

Rare Decays at LHCb

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b Focus week

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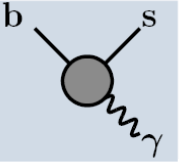
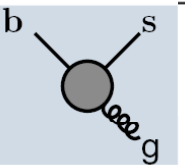
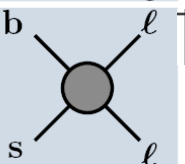
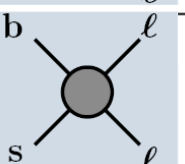


Introduction

- New physics can give effective Hamiltonian, \mathcal{H} , new operators \mathcal{O}_i or modified Wilson coefficients C_i

$$A(M \rightarrow F) = \langle F | \mathcal{H}_{\text{eff}} | M \rangle \quad \mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \sum_{i=1}^{10} C_i(\mu) \mathcal{O}_i(\mu)$$

- Rare B decays give a number of opportunities to constrain these contributions:

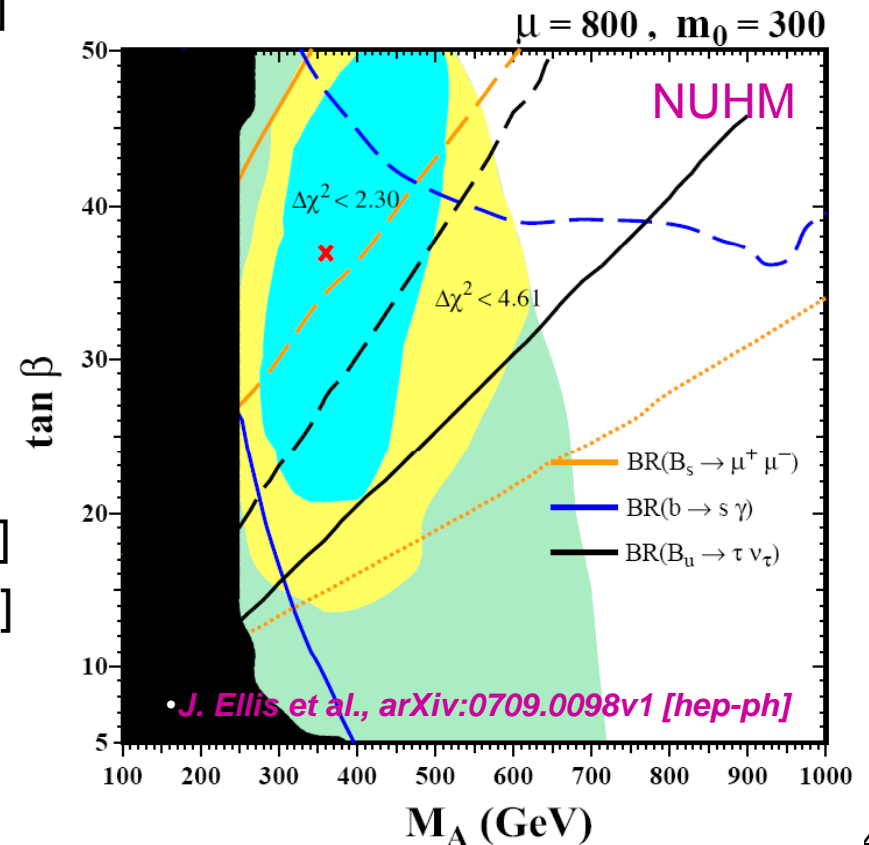
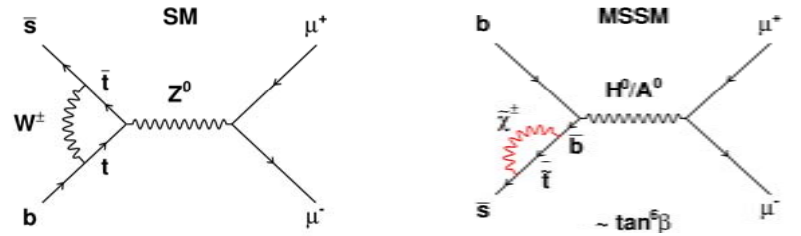
		magnitude	phase	helicity flip \mathcal{O}'_i
$\mathcal{O}_{7\gamma}$		$b \rightarrow s\gamma$	$a_{CP}(b \rightarrow s\gamma)$	$\Lambda_b \rightarrow \Lambda\gamma$ $B \rightarrow (K^* \rightarrow K\pi)\ell^+\ell^-$ $B \rightarrow (K^{**} \rightarrow K\pi\pi)\gamma$
\mathcal{O}_{8g}		$b \rightarrow s\gamma$ $B \rightarrow X_c$	$a_{CP}(b \rightarrow s\gamma)$ $B \rightarrow K\phi$	$\Lambda_b \rightarrow \Lambda\phi$ $B \rightarrow K^*\phi$
$\mathcal{O}_{9\ell,10\ell}$		$b \rightarrow s\ell^+\ell^-$	$A_{FB}(b \rightarrow s\ell^+\ell^-)$	$B \rightarrow (K^* \rightarrow K\pi)\ell^+\ell^-$
$\mathcal{O}_{S,P}$		$B_{d,s} \rightarrow \mu^+\mu^-$	$B_{d,s} \rightarrow \tau^+\tau^-$	$b \rightarrow s\tau^+\tau^-$

From G. Hiller [hep-ph/0308180]

$$B_s \rightarrow \mu\mu$$

$B_s \rightarrow \mu\mu$

- $B_s \rightarrow \mu\mu$ helicity suppressed
- Well predicted in SM:
 - $\text{BR}(B_s \rightarrow \mu\mu) = (3.35 \pm 0.32) \times 10^{-9}$ [1]
- Sensitive to (pseudo) scalar operators
 - MSSM: $\tan^6 \theta / M_A^4$ enhancement
 - **NUHM**: favours large $\tan \beta$ (~ 30)
- Current limits from Tevatron:
 - CDF $\text{BR} < 4.7 \times 10^{-8}$ 90% CL [2]
 - D0 $\text{BR} < 7.5 \times 10^{-8}$ 90% CL [3]



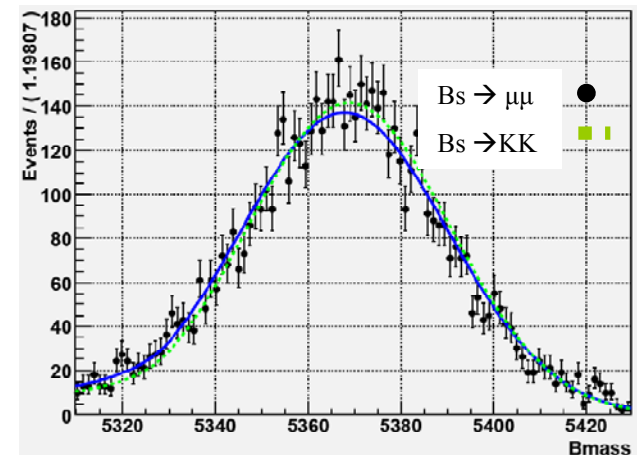
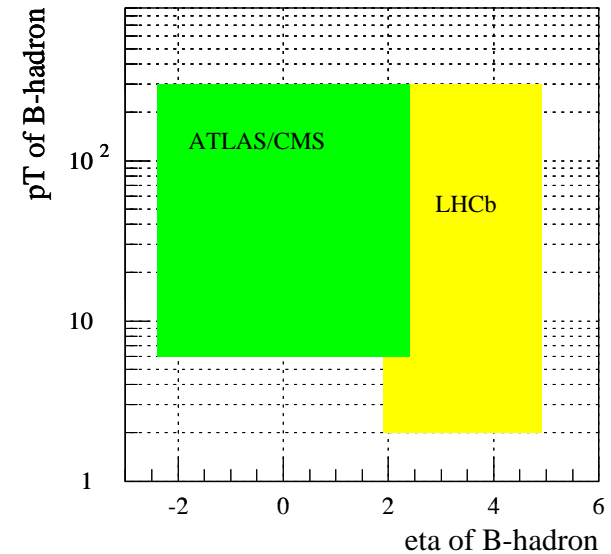
[1] hep-ph/0604050v5

[2] arXiv:0712.1708v1 [hep-ex]

[3] arXiv:0705.300v1 [hep-ex]

$B_s \rightarrow \mu\mu$ at LHCb

- Searching for $B_s \rightarrow \mu\mu$ with LHCb:
 - Large prodn x-secn for b's at high η , low p_T
 - At $L=2 \times 10^{32} \text{ cm}^2 \text{ s}^{-1}$, $10^{12} \text{ } b\bar{b}$ pairs in 10^7 s
 - Trigger has μ p_T threshold $> \sim 1 \text{ GeV}$
 - $\sim 1.5 \text{ kHz}$ inclusive μ , di- μ
 - Small event size
 - Can write this rate out, open analysis – can retain max. efficiency
 - High precision magnetic spectrometer
 - B_s mass resolution $\sim 20 \text{ MeV}$
(c.f. CMS $\sim 40 \text{ MeV}$, ATLAS $\sim 80 \text{ MeV}$)
 - Vertex detector very close to LHC beams
 - Excellent vtx, impact parameter resolution



Mass (MeV)

$B_s \rightarrow \mu\mu$ at LHCb

- Events classified according to geometrical likelihood, PID and B_s invariant mass:

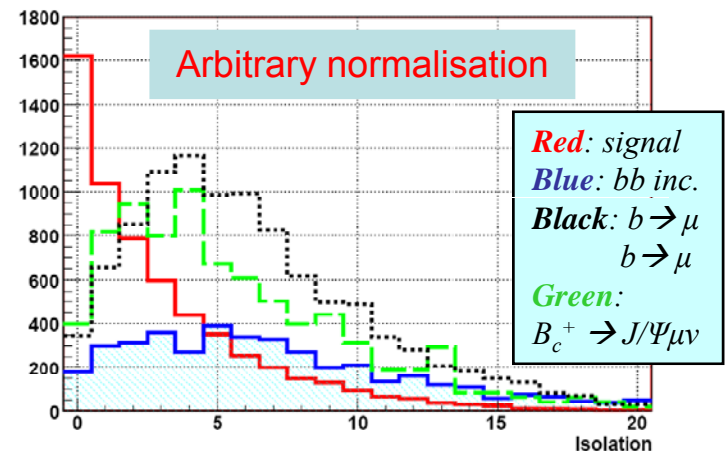
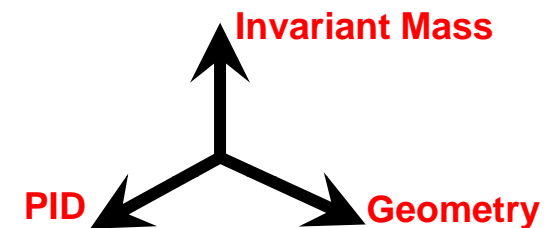
- Geometric likelihood:

- B_s Lifetime
- μ SIPS: Mu Impact Parameter Significance
- DOCA: Distance of closest approach
- B_s IP: B_s impact parameter to prim. vtx
- Isolation: No. of good secondary vtx that can be made with μ candidates

- PID:

- Calibration muons (MIPs in calorimeter, J/ψ muons)

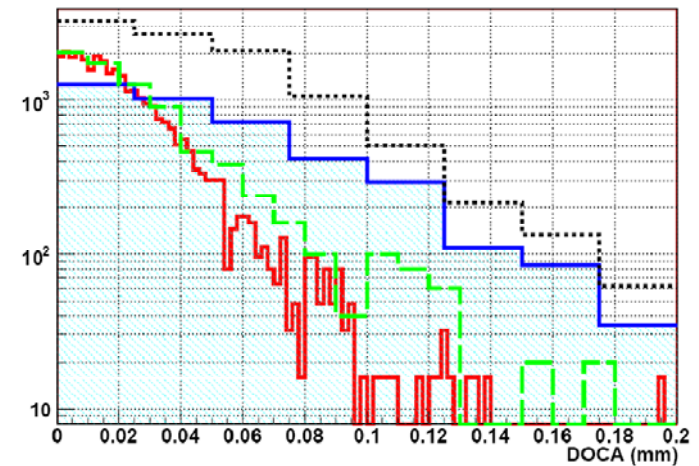
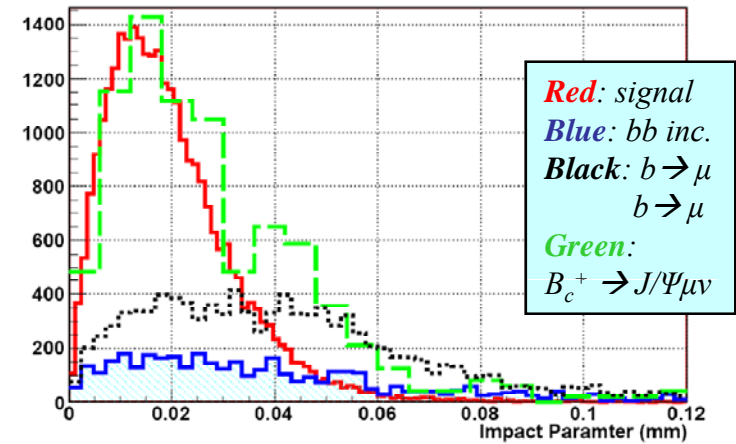
- B_s Invariant Mass



$B_s \rightarrow \mu\mu$ at LHCb

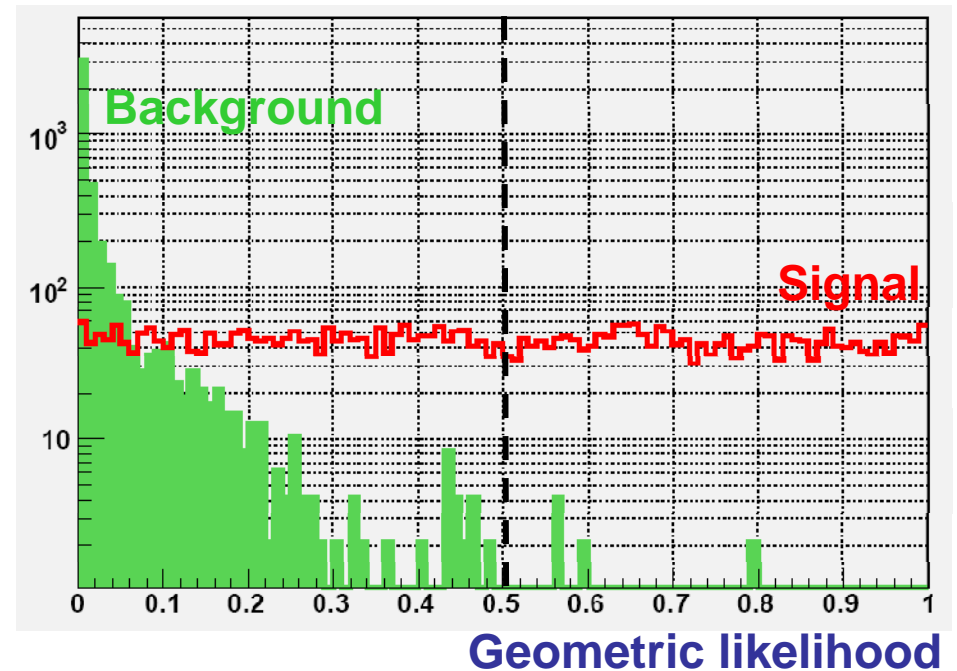
- Analysis:
 - Signal description: $B \rightarrow hh$ ($\sim 200k$ events/ $2fb^{-1}$)
 - Background estimation from mass sidebands
 - Normalisation: $B^+ \rightarrow J/\psi K^+$ ($2M$ events/ $2fb^{-1}$)
 - Dominant uncertainty on BR from relative B_s, B^+ hadronisation fraction $\sim 13\%$

$$BR = \frac{BR_n \cdot \epsilon_n^{REC} \epsilon_n^{SEL} \epsilon_n^{TRIG}}{\epsilon^{REC} \epsilon^{SEL} \epsilon^{TRIG}} \cdot \frac{f_n}{f_{B_s}} \cdot \frac{N}{N_n}$$

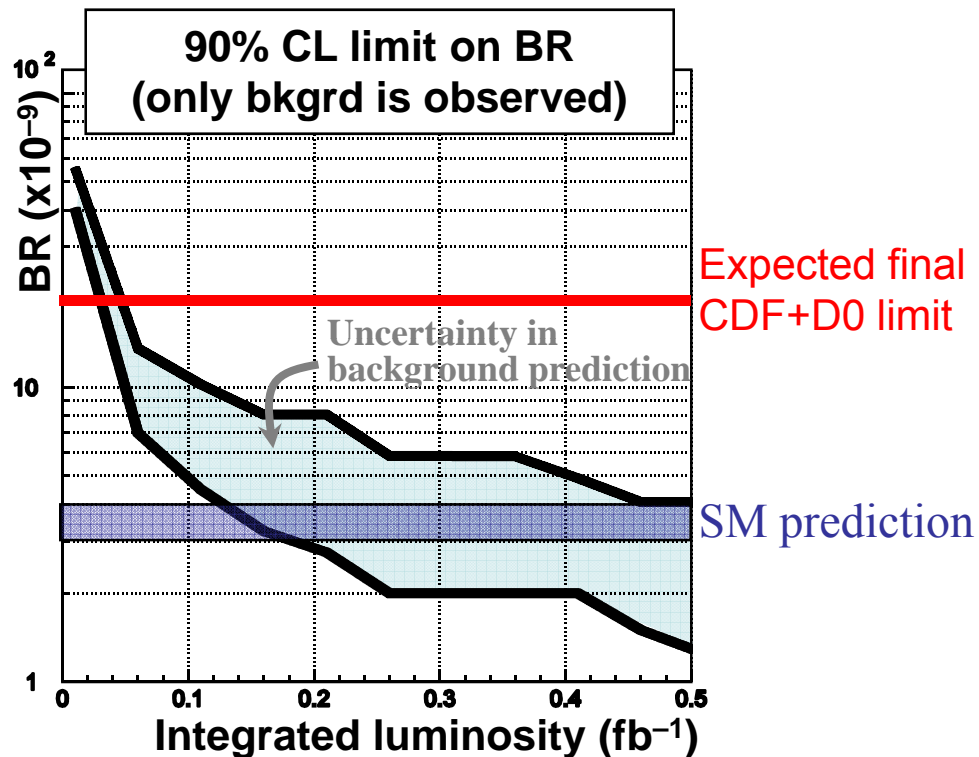


$B_s \rightarrow \mu\mu$ at LHCb

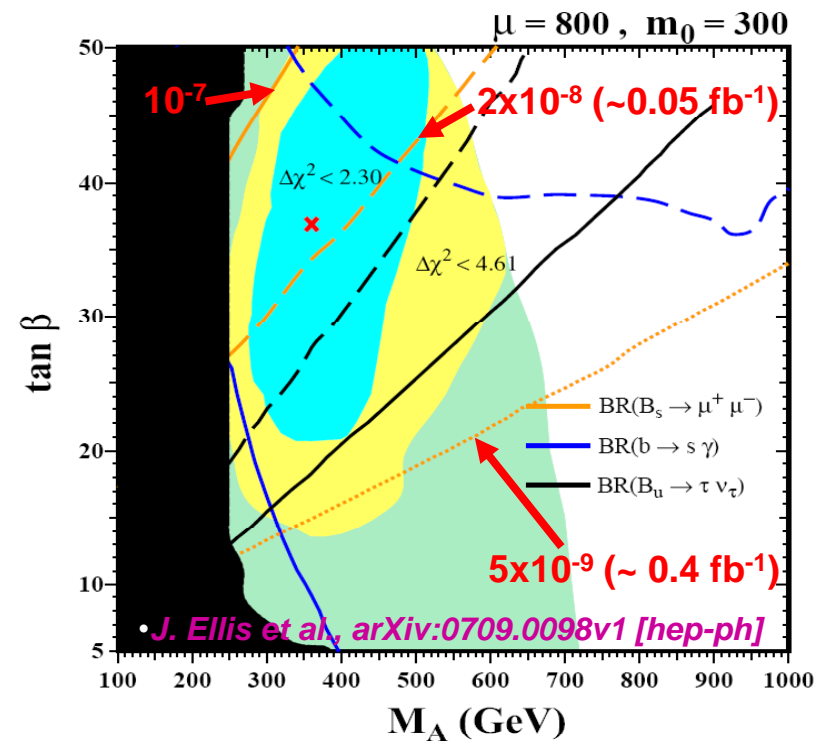
- Background:
 - Dominated by $b \rightarrow \mu$, $b \rightarrow \mu$, $b \rightarrow \mu$, $b \rightarrow c \rightarrow \mu$ also contributes
 - Mis-id ($B \rightarrow hh$), insignificant
 - Dominant exclusive bkgrd $B_c^+ \rightarrow J/\Psi \mu \nu$, tiny cf. $b \rightarrow \mu$, $b \rightarrow \mu$
 - Drell-yan insignificant at these masses
- Total efficiency for all geometric likelihood values $\sim 10\%$
- Taking events with $GL > 0.5$, assuming SM BR, with 2fb^{-1} :
 - Signal ~ 30 events
 - Bkgrd ~ 83 events



$B_s \rightarrow \mu\mu$ at LHCb



Exclusion:
 $0.1 \text{ fb}^{-1} \Rightarrow \text{BR} < 10^{-8}$
 $0.5 \text{ fb}^{-1} \Rightarrow < \text{SM}$



With SM Branching ratio
 $2 \text{ fb}^{-1} \Rightarrow 3\sigma$ evidence
 $6 \text{ fb}^{-1} \Rightarrow 5\sigma$ observation

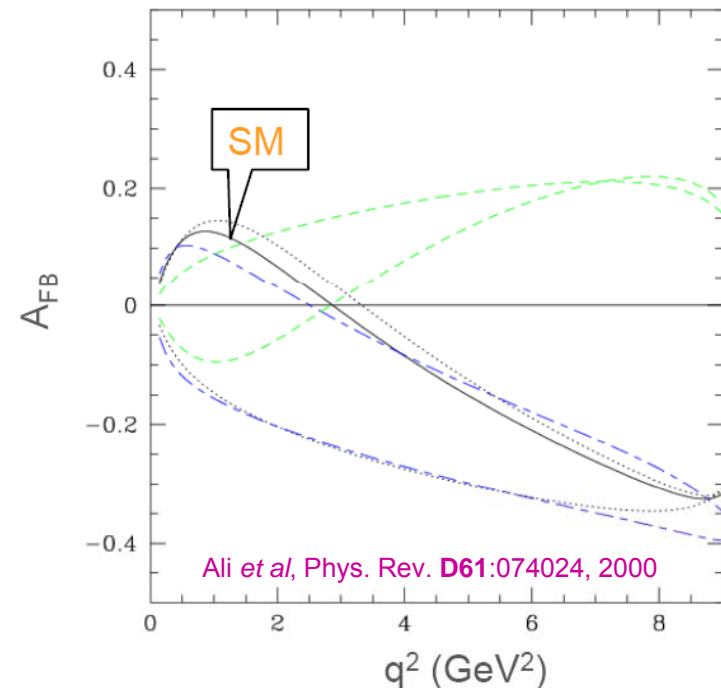
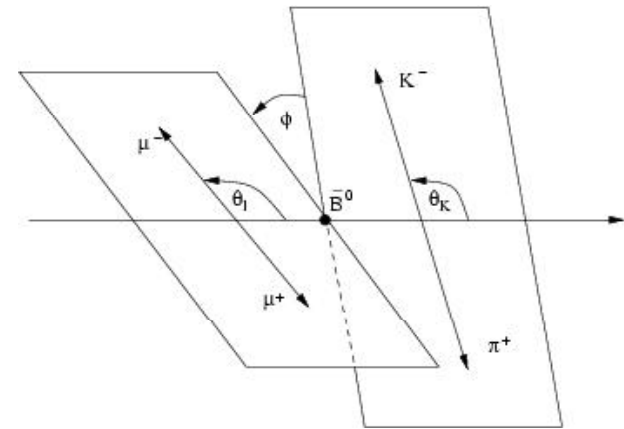
With 0.1 fb^{-1} can measure BR 9 (15) $\times 10^{-9}$ at 3 (5) σ

With 0.5 fb^{-1} can measure BR 5 (9) $\times 10^{-9}$ at 3 (5) σ

$$B_d \rightarrow K^* \mu \mu$$

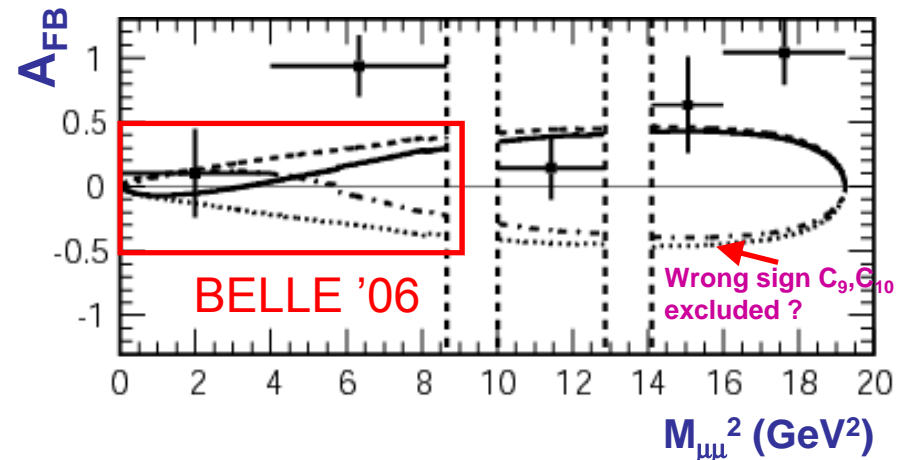
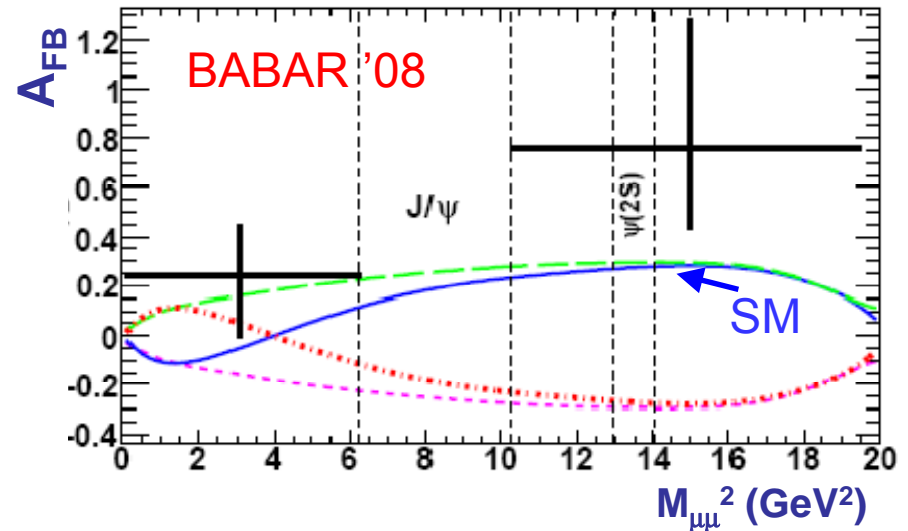
$B_d \rightarrow K^* \mu \mu$

- BR measured at B-factories, in agreement with SM:
 $BR(B_d \rightarrow K^* \mu \mu) = (1.22^{+0.38}_{-0.32}) \times 10^{-6}$ [1]
- Decay described by three angles (θ_l , ϕ , θ_{K^*})
- Angular distributions as function of q^2 gives sensitivity to NP contributions
- Forward-backward asymmetry A_{FB} in θ_l angle has received particular theoretical attention – predicted in a number of different models



$B_d \rightarrow K^* \mu \mu$ at LHCb

- B-factories each collected $O(100)$ signal events
- CDF has ~ 35 signal events
- Given projected total datasets these experiments, a total of < 1000 events might be observed at all facilities
- With $L = 2 \times 10^{32} \text{ cm}^2 \text{ s}^{-1}$, LHCb will observe this no. of events with $\sim 0.25 \text{ fb}^{-1}$ integrated luminosity

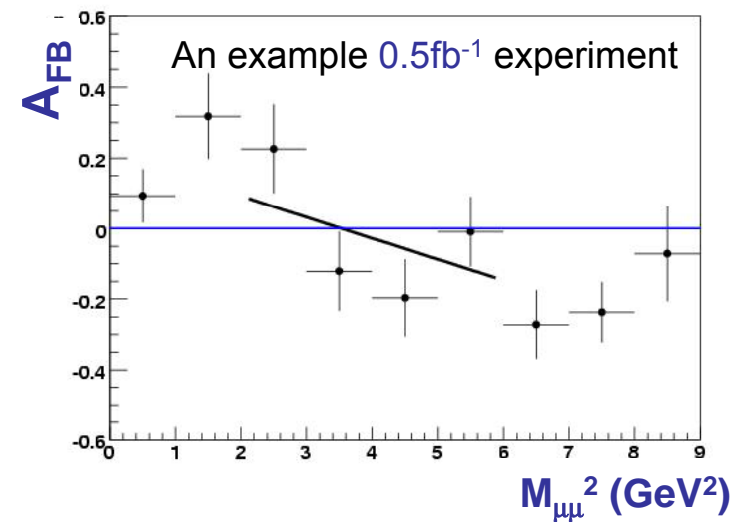
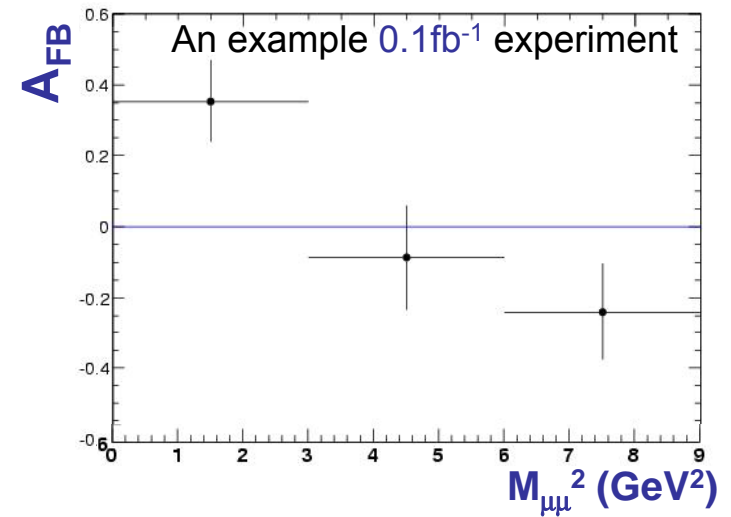


$B_d \rightarrow K^* \mu \mu$ at LHCb

- Signal selection:
 - Total selection efficiency $\sim 1\%$
 - 7200 signal events / 2fb^{-1} ($\sim 50\%$ below $m_{J/\Psi}$)
- Full A_{FB} spectrum of interest but zero-crossing point often computed:
 - $s^0_{\text{SM}} = 4.39^{+0.38}_{-0.35} \text{ GeV}^2$ [1]
 - (older value used in model →)
- Simple linear fit suggests precision:

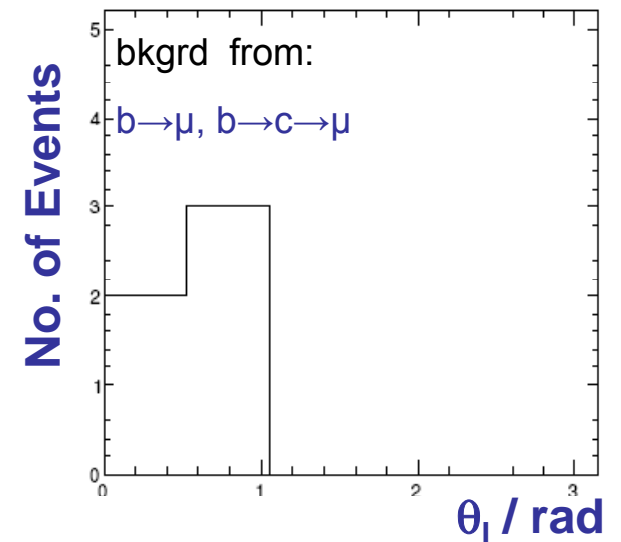
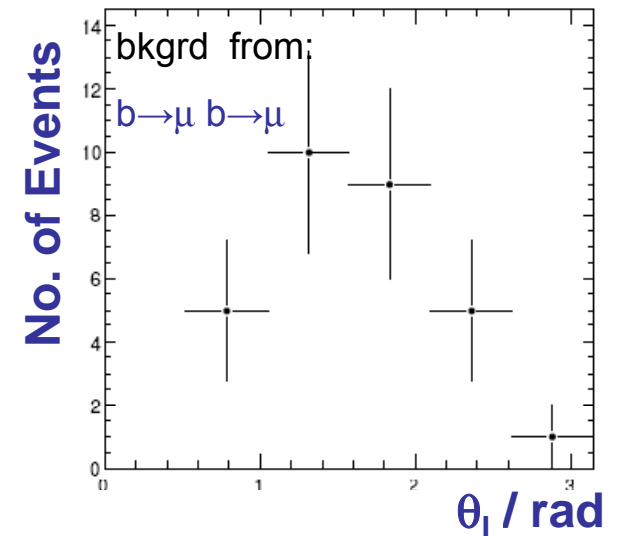
	0.5 fb^{-1}	2 fb^{-1}	10 fb^{-1}
$\sigma(s^0)$	0.8 GeV^2	0.5 GeV^2	0.3 GeV^2

- Looking at extended beyond linear fit



$B_d \rightarrow K^* \mu \mu$ at LHCb

- Background:
 - $b \rightarrow \mu$, $b \rightarrow \mu$ dominant contribution, symmetric distribution in θ_1 – scales A_{FB} observed
 - $b \rightarrow \mu$, $b \rightarrow c \rightarrow \mu$ significant contribution, asymmetric θ_1 distribution – effect on A_{FB} depends on θ_1 shape
 - As for $B_s \rightarrow \mu \mu$, don't observe any significant background from μ mis-id
 - Non-resonant $K \pi \mu \mu$ events not yet observed
 - Bkgrd rejection dependent on B_d mass resolu: $\sigma(m_{B_d}) \sim 15 \text{ MeV}$ (c.f. ATLAS 50 MeV)
 - B/S ~ 0.5
- Analysis issues:
 - In order to correct A_{FB} value measured, require knowledge relative angular efficiency:
 - p_T cuts on muons (in e.g. trigger), remove events with $\theta_1 \sim 0, \pi$
 - muon reconstruction requirements distort momentum spectrum



$B_d \rightarrow K^* \mu \mu$ at LHCb

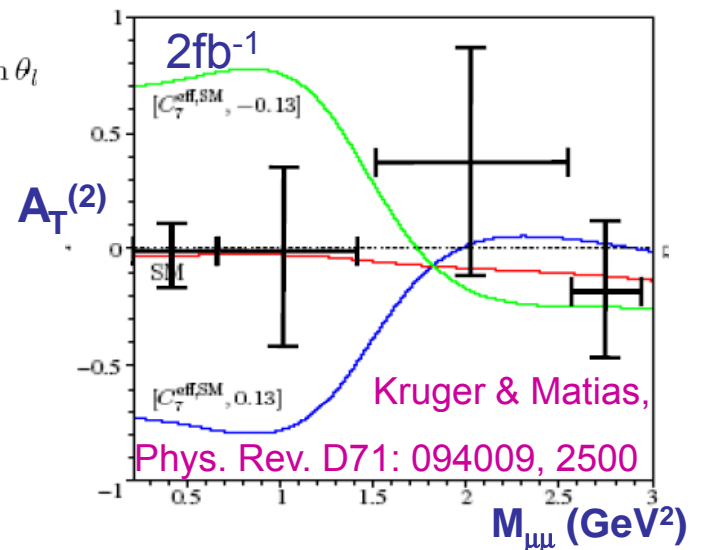
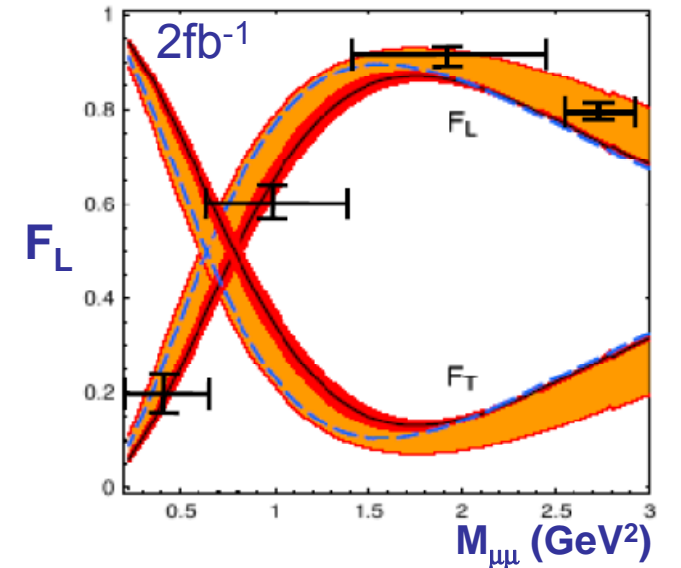
- Decays contain much more information than θ_l , A_{FB} distributions
- Fitting projections of θ_l , ϕ , θ_{K^*} angular distributions:

$$\frac{d\Gamma'}{d\phi} = \frac{\Gamma'}{2\pi} \left(1 + \frac{1}{2}(1 - F_L)A_T^{(2)} \cos 2\phi + A_{Im} \sin 2\phi \right)$$

$$\frac{d\Gamma'}{d\theta_l} = \Gamma' \left(\frac{3}{4}F_L \sin^2 \theta_l + \frac{3}{8}(1 - F_L)(1 + \cos^2 \theta_l) + A_{FB} \cos \theta_l \right) \sin \theta_l$$

$$\frac{d\Gamma'}{d\theta_K} = \frac{3\Gamma'}{4} \sin \theta_K (2F_L \cos^2 \theta_K + (1 - F_L) \sin^2 \theta_K)$$

→ fraction of longitudinal polarization, F_L ,
and transverse asymmetry $A_T^{(2)}$



$B_d \rightarrow K^* \mu \mu$ at LHCb

- Full angular fit also under investigation:

$$\frac{d^4 \Gamma_{\bar{B}_d}}{dq^2 d\theta_l d\theta_K d\phi} = \frac{9}{32\pi} I(q^2, \theta_l, \theta_K, \phi) \sin \theta_l \sin \theta_K$$

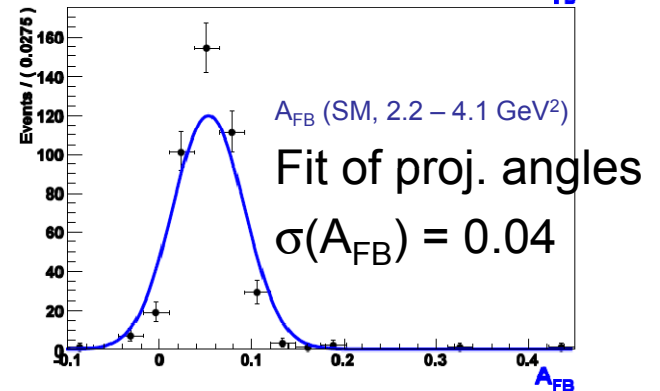
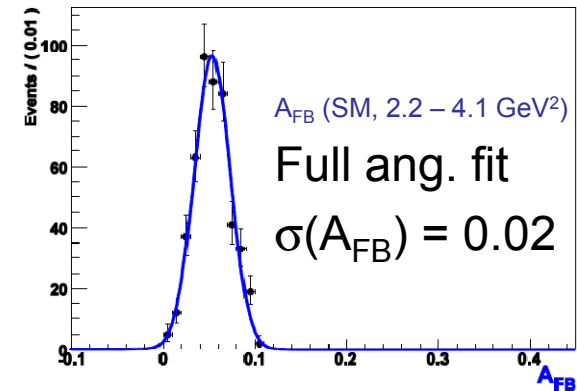
- Parameterised in terms of transversity amplitudes

– $A_0^{L,R}$, $A_{\perp}^{L,R}$, $A_{\parallel}^{L,R}$, 6 complex numbers

- Correlations give access to helicities

– Probe chiral structure NP operators

- Once have enough events in each q^2 bin for fit to converge \rightarrow better precision on A_{FB} , F_L , and A_T^2 (but require full acceptance correction)
- Can form any observable once have fitted all amplitudes – new theoretically clean observables with good NP sensitivity sought!



$$B_s \rightarrow \phi \gamma$$

$$B_d \rightarrow K^* \gamma, B_s \rightarrow \phi \gamma$$

- BR($B_d \rightarrow X_s \gamma$) measured by B-factories, rate in agreement with SM

$$\Gamma(B_q(\bar{B}_q) \rightarrow f^{CP} \gamma) \propto e^{-\Gamma_q t} \left(\cosh \frac{\Delta\Gamma_q t}{2} - \mathcal{A}^\Delta \sinh \frac{\Delta\Gamma_q t}{2} \pm \mathcal{C} \cos \Delta m_q t \mp \mathcal{S} \sin \Delta m_q t \right).$$

- B-factories measured CP asymmetry A_{CP} in $B_d \rightarrow K^*(K_s \pi^0) \gamma$:

$$A_{CP}(t) = \frac{\Gamma[\bar{B}_q \rightarrow \phi \gamma] - \Gamma[B_q \rightarrow \phi \gamma]}{\Gamma[\bar{B}_q \rightarrow \phi \gamma] + \Gamma[B_q \rightarrow \phi \gamma]}$$

$$A_{CP}(t) = -\frac{C \cos(\Delta m_q t) + S \sin(\Delta m_q t)}{\mathcal{A}^\Delta \sinh(\Delta\Gamma_q t/2) + \cosh(\Delta\Gamma_q t/2)}$$

In SM,

$C=0$ (direct CPV)

$S = \sin 2\psi \sin \phi$

$\mathcal{A}^\Delta = \sin 2\psi \cos \phi$

where ψ fraction of “wrong” polarization

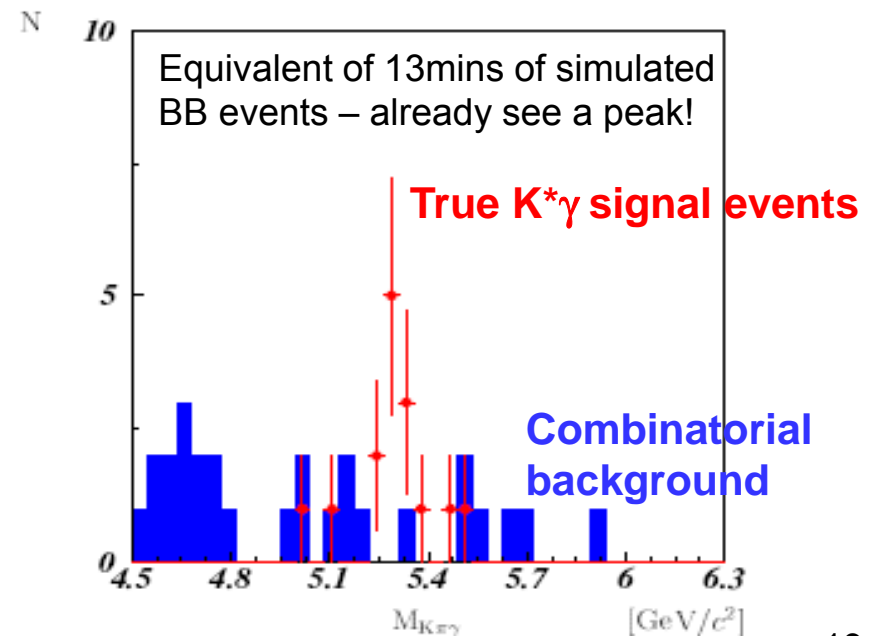
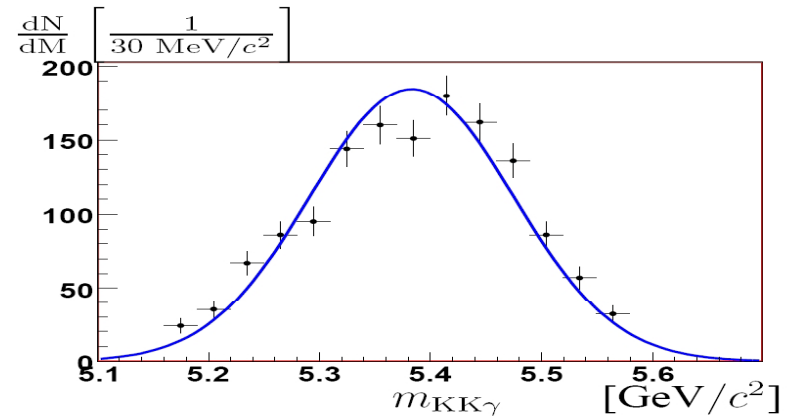
$$\rightarrow C = -0.03 \pm 0.14, S = -0.19 \pm 0.23$$

[HFAG]

- LHCb can perform analogous measurement in $B_s \rightarrow \phi \gamma$
 - As $\Delta\Gamma_s \neq 0$, $B_s \rightarrow \phi \gamma$ decay probes \mathcal{A}^Δ as well as C and S

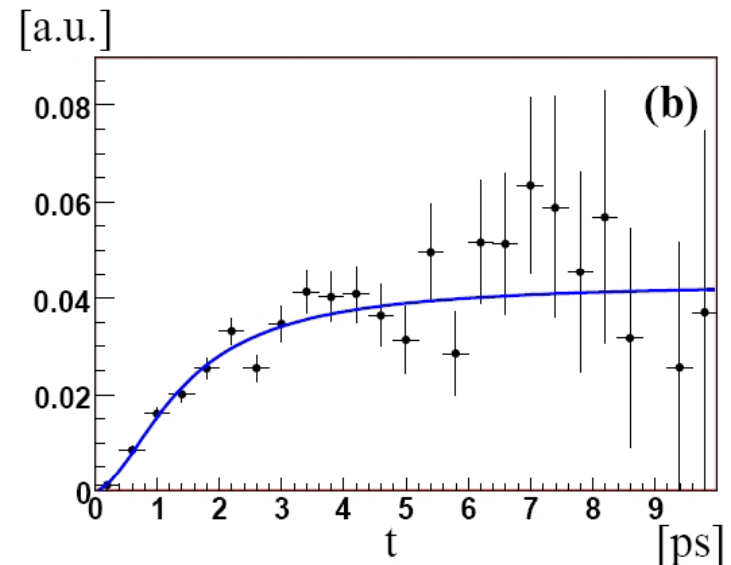
$B_s \rightarrow \phi \gamma$ at LHCb

- Signal Selection:
 - $E_T > 2.7 \text{ GeV}$
 - Mass resolu $\sim 90 \text{ MeV}$
 - Proper time resolu $\sim 80 \text{ fs}$
(not critical for measuring A^Δ)
 - Total Efficiency $\sim 0.3\%$
 - Yield:
 - $B_s \rightarrow \phi \gamma$
 - 11k / 2fb^{-1} with $B/S < 0.55$
 - $B_d \rightarrow K^*(K^+\pi^-)\gamma$
 - 68k / 2fb^{-1} with $B/S \sim 0.60$

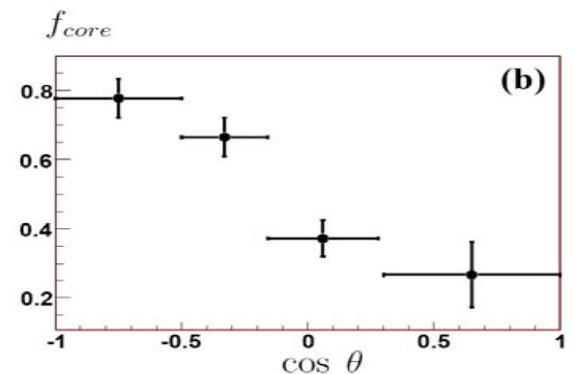
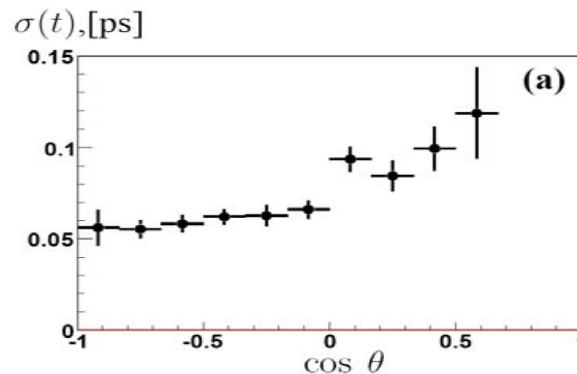


$B_s \rightarrow \phi \gamma$ at LHCb

- Analysis issues:
 - Acceptance function $a(t)$ ($B_d \rightarrow K^* \gamma$)
 - $\sigma(t)$ as function of topology
- Precision on A_{CP} parameters with $B_s \rightarrow \phi \gamma$ decays from 0.5 fb^{-1}
 - $\sigma(A^\Delta) = 0.3$ (no tagging required)
 - $\sigma(S, C) = 0.2$ (require tagging)



- With 2 fb^{-1} :
 - $\sigma(A^\Delta) = 0.22$
 - $\sigma(S, C) = 0.11$



Conclusions

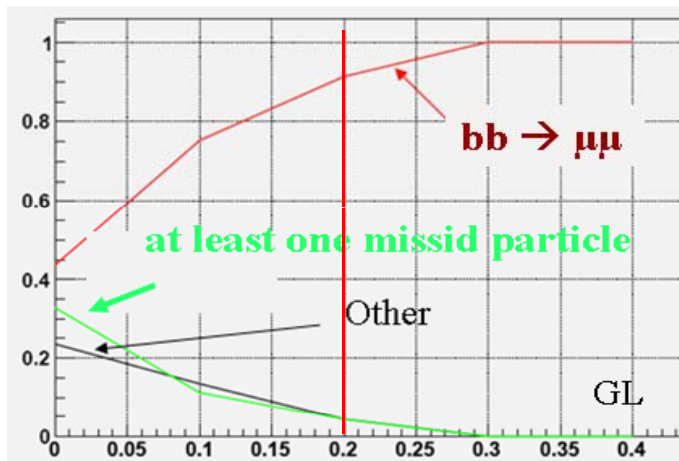
- Rare B decays in LHCb will find NP or constrain extensions of SM
- With the first data:
 - $B_s \rightarrow \mu\mu$ excluded at SM value with 0.5fb^{-1}
 - $B_d \rightarrow K^* \mu\mu$ measure A_{FB} spectrum, $\sigma(s_0) \sim 0.8\text{GeV}^2$ with 0.5fb^{-1}
- With 2fb^{-1} integrated luminosity:
 - $B_s \rightarrow \mu\mu$ evidence if SM BR (observation with 6fb^{-1} data)
 - $B_d \rightarrow K^* \mu\mu$ measure A_{FB} spectrum, $\sigma(s_0) \sim 0.5\text{GeV}^2$, new observables with more complex fits ($A^{(2)}_{\text{T}}$, ...)
 - $B_s \rightarrow \phi\gamma$ CP asymmetry $A_{\text{CP}} \rightarrow$ fraction of “wrong” polarization
- Host of other channels will be accessible:
 - Radiative : $\Lambda_b \rightarrow \Lambda\gamma$, $\Lambda_b \rightarrow \Lambda^* \gamma$, $B \rightarrow \rho^0\gamma$, $B \rightarrow \omega\gamma$, $\mu\mu\gamma$
 - $b \rightarrow sll$: $B^+ \rightarrow K^+ ll$ (R_K), $B_s \rightarrow \phi\mu\mu$
 - LFV : $B_q \rightarrow ll'$
 - ...

Other Channels

- Preliminary study of $B_s \rightarrow \phi \mu \mu$:
 - Expect ~ 1000 signal events from 2fb^{-1} data with $B/S < 0.9$ @ 90% CL
 - Factor 4 reduction in production rate B_s cf. B_d
 - The ϕ does not tag the B \rightarrow need flavour tagging, factor ~ 15 reduction
 \rightarrow expect $\sqrt{60}$ worse resolution than $B_d \rightarrow K^* \mu \mu$
 - Can make CP-averaged measurement of A_{FB} (if non-zero \Rightarrow CPV)
- Study of $b \rightarrow d$ transition $B_s \rightarrow K^* \mu \mu$ also planned:
 - Again, factor 4 reduction in production rate B_s cf. B_d
 - Rate reduced by $|V_{td}/V_{ts}|^2 = 0.208^2 \sim 1/25$
 - Given these reductions, expect will have to work harder to reduce background
 $\rightarrow \sim < 700$ events/ 2fb^{-1}

PID

“Robustness” of mis-id bkg estimation:

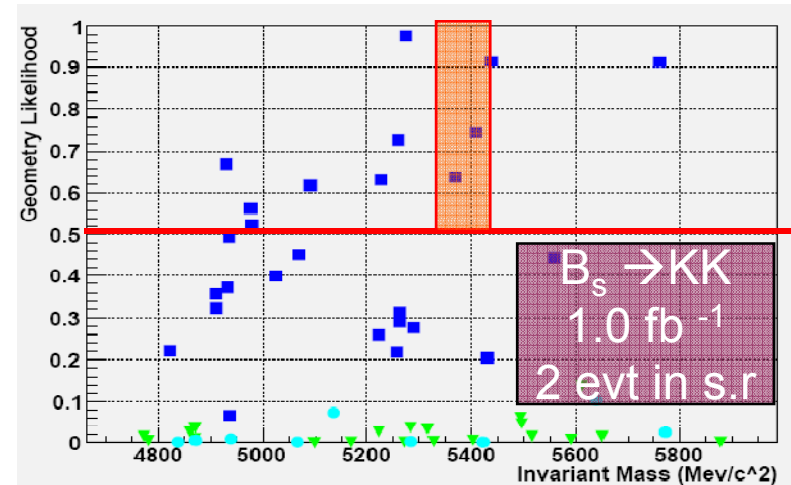


bb inclusive above $GL = 0.2$:

19 $b \rightarrow \text{dimuon}$

3 other muons

2 muon + mis-id \rightarrow **single mis-id probability needs to increase a factor ~ 10 to be of the same order as di-muon bkgd**



Double mis-id:

- dominated by $B \rightarrow hh$

- $\sim 4 \text{ evts/fb}^{-1} \rightarrow$ a factor ~ 50 less than dimuon

- **Mis-id needs to increase by a factor ~ 7 to be of the same order as dimuon bkgd**

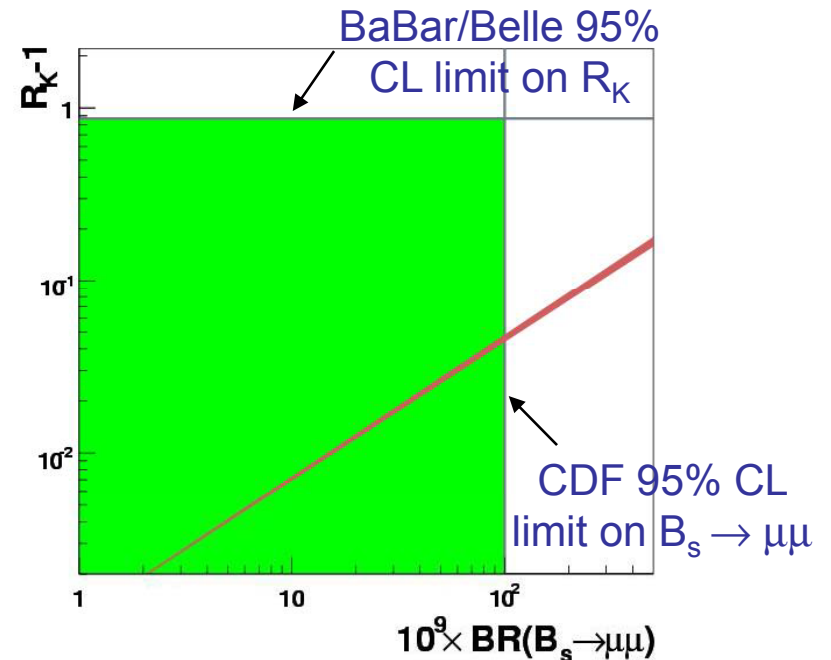
R_K in $B^+ \rightarrow K^+ \ell \ell$

- R_K theoretically well controlled in SM :

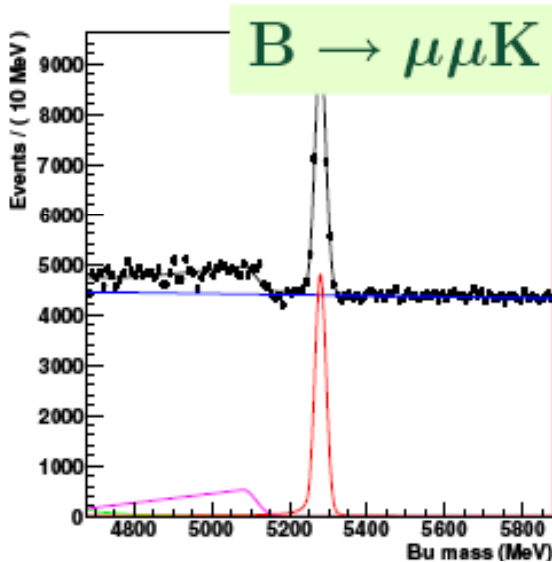
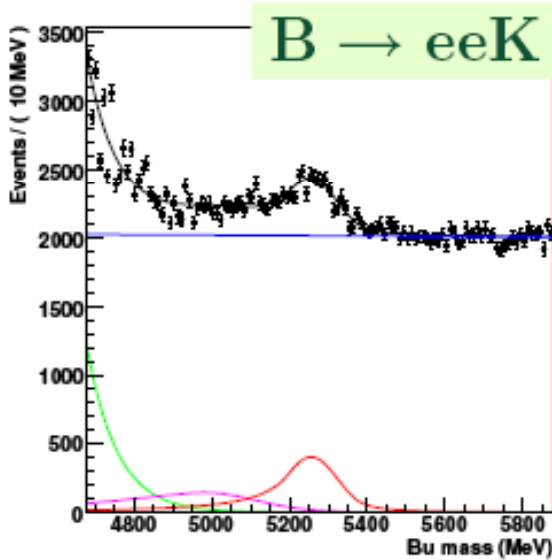
$$R_X = \frac{\int_{4m_\mu^2}^{q_{\max}^2} ds \frac{d\Gamma(B \rightarrow X \mu^+ \mu^-)}{ds}}{\int_{4m_\mu^2}^{q_{\max}^2} ds \frac{d\Gamma(B \rightarrow X e^+ e^-)}{ds}} \stackrel{\text{SM}}{=} \begin{cases} 1.000 \pm 0.001 & X = K \\ 0.991 \pm 0.002 & X = K^* \end{cases}$$

[Hiller & Krüger, PRD69 (2004) 074020]

- Effect of extensions to SM can be $O(10\%)$ e.g. from neutral Higgs boson exchange
- Related to $\text{BR}(B_s \rightarrow \mu\mu)$
- LHCb sensitivity with $B^+ \rightarrow K^+ \ell \ell$ has been investigated – can also be done with the K^* decay

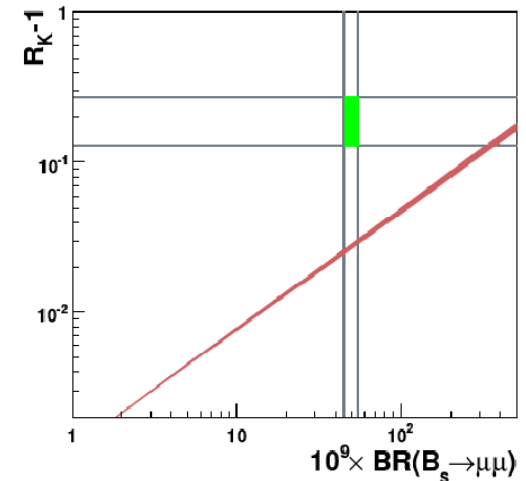


R_K in $B^+ \rightarrow K^+ \ell \ell$ (cont'd)



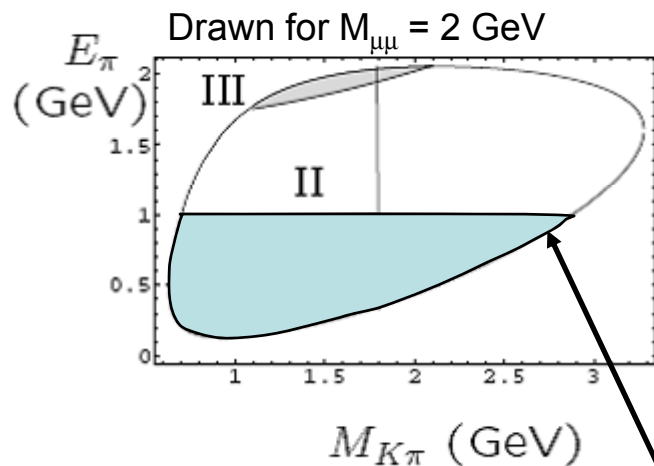
• Signal ■ $J/\psi K$ □ $K^* \ell \ell$ ○ $J/\psi K^*$ ◇ J/ψ ▲ $B\bar{B}$

- From 10 fb^{-1} data :
 - $B_d \rightarrow eeK$ $\sim 10k$
 - $B_d \rightarrow \mu\mu K$ $\sim 19k$
- Gives $R_K = 1 \text{ (fixed)} \pm 0.043$
- Possible status with 10 fb^{-1} data :
 - $BR(B_s \rightarrow \mu\mu) \sim 3 \times 10^{-9}$
 - $R_K \sim 1$ – compatible with MSSM with small $\tan \beta$
 - $R_K \neq 1$ – NP : right handed currents or broken lepton universality
 - $BR(B_s \rightarrow \mu\mu) \neq 3 \times 10^{-9}$
 - $R_K \sim 1$ – as above
 - $R_K = 1 + \epsilon$ – MFV



$B_d \rightarrow K^* \mu \mu$ – non-resonant bkgd

- Presently neglecting non-resonant background
- Limit can crudely be derived from BaBar data \rightarrow expect ~ 2000 events/ 2fb^{-1} ($\rightarrow B/S=0.5\pm0.2$)
- Has been suggested that, under certain kinematic conditions, these can be treated as signal [[Grinstein, Pirjol, hep-ph/0505155](#)]:

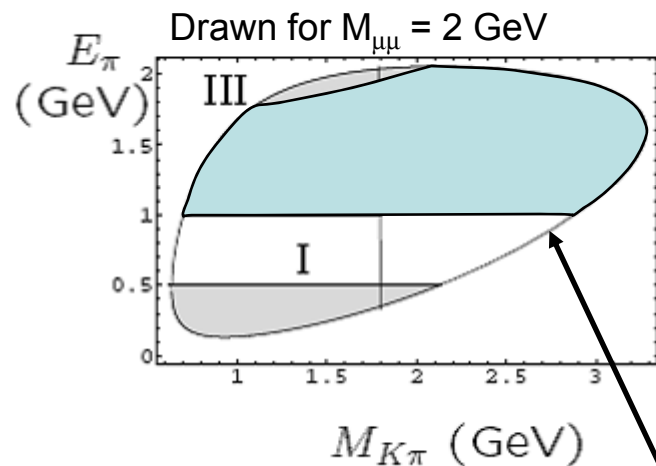


- **Region I: soft pion, energetic kaon**
 - Shifts zero of A_{FB} and larger theory errors
- Region II: energetic $K\pi$ pair
 - Can be treated as $B \rightarrow X\mu\mu$ and $X \rightarrow K\pi$
- Region III: soft kaon, energetic pion
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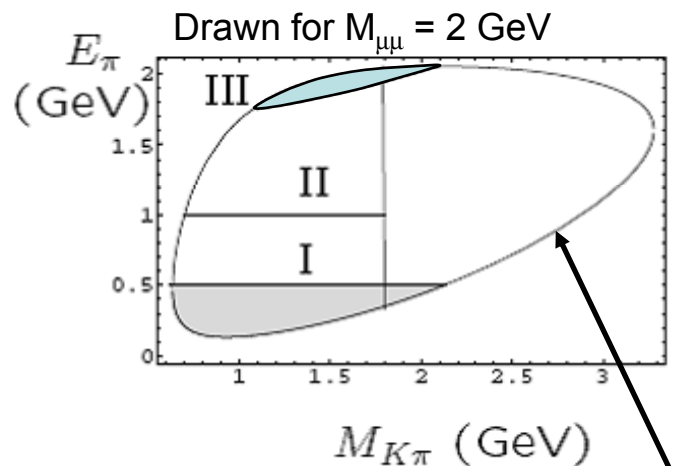


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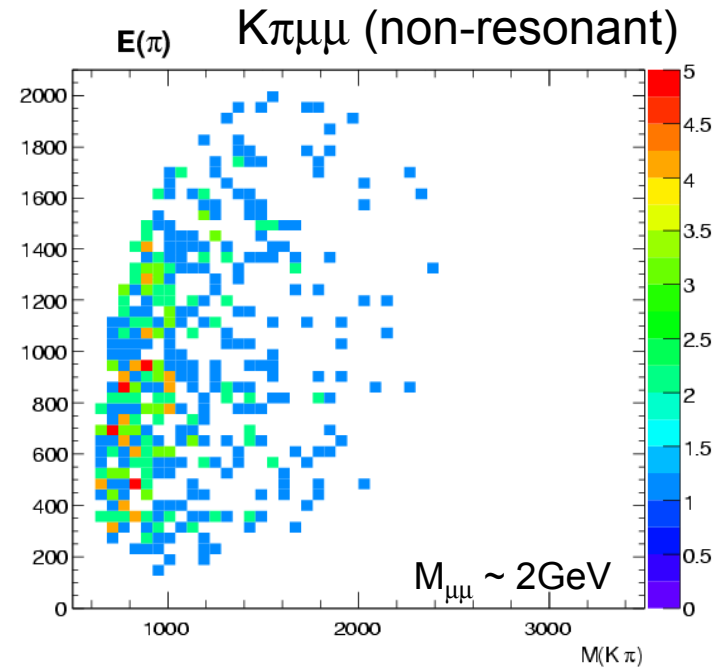
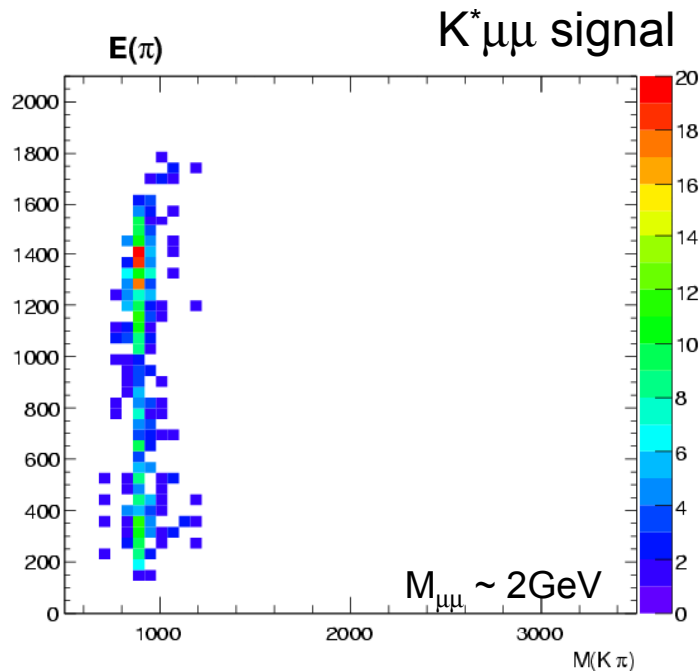


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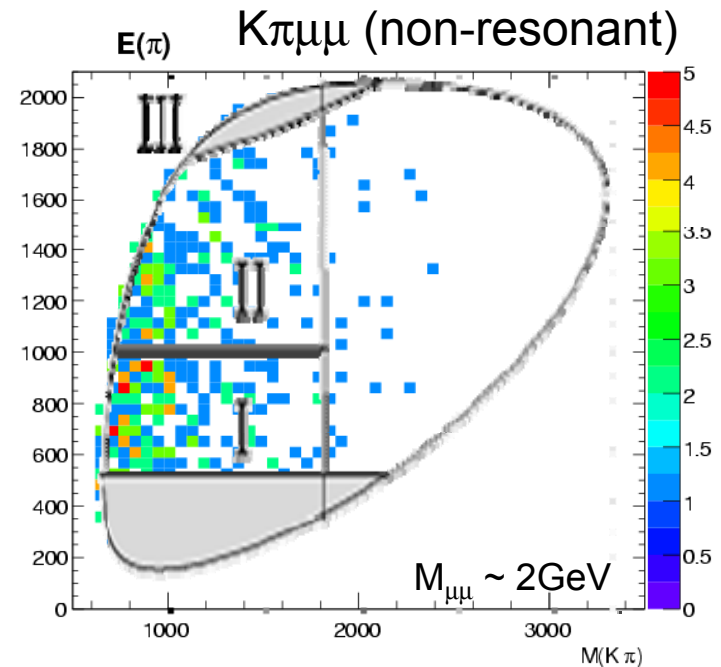
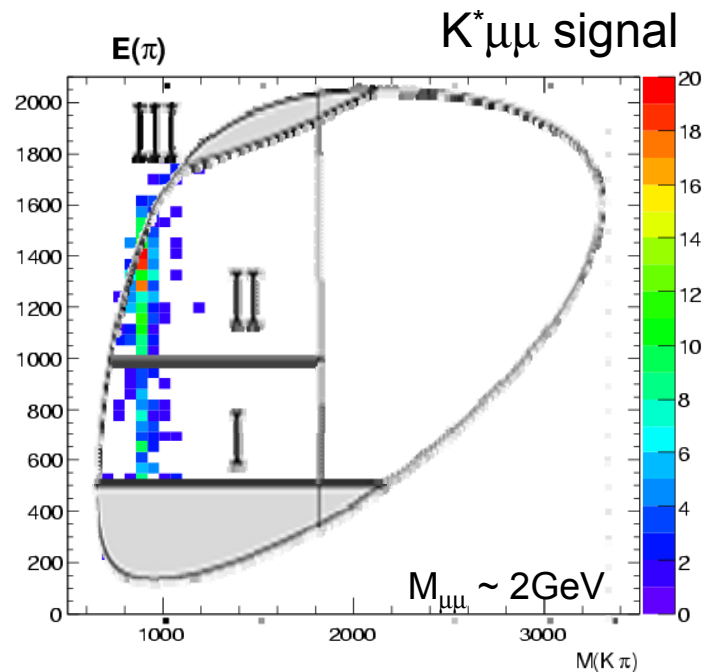


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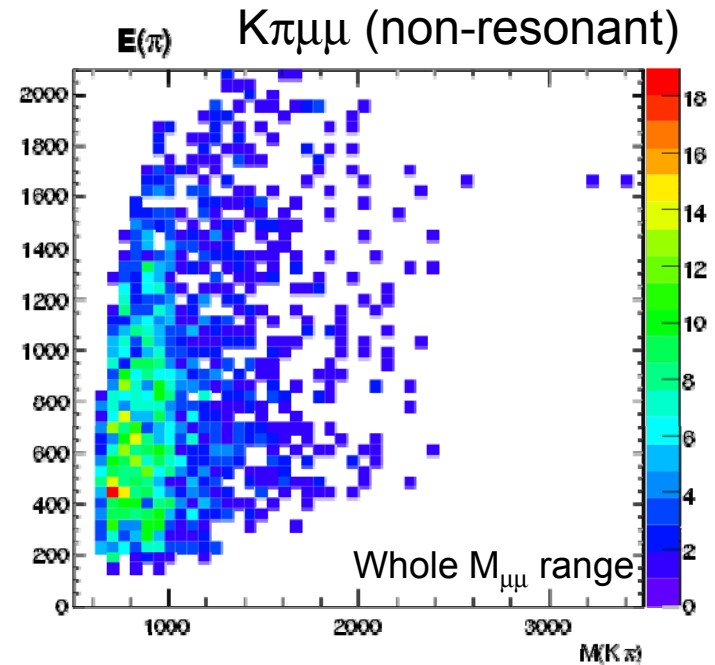
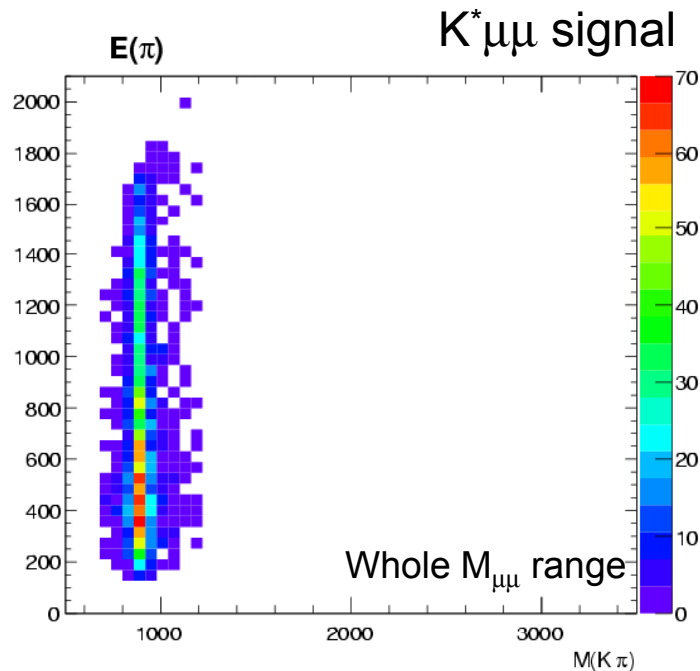


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- Plan to measure $d\Gamma/dm_{K\pi}$