

Towards an asymptotically safe model of electroweak interactions

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APPS 2011, Amsterdam

Based on: Fabbrichesi, Percacci, Townero, Zanusso PRD83,2011; Fabbrichesi, Percacci, Townero, Vecchi PRL107,2011; FB, Fabbrichesi, Percacci, Townero, Vecchi PLB705,2011; FB, Fabbrichesi, Percacci, Townero, Vecchi to appear.

Weinberg (1976)

- ▶ A quantum field theory that has a fixed point with a finite number of UV-attractive directions is said to be **asymptotically safe**
- ▶ The demanding that a theory is asymptotically free imposes constraints along the directions UV-repulsive and leave free parameters in the UV-attractive direction: **highly predictive**
- ▶ asymptotic safety may provide a **rationale** for picking acceptable quantum field theory more than demanding to a theory to be renormalizable

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Example...

$$\tilde{f} = kf$$

$$\frac{d\tilde{f}}{dt} = \tilde{f} - \frac{N}{64\pi^2} \tilde{f}^3$$

$$\tilde{f}^* = \pm \frac{8\pi}{\sqrt{N}}$$

UV-attractive

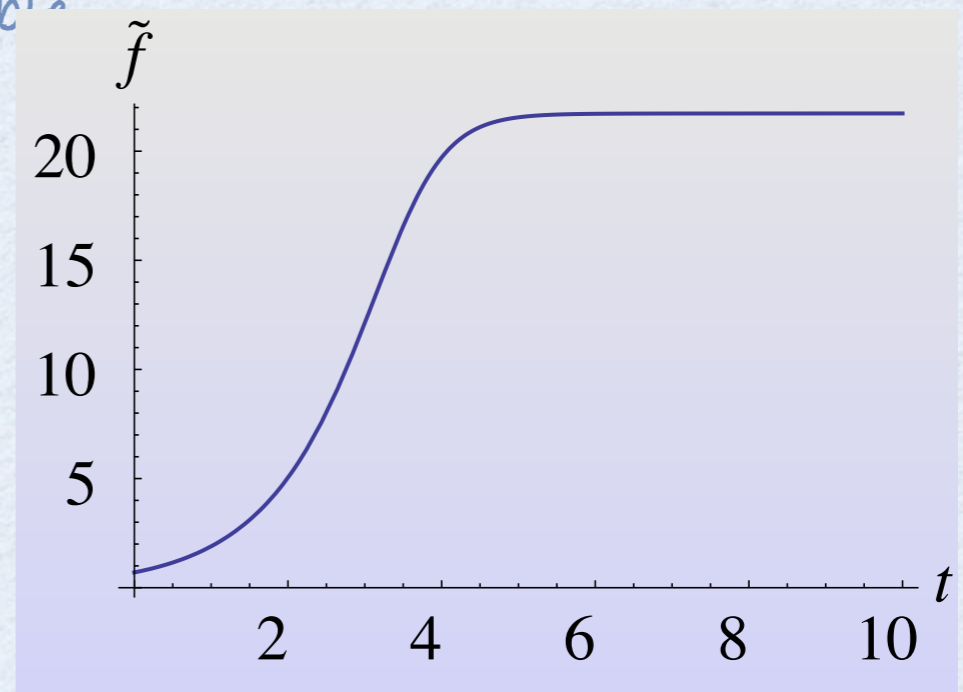
$$\tilde{f}^* = 0 \quad \text{UV-repulsive}$$

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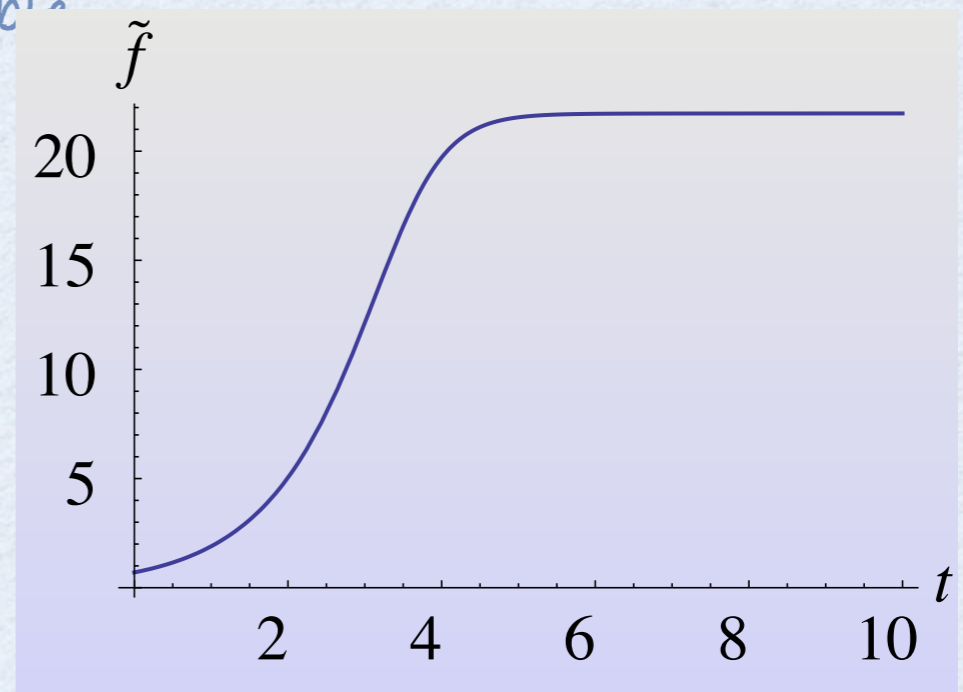


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drawback...

in the **RGE** evolution the theory may become strongly interacting thus non perturbatively. Perturbation theory maybe only a rough guide for a phenomenological approach

EW Non Linear Sigma Model

- ▶ Minimal realization of the SM: *only particles already discovered (NO HIGGS BOSON)*
- ▶ Fermions and gauge bosons couple to the Nambu-Goldstone bosons associated to the EW symmetry breaking
- ▶ It corresponds to take the limit of infinite mass of the higgs boson: *NLSM (so far no gauge)*

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A. Codello and R. Percacci, PLB 672 (2009) 280

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Real World...

- Gauge interactions
- EWPT?
- $pf > 1$ we should include higher order derivative terms $\mathcal{O}(p^4)$...
- Unitarity?
- Fermions

Assumptions:

- ▶ we use **perturbation theory** only as a rough guide
- ▶ one loop computations and analysis of the presence/consequence of UV-attractive FPs
- ▶ one loop results are **assumed** to hold at least qualitative in the non-perturbative solution
- ▶ when studying $O(p^4)$ operators and fermions we may "freeze" the gauge coupling and neglect them (they flow very slowly)

Gauging the NLSM

$$\frac{1}{f^2} \partial_\mu U^\dagger \partial^\mu U \quad \text{it has a } SU(2)_L \times SU(2)_R \text{ global symmetry} \quad U \rightarrow LUR^\dagger$$

$$\frac{1}{f^2} (D_\mu U)^\dagger D^\mu U \quad \text{we gauge } SU(2)_L \times U(1)_{Y=T_3R} \quad U \rightarrow LUR_3^\dagger$$

$$D_\mu U = \partial_\mu U + ig t^k W_\mu^k - ig' U t^3 B_\mu$$

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$$T = U(2t^3)U^\dagger$$

$$W_{\mu\nu} = t^k W_{\mu\nu}^k = \partial_\mu W_\nu - \partial_\nu W_\mu + ig[W_\mu, W_\nu]$$

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$$a_0 g^2 \frac{1}{f^2} [Tr(TV_\mu)]^2 + \frac{1}{2} a_1 g g' B_{\mu\nu} Tr(TW^{\mu\nu}) + \frac{1}{2} i a_2 g' B_{\mu\nu} Tr(T[V^\mu, V^\nu]) + i a_3 g Tr(W_{\mu\nu}[V^\mu, V^\nu])$$

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$$\underbrace{a_0 g^2}_{\text{controls } T} \frac{1}{f^2} [Tr(TV_\mu)]^2 + \underbrace{\frac{1}{2} a_1 g g'}_{\text{controls } S} B_{\mu\nu} Tr(TW^{\mu\nu}) + \frac{1}{2} i a_2 g' B_{\mu\nu} Tr(T[V^\mu, V^\nu]) + i a_3 g Tr(W_{\mu\nu}[V^\mu, V^\nu])$$

controls T

controls S

oblique parameters

$$T \propto [\Pi_{33}(0) - \Pi_{11}(0)]$$

$$S \propto [\Pi'_{33}(0) - \Pi'_{3B}(0)]$$

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$$g^2, g'^2 \ll \tilde{f}^2$$

$$\frac{dg^2}{dt} = -\frac{29}{2} \frac{g^4}{(4\pi)^2}$$

$$\frac{dg'^2}{dt} = \frac{1}{6} \frac{g'^4}{(4\pi)^2}$$

$$\frac{d\tilde{f}^2}{dt} = 2\tilde{f}^2 - \frac{1}{2} \frac{\tilde{f}^2}{(4\pi)^2} (\tilde{f}^2 a_0 (1 + 2a_0) + 6g^2 + 3g'^2)$$

$$\frac{da_0}{dt} = \frac{1}{2} \frac{1}{(4\pi)^2} (\tilde{f}^2 a_0 (1 - 2a_0) + \frac{3}{2} g'^2)$$

$$\frac{da_1}{dt} = \frac{1}{(4\pi)^2} (\tilde{f}^2 a_1 + \frac{1}{6})$$

FP	eigenvalue	eigenvector components		
		\tilde{f}	a_0	a_1
I	-1.99	1.00	11.6×10^{-6}	14.1×10^{-6}
I	1.99	-0.997	0.0795	-42.2×10^{-6}
I	3.98	0	0	1
II	-1.99	1.00	66.0×10^{-6}	29.9×10^{-6}
II	-0.996	-0.998	0.0563	-40×10^{-6}
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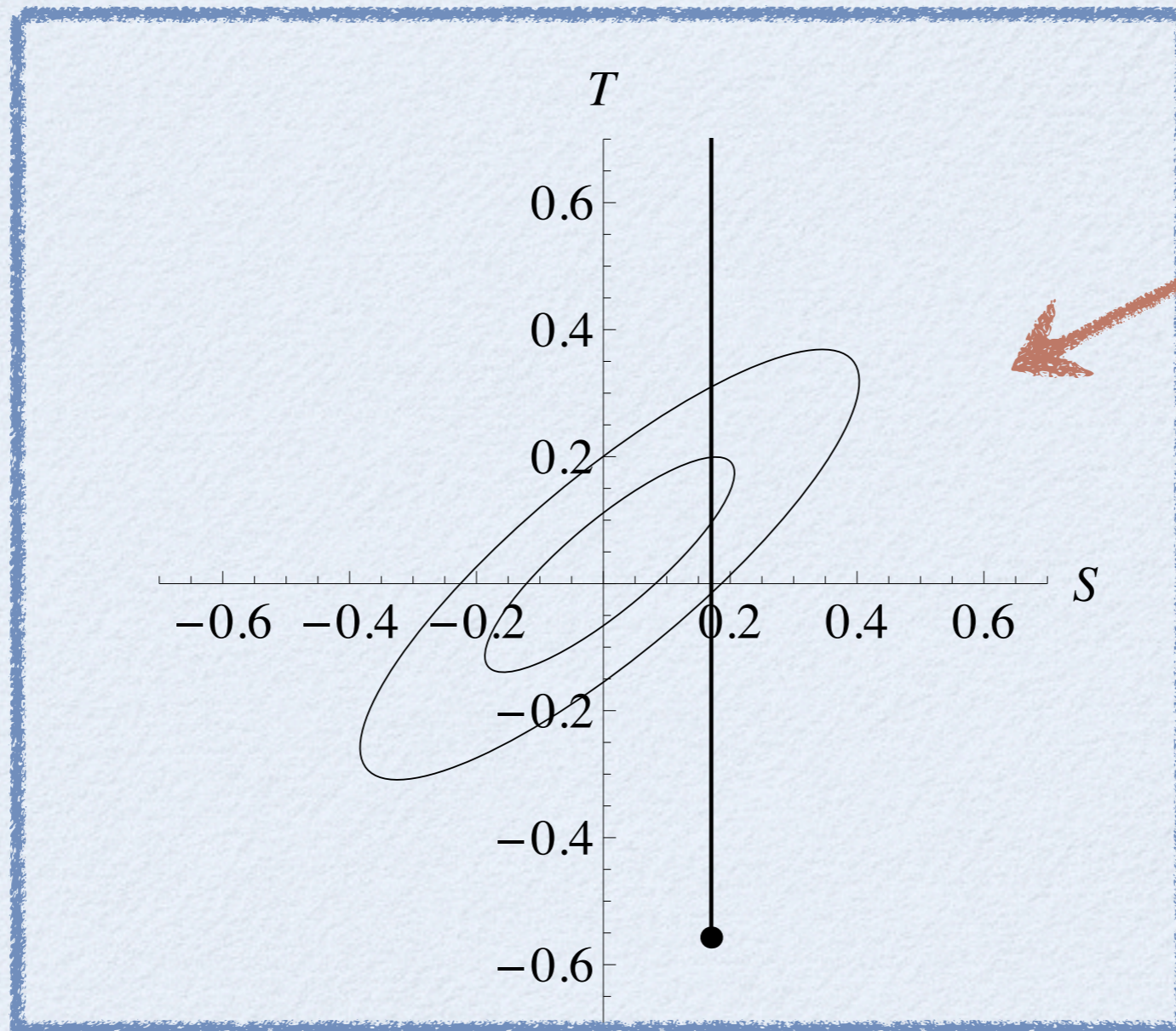
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UV repulsive, we have to fix it at the FP

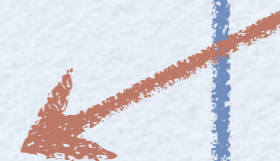
Gauging the NLSM

$$S = -16\pi a_1(m_Z) + \frac{1}{6\pi} \left[\frac{5}{12} - \log \left(\frac{m_H}{m_Z} \right) \right]$$

$$T = \frac{2}{\alpha_{em}} a_0(m_Z) - \frac{3}{8\pi \cos^2 \theta_W} \left[\frac{5}{12} - \log \left(\frac{m_H}{m_Z} \right) \right]$$



agreement with the
experimental bounds



Scattering amplitude and unitarity

$$A(\pi^i \pi^j \rightarrow \pi^k \pi^l) = A(s, t, u) \delta^{ij} \delta^{kl} + A(t, s, u) \delta^{ik} \delta^{jl} + A(u, s, t) \delta^{il} \delta^{jk}$$

isospin amplitudes
 $I=0,1,2$

$$\begin{cases} A_0(s, t, u) = 3A(s, t, u) + A(t, s, u) + A(u, s, t) \\ A_1(s, t, u) = A(t, s, u) - A(u, s, t) \\ A_2(s, t, u) = A(t, s, u) + A(u, s, t) \end{cases} \quad A(s, t, u) = s \frac{f^2}{4}$$

$$t_{IJ} = \frac{1}{64\pi} \int_{-1}^1 d\cos\theta P_J(\cos\theta) A_I(s, t, u) \quad \text{partial waves decomposition}$$

$$t_{00} = \frac{s f^2}{64\pi} = \frac{\tilde{f}^2}{64\pi} < \frac{1}{2} \quad \longrightarrow \quad N > 2\pi$$

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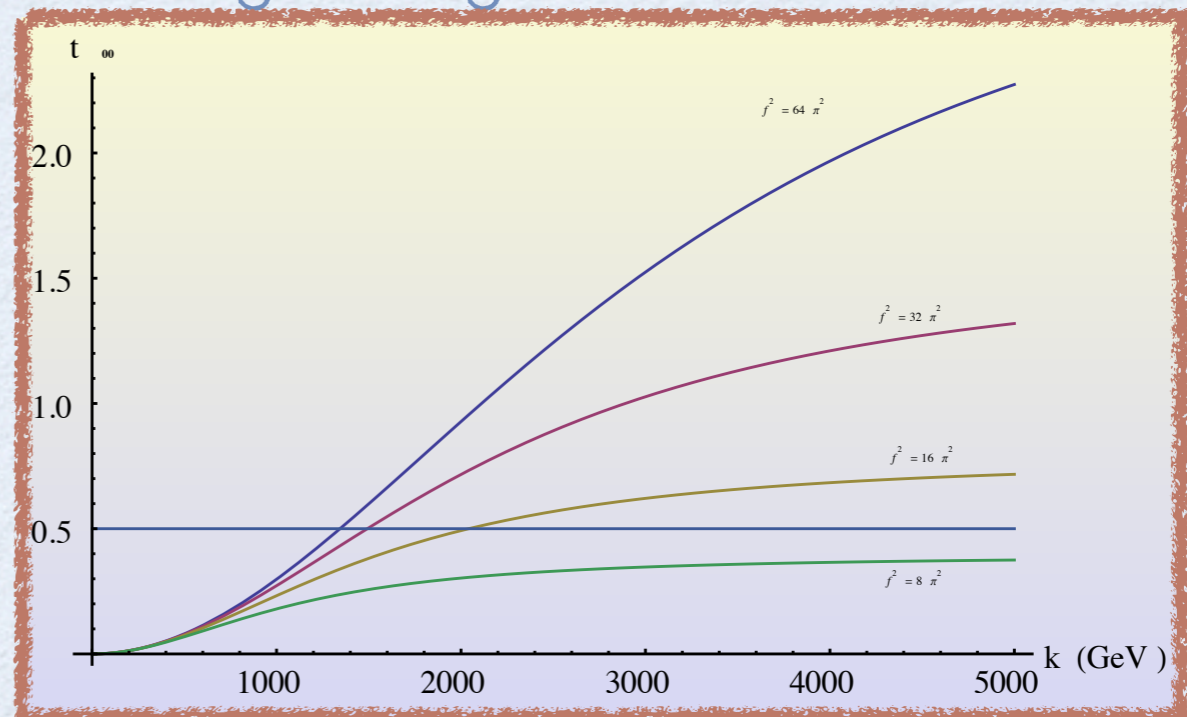
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for large N the NLSM does not violate unitarity, unfortunately EW symmetry has $N=2$, so...

$$\tilde{f}^* = \pm \frac{8\pi}{\sqrt{N}}$$



$\mathcal{O}(p^4)$ Resonances

$$a_4 [Tr(V_\mu V_\nu)]^2 + a_5 [Tr(V_\mu V^\mu)]^2$$



control the resonances

$$\frac{d\tilde{f}}{dt} = \tilde{f} - \frac{1}{4} \frac{\tilde{f}^3}{(4\pi)^2} - \frac{1}{6} \frac{\tilde{f}^5}{(4\pi)^2} (4a_4 + 7a_5)$$

$$\frac{da_4}{dt} = \frac{1}{12} \frac{1}{(4\pi)^2} \tilde{f}^2 (19a_4 + 10a_5) - \frac{1}{6} \frac{1}{(4\pi)^2} + \mathcal{O}(a_{4,5}^2 \tilde{f}^4)$$

$$\frac{da_5}{dt} = -\frac{1}{24} \frac{1}{(4\pi)^2} \tilde{f}^2 (22a_4 + 28a_5) - \frac{1}{12} \frac{1}{(4\pi)^2} + \mathcal{O}(a_{4,5}^2 \tilde{f}^4)$$

FP $\tilde{f}^* = 38.6, \quad a_4^* = 0.00016, \quad a_5^* = -0.00018$

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comparable to $O(p^6)$

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$\mathcal{O}(p^4)$ Resonances

IAM prescription

$$t_{00}^{(2)} = \frac{s f^2}{64\pi} = \frac{\tilde{f}^2}{64\pi} < \frac{1}{2}$$

$$t_{00}^{(4)} = \frac{s^2 f^4}{1024\pi} \left[\frac{16(11a_5 + 7a_4)}{3} + \frac{101/9 - 50 \log(s/\mu^2)/9 + 4i\pi}{16\pi^2} \right]$$

unitarized amplitude

$$t_{00}(s) = \frac{t_{00}^{(2)}}{1 - t_{00}^{(4)}/t_{00}^{(2)}} + \mathcal{O}(s^3)$$

the poles of the amplitude are interpreted as resonances



$$m_S^2 = \frac{12 v^2}{16 [11a_5(\mu) + 7a_4(\mu)] + \frac{101}{16\pi^2 \cdot 3}}$$

$$m_S \sim 600 \text{ GeV}$$

Preliminary!

Including the fermions

$$\mathcal{L}_\psi = \bar{\psi}_L i \gamma^\mu \partial_\mu \psi_L + \bar{\psi}_R i \gamma^\mu \partial_\mu \psi_R - \frac{2h}{f} (\bar{\psi}_L^a U \psi_R^a + H.c.)$$
$$m = \frac{2h}{f} = hv$$

Including the fermions

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Real World...

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- gauge interactions (no $SU(2)_R$)

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Real World...


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for the moment...

$$\frac{d\tilde{f}}{dt} = \tilde{f} - \frac{N}{64\pi^2} \tilde{f}^3 + \frac{N_c}{4\pi^2} h^2 \tilde{f}$$

$$\frac{dh}{dt} = \frac{1}{16\pi^2} \left(4N_c - 2\frac{N^2-1}{N} \right) h^3 + \frac{1}{64\pi^2} \frac{N^2-2}{N} h \tilde{f}^2$$

UV repulsive, FP not phenomenologically acceptable



Including fermions

$$\begin{aligned} \mathcal{L}_{\psi^4} = & \lambda_1 \left(\bar{\psi}_L^{ia} \psi_R^{ja} \bar{\psi}_R^{jb} \psi_L^{ib} \right) + \lambda_2 \left(\bar{\psi}_L^{ia} \psi_R^{jb} \bar{\psi}_R^{jb} \psi_L^{ia} \right) \\ & + \lambda_3 \left(\bar{\psi}_L^{ia} \gamma_\mu \psi_L^{ia} \bar{\psi}_L^{jb} \gamma^\mu \psi_L^{jb} + \bar{\psi}_R^{ia} \gamma_\mu \psi_R^{ia} \bar{\psi}_R^{jb} \gamma^\mu \psi_R^{jb} \right) \\ & + \lambda_4 \left(\bar{\psi}_L^{ia} \gamma_\mu \psi_L^{ib} \bar{\psi}_L^{jb} \gamma^\mu \psi_L^{ja} + \bar{\psi}_R^{ia} \gamma_\mu \psi_R^{ib} \bar{\psi}_R^{jb} \gamma^\mu \psi_R^{ja} \right) \end{aligned}$$

← dimensional parameters

$$\frac{d\tilde{f}}{dt} = \tilde{f} - \frac{1}{32\pi^2} \tilde{f}^3 + \frac{N_c}{4\pi^2} h^2 \tilde{f}$$

$$\frac{dh}{dt} = \frac{1}{16\pi^2} \left[4N_c - 3 + \frac{16}{\tilde{f}^2} (N_c \tilde{\lambda}_1 + \tilde{\lambda}_2) \right] h^3 + \frac{1}{64\pi^2} \left[\tilde{f}^2 - 16(N_c \tilde{\lambda}_1 + \tilde{\lambda}_2) \right] h$$

$$\frac{d\tilde{\lambda}_1}{dt} = 2\tilde{\lambda}_1 - \frac{1}{4\pi^2} \left[N_c \tilde{\lambda}_1^2 + \frac{3}{2} \tilde{\lambda}_1 \tilde{\lambda}_2 - 2\tilde{\lambda}_1 \tilde{\lambda}_3 - 4\tilde{\lambda}_1 \tilde{\lambda}_4 \right]$$

$$\frac{d\tilde{\lambda}_2}{dt} = 2\tilde{\lambda}_2 + \frac{1}{4\pi^2} \left[\frac{1}{4} \tilde{\lambda}_1^2 + 4\tilde{\lambda}_1 \tilde{\lambda}_3 + 2\tilde{\lambda}_1 \tilde{\lambda}_4 - \frac{3}{4} \tilde{\lambda}_2^2 + 2(2N_c + 1) \tilde{\lambda}_2 \tilde{\lambda}_3 + 2(N_c + 2) \tilde{\lambda}_2 \tilde{\lambda}_4 \right]$$

$$\frac{d\tilde{\lambda}_3}{dt} = 2\tilde{\lambda}_3 + \frac{1}{4\pi^2} \left[\frac{1}{4} \tilde{\lambda}_1 \tilde{\lambda}_2 + \frac{N_c}{8} \tilde{\lambda}_2^2 + (2N_c - 1) \tilde{\lambda}_3^2 + 2(N_c + 2) \tilde{\lambda}_3 \tilde{\lambda}_4 - 2\tilde{\lambda}_4^2 \right]$$

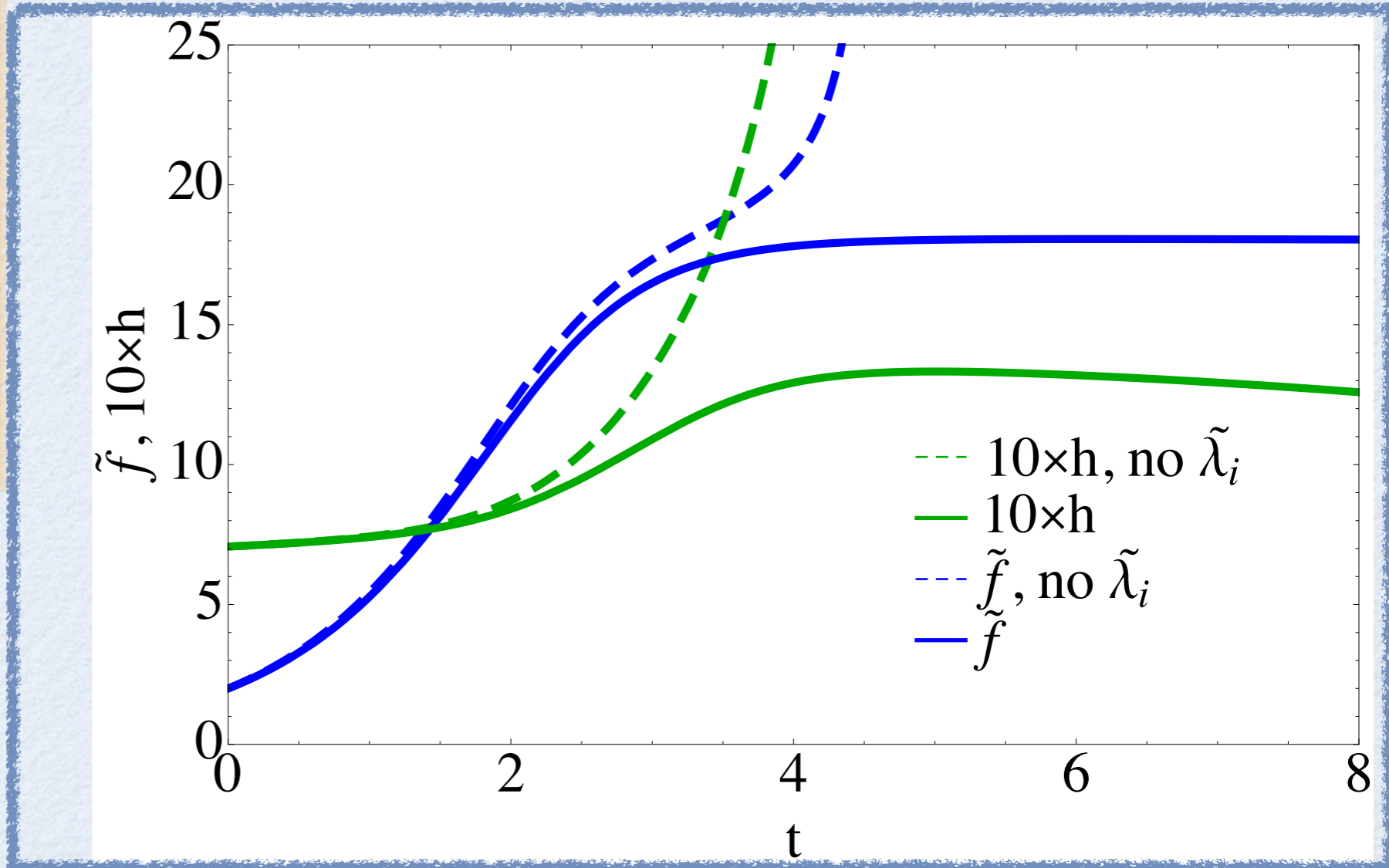
$$\frac{d\tilde{\lambda}_4}{dt} = 2\tilde{\lambda}_4 + \frac{1}{4\pi^2} \left[\frac{1}{8} \tilde{\lambda}_1^2 - 4\tilde{\lambda}_3 \tilde{\lambda}_4 + (N_c + 2) \tilde{\lambda}_4^2 \right].$$

Including fermions

	$\tilde{\lambda}_1$	$\tilde{\lambda}_2$	$\tilde{\lambda}_3$	$\tilde{\lambda}_4$	ϵ_h
fp0	0	0	0	0	0.5
fp1a	0	-28.71	-7.18	0	1.22
fp1b	0	0	7.85	-9.51	0.5
fp1c	0	25.61	-4.27	0	-0.15
fp1d	25.80	-1.77	0.19	-1.15	-1.42
fp2a	13.41	20.10	-3.80	-0.24	-1.03
fp2b	20.86	-3.56	7.04	-8.94	-1.00
fp2c	0	-36.55	2.34	-13.92	1.43
fp2d	0	0	-15.79	0	0.5
fp2e	37.17	-37.36	-8.43	-1.65	-1.38
fp2f	-2.92	32.59	4.67	-12.04	-0.10
fp3a	0.	31.67	4.67	-12.06	-0.30
fp3b	19.95	-8.59	-15.27	-0.36	-0.80
fp3c	31.22	-44.52	0.73	-13.38	-0.74
fp3d	-4.87	1.54	-5.42	-20.10	0.83
fp4	0	0	-5.42	-20.13	0.5

Including fermions

	$\tilde{\lambda}_1$	$\tilde{\lambda}_2$	$\tilde{\lambda}_3$	$\tilde{\lambda}_4$	ϵ_h
fp0	0	0	0	0	0.5
fp1a	0	-28.71	-7.18	0	1.22
fp1b	0	0	7.85	-9.51	0.5
fp1c	0	25.61	-4.27	0	-0.15
fp1d	25.80	-1.77	0.19	-1.15	-1.42
fp2a	13.41	20.10	-3.80	-0.24	-1.03
fp2b	20.86	-3.56	7.04	-8.94	-1.00
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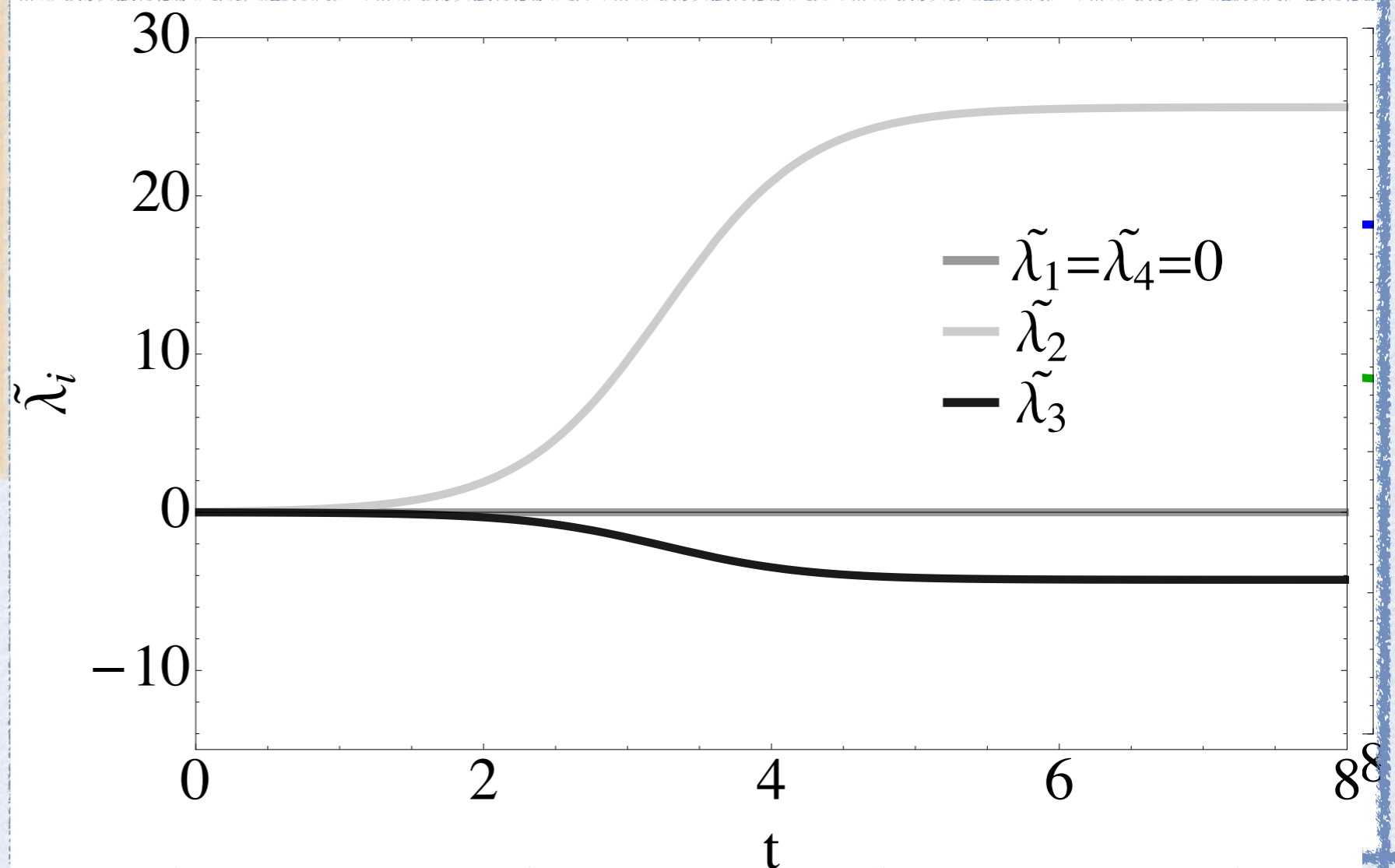


$$t = \log k/v$$

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Phenomenological constraints

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E. Eichten, K. D. Lane, M. E. Peskin, PRL 50 (1983) 811

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New J. Phys. 13 (2011) 053044

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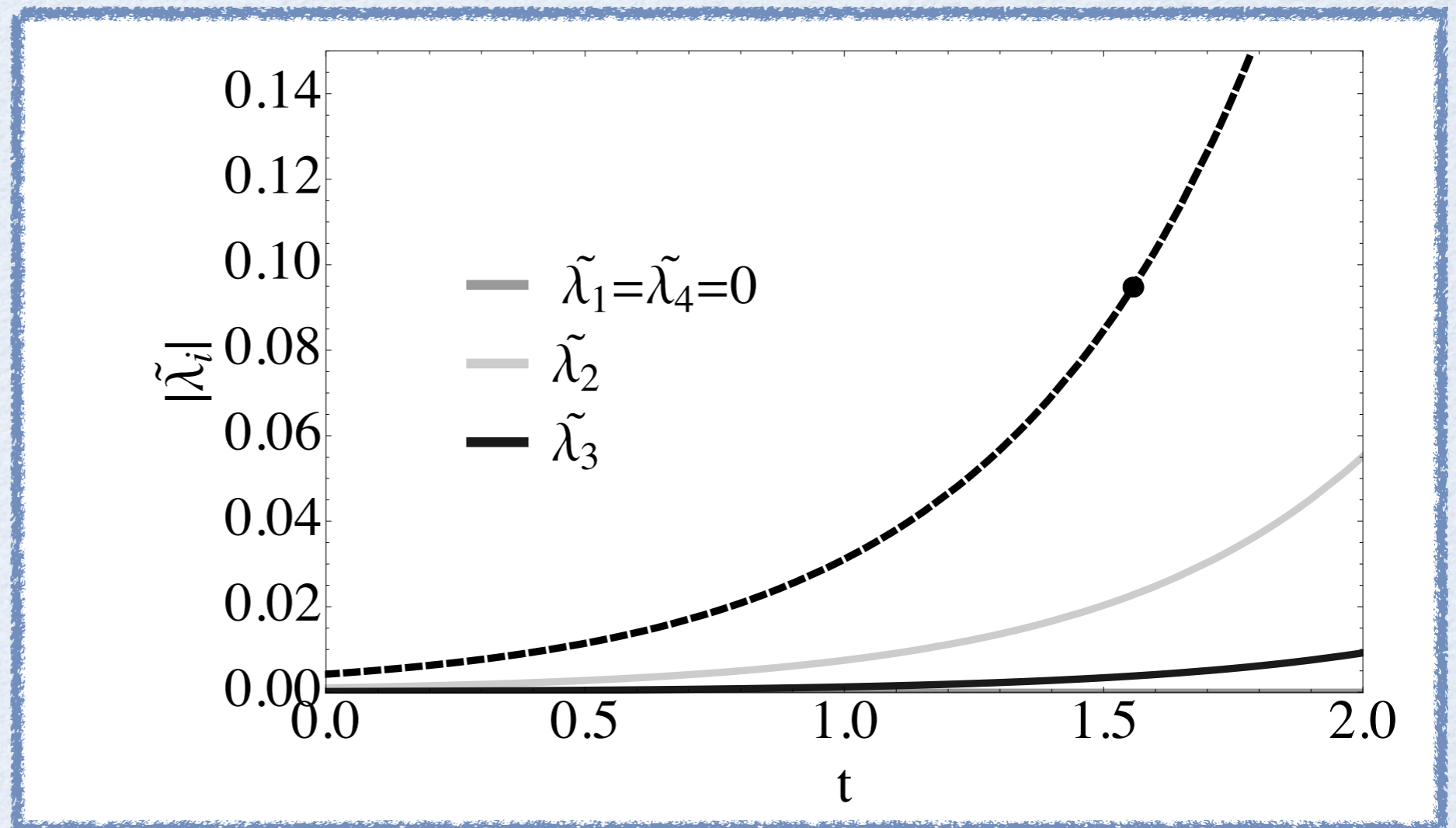
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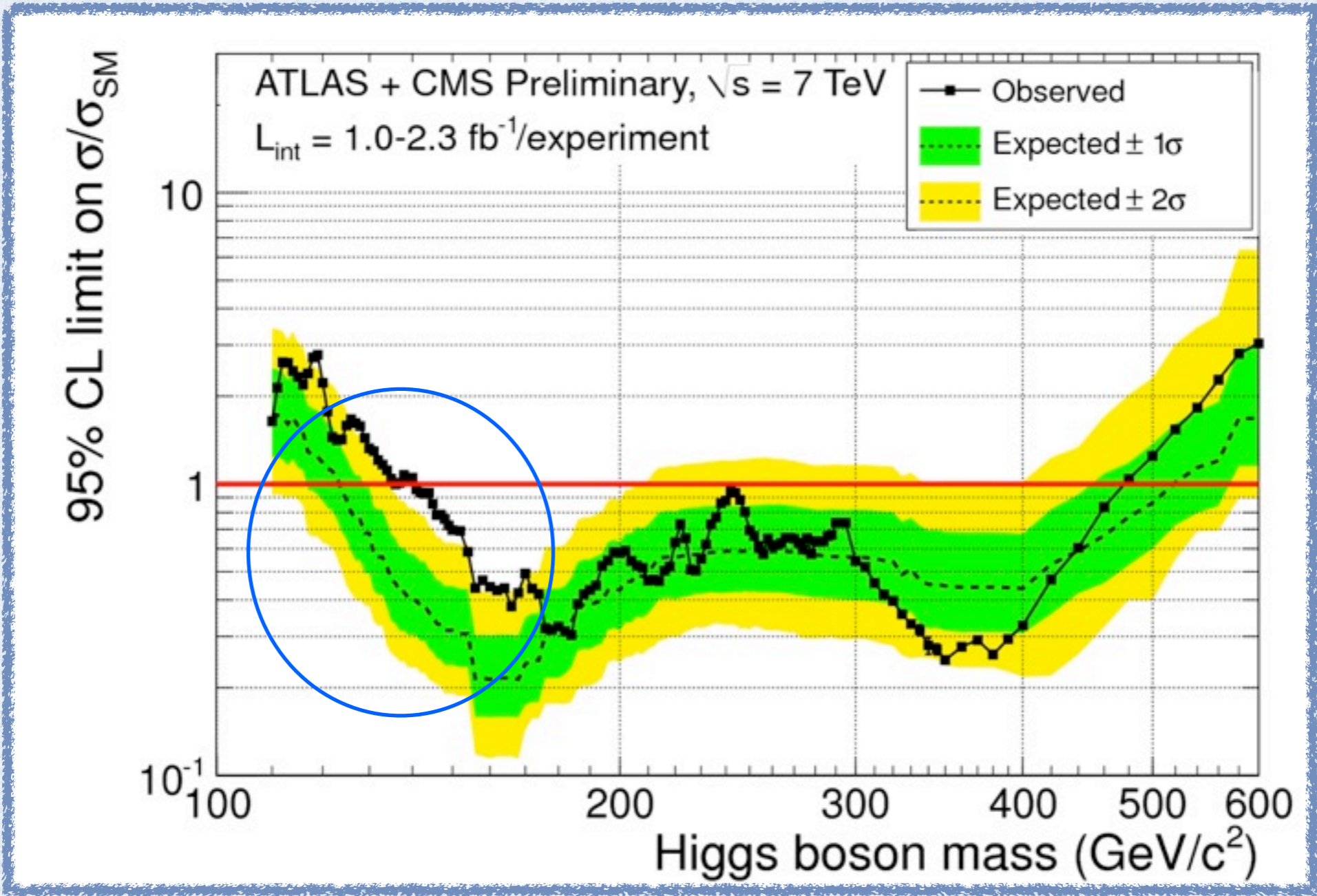
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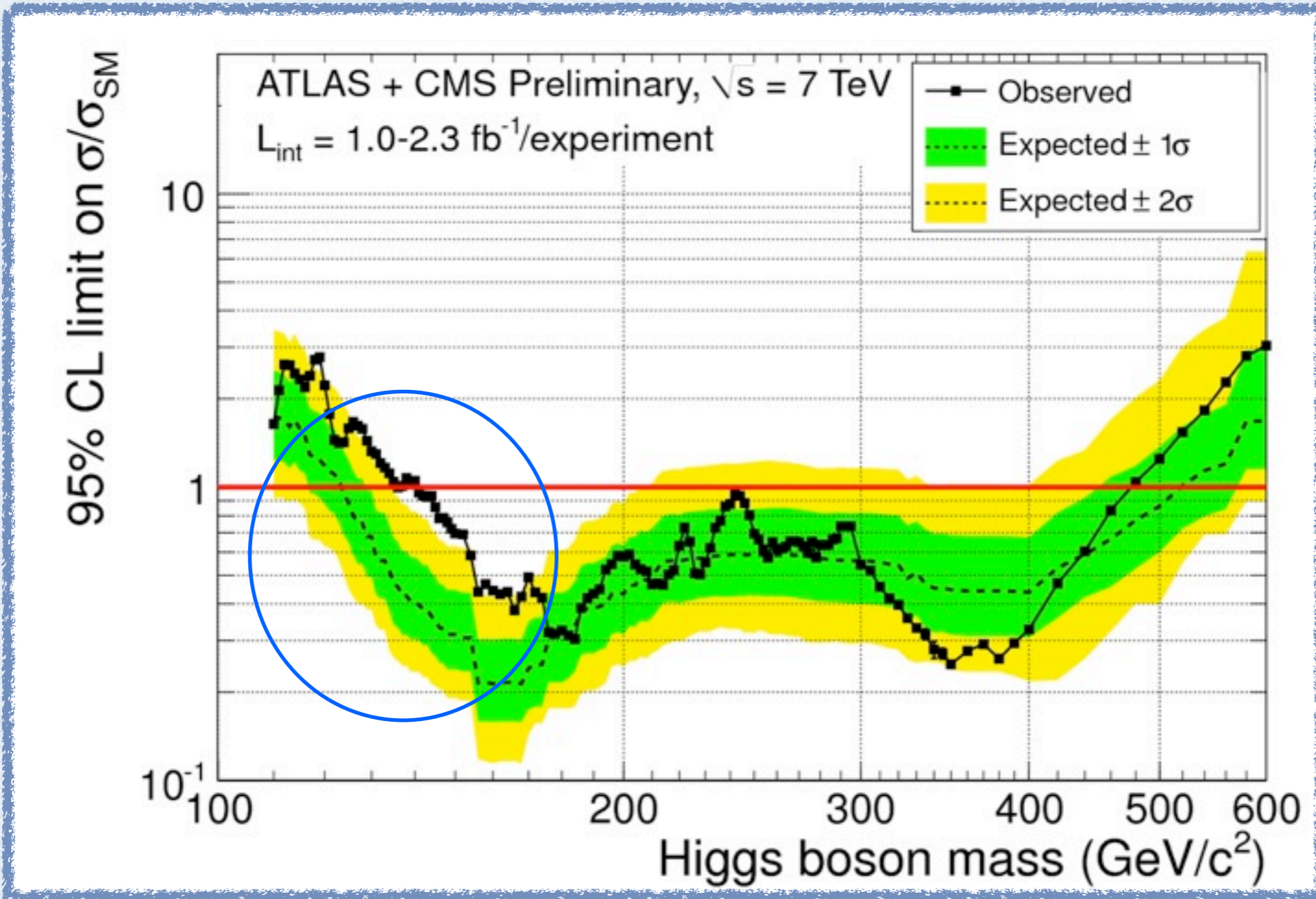
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Conclusions



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many efforts would spend into Higgs
reduced production, invisible decays,
non standard scenarios...

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- ▶ a scenario with **no Higgs boson** is a real possibility
- ▶ **asymptotic safe** description of EW interactions is competitive with other higgsless or composite framework
- ▶ **drawback**: we lack of satisfactory mathematical tools, perturbative computations are only a rough guide
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Thanks!