



# Observation of double charm production at LHCb

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On behalf of LHCb Collaboration

LHCb-PAPER-2012-003 (in preparation)





# Outline



**2×Charm**

**LHCb Detector & Data sample**

**Event Selection**

**2×Charm signals**

**Efficiency corrections**

**Systematics**

**Cross-sections & ratios**

**Properties of 2×Charm events**

**Conclusions**



# Heavy quark production in pp(gg)-collisions



LHC is LgC

- Open beauty & open charm :
  - "well known"
  - The measurements are in a reasonable agreement with *state-of-art* pQCD calculations
- Charmonium & bottomonium:
  - few open questions and puzzles
  - Polarization?
  - Color Singlet/CS vs Color Octet/CO
  - Recently very good progress with theory NNLO\*
- Double (charm)onia
  - Test for CO vs CS
  - $2 \times J/\psi$  is measured by
    - NA3 in 1982 [PLB 114 457, PLB 158, 85]
    - LHCb in 2011 [PLB 707 52]
  - LHCb measurement is in excellent agreement with pQCD calculations for
    - $gg \rightarrow 2 \times J/\psi$ 
      - $\sigma_{\text{LHCb}} = 5.1 \pm 1.0 \pm 1.1 \text{ nb}$
      - $\sigma_{\text{gg}} = 4 \text{ nb}$





# How to get 2xCharm?



- pQCD matrix elements  $gg \rightarrow 2 \times J/\psi$  and to  $gg \rightarrow c\bar{c}J/\psi$  and  $gg \rightarrow c\bar{c}c\bar{c}$ 
  - Agrees well for  $2 \times J/\psi$
- Intrinsic Charm:
  - Charm from (badly known) charm PDF
  - Lack of predictive power
- Double Parton Scattering
  - Simple paradigm with raising popularity

A.Berezhnoy *et al.*, [Phys Rev D57 4385 \(1998\)](#)

S.P.Baranov, [Phys Rev D73 074021 \(2000\)](#)

J.-P.Lansberg, [Eur.Phys.J. C61 693 \(2009\)](#)





# Double Parton Scattering

Google 240k documents



## [Double-Parton Scattering is Not Rare « Collider Blog](#)

[muon.wordpress.com/.../double-parton-scatt...](#) - Перевести эту страницу

29 Dec 2009 – The thrust of the Berger, Jackson and Shaughnessy paper is a study showing that clear evidence for **double-parton scattering** can be obtained ...

## [\[PDF\] Double Parton Scattering at the LHC –](#)

[moriond.in2p3.fr/QCD/2011/.../Berger.pdf](#) - Перевести эту страницу

Формат файлов: PDF/Adobe Acrobat - Быстрый просмотр

**Double Parton Scattering** at the LHC –. Dynamic and Kinematic Characteristics.

Example:  $pp \rightarrow b\bar{b}$  jet jet X. Edmond L Berger. Argonne National Laboratory ...

## [Phys. Rev. D 56, 3811 \(1997\): Double parton scattering in p\[over \]p ...](#)

[link.aps.org › ... › Volume 56 › Issue 7](#) - Перевести эту страницу

The process-independent parameter of **double parton scattering**,  $\sigma_{\text{eff}}$ , is obtained without reference to theoretical calculations by comparing observed DP events ...

## [Fresh look at double parton scattering - APS Link Manager](#)

[link.aps.org › ... › Volume 83 › Issue 11](#) - Перевести эту страницу

24 Jun 2011 – A revised formula for the inclusive cross section of a **double parton scattering** process in a hadron collision is suggested basing on the modified ...

## [Double Parton Scattering](#)

[www-cdf.fnal.gov/.../double\\_parton\\_summ...](#) - Перевести эту страницу

**Double Parton Scattering** in pbar-p Collisions at root  $s = 1.8$  TeV In a paper submitted to Physical Review Letters, the CDF collaboration announced the first ...

## [Signals for Double Parton Scattering at the Fermilab Tevatron](#)

[arxiv.org › hep-ph](#) - Перевести эту страницу

29 May 1996 – Abstract: Four **double-parton scattering** processes are examined at the Fermilab Tevatron energy. With optimized kinematical cuts and realistic ...

## [Double parton scattering of hadron-hadron interaction and its ...](#)

[arxiv.org › hep-ph](#) - Перевести эту страницу

25 Apr 1997 – Title: **Double parton scattering** of hadron-hadron interaction and its gluonic contribution. Authors: Hung Hsiang Liu (Inst. of Phys, Academia ...

## [\[PDF\] Signals for Double Parton](#)

[www.phys.psu.edu/~cteq/.../flaughter.pdf](#) - Перевести эту страницу

Формат файлов: PDF/Adobe Acrobat - Быстрый просмотр

**Double Parton Scattering** (DPS). Two parton-parton hard scatters in one pp collision. Extend knowledge of proton structure. 0 spatial distribution of partons inside ...

## [High Energy Physics Group - Double Parton Scattering](#)

[www.hep.phy.cam.ac.uk/theory/.../dps.html](#) - Перевести эту страницу

Cavendish High Energy Physics Group Research Theory **Double Parton Scattering**.

## [Is double parton scattering useful?](#)

[www.physicsforums.com/showthread.php?t...](#) - Перевести эту страницу

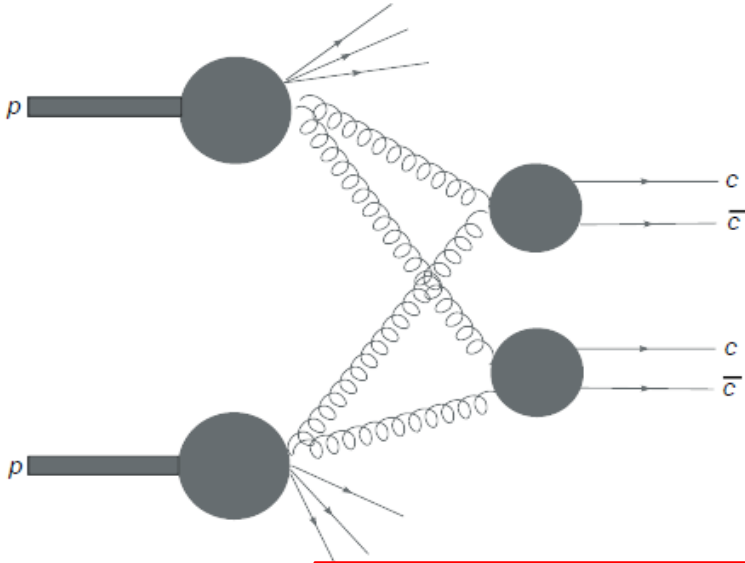
Заблокировать все результаты с [www.physicsforums.com](#)

Сообщений: 2 - Авторы: 2 - 19 июл 2011

Is **double parton scattering** useful? High Energy, Nuclear, Particle Physics discussion.



# DPS: simple paradigm



Two independent scattering processes  
Relations through (unknown)  $_2$ PDFs

$$\Gamma_{ij}(x_1, x_2; b_1, b_2; Q_1^2, Q_2^2) = D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) f(b_1) f(b_2),$$

Assume factorization of  $_2$ PDFs

$$D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_h^i(x_1; Q_1^2) D_h^j(x_2; Q_2^2).$$

(Can't be true for all  $x, Q^2$ )

Easy to make predictions!  
And the predictions are easy to test

$$\sigma_{\text{DPS}}^{AB} = \frac{m}{2} \frac{\sigma_{\text{SPS}}^A \sigma_{\text{SPS}}^B}{\sigma_{\text{eff}}}.$$

Universal (energy and process independent) factor

$$1/\sigma_{\text{eff}} = \int d^2b F^2(b)$$

$$\sigma_{\text{eff}}^{\text{DPS}} = 14.5 \pm 1.7_{-2.3}^{+1.7} \text{ mb}$$

CDF, F.Abe *et al.*, PDR 56 3811 (1997)



# 2×Charm as proton probe



- Intrinsic Charm Model:
  - we are testing/constraining (badly known) charm PDFs - typical uncertainties  $\times 2$
- Double Parton Scattering
  - Provide  $_2$ PDFs
  - Measure  $\sigma_{\text{eff}}$  - universal proton property





# 2×Charm @ LHCb



$$C = D^0, D^+, D_s, \Lambda_c$$

- We want to measure  $c\bar{c}c\bar{c}$

- $J/\psi C$  and  $CC$

- As bonus  $C\bar{C}$

- Dominated by the regular  $gg \rightarrow c\bar{c}$

- More information useful from correlations

- Gluon splitting, flavour creation, etc.

- Similar to CDF'2k+6

- In total 25 possible modes:

$$c\bar{c}c\bar{c} \quad (1 J/\psi J/\psi) + 4 J/\psi C + 10 CC$$

$$gg \rightarrow c\bar{c} \quad 10 C\bar{C}$$

$$2 < y_{J/\psi, C} < 4$$
$$3 < p_C^T < 12 \text{ GeV}/c$$
$$p_{J/\psi}^T < 12 \text{ GeV}/c$$



# Predictions for LHCb



| Mode                 | $\sigma_{gg}$        | $\sigma_{DPS}$  | $\sigma_{IC}$ |
|----------------------|----------------------|-----------------|---------------|
|                      | [nb]                 |                 |               |
| $J/\psi D^0$         | $10 \pm 6$           | $7.4 \pm 3.7$   | $146 \pm 39$  |
| $J/\psi D^+$         | $5 \pm 3$            | $2.6 \pm 1.3$   | $60 \pm 17$   |
| $J/\psi D_s^+$       | $1.0 \pm 0.8$        | $1.5 \pm 0.7$   | $24 \pm 7$    |
| $J/\psi \Lambda_c^+$ | $0.8 \pm 0.5$        | $0.9 \pm 0.5$   | —             |
|                      | [ $\mu b$ ]          |                 |               |
| $D^0 D^0$            | $\Sigma = 0.1 \mu b$ | $2.0 \pm 0.5$   | 1.5           |
| $D^0 D^+$            |                      | $1.7 \pm 0.4$   | 1.4           |
| $D^0 D_s^+$          |                      | $0.65 \pm 0.15$ | 0.4           |
| $D^0 \Lambda_c^+$    |                      | $1.5 \pm 0.5$   | 1.4           |
| $D^+ D^+$            |                      | $0.34 \pm 0.09$ | 0.3           |
| $D^+ D_s^+$          |                      | $0.27 \pm 0.07$ | 0.2           |
| $D^+ \Lambda_c^+$    |                      | $0.64 \pm 0.23$ |               |

$\sigma_{gg}$   
A.Berezhnoy *et al.*, [Phys Rev D57 4385 \(1998\)](#)  
S.P.Baranov, [Phys Rev D73 074021 \(2000\)](#)  
J.-P.Lansberg, [Eur.Phys.J. C61 693 \(2009\)](#)

$\sigma_{DPS}$   
based on LHCb measurements of  
 $\sigma_{J/\psi}$  [EPJ C71 1645]  
 $\sigma_C$  [LHCb-CONF-2010-013]

C.H.Kom, A.Kulesza & J.W.Stirling,  
[Phys.Rev.Lett. 107 082002 \(2011\)](#)  
S.P.Baranov, A.M.Snigirev and N.P.Zotov,  
[Phys.Lett. B705 116 \(2011\)](#)  
A.Novoselov, [arXiv:1105.62076](#)  
M.Luszczak, R.Maciula, A.Szczurek,  
[arXiv:1111.3255](#)

$\sigma_{IC}$   
based on Alekhin's PDFs  
S.Alekhin, PRD68 014002



**2×Charm**  
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# How to measure $2 \times \text{Charm}$ ?



- Need excellent detector:
  - Track reconstruction and momentum resolution
  - Hadron identification
  - Muon identification
  - Vertex/lifetime/impact parameter resolution
  - Efficient trigger for muons and hadrons
- Need high statistics...

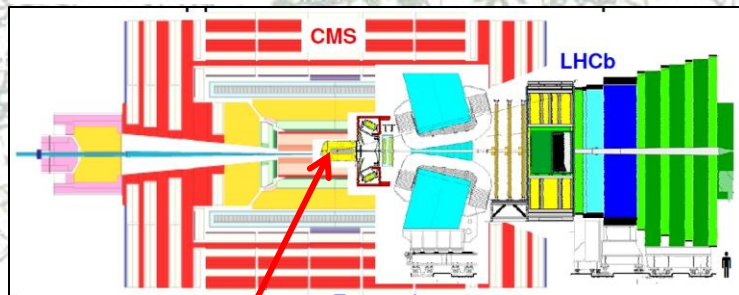
Natural choice: LHCb at LHC



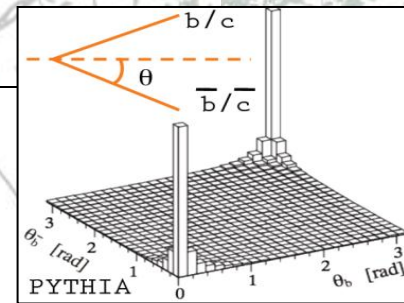
# LHCb: beauty detector



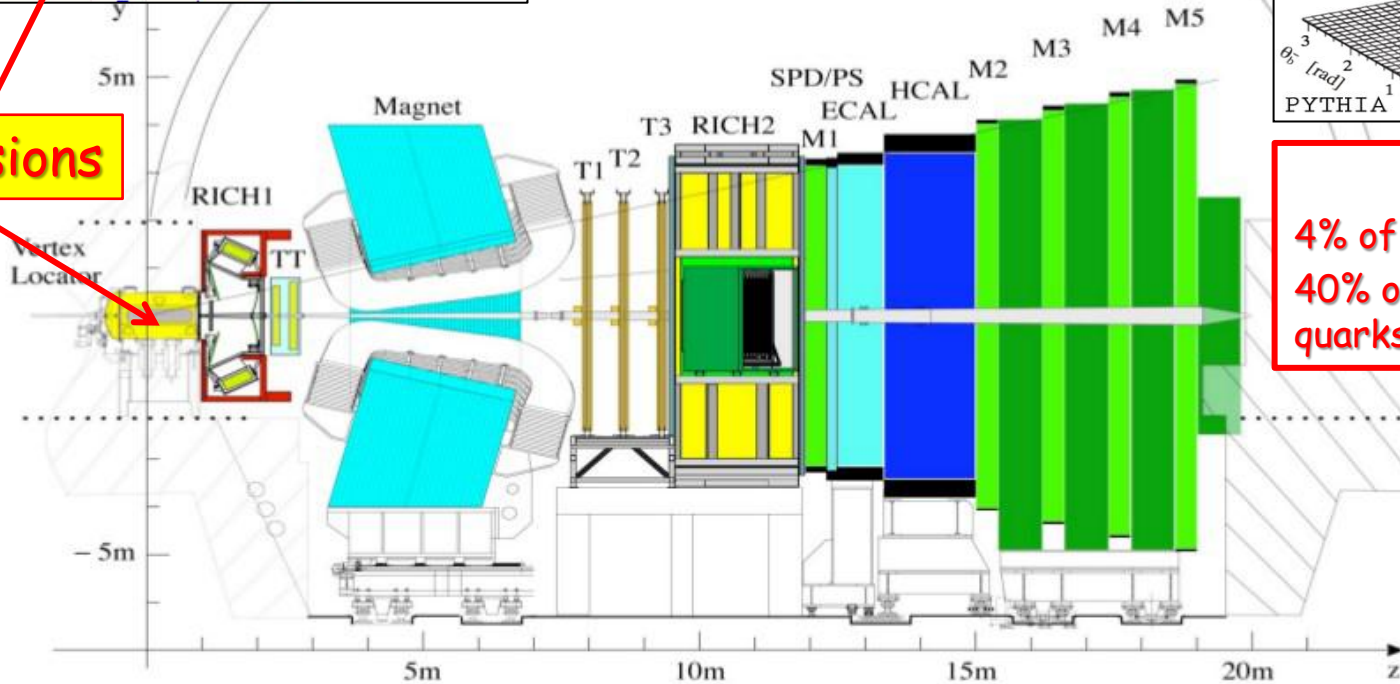
General purpose universal detector in forward region



pp-collisions



$2 < \eta < 5$   
4% of solid angle  
40% of heavy quarks

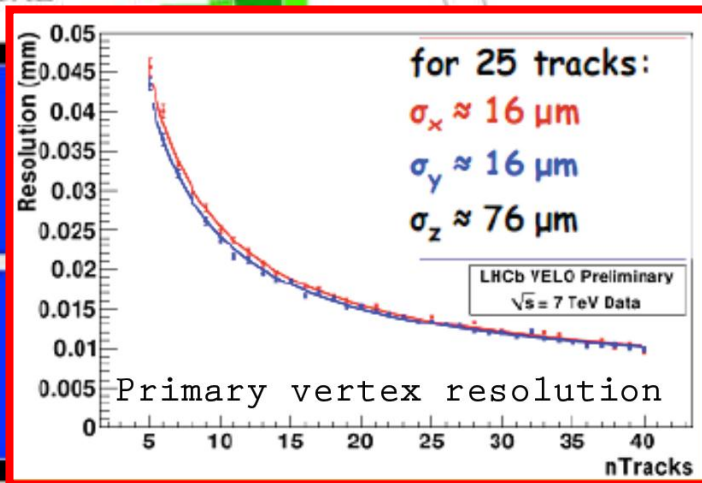
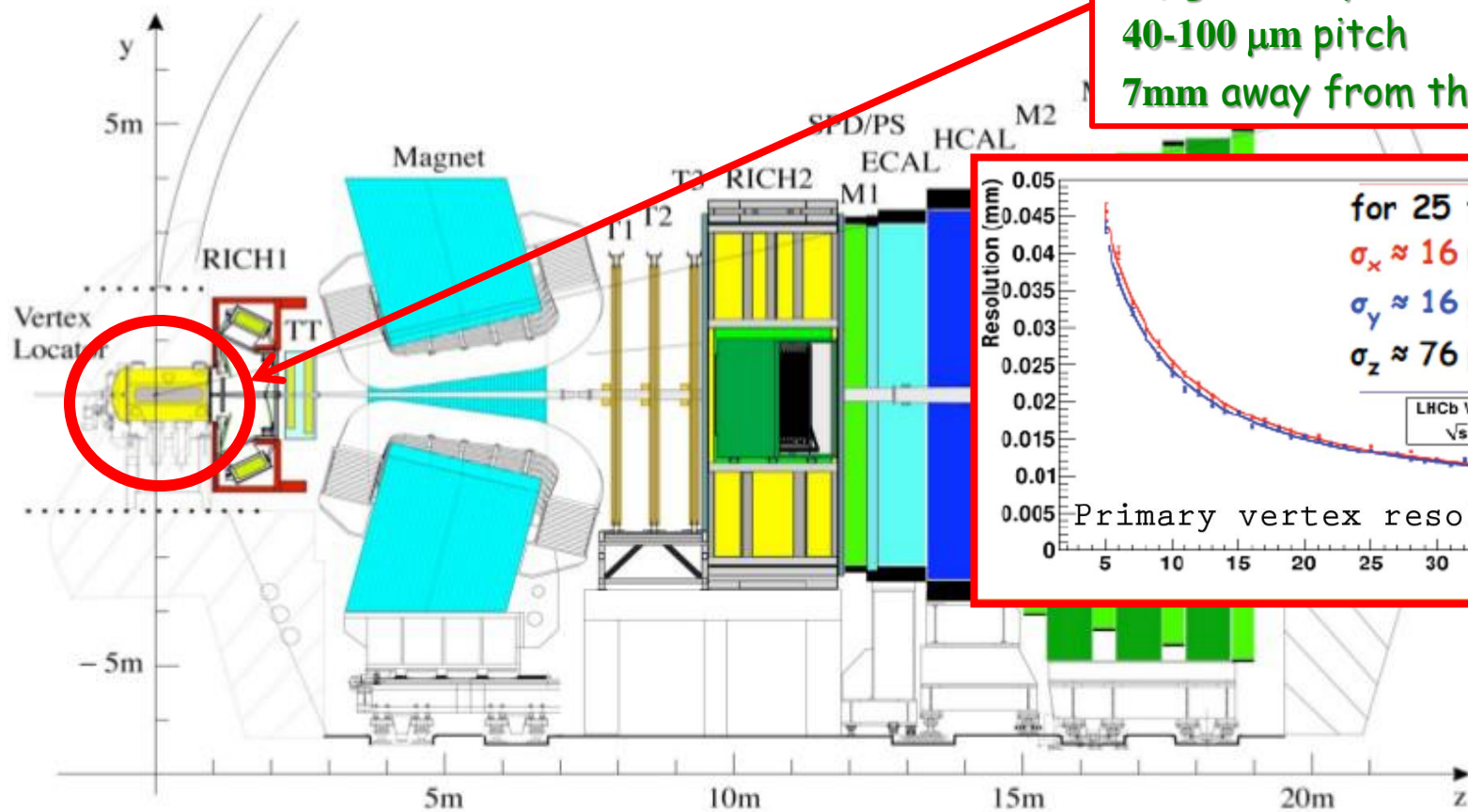




# VELO



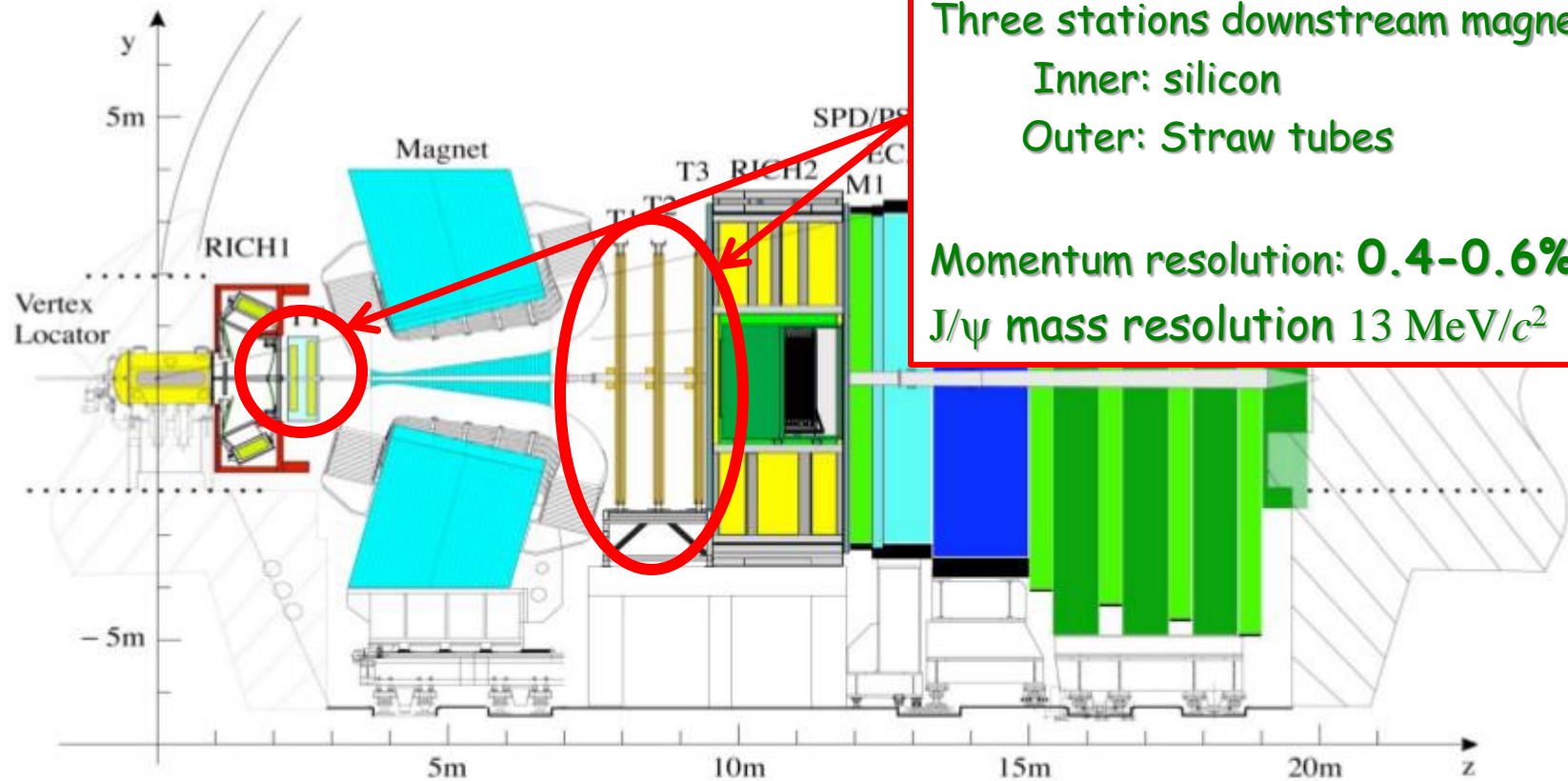
42×2 silicon strip planes  
r- $\phi$  geometry  
40-100  $\mu\text{m}$  pitch  
7mm away from the beam







# Tracking system



Two silicon stations upstream magnet  
Dipole magnet 4Tm  
Three stations downstream magnet  
Inner: silicon  
Outer: Straw tubes

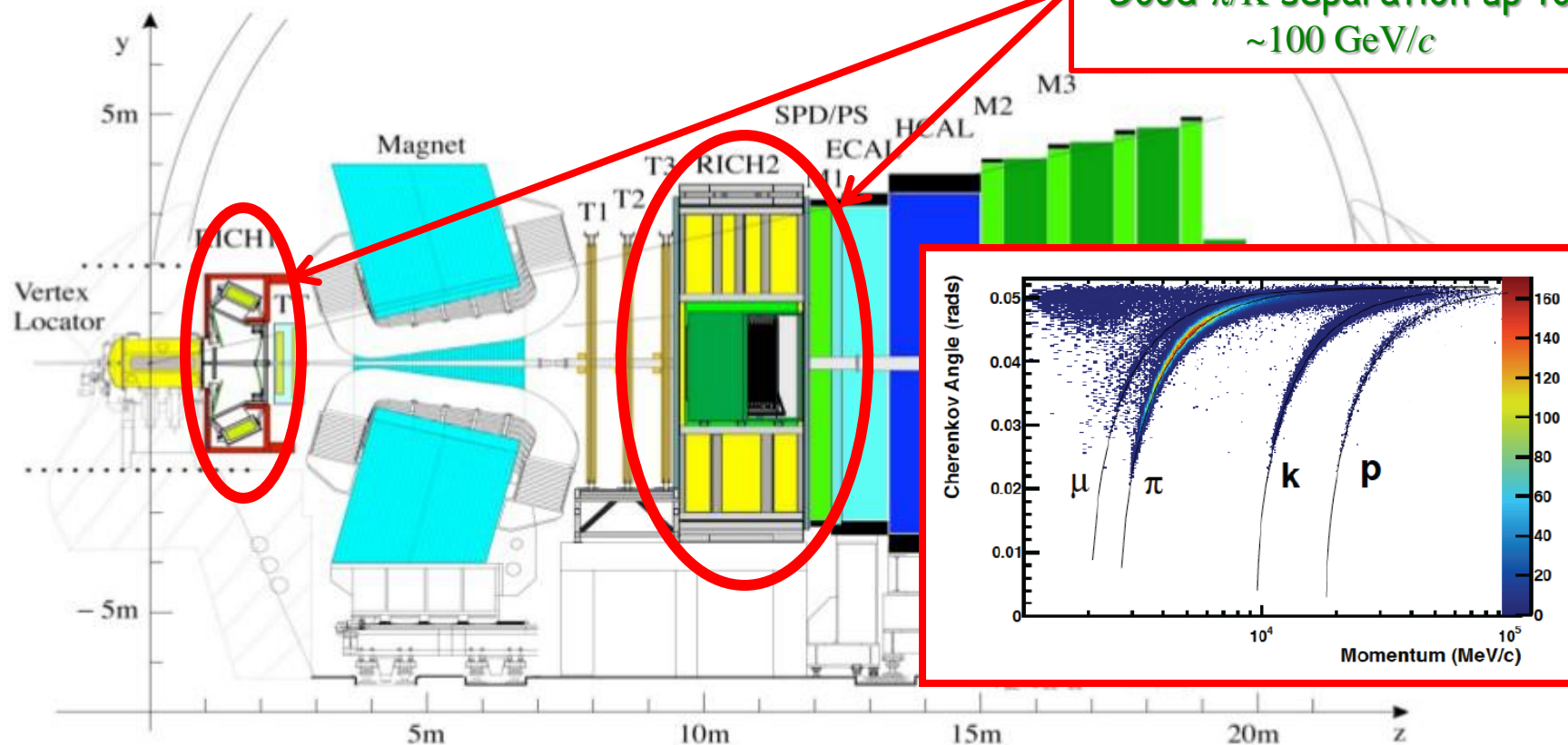
Momentum resolution: **0.4-0.6%**  
 $J/\psi$  mass resolution  $13 \text{ MeV}/c^2$



# Hadron ID



Two RICH detectors  
Good  $\pi/K$  separation up to  
 $\sim 100 \text{ GeV}/c$

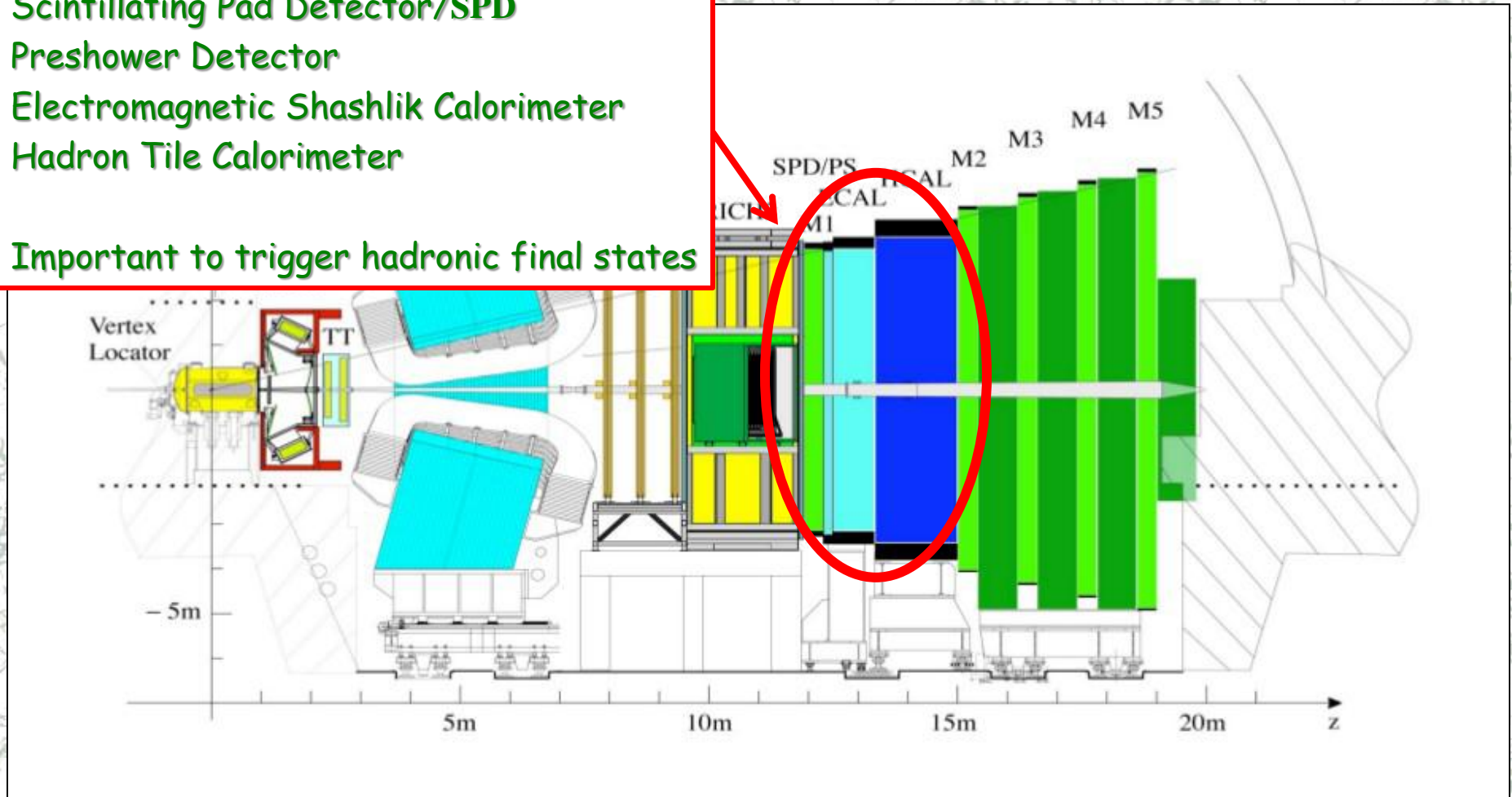




# Calorimeter system

Scintillating Pad Detector/SPD  
Preshower Detector  
Electromagnetic Shashlik Calorimeter  
Hadron Tile Calorimeter

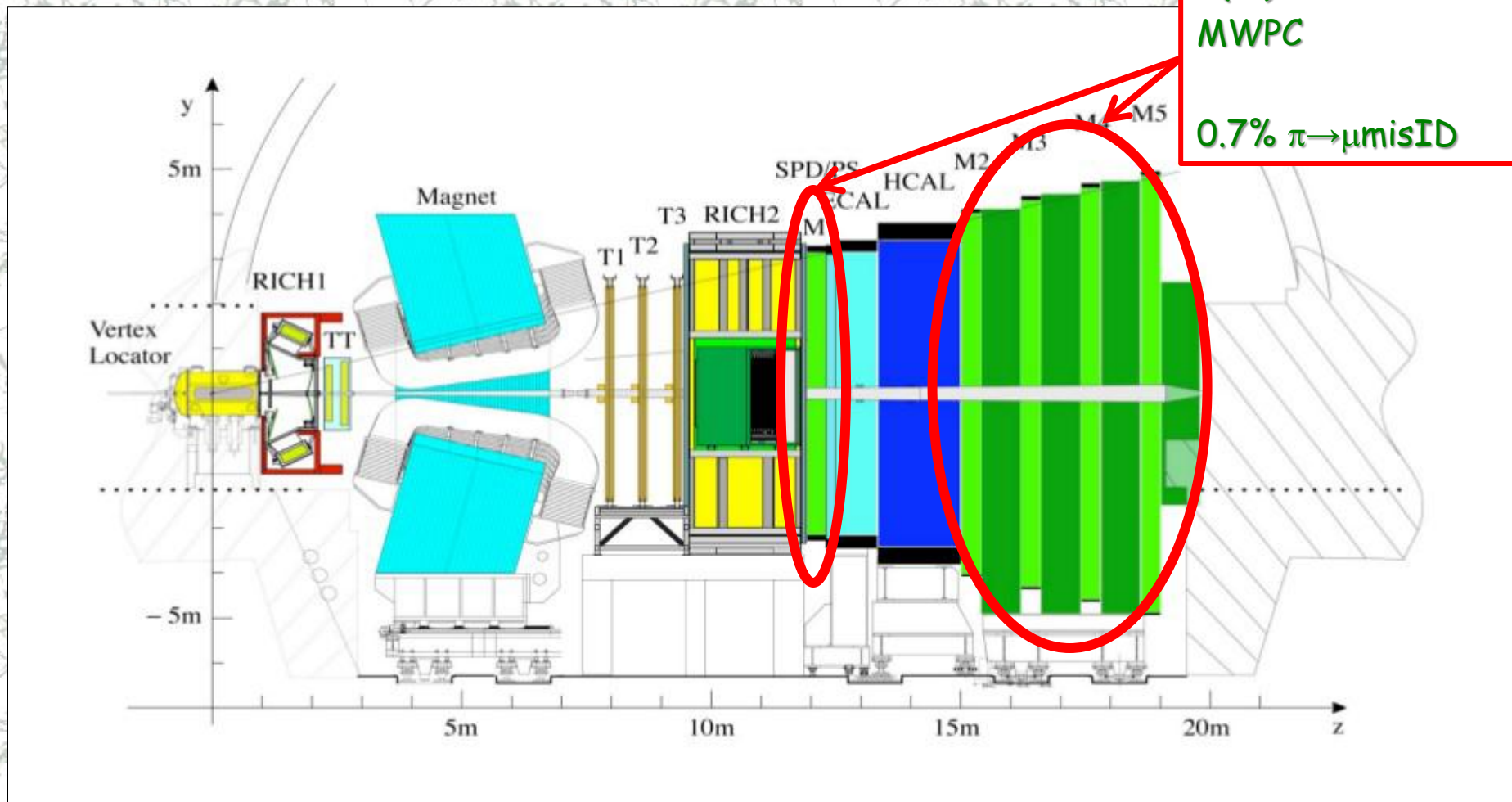
Important to trigger hadronic final states







# Muon system





# Trigger



## IO hardware

- high- $p^T$   $\mu$ ,  $2\mu$ ,  $h$ ,  $e^\pm$ ,  $\gamma$

## Software H1t1

- Reconstruct  $\mu$ ,  $2\mu$ ,  $h$
- cut on IP,  $p^T$ , mass

## Software H1t2

- Full reconstruction of  $J/\psi$
- Full reconstruction of open charm hadrons

10 MHz

1 MHz

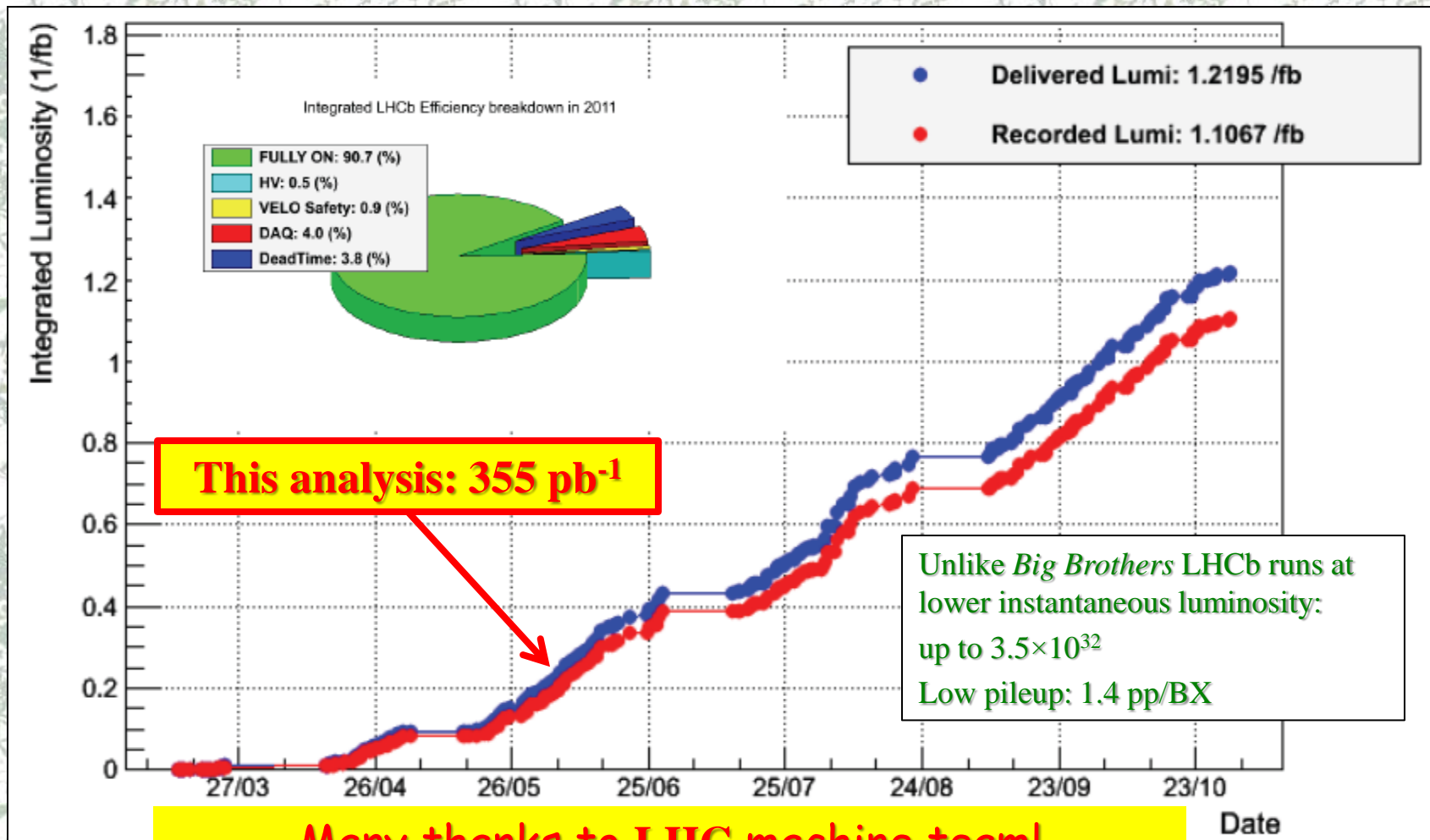
50 kHz

3 kHz

DAQ records information needed for off-line trigger matching, allowing determination of trigger efficiency directly from data



Lumi'2k+11 1.1fb<sup>-1</sup> recorded at  $\sqrt{s}=7\text{TeV}$



Many thanks to LHC machine team!





**2×Charm**  
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**2×Charm signals**  
**Efficiency corrections**  
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# Analysis strategy



- Determine the *model independent* cross-sections in LHCb fiducial volume

- Reconstruct prompt charm hadrons:

$$J/\psi \rightarrow \mu^+ \mu^-$$

$$D^0 \rightarrow K^- \pi^+, D^+ \rightarrow K^- \pi^+ \pi^+, D_s \rightarrow (K^+ K^-)_\phi \pi^+, \Lambda_c \rightarrow p^+ K^- \pi^+$$

- Take care about background and keep track on efficiency determination

- Use *sPlot* technique for background subtraction
- Use *per-event* efficiency correction
- Extract efficiencies from data (when possible)

$$2 < y < 4$$

$$3 < p_C^T < 12 \text{ GeV}/c$$

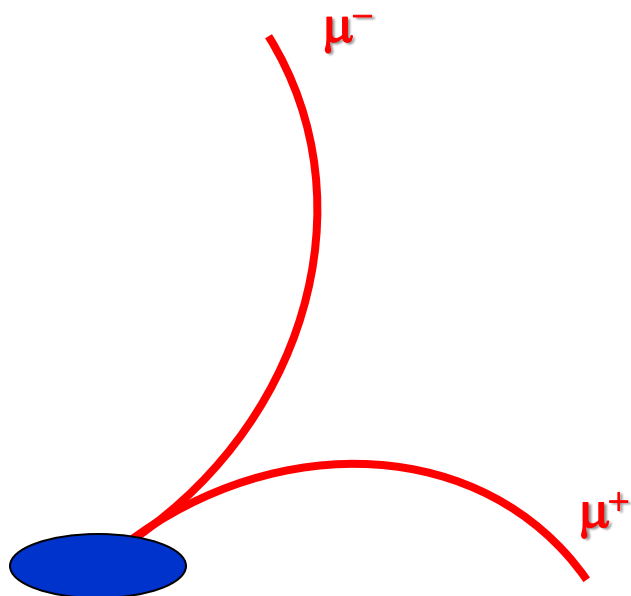
$$p_{J/\psi}^T < 12 \text{ GeV}/c$$



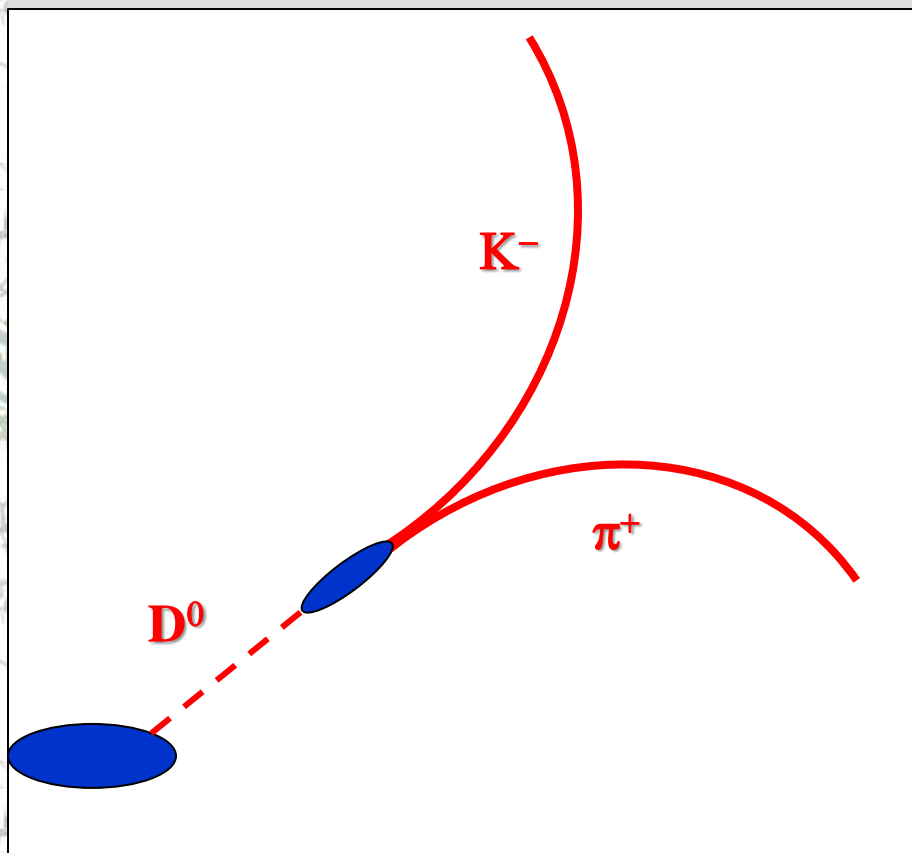
# Event Selection



$J/\psi$  two muons in common  
PV vertex



Open charm hadrons



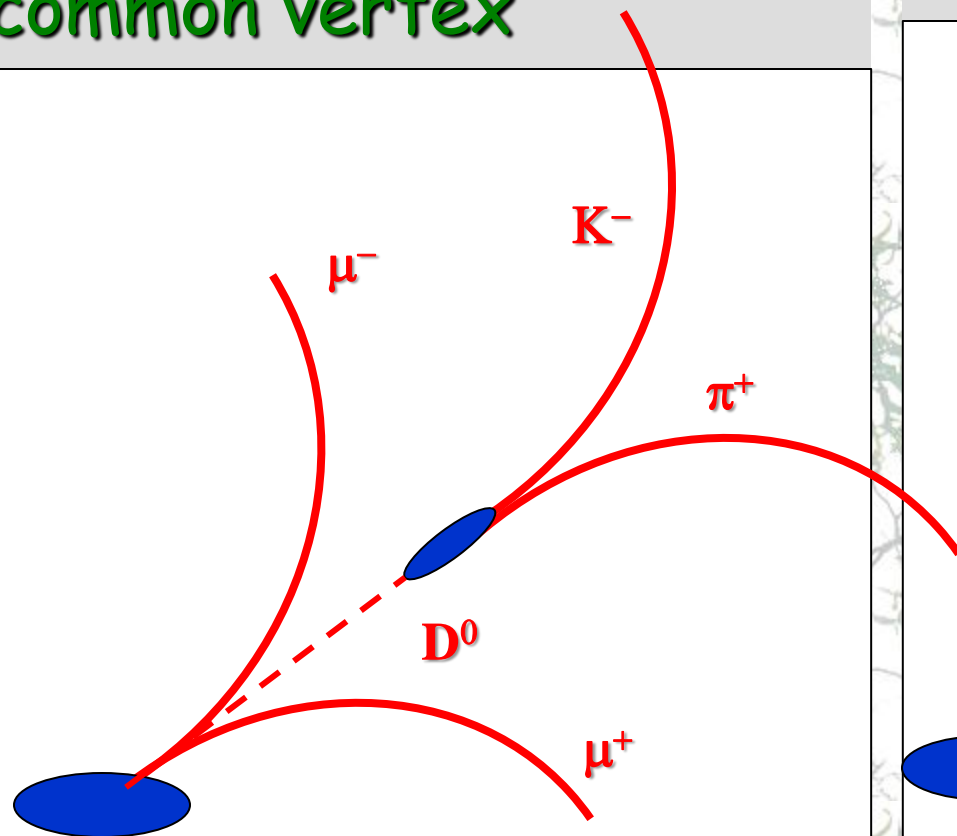




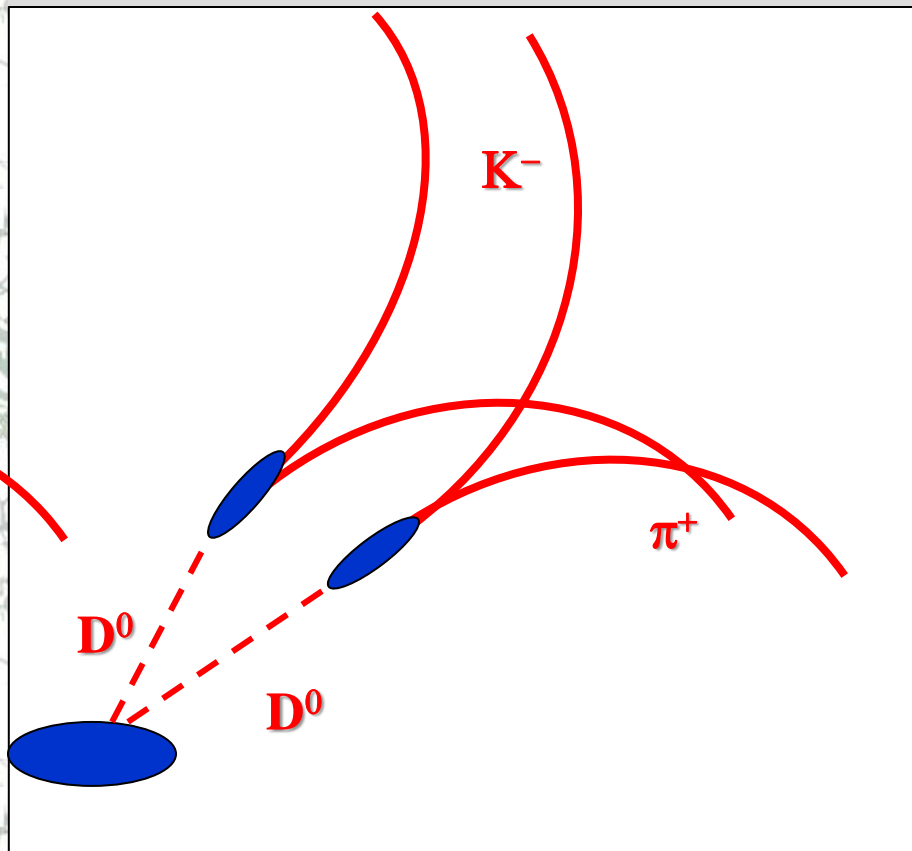
# Event Selection



$J/\psi C$  two charm with  
common vertex



2×Open charm hadrons





# Charm hadron reconstruction



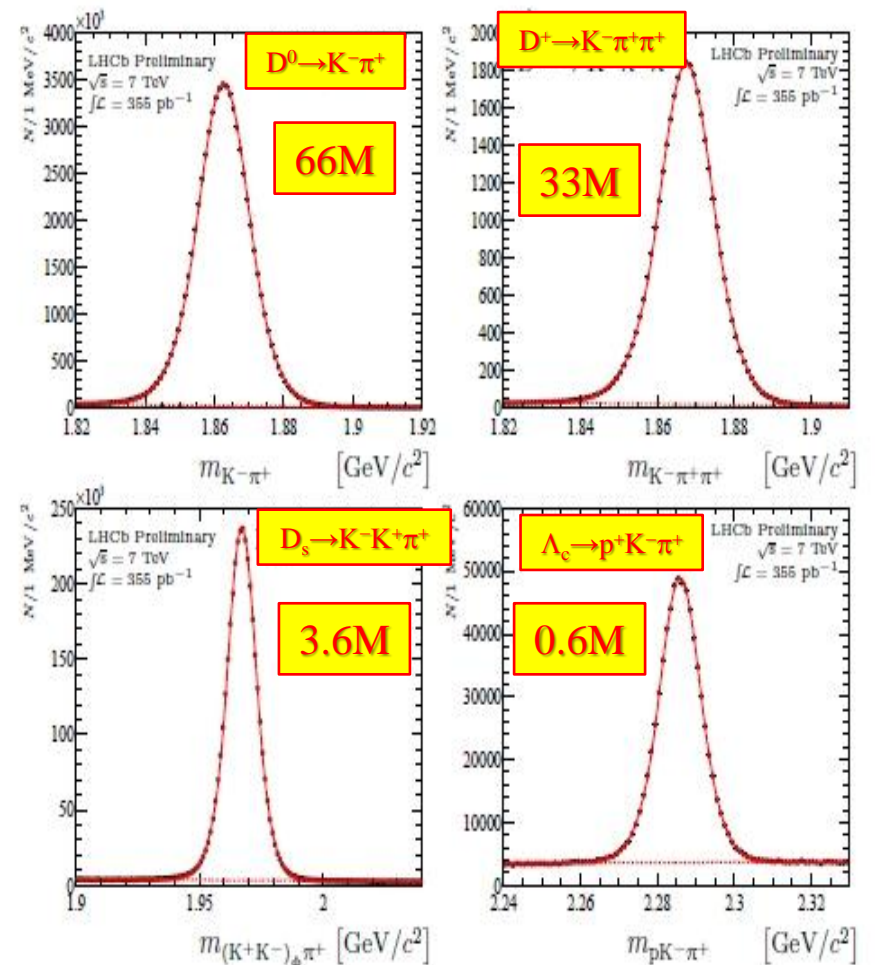
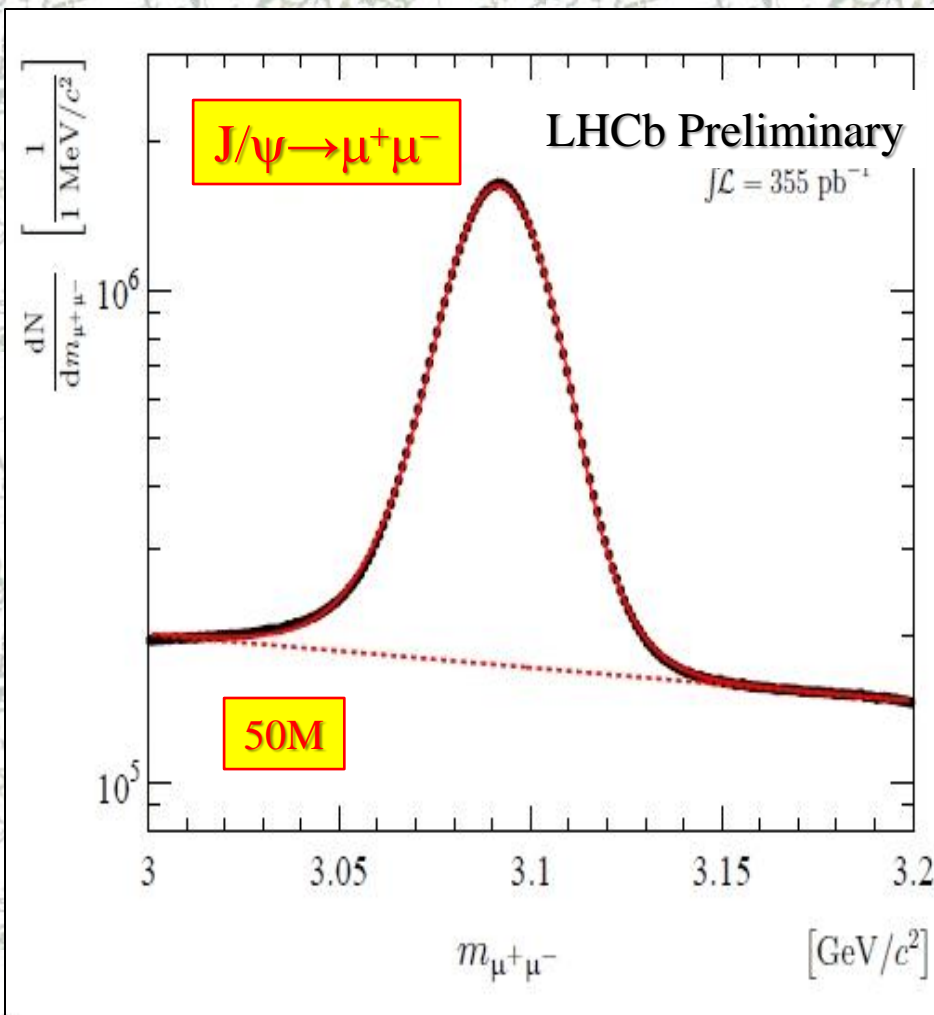
- Start from good quality tracks
- Apply positive PID  
 $\mu, K, \pi, p$
- Vertex quality cuts
- PV & *decay consistency*
- $c\tau$  cut for open charm hadrons
- As similar as possible (a bit tighter for  $\Lambda_c$ )

## " $3\sigma$ mantra"

- Daughter particles do not point to PV ( $>3\sigma$ )
- Mother particle does point to PV ( $<3\sigma$ )
- Mother particle has non-zero lifetime (except  $J/\psi$ )
- The decay structure is self-consistent



# Charm hadrons







## 2×Charm



- Require both hadrons consistent with the same PV - the only one cut  $\chi^2_{\text{fit}}(C_1 C_2)/\text{ndf} < 5$
- By construction: 100% efficiency for signal:
  - $\chi^2_{\text{fit}}(C_1 C_2) = \chi^2_{\text{fit}}(C_1) + \chi^2_{\text{fit}}(C_2)$
  - $\chi^2_{\text{fit}}(C_1)/\text{ndf} < 5$  &  $\chi^2_{\text{fit}}(C_2)/\text{ndf} < 5$
  - Remove particles from different PV (pileup)
- Apply trigger matching:
  - $J/\psi C$  require the event is triggered by  $J/\psi$
  - $CC$  and  $C\bar{C}$ : either of open charm hadrons triggers event



$2\times\text{Charm}$

LHCb Detector & Data sample  
Event Selection

$2\times\text{Charm}$  signals

Efficiency corrections

Systematics

Cross-sections & ratios

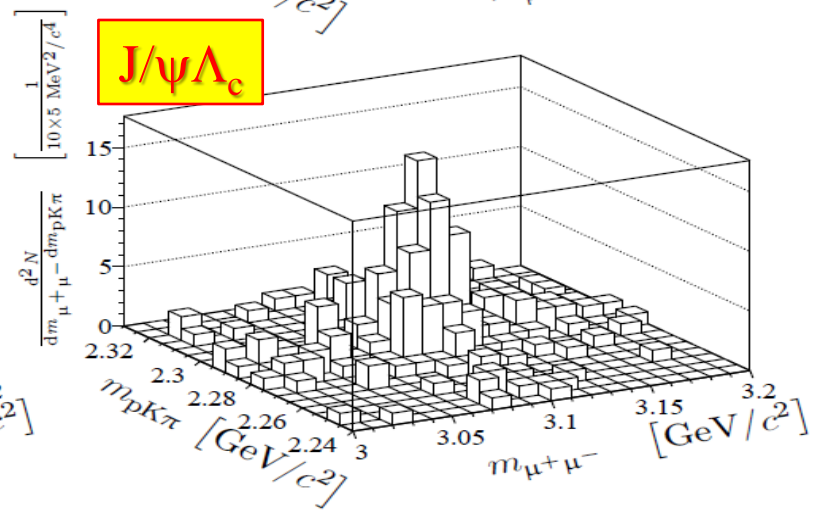
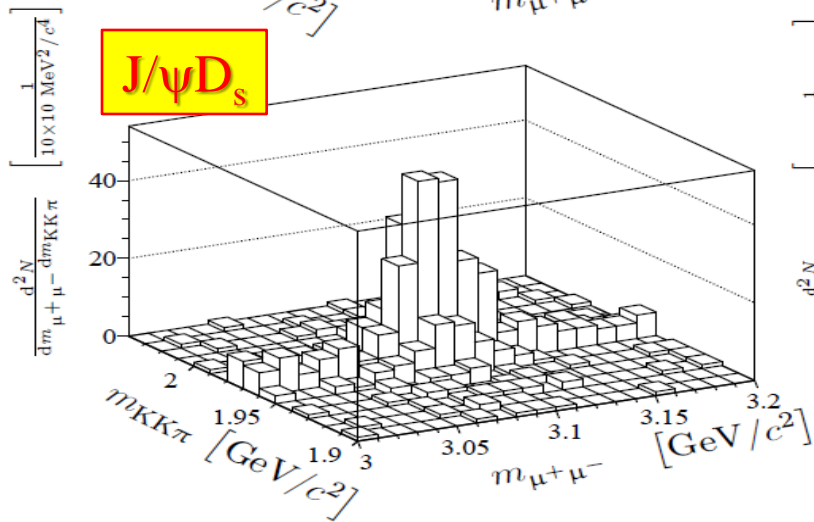
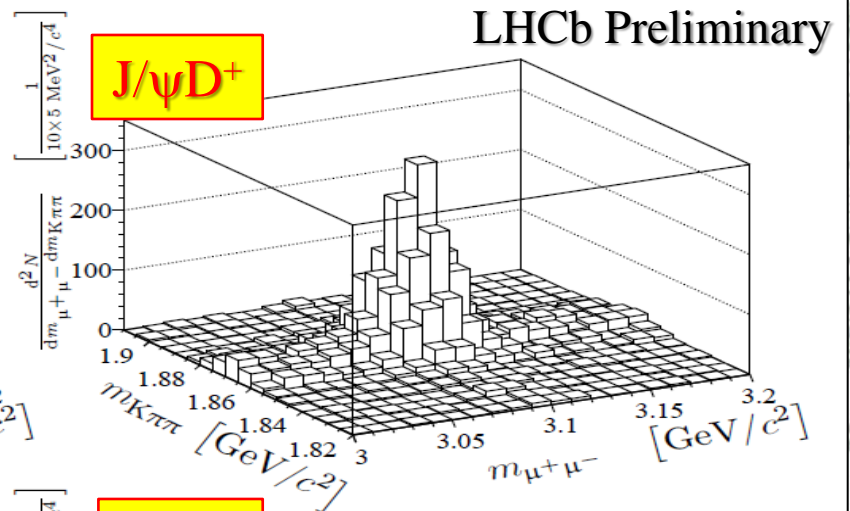
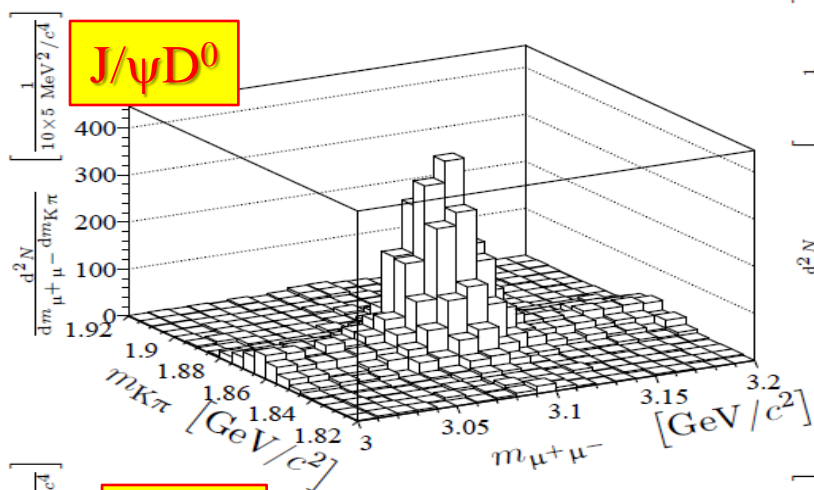
Properties of  $2\times\text{Charm}$  events

Conclusions



# $J/\psi C$ 2D-mass spectra

Clear  $c\bar{c}c\bar{c}$  signals!

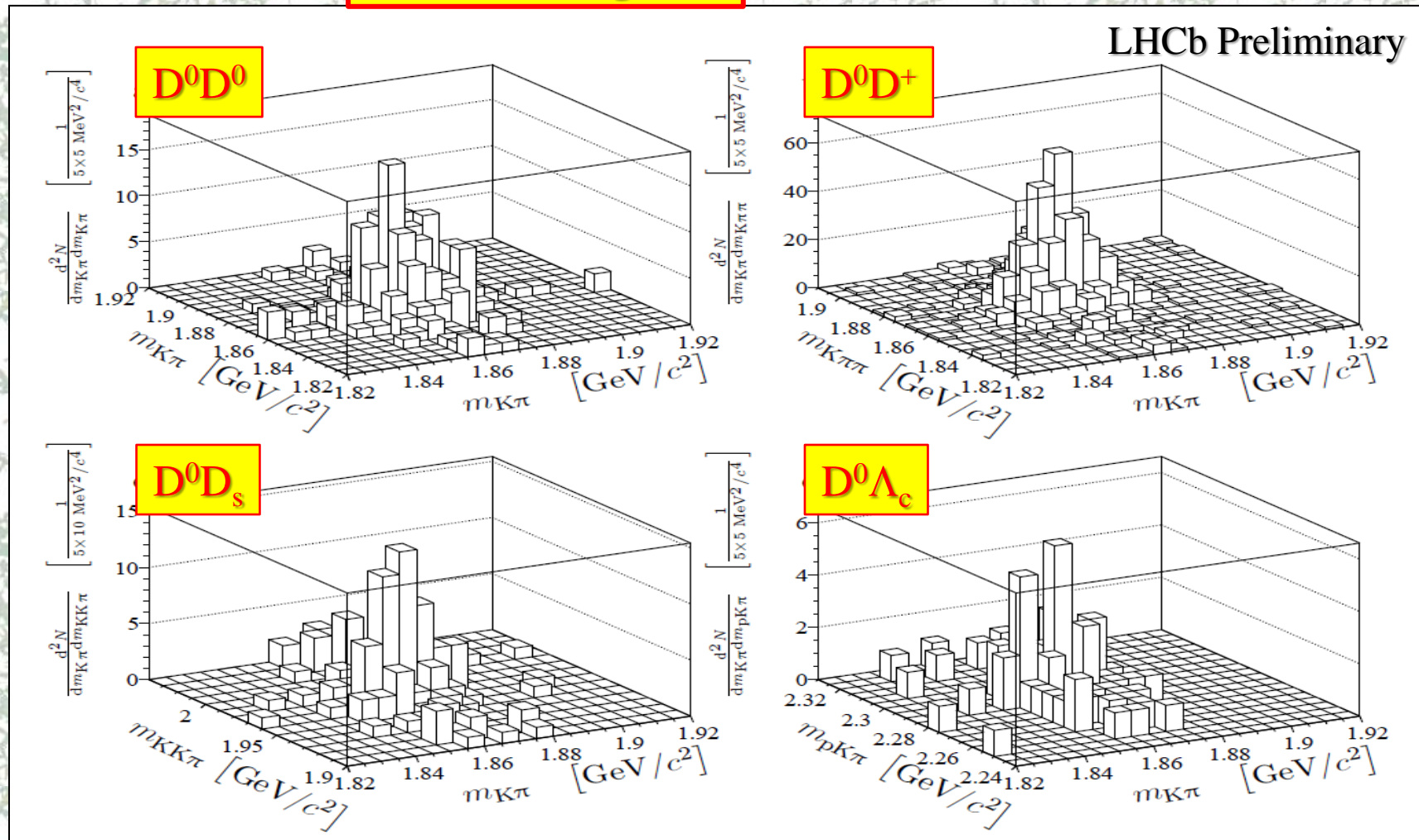






# $D^0C$ 2D-mass spectra

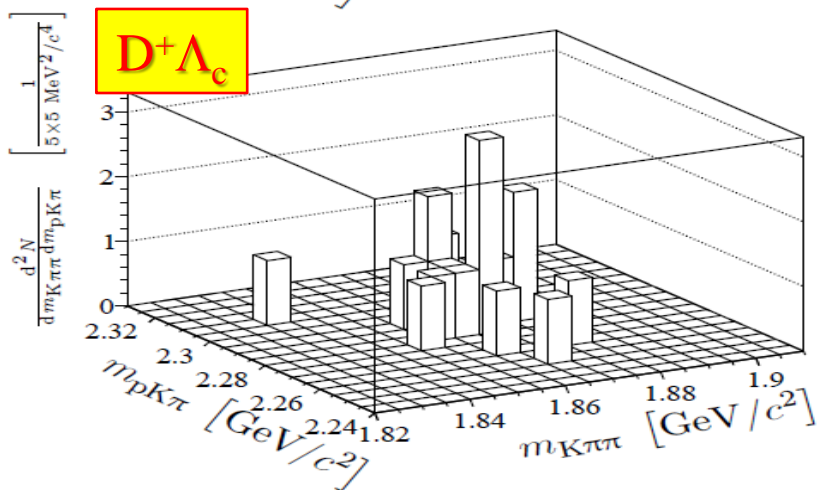
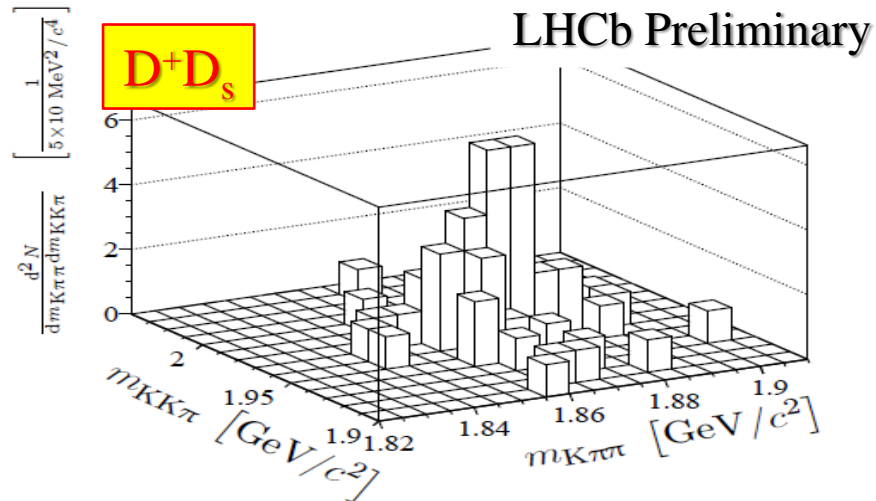
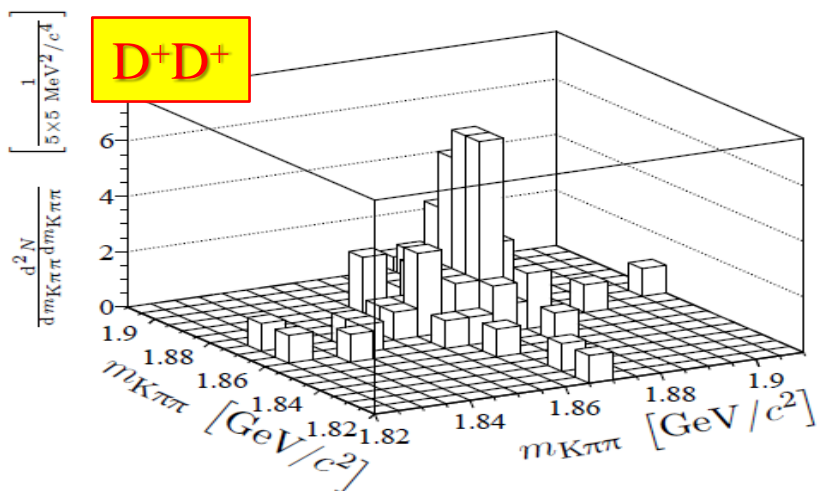
Clear  $c\bar{c}c\bar{c}$  signals!





# $D^+C$ 2D-mass spectra

$c\bar{c}c\bar{c}$



Not enough statistics (yet)  
for  $D_sD_s$ ,  $D_s\Lambda_c$  &  $\Lambda_c\Lambda_c$

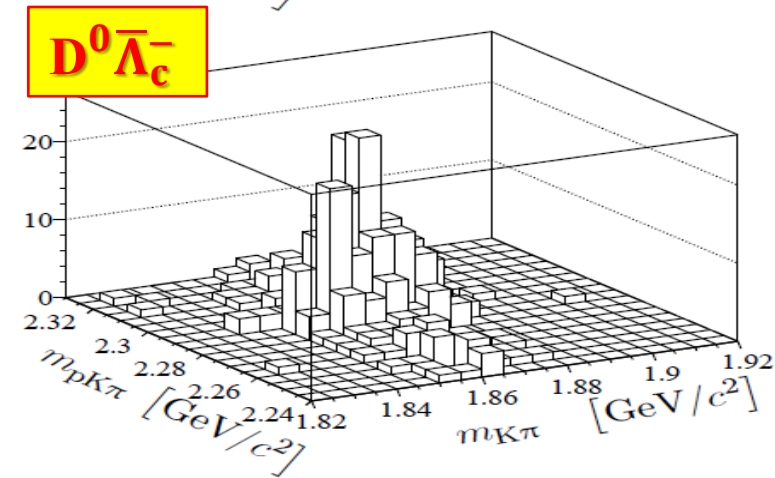
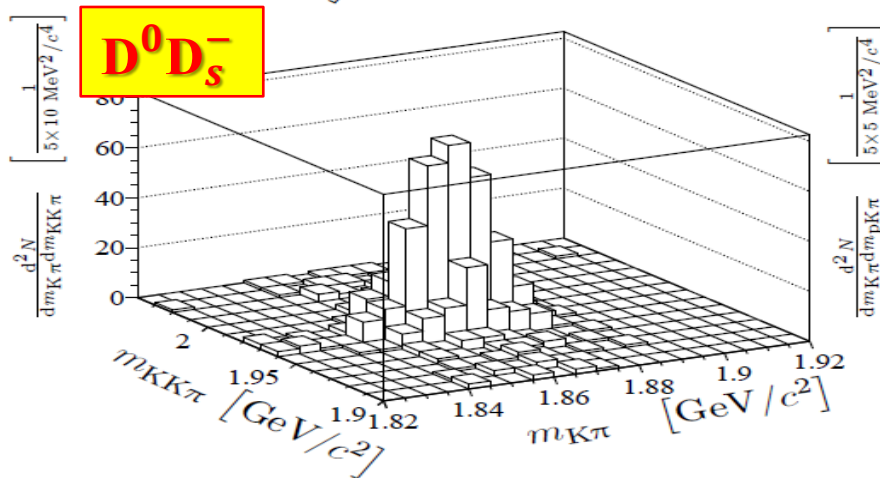
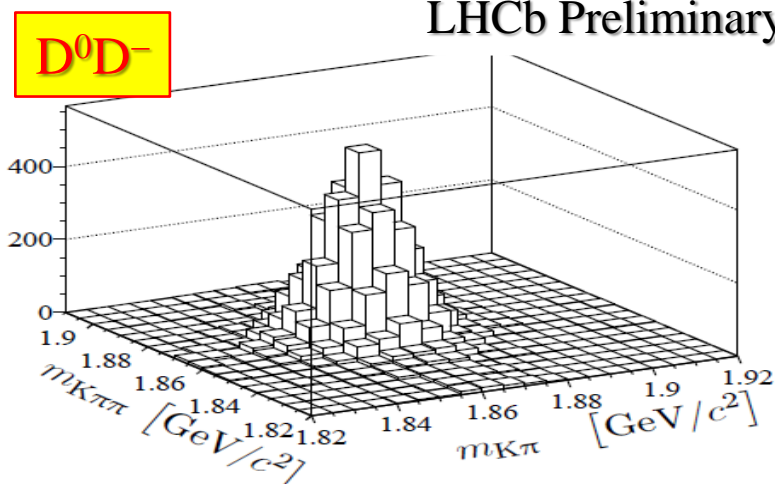
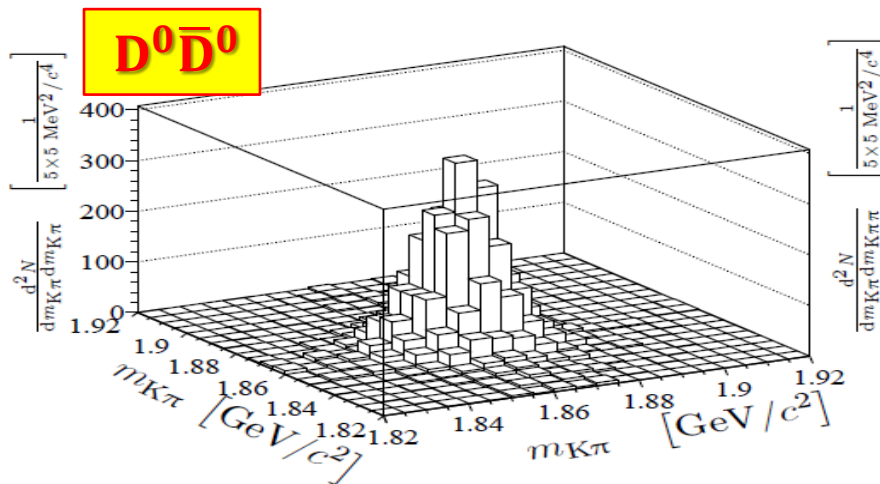




# $D^0 \bar{C}$ 2D-mass spectra

$$gg \rightarrow c\bar{c}$$

LHCb Preliminary







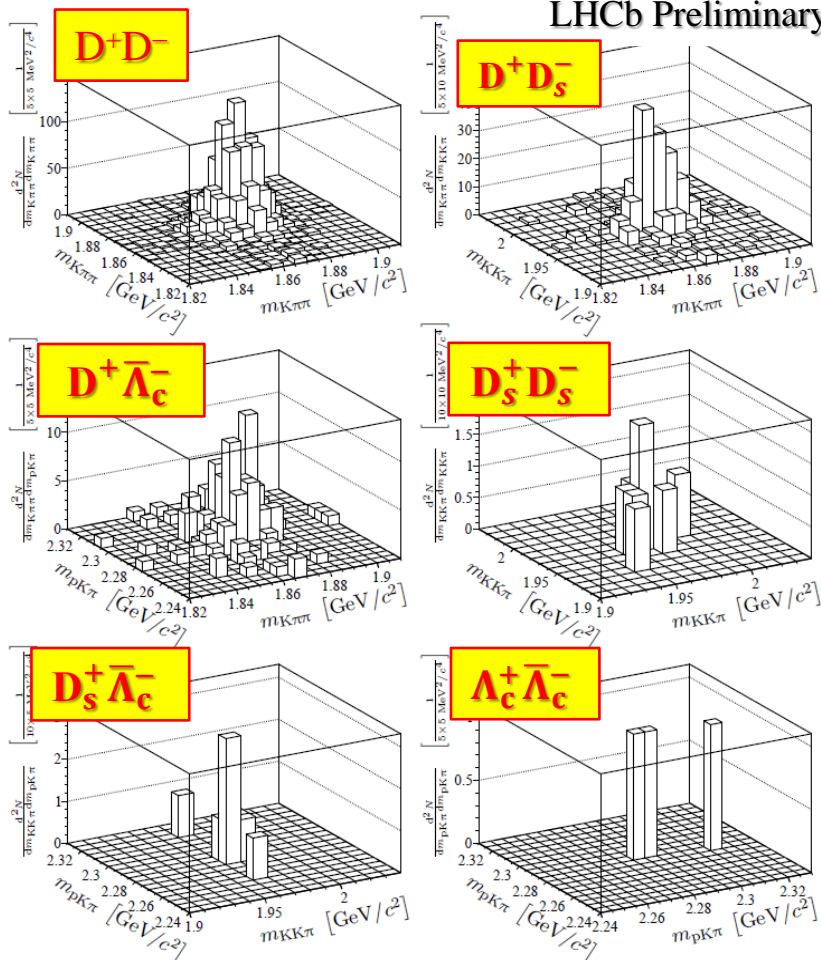
$c\bar{c}$

$gg \rightarrow c\bar{c}$

# 2D-mass spectra



LHCb Preliminary



## Signal Extraction

- 2D- unbinned maximum likelihood fit

$$F(m_i m_j) \propto N^{S_i \times S_j} \times S_i(m_i) S_j(m_j) + N^{S_i \times B_j} \times S_i(m_i) B_j(m_j) + N^{B_i \times S_j} \times B_i(m_i) S_j(m_j) + N^{B_i \times B_j} \times B_i(m_i) B_j(m_j)$$

Signal

J/ $\psi$ :

double-sided Crystal Ball

Open Charm:

«Bukin»

Background:

exponential

Extensive goodness-of-fit tests

Cross-check

(binned) fit-in-slices

Significance



# Yields & Significances



| Mode                 | Yield         | Significance | Goodness-of-fit[%] |
|----------------------|---------------|--------------|--------------------|
| $J/\psi D^0$         | $4875 \pm 86$ | $> 30\sigma$ | 59                 |
| $J/\psi D^+$         | $3323 \pm 71$ | $> 30\sigma$ | 26                 |
| $J/\psi D_s^+$       | $328 \pm 22$  | $13.6\sigma$ | 65                 |
| $J/\psi \Lambda_c^+$ | $116 \pm 14$  | $7.3\sigma$  | 98                 |

**$>5\sigma$**   
**4  $J/\psi C$**   
**6 CC**  
**7  $C\bar{C}$**

| Mode                    | $\mathcal{Y}$   | $\mathcal{S}_\sigma$ | $\mathcal{P}$ [%] |
|-------------------------|-----------------|----------------------|-------------------|
| $D^0 D^0$               | $1087 \pm 37$   | $27\sigma$           | 4.5               |
| $D^0 \bar{D}^0$         | $10080 \pm 105$ | $> 30\sigma$         | 33                |
| $D^0 D^+$               | $1177 \pm 39$   | $29\sigma$           | 24                |
| $D^0 D^-$               | $11224 \pm 112$ | $> 30\sigma$         | 36                |
| $D^0 D_s^+$             | $111 \pm 12$    | $8\sigma$            | 10                |
| $D^0 D_s^-$             | $859 \pm 31$    | $26\sigma$           | 13                |
| $D^0 \Lambda_c^+$       | $41 \pm 8$      | $5\sigma$            | 9                 |
| $D^0 \bar{\Lambda}_c^-$ | $308 \pm 19$    | $14\sigma$           | 35                |
| $D^+ D^+$               | $249 \pm 19$    | $12\sigma$           | 15                |
| $D^+ D^-$               | $3236 \pm 61$   | $> 30\sigma$         | 67                |
| $D^+ D_s^+$             | $52 \pm 9$      | $5\sigma$            | 54                |
| $D^+ D_s^-$             | $419 \pm 22$    | $18\sigma$           | 59                |
| $D^+ \Lambda_c^+$       | $21 \pm 5$      | $2.5\sigma$          | 36                |
| $D^+ \bar{\Lambda}_c^-$ | $137 \pm 14$    | $8\sigma$            | 7                 |



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Conclusions





# Per-event efficiencies: *as much as possible from data*



$$\varepsilon^{\text{tot}} = \varepsilon^{\text{acc\&rec\&sel}} \times \varepsilon^{\text{pid}} \times \varepsilon^{\text{trg}} \times \varepsilon^{\text{*track}}$$

$$\varepsilon^{\text{acc\&rec\&sel}} = \varepsilon_1^{\text{acc\&rec\&sel}} \times \varepsilon_2^{\text{acc\&rec\&sel}}$$

$$\varepsilon^{\text{pid}} = \prod \varepsilon^K \times \prod \varepsilon^\pi \times \prod \varepsilon^p \quad [ \quad \times \varepsilon^{2\mu, J/\psi} \quad ]$$

$$\varepsilon^{\text{*track}} = \prod \varepsilon^{\text{*track}}$$

$$\varepsilon^{\text{trg}}(J/\psi C) = \varepsilon^{\text{trg}}(J/\psi)$$

$$\varepsilon^{\text{trg}}(CC, C\bar{C}) = 1 - (1 - \varepsilon_1^{\text{trg}}) (1 - \varepsilon_2^{\text{trg}})$$

MC  
DATA  
Diff



# Efficiencies II

- $\epsilon_i^{\text{acc\&rec\&sel}}$  from (single charm) Monte Carlo Simulation
  - As function of  $p^T$  &  $y$  for  $D^0, D^+, D_s, \Lambda_c$
  - As function of  $p^T, y$  &  $\cos\theta^*$  for  $J/\psi$
- $\epsilon^K, \epsilon^\pi$  and  $\epsilon^p$  from DATA using  $\Lambda^0 \rightarrow p^+ \pi^-$  and  $D^{*+} \rightarrow (D^0 \rightarrow K^- \pi^+) \pi^+$ 
  - As function of  $p$  &  $\eta$  and #Tracks
- $\epsilon^{2\mu, J/\psi}$  from DATA, using inclusive  $J/\psi$  peak
  - As function of  $J/\psi$   $p^T$  &  $y$
- $\epsilon^{\text{trg}}(J/\psi)$  &  $\epsilon_i^{\text{trg}}$  from DATA using inclusive  $J/\psi, D^0, D^+, D_s^+, \Lambda_c^+$ 
  - As function of  $p^T$  &  $y$
- $\epsilon^{*\text{track}}$  from detailed DATA/MC comparison
  - As function of track  $p^T$  &  $\eta$



# Cross-section



- Use *Weight/Plot* technique:
  - Each event  $i$  has *weight*  $\omega_i$  from *Weight*
    - *Probability event to be signal*
  - This *weight* is corrected by  $1/\epsilon^{\text{TOT}}$

$$N^{\text{corr}} = \sum_i \frac{\omega_i}{\epsilon_i^{\text{tot}}}.$$

$$\sigma = \frac{N^{\text{corr}}}{\mathcal{L} \times \mathcal{B}_1 \times \mathcal{B}_2 \times \epsilon^{\text{GEC}}}$$

The price:

The inflation of "*statistical*" error  
Need good control over efficiency!





2×Charm  
LHCb Detector & Data sample  
Event Selection  
2×Charm signals  
Efficiency corrections  
**Systematics**  
Cross-sections & ratios  
Properties of 2×Charm events  
Conclusions



# Systematic uncertainties



- Dominant:
  - hadron track reconstruction uncertainty related to hadron interactions in detector:
    - *2% per hadron track*
- For modes with  $\Lambda_c$  and  $D_s$  large uncertainties due to uncertainties in branching fractions
  - cancelled in ratios
- Uncertainties related to signal extraction and efficiency corrections are small (1-3-5%)



**2×Charm**  
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# $J/\psi C$ cross-sections and ratios



LHCb Preliminary

| Mode                 | $\sigma$ [nb]                    |
|----------------------|----------------------------------|
| $J/\psi D^0$         | $161.0 \pm 3.7 \pm 10.3 \pm 6.5$ |
| $J/\psi D^+$         | $56.6 \pm 1.7 \pm 4.9 \pm 3.3$   |
| $J/\psi D_s^+$       | $30.5 \pm 2.6 \pm 2.6 \pm 2.2$   |
| $J/\psi \Lambda_c^+$ | $43.2 \pm 7.0 \pm 4.0 \pm 11.3$  |

Using LHCb measurements for  $\sigma_{J/\psi}$  [EPJ C71, 1645] and  $\sigma_C$  [LHCb-CONF-2010-013]

LHCb Preliminary

| Mode                 | $\sigma_{J/\psi C}/\sigma_{J/\psi}$ [ $10^{-3}$ ] | $\sigma_{J/\psi C}/\sigma_C$ [ $10^{-4}$ ] | $\sigma_{J/\psi} \sigma_C/\sigma_{J/\psi C}$ [mb] |
|----------------------|---|--|---|
| $J/\psi D^0$         | $16.18 \pm 0.38 \pm 1.31^{+3.38}_{-2.52}$         | $6.69 \pm 0.18 \pm 0.46$                   | $14.9 \pm 0.4 \pm 1.1^{+2.3}_{-3.1}$              |
| $J/\psi D^+$         | $5.69 \pm 0.17 \pm 0.62^{+1.19}_{-0.89}$          | $5.67 \pm 0.20 \pm 0.40$                   | $17.6 \pm 0.6 \pm 1.3^{+2.8}_{-3.7}$              |
| $J/\psi D_s^+$       | $3.07 \pm 0.26 \pm 0.35^{+0.64}_{-0.48}$          | $7.76 \pm 0.81 \pm 0.63$                   | $12.8 \pm 1.3 \pm 1.1^{+2.0}_{-2.7}$              |
| $J/\psi \Lambda_c^+$ | $4.34 \pm 0.70 \pm 1.21^{+0.91}_{-0.68}$          | $5.52 \pm 1.00 \pm 0.62$                   | $18.0 \pm 3.3 \pm 2.1^{+2.8}_{-3.8}$              |



# CC & C $\bar{C}$

# cross-sections

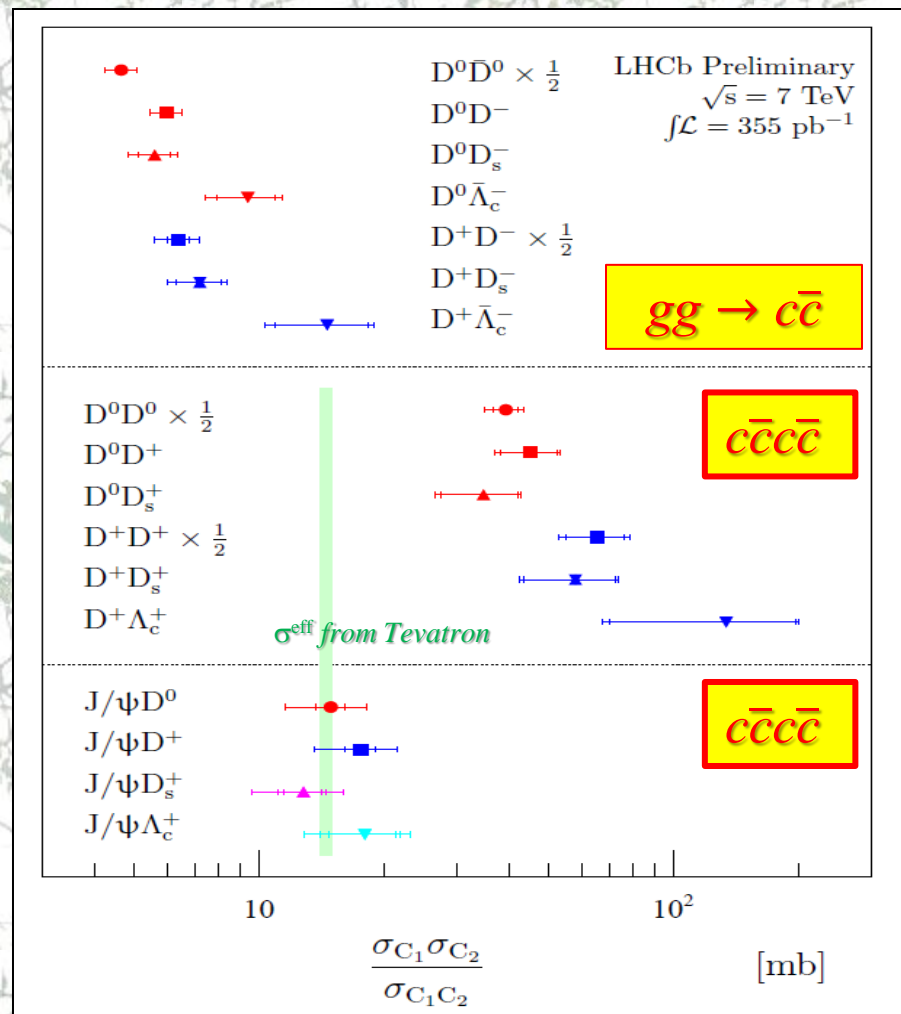
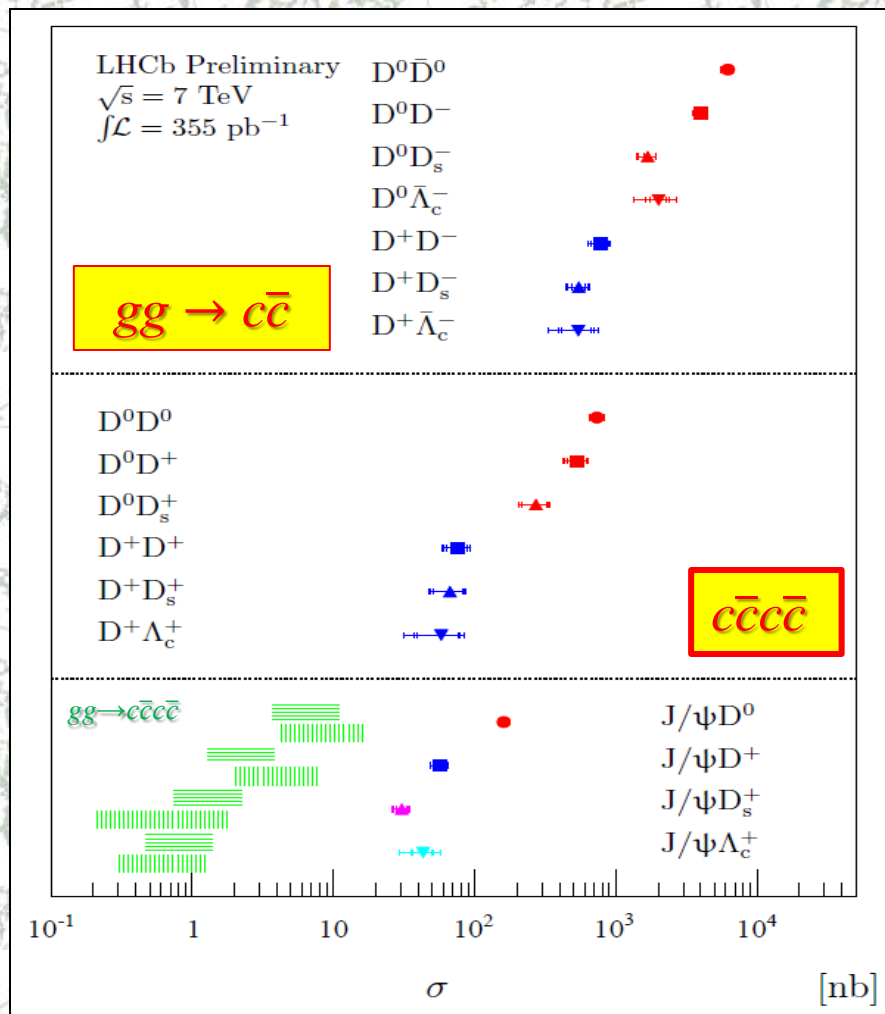


LHCb Preliminary

| Mode                    | $\sigma$ [nb]                  | $\sigma_{CC}/\sigma_{C\bar{C}}$ [%] | $\sigma_{C_1}\sigma_{C_2}/\sigma_{C_1C_2}$ [mb] |
|-------------------------|--------------------------------|-------------------------------------|---|
| D $^0$ D $^0$           | $687 \pm 43 \pm 66 \pm 33$     | $10.9 \pm 0.8$                      | $2 \times (42.2 \pm 2.8 \pm 3.6)$               |
| D $^0\bar{D}^0$         | $6225 \pm 123 \pm 561 \pm 280$ |                                     | $2 \times (4.65 \pm 0.13 \pm 0.40)$             |
| D $^0$ D $^+$           | $516 \pm 81 \pm 59 \pm 31$     | $12.8 \pm 2.1$                      | $46.6 \pm 7.3 \pm 4.2$                          |
| D $^0$ D $^-$           | $3985 \pm 91 \pm 439 \pm 231$  |                                     | $6.02 \pm 0.19 \pm 0.54$                        |
| D $^0$ D $_s^+$         | $266 \pm 53 \pm 33 \pm 20$     | $15.7 \pm 3.4$                      | $35.6 \pm 7.5 \pm 3.8$                          |
| D $^0$ D $_s^-$         | $1680 \pm 107 \pm 202 \pm 121$ |                                     | $5.6 \pm 0.5 \pm 0.6$                           |
| D $^0\Lambda_c^-$       | $2010 \pm 279 \pm 261 \pm 543$ | —                                   | $9.4 \pm 1.5 \pm 1.3$                           |
| D $^+D^+$               | $76 \pm 12 \pm 11 \pm 7$       | $9.6 \pm 1.6$                       | $2 \times (65.6 \pm 10.5 \pm 7.3)$              |
| D $^+D^-$               | $779 \pm 43 \pm 109 \pm 73$    |                                     | $2 \times (6.4 \pm 0.4 \pm 0.7)$                |
| D $^+D_s^+$             | $67 \pm 16 \pm 9 \pm 6$        | $12.1 \pm 3.3$                      | $58.6 \pm 14.5 \pm 5.9$                         |
| D $^+D_s^-$             | $547 \pm 57 \pm 77 \pm 45$     |                                     | $7.2 \pm 0.9 \pm 0.8$                           |
| D $^+\Lambda_c^+$       | $58 \pm 29 \pm 9 \pm 16$       | $10.7 \pm 5.9$                      | $134.8 \pm 68.3 \pm 19.8$                       |
| D $^+\bar{\Lambda}_c^-$ | $534 \pm 130 \pm 80 \pm 144$   |                                     | $14.6 \pm 3.7 \pm 2.1$                          |



# Cross-sections & ratios







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**Conclusions**



# Properties of $J/\psi C, CC$ & $C\bar{C}$ events



- Background subtracted & efficiency corrected distributions:

$J/\psi C$  &  $CC$

pQCD *some* correlations

DPS the production is essentially uncorrelated

$C\bar{C}$

Gluon splitting, flavour creation flavour excitation, etc...

$p^T(C_1), p^T(C_2)$

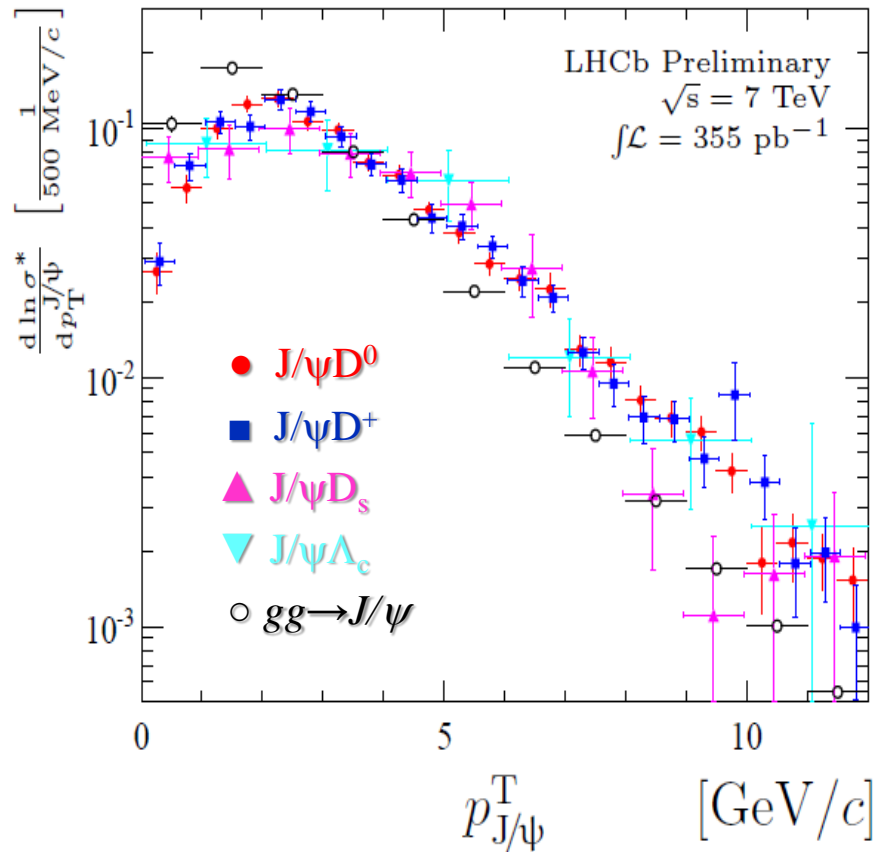
$\Delta\phi$  and  $\Delta y$

$m(C_1, C_2)$

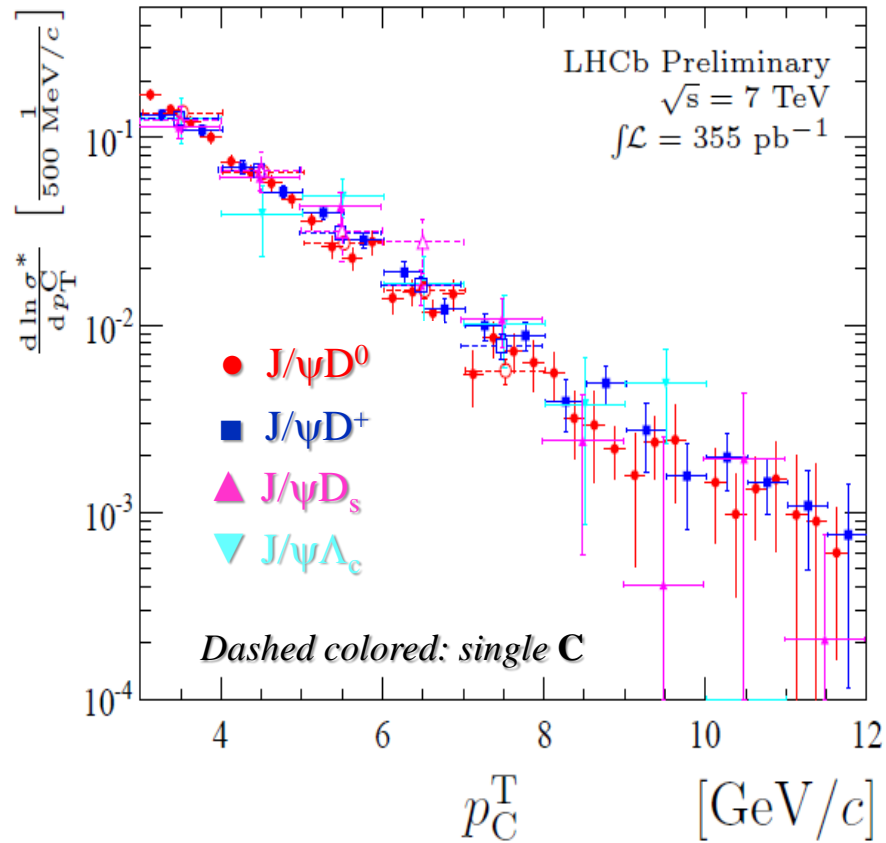


# $J/\psi C$ $p^T$ -spectra

Different from  $gg \rightarrow J/\psi$



Similar to  $gg \rightarrow c\bar{c}$

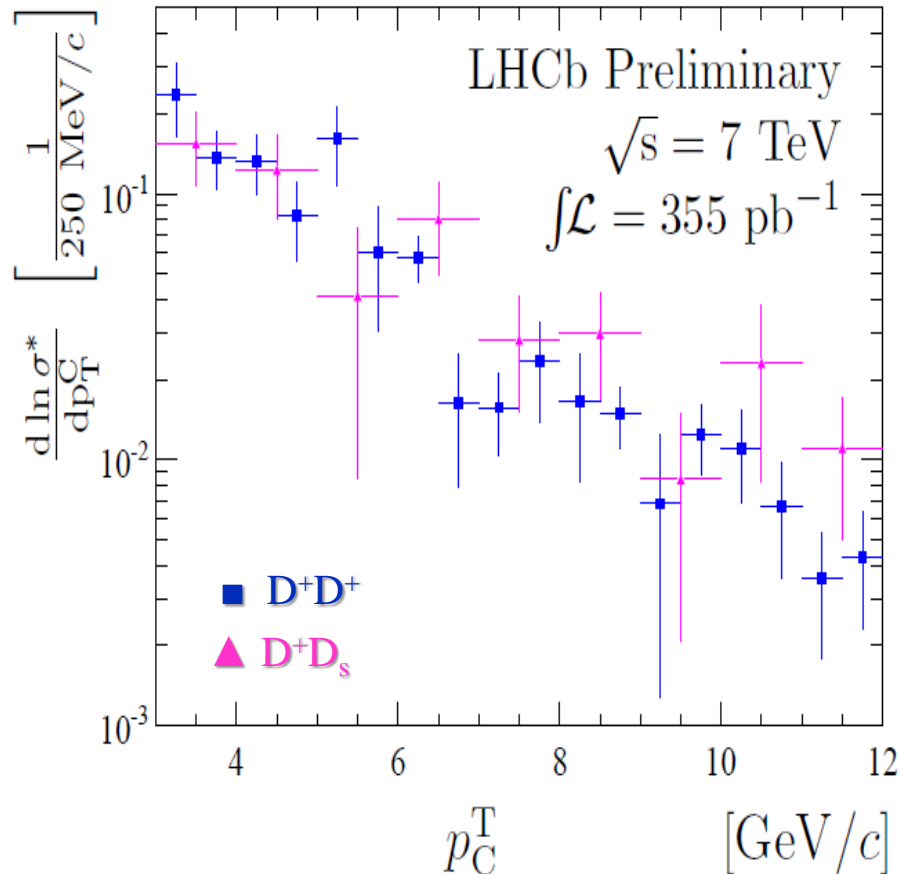
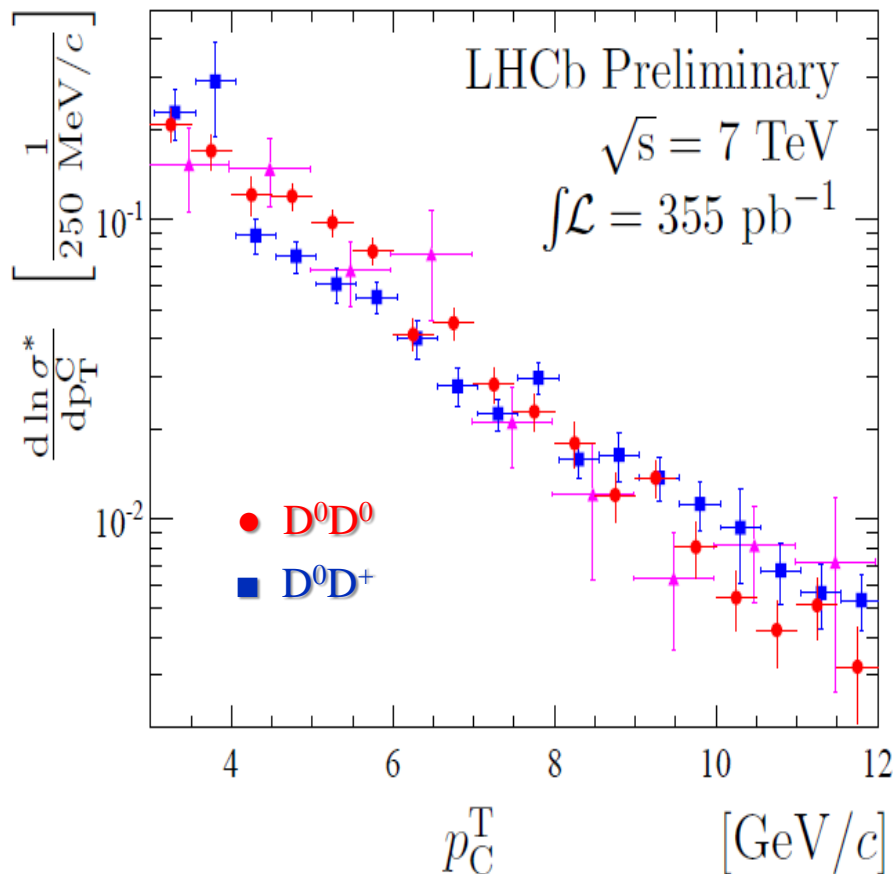






# CC $p^T$ -spectra

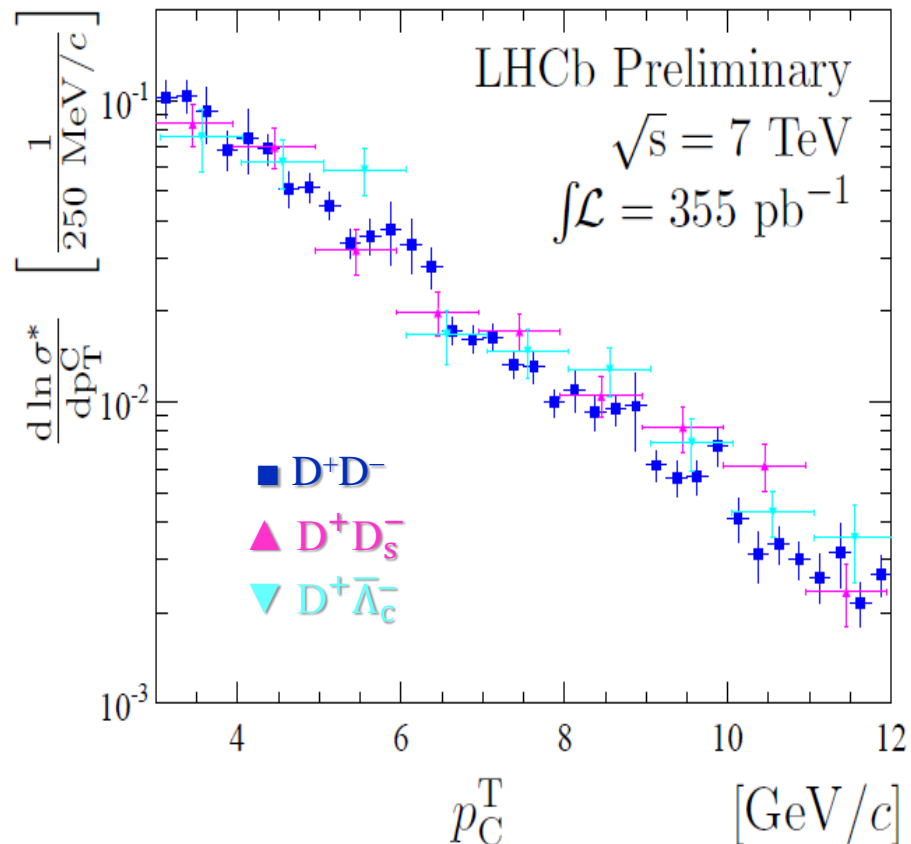
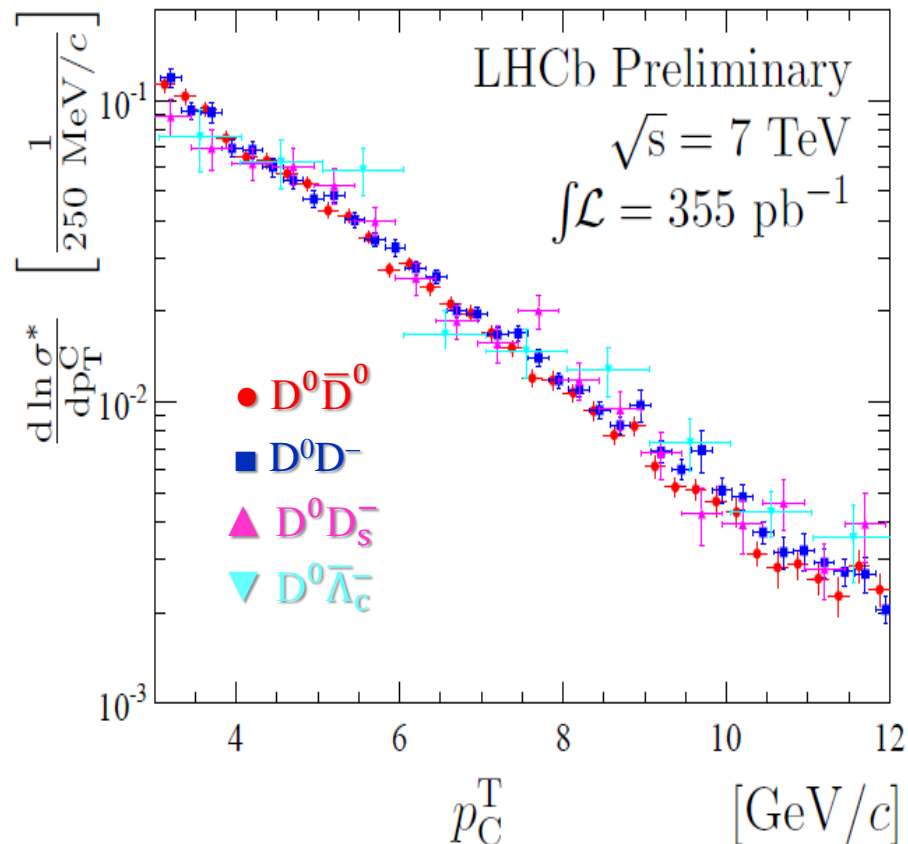
Spectra are flavour independent





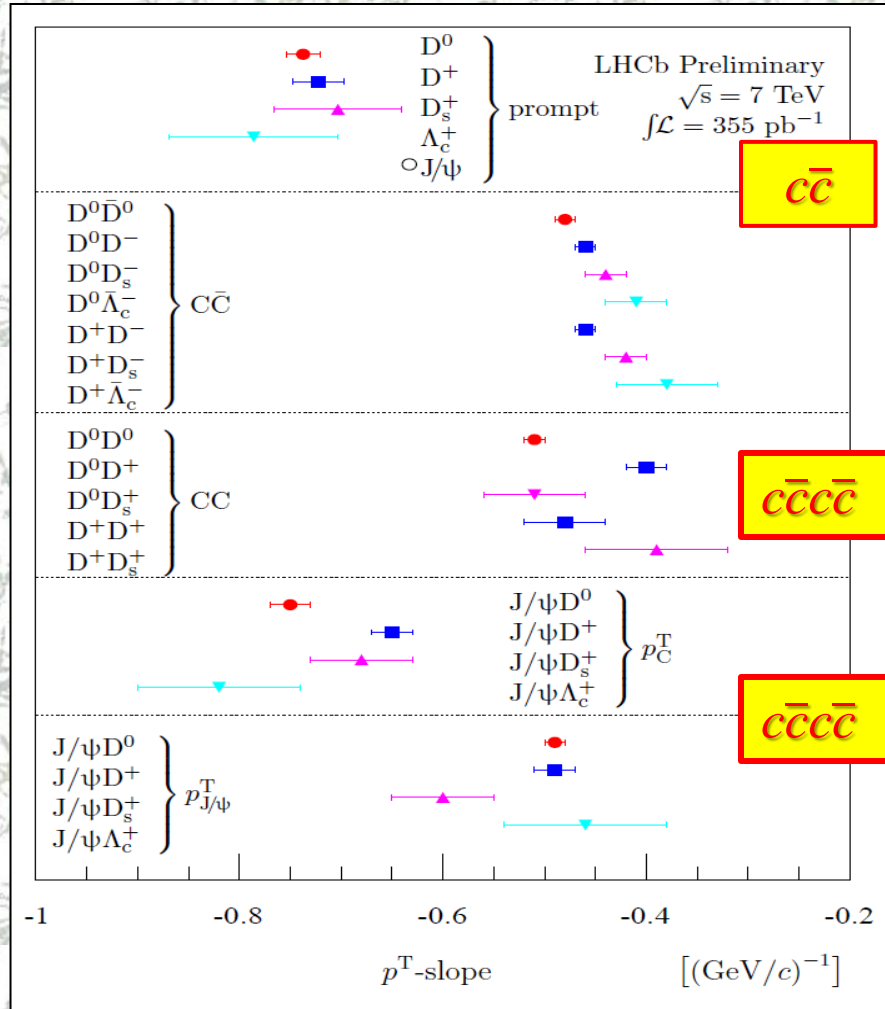
# $c\bar{c}$ $p^T$ -spectra

Spectra are flavour independent





# $p^T$ -slopes: $3 < p^T < 12 \text{ GeV}/c$



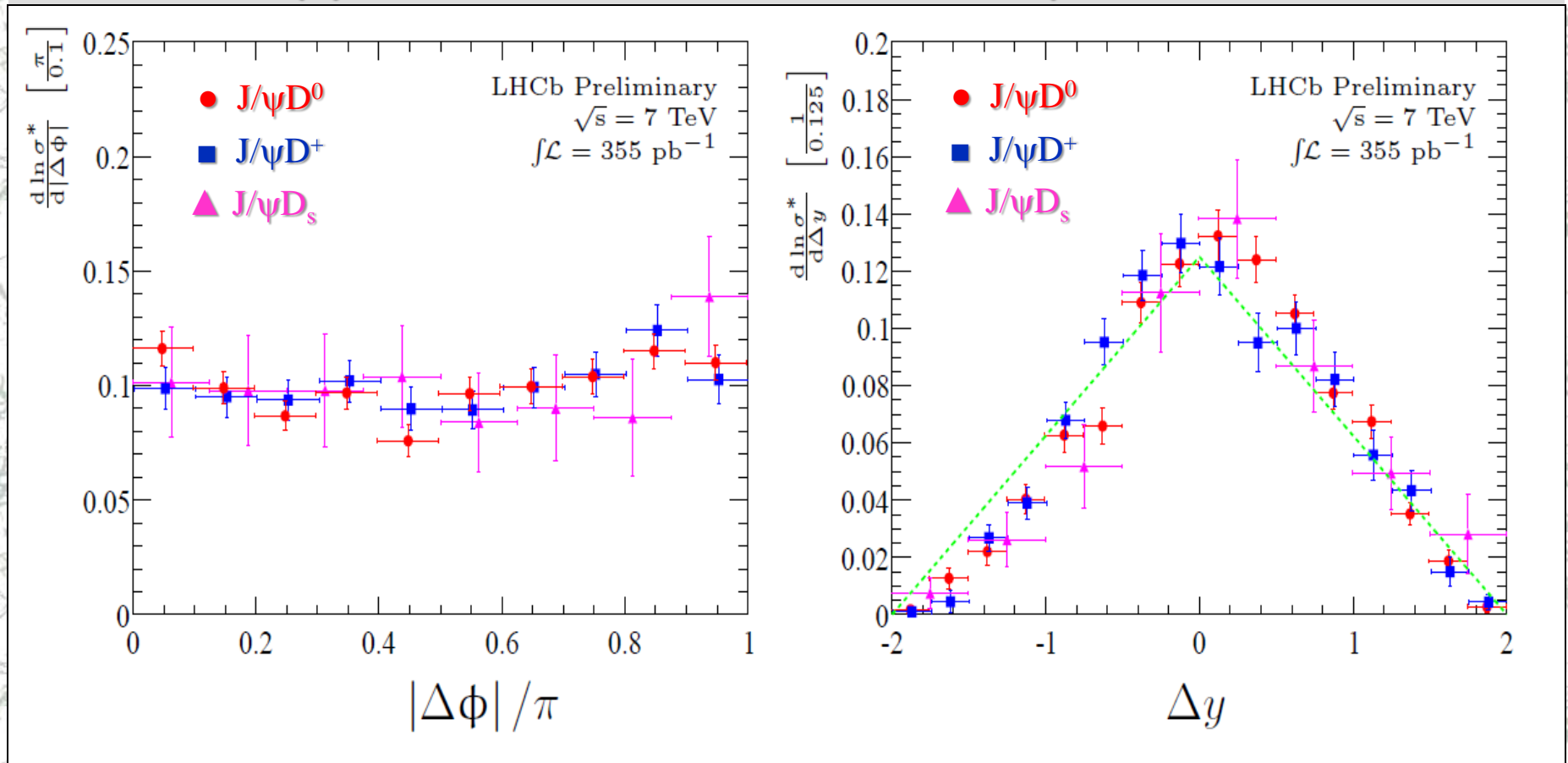
- Fit with *exponential*
- “Similar” within each category
- C from  $J/\psi C$  is similar to single C
- $J/\psi$  from  $J/\psi C$  is very different from single  $J/\psi$
- CC and  $C\bar{C}$  are similar and both are very different from single C





# $J/\psi C$ $\Delta\phi$ and $\Delta y$

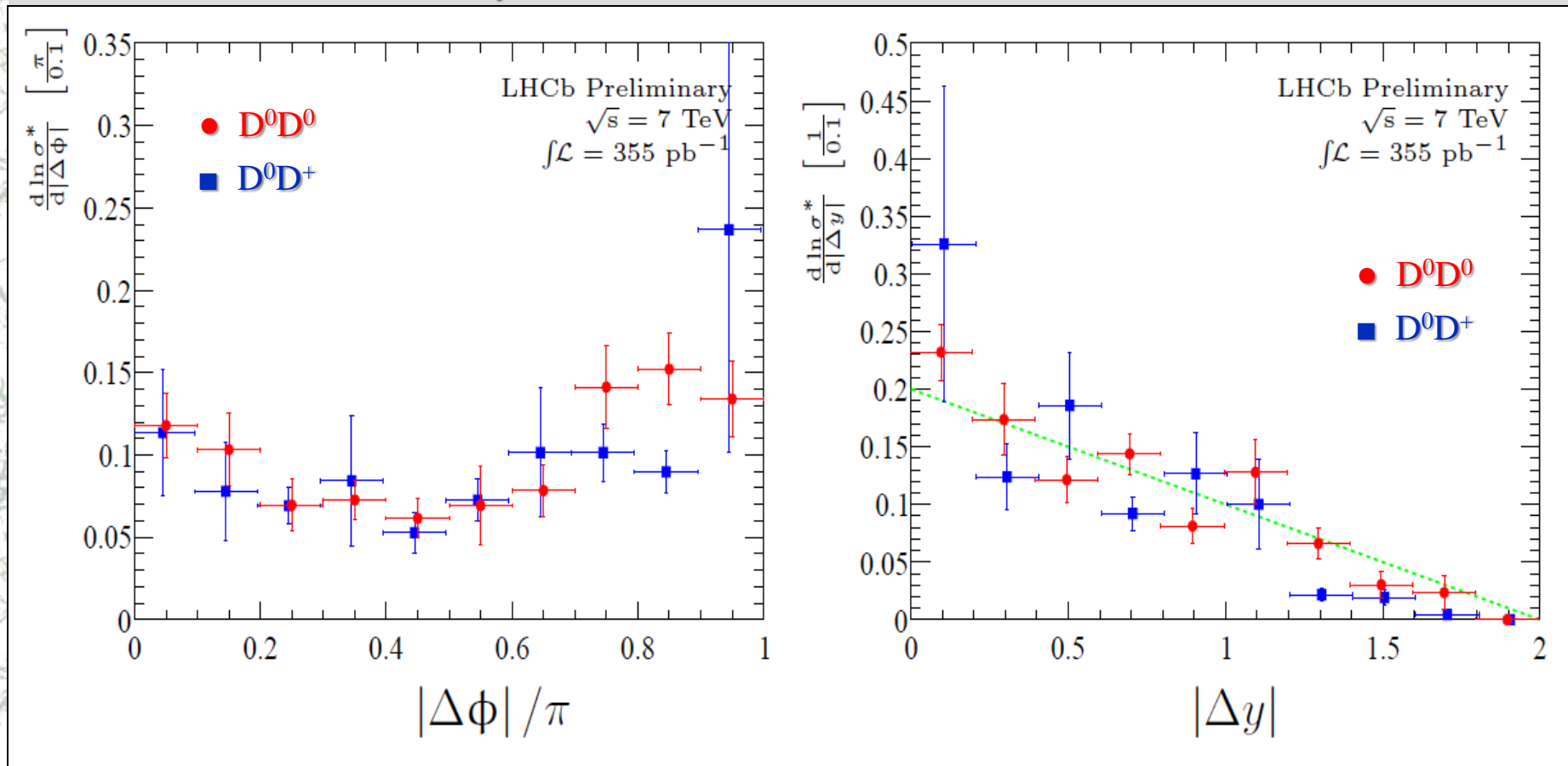
## Support for non-correlated production





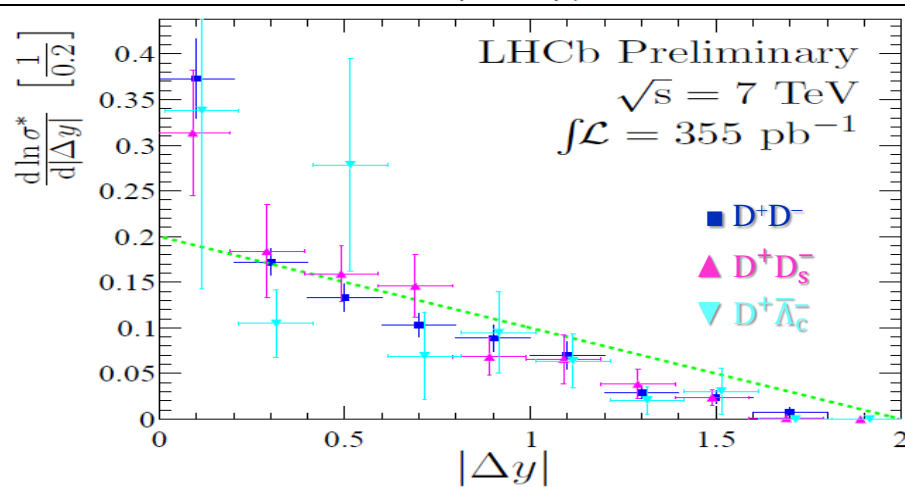
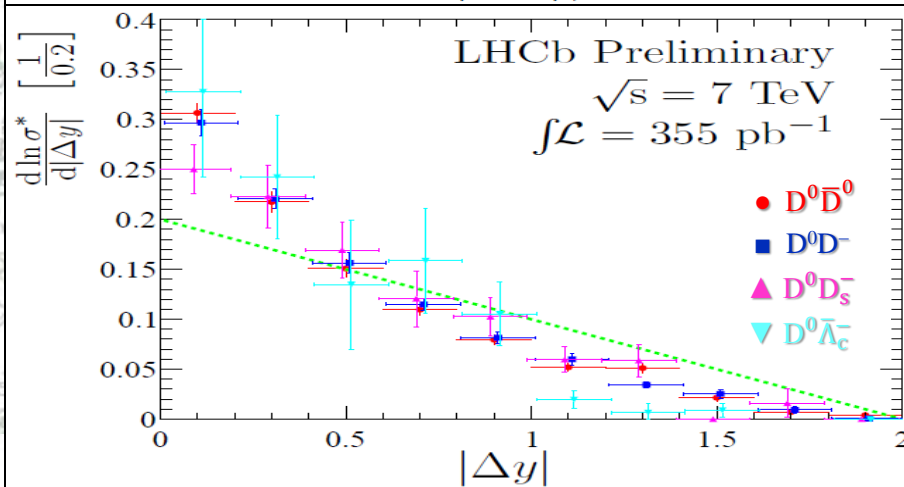
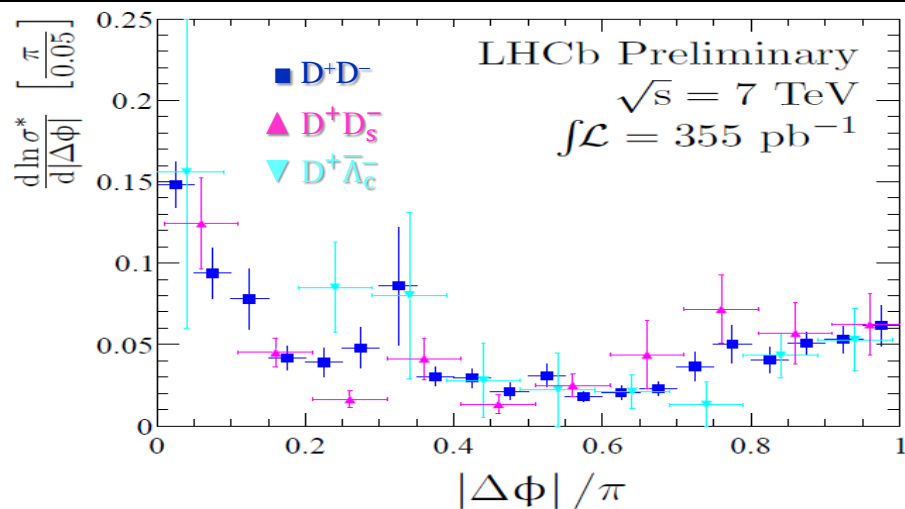
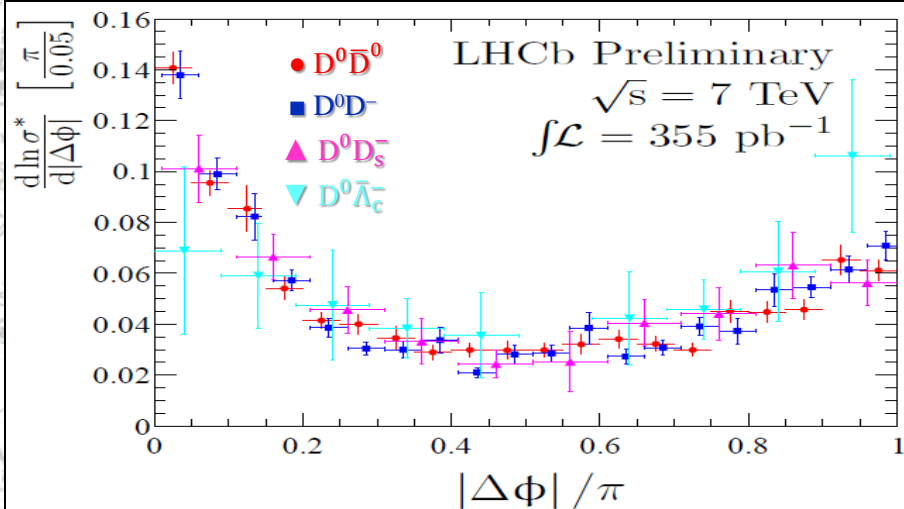
# CC $\Delta\phi$ and $\Delta y$

No prominent correlations?





# $c\bar{c}$ $\Delta\phi$ and $\Delta y$





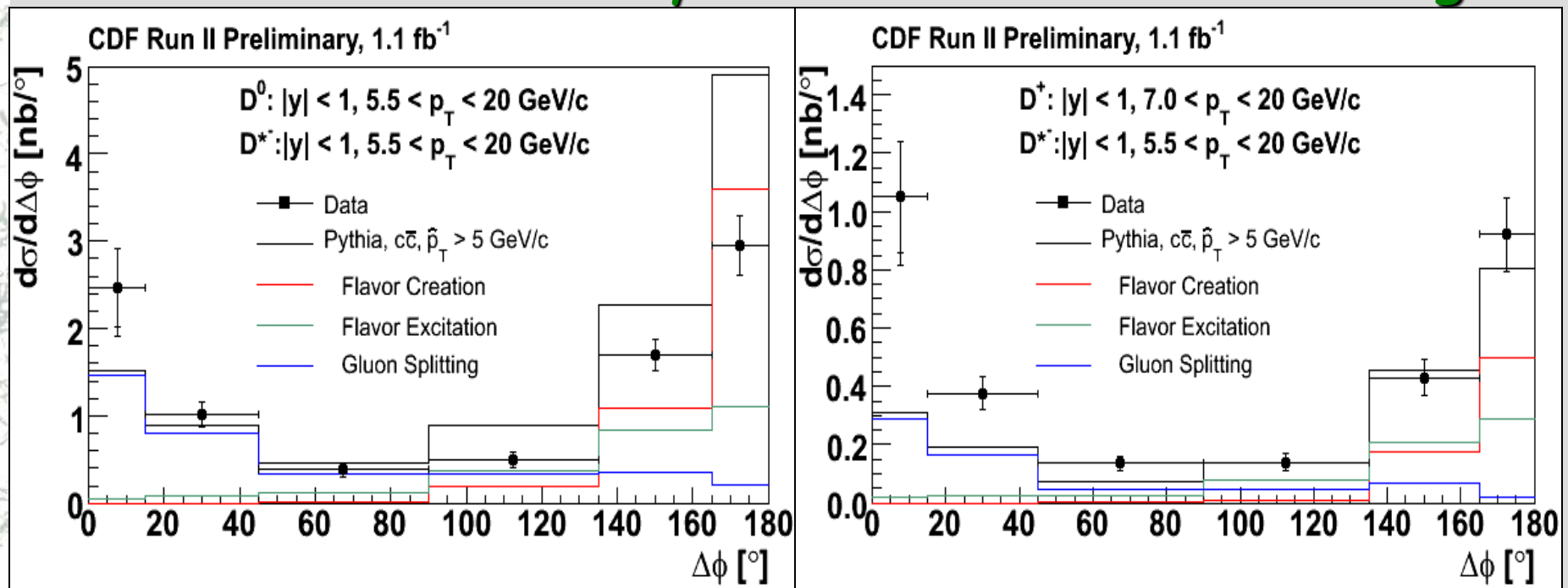


# Compare with CDF'2k+6

<http://www-cdf.fnal.gov/physics/new/bottom/060921.blessed-double-charm-corr/>

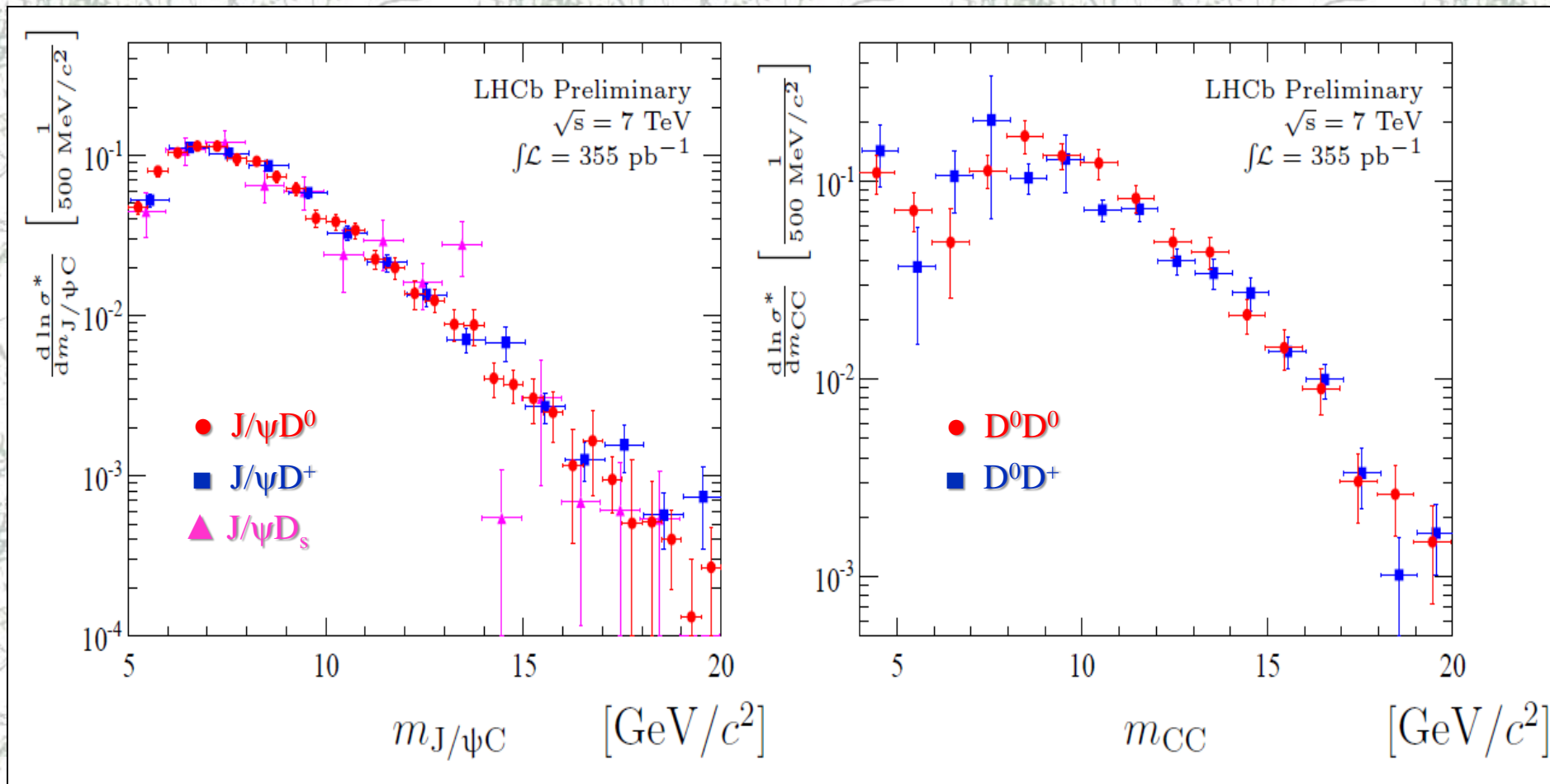
- CDF: azimuthal correlations for  $D^{(0,+)} D^{*-}$
- Large gluon splitting contribution

Very different kinematical region





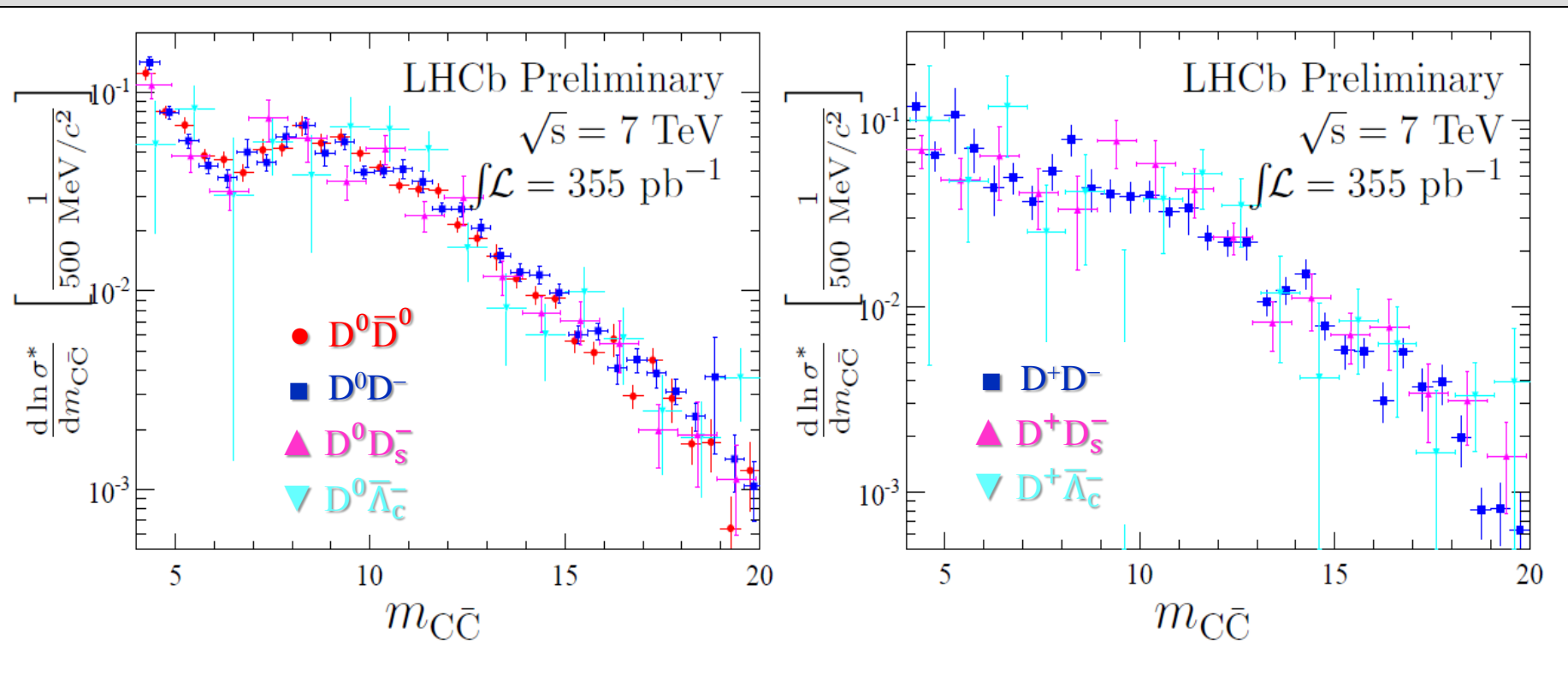
# $J/\psi C$ and $CC$ invariant mass





# $C\bar{C}$ invariant mass

- “Flavour” independent
- for  $m > 7 \text{ GeV}/c^2$ : very similar to  $CC$







# Global Event Activity



- Compare number of primary vertices, tracks, hits in subdetectors, ....
- No clear pattern has been observed
- No significant difference with respect to the single charm events with same selection
- (One more indirect argument against pileup)
  - decrease number of PVs (-1)
  - increase multiplicity ( $\times 1.5-2.0$ )



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# Comparison with models



**pQCD ( $gg \rightarrow c\bar{c}c\bar{c}$ )/MadOnia, DPS, Pythia, IC**

- pQCD is off by the factor  $\sim 20$
- Support for (factorization) DPS
  - excellent agreement for **J/ $\psi$ C**
  - factor  $\sim 3$  off for **CC**
  - general support for “*uncorrelated*” production
- Pythia fails to reproduce all the cross-section ratios and spectra.
- IC agrees on cross-section, but lack of well-defined predictions on spectra, correlations, ...





# Summary



- **$J/\psi C$**  production has been measured ( $>7\sigma$ ) for the first time at hadron machines  
*All four modes:  $J/\psi D^0$ ,  $J/\psi D^+$ ,  $J/\psi D_s$ ,  $J/\psi \Lambda_c$*
- **$CC$**  production has been observed for the first time for *six modes* with  $>5\sigma$  significance:  
 $D^0 D^0$ ,  $D^0 D^+$ ,  $D^0 D_s$ ,  $D^0 \Lambda_c$ ,  $D^+ D^+$ ,  $D^+ D_s$
- **$C\bar{C}$**  production have been measured for *seven modes*
- Cross-sections and ratios have been obtained
- $p^T$ -spectra,  $\Delta\phi$ ,  $\Delta y$  and  $m(C_1 C_2)$  have been studied

In total LHCb measured  $1 + 4 + 6 + 7 = 18$  modes from 25

Stay tuned: LHCb-PAPER-2012-003 in preparation



# THANK YOU



# thanks



- *Anatoly Likhoded* for inspiring efforts and stimulating discussions
- *Antoni Szczurek* for useful discussions on DPS
- *Jean-Philippe Lansberg* for the great help with MadOnia





# BACK UP



# Theory: double charm at LHCb



Table 1.1: Predictions for the production cross-sections of the  $J/\psi C$  and  $CC$  modes in the LHCb fiducial range given by the leading order  $gg \rightarrow J/\psi c\bar{c}$  matrix element [12, 13, 16]  $\sigma_{gg}$ , the double parton scattering approach,  $\sigma_{DPS}$  and the intrinsic charm model,  $\sigma_{IC}$ .

| Mode                 | $\sigma_{gg}$<br>State-of-art pQCD |               | $\sigma_{DPS}$  | $\sigma_{IC}$ |
|----------------------|------------------------------------|---------------|-----------------|---------------|
|                      | [nb]                               |               |                 |               |
| $J/\psi D^0$         | $10 \pm 6$                         | $7.4 \pm 3.7$ | $146 \pm 39$    | 220           |
| $J/\psi D^+$         | $5 \pm 3$                          | $2.6 \pm 1.3$ | $60 \pm 17$     | 100           |
| $J/\psi D_s^+$       | $1.0 \pm 0.8$                      | $1.5 \pm 0.7$ | $24 \pm 7$      | 30            |
| $J/\psi \Lambda_c^+$ | $0.8 \pm 0.5$                      | $0.9 \pm 0.5$ | $56 \pm 22$     | —             |
|                      | [ $\mu b$ ]                        |               |                 |               |
| $D^0 D^0$            |                                    |               | $2.0 \pm 0.5$   | 1.5           |
| $D^0 D^+$            |                                    |               | $1.7 \pm 0.4$   | 1.4           |
| $D^0 D_s^+$          |                                    |               | $0.65 \pm 0.15$ | 0.4           |
| $D^0 \Lambda_c^+$    |                                    |               | $1.5 \pm 0.5$   | 1.4           |
| $D^+ D^+$            |                                    |               | $0.34 \pm 0.09$ | 0.3           |
| $D^+ D_s^+$          |                                    |               | $0.27 \pm 0.07$ | 0.2           |
| $D^+ \Lambda_c^+$    |                                    |               | $0.64 \pm 0.23$ |               |

## PYTHIA

| Mode                            | $\sigma_{J/\psi C}^*$ [nb] |
|---------------------------------|----------------------------|
| $J/\psi D^0$                    | 160                        |
| $J/\psi D^+$                    | 58                         |
| $J/\psi D_s^+$                  | 33                         |
| $J/\psi \Lambda_c^+$            | 23                         |
| Mode                            | $\sigma_{CC,CC}^*$ [nb]    |
| $D^0 D^0$                       | $1.0 \times 10^3$          |
| $D^0 \bar{D}^0$                 | $17.4 \times 10^3$         |
| $D^0 D^+$                       | 680                        |
| $D^0 D^-$                       | $12.6 \times 10^3$         |
| $D^0 D_s^+$                     | 370                        |
| $D^0 D_s^-$                     | $6.8 \times 10^3$          |
| $D^0 \Lambda_c^+$               | 253                        |
| $D^0 \bar{\Lambda}_c^-$         | $4.8 \times 10^3$          |
| $D^+ D^+$                       | 120                        |
| $D^+ D^-$                       | $2.3 \times 10^3$          |
| $D^+ D_s^+$                     | 140                        |
| $D^+ D_s^-$                     | $2.5 \times 10^3$          |
| $D^+ \Lambda_c^+$               | 100                        |
| $D^+ \bar{\Lambda}_c^-$         | $1.8 \times 10^3$          |
| $D_s^+ D_s^+$                   | 39                         |
| $D_s^+ D_s^-$                   | 670                        |
| $D_s^+ \Lambda_c^+$             | 50                         |
| $D_s^+ \bar{\Lambda}_c^-$       | $0.9 \times 10^3$          |
| $\Lambda_c^+ \Lambda_c^+$       | 20                         |
| $\Lambda_c^+ \bar{\Lambda}_c^-$ | 370                        |



# Do we have pileup?



- 3 approaches:
  - Generator level MC with applied efficiency factors
    - Cross-check with inclusive  $J/\psi$ ,  $D^0$ ,  $D^+$ ,  $D_s$  and  $\Lambda_c$  MC samples
    - Good statistics, but some assumptions
  - Full simulation:
    - Low statistics, need some assumptions
  - Real data: vary  $\chi^2_{\text{fit}}/\text{ndf}$  cut
- All three methods: *pileup is totally negligible*
  - A tiny fraction of the statistical error





# Pileup from data

*pileup is totally negligible*

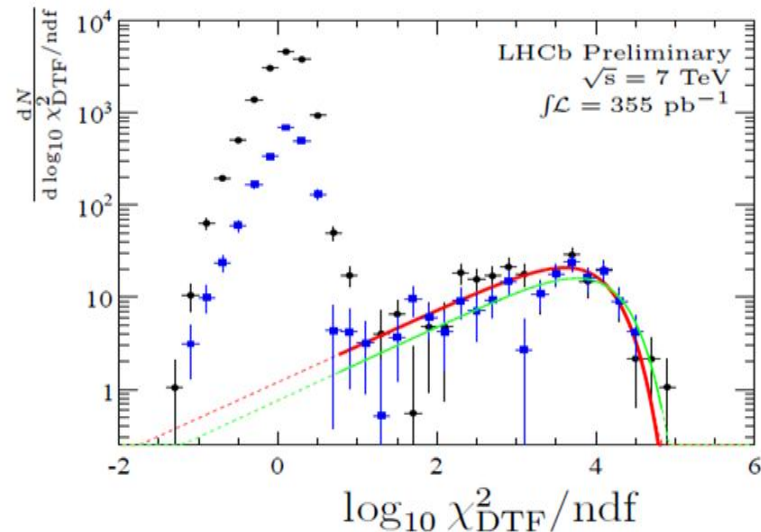
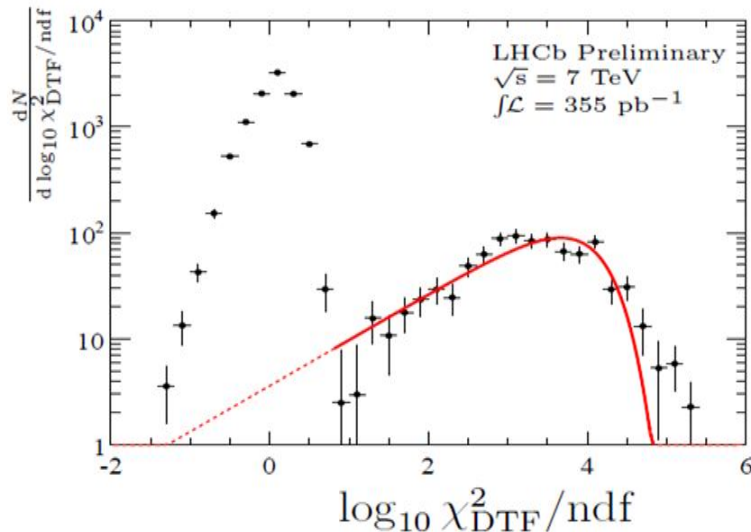


Figure 6.1: The background subtracted distributions of  $\chi^2_{\text{DTF}}/\text{ndf}$ . a) For  $J/\psi D^0$  events. The solid red line corresponds to the fit result in region  $\chi^2_{\text{DTF}}/\text{ndf} > 5$  by function described in text, the dashed line corresponds to the extrapolation of fit results to  $\chi^2_{\text{DTF}}/\text{ndf} < 5$  region. (b)  $D^0 D^0$  events (black circles corresponds to CC and blue rectangles corresponds to  $C\bar{C}$  case). The solid red (green) line corresponds to the fit result in region  $\chi^2_{\text{DTF}}/\text{ndf} > 5$  by function described in text, the dashed red (green) line corresponds to the extrapolation of fit results to  $\chi^2_{\text{DTF}}/\text{ndf} < 5$  region for CC and  $C\bar{C}$  cases respectively.

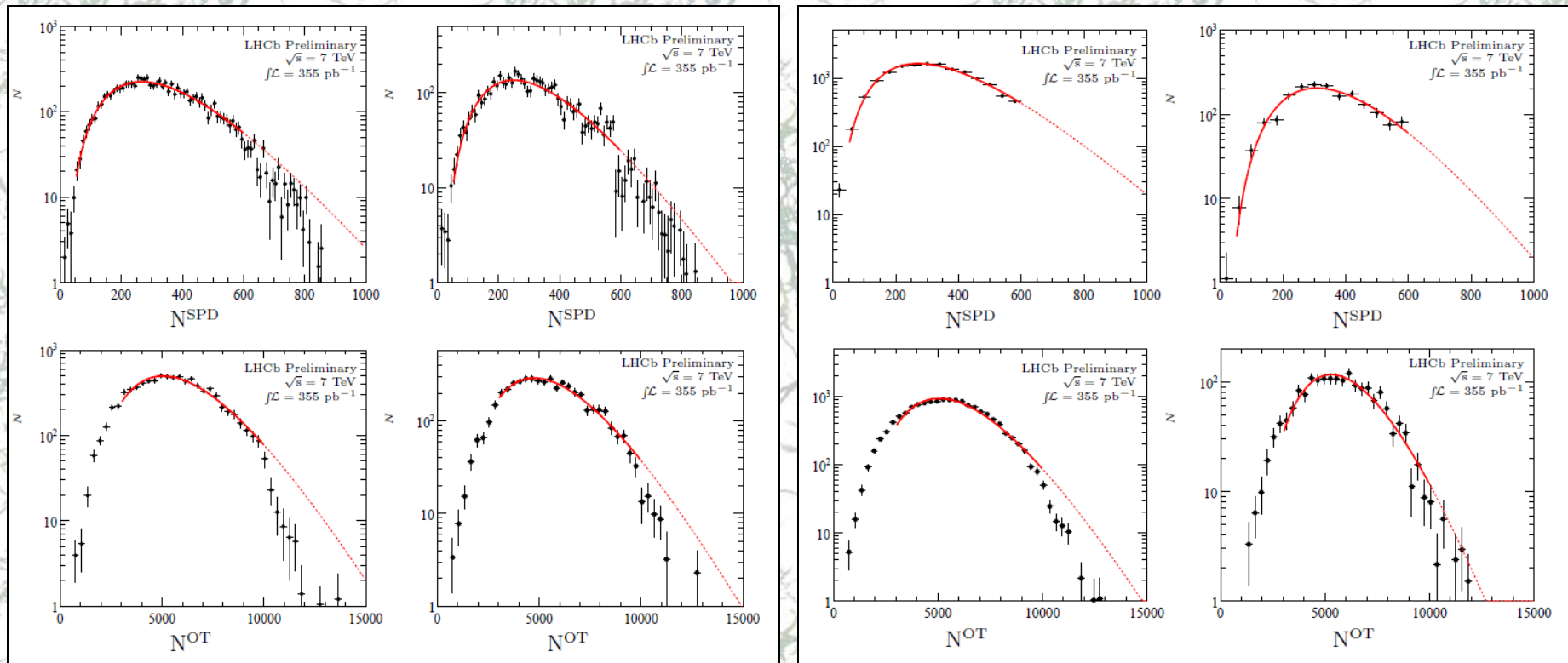


# Global Event Cuts



Global Event Cuts (activity in subdetectors, namely #hits in Outer Tracker and #hits in SPD detector) are applied during data taking to suppress few very busy events.

The effect is studied on the data itself. Efficiency  $\varepsilon^{\text{GEC}}$  is extracted through extrapolation





# DPS: a rather simple paradigm



LHC is LgC

$$\sigma_{\text{DPS}}^{AB} = \frac{m}{2} \sum_{i,j,k,l} \int \Gamma_{ij}(x_1, x_2, b_1, b_2, Q_1^2, Q_2^2) \times \hat{\sigma}_{ik}^A(x_1, x'_1, Q_1^2) \hat{\sigma}_{jl}^B(x_2, x'_2, Q_2^2) \\ \times \Gamma_{kl}(x'_1, x'_2, b_1 - b, b_2 - b, Q_1^2, Q_2^2) \times dx_1 dx_2 dx'_1 dx'_2 d^2 b_1 d^2 b_2 db,$$

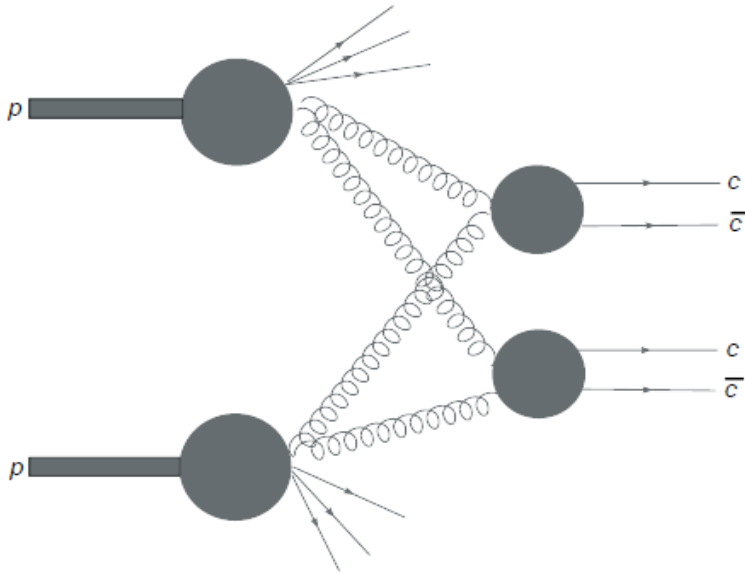
Single partonic x-section

$_2$ PDF (unknown)

$$\Gamma_{ij}(x_1, x_2; b_1, b_2; Q_1^2, Q_2^2) = D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) f(b_1) f(b_2),$$

$$D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_h^i(x_1; Q_1^2) D_h^j(x_2; Q_2^2).$$

Can't be true for all  $x, Q^2$



Both for total and (double) differential

$$\sigma_{\text{DPS}}^{AB} = \frac{m}{2} \frac{\sigma_{\text{SPS}}^A \sigma_{\text{SPS}}^B}{\sigma_{\text{eff}}}.$$

Easy to make predications!

And the predicitons are easy to test

Universal (energy and process independent) factor)

$$1/\sigma_{eff} = \int d^2 b F^2(b)$$





# Analysis strategy

- To measure:
  - Model independent cross-section in signal window
  - Various ratios (with minimal error)
- Rely on *per-event efficiency*
- Evaluate various techniques for signal extraction
  - Choose *Plot/Weight*
  - Correct *weight* from *Weight* by  $1/\epsilon$
  - Careful check for biases and correlations

The price:  
The *enormous* inflation  
of "*statistical*" error





# Event Selection



- Start from good tracks:
  - Minimal  $p^T$ , good track fit quality, remove clones
- For hadrons: fiducial cuts for good PID
- $(\mu, K, p, \pi)$  PID cuts are imposed

| Track Selection         |   |
|-------------------------|---|
| $\mu^\pm, h^\pm$        | $\chi_{\text{tr}}^2/\text{ndf} < 5$ & $\Delta^{\text{KL}} > 5000$             |
| $\mu^\pm$               | $p^T > 650 \text{ MeV}/c$   |
| $h^\pm$                 | $p^T > 250 \text{ MeV}/c$ & $2.0 < \eta < 5$ & $\chi_{\text{IP}}^2 > 9$       |
| $\pi^\pm, K^\pm$        | $3.2 \text{ GeV}/c < p < 100 \text{ GeV}/c$                                   |
| $p^\pm$                 | $10 \text{ GeV}/c < p < 100 \text{ GeV}/c$                                    |
| Particle Identification |   |
| $\mu^\pm$               | $\Delta^{\mu/h} \log \mathcal{L} > 0$   |
| $\pi^\pm$               | $\Delta^{\pi/K} \log \mathcal{L} > 2$   |
| $K^\pm$                 | $\Delta^{K/\pi} \log \mathcal{L} > 2$   |
| $p^\pm$                 | $\Delta^{p/K} \log \mathcal{L} > 10$ & $\Delta^{p/\pi} \log \mathcal{L} > 10$ |



# Charm hadron reconstruction



- Vertex quality cuts
- PV & decay consistency
- $c\tau$  cut
- As similar as possible (a bit tighter for  $\Lambda_c$ )

## "3 $\sigma$ mantra"

- Daughter particles do not point to PV ( $>3\sigma$ )
- Mother particle does point to PV ( $<3\sigma$ )
- Mother particle has non-zero lifetime (except  $J/\psi$ )
- The decay structure is self-consistent

|                                  |                       | J/ $\psi$<br>$\mu^+\mu^-$ | D <sup>0</sup><br>$K^-\pi^+$ | D <sup>+</sup><br>$K^-\pi^+\pi^+$ | D <sub>s</sub> <sup>+</sup><br>$(K^+K^-)_\phi\pi^+$ | $\Lambda_c^+$<br>$pK^-\pi^+$ |
|----------------------------------|-----------------------|---------------------------|------------------------------|-----------------------------------|---|------------------------------|
| $y$                              |                       |                           |                              | $2 < y < 4$                       |   |                              |
| $p^T$                            | [GeV/c]               | $< 12$                    |                              | $3 < p^T < 12$                    |   |                              |
| $\chi^2_{\text{VX}}$             |                       | $< 20$                    | $< 9$                        | $< 25$                            | $< 25$  | $< 25$                       |
| $\chi^2_{\text{IP}}$             |                       | —                         |                              |                                   | $< 9$   |                              |
| $\chi^2_{\text{fit}}/\text{ndf}$ |                       |                           |                              | $< 5$                             |   |                              |
| $c\tau$                          | [ $\mu\text{m}$ ]     | —                         |                              | $c\tau \geq 100$                  |   | $c\tau \geq 100$             |
|                                  |                       |                           |                              |                                   |   | $c\tau < 500$                |
| $ \cos \theta^* $                |                       | —                         | $< 0.9$                      | —                                 | —   | —                            |
| $m_{K^+K^-}$                     | [GeV/c <sup>2</sup> ] | —                         | —                            | —                                 | $< 1.04$  | —                            |
| $\min p_T^{h\pm}$                | [GeV/c]               | —                         | —                            | —                                 | —   | $\geq 0.5$                   |



# Systematic uncertainties



- Dominant:  
hadron track  
reconstruction uncertainty  
related to hadron  
interactions in detector:  
*2% per hadron track*

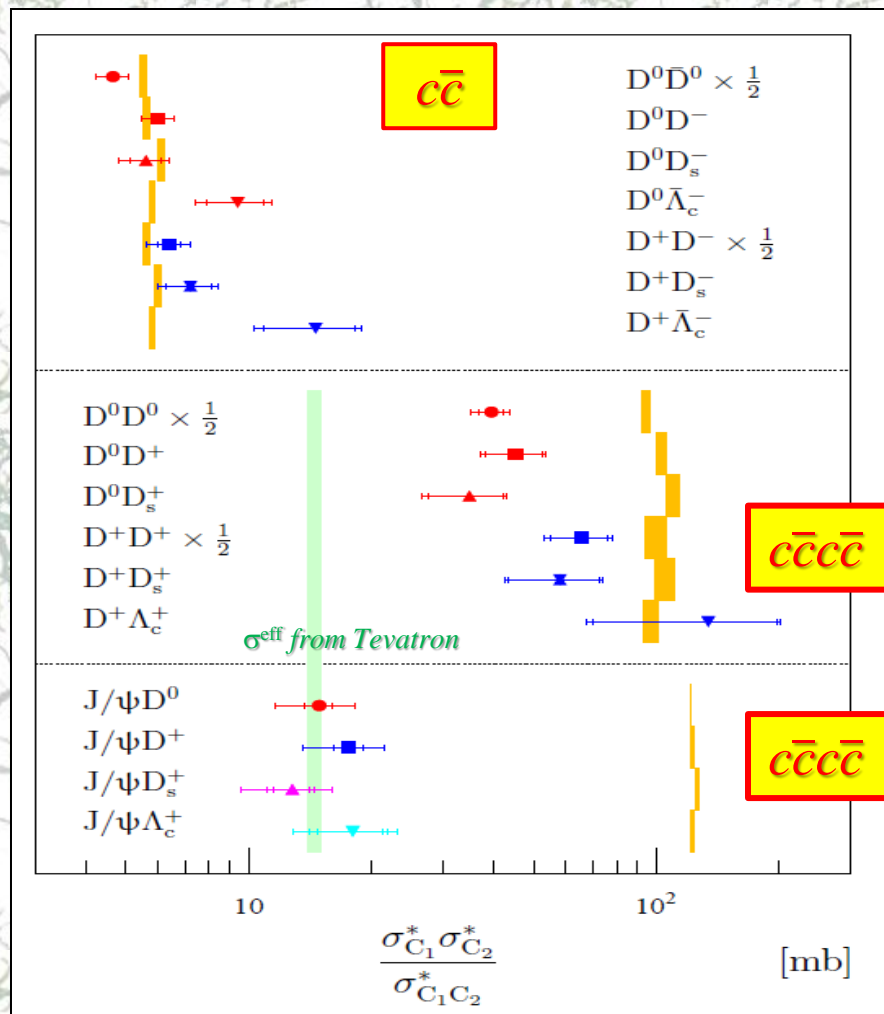
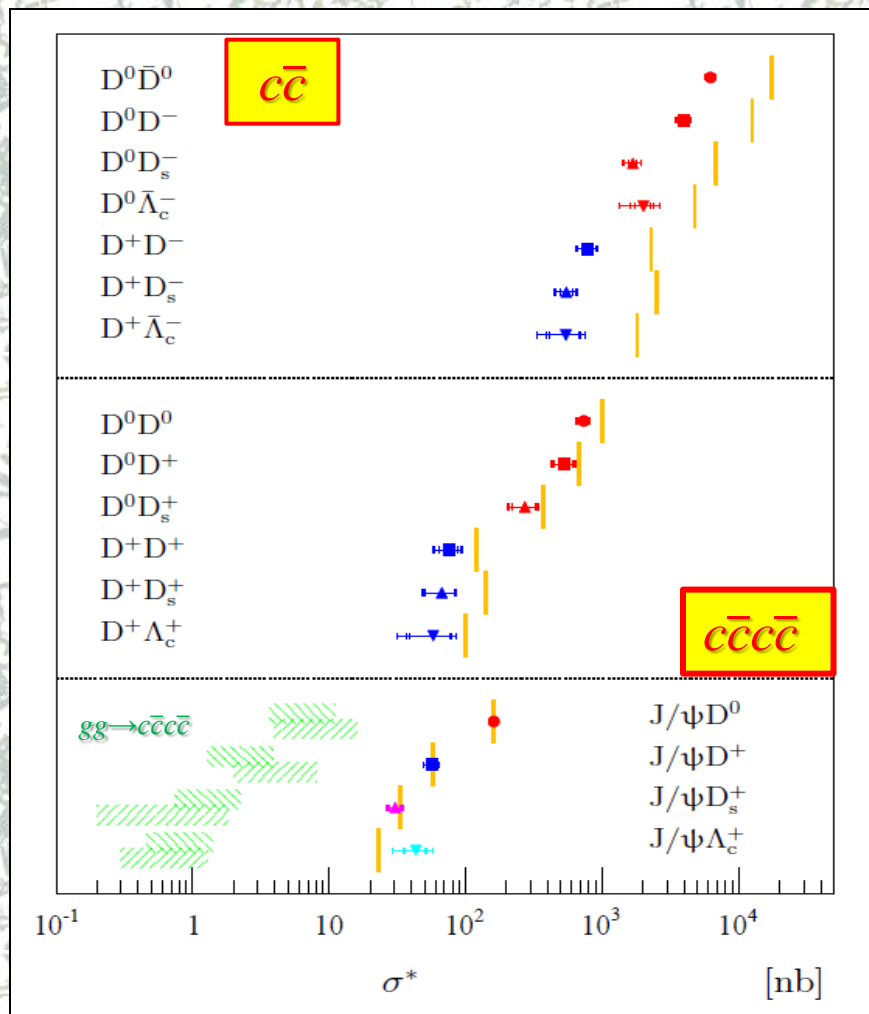
| Source  |  | $J/\psi D^0$ | $J/\psi D^+$ | $J/\psi D_s^+$ | $J/\psi \Lambda_c^+$ |
|---|--|--------------|--------------|----------------|----------------------|
| $J/\psi$ reconstruction                       | $\varepsilon_1^{\text{reco}}$          |              |              | 1.3            |                      |
| C reconstruction                              | $\varepsilon_2^{\text{reco}}$          | 0.7          | 0.8          | 1.7            | 3.3                  |
| Muon ID                                       | $\varepsilon_{J/\psi}^{\text{ID}}$     |              |              | 1.1            |                      |
| Hadron ID                                     | $\varepsilon_{\text{had}}^{\text{ID}}$ | 1.1          | 1.9          | 1.1            | 1.5                  |
| Tracking                                      | $\xi^{\text{trk}}$                     | 4.9          | 7.0          | 7.0            | 7.0                  |
| Trigger                                       | $\varepsilon_{J/\psi C}^{\text{trg}}$  |              |              | 3.0            |                      |
| $J/\psi$ polarization                         | $\varepsilon_{J/\psi}^{\text{reco}}$   |              |              | 3.0            |                      |
| Global event cuts                             | $\varepsilon^{\text{GEC}}$             |              |              | 0.7            |                      |
| Luminosity                                    | $\mathcal{L}$                          |              |              | 3.7            |                      |
| $\mathcal{B}(J/\psi \rightarrow \mu^+ \mu^-)$ | $\mathcal{B}_1$                        |              |              | 1.0            |                      |
| C branching ratios                            | $\mathcal{B}_2$                        | 1.3          | 4.3          | 6.0            | 26                   |
| Total   |  | 8            | 10           | 11             | 28                   |

| Source                                   |  | $D^0 D^0$ | $D^0 D^+$ | $D^0 D_s^+$ | $D^0 \Lambda_c^+$ |
|--|--|-----------|-----------|-------------|-------------------|
| $D^0 C$ reconstruction                   | $\varepsilon_2^{\text{reco}} \times \varepsilon_2^{\text{reco}}$ | 1.4       | 1.4       | 2.3         | 3.6               |
| Hadron ID                                | $\varepsilon_{\text{had}}^{\text{ID}}$                           | 1.2       | 1.8       | 1.6         | 2.4               |
| Tracking                                 | $\xi^{\text{trk}}$   | 8.5       | 10.7      | 10.6        | 10.6              |
| Trigger                                  | $\varepsilon_C^{\text{trg}}$                                     | 1.8       | 2.5       | 3.9         | 5.2               |
| Global event cuts                        | $\varepsilon^{\text{GEC}}$                                       |           |           | 1.0         |                   |
| Luminosity                               | $\mathcal{L}$  |           |           | 3.7         |                   |
| $\mathcal{B}(D^0 \rightarrow K^- \pi^+)$ | $\mathcal{B}_1$  |           |           | 1.3         |                   |
| C branching ratios                       | $\mathcal{B}_2$  | 1.3       | 4.3       | 6.0         | 26                |
| Total                                    |  | 10        | 12        | 14          | 30                |

| Source   |  | $D^+ D^+$ | $D^+ D_s^+$ | $D^+ \Lambda_c^+$ |
|--|--|-----------|-------------|-------------------|
| $D^+ C$ reconstruction                         | $\varepsilon_2^{\text{reco}} \times \varepsilon_2^{\text{reco}}$ | 1.4       | 2.2         | 4.0               |
| Hadron ID                                      | $\varepsilon_{\text{had}}^{\text{ID}}$                           | 2.3       | 2.4         | 3.0               |
| Tracking                                       | $\xi^{\text{trk}}$   |           | 12.8        |                   |
| Trigger  | $\varepsilon_C^{\text{trg}}$                                     | 3.7       | 5.8         | 5.0               |
| Global event cuts                              | $\varepsilon^{\text{GEC}}$                                       |           | 1.0         |                   |
| Luminosity                                     | $\mathcal{L}$  |           | 3.7         |                   |
| $\mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+)$ | $\mathcal{B}_1$  |           | 4.3         |                   |
| C branching ratios                             | $\mathcal{B}_2$  | 4.3       | 6.0         | 26                |
| Total  |  | 17        | 17          | 31                |



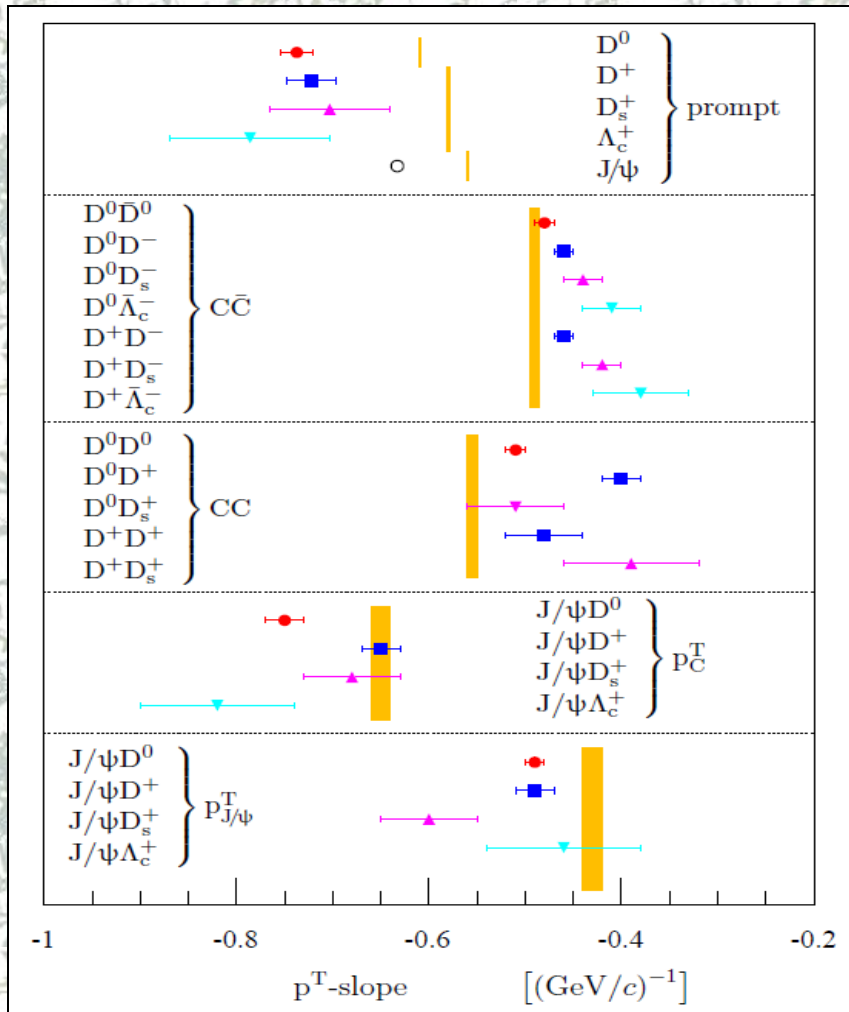
# Cross-sections & ratios







# $p^T$ -slopes: $3 < p^T < 12 \text{ GeV}/c$



- Fit with *exponential*
- “Similar” within each category
- C from  $J/\psi C$  is similar to single prompt C
- $J/\psi$  from  $J/\psi C$  is very different from prompt  $J/\psi$
- $CC$  and  $C\bar{C}$  are similar and both are very different from single prompt C