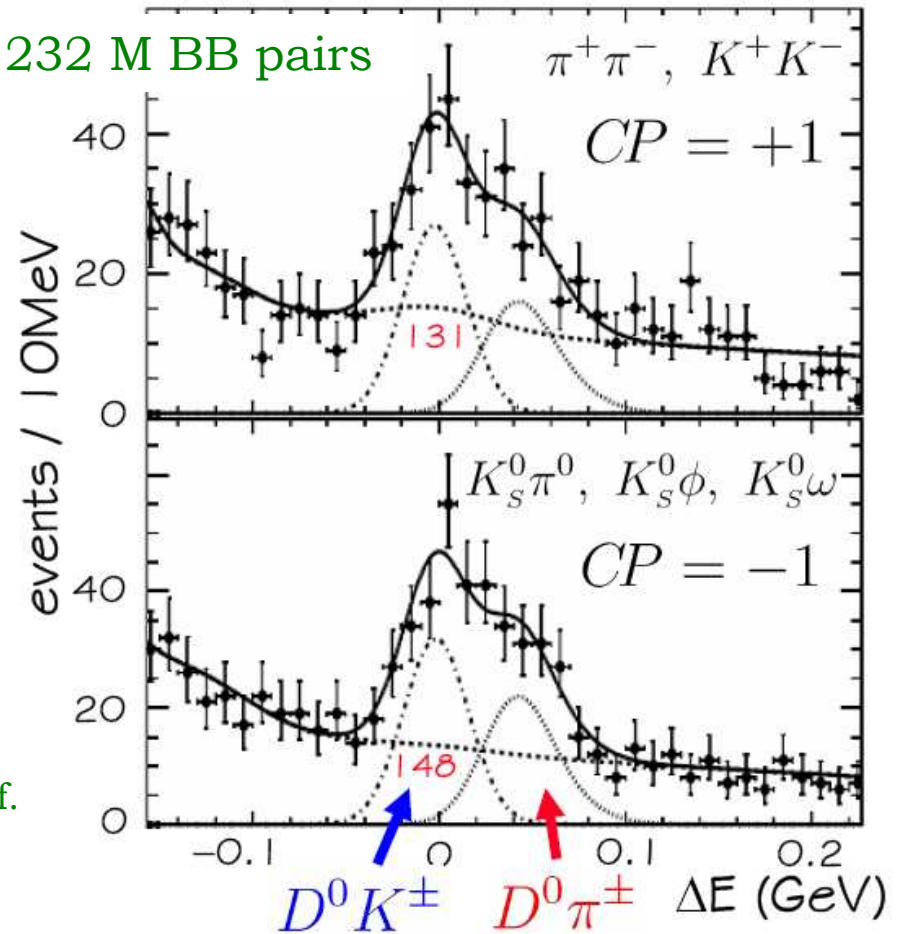
$$r^2 = x_{\pm}^2 + y_{\pm}^2 = \frac{R_{CP+} + R_{CP-} - 2}{2}, \quad \delta \text{ strong phase diff.}$$

$$x_+ = -0.082 \pm 0.053(\text{stat}) \pm 0.018(\text{syst}),$$

$$x_- = +0.102 \pm 0.062(\text{stat}) \pm 0.022(\text{syst}),$$

$$r^2 = -0.12 \pm 0.08(\text{stat}) \pm 0.03(\text{syst}).$$

232 M BB pairs



BaBar, PRD 73, 051105 (2006)



$B^+ \rightarrow D^0 K^+ : ADS$

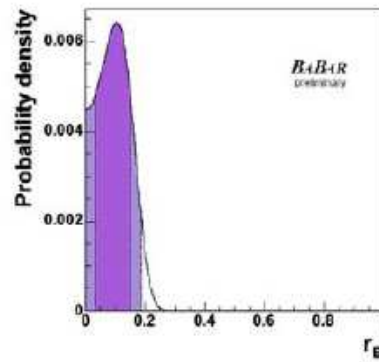
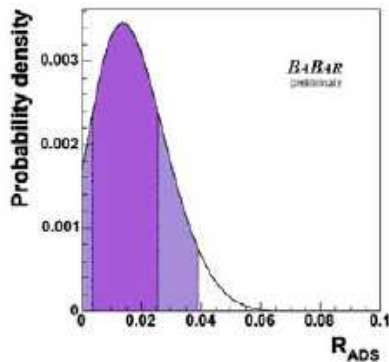
$B \rightarrow D[K\pi\pi^0]K$

$$\begin{aligned}
 R_{ADS} &\equiv \frac{\Gamma([K^+\pi^-\pi^0]_D K^-) + \Gamma([K^-\pi^+\pi^0]_D K^+)}{\Gamma([K^+\pi^-\pi^0]_D K^+) + \Gamma([K^-\pi^+\pi^0]_D K^-)} \\
 &= r_B^2 + r_D^2 + 2r_B r_D C \cos \gamma \\
 A_{ADS} &\equiv \frac{\Gamma([K^+\pi^-\pi^0]_D K^-) - \Gamma([K^-\pi^+\pi^0]_D K^+)}{\Gamma([K^+\pi^-\pi^0]_D K^-) + \Gamma([K^-\pi^+\pi^0]_D K^+)} \\
 &= 2r_B r_D S \sin \gamma / R_{ADS}
 \end{aligned}$$

$$r_B \equiv \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right|, \quad r_D^2 \equiv \frac{\mathcal{B}(D^0 \rightarrow K^+ \pi^- \pi^0)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0)}$$

hep-ex/0607065

$226 \times 10^6 B\bar{B}$ pairs



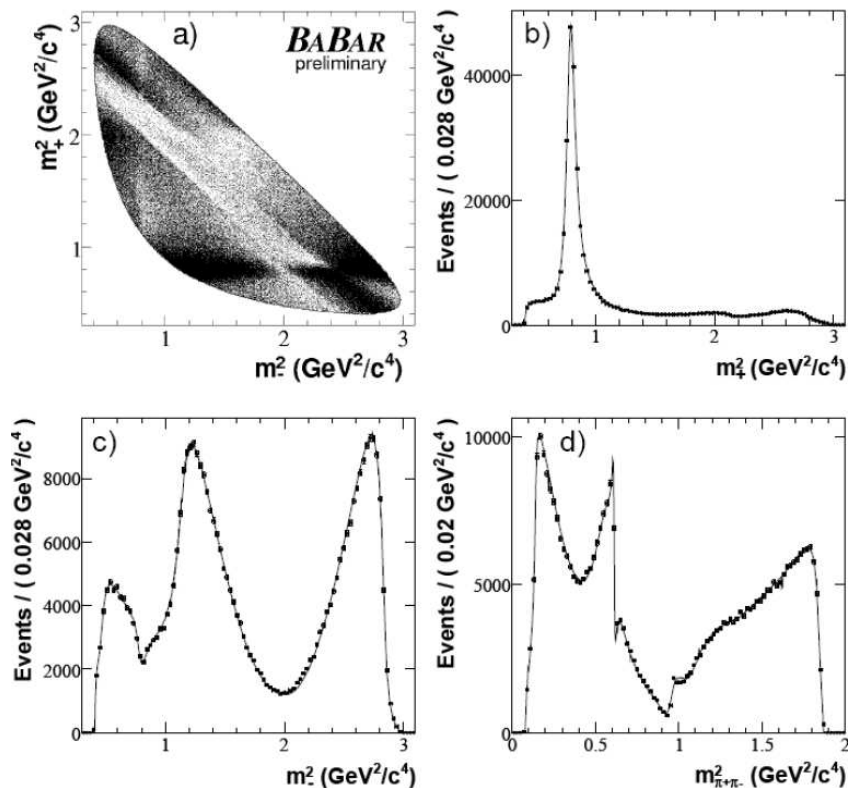
$$R_{ADS} = 0.012^{+0.012}_{-0.010} (stat)^{+0.010}_{-0.007} (syst)$$

$$r_B = 0.091 \pm 0.059$$



$B^+ \rightarrow D^{(*)0}[K_S \pi \pi] K^+ : \text{GGSZ (Dalitz)}$

Fit large and pure sample of flavor-tagged $D^0 K_S$ to determine the parameters of the Dalitz model f_{\pm} (Isobar model used by both BaBar and Belle)

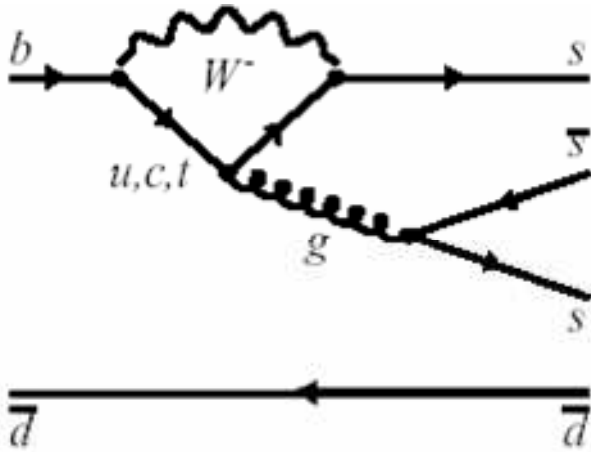


Component	$Re\{a_r e^{i\phi_r}\}$	$Im\{a_r e^{i\phi_r}\}$	Fit fraction (%)
$K^{*}(892)^-$	-1.223 ± 0.011	1.3461 ± 0.0096	58.1
$K_0^{*}(1430)^-$	-1.698 ± 0.022	-0.576 ± 0.024	6.7
$K_2^{*}(1430)^-$	-0.834 ± 0.021	0.931 ± 0.022	3.3
$K^{*}(1410)^-$	-0.248 ± 0.038	-0.108 ± 0.031	0.1
$K^{*}(1680)^-$	-1.285 ± 0.014	0.205 ± 0.013	0.6
$K^{*}(892)^+$	0.0997 ± 0.0036	-0.1271 ± 0.0034	0.5
$K_0^{*}(1430)^+$	-0.027 ± 0.016	-0.016 ± 0.017	0.0
$K_2^{*}(1430)^+$	0.019 ± 0.017	0.177 ± 0.018	0.1
$\rho(770)$	1	0	21.6
$\omega(782)$	-0.6219 ± 0.00099	0.03942 ± 0.00066	0.7
$f_2(1270)$	-0.699 ± 0.018	0.387 ± 0.018	2.1
$\rho(1450)$	0.253 ± 0.038	0.036 ± 0.055	0.1
Non-resonant	-0.99 ± 0.19	3.82 ± 0.13	8.5
$f_0(980)$	0.4465 ± 0.0057	0.2572 ± 0.0081	6.4
$f_0(1370)$	0.95 ± 0.11	-1.619 ± 0.011	2.0
σ	1.28 ± 0.02	0.273 ± 0.024	7.6
σ'	0.290 ± 0.010	-0.0655 ± 0.0098	0.9

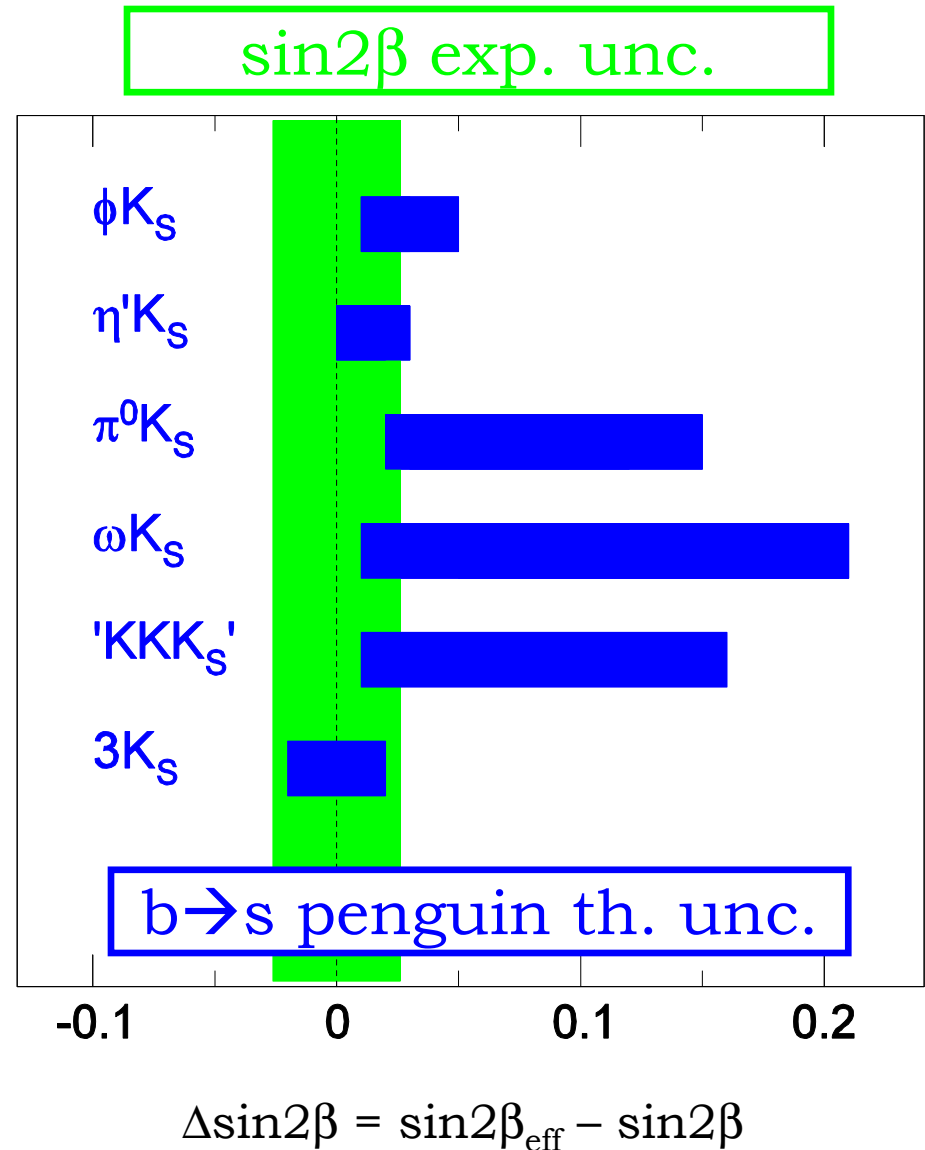
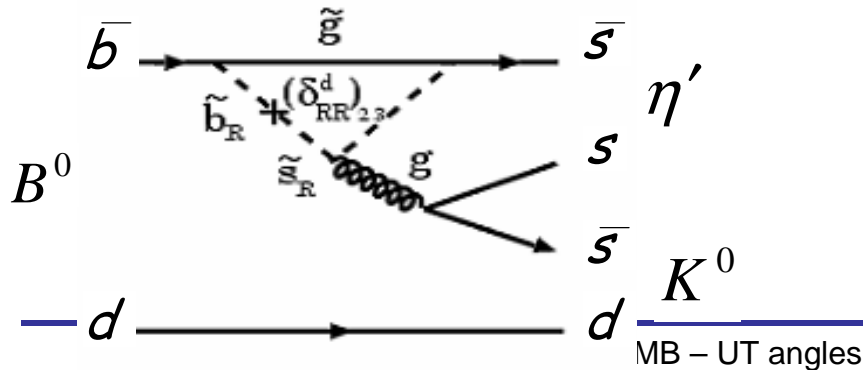
16 Breit-Wigner + constant term



Sin2β with penguins



- Beneke PLB 620 143 (2005)
- Mishima, Sanda PRD 72 114005 (2005)
- Williamson, Zupan PRD 74 014003 (2006)
- Cheng, Chua, Soni PRD 014006 (2005)

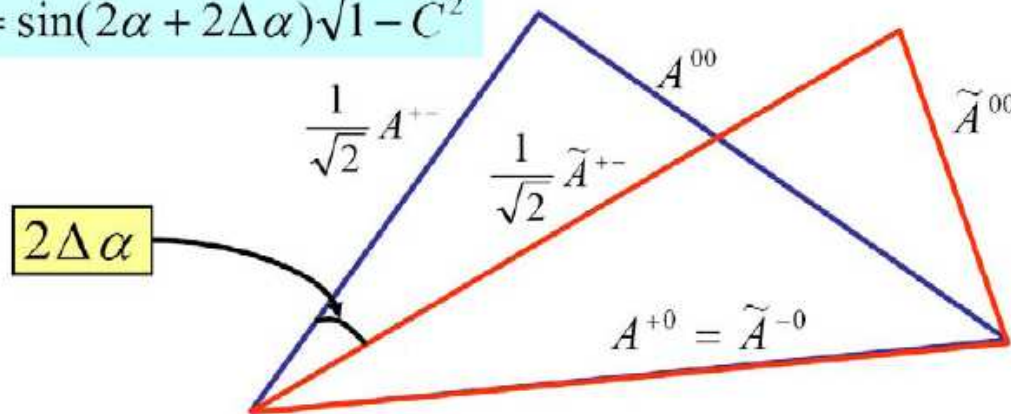




$|\alpha - \alpha_{\text{eff}}|$: Isospin analysis

- Use SU(2) to relate different hh final states

$$S = \sin(2\alpha + 2\Delta\alpha)\sqrt{1 - C^2}$$



$$A_{hh} = e^{+i\gamma} T + e^{-i\beta} P$$

$$\tilde{A}_{hh} = e^{-i\gamma} T + e^{+i\beta} P$$

$2\Delta\alpha$

$$A^{+0} = \frac{1}{\sqrt{2}} A^{+-} + A^{00}$$

$$\tilde{A}^{-0} = \frac{1}{\sqrt{2}} \tilde{A}^{+-} + \tilde{A}^{00}$$

$$A^{+-} = A(B^0 \rightarrow \pi^+ \pi^-)$$

$$\tilde{A}^{+-} = A(\bar{B}^0 \rightarrow \pi^+ \pi^-)$$

$$A^{00} = A(B^0 \rightarrow \pi^0 \pi^0)$$

$$\tilde{A}^{00} = A(\bar{B}^0 \rightarrow \pi^0 \pi^0)$$

$$A^{+0} = A(B^+ \rightarrow \pi^+ \pi^0)$$

$$\tilde{A}^{-0} = A(B^- \rightarrow \pi^- \pi^0)$$



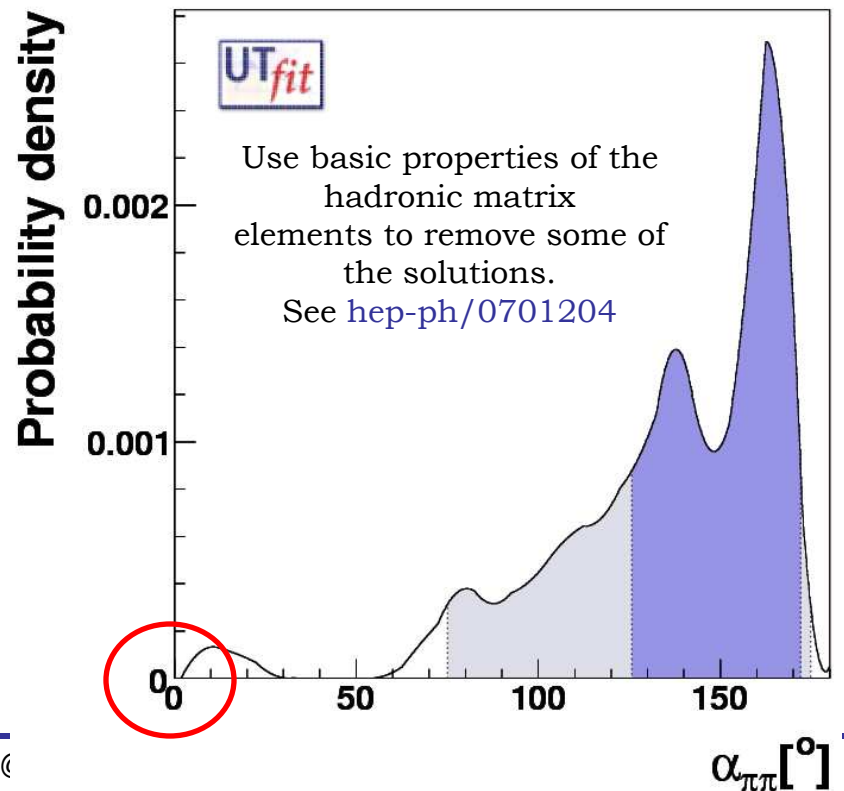
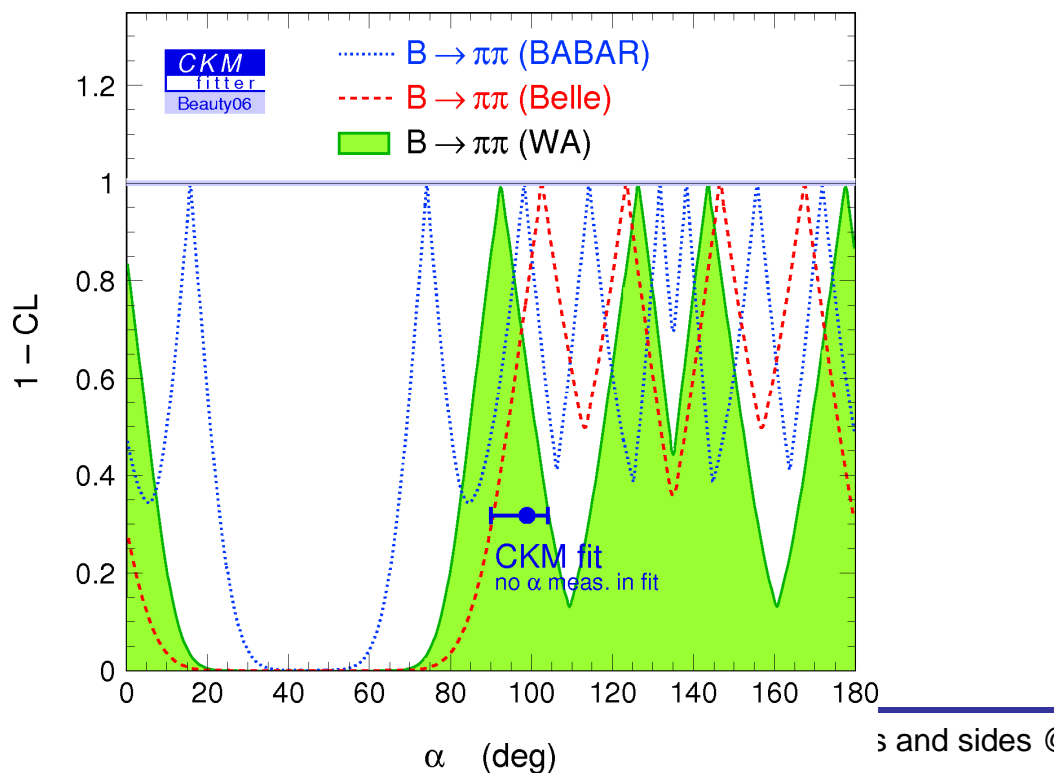
$B^0 \rightarrow \pi^+ \pi^-$

Using isospin relations

$$\text{BR}(B^0 \rightarrow \pi^+ \pi^-) = 5.2 \pm 0.2 \quad \text{HFAG } (10^{-6}) \quad -$$

$$\text{BR}(B^+ \rightarrow \pi^+ \pi^0) = 5.7 \pm 0.4 \quad A_{\text{CP}}(B^+ \rightarrow \pi^+ \pi^0) = 0.04 \pm 0.05$$

$$\text{BR}(B^0 \rightarrow \pi^0 \pi^0) = 1.3 \pm 0.2 \quad A_{\text{CP}}(B^0 \rightarrow \pi^0 \pi^0) = 0.36^{+0.33}_{-0.31}$$





hep-ex/0607097

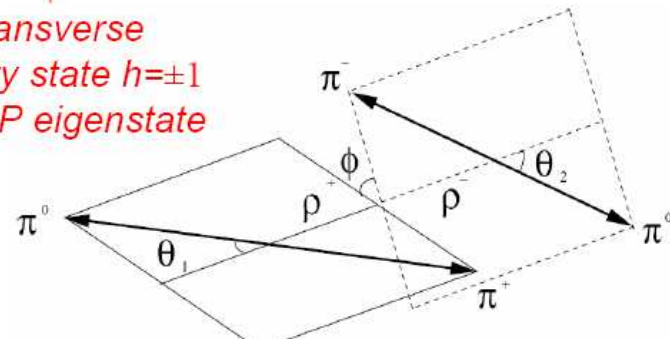
$B^0 \rightarrow \rho^+ \rho^-$ $347 \times 10^6 B\bar{B}$ pairs



- Extraction of α follows the same logic as for the $B \rightarrow \pi\pi$ system
- $\rho\rho$ is a VV state with 3 possible polarizations (L: A^0 ; T: A^+ & A^-)
- Angular analysis needed to determine CP content

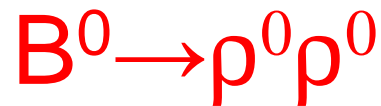
$$\frac{d^2 N}{d \cos \theta_1 d \cos \theta_2} \propto \underbrace{f_L \cos^2 \theta_1 \cos^2 \theta_2}_{\substack{\text{Longitudinal} \\ \text{Helicity state } h=0 \\ \text{CP}+1 \text{ eigenstate}}} + \underbrace{\frac{1}{4}(1-f_L) \sin^2 \theta_1 \sin^2 \theta_2}_{\substack{\text{Transverse} \\ \text{Helicity state } h=\pm 1 \\ \text{non-CP eigenstate}}}$$

$$f_L = 0.977 \pm 0.024 \begin{matrix} +0.015 \\ -0.013 \end{matrix}$$

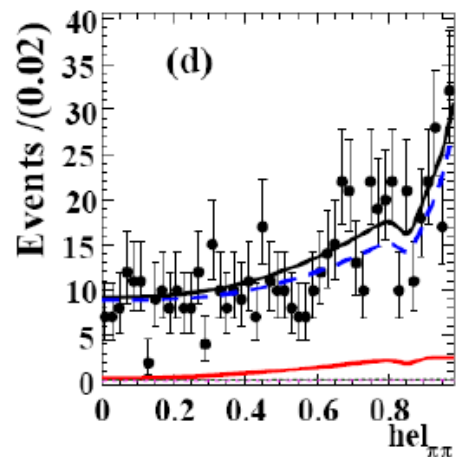
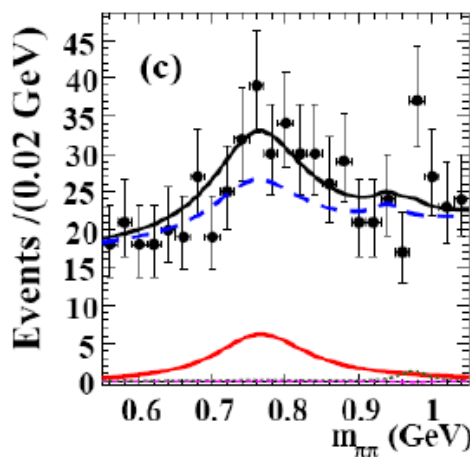
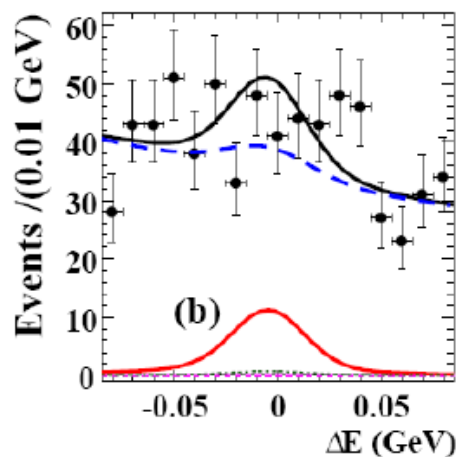
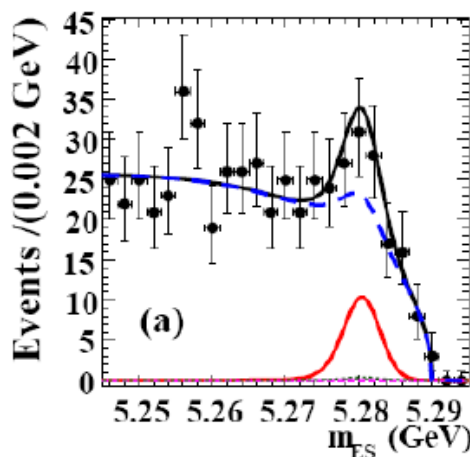




hep-ex/0612021
PRL accepted



$384 \times 10^6 B\bar{B}$ pairs



$$N_{\rho^0 \rho^0} = 100 \pm 32 \pm 17$$

3.5 σ evidence for $B \rightarrow \rho^0 \rho^0$

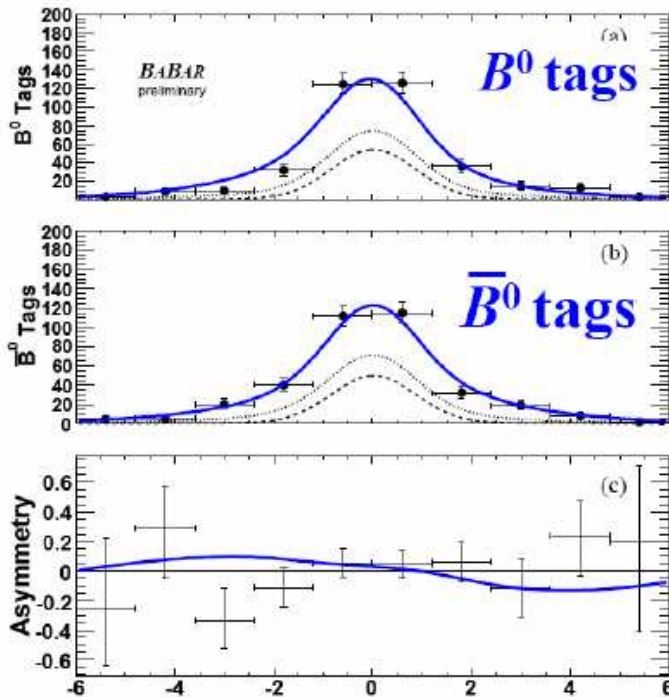
$$f_L(B^0 \rightarrow \rho^0 \rho^0) = 0.87 \pm 0.13 \pm 0.04$$

$$Br(B^0 \rightarrow \rho^0 \rho^0) = (1.07 \pm 0.33 \pm 0.19) \cdot 10^{-6}$$

Small $\rho^0 \rho^0$ BF \Rightarrow small penguin pollution



$B^{0(\pm)} \rightarrow \rho^{0(\pm)} \rho^0$



$B^0 \rightarrow \rho^+ \rho^-$

$$S_{long} = -0.19 \pm 0.21^{+0.05}_{-0.07}$$

$$C_{long} = -0.07 \pm 0.15 \pm 0.06$$

$$\alpha_{eff} = (95.5^{+6.9}_{-6.2})^\circ$$

$$Br(B^0 \rightarrow \rho\rho) = (23.5 \pm 2.2 \pm 4.1) \cdot 10^{-6}$$

$B^\pm \rightarrow \rho^\pm \rho^0$

hep-ex/0607092

$$Br(B^\pm \rightarrow \rho^\pm \rho^0) = (16.8 \pm 2.2 \pm 2.3) \cdot 10^{-6}$$

$$A_{CP}(B^\pm \rightarrow \rho^\pm \rho^0) = -0.12 \pm 0.13 \pm 0.10$$

$$f_L(B^\pm \rightarrow \rho^\pm \rho^0) = 0.905 \pm 0.042^{+0.023}_{-0.027}$$

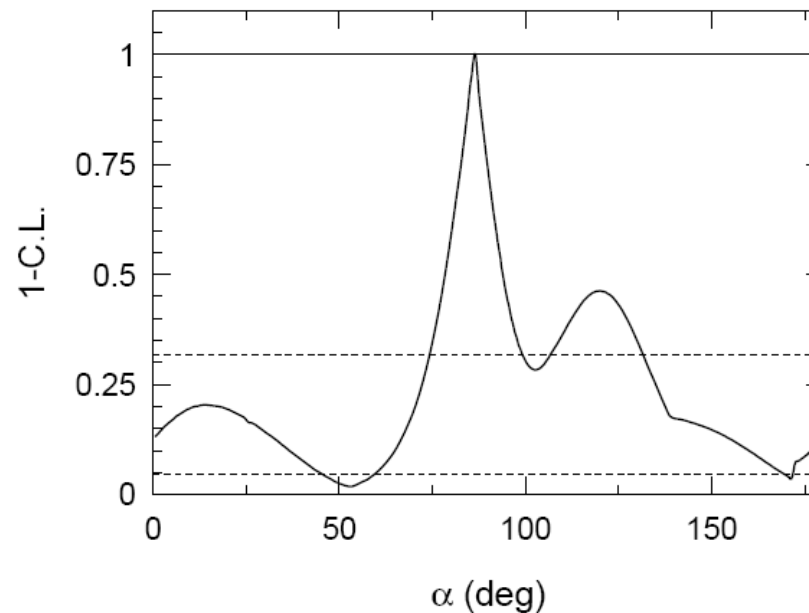


$B \rightarrow \pi\pi\pi^0$: Dalitz fit to α

- α from a fit to 26 parameters
- The method extracts α without ambiguities in $[0^\circ, 180^\circ]$

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375M BB



$$\alpha = (87^{+45}_{-13})^\circ$$

- results consistent with SM result ($\sim 90^\circ$)



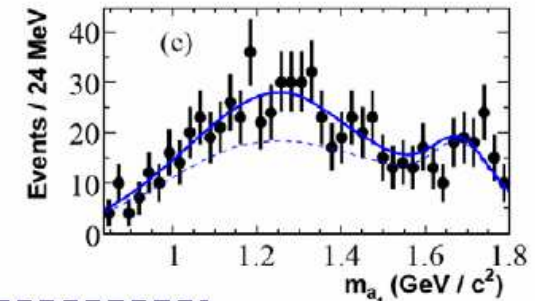
$B \rightarrow a_1 \pi : \alpha_{\text{eff}} \text{ and...}$

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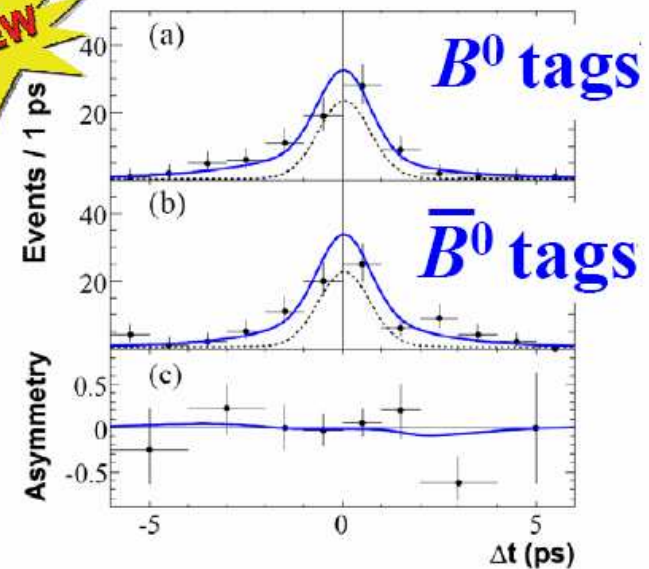
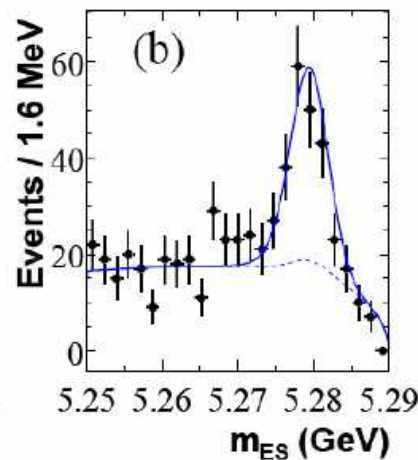
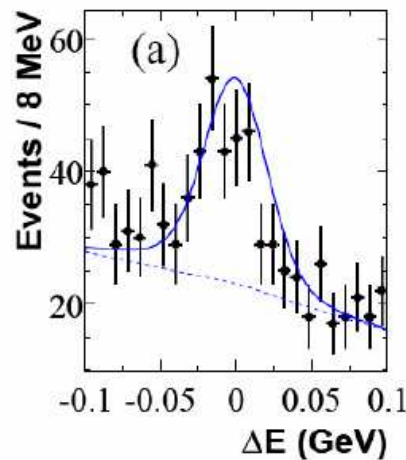
- First BF observation, significance 9.2σ

$$Br(B^0 \rightarrow a_1(1260) \pi) = (33.2 \pm 3.8 \pm 3.0) \cdot 10^{-6}$$

Reconstructed $a_1(1260) \rightarrow 3$ charged pions
Quasi-two body approximation



- First Time Dependent CPV analysis





$B \rightarrow a_1 \pi : \alpha_{\text{eff}} \text{ and } SU(3)$

$$\begin{aligned}
 S_{a_1\pi} &= 0.37 \pm 0.21 \pm 0.07 \\
 C_{a_1\pi} &= -0.10 \pm 0.15 \pm 0.09 \\
 A_{CP} &= -0.07 \pm 0.07 \pm 0.02
 \end{aligned}$$

$$\begin{aligned}
 \Delta S_{a_1\pi} &= -0.14 \pm 0.21 \pm 0.06 \\
 \Delta C_{a_1\pi} &= 0.26 \pm 0.15 \pm 0.07
 \end{aligned}$$

Using the measured CP parameters we determine the angle α_{eff} and one of the four solutions is compatible with the result of SM-based fits:

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$$\alpha_{\text{eff}} = 78.6^\circ \pm 7.3^\circ$$

SU(3) related modes

$$\boxed{a_1^+ K^- \text{ OR } a_1^+ K_S^0} + \left\{ \begin{array}{l} \boxed{(K_1^-(1270) \pi^+ \text{ and } K_1^-(1400) \pi^+)} \\ \text{OR} \\ \boxed{(K_1^0(1270) \pi^+ \text{ and } K_1^0(1400) \pi^+)} \end{array} \right.$$

... in progress!