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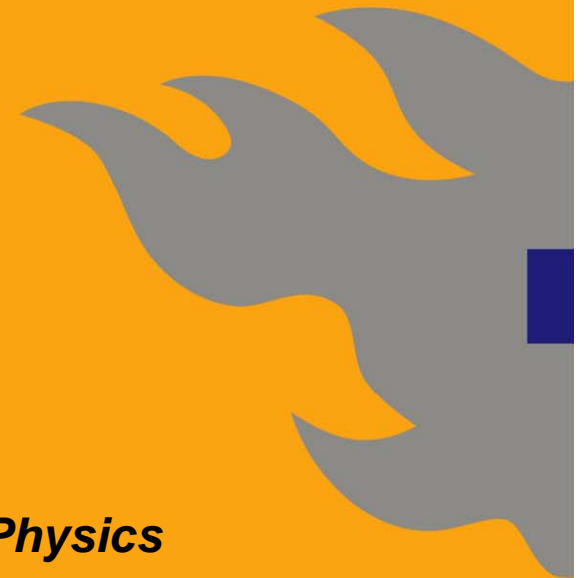
Atomistic simulations of breakdown triggers: progress report

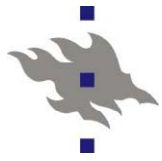
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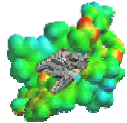
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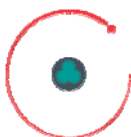
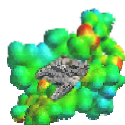


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- Our simulation approach
 - Molecular Dynamics + Laplace equation solution
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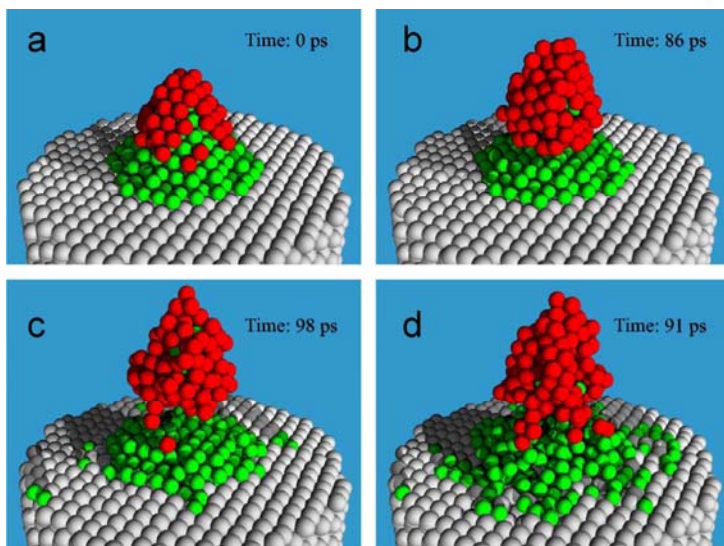
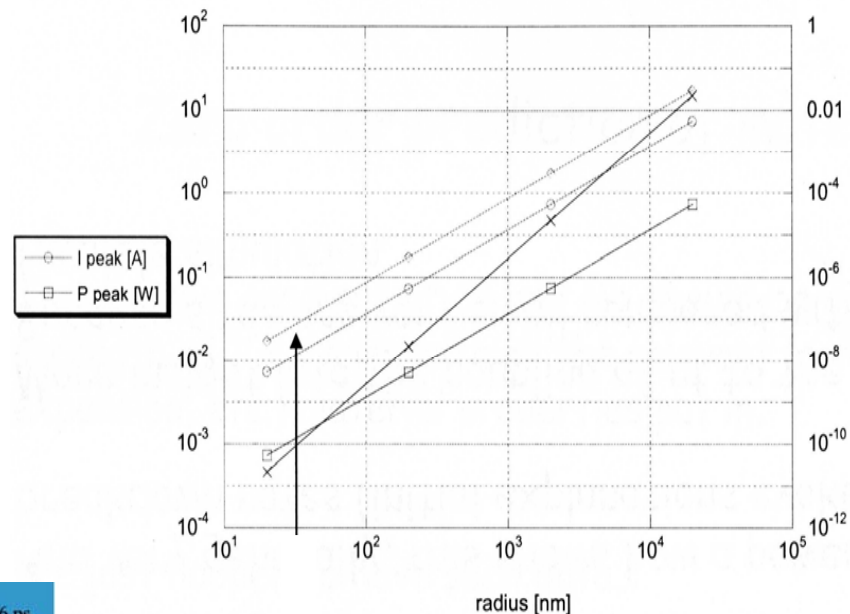
Why atomistic simulation?



Background 1

Sergio Calatroni's results indicate that the breakdown triggers at about 10 nm scale

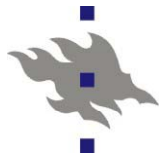
Parameters to obtain the melting point of the tip of a Cu cylinder of given radius and $\beta=30$



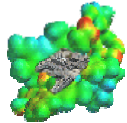
Background 2

Insepov has shown that nanobump + high electric field can lead to the cluster evaporation

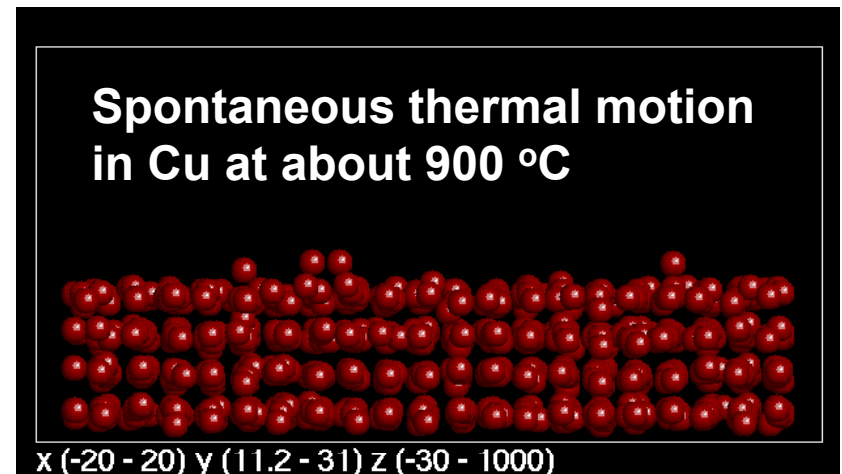
[Insepov et al, PRST-AB 7 (2004) 122001]



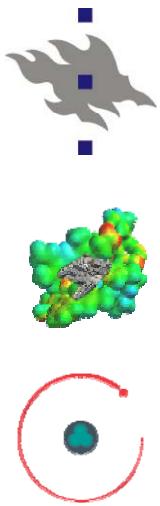
Motivation



- Breakdown takes place even if the surface is well-smoothed (no rough features are seen in SEM). Also the effect has been observed with many different materials
- => There must be a generic spontaneous roughening mechanism leading to the breakdown
 - But, metal surfaces are known **not** to form stable rough surfaces at room temperature
 - Due to thermal motion, some atoms can temporarily become adatoms
 - => Stable roughening requires an electric field!



What do we suggest?

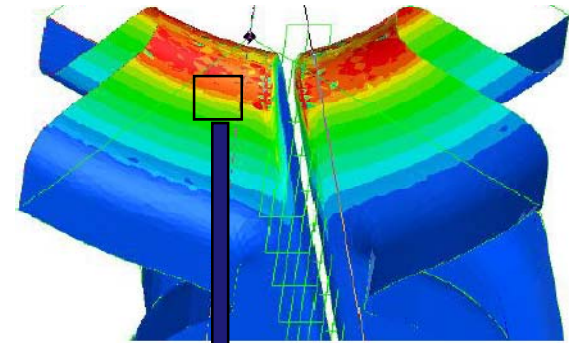


Gauss law states

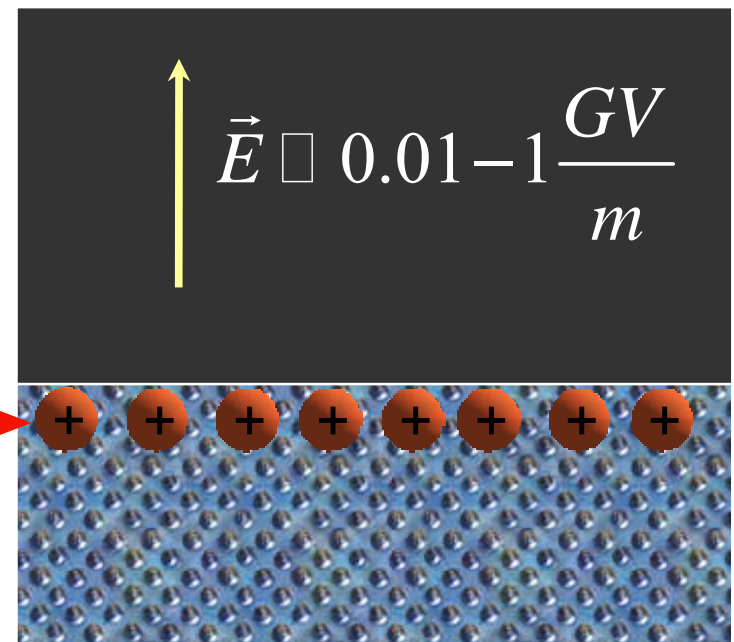
$$\sigma = \frac{Q_{surface}}{A_{surface}} = \epsilon_0 E$$

Due to the external electric field
the surface attains charge

Macroscopic field

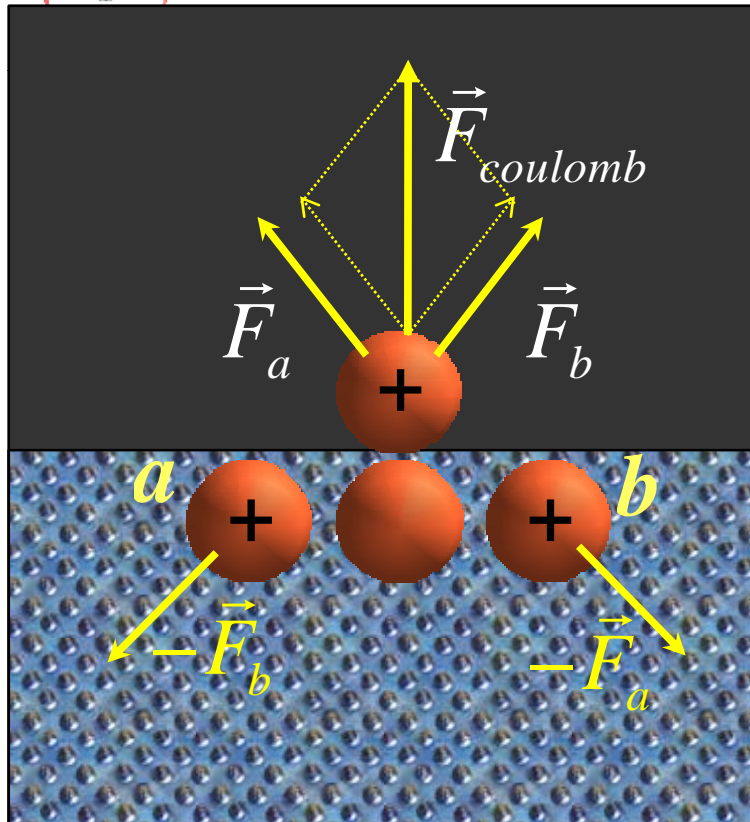
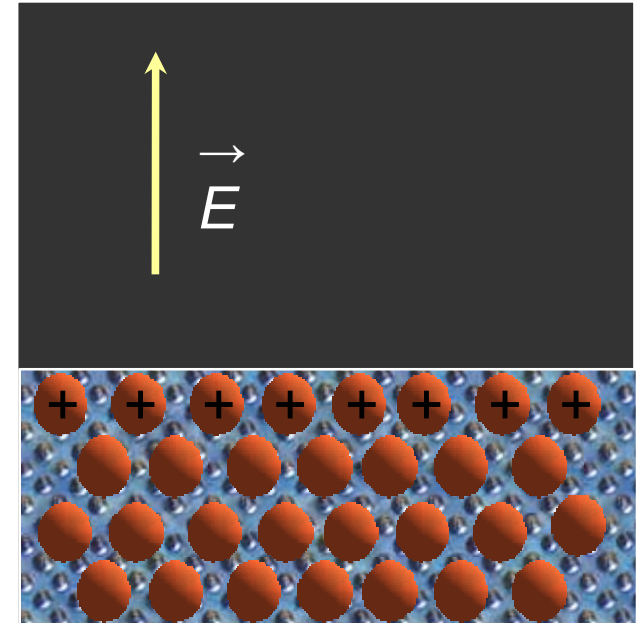
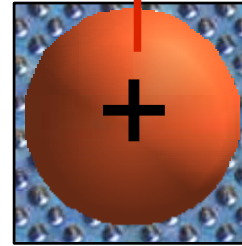


on atomic level:



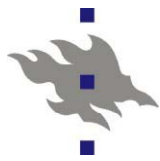
What does this mean for the atoms?

$$\vec{F}_{el} = \vec{E}q$$

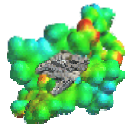


$$\vec{F}_a = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_a q_i}{r_{0i}^2} \hat{r}_{0i}$$

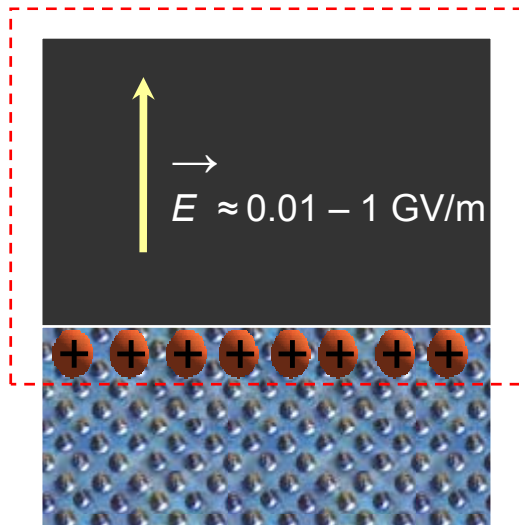
$\vec{F}_{el} + \vec{F}_{coulomb}$ give a driving force for roughening!



Simulation approach



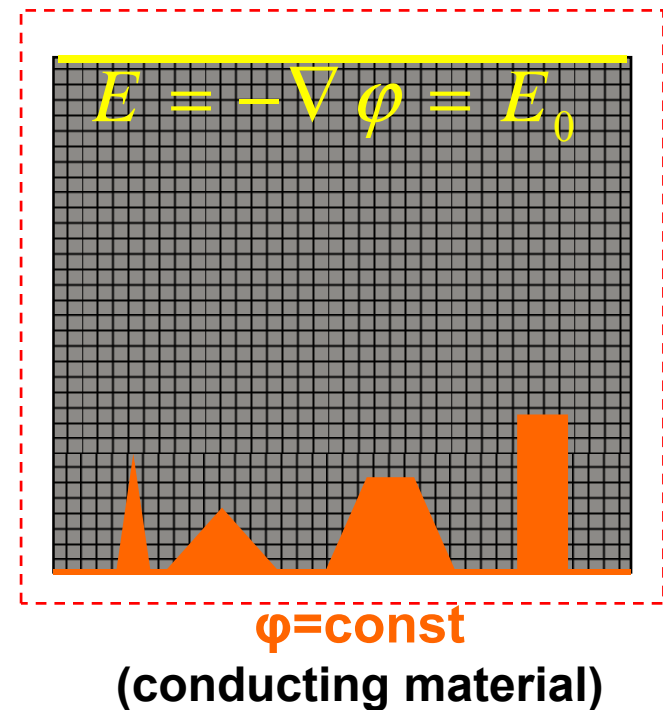
- The current state: we are building a hybrid Electrodynamics/Molecular Dynamics (HED-MD) code to simulate the effect of the electric field

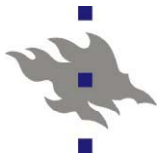


The effect of the electric field is introduced by means of solution of Laplace's equation

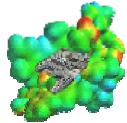
$$\nabla^2 \varphi = 0$$

with the mixed boundary condition





What do we have as output?



- Solution gives \vec{E} at each surface atom \vec{E}_i



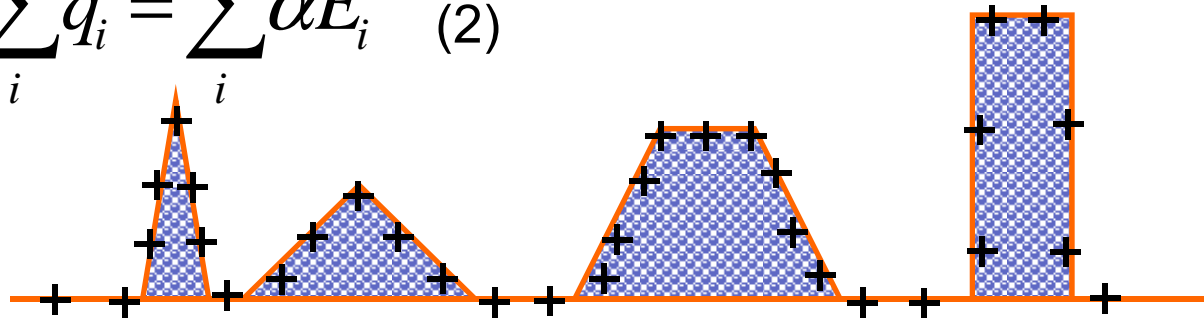
According to Gauss law

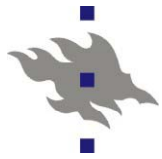
$$Q_{surface} = A_{surface} \epsilon_0 E_0$$

On the other hand, the charge of an atom is proportional to the electric field applied to that atom

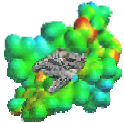
$$q_i \propto E_i \Rightarrow q_i = \alpha E_i \quad (1)$$

$$Q_{surface} = \sum_i q_i = \sum_i \alpha E_i \quad (2)$$





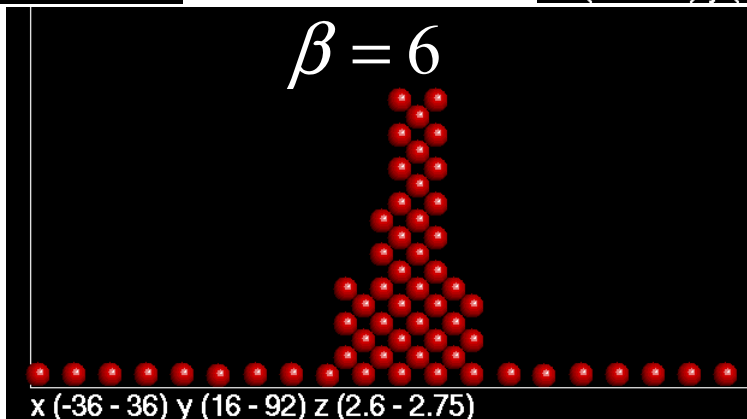
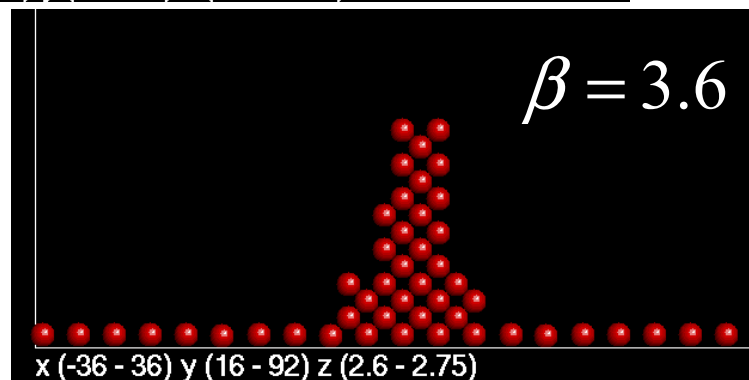
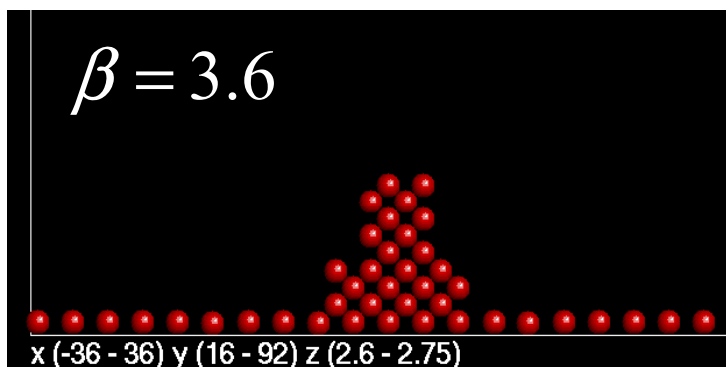
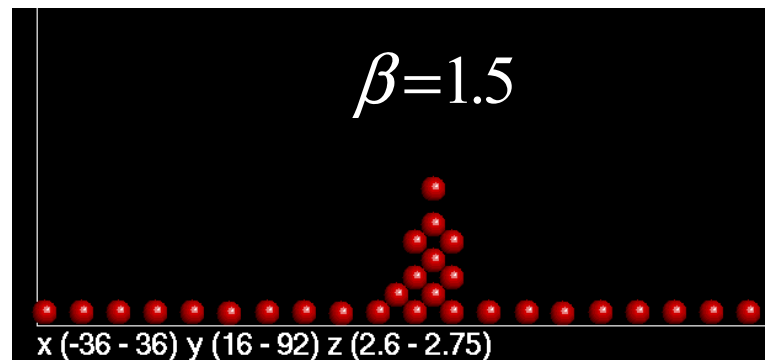
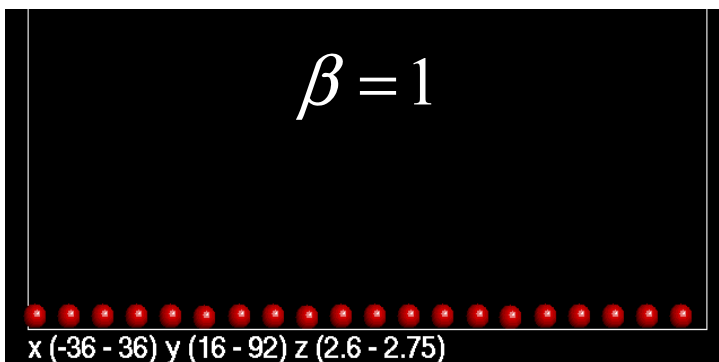
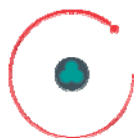
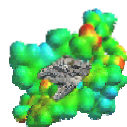
ED + MD: how does this work?



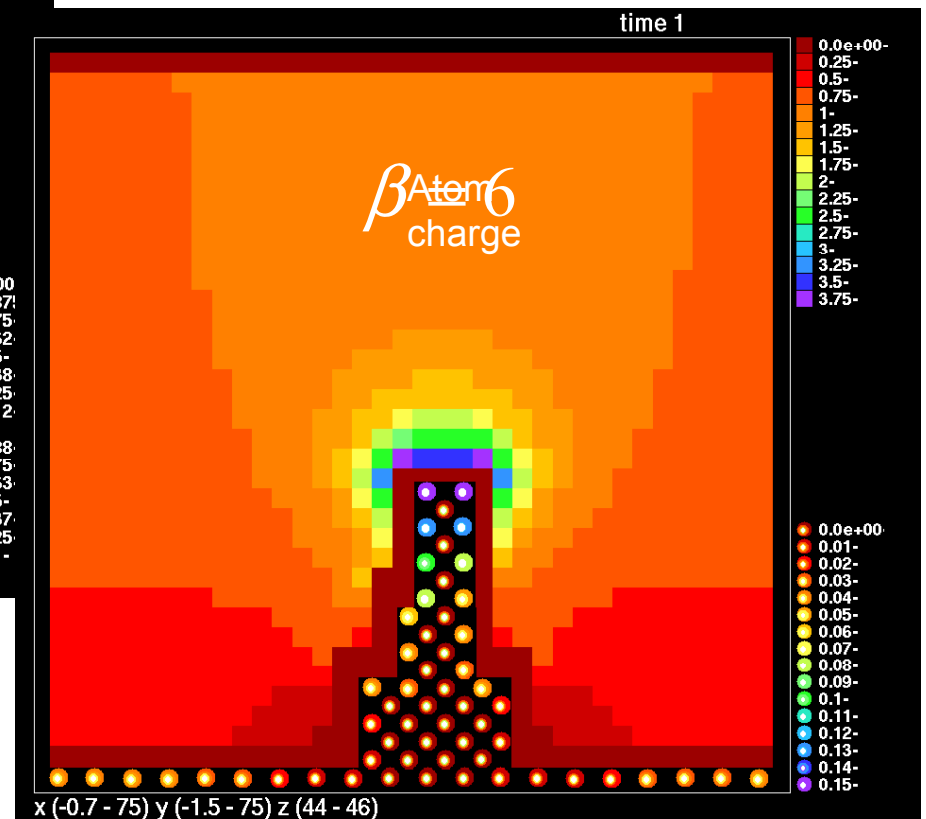
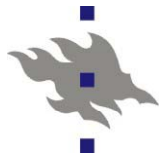
- We embed electrodynamics forces F_{el} and also calculate the Coulombic forces which appear between the charged surface atoms $F_{Coulomb}$, and use the sum of the forces in the MD code to correct the normal atom motions according to the applied electrical field.

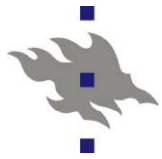


Enhancement factor β for different hillocks on the top of a Cu surface

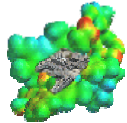


Solution of Laplace's equation for $\beta=3.6$ and $\beta=6$ and the charge distribution on the surface atoms





Outlook



- The solution of Laplace's equation must be speeded up due to the huge computational time consumption. We believe this is possible with application of some multigrid scheme
 - we are open for recommendations of suitable efficient methods...
- Dynamic simulation will be the next step to examine the roughening mechanism of the surface