

# Quantum Correlated Charm @ Threshold

*and  $\phi_3 = \gamma$   
from B Decays*

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\*Full disclosure: member of  
CLEO-c / BESIII / BelleII

# Outline

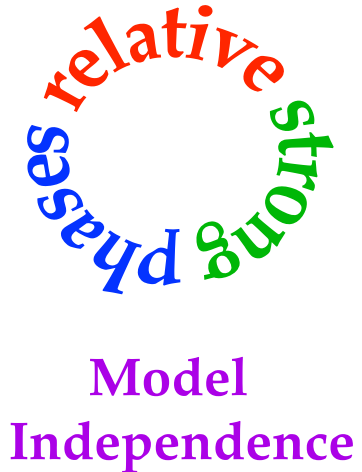
Introduction: Essentials

Overview of Results

Recent Published Results

Preliminary  $K_S \pi^+ \pi^-$  Results

Conclusion



- Access to relative  $D^0, D^{0\text{bar}}$  *strong phase differences*
  - Directly measure what B analyses need with *no models*
  - Useful inputs to *CKM  $\gamma$  extractions w/  $B \rightarrow D^{(*)} K^{(*)}, D^{(*)} \pi$*
  - Also relevant for *D mixing*
- ( *and just plain fun to see EPR-like correlations in HEP experiment! )*

# Introduction

Threshold production of charm with  $e^+e^- \rightarrow \psi$  (3770)

Decays to *coherent* pair of D mesons

$$\psi(3770) \rightarrow [ D^0 \quad D^{0\text{bar}} - D^{0\text{bar}} \quad D^0 ] / \sqrt{2} \quad (\text{Eq 1})$$

$$= - [ D_{\text{CP}^+} \quad D_{\text{CP}^-} - D_{\text{CP}^-} \quad D_{\text{CP}^+} ] / \sqrt{2} \quad (\text{Eq 2})$$

$$D_{\text{CP}^\pm} = [ D^0 \pm D^{0\text{bar}} ] / \sqrt{2}$$

Measure various combination of rates for:

one decay mode only  $\rightarrow$  “single tags”

two decay modes  $\rightarrow$  “double tags”

**Naïve** Get interference with CP tags since they project  
2<sup>nd</sup> meson into a  $D^0, D^{0\text{bar}}$  superposition (Eq 2)

**Truth** Yes, but we get interference even *without* CP tags:  
Terms in Eq 1 already interfere ...  
( 1<sup>st</sup> vs. 2<sup>nd</sup> D means +z vs. -z along decay axis )

# Decay Modes

## Flavored

Flavored semileptonic	$K^-e^+\nu, K^-\mu^+\nu$	Pure CF
Flavored hadronic	$K^-\pi^+, K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$	CF + DCSD

## Self-conjugate

2-body CP eigenstate	$K^-K^+, \pi^+\pi^-, K_S\pi^0, \dots$	SCS
Multi body	$K_S h^+h^-, K_L h^+h^-$	CF + DCSD
Multi body	$K^+K^-\pi^+\pi^-, \pi^+\pi^-\pi^0$	SCS
<b>Neither</b>	$K_S K^-\pi^+$	SCS

## Both

\* not possible \*

Blue modes: already used for  $\gamma$     green : future?    [ black: tag only ]

“h” = K,  $\pi$

CF : Cabibbo-Favored

SCS : Singly-Cabibbo-Suppressed

DCSD : Double-Cabibbo-Suppressed (Decay)

# Multi-Body “Coherence Factors”

**Simplified Two body:**

$$|A_1 + A_2|^2 = |A_1|^2 + |A_2|^2 + 2 A_1 A_2 e^{-i\delta} \quad | \quad 1, 2 = \text{CF, DCSD}$$

**Generalization → Atwood-Soni:**

Integrate over Dalitz plot; define real average amplitudes  
[  $\mathcal{A} \rightarrow A$  below ]

BUT this requires a “fudge factor” of  $\text{Re}^{-i\delta}$  for interference term

**Simplified Multi body:**

$$\int d \text{Dalitz} | \mathcal{A}_1 + \mathcal{A}_2 |^2 = | A_1 |^2 + | A_2 |^2 + 2 R e^{-i\delta} A_1 A_2 |$$

Define:  $R e^{-i\delta} = (\text{true cross-term}) / (\text{naïve} = A_1 A_2)$

Note:  $R < 1$  due to two reasons: varying phase & “ $|r(x)| \neq 1$ ”

$$A_{K^\pm \pi^\mp \pi^0}^2 = \int | \mathcal{A}_{K^\pm \pi^\mp \pi^0}(\mathbf{x}) |^2 d\mathbf{x}$$

$$R_{K\pi\pi^0} e^{-i\delta_D^{K\pi\pi^0}} = \frac{\int \mathcal{A}_{K^- \pi^+ \pi^0}(\mathbf{x}) \mathcal{A}_{K^+ \pi^- \pi^0}(\mathbf{x}) d\mathbf{x}}{A_{K^- \pi^+ \pi^0} A_{K^+ \pi^- \pi^0}}$$

# QC for Pedestrians I

## Simplest effect:

$$\psi(3770) \rightarrow [ D_{CP+} D_{CP-} - D_{CP-} D_{CP+} ] / \sqrt{2}$$

*Like CP* (++, --): cancels      *Unlike CP* (+-, -+): doubled

## My favorite general form:

\* Ignore mixing for now \*

$$\Gamma_{FG} / A_F^2 A_G^2 = [ r_F^2 + r_G^2 + 2 r_F r_G R_F R_G \cos(\delta_G - \delta_F) ]$$

or  $1 + r_F^2 r_G^2 + \dots$ : factor out  $A_i$  such that  $r < 1$

→  $r_{F,G}$  (averaged) amplitude ratios:  $\sim A(D^{0\text{bar}} \rightarrow F,G) / A(D^0 \rightarrow F,G)$

1 for CP eigenstates

$\sim \tan^2(\theta_C)$  for hadronic  $K^-$  modes [ DCSD/CF ]

0 for semileptonic → no interference

→  $R, \delta$ : Atwood-Soni coherence factors

$R=1; \delta = 0, \pi$  for CP eigenstates;

$R=1; \delta = ?$  for  $K^- \pi^+$

**Both non-trivial** for multi-body hadronic

# QC for Pedestrians II

**Need some double-tag rate with two “non-trivial” modes to fully separate parameters**

→ If not, get only  $\text{Re}[R e^{-i\delta}] = R \cos \delta$ , not separate  $(R, \delta)$   
[ Or, only  $c_i$ , not both  $c_i, s_i$  ]

**The reason this works is simple trigonometry:**

$$\cos(\delta_2 - \delta_1) = \cos\delta_1 \cos\delta_2 - \sin\delta_1 \sin\delta_2$$

With this, one has enough observables to separate  
( & can still use modes where one  $\delta_i = 0$  )

**Two “non-trivial” modes ?**

- Can be different values of  $n$  in  $K^-(n\pi)^+$  analyses
- Can even be different bins (i) in  $K_S \pi^+ \pi^- c_i, s_i$  analyses

# From Tags to Physics

## CP+ & CP- tags:

Switch of +- flips sign of interference term

Used for  $\gamma$ , but trivial: no need to study w/ charm [GLW]

## Semileptonic flavor tags:

No interference; clean normalization [ but pesky v... ]

## Hadronic flavor tags:

Normalization, modulo DCSD [ easier than semilep for exp. ]

Also modes we want to study [ADS]

## Multi-body self-conjugate

Modes we want to under study [GGSZ]

## Different analyses use different numbers of tag modes

CLEO  $K^-\pi^+$  & CLEO-c, BESIII  $K_S\pi^+\pi^-$  use *many* tags

BESIII  $K^-\pi^+$  uses only signal and CP tags



# Experimental Output

$K^-K^+, \pi^+\pi^-$	GLW	$\delta = 0, \pi$	
$K^- \pi^+$	ADS	$\delta$ (R=1)	get from threshold charm...
$K^- \pi^+ \pi^0, K^- \pi^+ \pi^+ \pi^-, K_S K^- \pi^+$	ADS+	R, $\delta$	
$K_S \pi^+ \pi^-, K_S K^+ K^-$	GGSZ	$c_i, s_i$	

$R, \delta$  are Atwood-Soni coherence factors for ADS modes

→ *No relative  $D^0$ - $D^{0\text{bar}}$  phase* in separate  $D^0, D^{0\text{bar}}$  Dalitz fits

e.g., if one fits N amplitudes to  $D^0, D^{0\text{bar}}$  separately: [  $D^*$ -tagged @ B factory ]  
only gets  $2(N-1) = 2N-2$  out of  $2N-1$  relative phases

→ Also *avoid Dalitz models*

$c_i, s_i$  are “Cartesian R,  $\delta$  in Dalitz bins” for GGSZ modes

→ Here, relative  $D^0$ - $D^{0\text{bar}}$  phase is trivial

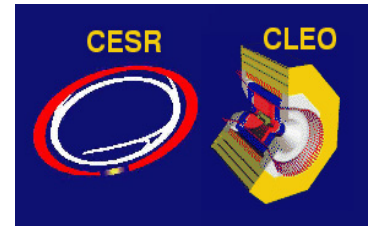
( distinction due to self-conjugate modes, not changing basis to  $c_i, s_i$  ! )

→ But we still *avoid Dalitz models*

# CLEO-c Results

**CLEO-c Data :** 0.8 fb<sup>-1</sup> @  $\Psi(3770)$  & 0.6 fb<sup>-1</sup> @ 4170 MeV 2003 - 08

$K^-\pi^+$	281 pb <sup>-1</sup> ( updated below )	PRL 100, 221801 (2008); PRD, 78, 012001 (2008) [= more details ]	
$K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$	818 pb <sup>-1</sup>	PRD 80, 031105(R) (2009)	
$K_S\pi^+\pi^-$	818 pb <sup>-1</sup>	PRD 80, 032002 (2009)	
$K_{S,L}h^+h^-$	818 pb <sup>-1</sup>	PRD 82, 112006 (2010)	
$K_S K^+\pi^-$	818 pb <sup>-1</sup> *	PRD 85, 092016 (2012)	
$K^-\pi^+$	→ 818 pb <sup>-1</sup>	PRD 86, 112001 (2012)	
$K^+K^-\pi^+\pi^-$	818 pb <sup>-1</sup> **	PRD 85, 122002 (2012)	{ isobar analysis; but <i>first</i> $D, D^{\text{bar}}$



also use high-E continuum { \* + 15 fb<sup>-1</sup> ~10 GeV  
\*\* + 24 fb<sup>-1</sup> ~10 GeV & 600 pb<sup>-1</sup> 4.17 GeV

# Today's Main Topics

## BESIII Results

**Dataset :**  $2.92 \text{ fb}^{-1}$  2010 - 11 ( 1  $\frac{2}{3}$  years )  $\rightarrow$  3.5x CLEO-c  
**Future ability :**  $\sim 4 \text{ fb}^{-1}$  / running year [ note:  $\mathcal{L}_{2011} \gg \mathcal{L}_{2010}$  ]

The logo for BESIII, featuring the letters 'B', 'E', 'S', and 'III' in a stylized font. 'B' is blue, 'E' is red, 'S' is green, and 'III' is black.

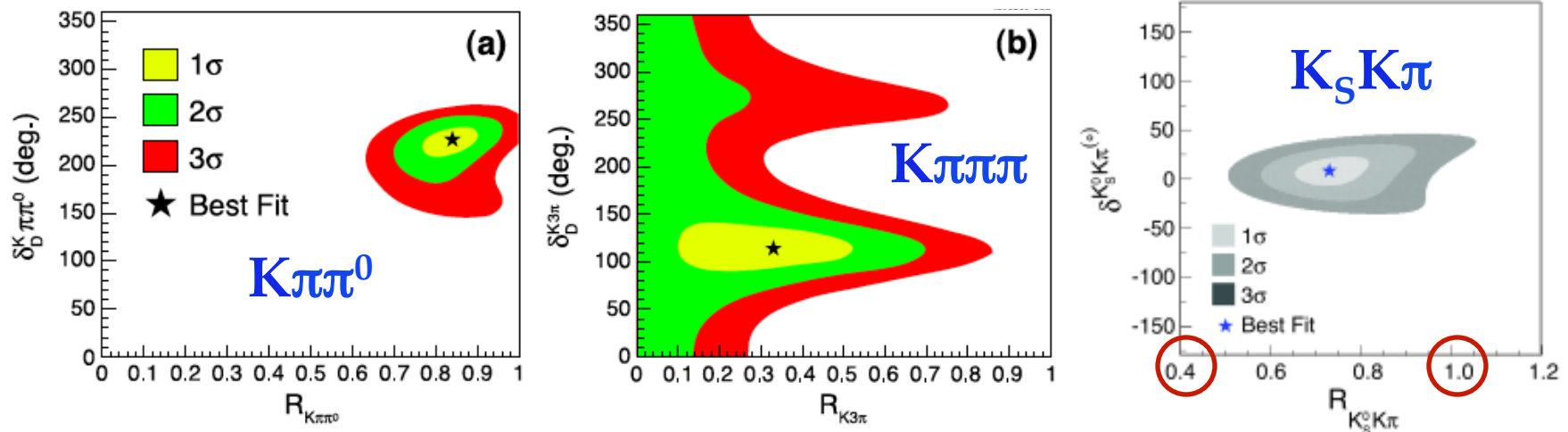
$K^-\pi^+$	$2.92 \text{ fb}^{-1}$	PLB 734, 227 (2014)
$K_S^0\pi^+\pi^-$	$2.92 \text{ fb}^{-1}$	Preliminary @ APS, Apr 2014
$Y_{CP}$	$2.92 \text{ fb}^{-1}$	Preliminary; will submit soon

[  $Y_{CP}$  : see slides by X.R. Lyu; talk running in parallel now ! ]

## CLEO-c "Legacy" Result

$K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$   $818 \text{ pb}^{-1}$  PLB 731, 197 (2014)  
[ CLEO-c data analyzed by past members, after collaboration disbanded ]

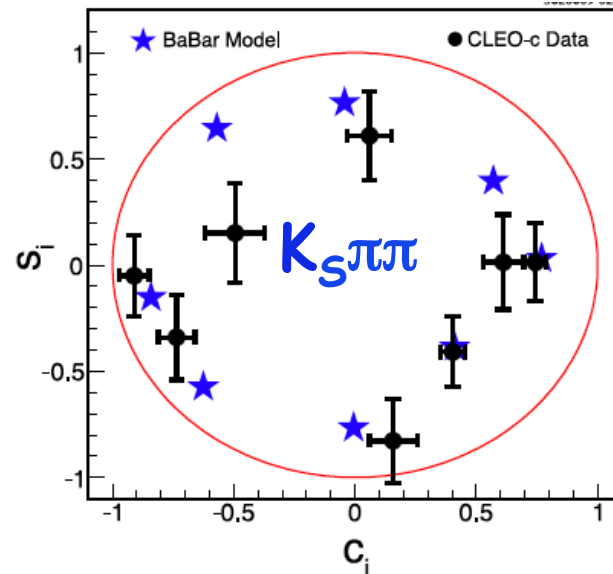
# CLEO-c Coherence Factors



*Small R for  $K\pi\pi$ : still useful for  $r_B$  !*

Or, we could bin across Dalitz plot

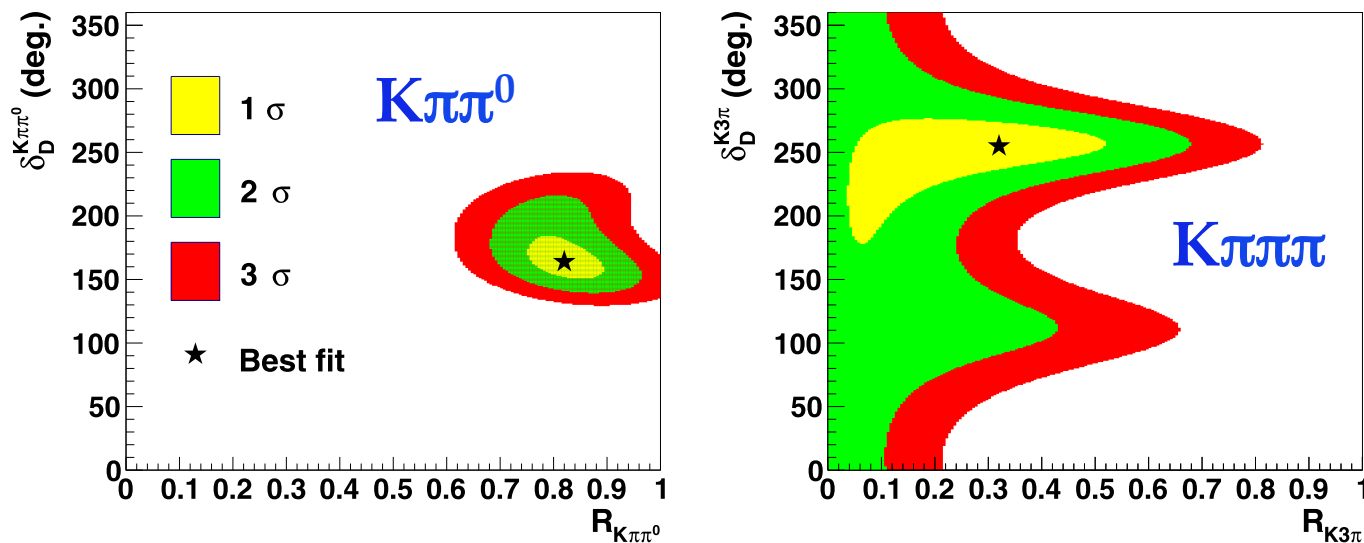
$c_i$  and  $s_i$ : bin-averaged  
 $\langle R \cos \delta \rangle$  and  $\langle R \sin \delta \rangle$



# $K^- (n\pi)^+$ Update

PLB 731, 197  
(2014) 818 pb<sup>-1</sup>

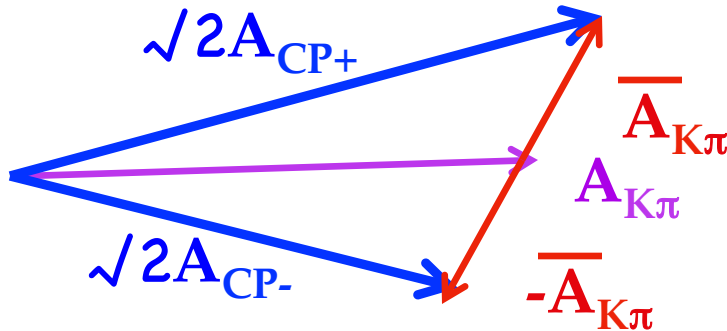
CLEO-c “Legacy data” publication  $\rightarrow$  not a collaboration result  
( but I personally believe it to be of equal quality )



Note:  
 $K\pi\pi\pi$  best fit  
now in other  
lobe...

- $\rightarrow$  Now includes  $K_S\pi^+\pi^-$  tags
- $\rightarrow$  Updated external inputs (BF, mixing,  $K\pi$ )

Simplified Picture: ( simple = no mixing )



Amplitude triangle:

$$CP_{\pm} = CF \pm DCSD$$

[ DCSD enhanced for visibility ! ]

Complex ratio  
DCSD/CF amplitude

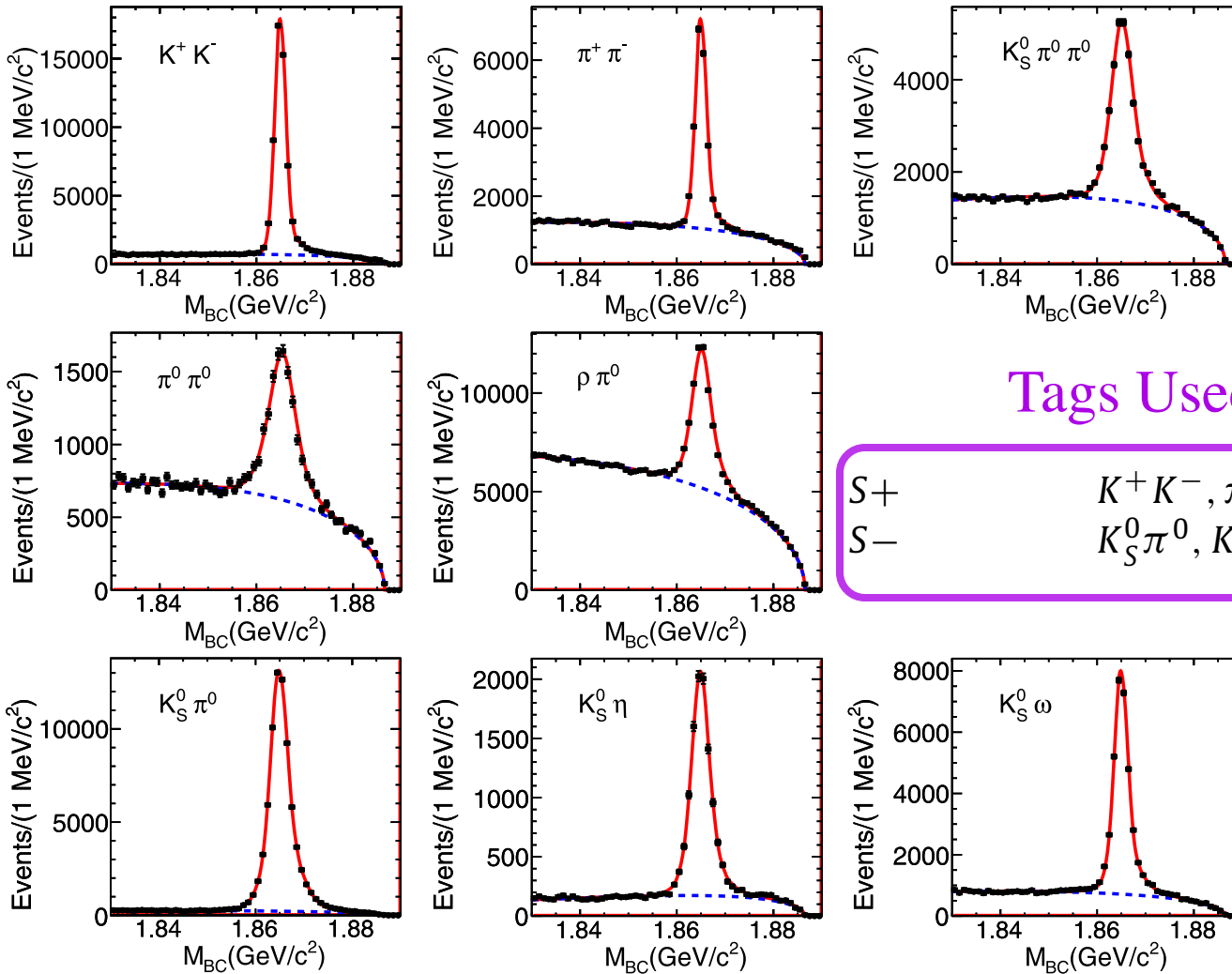
$$\frac{\langle K^- \pi^+ | \overline{D}^0 \rangle}{\langle K^- \pi^+ | D^0 \rangle} = -r e^{-i\delta_{K\pi}}$$

Flip CP of tag: reverses interference term

*CP-tagged rate asymmetry (essentially) measures  $r \cos \delta$*

$$\begin{aligned} \mathcal{A}_{CP} &= [ |A_{CP-}|^2 - |A_{CP+}|^2 ] / [ |A_{CP-}|^2 + |A_{CP+}|^2 ] && \leftarrow \text{measure} \\ &= r \cos \delta \quad (+ D \text{ mixing corrections: } y, R_{WS}) && \leftarrow \text{extract} \end{aligned}$$

## First BESIII Quantum Coherence result : *straightforward analysis*



Tags Used: 5 CP+, 3 CP-

$S+$	$K^+K^-, \pi^+\pi^-, K_S^0\pi^0\pi^0, \pi^0\pi^0, \rho^0\pi^0$
$S-$	$K_S^0\pi^0, K_S^0\eta, K_S^0\omega$

$$\mathcal{A}_{K\pi}^{CP} \equiv \frac{\mathcal{B}_{D^{S-} \rightarrow K^- \pi^+} - \mathcal{B}_{D^{S+} \rightarrow K^- \pi^+}}{\mathcal{B}_{D^{S-} \rightarrow K^- \pi^+} + \mathcal{B}_{D^{S+} \rightarrow K^- \pi^+}}$$

$S+$  ( $S-$ ) denotes the  $CP$ -even ( $CP$ -odd) eigenstate.

**Direct result : \***

$$\mathcal{A}_{CP} = (12.7 \pm 1.3 \pm 0.7)\%$$

$$2r \cos \delta_{K\pi} + y = (1 + R_{WS}) \cdot \mathcal{A}_{K\pi}^{CP}$$

Using external inputs for  $r_{K\pi}$ ,  $R_{WS}$ ,  $y$ , we extract :

$$\cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$$

Compare to CLEO-c:

$$\cos \delta_{K\pi} = 0.81^{+0.22}_{-0.18} {}^{+0.07}_{-0.06} \quad (\text{no external inputs})$$

$$\cos \delta_{K\pi} = 1.15^{+0.19}_{-0.17} {}^{+0.00}_{-0.08} \quad (\text{w/ external inputs})$$

\* HFAG can use this, I believe: they now omit final  $\delta_{K\pi}$  due to external inputs ...



**Classic “GGSZ mode”;** better precision than CLEO-c  
*Preliminary results presented @ APS meeting, Apr 2014*

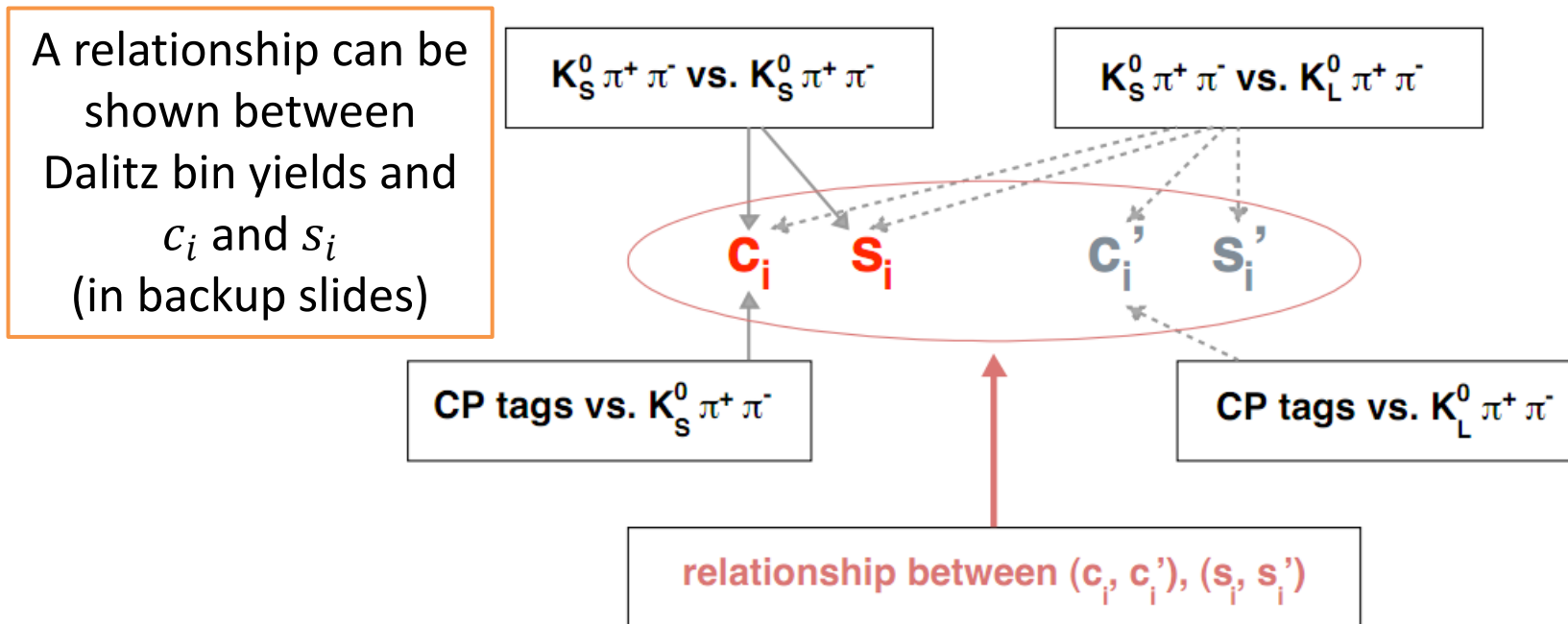
$K_S\pi^+\pi^-$  is the main topic: extract  $c_i, s_i$   
 $K_L\pi^+\pi^-$  is also used: extract  $c'_i, s'_i$   
relate to  $c_i, s_i$  with model corrections.

Aggressive use of tags, including partial reconstruction

*All results preliminary; as presented at April 2014 AP meeting*

# New $K_S \pi^+ \pi^-$ Results

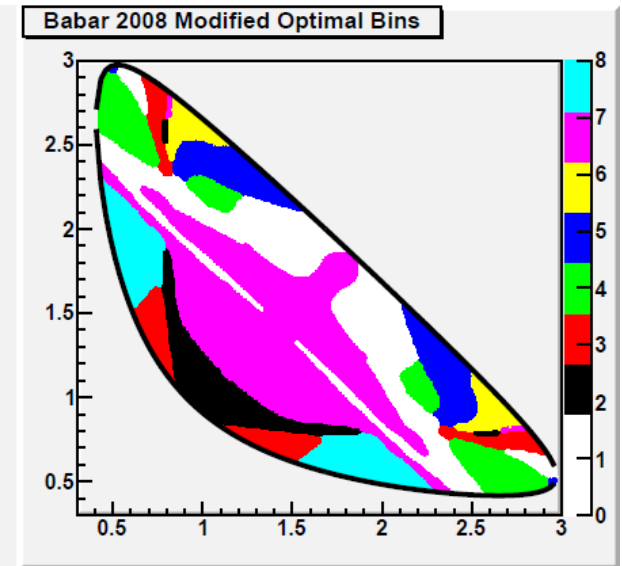
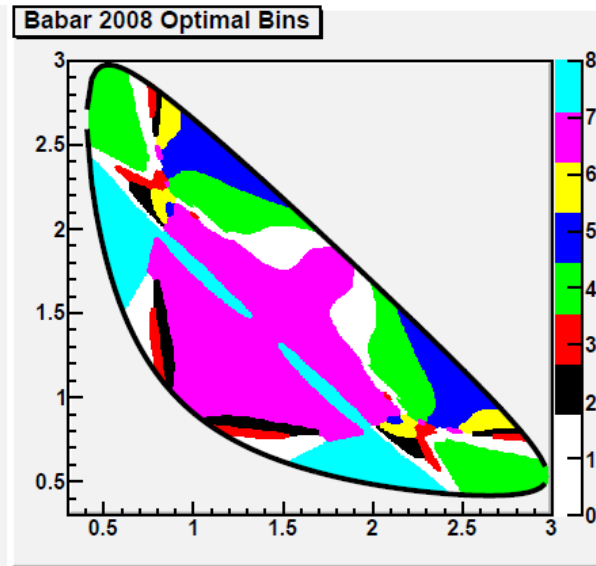
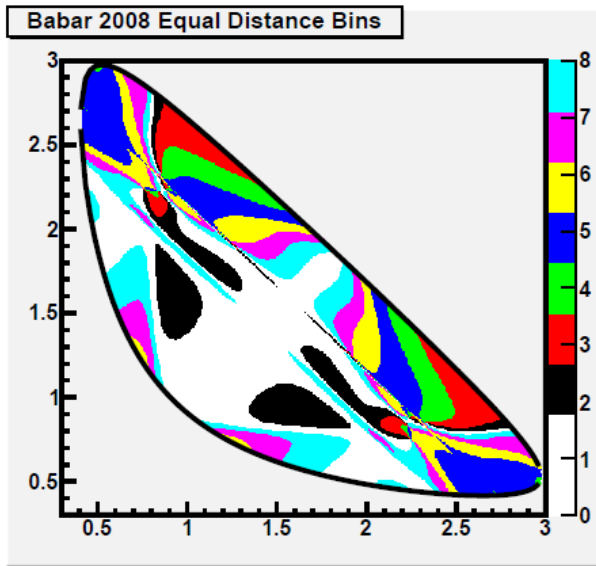
We can calculate  $c_i$  and  $s_i$  from double tags of  $D^0 \rightarrow K_S \pi^+ \pi^-$  vs  $D^0 \rightarrow (K_{S,L} \pi^+ \pi^-$  or CP eigenstates)



Only  $c_i, s_i$  from  $K_S \pi^+ \pi^-$  is used to calculate  $\gamma$ .

However adding in  $D^0 \rightarrow K_L \pi^+ \pi^-$  we can calculate  $c'_i, s'_i$  and use how they relate to  $c_i, s_i$  to further constrain our results in a Global fit.

Slide from Dan Ambrose, APS 2014



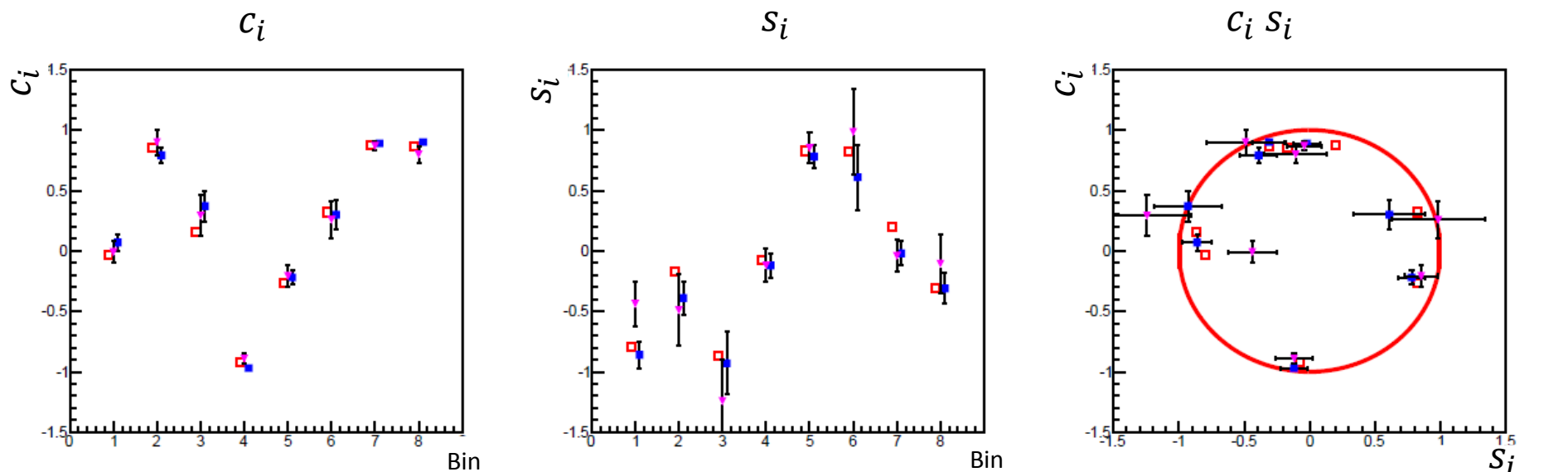
Result of splitting the Dalitz phase space into 8 equally spaced phase bins based on the BaBar 2008 Model.

Starting with the equally spaced bins, bins are adjusted to optimize the sensitivity to  $\gamma$ . A secondary adjustment smooths binned areas smaller than detector resolution.

Similar to the “optimal binning” except the expected background is taken into account before optimizing for  $\gamma$  sensitivity.

Source: CLEO Collaboration, *Physical Review D*, vol 82., pp. 112006 - 112035

Slide from Dan Ambrose, APS 2014



Bins	$C_i$		$S_i$	
	BES-III	CLEO-c	BES-III	CLEO-c
1	$0.066 \pm 0.066$	$-0.009 \pm 0.088$	$-0.843 \pm 0.119$	$-0.438 \pm 0.184$
2	$0.796 \pm 0.061$	$0.900 \pm 0.106$	$-0.357 \pm 0.148$	$-0.490 \pm 0.295$
3	$0.361 \pm 0.125$	$0.292 \pm 0.168$	$-0.962 \pm 0.258$	$-1.243 \pm 0.341$
4	$-0.985 \pm 0.017$	$-0.890 \pm 0.041$	$-0.090 \pm 0.093$	$-0.119 \pm 0.141$
5	$-0.278 \pm 0.056$	$-0.208 \pm 0.085$	$0.778 \pm 0.092$	$0.853 \pm 0.123$
6	$0.267 \pm 0.119$	$0.258 \pm 0.155$	$0.635 \pm 0.293$	$0.984 \pm 0.357$
7	$0.902 \pm 0.017$	$0.869 \pm 0.034$	$-0.018 \pm 0.103$	$-0.041 \pm 0.132$
8	$0.888 \pm 0.036$	$0.798 \pm 0.070$	$-0.301 \pm 0.140$	$-0.107 \pm 0.240$

\*\*\*Only statistical uncertainty is listed

BES III  
Preliminary

□ Model prediction  
● BES III  
▼ CLEO-c

Consistent agreement with CLEO-c measurements.

Source: CLEO Collaboration, Physical Review D, vol 82., pp. 112006 - 112035

Improved errors w.r.t. CLEO-c

Slide from Dan Ambrose, APS 2014

# My Selected Issues

BaBar  $K\pi\pi^0$  mixing result uses an isobar fit; gets rotated  $x''$ ,  $y''$   
Can't this be done in a model-independent way, using charm  
threshold data if needed ??? ( "Atwood-Soni for mixing" )

Efficiencies vary across D Dalitz plots

Charm and B factories differ; traffic in corrected variables

Current methods accurate ? Need Dalitz models to do well ?

Are studies of D mixing, D CPV,  $K_S$  CPV effects complete?

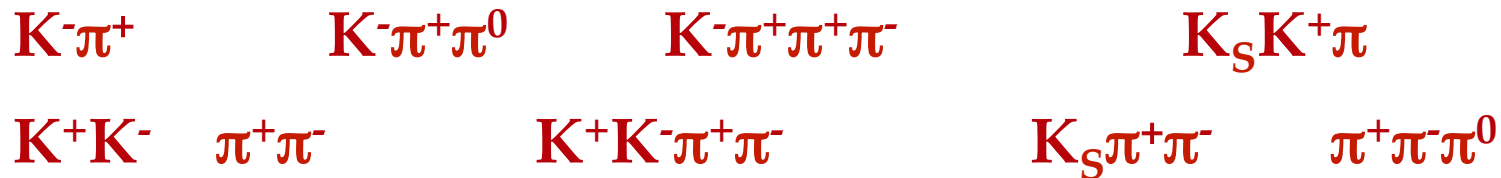
Assumptions of SM re: CPV could be more explicit

e.g., GGSZ assumes no weak phase between CF & DCSD ( I think! )

**Maintain a lively  $D \leftrightarrow B$  interchange & forge ahead !**

# Everything is a Special Case ! ( almost )

so if you were confused, you're probably not alone...



$K^-\pi^+$  only  $\delta$  ;  $K^-\pi^+\pi^0$ ,  $K^-\pi^+\pi^+\pi^-$  have both R &  $\delta$

Multi-body Self-conjugate modes:

If no CPV, only  $2(n-1)$  isobar phases, not  $2n-1$   
 threshold data only to avoid model dependence;  
 no “essential”  $D^0$ - $D^{0\text{bar}}$  phase

4-body: more complicated angular momenta than 3-body

$K_S$  modes: CF and DCSD give  $K^0$ ,  $K^{0\text{bar}}$ , not  $K_S$  directly



# Extracting CKM $\gamma$

without charm



with charm



# Conclusions

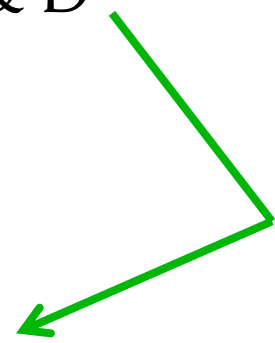
## Unique access to strong phases & ability to extract model-independent results with charm at threshold

- Started with many CLEO-c Results
- Still some activity with CLEO-c “legacy data” [  $\geq 1$  more paper? ]
- Now, the 3.5x larger BESIII dataset is producing results

## Interest of B physics users remains high

- LHCb is a huge addition to older B-factory data
- But  $e^+e^-$  will return soon with BelleII
- Important to keep active interaction between B & D

## Future prospects are bright

- More precision, new modes, new variables !
  - Need to maintain threshold analysis manpower
- 



# Selected Theory References

## Quantum Correlations

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## $D^0$ Mixing with $K_S K \pi$

- Malde & Wilkinson, Phys. Lett. B701, 353 (2011)

# Selected Theory References

## **“Attention PDG” : $K_S \neq 1/2$ of $K^0$ or $K^{0\text{bar}}$**

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## **D mixing and CKM $\gamma$ from $K_S\pi\pi$**

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## **D Direct CPV and CKM $\gamma$ from $B \rightarrow DK$**

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Wang, Phys. Rev. Lett. 110, 061802 (2013)

## **CPV in $K_S$ & CKM $\gamma$**

Grossman & Savastio, JHEP 03, 008 (2014)

## **$K_S$ decay time acceptance and CPV in tau, D**

Bigi & Sanda, Phys. Lett. B 625, 47 (2005)

Grossman & Nir, JHEP 04, 002 (2012)

## **$K_S$ detector interactions & B, D CPV**

Ko, Won, Golob, Pakhlov, Phys. Rev. D 84, 111501(R) (2011)