

The FAST experiment: A precise measurement of the muon lifetime τ_μ

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on behalf of the **FAST Collaboration**

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CERN ¹



CIEMAT ²



UNIGE ³

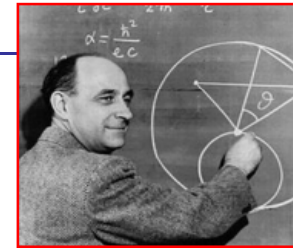


PSI ⁴



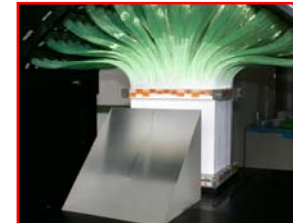
OUTLINE

- **Goal of the experiment & Theoretical motivations**



- **The FAST experiment**

- general experimental concept
- description of the setup elements



(beam; target; readout; DAQ; LV2 trigger)

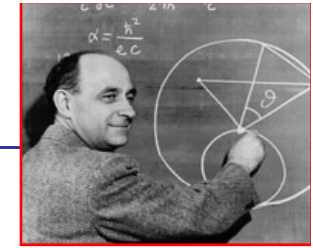
- **First Muon Lifetime Measurement**

- run 2006 **data sample**
- analysis procedure (from raw data to histograms)
- fit procedure (i.e. **muon lifetime measurement**)
- study of the **systematic uncertainty**



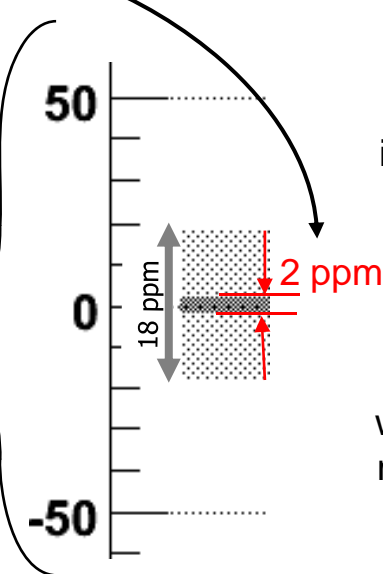
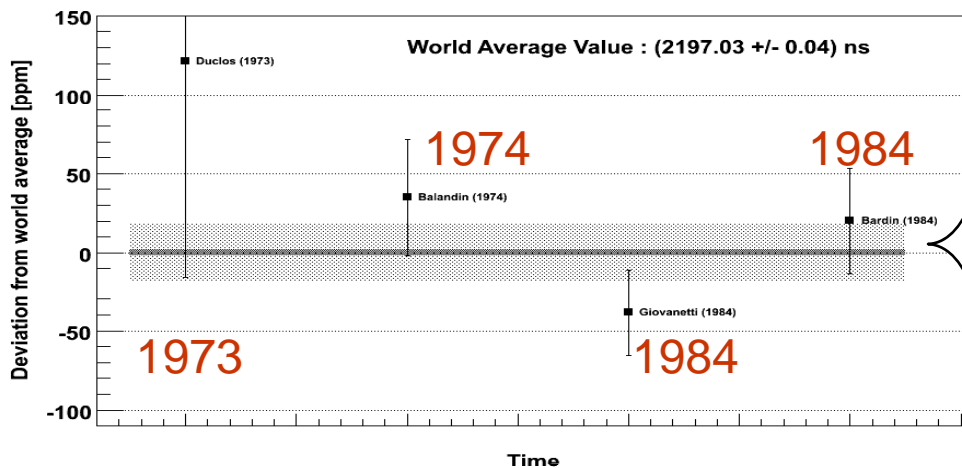
- **Conclusions & Future plans**

GOAL OF THE EXPERIMENT & MOTIVATIONS



FAST goal : precision measurement of the muon lifetime
 $\delta\tau_\mu/\tau_\mu \sim 2 \text{ ppm}$ [$\sim 4\text{ps}$]

Past muon lifetime measurements [PDG 06]



ULTIMATE FAST GOAL
 One order of magnitude improvement on the current world average

PRESENT ANALYSIS
 (2006 data sample):
 world average competitive muon lifetime measurement
 - as single experiment -

$$\tau_\mu^{-1} = \frac{G_F^2 m_\mu^5}{192\pi^3} (1 + \Delta q)$$

$$\frac{\delta\tau_\mu}{\tau_\mu} = 2 \text{ ppm} \Rightarrow \frac{\delta G_F}{G_F} = 1 \text{ ppm}$$

At present, the (exp) accuracy on τ_μ is the limiting factor for an improved precision on the Fermi Constant G_F

$$\left(\frac{\delta G_F}{G_F}\right)_{exp} = \frac{1}{2} \frac{\delta\tau_\mu}{\tau_\mu} - \frac{5}{2} \frac{\delta m_\mu}{m_\mu} + \left(4 \frac{m_{\nu_\mu}^2}{m_\mu^2}\right)$$

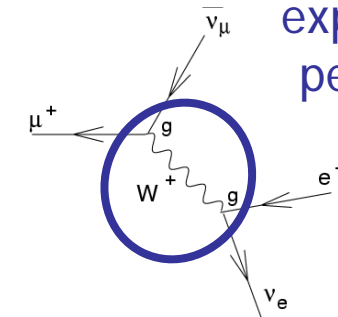
$$\left(\frac{\delta G_F}{G_F}\right)_{th.} = 0.3 \text{ ppm}$$

9 ppm

0.2 ppm

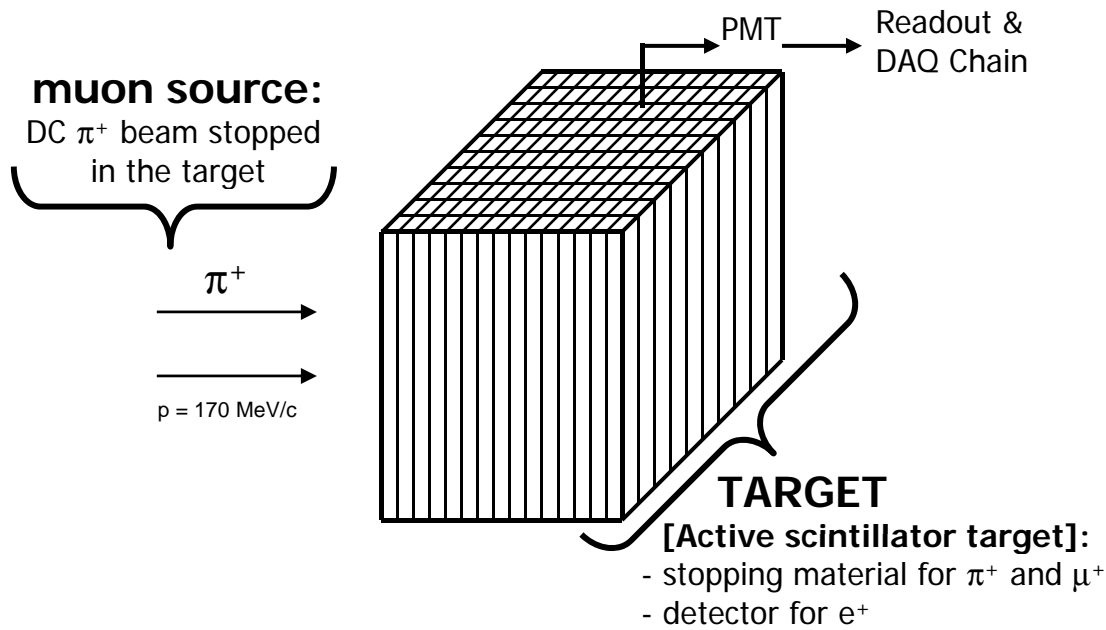
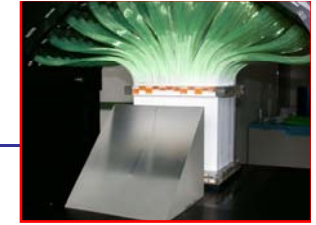
< 13 ppm

Ritbergen & Stuart,
 Phys.Rev.Lett. 82, 488 1999



FAST: high energy experiment performed at low energy scale

THE FAST EXPERIMENT



SIGNATURE FOR AN EVENT [$\pi \rightarrow \mu \rightarrow e$] :

- $\pi^+ \rightarrow \mu^+ \nu_\mu$ ($\tau_\pi \sim 26 \text{ ns}$) $E_\mu^{cin} \sim 4 \text{ MeV}$
 $\rho_\mu \sim 1.5 \text{ mm}$
- $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$ ($\tau_\mu \sim 2.2 \mu\text{s}$)

Signature:

- π^+ & μ^+ close in time & space [high pulses]
- e^+ track [mip's]

Size of the
statistical sample
→ max achievable precision

$$\frac{(\delta\tau)_{stat}}{\tau} = \frac{1}{\sqrt{N_{events}}}$$

$$\frac{\delta\tau_\mu}{\tau_\mu} \sim 2 \text{ ppm} \Rightarrow N_{events} \geq 2.5 \times 10^{11}$$

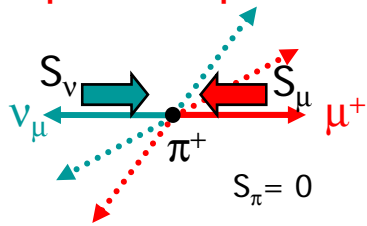
PARALLELISATION needed

i.e. treat more $\pi \rightarrow \mu \rightarrow e$ events at
the same time inside the target:

- High granularity of the target
- Tracking capabilities
- Ability to disentangle overlapping events
- High beam rate
- Huge data rate throughput
- Systematics under control

MUON SOURCE (i.e. DC π^+ BEAM)

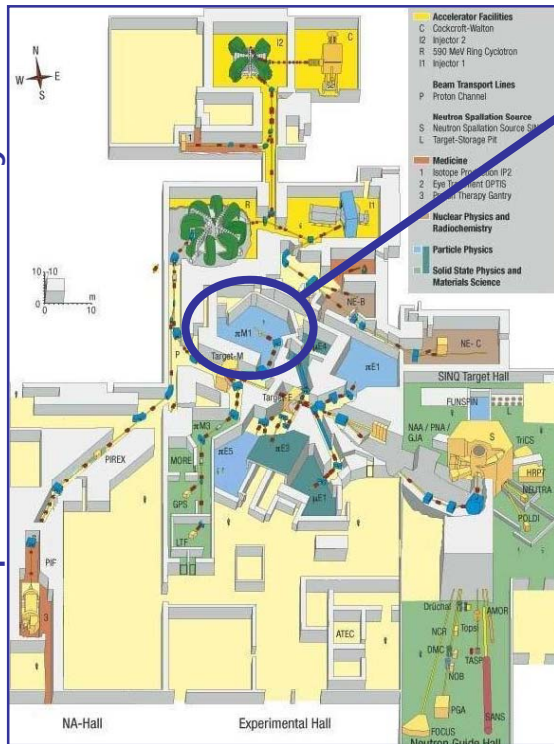
μ source = π decay at rest in the target
 → isotropic & unpolarized μ source



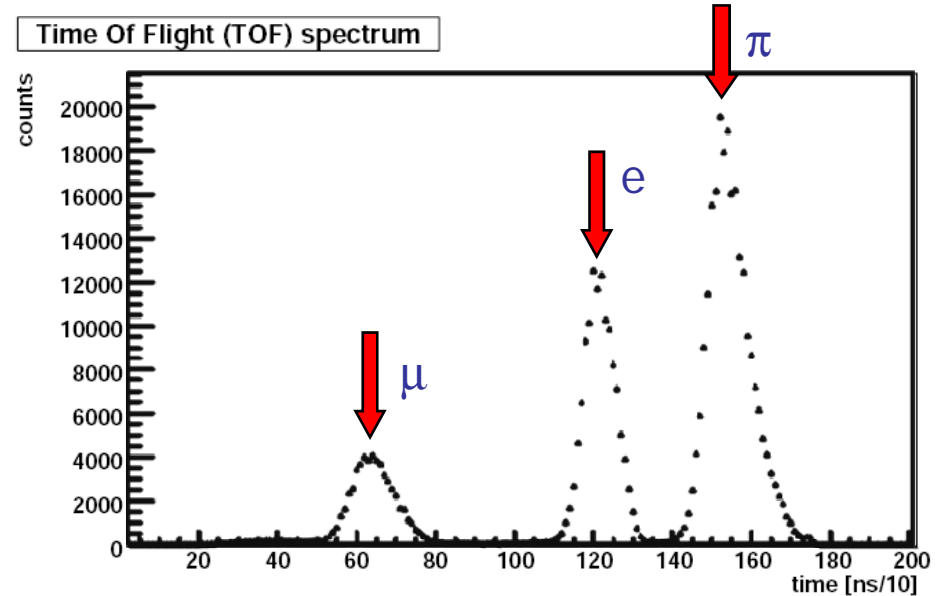
π M1 area at PSI :

- π M1 : π^+ DC beam
- momentum : **170 MeV/c** ($\pm 3\%$)
- RF frequency : 50.633 MHz (T=19.75 ns)
- beam size : variable (**$\sim 10 \times 10 \text{ cm}^2$**)
- intensity : variable (**$\sim 500 \text{ kHz}$**)
- purity : **$\sim 50\%$**

PSI Experimental Hall - layout

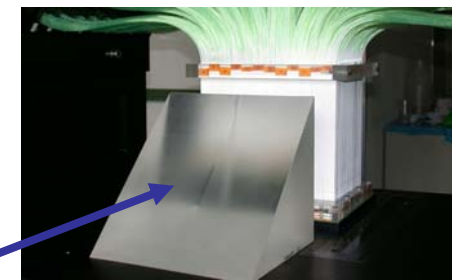
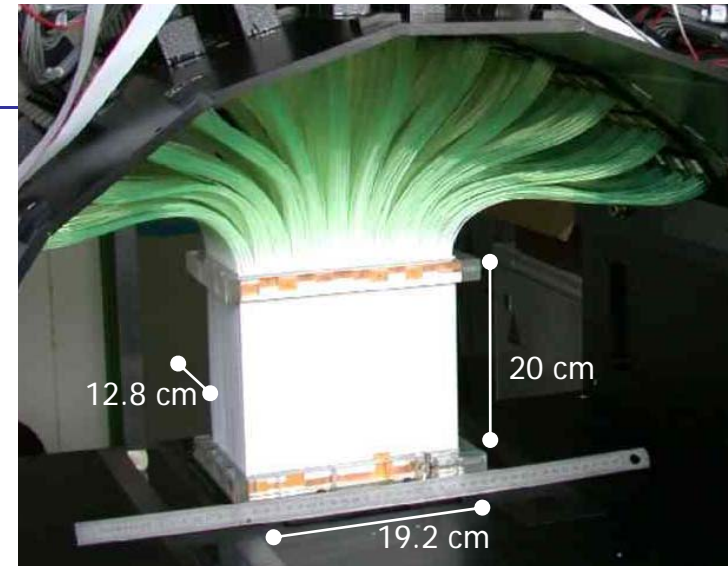


Time Of Flight (TOF) spectrum



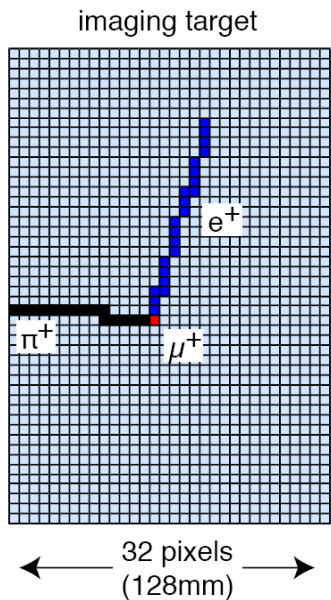
TARGET

- Active target :
 - stopping material for π^+/μ^+
 - detector for the particles
- Solid plastic scintillator (Bicron BC400)



- high granularity
- tracking capabilities
- fast imaging detector
- identical replicated **mini-detectors (pixels)**
- vertical arrangement 32 x 48

- wedge beam degrader to achieve a uniform distribution of the stopping pion points



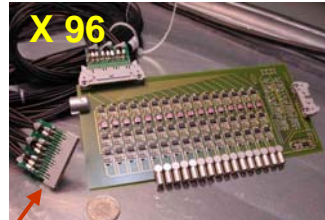
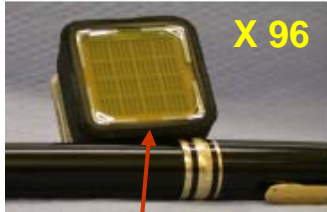
- **1536 pixels**
- 1 pixel = 1 scintillator bar ($4 \times 4 \times 200 \text{ mm}^3$) with 2 WLSF

BC400 solid plastic scintillator plates - 4x4x200mm³ bars - two grooves machined 2 WLSF (BCF-92) inserted and glued into the grooves diffusive reflective paint (BC-620) - bundle of 4x4 pixels [96 bundles] - fibers housed in a special mask



FAST READOUT & DAQ CHAIN

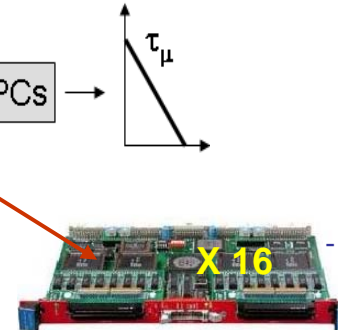
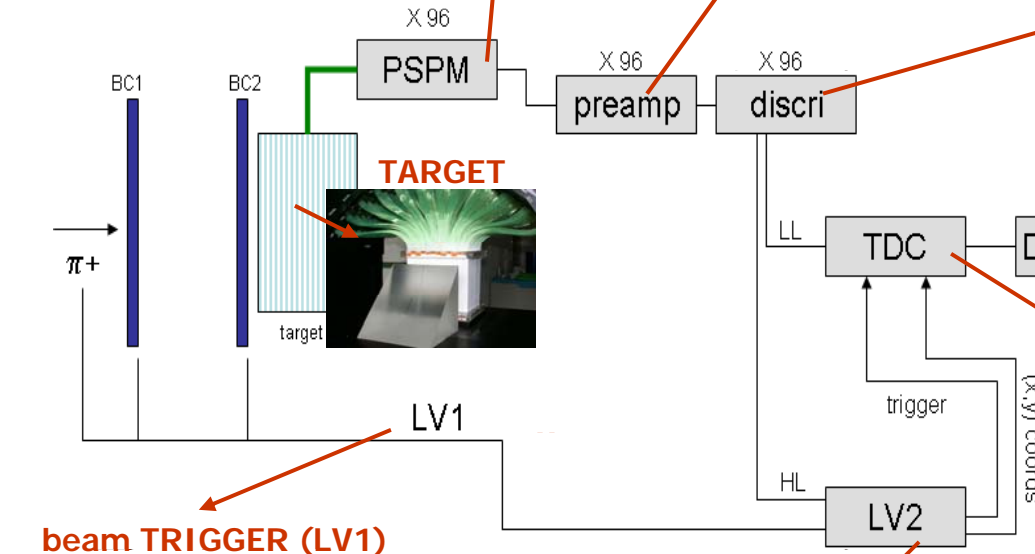
- Position Sensitive **PhotoMultipliers (PSPM's)**
- Hamamatsu H6568-10
- multianode (4x4)



- **Preamplifiers**
- shaper & preamp (x5)
- custom made units (PSI)



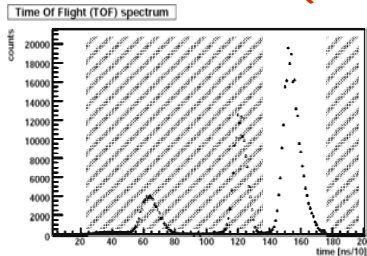
- **Double THR discriminators**
- LOW (LL) & HIGH (HL)
- LL → mip's (e⁺ tracks)
- HL → π⁺ / μ⁺ (stop points)
- remotely adjustable thr (50 mV – 2 V)
- custom made units (PSI)



- **CAEN v767 128-channs TDCs**

- time stamping of the raw pulses from discrici
- TDC time window: [-10, +20]μs w.r.t. Trigger
- trigger : π in the target (entry/π stop time)
- output of the TDCs: into the DAQ PC's

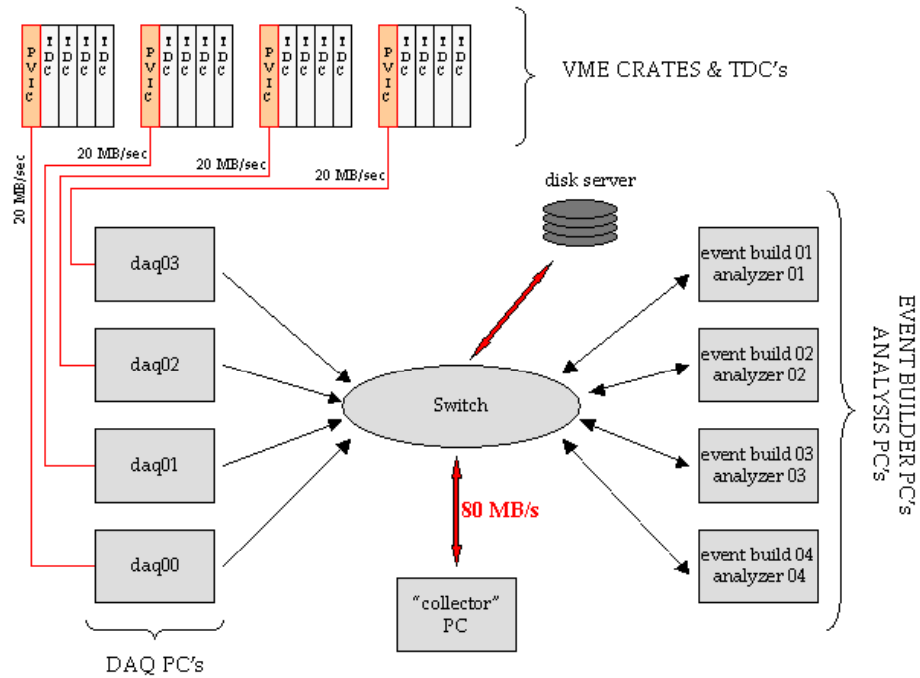
beam TRIGGER (LV1)



Second Level TRIGGER (LV2)

- Hardware trigger for the TDCs
- Selective trigger (definition of ROI, around the pion stopping point)
- Event quality selection
- **DATA REDUCTION SYSTEM**
- Custom made FPGA based electronics (CIEMAT)

DAQ ARCHITECTURE

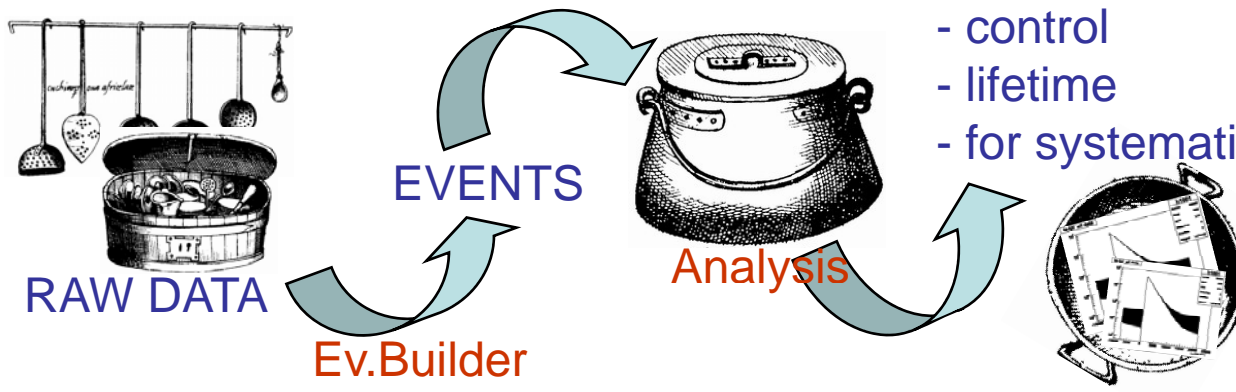


- 16 TDC's in 4 VME crates
 - VME-PCI interface: PVIC link (20 MB/s/node)

80 MB/sec (~ 7 TB/day):
max allowed data rate

- This has to be **ONLINE**
- The full set of data cannot be stored on disk
- Only histograms are saved as the output of the analysis process
- Histo: control, lifetime, syst

HISTOGRAMS:
 (~ 1200 histos)
 - control
 - lifetime
 - for systematics





RUN 2006

&

MUON LIFETIME
ANALYSIS

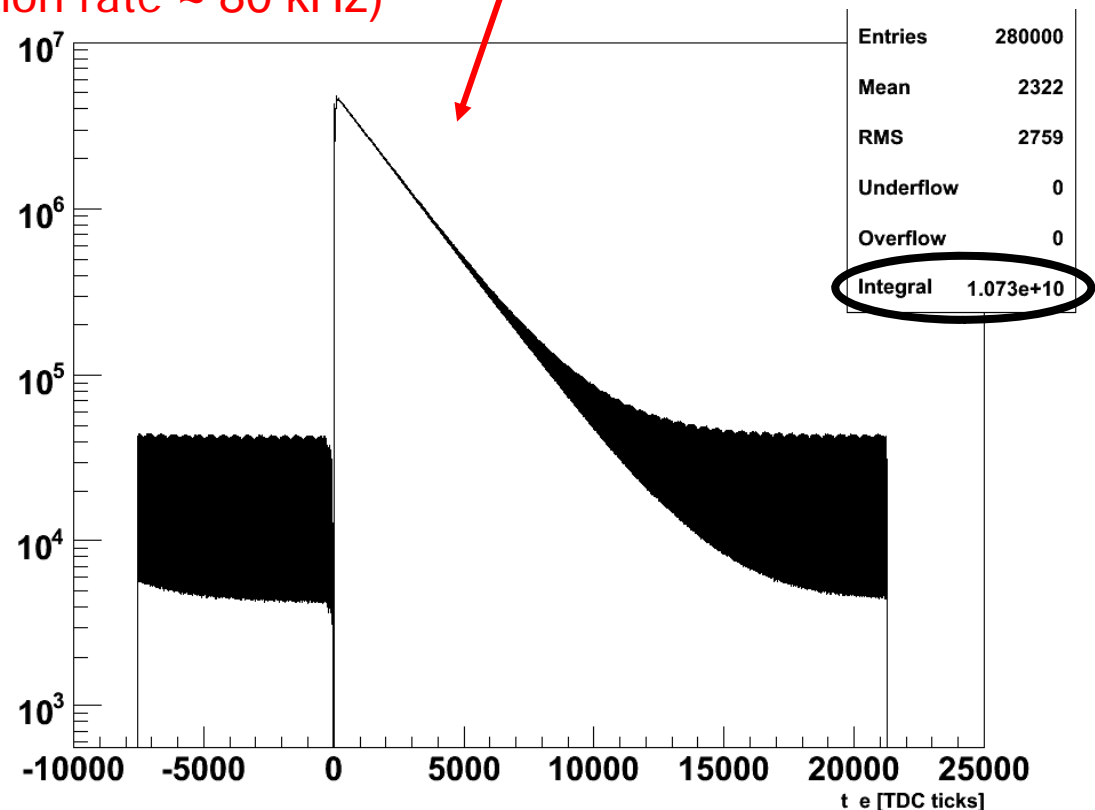
RUN 2006: DATA SAMPLE

- **3 weeks data taking** (Nov – Dec 2006)
- first physics data taking run for FAST
- running conditions very close to the final one except for the reduced adopted rate :
LV2 trigger rate ~ 30 kHz (pion rate ~ 80 kHz)

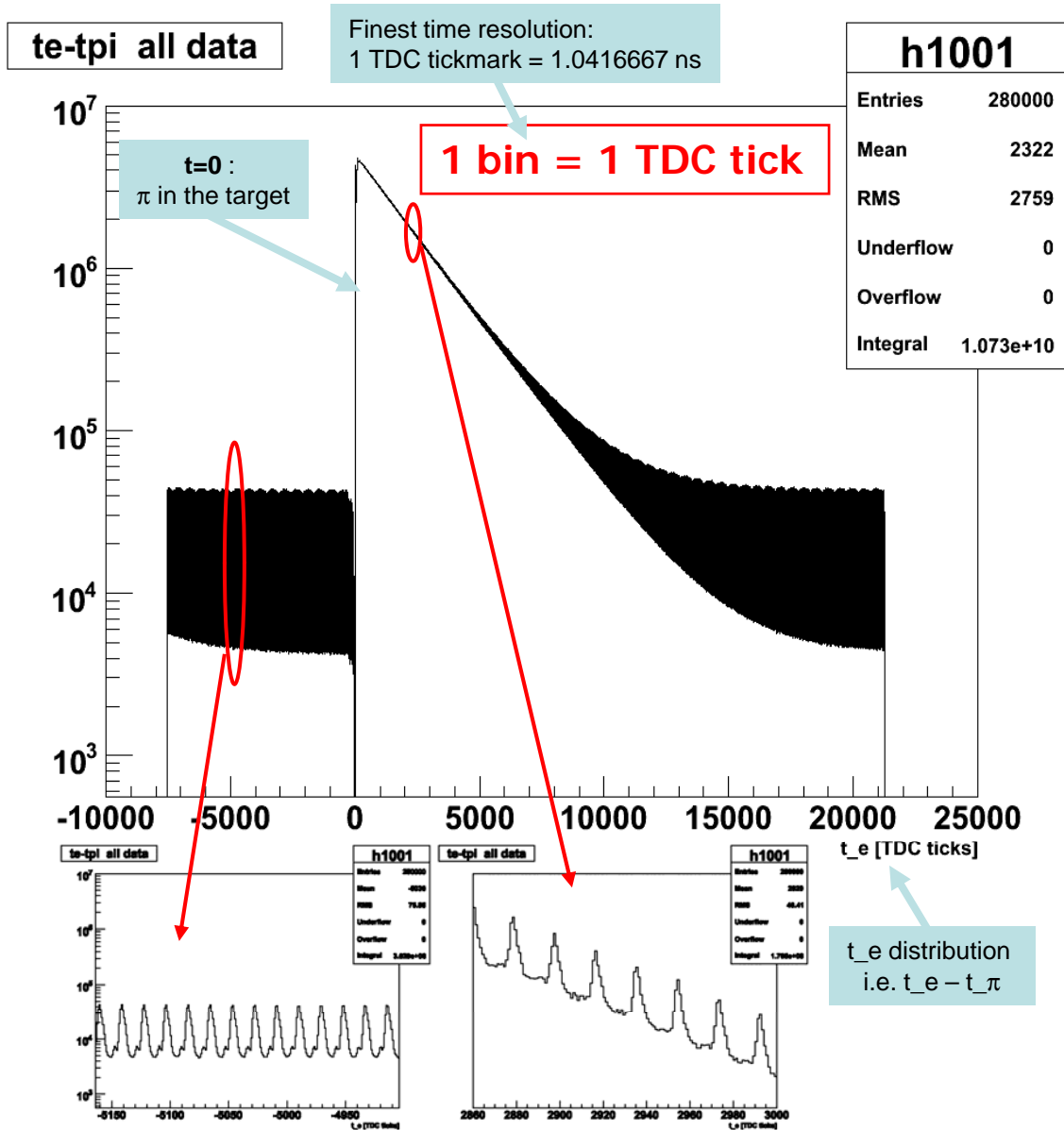
- **total statistics :**
 1.073×10^{10} events
→ precision comparable with world average

« THE » PLOT
Muon lifetime histogram

t_e distribution i.e. $t_e - t_\pi$
[in TDC tickmarks]



MUON LIFETIME HISTOGRAM

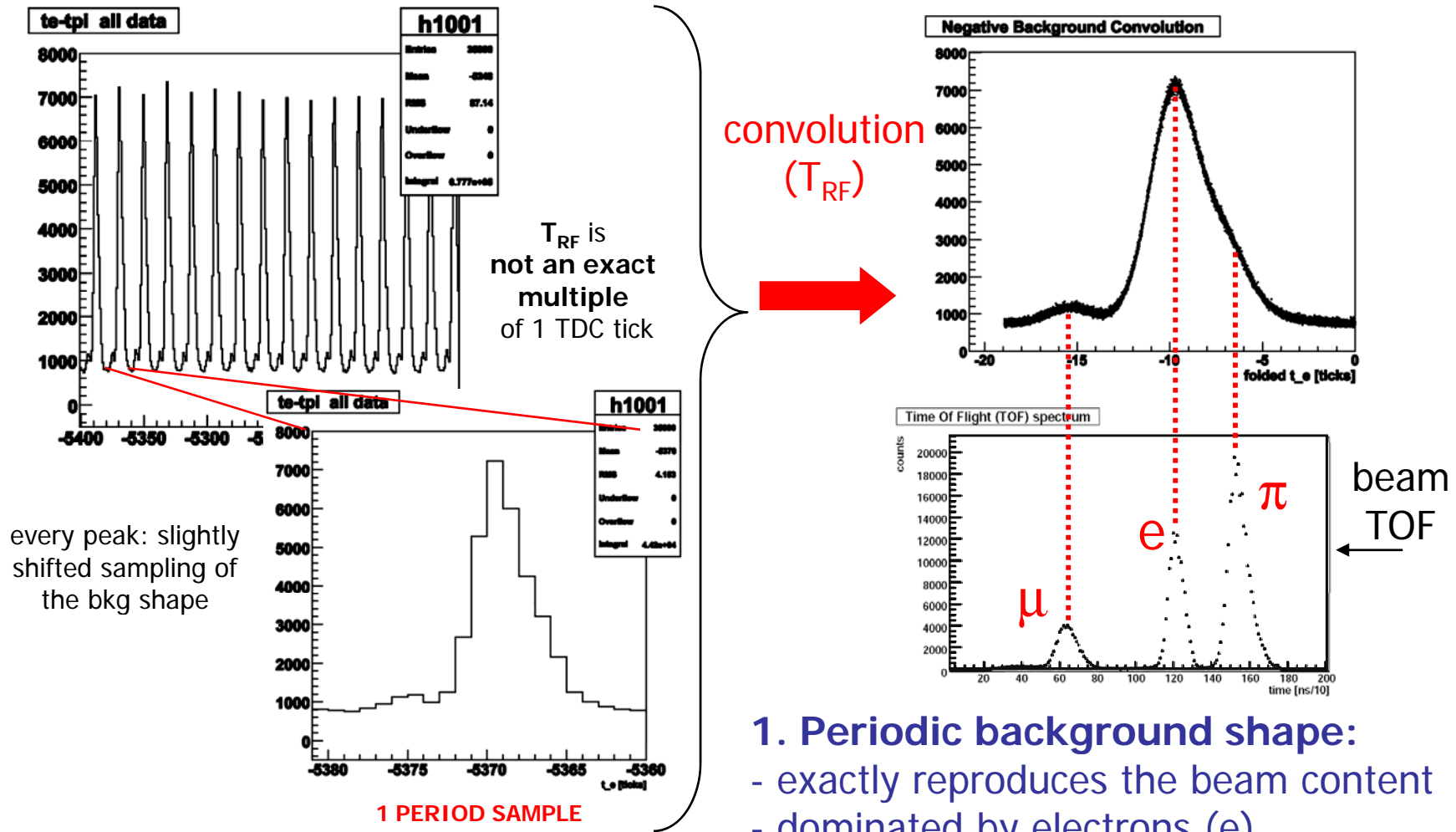


- **negative times (pure bkg events)**
description of the background (totally decoupled from the signal) from the negative times region
- & **positive times (signal+bkg)**
use the background description also for the positive times region
- **background: flat component**
no time dependent
- + RF periodicity structure (T_{RF})
beam induced background

measure $\tau_\mu = \text{fit distribution}$

- Fine binning distribution → study and understand all the structures of the data
→ RF structure
→ TDC non linearity
- Rebin the histogram (new bin = T_{RF}) to minimize the effects of the periodic background on the lifetime measurement
- Define a proper fitting function
- Binned maximum likelihood fit (TMinuit-ROOT) with τ_μ as free parameter

STEPS FOR THE FIT: 1. understand the background (t<0)



- 1. Periodic background shape:**
- exactly reproduces the beam content
 - dominated by electrons (e)

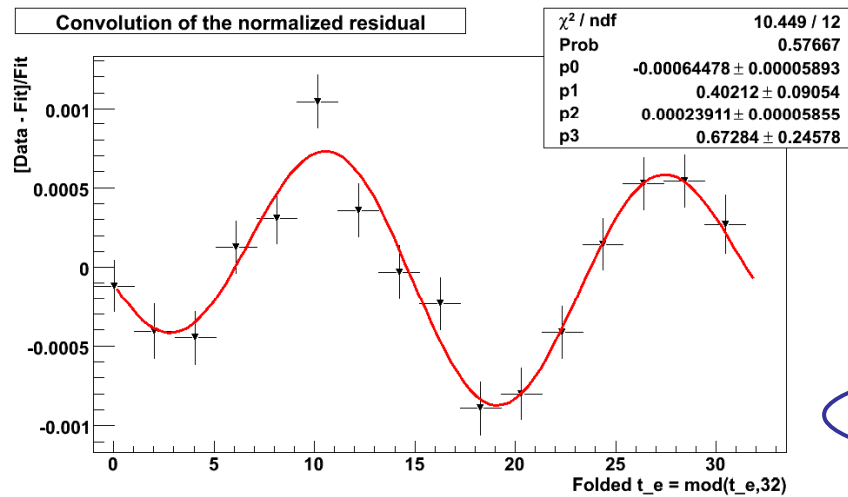
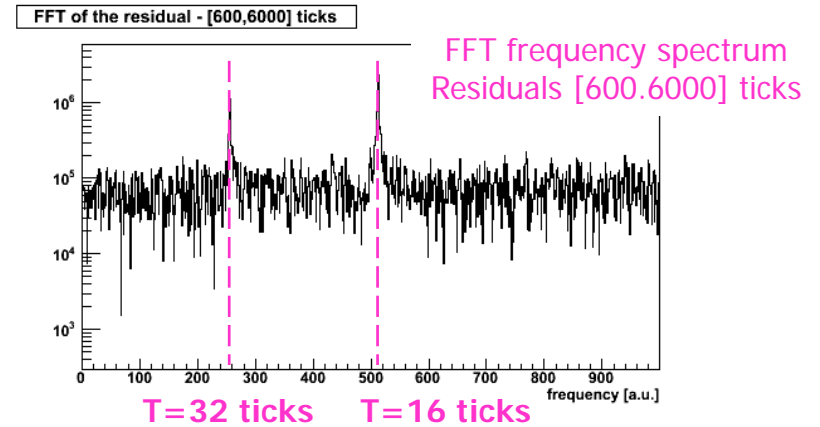
2. Extraction of the exact RF period from the fit of the negative background:

- $T_{RF} = (18.960051 \pm 0.000003)$ ticks \rightarrow 0.2 ppm

STEPS FOR THE FIT: 2. periodic structures in the data (t>0)

- Positive times region fit
- Fast Fourier Transform of its residual
- Convolution applied on the residual (T = 32)

↓ mod(t,32)



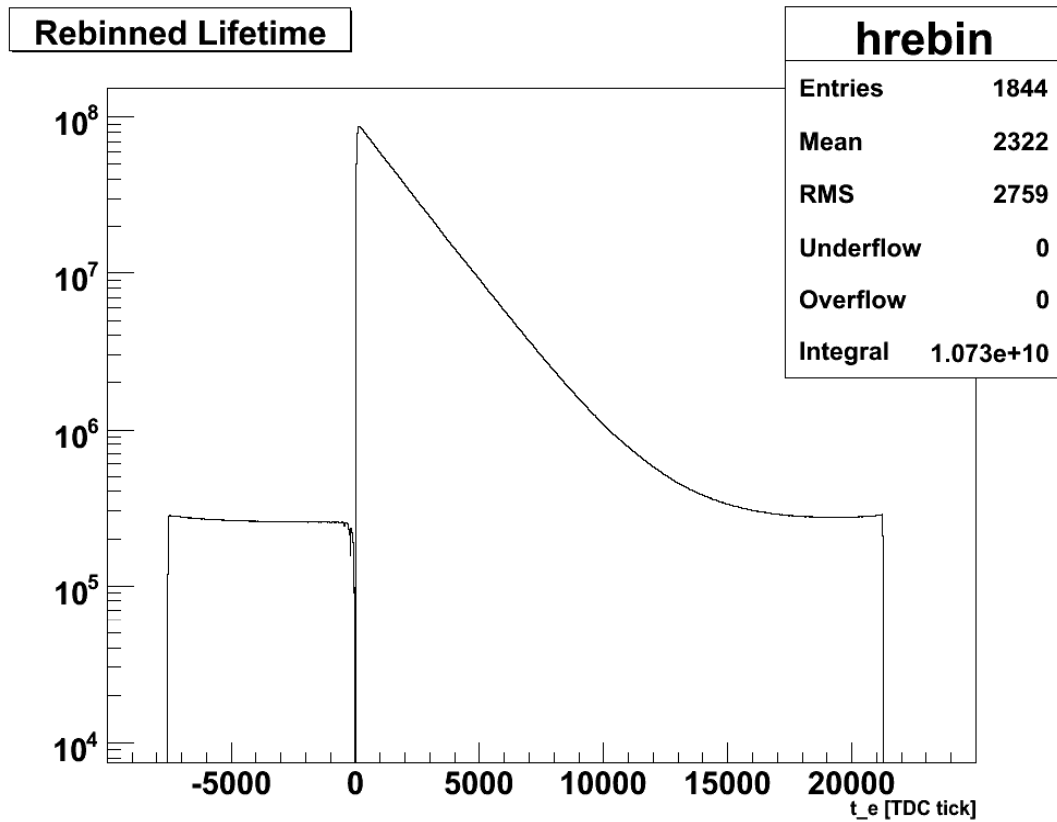
$$F_{tdc}(t) = p_1 \sin\left(\frac{2\pi t}{16} + p_2\right) + p_3 \sin\left(\frac{2\pi t}{32} + p_4\right)$$

Fitting function: $N(t) \longrightarrow [1 + F_{tdc}(t)] \times N(t)$

- TDC non linearity effects [TDC CLK = 32 ticks]
- per mille level effect
- confirmed also in lab tests

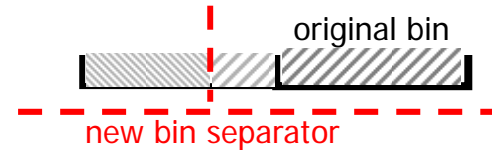
STEPS FOR THE FIT: 3. rebin the histogram

- Rebin the histogram** using the measured beam period T_{RF}
 - to minimize the influence of the periodic background on τ_{μ} measurement
 - information loss – but only on the details of the background, not the lifetime



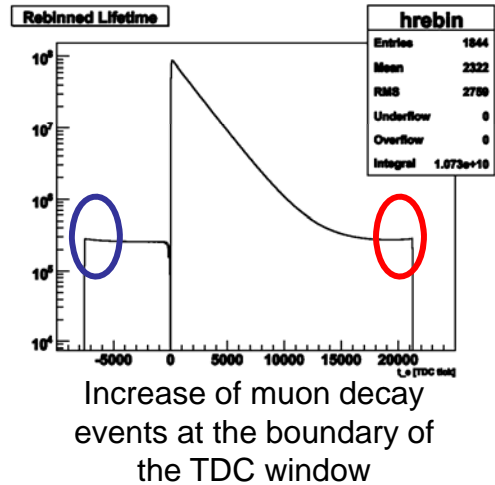
T_{RF}
 1 new bin = 18.960051 original bins

“SMART REBIN”
 i. e. rebin + bin sharing procedure :

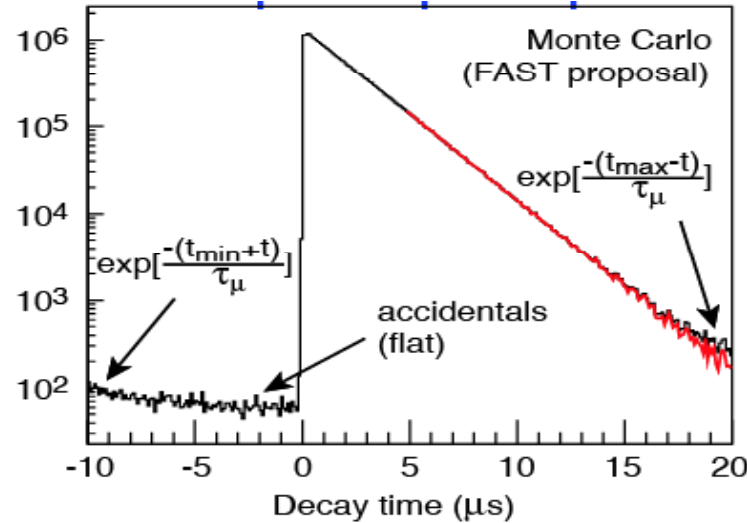


- different algorithms tried (uniform, linear, quadratic, exp) for the sharing of evts inside the original bin
 - no appreciable differences found (see systematics)
- default: uniform distribution inside the bin

STEPS FOR THE FIT: 4. boundary effects in the lifetime distr.



Already foreseen in the systematic study with MC simulations



Due to overlapping events in the TDC window $[t_{min}, t_{max}]$

(π_1, μ_1, e_1)

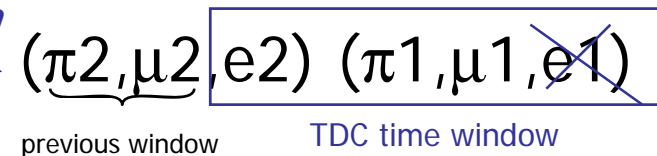
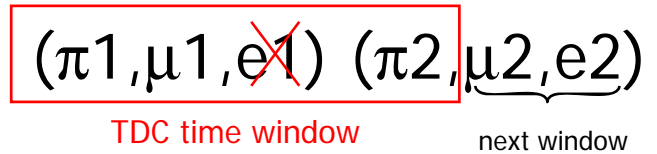
(π_1, μ_1, X)

(π_2, μ_2, e_2)

$X = \text{beam pcl} \rightarrow \text{beam induced bkg}$

$X = \pi_2 \rightarrow (\pi_1, \mu_1, \pi_2) \rightarrow \text{peaked at } t_{max}$

$X = e_2 \rightarrow (\pi_1, \mu_1, e_2) \rightarrow \text{peaked at } t_{min}$

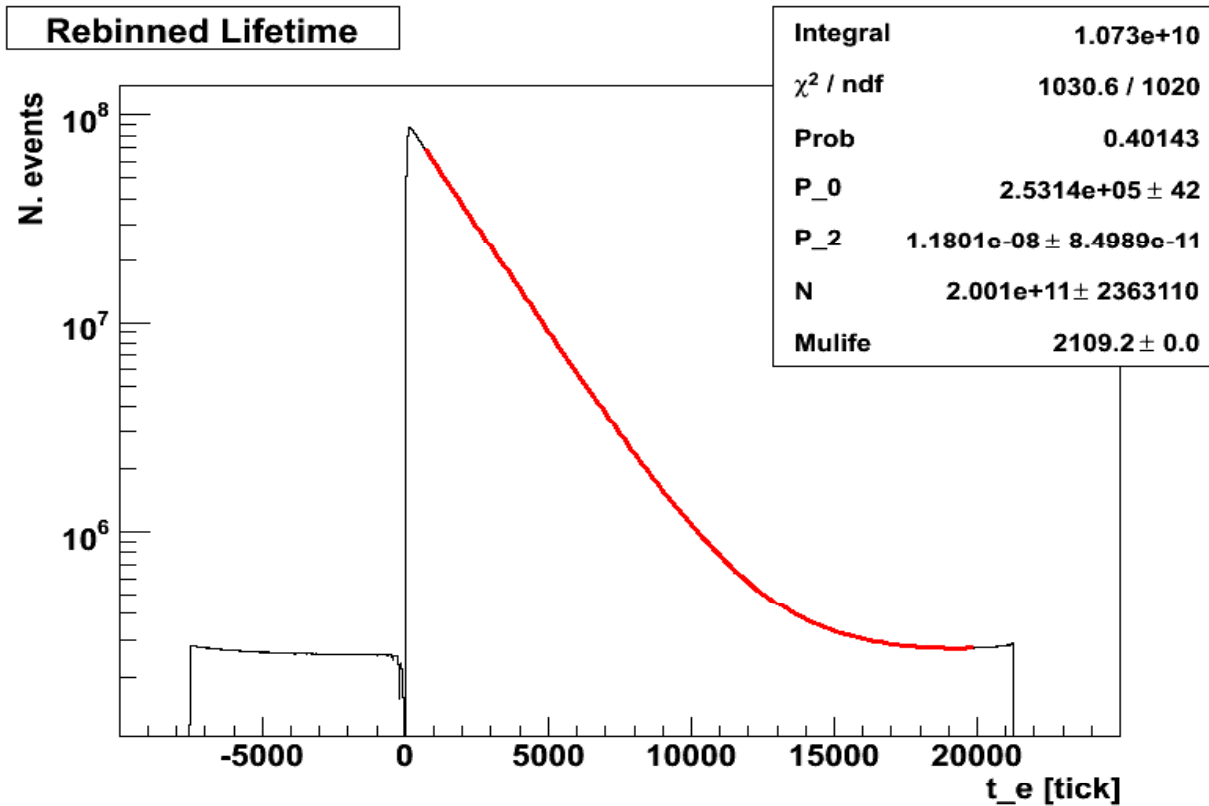


THE FIT

$$N(t) = [1 + F_{tdc}(t)] \times \left[P_0 + \frac{N_0}{\tau} (e^{-t/\tau} + P_2 e^{t/\tau}) \right]$$

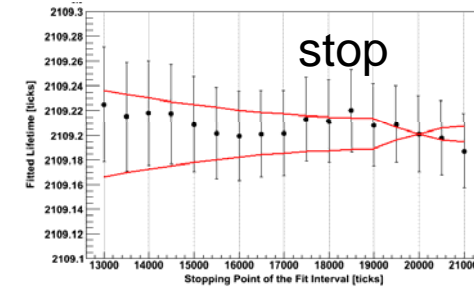
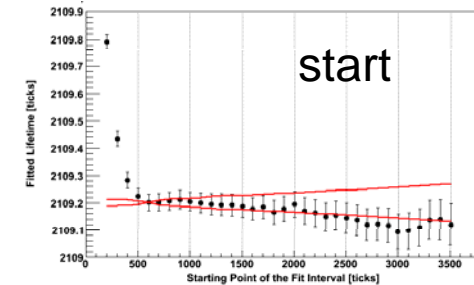
TDC non linearity
Accidental bkg
Signal
Time dependent background

no precise description of the periodic beam induced background is required



→ VERY HIGH QUALITY FIT

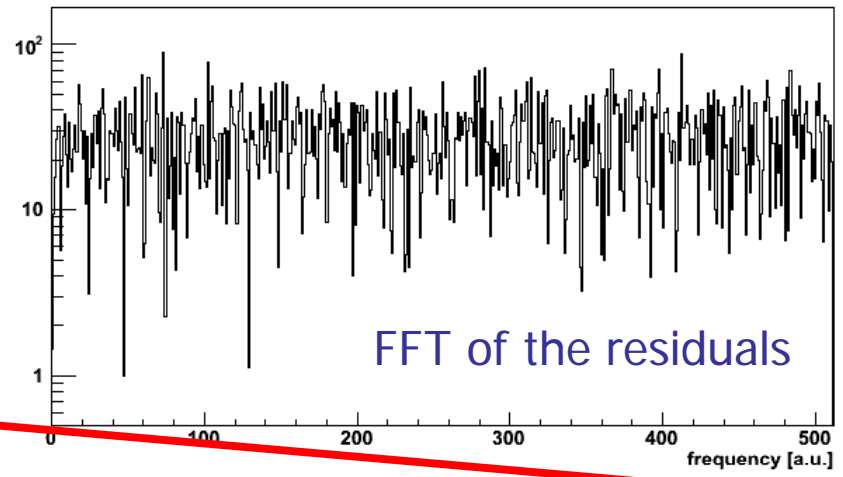
- Fit interval: [600,20000] ticks
Largest region of stable lifetime



FIT QUALITY

| | | |
|----------------------------------|-----------------------|--|
| Full Statistics Sample (Run2006) | | Fit: [600, 20000] ticks |
| Smart Rebin Method | | |
| χ^2/ndf | 1030.65/1020 = 1.0104 | |
| Prob(χ^2, ndf) | 0.4014 | |
| Fitted Parameters | | |
| Offset | P_0 | 253135 ± 39 |
| Exp. Tail Norm. | P_2 | $(1.180 \pm 0.008) \times 10^{-8}$ |
| Normalization | N_0 | $(2.00104 \pm 0.00002) \times 10^{11}$ |
| Lifetime [ticks] | τ | 2109.200 ± 0.031 |

FFT of the residual - [600,20000] ticks



| | P_0 | P_2 | N_0 | τ |
|--------|--------|--------|--------|--------|
| P_0 | 1.000 | -0.714 | -0.104 | -0.498 |
| P_2 | 0.714 | 1.000 | 0.084 | 0.335 |
| N_0 | -0.104 | 0.084 | 1.000 | -0.157 |
| τ | -0.498 | 0.335 | -0.157 | 1.000 |

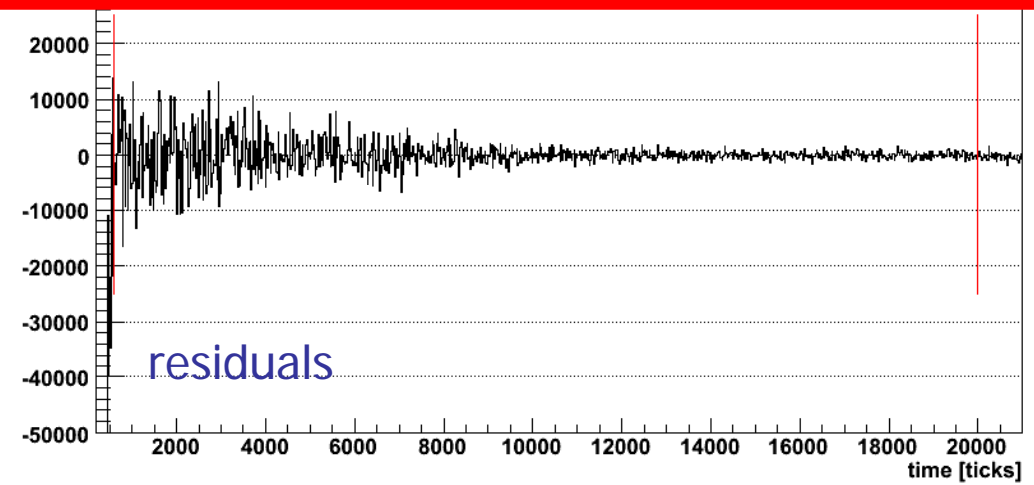
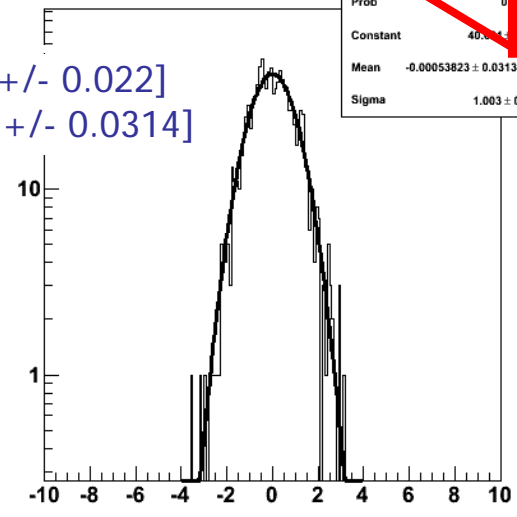
$$\tau_\mu = [2197.083 \pm 0.032] \text{ ns}$$

$$\left(\frac{\delta\tau_\mu}{\tau_\mu} \right)_{stat} = 15 \text{ ppm}$$

Pull = [Histo-Fit] / sqrt(Fit)

| | |
|---------------------|--------------------------|
| χ^2/ndf | 73.3 |
| Prob | 0 |
| Constant | 40.0 |
| Mean | -0.00053823 ± 0.03138592 |
| Sigma | 1.003 ± 0.022 |

$\sigma = [1.003 \pm 0.022]$
 $X = [-0.0005 \pm 0.0314]$



SYSTEMATICS STUDY

- Evaluated with **several dedicated histograms (produced online)**
- **Different classes of systematic errors studied**, with different sets of specific lifetime histograms
- **General recipe:**
 - Any deviation inconsistent with the statistical fluctuations is considered to be of systematic origin
 - **A PRIORI consistency criteria = 3 sigma's**
 1. Fit histograms corresponding to the sub-samples & compute the average
 2. Look if there are statistically incompatible points (i.e. deviation from the average $\Delta\tau_\mu > 3\sigma$)
 3. How much the average changes when those points are excluded
 4. Quote this variation as (signed) systematic shift

SUMMARY TABLE OF SYSTEMATICS

| Source of systematic | $\Delta\tau_\mu$ [ticks] | $\Delta\tau_\mu$ [ppm] |
|---|--------------------------------|-----------------------------|
| * Homogeneity of the Target | +0.016 | +7.6 |
| Fit Method | -0.011 | -5.2 |
| Lifetime Estimator (i.e. $t_e - t_\mu$ vs $t_e - t_\pi$) | +0.004 | +1.8 |
| μ SR and Isotropy of the Target | - | < 1 |
| * Time Stability (i.e. clock) | - | < 1 |
| * Beam Rate | - | < 1 |
| TDC performance (i.e. time smearing) | - | < 1 |
| TOTAL | ± 0.0137 | ± 6.5 |

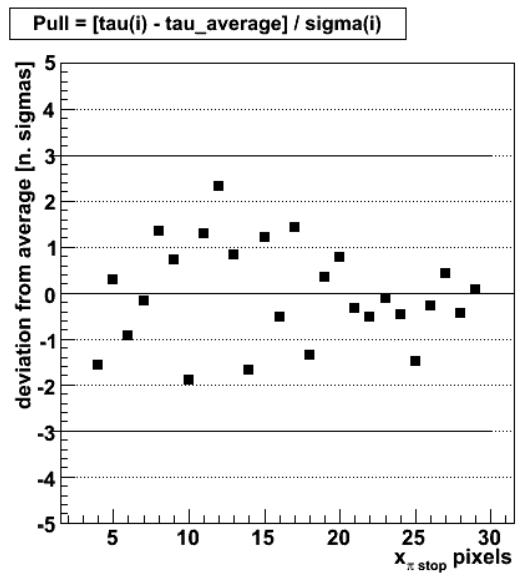
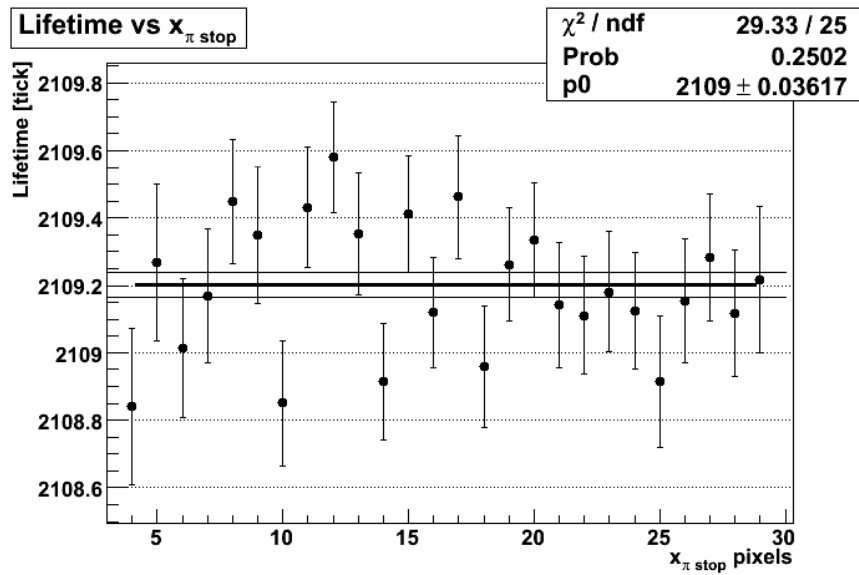
→ At present, the determination of the systematic uncertainty is limited by the statistics

→ There is no evidence of large systematic effects

* Examples described here

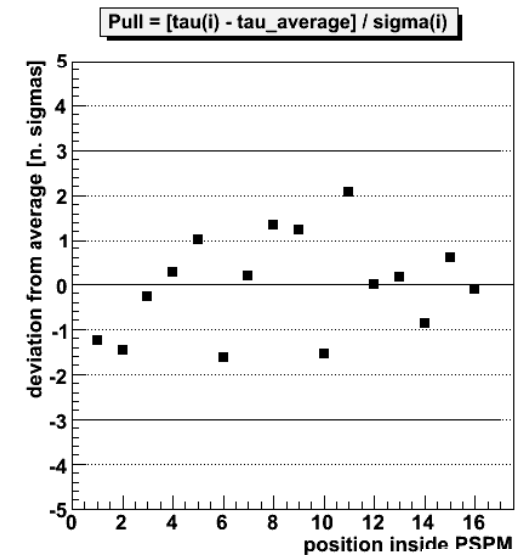
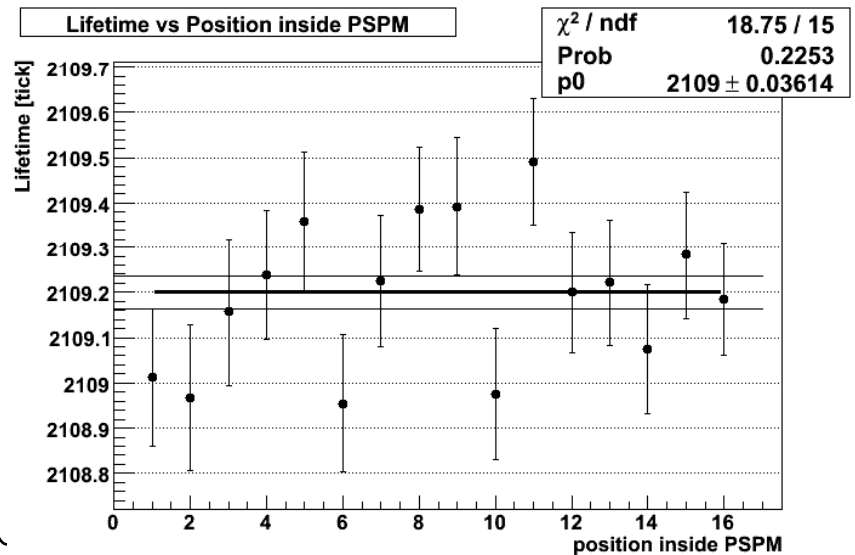
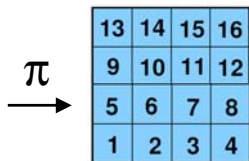
SYSTEMATICS: HOMOGENEITY OF THE TARGET

2 examples for no evidence of a systematic effect beyond the expected statistical fluctuations



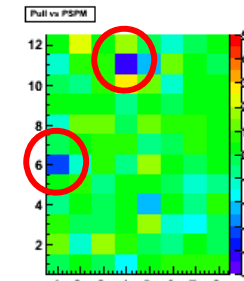
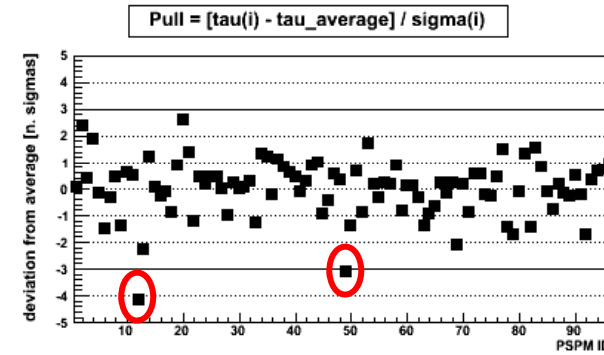
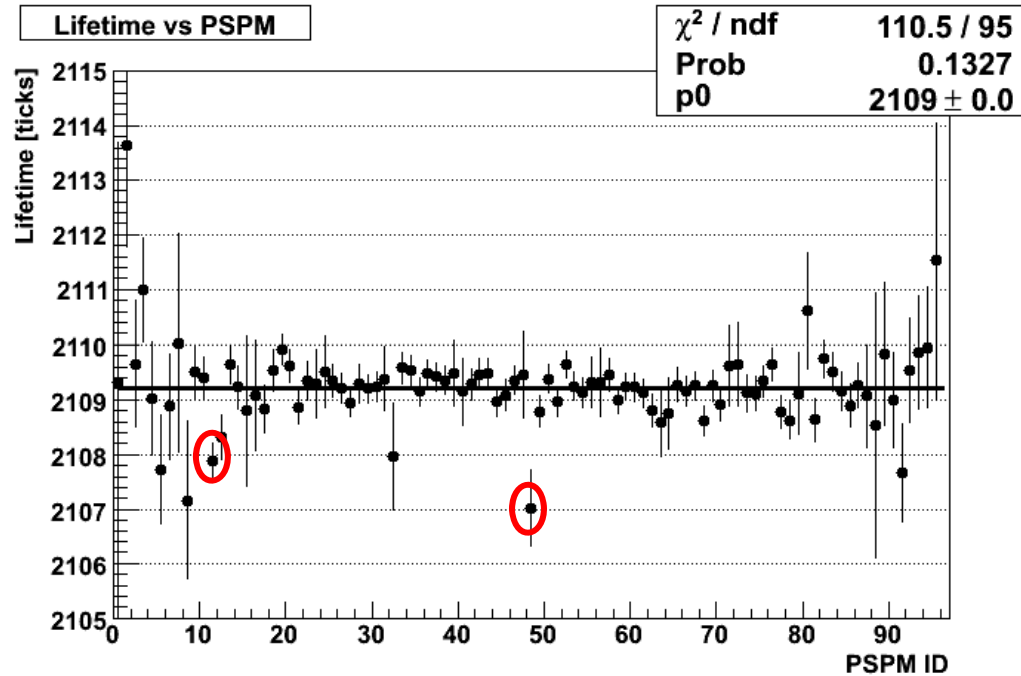
lifetime vs position of the pion in the target (x coord)

lifetime vs position of the pion inside the PSPM



SYSTEMATICS: HOMOGENEITY OF THE TARGET

Lifetime VS position of the tube in the target:



• evidence for a systematic effect – due to 2 tubes

$$\Delta\tau_{\mu} = +0.016 \text{ ticks} = +7.6 \text{ ppm}$$

SYSTEMATICS -- GEOMETRY :

- lifetime vs pion position (x,y) ✓
- lifetime vs position inside the PSPM ✓
- lifetime vs detection efficiency ✓
- lifetime vs position of PSMP in the target ✗
- lifetime vs position of TDC chip in the target ✓
- lifetime vs position of TDC in the target ✓

Systematics associated to the target (dis)homogeneity

$$\Delta\tau_{\mu} = +0.016 \text{ ticks} = +7.6 \text{ ppm}$$

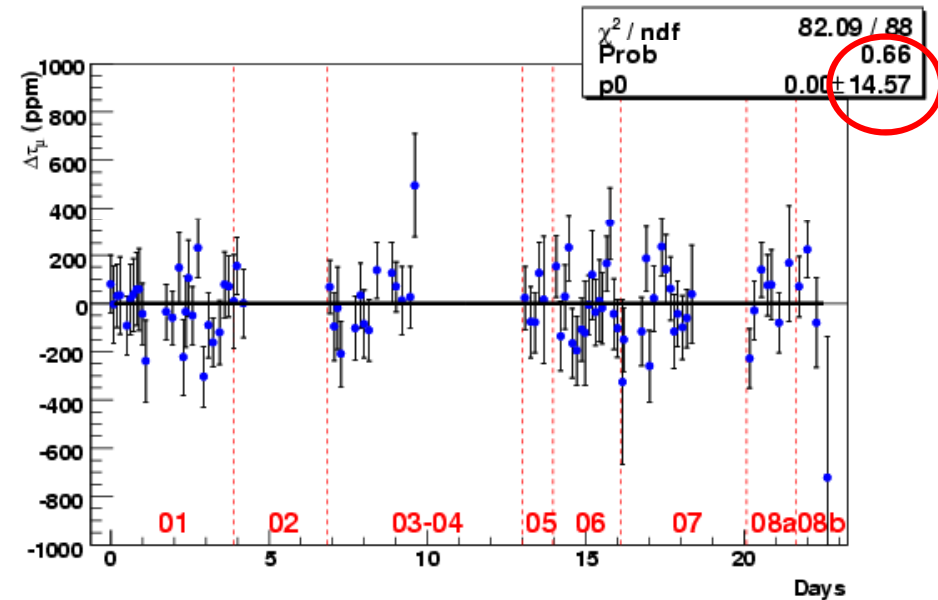
SYSTEMATICS : TIME STABILITY & RATE DEPENDENCE

TIME STABILITY

Data set divided in 89 subsets of similar size ($\sim 1.2 \cdot 10^8$ evts) similar duration (~ 4 hours)

Nominal fit applied to every subset:

GOOD TIME STABILITY WITHIN STATISTICAL UNCERTAINTY of 15 ppm

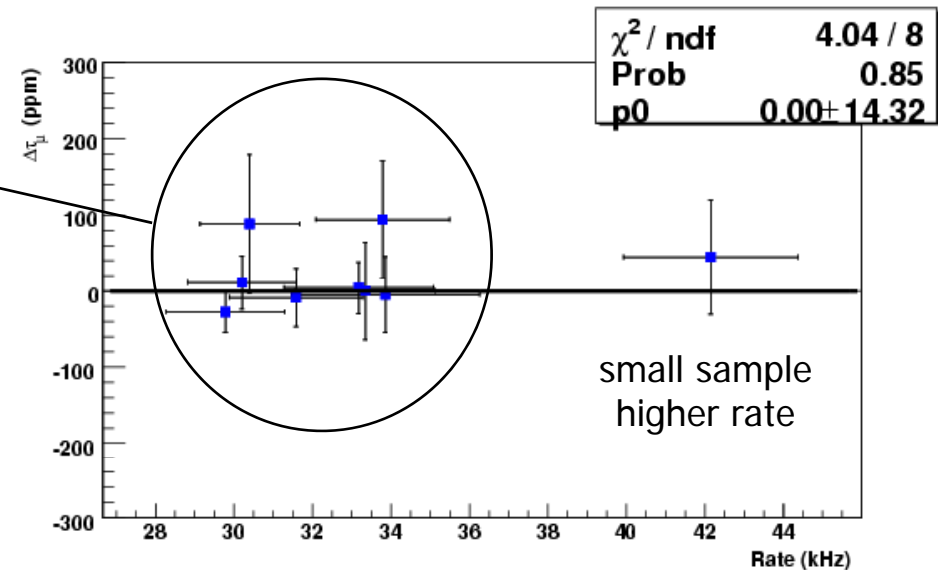


RATE DEPENDENCE

- Trigger rate (LV2) ~ 30 kHz
- Profit of the small spread in range to study lifetime VS rate

NO EFFECT OF SYSTEMATICS RELATED TO THE TRIGGER RATE

Limited rate interval available



RESULTS & CONCLUSIONS

first FAST precise measurement of the positive muon lifetime and Fermi Constant G_F :

- Run 2006, 3 weeks data taking / $1.073 \cdot 10^{10} \mu^+$ decay events / precision compatible with PDG
- Good agreement with the PDG / The uncertainty is totally dominated by the statistics

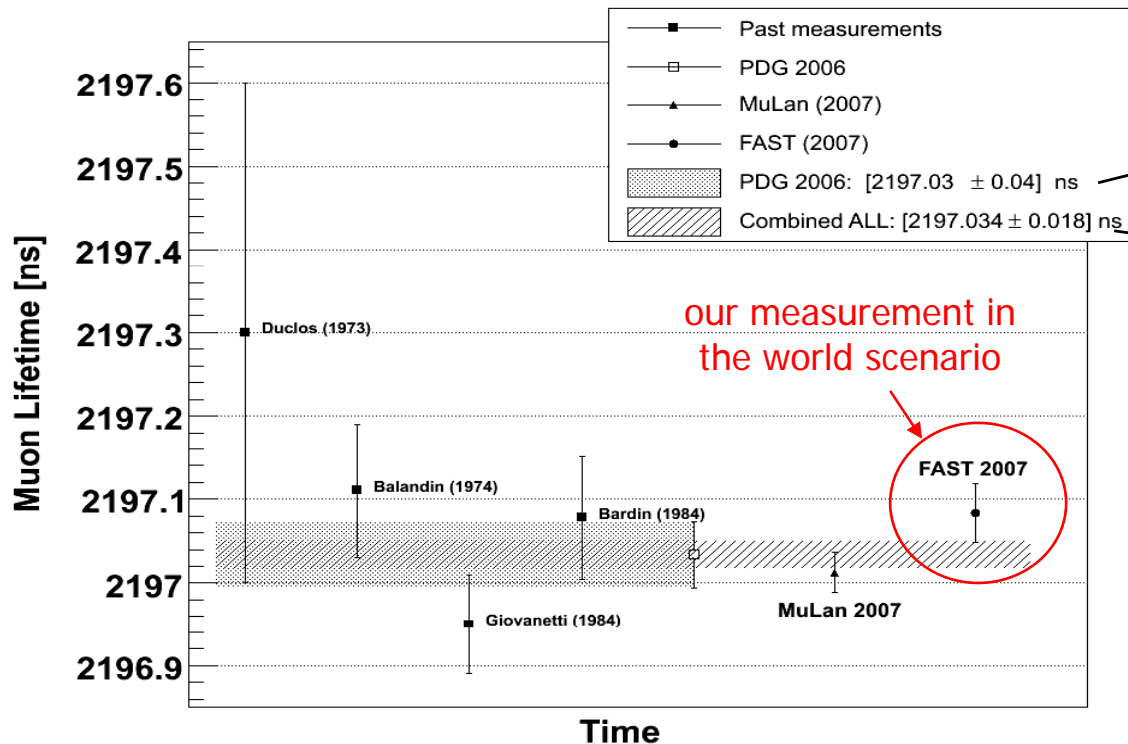
$$\tau_\mu = [2197.083 \pm 0.032 \text{ (stat)} \pm 0.015 \text{ (syst)}] \text{ ns}$$

$$\frac{\delta\tau_\mu}{\tau_\mu} = 16 \text{ ppm}$$

$$G_F = [1.166353 \pm 0.000009] \times 10^{-5} \text{ GeV}^{-2}$$

$$\frac{\delta G_F}{G_F} = 8 \text{ ppm}$$

arXiv: 0707.3904
[hep-ex]
&
submitted to PLB



G_F accuracy:
 18 ppm } 9 ppm
 8.2 ppm } 4 ppm

After more than 20 years
two new experiments
(MuLan & FAST) are
taking the lead

... ppm accuracy on G_F
is expected soon!

FUTURE PLANS FOR FAST

- RUN 2006 largely proved the reliability and feasibility of the measurement, but a few more steps are needed to achieve the final FAST goal

- **increase the working rate :**
30 kHz (LV2) → 100 – 120 kHz (LV2)

1. Solve some malfunctioning in the TDCs
(considering CAEN V767→V1190A replacement)
2. Double the DAQ hardware (number PVIC nodes)
(max bandwidth: 80 MB/s → 160 MB/s)
3. New mode of reading the TDCs
(continuous mode VS trigger matching mode)

- **analysis:**

1. Higher statistics: new/different systematics
2. Extended LV1 tagging (all pcls) i.e. pulsed structure is expected to be reduced



-
- **2007 beam time (from now to Dec) :**
final upgrade of the DAQ performance
 - **2008 beam time :**
data collection (at max rate) for the final measurement