

Electroweak and QCD corrections to Higgs-boson production in vector-boson fusion at the LHC

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in collaboration with M.Ciccolini and A.Denner

based on PRL 99 (2007) 161803 [arXiv:0707.0381, hep-ph] and PRD 77 (2008) 013002 [arXiv:0710.4749, hep-ph]

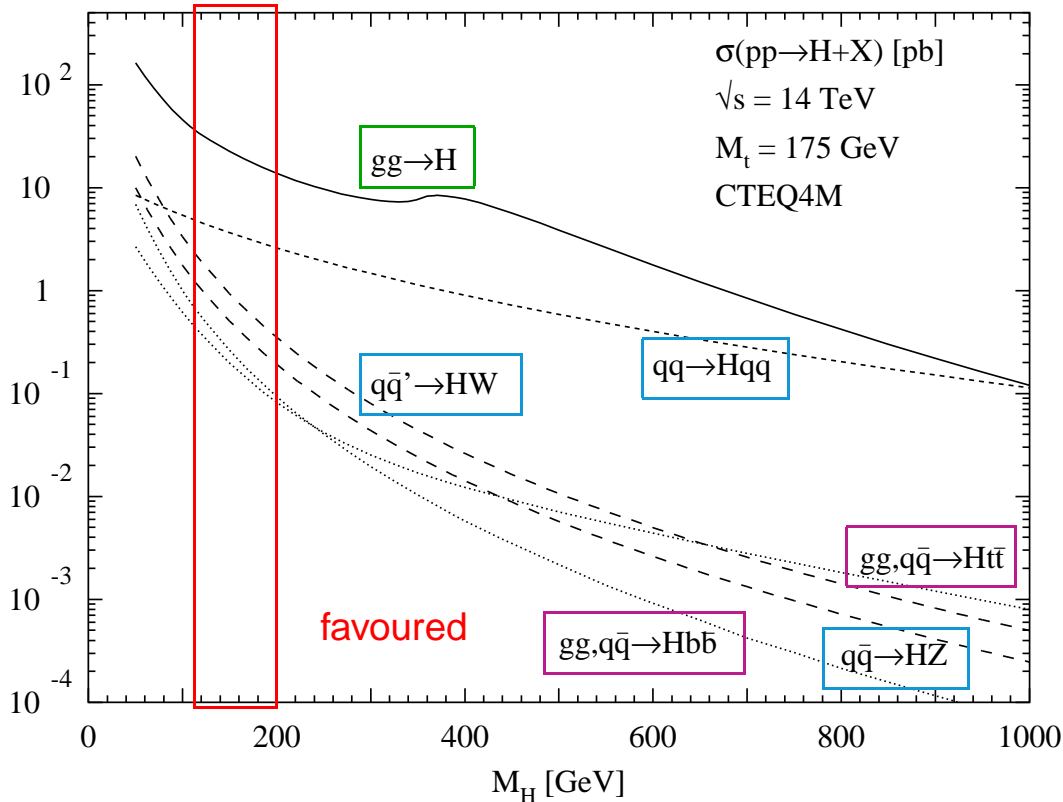
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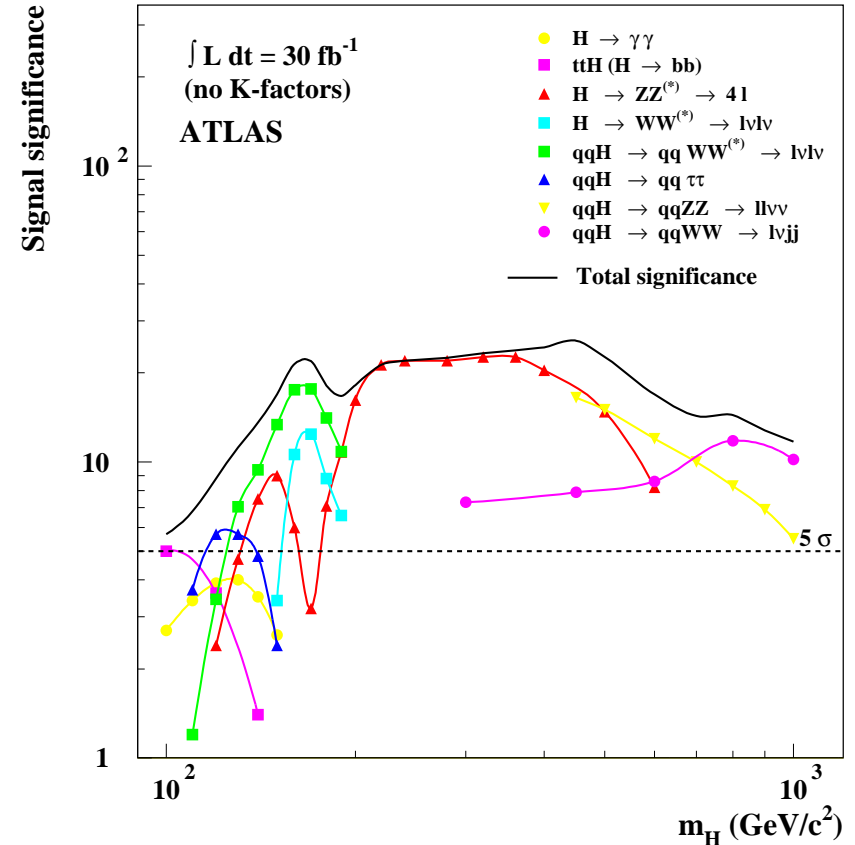
1 Introduction

Cross sections and significance of the Higgs signal at the LHC

Spira et al. '98



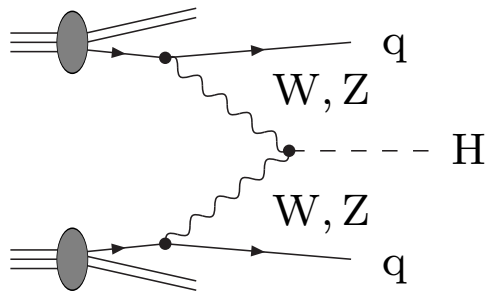
ATLAS '04



Higgs production via VBF (“ qqH ”) is cornerstone in Higgs search in entire M_H range

\rightarrow calculate / control higher orders to reduce theoretical uncertainty
 down to the level of PDF ($\sim 3\text{--}4\%$) and experimental uncertainties ($\sim 5\text{--}10\%$)

Process topology of Higgs production via VBF



colour exchange between quark lines suppressed

⇒ **small QCD corrections**

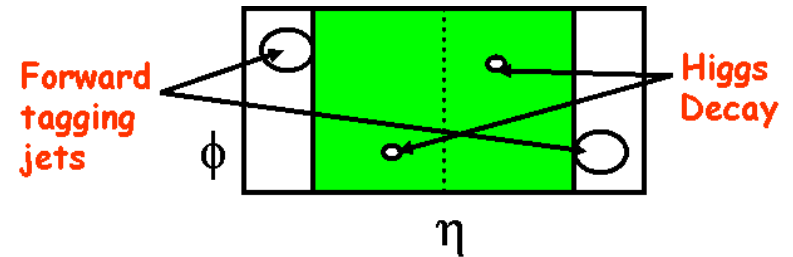
Han, Valencia, Willenbrock '92; Spira '98;
Djouadi, Spira '00; Figy, Oleari, Zeppenfeld '03

↪ “t-channel approximation” (vertex corrections)

VBF cuts and background suppression:

- 2 hard “tagging” jets demanded:
 $p_{Tj} > 20 \text{ GeV}, \quad |y_j| < 4.5$
- tagging jets forward–backward directed:
 $\Delta y_{jj} > 4, \quad y_{j1} \cdot y_{j2} < 0$

signature = Higgs + 2jets



↪ Suppression of background

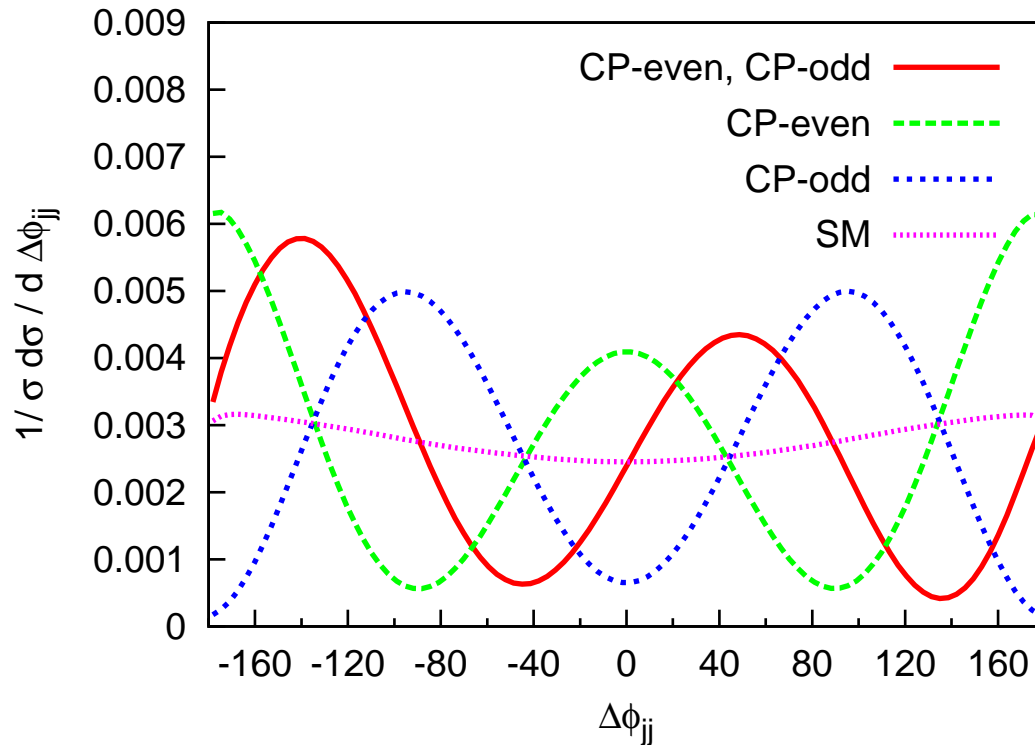
- from other (non-Higgs) processes,
such as $t\bar{t}$ or WW production Zeppenfeld et al. '94-'99
- induced by Higgs production via gluon fusion,
such as $gg \rightarrow ggH$ Del Duca et al. '06; Campbell et al. '06

WWH and ZZH coupling analyses

- Higgs via VBF plays important role in global Higgs couplings analysis

Dührssen et al. '04

- azimuthal angle difference $\Delta\phi_{jj}$ of tagging jets is sensitive to BSM effects:



Hankele, Klämke,
Zeppenfeld, Figy '06

(Individual contributions
without SM)

CP-even: $\mathcal{L} \propto HW_{\mu\nu}^+ W^{-,\mu\nu}, \quad \Gamma_{\mu\nu}^{HW^+W^-} \propto g_{\mu\nu}(k_+k_-) - k_{+,\nu}k_{-,\mu}$

CP-odd: $\mathcal{L} \propto H\tilde{W}_{\mu\nu}^+ W^{-,\mu\nu}, \quad \Gamma_{\mu\nu}^{HW^+W^-} \propto \epsilon_{\mu\nu\rho\sigma}k_+^\rho k_-^\sigma$

Work on radiative corrections to the production of Higgs+2jets

- **NLO QCD corrections to VBF in “*t*-channel approximation”** (vertex corrections)
 - ◇ total cross section Han, Valencia, Willenbrock '92; Spira '98; Djouadi, Spira '00
 - ◇ distributions Figy, Oleari, Zeppenfeld '03; Berger, Campbell '04

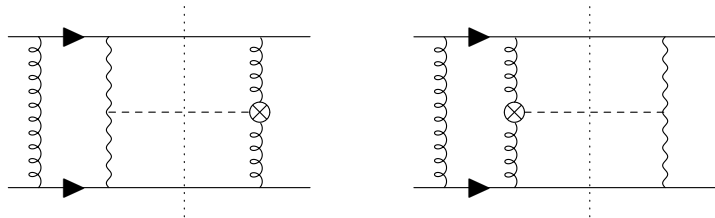
↪ impact $\sim 5\text{--}10\%$
- **NLO QCD corrections to gluon-initiated channels** (effective Hgg coupling) Campbell, R.K.Ellis, Zanderighi '06

↪ contribution to VBF $\sim 5\%$ Nikitenko, Vazquez '07 (NLO scale uncertainty $\sim 35\%$)
- **(full) NLO QCD+EW corrections to VBF** Ciccolini, Denner, S.D. '07

↪ NLO QCD \sim NLO EW $\sim 5\text{--}10\%$ → **discussed in this talk !**
- **QCD loop-induced interferences** between VBF and gluon-initiated channels Andersen, Binoth, Heinrich, Smillie '07
Bredenstein, Hagiwara, Jäger '08

↪ impact $\lesssim 10^{-3}\%$ (negligible!)
- **SUSY QCD+EW corrections** Hollik, Plehn, Rauch, Rzehak '08

↪ $|\text{MSSM} - \text{SM}| \lesssim 1\%$ for SPS points (2–4% for low SUSY scales)



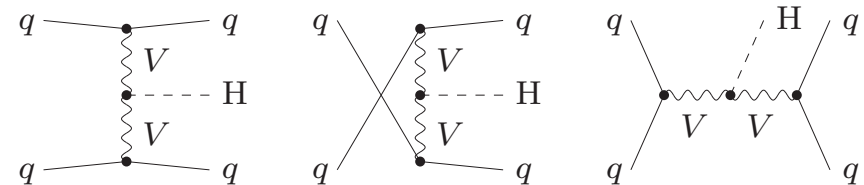
Andersen, Binoth, Heinrich, Smillie '07
Bredenstein, Hagiwara, Jäger '08

→ impact $\lesssim 10^{-3}\%$ (negligible!)

2 Details of the NLO calculation

EW production of Higgs+2jets in LO:

- many subcontributions from qq , $q\bar{q}$, and $\bar{q}\bar{q}$ channels
- each channel receives contributions from one or two topologies (“ t ”, “ u ”, “ s ”):



↪ all contributions and interferences taken into account in LO and NLO

EW production of Higgs+2jets in NLO:

- partonic channels for
 - ◇ one-loop diagrams: qq , $q\bar{q}$, $\bar{q}\bar{q}$
 - ◇ real QCD corrections qq , $q\bar{q}$, $\bar{q}\bar{q}$ (gluon emission), qg , $\bar{q}g$ (gluon induced)
 - ◇ real QED corrections qq , $q\bar{q}$, $\bar{q}\bar{q}$ (photon emission), $q\gamma$, $\bar{q}\gamma$ (photon induced)
- collinear initial-state singularities from QCD and QED splittings
 - ↪ factorization and PDF redefinition for QCD and QED singularities

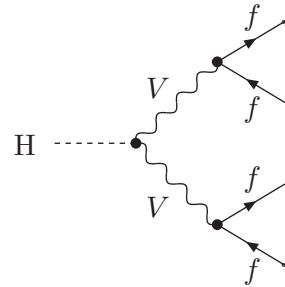
Recycling strategy:

obtain all LO and NLO amplitudes via crossing

from NLO EW and QCD corrections to $H \rightarrow WW/ZZ \rightarrow 4f$ Bredenstein, Denner, S.D., Weber '06

Survey of Feynman diagrams for NLO EW and QCD corrections

Lowest order:

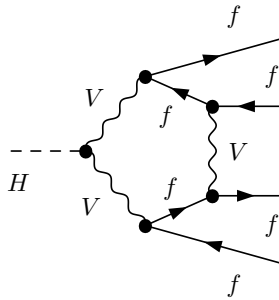


(one or two diagrams per flavour channel)

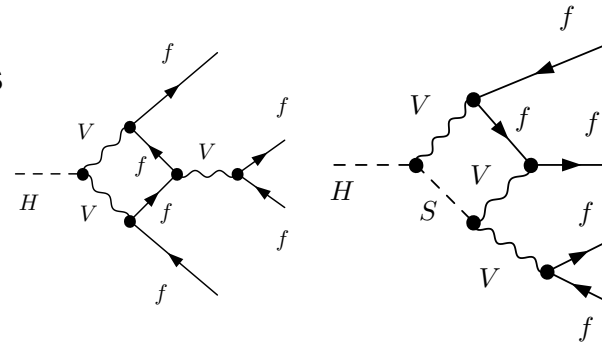
Typical one-loop diagrams:

diagrams = $\mathcal{O}(200-400)$

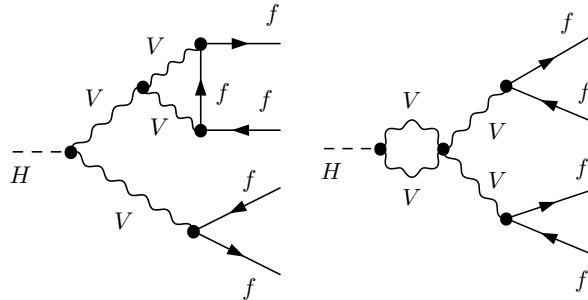
pentagons



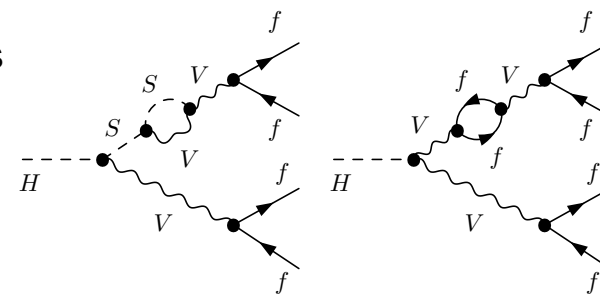
boxes



vertices



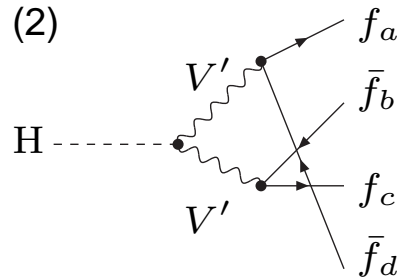
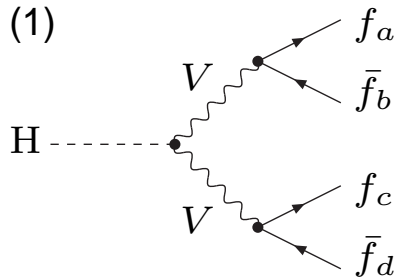
self-energies



+ tree graphs with real photons or gluons

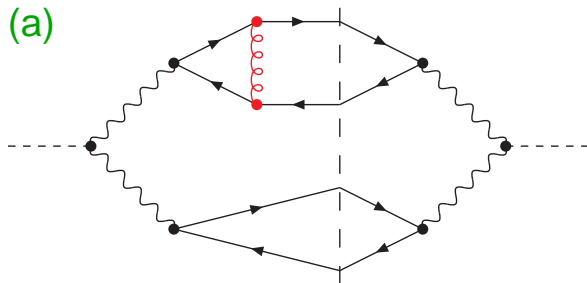
Classification of QCD corrections

Possible Born diagrams:

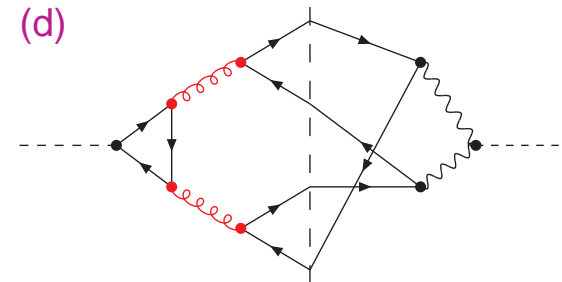
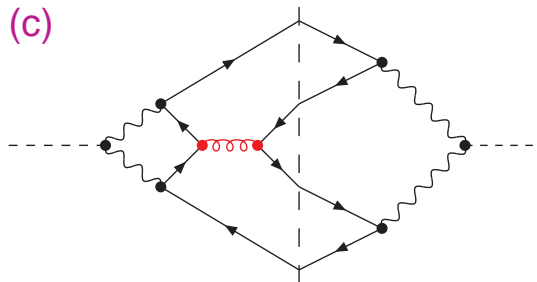
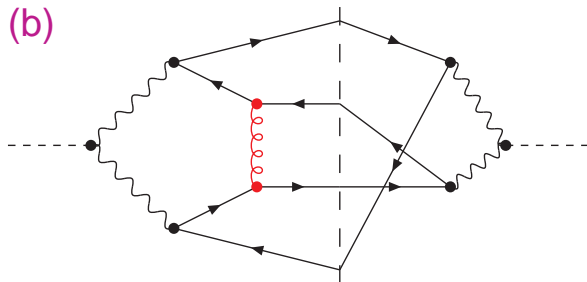


diagrams (2) only for $q\bar{q}q\bar{q}$ and $q\bar{q}q'\bar{q}'$ channels
 (q' = weak-isospin partner of q)

Classification of QCD corrections into four categories: (typical diagrams shown)



(a) contains previously known “ t -channel approximation”



(b,c,d) = corrections to interferences (only for $q\bar{q}q\bar{q}$ and $q\bar{q}q'\bar{q}'$ channels)

Technical details of the calculation:

↪ two independent calculations of each ingredient !

Virtual corrections:

- algebraic part:
 - ◇ version 1:
 - diagram generation with FEYNARTS 1 Böhm, Denner, Eck, Küblbeck '90,'92
 - algebraic reduction by in-house Mathematica routines
 - ◇ version 2:
 - diagram generation with FEYNARTS 3 Hahn '01
 - algebraic reduction based on FORMCALC Hahn, Perez-Victoria '99; Hahn '00
- tensor and scalar loop integrals:
two independent in-house libraries supporting complex masses in loops
- leading 2-loop heavy-Higgs effects $\propto G_\mu^2 M_H^4$ Ghinculov '95
Frink, Kniehl, Kreimer, Riesselmann '96

Real corrections:

- compact matrix elements via helicity spinor formalism
- multi-channel Monte Carlo integration Berends, Kleiss, Pittau '94; Kleiss, Pittau '94
- singularities isolated via two-cutoff slicing or dipole subtraction
Catani, Seymour '96; S.D. '00; S.D., Kabelschacht, Kasprzik '08

Main complications in the loop calculation:

- **numerical instabilities** in Passarino–Veltman reduction of tensor integrals
↪ new reduction methods developed [Denner, S.D. '02,'05](#)
- gauge-invariant treatment of **W and Z resonances** (appearing in s -channels)
↪ “complex-mass scheme” [Denner, S.D., Roth, Wieders '05](#)

New concepts already used in NLO EW correction to $e^+e^- \rightarrow 4f$ [Denner, S.D., Roth, Wieders '05](#)
and NLO QCD+EW corrections to $H \rightarrow 4f$ [Bredenstein, Denner, S.D., Weber '06](#)

Numerical evaluation of one-loop integrals

Passarino–Veltman reduction of tensor to scalar integrals

↪ inverse Gram determinants of external momenta

↪ **serious numerical instabilities where $\det(\text{Gram}) \rightarrow 0$**
(at phase-space boundary but not only !)

Our solutions: Denner, S.D., Nucl.Phys. B734 (2006) 62 [hep-ph/0509141]

- **1- and 2-point integrals** → stable direct calculation
- **3- and 4-point integrals** → two hybrid methods
 - (i) Passarino–Veltman \oplus seminumerical method \oplus analytical special cases
related to Ferroglia et al. '02
 - (ii) Passarino–Veltman \oplus expansions in small Gram and other kin. determinants
related to R.K.Ellis, Giele, Zanderighi '04,'05
- **5- and 6-point integrals**
 - ↪ stable reduction to lower-point integrals without Gram determinants
related to Binoth et al. '05

⇒ **Techniques ready for further applications**

(dim. regularization for IR singularities possible; complex masses supported)

The complex-mass scheme at NLO Denner, S.D., Roth, Wieders '05

Basic idea: $\text{mass}^2 = \text{location of propagator pole in complex } p^2 \text{ plane}$

\hookrightarrow consistent use of complex masses everywhere !

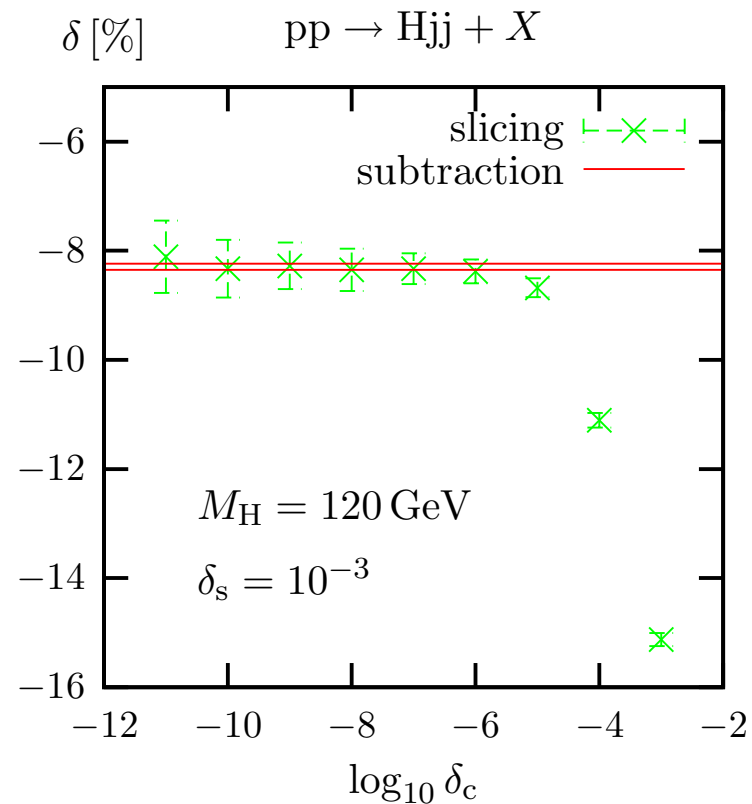
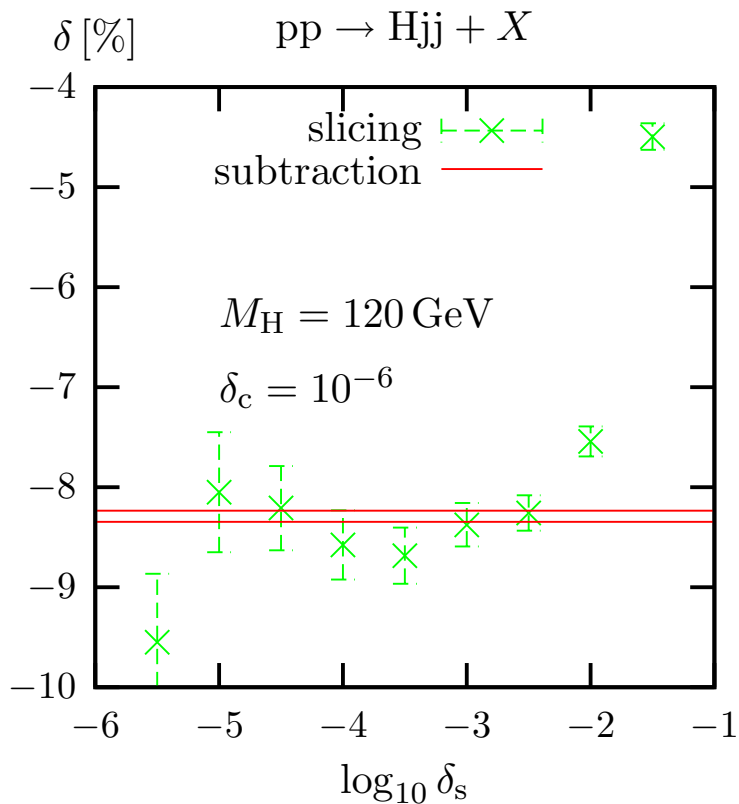
Application to gauge-boson resonances:

- replace $M_W^2 \rightarrow \mu_W^2 = M_W^2 - iM_W\Gamma_W$, $M_Z^2 \rightarrow \mu_Z^2 = M_Z^2 - iM_Z\Gamma_Z$
and define (complex) weak mixing angle via $c_W^2 = 1 - s_W^2 = \frac{\mu_W^2}{\mu_Z^2}$
- **virtues:**
 - ◇ gauge-invariant result (Slavnov–Taylor identities, gauge-parameter independence)
 \hookrightarrow unitarity cancellations respected !
 - ◇ perturbative calculations as usual (loops and counterterms)
 - ◇ no double counting of contributions (bare Lagrangian unchanged !)
- **drawbacks:**
 - ◇ unitarity-violating spurious terms of $\mathcal{O}(\alpha^2)$ \rightarrow but beyond NLO accuracy !
(from t -channel/off-shell propagators and complex mixing angle)
 - ◇ complex gauge-boson masses also in loop integrals

Checks:

- **UV structure** of virtual corrections
 - ↪ independence of reference mass μ of dimensional regularization
- **IR structure** of virtual + soft-photon corrections
 - ↪ independence of $\ln m_\gamma$ (m_γ = formally infinitesimal photon mass)
- **mass singularities** of virtual + related collinear photonic corrections
 - ↪ independence of $\ln m_{f_i}$ (m_{f_i} = small masses of external fermions)
- **gauge invariance** of amplitudes with $\Gamma_W, \Gamma_Z \neq 0$
 - ↪ identical results in 't Hooft–Feynman and background-field gauge
Denner, S.D., Weiglein '94
- **real corrections**
 - ↪ squared amplitudes compared with MADGRAPH
Stelzer, Long '94
- **combination of virtual and real corrections**
 - ↪ identical results with two-cutoff slicing and dipole subtraction
Catani, Seymour '96; S.D. '00; S.D., Kabelschacht, Kasprzik '08
- **two completely independent calculations of all ingredients !**

Comparison of subtraction and slicing results:



Ciccolini, Denner,
S.D. '07

$(\mu_{\text{ren}} = \mu_{\text{fact}} = M_H)$

- slicing cuts in partonic CM frame:

soft region: $E_\gamma < \delta_s \frac{\sqrt{\hat{s}}}{2}$, collinear cone: $1 - \cos(\theta_{\{\gamma, g\}q}) < \delta_c$

- slicing: 10^9 events, subtraction: 10^8 events

↪ subtraction is much more efficient!

3 Numerical results

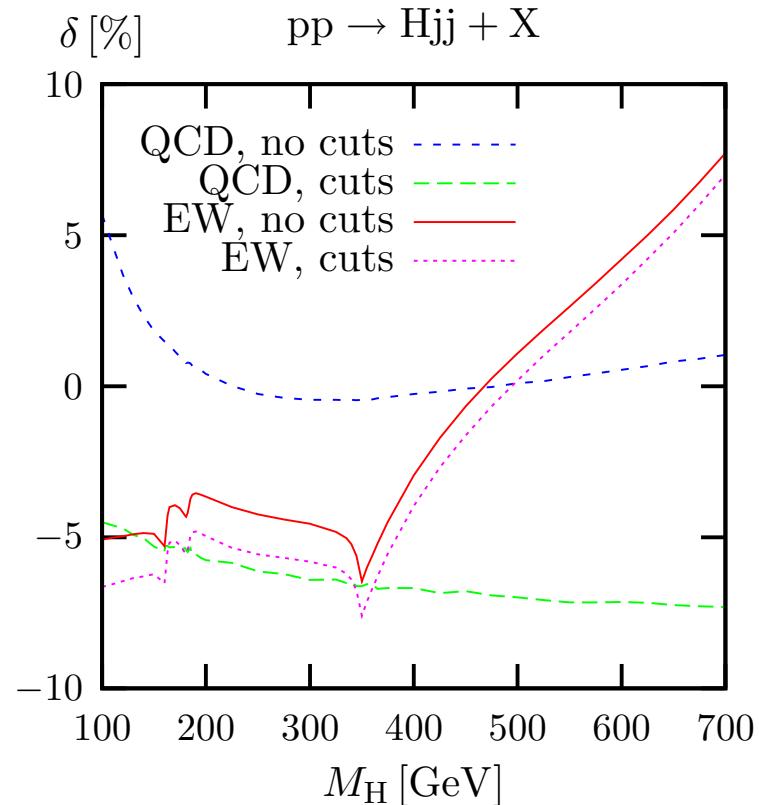
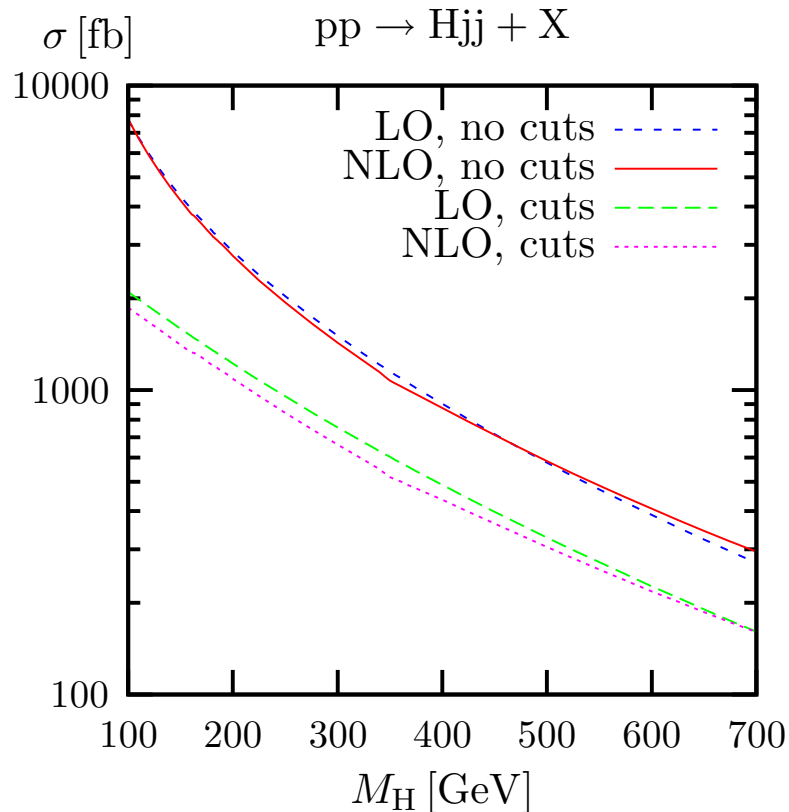
Definition of observables

- **Jet definition:** k_T algorithm as used at Tevatron run II Blazey et al. '00
↪ clusters partons with $|\eta| < 5$ into jets with $D = 0.8$ (photons included!)
- **VBF cuts:**
 - ◇ 2 hard “tagging” jets demanded: $p_{Tj_1} > p_{Tj_2} > 20 \text{ GeV}, \quad |y_{j_{1,2}}| < 4.5$
 - ◇ tagging jets forward–backward directed: $\Delta y_{jj} > 4, \quad y_{j_1} \cdot y_{j_2} < 0$
 - ◇ no cuts on Higgs momentum (should be adjusted to specific decays)

NLO settings:

- central scales: $\mu_{\text{ren}} = \mu_{\text{fact}} = M_W$
- PDFs: MRST2004QED which includes QED corrections and γ PDF
- $\alpha_s(\mu_{\text{ren}})$ with 5 active flavours (top-quark decoupled)
- α defined in G_μ scheme: $\alpha_{G_\mu} = \sqrt{2}G_\mu M_W^2 (1 - M_W^2/M_Z^2)/\pi$
↪ absorbs running of α from $Q = 0$ to EW scale and $\Delta\rho$ in $Wq\bar{q}'$ coupling

3.1 Results on integrated cross sections



Ciccolini, Denner,
S.D. '07

- **QCD** and **EW** corrections are of same generic size
- scale uncertainty $\sim 3\%$ within $M_W/2 < \mu_{\text{ren/fact}} < 2M_W$ in NLO ($\sim 10\%$ in LO)
- sensitivity to cuts: large for **QCD**, small for **EW** corrections
- heavy-Higgs corrections at $M_H \sim 700$ GeV: $\underbrace{G_\mu M_H^2}_{1\text{-loop}} \sim \underbrace{(G_\mu M_H^2)^2}_{2\text{-loop}} \sim 4\%$
 \hookrightarrow breakdown of perturbation theory

Size of specific corrections and subcontributions to cross sections:

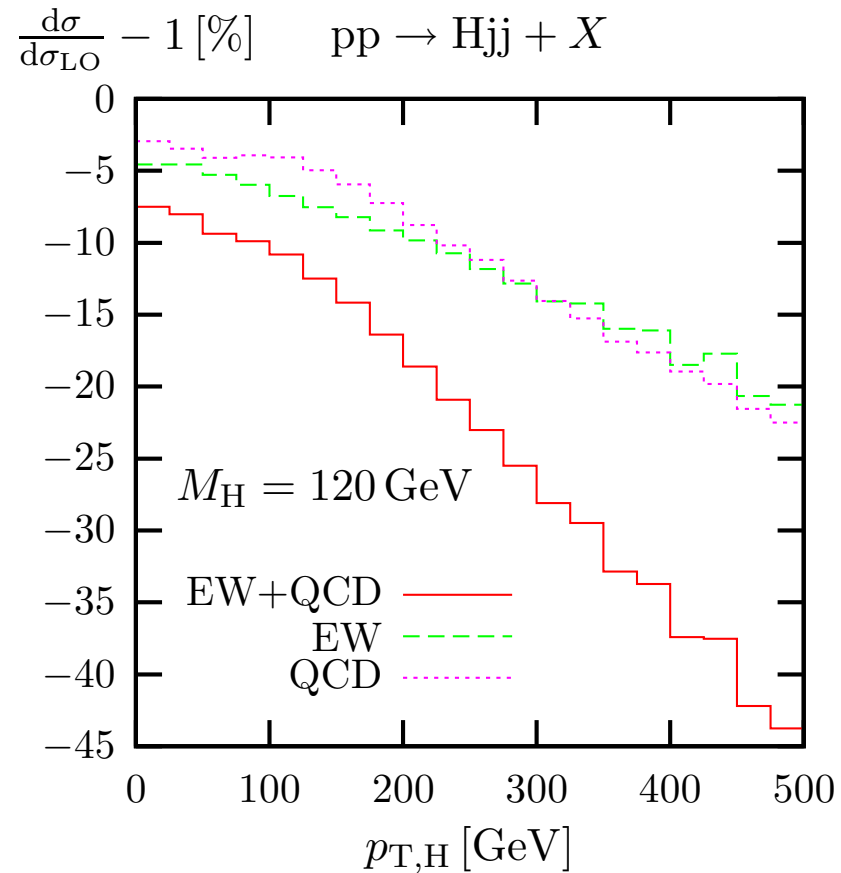
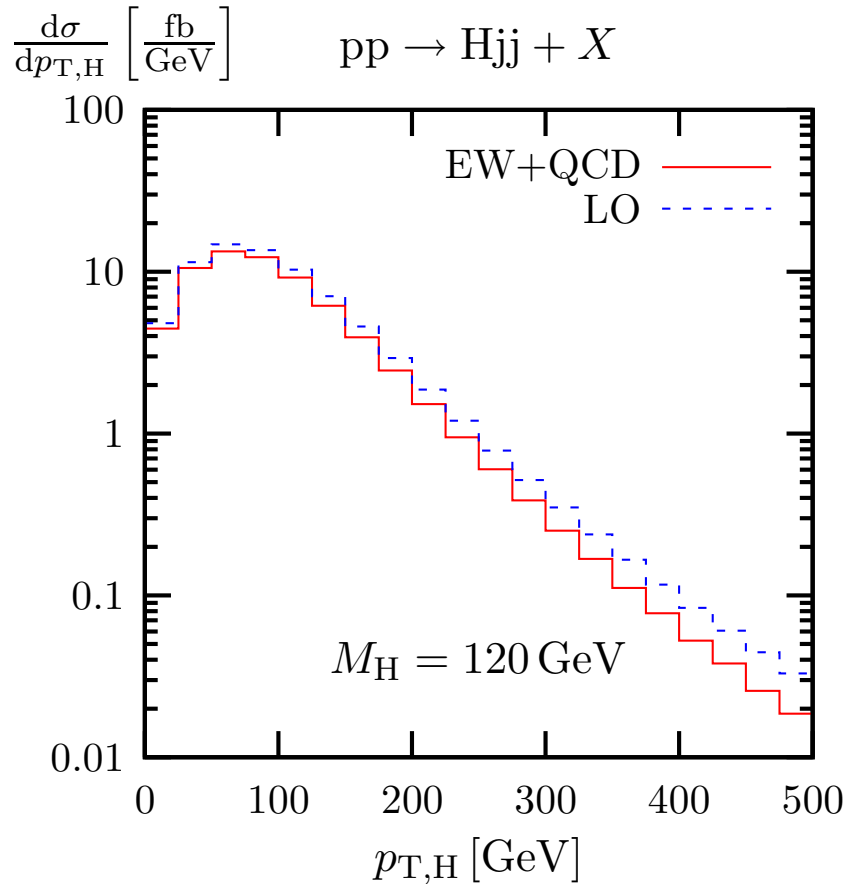
Ciccolini, Denner,
S.D. '07

M_H [GeV]	no cuts		VBF cuts		
	120–200	700	120–200	700	
various corrections:					
$\delta_{\text{QCD(a)}} [\%]$	4–0.5	+1	≈ -5	-7	$\mathcal{O}(5-10\%)$
$\delta_{\text{QCD(b+c+d)}} [\%]$	$\lesssim 0.2$	-0.1	< 0.1	< 0.1	negligible
$\delta_{\text{EW,qq}} [\%]$	≈ -6	+6	≈ -7	+5	$\mathcal{O}(5-10\%)$
$\delta_{\text{EW,q}\gamma} [\%]$	$\approx +1$	+2	$\approx +1$	+2	
$\delta_{G_\mu^2 M_H^4} [\%]$	< 0.1	+4	< 0.1	+4	negligible for $M_H < 400$ GeV
specific contributions:					
$\Delta_{s\text{-channel}} [\%]$	30–10	1	< 0.6	< 0.1	negligible with VBF cuts
$\Delta_{t/u\text{-interference}} [\%]$	< 0.5	< 0.1	< 0.1	< 0.1	negligible
$\Delta_{b\text{-quarks}} [\%]$	≈ 4	1	≈ 2	1	

3.2 Selected results on differential cross sections

Distribution in the Higgs transverse momentum $p_{T,H}$

Ciccolini, Denner, S.D. '07

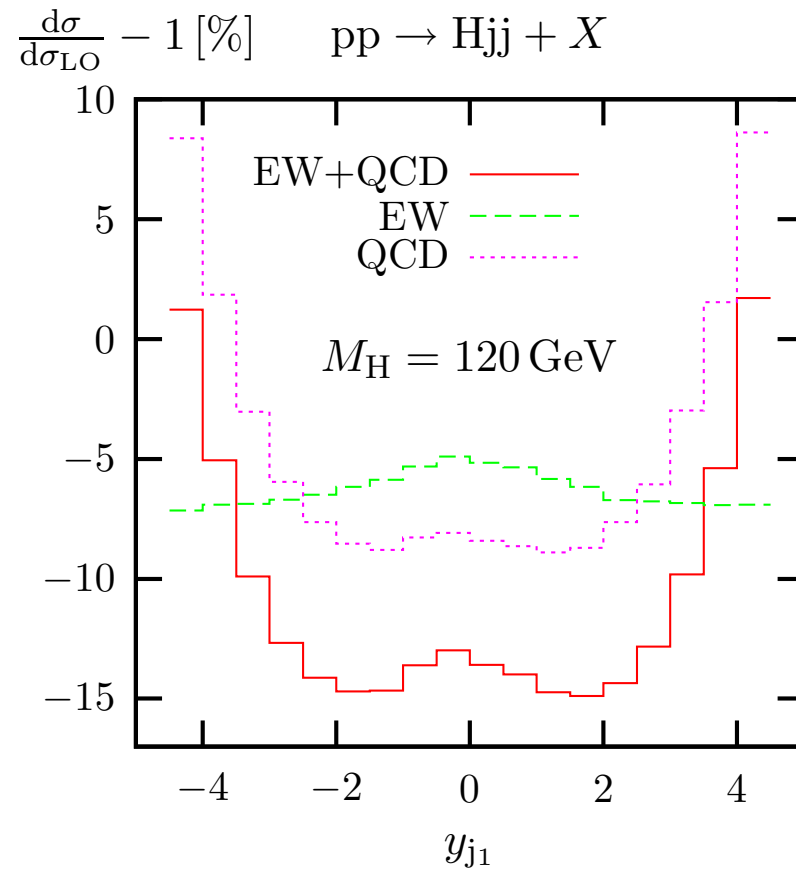
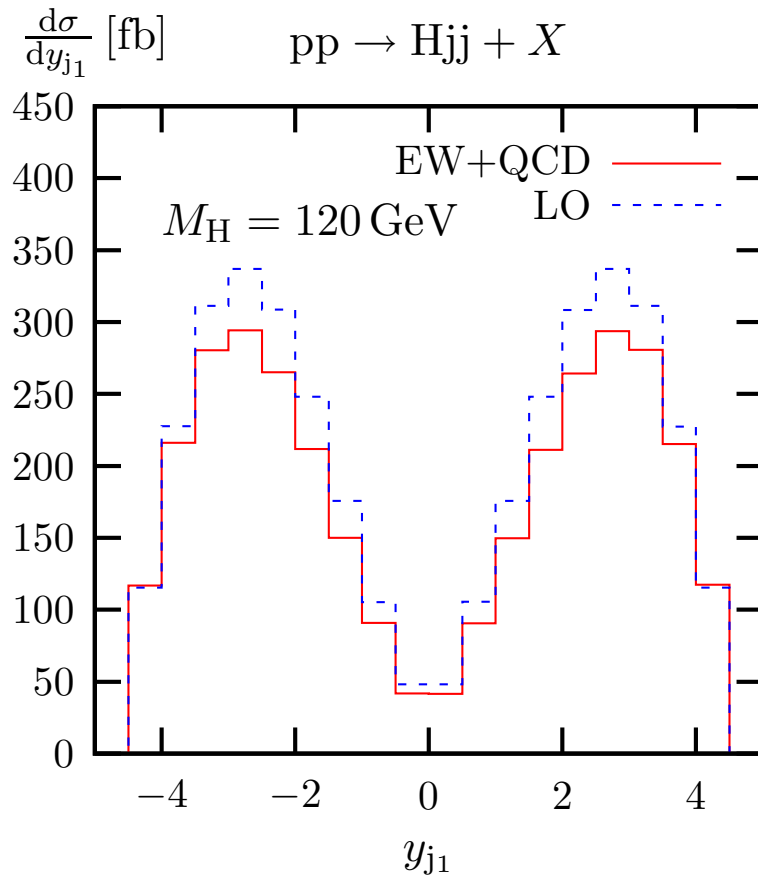


↪ QCD and EW corrections distort shapes

QCD+EW $\sim 20\%(40\%)$ at $p_{T,H} = 200 \text{ GeV}(500 \text{ GeV})$

Distribution in the rapidity y_{j_1} of the leading tagging jet

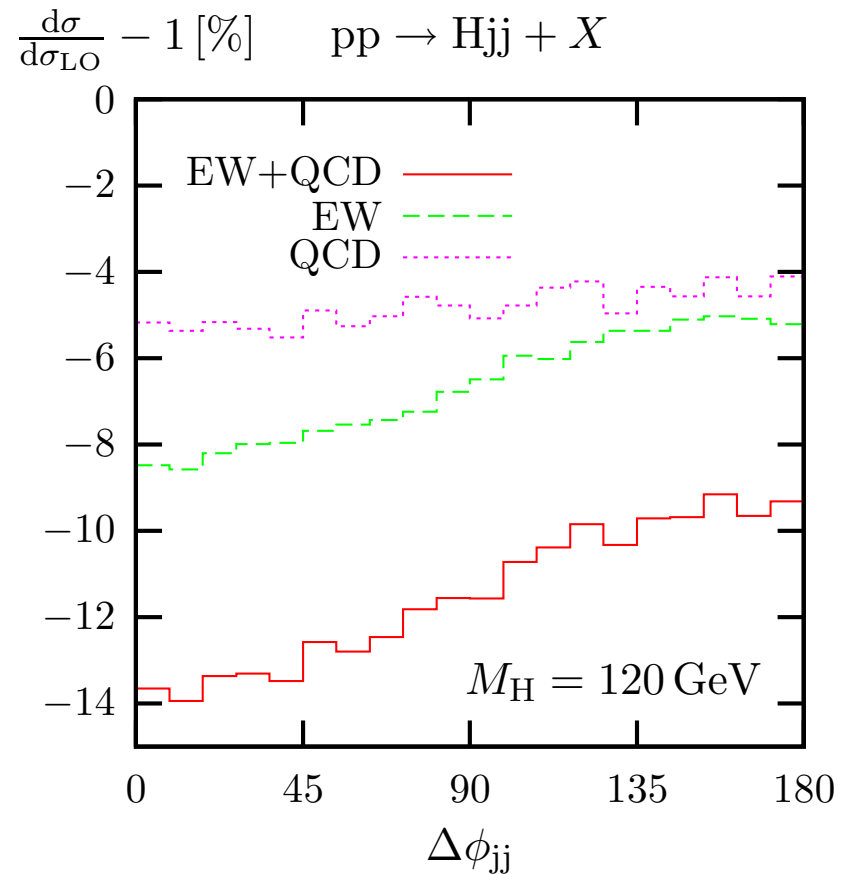
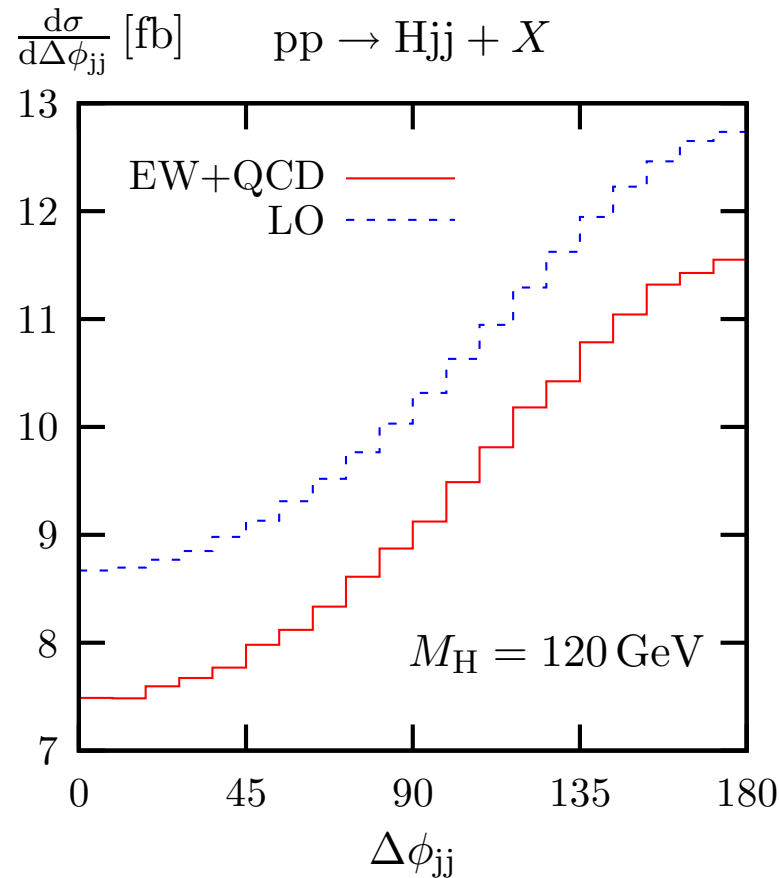
Ciccolini, Denner, S.D. '07



↪ Significant shape distortions by QCD effects, but EW effects almost uniform

Distribution in the azimuthal angle difference $\Delta\phi_{jj}$ of the tagging jets

Ciccolini, Denner, S.D. '07



↪ QCD+EW corrections induce small distortions similar to BSM effects

4 Conclusions

Higgs production via VBF is important at the LHC

- for Higgs discovery
- for Higgs coupling analyses

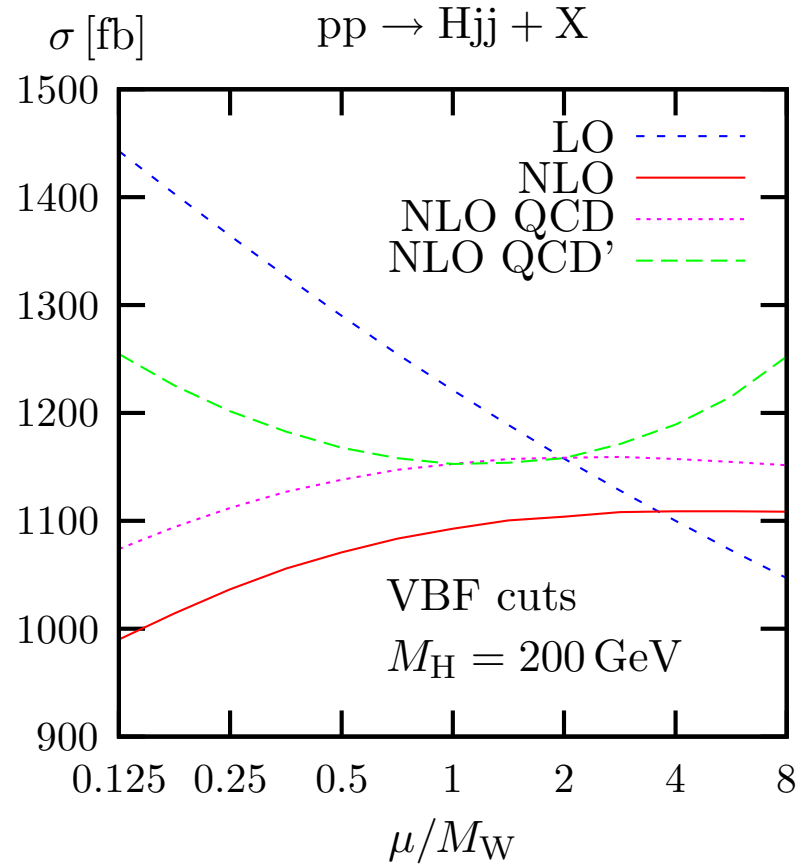
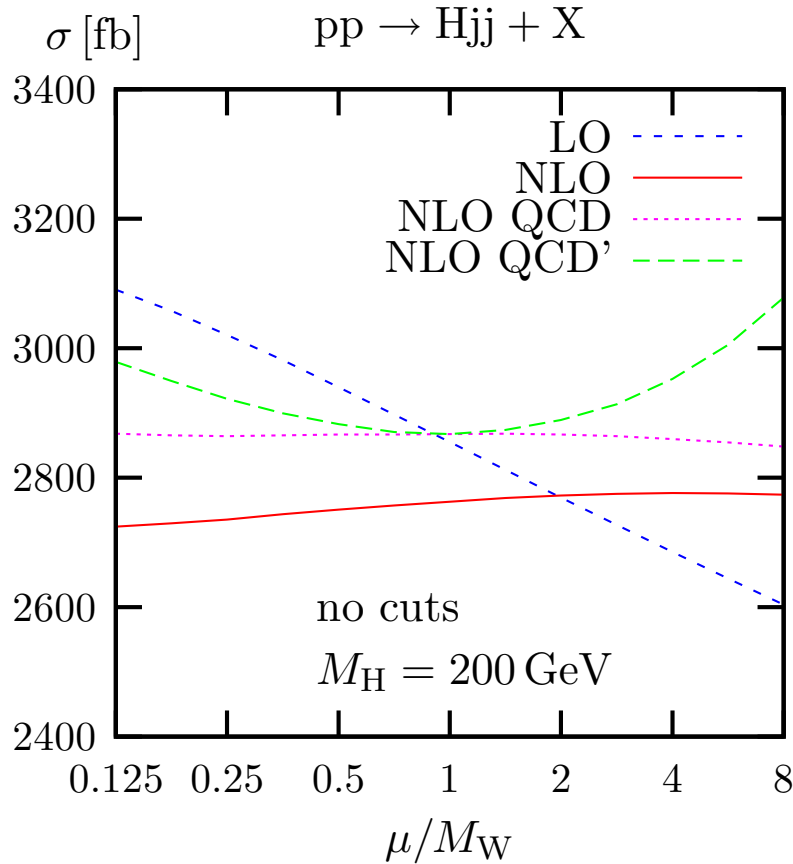
Recent progress in predictions:

- Full NLO QCD confirms validity of old “ t -channel approximation” for VBF setup
 - NLO EW corrections are as important as NLO QCD effects:
 - ◇ each = $\mathcal{O}(5-10\%)$ for cross sections
 - ◇ larger corrections to distributions which get distorted
 - ◇ heavy-Higgs effects negligible for $M_H < 400$ GeV,
but 1-loop \sim 2-loop at $M_H \sim 700$ GeV (breakdown of perturbation theory)
 - Suppressed effects ($\lesssim 1-2\%$ at least in VBF setup):
b-quarks in initial/final states, photon-induced processes, s -channel contributions,
interferences among $s/t/u$ channels, gluon-induced strong/weak interferences
- ↪ Theoretical accuracy (for intermediate Higgs masses)
matches uncertainties from PDFs and expected experimental errors

Extra slides

Scale dependence of LO and NLO cross sections

Ciccolini, Denner, S.D. '07

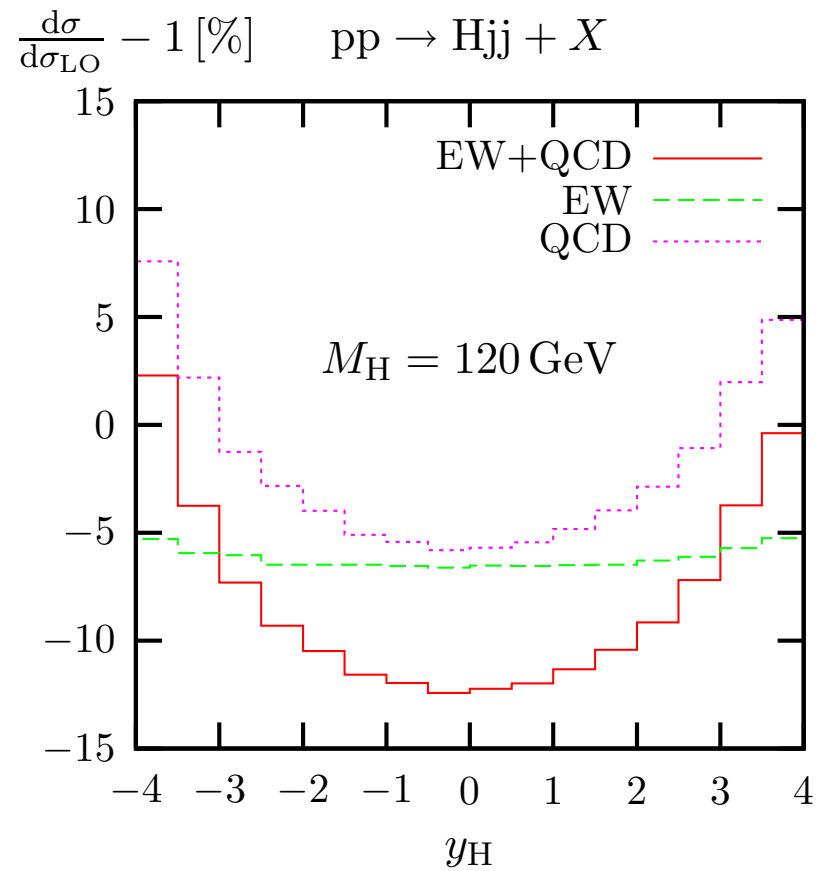
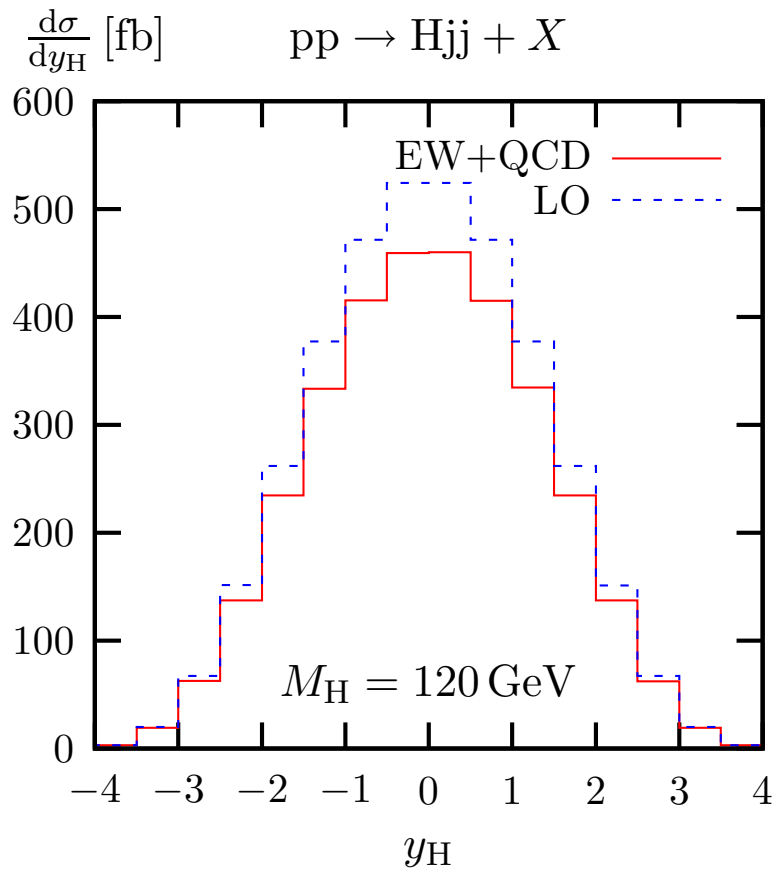


QCD: $\mu = \mu_{\text{fact}} = \mu_{\text{ren}}$

QCD': $\mu = \mu_{\text{fact}} = M_W^2 / \mu_{\text{ren}}$

Higgs rapidity distribution

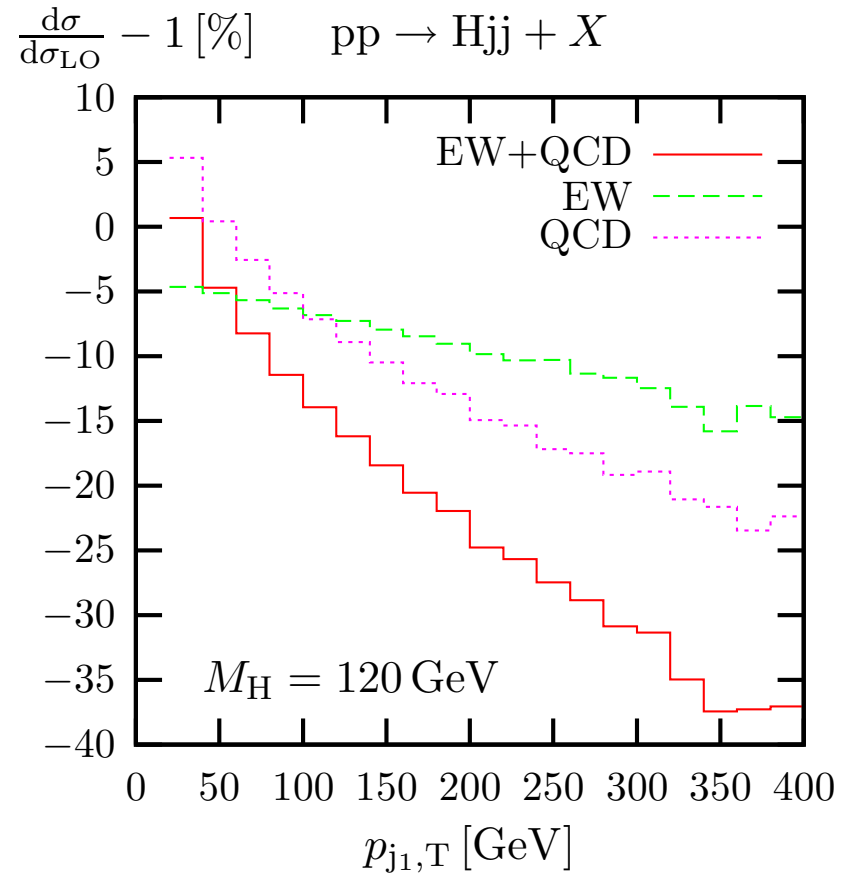
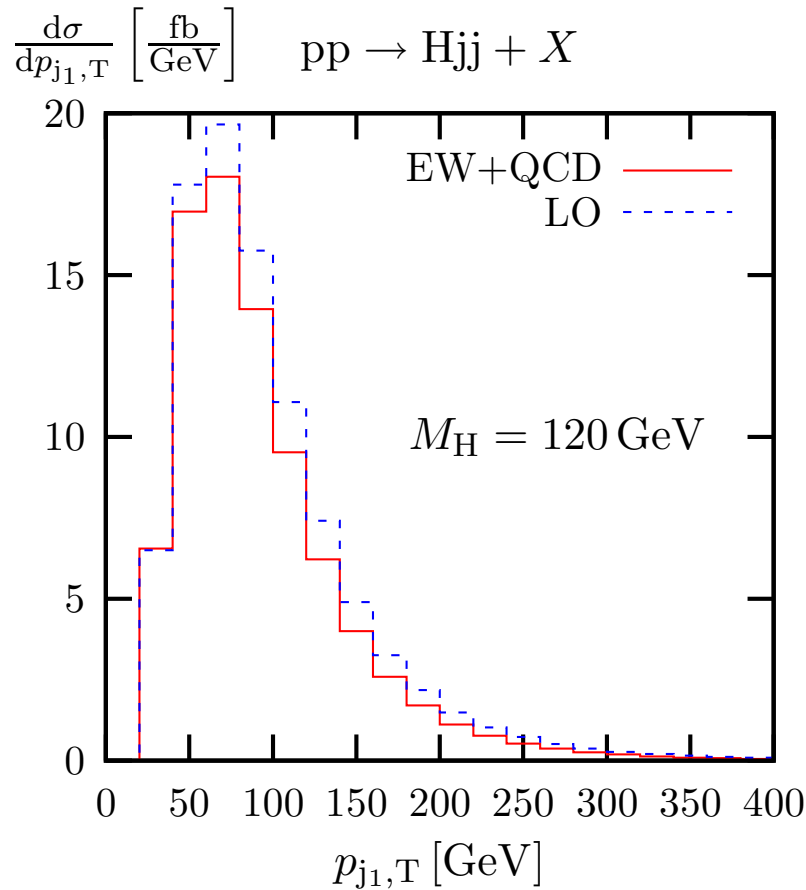
Ciccolini, Denner, S.D. '07



↪ Significant shape distortions by QCD effects, but EW effects almost uniform

Distribution in the transverse momentum p_{Tj_1} of the leading tagging jet

Ciccolini, Denner, S.D. '07

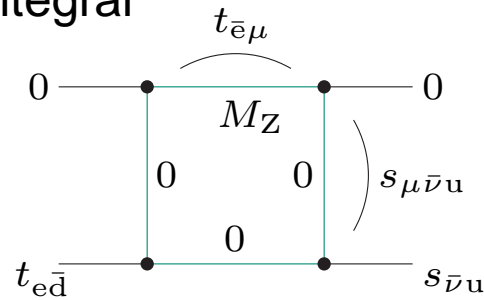


↪ QCD and EW corrections distort shapes

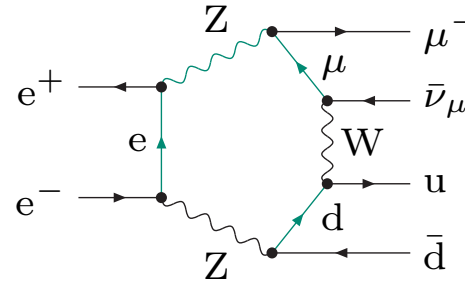
QCD+EW $\sim 25\%(40\%)$ at $p_{T,H} = 200 \text{ GeV}(500 \text{ GeV})$

A typical example with small Gram determinant:

Box integral



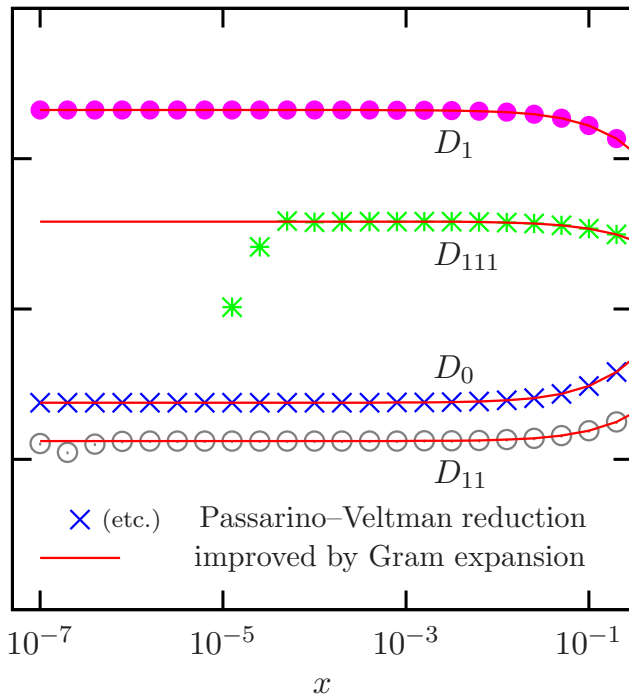
appears, e.g., in subgraph of diagram



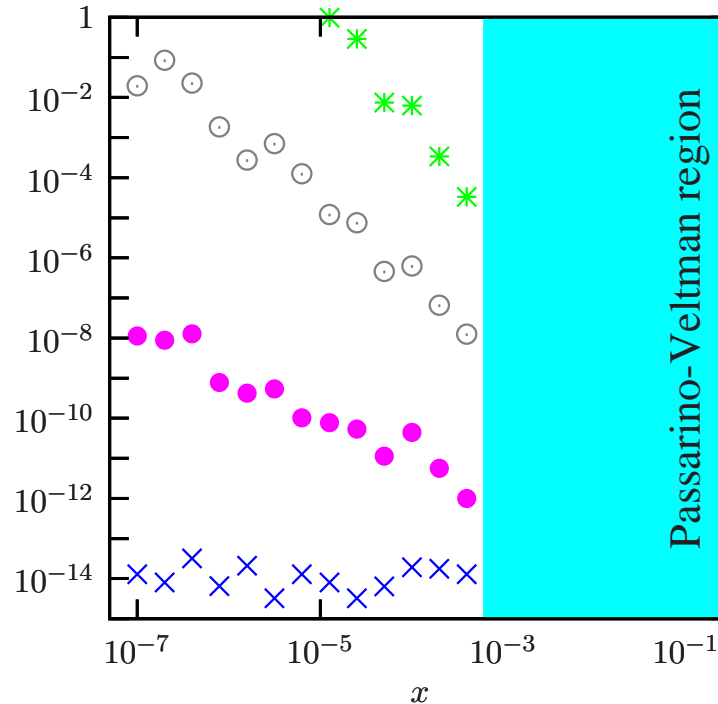
Gram det.: $\det(\text{Gram}) \rightarrow 0$ if $t_{e\bar{d}} \rightarrow t_{\text{crit}} \equiv \frac{s_{\mu\nu u}(s_{\mu\nu u} - s_{\nu u} + t_{\bar{e}\mu})}{s_{\mu\nu u} - s_{\nu u}}$

Numerical comparison: maximal tensor rank = 6 (similar to $ee \rightarrow 4f$ application)

Absolute predictions



Relative deviations from "best"



$$x \equiv \frac{t_{e\bar{d}}}{t_{\text{crit}}} - 1$$

$$s_{\mu\nu u} = +2 \times 10^4 \text{ GeV}^2$$

$$s_{\nu u} = +1 \times 10^4 \text{ GeV}^2$$

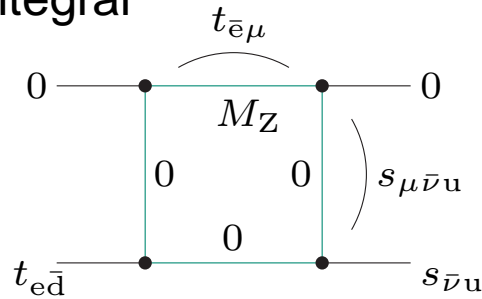
$$t_{\bar{e}\mu} = -4 \times 10^4 \text{ GeV}^2$$

$$t_{\text{crit}} = -6 \times 10^4 \text{ GeV}^2$$

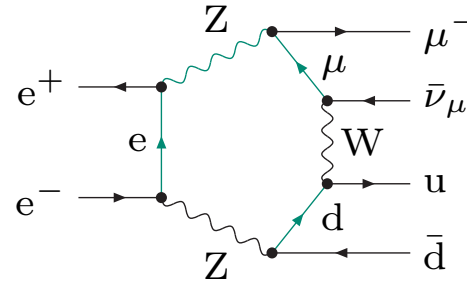
PV reduction breaks down, but Gram exp. stable for $\det(\text{Gram}) \rightarrow 0$!

A typical example with small Gram determinant:

Box integral



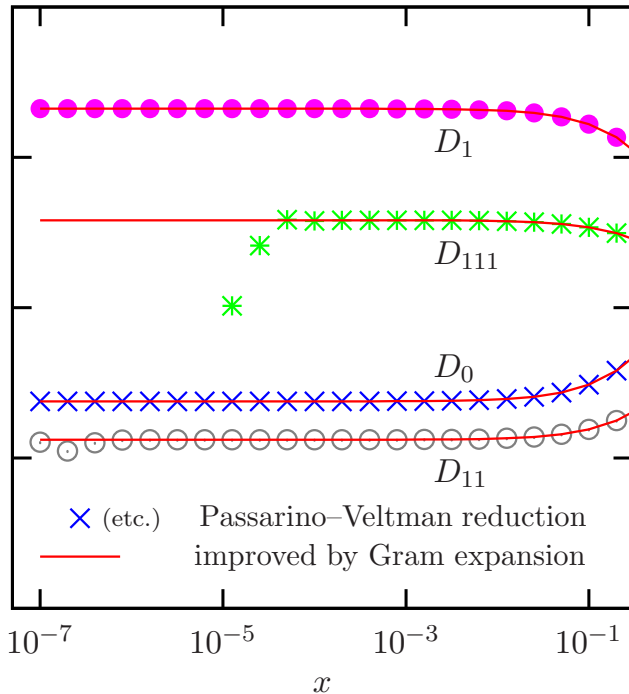
appears, e.g., in subgraph of diagram



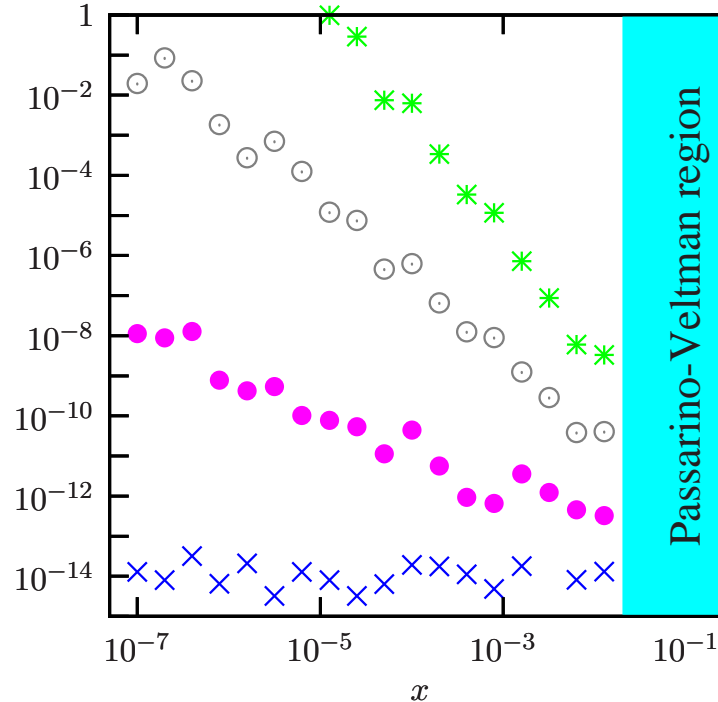
Gram det.: $\det(\text{Gram}) \rightarrow 0$ if $t_{e\bar{d}} \rightarrow t_{\text{crit}} \equiv \frac{s_{\mu\nu u}(s_{\mu\nu u} - s_{\nu u} + t_{\bar{e}\mu})}{s_{\mu\nu u} - s_{\nu u}}$

Numerical comparison: maximal tensor rank = 12

Absolute predictions



Relative deviations from "best"



$$x \equiv \frac{t_{e\bar{d}}}{t_{\text{crit}}} - 1$$

$$s_{\mu\nu u} = +2 \times 10^4 \text{ GeV}^2$$

$$s_{\nu u} = +1 \times 10^4 \text{ GeV}^2$$

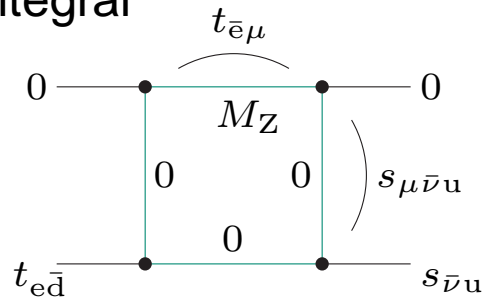
$$t_{\bar{e}\mu} = -4 \times 10^4 \text{ GeV}^2$$

$$t_{\text{crit}} = -6 \times 10^4 \text{ GeV}^2$$

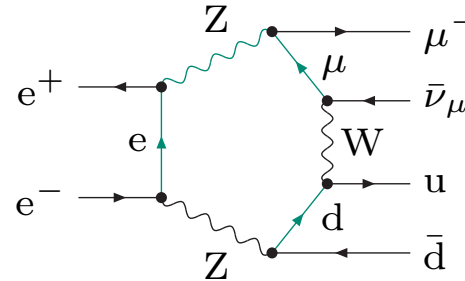
PV reduction breaks down,
but Gram exp. stable
for $\det(\text{Gram}) \rightarrow 0$!

A typical example with small Gram determinant:

Box integral



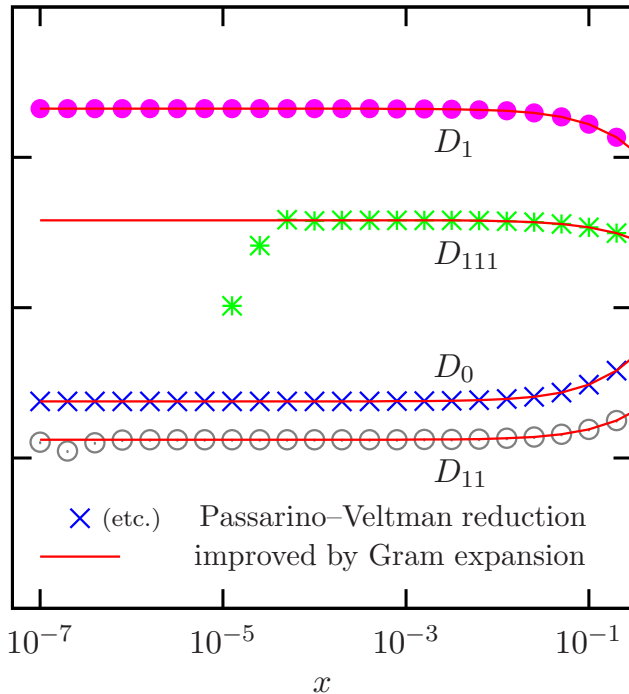
appears, e.g., in subgraph of diagram



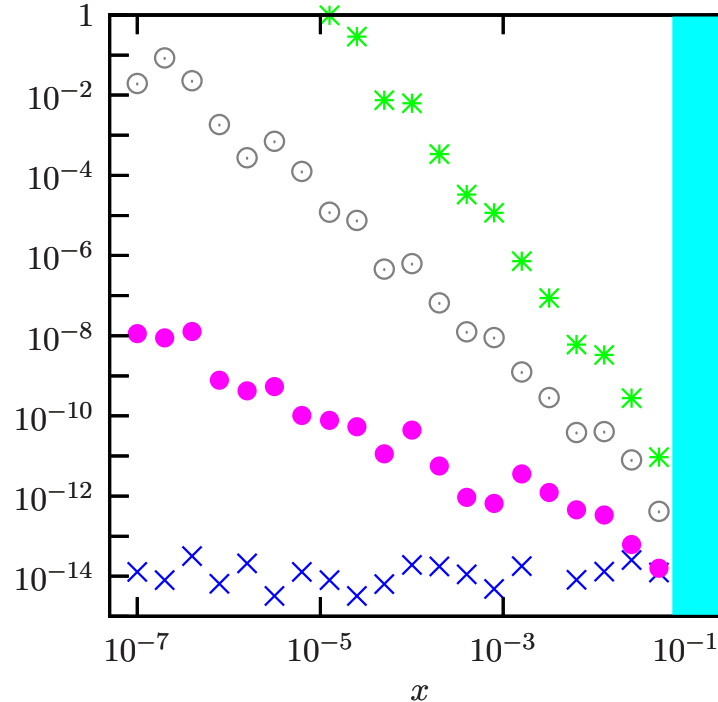
Gram det.: $\det(\text{Gram}) \rightarrow 0$ if $t_{e\bar{d}} \rightarrow t_{\text{crit}} \equiv \frac{s_{\mu\nu u}(s_{\mu\nu u} - s_{\nu u} + t_{\bar{e}\mu})}{s_{\mu\nu u} - s_{\nu u}}$

Numerical comparison: maximal tensor rank = 25

Absolute predictions



Relative deviations from "best"



$$x \equiv \frac{t_{e\bar{d}}}{t_{\text{crit}}} - 1$$

$$s_{\mu\nu u} = +2 \times 10^4 \text{ GeV}^2$$

$$s_{\nu u} = +1 \times 10^4 \text{ GeV}^2$$

$$t_{\bar{e}\mu} = -4 \times 10^4 \text{ GeV}^2$$

$$t_{\text{crit}} = -6 \times 10^4 \text{ GeV}^2$$

PV reduction breaks down,
but Gram exp. stable
for $\det(\text{Gram}) \rightarrow 0$!