

# SUSY-QCD Corrections to Higgs Processes

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# Overview

- Survey of the **MSSM Higgs Sector**
- Status of **SM QCD Corrections** to Higgs Production
- SUSY QCD Corrections:
  - **Gluon fusion**
  - Production of a **Higgs with one b jet**
  - **Pair Production** in Bottom quark fusion
- Summarize and Conclude

# Brief Review of MSSM Higgs Sector

- **MSSM Higgs Sector** = Type II Higgs Doublet Model (2HDM)

$$H_d = \begin{pmatrix} h_d^+ \\ \frac{1}{\sqrt{2}}(v_1 + h_d^0 + i\chi_d^0) \end{pmatrix}, \quad H_u = \begin{pmatrix} \frac{1}{\sqrt{2}}(v_2 + h_u^0 - i\chi_u^0) \\ -h_u^- \end{pmatrix}$$

- After EWSB, **W and Z acquire masses** and set

$$(v_{SM})^2 = (v_1)^2 + (v_2)^2 = (246 \text{ GeV})^2 \rightarrow \boxed{\tan\beta = v_2 / v_1}$$

- **Five physical** degrees of freedom remain:

$$\boxed{h^0, H^0, A^0, H^\pm}$$

- At tree-level, MSSM Higgs sector described by **two parameters  $\tan\beta$  and  $M_A$** :

$$M_{H^\pm}^2 = M_A^2 + M_W^2$$
$$M_{h,H}^2 = \frac{1}{2} \left\{ M_A^2 + M_Z^2 \mp \sqrt{(M_A^2 + M_Z^2)^2 - 4M_Z^2 M_A^2 \cos^2 2\beta} \right\}$$
$$\tan 2\alpha = \tan 2\beta \left( \frac{M_A^2 + M_Z^2}{M_A^2 - M_Z^2} \right)$$

# MSSM Higgs Sector (cont.)

- Tree-level relations receive **large radiative corrections** of order  $(m_t)^4$  !  
(e.g.,  $m_h(max) \approx 130 \text{ GeV}$ )
- These corrections can be accounted for by using **effective  $\alpha$**  and **radiatively-corrected Higgs masses** (e.g., “FeynHiggs”).
- **MSSM Higgs interactions with SM matter:**

	$\phi$	$g_u^\phi$	$g_d^\phi$	$g_V^\phi$
SM	$H$	1	1	1
MSSM	$h$	$\cos \alpha / \sin \beta$	$-\sin \alpha / \cos \beta$	$\sin(\beta - \alpha)$
	$H$	$\sin \alpha / \sin \beta$	$\cos \alpha / \cos \beta$	$\cos(\beta - \alpha)$
	$A$	$1/\text{tg}\beta$	$\text{tg}\beta$	0

(from Muhlleitner and Spira, hep-ph/0612254)



# SUSY QCD Sector

- Concerned with superpartners of gluons (“gluinos”) and quarks (“squarks”)
- Gluinos receive their mass via “Soft SUSY” breaking parameters... i.e., no direct interactions with Higgs bosons ( $m_g = M_3$ ).
- Scalar superpartners of LH and RH fermions mix. Mass eigenstates are related to current eigenstates by mixing angles  $\theta_f$ :

$$\begin{aligned}\tilde{f}_1 &= \tilde{f}_L \cos \theta_f + \tilde{f}_R \sin \theta_f \\ \tilde{f}_2 &= -\tilde{f}_L \sin \theta_f + \tilde{f}_R \cos \theta_f.\end{aligned}$$

$$\sin 2\theta_f = \frac{2m_f(A_f - \mu r_f)}{M_{\tilde{f}_1}^2 - M_{\tilde{f}_2}^2}$$

- Note: mixing effects only important for 3rd generation sfermions
- Couplings to MSSM Higgs bosons:

$$\begin{aligned}g_{\tilde{f}_L \tilde{f}_L}^\phi &= m_f^2 g_1^\phi + M_Z^2 (I_{3f} - e_f \sin^2 \theta_W) g_2^\phi \\ g_{\tilde{f}_R \tilde{f}_R}^\phi &= m_f^2 g_1^\phi + M_Z^2 e_f \sin^2 \theta_W g_2^\phi \\ g_{\tilde{f}_L \tilde{f}_R}^\phi &= -\frac{m_f}{2} (\mu g_3^\phi - A_f g_4^\phi),\end{aligned}$$

$\tilde{f}$	$\phi$	$g_1^\phi$	$g_2^\phi$	$g_3^\phi$	$g_4^\phi$
$\tilde{u}$	$h$	$\cos \alpha / \sin \beta$	$-\sin(\alpha + \beta)$	$-\sin \alpha / \sin \beta$	$\cos \alpha / \sin \beta$
	$H$	$\sin \alpha / \sin \beta$	$\cos(\alpha + \beta)$	$\cos \alpha / \sin \beta$	$\sin \alpha / \sin \beta$
	$A$	0	0	-1	$1/\text{tg} \beta$
$\tilde{d}$	$h$	$-\sin \alpha / \cos \beta$	$-\sin(\alpha + \beta)$	$\cos \alpha / \cos \beta$	$-\sin \alpha / \cos \beta$
	$H$	$\cos \alpha / \cos \beta$	$\cos(\alpha + \beta)$	$\sin \alpha / \cos \beta$	$\cos \alpha / \cos \beta$
	$A$	0	0	-1	$\text{tg} \beta$

# SM Higgs Production: Status of N<sup>n</sup>LO Corrections

- Gluon fusion:

- @ NNLO QCD (large  $m_t$ )
- @ NLO QCD (arbitrary  $m_t$ )
- NNLL soft-gluon resummation

- Weak VBF:

- @ NLO QCD

- “Higgs-strahlung” ( $Wh$  or  $Zh$ ):

- @ NNLO QCD
- @ NLO EW

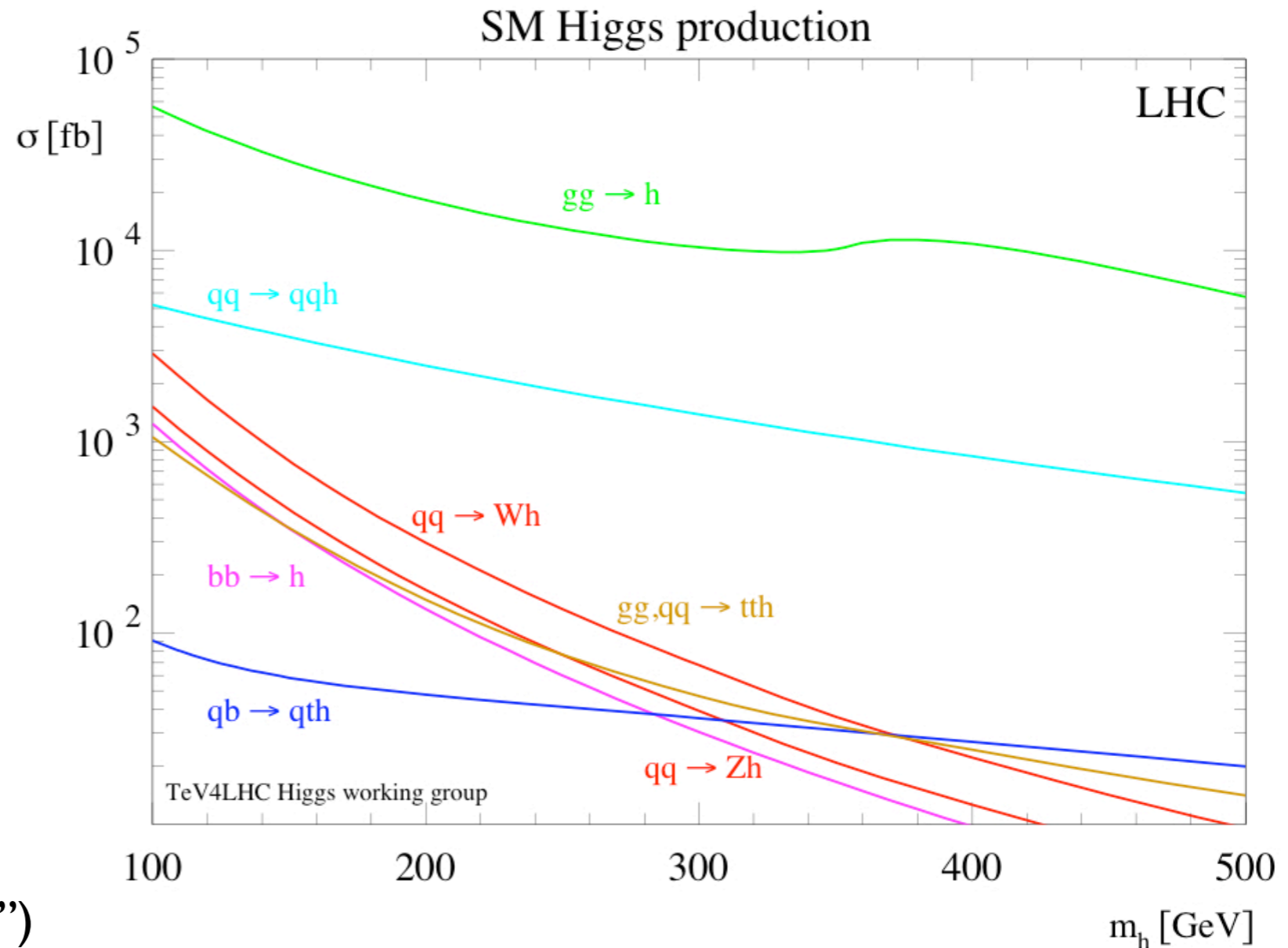
- Production with pairs of tops:

- @ NLO QCD

- Production with bottom quarks:

- $bb \rightarrow h$  @ NNLO QCD (“5FNS”)
- $gg \rightarrow bbh$  @ NLO QCD (“4FNS”)
- Excellent agreement between 5FNS and 4FNS

(from T. Hahn et al., hep-ph/0607308)



# MSSM Higgs Production

- Gluon fusion:

$$\frac{\Gamma(\phi \rightarrow gg)_{\text{MSSM}}}{\Gamma(\phi \rightarrow gg)_{\text{SM}}} \leftarrow \text{ONLY ONE-LOOP SUSY DIAGRAMS!}$$

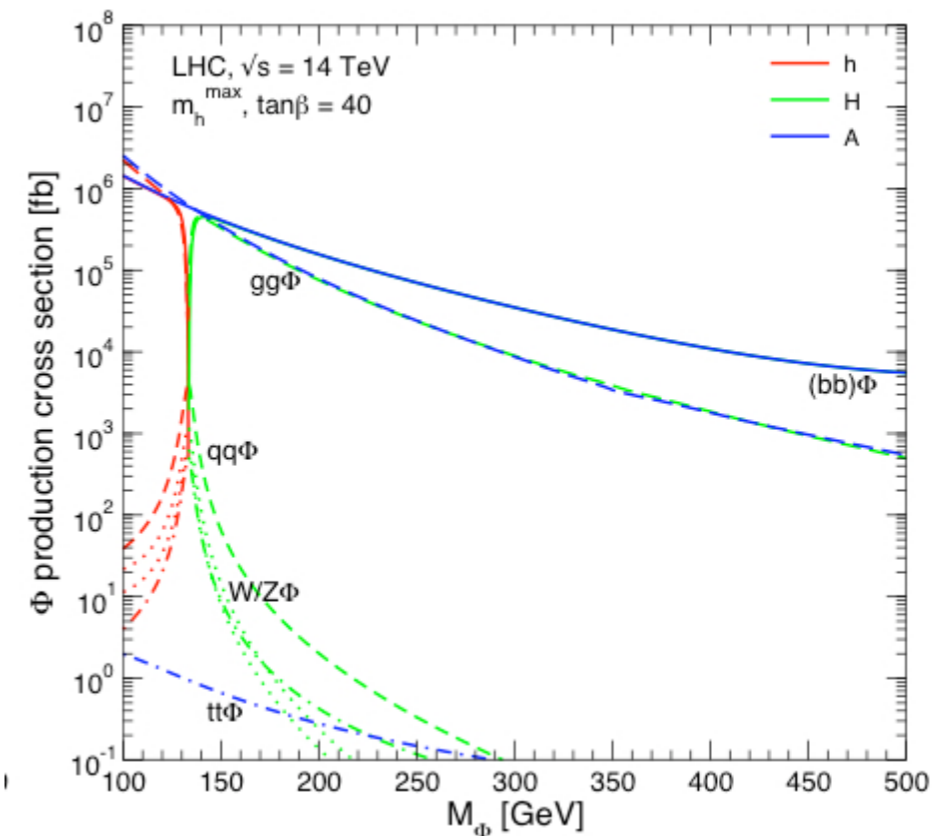
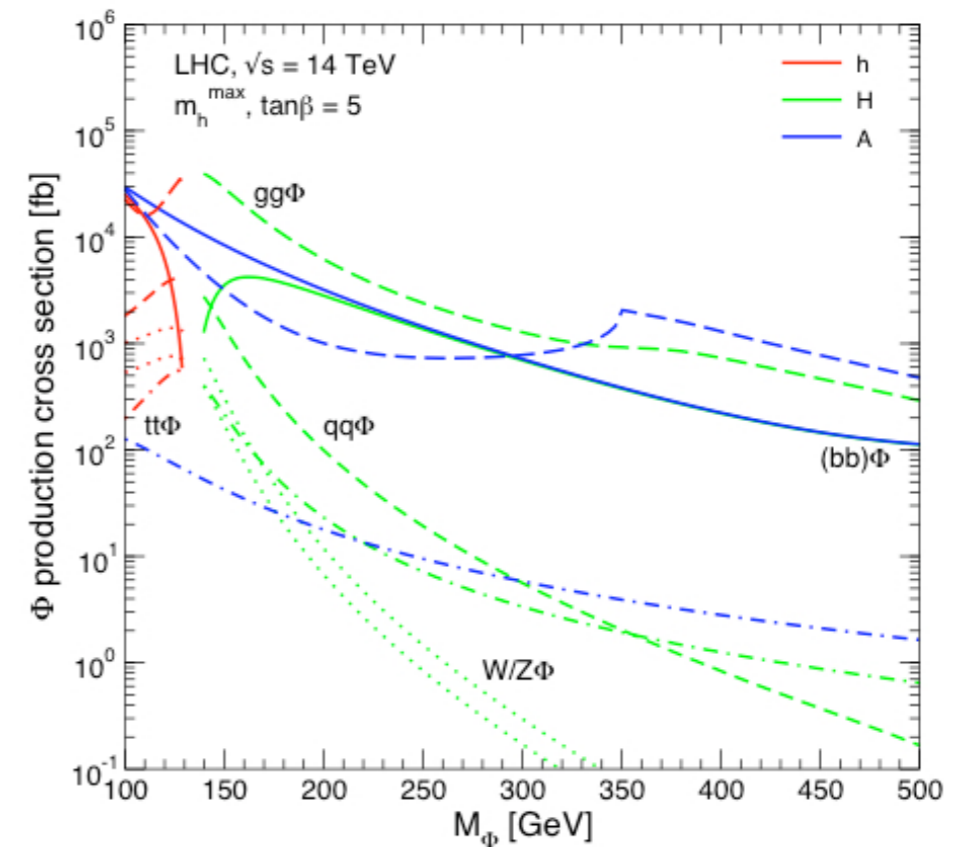
- “Higgs-strahlung” and Weak VBF:

$$\frac{|g_{\phi VV, \text{MSSM}}|^2}{|g_{\phi VV, \text{SM}}|^2}, \quad V = W, Z \leftarrow \text{HIGGS PROPAGATOR CORRECTIONS ONLY!}$$

- Production with Bottom Quarks:

$$bb \rightarrow h: \quad \frac{\Gamma(\phi \rightarrow b\bar{b})_{\text{MSSM}}}{\Gamma(\phi \rightarrow b\bar{b})_{\text{SM}}} \leftarrow \text{INCLUDES FULL QCD + SQCD CORRECTIONS}$$

$$gg \rightarrow bbh: \quad \left( \frac{g_{bbh}^{\text{MSSM}}}{g_{bbh}^{\text{SM}}} \right)^2 \leftarrow \text{INCLUDES SQCD CORRECTIONS TO } bbh \text{ VERTEX... BUT, FOR ON-SHELL QUARKS!}$$

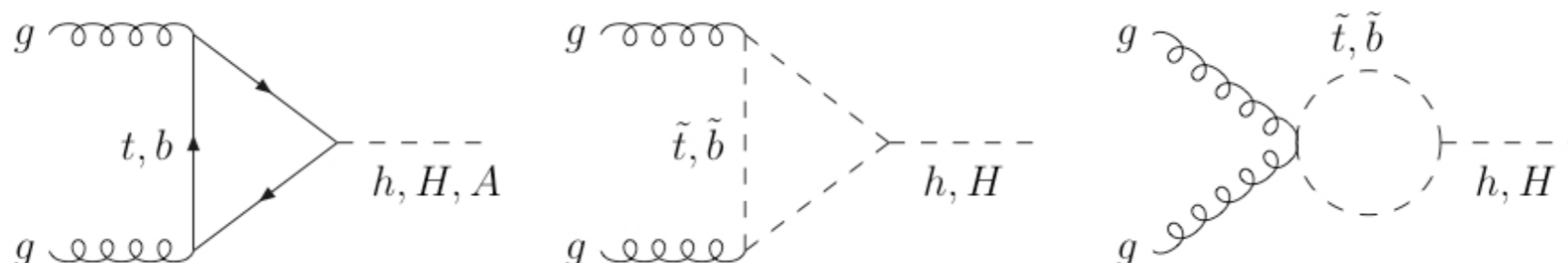


# SQCD Corrections to Gluon Fusion



# Gluon Fusion in SQCD

- In the MSSM, gluon fusion @ LO proceeds via heavy quark and squark loops:



- Pure **SM QCD corrections** to the quark loop amplitudes:
  - $O(\alpha_s^2)$  → S. Dawson; Djouadi, Spira and Zerwas
  - $O(\alpha_s^3)$  → Chetyrkin, Kniehl and Steinhauser; Kramer, Laenen and Spira
  - $O(\alpha_s^4)$  → Chetyrkin, Kniehl and Steinhauser
- **Full SQCD corrections** with arbitrary (s)quark and Higgs masses = “Hard Work” (G.W. Bush)
  - Two-loop integrals with up to **3 different mass scales!!**
  - **Progress is being made!**  
(see Anastasiou, Beerli and Daleo, arXiv:0803.3065)

# Gluon Fusion @ NLO in SQCD: EFT Approach

- **Effective Field Theory Approach** (Harlander & Steinhauser, hep-ph/0409010)
  - Good for “most” of MSSM parameter space:
    - 1) neglect effects from **bottom loops** (work in “Decoupling limit”)
    - 2) neglect **sbottom loops** (minimal mixing and degenerate masses)
    - 3) Appropriate for **light higgs only** ( $m_h^2 \ll (2 m_{\text{loop}})^2$ )
- Effective Lagrangian constructed from full theory by **integrating out** the **top quark** and **all SUSY partners** (stops and gluino):

$$\mathcal{L}_{\text{eff}} = -\frac{h}{v} C_1^{\text{B}} \mathcal{O}_1^{\text{B}}, \quad \mathcal{O}_1^{\text{B}} = \frac{1}{4} G_{a,\mu\nu}^{\text{B}} G_a^{\text{B},\mu\nu}$$

where:

$$C_1 = -\frac{\alpha_s}{3\pi} \left[ c_1^{(0)} + \frac{\alpha_s}{\pi} c_1^{(1)} + \mathcal{O}(\alpha_s^2) \right]$$

- $C_1$  coefficient extracted by **matching to ggh vertex** calculated in the full MSSM

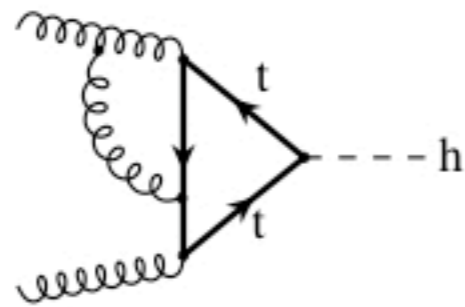
# Gluon Fusion in the EFT Approach (cont.)

- The LO coefficient:

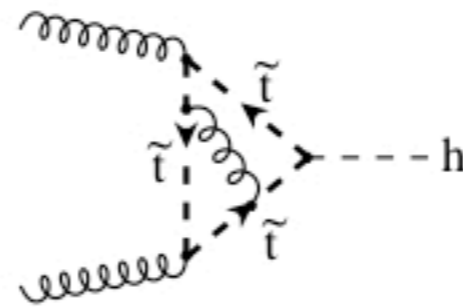
$$c_1^{(0)} = c_{1,t}^{(0)} + c_{1,\tilde{t}}^{(0)}, \quad c_{1,t}^{(0)} = \frac{\cos \alpha}{\sin \beta},$$
$$c_{1,\tilde{t}}^{(0)} = \frac{\cos \alpha}{\sin \beta} \left[ \frac{1}{4} \left( \frac{m_t^2}{m_{\tilde{t}_1}^2} + \frac{m_t^2}{m_{\tilde{t}_2}^2} \right) + \frac{\sin^2 2\theta_t}{8} \left( 1 - \frac{m_{\tilde{t}_1}^2}{2m_{\tilde{t}_2}^2} - \frac{m_{\tilde{t}_2}^2}{2m_{\tilde{t}_1}^2} \right) \right]$$
$$+ \frac{1}{8} \mu_{\text{SUSY}} m_t \frac{\cos(\alpha - \beta)}{\sin^2 \beta} \sin 2\theta_t \left[ \frac{1}{m_{\tilde{t}_1}^2} - \frac{1}{m_{\tilde{t}_2}^2} \right]$$
$$+ \frac{c_1^{\text{EW}} + c_2^{\text{EW}}}{16} \left( \frac{m_t^2}{m_{\tilde{t}_1}^2} + \frac{m_t^2}{m_{\tilde{t}_2}^2} \right) + \frac{c_1^{\text{EW}} - c_2^{\text{EW}}}{16} \cos 2\theta_t \left( \frac{m_t^2}{m_{\tilde{t}_1}^2} - \frac{m_t^2}{m_{\tilde{t}_2}^2} \right)$$

- $\sin^2(2\theta_t)$  term  $< 0$  : top and stop contributions can **cancel each other!**
- $c_1^{(l)}$  provided in the form of a FORTRAN code (“evalcsusy.f”)
- Two scenarios:
  - **“Snowmass Point and Slope 1a”** ( $\tan\beta = 10$ , etc.)
  - **“Gluophobic” scenario:** parameters chosen s.t. **LO cancellation is large**

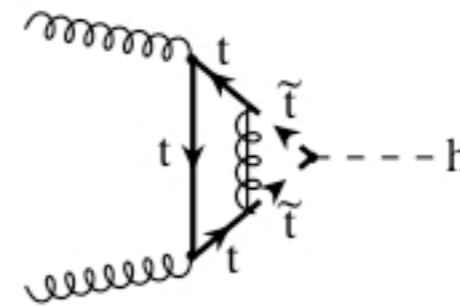
# Corrections to ggh Vertex



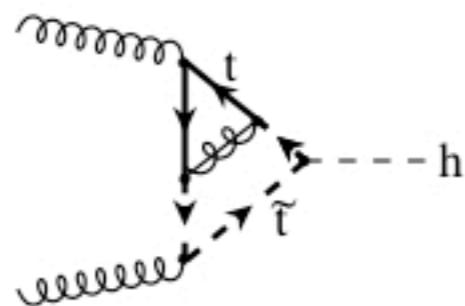
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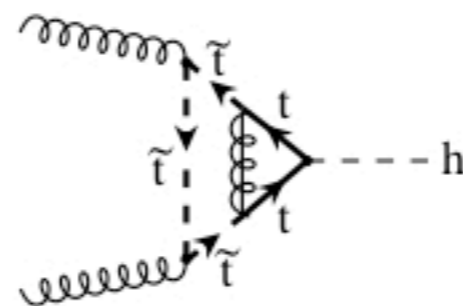
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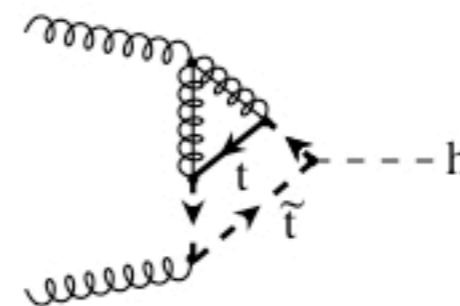
(f)



(g)



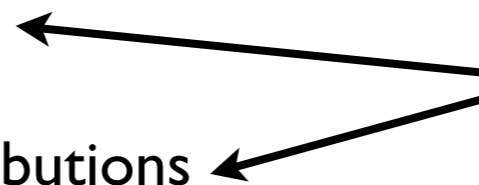
(h)



(i)

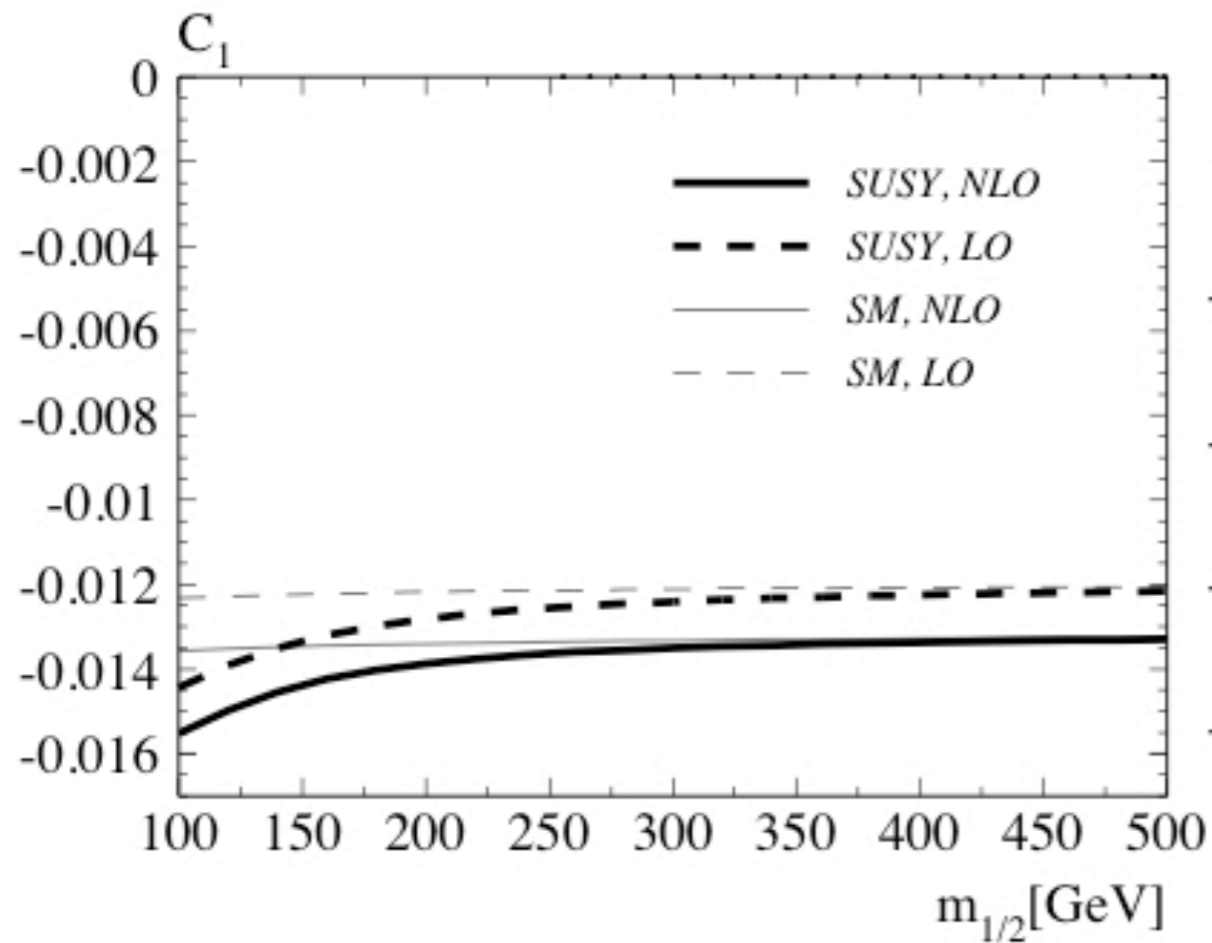
Three types of contributions:

- Pure top contributions (separately finite)
- Pure stop contributions
- Mixed top/stop/gluino contributions

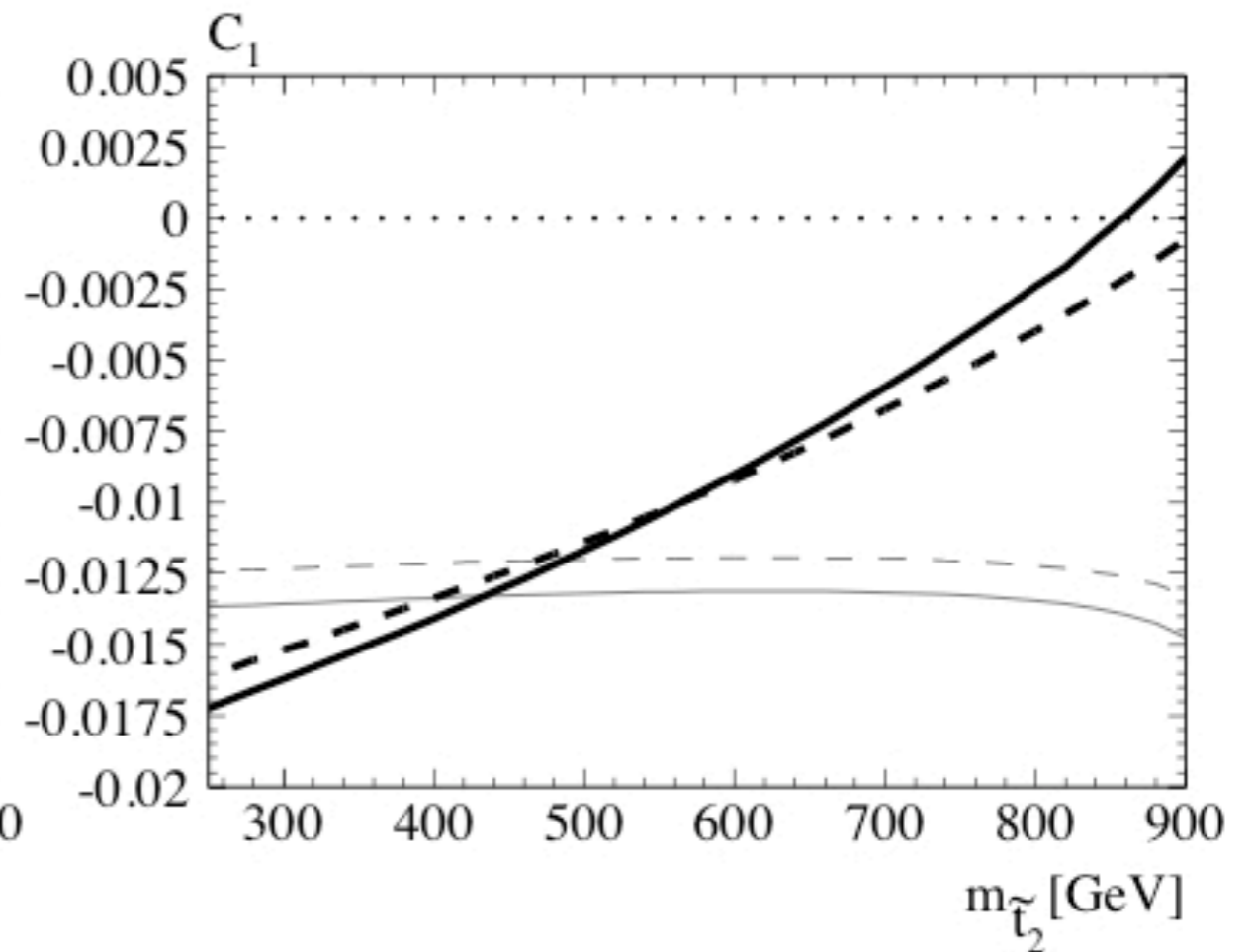


Sum is UV finite

# $C_1$ @ NLO in SQCD



(a)



(b)

## SPS1a Scenario:

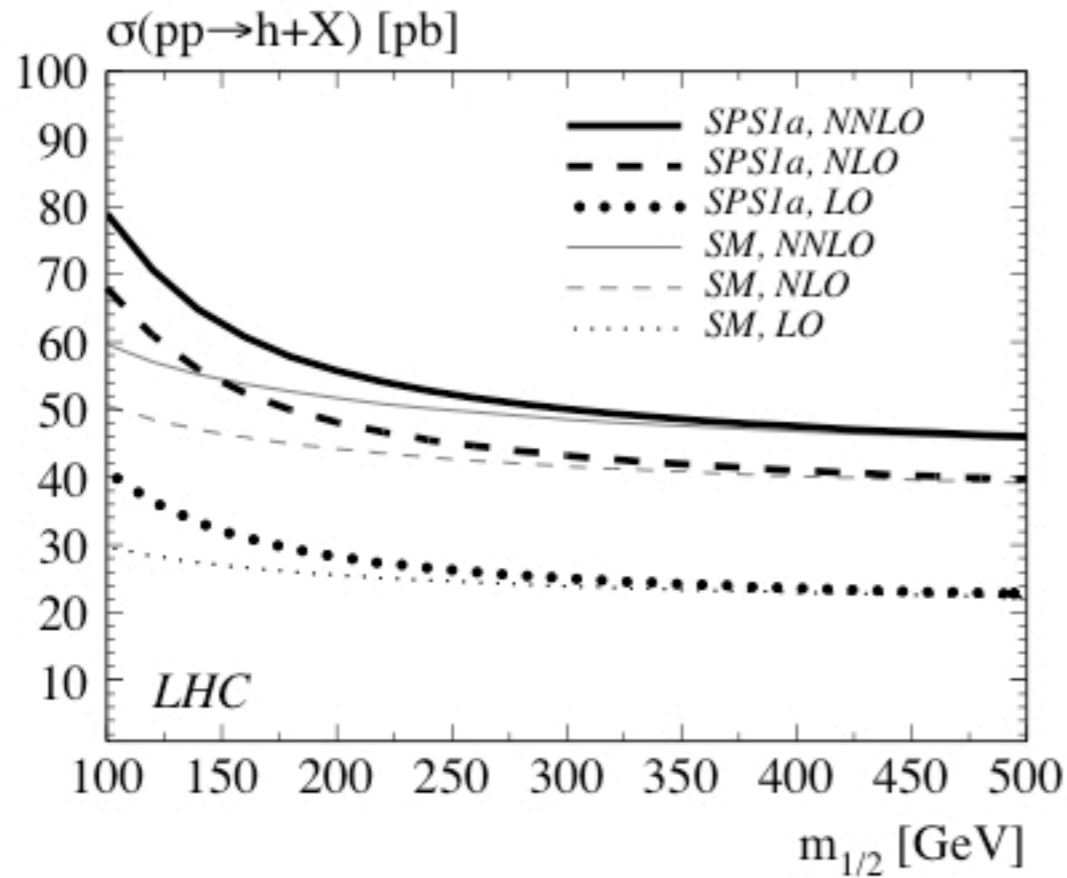
- **NLO/LO  $\approx 8\%$**
- SQCD corrections **negligible** over most of  $m_{1/2}$  range
- **SUSY/SM  $\approx 15\%$**  around  $m_{1/2} = 100$  GeV

## "Gluophobic" Scenario:

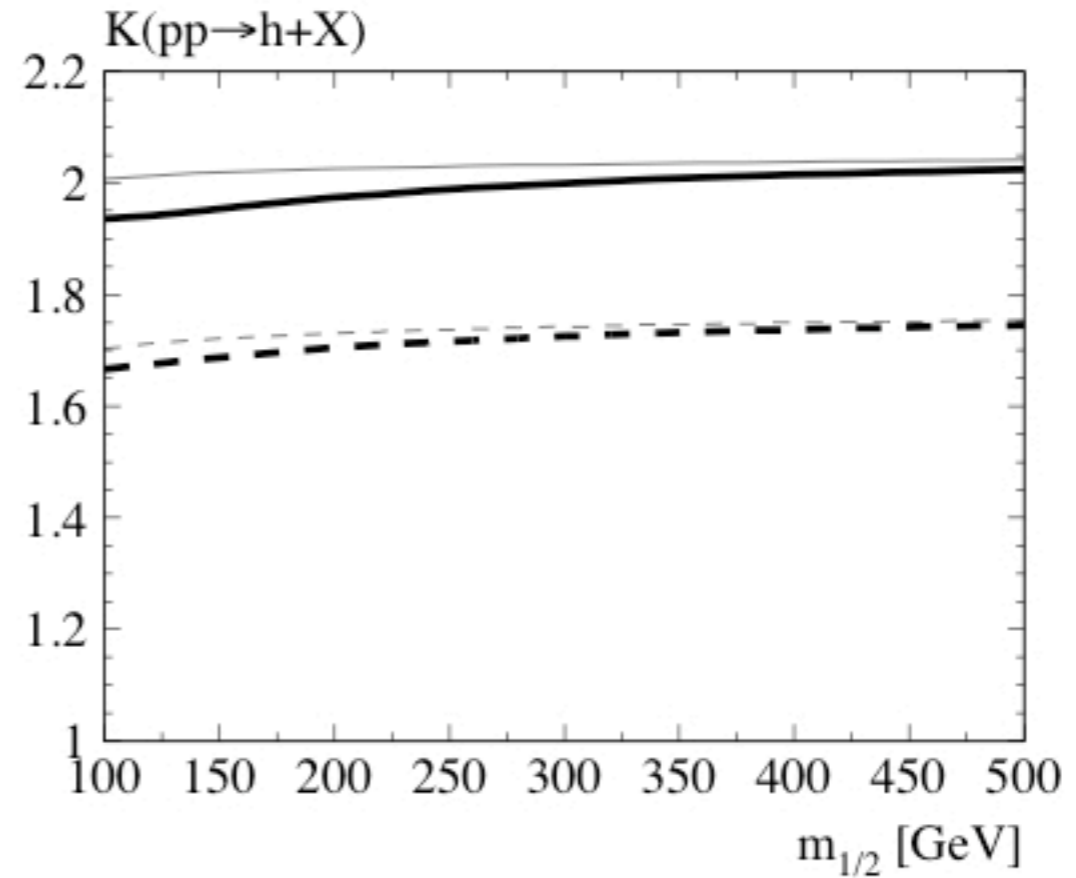
- **Large variation** of  $C_1$
- LO (NLO) **changes sign** around  $m_{\tilde{t}_2} \approx 900$  (850) GeV
- NLO corrections **significant at edges**



# NLO SQCD Cross Section: SPS1a



(a)



(b)

## Hadronic Cross section @ LHC:

- **MSSM/SM  $\approx 34\%$**  for  $m_{1/2} = 100$  GeV
- Difference **decreases rapidly** for larger  $m_{1/2}$

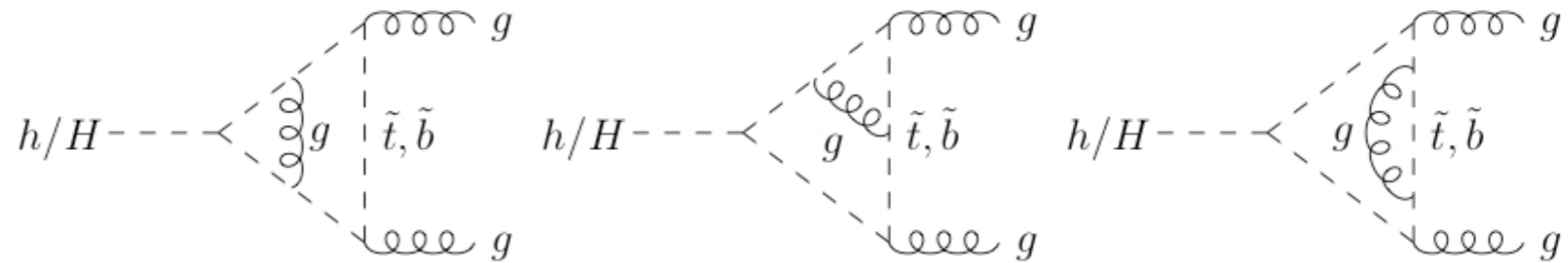
## K Factor @ LHC:

- **NLO K factor  $\approx 1.7$**
- Difference between SM and MSSM **mainly a LO effect**

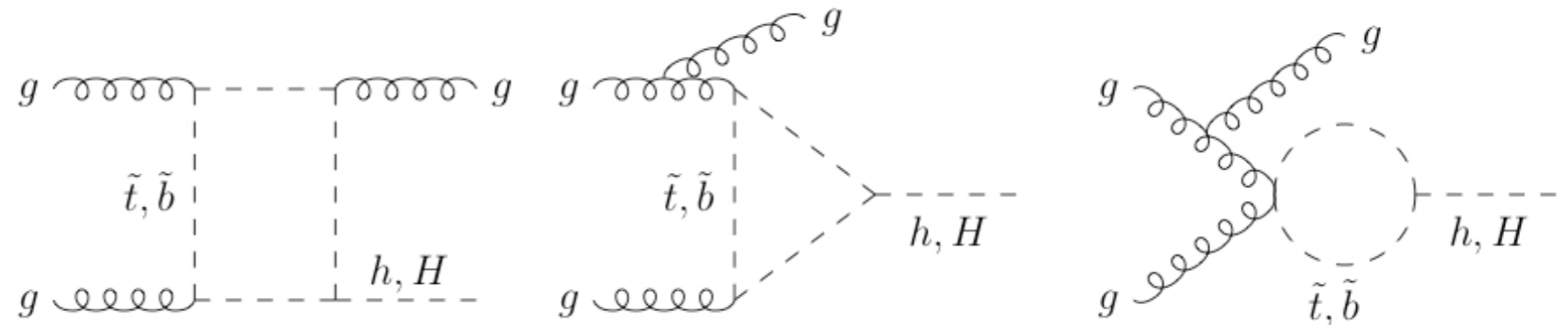
# Gluon Fusion, Take Two: Squark Loops @ NLO QCD

- **First step towards a full NLO SQCD calculation:** compute pure SM QCD corrections to gluon fusion **via squark loops** (both stop and sbottom) (Muhlleitner and Spira, hep-ph/0612254)

Virtual Corrections



Real Corrections

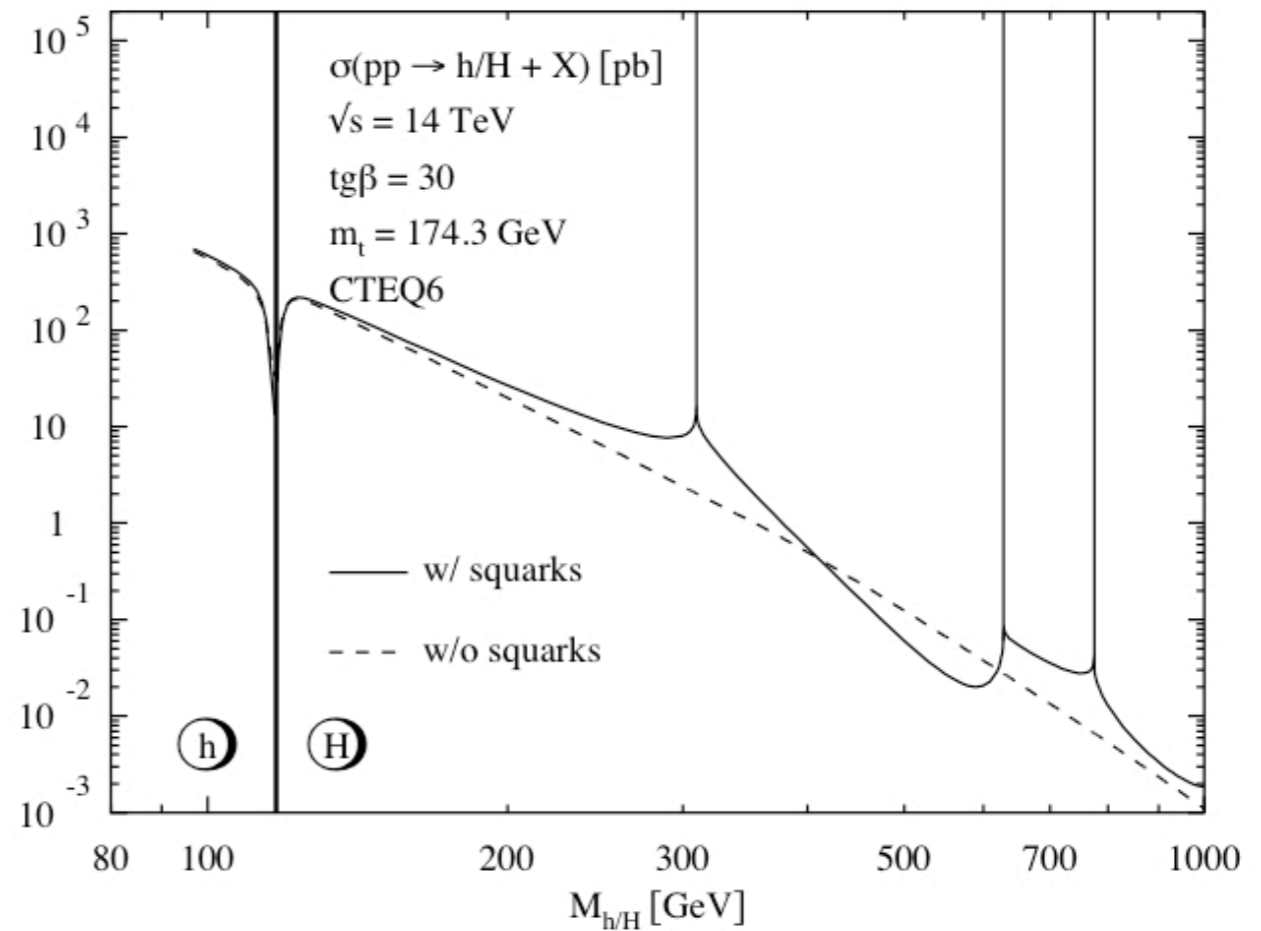
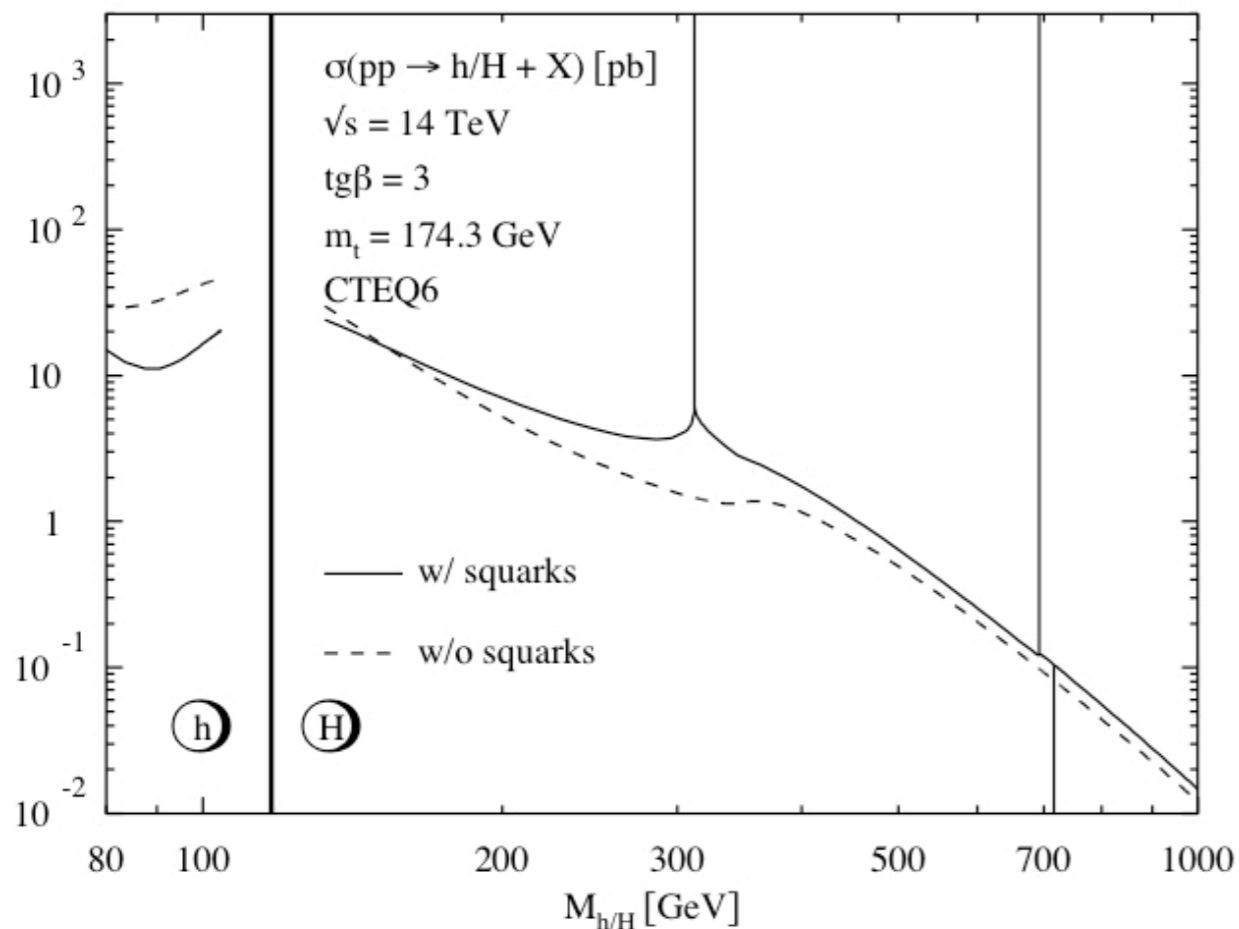


- **Hadronic cross section** takes the form:

$$\sigma(pp \rightarrow h/H + X) = \sigma_0^{h/H} \left[ 1 + C^{h/H} \frac{\alpha_s}{\pi} \right] \tau_{h/H} \frac{d\mathcal{L}^{gg}}{d\tau_{h/H}} + \Delta\sigma_{gg}^{h/H} + \Delta\sigma_{gq}^{h/H} + \Delta\sigma_{q\bar{q}}^{h/H}$$

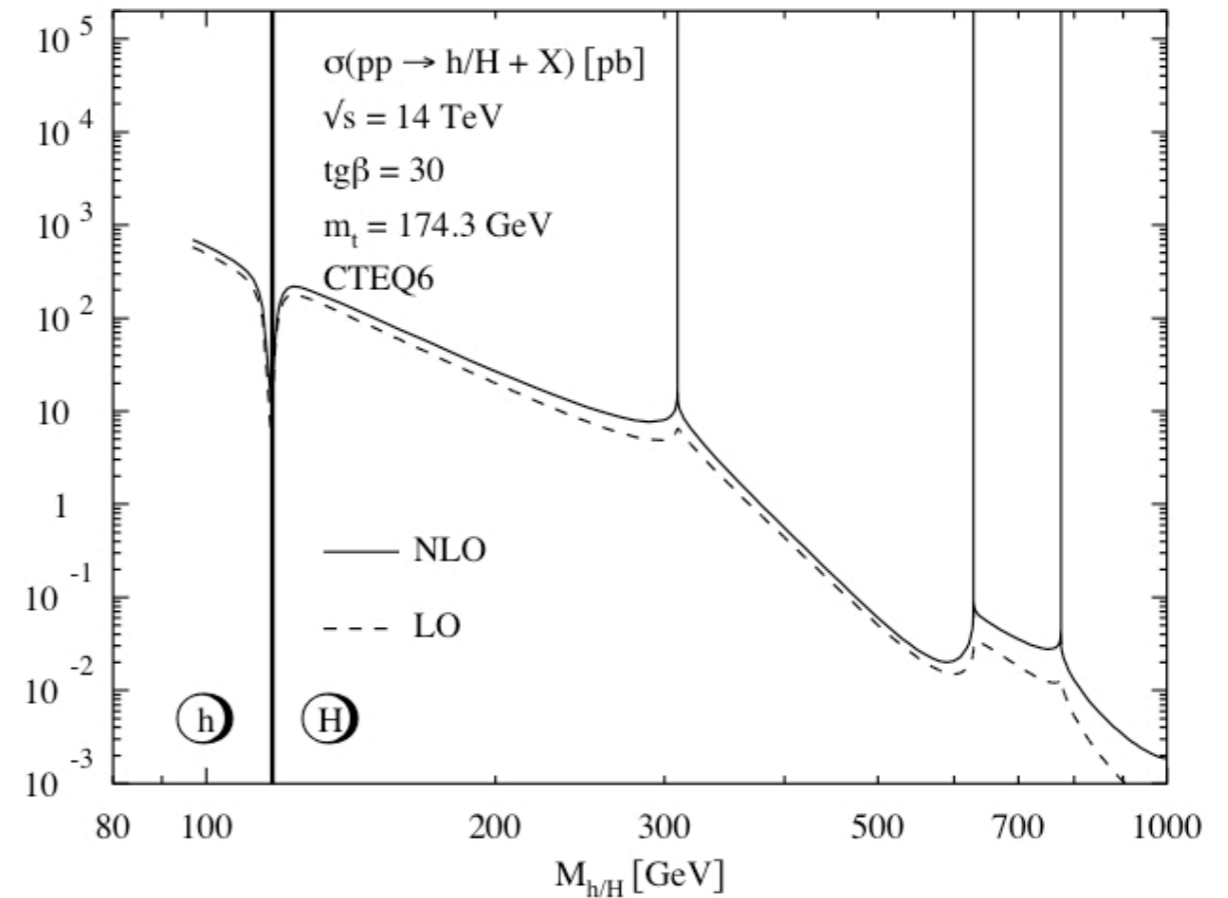
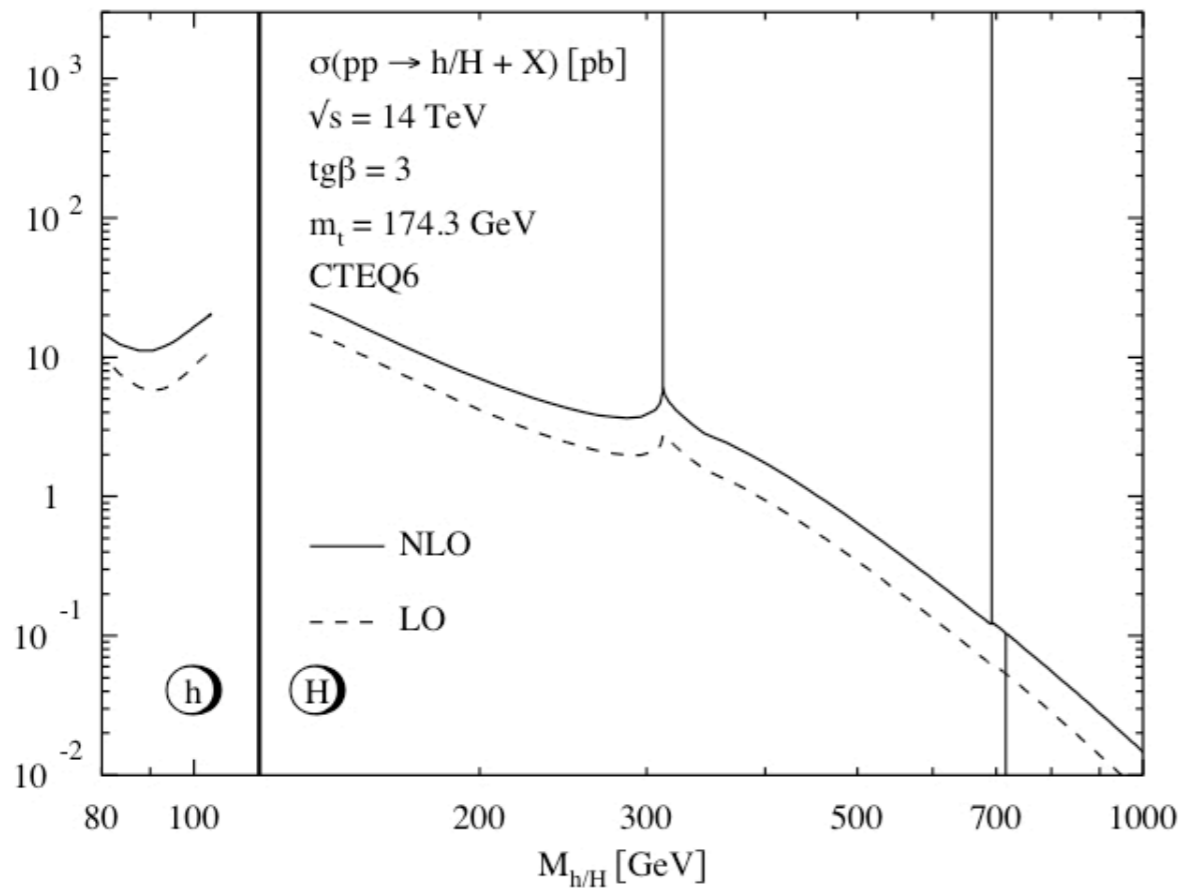
- Considered the **“gluophobic” scenario**

# Squark Mass Effects in Gluon Fusion



- “Spikes” = **squark mass thresholds** ( $t_1 t_1$ ,  $b_1 b_1$  and  $b_2 b_2$  respectively)
- “Gluophobic” scenario: **squark loops** alter c.s. by up to **factors of 3!**
- ... especially in regions **close to and beyond** squark mass thresholds.
- “Feature holds in **other MSSM scenarios.**”

# Squark Loop Effects: LO vs. NLO



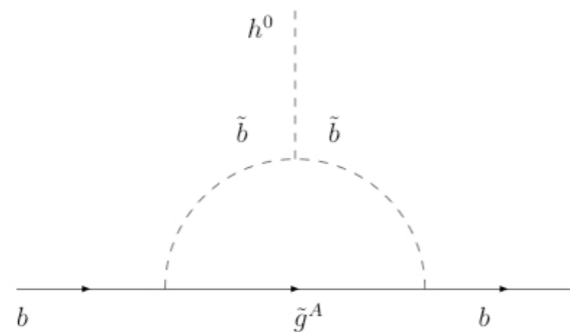
- **QCD+SQCD** corrections **increase c.s. by 10-100%**
- ... but, can be **significantly larger** in regions of **large destructive interference**
- Residual **scale-dependence lowered** from 50% to 20%
- K factors **develop squark mass dependence** up to 20% (**larger than top mass dependence!**)

# SQCD Corrections in Higgs Production with Bottom Quarks



# MSSM Higgs Production with a Single b

- **Discovery mode at Tevatron** (w/  $h \rightarrow bb$ ) and important at LHC (w/  $H \rightarrow \tau\tau$ )
- QCD corrections in **full agreement!**
  - “5FNS” =  $gb \rightarrow bh$  [Campbell, Ellis, Maltoni and Willenbrock]
  - “4FNS” =  $gg \rightarrow b(b)h$  [Dawson et al.; Dittmaier et al.]
- Claim: most important **SUSY corrections** come from **bbh vertex**
  - Computed in **EFT approach** [Carena et al.]:



$$g_{hbb} \rightarrow g_{hbb} \frac{1 - \Delta_b / (\tan \beta \tan \alpha)}{1 + \Delta_b}$$

- where:

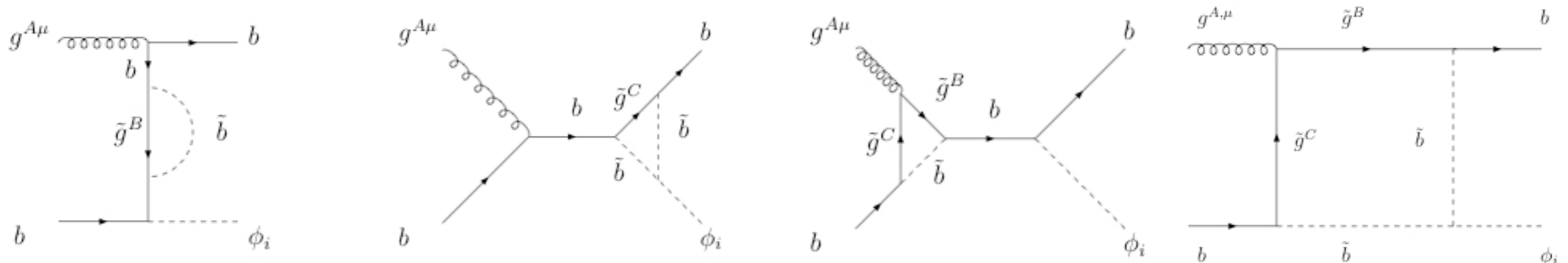
$$\Delta_b = \frac{2\alpha_s(\mu_R)}{3\pi} m_{\tilde{g}} \mu \tan \beta I(m_{\tilde{b}_1}, m_{\tilde{b}_2}, m_{\tilde{g}})$$

Sums all SQCD corrections to bbh vertex to all orders!

- But,  $\Delta_b$  computed in  $m_h^2 \ll (M_{SUSY})^2$  limit and w/ **on-shell** bottom quarks

# Complete SQCD Corrections to $gb \rightarrow b\phi$

- Goal: compute **full SQCD corrections** and test EFT claim [S. Dawson and CBJ]
- **Virtual corrections**:



- Define various cross sections:

“IBA”

$$\frac{d\hat{\sigma}_{IBA}}{dt} \equiv \frac{d\hat{\sigma}_{Born}}{dt} \left( \frac{g_{bb\phi}}{g_{bb\phi}^{LO}} \right)^2$$

“Gluon Only” = QCD Corrected c.s.

$$\sigma_{NLO}(pp \rightarrow b\phi)_{QCD} \equiv \left( \frac{g_{bb\phi}}{g_{bb\phi}^{LO}} \right)^2 \sigma_{LO}(pp \rightarrow b\phi) + \delta\sigma_{QCD}(pp \rightarrow b\phi)$$

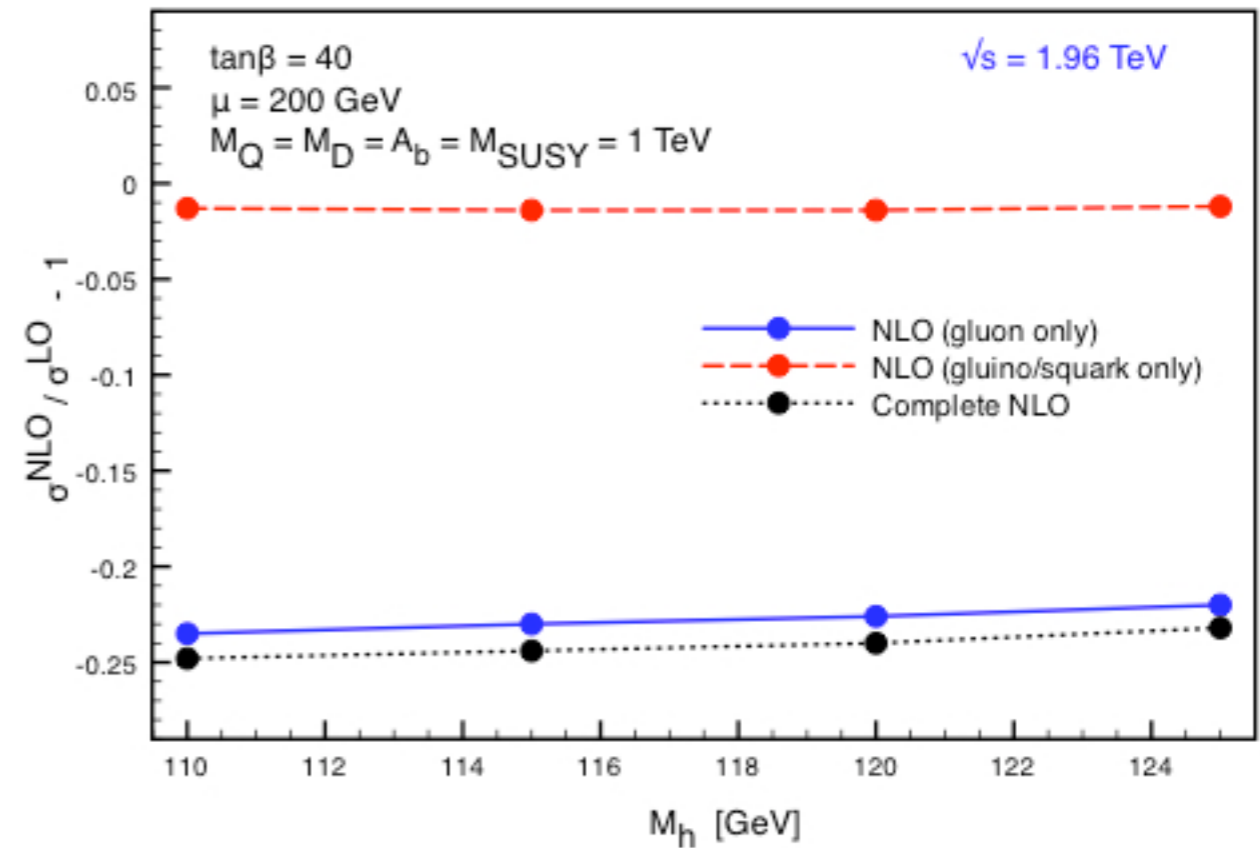
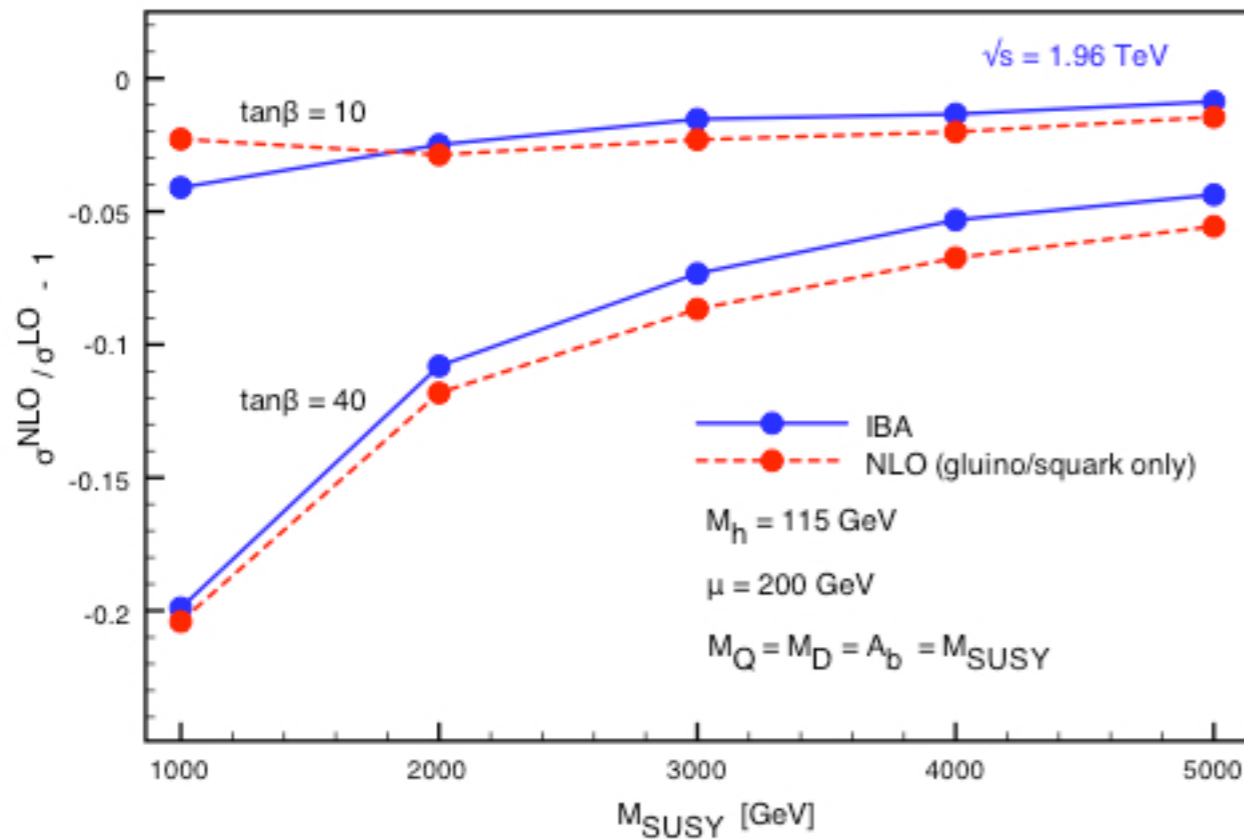
“Gluino/Squark Only” = SQCD Corrected c.s.

$$\sigma_{NLO}(pp \rightarrow b\phi)_{SQCD} = \int dx_1 dx_2 \left[ g(x_1, \mu) b(x_2, \mu) \int dt \left( \frac{d\hat{\sigma}_{SQCD}}{dt} \right) + (x_1 \leftrightarrow x_2) \right]$$

“Complete NLO” = QCD + SQCD

$$\sigma_{NLO}(pp \rightarrow b\phi)_{QCD+SQCD} \equiv \sigma_{NLO}(pp \rightarrow b\phi)_{SQCD} + \delta\sigma_{QCD}$$

# Testing the EFT Claim



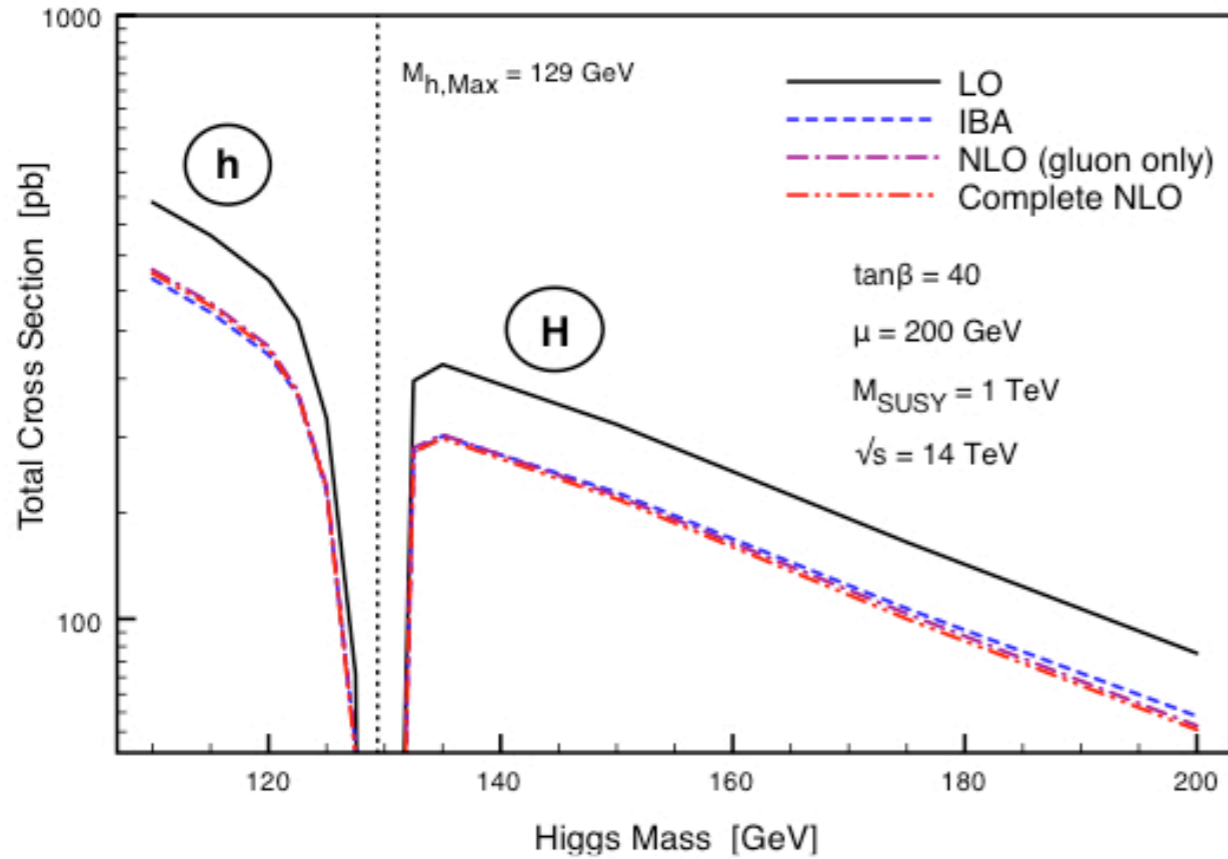
## IBA vs. Gluino/Squark Only:

- Light Higgs @ Tevatron (similar results for all Higgs at both machines)
- Difference at **percent level** (IBA works for large  $M_{\text{SUSY}}$ )
- Results approach “**decoupling limit**”

## QCD vs. SQCD:

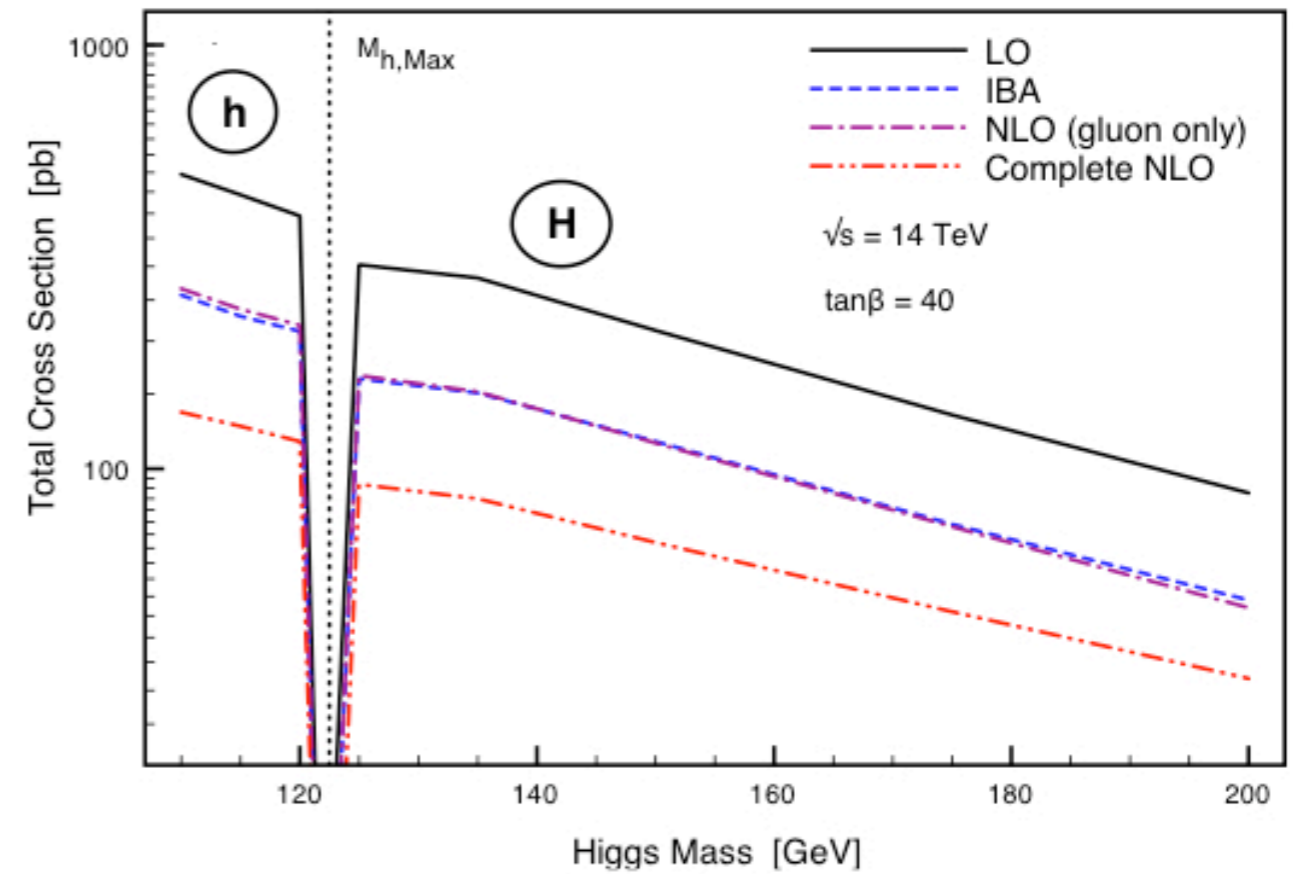
- Note: **large  $M_{\text{SUSY}}$**  (see next slide...)
- **QCD corrections dominate!**
- SQCD at **1-2% level**

# $gb \rightarrow b\varphi$ @ the LHC



## Large $M_{SUSY}$ Scenario:

- **Almost all** of NLO corrections accounted for by **EFT approach**
- Additional SQCD corrections **tiny**
- ... QCD corrections too!



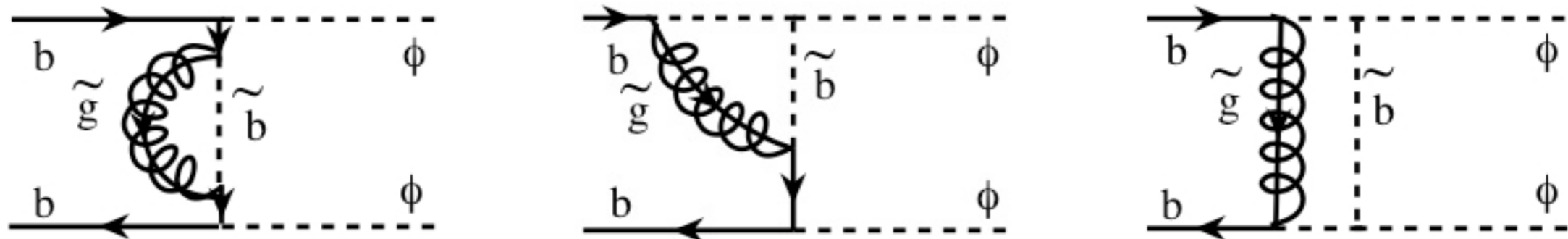
## “More Optimistic” Scenario:

- $m_g = m_{b_1} = 250$  GeV,  $m_{b_2} = 350$  GeV
- Still **QCD corrections tiny**, but...
- **SQCD corrections dominate and significantly reduce c.s. !**

# MSSM Higgs Pair Production from Bottom Quark Fusion

[S. Dawson, C. Kao and Y. Wang]

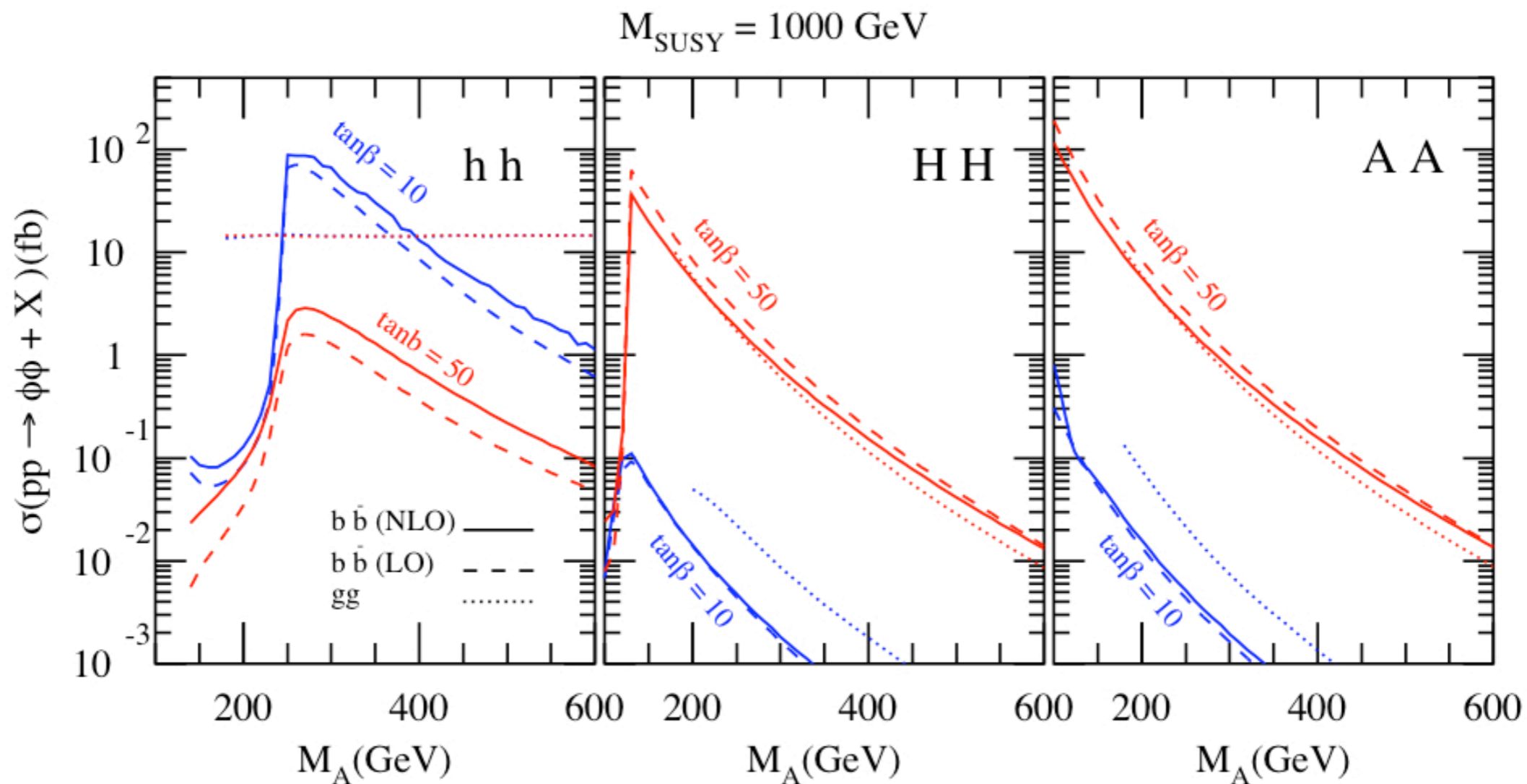
- Production rate for light Higgs from **bb fusion** > **gg fusion** channel for  $\tan\beta \leq 35$  and moderate values of  $M_A$  ( $M_A \approx 300$  GeV)
- Prospect for measuring the **Higgs tri-linear coupling**
- QCD corrections **significantly increase** the total cross section [S. Dawson, C. Kao and Y. Wang]
- SQCD corrections:



- Study results for both the **MSSM** and **mSUGRA** scenarios
- Compared results for **bb → hh** to **gg → hh** [Plehn, Spira and Zerwas; Bendezu and Kniehl]

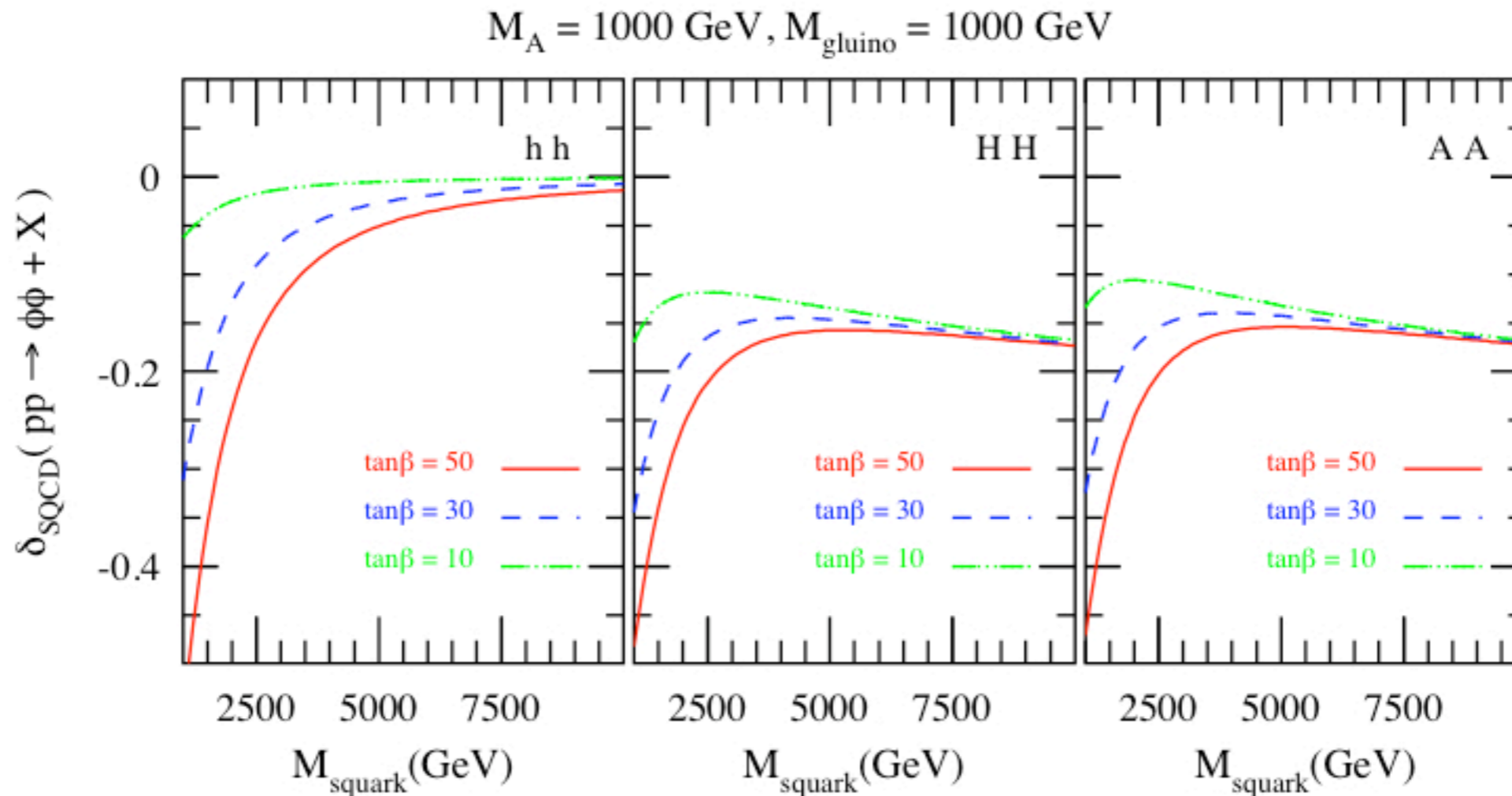


# Gluon Fusion vs. Bottom Quark Fusion



- For  $\tan\beta = 10$ :
  - Cross section for hh production **can be much larger** for bb
  - HH, AA production **suppressed** compared to gg
- For  $\tan\beta = 50$ :
  - hh channel in b quark fusion **suppressed** compared to gg
  - HH, AA **comparable** in both channels

# SQCD Corrections with Heavy Squarks



- NLO SQCD cross section **normalized to Born** cross section
- Cross section for  $hh$  **approaches decoupling** for large squark masses (similar to  $gb \rightarrow bh$  behavior)
- Cross sections for  $HH/AA$  **approach non-zero constant**

# Summary

- **QCD corrections** to all **MSSM Higgs production** processes now under **complete control** (some @ NNLO QCD, NLO EW, etc.)
- Recently, a lot of effort going into **SUSY corrections**.
- **Gluon fusion**:
  - **EFT approach**:
    - ✓ valid for “**most**” of MSSM parameter space
    - ✓ SQCD corrections **typically small**
  - **QCD corrections to Squark loops**
    - ✓ Corrections can be **quite large** around **squark mass thresholds**
  - Ongoing effort to calculate **full two-loop amplitudes** in SQCD
- **Production with Bottom Quarks**:
  - $gb \rightarrow b\varphi$ : EFT approach valid for **large SUSY masses**, but inadequate for more “**optimistic**” scenarios
  - $bb \rightarrow \varphi\varphi$ : SQCD corrections **significant for several regions** of MSSM parameter space

# Fate of the MSSM Higgs Sector?

Annie Taylor



Became first person to ride  
a barrel over Niagara Falls  
on Oct. 24, 1901...  
and survive.

Charles Stephens



Englishman Charles G. Stephens  
equipped his wooden barrel with an  
anvil for ballast. Charles tied himself to  
the anvil for security. After the plunge,  
Charles' right arm was the only item  
left in the barrel.