

Aspetti teorici della Fisica del Sapore

### **Two Important Experimental Novelties:**

$$\Delta m_s = (17.77 \pm 0.10 \pm 0.07) \text{ ps}^{-1}$$

Belle: 
$$(1.79 + 0.56 + 0.39 - 0.46) + 0.49 - 0.46$$
  $) \times 10^{-4}$  BaBar:  $(0.88 + 0.68 - 0.67) = 0.11) \times 10^{-4}$   
Average:  $(1.31 \pm 0.48) \times 10^{-4}$ 

$$\sin 2 \beta_{\text{measured}} = 0.726 \pm 0.037 \implies 0.675 \pm 0.026$$

Dipartimento di Fisica di Roma La Sapienza

Guido Martinelli

# **STANDARD MODEL**

- 1) Generalities
- 2) Predictions vs Postdictions
- 3) Lattice vs angles
- 4)  $V_{ub}$  inclusive,  $V_{ub}$  exclusive vs sin  $2\beta$
- 5) Experimental determination of lattice parameters

# **Flavor Physics Beyond the SM**

# N(N-1)/2 angles and (N-1)(N-2)/2 phases

N=3 3 angles + 1 phase KM the phase generates complex couplings i.e. <u>CP</u> <u>violation;</u>

6 masses +3 angles +1 phase = 10 parameters

V <sub>ud</sub>	V <sub>us</sub>	V <sub>ub</sub>
V <sub>cd</sub>	V <sub>cs</sub>	V <sub>cb</sub>
V <sub>tb</sub>	V <sub>ts</sub>	V <sub>tb</sub>

NO Flavour Changing Neutral Currents (FCNC) at Tree Level (FCNC processes are good candidates for observing NEW PHYSICS)

CP Violation is natural with three quark generations (Kobayashi-Maskawa)

With three generations all CP phenomena are related to the same unique parameter (δ)



## Quark masses & Generation Mixing



$$|V_{ud}| = 0.9735(8)$$
  

$$|V_{us}| = 0.2196(23)$$
  

$$|V_{cd}| = 0.224(16)$$
  

$$|V_{cs}| = 0.970(9)(70)$$
  

$$|V_{cb}| = 0.0406(8)$$
  

$$|V_{ub}| = 0.00409(25)$$
  

$$|V_{tb}| = 0.99(29)$$
  
(0.999)

# The Wolfenstein Parametrization

<mark>ν<sub>td</sub></mark> λ ~ 0.2 n ~ 0.2	A ~ 0. 0 ~ 0.	$\begin{cases} Sin \ \theta_1 \\ Sin \ \theta_2 \\ Sin \ \theta_1 \\ Sin \ \theta_1 \end{cases}$	$2 = \lambda$ $3 = A \lambda^{2}$ $3 = A \lambda^{3}(\rho - i \eta)$
$\begin{array}{c} A  \lambda^3  \times \\ (1 - \rho - i \eta) \end{array}$	-A λ <sup>2</sup>	1	
- λ	1 - 1/2 $\lambda^2$	A $\lambda^2$	+ O(λ <sup>4</sup> )
1 - 1/2 $\lambda^2$	λ	A λ <sup>3</sup> (ρ - i η)	V <sub>ub</sub>



Physical quantities correspond to invariants under phase reparametrization i.e.  $|a_1|, |a_2|, ..., |e_3|$  and the area of the Unitary Triangles

$$J = Im (a_1 a_2^*) = |a_1 a_2| Sin \beta$$
  
a precise knowledge of the  
moduli (angles) would fix J  
$$\mathcal{V}_{ud}^* V_{ub} + V_{cd}^* V_{cb} + V_{td}^* V_{tb} = 0$$





SEVERAL UNITARITY TRIANGLE ANALYSES, USING METHODS BASED ON THE **"BAYESIAN "** APPROACH, HAVE BEEN MADE DURING THE LAST DECADE



BaBar Meeting 14/2/01

Measure
$$V_{CKM}$$
Other NP parameters $\Gamma(b \rightarrow u)/\Gamma(b \rightarrow c)$  $\bar{\rho}^2 + \bar{\eta}^2$  $\bar{\Lambda}, \lambda_1, F(1), \ldots$  $\epsilon_K$  $\eta [(1 - \bar{\rho}) + \ldots]$  $B_K$  $\Delta m_d$  $(1 - \bar{\rho})^2 + \bar{\eta}^2$  $f_{B_d}^2 B_{B_d}$  $\Delta m_d/\Delta m_1$  $(1 - \bar{\rho})^2 + \bar{\eta}^2$  $\xi$  $A_{CP}(B_d \rightarrow J/\psi K_s)$  $\sin 2\beta$  $-$ 

For details see: UTfit Collaboration hep-ph/0501199 hep-ph/0509219 hep-ph/0605213 hep-ph/0606167 http://www.utfit.org

$$Q^{EXP} = V_{CKM} imes \langle H_F | \hat{O} | H_I 
angle$$

# sin 2β is measured directly from $\frac{1}{2}$ J/ψ K<sub>s</sub> decays at Babar & Belle

$$\oint_{J/\psi K_{s}} = \frac{\Gamma(B_{d}^{0} \rightarrow J/\psi K_{s}, t) - \Gamma(B_{d}^{0} J/\psi K_{s}, t)}{\Gamma(B_{d}^{0} \rightarrow J/\psi K_{s}, t) + \Gamma(B_{d}^{0} - J/\psi K_{s}, t)}$$

$$A_{J/\psi K_s} = \sin 2\beta \sin (\Delta m_d t)$$

### DIFFERENT LEVELS OF THEORETICAL UNCERTAINTIES (STRONG INTERACTIONS)

1) First class quantities, with reduced or negligible uncertainties  $A_{CP}(B \rightarrow J/\psi K_s) \quad \gamma \quad from \ B \rightarrow DK$ 

 $K^0 \rightarrow \pi^0 \nu \bar{\nu}$ 

2) Second class quantities, with theoretical errors of O(10%) or less that reliably estimated  $\epsilon_K \qquad \Delta M_{d,s}$  $\Gamma(B \to c, u), \qquad K^+ \to \pi^+ v \bar{v}$ 

3) Third class quantities, for which theoretical predictions are model dependent (BBNS, charming, etc.) In case of discrepacies we cannut tell whether is <u>new physics or</u>  $B \rightarrow K \pi \quad B \rightarrow \pi^0 \pi^0 = B \rightarrow \phi K_s$ 

# Classical Quantities used in the Standard UT Analysis



levels @

68% (95%) CL



### New Quantities used in the UT Analysis

# **UT-ANGLES**

Several new determinations of UT angles are now available, thanks to the results coming from the B-Factory experiments



New bounds are available from rare B and K decays. They do not still have a strong impact on the global fit and they are not used at present.

 $\underline{K \to \pi \vee \nu}$ 





 $(B \rightarrow \rho/\omega \gamma)/(B \rightarrow K^*\gamma)$ 





### THE COLLABORATION



M.Bona, M.Ciuchini, E.Franco, V.Lubicz,

G.Martinelli, F.Parodi, M.Pierini,

P.Roudeau, C.Schiavi, L.Silvestrini,

V. Sordini, A.Stocchi, V.Vagnoni

Roma, Genova, Annecy, Orsay, Bologna 2006 ANALYSIS

- New quantities e.g. B -> DK included
- Upgraded exp. numbers (after ICHEP)
  - CDF & Belle new measurements









### A closer look to the analysis:

- 1) Predictions vs Postdiction
- 2) Lattice vs angles
- 3)  $V_{ub}$  inclusive,  $V_{ub}$  exclusive vs sin  $2\beta$
- 4) Experimental determination of lattice parameters

## CKM origin of CP Violation in K<sup>0</sup>- K<sup>0</sup> Mixing



Comparison of  $\sin 2\beta$  from direct measurements (Aleph, Opal, Babar, Belle and CDF) and UT analysis  $\sin 2 \beta_{\text{measured}} = 0.675 \pm 0.026$ correlation (tension)  $\sin 2 \beta_{\text{UTA}} = 0.755 \pm 0.040$ with  $V_{ub}$ , see later  $\sin 2 \beta_{\text{IJTA}} = 0.698 \pm 0.066$  $\sin 2 \beta_{\text{UTA}} = 0.65 \pm 0.12$ prediction from Ciuchini et al. (2000) Prediction 1995 from Ciuchini, Franco, G.M., Reina, Silvestrini  $\sin 2 \beta_{tot} = 0.701 \pm 0.022$ Very good agreement

no much room for physics beyond the SM !!





# NEWS from NEWS (Standard Model)



#### Theoretical predictions of $\Delta m_s$ in the years



### A closer look to the analysis:

- 1) Predictions vs Postdictions
- 2) Lattice vs angles
- 3)  $V_{ub}$  inclusive,  $V_{ub}$  exclusive vs sin  $2\beta$
- 4) Experimental determination of lattice parameters

Comparable accuracy due to the precise  $\sin 2\beta$ value and substantial improvement due to the new  $\Delta m_s$  measureme

<u>Crucial to improve</u> <u>measurements of the</u> <u>angles, in particular</u> (tree level NP-free determination)

> Still imperfect agreement in  $\overline{\eta}$  due to sin2 $\beta$  and  $V_{ub}$ tension

The UT-angles fit does not depend on theoretical calculations (treatement of errors is not an issue)



### ANGLES VS LATTICE

A closer look to the analysis:

- 1) Predictions vs Postdictions
- 2) Lattice vs angles
- 3)  $V_{ub}$  inclusive,  $V_{ub}$  exclusive vs sin  $2\beta$
- 4) Experimental determination of lattice parameters





Inclusive: uses non perturbative parameters most not from lattice QCD (fitted from the lepton spectrum)



### 1) Use only exclusive and predict inclusive 2) Use only inclusive and predict exclusive



# Tension between inclusive Vub and the rest of the fit





**Potentially large NP contributions** (i.e. MSSM at large tanβ, Isidori & Paradisi)

f <sub>B</sub> = (190 ± 14) MeV V <sub>ub</sub> = (36.7 ± 1.5) 10 <sup>-4</sup>	<mark>[UTA]</mark> [UTA]	$BR(B \rightarrow \tau \nu_{\tau}) = (0.89 \pm 0.16) \times 10^{-4}$ (Best SM prediction)
f <sub>B</sub> = (189 ± 27) MeV V <sub>ub</sub> = (35.0 ± 4.0) 10 <sup>-4</sup>	[LQCD] [Exclusive]	$BR(B \rightarrow \tau V_{\tau}) = (0.84 \pm 0.30) \times 10^{-4}$ (Independent from
f <sub>B</sub> = (189 ± 27) MeV V <sub>ub</sub> = (44.9 ± 3.3) 10 <sup>-4</sup>	[LQCD] [Inclusive]	other NP effects) $BR(B \rightarrow \tau v_{\tau}) = (1.39 \pm 0.44) \times 10^{-4}$

From BR(B $\rightarrow \tau v_{\tau}$ ) and V<sub>ub</sub>(UTA):  $f_B = (237 \pm 37)$  MeV

# Hadronic Parameters From UTfit

- 1) Predictions vs Postdictions
- 2) Lattice vs angles
- 3)  $V_{ub}$  inclusive,  $V_{ub}$  exclusive vs sin  $2\beta$
- 4) Experimental determination of lattice parameters



## IMPACT of the NEW MEASUREMENTS on LATTICE HADRONIC PARAMETERS

 $f_{B_s} \hat{B}_{B_s}^{1/2} \quad \xi \quad \hat{B}_K$ 

Comparison between experiments and theory







SPECTACULAR AGREEMENT (EVEN WITH QUENCHED LATTICE QCD)

# exps vs predictions







OLD





#### Only tree level processes



### Even in the favourable case in which the theory above the cutoff is weakly coupled, such as in the Minimal Supersymmetric Standard Model (MSSM), large contributions to FCNC and CP processes are expected contrary to the increasigly precise experimental measurements.

### **FLAVOUR PUZZLE**

### **FLAVOUR PUZZLE**

Model Independent Analysis of 
$$\Delta F = 2$$
  

$$C_{B_q} e^{2i\phi_{B_q}} = \frac{\langle B_q^0 | H_{eff}^{full} | \bar{B}_q^0 \rangle}{\langle B_q^0 | H_{eff}^{SM} | \bar{B}_q^0 \rangle}, \quad q = s, d$$

$$\Delta m_d^{exp} = C_{B_d} \Delta m_d^{SM}, \quad \sin 2\beta^{exp} = \sin(2\beta^{SM} + 2\phi_{B_d}),$$

$$\alpha^{exp} = \alpha^{SM} - \phi_{B_d}$$

$$C_{\varepsilon_K} = \frac{Im \left[ \langle K^0 | H_{eff}^{full} | \bar{K}^0 \rangle \right]}{Im \left[ \langle K^0 | H_{eff}^{SM} | \bar{K}^0 \rangle \right]},$$

$$\varepsilon_K^{exp} = C_{\varepsilon_K} \varepsilon_K^{SM}$$

### The Unitarity Triangle in the presence of NP



#### **Additional contraints**



Not precise enough to bound CKM in SM ... but good for reducing NP allowed (experimental error too large)... parameter space

#### **Additional contraints**

**CP** aymmetry in dimuon evel DØnote 5042-CONF\_V1.4





### **Additional contraints**

 $\Delta \Gamma_{\rm s} / \Gamma_{\rm s}$ 

$$\frac{\Delta\Gamma_q}{\Delta m_q} = -2\frac{\kappa}{C_{B_q}} \left\{ \cos\left(2\phi_{B_q}\right) \left(n_1 + \frac{n_6 B_2 + n_{11}}{B_1}\right) - \frac{\cos\left(\phi_q^{\rm SM} + 2\phi_{B_q}\right)}{R_t^q} \left(n_2 + \frac{n_7 B_2 + n_{12}}{B_1}\right) + \frac{\cos\left(2(\phi_q^{\rm SM} + \phi_{B_q})\right)}{R_t^{q^2}} \left(n_3 + \frac{n_8 B_2 + n_{13}}{B_1}\right) + \cos\left(\phi_q^{\rm Pen} + 2\phi_{B_q}\right) C_q^{\rm Pen} \left(n_4 + n_9 \frac{B_2}{B_1}\right) - \cos\left(\phi_q^{\rm SM} + \phi_q^{\rm Pen} + 2\phi_{B_q}\right) \frac{C_q^{\rm Pen}}{R_t^q} \left(n_5 + n_{10} \frac{B_2}{B_1}\right) \right\}$$

	SM	SM+NP	exp
$10^3 \Delta \Gamma_d / \Gamma_d$	$2.8\pm2.7$	$2.0\pm1.8$	$9\pm37$
$\Delta \Gamma_s / \Gamma_s$	$0.10\pm0.06$	$0.00\pm0.08$	$0.25\pm0.09$

The experimental measurement of  $\Delta\Gamma_s$  actually measures  $\Delta\Gamma_s \cos(\beta_s + \phi_{Bs})$ (Dunietz et al., hep-ph/0012219)

→ NP can only decrease the experimental result with respect to the SM value

Since all the other parameters are fixed by other constraints, this gives the first available bound on NP phase in B<sub>s</sub> mixing!

![](_page_48_Figure_0.jpeg)

# Using all available constraints in NP generalized analysis

![](_page_49_Figure_1.jpeg)

Observable	ρ, η	$C_{Bd}, \phi_{Bd}$	C <sub>εK</sub>	$C_{Bs}, \phi_{Bs}$
V <sub>ub</sub> /V <sub>cb</sub>	X			
γ (DK)	X			
٤ <sub>K</sub>	X		X	
sin2β	X	X		
∆m <sub>d</sub>	X	X		
α (ρρ, ρπ, ππ)	X	X		
A <sub>SL</sub> B <sub>d</sub>	X	X		
$\Delta \Gamma_{d} / \Gamma_{d}$	X	X		
∆m <sub>s</sub>				X
A <sub>CH</sub>	X	X		X
$\Delta\Gamma_{\rm s}/\Gamma_{\rm s}$	X			X

ICHEP 06, Moscow, 28<sup>th</sup> July 2006

### MFV: Universal Unitarity Triangle using constraints Fit

Just using constraints which are insensitive to NP in MFV scenarios

ρ = 0.153 ± 0.030 (ρ = 0.166 ± 0.029 in SM)

![](_page_50_Figure_3.jpeg)

#### **Output of UUT fit**

Parameter	Output	Parameter	Output
$\overline{ ho}$	$0.162\pm0.033$	$\overline{\eta}$	$0.342 \pm 0.019$
$\alpha[^{\circ}]$	$92.9 \pm 5.3$	$\beta[^{\circ}]$	$22.2 \pm 1.0$
$\gamma[^\circ]$	$64.5\pm5.2$	$\sin 2eta$	$0.698 \pm 0.023$
$\sin 2\beta_s$	$0.037 \pm 0.002$	$\mathrm{Im}\lambda_{\mathrm{t}} \ [10^{-5}]$	$13.8\pm0.8$
$V_{ub}[10^{-3}]$	$3.69\pm0.15$	$V_{cb}[10^{-2}]$	$4.18\pm0.07$
$V_{td}[10^{-3}]$	$8.5\pm0.4$	$ V_{td}/V_{ts} $	$0.208 \pm 0.009$
$R_b$	$0.380 \pm 0.015$	$R_t$	$0.904 \pm 0.035$

In MFV extensions of the SM one can determine CKM parameters independently of NP constributions, but using angles, tree level processes and mixing amplitudes ratio

# MFV scenario: translating into a test of the NP scale

NP enters the game as additional contribution to the top box diagram (D'Ambrosio et al. hep-ph/0207036)

 $S_0(x_t) o S_0(x_t) + \delta S_0(x_t)$ 

Common shift  $\delta S^0$  to Inami-Lim fur in B and K mixing in case of small while two dinstict shifts for large t (bottom Yukawa coupling importa)

$$\delta S_0(x_t) = 4 a \left(rac{\Lambda_0}{\Lambda}
ight)^2$$

a = 1 (as a reference)  $\Lambda_0 = 2.4 \text{ TeV}$  $\Lambda_0$  is the equivalent SM scale

![](_page_51_Figure_6.jpeg)

### CONCLUSIONS

SM Predictions of Bayesian Analysis, using Lattice QCD confirmed by Experiments (sin 2  $\beta_{UTA}$  and  $\Delta m_s$ )

Extraordinary experimental progresses allow the extraction of several hadronic quantities from the data.

It is very important to reduce the lattice errors particularly for  $\mathsf{B}_{\mathsf{K}}$ 

A special effort must be done for the semileptonic form factors necessary to the extraction of V<sub>ub</sub>

It is crucial to reduce the error on the direct determination of the angle  $\gamma$ 

from B -> DK, D\*K and DK\* decays

# **PROGRESS SINCE 1988**

![](_page_53_Figure_1.jpeg)