



Towards NLO predictions for 4 b-jets at the LHC

supported by the Scottish
Universities Physics Alliance



in collaboration with T. Binoth, A. Guffanti,
J.-Ph. Guillet, J. Reuter

- ▷ Thomas Reiter, The University of Edinburgh
- ▷ Loopfest VII, Buffalo, 16 May 2008



Overview

The Promise of the LHC

Structure of the Amplitude

Golem90: Numerical Reduction of Tensor Integrals

The Status of the Calculation

To-Do List



The Promise of the LHC

If the SM (MSSM) is implemented in nature

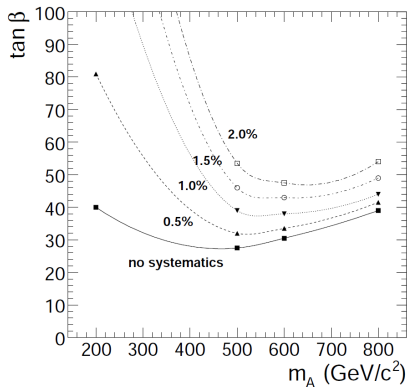
- ▶ the LHC will find the SM Higgs boson or ...
- ▶ ... at least one MSSM Higgs boson.
- ▶ “At large $\tan \beta$ the $b\bar{b}\tau^+\tau^-$ and $b\bar{b}b\bar{b}$ final states may provide the only access to two of the three neutral MSSM Higgs bosons.” [Dai, Gunion, Vega (1995); also Richter-Was, Froidevaux]
- ▶ Number of assumptions about irreducible QCD backgrounds spoil the result.
- ▶ “Explicit calculations of the actual K factors are needed.” [ibid.]

$$b\bar{b}H \rightarrow b\bar{b}b\bar{b}$$

Effect of background uncertainty
on discovery reach (2σ contours)

- ▶ big improvements possible by
NLO background calculation
- ▶ in combination with $b\bar{b}\tau^+\tau^-$
good prospects

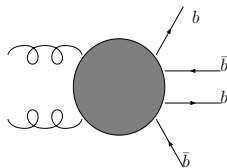
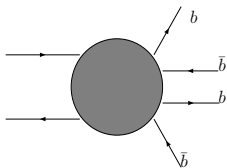
[Fig.: CMS Physics TDR]





The $q\bar{q} \rightarrow b\bar{b}b\bar{b}$ Process

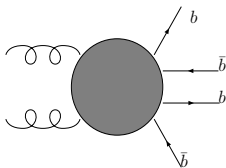
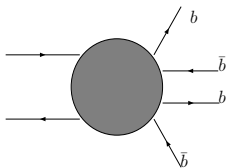
- ▶ $pp \rightarrow b\bar{b}b\bar{b}$ irreducible background for SUSY Higgs searches.
- ▶ 4- b and 4-jet are on the Experimentalists' Wish List.
[Les Houches 2007]
- ▶ $q\bar{q} \rightarrow b\bar{b}s\bar{s}$ is subprocess of 4-jets and (up to combinatorics) of $pp \rightarrow b\bar{b}b\bar{b}$.





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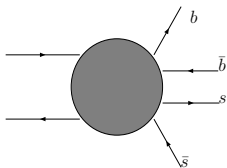
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The Structure of the Amplitude

The full NLO cross-section can be written as

$$\sigma^{\text{NLO}} = \int_N d\sigma^{\text{LO}} + \int_N \left(d\sigma^{\mathcal{V}} + \int_1 d\sigma^{\mathcal{A}} \right)_{\epsilon=0} + \int_{N+1} \left(d\sigma^{\mathcal{R}} - d\sigma^{\mathcal{A}} \right)_{\epsilon=0}$$

- ▶ leading order contribution
- ▶ virtual corrections
- ▶ real emission
- ▶ subtraction terms [Catani, Seymour]

This talk: mainly $\int_N (d\sigma^{\mathcal{V}} + \int_1 d\sigma^{\mathcal{A}})_{\epsilon=0}$



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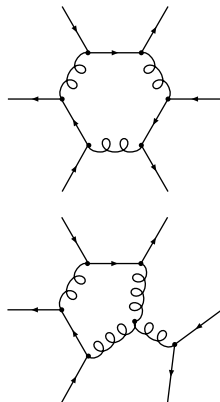
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The Structure of the Virtual Corrections

- ▶ Feynman diagram based approach
- ▶ High complexity due to pentagons and hexagons
- ▶ Standard techniques typically fail
- ▶ Improved reduction method for tensor integrals
- ▶ No complete calculation of this complexity for LHC published yet





The Structure of the Virtual Corrections (II)

Using **helicity projections**:

$$d\sigma^\nu = d\Phi^{(N)} \sum_{\{\lambda\}} \left(\mathcal{M}^{\text{LO}}(\{\lambda\}, \{p\})^\dagger \otimes \mathcal{M}^\nu(\{\lambda\}, \{p\}) + \text{h.c.} \right) F_j^{(N)}$$

$$\mathcal{M}_i^\nu = c(\{\lambda\}, \{p\}) \sum_{\text{diagrams}} \sum_{\mathcal{F}} \text{tr}^{\{\lambda\}} \{ \{p\}_{i,\mathcal{F}} \} \mathcal{F}(S)$$

$$\mathcal{F}(S) \in \left\{ A^{N',r}(j_1, \dots; S), B^{N',r}(j_1, \dots; S), C^{N',r}(j_1, \dots; S) \right\}$$

- ▶ Form factors $\mathcal{F}(S)$ from tensor integrals (see next slide).
- ▶ Coefficients products of Dirac traces $\text{tr}^{\{\lambda\}} \{ \{p\}_{i,\mathcal{F}} \}$.
- ▶ Non-trivial color structure \Rightarrow Color flow decomposition



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The Structure of the Virtual Corrections(III)

Form factor representation for tensor integrals

$$\begin{aligned}
 \int \frac{d^n k q_{a_1}^{\mu_1} \cdots q_{a_r}^{\mu_r}}{(q_1^2 - m_1^2) \cdots (q_N^2 - m_N^2)} &= \sum_{j_1, \dots, j_r} [\Delta_{j_1 \bullet}^\bullet \cdots \Delta_{j_r \bullet}^\bullet]_{a_1, \dots, a_r}^{\mu_1 \dots \mu_r} A_{j_1, \dots, j_r}^{N, r}(S) \\
 &+ \sum_{j_1, \dots, j_{r-2}} [g^{\bullet\bullet} \Delta_{j_1 \bullet}^\bullet \cdots \Delta_{j_{r-2} \bullet}^\bullet]_{a_1, \dots, a_r}^{\mu_1 \dots \mu_r} B_{j_1, \dots, j_{r-2}}^{N, r}(S) \\
 &+ \sum_{j_1, \dots, j_{r-4}} [g^{\bullet\bullet} g^{\bullet\bullet} \Delta_{j_1 \bullet}^\bullet \cdots \Delta_{j_{r-4} \bullet}^\bullet]_{a_1, \dots, a_r}^{\mu_1 \dots \mu_r} C_{j_1, \dots, j_{r-4}}^{N, r}(S)
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Go1em90: Tensor Reduction made Easy

Reduction of the tensor integrals:

- ▶ one of the main problems in (one) loop calculations:
- ▶ Either avoid it... [Unitarity methods: many names]
- ▶ ...or do it in a smart way.
- ▶ We use algebraic/numerical approach.
[Binoth, Guillet, Heinrich, Pilon, Schubert]
 - ▶ Reduction of 1- and 2-point integrals: trivial
 - ▶ Reduction of ($N \geq 5$) point integrals:
always reduce to 3- and 4-point problems
- ▶ What about 3- and 4-point integrals?



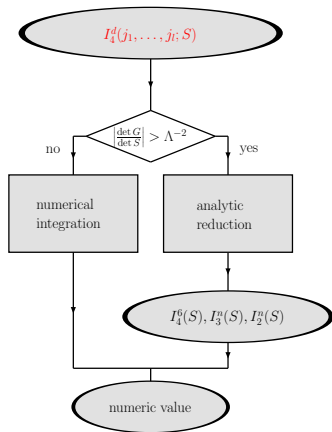
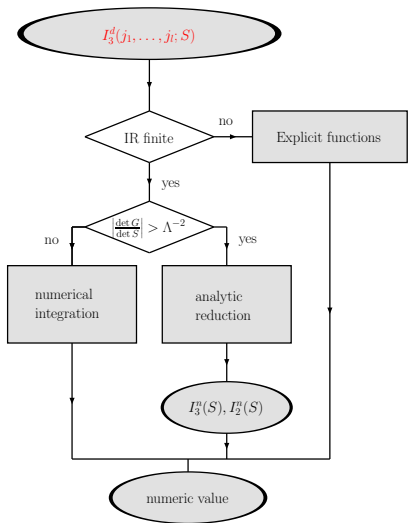
Go1em90: Tensor Reduction made Easy (II)

Use of extended set of basis functions

$$A^{N,r}(S), B^{N,r}(S), C^{N,r}(S) \rightsquigarrow I_N^d(j_1, \dots, j_l; S)$$

$$I_N^d(j_1, \dots, j_l; S) = (-1)^N \Gamma(N - d/2) \times \\ \int_0^1 dz_1 \cdots dz_N \delta(1 - \sum z_i) \frac{z_{j_1} \cdots z_{j_l}}{(-\frac{1}{2} z_i S_{ik} z_k - i\delta)^{N-d/2}}$$

- ▶ Required for $N \in \{3, 4\}$ only
- ▶ Reduction and numerical calculation possible



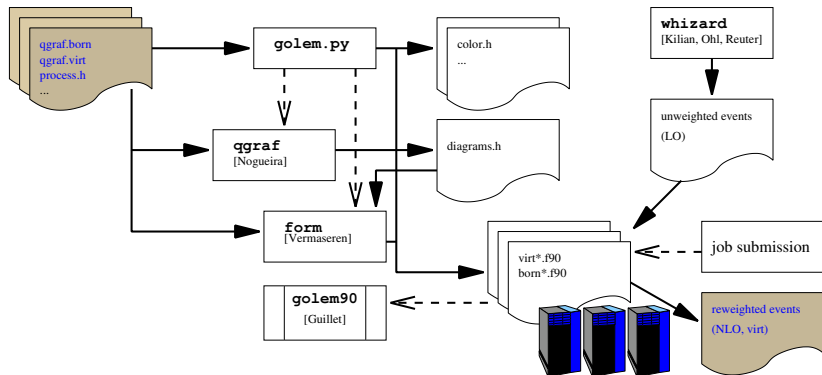


Preliminary Setup

Tensor reduction is only part of a larger setup:

- ▶ Formfactors $A^{N,r}$, $B^{N,r}$, $C^{N,r}$ implemented in Go1em90
- ▶ Automated framework to build amplitude (see next slides)
- ▶ Aim: start from minimal set of input files

Preliminary Setup





Results: $u\bar{u} \rightarrow b\bar{b}s\bar{s}$ (virtual)

Results are based on

- ▶ 200,000 unweighted LO-events, generated from Whizard [Ohl,Kilian,Reuter]
- ▶ reweighted with local K-factor
- ▶ cuts: $p_T > 50$ GeV, $\eta < 3$, $\Delta R > 0.3$
- ▶ $\mu = \sum p_T/4$, $\mu_F = 100$ GeV, CTEQ6m, $\sqrt{s} = 14$ TeV

$$\langle O \rangle_{\text{LO}} = \frac{\sigma^{\text{LO}}}{N} \sum_E O(E)$$

$$\langle O \rangle_{\mathcal{V}} = \frac{\sigma^{\text{LO}}}{N} \sum_E \frac{d\sigma^{\text{LO}} + d\sigma^{\mathcal{V}} + \int_1 d\sigma^{\mathcal{A}}}{d\sigma^{\text{LO}}} O(E)$$

$E \in$ unweighted events

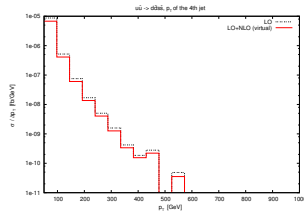
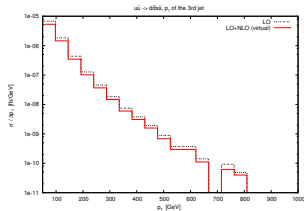
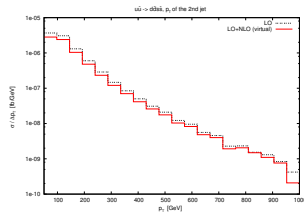
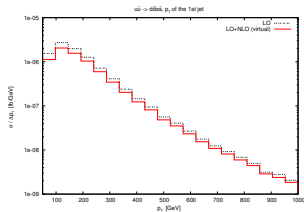


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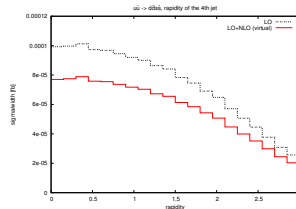
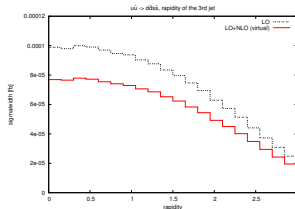
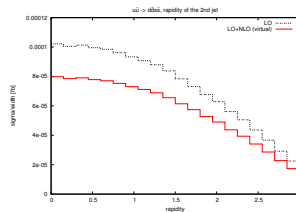
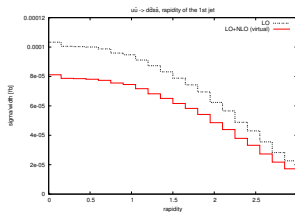
We find

- ▶ Numerical evaluation very stable:
 1. cancellation of IR-poles
all points passed test
 2. “suspicious” points (i.e. $K > 10$)
2.4‰ failed, re-evaluated with quadruple precision
- ▶ K-factor contribution: **0.78** ($\pm 0.22\%$ stat.)

p_T Distributions: $u\bar{u} \rightarrow b\bar{b}s\bar{s}$ (virtual)



Rapidity Distributions: $u\bar{u} \rightarrow b\bar{b}s\bar{s}$ (virtual)





Tests

- Comparison diagram by diagram for single phase space points by two independent codes:

	This Code	Alternative
Diagram Generation	QGraf	Feynarts
Simplification	Form	Form, Maple
Representation	numerical form factors	analytic basis integrals
Numerical Evaluation	Fortran90	Maple

- Cancellation of infrared poles
- Independent analytic calculation for up to 3-point diagrams.



Nowadays people ask about ...

On a single computer (4× Intel[®] Xeon[®], 3 GHz)

- ▶ $\mathcal{O}(1s)$ per phase space point.
(includes all helicities, all colors: no hidden cost)
- ▶ 200k points took 60 CPUh.
- ▶ My opinion: performance debate is overrated:
 - ▶ Problem is "Embarrassingly Parallel"
 - ▶ Edinburgh Compute and Data Facility (ECDF)
 - ▶ 200k points took 12 minutes (on 345 nodes).
 - ▶ CPU time is relatively cheap: $\approx 10g$ of peanuts
 - ▶ ... compared to a PhD-student: ≈ 20 tons of peanuts.



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 - ▶ ... compared to a PhD-student: ≈ 20 tons of peanuts.



Nowadays people ask about run time

On a single computer (4× Intel[®] Xeon[®], 3 GHz)

- ▶ $\mathcal{O}(1s)$ per phase space point.
(includes all helicities, all colors: no hidden cost)
- ▶ 200k points took 60 CPUh.
- ▶ My opinion: performance debate is overrated:
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Conclusion

I have presented

- ▶ first results for 6-quark amplitude
- ▶ outline of a (fairly) automated, Feynman diagram based, NLO matrix element generator (aka GOLEM)
- ▶ application of a Fortran90 library for reduction of tensor integrals (Go1em90)

Currently in progress:

- ▶ real emission and dipoles
- ▶ tighter integration into MC program
- ▶ full $b\bar{b}b\bar{b}$ amplitude
- ▶ Further (long term) targets:
 - ▶ generality (e.g. masses, particle content)
 - ▶ easier setup, more automation
 - ▶ improved performance