

An aerial photograph of a valley with a patchwork of green and brown fields. In the distance, there are blue mountains with snow-capped peaks under a clear blue sky. A red oval is drawn around the central part of the valley, framing the title text.

# Interplay of Collider and Flavour Physics

Introduction: John Ellis

# Open Questions beyond the Standard Model

- What is the origin of particle masses?  
due to a Higgs boson? + other physics?  
solution at energy  $< 1$  TeV (1000 GeV)
- Why so many flavours of matter particles?  
mixing and CP violation?
- Unification of the fundamental forces?  
at very high energy  $\sim 10^{16}$  GeV?  
probe directly via neutrino physics, indirectly via masses, couplings
- Quantum theory of gravity?  
(super)string theory: extra space-time dimensions?

LHC

LHC

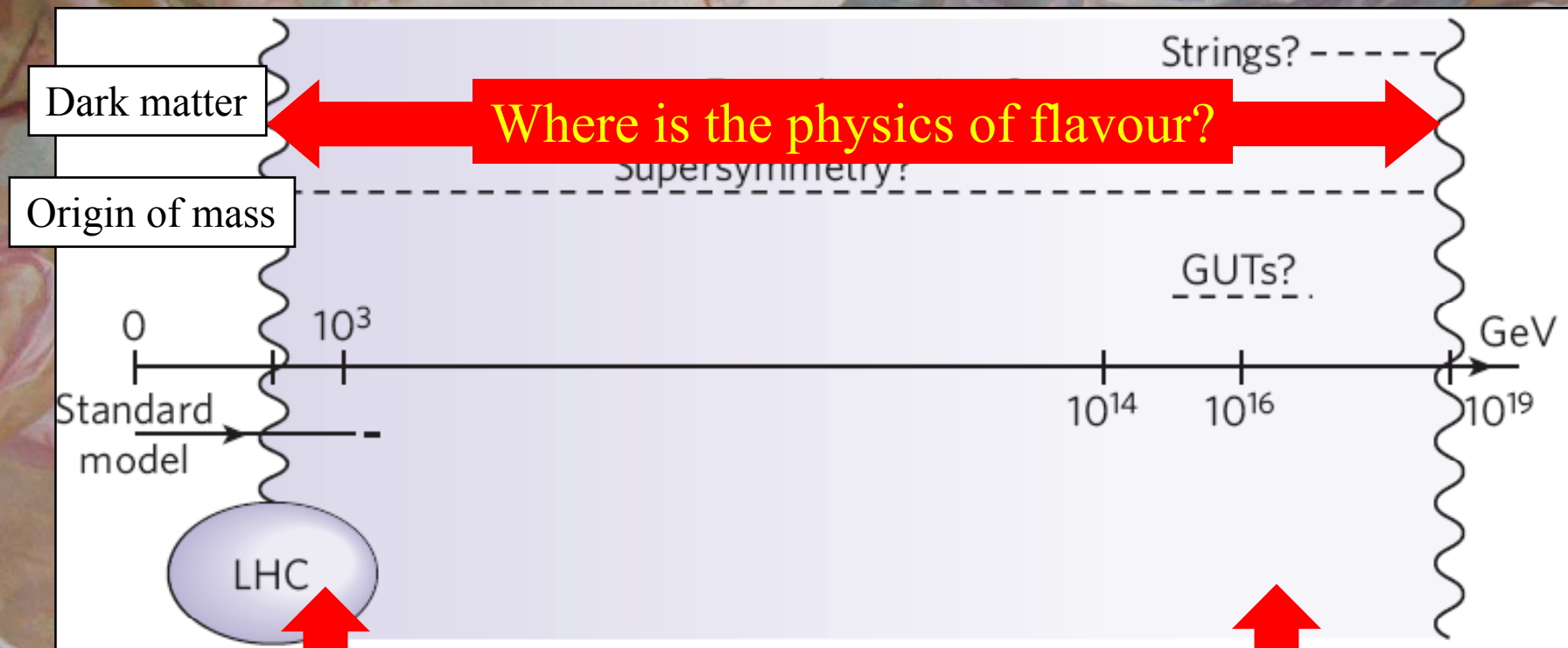
LHC

LHC

# High- $p_T$ Physics Meets Flavour

- The major particle physics objectives of the LHC
  - ATLAS, CMS, LHCb
- Good reasons to expect new physics at the TeV scale:
  - Higgs, naturalness, dark matter
- No clue where flavour physics originates
- What is flavour structure of TeV physics?
- How to reveal it?
  - Combine direct and indirect approaches

# At what Energy is the New Physics?



Where is the physics of flavour?

A lot accessible to the LHC

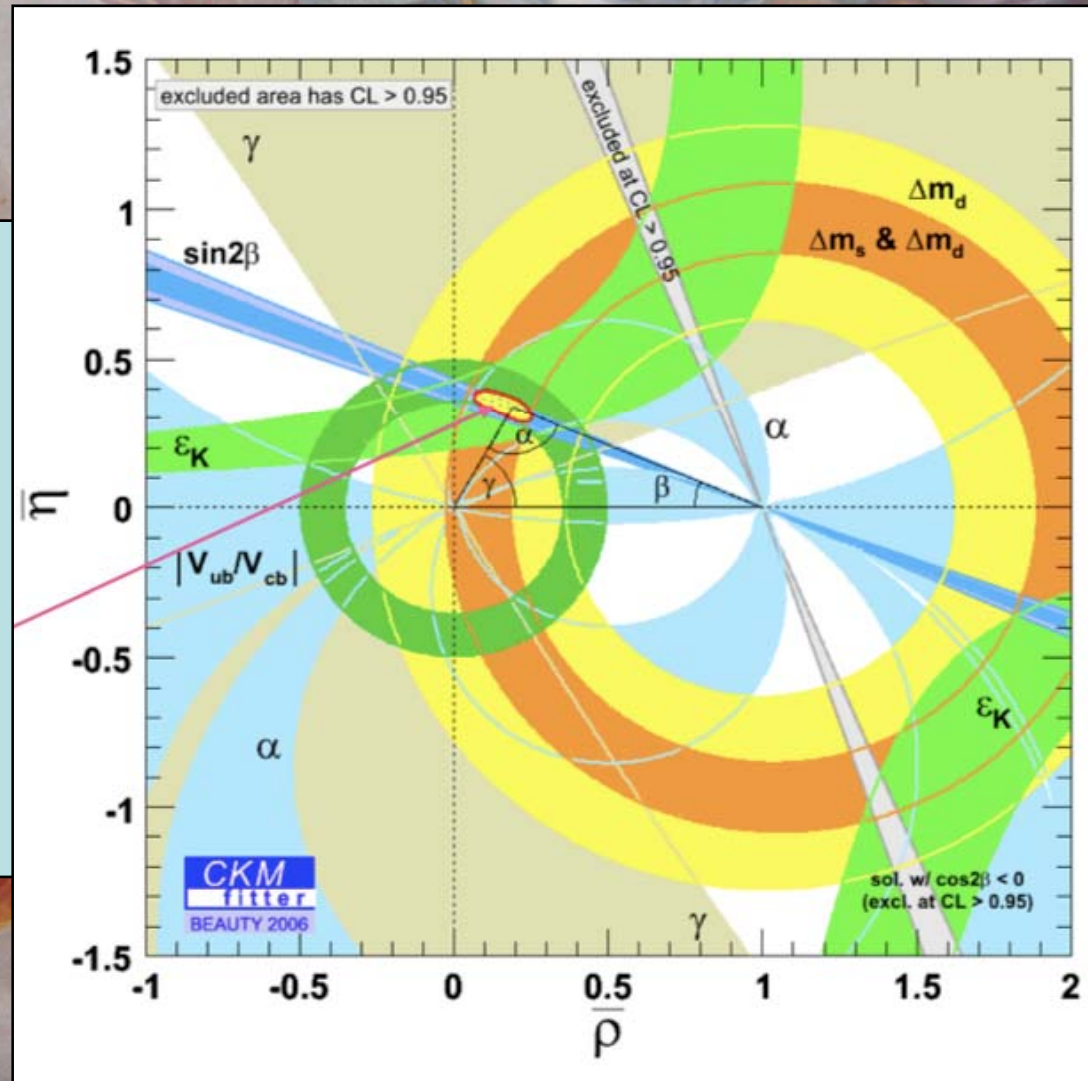
Some accessible only indirectly

# The Dogs that did (not) Bark

- In the quark sector:
  - CKM model describes perfectly the available data on quark mixing and CP violation
  - Passes consistency tests
- In the lepton sector:
  - MNS model describes neutrino mixing
  - No consistency tests
  - Muon anomalous magnetic moment may suggest new physics at the TeV scale

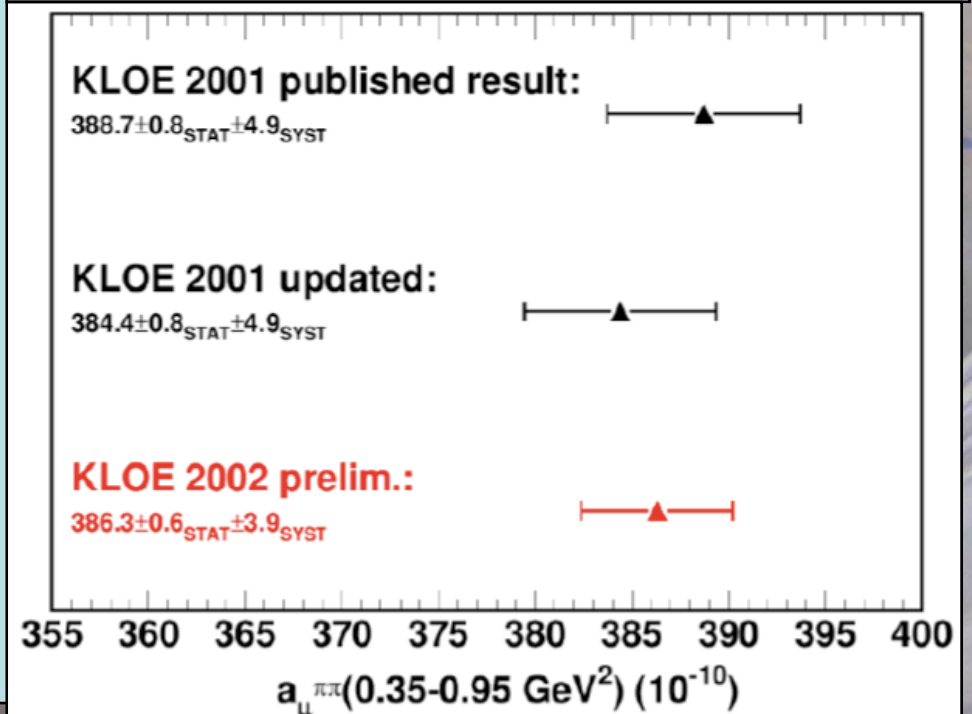
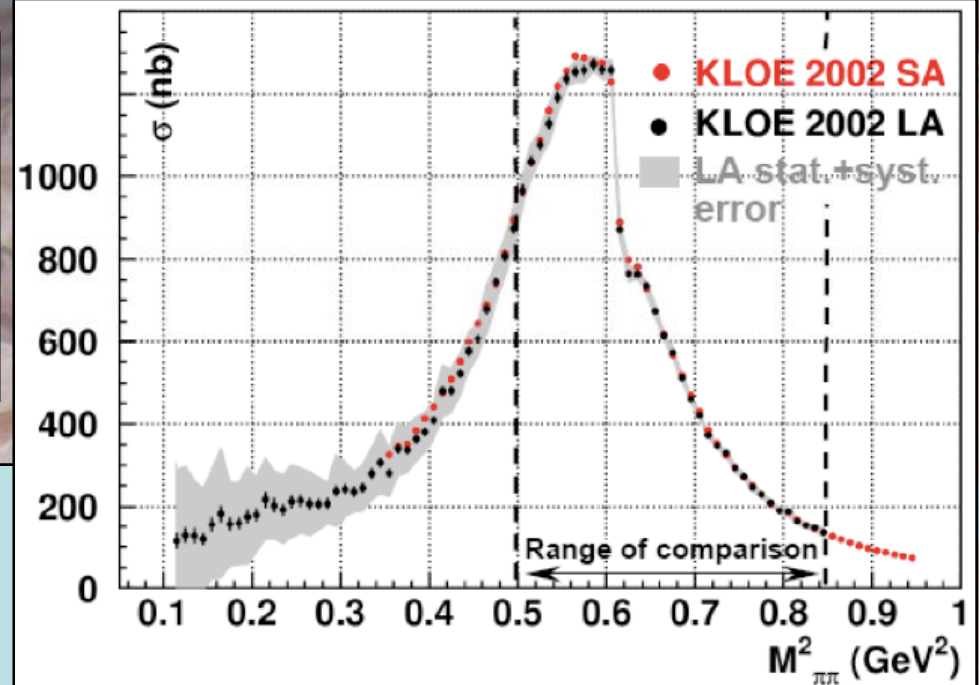
# Flavour and CP Violation

- CKM model successful at present
- A pillar of the Standard Model
- What lies beyond it?



# Quo Vadis $g_\mu - 2?$

- New  $e^+e^-$  data agree with previous
- Strengthen discrepancy – now  $3.4 \sigma$
- New  $\tau$  decay analysis apparently disagrees with previous, consistent with  $e^+e^-$



# Minimal Supersymmetric Extension of Standard Model (MSSM)

- Particles + spartners

$$\begin{pmatrix} \frac{1}{2} \\ 0 \end{pmatrix} \text{ e.g., } \begin{pmatrix} \ell \text{ (lepton)} \\ \tilde{\ell} \text{ (slepton)} \end{pmatrix} \text{ or } \begin{pmatrix} q \text{ (quark)} \\ \tilde{q} \text{ (squark)} \end{pmatrix} \begin{pmatrix} 1 \\ \frac{1}{2} \end{pmatrix} \text{ e.g., } \begin{pmatrix} \gamma \text{ (photon)} \\ \tilde{\gamma} \text{ (photino)} \end{pmatrix} \text{ or } \begin{pmatrix} g \text{ (gluon)} \\ \tilde{g} \text{ (gluino)} \end{pmatrix}$$

- 2 Higgs doublets, coupling  $\mu$ , ratio of v.e.v.'s =  $\tan \beta$
- Unknown supersymmetry-breaking parameters:  
Scalar masses  $m_0$ , gaugino masses  $m_{1/2}$ ,  
trilinear soft couplings  $A_\lambda$ , bilinear soft coupling  $B_\mu$
- Assume universality? constrained MSSM = CMSSM  
Single  $m_0$ , single  $m_{1/2}$ , single  $A_\lambda, B_\mu$ : not string?
- Not the same as minimal supergravity (mSUGRA)
- Gravitino mass, additional relations

$$m_{3/2} = m_0, B_\mu = A_\lambda - m_0$$



# Mass Renormalizations

- **Assuming universality at the GUT scale**
- Gaugino masses:
  - $M_a = (\alpha_a / \alpha_{\text{GUT}}) m_{1/2}$ , e.g.,  $\rightarrow M_2 / M_3 = \alpha_2 / \alpha_3$
- Squark and slepton masses:
  - Squark mass<sup>2</sup>:  $m_0^2 + 6 m_{1/2}^2$
  - Left-handed slepton mass<sup>2</sup>:  $m_0^2 + 0.5 m_{1/2}^2$
  - Right-handed slepton mass<sup>2</sup>:  $m_0^2 + 0.15 m_{1/2}^2$
- Minimal flavour violation (MFV):
  - Flavour mixing of squarks and sleptons induced by CKM, MNS mixing

# Current Constraints on CMSSM

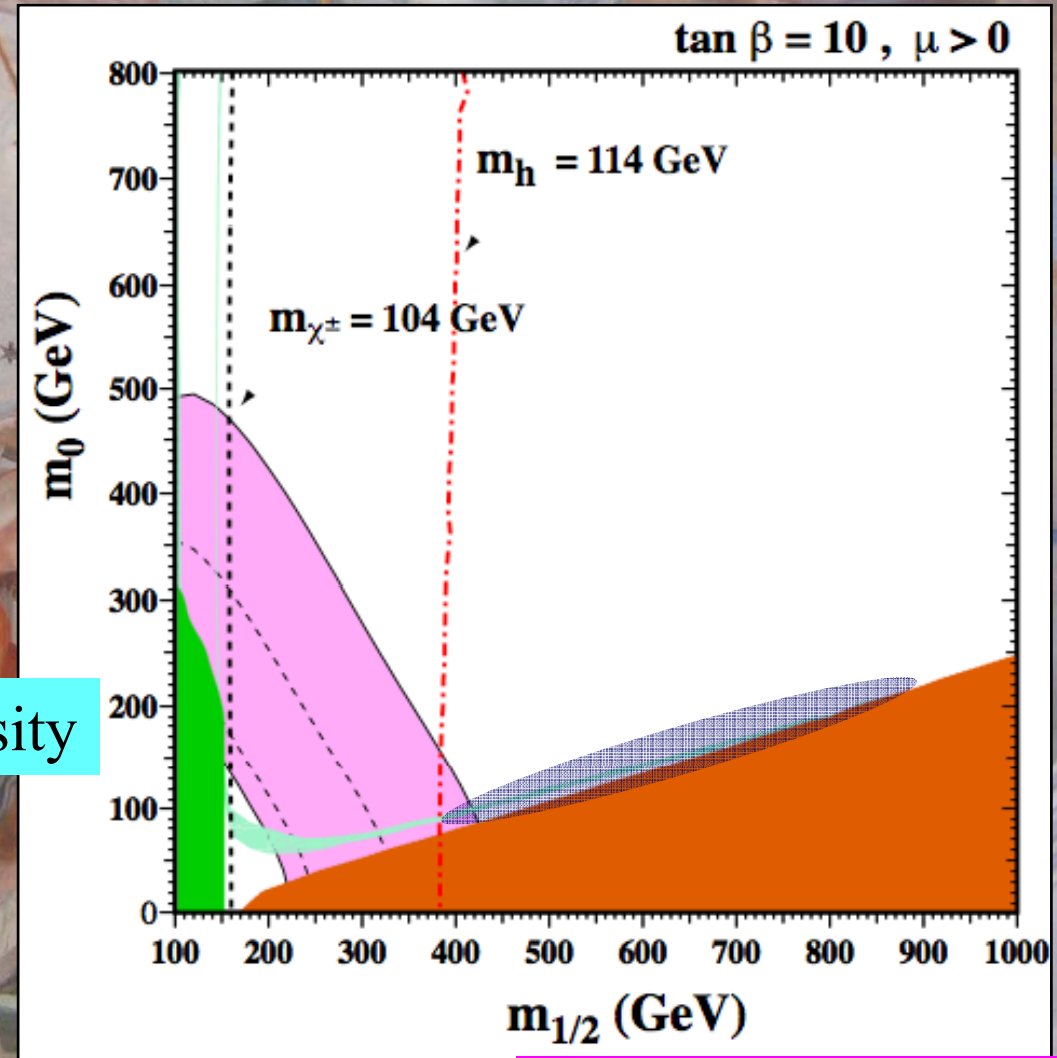
Assuming the lightest sparticle is a neutralino

Excluded because stau LSP

Excluded by  $b \rightarrow s$  gamma

WMAP constraint on relic density

Preferred (?) by latest  $g - 2$



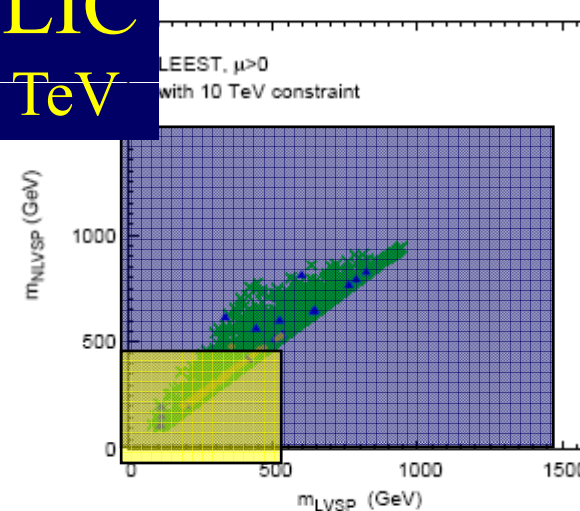
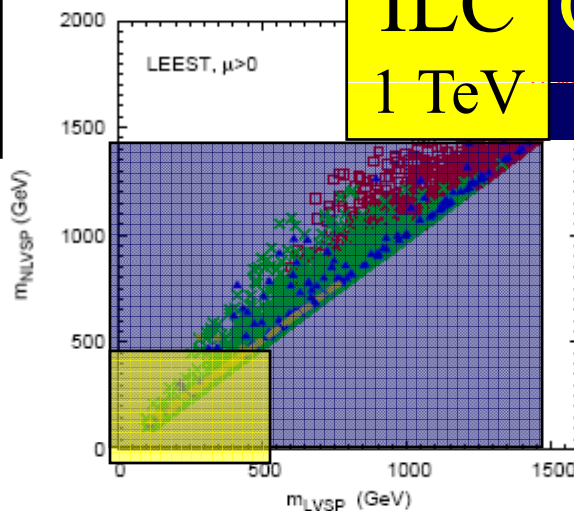
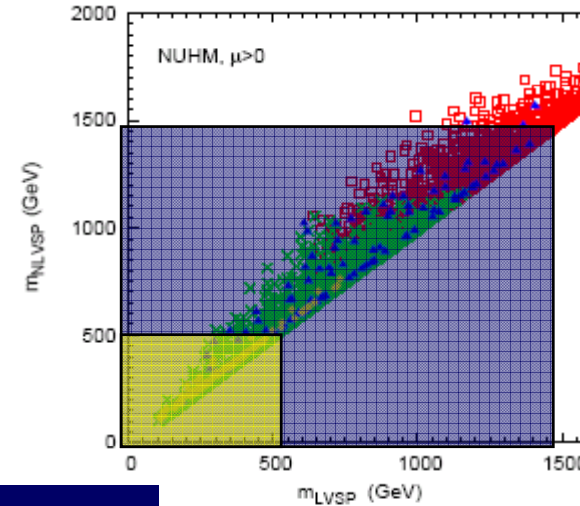
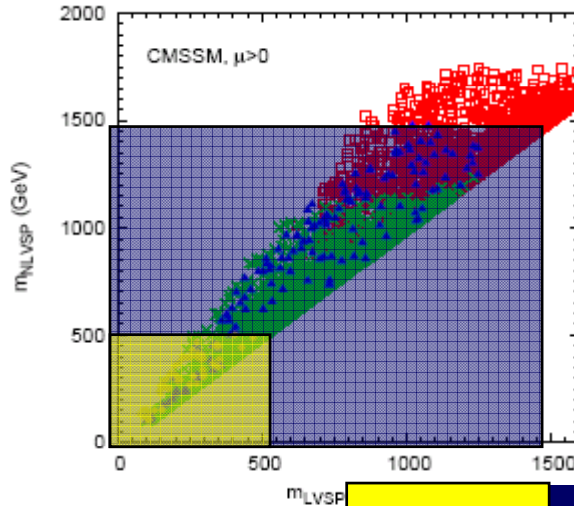
# Sparticles may not be very light

Full  
Model  
samples

Detectable  
@ LHC

Provide  
Dark Matter

Dark Matter  
Detectable  
Directly



ILC  
1 TeV

CLIC  
3 TeV

→ Second lightest visible sparticle

Lightest visible sparticle →

JE + Olive + Santoso + Span

Can one estimate the scale of supersymmetry?

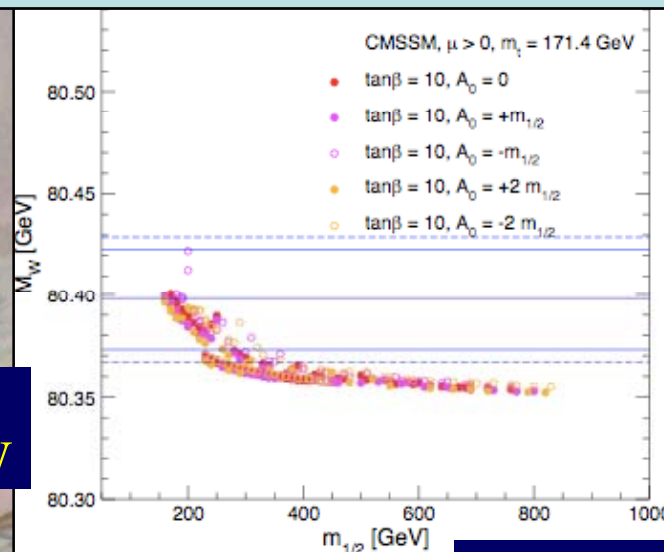
# Precision Observables vs Susy

Sensitivity to  $m_{1/2}$  in CMSSM along WMAP lines for different  $A$

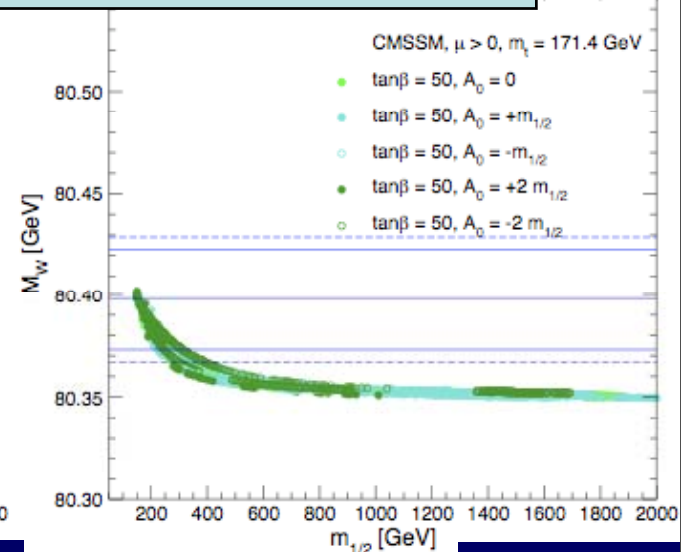
$m_W$

$\sin^2\theta_W$

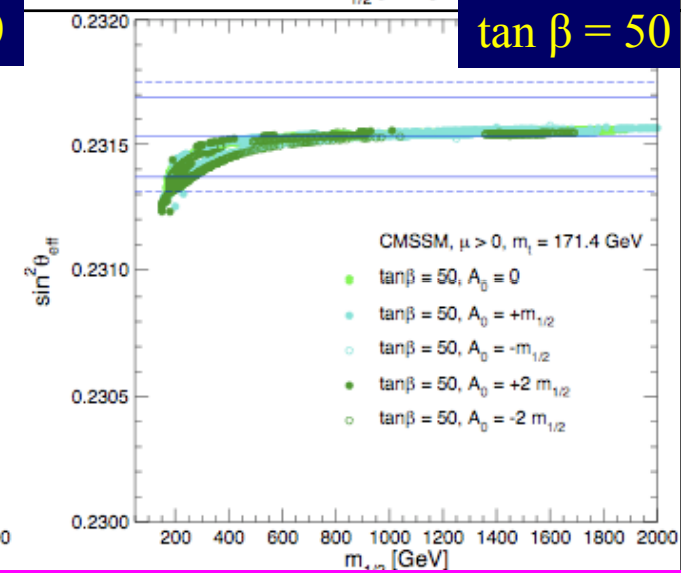
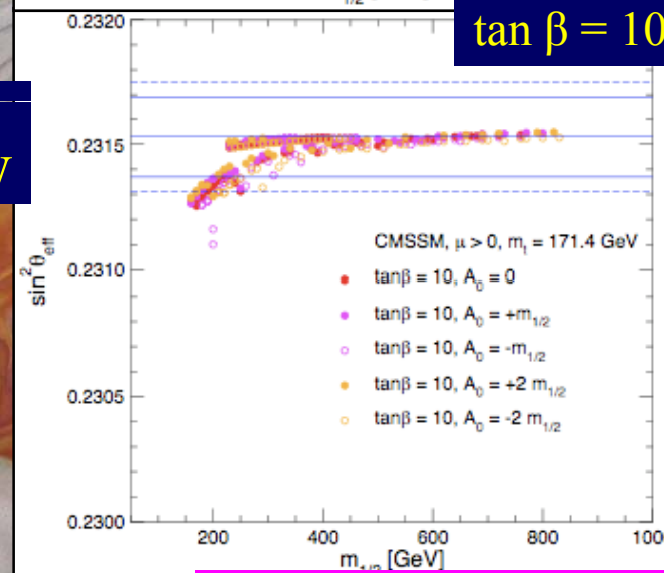
Present & possible future errors



$\tan\beta = 10$



$\tan\beta = 50$



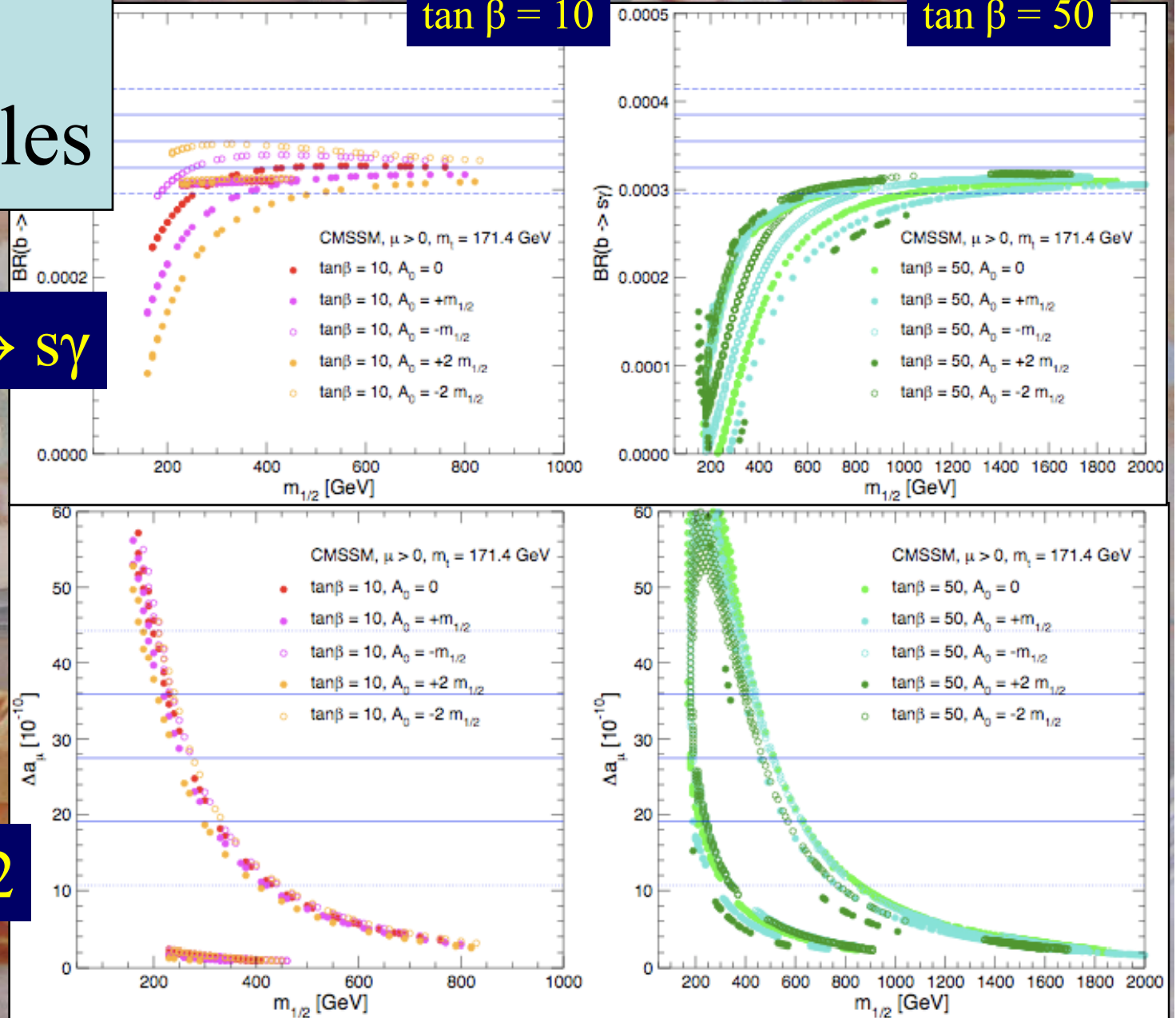
# More Observables

$b \rightarrow s\gamma$

$g_\mu - 2$

$\tan \beta = 10$

$\tan \beta = 50$



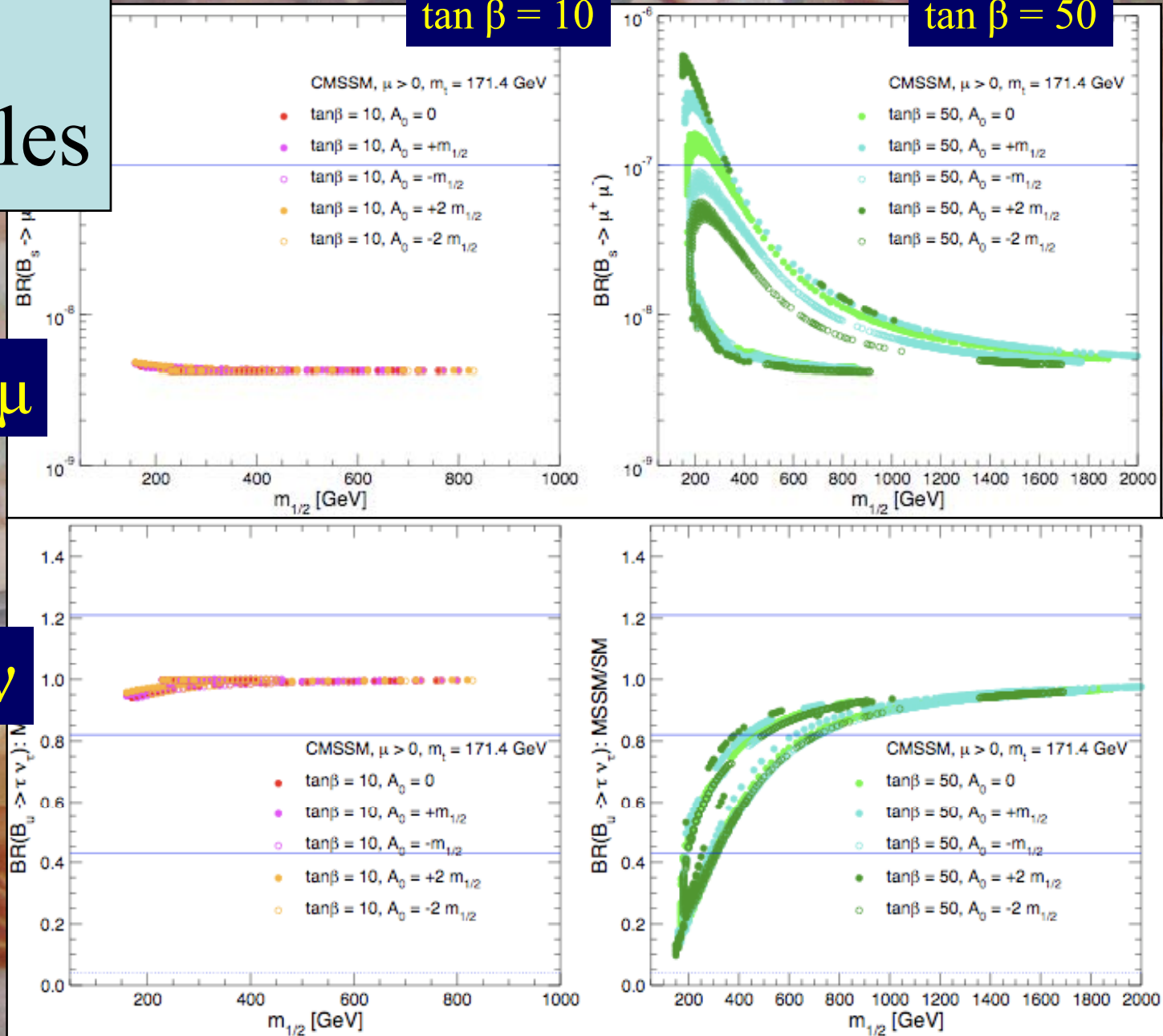
# More Observables

$$B_s \rightarrow \mu\mu$$

$$B_u \rightarrow \tau\nu$$

$\tan\beta = 10$

$\tan\beta = 50$



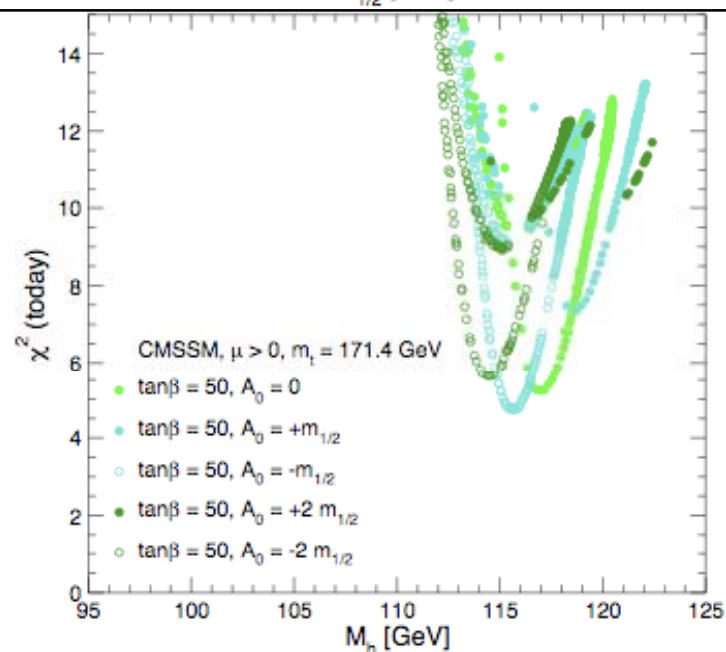
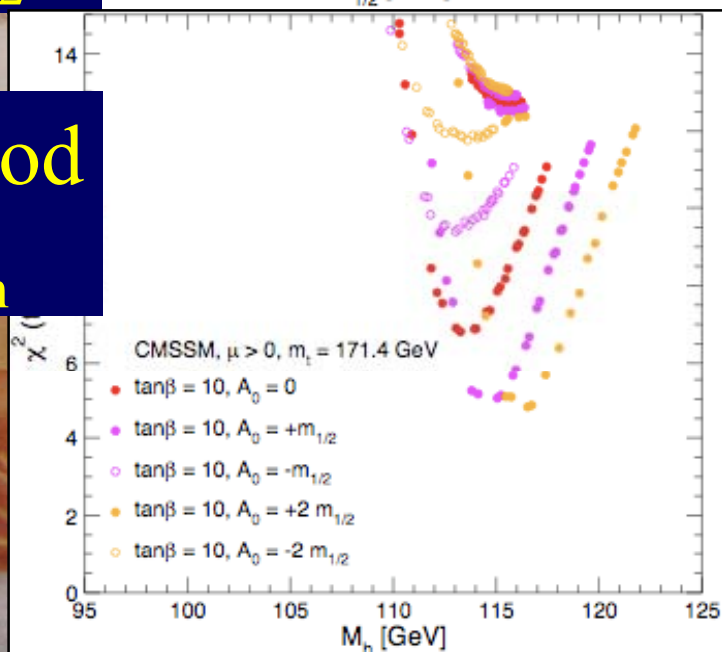
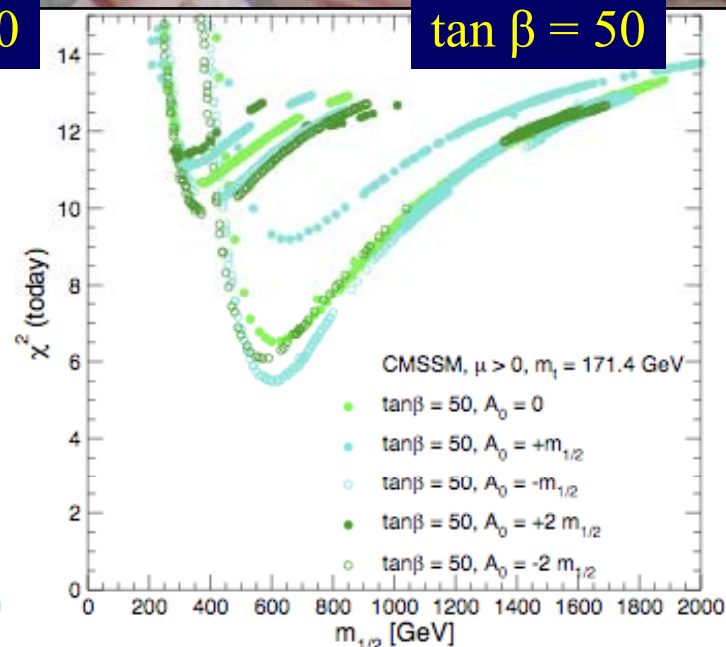
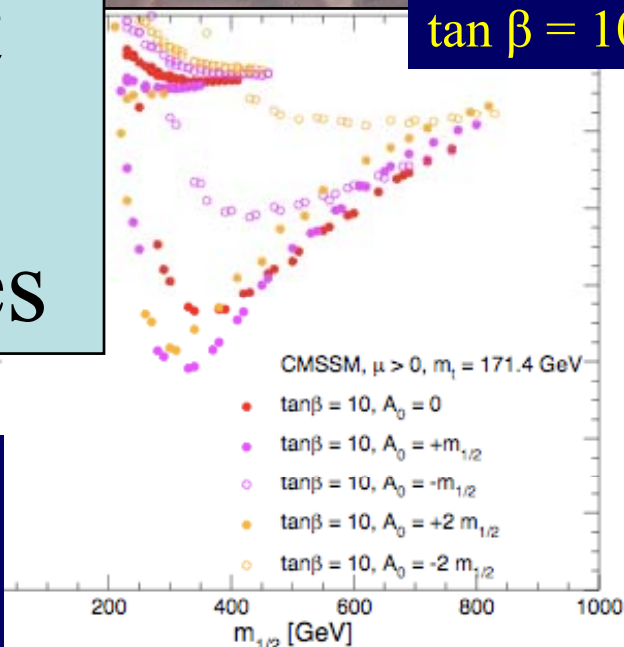
# Global Fit to all Observables

Likelihood  
for  $m_{1/2}$

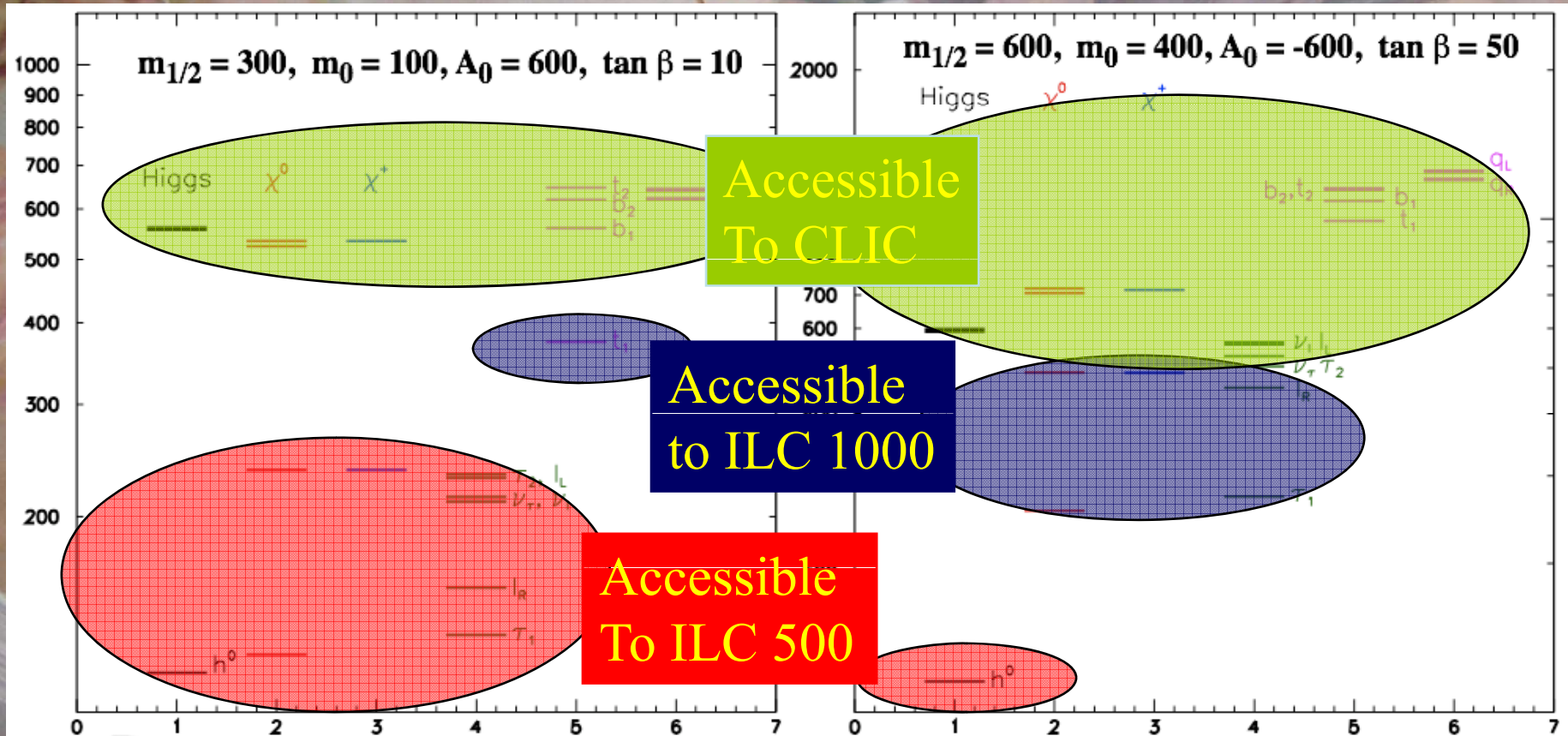
Likelihood  
for  $M_h$

$\tan \beta = 10$

$\tan \beta = 50$



# Spectra at Best-Fit Points



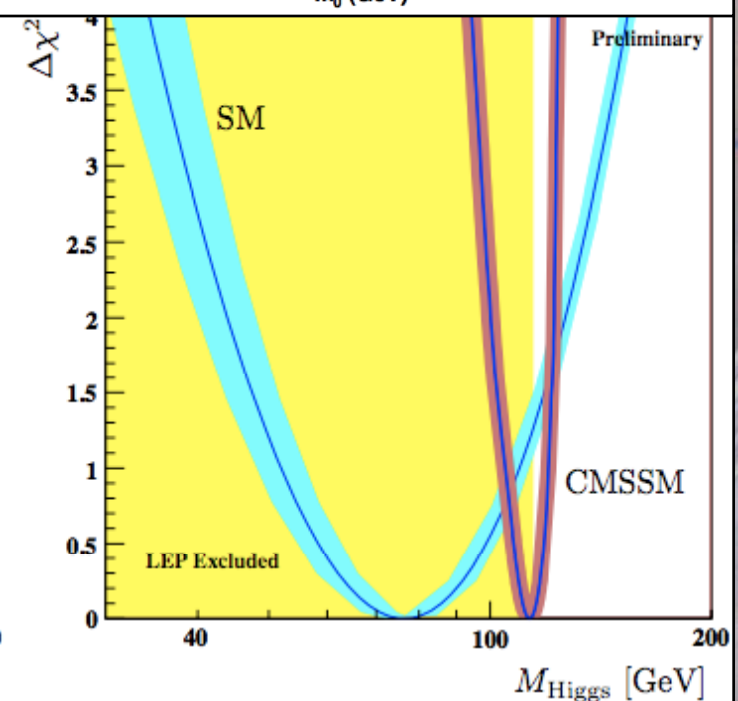
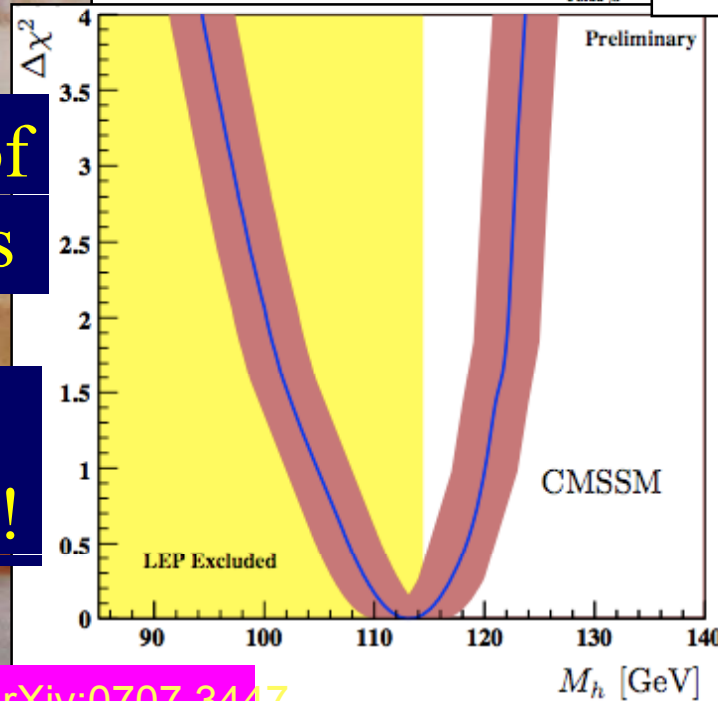
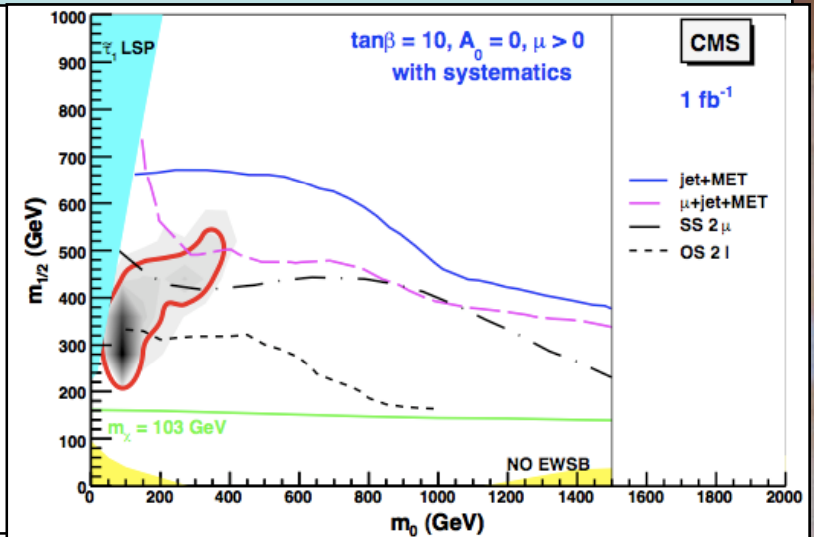
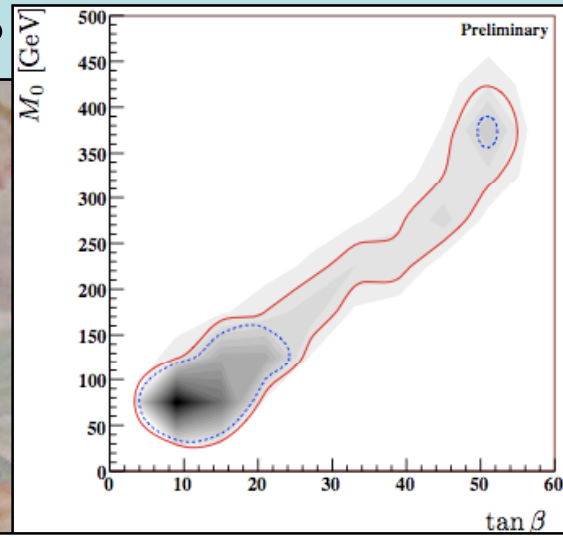


# Markov Chain Monte Carlo Analysis of Electroweak B Observables

More complete analysis of parameter space

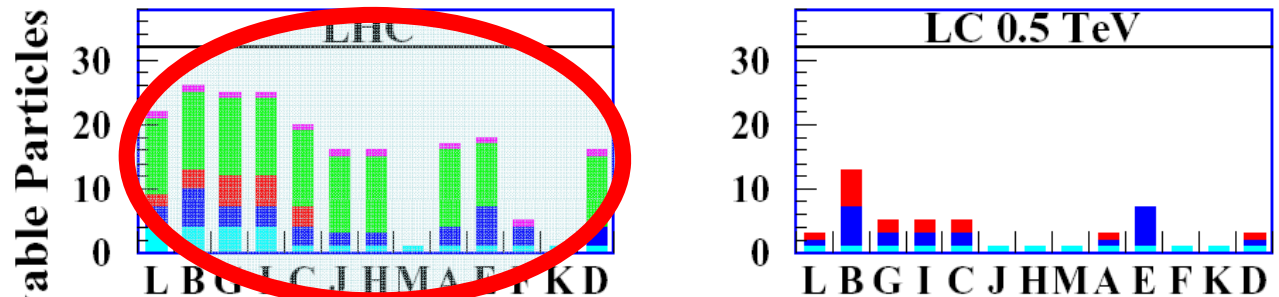
Larger set of observables

Better Graphics!



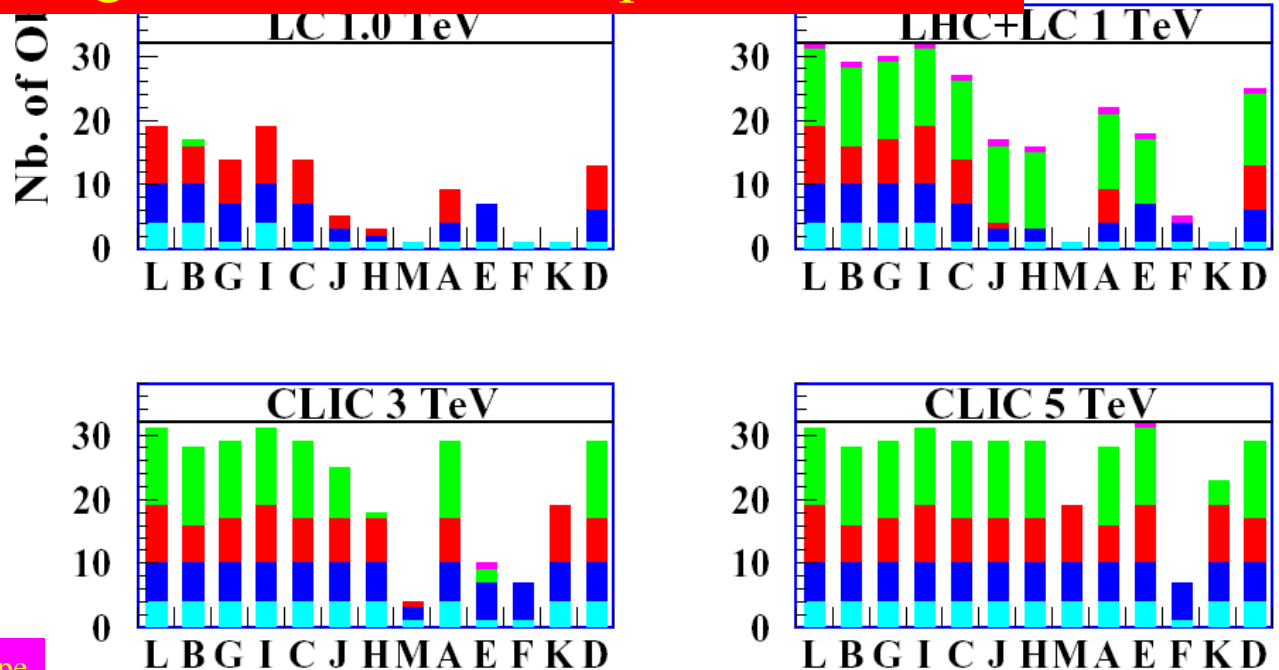
# Summary of LHC Scapabilities ... and Other Accelerators

█ gluino    █ squarks    █ sleptons    █  $\chi$     █ H  
**Post-WMAP Benchmarks**



How to distinguish the different squark flavours?

LHC almost  
'guaranteed'  
to discover  
supersymmetry  
if it is relevant  
to the mass problem



# Non-Universal Scalar Masses

- Different sfermions with same quantum #s?  
e.g., d, s squarks?  
disfavoured by upper limits on flavour-changing neutral interactions
- Squarks with different #s, squarks and sleptons?  
disfavoured in various GUT models  
e.g.,  $d_R = e_L$ ,  $d_L = u_L = u_R = e_R$  in SU(5), all in SO(10)
- Non-universal susy-breaking masses for Higgses?  
No reason why not!

# Minimal Flavour Violation (MFV)

- All squark mixing due to CKM matrix
- Universal scalar masses at high scale for sparticles with same quantum numbers
- Parametrization:

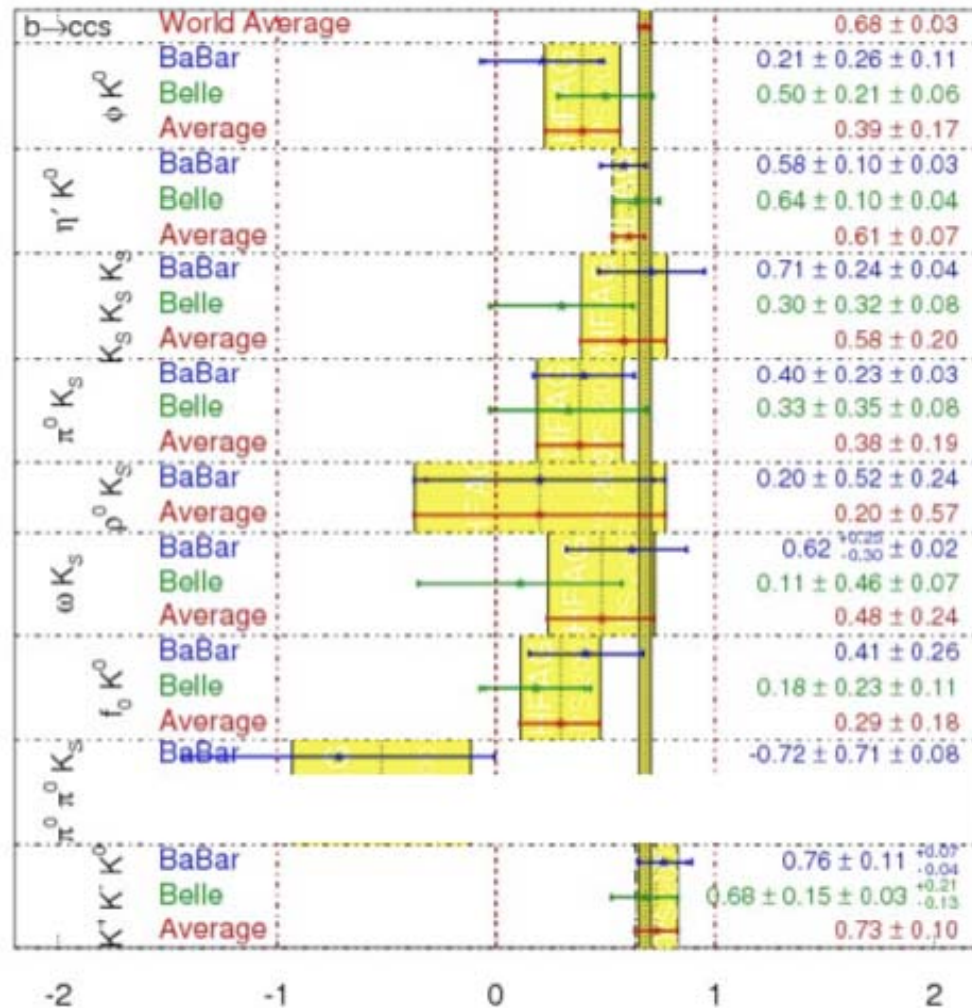
$$M_{1,2,3}, \quad M_{H_{u,d}}^2, \quad \widetilde{M}_{Q,L,U,D,E}^2 = \widetilde{M}_{Q,L,U,D,E}^2 \mathbf{1}_3, \quad A_{u,d,e} = A_{u,d,e} \mathbf{1}_3$$

- Maximally CP-violating MFV (MCPMFV) model has 19 parameters, of which 6 violate CP:

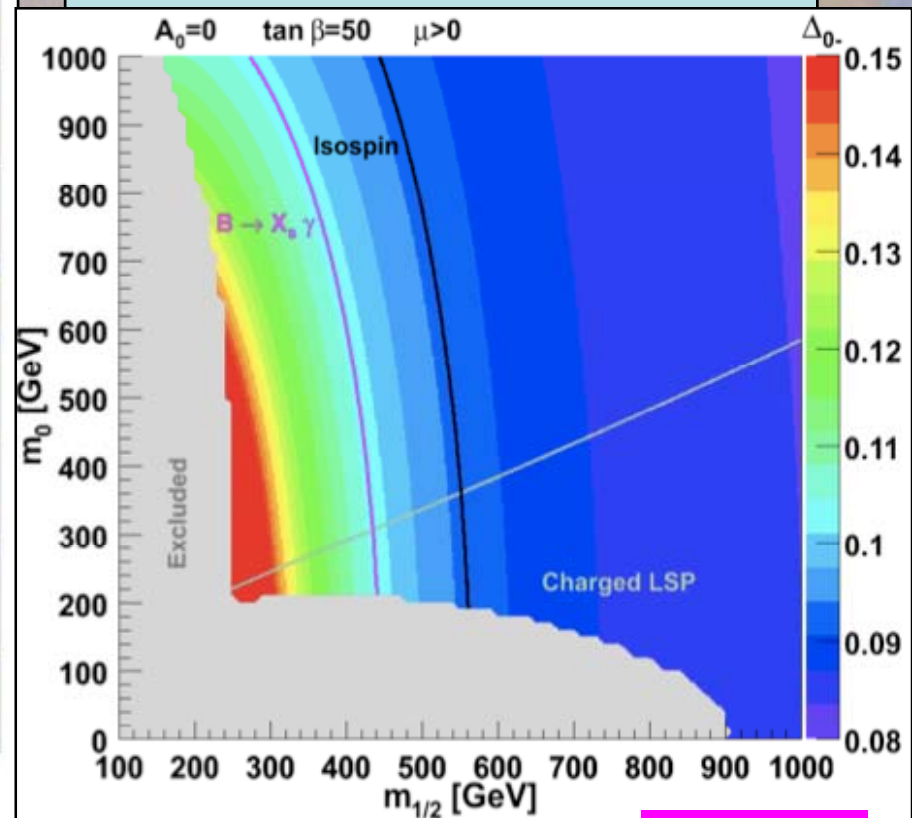
$$\text{Im } M_{1,2,3} \text{ and } \text{Im } A_{u,d,e}$$

- Often assume universal  $\text{Im}M_\alpha$ ,  $\text{Im}A_f$ , but non-universality compatible with MFV: **MCPMFV**

# Flavour in the LHC Era: Supersymmetric B Physics?



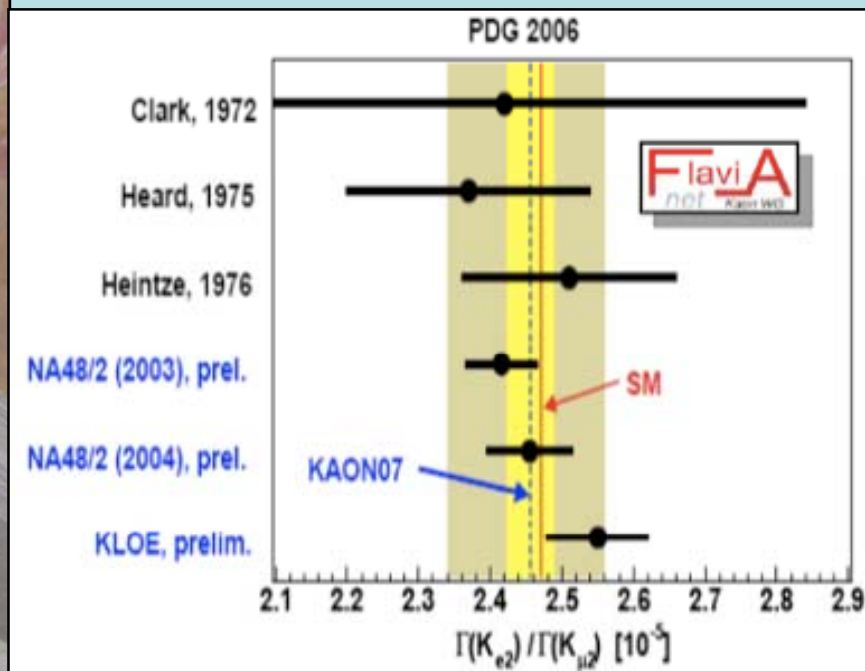
Discrepancies in B decays?  
Isospin asymmetry in  $B \rightarrow K^* \gamma$ ?



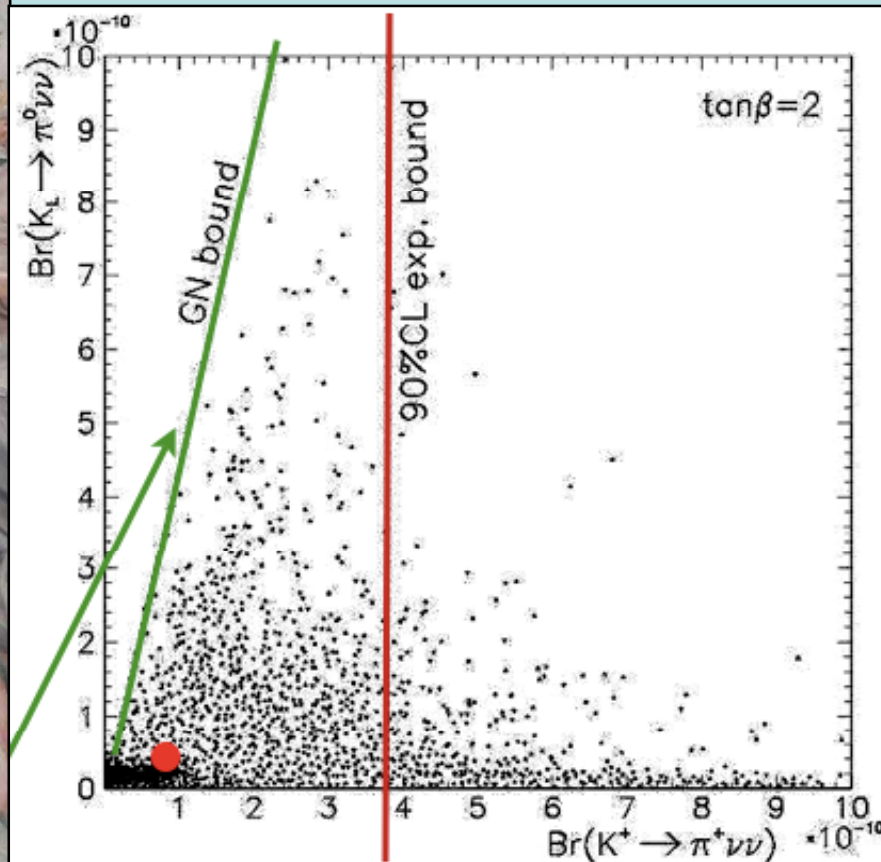
# Flavour in the LHC Era: Supersymmetric K Physics?

- Violation of universality in  $K \rightarrow e$

$$R_K^{LFV} \simeq R_K^{SM} \left[ 1 + \left( \frac{m_K^4}{M_H^4} \right) \left( \frac{m_\tau^2}{m_e^2} \right) |\Delta_R^{31}|^2 \tan^6 \beta \right]$$



- $K \rightarrow \pi \nu \nu$  decays?



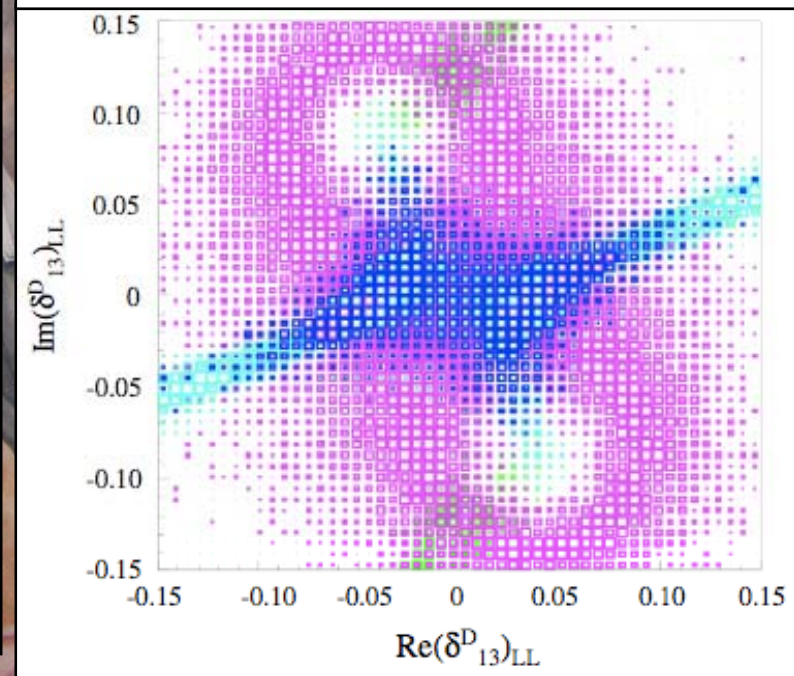
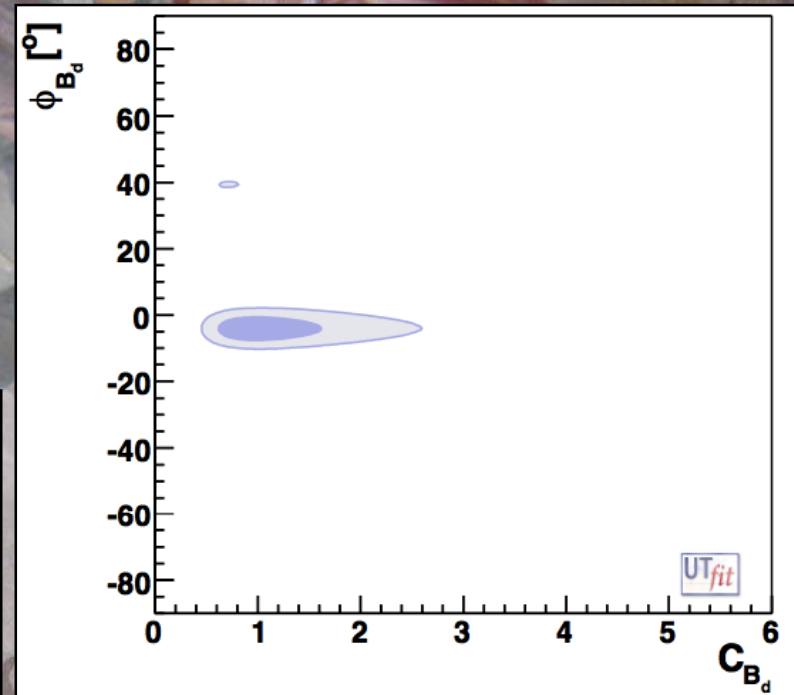
# Constraints Imposed by Success of CKM

- Limits on new physics in  $B_d$  mixing
- Constraint on  $D_{LL}$  mixing in supersymmetry:

$$(\delta^D_{13})_{LL} = \frac{(M^D_{13})^2_{LL}}{\langle M^D_{11} \rangle \langle M^D_{33} \rangle}$$

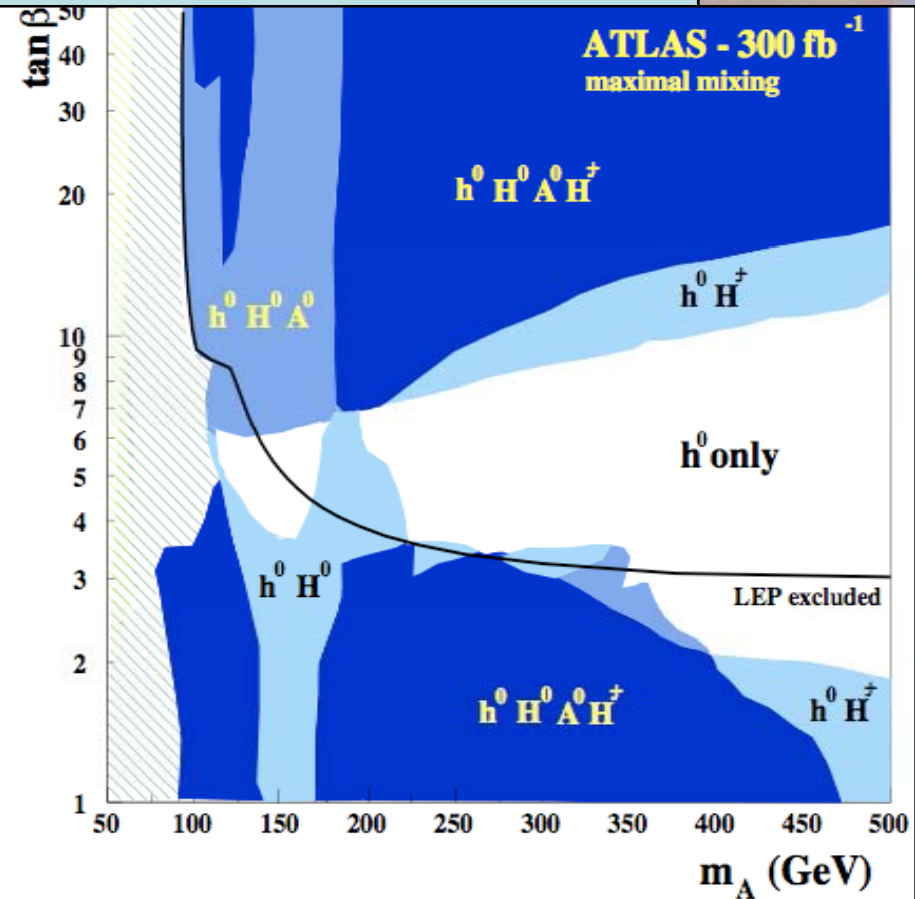
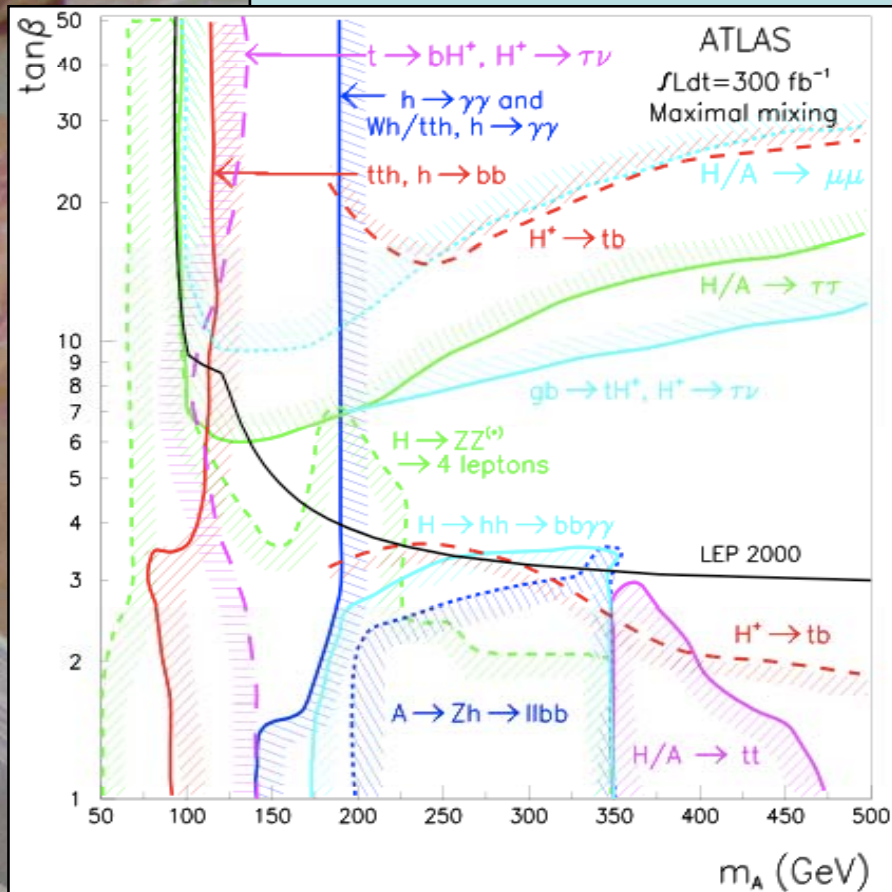
imposed by  $B_d$  mixing

- Analogous constraints on other mixing parameters



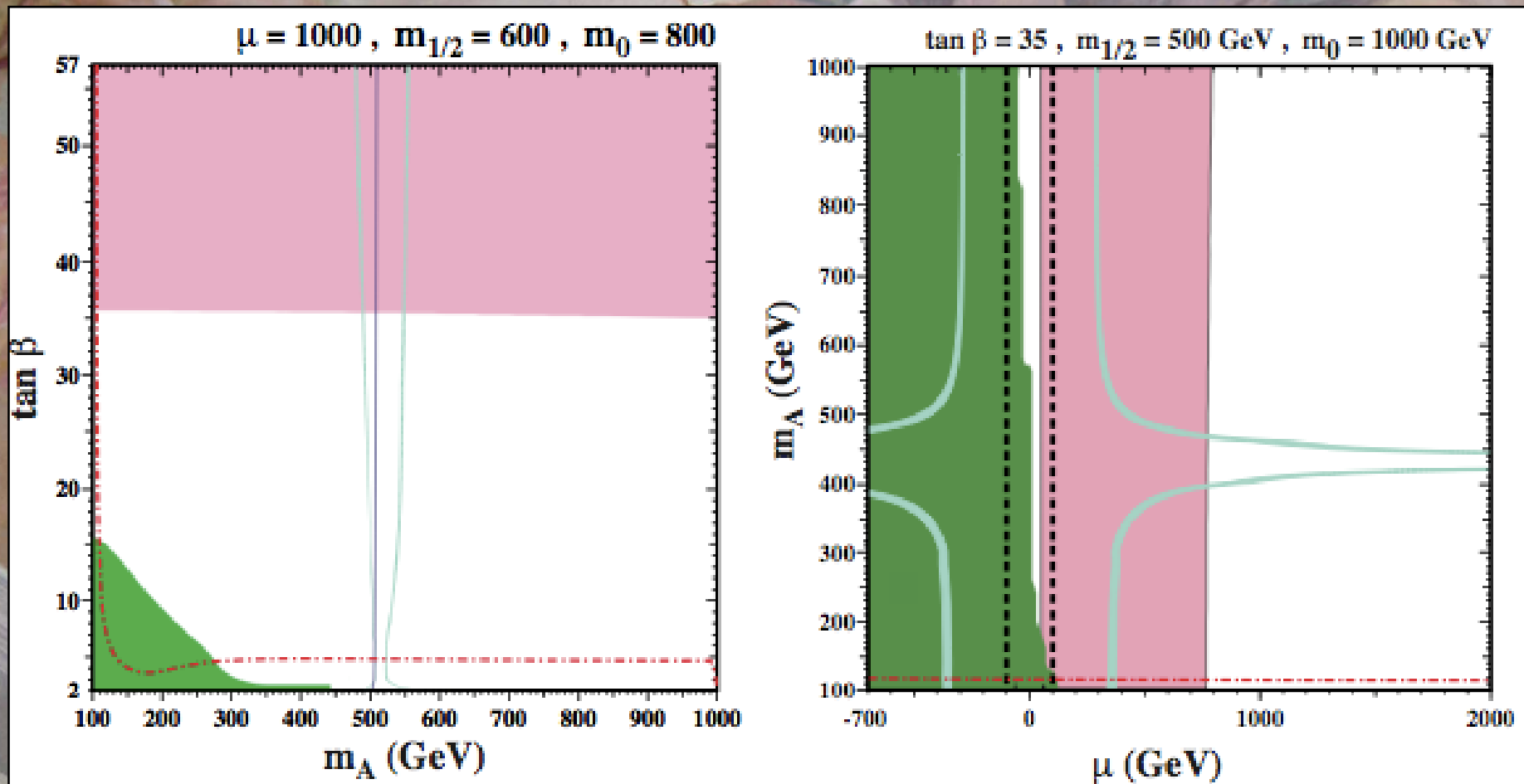
# Prospects for SUSY Higgses @ LHC

Cover entire plane at least (only)





# Most of $(m_A, \tan \beta)$ Planes **NOT** WMAP-Compatible



# Non-Universal Scalar Masses

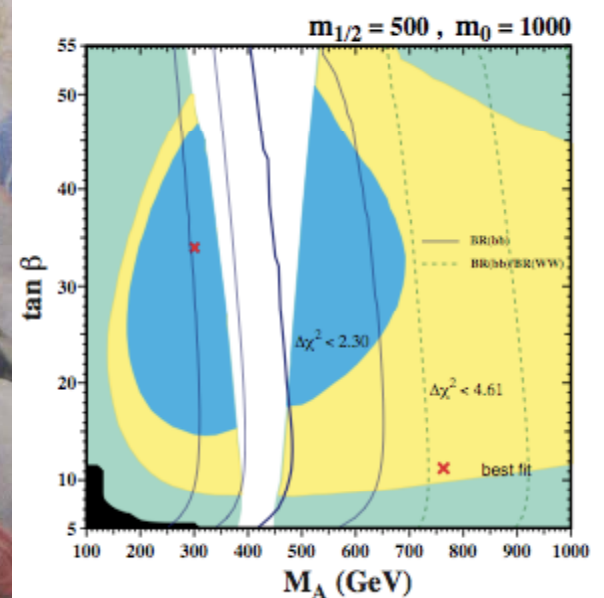
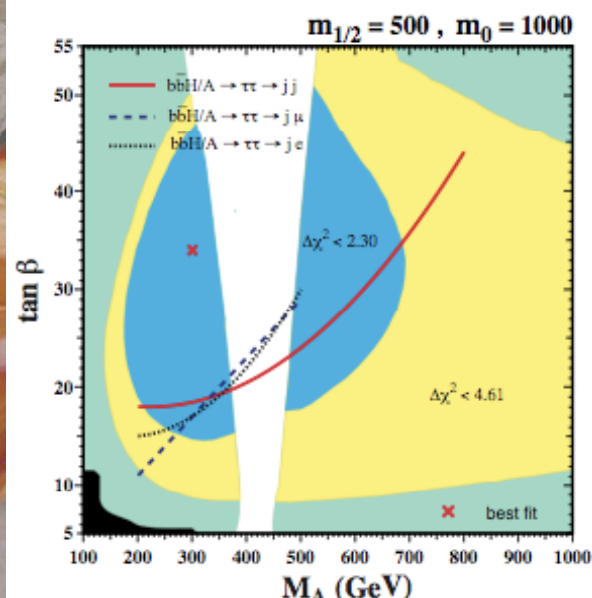
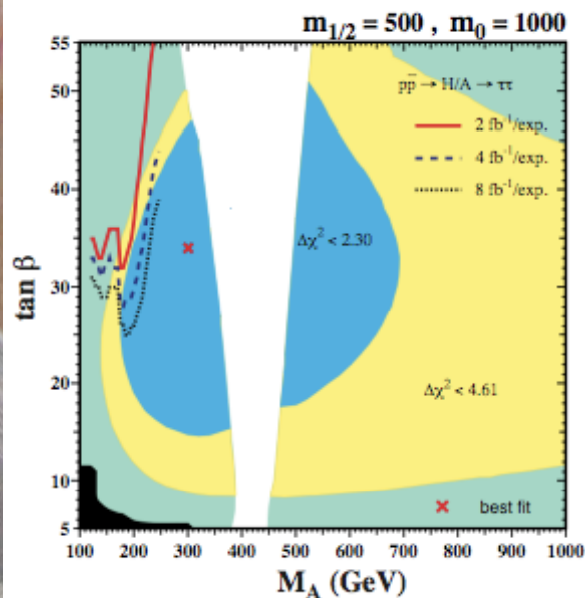
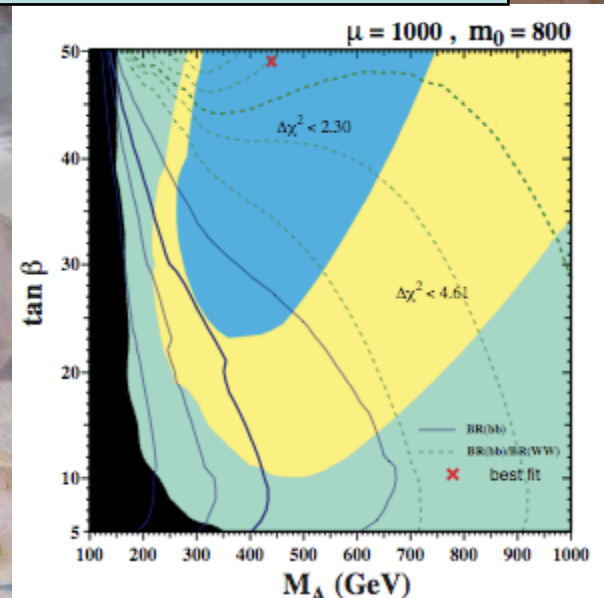
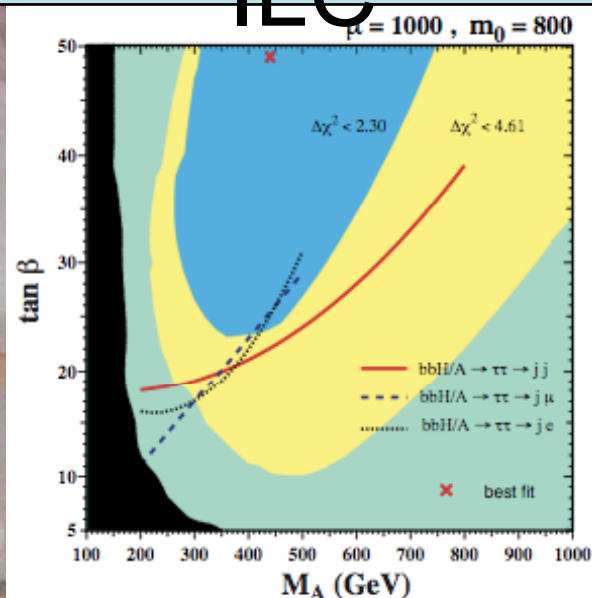
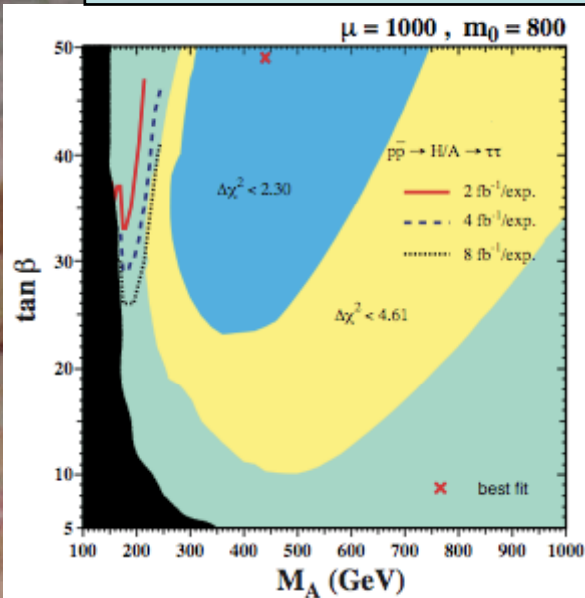
- Different sfermions with same quantum #s?  
e.g., d, s squarks?  
disfavoured by upper limits on flavour-changing neutral interactions
- Squarks with different #s, squarks and sleptons?  
disfavoured in various GUT models  
e.g.,  $d_p = e_p$ ,  $d_L = u_L = u_R = e_R$  in SU(5), all in SO(10)
- Non-universal susy-breaking masses for Higgses?  
No reason why not!

NUHM

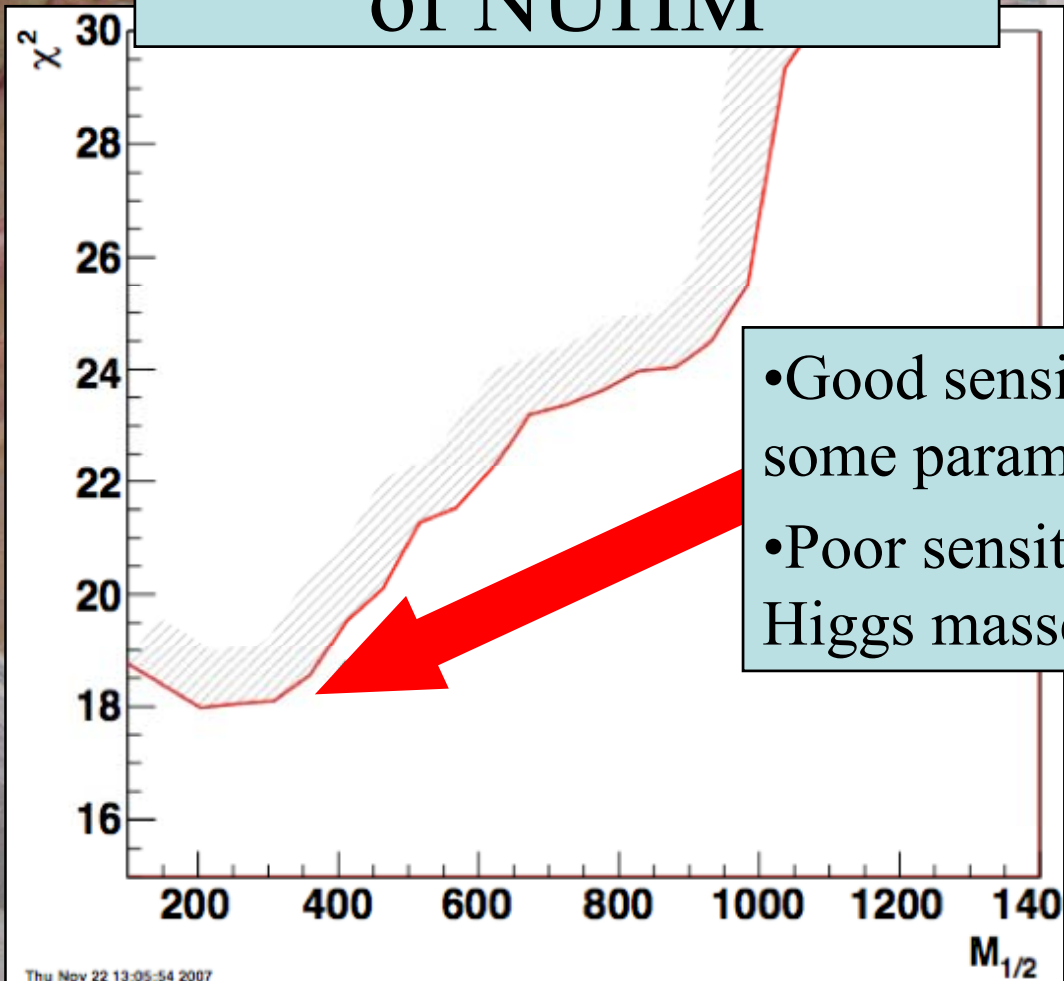
# WMAP-Compatible ( $m_A$ , $\tan\beta$ ) Surfaces in NUHM

- Within CMSSM, generic choices of  $m_A$ ,  $\tan\beta$  do not have correct relic density
- Use extra NUHM parameters to keep  $\Omega_\chi h^2$  within WMAP range, e.g.,
  - $m_0 = 800$  GeV,  $\mu = 1000$  GeV,  $m_{1/2} \sim 9/8 m_A$
  - $m_{1/2} = 500$ ,  $m_0 = 1000$ ,  $\mu \sim 250$  to 400 GeV
- Make global fit to electroweak and B observables
- Analyze detectability @  
Tevatron/LHC/ILC

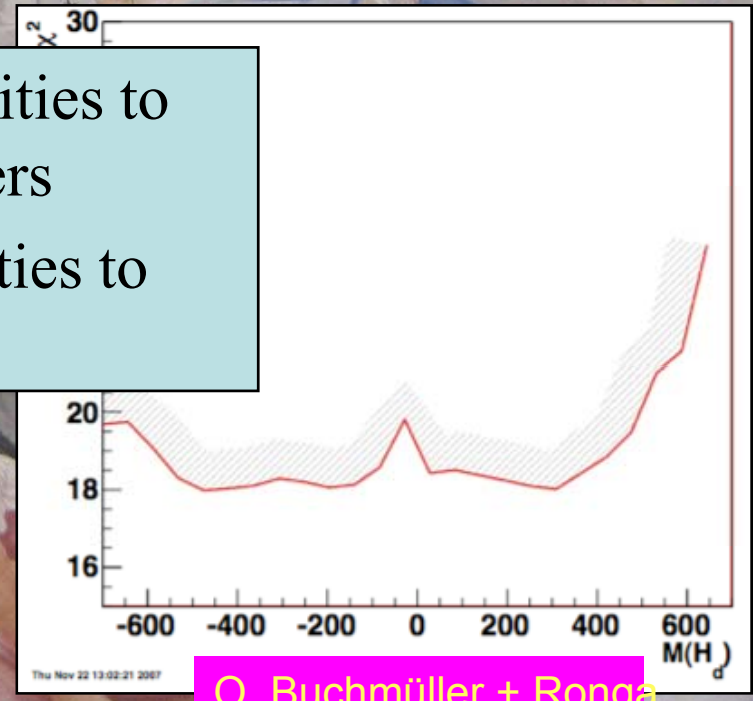
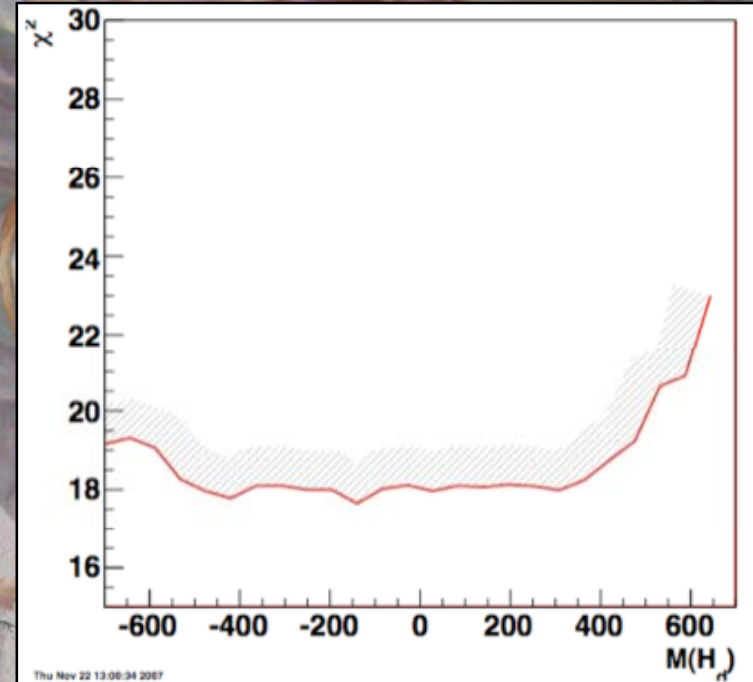
# WMAP Surfaces @ Tevatron, LHC, ILC



# Markov Chain Monte Carlo (MCMC) Analysis of NUHM

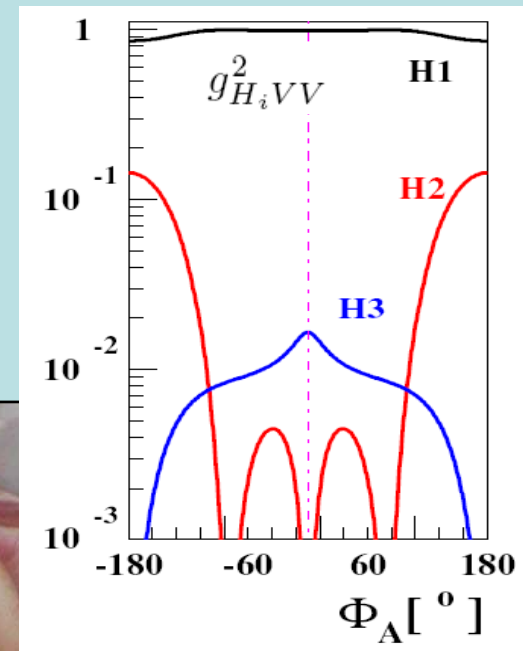
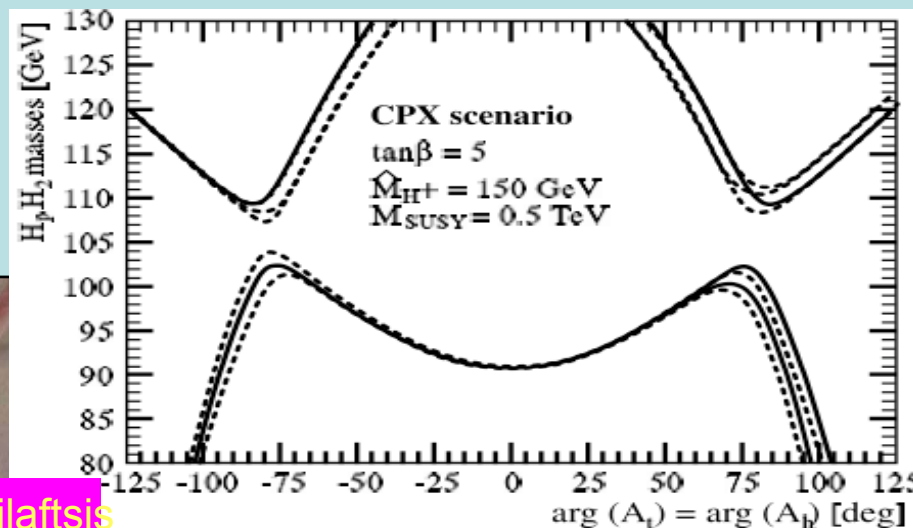


- Good sensitivities to some parameters
- Poor sensitivities to Higgs masses

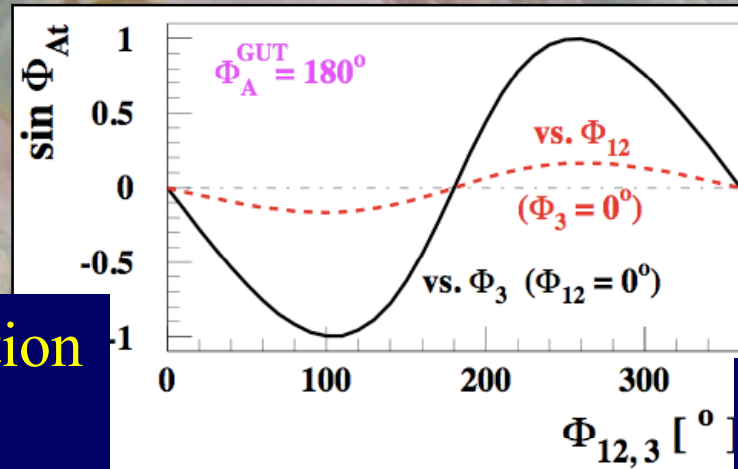


# Complexification of CMSSM

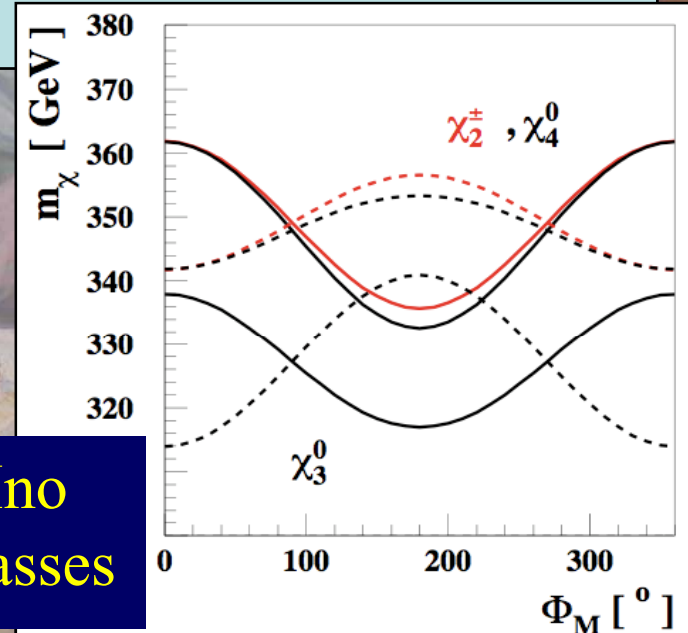
- With universality, just two new CP-violating parameters:
  - $\text{Arg}(M_a \mu), \text{Arg}(A_f \mu)$
- Loop-induced mixing  $\sim \frac{3}{16\pi^2} \frac{\text{Im}(A_f \mu)}{m_{\tilde{f}_2}^2 - m_{\tilde{f}_1}^2}$ 
  - $(h, H, A) \rightarrow (H_1, H_2, H_3)$  with indefinite CP
- Effects on masses, couplings



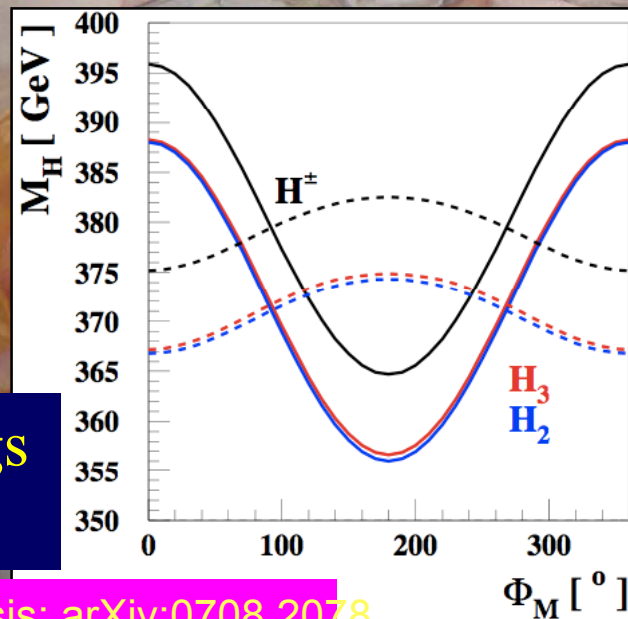
# Effects of CP Phases in MCPMFV



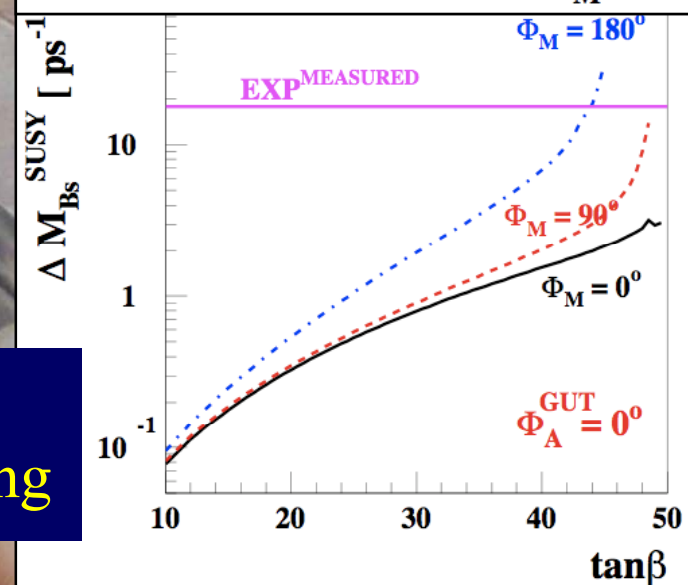
Renormalization  
of phases



Ino  
masses



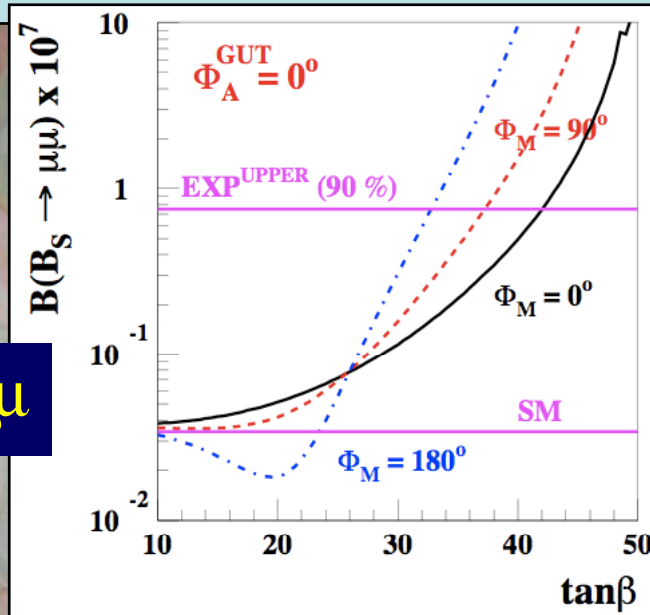
Heavy Higgs  
masses



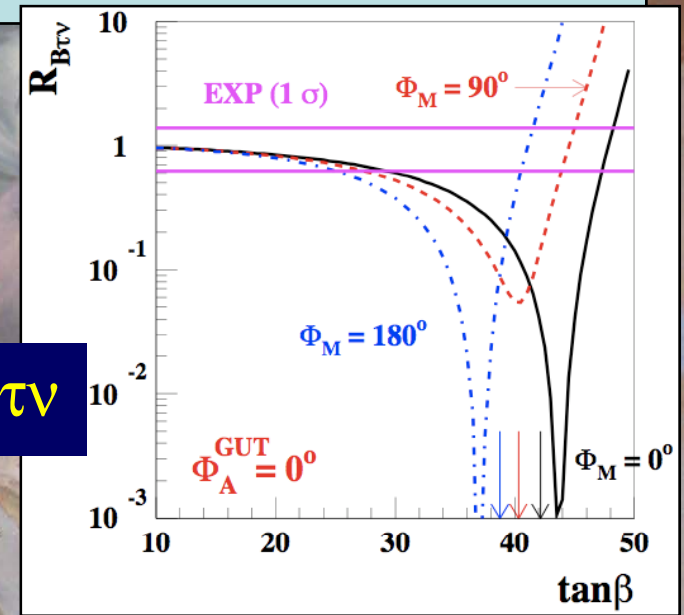
$B_s$   
mixing

# Effects of CP Phases in MCPMFV

$B_s \rightarrow \mu\mu$

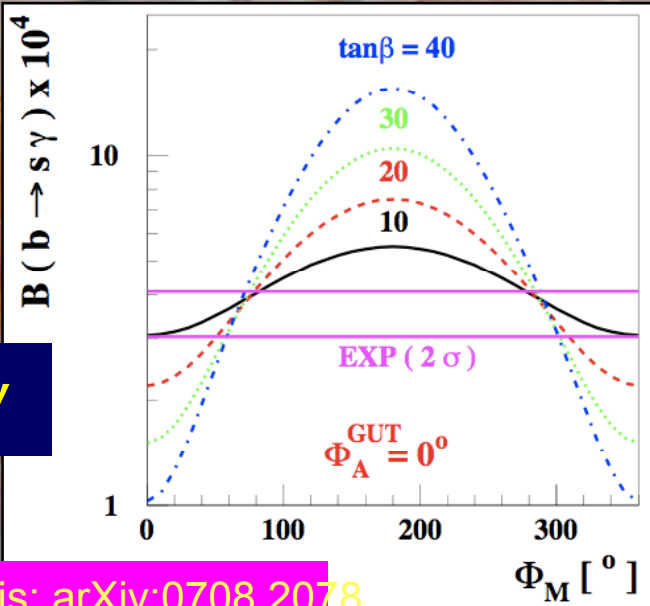


$B_u \rightarrow \tau\nu$

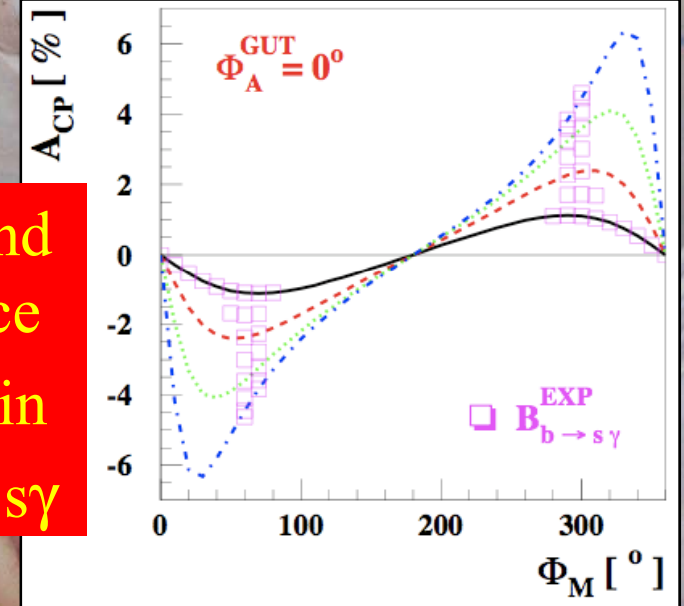


Different regions allowed for different phases ...

$b \rightarrow s\gamma$



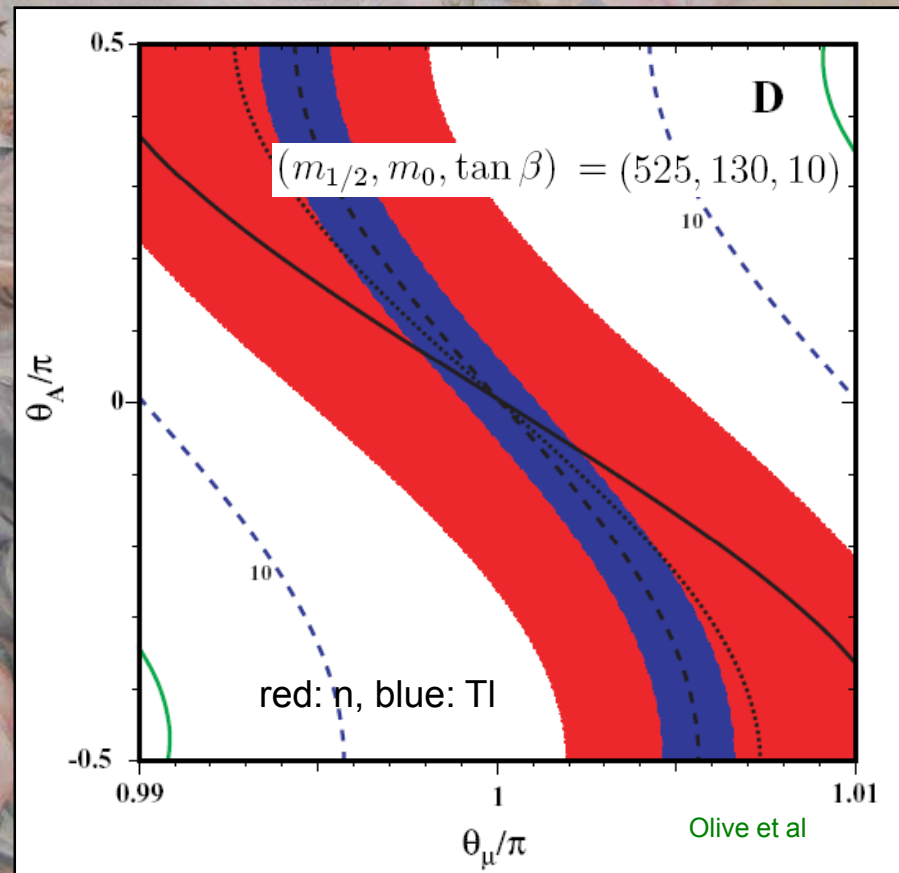
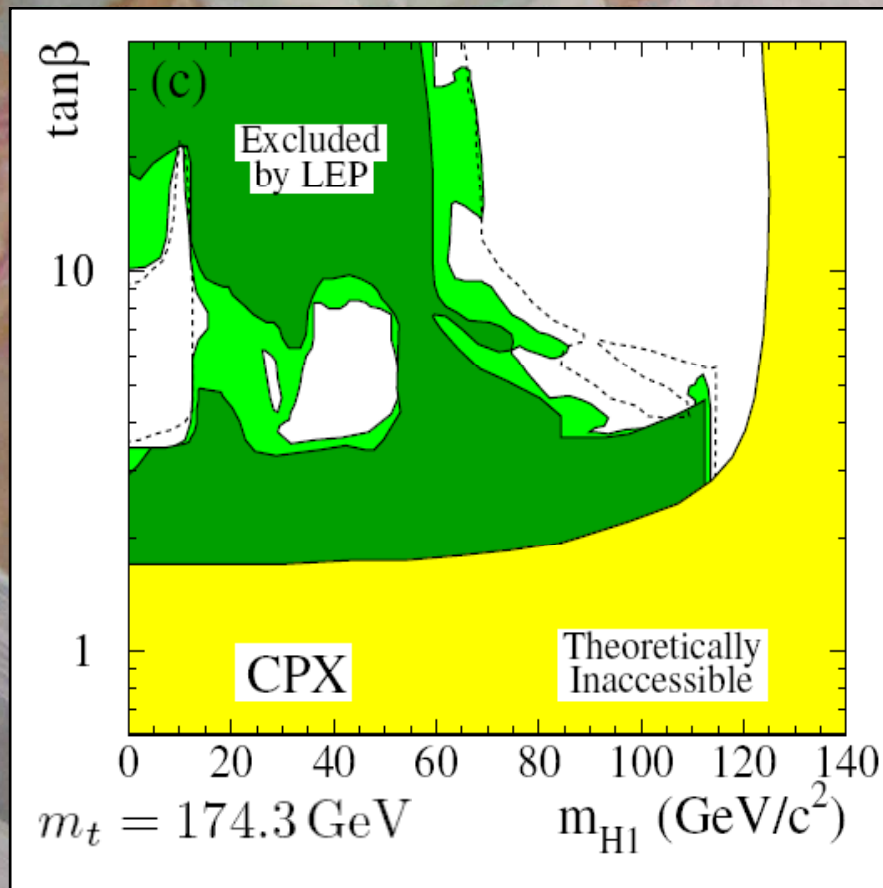
... and hence  $A_{\text{CP}}$  in  $b \rightarrow s\gamma$





# Experimental Constraints

From LEP, from electric dipole moments



## Lepton Flavour Violation

### Parameters in Minimal Seesaw Model

- Effective light-neutrino theory

$$-\mathcal{L}_\nu \supset (Y_\nu)_{ij} H \bar{N}_i \begin{pmatrix} \nu \\ L \end{pmatrix}_j + \underbrace{\frac{1}{2} \bar{N}_i \mathcal{M}_{ij} \bar{N}_j}$$

- 3 masses, 3 mixing angles, 3 CP-violating phases
- Additional 9 parameters associated with heavy singlet ‘right-handed’ neutrinos:
  - 3 more masses, 3 more mixing angles,
  - 3 more CP-violating phases
- 12 contribute to leptogenesis, not MNS phase  $\delta$
- If supersymmetric, 16 parameters contribute to renormalization of soft susy-breaking  $m_0$

# How to Measure Neutrino Parameters?

7 measurable:  
 $m_{1,2,3}, \theta_{12}, \theta_{13}, \theta_{23}, \delta$   
 not  $\varphi_{1,2}$ ?

Seesaw mechanism  
 $M_\nu$   
 9 effective parameters

$$\epsilon_{ij} = \frac{1}{8\pi} \frac{1}{(Y_\nu Y_\nu^\dagger)_{ii}} \text{Im} \left( (Y_\nu Y_\nu^\dagger)_{ij} \right)^2 f \left( \frac{M_j}{M_i} \right)$$

CP violation in decays  
 of heavy neutrinos

Leptogenesis  
 $Y_\nu Y_\nu^\dagger, M_{N_1}$   
 9+3 parameters

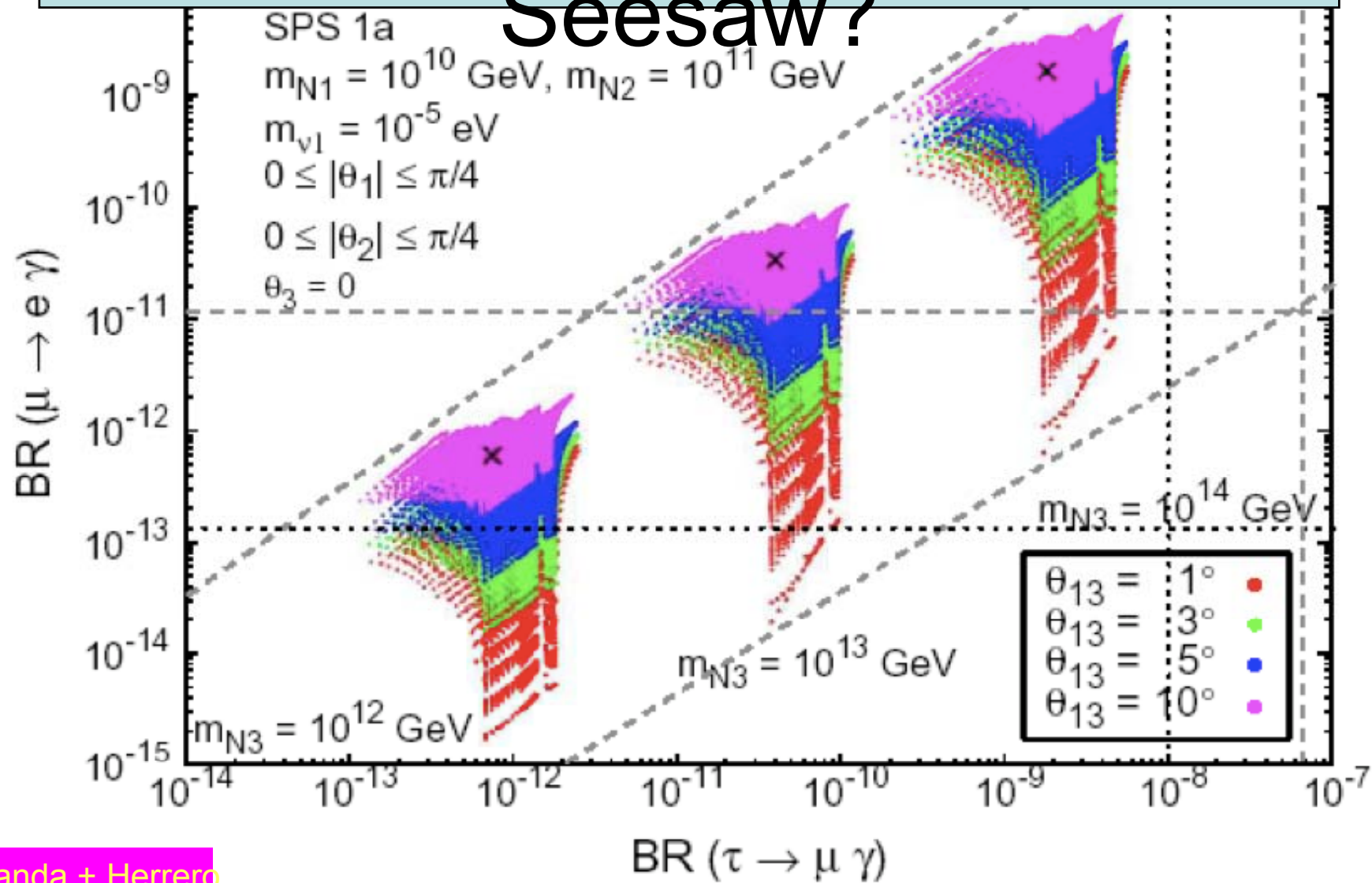
$Y_\nu, M_{N_1}$   
 15+3 physical  
 parameters

$$(\delta m_{\bar{L}}^2)_{ij} \ni -\frac{1}{8\pi^2} (3m_0^2 + A_0^2) (Y_\nu^\dagger Y_\nu)_{ij} \text{Ln} \left( \frac{M_{GUT}}{M} \right),$$

Induces flavour-changing  
 decays of charged leptons,  
 CP violation

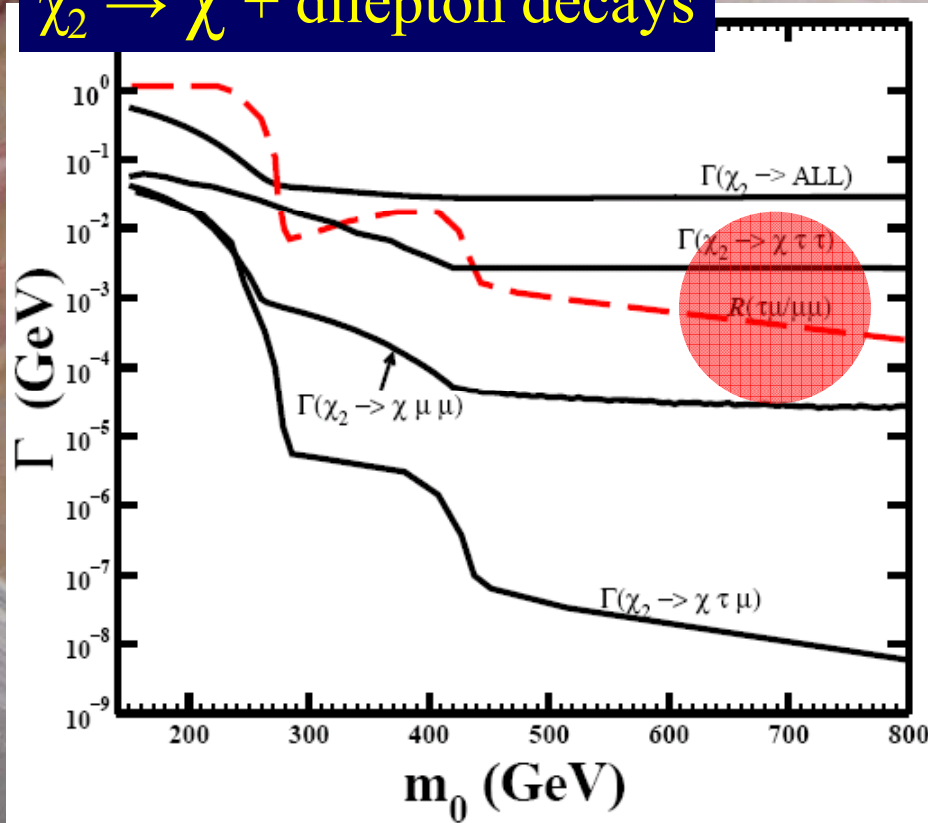
Renormalization  
 $Y_\nu^\dagger L Y_\nu, M_{N_1}$   
 13+3 parameters

# Flavour in the LHC Era: LFV in Supersymmetric Seesaw?

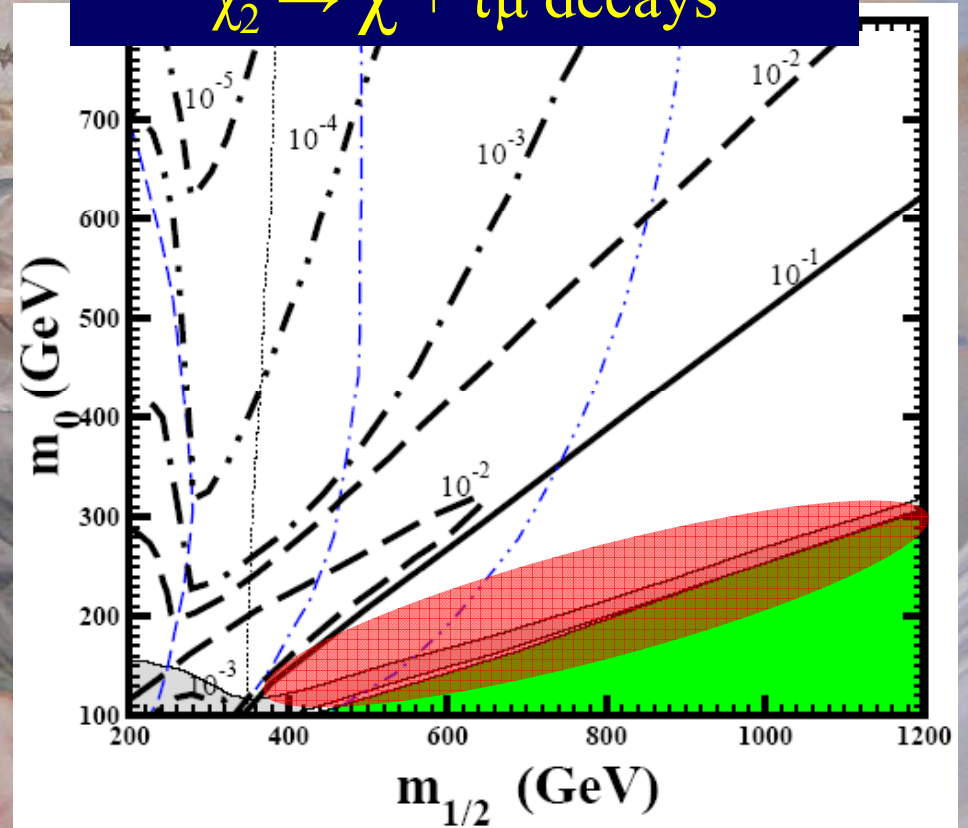


# Flavour Violation in Sparticle Decays @ LHC?

Possible rates for  
 $\chi_2 \rightarrow \chi + \text{dilepton decays}$



Possible branching ratios for  
 $\chi_2 \rightarrow \chi + \tau\mu$  decays



# Outlook

- Flavour is (perhaps) the most open problem in particle physics
  - The LHC will provide many flavour probes
- If the LHC discovers new physics at the TeV scale (supersymmetry, extra dimensions, ...), flavour problem will become more acute
  - What is flavour structure of new physics?
  - Low-energy effects of this TeV flavour physics?
- **Plenty of collider  $\leftrightarrow$  flavour interplay to play with!**