

Higgs-boson pair production in the $D=6$ extension of the SM

*LHC Higgs XS
HH Subgroup Meeting*

CERN, 8.12.2014

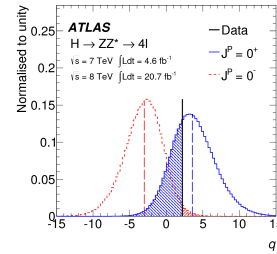
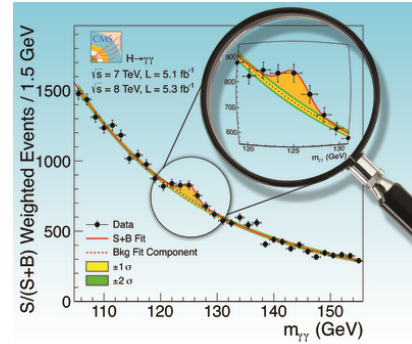
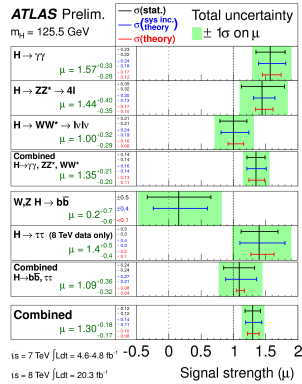
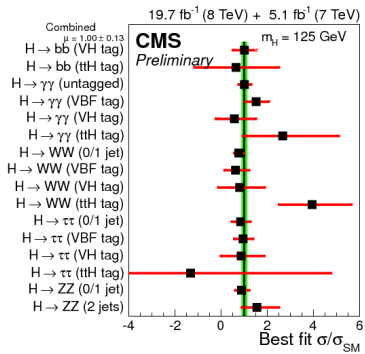
Florian Goertz
CERN



arXiv: 1410.3471
FG, Papaefstathiou, Yang, Zurita

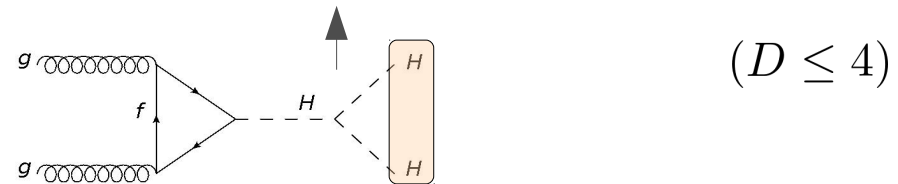
Introduction

- Is it the SM-Higgs Boson?
- Scale of New Physics?



Important test: Higgs potential $V(h) = \frac{1}{2}m_h^2 h^2 + \lambda_{hhh} v h^3 + \frac{1}{4}\lambda_{hhhh} h^4$

self couplings



$$\lambda_{hhhh}^{SM} = \lambda_{hhhh}^{SM} = \frac{m_h^2}{2v^2} \approx 0.13$$

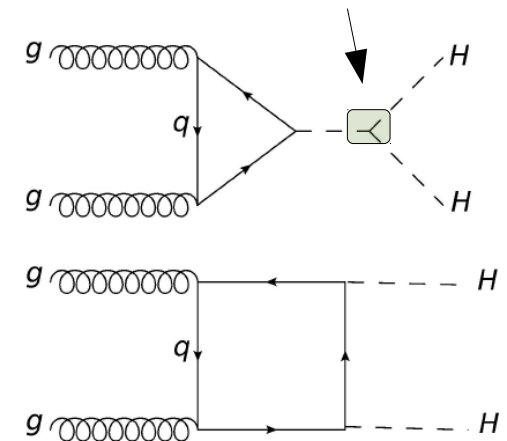
Measuring λ_{hhh}

Expected constraints on $\lambda \equiv \lambda_{hhh}/\lambda_{hhh}^{\text{SM}}$ @LHC

- Simple approach: addition of a single $D=6$ operator $\leftrightarrow \lambda_{hhh} \neq \lambda_{hhh}^{\text{SM}}$

Process	600 fb ⁻¹ (1 σ)	3000 fb ⁻¹ (1 σ)
$b\bar{b}\tau^+\tau^-$	(0.57, 1.64)	(0.69, 1.40)
$b\bar{b}W^+W^-$	(0.46, 1.95)	(0.65, 1.46)
$b\bar{b}\gamma\gamma$	(0.09, 4.83)	(0.48, 1.87)

from FG, Papaefstathiou, Yang, Zurita, 1301.3492



- assumed $\lambda_{\text{true}} = 1$
- Reduce error by employing ratio $C_{hh} = \frac{\sigma(gg \rightarrow hh)}{\sigma(gg \rightarrow h)} \equiv \frac{\sigma_{hh}}{\sigma_h}$

Combination yields $\sim 30\%$ accuracy with 3000 fb⁻¹

Full Analysis: Higgs EFT

- Assume (unspecified) New Physics at a scale $\Lambda \gg v$
 \rightarrow leading effects: $D=6$ operators built of SM content

Buchmuller, Wyler, NPB 268(1986)621–653

Grzadkowski, Iskrzynski, Misiak, Rosiek, 1008.4884

Here:

$$\begin{aligned} \mathcal{L} = \mathcal{L}_{\text{SM}} &+ \frac{c_H}{2\Lambda^2} (\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2} \lambda |H|^6 \\ &- \left(\frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \frac{c_\tau}{\Lambda^2} y_\tau |H|^2 \bar{L}_L H \tau_R + \text{h.c.} \right) \\ &+ \frac{\alpha_s c_g}{4\pi \Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} + \frac{\alpha' c_\gamma}{4\pi \Lambda^2} |H|^2 B_{\mu\nu} B^{\mu\nu} + \mathcal{O}_{WW} (+\mathcal{L}_{\text{CP}} + \mathcal{L}_{4f}) \end{aligned}$$

- Neglected operators that are strongly constrained from precision tests

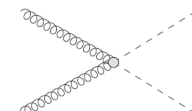
See e.g.: Elias-Miro, Espinosa, Masso, Pomarol, 1308.1879; Pomarol, Riva, 1308.2803; Corbett, Eboli, Gonzalez-Fraile, Gonzalez-Garcia 1207.1344, 1211.4580, 1304.1151; Falkowski, Riva, Urbano, 1303.1812; Contino, Ghezzi, Grojean, Muhlleitner, Spira, 1303.3876; Dumont, Fichet, von Gersdorff 1304.3369; Falkowski, Riva, 1411.0669, Trott 1409.7605, ...

For non-linear realization, see e.g. Grinstein, Trott 0704.1505; Contino, Grojean, Moretti, Piccinini, Rattazzi 1002.1011

$$\mathcal{O}_{WW} = \tilde{c}_{HW} (D^\mu H)^\dagger \sigma_k (D^\nu H) W_{\mu\nu}^k + \tilde{c}_{HB} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} + \tilde{c}_W (H^\dagger \sigma_k \overleftrightarrow{D}^\mu H) D^\nu W_{\mu\nu}^k + \tilde{c}_B (H^\dagger \overleftrightarrow{D}^\mu H) \partial^\nu B_{\mu\nu}$$

Only one free parameter

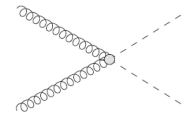
Higgs Boson EFT

$$\begin{aligned}
 \mathcal{L} = \mathcal{L}_{\text{SM}} &+ \frac{c_H}{2\Lambda^2} (\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2} \lambda |H|^6 \quad \text{Pure Higgs} \\
 &- \left(\frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \frac{c_\tau}{\Lambda^2} y_\tau |H|^2 \bar{L}_L H \tau_R + \text{h.c.} \right) \quad \text{Yukawa type} \\
 &+ \frac{\alpha_s c_g}{4\pi\Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} + \frac{\alpha' c_\gamma}{4\pi\Lambda^2} |H|^2 B_{\mu\nu} B^{\mu\nu}
 \end{aligned}$$


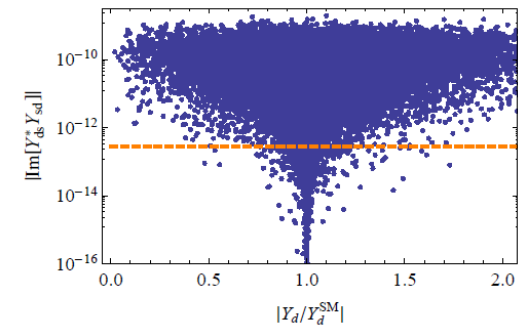
Higgs Boson EFT

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \underbrace{\frac{c_H}{2\Lambda^2}(\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2}\lambda |H|^6}_{\text{Pure Higgs}} \underbrace{- \left(\frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \frac{c_\tau}{\Lambda^2} y_\tau |H|^2 \bar{L}_L H \tau_R + \text{h.c.} \right)}_{\text{Yukawa type}}$$

$$+ \underbrace{\frac{\alpha_s c_g}{4\pi\Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} + \frac{\alpha' c_\gamma}{4\pi\Lambda^2} |H|^2 B_{\mu\nu} B^{\mu\nu}}_{\text{Gauge}}$$



- What about light-quark Yukawas
→ can assume MFV, but even should be negligible on more general grounds: FCNCs



FG, 1406.0102

$gg \rightarrow hh$

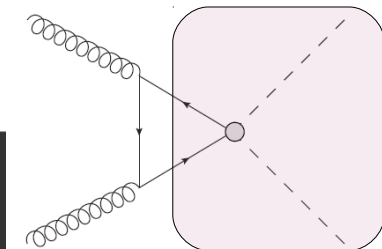
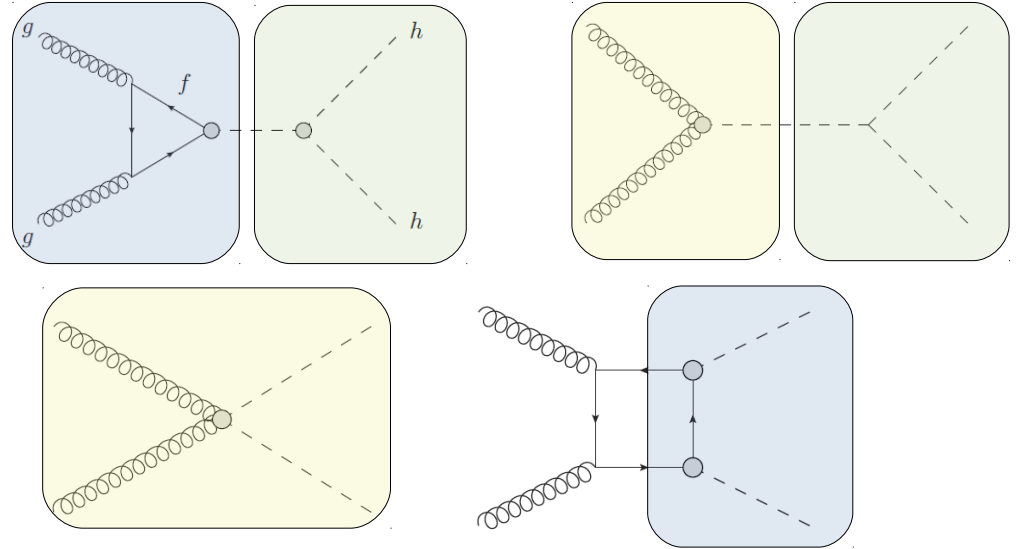
Relevant Terms:

$$\mathcal{L}_{hh} = - \frac{m_h^2}{2v} \left(1 - \frac{3}{2}c_H + c_6 \right) h^3$$

$$+ \frac{\alpha_s c_g}{4\pi} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu}$$

$$- \left[\frac{m_t}{v} \left(1 - \frac{c_H}{2} + c_t \right) \bar{t}_L t_R h + \text{h.c.} \right]$$

$$- \left[\frac{m_t}{v^2} \left(\frac{3c_t}{2} - \frac{c_H}{2} \right) \bar{t}_L t_R h^2 + \text{h.c.} \right]$$



$$c_i \rightarrow c_i \Lambda^2 / v^2$$

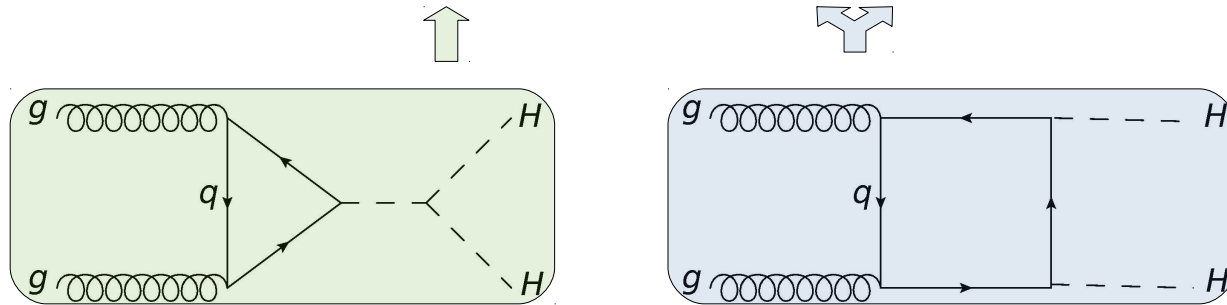
$$H = \exp \left(-i \frac{T \cdot \xi}{v} \right) \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h \end{pmatrix}$$

$$h \rightarrow \left(1 - \frac{c_H v^2}{2\Lambda^2} \right) h - \frac{c_H v}{2\Lambda^2} h^2 - \frac{c_H}{6\Lambda^2} h^3$$

non-linear redefinition:
removes momentum-dependent interactions

Cross Section in SM (LO)

$$\frac{d\hat{\sigma}(gg \rightarrow hh)}{d\hat{t}} = \frac{G_F^2 \alpha_s^2}{256(2\pi)^3} \left[\overset{\text{spin-0}}{\boxed{C_\Delta F_\Delta}} + \boxed{C_\square F_\square}^2 + \overset{\text{spin-2}}{\boxed{C_\square G_\square}}^2 \right]$$



$$C_\Delta = \frac{3m_h^2}{\hat{s} - m_h^2},$$

$$F_\Delta = \frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2),$$

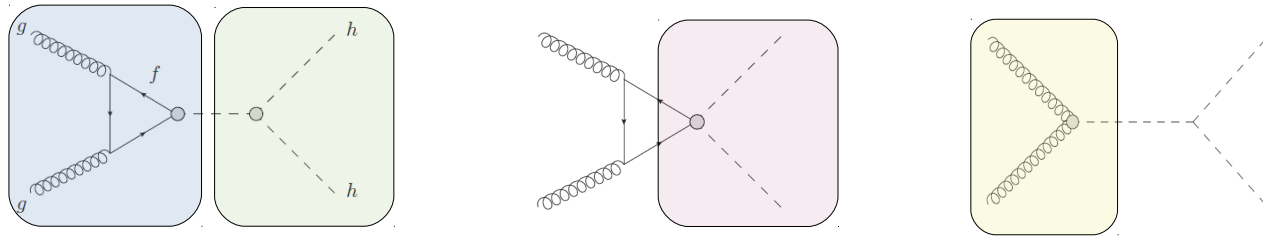
$$C_\square = 1$$

$$F_\square = -\frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2),$$

$$G_\square = \mathcal{O}(\hat{s}/m_Q^2)$$

See Plehn, Spira, Zerwas [ph/9603205](#)

Cross Section in $D=6$ EFT

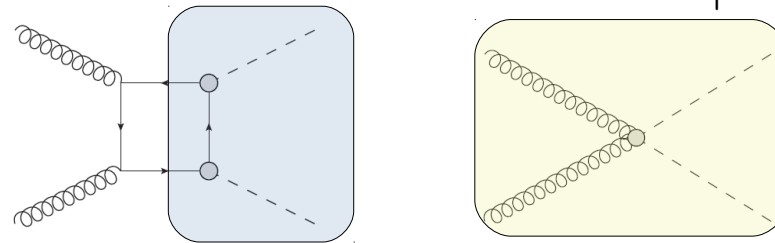


$$\left. \frac{d\hat{\sigma}(gg \rightarrow hh)}{d\hat{t}} \right|_{\text{EFT}} = \frac{G_F^2 \alpha_s^2}{256(2\pi)^3} \left\{ \left| C_\Delta F_\Delta (1 - 2c_H + c_t + c_6) + 3F_\Delta (3c_t - c_H) + 2c_g C_\Delta \right. \right. \\ \left. \left. + C_\square F_\square (1 - c_H + 2c_t) + 2c_g C_\square \right|^2 + \left| C_\square G_\square \right|^2 \right\}$$

$$C_\Delta = \frac{3m_h^2}{\hat{s} - m_h^2}, \quad C_\square = 1$$

$$F_\Delta = \frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2), \quad F_\square = -\frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2),$$

$$G_\square = \mathcal{O}(\hat{s}/m_Q^2)$$



Implemented in MC generator Herwig++

Normalize to NNLO: de Florian, Mazzitelli, 1309.6594

See Plehn, Spira, Zerwas [ph/9603205](#)

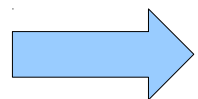
Higgs Decays in $D=6$ EFT

Mode	tree	1 loop QCD	1 loop
$h \rightarrow bb$	c_H, c_b	c_H, c_b	c_H, c_b, c_t, c_6, c_W
$h \rightarrow \tau\tau$	c_H, c_τ	-	c_H, c_τ, c_6, c_W
$h \rightarrow \gamma\gamma$	c_γ	- Loop + $1/\Lambda^2$ suppressed wrt SM	$c_H, c_b, c_t, c_\tau, c_W$
$h \rightarrow WW$	c_H, c_{HW}, c_W		$c_H, c_W, c_b, c_t, c_\tau, c_6$
...			
$gg \rightarrow hh$	c_g	c_t, c_b	c_t, c_b, c_H, c_6
$gg \rightarrow h$	c_g	c_t, c_b, c_H	c_t, c_b, c_H

Bold coefficients included in analysis

(via eHDECAY: Contino, Ghezzi, Grojean, Muhlleitner, Spira, 1403.3381)

Don't include suppressed (loop) operators in loop topologies

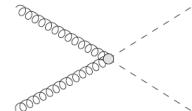


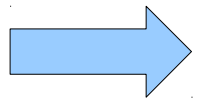
6 Parameters: $\{c_6, c_H, c_t, c_b = c_\tau, c_g, c_\gamma\}$

Unique accessibility in hh production!

HH in D=6 EFT

Reminder:

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \underbrace{\frac{c_H}{2\Lambda^2} (\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2} \lambda |H|^6}_{\text{Pure Higgs}} \underbrace{- \left(\frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \frac{c_\tau}{\Lambda^2} y_\tau |H|^2 \bar{L}_L H \tau_R + \text{h.c.} \right)}_{\text{Yukawa type}} + \underbrace{\frac{\alpha_s c_g}{4\pi \Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} + \frac{\alpha' c_\gamma}{4\pi \Lambda^2} |H|^2 B_{\mu\nu} B^{\mu\nu}}_{\text{Gauge}}$$




6 Parameters: $\{c_6, c_H, c_t, c_b = c_\tau, c_g, c_\gamma\}$



Unique accessibility in hh production!

Analysis

- Focus on $hh \rightarrow b\bar{b}\tau^+\tau^-$
@LHC14

Dolan, Englert, Spannowsky, 1206.5001

Baglio, Djouadi, Grober, Muhlleitner, Quevillon; 1212.5581

Barr, Dolan, Englert, Spannowsky,, 1309.6318

Maierhoefer, Papaefstathiou, 1401.0007

- Main backgrounds:
- $pp \rightarrow t\bar{t} \rightarrow b\bar{b}\tau^+\tau^- (+E_{\text{mis}})$

Generated with **aMC@NLO**
(+ HERWIG++)

Frixione et. al., 1010.0568

Frederix et. al., 1104.5613

Alwall et. al., 1405.0301

- $pp \rightarrow ZZ \rightarrow b\bar{b}\tau^+\tau^-$

- $pp \rightarrow hZ \rightarrow b\bar{b}\tau^+\tau^-$

Analysis: $hh \rightarrow b\bar{b}\tau^+\tau^-$

- Main backgrounds:

Generated with **aMC@NLO**
(+ HERWIG++)

Frixione et. al., 1010.0568

Frederix et. al., 1104.5613

Alwall et. al., 1405.0301

- $pp \rightarrow t\bar{t} \rightarrow b\bar{b}\tau^+\tau^- (+E_{\text{mis}})$

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- $pp \rightarrow hZ \rightarrow b\bar{b}\tau^+\tau^-$

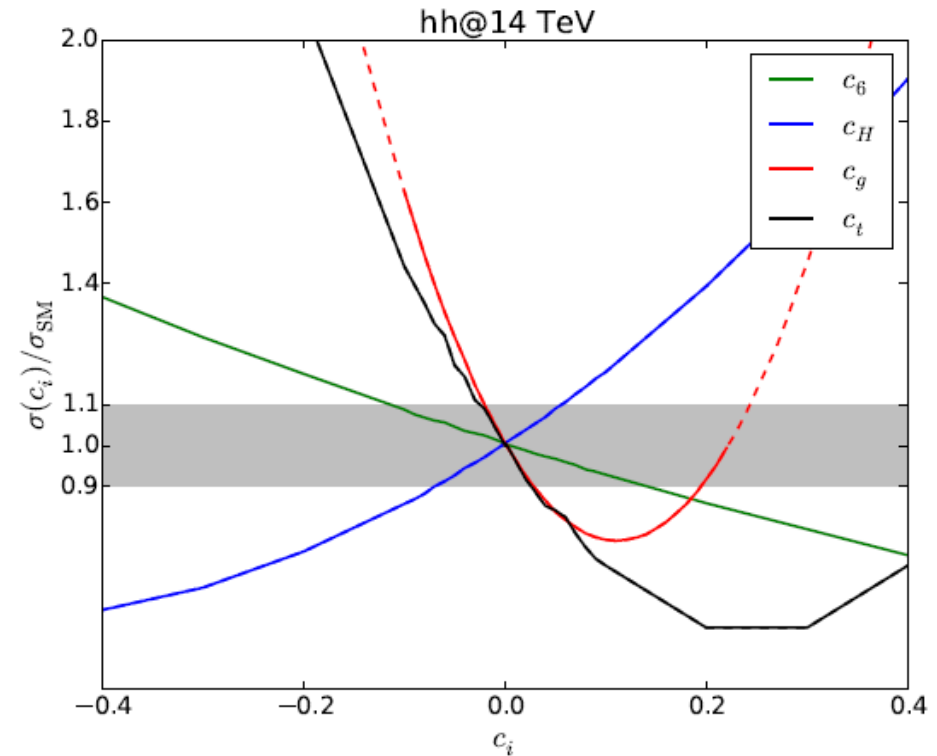
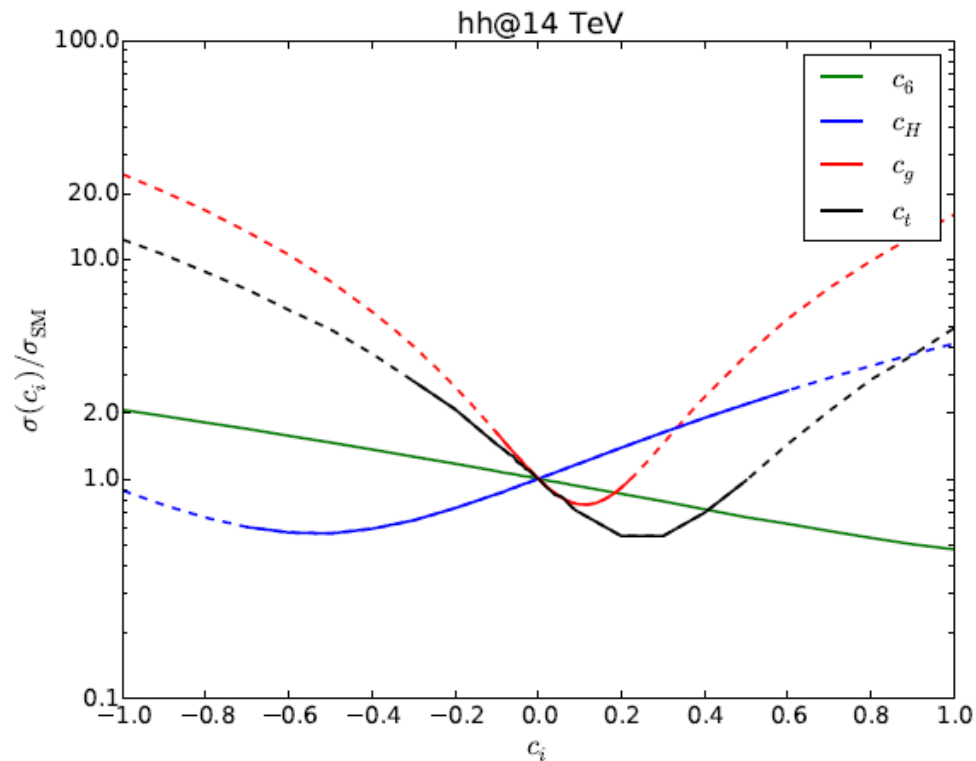
Cuts:

- Two τ -tagged jets with $p_{\perp} > 20 \text{ GeV}$
- one fat jet with $R = 1.4$ (CA), two hardest sub-jets b -tagged ($|\eta| < 2.5$)
Butterworth, Davison, Rubin, Salam, 0802.2470
- $m_{\tau^+\tau^-}, m_{\text{fat}} \in [m_h - 25 \text{ GeV}, m_h + 25 \text{ GeV}]$
- $p_{\perp}^{\text{fat}}, p_{\perp}^{\tau\tau} > 100 \text{ GeV}, \Delta R(h, h) > 2.8, p_{\perp}^{hh} < 80 \text{ GeV}$

b, τ -tagging efficiencies: 70 %

see: Dolan, Englert, Spannowsky, 1206.5001;
Maierhoefer, Papaefstathiou, 1401.0007

$gg \rightarrow hh$ Cross Section in EFT



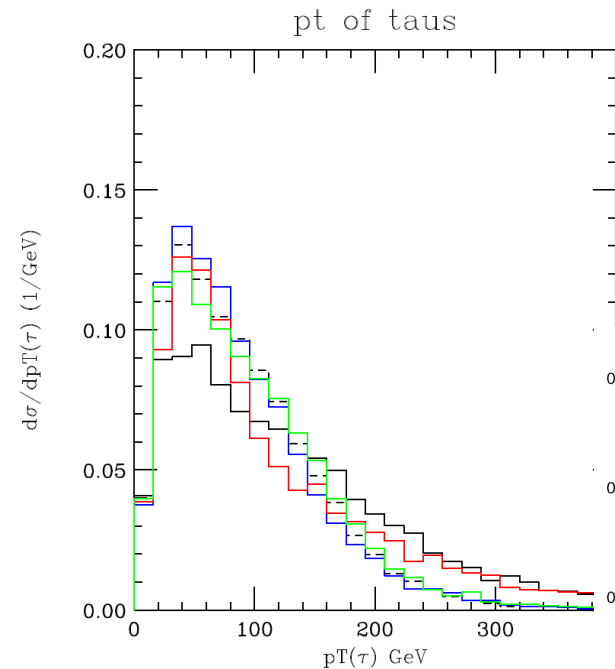
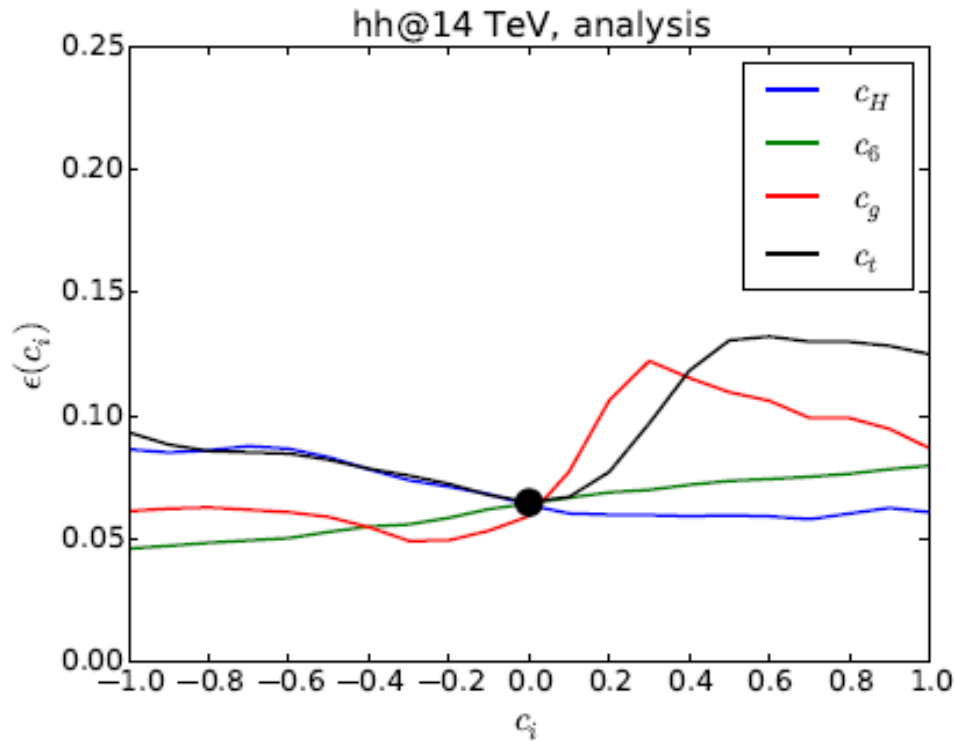
MSTW2008nlo_nf4 PDF

- Effect of varying individual Wilson coefficients
- Dashed: parameter-range excluded from current h data at the LHC
 → used HiggsBounds, HiggsSignals on cross sections calculated via eHDECAY

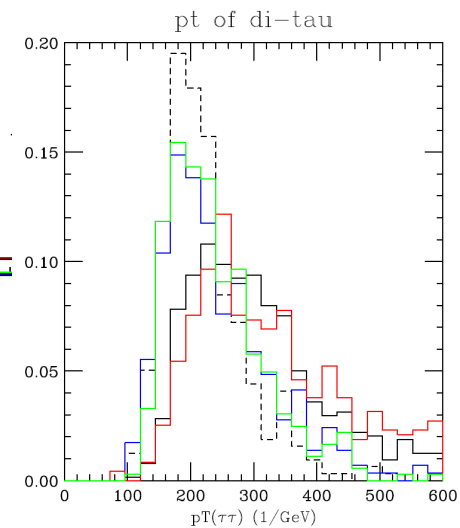
Bechtle et.al., 1311.0055, 1305.1933

$gg \rightarrow hh$ after cuts

Efficiency



$c_i=0.5$

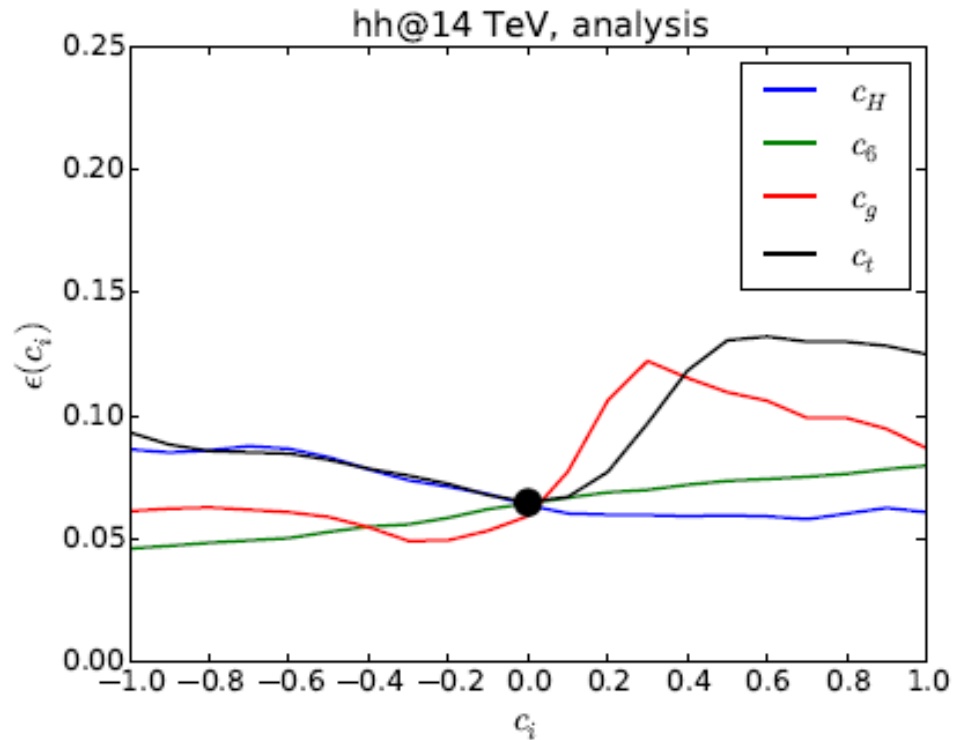


MC generator important for analysis

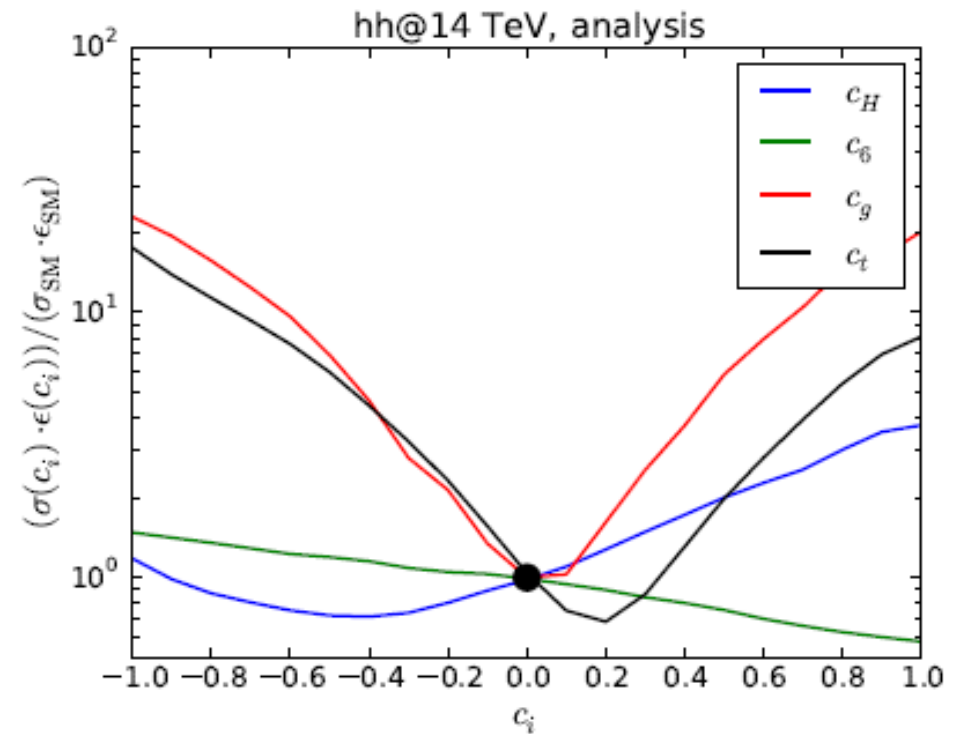
→ describe distributions, which determine efficiencies $\epsilon(c_i)$

$gg \rightarrow hh$ after cuts

Efficiency



Cross Section



MC generator important for analysis

→ describe distributions, which determine efficiencies $\epsilon(c_i)$

Full Analysis

- Start with model where only $c_6 \neq 0$ (unconstrained from single h)

↳ Vary only λ as done in previous studies (\rightarrow BRs unchanged)

- $S(c_6)$ signal + B background events @ given L_{int}
- $N(c_6) = S(c_6) + B$, $\delta N^2 = \delta S^2 + \delta B^2 + S^2 f_{\text{th}}^2$

$$\delta N^2 = N + S^2 f_{\text{th}}^2$$

30% $\sim 10\%$ (scale) + 10% (pdf + α_s) + 10% (m_t)

Full Analysis

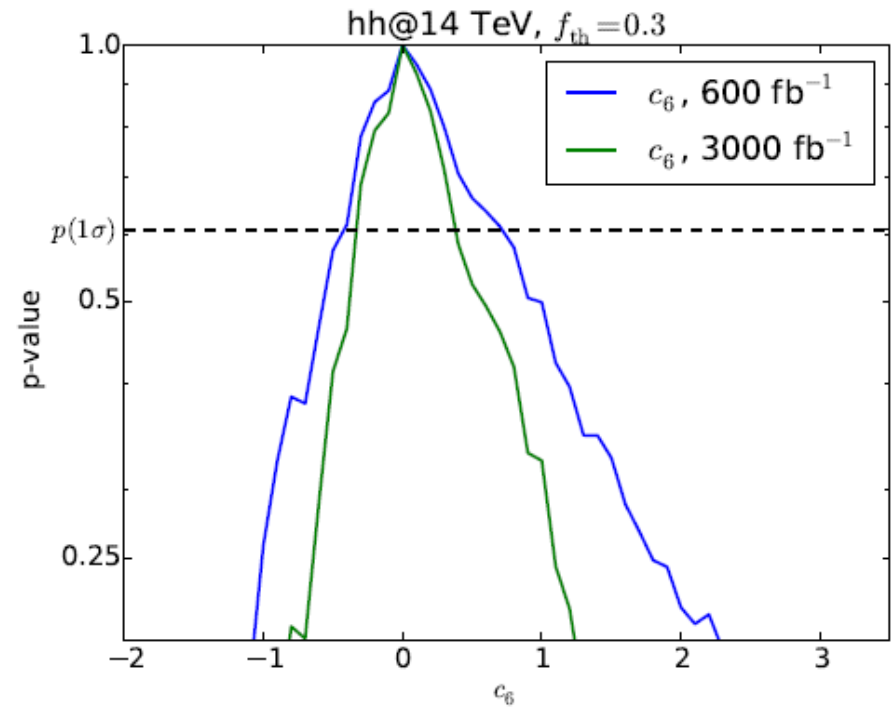
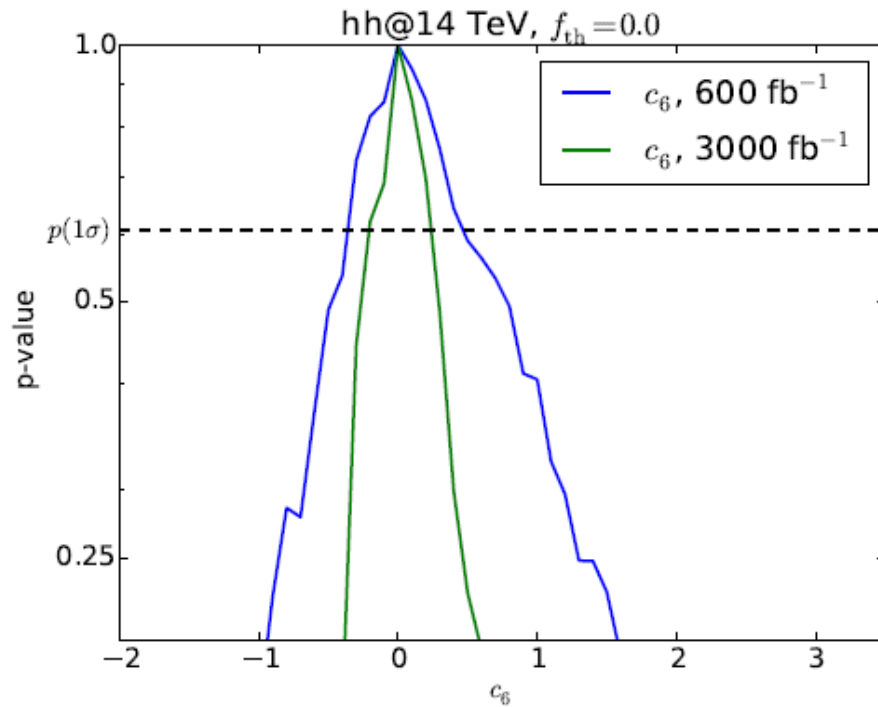
- Start with model where only $c_6 \neq 0$ (unconstrained from single h)
↳ Vary only λ as done in previous studies (\rightarrow BRs unchanged)

$$\delta N^2 = N + S^2 f_{\text{th}}^2$$

- Expected constraint on c_6 , assuming the SM to be true ($c_6=0$):

Compute how many standard deviations $\delta N(c_6)$ away a given $N(c_6)$, as predicted from theory, is from $N(c_6 = 0)$.

Full Analysis



$$c_6^{1\sigma}(600 \text{ fb}^{-1}) \in (-0.4, 0.5), \quad c_6^{1\sigma}(3000 \text{ fb}^{-1}) \in (-0.3, 0.3), \quad f_{th}=0$$

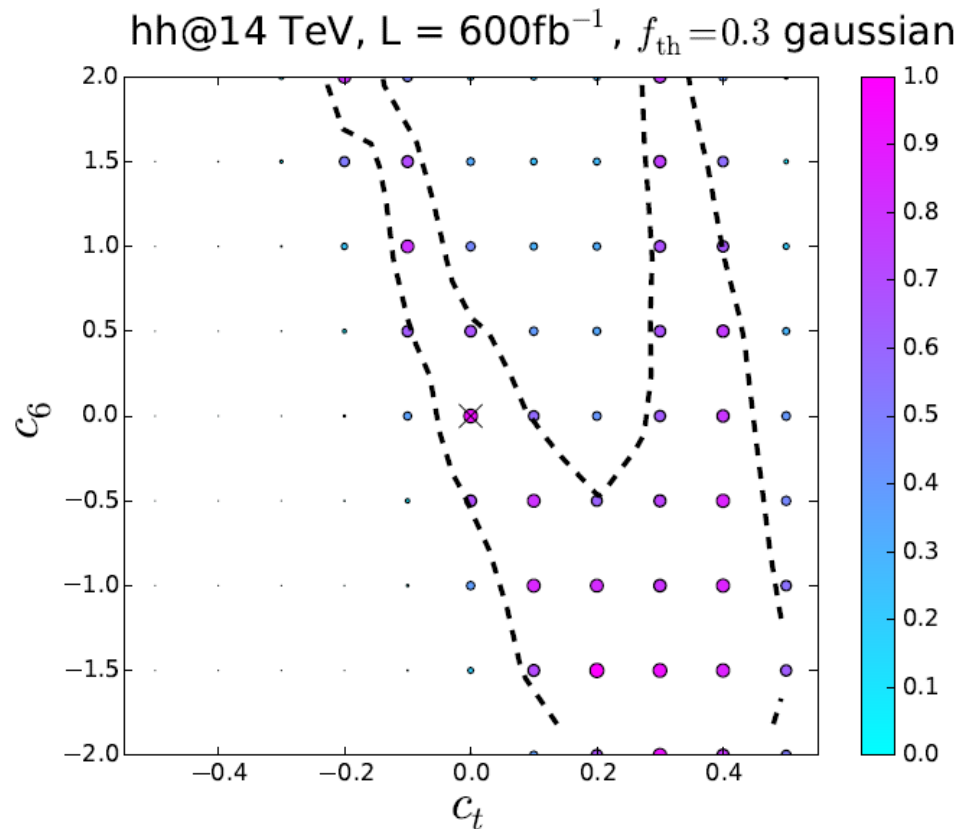
$$c_6^{1\sigma}(600 \text{ fb}^{-1}) \in (-0.5, 0.8), \quad c_6^{1\sigma}(3000 \text{ fb}^{-1}) \in (-0.4, 0.4), \quad f_{th}=0.3$$

$(c_6 > 0)$ —region more challenging as cross section reduced \rightarrow larger uncertainty

Full $D=6$ Theory

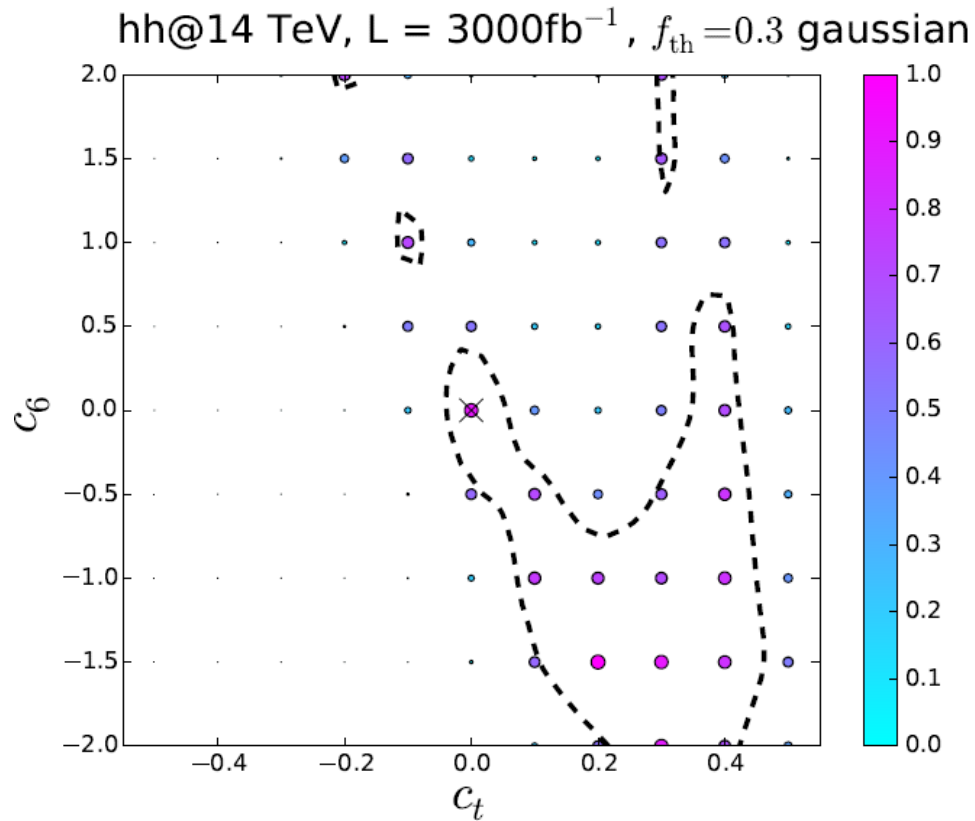
- Again assume SM ($c_i=0$) and calculate distance of predicted $N(c_6, \dots, c_b)$ from $N(c_6 = 0, \dots, c_b = 0)$ in units of $\delta N(c_6, \dots, c_b)$
- Show results in 2D grids (c_6, c_i), $i=H,g,\gamma,t,b$
- Marginalize over other directions with a Gaussian weight, given by projected errors on the coefficients from single h measurements ($\sim 10\%$ @ $(600-3000) \text{ fb}^{-1}$)
 - ➡ in the future use real constraints (like p -values from HiggsBounds/Signals)
- Draw iso-contours corresponding to probability-drop of 1σ

Results: $c_t - c_6$

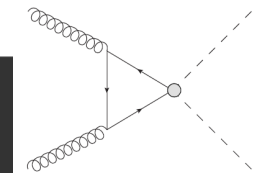
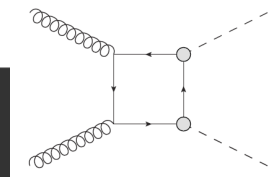
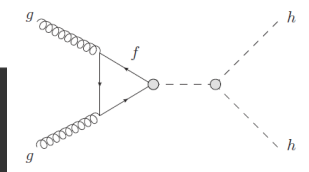


- *Clear correlation visible: Enhanced hh cross section due to negative c_t can be compensated by reduction due to positive c_6*

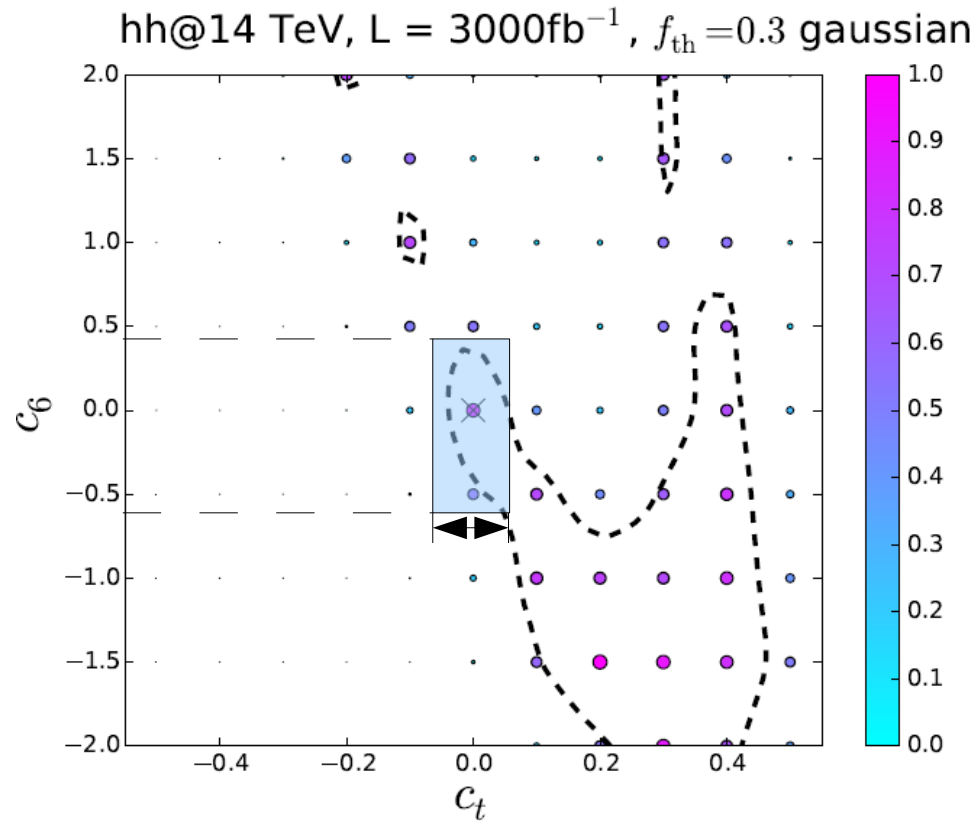
$c_t - c_6$



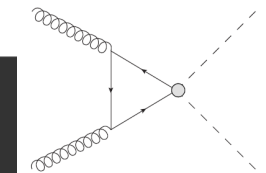
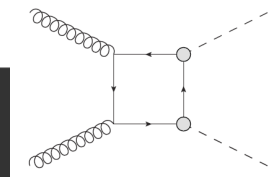
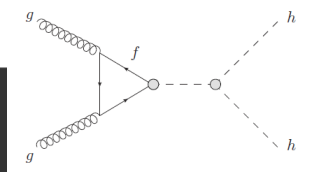
- Precise knowledge on 'top Yukawa' c_t helpful to improve the range for c_6
- On the other hand, could also obtain meaningful information on c_t in hh



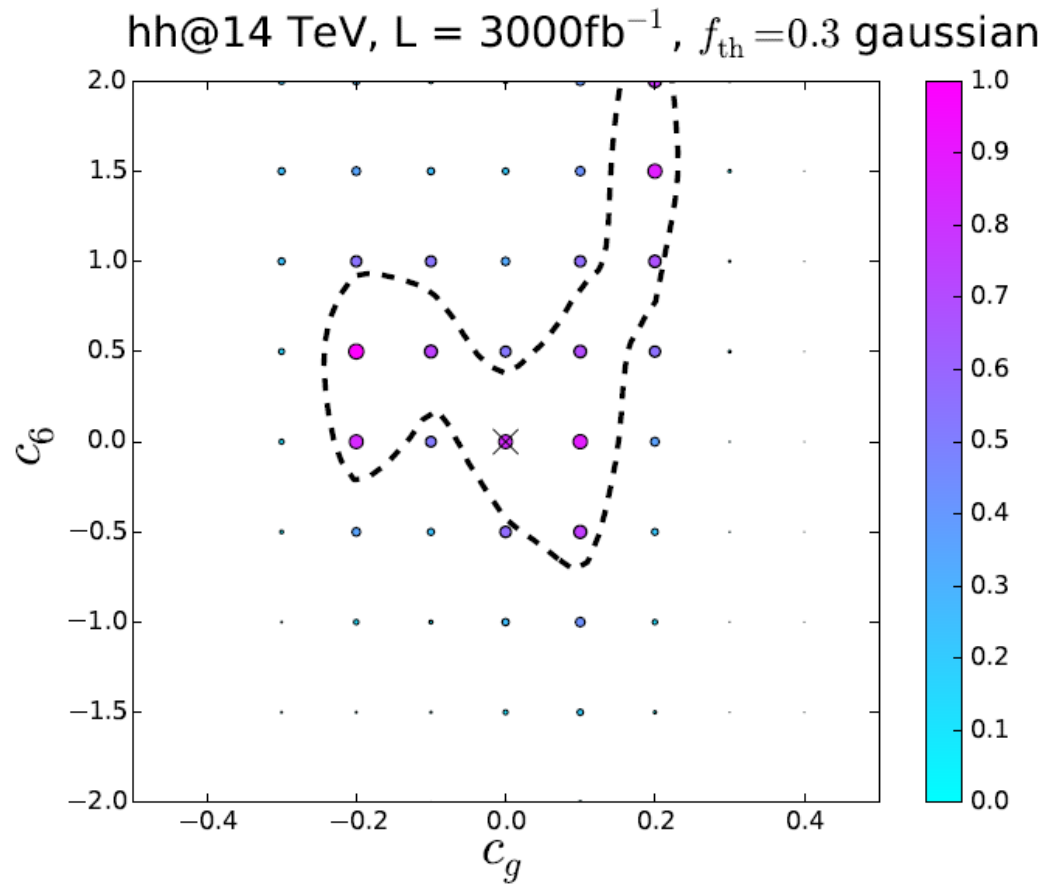
$c_t - c_6$



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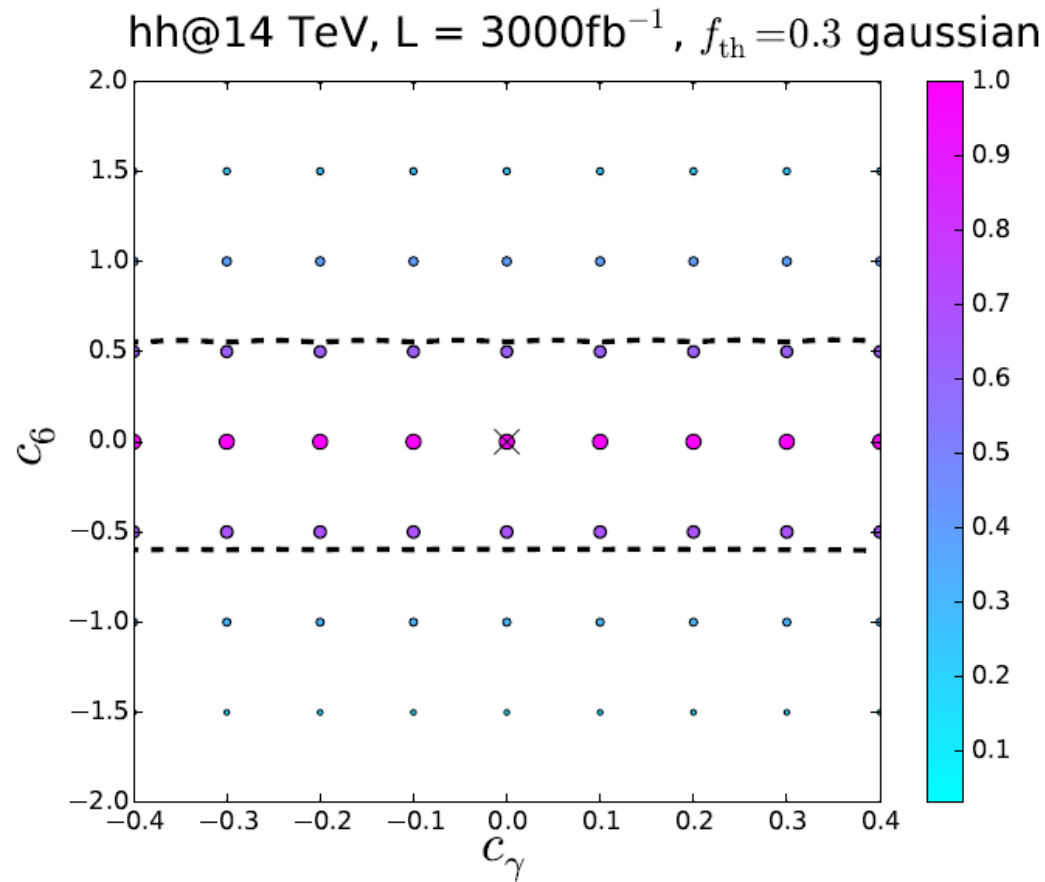


$$c_9 - c_6$$



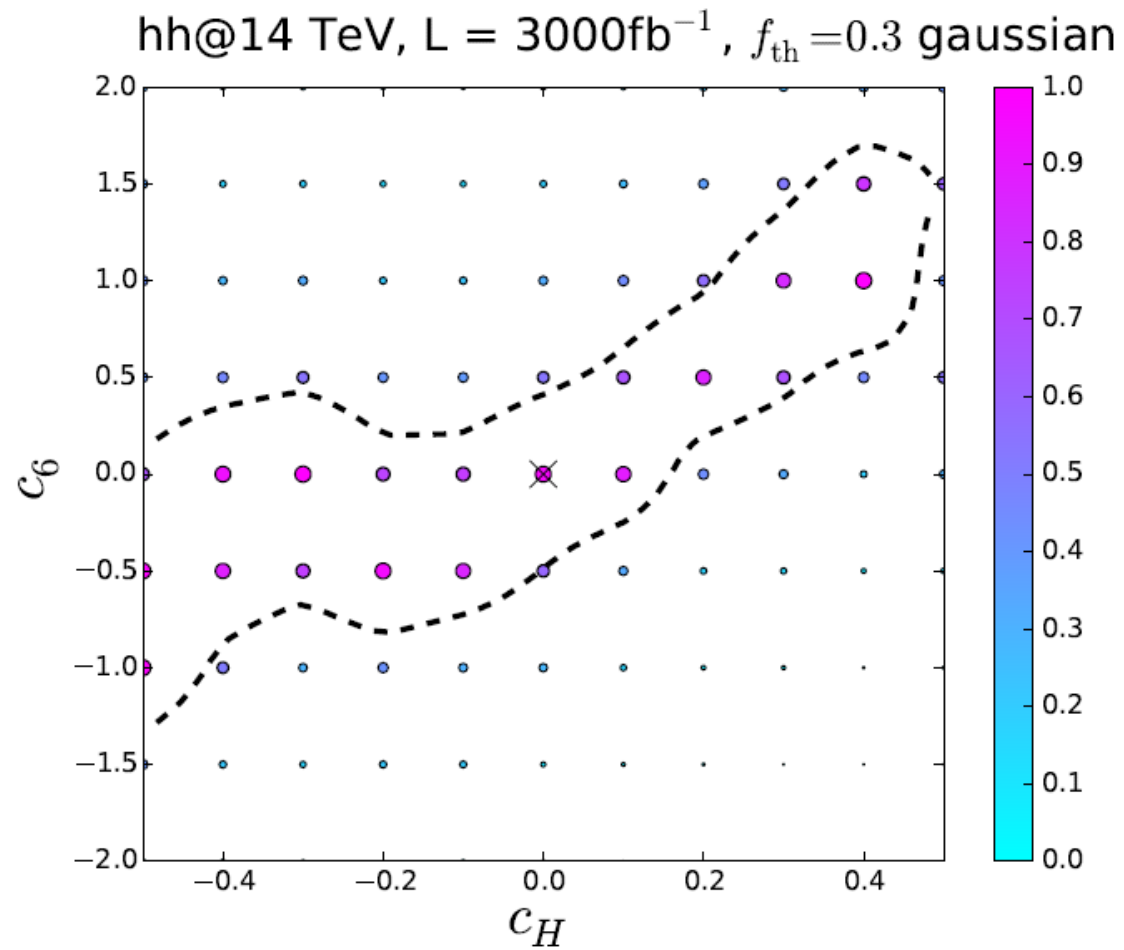
- Again compensation of effects from different operators possible
 \rightarrow range for c_6 depends significantly on other coefficients

$$c_\gamma - c_6$$

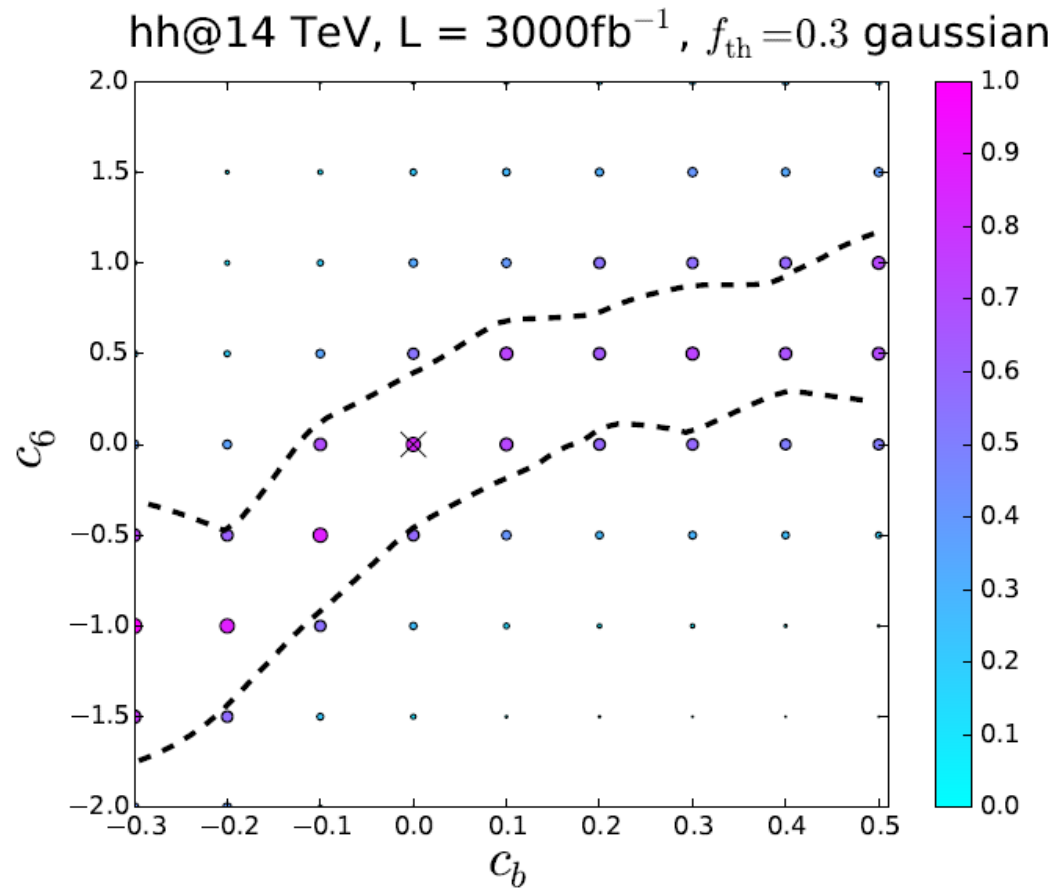


- As expected: negligible dependence on c_γ

$$c_H^{-1} c_6$$

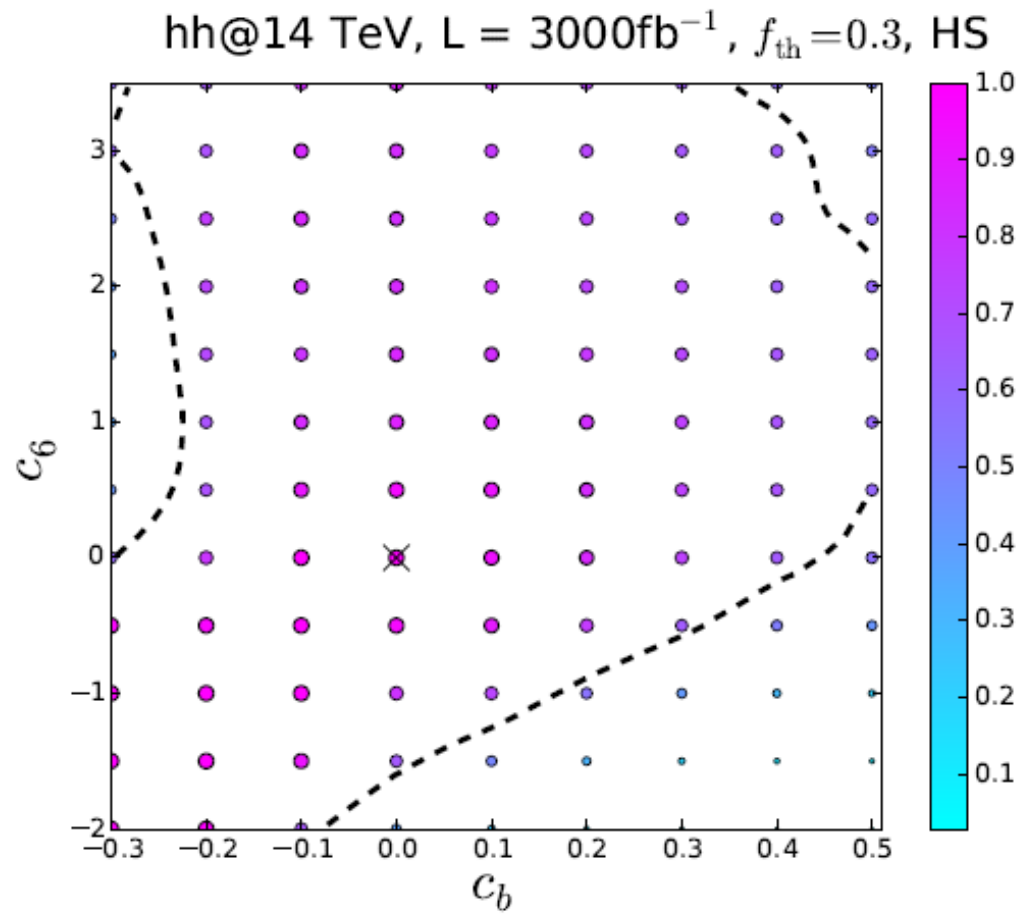


$$(c_b=c_\tau)-c_6$$



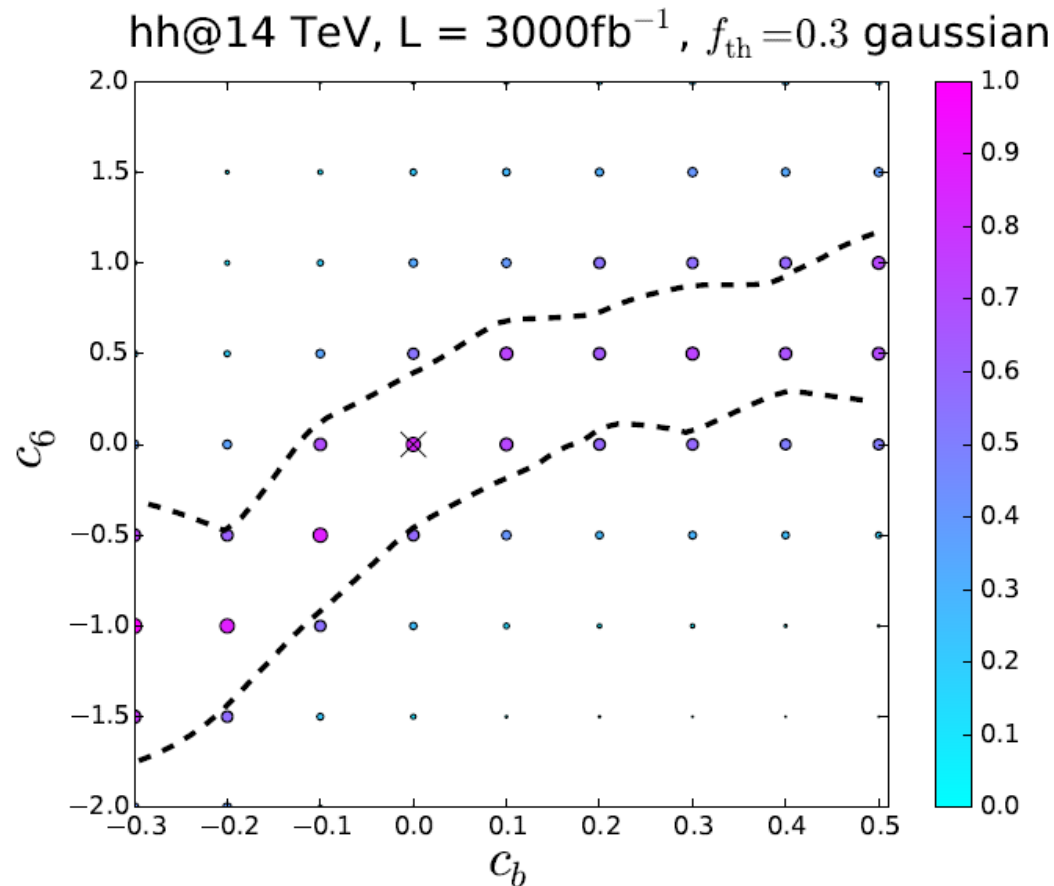
- Reduced BR due $(c_b=c_\tau)<0$ to can be compensated by enhanced production cross section due to negative c_6 and vice versa

$$(c_b = c_\tau) - c_6$$



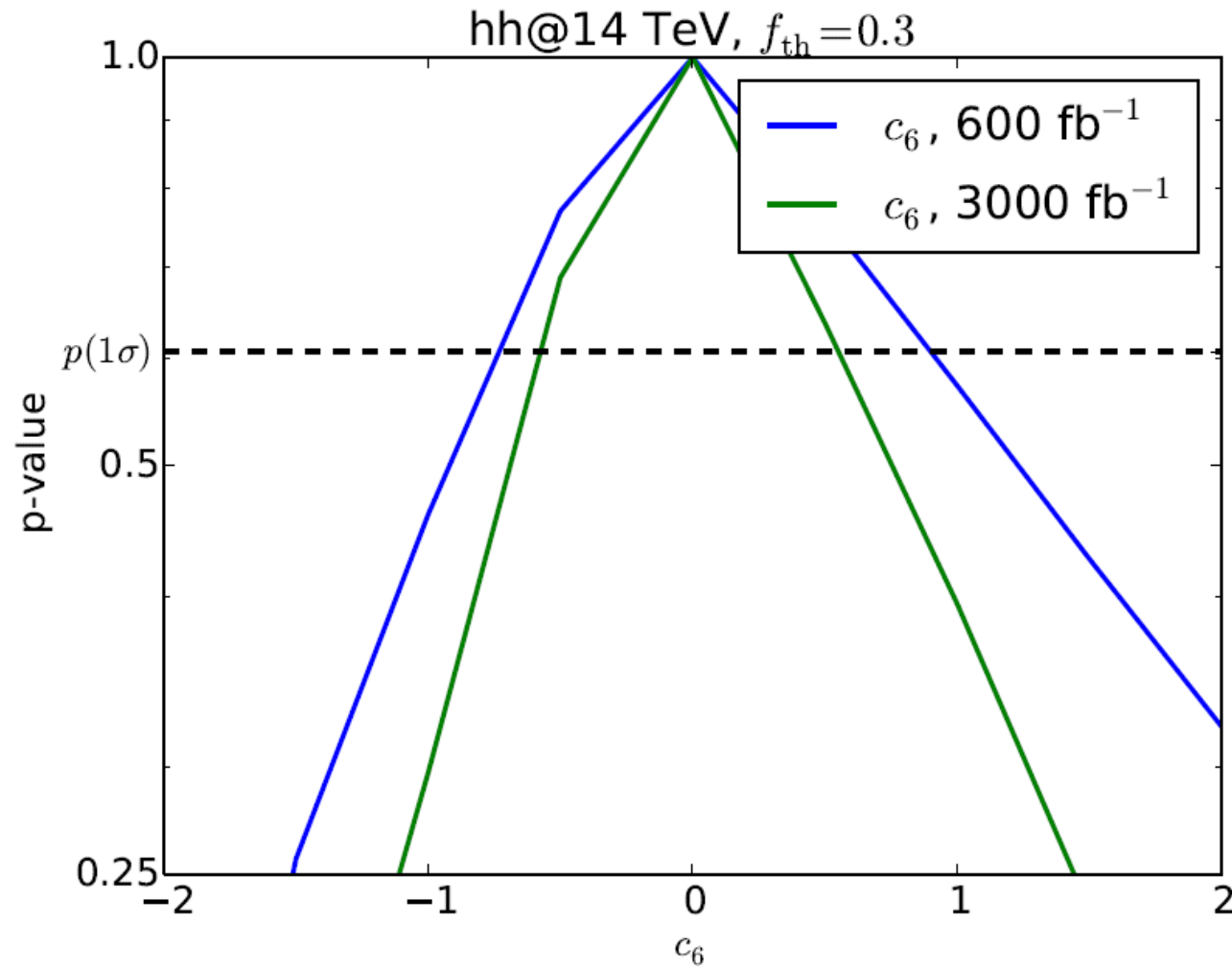
- Marginalize over other directions with **current** p -values for coefficients from single- h measurements (using HiggsBounds/Signals)

$$(c_b = c_\tau) - c_6$$



- Precise knowledge of other Wilson coefficients necessary for reasonable bounds on c_6

Full Marginalization $\rightarrow c_6$



Final Results

Expected 1σ constraints at the 14 TeV LHC, assuming $f_{th} = 30\%$

model	$L = 600 \text{ fb}^{-1}$	$L = 3000 \text{ fb}^{-1}$
c_6 -only	$c_6 \in (-0.5, 0.8)$	$c_6 \in (-0.4, 0.4)$
full (future)	$c_6 \in (-0.8, 0.9)$	$c_6 \in (-0.6, 0.6)$
$c_6 - c_t - c_\tau - c_b$ (future)	$c_6 \in (-0.8, 0.8)$	$c_6 \in (-0.6, 0.5)$

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$c_6 - c_t - c_\tau - c_b$ (future)	$c_6 \in (-0.8, 0.8)$	$c_6 \in (-0.6, 0.5)$

- Use real p -values from current single Higgs measurements in marginalization:

full	$c_6 \gtrsim -1.3$	$c_6 \gtrsim -1.2$
$c_6 - c_t - c_\tau - c_b$	$c_6 \gtrsim -2.0$	$c_6 \in (-1.8, 2.3)$

Conclusions and Outlook

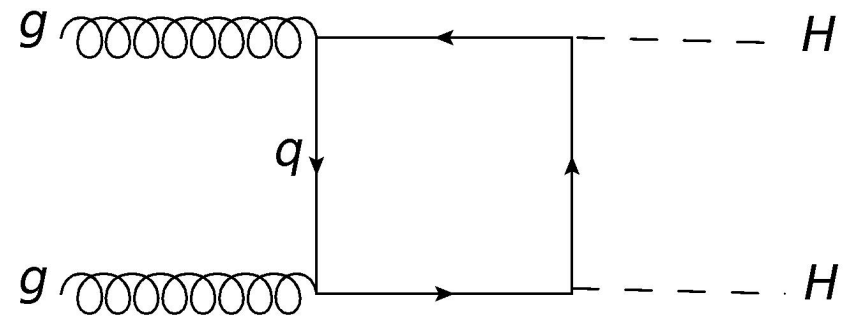
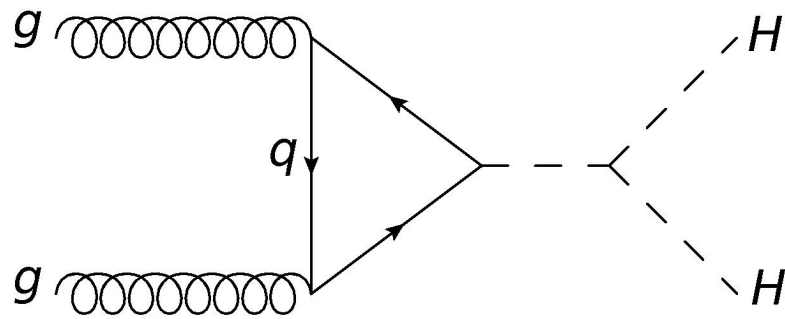
Analysis of hh productions can offer viable additional information on the $D=6$ extension of the SM

Some Current/Future Directions:

- Break degeneracy $c_b=c_\tau$ + consider different projections
- Optimize analysis for different regions of parameter space
- Include other decay channels
- Consider distributions to improve bounds

Backup: HH @ LHC

- Most important mechanism: $gg \rightarrow hh$



Eboli, Marques, Novaes, Natale, PLB 197(1987)269

Glover, van der Bij, NPB 309(1988)282

Dawson, Dittmaier, Spira, PRD 58(1998)115012

Grigo, Hoff, Melnikov, Steinhauser, 1305.7340

de Florian, Mazzitelli, 1305.5206, 1309.6594

see also Maltoni, Vryonidou, Zaro, 1408.6542

$$\sigma(gg \rightarrow hh)_{\text{LO}} \sim 17 \text{ fb}$$

$$\sigma(gg \rightarrow hh)_{\text{NLO}} \sim 33 \text{ fb}$$

$$\sigma(gg \rightarrow hh)_{\text{NNLO}} \sim 40 \text{ fb}$$

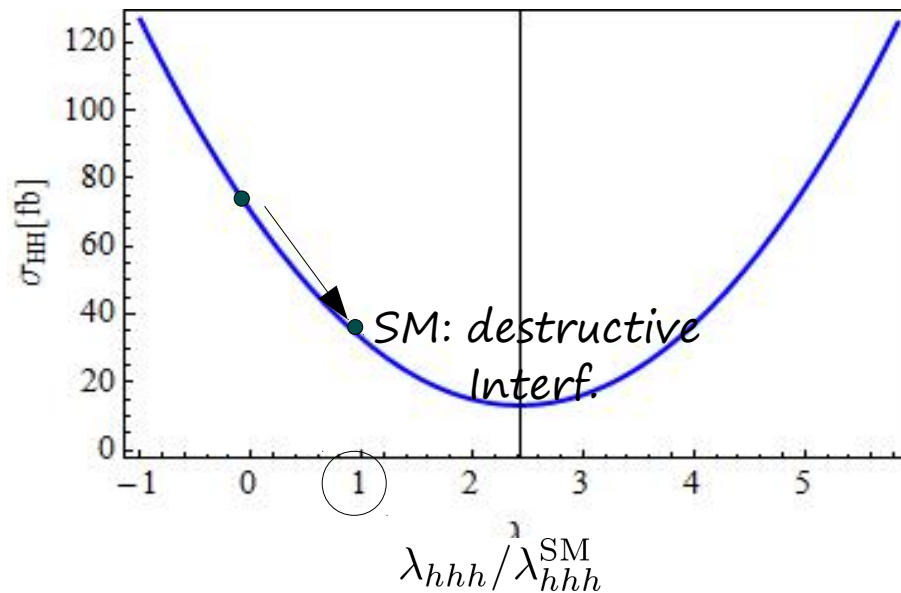
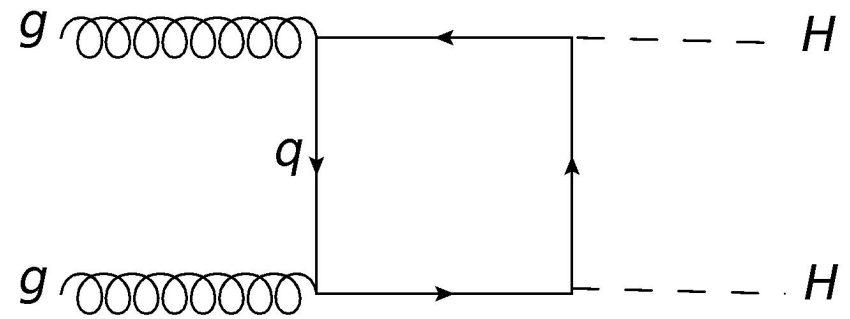
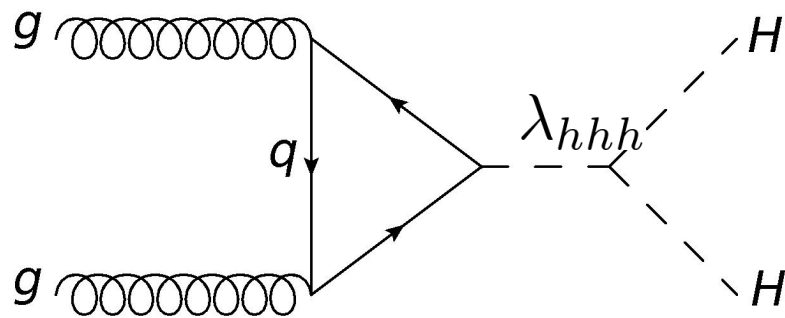
Theoretical error (NNLO): $f_{th} \sim 10\% (\text{scale}) + 10\% (\text{pdf} + \alpha_s) + 10\% (m_t^{-1})$

LHC@14TeV

$m_h \sim 125 \text{ GeV}$

Backup: HH @ LHC

- Most important mechanism: $gg \rightarrow hh$



Backup: Decay Channels

$$hh \rightarrow b\bar{b}\gamma\gamma$$

Baur, Plehn, Rainwater, hep-ph/0310056

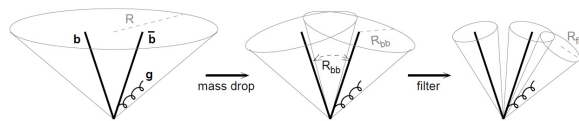
Significance @ 600 fb⁻¹

$$\lesssim 2\sigma \quad (S/B=6/12)$$

$$hh \rightarrow b\bar{b}\tau^+\tau^-$$

Dolan, Englert, Spannowsky, 1206.5001

$$\sim 4.5\sigma \quad (S/B=57/119)$$



Butterworth, Davison,
Rubin, Salam, 0802.2470

$$hh \rightarrow b\bar{b}W^+W^-$$

Papaefstathiou, Yang, Zurita, 1209.1489

$$\sim 3\sigma \quad (S/B=12/8)$$

Theorists' analyses!

Backup: Hbounds/Signals Ranges

coefficient	μ_f	σ_f
c_H	-0.035	0.225
c_t	-0.04	0.17
c_b	0.0	0.18
c_g	-0.01	0.06
c_γ	-0.25	0.62

assuming gaussian distributions

Backup: Parameter-Space Scan

- Show results in 2D grids (c_6, c_i) , $i=H,g,\gamma,t,b$
- Marginalize over other directions, varying the coefficients in the 95% CL allowed regions, obtained from HiggsBounds/Signals (with a Gaussian weight)

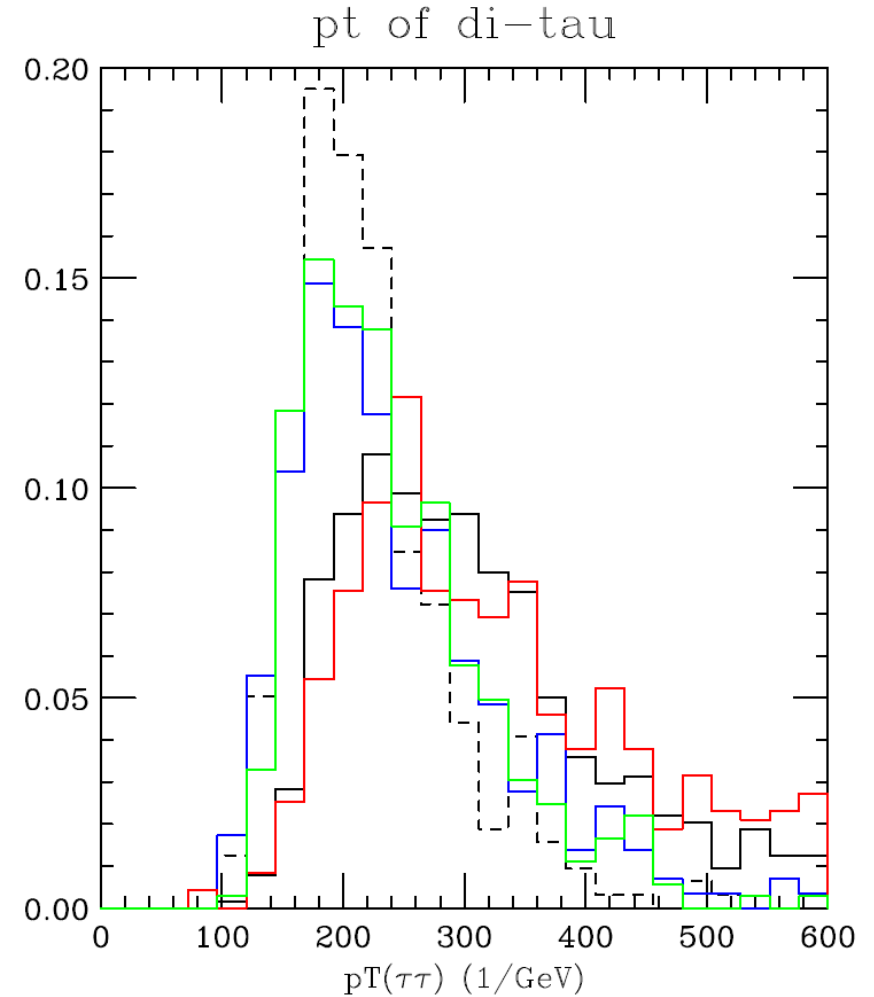
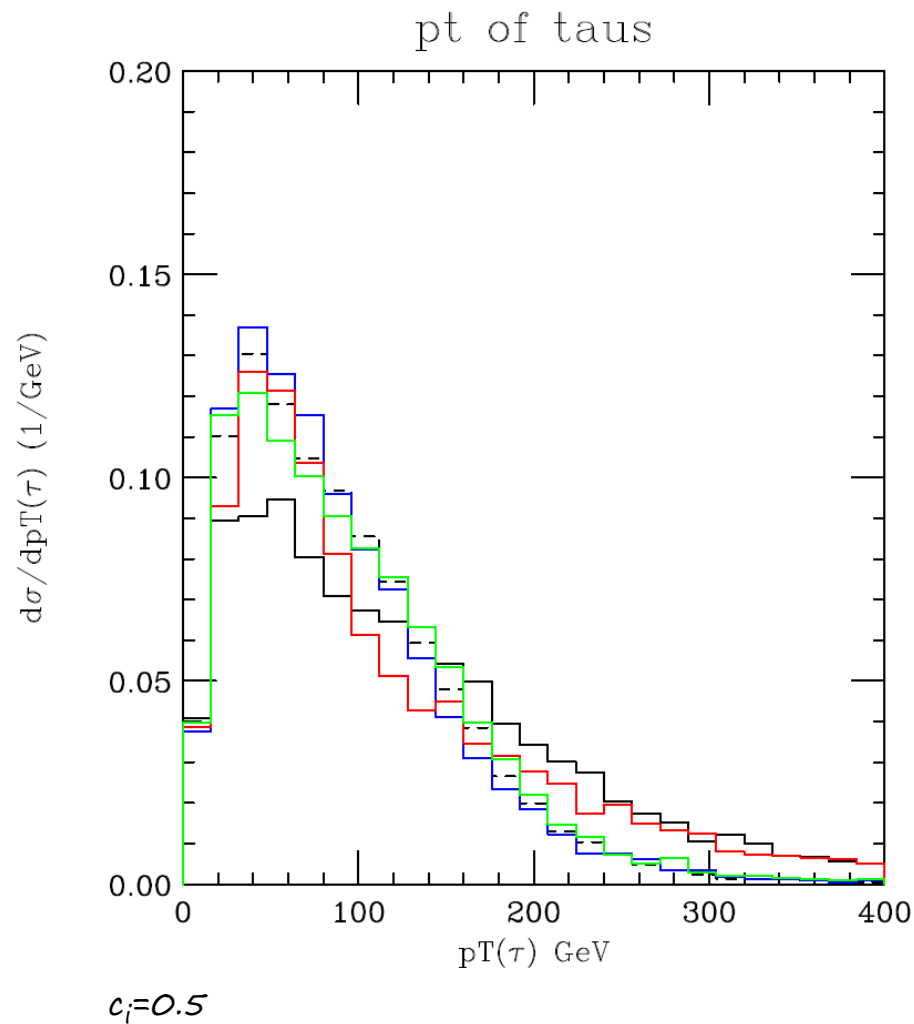
$$p(c_i, c_6) = \frac{\bar{p}(c_i, c_6)}{\max(\bar{p}(c_i, c_6))}, \quad \bar{p}(c_i, c_6) = \frac{\sum_{\{c_f\}} p(c_6, c_i, \{c_f\}) \times p_{\text{Gauss.}}(\{c_f\})}{\sum_{\{c_f\}} p_{\text{Gauss.}}(\{c_f\})}$$

$$p_{\text{Gauss.}}(\{c_f\}) = \prod_f \frac{1}{\sigma_f \sqrt{2\pi}} \exp \left\{ -\frac{(c_f - \mu_f)^2}{2\sigma_f^2} \right\}$$

Projections: $\mu_f = 0$, $\sigma_H = 0.1$, $\sigma_{b,\tau,t} = 0.05$, $\sigma_g = 0.017$, $\sigma_\gamma = 0.13$ ($\sim 10\%$ effects)

- Draw iso-contours corresponding to probability-drop of 1σ

Backup: Distributions



Backup: Distributions

