

# Recent results and prospects for charm mixing and CPV at Threshold

**Xiao-Rui Lyu**

*(E-mail: [xiaorui@ucas.ac.cn](mailto:xiaorui@ucas.ac.cn))*

**University of Chinese Academy of Sciences (UCAS), Beijing**

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# Outline

- Introduction
- Recent results from charm threshold data
  - mixing parameter  $y_{CP}$
  - strong phase  $\delta_{K\pi}$   
*(see Roy Briere's talk for  $\delta_{KS\pi+\pi^-}$  measurement at BESIII)*
  - CP asymmetries
- Prospects on future (dedicated) charm facility
- Summary

# Neutral $D$ meson oscillation

$D^0$  and  $\bar{D}^0$  can transfer into each other, like K, B and Bs mesons

- The mass eigenstates are

$$|D_1\rangle = p|D^0\rangle + q|\bar{D}^0\rangle$$

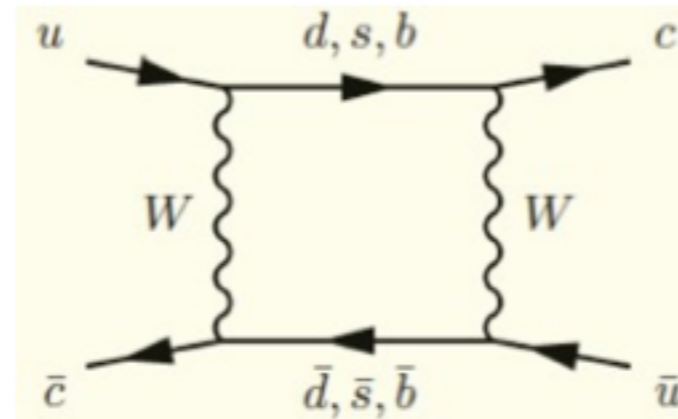
$$|D_2\rangle = p|D^0\rangle - q|\bar{D}^0\rangle$$

- With eigenvalues

$$\mu_1 = m_1 - \frac{i}{2}\Gamma_1$$

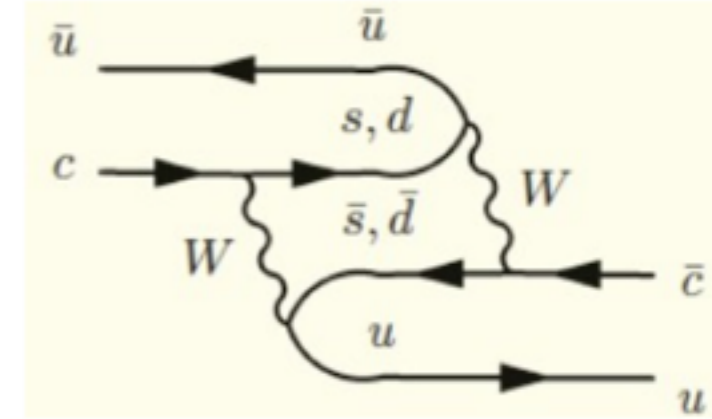
$$\mu_2 = m_2 - \frac{i}{2}\Gamma_2$$

Short-distance:



CKM suppression:  $b$   
GIM suppression:  $d, s$

Long-distance:



$$m \equiv \frac{m_1 + m_2}{2}, \quad \Delta m \equiv m_2 - m_1$$

$$\Gamma \equiv \frac{\Gamma_1 + \Gamma_2}{2}, \quad \Delta\Gamma \equiv \Gamma_2 - \Gamma_1$$

$x$  mixing: **Channel for New Physics.**

$y$  (long-distance) mixing: SM background.

$$x \equiv \frac{\Delta m}{\Gamma}$$

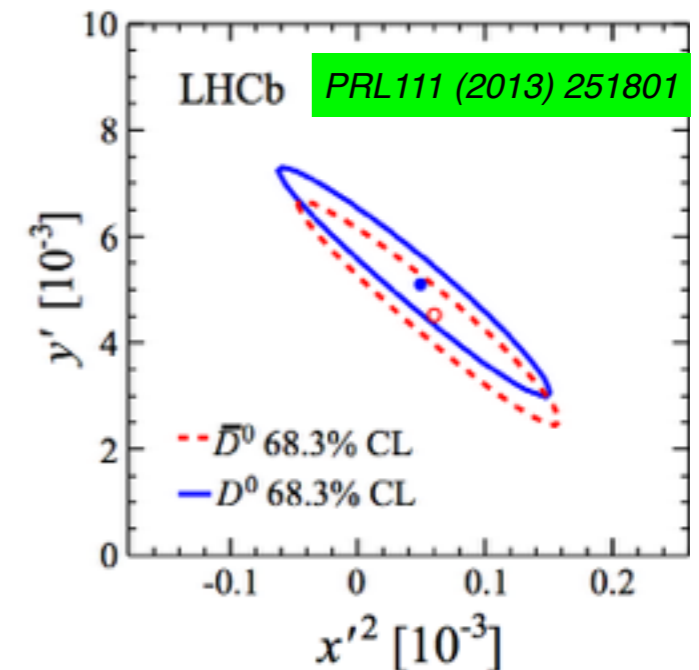
$$y \equiv \frac{\Delta\Gamma}{2\Gamma}$$

# $D$ meson oscillation

- ✓ **short distance** is highly suppressed by the **GIM mechanism** and by the **CKM matrix elements** within the SM:  $x \sim O(10^{-5})$ ;  $y \sim O(10^{-7})$ 
  - new physics might manifest in the loop, such as FCNC processes with up-type quark, complementary to those with down quarks (K or B mesons, already studied with observed CPV)
- ✓ long distance is dominant:  $(x, y) \sim O(10^{-3})$ 
  - but theoretical uncertainty is large
- ✓ Observation of  $D\bar{D}$  oscillation by CDF and LHCb
 

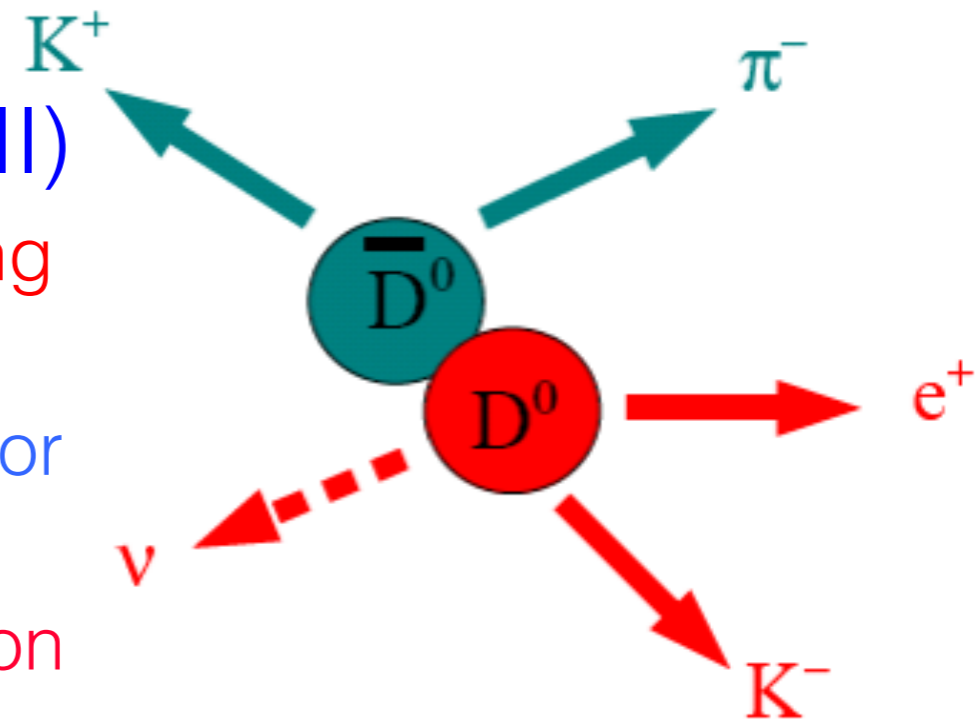
$$y' \equiv y \cos \delta_{K\pi} - x \sin \delta_{K\pi}$$

$$x' \equiv x \cos \delta_{K\pi} + y \sin \delta_{K\pi}$$
- ✓ Improving the constraints on the charm mixing parameters is important for testing the SM, such as long-distance effect
- ✓ At charm threshold, **strong phase** is a unique contribution:
  - to extract the mixing parameter  $(x, y)$  from  $(x', y')$
  - to (over-)constrain the CKM unitarity triangle, which is crucial for searching for new physics



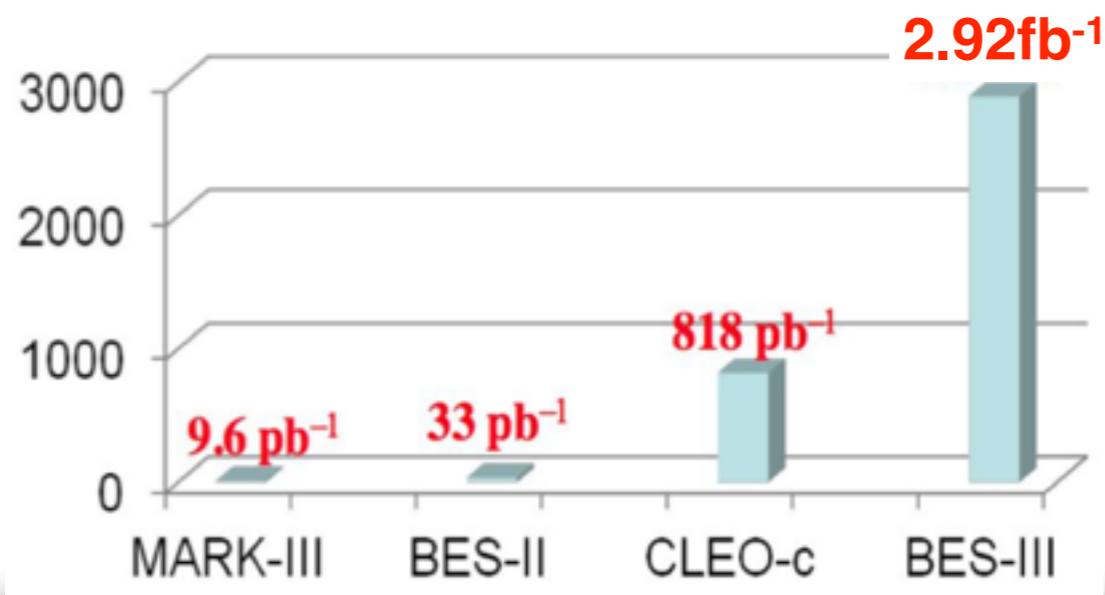
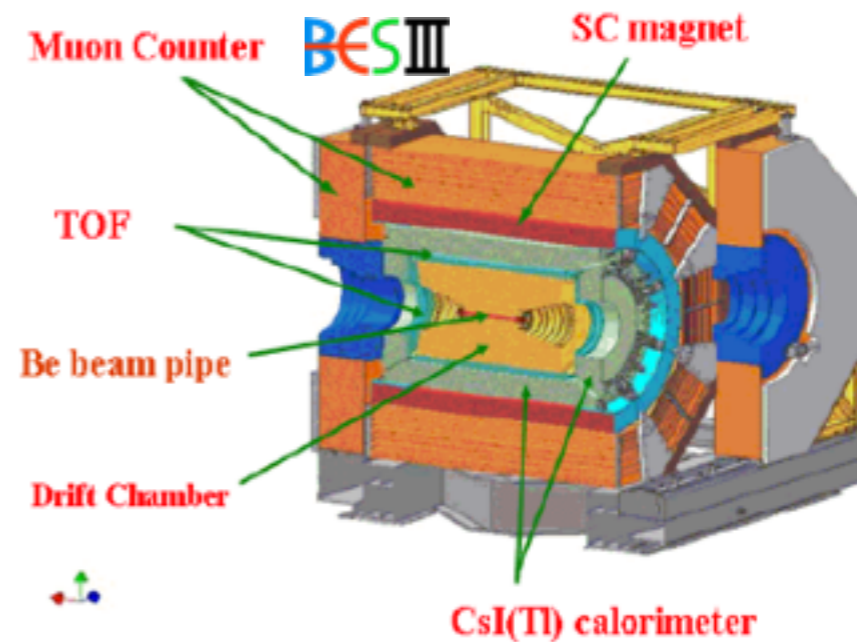
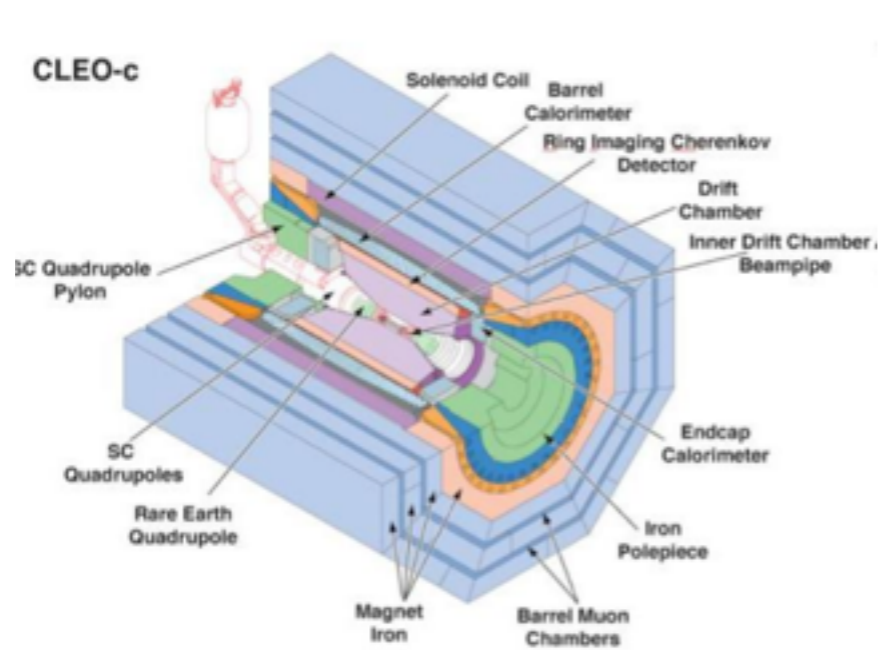
# Charm facilities

- Hadron colliders (huge cross-section, energy boost)
  - Tevetron (CDF, D0)
  - LHC (LHCb, CMS, ATLAS)
- $e^+e^-$  Colliders (more kinematic constraints, clean environment,  $\sim 100\%$  trigger efficiency)
  - B-factories (Belle, BaBar)
  - Threshold production (CLEOc, BESIII)
    - ★ Quantum Correlations (QC) and CP-tagging are unique
    - ★ Only D meson pairs, no extra CM Energy for pions: clean backgrounds
    - ★ Lots of systematic uncertainties cancellation while applying double tag technique



# Data samples at charm threshold

- ◆ **CLEO-c: 818 pb<sup>-1</sup> @ $\psi(3770)$**
- ◆ **BESIII: 2.9 fb<sup>-1</sup> (~3.5 x CLEO-c data) @ $\psi(3770)$**

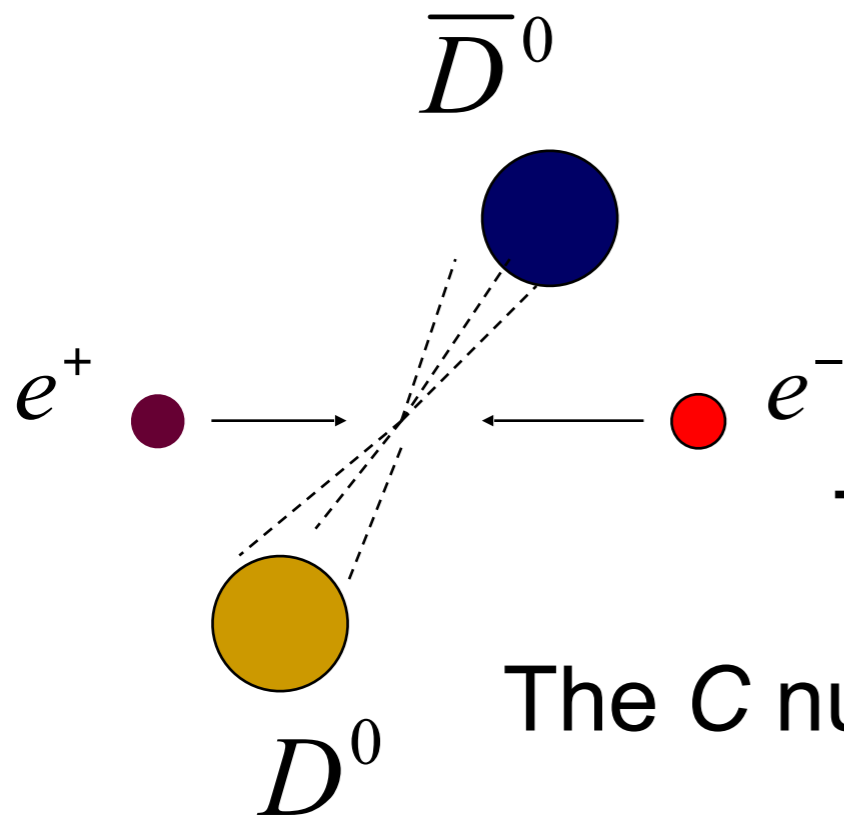


**In the future, in total BESIII will accumulate ~10/fb data @ $\psi(3770)$**

# The decay rate of a correlated state

For a physical process producing  $D^0 \bar{D}^0$  such as

$$e^+ e^- \rightarrow \psi'' \rightarrow D^0 \bar{D}^0$$



The  $D^0 \bar{D}^0$  pair will be a quantum-correlated state.

The quantum number of  $\psi''$  is  $J^{PC} = 1^{--}$

The C number of  $D^0 \bar{D}^0$  pair in this process is  $C = -$

*Taking advantage the quantum coherence of  $D\bar{D}$  pairs, we can study the  $D$  mixing and CPV in a unique way*

- ▶ *strong phase in  $D$  decays*
- ▶  *$D$  mixing parameters*
- ▶ *direct CP violation*
- ▶ *...*

# Time-integrated decay rates

◆ No time dependent information at Charm threshold

◆ Anti-symmetric wavefunction:

$$\Gamma_{ij}^2 = |\langle i|D^0\rangle\langle j|\bar{D}^0\rangle - \langle j|D^0\rangle\langle i|\bar{D}^0\rangle|^2$$

◆ Double tag rates:

$$A_i^2 A_j^2 [1 + r_i^2 r_j^2 - 2r_i r_j \cos(\delta_i + \delta_j)]$$

◆ CP tag:  $r=1, \delta=0$  or  $\pi$ ;  $l^\pm$  tag:  $r=0$

◆ Single and Double tag rates

$$\text{◆ } z_f \equiv 2 \cos \delta_f, r_f \equiv \frac{A_{DCS}}{A_{CF}}, R_M \approx \frac{x^2 + y^2}{2}$$

Selected references:

Goldhaber and Rosner, PRD 15, 1254 (1977)

Bigi and Sanda, PLB 171, 320 (1986)

Xing, PRD 55, 196 (1997)

Gronau, Grossman, Rosner, PLB 508, 37 (2001)

Atwood and Petrov, PRD 71, 054032 (2005)

Asner and Sun, PRD 73, 034024 (2006); PRD 77, 019901(E) (2008)

C-odd	$f$	$\bar{f}$	$l^+$	$l^-$	CP+	CP-
$f$	$R_M [1 + r_f^2 (2 - z_f^2) + r_f^4]$					
$\bar{f}$	$1 + r_f^2 (2 - z_f^2) + r_f^4$	$R_M [1 + r_f^2 (2 - z_f^2) + r_f^4]$				
$l^+$	$r_f^2$	$1$	$R_M$			
$l^-$	$1$	$r_f^2$	$1$	$R_M$		
CP+	$1 + r_f (r_f + z_f)$	$1 + r_f (r_f + z_f)$	$1$	$1$	$0$	
CP-	$1 + r_f (r_f - z_f)$	$1 + r_f (r_f - z_f)$	$1$	$1$	$4$	$0$
Single Tag		$1 + r_f^2 + r_f z_f y$		$1$		$2(1 \mp y)$



# Analysis techniques

## Quantum Correlated topics

- ◆ **Mixing ( $x^2+y^2$ ):  $D\bar{D} \rightarrow (K^-l^+\nu)^2, (K^-\pi^+)^2$**
- ◆ **Strong phase  $\cos\delta$ : Double Tag Events:  $K^-\pi^+$  vs  $CP\pm$**
- ◆ **Charm Mixing ( $y_{CP}$ ): Flavor Tag vs  $CP\pm$**
- ◆ **DCS: Wrong sign decays  $K^-\pi^+$  vs  $K^-l^+\nu$**
- ◆ **Strong phase  $c_i, s_i$  (Dalitz) :  $K_S\pi^+\pi^-$  vs  $CP\pm$ ;  $K_S\pi^+\pi^-$  vs Flavor Tag;  $K_S\pi^+\pi^-$  vs  $K_{S,L}\pi^+\pi^-$**
- ◆ **Typical Kinematic variables for full reconstruction**
  - ◆ **Energy difference & Beam Constrained mass**

$$\Delta E = E_D - E_{\text{Beam}}$$

$$M_{\text{BC}} = \sqrt{E_{\text{Beam}}^2 - \vec{p}_D^2}$$

## Global fit method

- ◆ **Combined analysis to extract mixing parameters, DCS, strong phase plus charm hadronic branching fractions**

# Global Analysis at CLEO-c (818 pb<sup>-1</sup>)

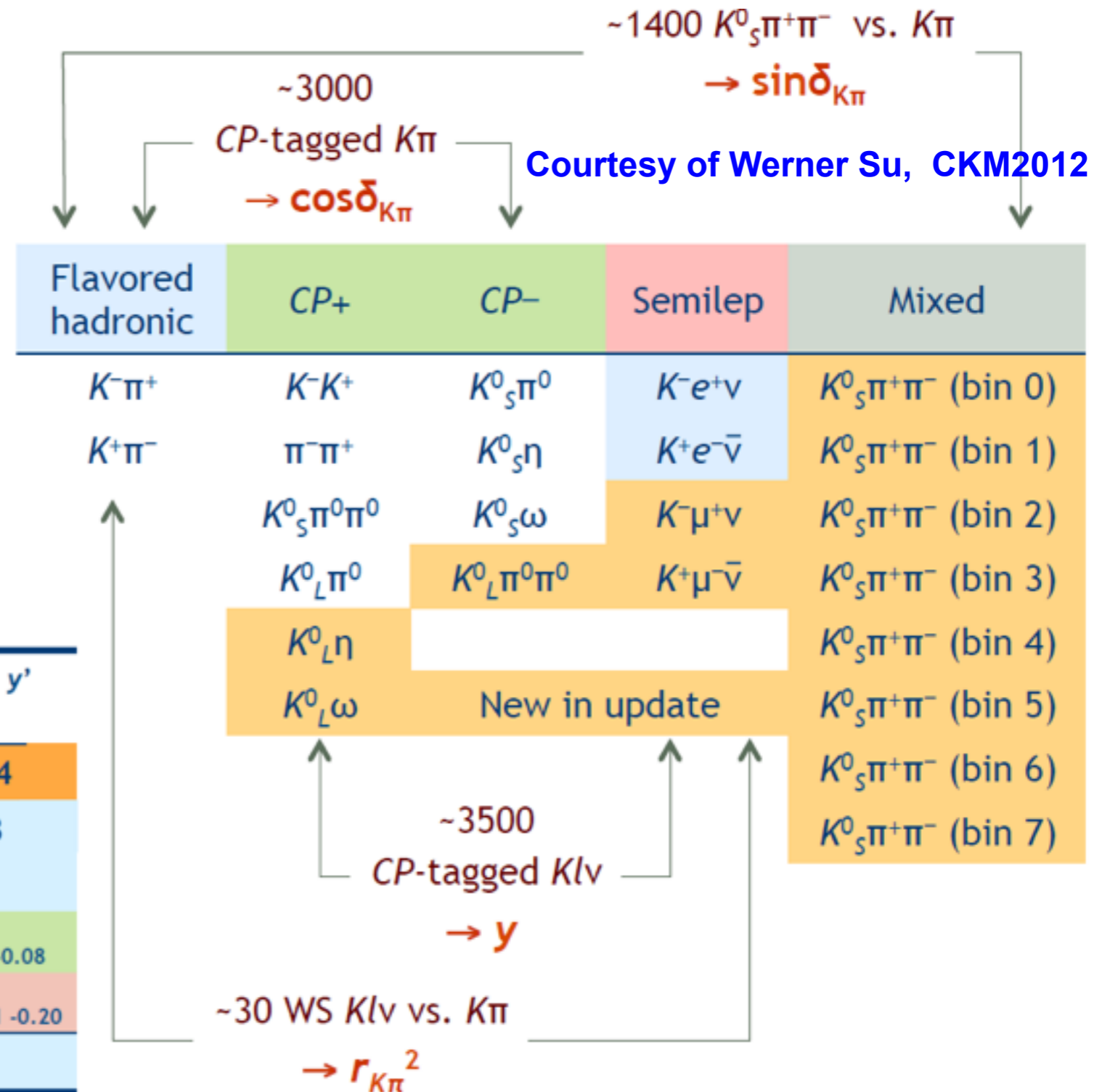
**PRD86, 112001(2012)**

- Updated analysis from the one in 2008:

$$\cos \delta = 1.03^{+0.31}_{-0.17} \pm 0.06$$

[PRL100, 221801 (2008); PRD78, 012001 (2008)]

- Included more modes
  - more ST and DT modes
  - $K_S \pi^+ \pi^-$  strong phase bins [PRD80, 032002 (2008)]
- 251 yield measurements!



Parameter	Fit: no ext. meas. (standard)	Fit: w/ ext. $y, x, y'$ (extended)
$y$ ( $10^{-2}$ )	$4.2 \pm 2.0 \pm 1.0$	<b><math>0.636 \pm 0.114</math></b>
$\chi^2$ ( $10^{-3}$ )	$0.6 \pm 2.3 \pm 1.1$	$0.022 \pm 0.023$
$r_{K\pi}^2$ ( $10^{-3}$ )	$5.33 \pm 1.07 \pm 0.45$	$3.33 \pm 0.08$
$\cos \delta_{K\pi}$	$0.81^{+0.22+0.07}_{-0.18-0.05}$	$1.15^{+0.19+0}_{-0.17-0.08}$
$\sin \delta_{K\pi}$	$-0.01 \pm 0.41 \pm 0.04$	$0.56^{+0.32+0.21}_{-0.31-0.20}$
$\delta_{K\pi}$ ( $^\circ$ ) [derived]	$10^{+28+13}_{-53-0}$	$18^{+11}_{-17}$

# $y_{CP}$ measurement

(BESIII: 2.92 fb<sup>-1</sup>)

We measure the  $y_{CP}$  using  $CP$ -tagged semi-leptonic  $D$  decays, which allows to access  $CP$  asymmetry in mixing and decays.

★ Single tag decay rate (CP tags)

$$\mathcal{B}_{CP\pm} \propto 2|A_{CP\pm}|^2(1 \mp y)$$

★ Double tag decay rates (flavor tags + CP tags)

$$\mathcal{B}_{l;CP\pm} \propto |A_l|^2|A_{CP\pm}|^2$$

★ Neglect term  $y^2$  or high order

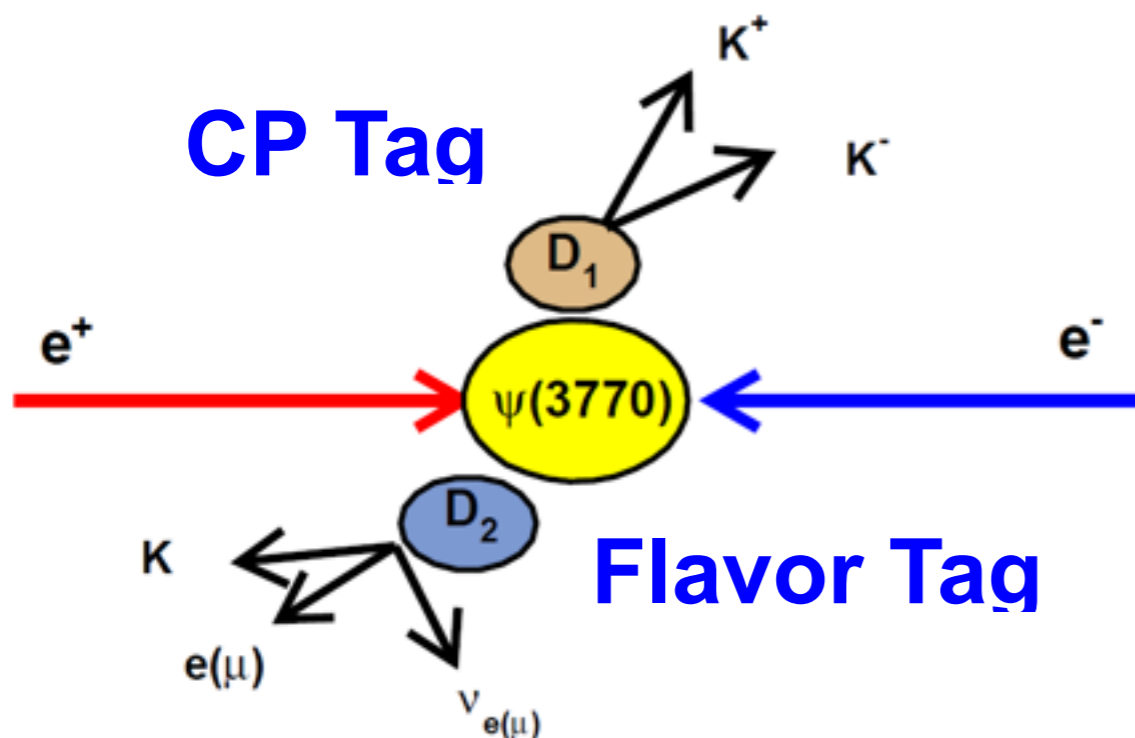
$$y_{CP} = \frac{1}{4} \left( \frac{\mathcal{B}_{l;CP+}\mathcal{B}_{CP-}}{\mathcal{B}_{l;CP-}\mathcal{B}_{CP+}} - \frac{\mathcal{B}_{l;CP-}\mathcal{B}_{CP+}}{\mathcal{B}_{l;CP+}\mathcal{B}_{CP-}} \right)$$

◆ Reconstructed modes:

◆ Flavor tags:  $K e \nu_e, K \mu \nu_\mu$

◆ CP+ tags (3 modes):  $K^-K^+, \pi^+\pi^-, K_S^0\pi^0\pi^0,$

◆ CP- tags (3 modes):  $K_S^0\pi^0, K_S^0\eta, K_S^0\omega$



# signals to determine $y_{CP}$

(BESIII: 2.92 fb<sup>-1</sup>)

## ◆ Single tag yields extraction:

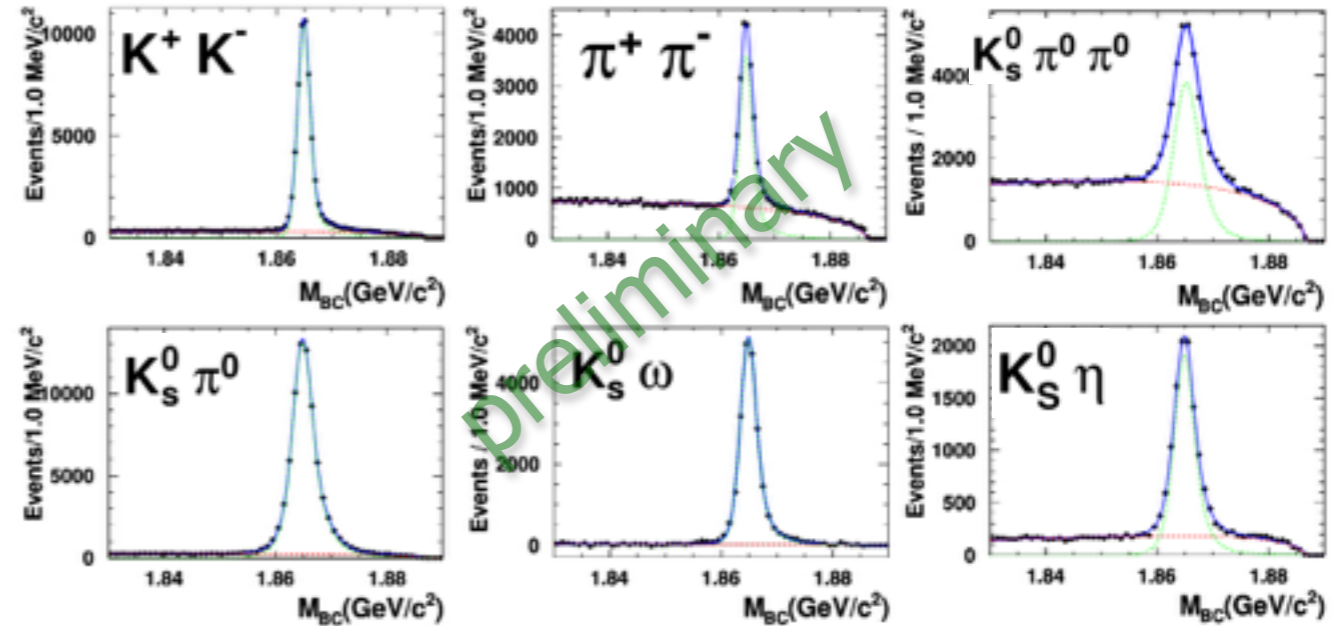
- ◆ Singal shape:  $\sigma \otimes \text{MC-truth}$
- ◆ Background: ARGUS function
- ◆ Kinematic variable:  $M_{BC}$

## ◆ Double tag yields extraction:

- ◆ Singal shape:  $\sigma \otimes \text{MC-truth}$
- ◆ Background: Polynomial
- ◆  $K\pi\pi^0$  background shape from data
- ◆ Kinematic variable:

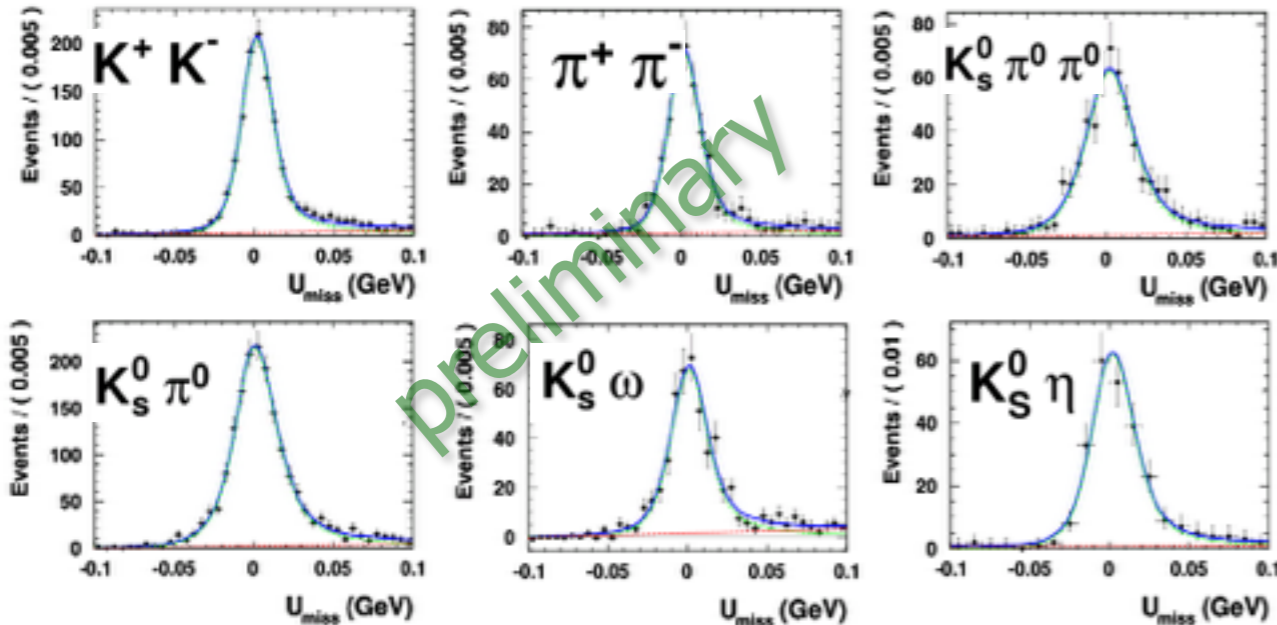
$$U_{\text{miss}} = E_{\text{miss}} - |\vec{P}_{\text{miss}}| \quad (\approx 0 \text{ for signals})$$

### CP STs

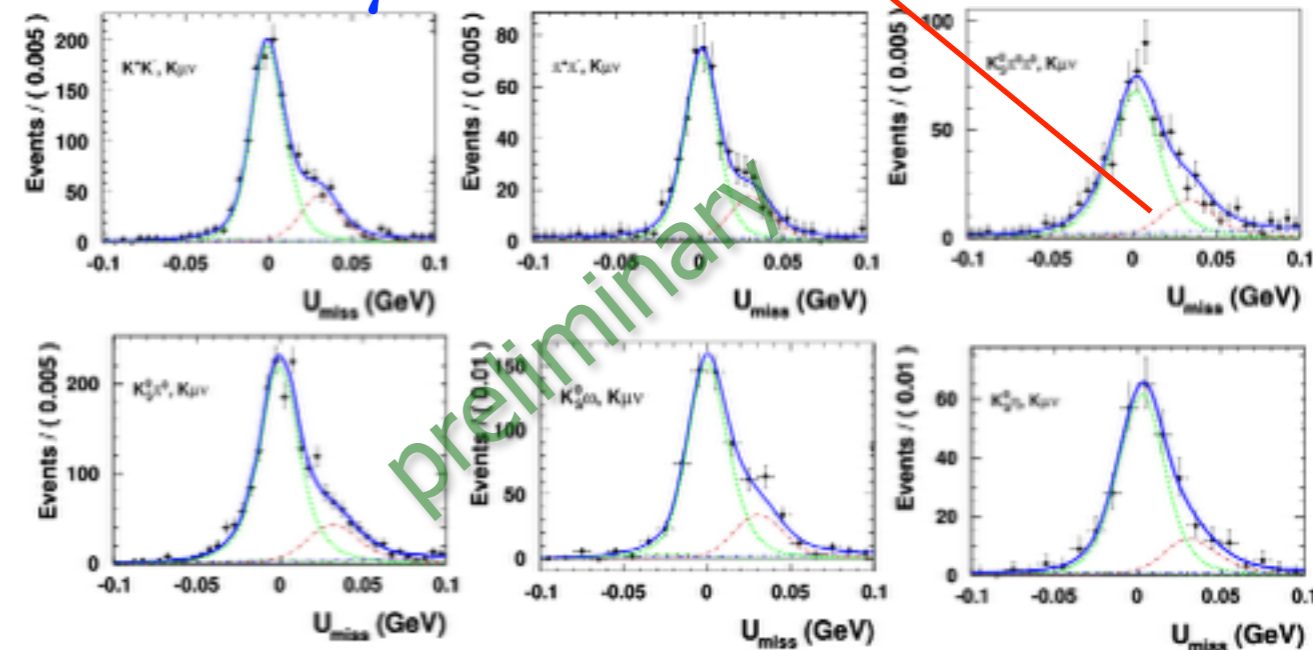


peaking bkg. from  $K\pi\pi^0$

### DTs of $K_{\text{ev}}$ mode



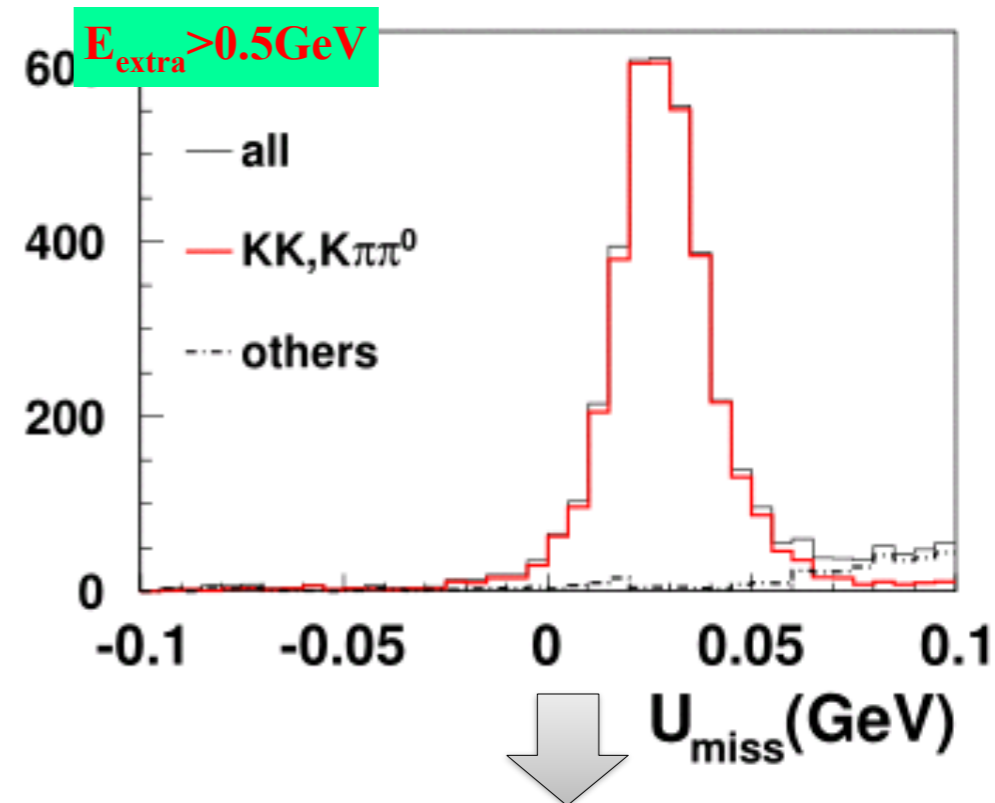
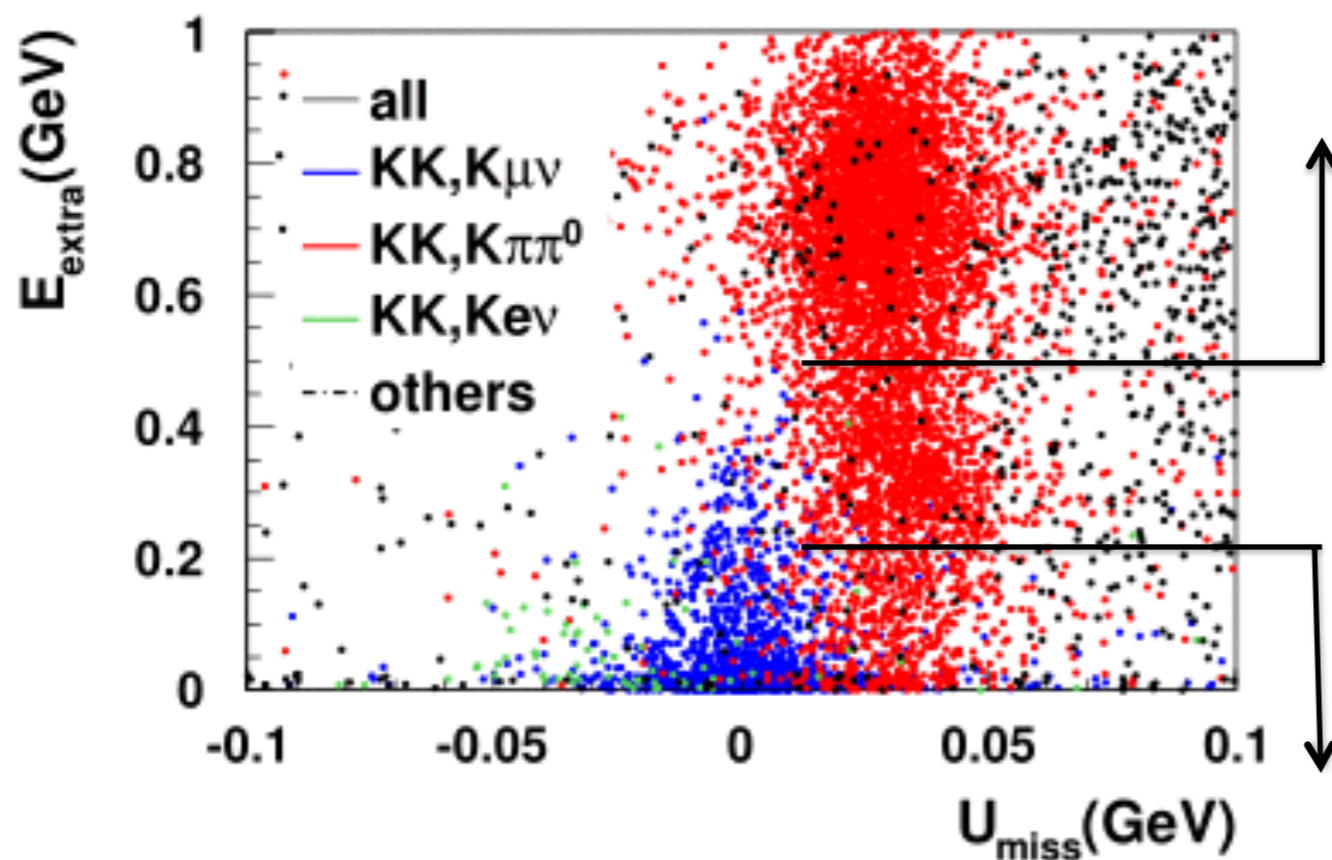
### DTs of $K_{\mu\nu}$ mode



# $K\pi\pi^0$ backgrounds in $K\mu\nu$ modes

define  $E_{\text{extra}}$  as total energy of the remaining showers other than those being used

take  $E_{\text{extra}} > 0.5\text{GeV}$  as control sample to estimate the shape and size of  $K\pi\pi^0$  backgrounds

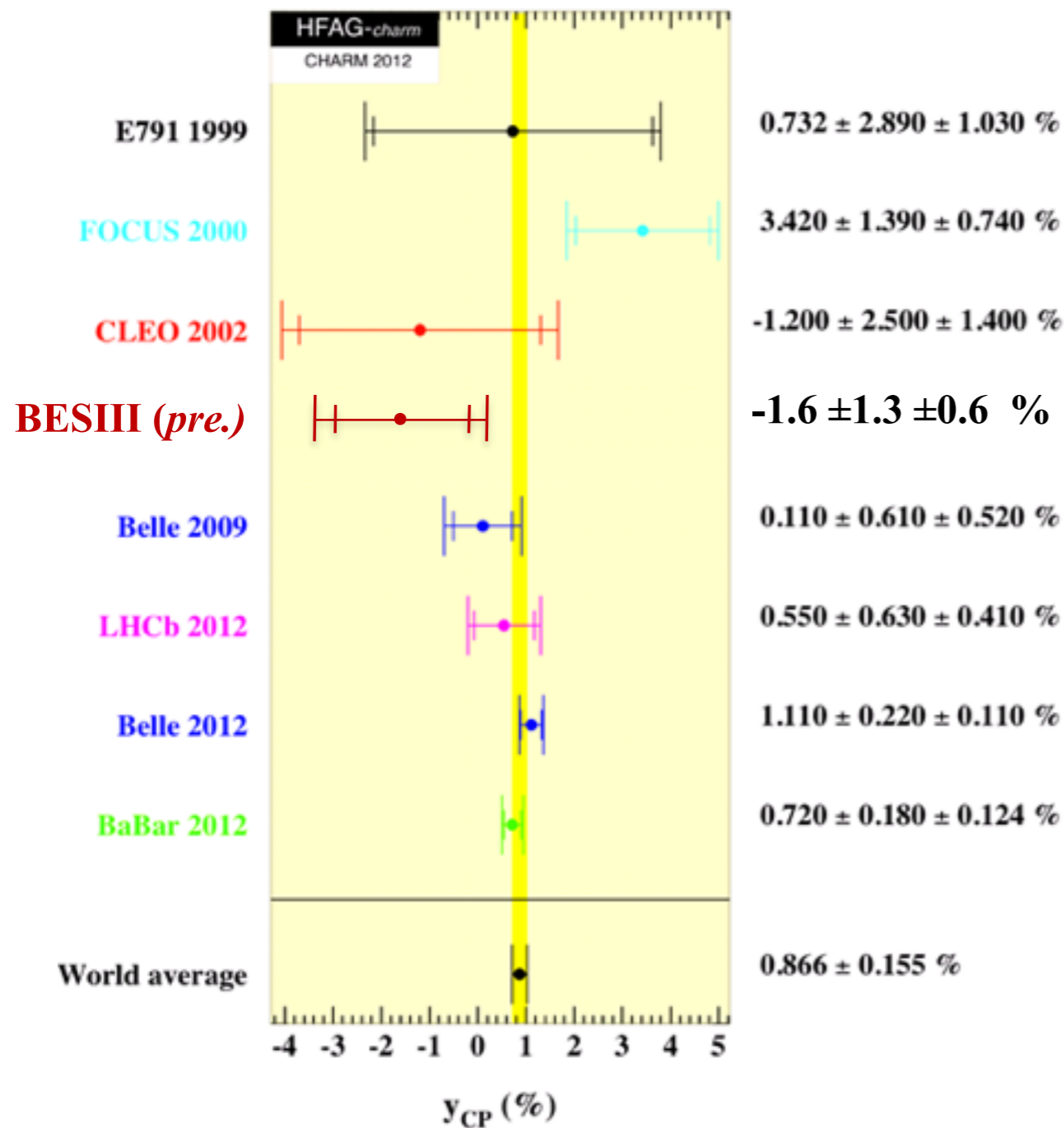


**shape** : MC shape smeared by a Gaussian, whose parameters are obtained from fit to the control sample

**size**: scale the MC-determined size in the signal region with the ratio of the number of  $K\pi\pi^0$  events in data to that in MC in the control sample

# $y_{CP}$ preliminary result

(BESIII: 2.92 fb<sup>-1</sup>)



CLEOc 2012:

[PRD 86 (2012) 112001]

$$y_{CP} = (4.2 \pm 2.0 \pm 1.0)\%$$

## BESIII preliminary result:

$$y_{CP} = -1.6\% \pm 1.3\%(\text{stat.}) \pm 0.6\%(\text{syst.})$$

- result is statistically limited
- systematic uncertainty is relatively small
- most precise measurement with QC D mesons
- in the limit of no CPV,  $y_{CP} = y$

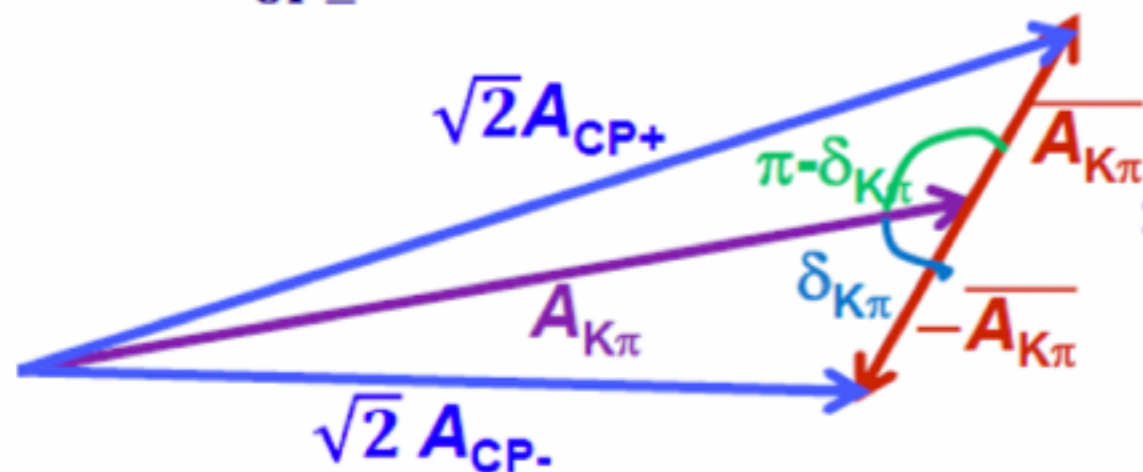
Paper is close to be submitted to journal.

# Strong Phase $\delta_{K\pi}$ (BESIII: 2.92 fb<sup>-1</sup>)

Strong phase:  $\frac{\langle K^- \pi^+ | \bar{D}^0 \rangle^{DCS}}{\langle K^- \pi^+ | D^0 \rangle^{CF}} \equiv -r_{K\pi} e^{-i\delta_{K\pi}}$

Quantum correlation  $\rightarrow$  Interference  $\rightarrow$  access strong phase!

$$\langle K\pi | D_{CP\pm} \rangle = (\langle K\pi | D^0 \rangle \pm \langle K\pi | \bar{D}^0 \rangle) / \sqrt{2} \Rightarrow \sqrt{2} A_{CP\pm} = A_{K\pi} \pm \bar{A}_{K\pi}$$



$$\Rightarrow 2r_{K\pi} \cdot \cos \delta_{K\pi} \approx A_{CP \rightarrow K\pi} \equiv \frac{|A_{CP-}|^2 - |A_{CP+}|^2}{|A_{CP-}|^2 + |A_{CP+}|^2}$$

$$= \frac{Br(D_{CP-} \rightarrow K\pi) - Br(D_{CP+} \rightarrow K\pi)}{Br(D_{CP-} \rightarrow K\pi) + Br(D_{CP+} \rightarrow K\pi)}$$

- ◆ Measuring  $\delta_{K\pi}$  from rate differences if using external  $r_{K\pi}$
- ◆ Reconstructed modes:
  - ◆ Flavor tags:  $K^-\pi^+, K^+\pi^-$
  - ◆ CP+ tags (5 modes):  $K^-K^+, \pi^+\pi^-, K_S^0\pi^0\pi^0, \pi^0\pi^0, \rho^0\pi^0$
  - ◆ CP- tags (3 modes):  $K_S^0\pi^0, K_S^0\eta, K_S^0\omega$

- ◆ Signal reconstruction:
  - ◆ Single Tag (ST): CP tags
  - ◆ Double Tag (DT) :  $K\pi$  + CP Tag
  - ◆ Kinematic variable: Beam Constrained Mass ( $M_{BC}$ )
  - ◆ Singal shape:  $\sigma \otimes$  MC-truth
  - ◆ Background shape: ARGUS function

$$\text{◆ } Br(D_{CP\pm} \rightarrow K\pi) = \frac{n_{K\pi,CP\pm}}{n_{CP\pm}} \cdot \frac{\epsilon_{CP\pm}}{\epsilon_{K\pi,CP\pm}}$$

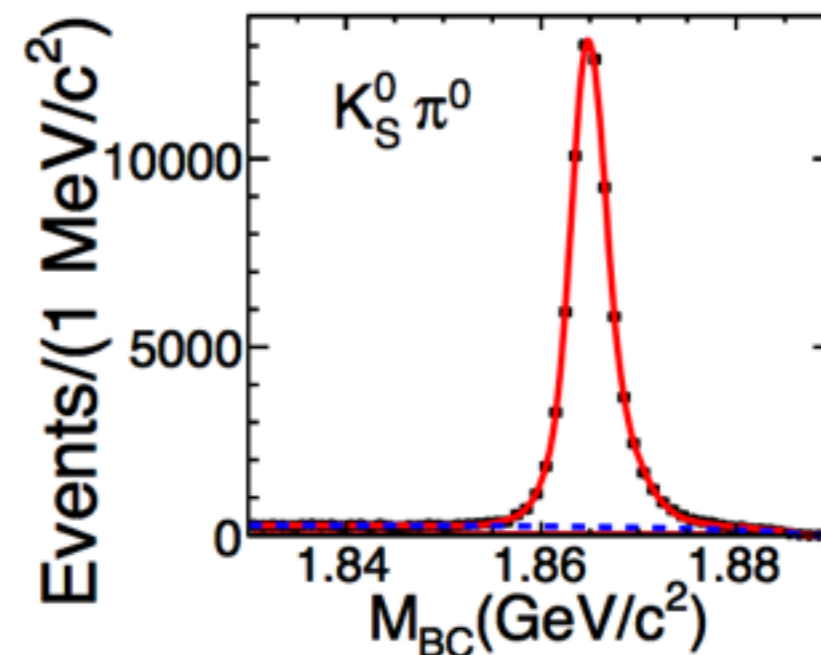
- ◆  $n_{K\pi,CP\pm}$  and  $n_{CP\pm}$  are event yields for DT and ST from  $M_{BC}$  fit
- ◆  $\epsilon_{K\pi,CP\pm}$  and  $\epsilon_{CP\pm}$  are detection efficiencies of DT and ST from MC simulation
- ◆ Most systematics cancelled for ratio  $\epsilon_{CP\pm} / \epsilon_{K\pi,CP\pm}$

## BESIII direct product of results:

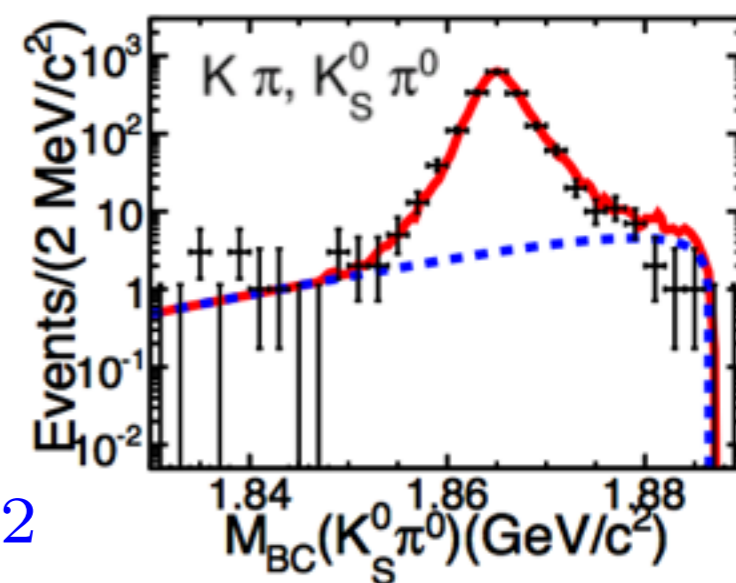
$$A_{CP \rightarrow K\pi} = (12.7 \pm 1.3 \pm 0.7) \times 10^{-2}$$

**Improvement from previous results and inputs for world average fit!**

### Single Tags



### Double Tags





$$\delta_{K\pi} \text{ in } D \rightarrow K\pi$$

◆ If we don't ignore the mixing effect

$$\text{◆ } 2r_{K\pi} \cos \delta_{K\pi} + y = (1 + R_{WS}) \cdot A_{CP \rightarrow K\pi}$$

$$\text{◆ } R_{WS} \equiv \frac{\Gamma(D^0 \rightarrow K^+ \pi^-)}{\Gamma(D^0 \rightarrow K^- \pi^+)} = r_{K\pi}^2 + r_{K\pi} y' + \frac{(x^2 + y^2)}{2}$$

with external inputs from HFAG2014 and PDG:

$$r_{K\pi}^2 = (3.50 \pm 0.04) \times 10^{-3}; \quad y_{CP} = (6.7 \pm 0.9) \times 10^{-3}; \quad R_{WS} = (3.80 \pm 0.05) \times 10^{-3}$$

$$\text{BESIII results: } \cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$$

- The third error is due to the input parameters
- The statistical errors dominant the precision
- World best precision

**CLEO-c results** [*Phys. Rev. D* 86 (2012) 112001]

$$\cos \delta_{K\pi} = 0.81_{-0.18-0.05}^{+0.22+0.07}$$

$$\cos \delta_{K\pi} = 1.15_{-0.17-0.08}^{+0.19+0.00} \quad (\text{globalfit})$$

In the next 5 years, BESIII will in total accumulate about 10 /fb on-threshold  $D$  data:

→ precision of  $\cos \delta_{K\pi}$  will reach  $\sim 0.06$ : level of syst. err.

**CP asymmetry:** 
$$A_{CP}(f) = \frac{\Gamma(f) - \Gamma(\bar{f})}{\Gamma(f) + \Gamma(\bar{f})}$$

★ CPV in charm:

❖ SM:  $\leq$  a few %

❖ NP:  $> \sim 1\%$

★ World precision:  $\sim 0.1\%$

★ CLEO-c measured  $A_{CP}$  based on single tag events

❖ at the order 1% for all modes

❖ no evidence of CPV

❖ systematics dominant

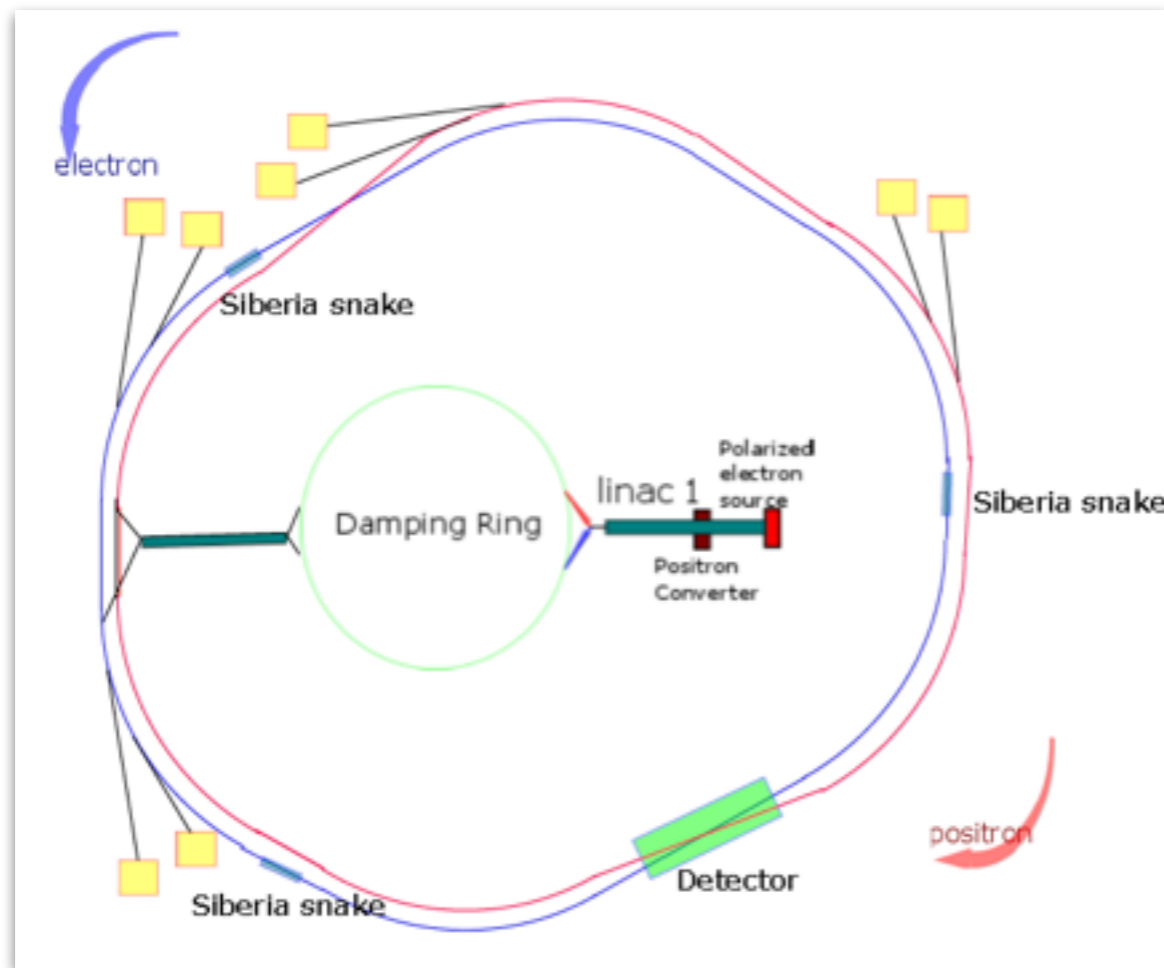
(CLEO-c: 818 pb<sup>-1</sup>)

Mode	CP Asymmetry (%)
$D^0 \rightarrow K^- \pi^+$	$0.3 \pm 0.3 \pm 0.6$
$D^0 \rightarrow K^- \pi^+ \pi^0$	$0.1 \pm 0.3 \pm 0.4$
$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$	$0.2 \pm 0.3 \pm 0.4$
$D^+ \rightarrow K^- \pi^+ \pi^+$	$-0.3 \pm 0.2 \pm 0.4$
$D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0$	$-0.3 \pm 0.6 \pm 0.4$
$D^+ \rightarrow K_S^0 \pi^+$	$-1.1 \pm 0.6 \pm 0.2$
$D^+ \rightarrow K_S^0 \pi^+ \pi^0$	$-0.1 \pm 0.7 \pm 0.2$
$D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-$	$0.0 \pm 1.2 \pm 0.3$
$D^+ \rightarrow K^+ K^- \pi^+$	$-0.1 \pm 0.9 \pm 0.4$

- With the LHCb's updates ( $\sim 0.1\%$ ), CPV test becomes not sensitive in charm factory
- In future charm factory, it is important to reduce the systematic uncertainty by using a large D threshold sample

# High Intensity Electron Positron Accelerator (HIEPA)

- China is proposing a future super-tau-charm factory: HIEPA
- Providing peak luminosity about  $1 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$  at **4 GeV** for physics at **tau charm** sector, covering  $E_{\text{cm}} = 2\text{-}7 \text{ GeV}$ .



by 2016: CDR & TDR

**with  $1 \text{ ab}^{-1}$  data @HIEPA**

- ✓ Direct CP violation in  $D^+ \rightarrow hh$   
sensitivity:  $10^{-3} \sim 10^{-4}$
- ✓  $\Delta(\cos\delta_{K\pi}) \sim 0.007$ ;  $\Delta(\delta_{K\pi}) \sim 2^\circ$
- ✓  $R_M = (x^2 + y^2)/2 \sim 10^{-5}$  in  $K\pi$  and  
Kev channels
- ✓ Probe  $y$ :  $\Delta y_{\text{CP}} < 0.1\%$

clean background and better systematic control in threshold production would be complementary to the future  $B$  factory results

# Summary

- ◆ Data at charm threshold provide unique ingredient on identifying  $D$ - $\underline{D}$  oscillations and CPV in charm sector
- ◆ CLEO-c have made great progress and paved a way for subsequent precision experiment
- ◆ BESIII has been involved in the world campaign
  - ▶ Many more QC analyses are undergoing.
  - ▶ The global fit package has been developed to measure strong phases and mixing parameters.
  - ▶ Precision required more stringent systematic control
- ◆ A super-tau-charm factory in China is being proposed:
  - ◆ Complementary to precision measurements at BELLEII and upgraded LHCb

**International Workshop on Physics  
at Future High Intensity Collider @ 2-7GeV in China**

January 13-16, 2015,  
University of Science and Technology of China (USTC),  
Hefei, Anhui, China

**AIM** to explore possible future collider project post BEPCII/  
BESIII. HIEPA is one of the options.



website: <http://cicpi2011.lcg.ustc.edu.cn/hiepa2015/>  
online registration: Sep. 8 — Dec. 08, 2014

*Thank you!*

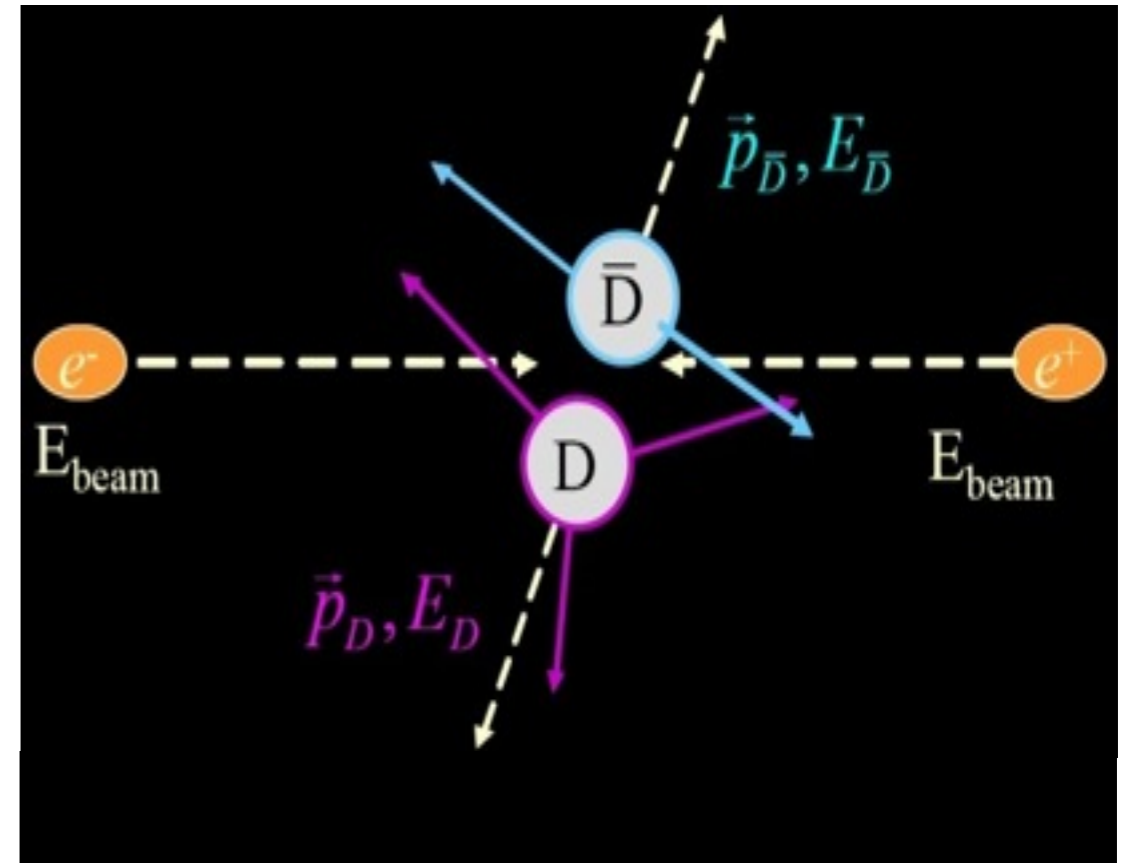
**Danke!**

谢谢!

# Charm tagging at the $\psi(3770)$

$$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$$

- ◆ Pure  $D\bar{D}$  final state, no additional particles ( $E_D = E_{\text{beam}}$ ).
- ◆ Low multiplicity  $\sim 5-6$  charged particles / event
- ◆ More kinematical constraints to reconstruct decay channels with  $\nu$
- ◆ **Single Tag (ST)**
  - ◆ Reconstruct one  $D$  meson
- ◆ **Double Tag (DT)**
  - ◆ Tag one  $D$  meson in a selected *tag mode*. Study the other  $D$  (*signal D*).
- ◆ **Flavor Tag**
  - ◆ Tag the flavor of  $D^0$  or  $\bar{D}^0$
- ◆ **CP tag ( $CP_{\pm}$ )**
  - ◆ Tag the CP eigenstate:  $D_{CP+}$  or  $D_{CP-}$ .



# Toward global fit at BESIII

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- **least squares fitter: used for extracting expected physics parameters from the correlated experimental data**
- **Monte Carlo validation of the fitter**

❖ MC study corresponding to 3.0 /fb data

❖ input parameters:

$$\delta_{K\pi} = 22.1^{+9.7}_{-11.1} (^\circ),$$

$$y_D = 0.75 \pm 0.12(\%)$$

❖ output after constrains :

$$\delta_{K\pi} : \pm 8.3(^\circ), \quad y_D : \pm 0.10(\%)$$

$D$ decay mode	$f^{cor}$
$K^-\pi^+$	$1 + R_{WS}$
$K^+K^-$	2
$K_S\pi^0$	2
$K^-\pi^+, K^+\pi^-$	$(1 + R_{WS})^2 - 4r \cos \delta_{K\pi} (r \cos \delta_{K\pi} + y_D)$
$K^-\pi^+, K^+K^-$	$1 + R_{WS} + 2r \cos \delta_{K\pi} + y_D$
$K^-\pi^+, K_S\pi^0$	$1 + R_{WS} - 2r \cos \delta_{K\pi} - y_D$
$K^-\pi^+, K^+e^-\bar{\nu}_e$	$1 - ry_D \cos \delta_{K\pi} - rx_D \sin \delta_{K\pi}$
$K^+K^-, K_S\pi^0$	4
$K^+K^-, Ke\nu_e$	$2(1 + y_D)$
$K_S\pi^0, Ke\nu_e$	$2(1 - y_D)$

- ~15% improvement on the parameters
- We expect larger improvements on the strong phase and mixing parameters based on 10 /fb data at BESIII