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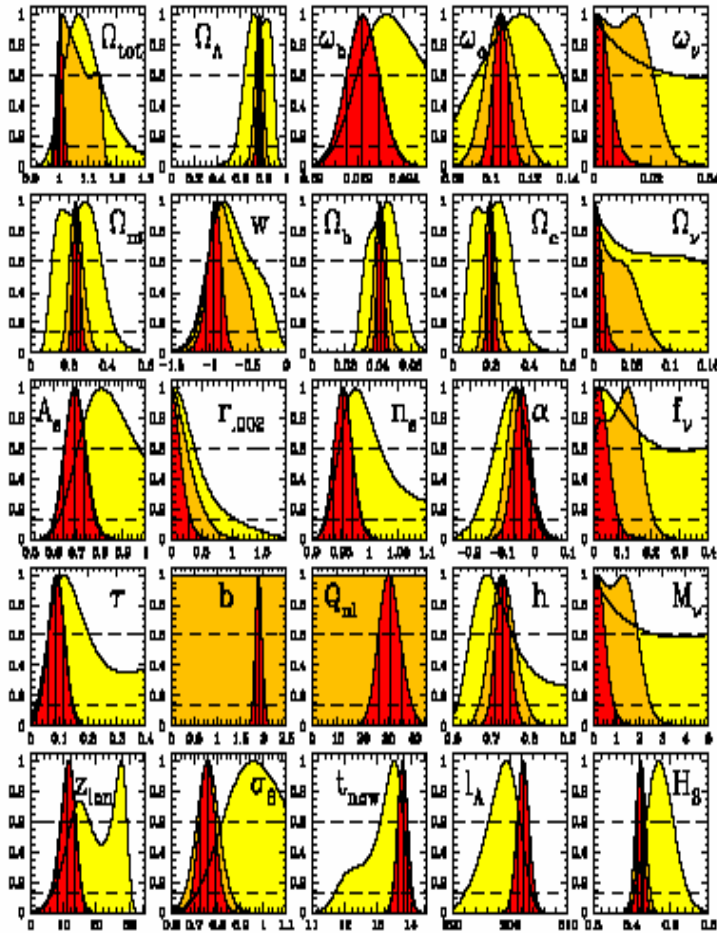
# **Electroweak Baryogenesis (EWBG) versus Leptogenesis**

Pasquale Di Bari  
(Max Planck, Munich)



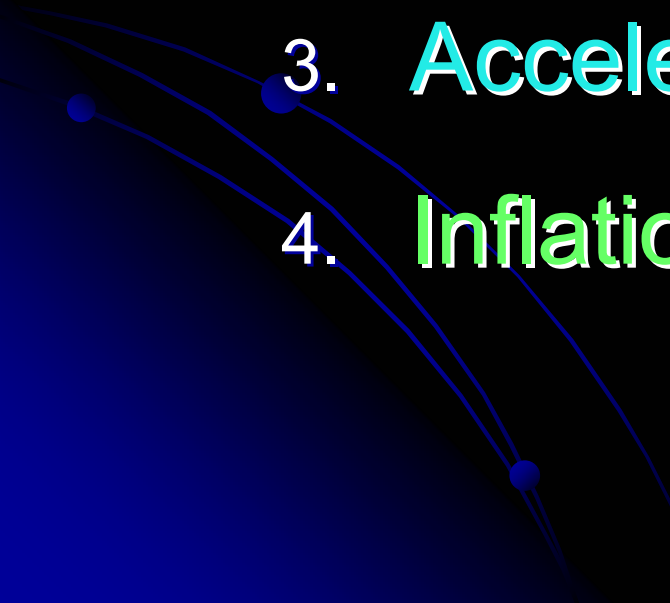
# Toward a Cosmological SM ?

(Tegmark et al. 2005)

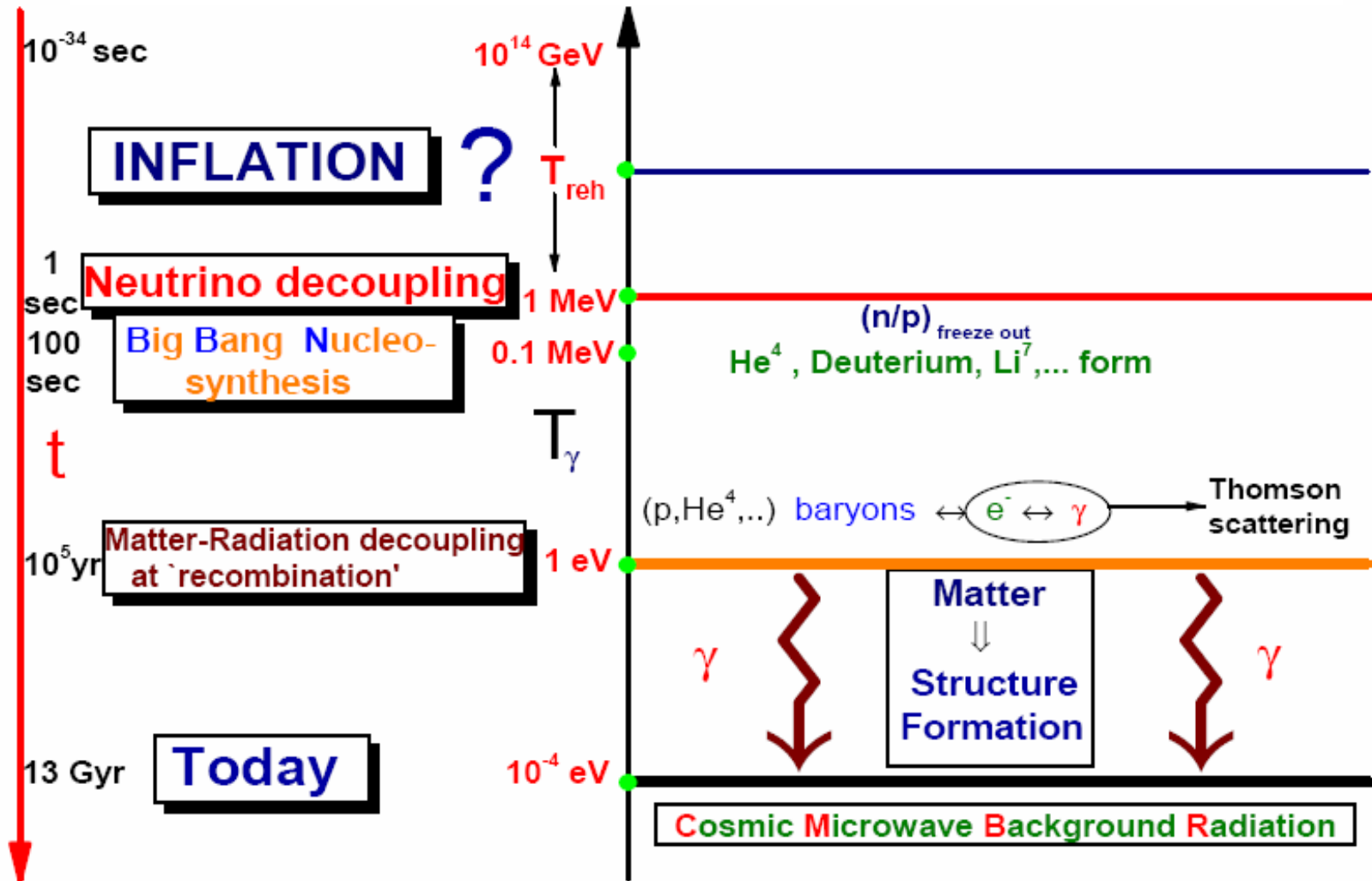


Parameter	WMAP 3 years + SDSS	Description
$\Omega_0$	$1.003^{+0.010}_{-0.009}$	Density parameter
	$\Omega_0 = 1$ (Flat Universe prior)	
$h$	$0.730^{+0.019}_{-0.019}$	Present expansion rate
$q_0$	$-0.66 \pm 0.1$	Deceleration parameter
$t_0$ (Gyr)	$13.76 \pm 0.15$	Age of the Universe
$T_0$ (K)	$2.725 \pm 0.001$	CMB temperature
$\Omega_B$	$0.0416 \pm 0.0019$	Baryon Density
$\Omega_{\text{CDM}}$	$0.197 \pm 0.016$	Cold Dark Matter Density
$\Omega_\Lambda$	$0.761 \pm 0.017$	Dark Energy Density
$w$	$-0.941^{+0.087}_{-0.101}$	Dark Energy Equation of State
$n_s$	$0.948^{+0.014}_{-0.018}$	Scalar index
$\sum_i m_{\nu_i}$	$< 0.94 \text{ eV} (95\% \text{ CL})$	Sum of neutrino masses

# Puzzles of Modern Cosmology

1. **Matter - antimatter asymmetry**
  2. **Dark matter**
  3. **Accelerating Universe**
  4. **Inflation**
- 

# Thermal history of the Universe



# Matter-antimatter asymmetry

- Symmetric Universe with matter- anti matter domains ?  
Excluded by CMB + cosmic rays

$$\Rightarrow \eta_B^{\text{CMB}} = (6.3 \pm 0.3) \times 10^{-10} \gg \eta_{\bar{B}}$$

- Pre-existing ? It conflicts with inflation ! (Dolgov '97)

$\Rightarrow$  dynamical generation (baryogenesis)

(Sakharov '67)

# Models of Baryogenesis

- From phase transitions:
  - **EWBG:**
    - \* in the SM
    - \* **in the MSSM**
    - \* in the NMSSM
    - \* in the 2 Higgs model
    - \* .....
  - Affleck-Dine:
    - at preheating
      - Q-balls
    - .....
- From Black Hole evaporation
  - Spontaneous Baryogenesis
  - .....
- From heavy particle decays:
  - GUT Baryogenesis
  - **LEPTOGENESIS**

# Baryogenesis in the SM ?

All 3 Sakharov conditions are fulfilled in the SM:

1. baryon number violation at  $T \gtrsim 100$  GeV,
2. CP violation in the quark CKM matrix,
3. departure from thermal equilibrium (an arrow from the expansion of the Universe)

# Baryon Number Violation at finite T

(‘t Hooft

Although at  $T=0$  baryon number violating processes are inhibited,  
at finite T:

$$\Gamma(\Delta B \neq 0) \propto T^4 \exp \left[ -\kappa \frac{v(T)}{T} \right]$$

$$v \equiv \langle \Phi \rangle = \begin{cases} 0 & \text{for } T \gtrsim T_c \text{ (unbroken)} \\ v(T_c) & \text{for } T \lesssim T_c \end{cases}$$

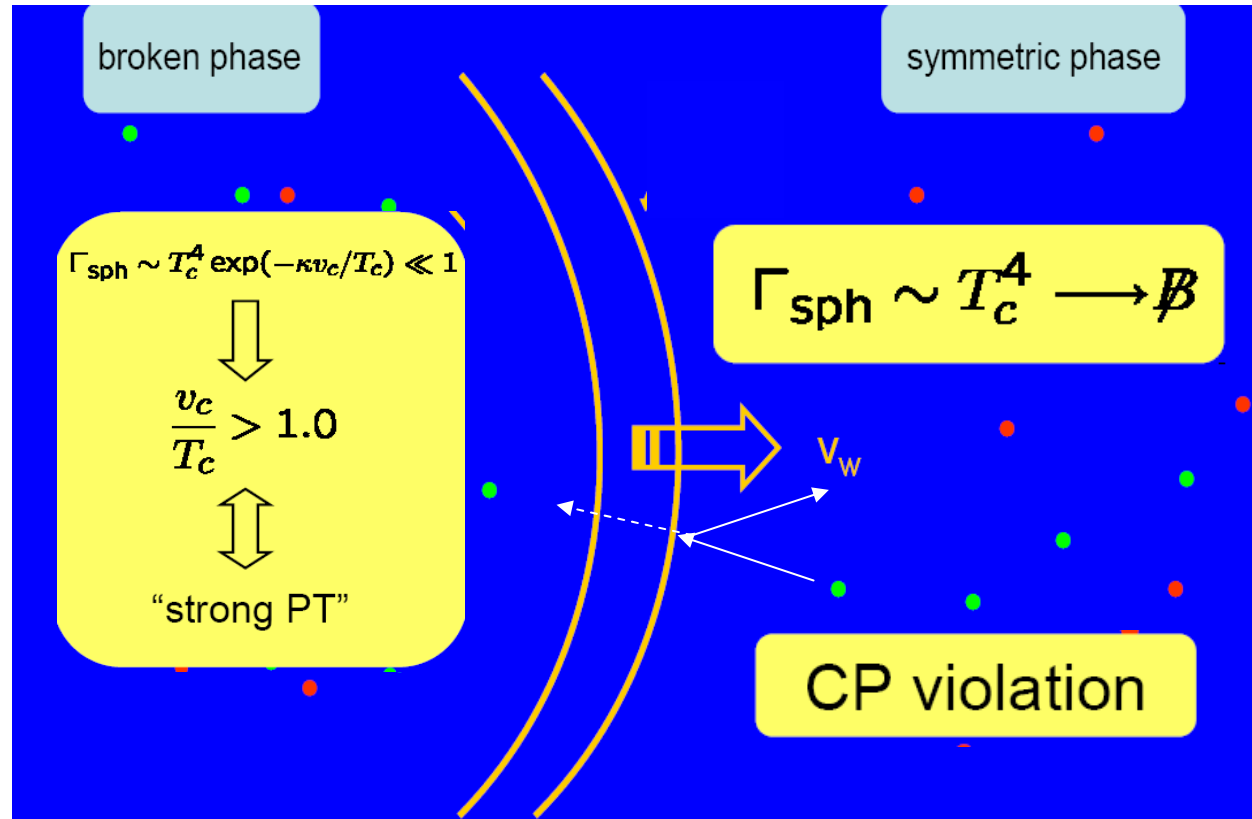
- Baryon number violating processes are unsuppressed at  $T \gtrsim T_c \simeq 100$
- Anomalous processes violate lepton number as well but preserve B-L !

I **There can be enough departure from thermal equilibrium ?**



# EWBG in the SM

If the EW phase transition (PT) is **1st order**  $\Rightarrow$  **broken phase bubbles nucleate**



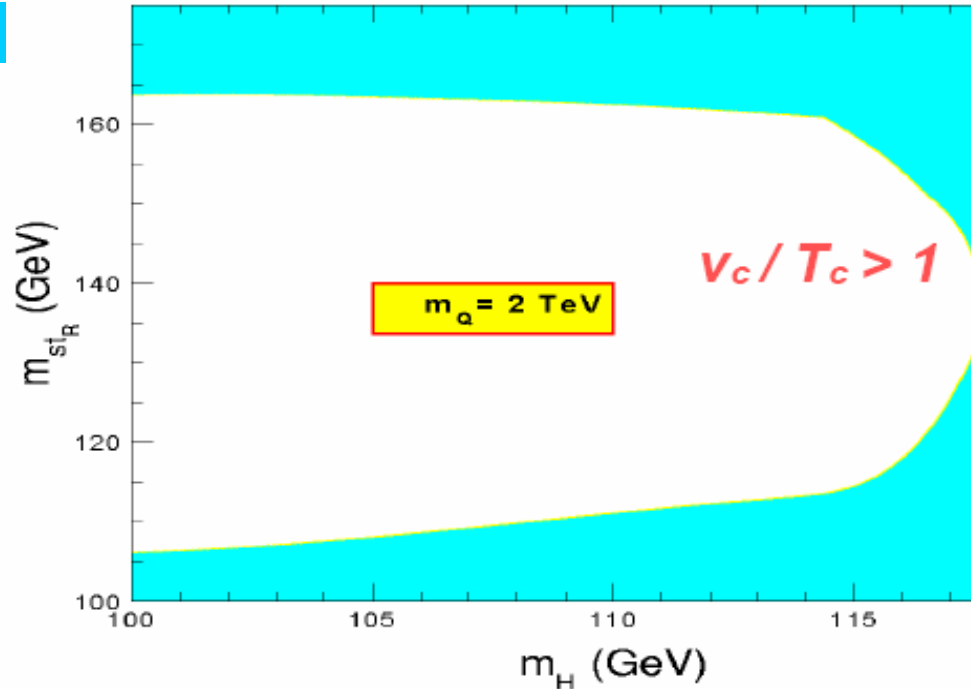
In the SM the ratio  $v_c/T_c$  is directly related to the **Higgs mass** and only for  $M_h < 40 \text{ GeV}$  one can have a strong PT  $\Rightarrow$  **EW baryogenesis in the SM** is ruled out by the LEP lower bound  $M_h \gtrsim 114 \text{ GeV}$ ! (also not enough ~~CP~~)

$\Rightarrow$  **New Physics is needed!**

# EWBG in the MSSM

- Additional bosonic degrees of freedom (dominantly the **light stop** contribution) can make the EW phase transition more strongly first order if :

M.Carena, M. Quiros, C.W.' 98



- Notice that there is a tension between the strong PT requirement and the bound on  $M_h$  and in particular one has to impose  $5 \lesssim \tan \beta \lesssim 10$
- In addition there are severe constraints from the simultaneous requirement CP violation in the bubble walls without generating too large **electric dipole of the electron**: **is EWBG still alive ?**

# Is EWBG still alive ?

## 3 possible attitudes:

- **Optimistic:** Not only it is alive but the allowed region in the MSSM parameter space has interesting features also to solve another of the cosmological puzzles: Dark Matter  
(Carena et al. '05)
- **Realistic:** EWBG in the MSSM has strong constraints but these can be relaxed within other frameworks:
  - in the NMSSM  
(Pietroni '92, Davies et al. '96, Huber and Schmidt '01)
  - in the nMSSM  
(Wagner et al. '04)
  - in left-right symmetric models at B-L symmetry breaking  
(Mohapatra and Zhang '92)
  - .....
- **Pessimistic:** We need some other mechanism; SUSY has not yet been discovered but on the other hand ....

# Neutrino masses: $m_1 < m_2 < m_3$

neutrino mixing data

2 possible schemes: **normal** or **inverted**

$$m_3^2 - m_2^2 = \Delta m_{\text{atm}}^2 \text{ or } \Delta m_{\text{sol}}^2 \quad m_{\text{atm}} \equiv \sqrt{\Delta m_{\text{atm}}^2 + \Delta m_{\text{sol}}^2} \simeq 0.05 \text{ eV}$$

$$m_2^2 - m_1^2 = \Delta m_{\text{sol}}^2 \text{ or } \Delta m_{\text{atm}}^2 \quad m_{\text{sol}} \equiv \sqrt{\Delta m_{\text{sol}}^2} \simeq 0.009 \text{ eV}$$

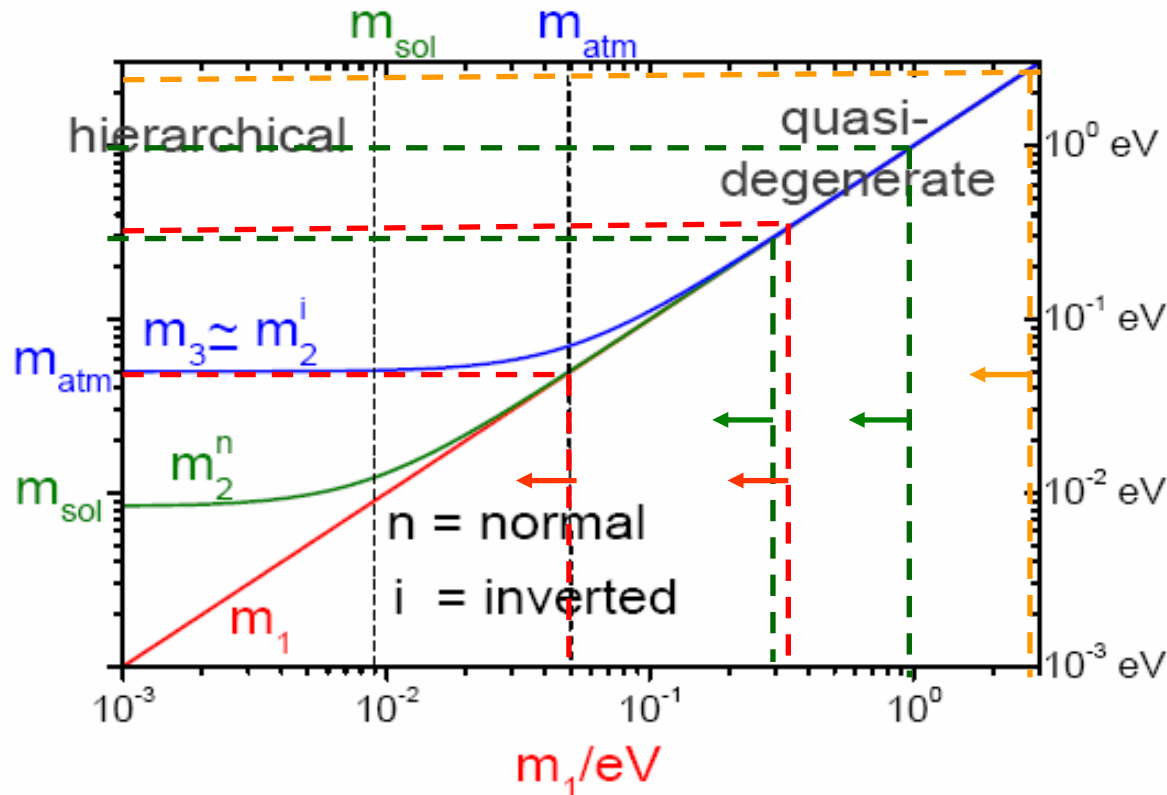
**Tritium  $\beta$  decay** :  $m_e < 2.3 \text{ eV}$   
(Mainz 95% CL)

**$\beta\beta 0\nu$**  :  $m_{\beta\beta} < 0.3 - 1.0 \text{ eV}$   
(Heidelberg-Moscow 90% CL,  
similar result by CUORICINO)

using the flat prior ( $\Omega_0=1$ ):

**CMB+LSS** :  $\Sigma m_i < 0.94 \text{ eV}$   
(WMAP+SDSS)

**CMB+LSS + Ly $\alpha$**  :  $\Sigma m_i < 0.17 \text{ eV}$   
(Seljak et al.)



# Minimal RH neutrino implementation

SM + RH neutrinos with Yukawa coupling and Majorana mass term:

$$\mathcal{L}_Y = -\bar{l}_L \phi h \nu_R - \frac{1}{2} \bar{\nu}_R^c M_R \nu_R + h.c.$$

After spontaneous symmetry breaking  $\Rightarrow m_D = v h$  ( $v \equiv \langle \phi_0 \rangle$ )

$$\mathcal{L}_{\text{mass}}^\nu = -\frac{1}{2} \left[ (\bar{\nu}_L^c, \bar{\nu}_R) \begin{pmatrix} \cancel{m_D} & m_D^T \\ m_D & M_R \end{pmatrix} \begin{pmatrix} \nu_L \\ \nu_R^c \end{pmatrix} \right] + h.c.$$

## 3 limiting cases :

- pure Dirac:  $M_R = 0$
- pseudo-Dirac :  $M_R \ll m_D$
- see-saw limit:  $M_R \gg m_D$

# See-saw mechanism

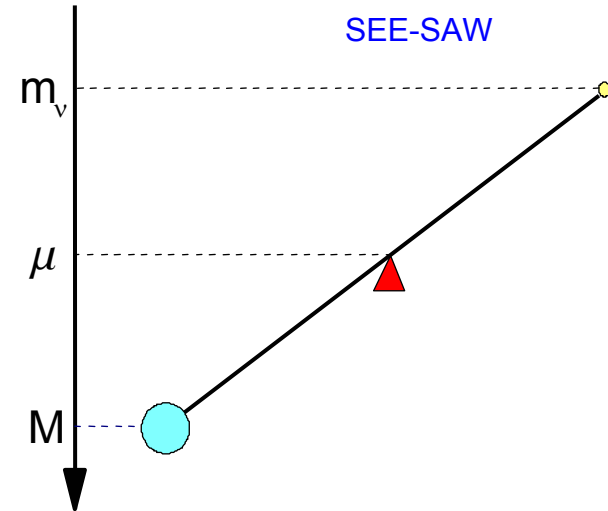
3 light LH neutrinos:

$$m_\nu = -m_D \frac{1}{M_R} m_D^T$$

$N \geq 2$  heavy RH neutrinos:

$N_1, N_2, \dots$

$$\max[\lambda_{m_D}^i] \equiv \mu \ll M_1 \leq M_2 \leq \dots$$



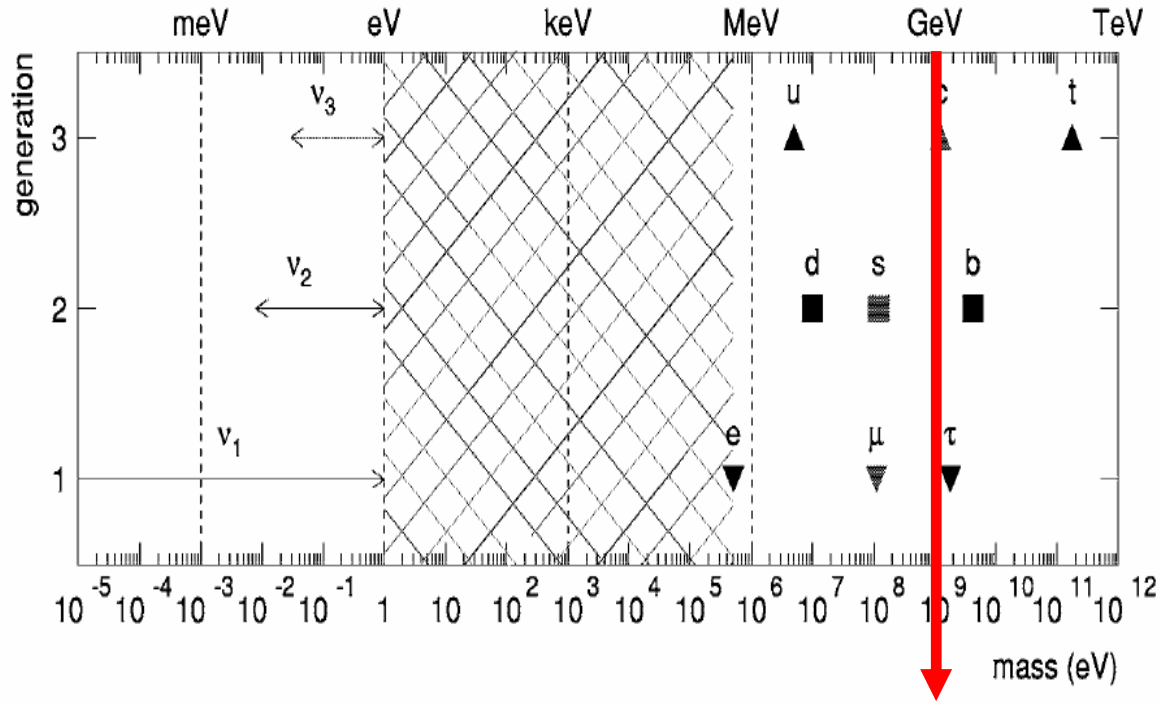
- All eigenstates (light and heavy neutrinos) are **Majorana neutrinos** (self-conjugate particles)

$$(N = \nu_R + \nu_R^c, \nu = \nu_L + \nu_L^c) \Rightarrow \beta\beta 0\nu \text{ decay}$$

Typical 1 generation example:

$$\mu \sim M_{EW} \sim 100 \text{ GeV}, m_\nu \simeq m_{\text{atm}} \sim 0.1 \text{ eV}$$

$$\Rightarrow M_R \sim 10^{14} \text{ GeV} \lesssim M_{GUT}$$



$$\mu_* \sim 1 \text{ GeV}$$

$\mu > \mu^*$   $\implies$  high pivot see-saw scale  $\implies$  'heavy' RH neutrinos

$\mu < \mu^*$   $\implies$  low pivot see-saw scale  $\implies$  'light' RH neutrinos

# Basics of leptogenesis

(Fukugita, Yanagida '86)

$M, m_D, m_\nu$  are complex matrices  $\Rightarrow$  natural source of CP violation

$$N_i \xrightarrow{\Gamma} l H^\dagger \qquad N_i \xrightarrow{\bar{\Gamma}} \bar{l} H$$

**CP asymmetry**

$$\varepsilon_i \equiv -\frac{\Gamma_i - \bar{\Gamma}_i}{\Gamma_i + \bar{\Gamma}_i}$$

If  $\varepsilon_i \neq 0$  a **lepton asymmetry** is generated from  $N_i$  decays and partly converted into a **baryon asymmetry** by **sphaleron processes** if  $T_{\text{reh}} \gtrsim 100 \text{ GeV}$  ! (Kuzmin, Rubakov, Shaposhnikov, '85)

$$N_{B-L}^{\text{fin}} = \sum_i \varepsilon_i \kappa_i^{\text{fin}} \Rightarrow \eta_B = a_{\text{sph}} \frac{N_{B-L}^{\text{fin}}}{N_\gamma^{\text{rec}}}$$

**efficiency factors  $\simeq$  # of  $N_i$  decaying out-of-equilibrium**



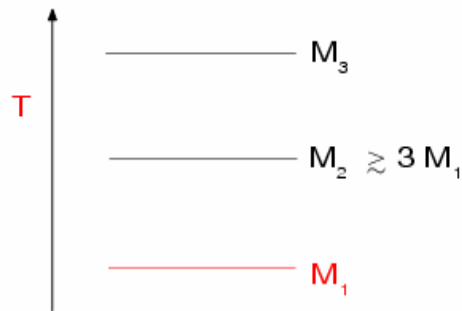
# The traditional picture

- flavor composition of leptons is neglected
- hierarchical heavy neutrino spectrum
- asymmetry generated from the lightest RH neutrino decays ( $N_1$ -dominated scenario)

# $N_1$ - dominated scenario

Assume:

1. hierarchical heavy neutrino spectrum



$$\Rightarrow N_{B-L}^{\text{fin}} \simeq (\varepsilon_3 \kappa_3^{T \gg M_1} + \varepsilon_2 \kappa_2^{T \gg M_1}) e^{-K_1} + \varepsilon_1 \kappa_1^{\text{fin}}$$

2. • strong wash-out ( $K_1 \gg 1$ )

decays and inverse processes are fast compared to the expansion of the Universe

or

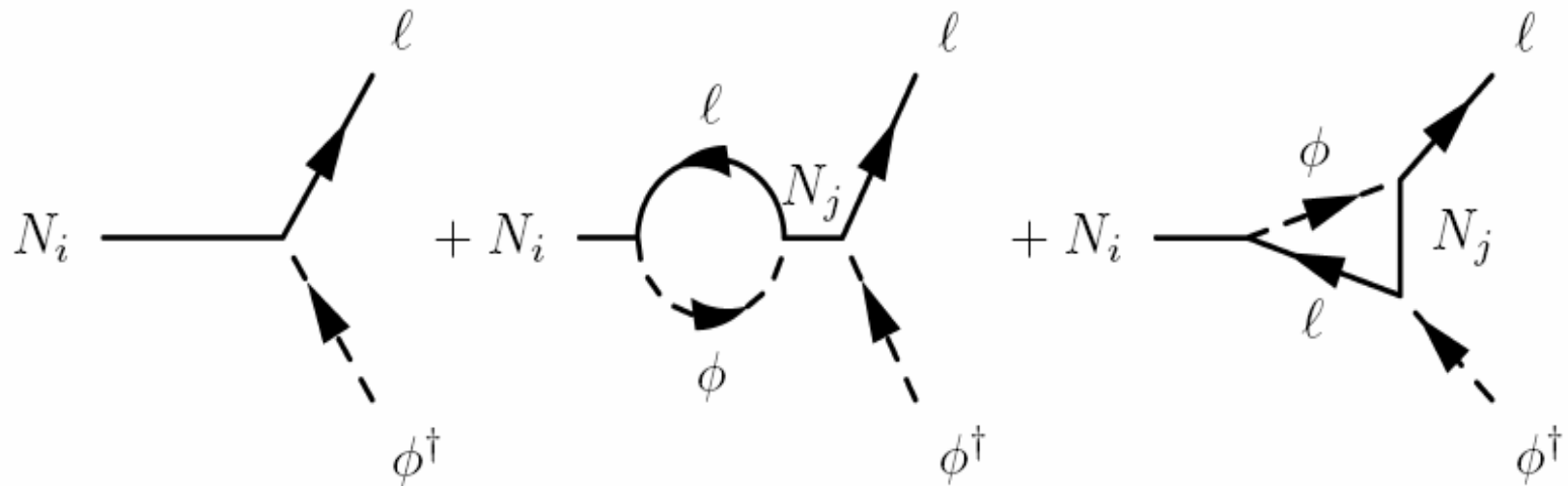
- weak wash-out ( $K_1 \lesssim 1$ ) and  $|\varepsilon_3|, |\varepsilon_2| \ll |\varepsilon_1|$

$$\Rightarrow N_{B-L}^{\text{fin}} = \sum_i \varepsilon_i \kappa_i^{\text{fin}} \simeq \varepsilon_1 \kappa_1^{\text{fin}}$$

It does not depend on low energy phases !

# CP asymmetry

(Flanz,Paschos,Sarkar'95; Covi,Roulet,Vissani'96; Buchmüller,Plümacher'98)



Assuming  $|M_{j \neq i} - M_i| \gg |\Gamma_{j \neq i} - \Gamma_i|$  (off-resonance condition),

the interference between tree level and one-loop diagrams (self energy + vertex) yields:

$$\epsilon_i \simeq \frac{1}{8\pi v^2 (m_D^\dagger m_D)_{ii}} \sum_{j=2,3} \text{Im} \left[ (m_D^\dagger m_D)_{ij}^2 \right] \times \left[ f_V \left( \frac{M_j^2}{M_i^2} \right) + f_S \left( \frac{M_j^2}{M_i^2} \right) \right]$$

$\Rightarrow$  the  $\epsilon_i$ 's depend on  $m_D$  only through  $m_D^\dagger m_D \Rightarrow U$  cancels out !

# Decays and Inverse Decays

$$\frac{dN_{N_1}}{dz} = -D_1 (N_{N_1} - N_{N_1}^{\text{eq}})$$

$$\frac{dN_{B-L}}{dz} = -\varepsilon_1 \frac{dN_{N_1}}{dz} - W_{ID} N_{B-L}$$

$$D_1 = \frac{\Gamma_{D,1}}{H z} = K_1 z \left\langle \frac{1}{\gamma} \right\rangle, \quad W_{ID} \propto D_1 \propto K_1$$

$$K_i \equiv \frac{\Gamma(N_i \rightarrow l \Phi^\dagger)|_{T \rightarrow 0}}{H(T=M_i)} = \frac{(m_D^\dagger m_D)_{ii}}{M_i}$$

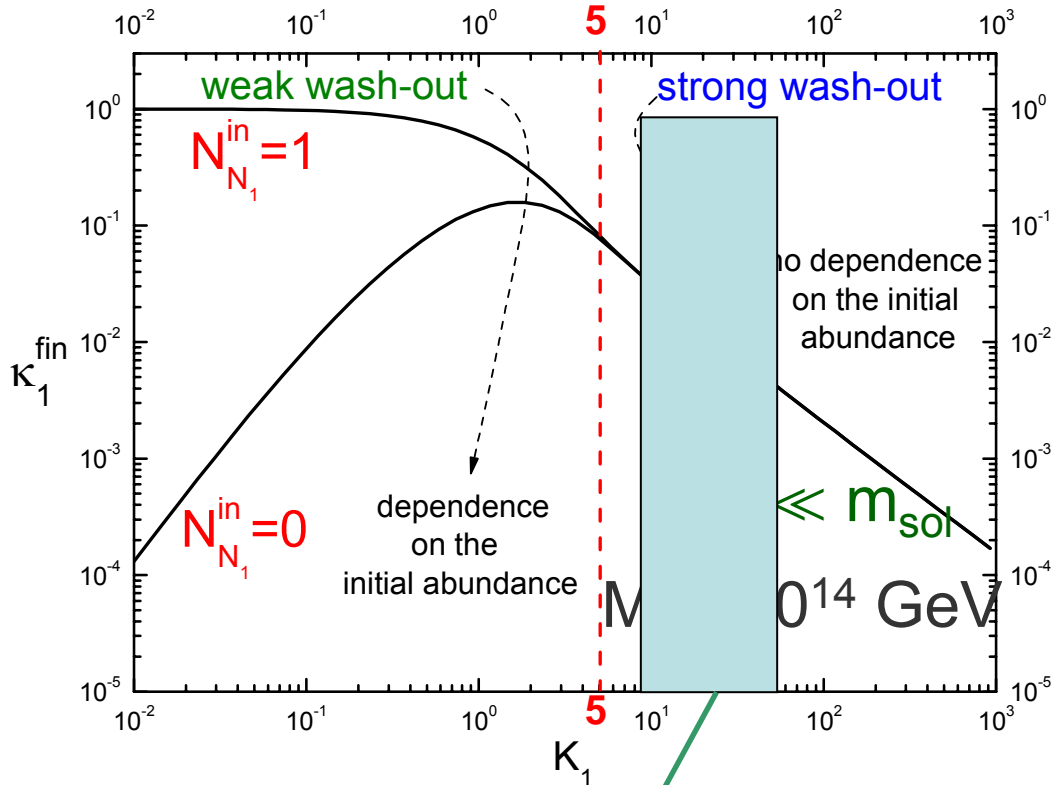
“decay parameters”

$$N_{B-L}(z; K_1, z_{\text{in}}) = N_{B-L}^{\text{in}} e^{-\int_{z_{\text{in}}}^z dz' W_{ID}(z')} + \varepsilon_1 \kappa_1(z)$$

$$\kappa_1(z; K_1, z_{\text{in}}) = - \int_{z_{\text{in}}}^z dz' \left[ \frac{dN_{N_1}}{dz'} \right] e^{-\int_{z'}^z dz'' W_{ID}(z'')}$$

- Weak wash-out regime for  $K_1 \lesssim 1$  (out-of-equilibrium picture recovered for  $K_1 \rightarrow 0$ )
- Strong wash-out regime for  $K_1 \gtrsim 1$

# Dependence on the initial conditions



$$K_{\text{sol}} \simeq 9 \lesssim K_1 \lesssim 50 \simeq K_{\text{atm}}$$

Neutrino mixing data favor the strong wash-out regime !

# Neutrino mass bounds

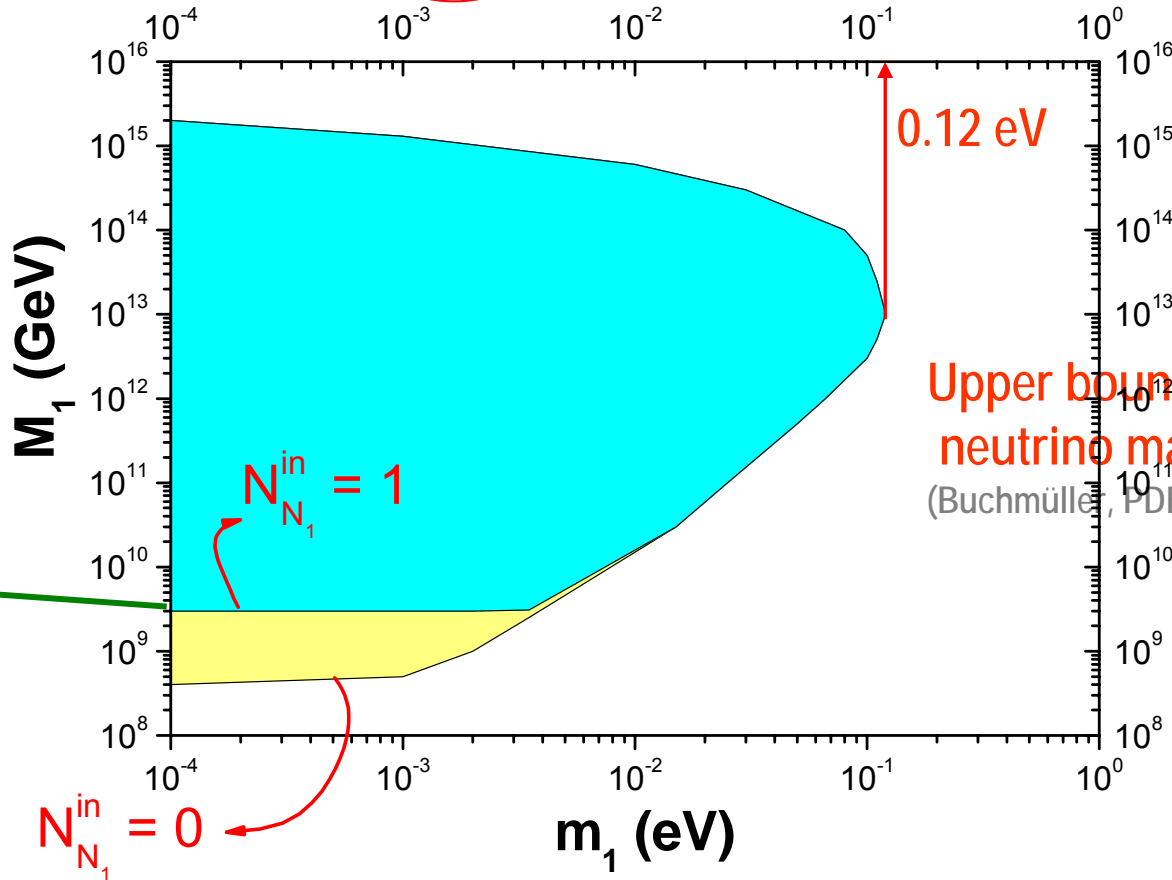
$$\eta_B^{\max}(m_1, \tilde{m}_1, M_1) \simeq 10^{-2} \epsilon_1^{\max}(M_1) \frac{m_{\text{atm}}}{m_3 + m_1} f(m_1, \tilde{m}_1) \kappa_f(\tilde{m}_1) e^{-\frac{M_1}{10^{14} \text{ GeV}} \frac{\sum_i m_i^2}{m_{\text{atm}}^2}} \geq \eta_B^{\text{CMB}}$$

$\sim 10^{-6} (M_1 / 10^{10} \text{ GeV})$

Lower bound on  $M_1$

(Davidson, Ibarra '02; Buchmüller, PDB, Plümacher '02)

$3 \times 10^9 \text{ GeV}$



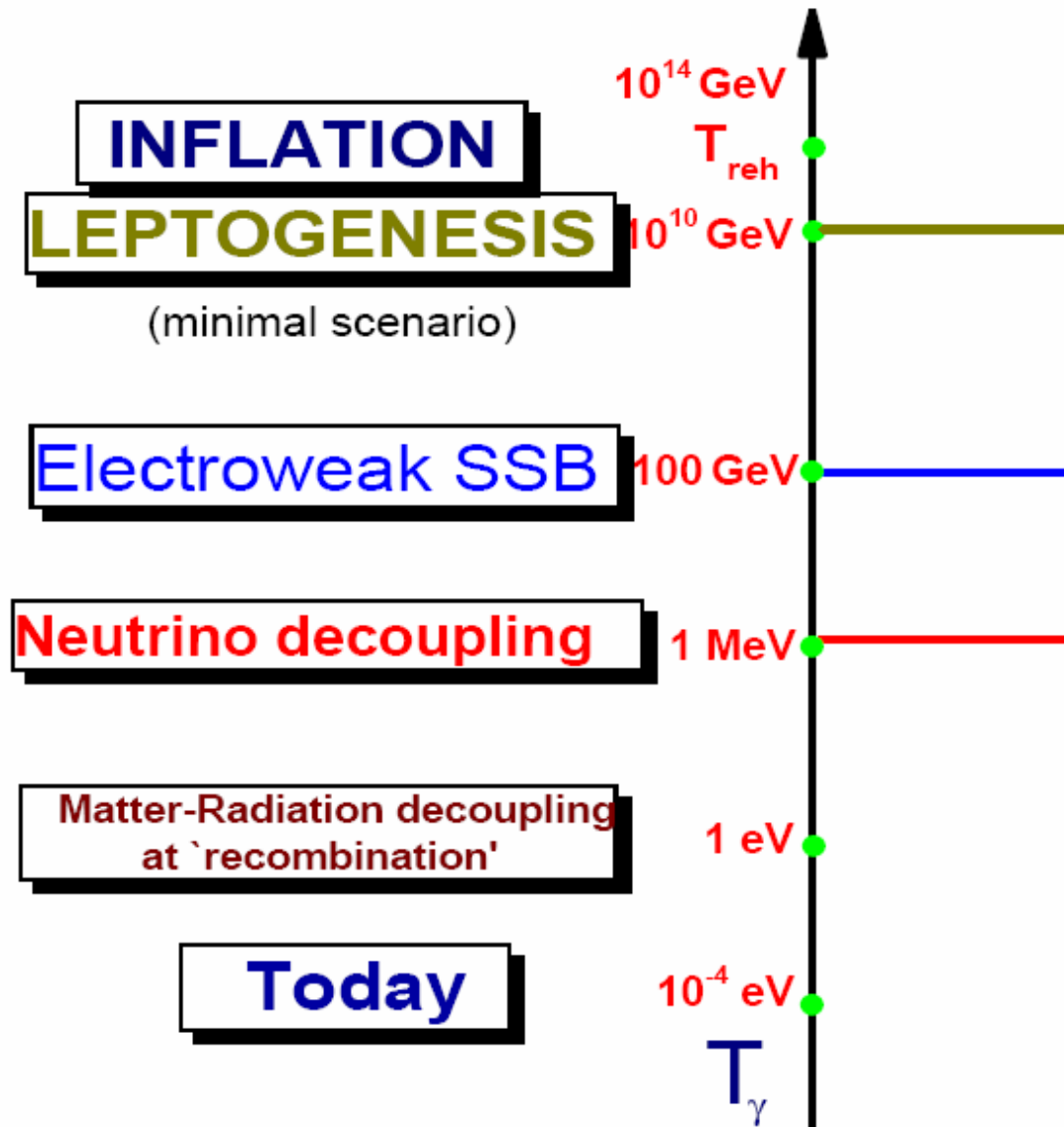
Upper bound on the absolute neutrino mass scale

(Buchmüller, PDB, Plümacher '02)

Lower bound on  $T_{\text{reh}} : T_{\text{reh}} \lesssim 1.5 \times 10^9 \text{ GeV}$

(Buchmüller, PDB, Plümacher '04)

# The need of a very hot Universe for Leptogenesis



# Beyond the traditional picture

- **N<sub>2</sub>-dominated scenario**
- **beyond the hierarchical limit**
- **flavor effects**



# N<sub>2</sub>-dominated scenario

(PDB'05)

See-saw orthogonal matrix:

$$\text{For } \Omega \simeq \begin{pmatrix} 1 & 0 & 0 \\ 0 & \Omega_{22} & \sqrt{1 - \Omega_{22}^2} \\ 0 & -\sqrt{1 - \Omega_{22}^2} & \Omega_{22} \end{pmatrix} \Rightarrow$$

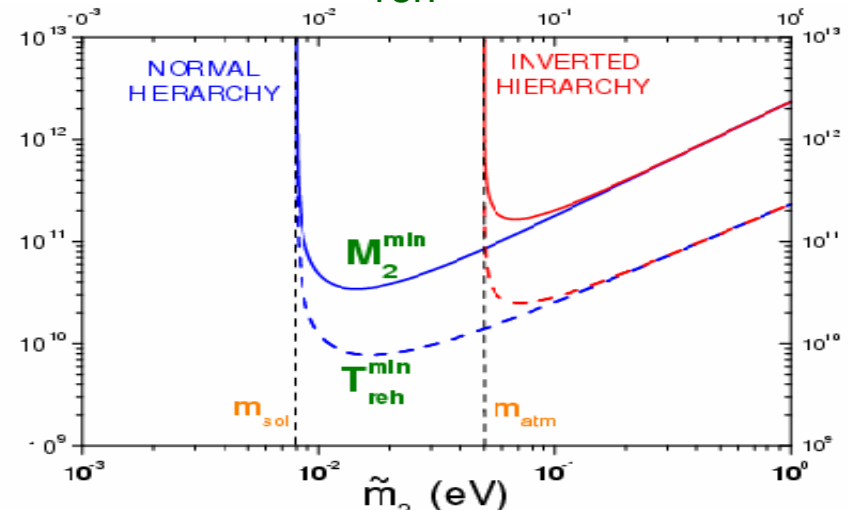
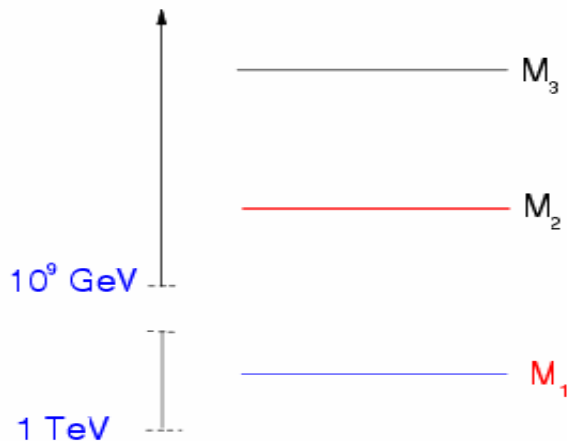
(Casas, Ibarra'01)

$$m_\nu = -m_D \frac{1}{M} m_D^T \Leftrightarrow \Omega^T \Omega = I$$

$$m_D = U \begin{pmatrix} \sqrt{m_1} & 0 & 0 \\ 0 & \sqrt{m_2} & 0 \\ 0 & 0 & \sqrt{m_3} \end{pmatrix} \Omega \begin{pmatrix} \sqrt{M_1} & 0 & 0 \\ 0 & \sqrt{M_2} & 0 \\ 0 & 0 & \sqrt{M_3} \end{pmatrix}$$

1.  $\varepsilon_1 = 0 \Rightarrow$  no asymmetry from  $N_1$ -decays but ...
2.  $\varepsilon_2 \sim \bar{\varepsilon}(M_2) \Rightarrow$  ... it can be produced from  $N_2$ -decays and ...
3.  $\tilde{m}_1 = m_1 \Rightarrow$  ... no washed-out if  $m_1 \lesssim 10^{-3}$  eV!
4.  $K_2 \geq K_{\text{sol}} \gg 1 \Rightarrow$  no dependence on the initial conditions!

The lower bound on  $M_1$  disappears and is replaced by a lower bound on  $M_2$ . The lower bound on  $T_{\text{reh}}$  remains



# Beyond the hierarchical limit

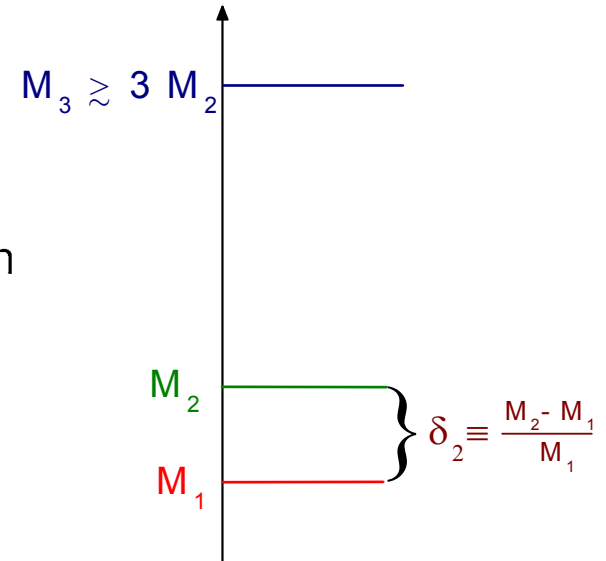
(Pilafitsis '97, Hambye et al '03, Blanchet, PDB '06)

Assume:

- partial hierarchy:  $M_3 \gg M_2, M_1$

$$\Rightarrow |\varepsilon_3| \ll |\varepsilon_2|, |\varepsilon_1| \quad \text{and} \quad \kappa_3^{\text{fin}} \ll \kappa_2^{\text{fin}}, \kappa_1^{\text{fin}}$$

$$N_{B-L}^{\text{fin}} \simeq \varepsilon_1 \kappa_1^{\text{fin}} + \varepsilon_2 \kappa_2^{\text{fin}}$$



- heavy  $N_3$ :  $M_3 \gg 10^{14}$  GeV

3 Effects play simultaneously a role for  $\delta_2 \lesssim 1$ :

- $$\left\{ \begin{array}{l} 1) \text{ the two wash-out add up} \Rightarrow N_{B-L}^{\text{fin}} \searrow \\ 2) \varepsilon_2 \kappa_2^{\text{fin}} \sim \varepsilon_1 \kappa_1^{\text{fin}} \Rightarrow N_{B-L}^{\text{fin}} \nearrow \\ 3) \text{ both } \varepsilon_1, \varepsilon_2 \propto \delta_2^{-1} \text{ for } \delta_2 \ll 0.1 \Rightarrow N_{B-L}^{\text{fin}} \nearrow \end{array} \right.$$

For  $\delta_2 \lesssim 0.01$  (degenerate limit):

$$(M_1^{\text{min}})_{\text{DL}} \simeq 4 \times 10^9 \text{ GeV} \left( \frac{\delta_2}{0.01} \right) \quad \text{and} \quad (T_{\text{reh}}^{\text{min}})_{\text{DL}} \simeq 5 \times 10^8 \text{ GeV} \left( \frac{\delta_2}{0.01} \right)$$

# Flavor effects

(Nardi,Roulet'06;Abada et al.'06;Blanchet,PDB'06)

$$N_1 \longrightarrow l_1 H^\dagger, \quad N_1 \longrightarrow \bar{l}'_1 H$$

Flavour composition:

$$|l\rangle = \sum_\alpha \langle l_\alpha | l_1 \rangle |l_\alpha\rangle \quad (\alpha = e, \mu, \tau)$$

$$|\bar{l}'_1\rangle = \sum_\alpha \langle l_\alpha | \bar{l}'_1 \rangle |\bar{l}_\alpha\rangle$$

**Does it play any role ?** No if  $M_1 > \mathcal{O}(10^{12} \text{ GeV})$

However for lower values of  $M_1$  the  $\tau$ -Yukawa interactions,

$$-\bar{l}_{L\alpha} \phi f_{\alpha\alpha} e_{R\alpha}, \quad (\alpha = \tau)$$

are fast enough to break the coherent evolution of the  $|l_1\rangle$  and  $|\bar{l}'_1\rangle$  quantum states that are projected on the flavor basis!

projectors:

$$P_{1\alpha} \equiv |\langle l_\alpha | l_1 \rangle|^2 = P_{1\alpha}^0 + \frac{\Delta P_{1\alpha}^0}{2} \quad (\sum_\alpha P_{1\alpha} = 1)$$

$$\bar{P}_{1\alpha} \equiv |\langle \bar{l}_\alpha | \bar{l}'_1 \rangle|^2 = P_{1\alpha}^0 - \frac{\Delta P_{1\alpha}^0}{2} \quad (\sum_\alpha \bar{P}_{1\alpha} = 1)$$

these 2 terms correspond to **2 different flavor effects** :

- In each inverse decay  $H^\dagger + l_\alpha \rightarrow N_1$  the Higgs interacts now with incoherent flavor eigenstates !

$\Rightarrow$  **the wash-out is reduced** and  $K_1 \rightarrow K_{1\alpha} \equiv P_{1\alpha}^0 K_1$

- In general  $|\bar{l}'_1\rangle \neq CP|l_1\rangle$  and this produces an **additional CP violating contribution** to the

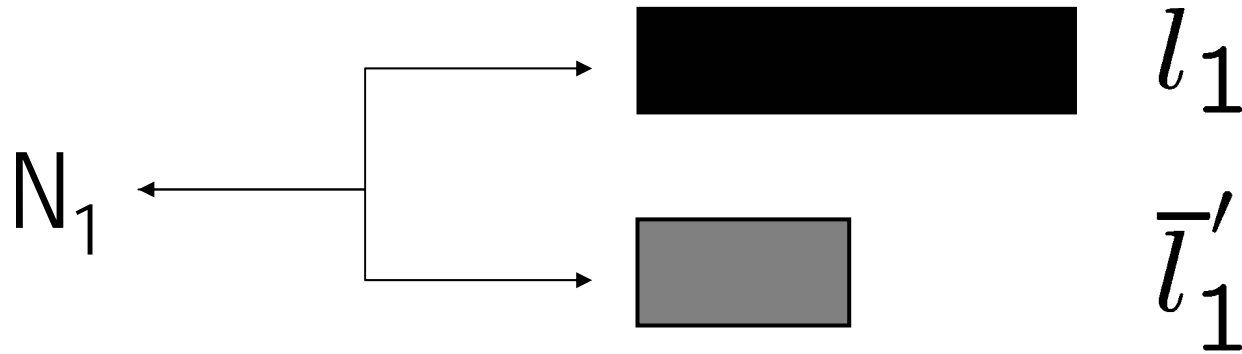
**flavoured CP asymmetries**

$$\varepsilon_{1\alpha} \equiv -\frac{P_{1\alpha} \Gamma_1 - \bar{P}_{1\alpha} \bar{\Gamma}_1}{\Gamma_1 + \bar{\Gamma}_1} = P_{1\alpha}^0 \varepsilon_1 + \frac{\Delta P_{1\alpha}^0}{2}$$

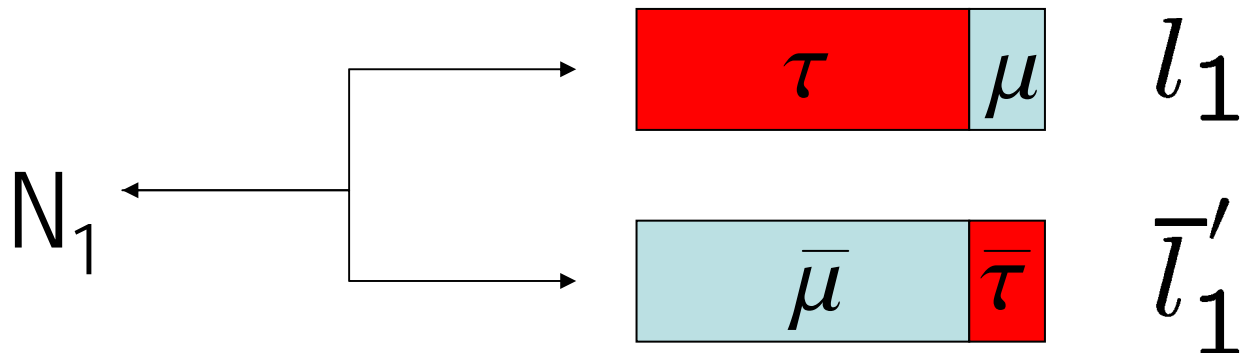
Interestingly one has that this additional contribution depends on U !

# In pictures:

1)  $\Gamma \neq \bar{\Gamma}$



2)  $|\bar{l}'_1\rangle \neq CP|l_1\rangle$



# Flavoured Kinetic Equations

It is then necessary to track the asymmetries separately in each flavor:

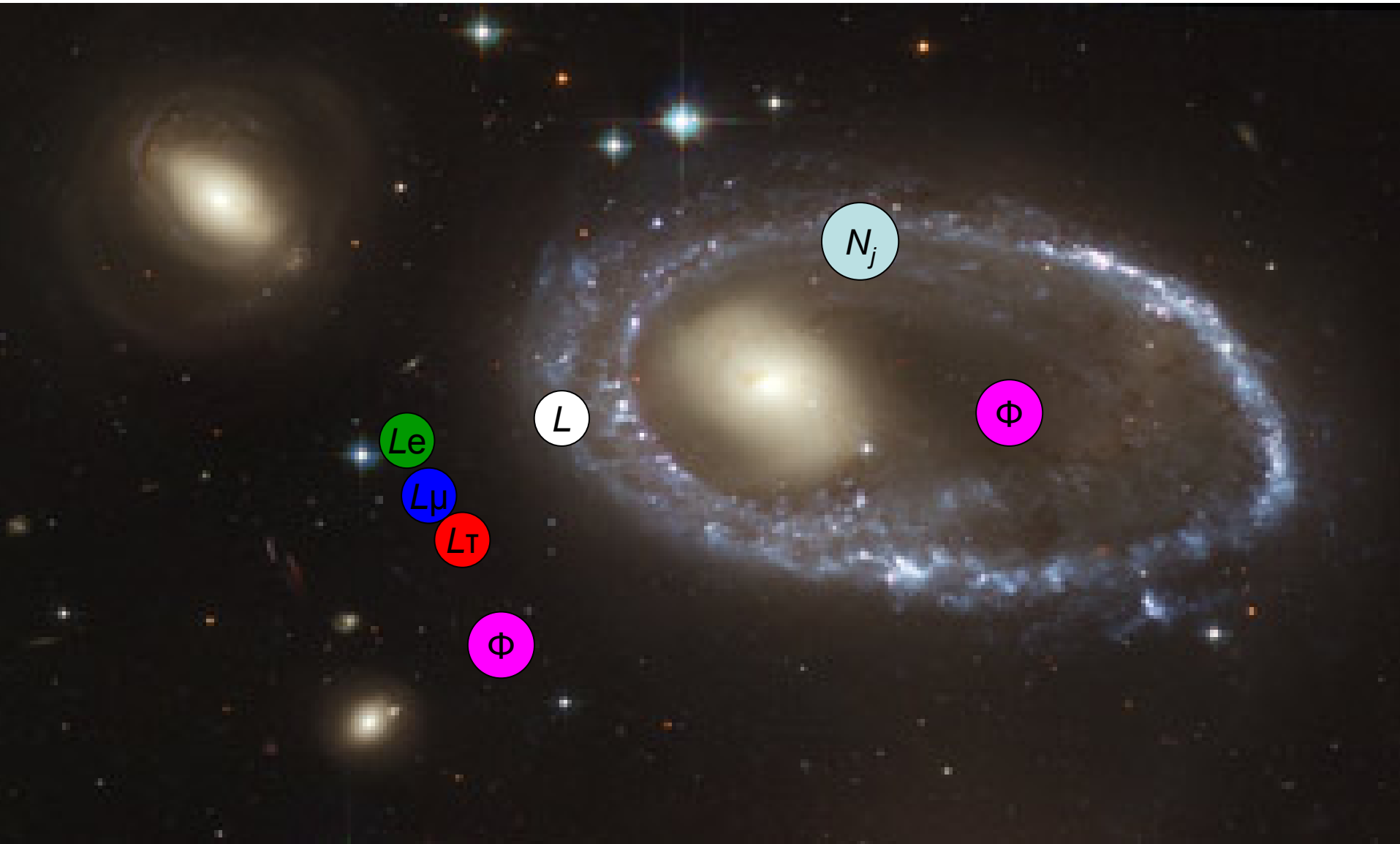
$$\Delta_\alpha \equiv \frac{B}{3} - L_\alpha$$

$$\frac{dN_{N_1}}{dz} = -D_1 (N_{N_1} - N_{N_1}^{\text{eq}})$$

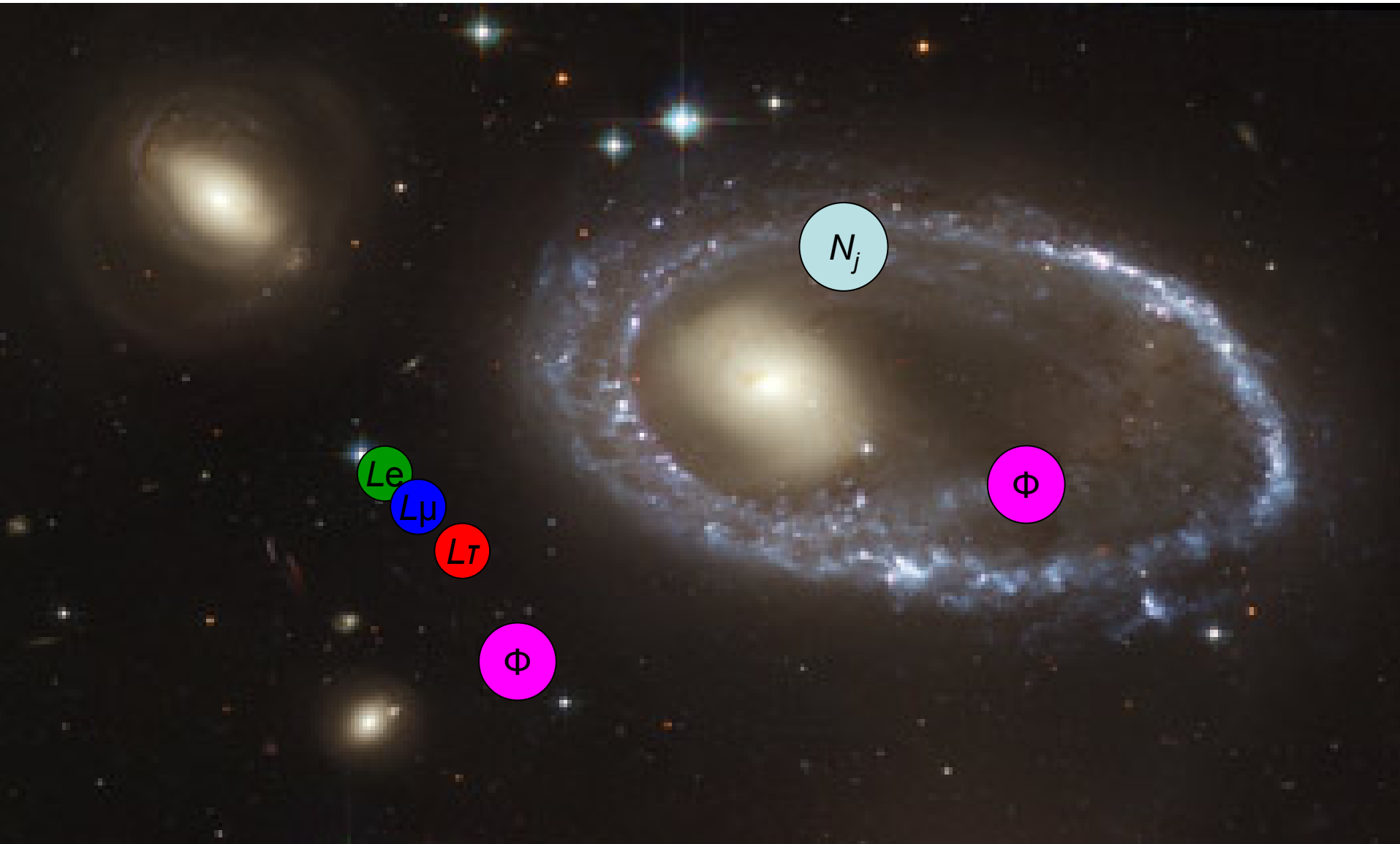
$$\frac{dN_{\Delta_\alpha}}{dz} = -\varepsilon_{1\alpha} \frac{dN_{N_1}}{dz} - P_{1\alpha}^0 W_{ID} N_{\Delta_\alpha}$$

$$N_{B-L} = \sum_{\alpha} N_{\Delta_\alpha}$$

# NO FLAVOR



# WITH FLAVOR





# General scenarios ( $K_1 \gg 1$ )

## – Alignment case

$$P_{1\alpha} = \bar{P}_{1\alpha} = 1 \quad \text{and} \quad P_{1\beta \neq \alpha} = \bar{P}_{1\beta \neq \alpha} = 0 \quad \Rightarrow \quad \frac{N_{B-L}^f}{[N_{B-L}^f]_{\text{unfl}}} = 1$$

## – Democratic (semi-democratic) case

$$P_{1\alpha} = \bar{P}_{1\alpha} = 1/3 \quad (P_{1\alpha} = 0, P_{1\beta \neq \alpha} = 1/2) \quad \Rightarrow \quad \frac{N_{B-L}^f}{[N_{B-L}^f]_{\text{unfl}}} \simeq 3$$

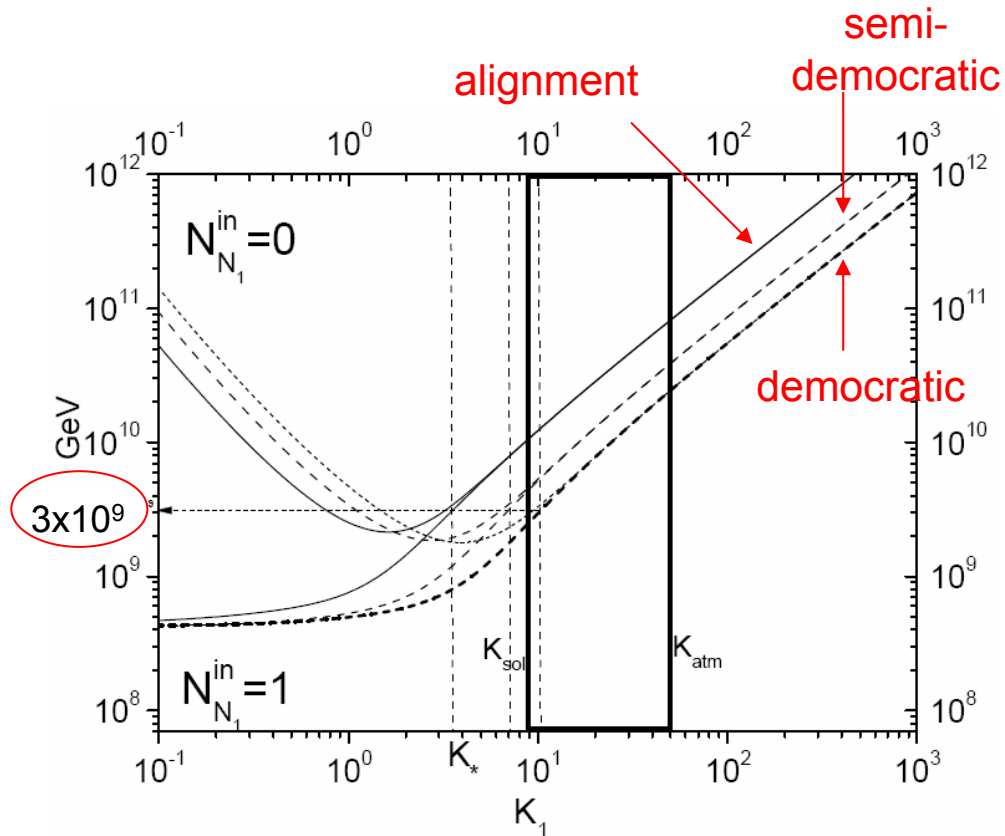
## – One-flavor dominance

$$P_{1\alpha}^0 \ll P_{1\beta \neq \alpha}^0 \sim \mathcal{O}(1) \quad \text{and} \quad \varepsilon_{1\alpha} \simeq \varepsilon_{1\beta \neq \alpha} \quad \Rightarrow \quad \frac{N_{B-L}^f}{[N_{B-L}^f]_{\text{unfl}}} \gg 1$$

big effect!

# Lower bound on $M_1$

(Blanchet, PDB'06)



→ The lowest bounds independent of the initial conditions (at  $K_1 = K_*$ ) don't change! (Blanchet, PDB '06)

But for a fixed  $K_1$ , there is a relaxation of the lower bounds of a factor 2 (semi-democratic) or 3 (democratic), but it can be much larger in the case of one flavor dominance.

# A relevant specific case

- Let us consider:

$$\Omega = R_{13} = \begin{pmatrix} \sqrt{1 - \omega_{31}^2} & 0 & -\omega_{31} \\ 0 & 1 & 0 \\ \omega_{31} & 0 & \sqrt{1 - \omega_{31}^2} \end{pmatrix}$$

- Since the projectors and flavored asymmetries depend on  $U$   
 $\Rightarrow$  one has to plug the information from neutrino mixing experiments

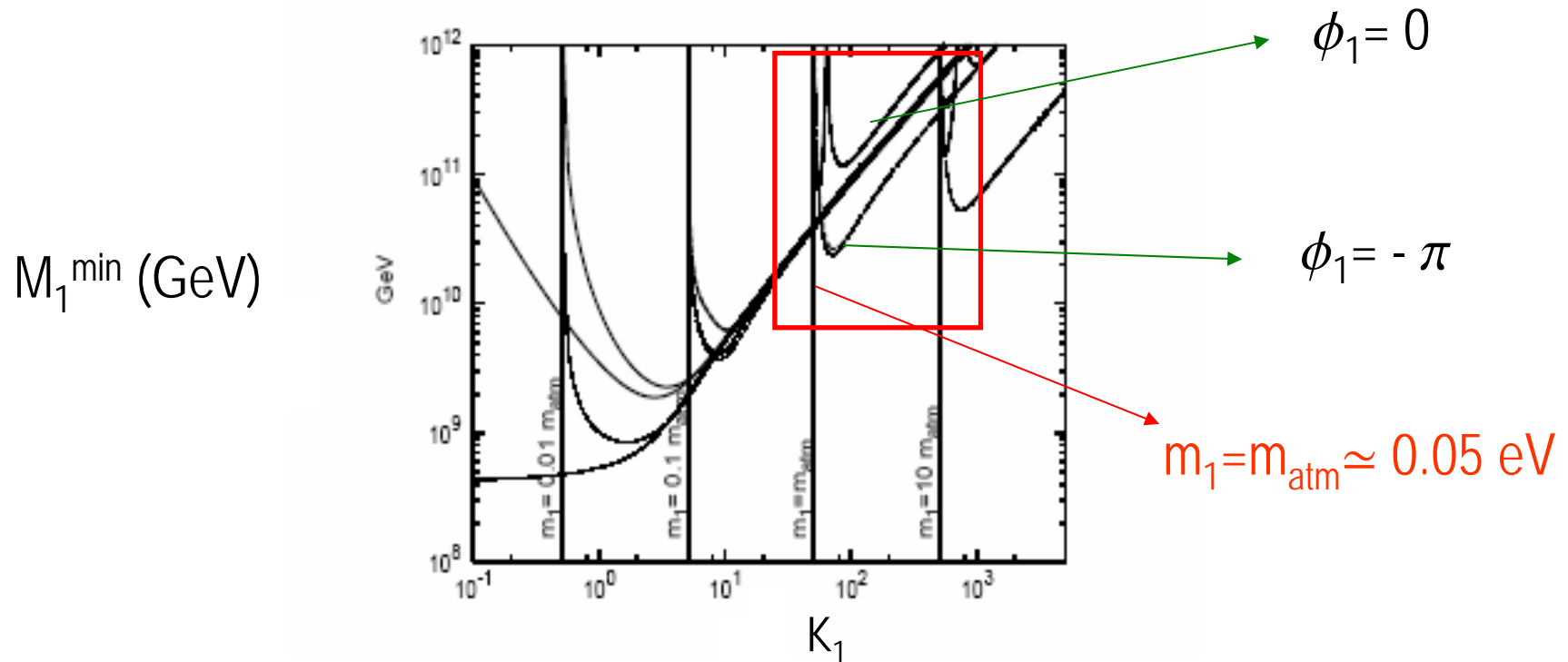
- For  $m_1=0$  (fully hierarchical light neutrinos)  
 $\Rightarrow P_{1e}^0 \simeq 0, \quad P_{1\mu}^0 \simeq P_{1\tau}^0 \simeq 1/2, \quad \Delta P_{1\alpha} = 0$

$\Rightarrow$  Semi-democratic case

Flavor effects represent just a correction in this case !

# The role of Majorana phases

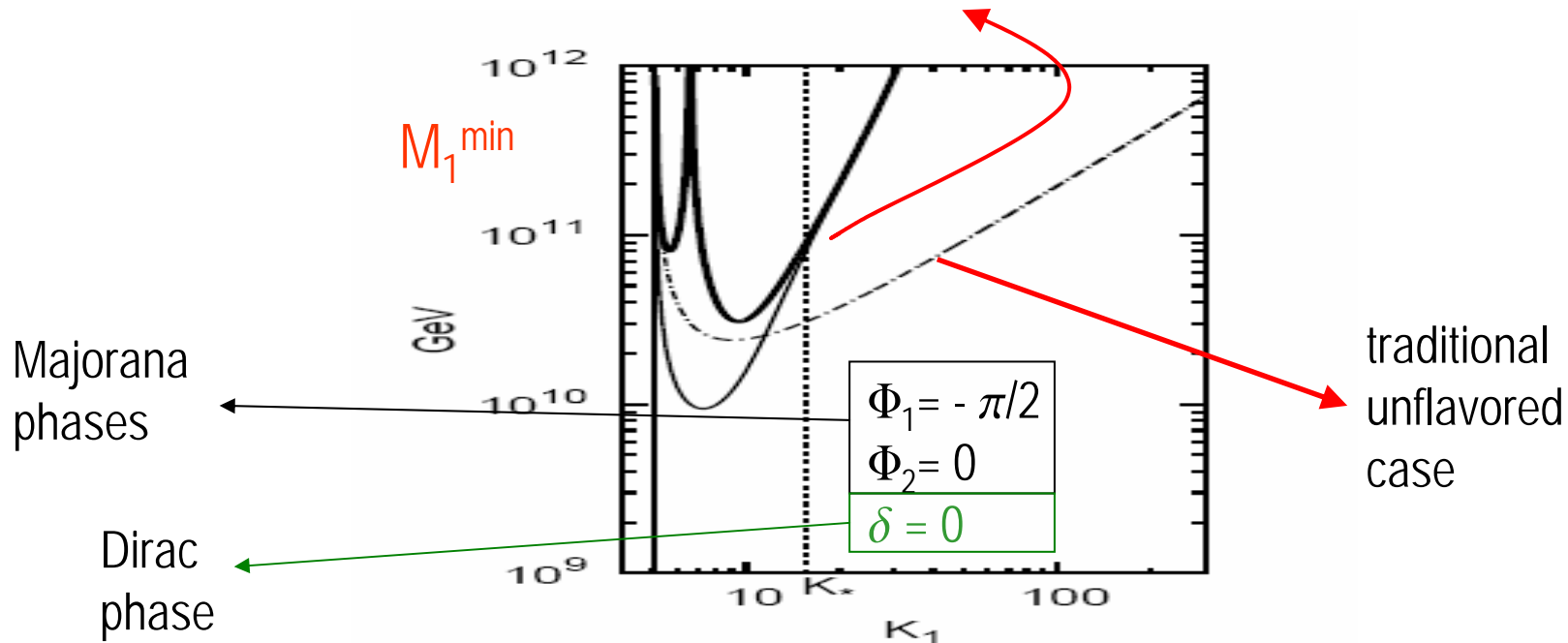
- However allowing for a non-vanishing  $m_1$  the effects become much larger especially when Majorana phases are turned on !



$$U = \begin{pmatrix} c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i\delta} \\ -s_{12} c_{23} - c_{12} s_{23} s_{13} e^{i\delta} & c_{12} c_{23} - s_{12} s_{23} s_{13} e^{i\delta} & s_{23} c_{13} \\ s_{12} s_{23} - c_{12} c_{23} s_{13} e^{i\delta} & -c_{12} s_{23} - s_{12} c_{23} s_{13} e^{i\delta} & c_{23} c_{13} \end{pmatrix} \times \text{diag}(e^{i\frac{\Phi_1}{2}}, e^{i\frac{\Phi_2}{2}}, 1),$$

# Leptogenesis from low energy phases ?

Let us now further impose  $\Omega$  real setting  $\text{Im}(\omega_{13})=0$



- The lower bound gets more stringent but still successful leptogenesis is possible just with CP violation from 'low energy' phases that can be tested in  $\beta\beta 0\nu$  decay (Majorana phases) and neutrino mixing (Dirac phase)
- Moreover considering the degenerate limit these lower bounds can be relaxed: this is important for ' $\delta$ -leptogenesis' ! (Anisimov, Blanchet, PDB, in preparation)

# Conclusions

- Leptogenesis has at the moment a clear advantage on EWBG: **neutrino masses have been discovered** and even in the right range; a discovery of CP violation in neutrino mixing would represent another success;
- EWBG has the nice virtue to be highly predictive (therefore also falsifiable): LHC, ILC, DM direct searches, EDM's, gravitational waves in LISA (Riotto et al. '01) ;
- **EWBG discovery would kill leptogenesis** making it useless;
- However, if nothing beyond a SM Higgs will be found then this would represent another positive test for leptogenesis and a definitive death of EWBG

# The orthogonal seesaw matrix

(Casas, Ibarra'01)

$$m_\nu = -m_D \frac{1}{M} m_D^T \Leftrightarrow \boxed{\Omega^T \Omega = I}$$

$$\boxed{m_D} = \left[ U \begin{pmatrix} \sqrt{m_1} & 0 & 0 \\ 0 & \sqrt{m_2} & 0 \\ 0 & 0 & \sqrt{m_3} \end{pmatrix} \Omega \begin{pmatrix} \sqrt{M_1} & 0 & 0 \\ 0 & \sqrt{M_2} & 0 \\ 0 & 0 & \sqrt{M_3} \end{pmatrix} \right] \left( \begin{array}{l} U^\dagger U = I \\ U^\dagger m_\nu U^* = -D_m \end{array} \right)$$

*theory*

“observables”

- parameter counting:  $6 + 3 + 6 + 3 = 18$
- **experiments**  $\Rightarrow$  information on the 9 ‘low energy’ parameters in  $m_\nu = -U D_m U^T$ :
  - we **measure 4**:  $m_{\text{atm}}$ ,  $m_{\text{sol}}$ ,  $\theta_{23} \simeq 45^\circ$ ,  $\theta_{12} \simeq 32^\circ \simeq 45^\circ - \theta_C$
  - we still **miss five**:  $m_1 \lesssim 1 \text{ eV}$ ,  $\theta_{13} \lesssim 14^\circ$ ,  $\delta, \varphi_1, \varphi_2$
- the 9 parameters in  $\Omega$  and in  $M_i$  escape conventional investigation: the **dark side** !
- **leptogenesis**  $\Rightarrow$  information on  $\Omega$ ,  $M_i$  and also on  $m_1$  but  $\varepsilon_i = \varepsilon_i(m_D^\dagger m_D)$ 
  - $\Rightarrow$   **$U$  cancels out**: in general we cannot test leptogenesis with  **$\mathcal{CP}$  in neutrino mixing** !

# (Unflavored) Kinetic Equations

$$z = \frac{M_1}{T}$$

$$\begin{aligned} \frac{dN_{N_i}}{dz} &= -(D_i + S_i)(N_{N_i} - N_{N_i}^{\text{eq}}) \\ \frac{dN_{B-L}}{dz} &= \sum_i \varepsilon_i (D_i + S_i) (N_{N_i} - N_{N_i}^{\text{eq}}) - N_{B-L} \sum_i W_i^{\text{ID}} \end{aligned}$$

CP violation in decays

Wash-out term from inverse decays

$$D_i \equiv \frac{\Gamma_{D,i}}{H(z)z} = K_i z \langle \frac{1}{\gamma} \rangle, \quad W_i^{\text{ID}} \propto D_i \propto K_i$$

“decay parameters”

$$K_i \equiv \frac{\Gamma(N_i \rightarrow l\Phi^\dagger)|_{T \rightarrow 0}}{H(T=M_i)} = \frac{(m_D^\dagger m_D)_{ii}}{M_i}$$

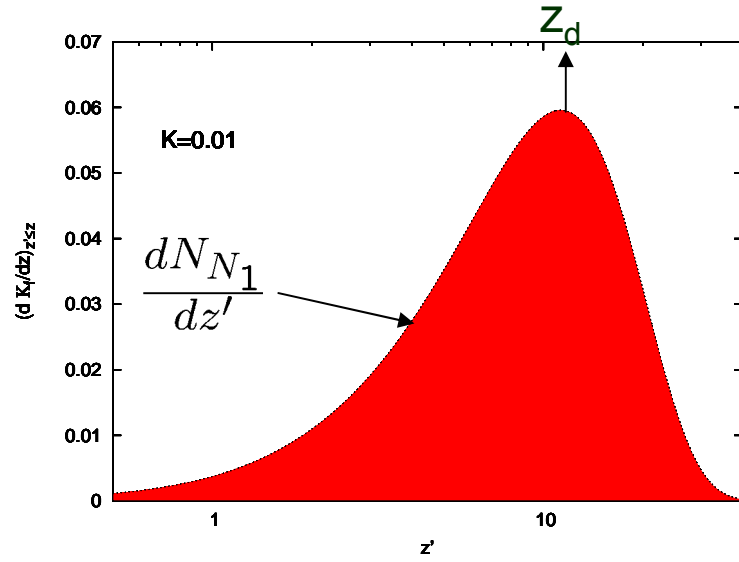
- Strong wash-out when  $K_i \gtrsim 3$
- Weak wash-out when  $K_i \ll 3$



$$z \equiv M_1 / T$$

$$K_1 \equiv t_U(T=M_1) / \tau_1$$

## WEAK WASH-OUT



$$\left. \frac{dK_1}{dz'} \right|_{z' \leq z}$$

