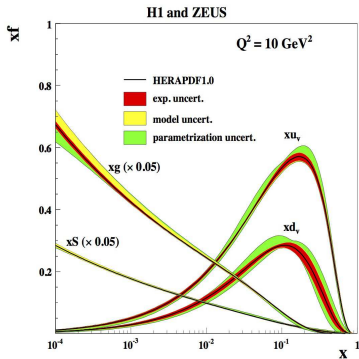
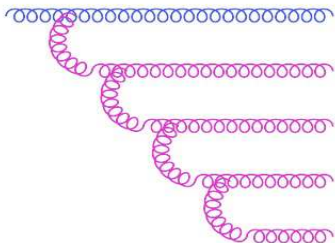


Some CGC predictions for $p+A$ run at the LHC and their implications for EIC

A. H. Rezaeian

Universidad Tecnica Federico Santa Maria

Physics Opportunities at an Electron-Ion Collider (POETIC 2013)



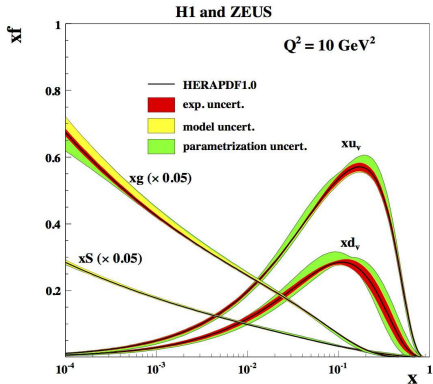
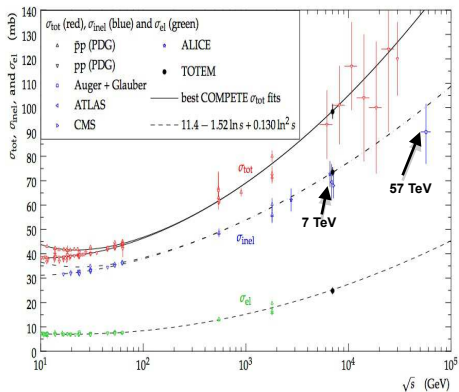
$$\frac{\partial \phi(\mathbf{x}, \mathbf{k}_\perp)}{\partial \ln(\mathbf{x}_0/\mathbf{x})} \approx \mathcal{K} \otimes \phi(\mathbf{x}, \mathbf{k}_\perp) \longrightarrow \phi_{\text{BFKL}} \sim \mathbf{x}^{-\alpha_s \omega}$$

“BFKL eqn”

Balitsky- Fadin-Kuraev-Lipatov

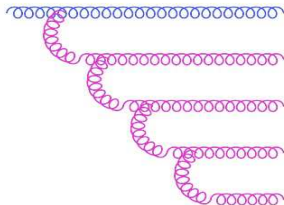
- Both DGLAP and BFKL are linear evolution equations: exponential growth of the gluon distributions at small- x
- **Linear \implies unstable growth of the gluon distribution!**

Growth of the gluon distribution at small-x, where do gluons go?



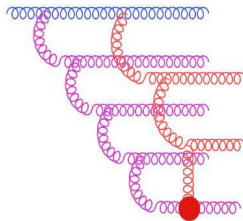
• Unitarity or Froissart bound: $\sigma_{tot} < c \ln^2(s)$: Gluon saturation at small-x

BFKL versus BK-JIMWLK evolution equation



$$\frac{\partial \phi(\mathbf{x}, \mathbf{k}_\perp)}{\partial \ln(\mathbf{x}_0/\mathbf{x})} \approx \mathcal{K} \otimes \phi(\mathbf{x}, \mathbf{k}_\perp)$$

“BFKL eqn”



$$\frac{\partial \phi(\mathbf{x}, \mathbf{k}_\perp)}{\partial \ln(\mathbf{x}_0/\mathbf{x})} \approx \mathcal{K} \otimes \phi(\mathbf{x}, \mathbf{k}_\perp) - \phi(\mathbf{x}, \mathbf{k}_\perp)^2$$

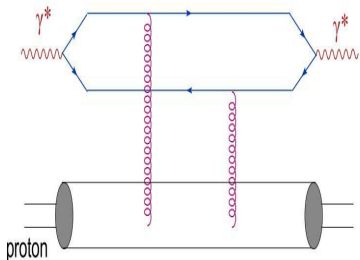
radiation
recombination

“BK-JIMWLK eqns”

Balitsky, Kovchegov, Jalilian-Marian, Iancu, McLerran, Weigert, Leonidov, and Kovner (1997-2000)

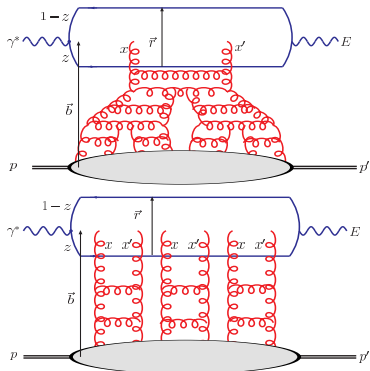
- High energy/density: recombination processes \implies **saturation**:
The number of partons created at a given step depends non-linearly on the number of partons present previously.
- **Nonlinear** \implies **stable fixed point at high energy!**

Unitary problem, black disk limit and saturation



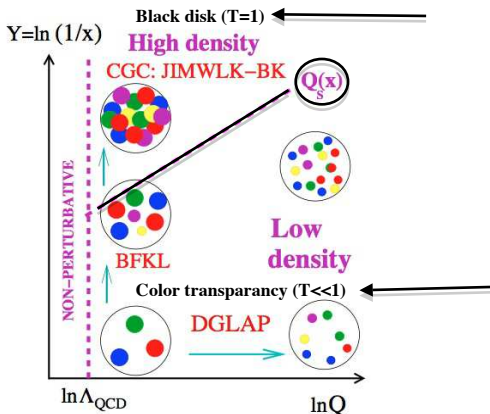
$$T(x, r, b) \simeq \alpha_s r^2 \frac{xG(x, 1/r^2)}{\pi R^2} \equiv \alpha_s n(x, Q^2 \sim 1/r^2)$$

Unitarization



Strong scattering $T \sim 1 \iff$ High gluon density $n \sim 1/\alpha_s \implies$ gluon saturation

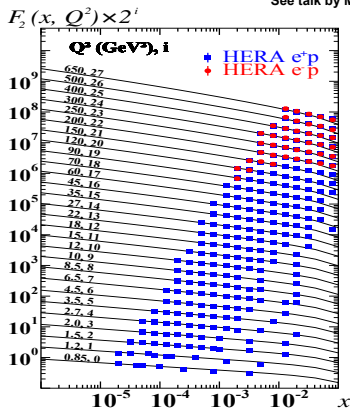
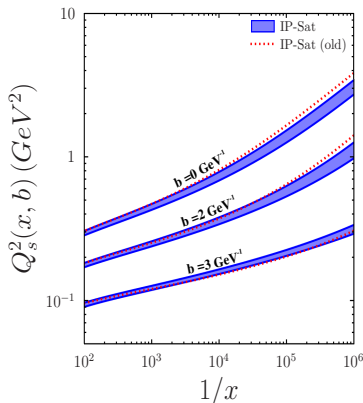
To preserve unitarity \iff Multiple scattering is important: $(\alpha_s n)^n \sim 1$



- Dilute regime:** Bjorken limit in QCD $s \rightarrow \infty; Q^2 \rightarrow \infty; x \approx \frac{Q^2}{s} = \text{fixed}$
 Asymptotic freedom, Machinery of precision pQCD...
- Dense regime:** Regge limit in QCD $s \rightarrow \infty; x \rightarrow 0; Q^2 = \text{fixed}$
 Physics of strong fields in QCD, Saturation/CGC...

Saturation (IP-Sat) description of recent combined HERA data

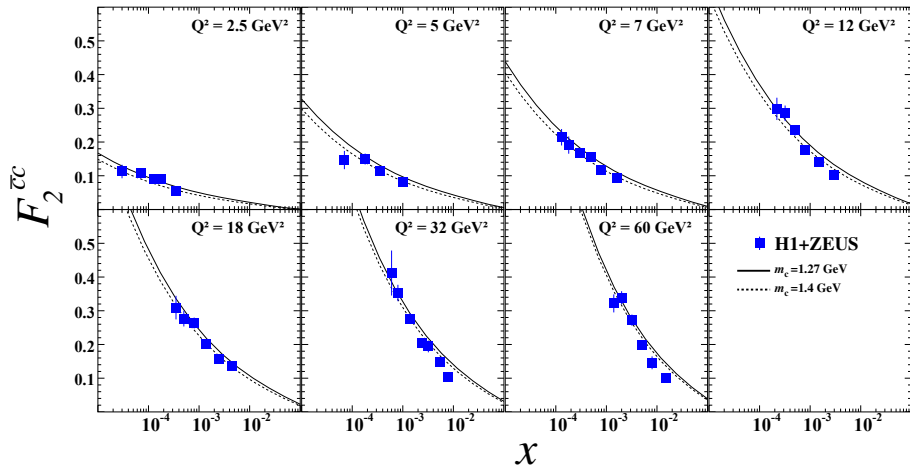
See talk by Marat Siddikov



Rezaeian, Siddikov, Van de Klundert, Venugopalan, arXiv:1212.2974

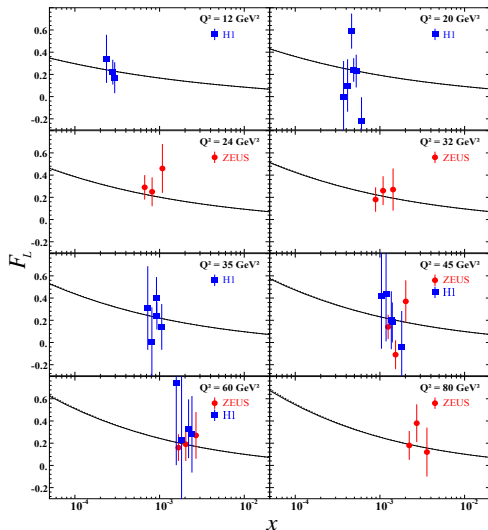
- Saturation scale extracted from **old** and **new** combined data have similar trend although parameters of the model change significantly:
 Old IP-Sat & combined data: $\chi^2/d.o.f \approx 3$ Revised IP-Sat: $\chi^2/d.o.f \approx 1$.

CGC description of recent combined HERA data: Charm structure function

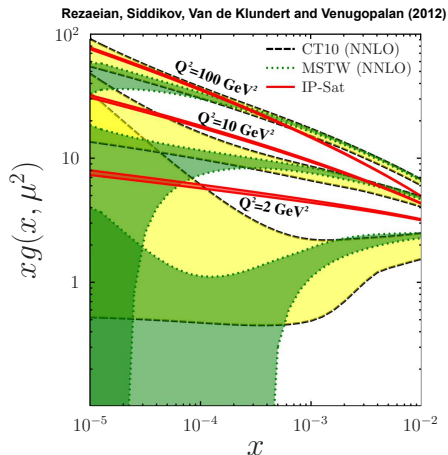


● $F_2^{c\bar{c}}$ data (combined from HERA) not included in the fit!

CGC description of recent combined HERA data: F_L structure function



- F_L data not included in the fit (Combined data are not yet available).

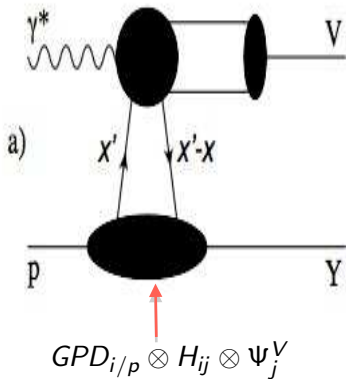


- Color dipole (or CGC) approach (small- x resummation): ground state constructed from classical color field background \rightarrow stable results at small- x .
- Collinear factorization: ground state constructed from free-field-vacuum.

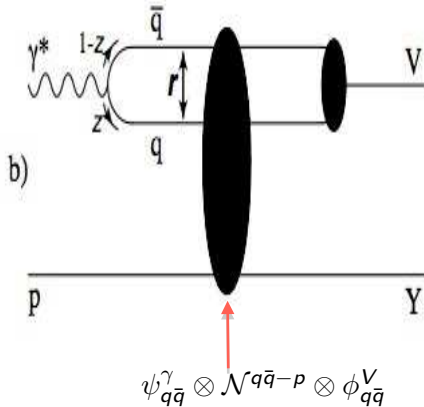
Diffractive vector meson production and DVCS : $\gamma^* + p \rightarrow V + p$ with

$$V = J/\psi, \rho, \phi, \gamma$$

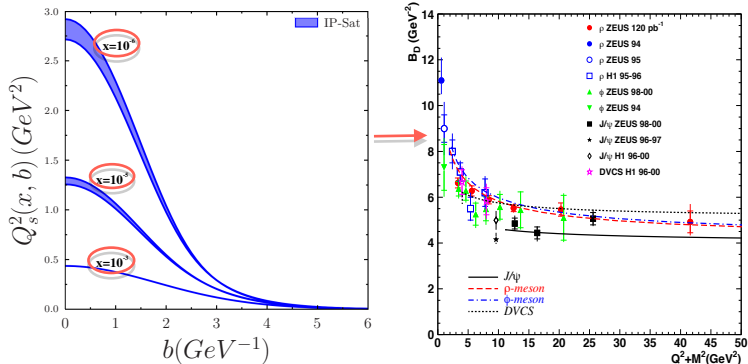
Collinear factorization (GPD+DGLAP)



Color dipole factorization (dipole + small- x evolution)

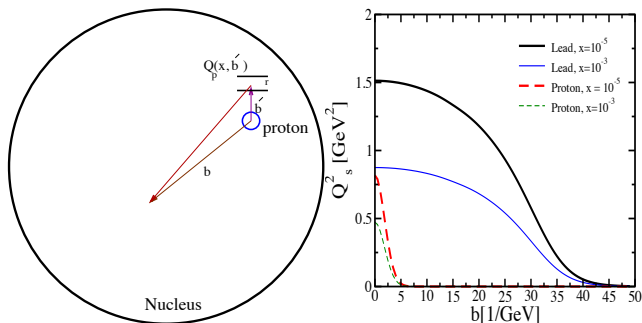


Rezaeian, Siddikov, Van de Klundert, Venugopalan, arXiv:1212.2974



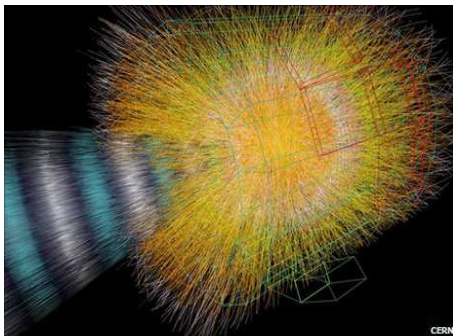
$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} \approx e^{-B_G|t|} \text{ (large } Q^2 \text{ or small } r) \implies Q_s^2(x, b) \approx Q_s^2(x) e^{-b^2/2B_G}$$

- At a fixed Q^2 , the typical dipole size is bigger for lighter vector meson \implies validity of the above asymptotic expression is postponed to a higher Q^2 .
- Universality of extracted impact-parameter distribution of the proton.



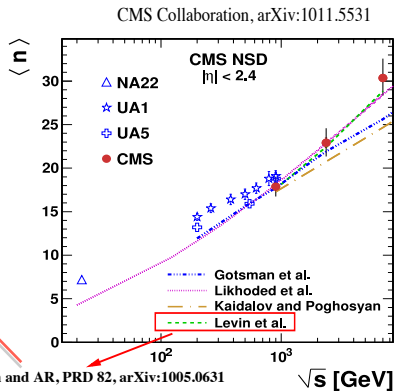
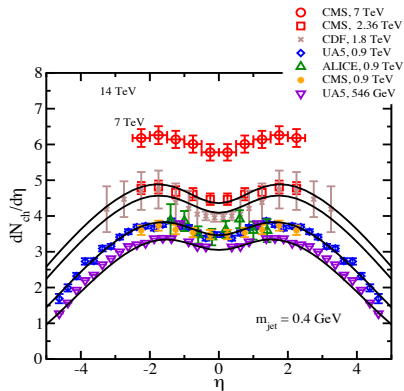
- $Q_{sA}^2(x; b) = K \int d^2\vec{b}' T_A(\vec{b} - \vec{b}') Q_{sp}^2(x; b')$.
- $Q_{sA}^2 \approx Q_{sp}^2 A^{1/3}$ since typical $b' \ll b \sim R_A$.
- $Q_{sA}^2 \rightarrow K Q_{sA}^2$, $K \approx 2$ will change hadron multiplicity at LHC less than 5%.

To extract $Q_{sA}(x; b)$ from data: t -distributions of diffractive processes with nuclear target are needed (**EIC**).



- 99% of the produced particles have $p_T < 2$ GeV
- x : fraction of target momentum carried by parton
- $x \approx p_T/\sqrt{s} \approx 10^{-2}$ at RHIC ($\sqrt{s} = 200$ GeV)
- $x \approx p_T/\sqrt{s} \approx 10^{-4}$ at the LHC ($\sqrt{s} = 2.76 \div 7$ TeV)

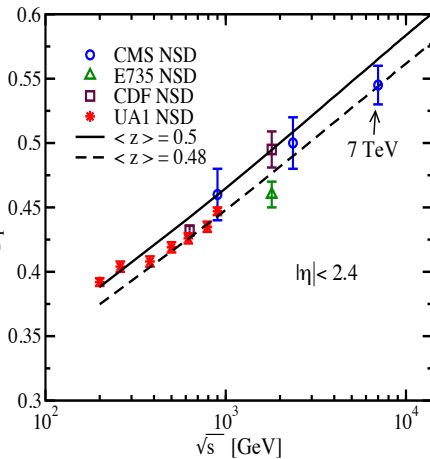
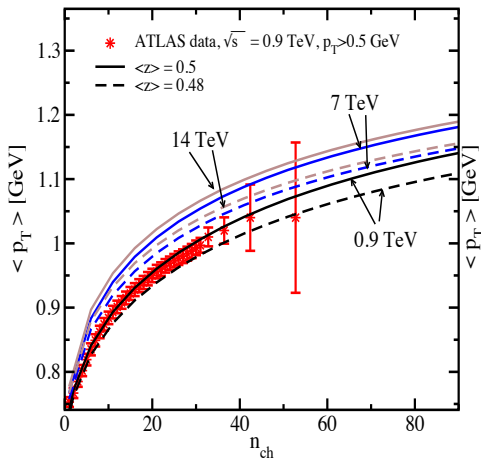
Are there any indications of saturation/CGC at the LHC in pp collisions?



- Correct energy/rapidity and centrality dependence of charged-hadron multiplicity (Levin and Rezaeian, 2010).

- Are there any other signature of saturation in pp@LHC(7 TeV)?
The Ridge: See Raju Venugopalan's talk

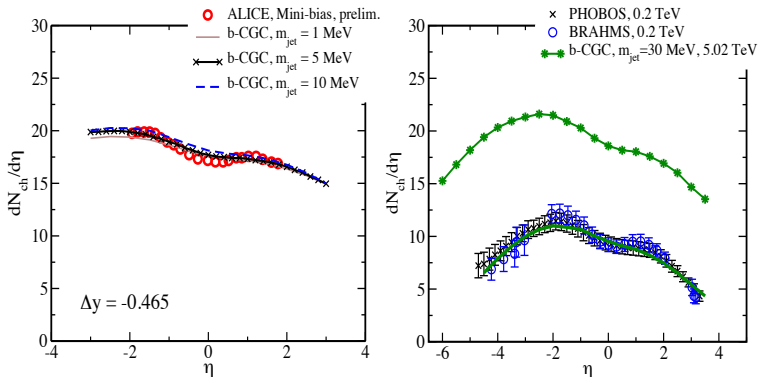
More evidence of saturation at the LHC



- $\langle p_T \rangle \sim \langle z Q_s \rangle$ ✓
- $\langle p_T \rangle \sim \langle z Q_s (n_{ch}; x) \rangle$ ✓

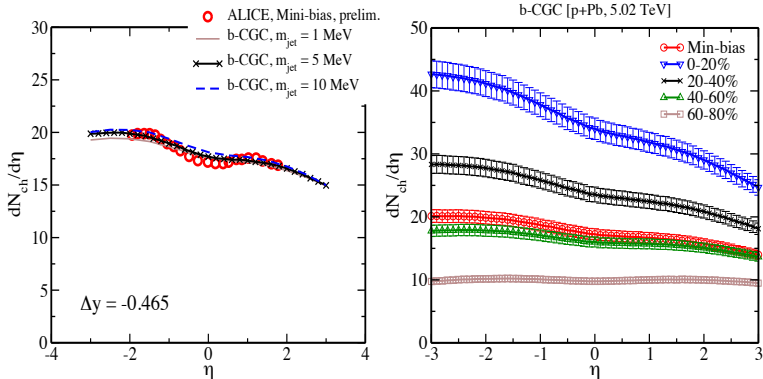
In the CGC framework, dynamical saturation scale plays role of infrared cutoff!.

Rezaeian, PLB718 (2013) 1058; PRD85 (2012) 014028



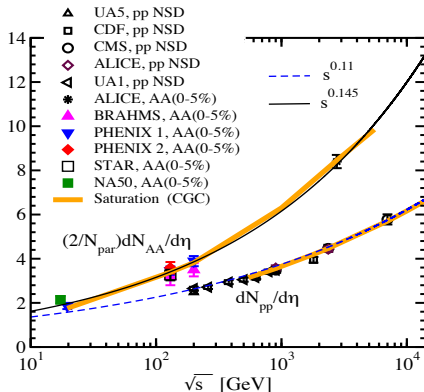
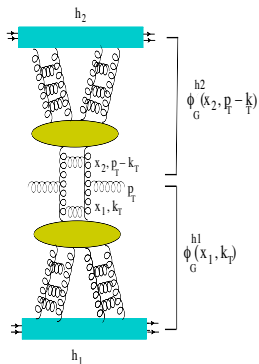
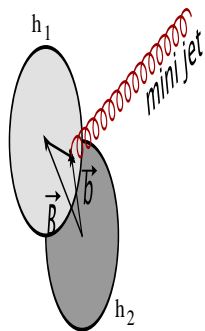
- Two free parameters mini-jet mass m_{jet} and overall normalization (are related to hadronization) cannot be uniquely fixed by only RHIC data $\Rightarrow 5 \div 15\%$ uncertainties.
- $m_{jet} = m_{\text{current quark}}$ gives a good description of both RHIC and ALICE data.

Charged hadron multiplicity in p+A@LHC at different centralities



- Centrality dependence of multiplicity in p+A@LHC: a very non-trivial test of saturation physics.

Levin and Rezaeian, **D82** (2010) 014022, **D83** (2011) 114001

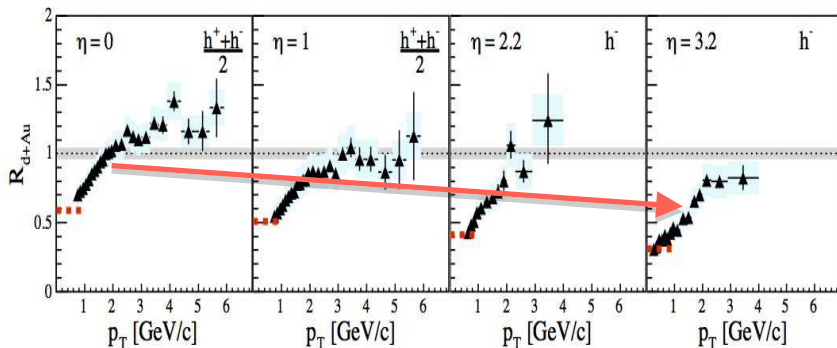


$$\frac{dN_h}{d\eta} \propto Q_s^2 \propto s^{\lambda/2} = s^{0.11 \div 0.145}$$

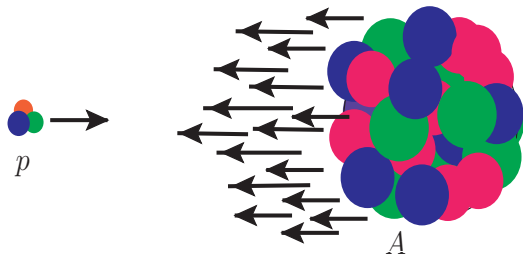
Signatures of the CGC in d+A@RHIC: Initial-state effect

$$R_{pA}(\eta, p_{\perp}) \equiv \frac{1}{N_{coll}} \frac{dN_h}{d^2 p_{\perp} d\eta} \Big|_{pA} \simeq \frac{1}{A^{1/3}} \frac{\Phi_A(Y, p_{\perp})}{\Phi_p(Y, p_{\perp})}.$$

- Suppression of single inclusive hadron production at forward rapidities



p+A@LHC Sep 2012 & Feb 2013



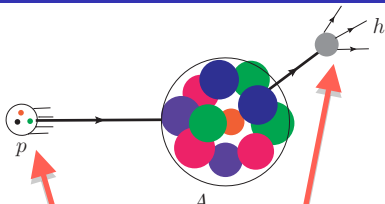
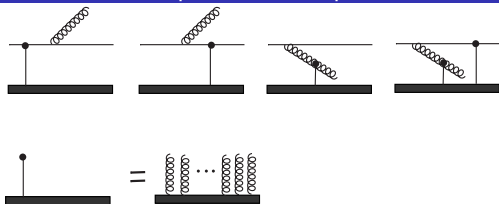
$$y_{forward}^{RHIC} \Leftrightarrow y_{mid-rapidity}^{LHC}$$

Suppression or not?



- Test of saturation/CGC dynamics, based-line for future experiments: EIC, LHeC
- Based-line for A+A collisions at the LHC.

Inclusive hadron production in pA collisions; revisited



Altinoluk and Kovner, PRD83, arXiv:1102.5327

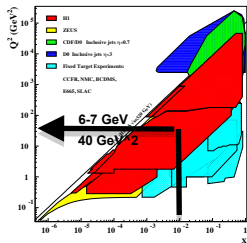
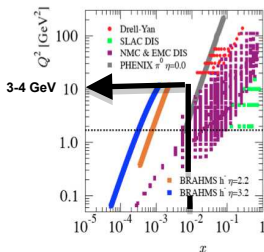
Chirilli, Xiao and Yuan, PRL108, arXiv:1112.1061

$$\frac{dN^{pA \rightarrow hX}}{d^2p_T d\eta} = \frac{K}{(2\pi)^2} \left[\int_{x_F}^1 \frac{dz}{z^2} \left[x_1 f_g(x_1, Q^2) N_A(x_2, \frac{p_T}{z}) D_{h/g}(z, Q) + \sum_q x_1 f_q(x_1, Q^2) N_F(x_2, \frac{p_T}{z}) D_{h/q}(z, Q) \right] \right. \\ \left. + \int_{x_F}^1 \frac{dz}{z^2} \frac{\alpha_s}{2\pi^2} \frac{z^4}{p_T^4} \int_{k_T^2 < Q^2} d^2k_T k_T^2 N_F(k_T, x_2) \int_{x_1}^1 \frac{d\xi}{\xi} \sum_{i,j=q,\bar{q},g} w_{i/j}(\xi) P_{i/j}(\xi) x_1 f_j(\frac{x_1}{\xi}, Q) D_{h/i}(z, Q) \right]$$

$$\frac{\partial \mathcal{N}_{A(F)}(r, x)}{\partial \ln(x_0/x)} = \int d^2\vec{r}_1 K^{\text{run}}(\vec{r}, \vec{r}_1, \vec{r}_2) \left[\mathcal{N}_{A(F)}(r_1, x) + \mathcal{N}_{A(F)}(r_2, x) - \mathcal{N}_{A(F)}(r, x) - \mathcal{N}_{A(F)}(r_1, x) \mathcal{N}_{A(F)}(r_2, x) \right]$$

Initial condition: $\Rightarrow \mathcal{N}(r, Y=0) = 1 - \exp \left[-\frac{(r^2 Q_{0s}^2)^\gamma}{4} \ln \left(\frac{1}{\Lambda r} + e \right) \right]$

Albacete et al (2011-2012)

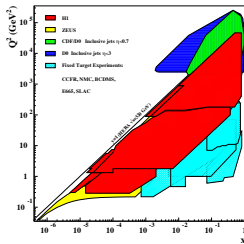
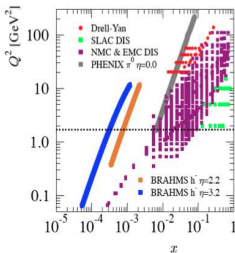


- Available data (HERA+RHIC+LHC) cannot **uniquely** determine the initial condition (initial saturation scale) of the BK equation.

For proton: $p_t \leq 6 \text{ GeV}$, $x \leq 0.01$: $Q_{0p}^2 \approx 0.168 \text{ GeV}^2$ with $\gamma \approx 1.119$

- For heavy nuclei: $Q_{0A}^2 = cA^{1/3} Q_{0p}^2$,

$p_t \leq 4 \text{ GeV}$, $x \leq 0.01$: $c \approx 0.5 \implies Q_{0A}^2 \approx (3 \div 4) Q_{0p}^2$



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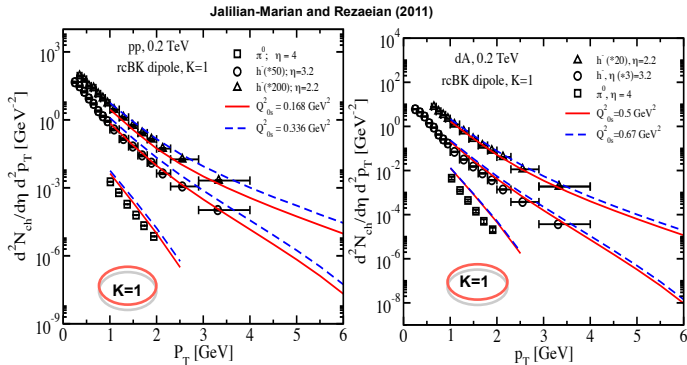
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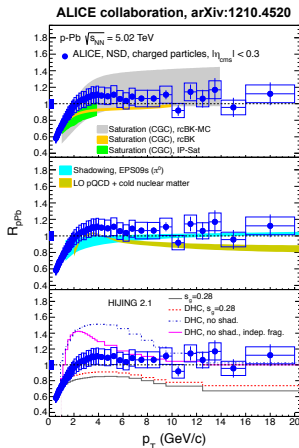
$$R_{pA}^{ch}(p_T \gg 1) = \frac{Q_{0A}^2 S_A}{Q_{0p}^2 A S_p} \approx \frac{Q_{0A}^2}{Q_{0p}^2 A^{1/3}} \rightarrow 1 \implies Q_{0A}^2 = cA^{1/3} Q_{0p}^2 \text{ with } c \approx 1$$

$3 \div 4 Q_{0p}^2 \leq Q_{0A}^2(x_0 = 0.01) \leq 6 \div 7 Q_{0p}^2$ $Q_{0A}^2 = NQ_{0p}^2$ with $N = 3 \div 7$.



- What is the role of cold matter energy loss which is not included in the above? Kopeliovich, Frankfurt, Strikman; Neufeld, Vitev, Zhang.

CGC predictions for R_{pA}^h in p+Pb@LHC and ALICE data



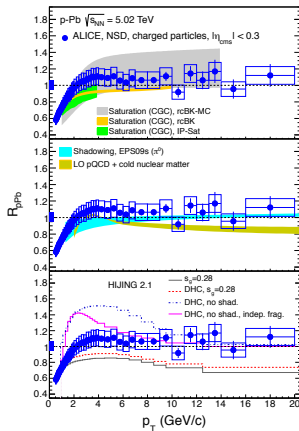
CGC predictions are from:

Tribedy and Venugopalan, PLB710, arXiv:1112.2445.

Albacete, Dumitru, Fujii and Nara, NPA897, arXiv:1209.2001.

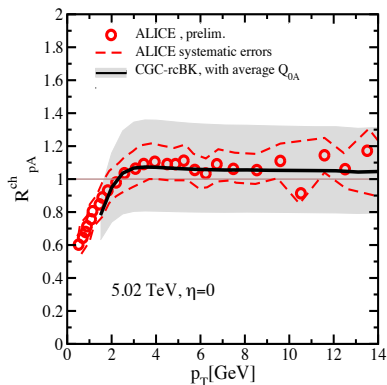
Rezaeian, PLB718, arXiv:1210.2385.

CGC predictions for R_{pA}^h in p+Pb@LHC and ALICE data



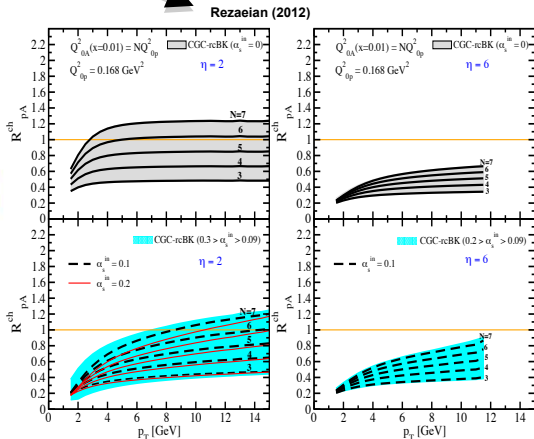
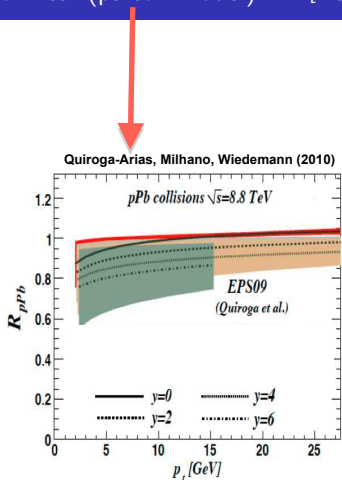
- Data seem to rule out any (or strong) Cronin-type peak!.
- Npdf may be questionable if R_{pA}^h remains above one at high- p_T !

Rezaeian, PLB718, arXiv:1210.2385



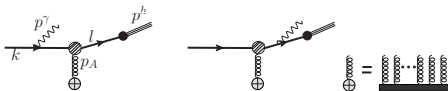
- The black curve corresponds to $Q_{0A}^2 = NQ_{0p}^2$ with the average $N = 5$.

Collinear (parton model) v. k_t -factorization (CGC) at the LHC



- The CGC predicts more suppression for R_{pA}^h at forward rapidities and low- p_T compared to the standard parton model approach.

Photon-hadron production in high-energy pA collisions: $p + A \rightarrow \gamma + h + X$



Kopeliovich, Tarasov, Schafer (1999)

Gelis and Jalilian-Marian (2002)

Baier, Mueller and Schiff (2004)

Jalilian-Marian and Rezaeian (2012)

$$\frac{d\sigma_{pA \rightarrow q(l)\gamma(p^\gamma)X}}{d^2b_T d^2p_T^\gamma d^2l_T^\gamma d\eta_\gamma d\eta_h} = \frac{K e_q^2 \alpha_{em}}{\sqrt{2}(4\pi^4)} \frac{p^-}{(p_T^\gamma)^2 \sqrt{S}} \frac{1 + (\frac{l^-}{k^-})^2}{[p^- l_T^- - l^- p_T^\gamma]^2}$$

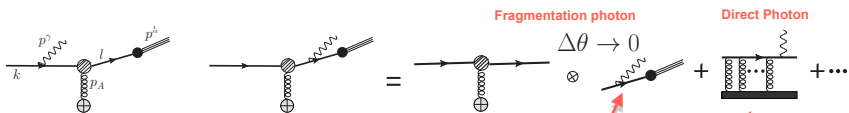
$$\delta[x_q - \frac{l_T^-}{\sqrt{S}} e^{\eta_h} - \frac{p_T^\gamma}{\sqrt{S}} e^{\eta_\gamma}] \left[2l^- p^- l_T^- \cdot p_T^\gamma + p^- (k^- - p^-) l_T^2 + l^- (k^- - l^-) (p_T^\gamma)^2 \right] N_F(|l_T^- + p_T^\gamma|, x_g)$$

$$x_q = x_{\bar{q}} = \frac{1}{\sqrt{S}} \left(p_T^\gamma e^{\eta_\gamma} + \frac{p_T^h}{z_f} e^{\eta_h} \right), \quad x_g = \frac{1}{\sqrt{S}} \left(p_T^\gamma e^{-\eta_\gamma} + \frac{p_T^h}{z_f} e^{-\eta_h} \right),$$

$$z_f = p_T^h / l_T^-, \quad \text{with} \quad z_f^{\min} = \frac{p_T^h}{\sqrt{S}} \left(\frac{e^{\eta_h}}{1 - \frac{p_T^\gamma}{\sqrt{S}} e^{\eta_\gamma}} \right).$$

$$\frac{d\sigma_{pA \rightarrow h(p^h)\gamma(p^\gamma)X}}{d^2b_T d^2p_T^\gamma d^2p_T^h d\eta_\gamma d\eta_h} = \int_{z_f^{\min}}^1 \frac{dz_f}{z_f} \int dx_q f_q(x_q, Q^2) \frac{d\sigma_{pA \rightarrow q(l)\gamma(p^\gamma)X}}{d^2b_T d^2p_T^\gamma d^2l_T^\gamma d\eta_\gamma d\eta_h} D_{h/q}(z_f, Q^2)$$

Prompt photon production in high-energy pA collisions

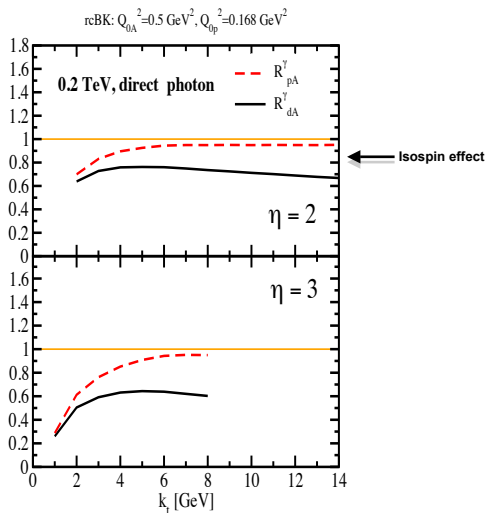


$$\frac{d\sigma^{pA \rightarrow \gamma(p^\gamma)} X}{d^2 b_T d^2 p_T^\gamma d\eta_\gamma} = \frac{K}{(2\pi)^2} \left[\int_{x_q^{min}}^1 dx_q f_q(x_q, Q^2) \frac{1}{z} N_F(x_g, p_T^\gamma/z) D_{\gamma/q}(z, Q^2) \right. \\ \left. + \frac{e_q^2 \alpha_{em}}{2\pi^2 (p_T^\gamma)^4} \int_{x_q^{min}}^1 dx_q f_q(x_q, Q^2) z^2 [1 + (1-z)^2] \int_{l_T^2 < Q^2} d^2 \vec{l}_T^2 l_T^2 N_F(\bar{x}_g, l_T) \right],$$

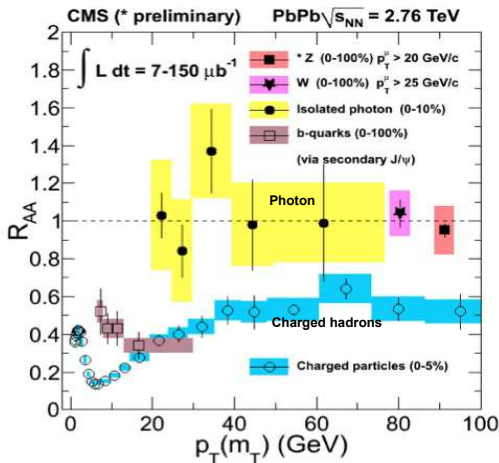
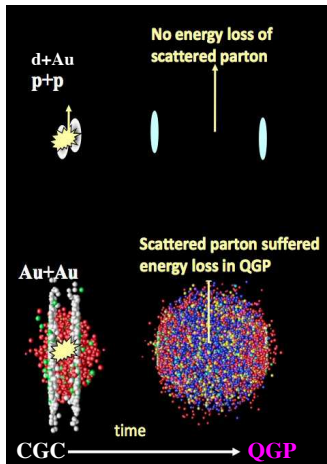
$$x_g = x_q e^{-2\eta_\gamma}, \quad \bar{x}_g = \frac{1}{x_q S} \left[\frac{(p_T^\gamma)^2}{z} + \frac{(l_T - p_T^\gamma)^2}{1-z} \right], \quad z = \frac{p_T^\gamma}{x_q \sqrt{S}} e^{\eta_\gamma}, \quad \text{with } x_q^{min} = \frac{p_T^\gamma}{\sqrt{S}} e^{\eta_\gamma}.$$

- Both fragmentation and direct photon are sensitive to saturation via N_F . However, direct photon is more sensitive to the saturation effects.
- pA is different from dA (unlike hadron production) due to charge squared of quarks \rightarrow non-trivial isospin effect.

pA vs. dA at RHIC



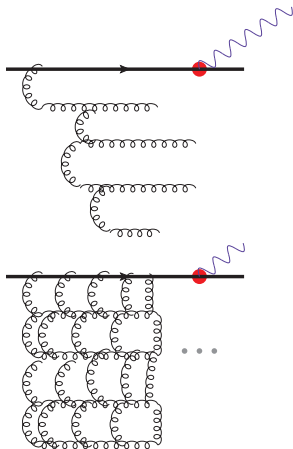
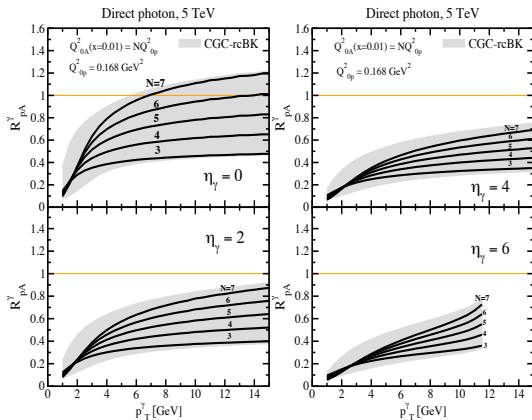
- Sizable isospin effect \rightarrow suppression at high transverse momentum (NOT due to saturation effect).



- Fundamental properties of QGP: All hadrons are strongly quenched except prompt photon.**

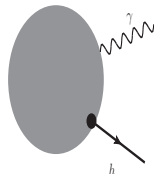
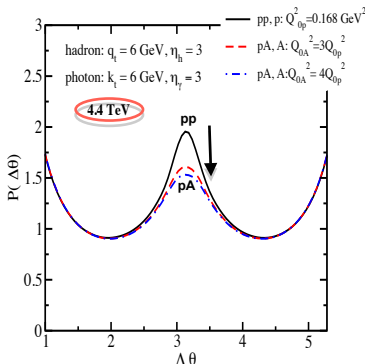
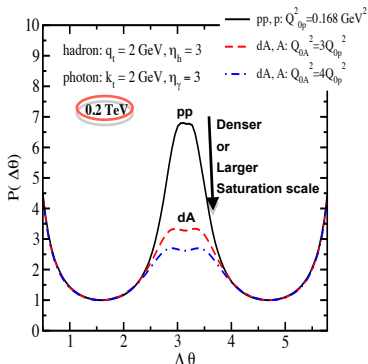
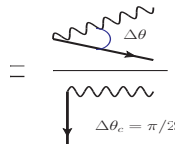
Direct photon production at the LHC in p+A collisions

Rezaeian, PLB718 (2013) 1058 [arXiv:1210.2385]



Prompt photons are not suppressed in QGP, but are subject to suppression in CGC medium due to gluon saturation.

$$P(\Delta\theta) = \frac{d\sigma^{p(d)} T \rightarrow h(q) \gamma(k) X}{d^2\vec{b}_t dk_t^2 dq_t^2 dy_\gamma dy_l d\theta} [\Delta\theta] / \frac{d\sigma^{p(d)} T \rightarrow h(q) \gamma(k) X}{d^2\vec{b}_t dk_t^2 dq_t^2 dy_\gamma dy_l d\theta} [\Delta\theta = \Delta\theta_c]$$

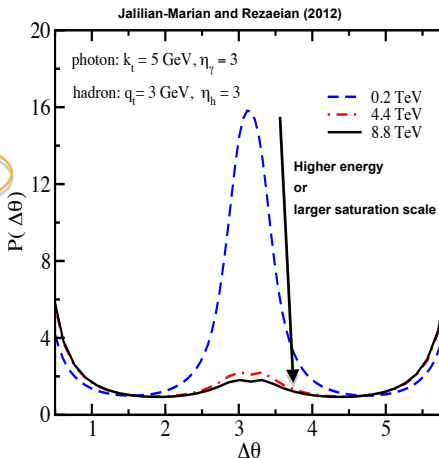


- Denser nuclei (or bigger saturation scale) → more suppression of away-side correlations. Jalilian-Marian, Rezaeian, PRD86 [arXiv:1204.1319]

Decorrelation is universal:
Dihadron, photon-hadron, DY

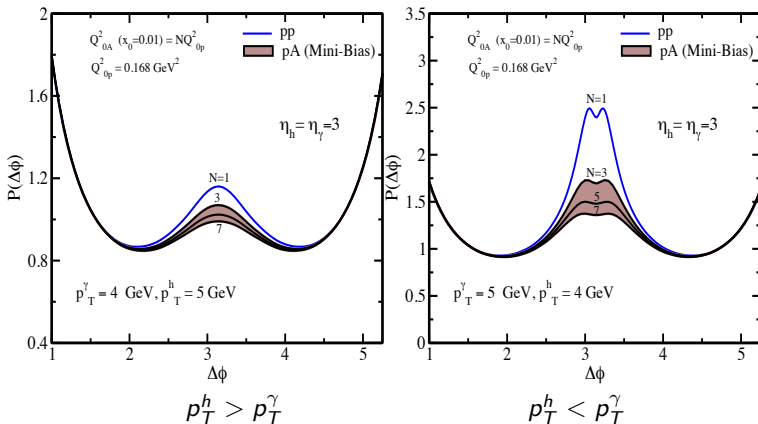
The advantage of photon-hadron:
ONLY dipole appears, no 4-points

For DY see:
Stasto, Xiao, Zaslavsky (2012)



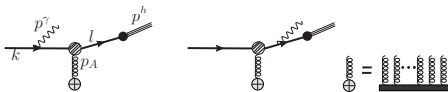
- Higher energy \rightarrow more suppression of away-side correlations.

Rezaeian, PRD86 [arXiv:1209.0478]



- Photon-hadron correlations can have a double or single peak structure depending on ratio of $z_T = p_T^h/p_T^\gamma$.

Photon-hadron production in high-energy pA collisions: $p + A \rightarrow \gamma + h + X$



$$\frac{d\sigma^{qA \rightarrow q(l)\gamma(p^\gamma)X}}{d^2b_T^2 d^2p_T^{\gamma} d^2l_T^{\gamma} d\eta_\gamma d\eta_h} = \frac{K e_q^2 \alpha_{em}}{\sqrt{2}(4\pi^4)} \frac{p^-}{(p_T^\gamma)^2 \sqrt{S}} \frac{1 + (\frac{l^-}{k^-})^2}{[p^- l_T^- - l^- p_T^\gamma]^2}$$

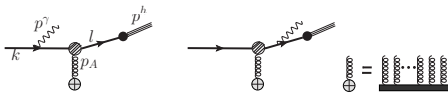
$$\delta[x_q - \frac{l_T^-}{\sqrt{S}} e^{\eta_h} - \frac{p_T^\gamma}{\sqrt{S}} e^{\eta_\gamma}] \left[2l^- p^- l_T^- \cdot p_T^\gamma + p^- (k^- - p^-) l_T^2 + l^- (k^- - l^-) (p_T^\gamma)^2 \right] N_F(|\vec{l}_T + \vec{p}_T^\gamma|, x_g)$$

$$\frac{d\sigma^{pA \rightarrow h(p^h)\gamma(p^\gamma)X}}{d^2b_T^2 d^2p_T^{\gamma} d^2p_T^{h} d\eta_\gamma d\eta_h} = \int_{z_f^{\min}}^1 \frac{dz_f}{z_f} \int dx_q f_q(x_q, Q^2) \frac{d\sigma^{qA \rightarrow q(l)\gamma(p^\gamma)X}}{d^2b_T^2 d^2p_T^{\gamma} d^2l_T^{\gamma} d\eta_\gamma d\eta_h} D_{h/q}(z_f, Q^2)$$

Photon-hadron correlations have a double peak structure if:

- $|\vec{l}_T + \vec{p}_T^\gamma| = 0 \rightarrow \sigma(q + A \rightarrow \gamma(p^\gamma) + q(l) + X) = 0$
- Existence of saturation scale: $p_T^2 N_F(p_T, x_g)$ has a maximum at $p_T \sim Q_s$.

Photon-hadron production in high-energy pA collisions: $p + A \rightarrow \gamma + h + X$



$$\frac{d\sigma^{pA \rightarrow q(l)\gamma(p^\gamma)X}}{d^2b_T^- d^2p_T^\gamma d^2l_T^- d\eta_\gamma d\eta_h} = \frac{Ke_q^2 \alpha_{em}}{\sqrt{2}(4\pi^4)} \frac{p^-}{(p_T^\gamma)^2 \sqrt{S}} \frac{1 + (\frac{l^-}{k^-})^2}{[p^- l_T^- - l^- p_T^\gamma]^2}$$

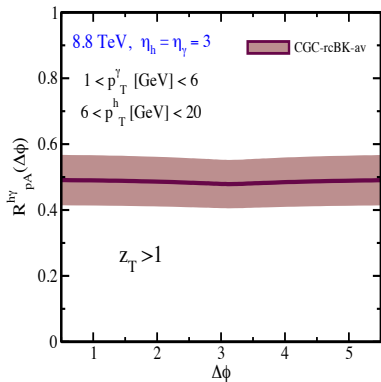
$$\delta[x_q - \frac{l_T^-}{\sqrt{S}} e^{\eta_h} - \frac{p_T^\gamma}{\sqrt{S}} e^{\eta_\gamma}] \left[2l^- p^- l_T^- \cdot p_T^\gamma + p^- (k^- - p^-) l_T^2 + l^- (k^- - l^-) (p_T^\gamma)^2 \right] N_F(|\vec{l}_T + \vec{p}_T^\gamma|, x_g)$$

$$\frac{d\sigma^{pA \rightarrow h(p^h)\gamma(p^\gamma)X}}{d^2b_T^- d^2p_T^\gamma d^2p_T^h d\eta_\gamma d\eta_h} = \int_{z_f^{min}}^1 \frac{dz_f}{z_f} \int dx_q f_q(x_q, Q^2) \frac{d\sigma^{pA \rightarrow q(l)\gamma(p^\gamma)X}}{d^2b_T^- d^2p_T^\gamma d^2l_T^- d\eta_\gamma d\eta_h} D_{h/q}(z_f, Q^2)$$

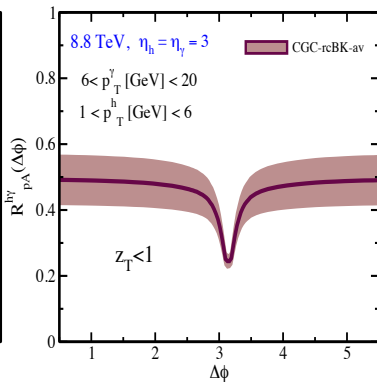
Photon-hadron correlations have a double peak structure if:

$$z_T = \frac{p_T^h}{p_T^\gamma} \leq 1 \quad \text{and} \quad p_T^\gamma \frac{(e^{\eta_h} + e^{\eta_\gamma})}{\sqrt{S}} \leq 1.$$

Nuclear modification of semi-inclusive $\gamma - \pi^0$ production at the LHC



$$p_T^h > p_T^\gamma$$



$$p_T^h < p_T^\gamma$$

The $\gamma - \pi^0$ azimuthal correlation; coincidence probability

- In the contrast to dihadron production, here we have freedom to select the trigger particle to be a produced prompt photon or a hadron.
Rezaeian, PRD 86, arXiv:1209.0478.

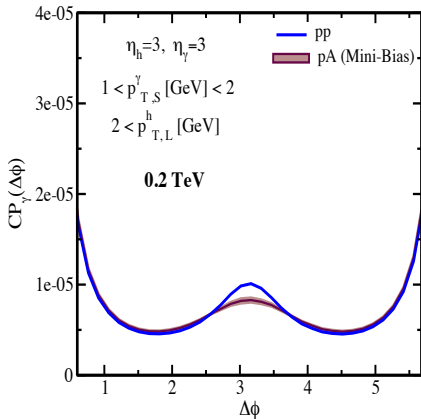
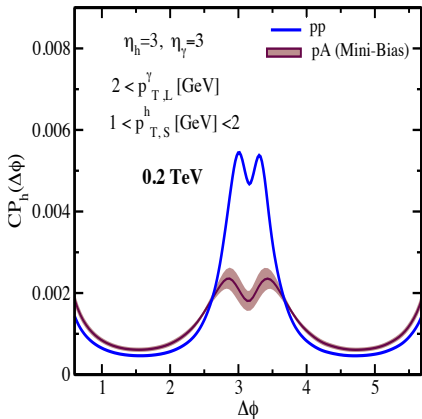
Trigger(leading) particle is a prompt photon:

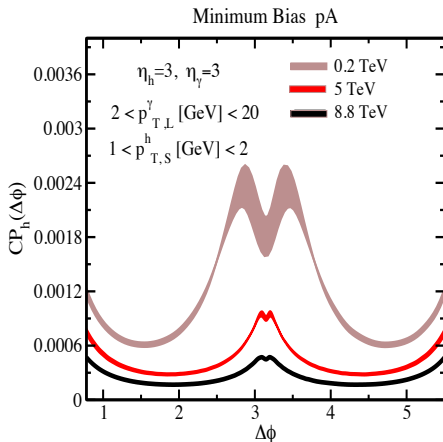
$$CP_h(\Delta\phi; p_{T,S}^h, p_{T,L}^\gamma; \eta_\gamma, \eta_h) = N_h^{\text{pair}}(\Delta\phi)/N_{\text{photon}} = \frac{2\pi \int_{p_{T,L}^\gamma} dp_{T,L}^\gamma p_T^\gamma \int_{p_{T,S}^h} dp_{T,S}^h p_T^h \frac{dN^{pA \rightarrow h(p_T^h)} \gamma(p_T^\gamma) X}{d^2 p_T^\gamma d^2 p_T^h d\eta_\gamma d\eta_h}}{\int_{p_{T,L}^\gamma} dp_{T,L}^\gamma p_T^\gamma \frac{dN^{pA \rightarrow \gamma(p_T^\gamma) X}}{d^2 p_T^\gamma d\eta_\gamma}}$$

Trigger particle is a hadron:

$$CP_\gamma(\Delta\phi; p_{T,S}^\gamma, p_{T,L}^h; \eta_\gamma, \eta_h) = N_\gamma^{\text{pair}}(\Delta\phi)/N_{\text{hadron}} = \frac{2\pi \int_{p_{T,L}^h} dp_{T,L}^h p_T^h \int_{p_{T,S}^\gamma} dp_{T,S}^\gamma p_T^\gamma \frac{dN^{pA \rightarrow h(p_T^h)} \gamma(p_T^\gamma) X}{d^2 p_T^\gamma d^2 p_T^h d\eta_\gamma d\eta_h}}{\int_{p_{T,L}^h} dp_{T,L}^h p_T^h \frac{dN^{pA \rightarrow h(p_T^h) X}}{d^2 p_T^h d\eta_h}}$$

The $\gamma - \pi^0$ coincidence probability at RHIC





- Higher energy \rightarrow more suppression of away-side correlations and diminishing the double peak (Rezaeian, PLB718, arXiv:1210.2385).

Conclusion:

The CGC picture at RHIC and HERA at small- x is consistent with the LHC data ($p+p$, $p+A$, $A+A$) so far: the upcoming $p+A$ data at the LHC is crucial test of gluon saturation/CGC.

- Await to be verified:

- Centrality dependence of the multiplicity distribution.
- Suppression of inclusive charged hadron, and direct photon production at *very* forward rapidities.
- Suppression of away-side photon-hadron (and dihadron) correlations at forward rapidities.

Standard (DGLAP-like) QCD calculations cannot reproduce none of $\gamma - \pi^0$ away-side decorrelation features

$$Q_{sA}^2 \propto A^\alpha Q_{sp}^2 \text{ at small-}x \text{ and low } Q^2$$

- Empirical geometric scaling and DIS data:

Armesto, Salgado and Wiedemann (2004):

$$Q_{sA}^2 = c_1 A^{4/9} Q_{sp}^2 \implies Q_{sA}^2 \approx 3.1 Q_{sp}^2$$

- BK-JIMWLK equation and DIS data

McLerran and Venugopalan (1994), Albacete et al. (2010), Dusling, Gelis, Lappi and Venugopalan (2010), Rezaeian and Levin (2010)

$$Q_{sA}^2 = c_2 A^{1/3} Q_{sp}^2 \implies Q_{sA}^2 \approx 2.96 Q_{sp}^2$$

- Running-coupling BFKL evolution near the saturation boundary

Mueller (2003): $Q_{sA}^2 = c_3 A^0 Q_{sp}^2$, is **independent** of A .

➤ Available data cannot **uniquely** determine the A -dependence of the saturation scale \implies needs for EIC and $p+A@LHC$ with different A .