

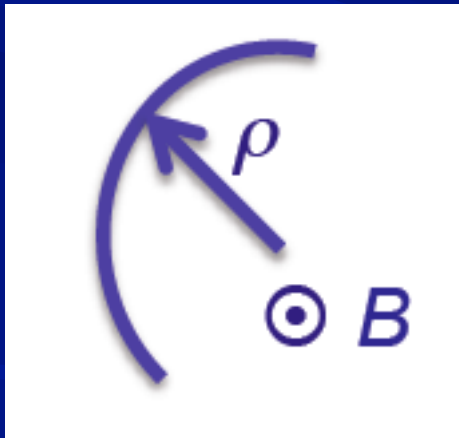
# Detectors for Particle Physics

Scintillators and Gaseous detector

**D. Bortoletto**  
**Purdue University**

# Tracking

- Particle detection has many aspects:
  - Particle counting
  - Particle Identification = measurement of mass and charge of the particle
  - Tracking
- Charged particles are deflected by B fields such that:



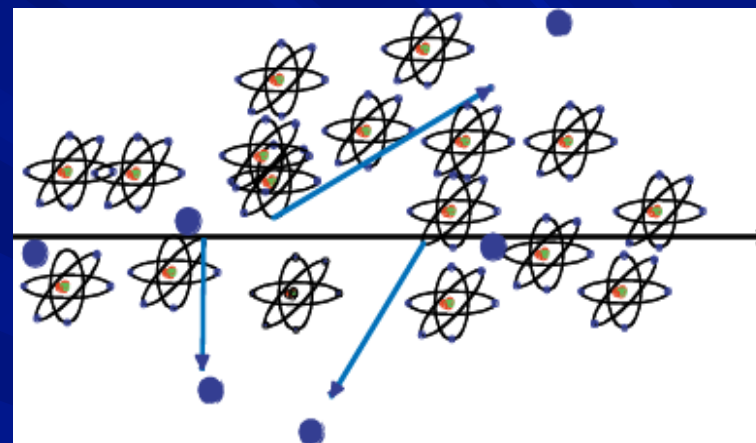
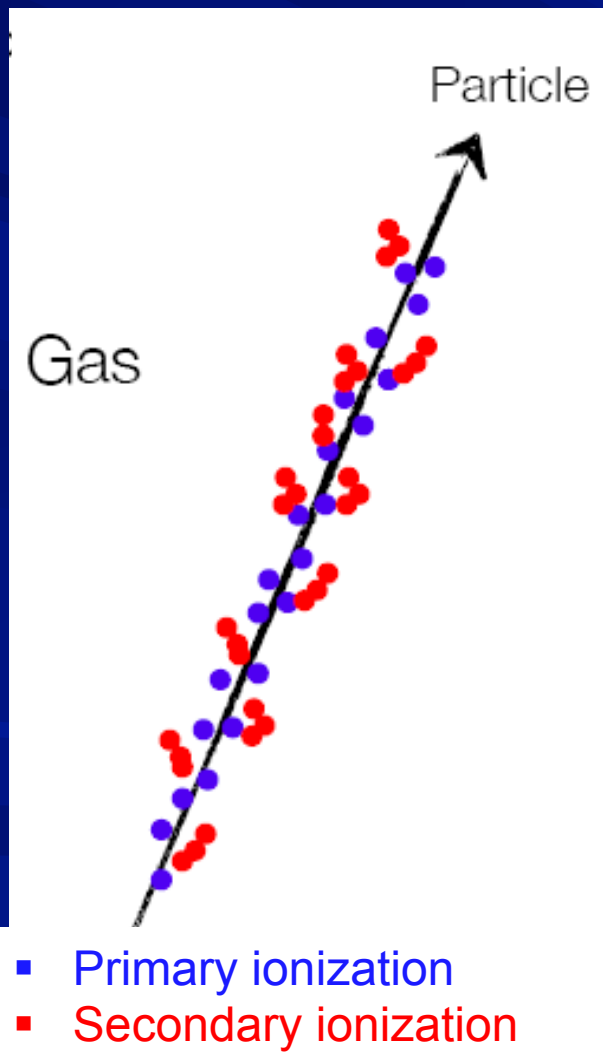
$$\rho = \frac{p_T}{q|B|} = \frac{\gamma m_0 \beta c}{q|B|}$$

- By measuring the radius of curvature we can determine the momentum of a particle
- If we can measure also  $\beta$  independently we can determine the particle mass.



# Signal creation

- Charged particle traversing matter leave excited atoms, electron-ion pairs (gases) and electrons-hole pairs (solids)



- Excitation: The photons emitted by the excited atoms in transparent materials can be detected with photon detectors
- Ionization: By applying an electric field in the detector volume, the ionization electrons and ions can be collected on electrodes and readout

# Scintillators

- $dE/dx$  converted into visible light and then it is detected via photo-sensor (photomultipliers, SiPM,....)
- Main features
  - Sensitivity to energy
  - Fast time response
  - Pulse shape discrimination
- Requirements:
  - High efficiency for conversion of exciting energy to fluorescent radiation
  - Transparency to its fluorescent radiation to allow transmission of light
  - Emission of light in a spectral range detectable for photosensors
  - Short decay time to allow fast response



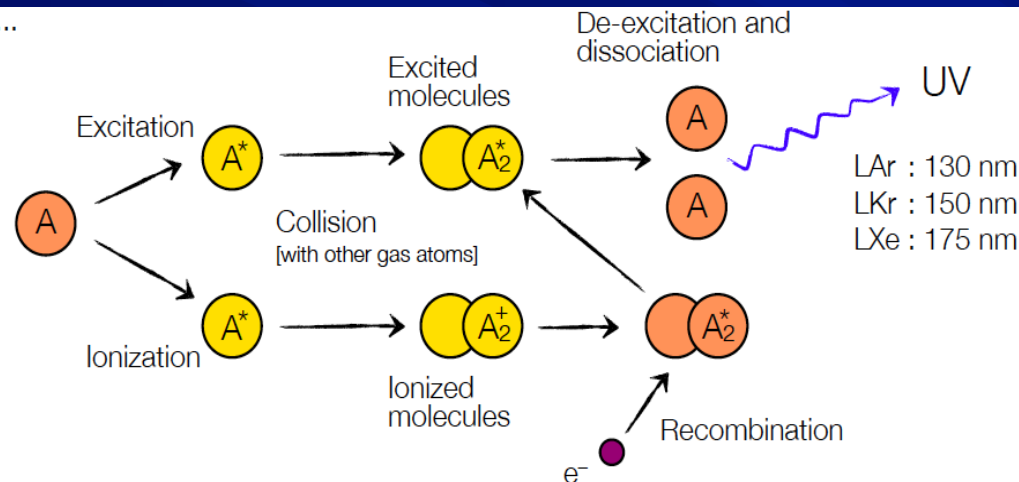
Plastic Scintillator BC412



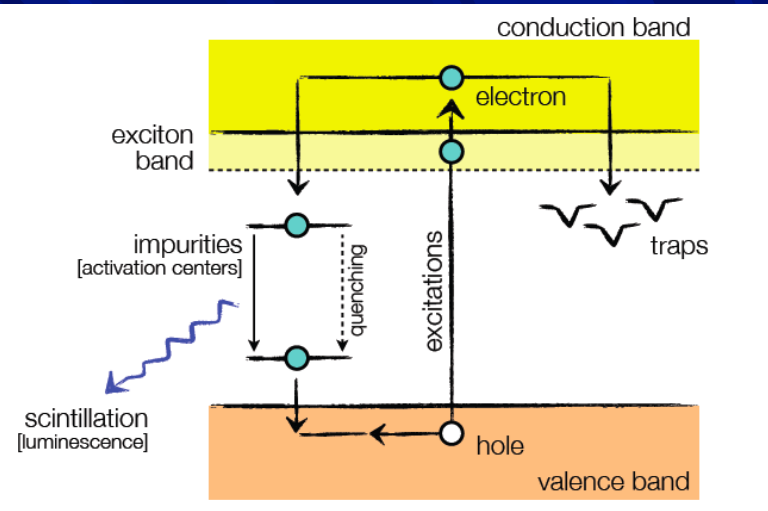


# Scintillators

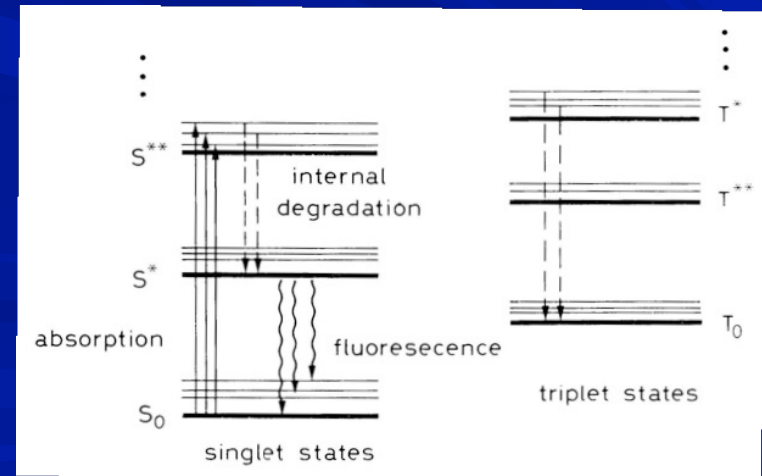
- Inorganic (Sodium iodide (NaI), Cesium iodide (CsI),...)



- Organic (aromatic hydrocarbon compounds which contain benzene ring structures such as polymer scintillators, polystyrene, anthracene...)
  - Molecule structure generates energy levels with transition  $\lambda=360-500$  nm

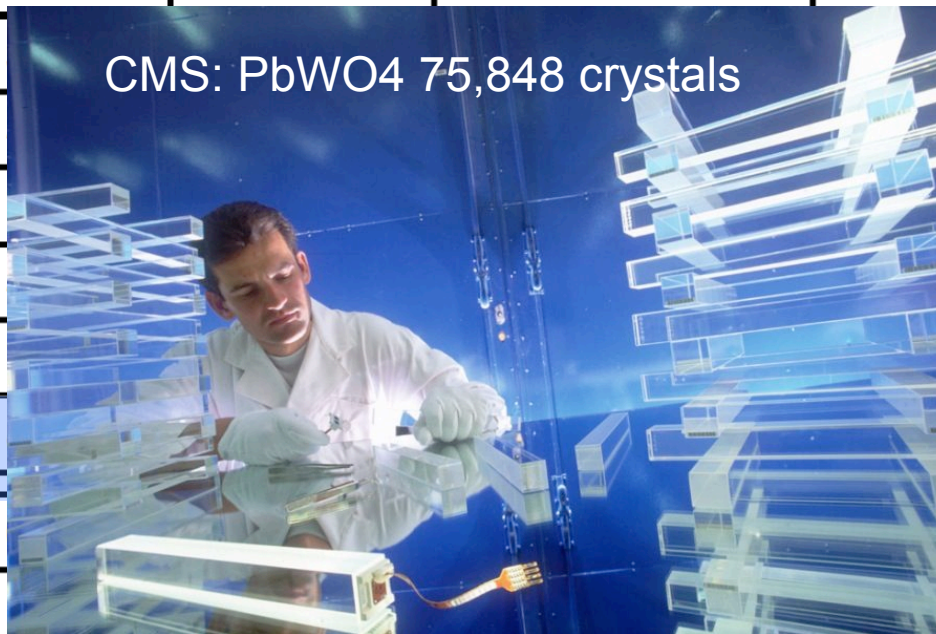


- Noble gasses (Liquid Argon, Liquid Xenon...)



# Inorganic scintillators

Scintillator material	Density [g/cm <sup>3</sup> ]	Refractive Index	Wavelength [nm] for max. emission	Decay time constant [μs]	Photons/MeV
Nal	3.7	1.78	303	0.06	$8 \cdot 10^4$
Nal(Tl)				0.25	$4 \cdot 10^4$
CsI(Tl)				0.10	$1.1 \cdot 10^4$
Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub>				0.30	$2.8 \cdot 10^3$
CsF				0.003	$2 \cdot 10^3$
LSO				0.04	$1.4 \cdot 10^4$
PbWO <sub>4</sub>				0.006	$2 \cdot 10^2$
LHe				1/1.6	$2 \cdot 10^2$
LAr				5/0.86	$4 \cdot 10^4$
LXe	3.1	1.60 <sup>*</sup>	150	0.003/0.02	$4 \cdot 10^4$



CMS: PbWO<sub>4</sub> 75,848 crystals

\* at 170 nm



# Organic Scintillators

Scintillator material	Density [g/cm <sup>3</sup> ]	Refractive Index	Wavelength [nm] for max. emission	Decay time constant [ns]	Photons/MeV
Naphtalene	1.15	1.58	348	11	$4 \cdot 10^3$
Antracene	1.25	1.59	448	30	$4 \cdot 10^4$
p-Terphenyl	1.23	1.65	391	6-12	$1.2 \cdot 10^4$
NE102*	1.03	1.58	425	2.5	$2.5 \cdot 10^4$
NE104*	1.03	1.58	405	1.8	$2.4 \cdot 10^4$
NE110*	1.03	1.58	437	3.3	$2.4 \cdot 10^4$
NE111*	1.03	1.58	370	1.7	$2.3 \cdot 10^4$
BC400**	1.03	1.58	423	2.4	$2.5 \cdot 10^2$
BC428**	1.03	1.58	480	12.5	$2.2 \cdot 10^4$
BC443**	1.05	1.58	425	2.2	$2.4 \cdot 10^4$

\* Nuclear Enterprises, U.K.  
 \*\* Bicron Corporation, USA

# Scintillator comparison

## ■ Inorganic Scintillators

- Advantages
  - high light yield [typical;  $\epsilon_{sc} \approx 0.13$ ]
  - high density [e.g.  $PbWO_4$ : 8.3 g/cm<sup>3</sup>]
  - good energy resolution (→ Calorimeters)
- Disadvantages complicated crystal growth
- large temperature dependence

Light yield  $\epsilon_{sc} \equiv$  fraction of energy loss going into photons

EXPENSIVE

## ■ Organic Scintillators

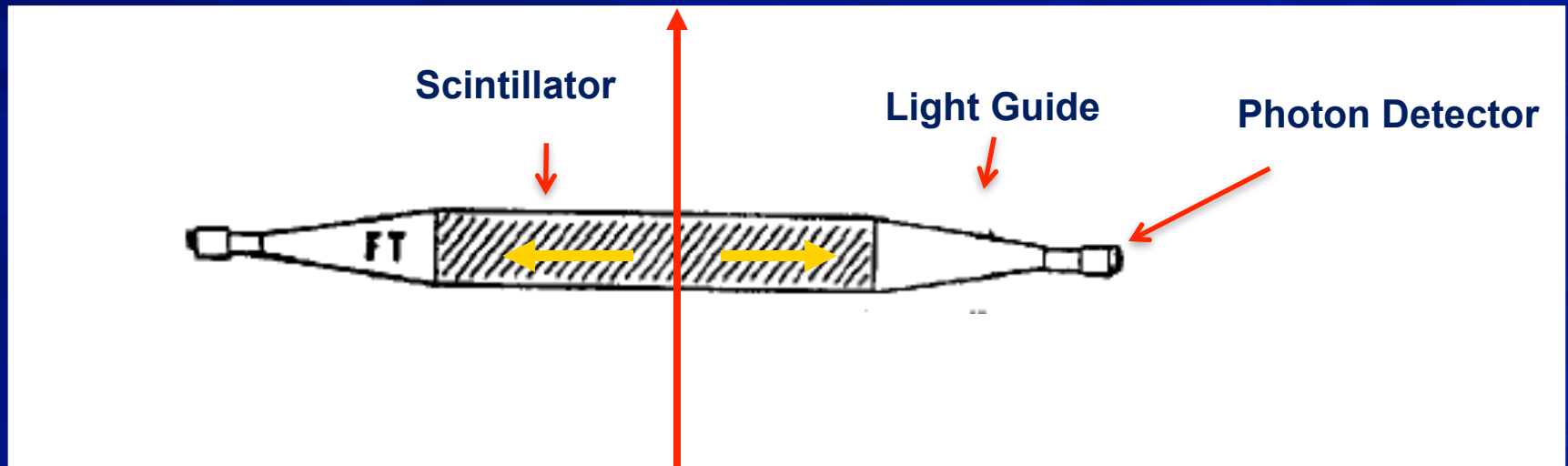
- Advantages
  - very fast
  - easily shaped
  - small temperature dependence
  - pulse shape discrimination possible
- Disadvantages
  - lower light yield [typical;  $\epsilon_{sc} \approx 0.03$ ]
  - radiation damage

CHEAP



# Scintillators

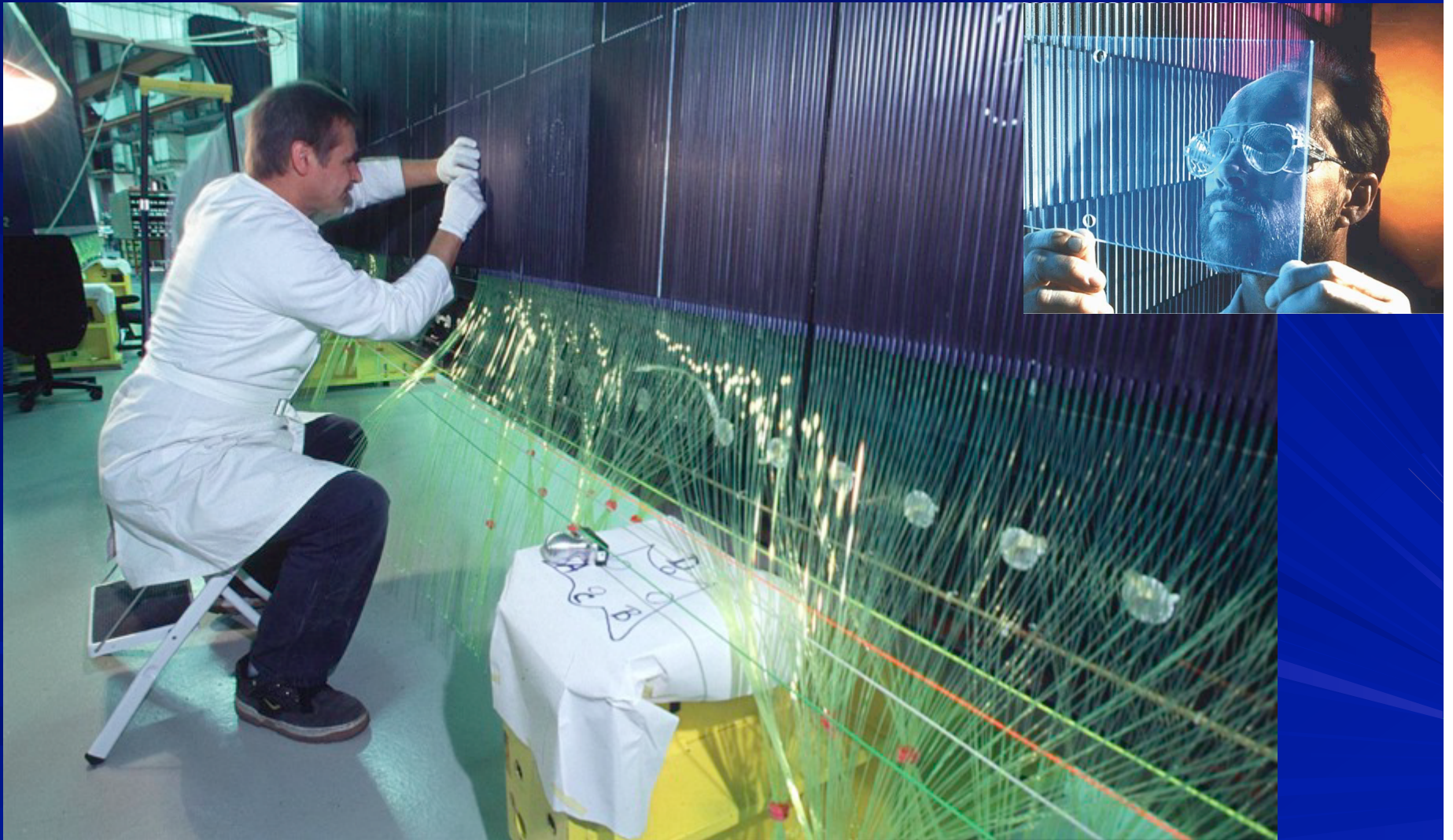
- Photons are being reflected towards the ends of the scintillator.
- A light guide brings the photons to the Photomultipliers where the photons are converted to an electrical signal.



- By segmentation one can arrive at spatial resolution.
- Because of the excellent timing properties ( $<1\text{ns}$ ) the arrival time, or time of flight, can be measured very accurately  $\rightarrow$  Trigger, Time of Flight.

# Scintillator

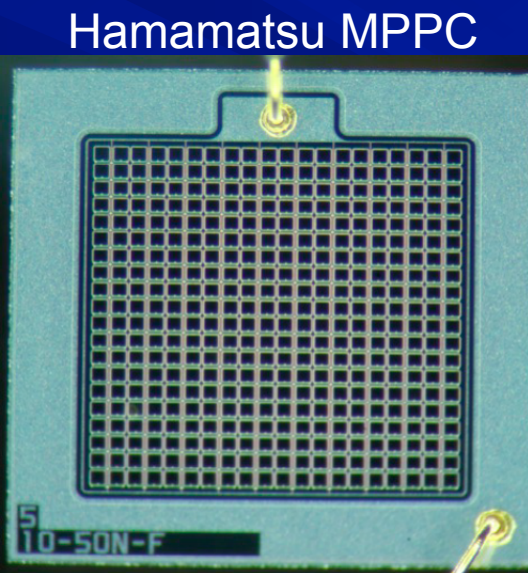
ATLAS Tile Calorimeter



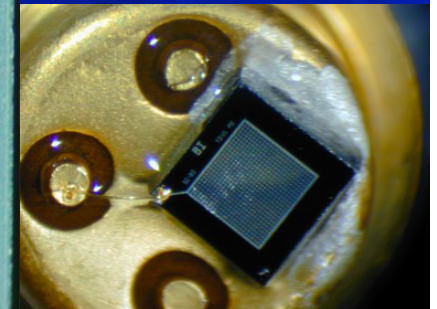


# Photo-detectors

- Convert light into an electronic signal by using the photo-electric effect to convert photons into photo-electrons (p.e.)
- Requirement :
  - High Photon Detection Efficiency (PDE) or
  - Quantum Efficiency;  $Q.E. = N_{p.e.}/N_{photons}$
- Photomultipliers
- SiPM

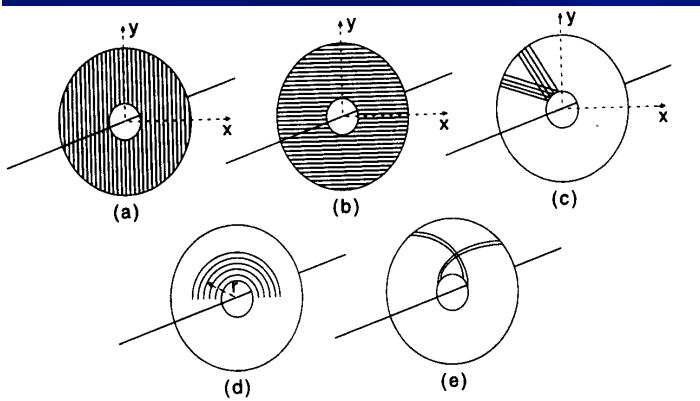


One of the first  
SiPM  
Pulsar, Moscow

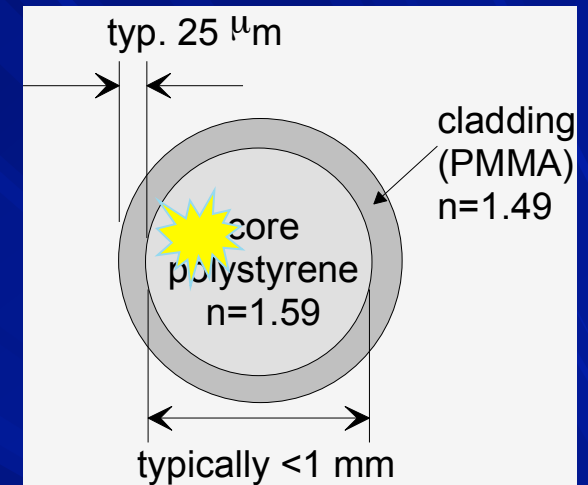
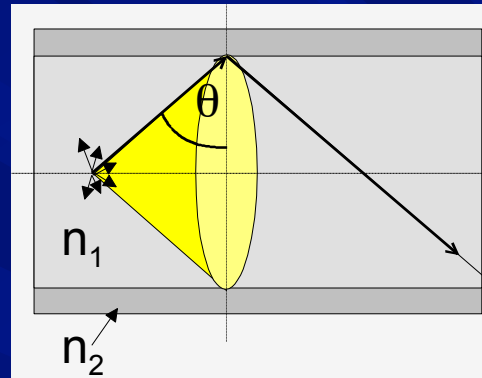


# Fiber Tracking

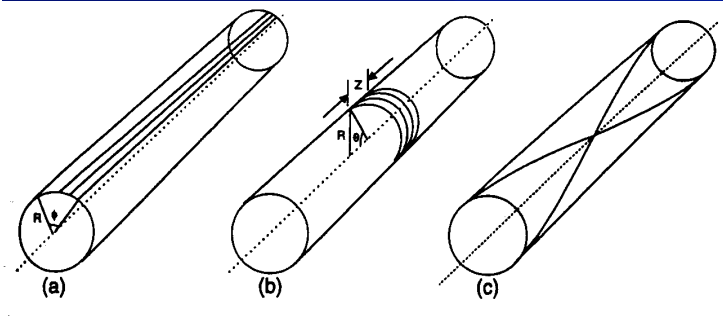
## Planar geometries (end cap)



## Light transport by total internal reflection



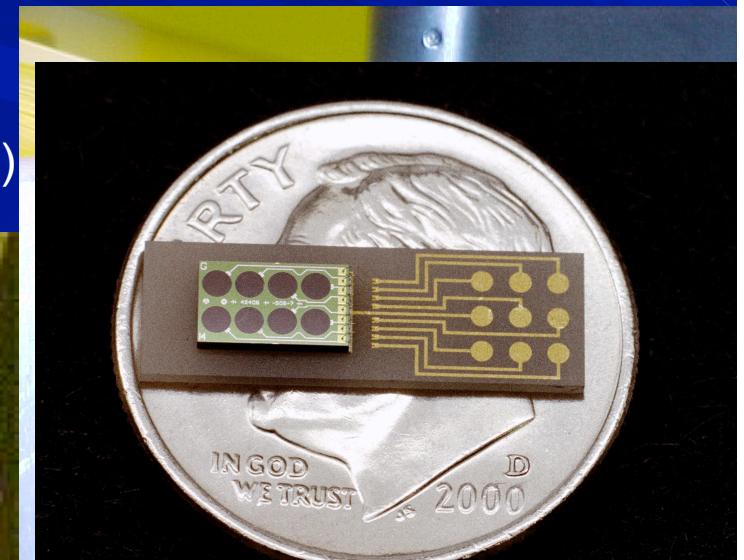
## Circular geometries (barrel)



- High geometrical flexibility
- Fine granularity
- Low mass
- Fast response (ns)

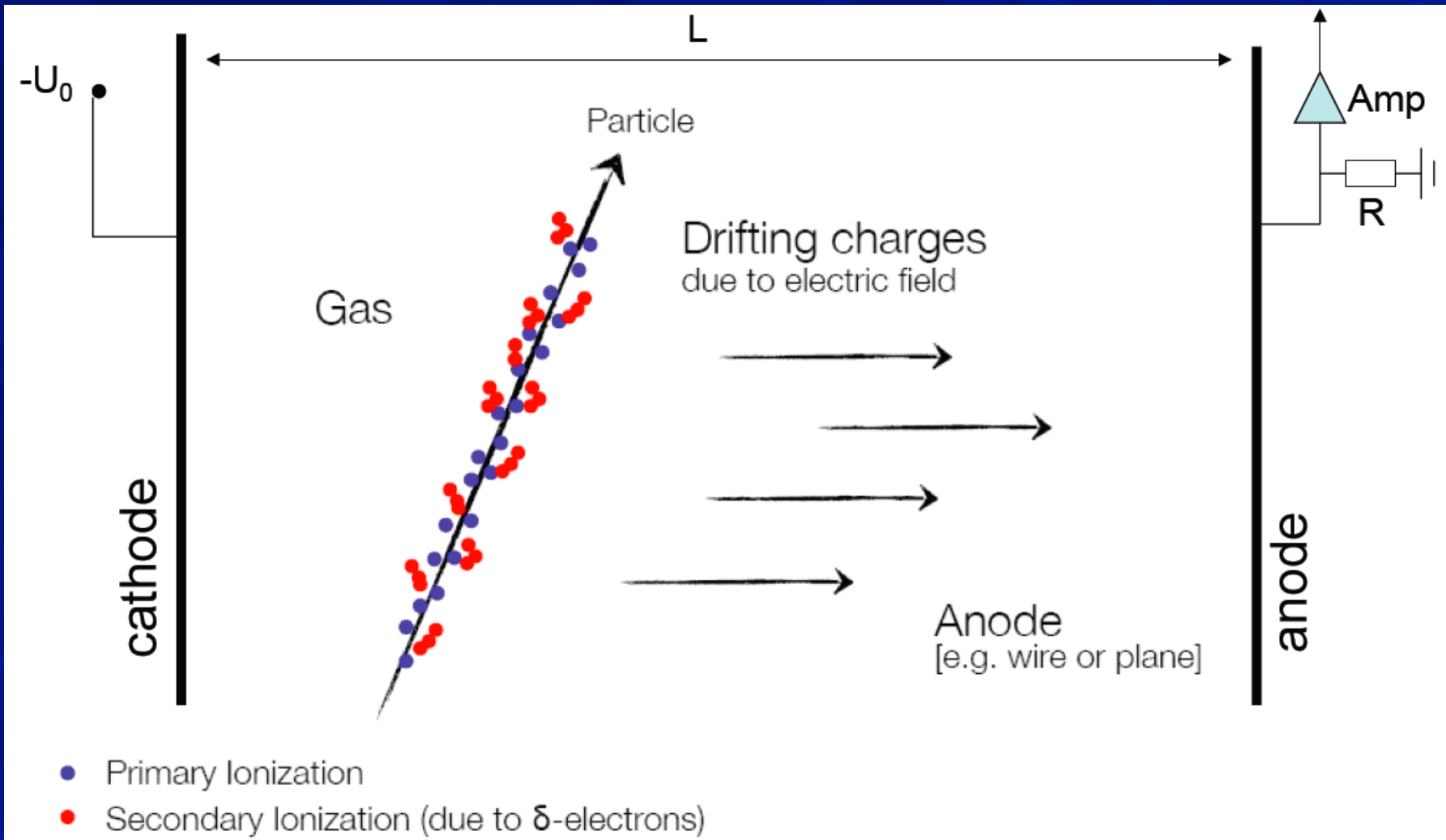
(R.C. Ruchti, Annu. Rev. Nucl. Sci. 1996, 46,281)

## D0 fiber tracker





# Gas Detectors: primary

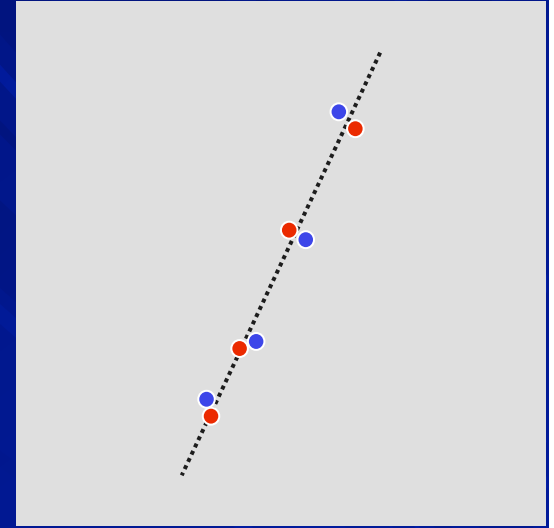


# Primary and secondary ionization

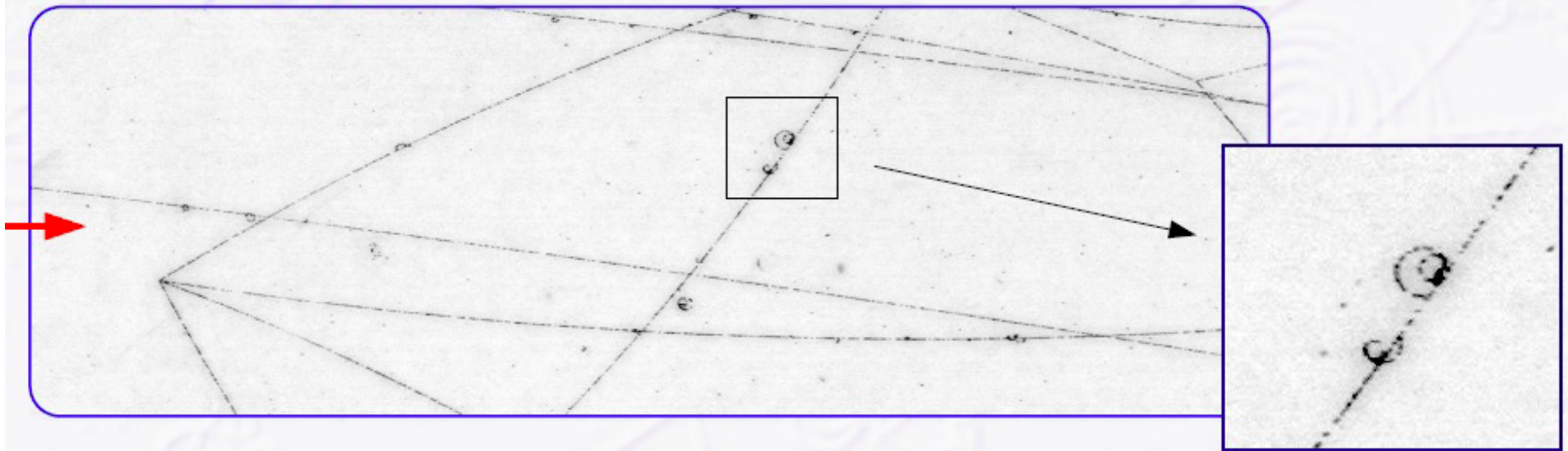
- Coulomb interactions between E field of the particle and of the molecules of the medium produce electron-ion pairs.

- Minimum ionizing particles in argon NTP
  - $\langle n_p \rangle: 25 \text{ cm}^{-1}$

- Primary electrons can ionize the medium producing local e-ion clusters. Electron can have energy to



tracks in CERN 2m bubble chamber





# Most common gases

Gas	$\rho$ (g/cm <sup>3</sup> ) (STP)	$I_0$ (eV)	$W_i$ (eV)	$dE/dx$ (MeVg <sup>-1</sup> cm <sup>2</sup> )	$n_p$ (cm <sup>-1</sup> )	$n_t$ (cm <sup>-1</sup> )
H <sub>2</sub>	$8.38 \cdot 10^{-5}$	15.4	37	4.03	5.2	9.2
He	$1.66 \cdot 10^{-4}$	24.6	41	1.94	5.9	7.8
N <sub>2</sub>	$1.17 \cdot 10^{-3}$	15.5	35	1.68	(10)	56
Ne	$8.39 \cdot 10^{-4}$	21.6	36	1.68	12	39
Ar	$1.66 \cdot 10^{-3}$	15.8	26	1.47	29.4	94
Kr	$3.49 \cdot 10^{-3}$	14.0	24	1.32	(22)	192
Xe	$5.49 \cdot 10^{-3}$	12.1	22	1.23	44	307
CO <sub>2</sub>	$1.86 \cdot 10^{-3}$	13.7	33	1.62	(34)	91
CH <sub>4</sub>	$6.70 \cdot 10^{-4}$	13.1	28	2.21	16	53
C <sub>4</sub> H <sub>10</sub>	$2.42 \cdot 10^{-3}$	10.8	23	1.86	(46)	195

Quelle: K. Kleinknecht, *Detektoren für Teilchenstrahlung*, B.G. Teubner, 1992

# Ionization statistics

- Multiple ionizing collisions follow Poisson's statistics:

$$\langle n_p \rangle = \frac{L}{\lambda}$$

$$\lambda = \frac{1}{n_e \sigma_I}$$

$$P_{n_p}^{\langle n_p \rangle} = \frac{\langle n_p \rangle^{n_p} e^{-\langle n_p \rangle}}{n_p!}$$

$\sigma_I$ : Ionization x-section  
 $n_e$ : Electron density  
 $L$ : Thickness

Typical values of the mean free path  $\lambda$

- He 0.25 cm
- Air 0.052 cm
- Xe 0.023 cm

- Efficiency:

$$\varepsilon = 1 - P_0^{\langle n_p \rangle} = 1 - e^{-\langle n_p \rangle}$$

L(mm)	$\varepsilon(\%)$ for $\langle n_p \rangle = 2.5/\text{mm}$
1	91.8
2	99.3

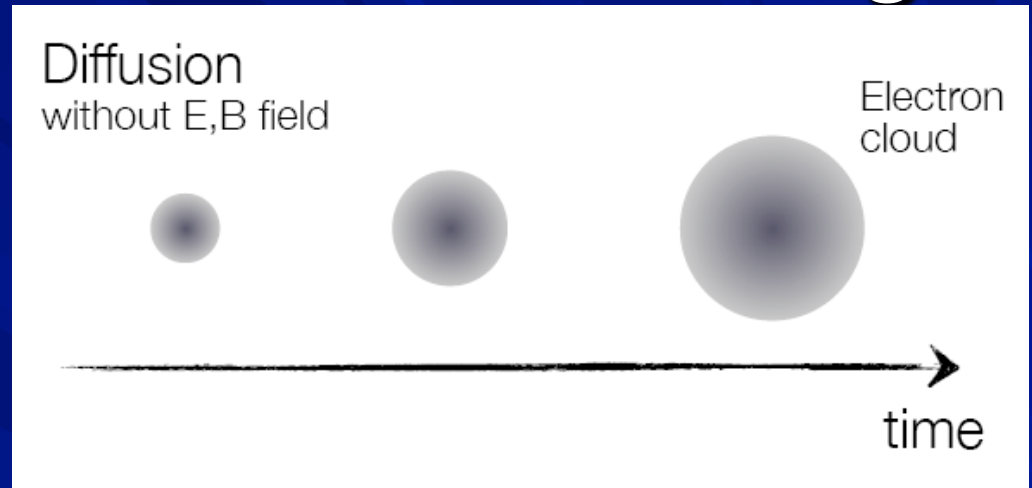
- Other important parameters are:

- Recombination and electron attachment due to Electro-negative gases which bind electrons; e.g.:  $O_2$ , Freon,  $Cl_2$ ,  $SF_6$  ...  $\rightarrow$  influences detection efficiency
- Diffusion  $\rightarrow$  Influences the spatial resolution
- Mobility of charges  $\rightarrow$  Influences the timing behavior of gas detectors
- Avalanche process via impact ionization:  $\rightarrow$  Important for the gain factor of the gas detector ...

# Transport of electrons/ions in a gas

- Diffusion is evaluated using the classical kinetic theory of gases

$$\frac{dN}{dx} = \frac{N_0}{\sqrt{4\pi Dt}} \exp\left(-\frac{x^2}{4Dt}\right)$$



- e<sup>-</sup>/ions are distributed with a Gaussian spread  $\sigma(r)$  after a diffusion time  $t$

$$\sigma(r) = \sqrt{6Dt}$$

The diffusion coefficient  $D$ , depends on the pressure  $P$  and the temperature  $T$

$$D = \frac{1}{3} v \lambda = \frac{2}{3\sqrt{\pi}} \frac{1}{P\sigma_0} \sqrt{\frac{(kT)^3}{m}}$$

- The Mean-free path of electrons/ions in the path
- The mean velocity according to Maxwell distribution
- $m$  is the mass of the particle

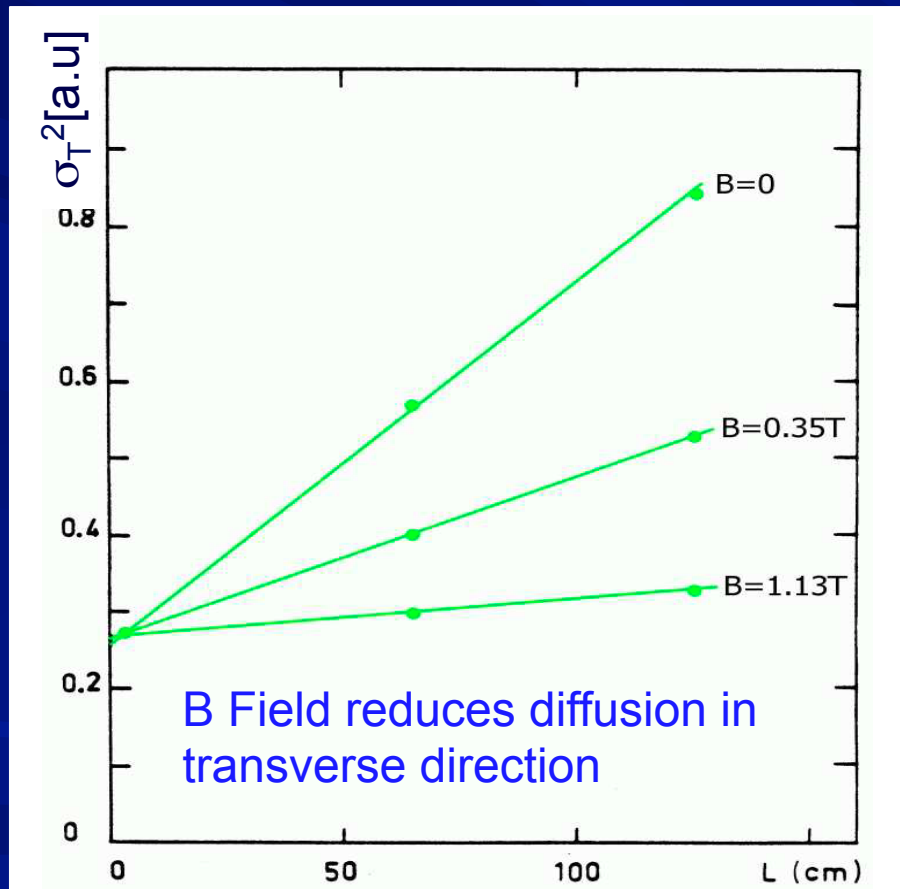
$$\lambda = \frac{1}{\sqrt{2}} \frac{kT}{\sigma_0 P}$$

$$v = \sqrt{\frac{8kT}{\pi m}}$$

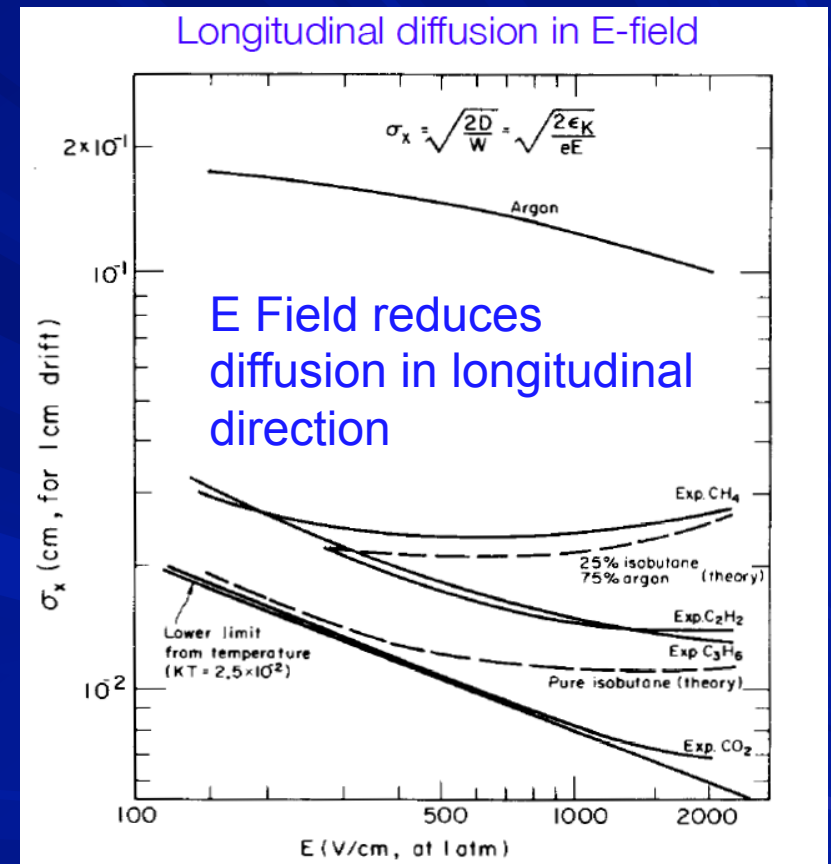


# Drift and diffusion in E and B fields

- Transverse diffusion as function of drift length for different B fields



- Longitudinal diffusion as function of E field



Transport equation is usually solved numerically using programs like Magboltz and Garfield

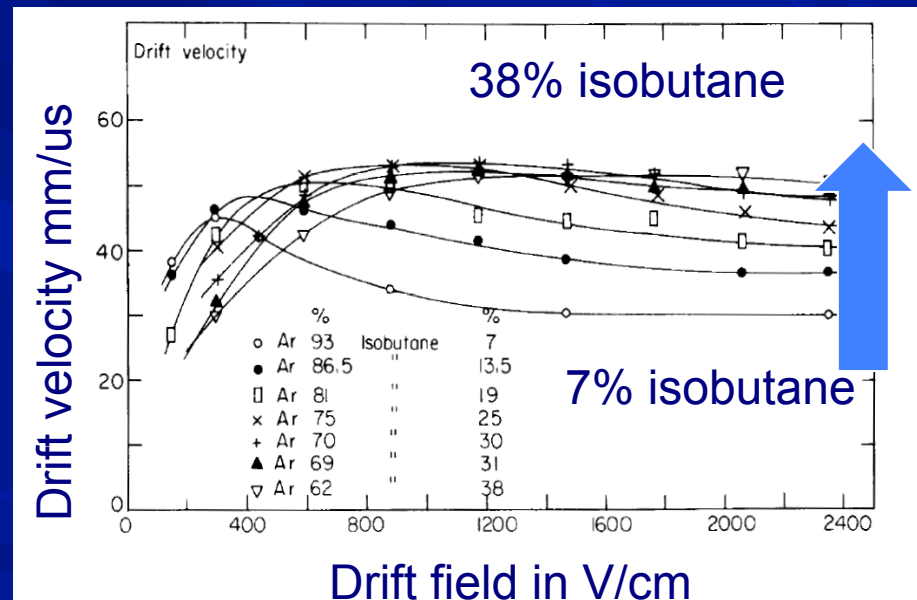
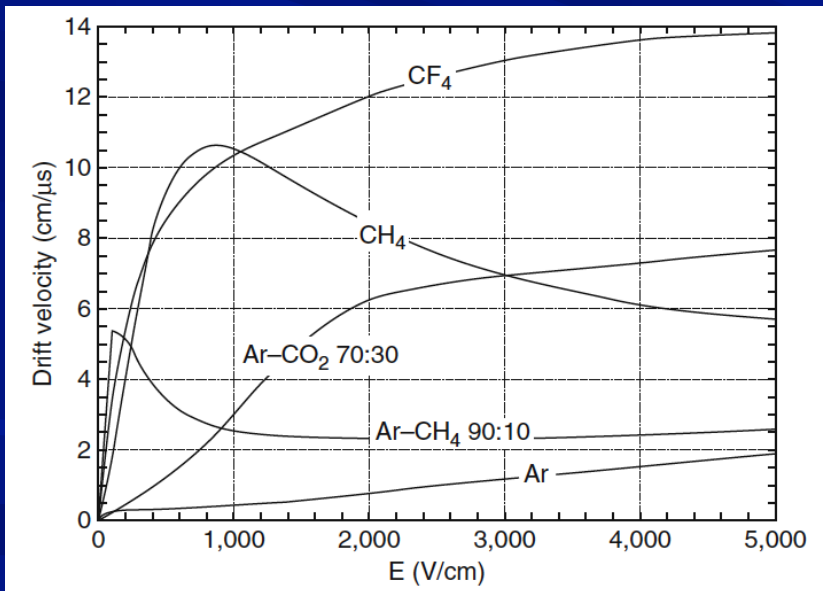
# Drift and mobility

- In an external E-field electrons/ions obtain velocity  $v_D$  in addition to thermal motion; on average electrons/ions move along field lines of electric field E

$$\vec{v}_D = \mu_{\pm} |\vec{E}|$$

Typical values of  $v_D$

- $E \sim 1 \text{ kV / cm}$
- $v_d \approx \text{cm/ms}$  for ions
- $v_d \approx \text{cm}/\mu\text{s}$  for e-



- Since the collection time is inversely proportional to the drift velocity, diffusion effects are reduced in gases such as CF<sub>4</sub> that have high drift

# Avalanche Multiplication

- The primary ionization signal is very small in a gas layer: in 1 cm of Ar/CO<sub>2</sub> (70:30) at NTP only ~100 electron-ion pairs are created → use an “internal gas amplification” mechanism to increase signal
- Large E fields → large electron kinetic energy → avalanche formation

$$- dn = n \alpha dx$$

$\alpha$ =Townsend Coefficient

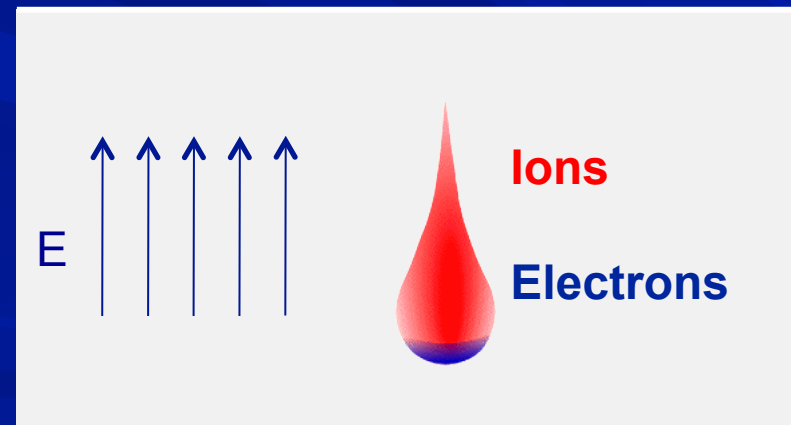
$$- n(x) = n_0 e^{\alpha x}$$

$n(x)$ =electrons at location  $x$

- Gain or Amplification is:

$$G = \frac{n}{n_0} = e^{\alpha x}$$

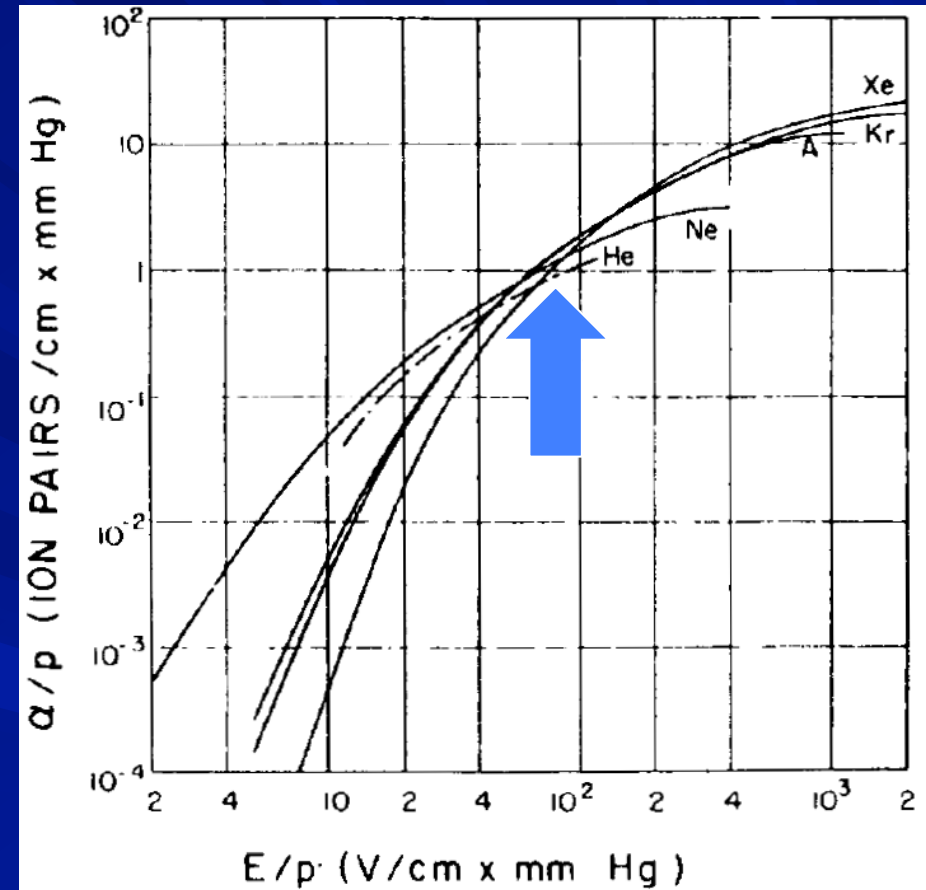
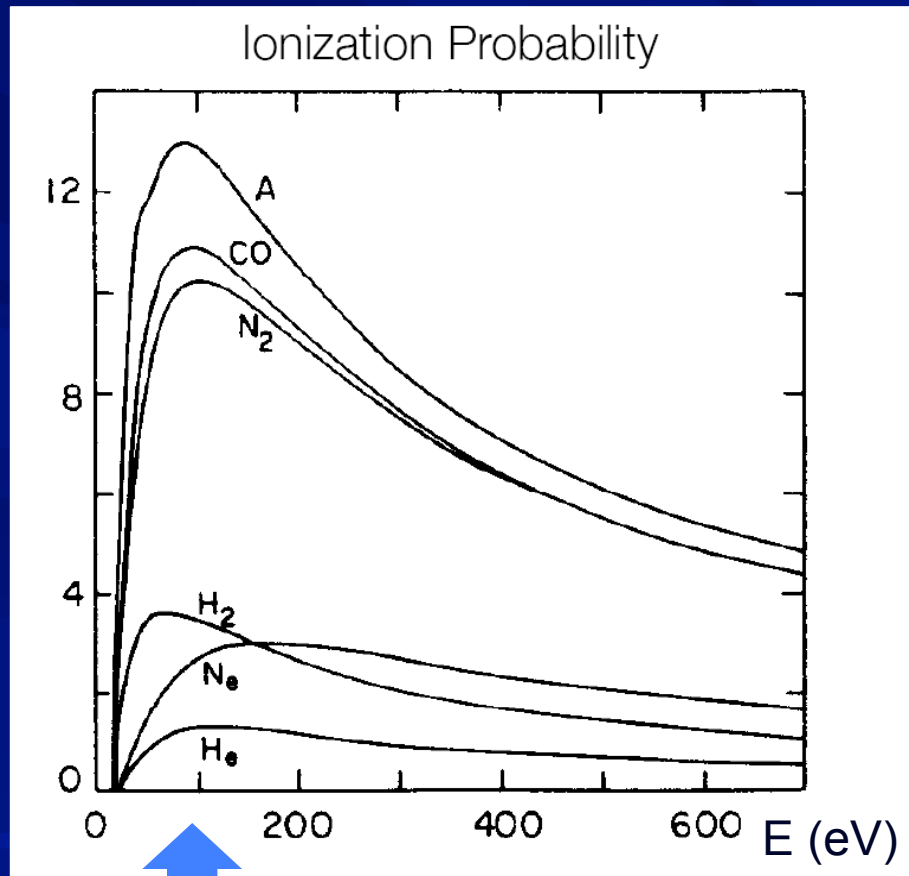
- Raether's limit  $G \approx 10^8$ , since after that sparking can occur



Drop-like shape of an avalanche



# Avalanche multiplication

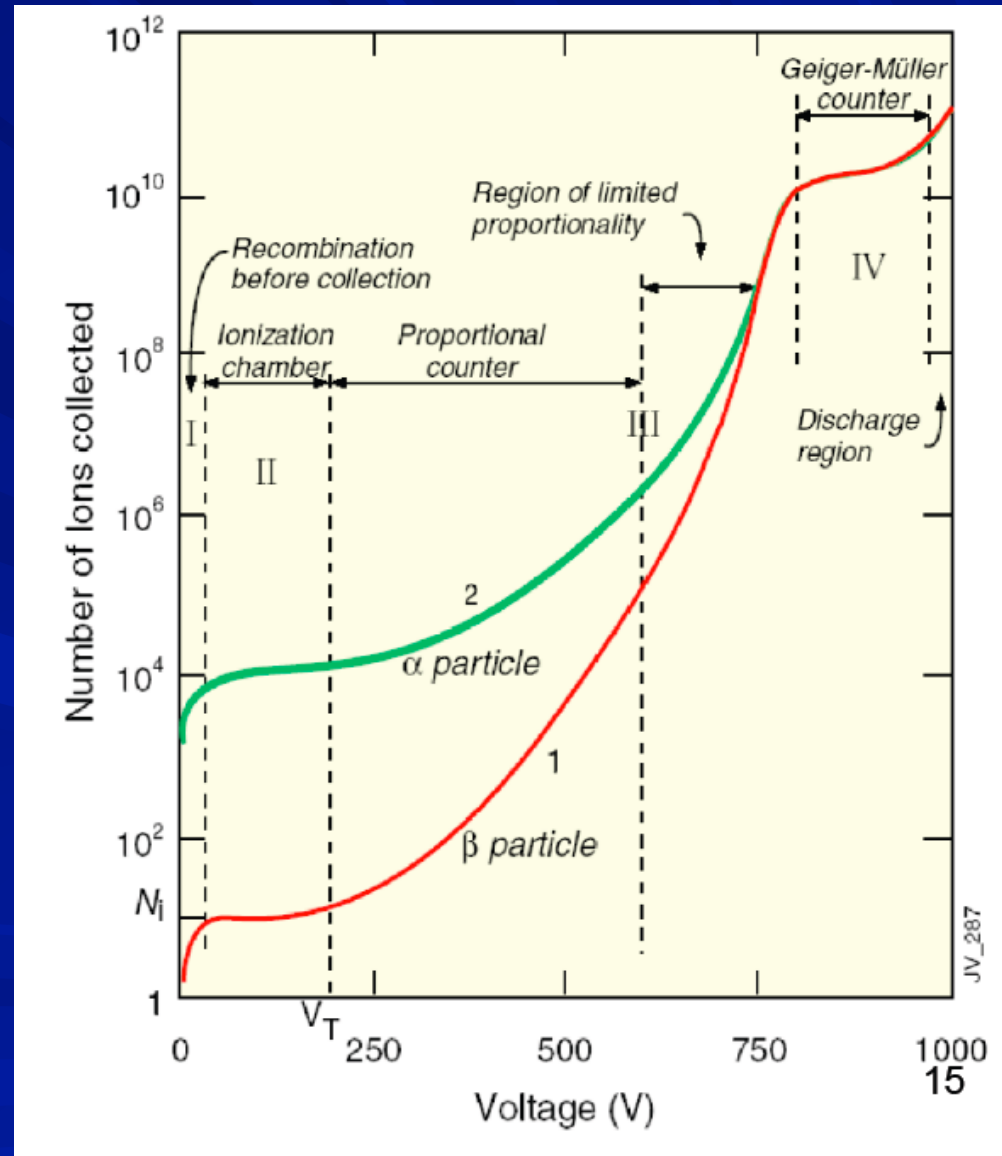


- Need an energy of 75-100 eV for High ionization probability (and need to gain it in a few  $\mu\text{m}$ )

- $E=75 \text{ kV/cm}$  to reach  $\alpha=1$

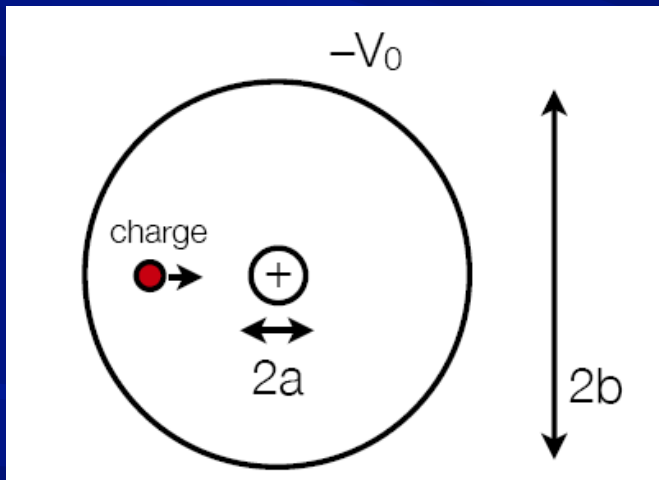
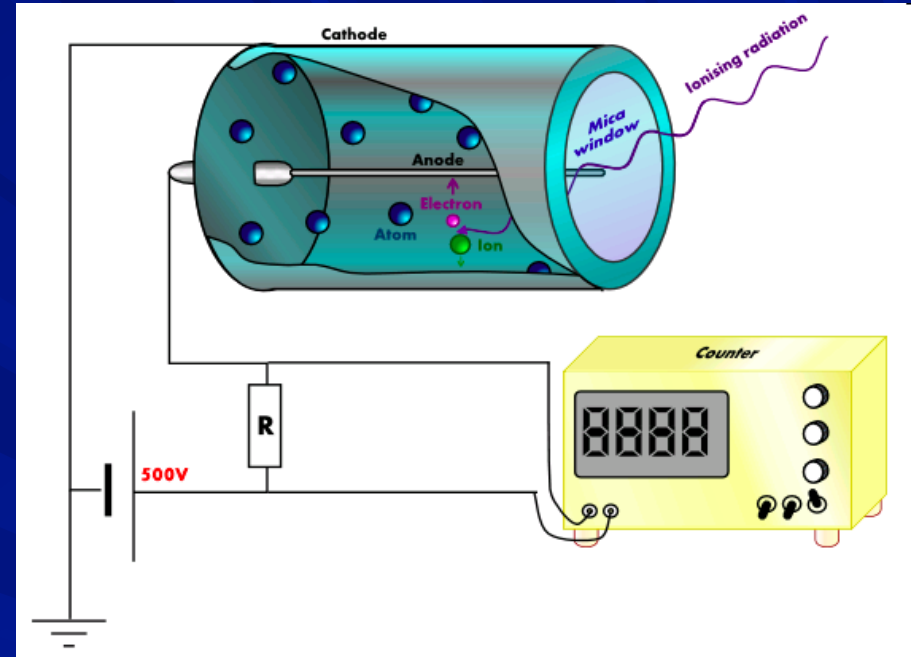
# Gas amplification factor

- **Ionization mode:** full charge collection; no amplification;  $G=1$
- **Proportional mode:** multiplication; signal proportional to original ionization  $\Rightarrow$  measurement of  $dE/dx$ . Secondary avalanches needs quenching;  $G \approx 10^4-10^5$
- **Limited Proportional (Saturated, Streamer mode):** strong photo-emission; Require strong quenchers. High gain  $10^{10} \Rightarrow$  large signal, simple electronics
- **Geiger mode:** Massive photo emission. Full length of anode affected. Discharge stopped by HV cut



# Proportional counter

- Cylindrical proportional counter:
  - Single anode wire in a cylindrical cathode
  - $E \sim 1/r$ : weak field far from the wire
  - electrons/ions drift in the volume
  - multiplication occurs only near the anode



$$E = \frac{V}{r \ln(a/b)}$$

- Close to wire E-field very large
- Use thin wire

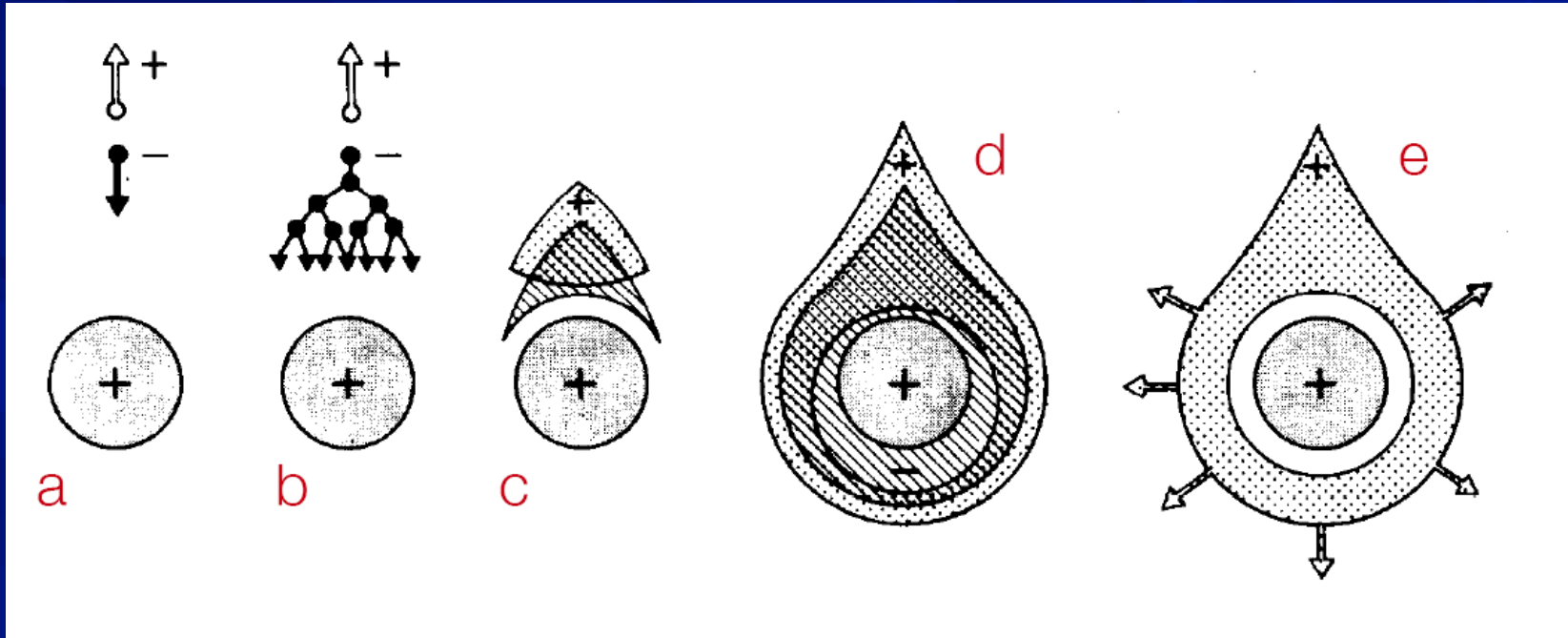
- The kinetic energy of the electrons becomes very large near the wire and can produce secondary ionization

$$\Delta T_{kin} = e\Delta U$$



# Avalanche development

- Time development of avalanche near the wire of a proportional counter

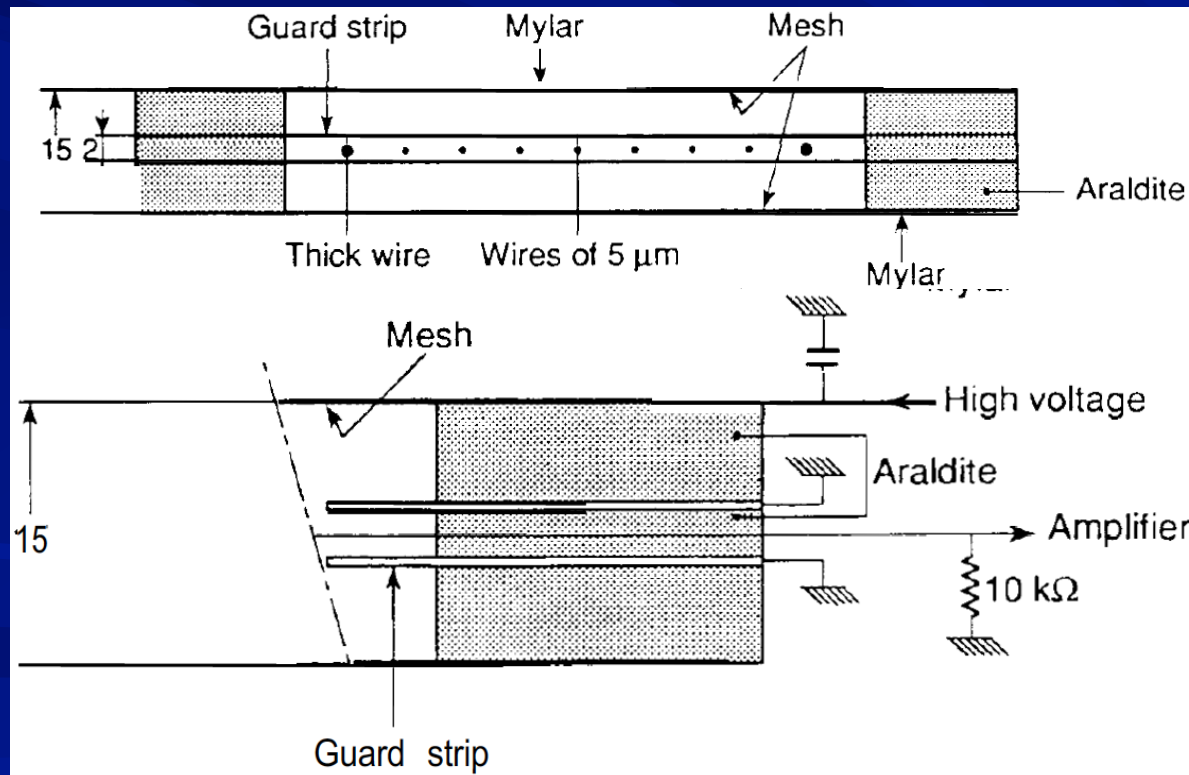
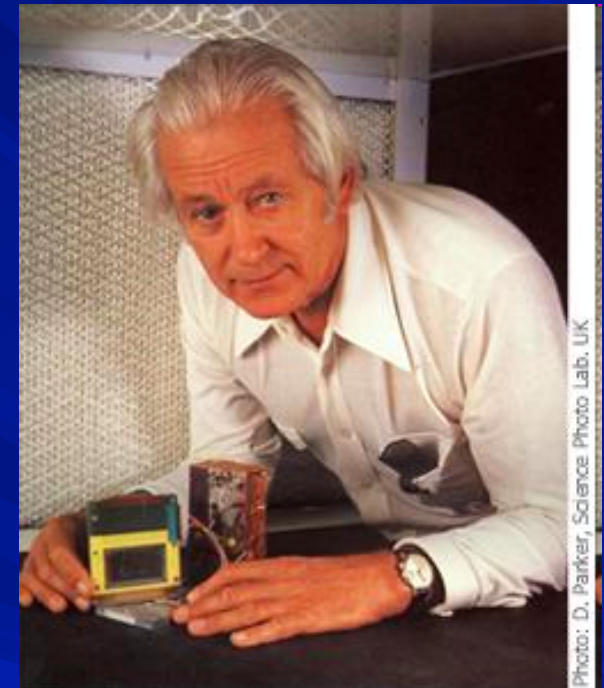


- single primary electron proceeds towards the wire anode,
- In the region of increasingly high field avalanche multiplication starts
- electrons and ions are subject to lateral diffusion,
- a drop-like avalanche develops which surrounds the anode wire,
- the electrons are quickly collected ( $\sim 1$  ns) while the ions begin drifting towards the cathode generating the signal at the electrodes

# Multiwire proportional chambers

- A proportional counter does not provide the position of the incident particle
- Charpak developed of multi-wire proportional chamber

G. Charpak Nobel price ('92)

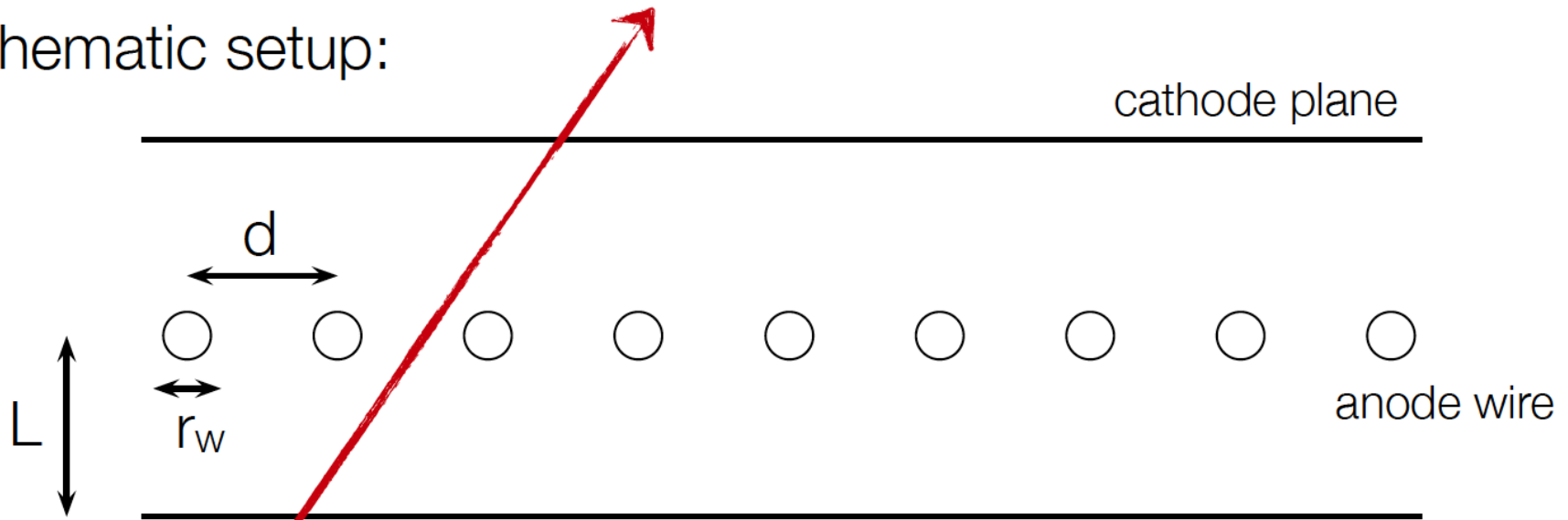


Construction details of the original design of Charpak's multi-wire chambers (from Nobel lecture)

Sense wire =  $2\mu$  diameter  
 $d = 2$  mm

# Multi-Wire Proportional Chamber

Schematic setup:



Parameters:

$d = 2 - 4 \text{ mm}$   
 $r_w = 20 - 25 \text{ }\mu\text{m}$   
 $L = 3 - 6 \text{ mm}$   
 $U_0 = \text{several kV}$

Total area:  $O(\text{m}^2)$

Features:

Tracking of charged particles  
Some PID capabilities via  $dE/dx$   
Large area coverage  
High rate capabilities

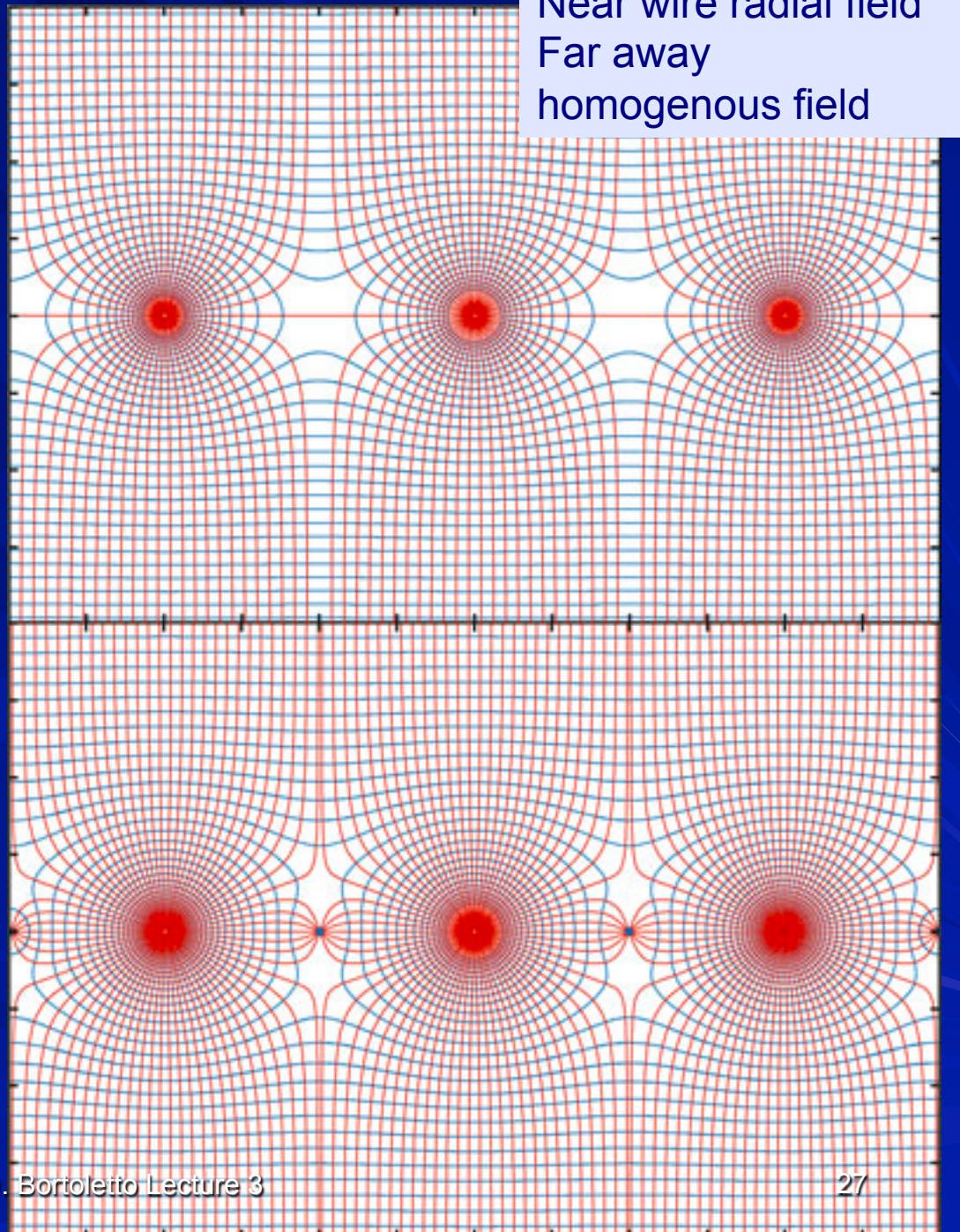
particle track



# Field distribution

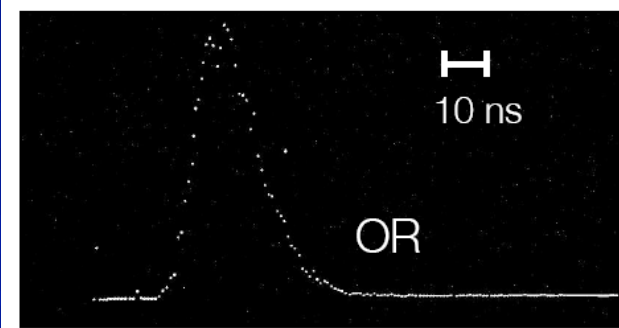
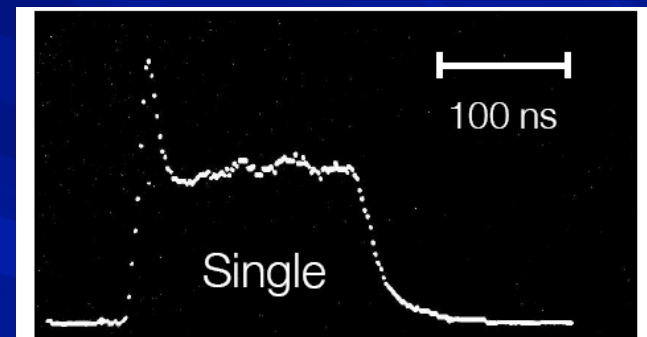
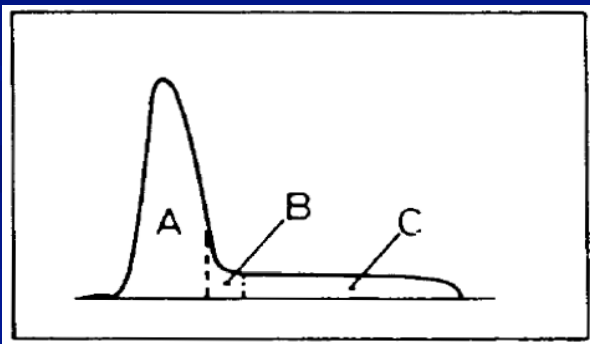
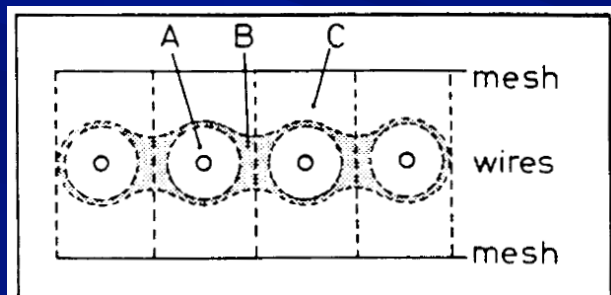
- MWPC: Operation is difficult at smaller wire spacings.
  - The electrostatic repulsion for thin ( $10\ \mu\text{m}$ ) anode wires causes mechanical instability above a critical wire length of less than 25 cm for 1-mm
- Drift chambers
  - a thicker wire at proper voltage between anodes (field wire) reduces the field at the middle point between anodes and improves charge collection
  - Linearity of the space-to-drift-time relation  $\rightarrow$  resulting in better spatial resolution

Near wire radial field  
Far away  
homogenous field



# MWPC performance

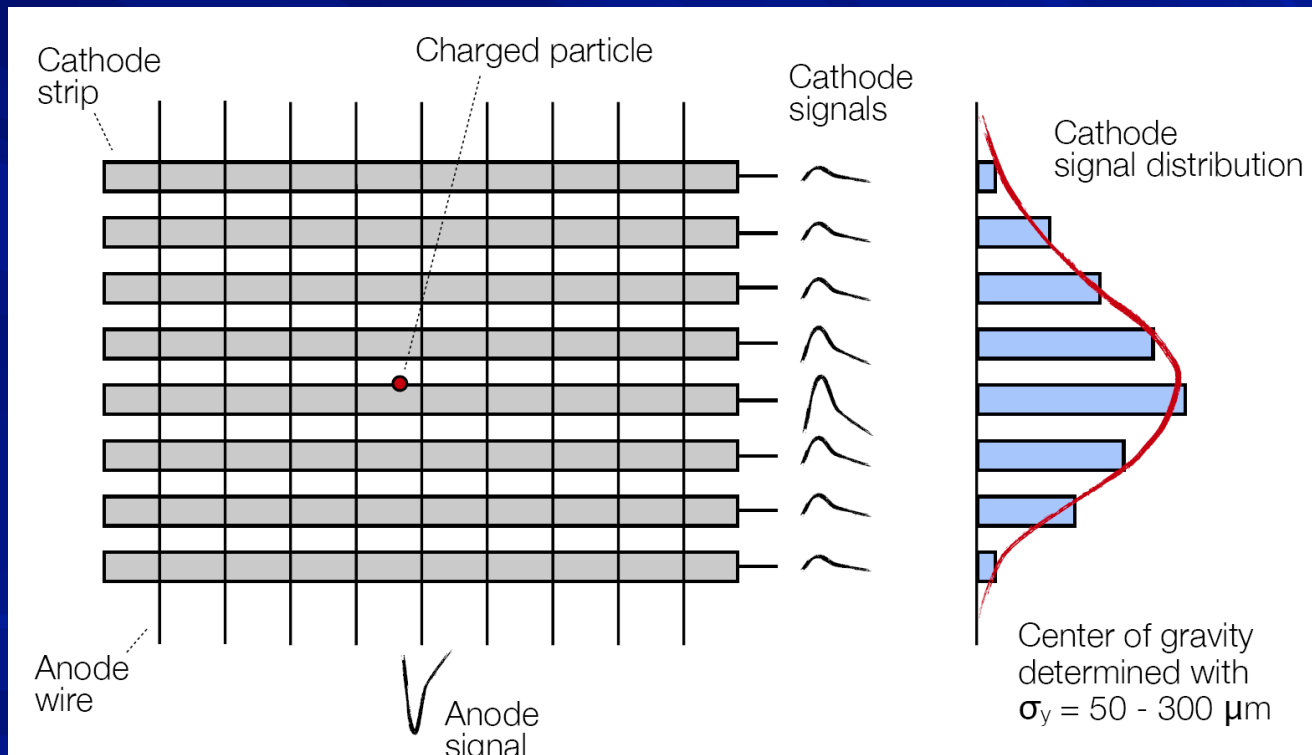
- Signal generation:
  - Electrons drift to closest wire. Gas amplification near wire → avalanche
  - Signal generation due to electrons and slow ions (mainly slow ions, see backup)
- Timing resolution:
  - Depends on location of particle
  - For fast response: OR of all channels ... [Typical:  $\sigma_t = 10$  ns]





# MWPC: space point resolution

- Space point resolution: Only information about closest wire  $\rightarrow \sigma_x = d/\sqrt{12}$  [ $d=2-4$  mm,  $\sigma_x \sim 0.6-1$ mm]
- Possible improvements: segmented cathode

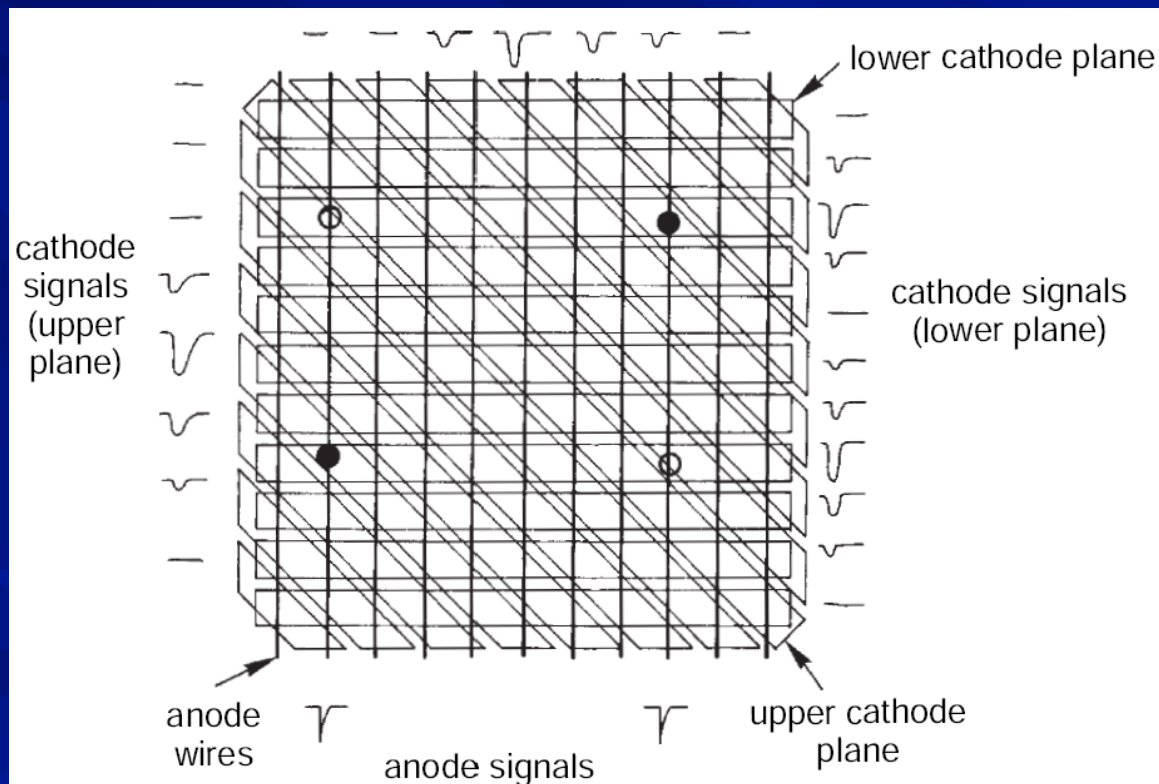


- 2-dim.: use 2 MWPCs with different orientation
- -3-dim.: several layers of such X-Y-MWPC combinations



# 2D MWPC

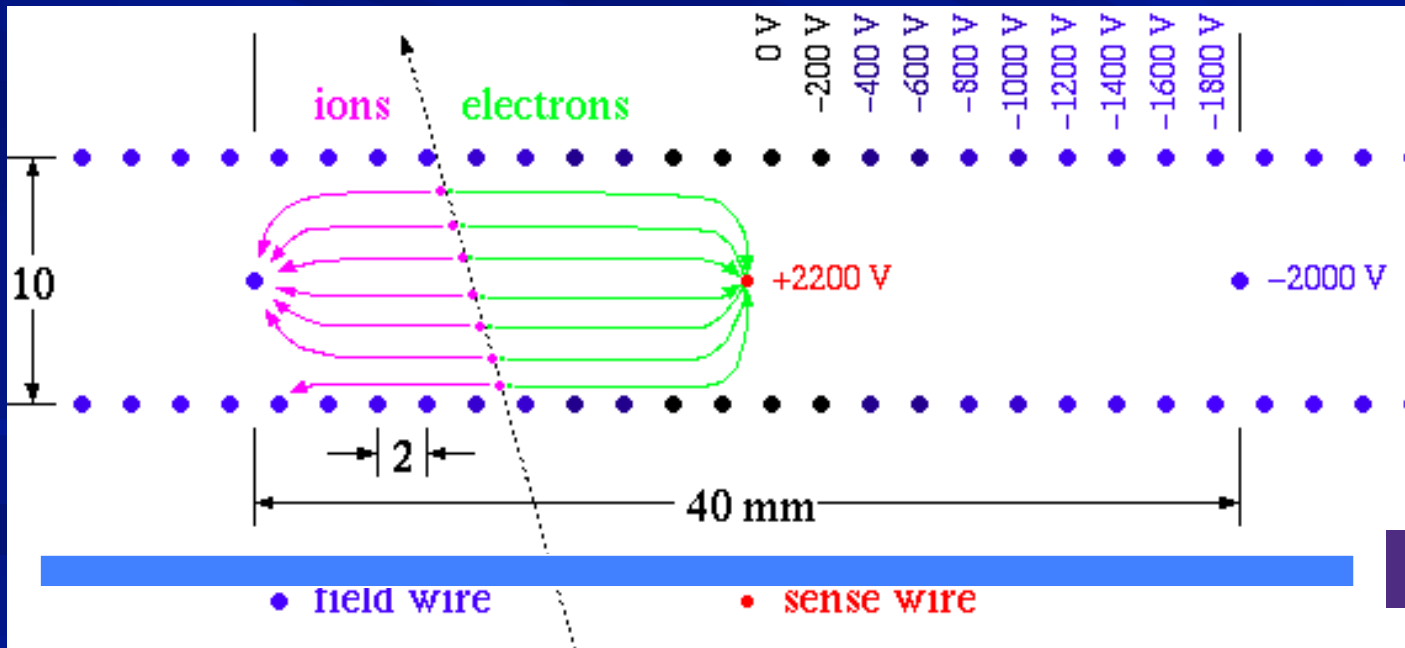
- Substantial improvement can be obtained using cathode strip/pads:
  - 2D information
  - High spatial resolutions due to center of gravity
  - Resolve ambiguities using strip pattern



- true hit
- ghost hit

# Drift chambers

- Obtain spatial information by measuring the electrons drift time
  - time measurement started by an external (fast) detector, i.e. scintillator counter
  - electrons drift to the anode (sense wire), in the field created by the cathodes
  - the electron arrival at the anode stops the time measurement



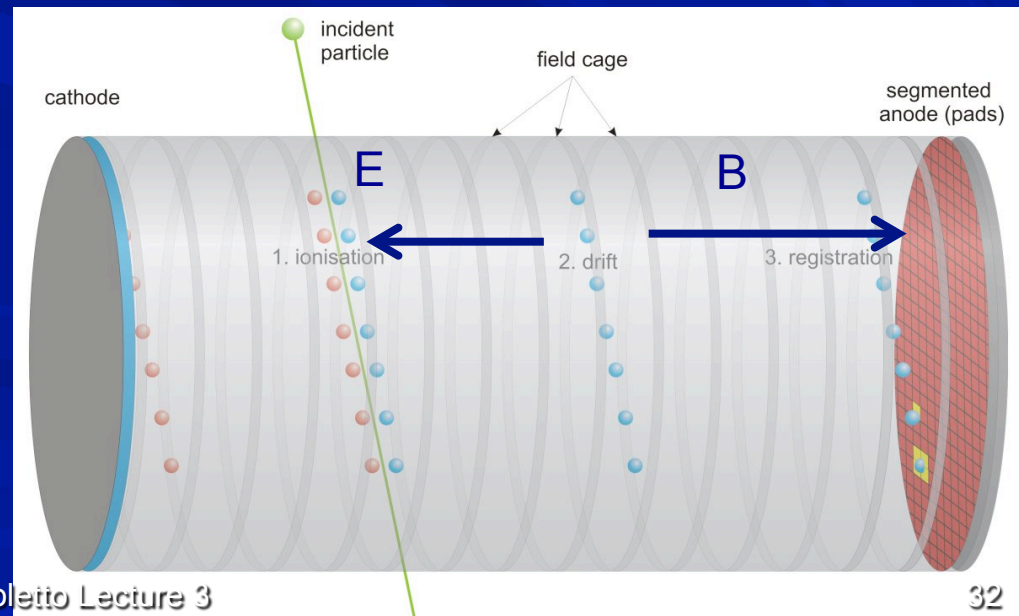
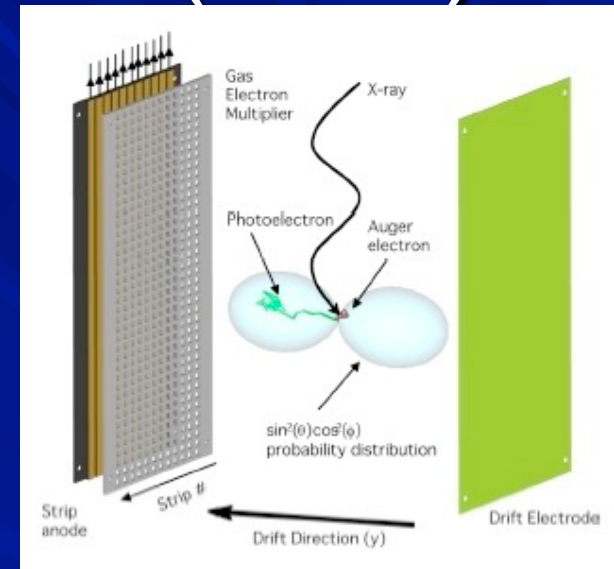
$$x = \int_0^{t_D} v_D dt$$

Need well-defined drift field

Scintillator counter

# Time Projection chamber (TPC)

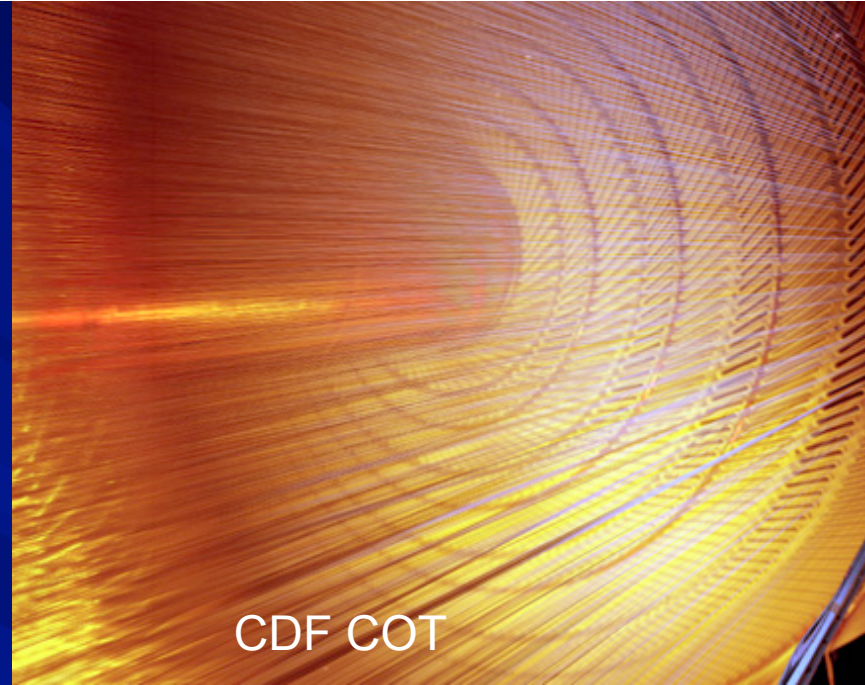
- Full 3-D reconstruction
  - XY: MWPC and pads of MWPC at the endcap
  - Z: from drift time measurement (several meters)
    - Field cage for very homogenous electric field
- Typical resolution
  - z and y  $\approx$  mm, x=150-300  $\mu$ m
  - dE/dx  $\approx$  5-10%
- Advantages:
  - Complete track information  $\rightarrow$  good momentum resolution
  - Good particle ID by dE/dx
- Challenges
  - Long drift time limited rate
  - Large volume (precision)
  - Large voltages (discharges)
  - Large data volume
  - Difficult operation at high rate







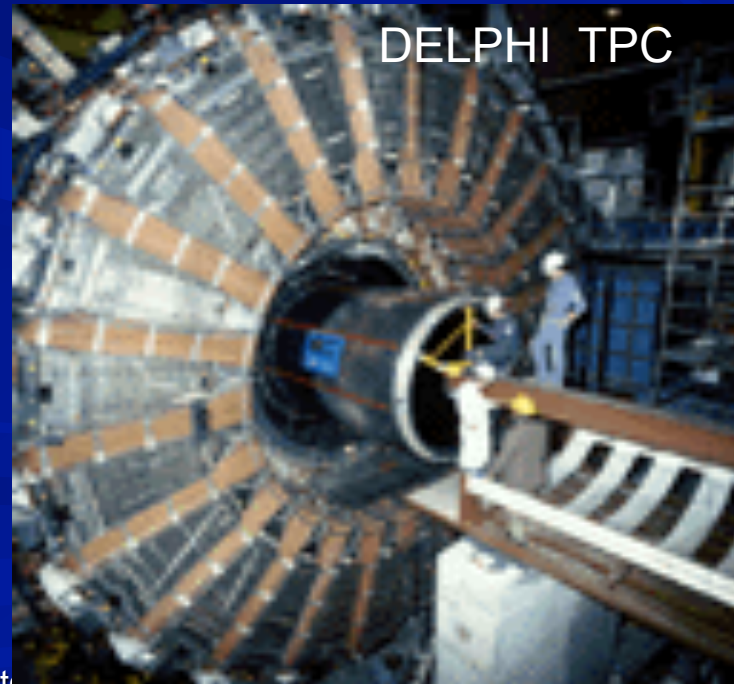
ALEPH TPC



CDF COT



OPAL JET  
CHAMBER

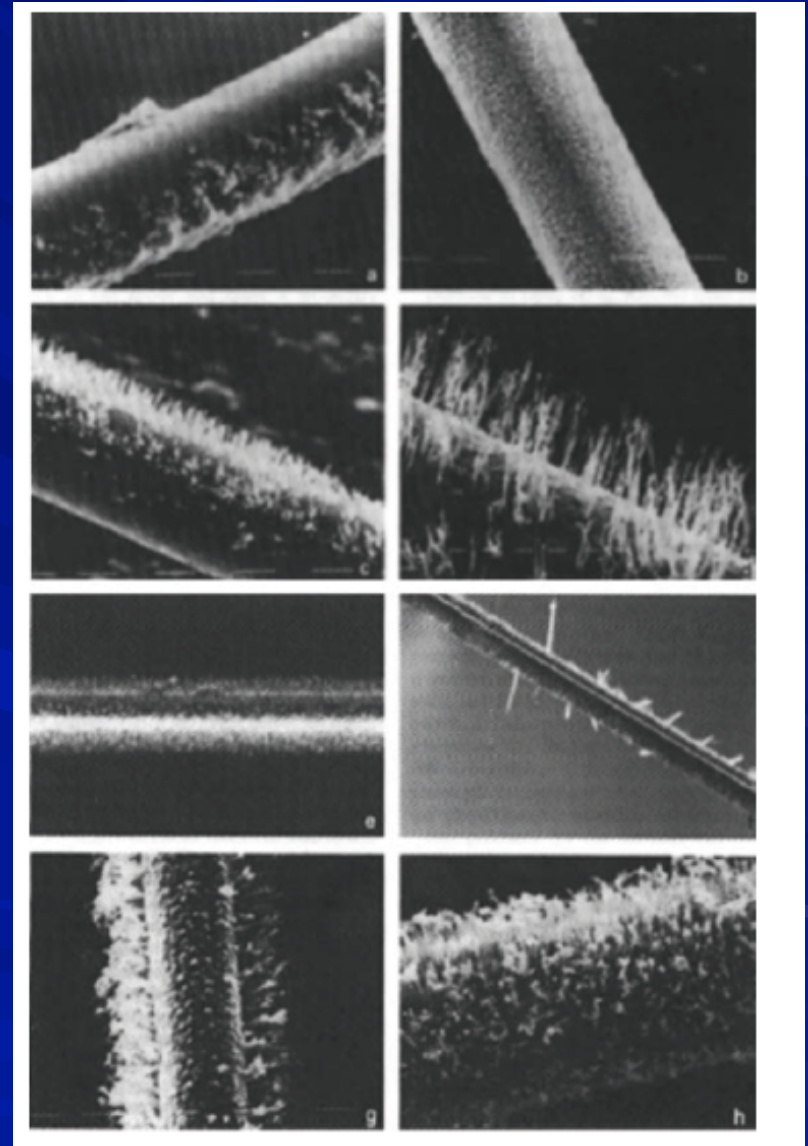


DELPHI TPC



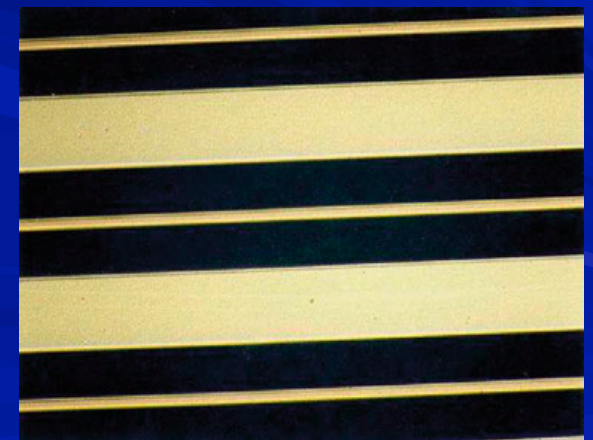
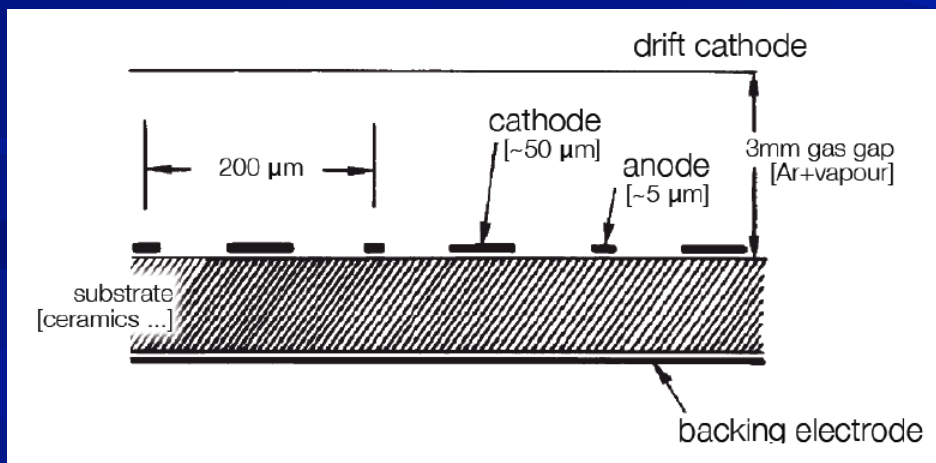
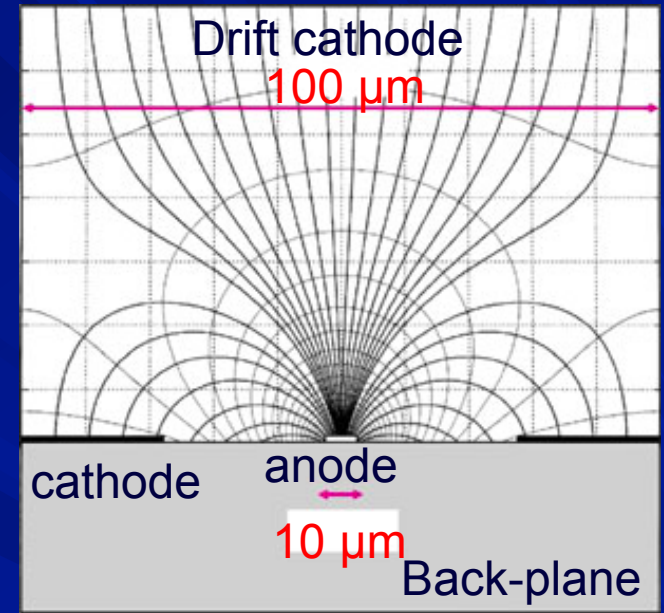
# Aging in wire chambers

- Consequences of avalanche
  - Formation of radicals i.e. molecule fragments
  - Polymerization yield long chains of molecules
  - Polymers may be attached to the electrodes
  - Reduction of gas amplification
- Important to avoid contamination



# Micro-strip gas chambers (MSGC)

- Replace wires with electrodes on printed circuit board
- Photolithography techniques allow  $100\ \mu\text{m}$  pitch
  - Higher granularity over wire chambers
  - High-rate capability  $>10^6\ \text{Hz}/\text{mm}^2$
  - Excellent spatial resolution ( $\sim 30\ \mu\text{m}$ )
  - Time resolution in the ns range.
- MSGC were first developed in 1990s
  - Initial problems sparks and anode destruction



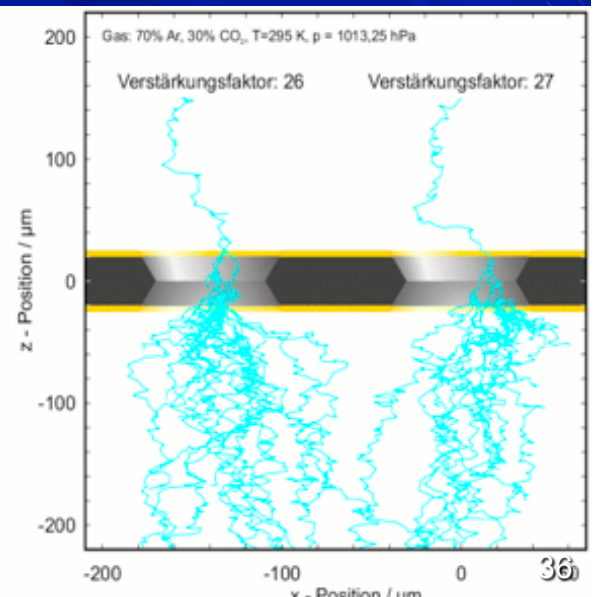
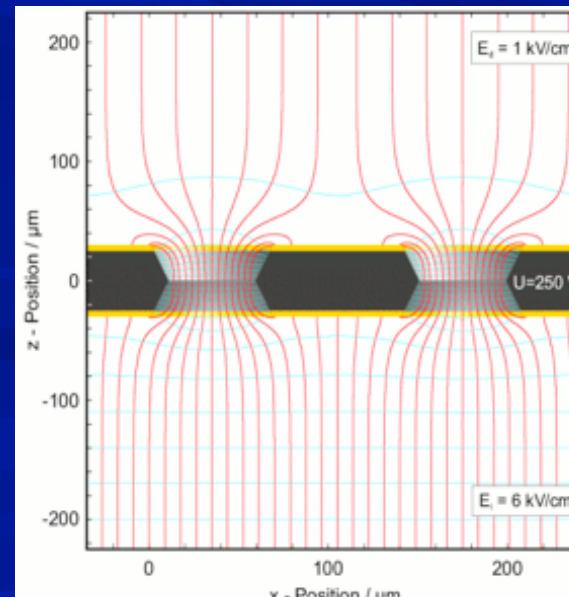
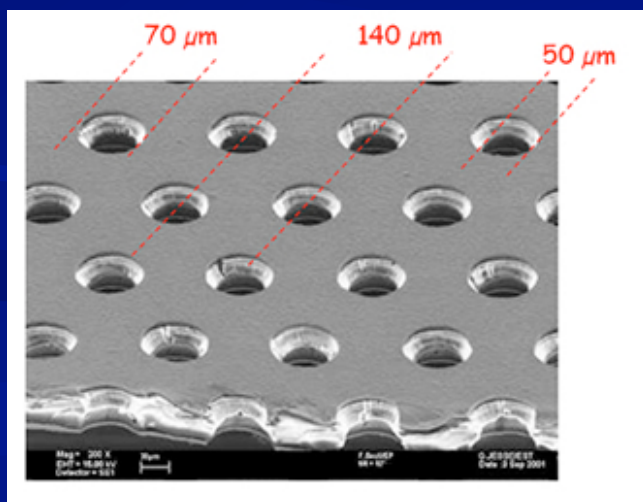
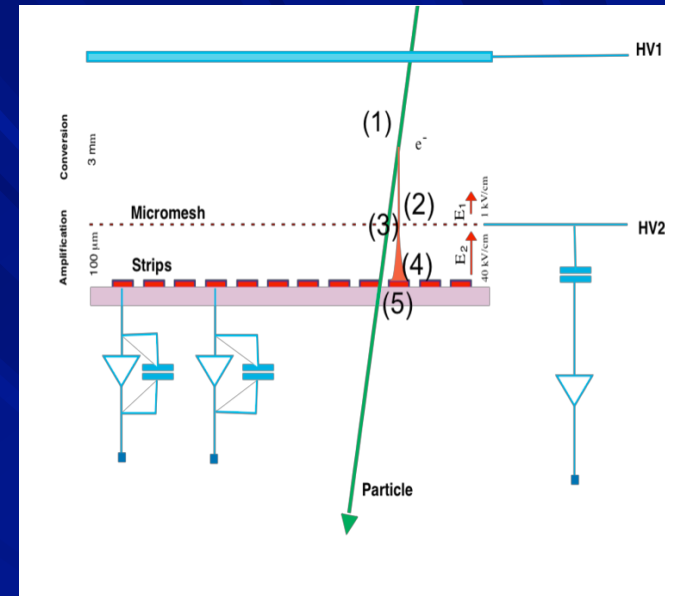
# Micromegas and GEM

## ■ Micromegas

- Gas volume divided in two by metallic micro-mesh
- Gain =  $10^4$  and a fast signal of 100ns.

## ■ GEM (Gas Electron Multipliers, Sauli 1996)

- Thin insulating Kapton foil coated with metal film
- Chemically produced holes pitch  $\approx 100 \mu\text{m}$
- Electrons are guided by high drift field of GEM which generates avalanche
  - Electric field strength is in the order of some 10 kV/cm
  - Avalanche gain of 100 – 1000

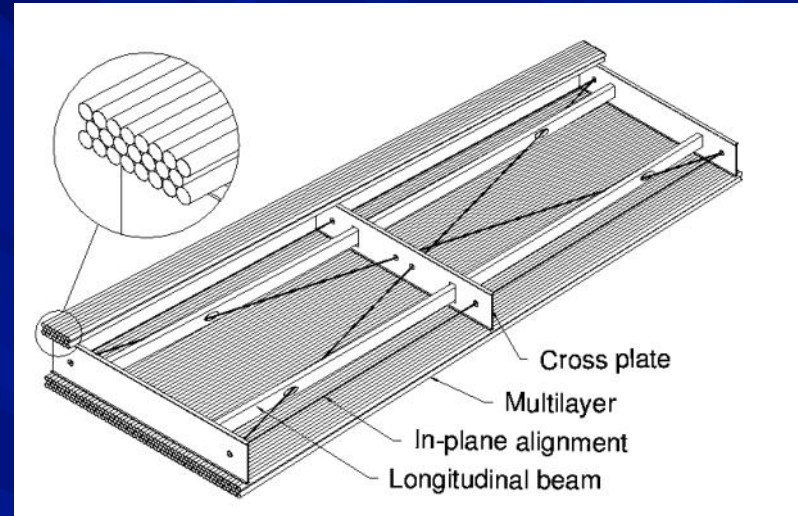
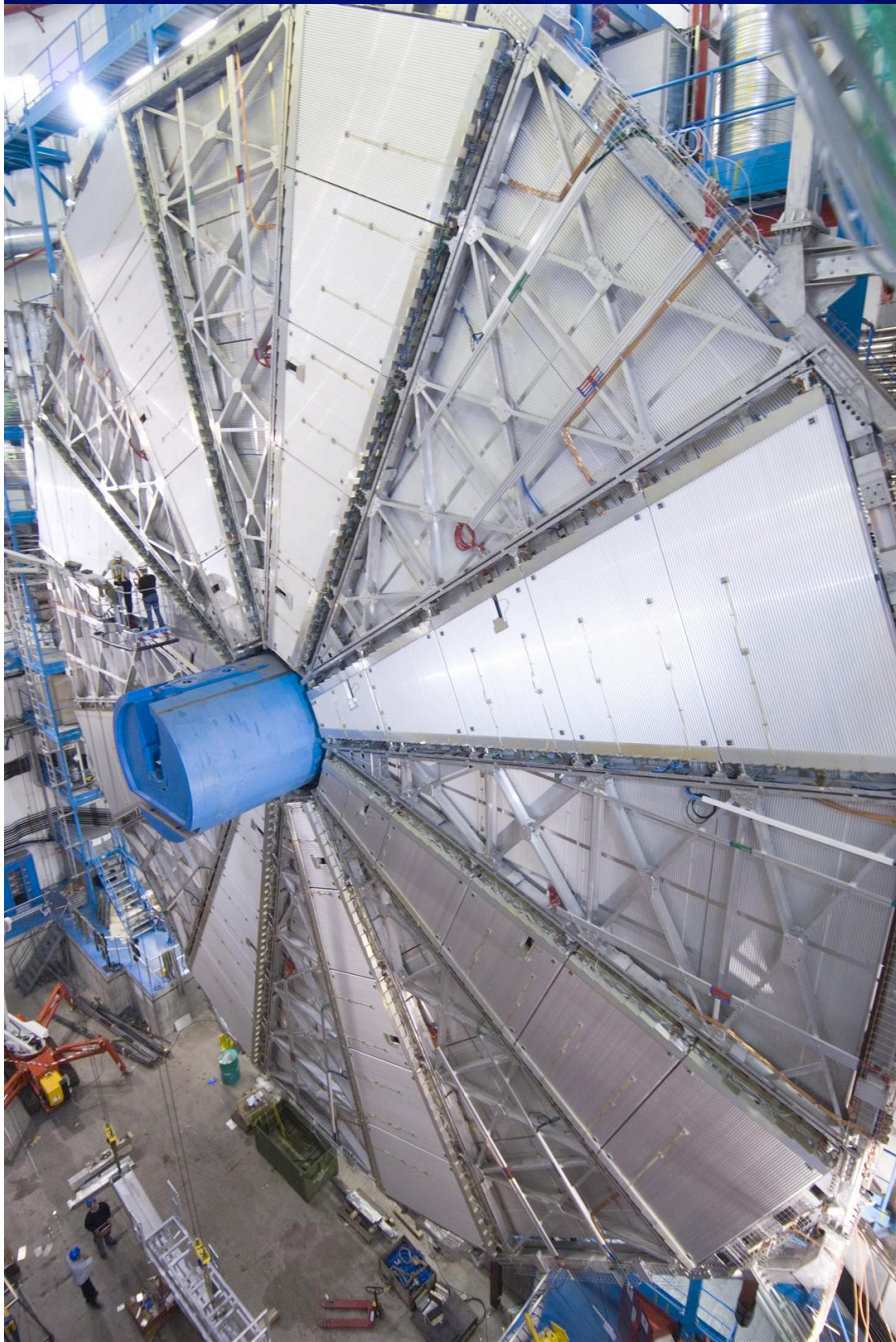




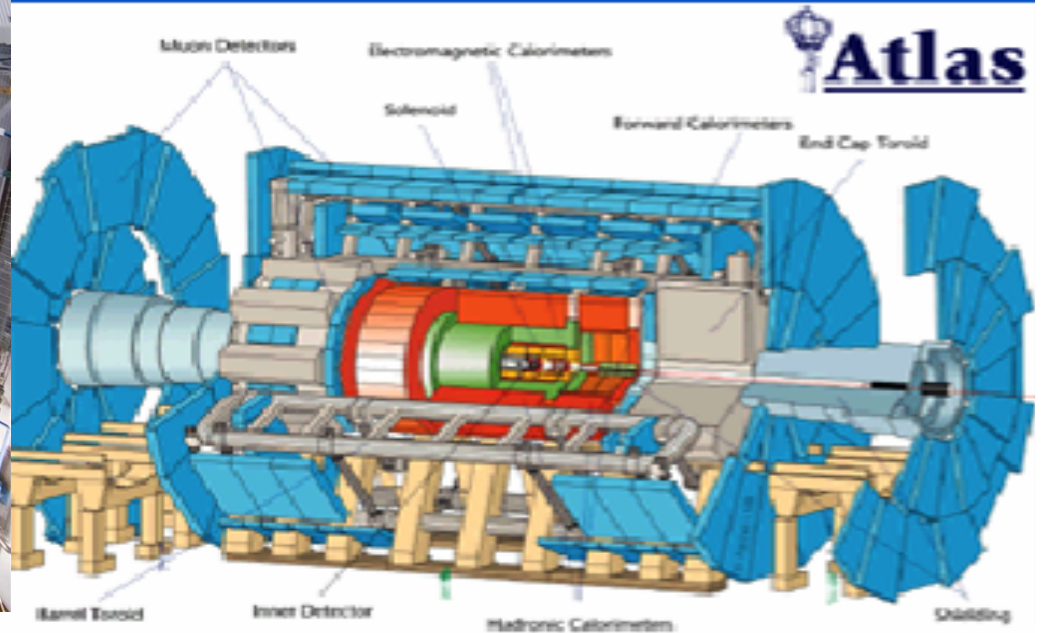
# GAS detectors at the LHC

- **The LHC experiments use gas detectors mainly for large scale muons detectors**
- **While the principle detecting elements are quit traditional many aspects have improved dramatically:**
  - **Readout electronics (integration, radiation resistance)**
  - **Excellent understanding and optimization of detector physics effects (HEED, MAGBOLTZ, GARFIELD)**
  - **Improvement in ageing characteristics due to special gases**
- **The principles are traditional but all other aspects are 100% state of the art.**

# ATLAS drift tubes

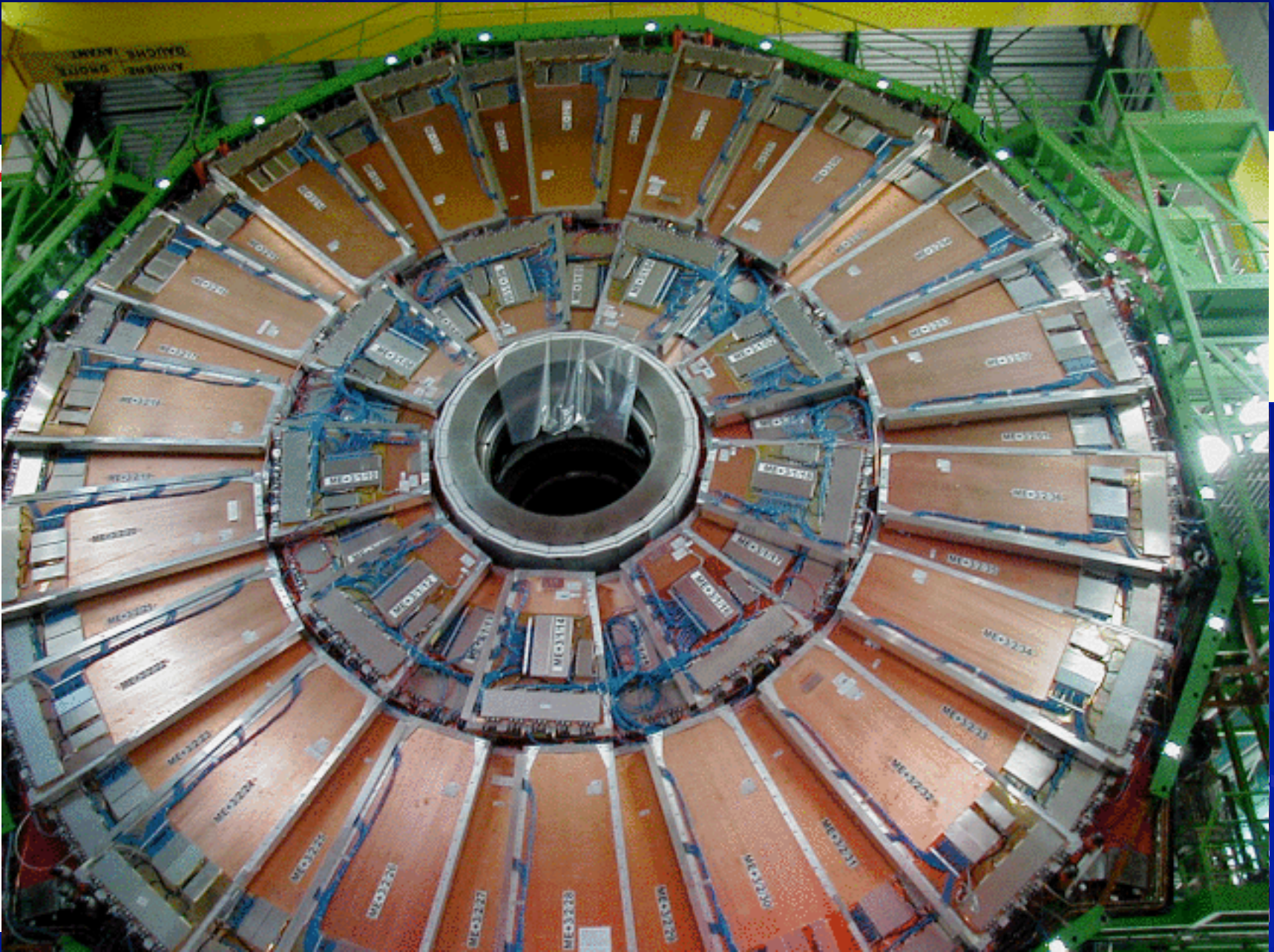


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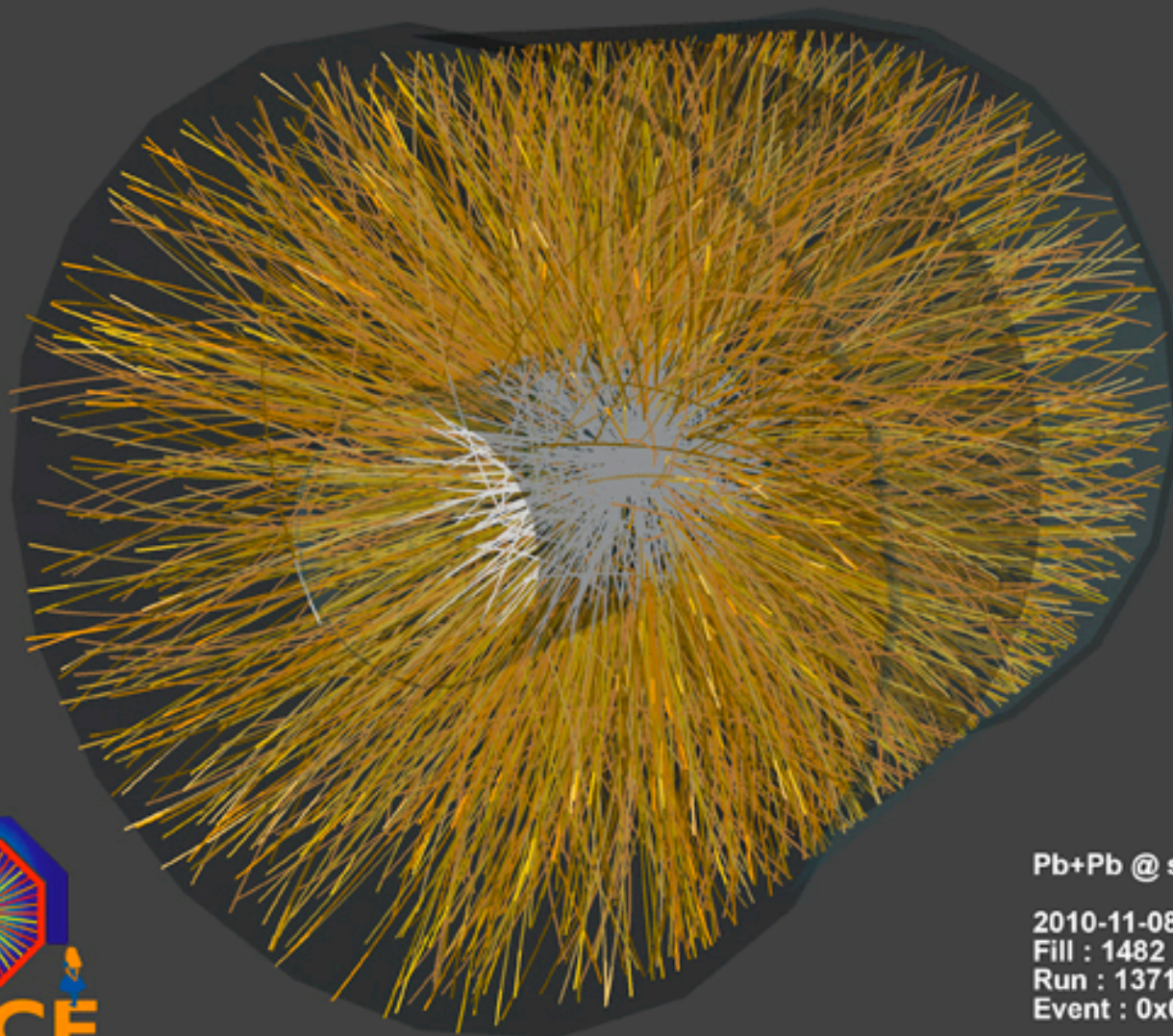




EN







Pb+Pb @  $\sqrt{s} = 2.76$  ATeV

2010-11-08 11:29:42

Fill : 1482

Run : 137124

Event : 0x00000000271EC693



# The upgrades

- **ATLAS:**
  - **TRT (Transition Radiation Tracker) replaced by Silicon Tracker**
- **CMS & ATLAS**
  - **Muons System detectors will mainly remain unchanged**
    - Addition of chambers to add redundancy
    - Possible addition of GEM at low eta where the rates are higher

# Literature

- D.H. Wilkinson: *Ionization Chambers and Counters* (Cambridge Univ. Press, 1950)
- S.A. Korff: *Electron and Nuclear Counters* (Van Nostrand, 1955)
- P. Rice-Evans: *Spark, Streamer, Proportional and Drift Chambers* (Richelieu, 1974)
- F. Sauli: *Principles of Operation of Multiwire Proportional and Drift Chambers* (CERN 77-09, 1977)
- Th. Ferbel, Editor: *Techniques and Concepts of High-energy Physics* (Plenum, 1983)
- R.C. Fernow: *Introduction to Experimental Particle Physics* (Cambridge Univ. Press, 1986)
- W.R. Leo: *Techniques for Nuclear and Particle Physics Experiments* (Springer, 1987)
- C. Fabjan and J. Pilcher, ed.: *Instrumentation in Elementary Particle Physics* (World Scientific, 1988)
- C.F.G. Delaney and E.C. Finch: *Radiation Detectors* (Clarendon Press, 1992)
- R. Gilmore: *Single Particle Detection and Measurement* (Taylor and Francis, 1992)
- F. Sauli, ed.: *Instrumentation in High Energy Physics* (World Scientific, 1992)
- K. Grupen: *Particle Detectors* (Cambridge Monographs on Part. Phys. 1996)
- K. Kleinknecht: *Detectors for Particle Radiation* (Cambridge Univ. Press 1998)
- G.F. Knoll: *Radiation Detection and Measurements, 3d Ed.* (Wiley, 2000)
- W. Blum, W. Riegler and L. Rolandi: *Particle Detection with Drift Chambers, 2d Ed.* (Springer 2008)

# ■ BACKUP

# Signal pulse formation and shape

$$dV = \frac{q}{lCV_0} \frac{d\phi(r)}{dr} dr \quad \text{with } \phi(r) = -\frac{CV_0}{2\pi\epsilon_0} \ln \frac{r}{a}$$

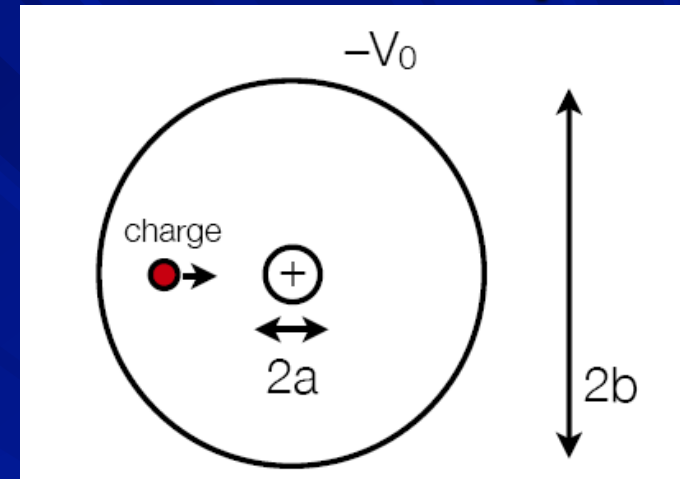
- Integrate from  $r'$  : point where the multiplication starts
- The induced voltage from electrons is:

$$V^- = -\frac{q}{lCV_0} \int_{a+r'}^a \frac{d\phi(r)}{dr} dr = -\frac{q}{lCV_0} \left[ \frac{CV_0}{2\pi\epsilon_0} \ln \left( \frac{a+r'}{a} \right) \right]$$

$$= -\frac{q}{2\pi\epsilon_0 l} \left[ \ln \left( \frac{a+r'}{a} \right) \right]$$

- The total induced voltage for ions is

$$V^+ = \frac{q}{lCV_0} \int_{a+r'}^b \frac{d\phi(r)}{dr} dr = -\frac{q}{2\pi\epsilon_0 l} \left[ \ln \left( \frac{b}{a+r'} \right) \right]$$



Cross check:  
 $V = V^+ + V^- = -q/lC$   
 $C = 2\pi\epsilon_0 / \ln(b/a)$

- The ratio  $V^-/V^+$  is:

$$\frac{V^-}{V^+} = \frac{\ln \left( \frac{a+r'}{a} \right)}{\ln \left( \frac{b}{a+r'} \right)}$$

For  $a=10 \mu\text{m}$ ,  $b=10 \text{mm}$ ,  $r'=1 \mu\text{m}$   $\rightarrow V^-/V^+=0.013 \rightarrow$  Signal is mainly due to ions



# Signal pulse formation and shape

- Ignoring electron signal and setting  $r(0)=a$

$$V(t) = \int_{r(0)}^{r(t)} \frac{dV}{dr} dr = -\frac{q}{2\pi\epsilon_0 l} \ln \frac{r(t)}{a}$$

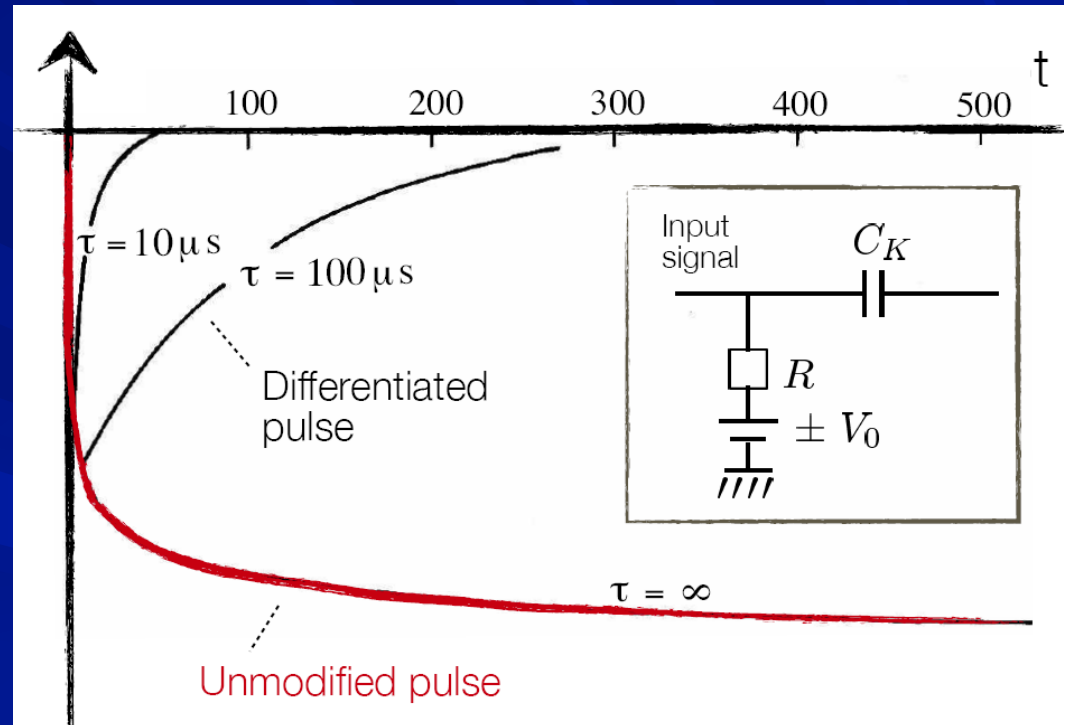
$$v_D = \frac{dr}{dt} = \mu E(r) = \frac{\mu C V_0}{2\pi\epsilon_0} \frac{1}{r}$$

$$r dr = \frac{\mu C V_0}{2\pi\epsilon_0} dr$$

$$r(t) = \left( a^2 + \frac{\mu C V_0}{\pi\epsilon_0} t \right)^{1/2}$$

$$V(t) = -\frac{q}{4\pi\epsilon_0 l} \ln \left( 1 + \frac{\mu C V_0}{\pi\epsilon_0 a^2} t \right) = -\frac{q}{4\pi\epsilon_0 l} \ln \left( 1 + \frac{t}{t_0} \right)$$

$$t_0 = \frac{\pi\epsilon_0 a^2}{\mu C V_0}$$



# Signal shape

- Total drift time  $T$

$$r(T) = b$$

$$b = \left( a^2 + \frac{\mu C V_0}{\pi \epsilon_0} \right)^{1/2}$$

$$T = \frac{\pi \epsilon_0}{\mu C V_0} (b^2 - a^2) = t_0 \left( \frac{b^2}{a^2} - 1 \right)$$

$$t_0 = \frac{\pi \epsilon_0}{\mu C V_0}$$

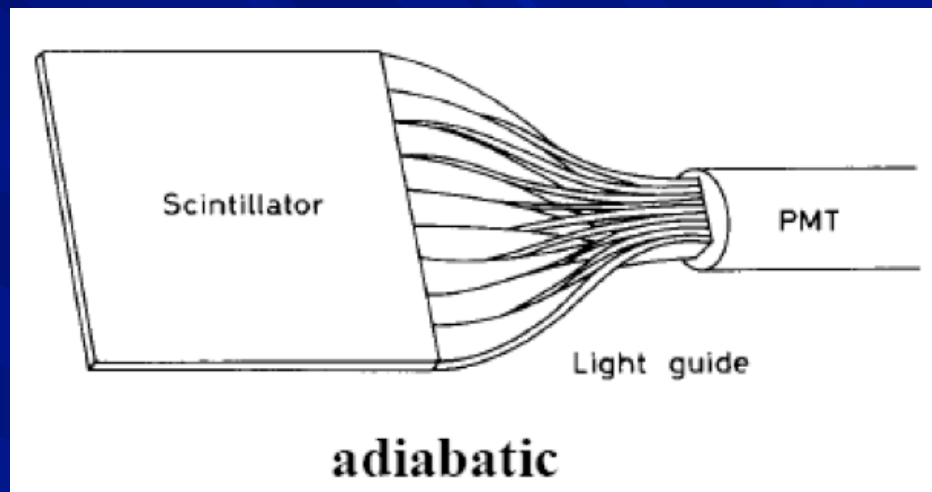
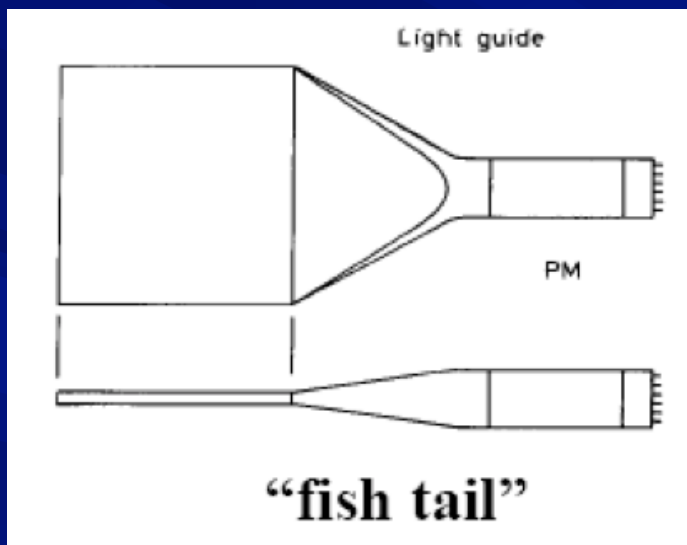
- We can determine  $V(a/b T)$

$$\begin{aligned} V\left(\frac{a}{b} \cdot T\right) &= -\frac{q}{4\pi\epsilon_0} \ln\left(1 + \frac{\frac{a}{b} \cdot T}{t_0}\right) = -\frac{q}{4\pi\epsilon_0} \ln\left(1 + \frac{a}{b} \left(\frac{b^2}{a^2} - 1\right)\right) \\ &= -\frac{q}{4\pi\epsilon_0} \ln\left(\frac{b}{a}\right) = -\frac{1}{2} \frac{q}{lC} \quad \text{with } C = \frac{2\pi\epsilon_0}{\ln(b/a)} \end{aligned}$$

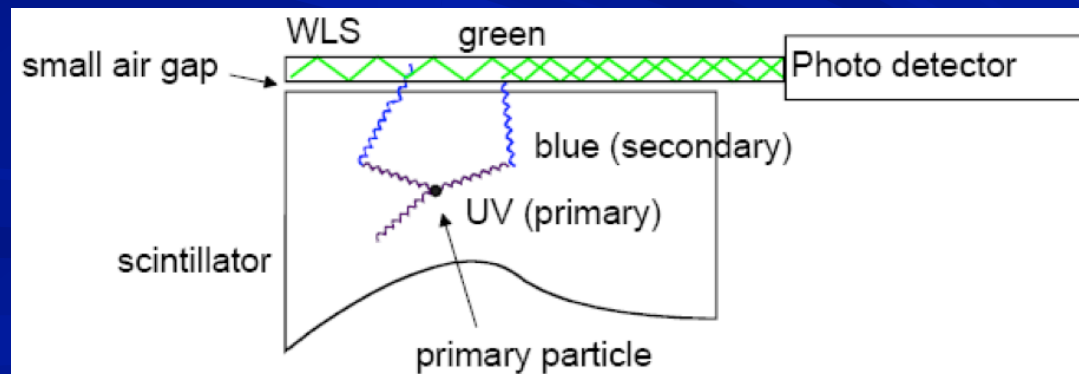
Typically  $a/b \approx 10^{-3}$ ,  
i.e. after  $10^{-3} T$  already  
half of the signal  
voltage is reached ...  
Choice of suitable RC-  
circuit allows short  
(differentiated)  
signals ...

# Geometries

- Light guides: transfer by total internal reflection + outer reflector

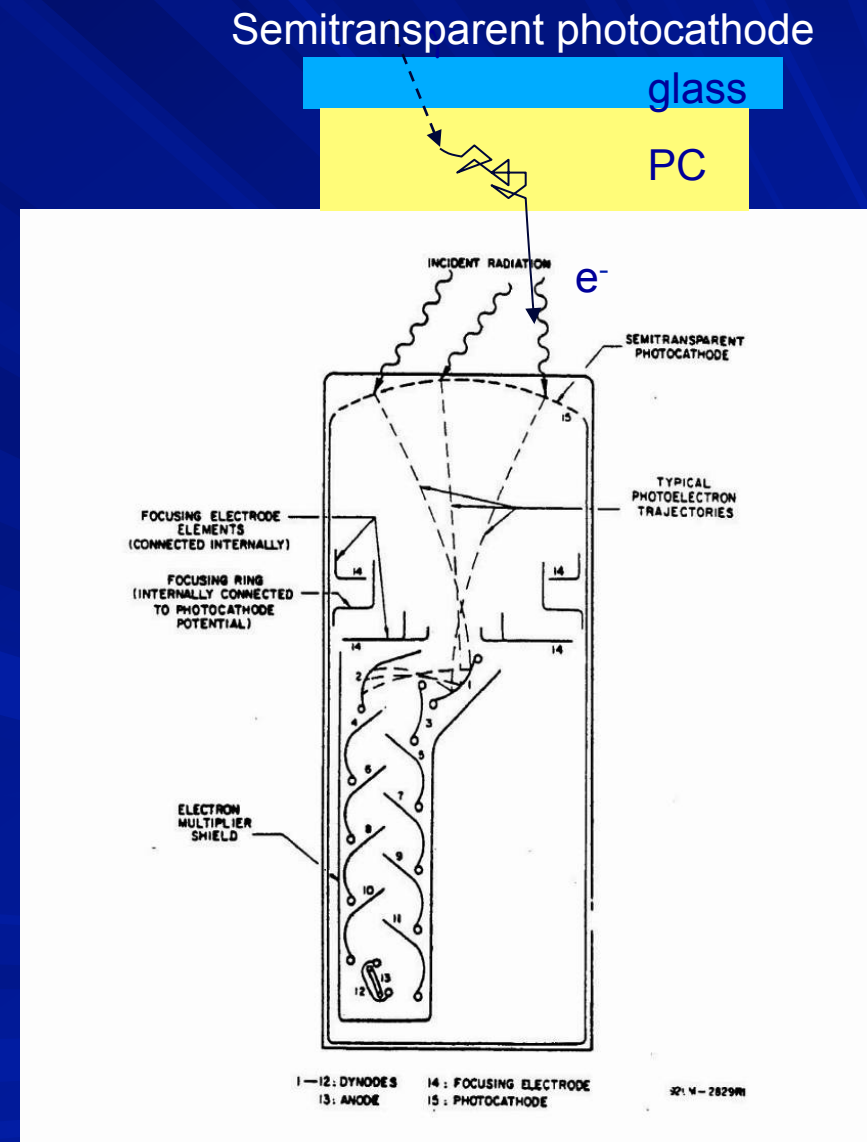


- UV light enters the WLS material
- Light is transformed into longer wavelength
- Total internal reflection inside the WLS material
- 'Transport' of the light to the photo detector



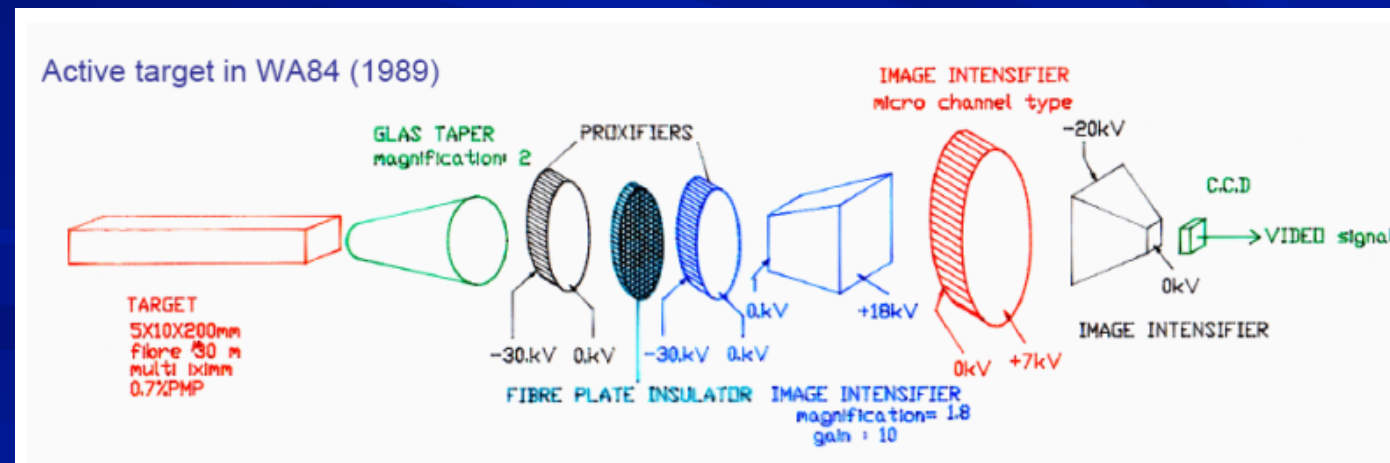
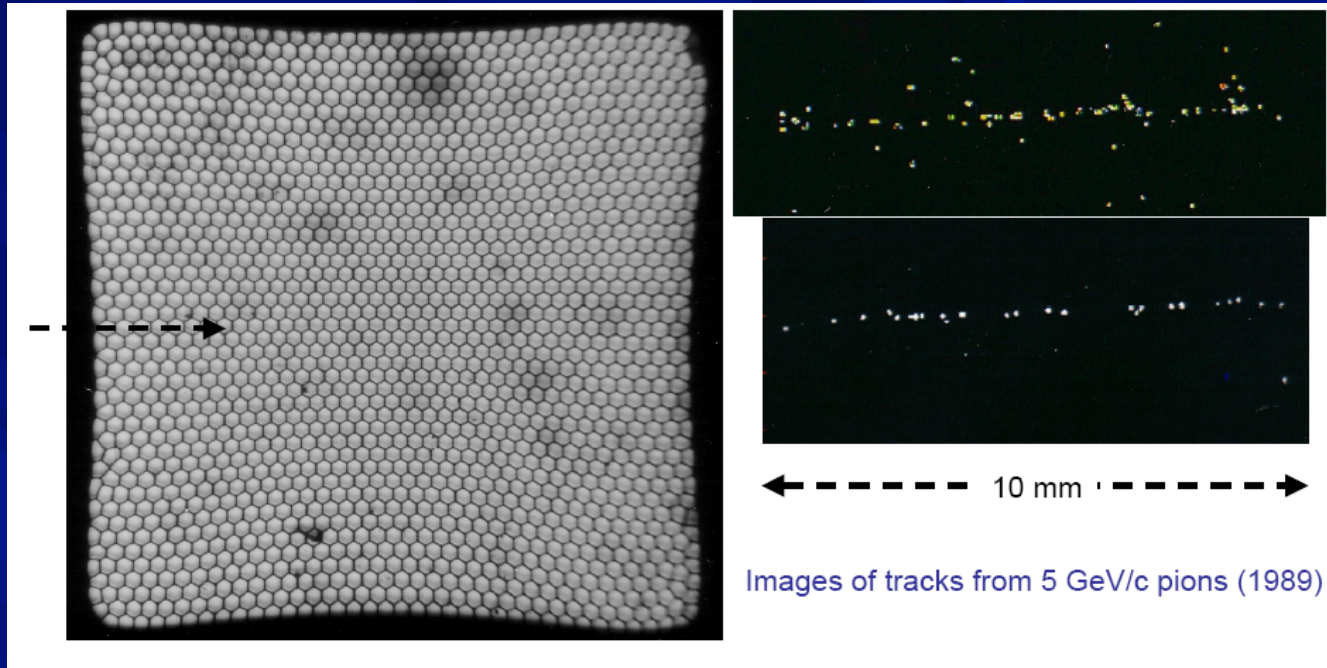
# Photomultipliers

- Scintillators are well established and cheap techniques to detect photons → Photomultipliers and the fast response time → 1 to 100ns
- Schematic of a Photomultiplier:
  - Typical Gains (as a function of the applied voltage):  $10^8$  to  $10^{10}$
  - Typical efficiency for photon detection:  $< 20\%$
  - For very good PMs: registration of single photons possible.
  - Example: 10 primary Electrons, Gain  $10^7 \rightarrow 10^8$  electrons in  $T \approx 10$ ns.  
 $I = Q/T = 10^8 * 1.603 * 10^{-19} / 10 * 10^{-9} = 1.6$ mA.
  - Across a  $50 \Omega$  Resistor →  $U = R * I = 80$ mV.





# Fiber Tracking



Readout of photons in a cost effective way is rather challenging.  
D. Bortoletto Lecture 3

# Drift and mobility

- In an external E-field electrons/ions obtain velocity  $\mathbf{v}_D$  in addition to thermal motion; on average electrons/ions move along field lines of electric field E

$$\vec{v}_D = \mu_{\pm} |\vec{E}|$$

typical:

$E \sim 1 \text{ kV / cm-atm}$

$v_d \approx \text{cm/ms}$  for ions

$v_d \approx \text{cm}/\mu\text{s}$  for e-

$$\frac{D}{\mu} = \frac{kT}{e}$$

$\mu_+$  : ion mobility

for ions  $\mathbf{v}_D \sim E/P$ , i.e. for constant pressure constant mobility

$\mu_-$  : electron mobility in cold gas approximation ( $T_{\text{kin}} \sim kT$ )

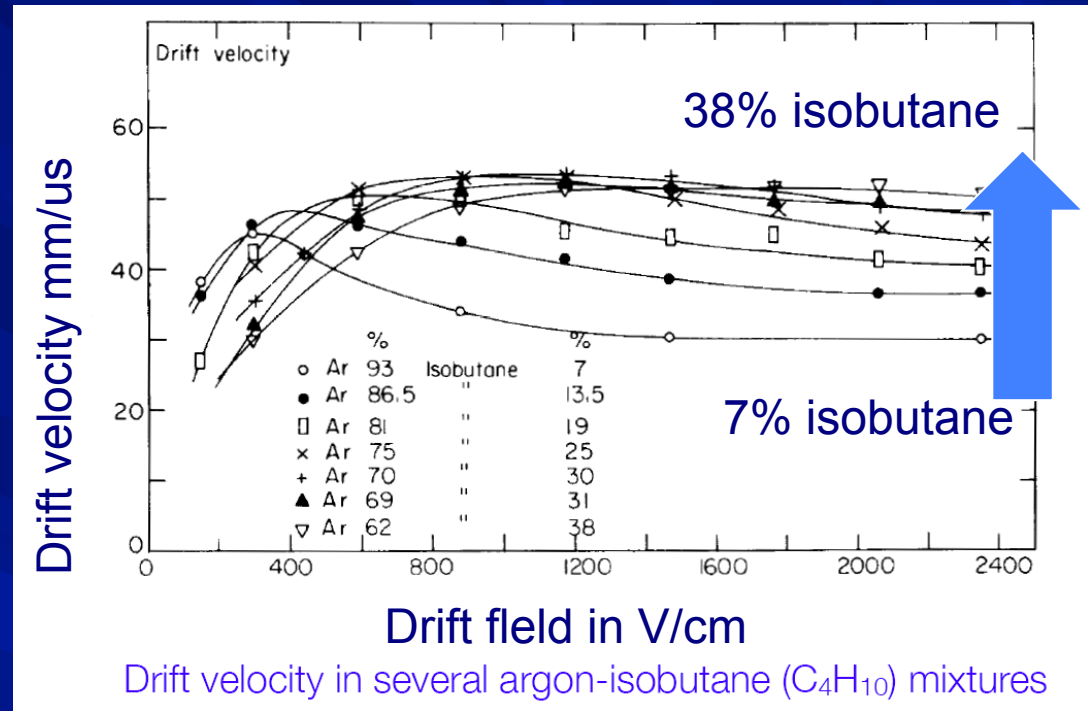
$\rightarrow \mathbf{v}_D \sim E$ ,  $\mu = \text{const.}$

in a hot gas ( $T_{\text{kin}} \gg kT$ )  $\rightarrow \mathbf{v}_D = \text{const.}$ ,  $\mu = \text{not const.}$

Einstein relation for ideal gases in thermal equilibrium  
The gain in velocity may affect the diffusion rate and thereby the time behavior of the detector (e.g. drift chamber)

# Drift Velocity

- $v_d$  and  $D$  of  $e^-$  depend on the inelastic cross section involving the rotational and vibrational levels of molecules.
- The inelastic cross section in noble gases = 0 below excitation and ionization thresholds.

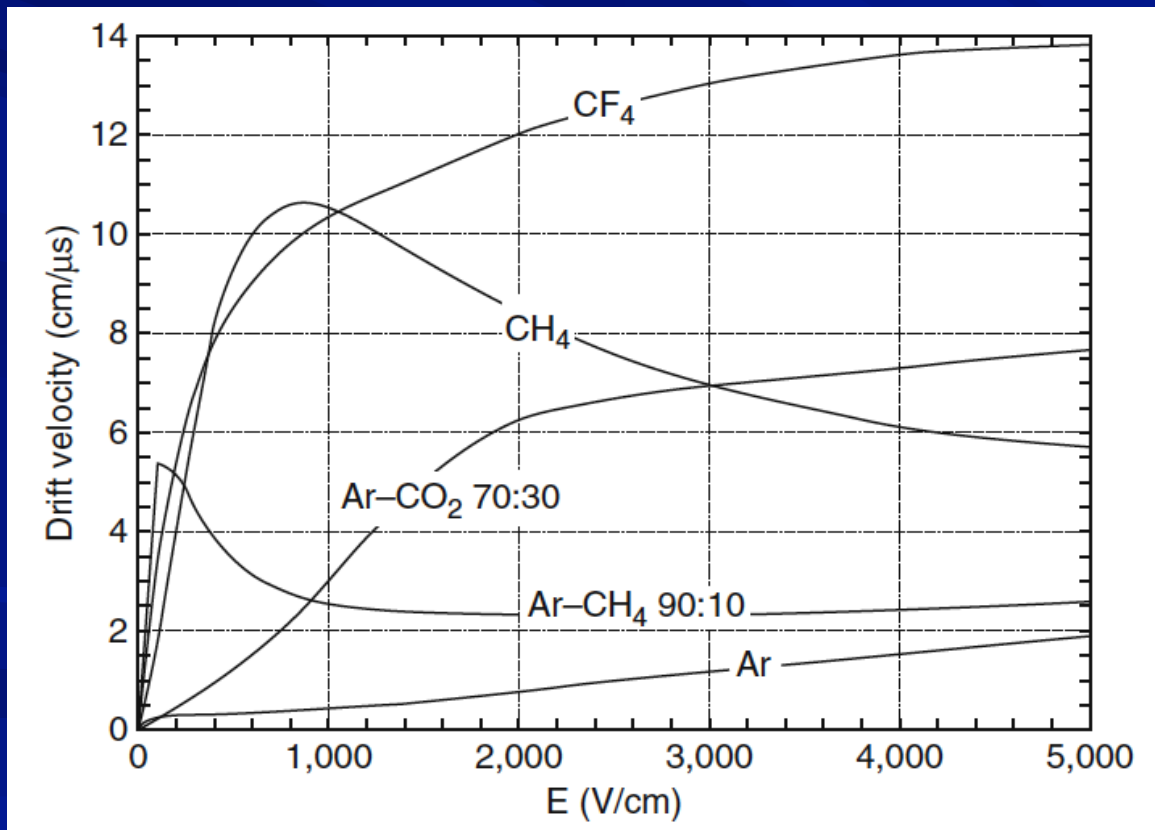


- Large  $v_d$  are achieved by adding polyatomic gases (usually  $CH_4$ ,  $CO_2$ , or  $CF_4$ ), which “cool” the electrons (because of their large inelastic cross section at moderate energies) and absorb the ultraviolet (UV) photons emitted by the excited inert gas atoms



# Drift velocity

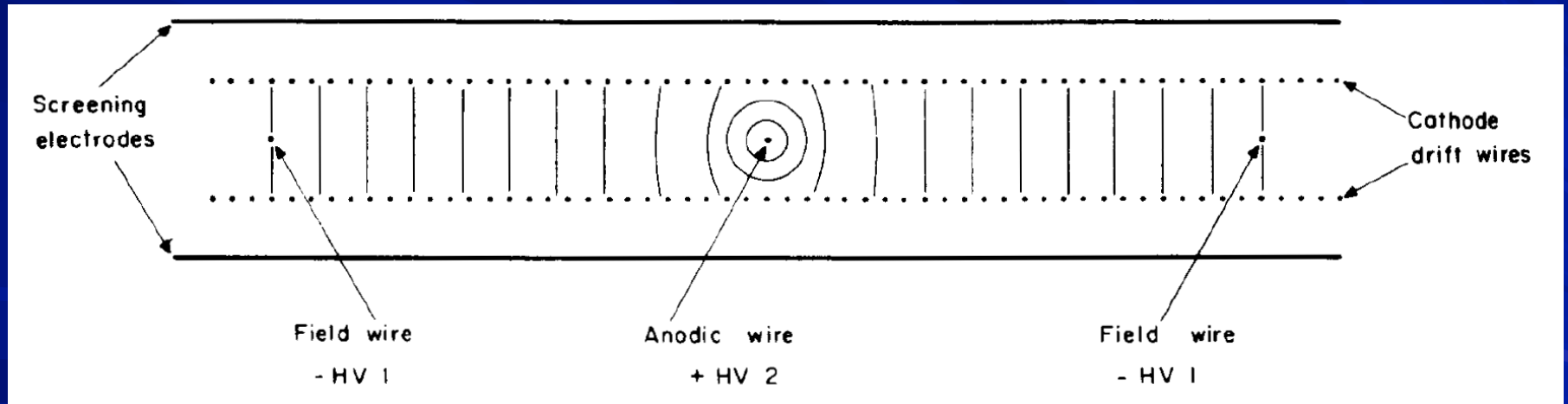
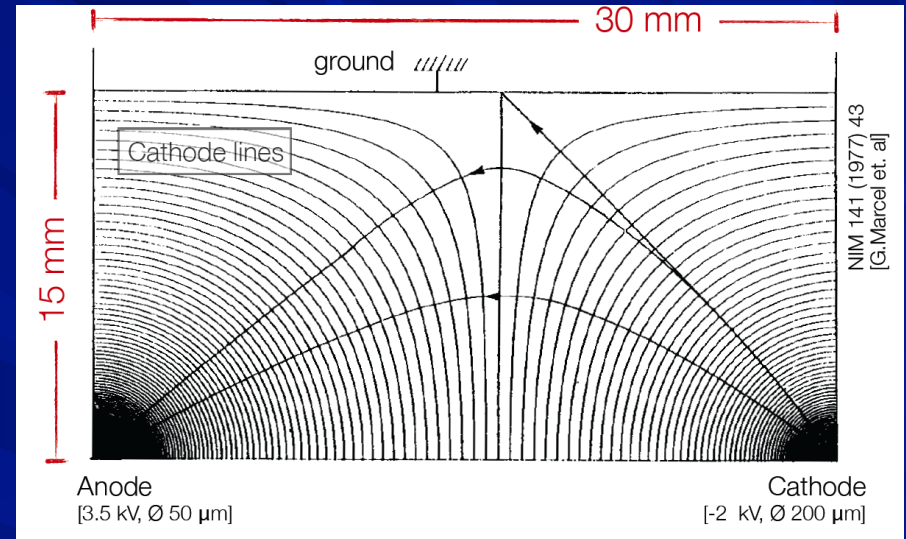
- Values of drift velocity for some commonly used gases at NTP, computed with the MAGBOLTZ program (see <http://consult.cern.ch/writeup/magboltz>)



- Using fast CF<sub>4</sub>-based mixtures at fields around kV/cm<sup>-1</sup>, the electron drift velocity is around 10 cm · μs<sup>-1</sup>.
- Since the collection time is inversely proportional to the drift velocity, diffusion effects are reduced in gases such as CF<sub>4</sub> that have high drift

# Field in drift chamber

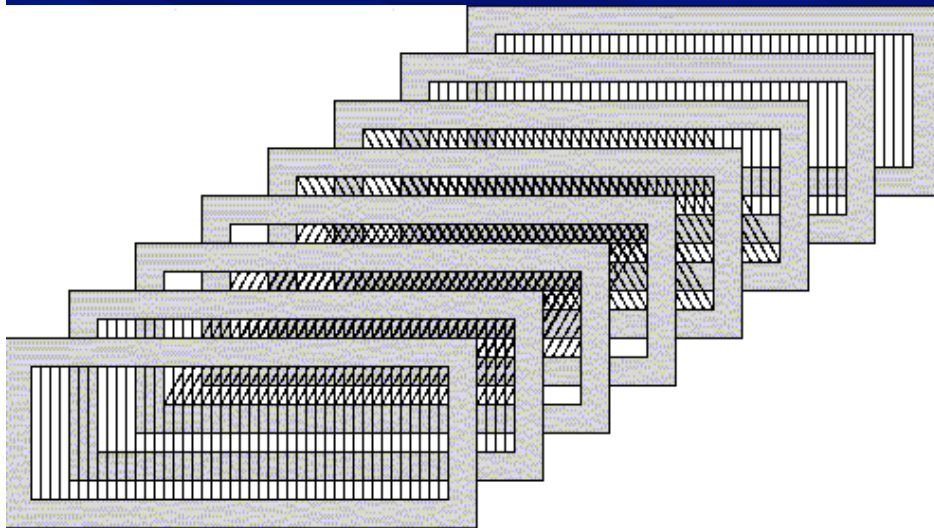
- Field wires avoid low field regions → long drift-times
- Uniform drift field requires:
  - Gap length/wire spacing  $\approx 1$ 
    - i.e. for typical wire spacing → thick chambers O(cm)



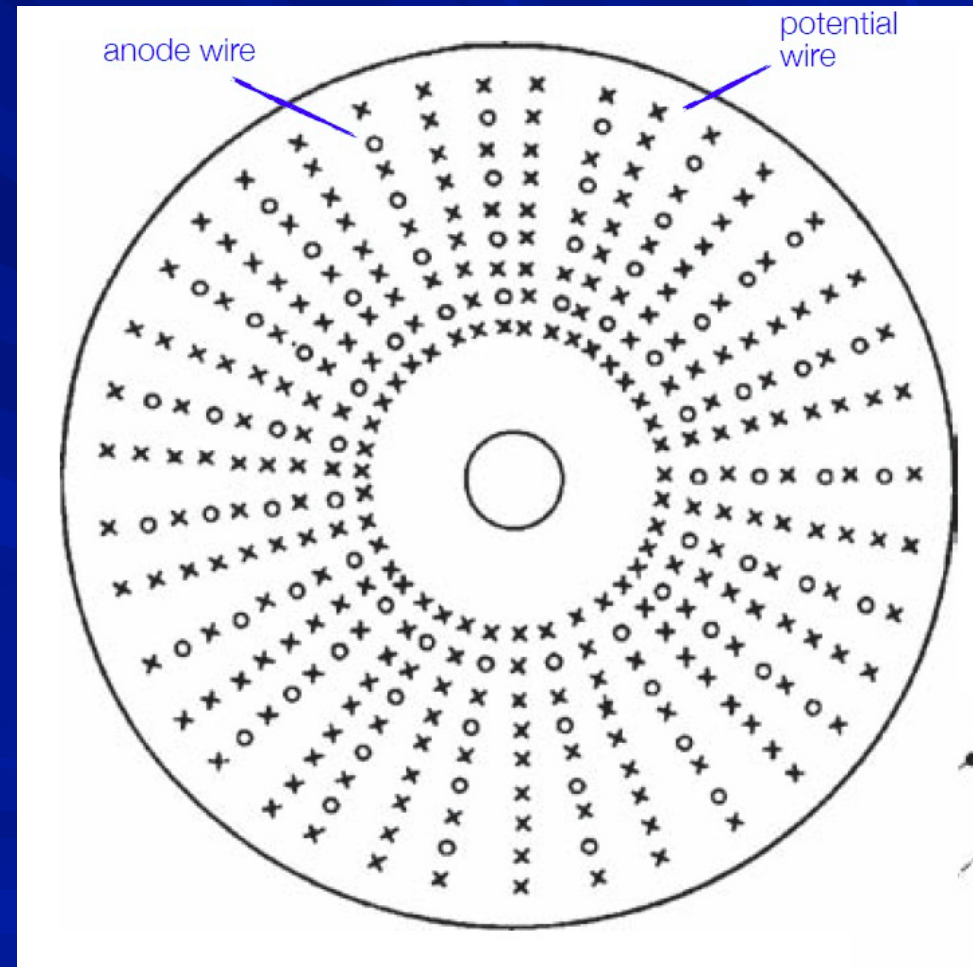
- Adjustable field multi-wire drift chamber with voltage divider via cathode wire planes
- Space point resolution limited by mechanical accuracy  $\approx 200 \mu\text{m}$
- Hit density needs to be low.

# Tracking detectors

- Tracking at fixed target experiments:
  - Multi-layer MWPC or drift chamber



- Tracking at collider experiments:
  - cylindrical drift chamber





# TPC Technical solutions

- Problem with space charge effects due to slow moving ions lead to changes in the drift region E- field
- Solved by gating grid which must be triggered

