

Lessons learnt from aligning the CMS Silicon Tracker

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Overview

CMS Experiment at the LHC

- CMS detector

- CMS Silicon Tracker

CMS Tracker alignment challenge

- Track based alignment

Tracker alignment in CMS during LHC Run I

- Treatment of surface deformations

- Large Structure movements and prompt calibration

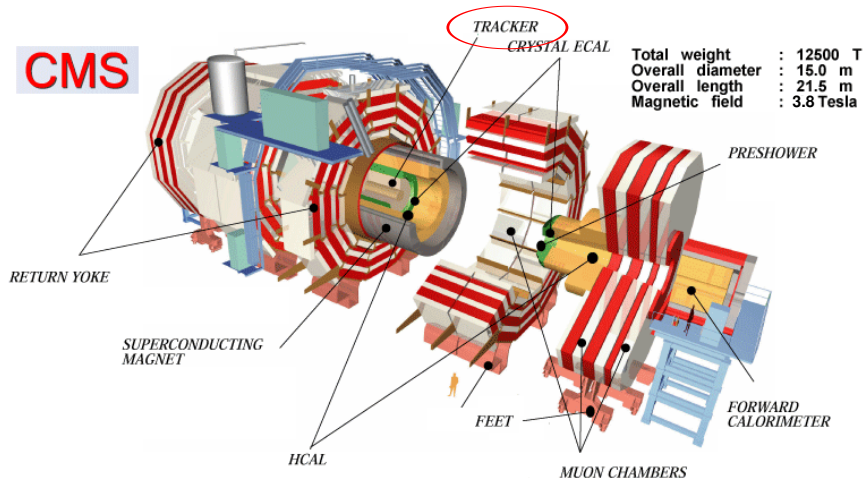
- Treatment of weak modes

- Getting rid of the ϕ -dependent curvature bias

- Lorentz Angle calibration in the alignment framework

Summary

The CMS Detector at the LHC



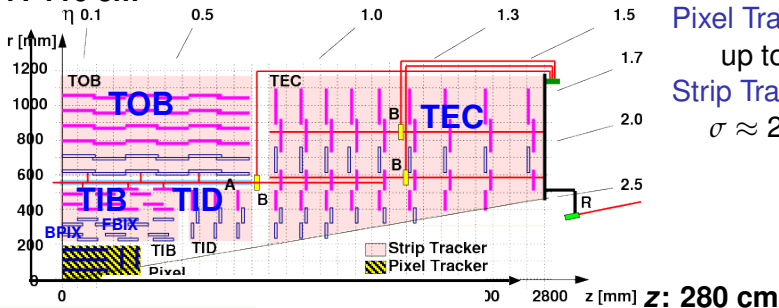
Features of the CMS Detector

- ▶ Large Solenoid: $B = 3.8$ T.
- ▶ All Silicon Inner Tracker.

The CMS Tracker: All Silicon

***rz*-view (upper right quarter)**

***r*: 110 cm**



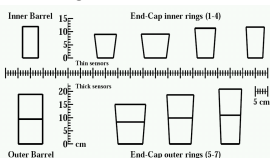
Single Hit Resolution

Pixel Tracker:

up to $\sigma = 9 \mu\text{m}$

Strip Tracker:

$\sigma \approx 20 - 60 \mu\text{m}$



**TOB and outer TEC:
two chained sensors**

- ▶ 1440 silicon pixel modules
- ▶ 15148 silicon strip modules (24244 sens.)
- ▶ Strips generally measure $r-\phi$ direction
- ▶ Some radii: additional modules rotated by 100 mrad

Alignment challenge: $\mathcal{O}(100k)$ parameters!

Why alignment is needed?

- ▶ Intrinsic resolutions:
 - ▶ $\sigma_{hit}=9 \mu\text{m}$ for Pixel
 - ▶ $\sigma_{hit}=20\text{-}60 \mu\text{m}$ for Strip
- ▶ $\sigma_{meas} \sim \sqrt{\sigma_{hit}^2 + \sigma_{align}^2}$
- ▶ Momentum resolution is:

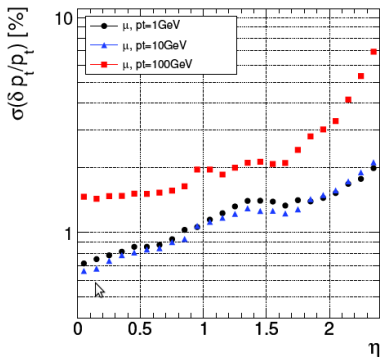
$$\frac{\delta p_T}{p_T} = C_1 \cdot p_T \oplus C_2$$

- ▶ C_1 depends on geometry:

$$C_1 \sim \frac{\sigma_{meas}}{B \cdot L^2 \cdot \sqrt{n}}$$

⇒ **Need to keep $\sigma_{align} < 10 \mu\text{m}$!**

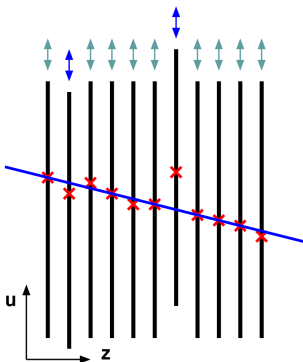
- ▶ Alignment is essential to guarantee CMS Tracker design performance!



CMS P-TDR (2006)

Tracker momentum resolution for single μ , CMS Simulation.

Track Based Alignment: Principle



Simple Example


- ▶ parallel planes measuring 1D
 - ▶ displaced in measurement direction
 - ▶ fit $\mathcal{O}(10^4)$ straight tracks: $u = F_{\mathbf{a}}(z) = a_1 + a_2 \cdot z$
 - ▶ residual $r_i = m_i - F_{\hat{\mathbf{a}}}$ at plane i :
shift of plane i leads to $\langle r_i \rangle \neq 0$
 - ▶ cannot simply shift plane by $-\langle r_i \rangle$: depends on shifts of other planes
- ⇒ tracks correlate alignment parameters

Global Fit Approach (e.g. Least Squares)

- ▶ Simultaneous fit of **all** parameters: shifts, track parameters!
- ▶ Minimise sum of squares of residuals, $\chi^2(\mathbf{a}) = \sum_k \left(\frac{m_k - F_{\mathbf{a}}}{\sigma_k} \right)^2$.
- ▶ $\mathbf{a} = (\mathbf{a}^{global}, \mathbf{a}_1^{local}, \dots, \mathbf{a}_n^{local})^T$
 - ▶ global: alignment parameters,
 - ▶ local: track parameters.

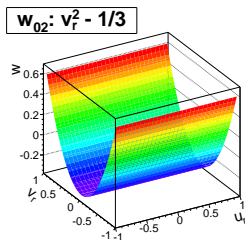
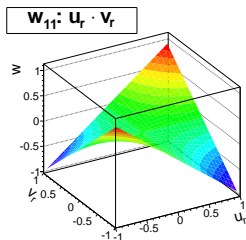
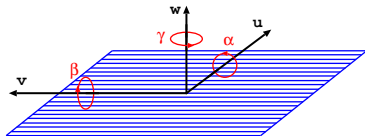
Track Based Alignment

Global Fit Approach

- ▶ Linearising track model and minimisation requiring $\frac{d\chi^2(a)}{da} = 0$:
⇒ Normal equations of least squares $\mathbf{C} \mathbf{a} = \mathbf{b}$.
- ▶ Local parameters appear in part of the data only:
⇒ Block structure in \mathbf{C} , use matrix algebra to reduce problem:
$$\mathbf{C}' \mathbf{a}^{global} = \mathbf{b}'.$$
- ▶ Matrix \mathbf{C}' , vector \mathbf{b}' summing up contributions from all tracks.
- ▶ Solving $\mathbf{C}' \mathbf{a}^{global} = \mathbf{b}'$ provides alignment solution in one step.
⇒ All correlations from tracks taken care of.
- ▶ Need clever algorithms for $> 100\,000$ global parameters:
⇒ **Millepede II^a** and **General Broken Lines Track Refit** .

^adeveloped by **V. Blobel at the University of Hamburg** (maintenance and development now by **Helmholtz Terascale Alliance**)

Track-based Alignment in CMS



Alignment Parameters in CMS

- ▶ Millepede II algorithm with $\sim 200,000$ free alignment parameters.
- ▶ 8 (9) parameters per strip (pixel) sensor:
 - ▶ 5/6 rigid body like parameters (one insensitive for strips),
 - ▶ 3 bow parameters.
- ▶ Time dependent rigid body parameters for larger structures:
 - ▶ several different time periods in common fit,
 - ⇒ moving structures, modules constant within.
- ▶ $Z \rightarrow \mu^+ \mu^-$ combined object, adding Z mass “measurement”.

Tracker alignment in CMS during LHC Run I

CMS Tracker Alignment Achievements in Run-I

- ▶ In the following slides, a few benchmark results from CMS Tracker alignment will be shown.
- ▶ CMS can fairly enough claim to have been able to align the Tracker with $\mathcal{O}(1 \div 10 \mu\text{m})$ precision.
- ▶ Results are well documented in the 2011 data alignment paper: [TRK-11-001](#), now published as JINST 9 (2014) P06009.
 - ▶ Result of the intensive dedicated work of the members of the tracker alignment group over many years. Represents a milestone document of CMS ...
- ▶ ... nevertheless we continue learning and we hope to improve Run-II alignment with several new improvements.

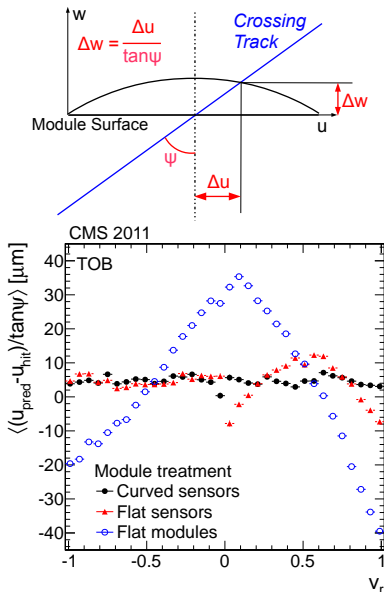
Alignment sensor deformations

Kinks and bows

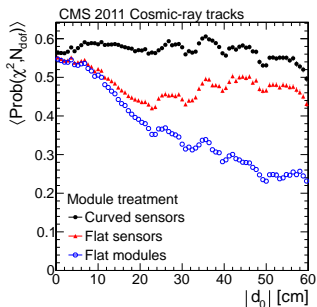
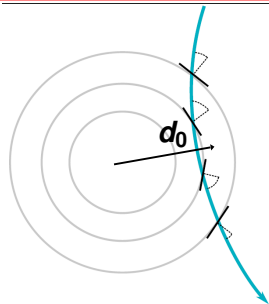
- ▶ In reality, sensors not planar: non-perpendicular tracks are biased, depending on $\tan \psi$!
- ▶ Investigate surface shape using:

$$\Delta u = \Delta w \cdot \tan \psi$$

- ▶ Increasingly important for inner layers (bias up to $\sim 100 \mu\text{m}$)
- ▶ Alignment determines bow parameters, taken into account in hit reconstruction.
- ▶ Also angles and offsets between daisy-chained modules in outer Tracker are corrected.



Sensor Bow Treatment Improves Cosmic Tracking



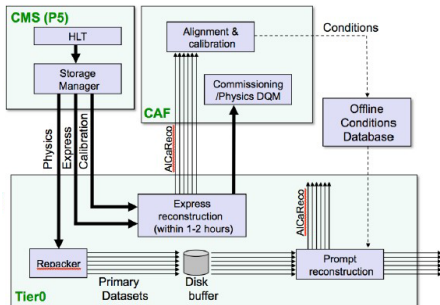
Cosmic tracks mainly come from above

- ▶ Increasing d_0 increases average track angle from sensor normal,
⇒ increasing sensitivity to deviation from flat sensors.
 - ▶ Average $\langle \text{Prob}(\chi^2, ndf) \rangle$ vs d_0 shows improvements from **flat modules** via **flat sensors**, to **curved sensors**.
 - ▶ Remaining structure related to radii of layers: material.
- ⇒ Nicely shows how fundamental are comsics data for alignment!

Prompt Large Structures Alignment

Prompt Calibration Loop (PCL)

1. Determines 6 alignment parameters for high-level-structures of pixel on “*express*” data.
2. if **movements detected**: new alignment delivered for prompt data.
3. provides feedback within 48 hours with latest data to reconstruct the same run.



Pixel Alignment in PCL

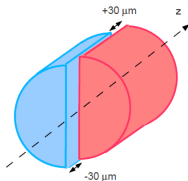
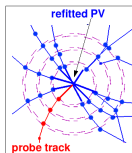
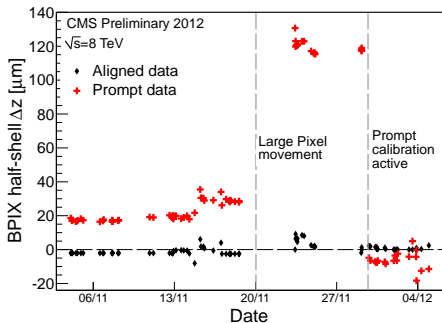
- ▶ Alignment of larger rigid structures (frames of modules, layers, subdetectors)

⇒ **faster and less tracks required!**

PCL and Pixel movements

- ▶ During last month of p - p run in 2012 PCL was running for monitoring (but not active)
- ▶ Major sudden movement of pixel half-shells along z detected in November 22nd ($\Delta z \approx 100 \mu\text{m}$! in coincidence with cooling failure)

⇒ **PCL activated on Nov 30th to recover.**



Weak Modes

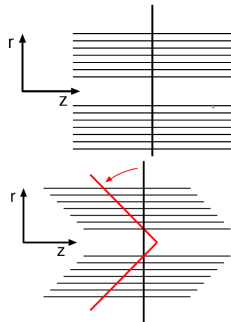
▶ Minimization of residuals insensitive to some global distortions ($\Delta\chi^2 \approx 0$),

▶ These “weak modes” can however bias track parameters

▶ **Example 1: “telescope”:**

$$\Delta Z \propto r$$

▶ creates bias in η

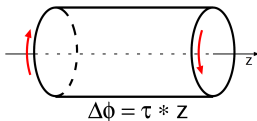


▶ **Solution: cosmic muon tracks**

▶ **Example 2: “twist”:**

$$\Delta\phi \propto z$$

▶ curvature bias of charged particles



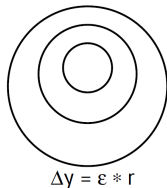
▶ weak mode even with cosmic muon tracks

▶ Solution: 0T cosmic muon tracks or mass constraint ($Z \rightarrow \mu\mu$)

▶ **2 muons from Z decay fitted together**

▶ **Example 3: “sagitta”:**

$$\Delta r \propto y$$



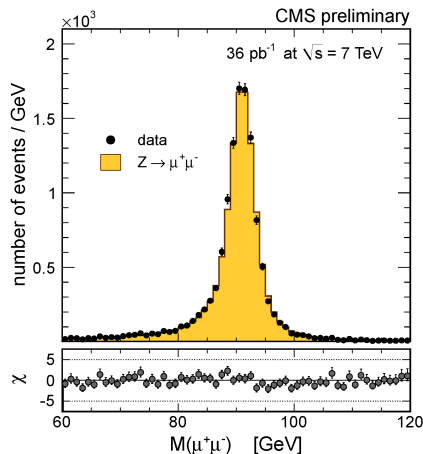
▶ curvature bias suspected in 2011,

▶ observed variation of Z mass as function of ϕ of positively charged muon

▶ ϕ -dependent curvature bias

Muon Curvature Bias

- ▶ Several systematic distortions can bias track curvature $\kappa \sim \pm 1/\rho_T$
- ▶ $Z^0 \rightarrow \mu^+\mu^-$ events reveal this bias: invariant mass fitted as function of muon direction (η, ϕ) , separating μ^+ and μ^-



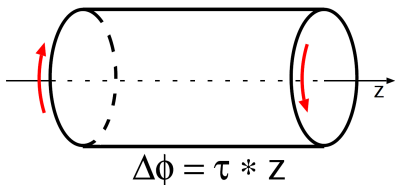
Validation with $Z \rightarrow \mu\mu$ decays

- ▶ invariant mass distribution fitted with wide fit range 75-105 GeV/c^2 , Z^0 width set to PDG value of 2.495 GeV/c^2
- ▶ Fit function: a Breit-Wigner function convoluted with Crystal ball function (models finite track resolution and radiative tail) + exponential background

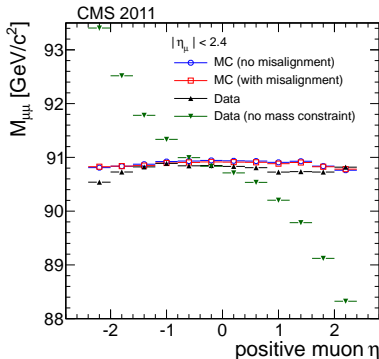
Necessity of Z^0 events in controlling weak modes

- ▶ Reconstructed $Z^0 \rightarrow \mu^+ \mu^{-1}$ mass peak as function of η_{μ^+} in 2011

Pseudorapidity of the positive muon $\eta(\mu^+)$



- ▶ Twist distortion is weak mode even using cosmics
- ▶ The red curve: alignment without mass constraint



- ▶ Results in curvature changes, biasing measured p_T of positive or negative tracks oppositely.

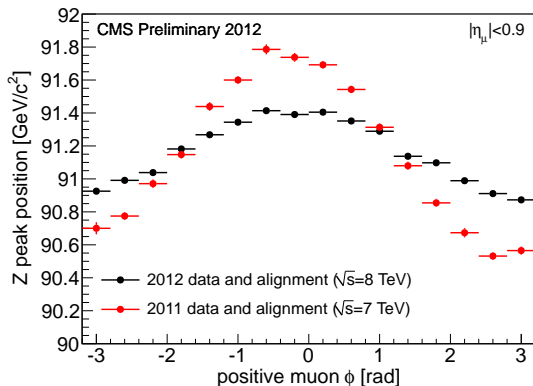
⇒ Reconstructed Z mass depends on muon charge and η

¹N.B.: this study does not illustrate CMS muon reconstruction and calibration performance; momentum calibration is applied

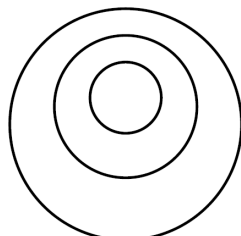
ϕ -bias in reconstructed Z^0 mass peak

- ▶ Reconstructed $Z^0 \rightarrow \mu^+ \mu^{-2}$ mass peak as function of $\phi(\mu^+)$
- ▶ Amplitude of sinusoidal shape clearly decreased with weighted input data, from 0.7 GeV/c^2 to 0.3 GeV/c^2 in barrel

Azimuthal angle ϕ of μ^+ , barrel muons



"Sagitta"-like distortion causes this kind of effect

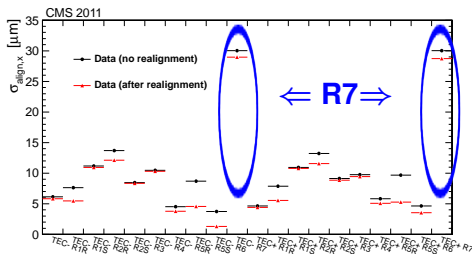


$$\Delta y = \epsilon * r$$

²N.B.: this study does not illustrate CMS muon reconstruction and calibration performance; momentum calibration is applied in addition in physics analyses

Alignment Precision and TEC Ring 7

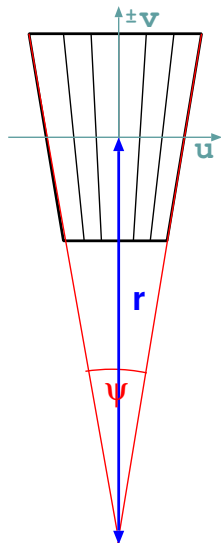
2011 Data (not aligned)
VS
2011 Data (aligned)



Local Alignment precision measured by:

- ▶ tuning width of normalised residuals (r_{hit}/σ_{hit}) to ideal MC conditions ($\sigma_{hit}^2 \rightarrow \sigma_{hit}^2 + \sigma_{align}^2$): all MC/data mismatch (hit/track uncertainties, etc.) assigned to misalignment.
- ▶ This method on 2011 data revealed $\sigma_{align} < 10 \mu\text{m}$ basically everywhere.
- ▶ **Exception: TEC Ring 7 (i.e. outermost radii)**, although OK for MC misalignment scenario (using same alignment procedures).

Alignment of the Tracker Endcaps



Endcap module

Treatment of Local y in Alignment

- ▶ Just not taken into account before in alignment procedures for strip modules!
- ▶ OK in barrel where strips parallel to local y -axis.
- ▶ In endcaps, strips are not parallel to y :
 - ▶ still no y -measurements,
 - ▶ still probably not problematic in pattern recognition,
 - ▶ but x' -residuals noticeably affected.
- ▶ Indeed have handle on this degree of freedom
- ▶ Just few thousand parameters more in the fit
- ▶ ...

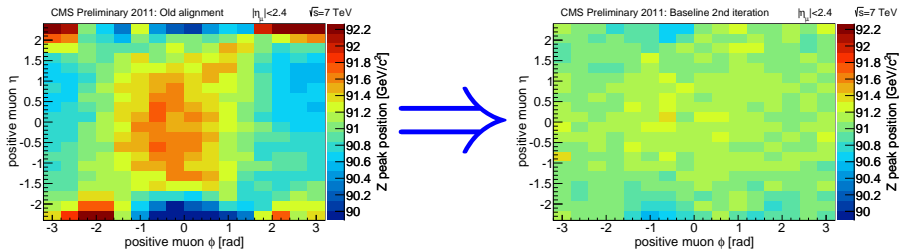
How we got rid of the ϕ -bias

- ▶ Deep investigations triggered by the fact that the APE in data in TEC Ring 7 was off by factor 3/($>20 \mu\text{m}$) from the equivalent MC value while everywhere else it was not off by more than a few μm , found that:
 - ⇒ Geometry description in reconstruction software and design drawings of TEC Ring 7 **were radially off by 1.33 mm.**
 - ▶ this macroscopic error **was not the (main) reason of the problem**, it just helped to spot it:
 - ▶ Minor systematic radial ring misplacements became visible as well once local- y was a free parameter.
 - ▶ just the case that all TEC modules are a bit off in x and y from design drawings (as is the case for ALL modules), **⇒but only corrected in r - ϕ (in contrast to the barrel and FPix), lead to the ϕ bias.**

Effects of cure of the ϕ -bias

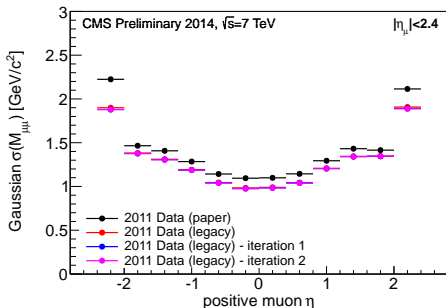
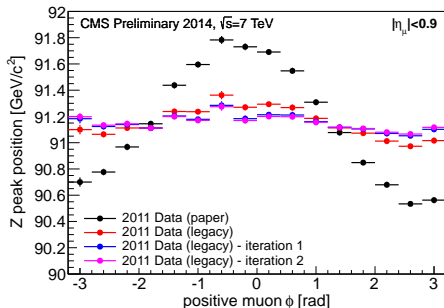
$Z \rightarrow \mu\mu$ validation for 2011 Alignment Legacy

- ▶ Mass bias in μ -track η - ϕ bins (pre and post-alignment).



- ▶ Desired result: No modulation.
- ▶ **This is the striking result!** Modulation in ϕ strongly reduced when releasing local- y in Tracker Endcap Alignment.
- ▶ Available since some time in $\sqrt{s} = 7$ TeV reprocessed datasets.

Effects of cure of the ϕ -bias



- ▶ Left: the resonant peak position, right: Gaussian width $\sigma(M_{\mu\mu})$ minus natural width of the Z, from fit to the lineshape³

$$f(m_{\mu\mu}; \sigma, M_Z, \Gamma_Z) = \int_{-\infty}^{\infty} \text{CB}(m_{\mu\mu}; \alpha, n, \sigma) \times \text{BW}(m_{\mu\mu} - m'; M_Z, \Gamma_Z) dm'$$

- ▶ **An overall improvement of about 10% is visible**
- ▶ We are going to repeat this for 2012 data plus something even better...

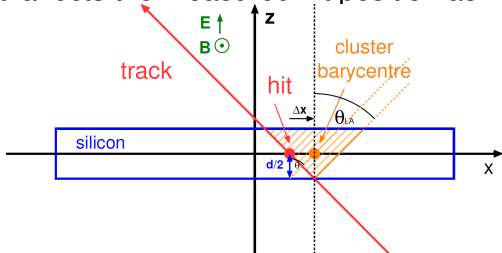
³(Breit-Wigner convolved with Crystal-Ball)

Lorentz Angle calibration and alignment

- ▶ Charge drift in magnetic field affects the measured hit position as

$$\Delta x = \tan(\theta_{LA}) \cdot \frac{d}{2}$$
$$\tan(\theta_{LA}) = \mu \cdot B_y$$

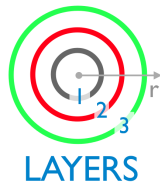
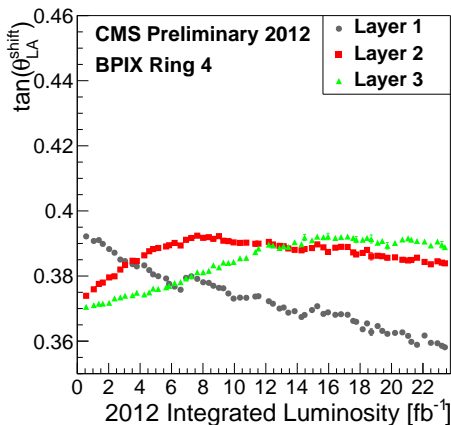
d = module thickness
 μ = mobility



- ▶ θ_{LA} depends e.g. on bias voltage, temperature and irradiation dose.
- ▶ To correct this effect most precisely:
 $\tan(\theta_{LA})$ calibration integrated in MILLEPEDE II alignment procedure.
- ▶ Data with magnetic field ON and OFF used simultaneously:
(isolated muons, $Z^0 \rightarrow \mu^+ \mu^-$, cosmic ray muons and field OFF collision data)
- ▶ Granularity: 3 layers, 8 rings, 65 periods of time \rightarrow 1560 additional parameters

\Rightarrow foresee to use it in the “Legacy” $\sqrt{s} = 8\text{TeV}$ data alignment

Lorentz Angle calibration in the Pixels (2012)



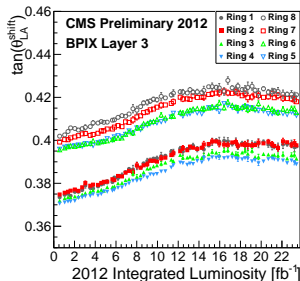
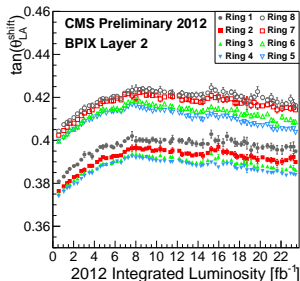
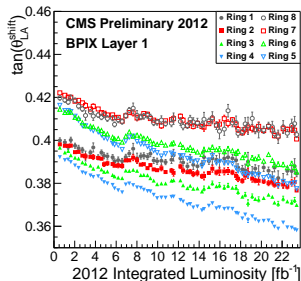
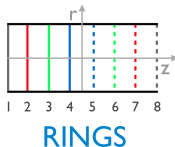
- ▶ Temperature and bias voltage stable in 2012.
- ⇒ Time dependence due to irradiation.
- ▶ About 3 μm effect.

- ▶ Raising for layer 2 & 3 not fully understood.
- ▶ Less radiation at larger radii stretches curves and shifts right.
- ⇒ Qualitatively the same curves for all layers.

A few μm effect, but will be relevant in 2015 with increased LHC

Lorentz Angle calibration in the Pixels (2012)

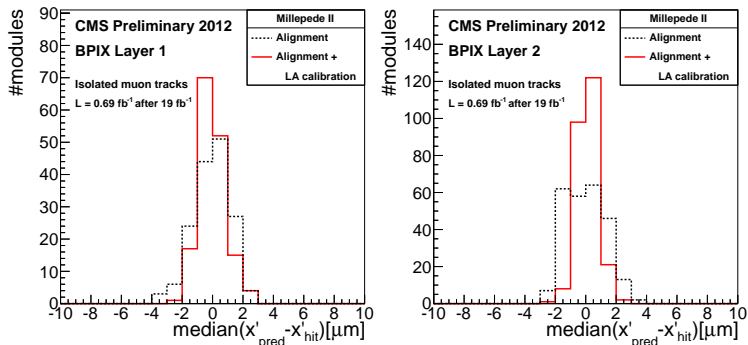
- ▶ For each layer: LA for modules of one ring as function of integrated luminosity
- ▶ Offset between R1-4 and R5-8 related to different bias voltages (one group not grounded).



- ▶ Slow decrease pronounced for innermost rings
- ▶ Increase followed by a decrease; more rapid for layer 2 smaller difference between rings.

Lorentz Angle Validation

- ▶ LA calibration validated comparing **combined Millepede approach (alignment + LA)** to alignment with standalone calibration. Independent set of tracks from isolated- μ used in validation.



- ▶ Distribution of median of unbiased residuals (DMR) between measured and predicted hit position for each module.
- ▶ **Small, but visible improvement using combined approach.**

Summary - I

- ▶ Large CMS silicon tracker is a challenge for alignment
- ▶ Alignment of ~ 200.000 alignment parameters was performed routinely for 2 years
- ▶ Alignment local precision has been brought below $10 \mu\text{m}$ in most regions of the Tracker. Track-based alignment *in situ* allowed such performance.
 1. Survey input was basically useless ...
 2. Laser Alignment System (LAS) input not exploited to full potential, but likely not necessary (except maybe for monitoring)
- ▶ Dataset input is vital: **need plenty of tracks from different topologies**:
 1. Field-on and field-off cosmic data was instrumental to control weak modes and to measure deviation-from-flatness of sensors.
 2. Resonant di-muon ($Z \rightarrow \mu\mu$) datasets are crucial to control “twist-like” deformations.
 3. Field-off data helps in disentangling misalignment from Lorentz Angle biases.

Summary - II

- ▶ Main working horse in past 2-3 years: **Millepede-II with General Broken Lines**
- ▶ The Global fit approach is powerful, but demands clean input:
 - ⇒ Incorrect parametrization of the geometry model can lead to large “weak mode” effects if not all the DOF are taken into account correctly (see ϕ -bias issue).
 - ▶ It is **ESSENTIAL to simultaneously calibrate** pure position constants and **ALL other position sensitive** calibration parameters such as the Lorentz Angle (LA).
- ▶ Showed capability to calibrate LA with $\sqrt{s} = 8$ TeV data.
 - ▶ especially important in view of RUN II in the Tracker innermost region (Pixel) where high irradiation dose will generate strong time dependencies.
- ▶ **Recent alignment improvements:**
 - ▶ Prompt Calibration Loop operational (end of 2012): **able to follow promptly movements up to 150 μm !**
 - ▶ Curvature bias modes in better control with $Z^0 \rightarrow \mu^+ \mu^-$ events.
 - ▶ Alignment framework extended to treat calibration parameters.

A few closing words ...

- ▶ The title of the talk should read: lessons learnt aligning the CMS silicon Tracker in Run-I;
 - ⇒ During Run-I, LHC,CMS and the Tracker were not operated at design conditions (different luminosity conditions, different detector temperatures, ...)
 - ▶ LHC Run-II data can still provide exciting alignment challenges, small input biases are know to generate large effects 😊!

Thanks!

- ▶ A relevant part of the CMS Tracker Alignment effort in the last decade has been carried by the DESY-CMS Group, **which I would like to acknowledge gratefully on behalf of the CMS collaboration.**
- ▶ I am especially indebted, also for the material shown here, with a former member, *G. Flucke*, who paved the way to most of these results and moved on in the meantime to other projects.

Backup Slides

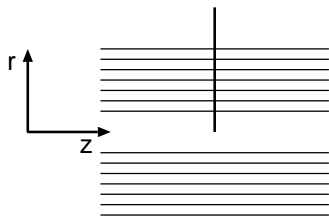
Problem of Track Based Alignment: Weak Modes

Minimising residuals can be insensitive to certain global distortions.

- ▶ Potential bias on track parameters.
- ▶ Dependent on data fed into matrix.

Example: Telescoping

Shift in z growing linear with radius r



- ▶ Magnetic field $\mathbf{B} \parallel z$:
tracks are straight lines in rz

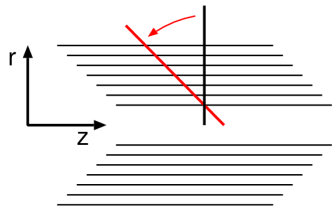
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- ▶ Magnetic field $\mathbf{B} \parallel z$:
tracks are straight lines in rz
- ▶ This distortion does not change that!
- ▶ \Rightarrow Bias in η

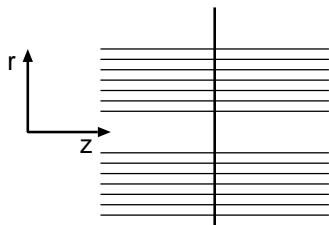
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- ▶ Magnetic field $\mathbf{B} \parallel z$:
tracks are straight lines in rz
 - ▶ This distortion does not change that!
 - ▶ \Rightarrow Bias in η
- Solution:
- ▶ Adding cosmic tracks.

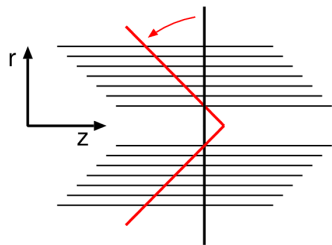
Problem of Track Based Alignment: Weak Modes

Minimising residuals can be insensitive to certain global distortions.

- ▶ Potential bias on track parameters.
- ▶ Dependent on data fed into matrix.

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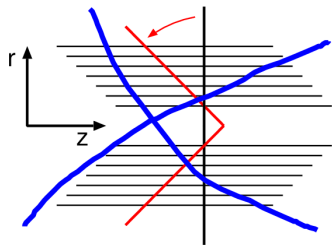
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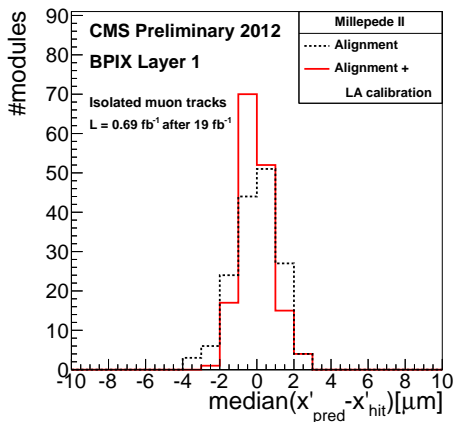
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 - ▶ Telescope effect bends track: not allowed by track model.

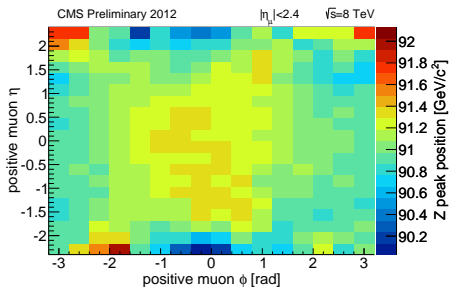
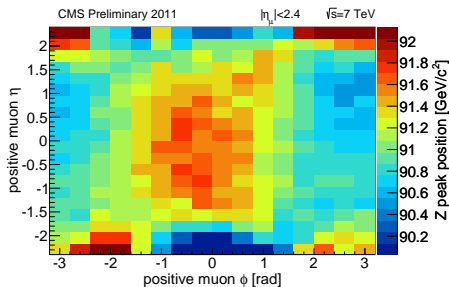
Lorentz Angle validation, BPIX layers 3

- ▶ LA calibration validated by comparing to alignment with standalone calibration.
 - ▶ Distribution of median of unbiased residuals (DMR) between measured and predicted hit position for each module. Independent set of tracks from isolated muons used in validation (from end of 2012).
-
- ▶ Clear improvement using integrated alignment and calibration.
 - ▶ Double peak illustrates inconsistency between LA and alignment, corrected in the combined approach.
 - ▶ A few μm effect, but this approach will be more relevant in 2015 with increased LHC luminosity.



Improvement in $Z \rightarrow \mu\mu$ decay validation

- ▶ Reconstructed $Z \rightarrow \mu^+\mu^-$ mass peak as function of both pseudorapidity η and azimuthal angle ϕ of positive muon
- ▶ Z-axis same in both pictures, centered at peak value of all 2011 events (91.08 GeV/c^2)



- ▶ Overall pattern significantly reduced for 2012!

⁴N.B.: this study does not illustrate CMS muon reconstruction and calibration performance; momentum calibration is applied in addition in physics analyses

Millepede II

An Experiment-Independent Global Fit Tool

(originally by V. Blobel, further developed by C. Kleinwort)

Task of the Global Fit Tool

- ▶ Setting up and Solving Matrix Equation

$$\mathbf{C}' \mathbf{a}^{global} = \mathbf{b}',$$

- ▶ from millions of tracks (containing outlier hits),

- ▶ \mathbf{C}' is $n \times n$ matrix:
 - ▶ here $n \approx 200\,000$,
 - ▶ typically sparse.

⇒ **Very demanding for memory and CPU.**

Input from Experiment

- ▶ Linearised track fit information:

- ▶ residuals with uncertainties,
- ▶ derivatives $\frac{\partial F}{\partial a^{local}}$ and $\frac{\partial F}{\partial a^{global}}$,

- ▶ Global parameter constraints: $\sum d_i a_i^{global} = e.$

Millepede II

Features: Computing Aspects

- ▶ Successor of Millepede I: able to deal with much larger number of parameters.
- ▶ Stand alone Fortran program.
- ▶ Reading (zipped) binary input from Fortran or C++.
- ▶ Optimised for speed:
 - ▶ iterative MINRES to solve $\mathbf{C}' \mathbf{a}^{global} = \mathbf{b}'$,
 - ▶ CPU intense parts parallelised using OpenMP®,
 - ▶ local fit detects bordered band matrices (\Rightarrow Broken Line Fit),
 - \Rightarrow reading data from disc and memory access remaining bottlenecks.
- ▶ Optimised for memory space:
 - ▶ symmetric \mathbf{C}' would need 160 GB in double precision,
 - ▶ reduction due to sparsity
 - ▶ compression by bit packed addressing of continuous non-zero blocks,
 - ▶ and by single precision for elements summing up from few tracks.

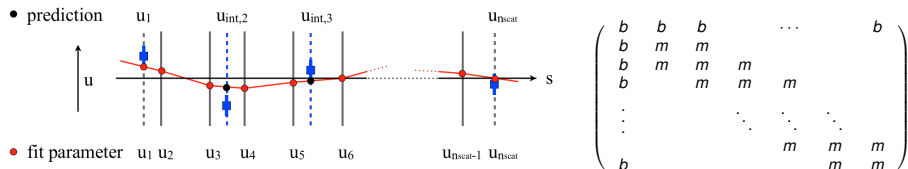
Track Fit

- ▶ Charged particle in magnetic field: need 5 helix parameters.
 - ▶ Traversing material: multiple scattering effects.
(relevant for “heavy” tracking detectors)
 - ▶ Usually treated by progressive track fit: Kalman filter.
 - ▶ Millepede II needs global fit:
 - ⇒ 2 scattering angles per thin scatterer,
 - ⇒ $5 + 2n_{scat}$ explicit track parameters.
 - ▶ Reaching > 50 parameters for cosmic tracks in CMS tracker.
- ⇒ Danger of CPU consuming single track fits when building matrix equation $\mathbf{C} \mathbf{a}^{global} = \mathbf{b}$.

Way out:

- ▶ General Broken Lines Track Refit

General Broken Lines Track Refit



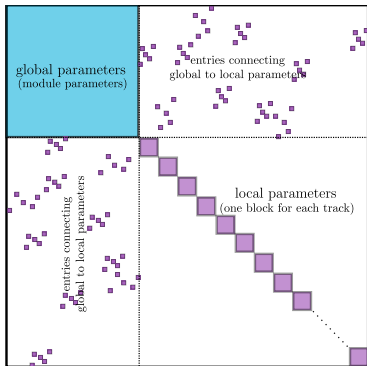
Concept: Define Track Parameters with Local Meaning

- ▶ Reparametrise: $\mathbf{a}^{local} = (\Delta q/p, \mathbf{u}_1, \dots, \mathbf{u}_{n_{scat}})$.
- ▶ \mathbf{u}_j : 2D offsets in local system at each scatterer.
- ▶ Predictions \mathbf{u}_{int} for measurements: interpolating between scatterers.
- ▶ Kink angles from triplets of adjacent scatterers.

⇒ Local fit $\mathbf{A} \cdot \mathbf{x} = \mathbf{b}$:

- ▶ bordered band matrix, band width $m \leq 5$, border size $b = 1$.
- ▶ Fast solution by root free Cholesky decomposition:
 - ▶ Effort to calculate \mathbf{x} : $\sim n_{par} \cdot (m + b)^2$, \mathbf{A}^{-1} : $\sim n_{par}^2 \cdot (m + b)$
- ▶ Equivalent to standard CMS Kalman filter track fit.

Alignment is big data!



a) Millepede-II is a Physics at the Terascale project.

- ▶ What we call *global parameters* are the calibration constants to be determined.
- ▶ A full alignment for every module (3 positions, 3 rotation, 3 surface deformation) determines $O(200\,000)$ numbers
- ▶ We need to solve a linear equation system of this size and use special high-RAM machines for this.
- ▶ Most recent sets of alignment constants delivered by [Millepede-II^{a\)}](#).
- ▶ A variety of datasets (MinBias, $Z \rightarrow \mu\mu$, single μ , Cosmics) in large numbers are required ($> 10^7$ events).
- ▶ Running one job takes about 24 hours of wall-clock time.

2012 “Legacy” alignment with $\sqrt{s} = 8$ TeV data

Offline-Validation with Isolated- μ Tracks

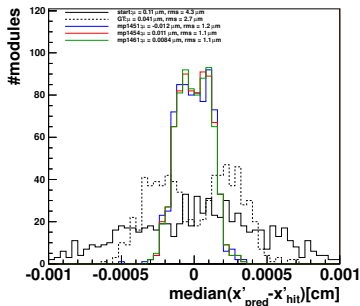
- ▶ **Goal:** to reach a stable reference alignment for 2012 data.
 - ▶ Including latest alignment procedures (Lorentz Angle & BackPlane corr. calibration).

☑ **High precision after alignment**.

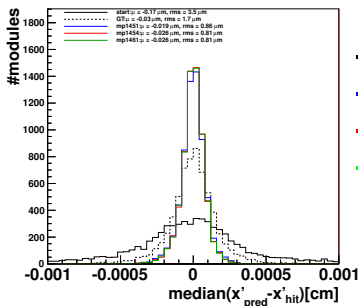
- ▶ Starting Tracker Alignment from 2011 Legacy Alignment

⇒ Stable after 0th iteration. And we include BP as well.

Distribution of the median of the residuals in BPIX



Distribution of the median of the residuals in TEC



— start geometry
— 0th iteration
— 1st iteration
— 2nd iteration
- - - Geometry for reprocessing