






# Beam instabilities (I)

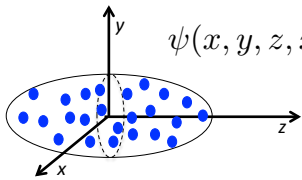
Giovanni Rumolo  
in CERN Accelerator School, Advanced Level, Warsaw  
Wednesday 30.09.2015



## What is a beam instability?

- What is a beam instability?
  - A beam becomes unstable when a moment of its distribution exhibits an exponential growth (e.g. mean positions  $\langle x \rangle$ ,  $\langle y \rangle$ ,  $\langle z \rangle$ , standard deviations  $\sigma_x$ ,  $\sigma_y$ ,  $\sigma_z$ , etc.) – resulting into beam loss or emittance growth!



$$\psi(x, y, z, x', y', \delta)$$

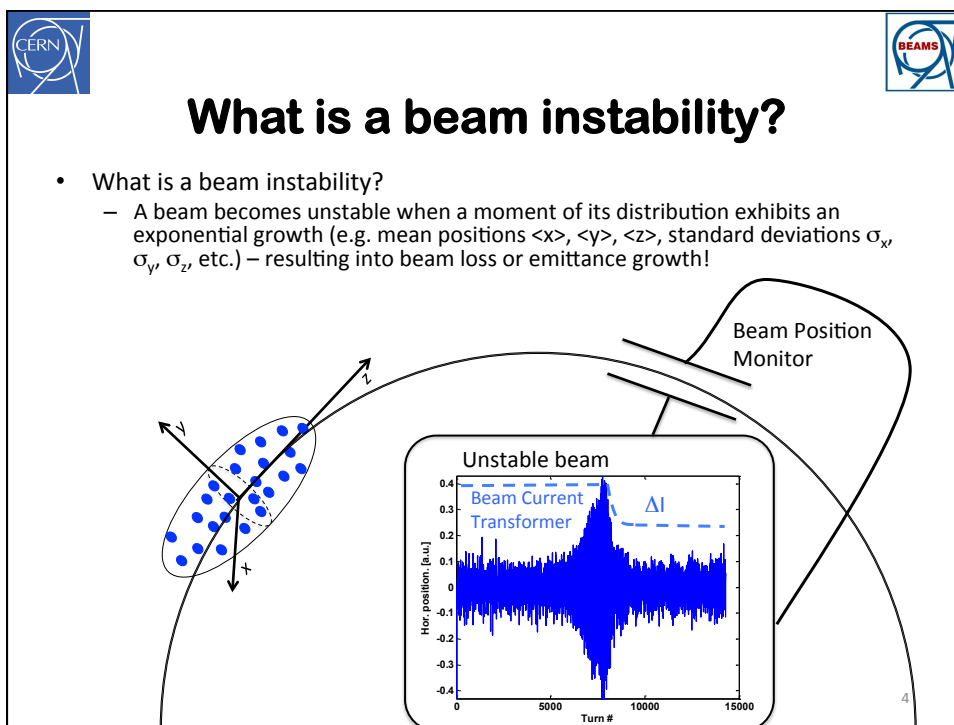
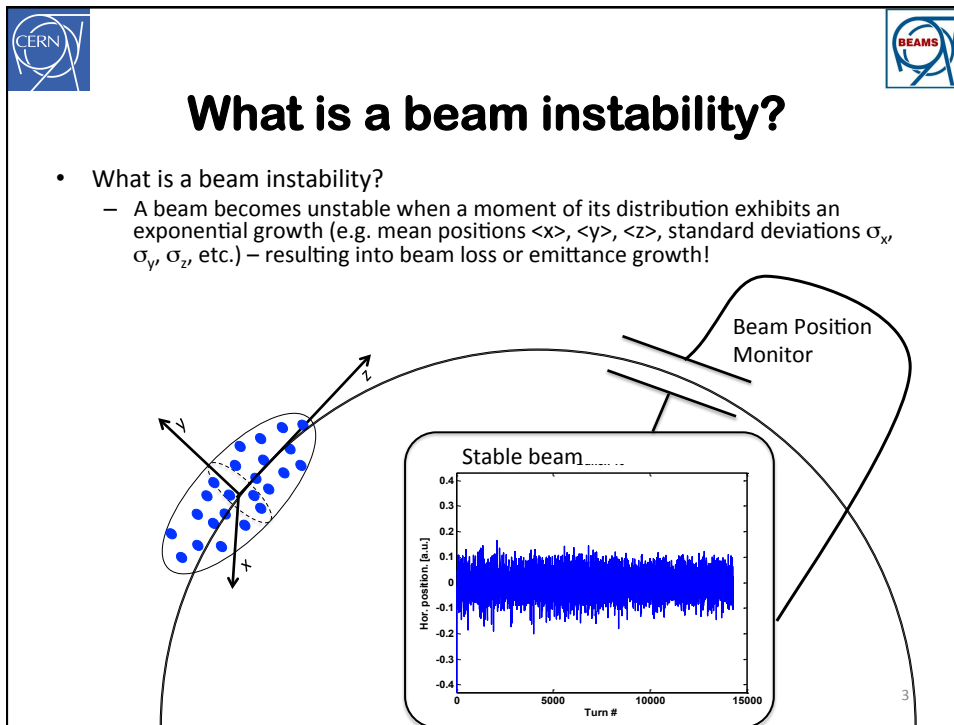
$$N = \int_{-\infty}^{\infty} \psi(x, y, z, x', y', \delta) dx dx' dy dy' dz d\delta$$

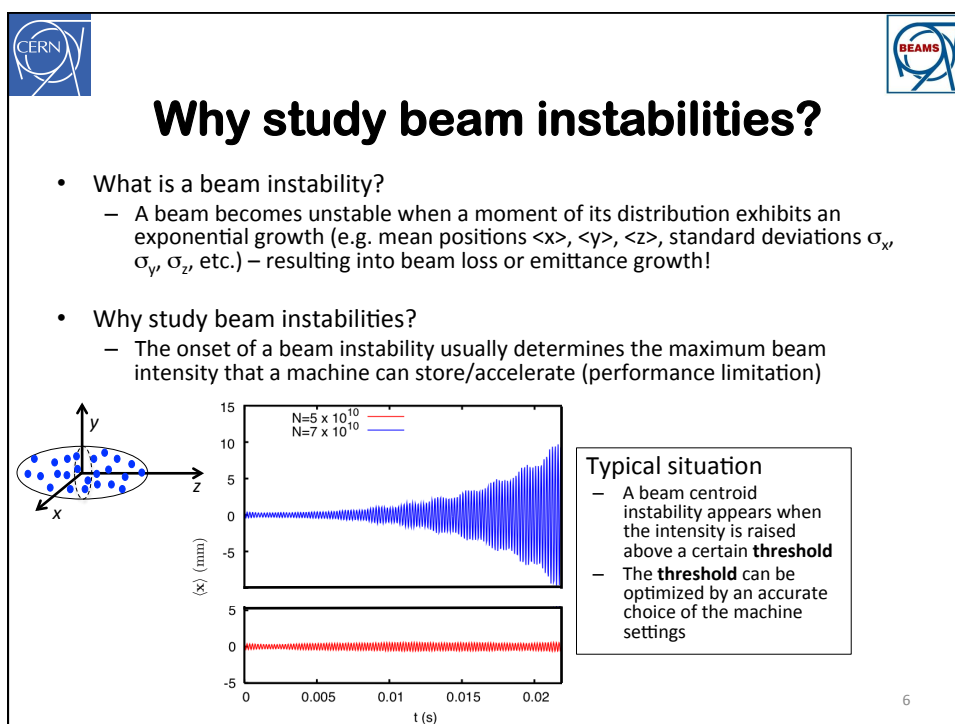
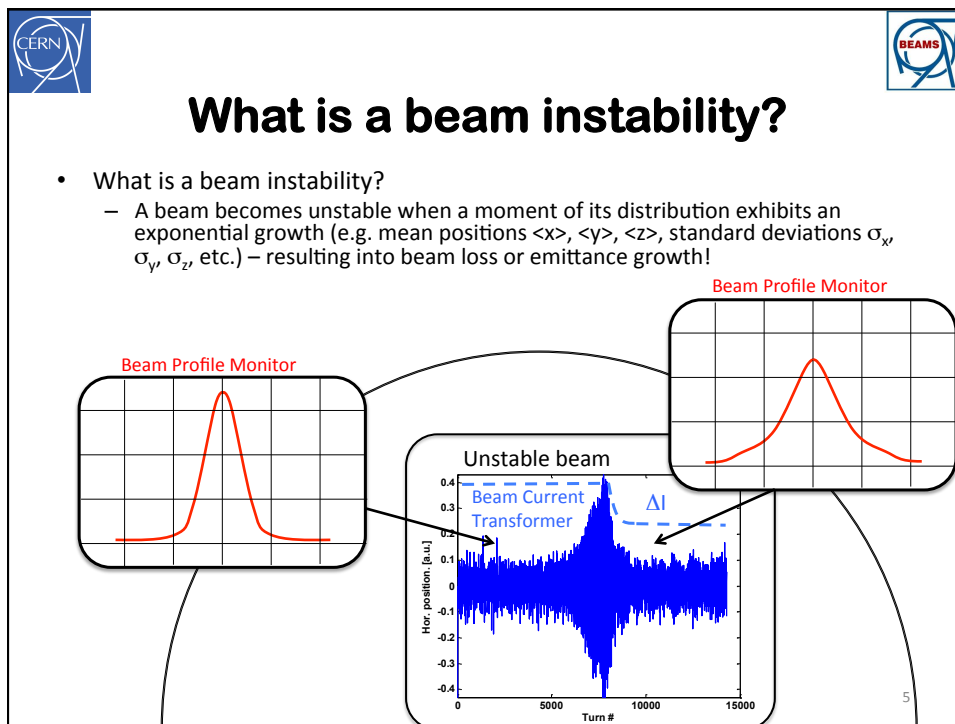
$$\langle x \rangle = \frac{1}{N} \int_{-\infty}^{\infty} x \psi(x, y, z, x', y', \delta) dx dx' dy dy' dz d\delta$$

$$\sigma_x^2 = \frac{1}{N} \int_{-\infty}^{\infty} (x - \langle x \rangle)^2 \psi(x, y, z, x', y', \delta) dx dx' dy dy' dz d\delta$$

And similar definitions for  $\langle y \rangle$ ,  $\sigma_y$ ,  $\langle z \rangle$ ,  $\sigma_z$

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## Why study beam instabilities?

- What is a beam instability?
  - A beam becomes unstable when a moment of its distribution exhibits an exponential growth (e.g. mean positions  $\langle x \rangle$ ,  $\langle y \rangle$ ,  $\langle z \rangle$ , standard deviations  $\sigma_x$ ,  $\sigma_y$ ,  $\sigma_z$ , etc.) – resulting into beam loss or emittance growth!
- Why study beam instabilities?
  - The onset of a beam instability usually determines the maximum beam intensity that a machine can store/accelerate (performance limitation)
  - Understanding the type of instability limiting the performance, and its underlying mechanism, is essential because it:
    - Allows identifying the source and possible measures to mitigate/suppress the effect
    - Allows dimensioning an active feedback system to prevent the instability

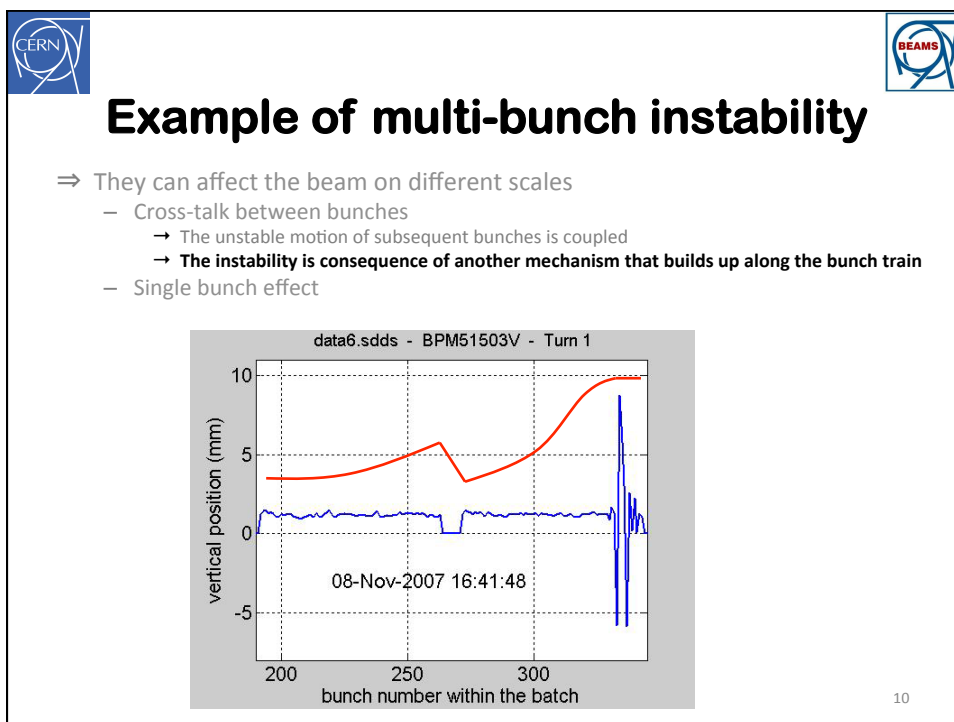
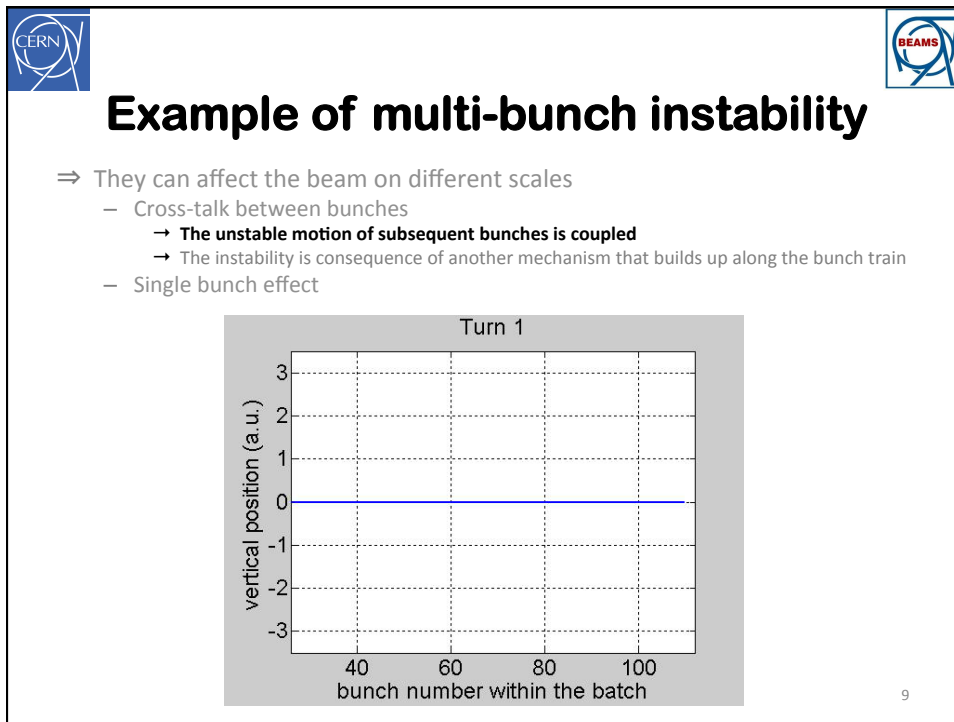
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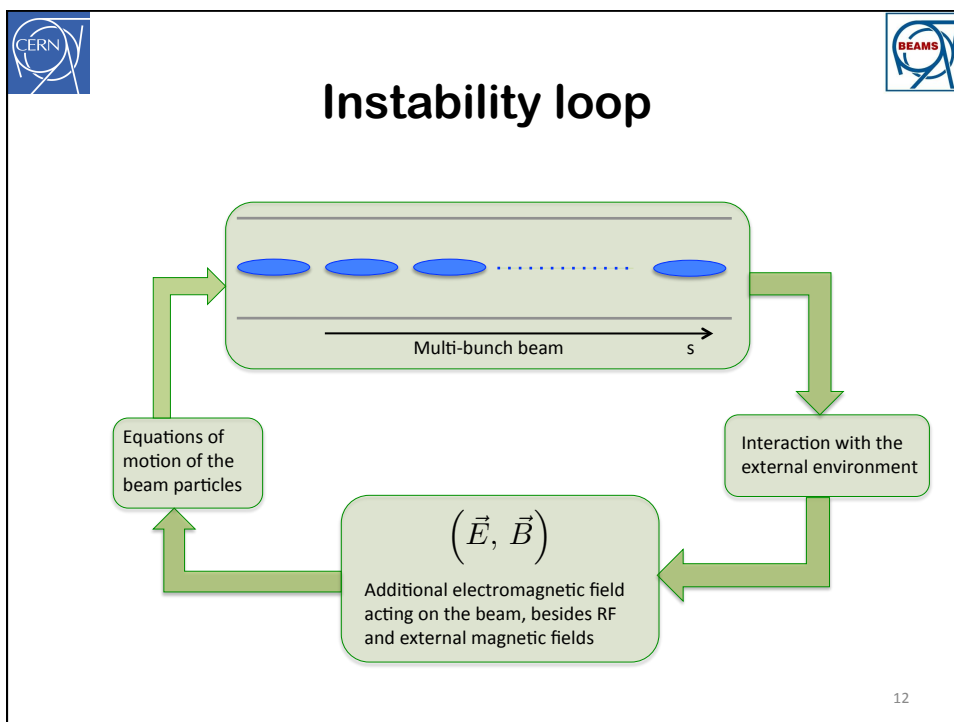
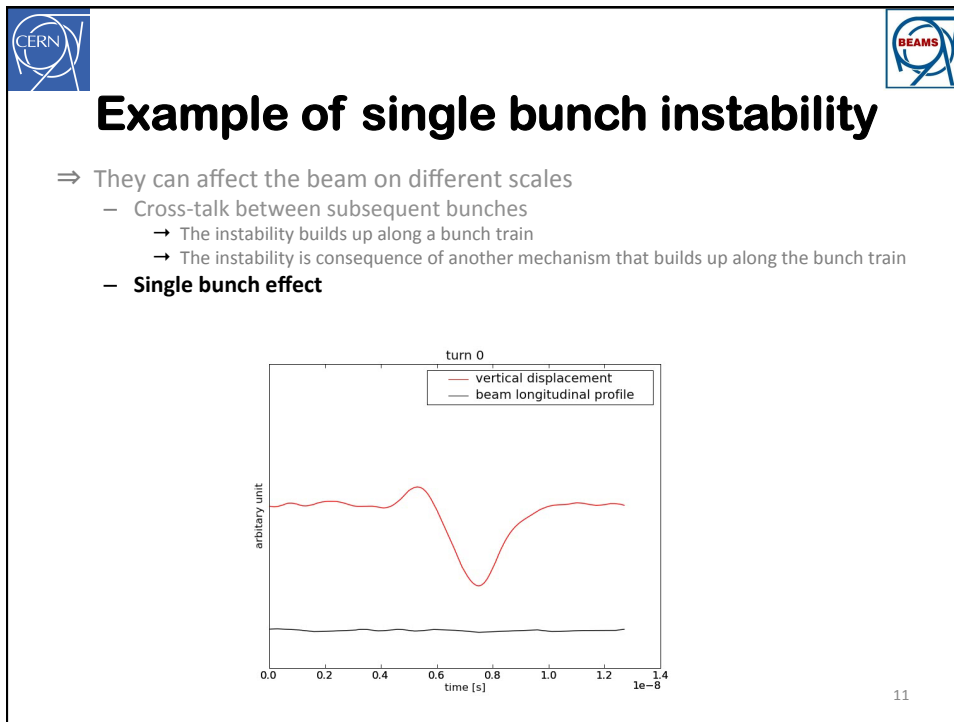


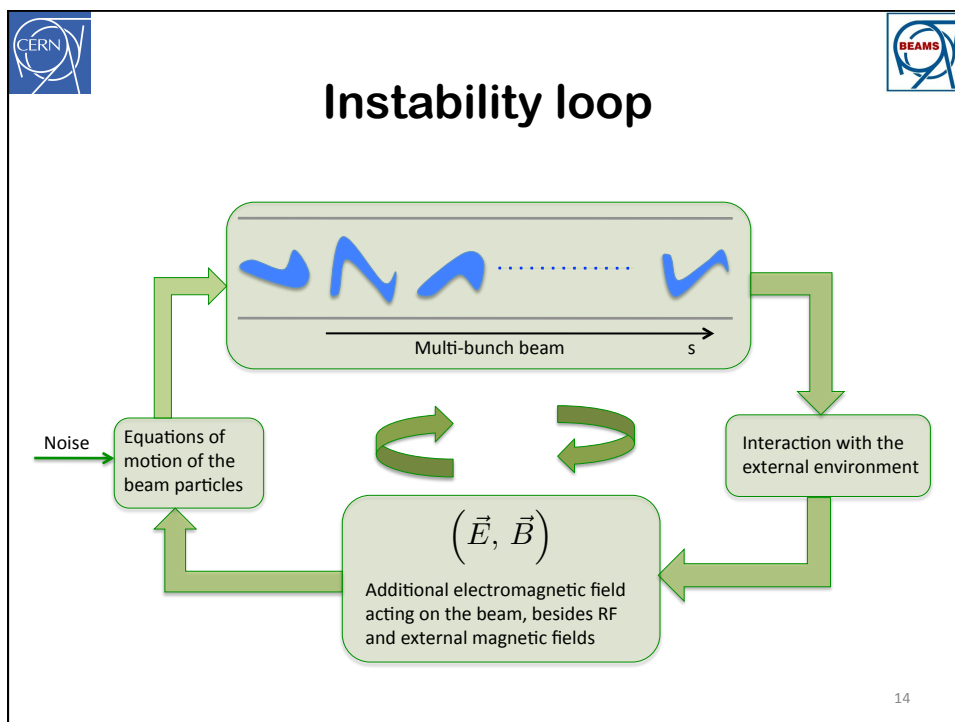
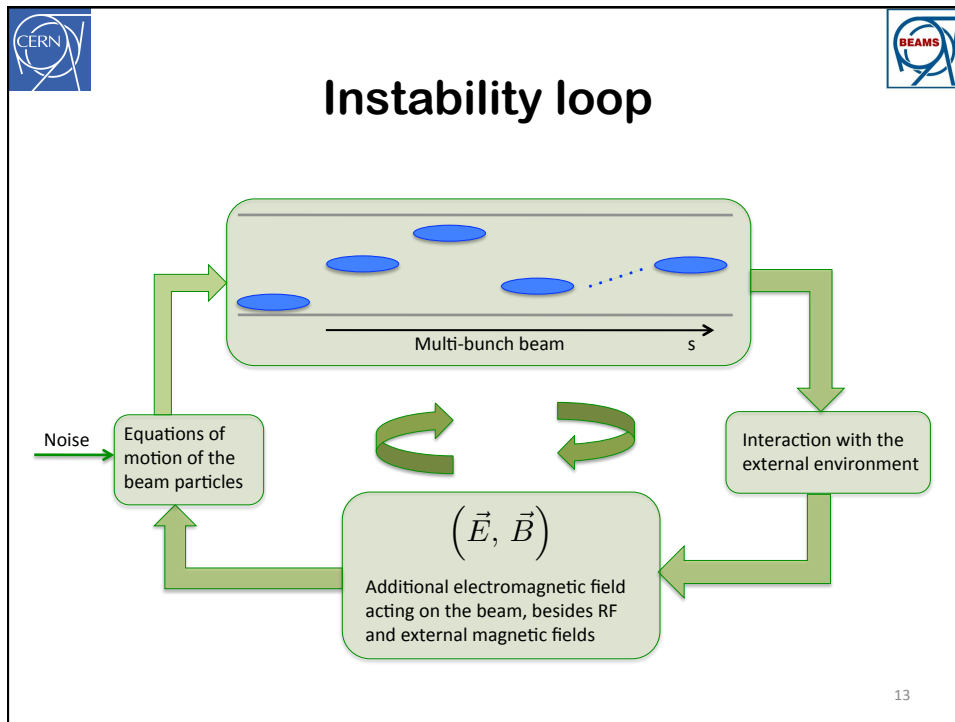
## Types of beam instabilities

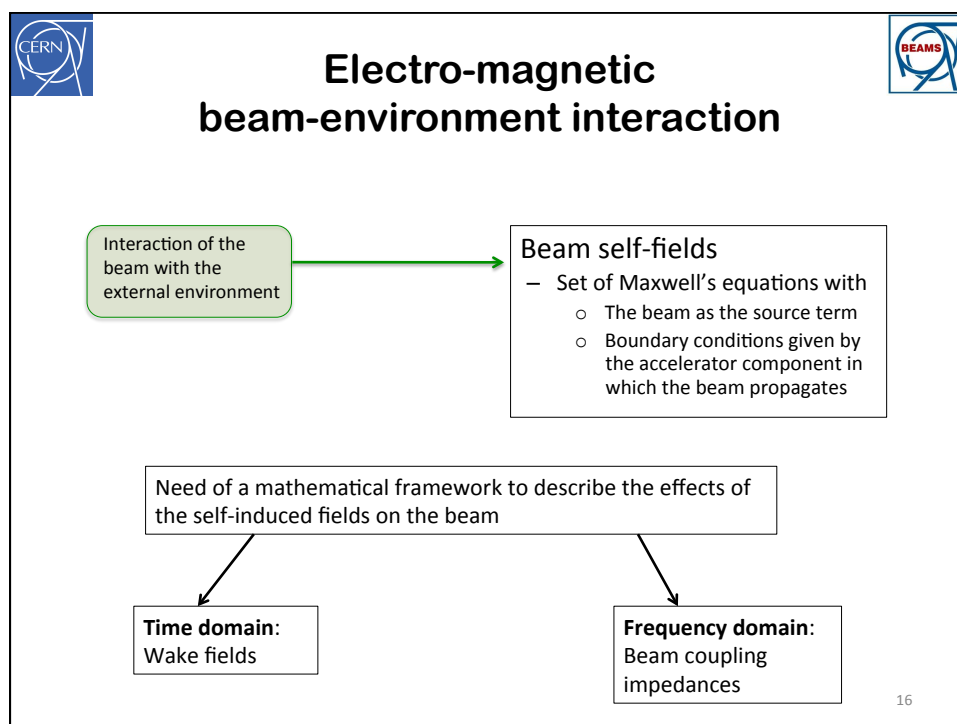
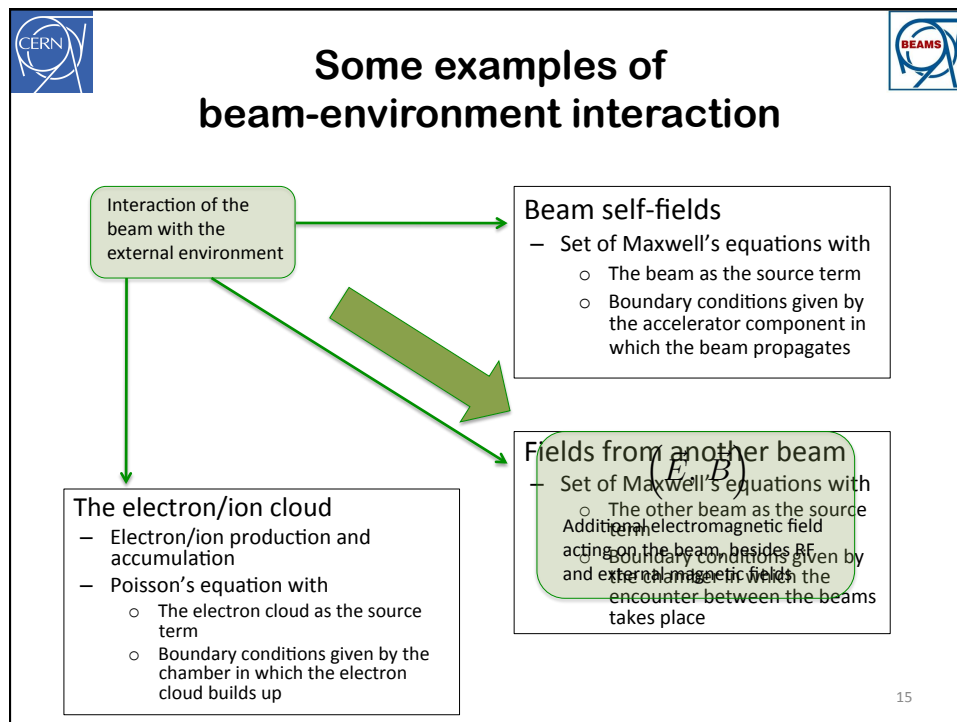
- ⇒ Beam instabilities occur in both linear and circular machines
  - Longitudinal plane ( $z, \delta$ )
  - Transverse plane ( $x, y, x', y'$ )
- ⇒ Beam instabilities can affect the beam on different scales
  - Cross-talk between bunches
    - The unstable motion of subsequent bunches is coupled
    - The instability is consequence of another mechanism that builds up along the bunch train
  - Single bunch effect
  - Coasting beam instabilities

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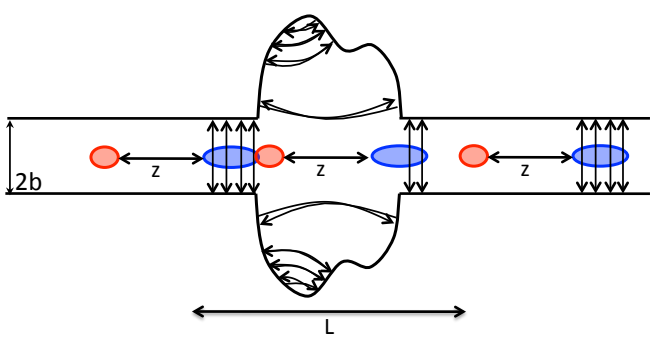








## Wake fields (general)





 Source,  $q_1$

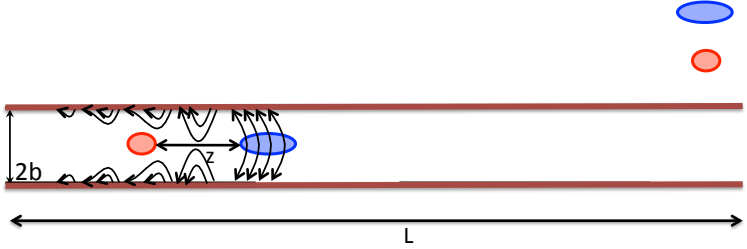
 Witness,  $q_2$


- While **source** and **witness** ( $q_i \delta(s-ct)$ ), distant by  $z < 0$ , move in a perfectly conducting chamber, the witness does not feel any force ( $\gamma \gg 1$ )
- When the **source** encounters a discontinuity (e.g., transition, device), it produces an electromagnetic field, which trails behind (wake field)
  - The **source** loses energy
  - The **witness** feels a net force all along an effective length of the structure,  $L$


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## Wake fields (general)

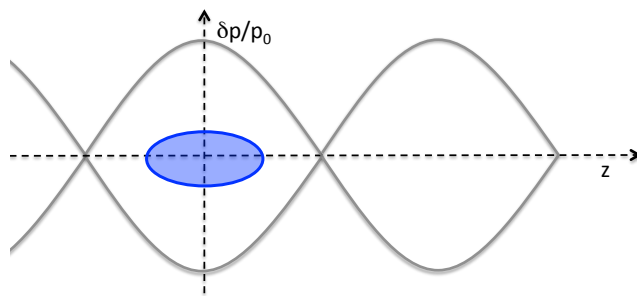


 Source,  $q_1$


 Witness,  $q_2$

- Not only geometric discontinuities cause electromagnetic fields trailing behind **sources** traveling at light speed.
- For example, a pipe with finite conductivity causes a delay in the induced currents, which also produces delayed electromagnetic fields
  - No ringing, only slow decay
  - The **witness** feels a net force all along an effective length of the structure,  $L$
- In general, also electromagnetic boundary conditions other than PEC can be the origin of wake fields.


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# 1. The longitudinal plane



## Longitudinal wake function: definition





$$\int_0^L F_{\parallel}(s, z) ds = -q_1 q_2 W_{\parallel}(z)$$

$$F_{\parallel}(s, z) = q_2 E_z(s, z)$$

$$\Delta E_2 \Rightarrow \frac{\Delta E_2}{E_0} = \left( \frac{\gamma^2 - 1}{\gamma^2} \right) \frac{\Delta p_2}{p_0}$$

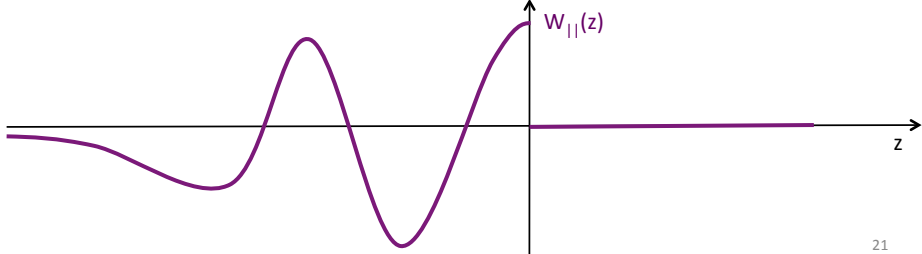
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## Longitudinal wake function: properties

$$W_{\parallel}(z) = -\frac{\Delta E_2}{q_1 q_2} \quad \begin{matrix} z \rightarrow 0 \\ q_2 \rightarrow q_1 \end{matrix} \quad W_{\parallel}(0) = -\frac{\Delta E_1}{q_1^2}$$

- The value of the wake function in 0,  $W_{\parallel}(0)$ , is related to the **energy lost** by the source particle in the creation of the wake
- $W_{\parallel}(0) > 0$  since  $\Delta E_1 < 0$
- $W_{\parallel}(z)$  is discontinuous in  $z=0$  and it vanishes for all  $z > 0$  because of the ultra-relativistic approximation



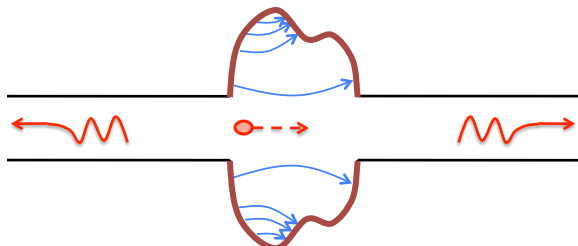
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## The energy balance

$$W_{\parallel}(0) = -\frac{\Delta E_1}{q_1^2} \quad \text{What happens to the energy lost by the source?}$$

- In the global energy balance, the energy lost by the source splits into
  - Electromagnetic energy of the **modes that remain trapped** in the object
    - ⇒ Partly dissipated on **lossy walls** or into purposely designed inserts or **HOM absorbers**
    - ⇒ Partly transferred to **following particles** (or the same particle over successive turns), possibly feeding into an instability!
  - Electromagnetic energy of **modes that propagate** down the beam chamber (above cut-off), which will be eventually lost on surrounding lossy materials



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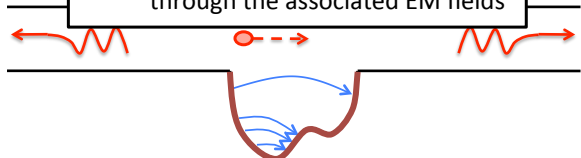
## The energy balance

$$W_{\parallel}(0) = -\frac{\Delta E_1}{q_1^2}$$



What happens to the energy lost by the source?

- In the global energy balance, the energy lost by the source splits into
  - Electromagnetic energy of the **modes that remain trapped** in the object
    - ⇒ Partly dissipated on **lossy walls** or into purposely designed inserts or **HOM absorbers**
    - ⇒ Partly stored in the object
  - Electromagnetic energy (above c)
    - ⇒ It causes **beam induced heating** of the beam environment (damage, outgassing)
    - ⇒ It feeds into both **longitudinal and transverse instabilities** through the associated EM fields

particle over  
beam chamber  
lossy materials



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## Longitudinal impedance

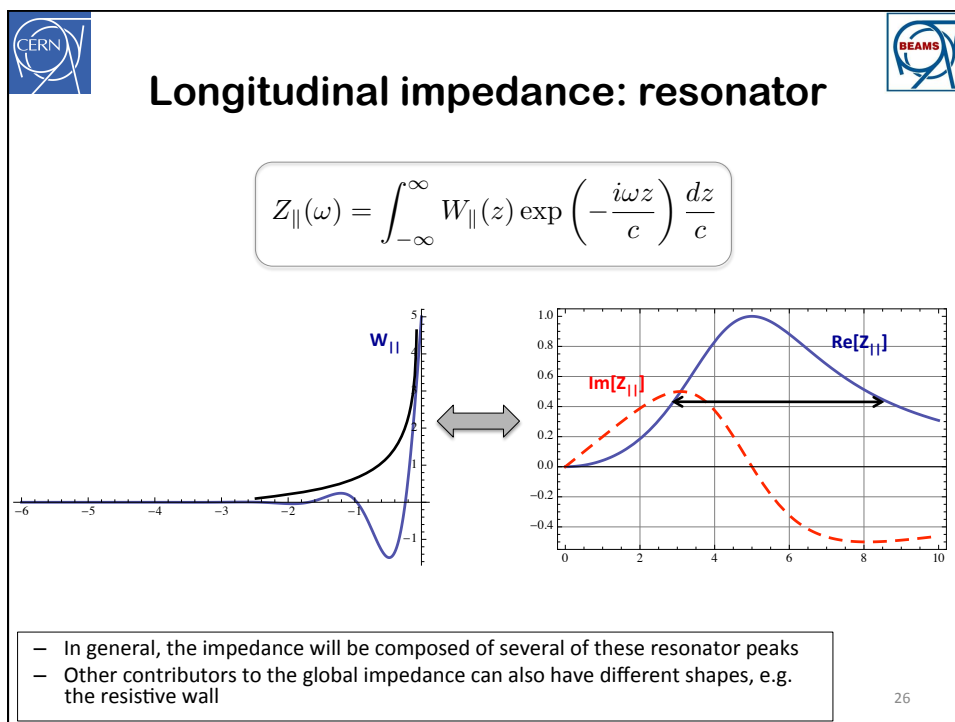
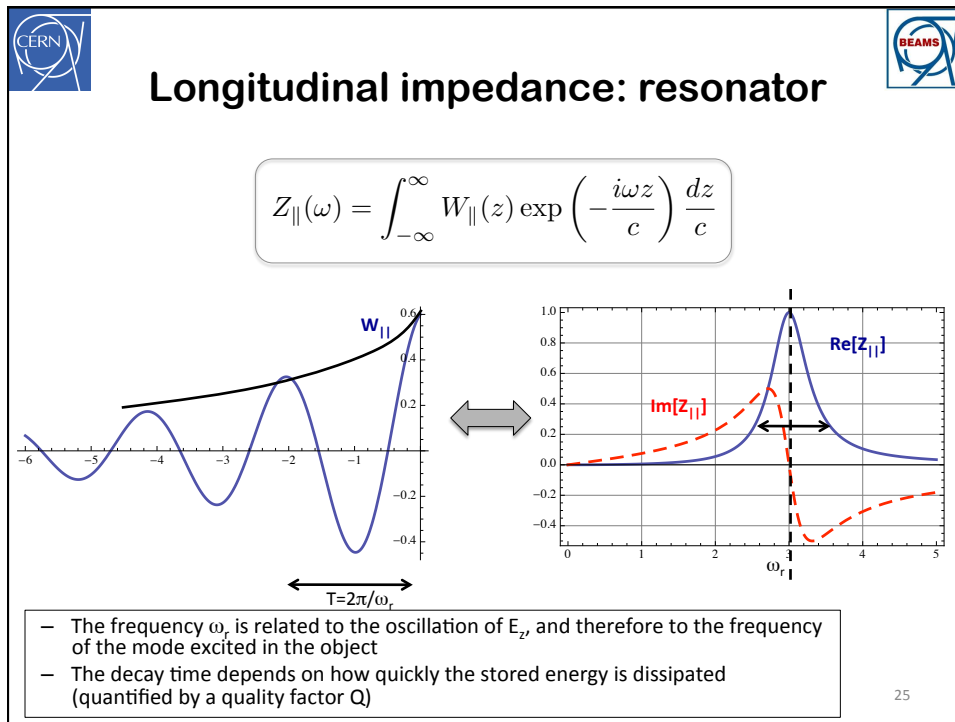
- The wake function of an accelerator component is basically its Green function in time domain (i.e., its response to a pulse excitation)
  - ⇒ Very useful for macroparticle models and simulations, because it can be used to describe the driving terms in the single particle equations of motion!
- We can also describe it as a transfer function in frequency domain
- This is the definition of **longitudinal beam coupling impedance** of the element under study

$$Z_{\parallel}(\omega) = \int_{-\infty}^{\infty} W_{\parallel}(z) \exp\left(-\frac{i\omega z}{c}\right) \frac{dz}{c}$$

$Z_{\parallel}(\omega)$   
↓  
[Ω]

$W_{\parallel}(z)$   
↓  
[Ω/s]

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## Longitudinal wake & impedance Equations of the resonator



$$Z_{||}^{\text{Res}}(\omega) = \frac{R_{s||}}{1 + iQ \left( \frac{\omega}{\omega_r} - \frac{\omega_r}{\omega} \right)}$$

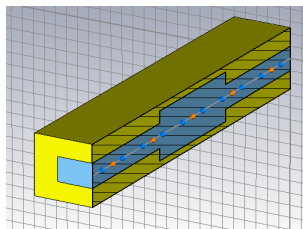
$$W_{||}^{\text{Res}}(z) = \begin{cases} 2\alpha_z R_{s||} \exp\left(\frac{\alpha_z z}{c}\right) \left[ \cos\left(\frac{\bar{\omega} z}{c}\right) + \frac{\alpha_z}{\bar{\omega}} \sin\left(\frac{\bar{\omega} z}{c}\right) \right] & \text{if } z < 0 \\ \alpha_z R_{s||} & \text{if } z = 0 \\ 0 & \text{if } z > 0 \end{cases}$$

$$\alpha_z = \frac{\omega_r}{2Q} \quad \bar{\omega} = \sqrt{\omega_r^2 - \alpha_z^2}$$

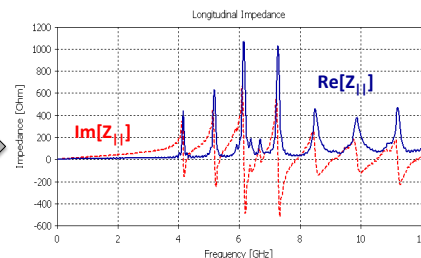
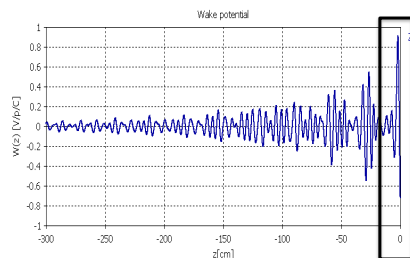
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## Longitudinal impedance: cavity

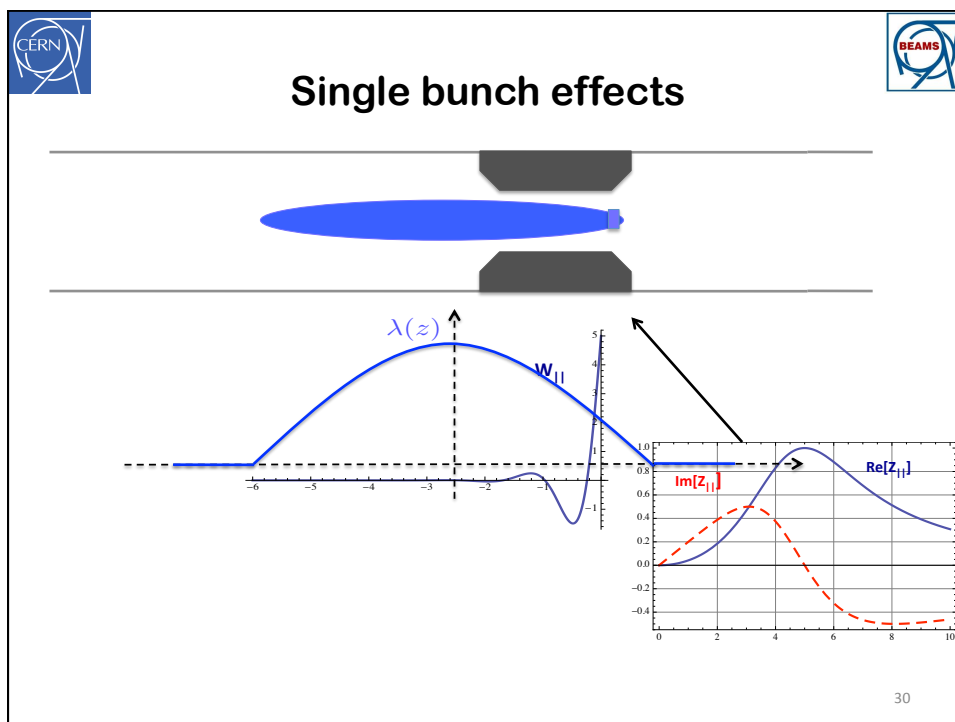
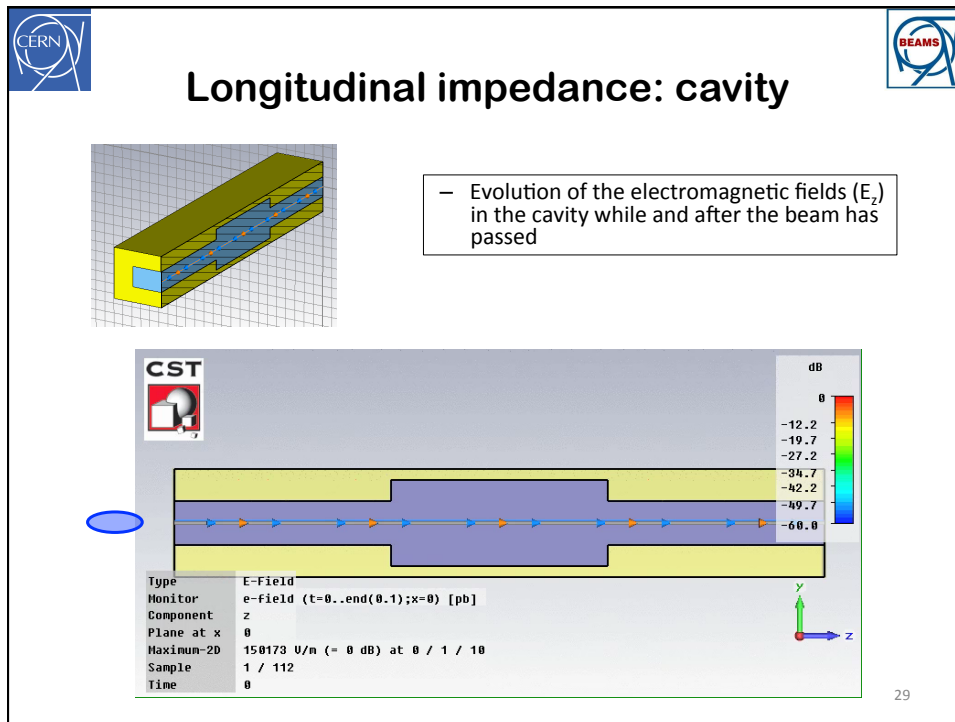


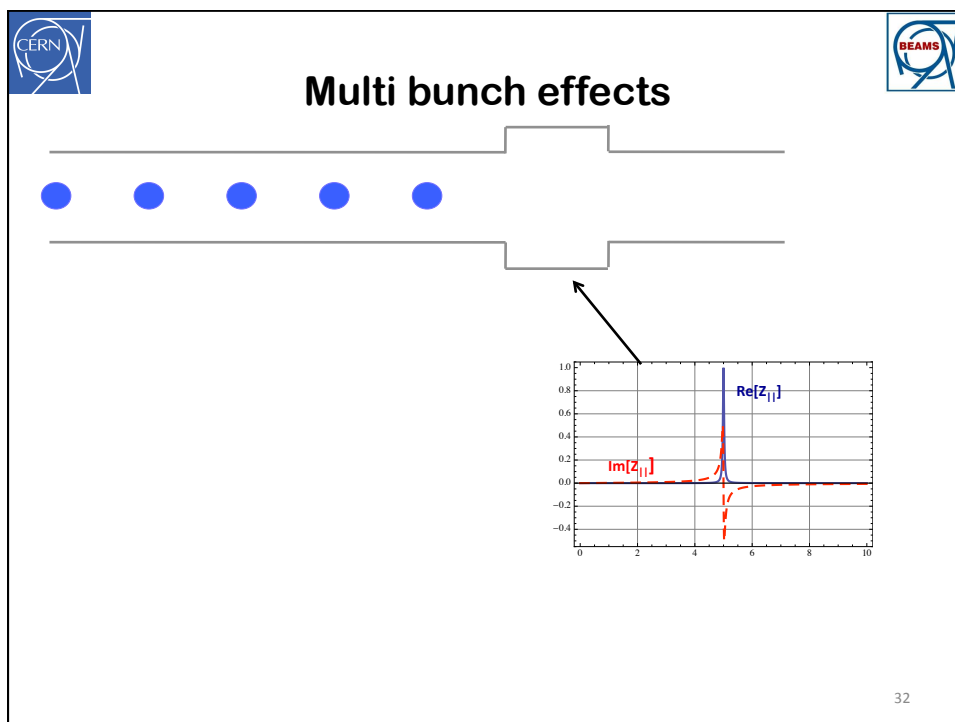
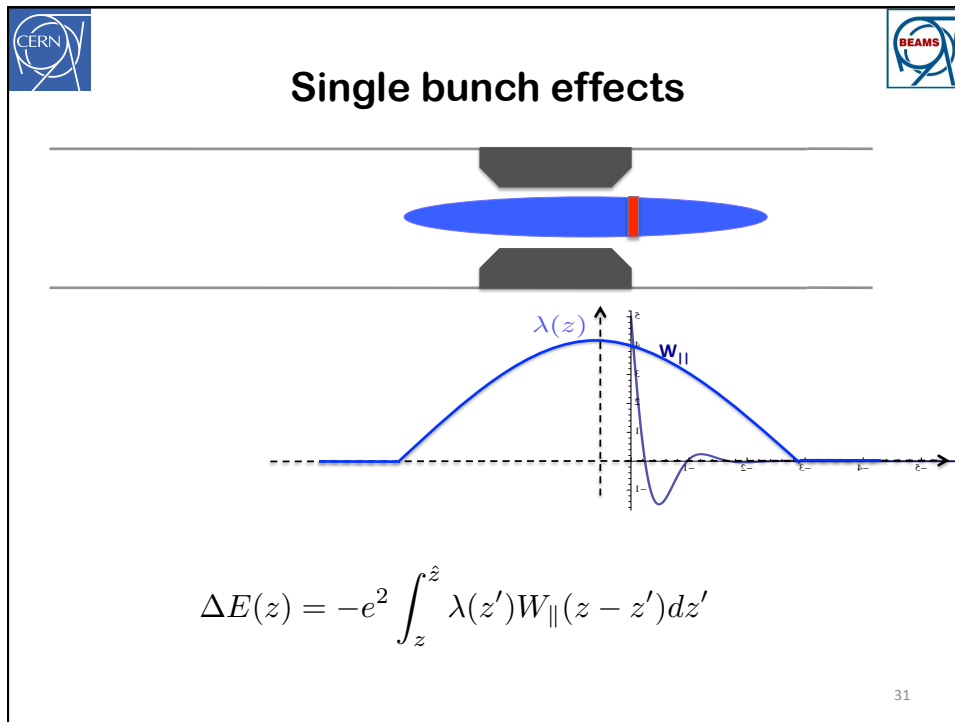
- A more complex example: a simple pill-box cavity with walls having finite conductivity
- Several modes can be excited
  - Below the pipe cut-off frequency the width of the peaks is only determined by the finite conductivity of the walls
  - Above, losses also come from propagation in the chamber



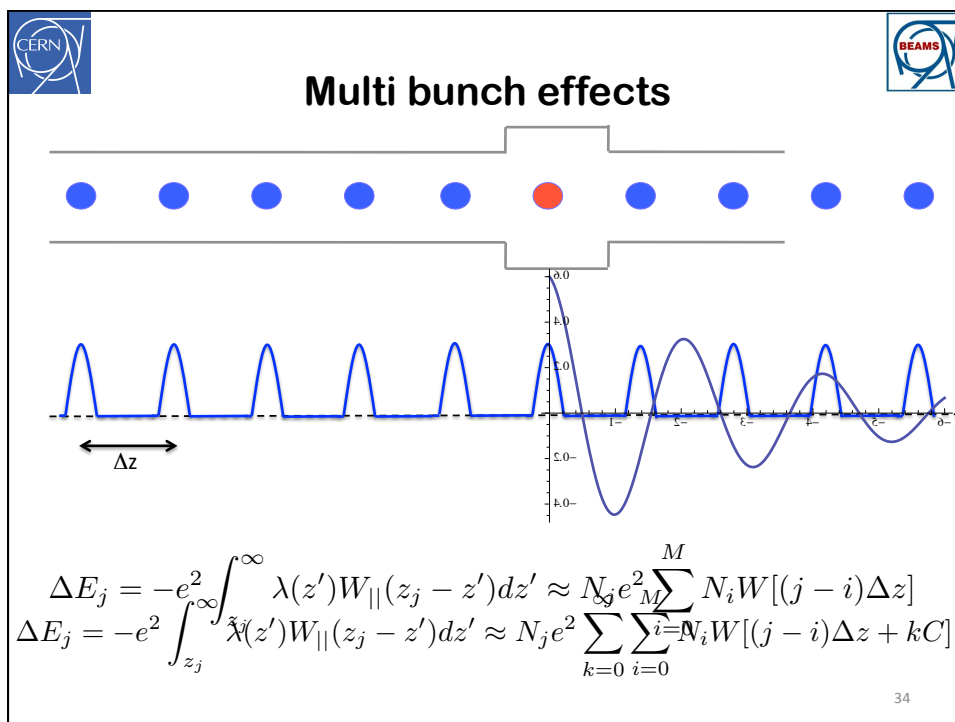
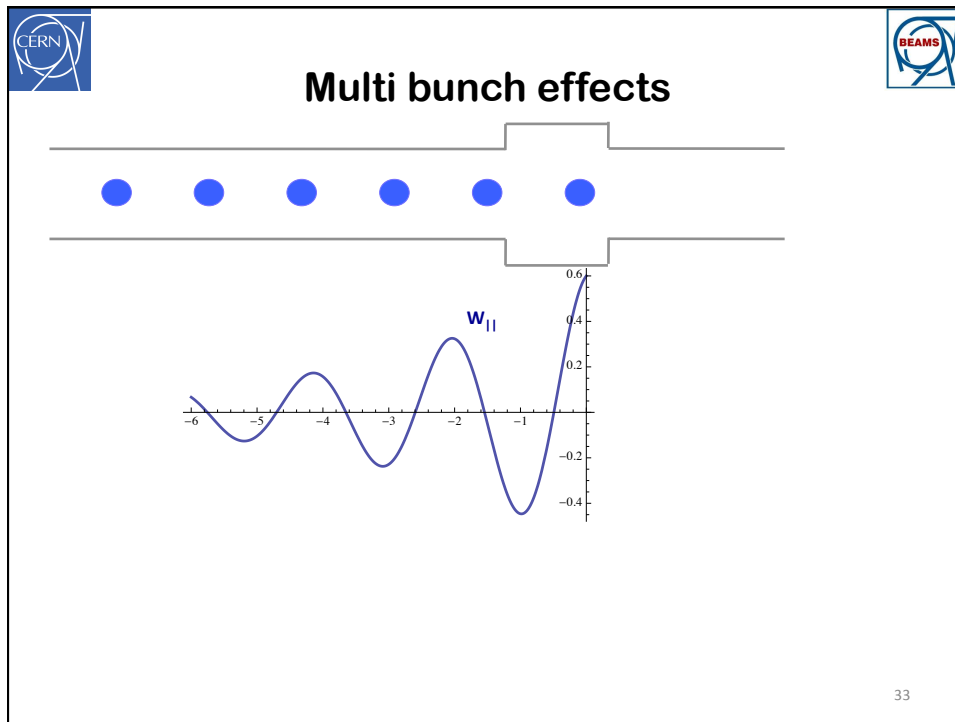
Note  $W_{||}(0) < 0$ , CST uses opposite convention!!

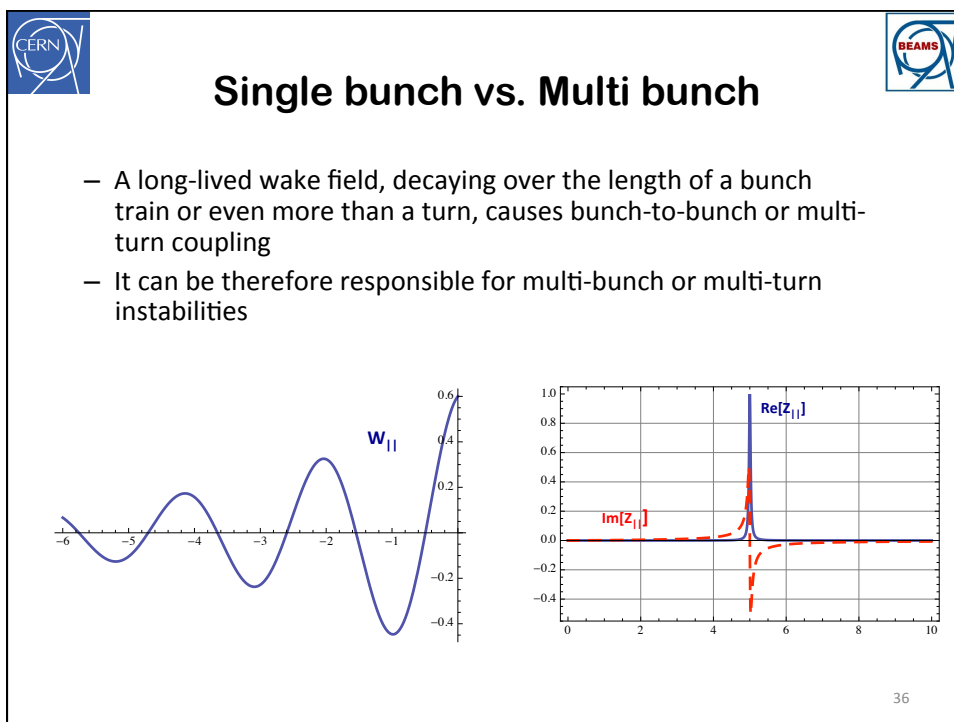
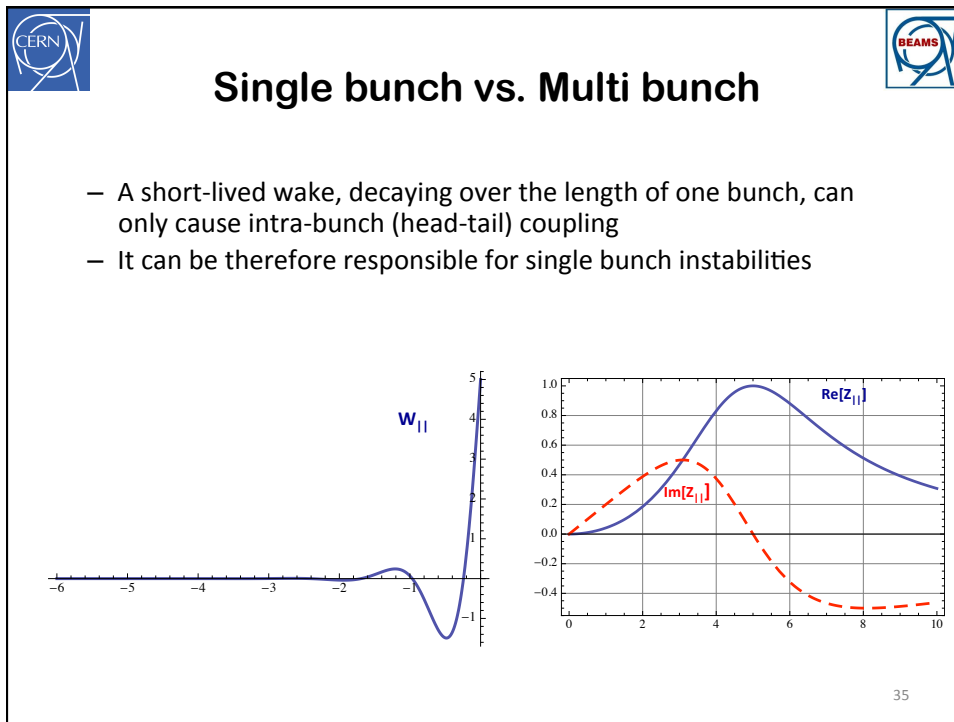
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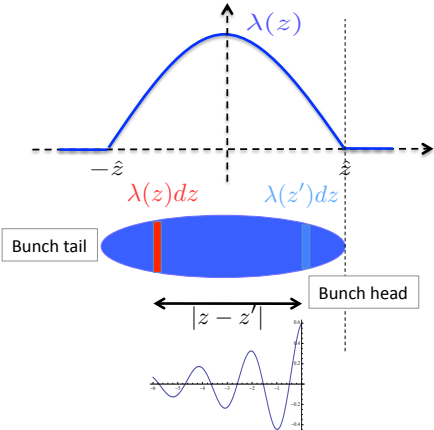
- Detailed calculations:
  - Energy loss
  - Robinson instability
- Qualitative descriptions:
  - Coupled bunch instabilities
  - Single bunch modes

[1] "Physics of Collective Beam Instabilities in High Energy Accelerators", A. W. Chao

## Energy loss of a bunch (single pass)

- The energy kick  $\Delta E(z)$  on each particle  $e$  in the witness slice  $\lambda(z)dz$  is the integral of the contributions from the wakes left behind by all the preceding  $e\lambda(z')dz$  slices (sources)
- The total energy loss  $\Delta E$  of the bunch can then be obtained by integrating  $\Delta E(z) \lambda(z)$  over the full bunch extension



$$\Delta E(z) = -e^2 \int_z^{\hat{z}} \lambda(z') W_{||}(z - z') dz'$$

$$\Delta E = \int_{-\hat{z}}^{\hat{z}} \lambda(z) \Delta E(z) dz$$

$$\Delta E = -\frac{e^2}{2\pi} \int_{-\infty}^{\infty} \tilde{\lambda}(\omega) \tilde{\lambda}^*(\omega) Z_{||}(\omega) d\omega =$$

$$-\frac{e^2}{2\pi} \int_{-\infty}^{\infty} |\tilde{\lambda}(\omega)|^2 \text{Re} [Z_{||}(\omega)] d\omega$$

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## Energy loss of a bunch (multi-pass)

- The total energy loss  $\Delta E$  of the bunch can still be obtained by integrating  $\Delta E(z)$  over the full bunch extension
- $\Delta E(z)$  this time also includes contributions from all previous turns, spaced by multiples of the ring circumference  $C$

$$\Delta E = -\frac{e^2}{2\pi} \int_{-\infty}^{\infty} \lambda(z) dz \int_{-\infty}^{\infty} dz' \lambda(z') \sum_{k=-\infty}^{\infty} W_{\parallel}(kC + z - z') dz'$$

$$\sum_{k=-\infty}^{\infty} W_{\parallel}(kC + z - z') = \frac{c}{C} \sum_{p=-\infty}^{\infty} Z_{\parallel}(p\omega_0) \exp\left[-\frac{ip\omega_0(z - z')}{c}\right]$$

$$\Delta E = -\frac{e^2\omega_0}{2\pi} \sum_{p=-\infty}^{\infty} Z_{\parallel}(p\omega_0) \underbrace{\int_{-\infty}^{\infty} \lambda(z) \exp\left(\frac{-ip\omega_0 z}{c}\right) dz}_{\tilde{\lambda}(p\omega_0)} \underbrace{\int_{-\infty}^{\infty} \lambda(z') \exp\left(\frac{ip\omega_0 z'}{c}\right) dz'}_{\tilde{\lambda}^*(p\omega_0)}$$

$$\Delta E = -\frac{e^2\omega_0}{2\pi} \sum_{p=-\infty}^{\infty} |\tilde{\lambda}(p\omega_0)|^2 \text{Re}[Z_{\parallel}(p\omega_0)]$$

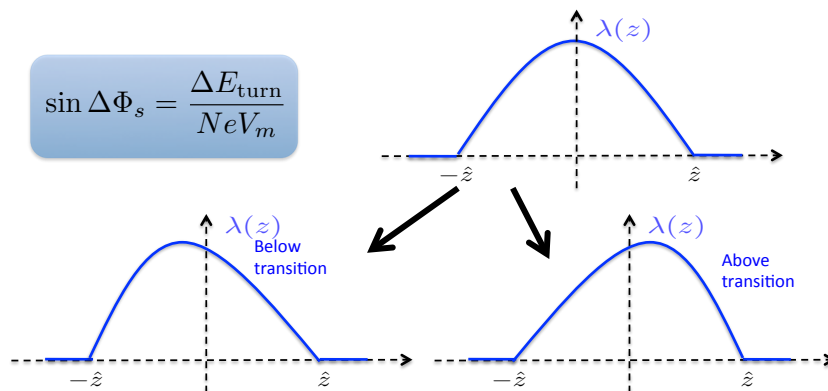
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## Energy loss per turn: stable phase shift

- The RF system has to compensate for the energy loss by imparting a net acceleration to the bunch
- Therefore, the bunch readjusts to a new equilibrium distribution in the bucket and moves to a synchronous angle  $\Delta\Phi_s$

$$\sin \Delta\Phi_s = \frac{\Delta E_{\text{turn}}}{NeV_m}$$




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### Example

## Gaussian bunch and power loss with a broad-band resonator impedance



$$\lambda(z) = \frac{N}{\sqrt{2\pi}\sigma_z} \exp\left(-\frac{z^2}{2\sigma_z^2}\right) \xLeftrightarrow{\mathcal{F}} \tilde{\lambda}(\omega) = N \exp\left(-\frac{\omega^2\sigma_z^2}{2c^2}\right)$$

$$\int_{-\infty}^{\infty} |\tilde{\lambda}(\omega)|^2 \operatorname{Re}[Z_{||}(\omega)] d\omega$$

can be calculated with  $Z_{||}(\omega) = Z_{||}^{\text{Res}}(\omega)$  from previous slide in the two limiting cases


$\sigma_z \gg \frac{c}{\omega_r}$ 

Need to expand  $\operatorname{Re}[Z_{||}(\omega)]$  for small  $\omega$


$\sigma_z \ll \frac{c}{\omega_r}$ 

Can assume  $|\tilde{\lambda}(\omega)|$  constant over  $\operatorname{Re}[Z_{||}(\omega)]$

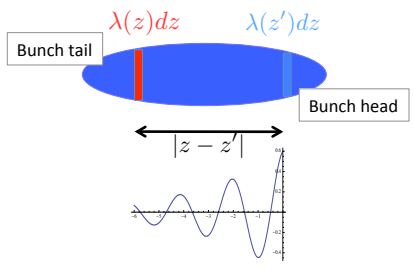
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### Single particle equations of the longitudinal motion in presence of wake fields





- The single particle in the witness slice  $\lambda(z)dz$  will feel the force from the RF, from the bunch own space charge, and that associated to the wake
- The wake contribution can extend to several turns



$$\underbrace{\frac{d^2z}{dt^2} + \frac{\eta e V_{\text{rf}}(z)}{m_0 \gamma C}}_{\text{External RF}} = \underbrace{\frac{\eta e^2}{m_0 \gamma C} \sum_{k=-\infty}^{\infty} \int_{-\infty}^{\infty} \lambda(z' + kC) W_{||}(z - z' - kC) dz'}_{\text{Wake fields}}$$

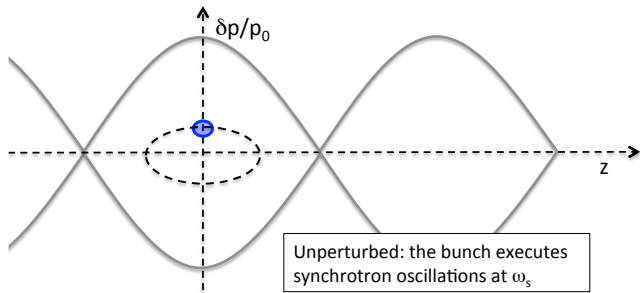
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## The Robinson instability



– To illustrate the Robinson instability we will use some simplifications:

- ⇒ The bunch is point-like and feels an external linear force (i.e. it would execute linear synchrotron oscillations in absence of the wake forces)
- ⇒ The bunch additionally feels the effect of a multi-turn wake



Unperturbed: the bunch executes synchrotron oscillations at  $\omega_s$

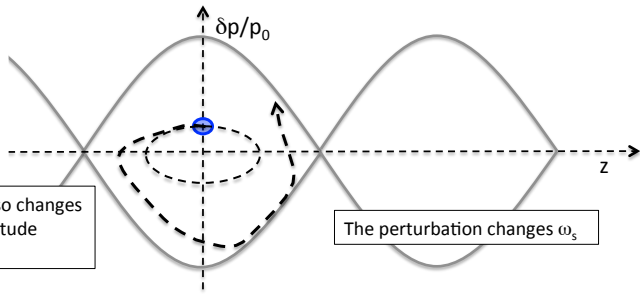
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## The Robinson instability

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- ⇒ The bunch is point-like and feels an external linear force (i.e. it would execute linear synchrotron oscillations in absence of the wake forces)
- ⇒ The bunch additionally feels the effect of a multi-turn wake



The perturbation also changes the oscillation amplitude  
Unstable motion

The perturbation changes  $\omega_s$

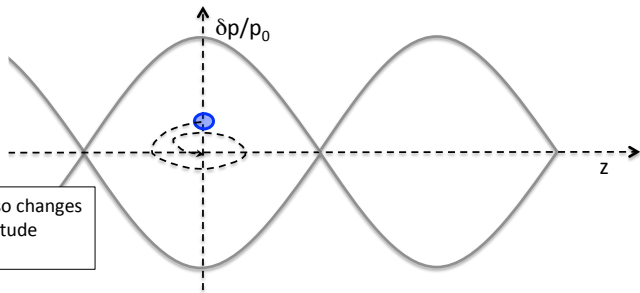
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## The Robinson instability



– To illustrate the Robinson instability we will use some simplifications:

- ⇒ The bunch is point-like and feels an external linear force (i.e. it would execute linear synchrotron oscillations in absence of the wake forces)
- ⇒ The bunch additionally feels the effect of a multi-turn wake



The perturbation also changes the oscillation amplitude  
Damped motion

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## The Robinson instability

– To illustrate the Robinson instability we will use some simplifications:



- ⇒ The bunch is point-like and feels an external linear force (i.e. it would execute linear synchrotron oscillations in absence of the wake forces)
- ⇒ The bunch additionally feels the effect of a multi-turn wake

$$\frac{d^2 z}{dt^2} + \omega_s^2 z = \frac{Ne^2 \eta}{Cm_0 \gamma} \sum_{k=-\infty}^{\infty} W_{\parallel} [z(t) - z(t - kT_0) - kC]$$

We assume that the wake can be linearized on the scale of a synchrotron oscillation

$$W_{\parallel} [z(t) - z(t - kT_0) - kC] \approx W_{\parallel}(kC) + W'_{\parallel}(kC) \cdot [z(t) - z(t - kT_0)]$$

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## The Robinson instability

$$W_{\parallel} [z(t) - z(t - kT_0) - kC] \approx \cancel{W_{\parallel}(kC)} + W'_{\parallel}(kC) \cdot [z(t) - z(t - kT_0)]$$

⇒ The term  $\sum W_{\parallel}(kC)$  only contributes to a constant term in the solution of the equation of motion, i.e. the synchrotron oscillation will be executed around a certain  $z_0$  and not around 0. This term represents the stable phase shift that compensates for the energy loss



⇒ The dynamic term proportional to  $z(t) - z(t - kT_0) \approx kT_0 dz/dt$  will introduce a “friction” term in the equation of the oscillator, which can lead to instability!

$$z(t) \propto \exp(-i\Omega t)$$

$$\Omega^2 - \omega_s^2 = -\frac{Ne^2\eta}{Cm_0\gamma} \sum_{k=-\infty}^{\infty} [1 - \exp(-ik\Omega T_0)] \cdot W'_{\parallel}(kC)$$

$$i \cdot \frac{1}{C} \sum_{p=-\infty}^{\infty} [p\omega_0 Z_{\parallel}(p\omega_0) - (p\omega_0 + \Omega) Z_{\parallel}(p\omega_0 + \Omega)]$$

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## The Robinson instability

⇒ We assume a small deviation from the synchrotron tune

⇒  $\text{Re}(\Omega - \omega_s) \rightarrow$  Synchrotron tune shift

⇒  $\text{Im}(\Omega - \omega_s) \rightarrow$  Growth/damping rate, only depends on the dynamic term, if it is positive there is an instability!

$$\Omega^2 - \omega_s^2 \approx 2\omega_s (\Omega - \omega_s)$$

$$\Delta\omega_s = \text{Re}(\Omega - \omega_s) = \left( \frac{e^2}{m_0 c^2} \right) \frac{N\eta}{2\gamma T_0^2 \omega_s} \times$$



$$\times \sum_{p=-\infty}^{\infty} [p\omega_0 \text{Im} Z_{\parallel}(p\omega_0) - (p\omega_0 + \omega_s) \text{Im} Z_{\parallel}(p\omega_0 + \omega_s)]$$

Complex frequency shift

$$\tau^{-1} = \text{Im}(\Omega - \omega_s) = \left( \frac{e^2}{m_0 c^2} \right) \frac{N\eta}{2\gamma T_0^2 \omega_s} \sum_{p=-\infty}^{\infty} (p\omega_0 + \omega_s) \text{Re} Z_{\parallel}(p\omega_0 + \omega_s)$$

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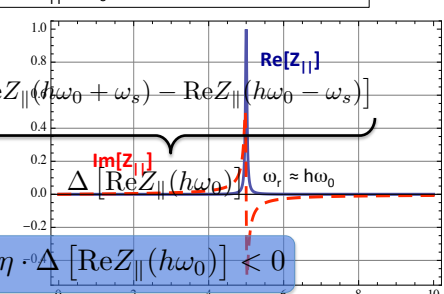
## The Robinson instability

$$\tau^{-1} = \text{Im}(\Omega - \omega_s) = \left( \frac{e^2}{m_0 c^2} \right) \frac{N\eta}{2\gamma T_0^2 \omega_s} \sum_{p=-\infty}^{\infty} (p\omega_0 + \omega_s) \text{Re}Z_{||}(p\omega_0 + \omega_s)$$



⇒ We assume the impedance to be peaked at a frequency  $\omega_r$  close to  $h\omega_0 \gg \omega_s$  (e.g. RF cavity fundamental mode or HOM)

⇒ Only two dominant terms are left in the summation at the RHS of the equation for the growth rate

⇒ Stability requires that  $\eta$  and  $\Delta[\text{Re}Z_{||}(h\omega_0)]$  have different signs

$$\tau^{-1} = \left( \frac{e^2}{m_0 c^2} \right) \frac{N\eta h\omega_0}{2\gamma T_0^2 \omega_s} \underbrace{[\text{Re}Z_{||}(h\omega_0 + \omega_s) - \text{Re}Z_{||}(h\omega_0 - \omega_s)]}_{\Delta[\text{Re}Z_{||}(h\omega_0)]}$$


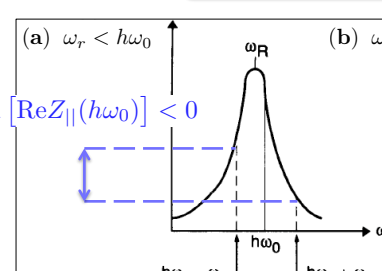
Stability criterion →  $\eta \cdot \Delta[\text{Re}Z_{||}(h\omega_0)] < 0$

## The Robinson instability

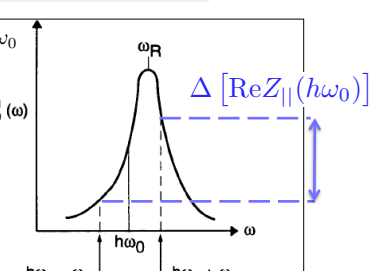
Stability criterion →  $\eta \cdot \Delta[\text{Re}Z_{||}(h\omega_0)] < 0$

(a)  $\omega_r < h\omega_0$



$\Delta[\text{Re}Z_{||}(h\omega_0)] < 0$

(b)  $\omega_r > h\omega_0$



$\Delta[\text{Re}Z_{||}(h\omega_0)] > 0$

**Figure 4.4.** Illustration of the Robinson stability criterion. The rf fundamental mode is detuned so that  $\omega_r$  is (a) slightly below  $h\omega_0$  and (b) slightly above  $h\omega_0$ . (a) is Robinson damped above transition and antidamped below transition. (b) is antidamped above transition and damped below transition.

	$\omega_r < h\omega_0$	$\omega_r > h\omega_0$
Above transition ( $\eta > 0$ )	stable	unstable
Below transition ( $\eta < 0$ )	unstable	stable

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## The Robinson instability

$$\tau^{-1} = \text{Im}(\Omega - \omega_s) = \left( \frac{e^2}{m_0 c^2} \right) \frac{N\eta}{2\gamma T_0^2 \omega_s} \sum_{p=-\infty}^{\infty} (p\omega_0 + \omega_s) \text{Re}Z_{\parallel}(p\omega_0 + \omega_s)$$

- ⇒ Other types of impedances can also cause instabilities through the Robinson mechanism
- ⇒ However, a smooth broad-band impedance with no narrow structures on the  $\omega_0$  scale cannot give rise to an instability
  - ✓ Physically, this is clear, because the absence of structure on  $\omega_0$  scale in the spectrum implies that the wake has fully decayed in one turn time and the driving term in the equation of motion also vanishes

$$\sum_{p=-\infty}^{\infty} (p\omega_0 + \omega_s) \text{Re}Z_{\parallel}(p\omega_0 + \omega_s) \rightarrow \frac{1}{\omega_0} \int_{-\infty}^{\infty} \omega \text{Re}Z_{\parallel}(\omega) d\omega \rightarrow 0$$



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## Other longitudinal instabilities

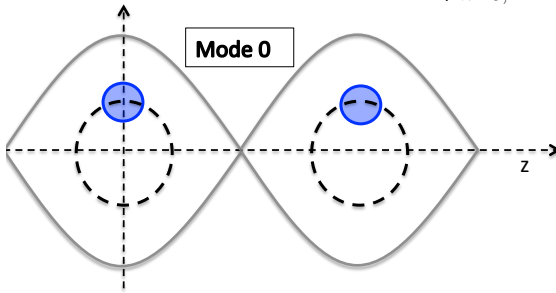
- The Robinson instability occurs for a single bunch under the action of a multi-turn wake field
  - It contains a term of coherent synchrotron tune shift
  - It results into an unstable rigid bunch dipole oscillation
  - It does not involve higher order moments of the bunch longitudinal phase space distribution
- Other important collective effects can affect a bunch in a beam
  - Potential well distortion (resulting in synchronous phase shift, bunch lengthening or shortening, synchrotron tune shift/spread)
  - Coupled bunch instabilities
  - High intensity single bunch instabilities (e.g. microwave instability)
  - Coasting beam instabilities (e.g. negative mass instability)
- To be able to study these effects we would need to resort to a more detailed description of the bunch(es)
  - Vlasov equation (kinetic model)
  - Macroparticle simulations

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## Coupled bunch modes

- M bunches can exhibit M different modes of coupled rigid bunch oscillations in the longitudinal plane



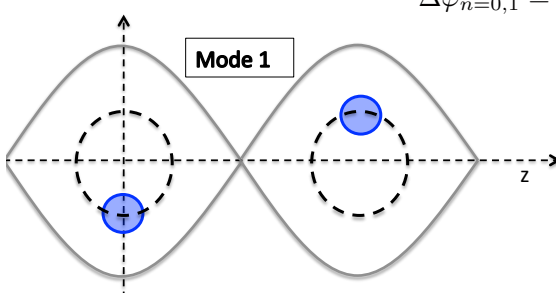
$\Delta\varphi_{n=0,1} = \frac{2\pi n}{N_b}$

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## Coupled bunch modes

- M bunches can exhibit M different modes of coupled rigid bunch oscillations in the longitudinal plane



$\Delta\varphi_{n=0,1} = \frac{2\pi n}{N_b}$

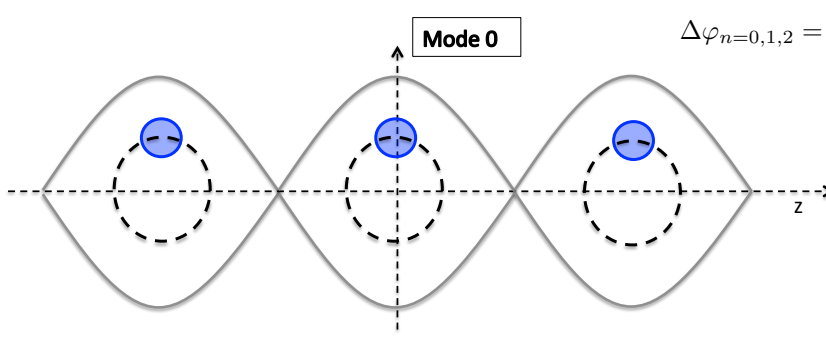
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## Coupled bunch modes



- M bunches can exhibit M different modes of coupled rigid bunch oscillations in the longitudinal plane
- Any rigid coupled bunch oscillation can be decomposed into a combination of these basic modes

**Mode 0**



$\Delta\varphi_{n=0,1,2} = \frac{2\pi n}{N_b}$

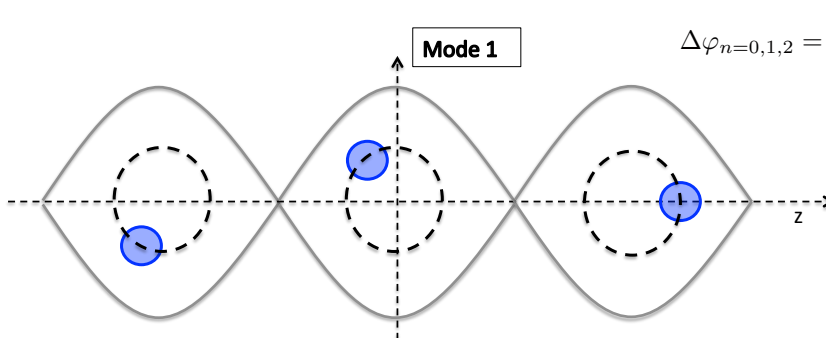
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## Coupled bunch modes



- M bunches can exhibit M different modes of coupled rigid bunch oscillations in the longitudinal plane
- Any rigid coupled bunch oscillation can be decomposed into a combination of these basic modes

**Mode 1**



$\Delta\varphi_{n=0,1,2} = \frac{2\pi n}{N_b}$

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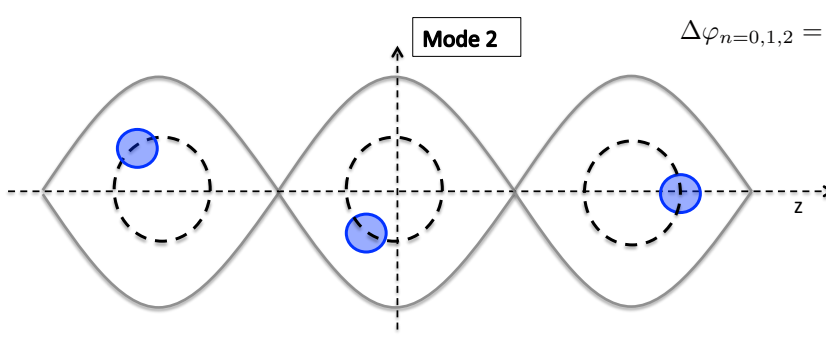
## Coupled bunch modes

- M bunches can exhibit M different modes of coupled rigid bunch oscillations in the longitudinal plane
- Any rigid coupled bunch oscillation can be decomposed into a combination of these basic modes



⇒ **This modes can become unstable under the effect of long range wake fields**

Mode 2

$$\Delta\varphi_{n=0,1,2} = \frac{2\pi n}{N_b}$$



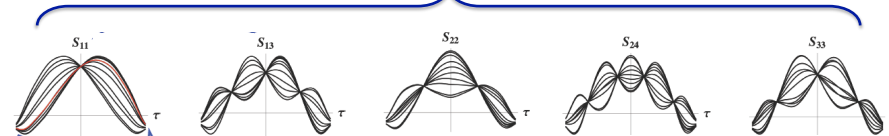
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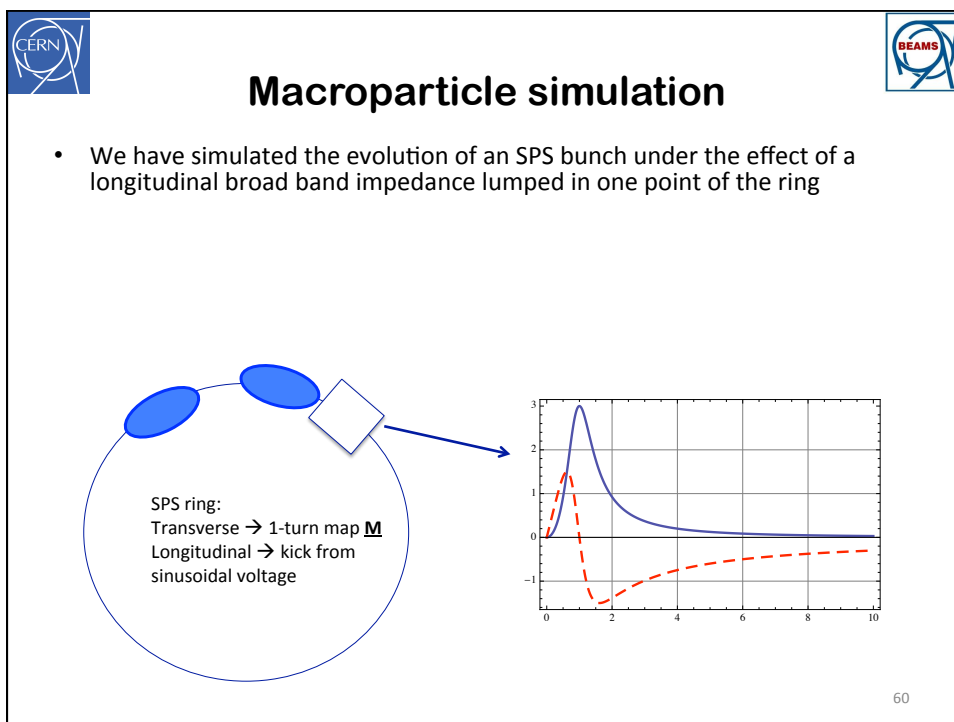
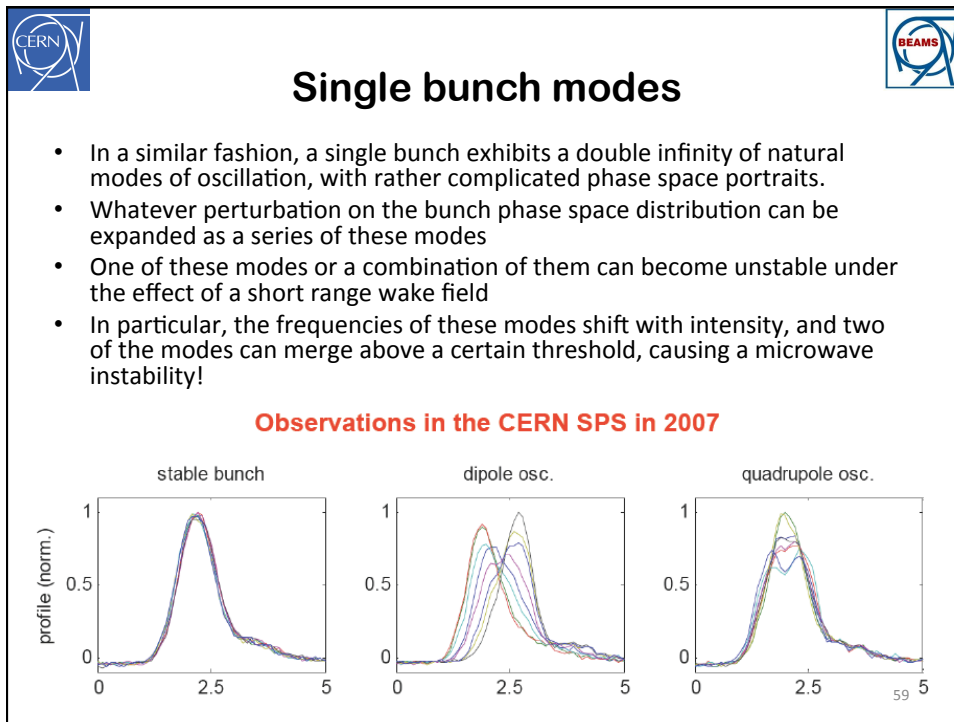
## Single bunch modes

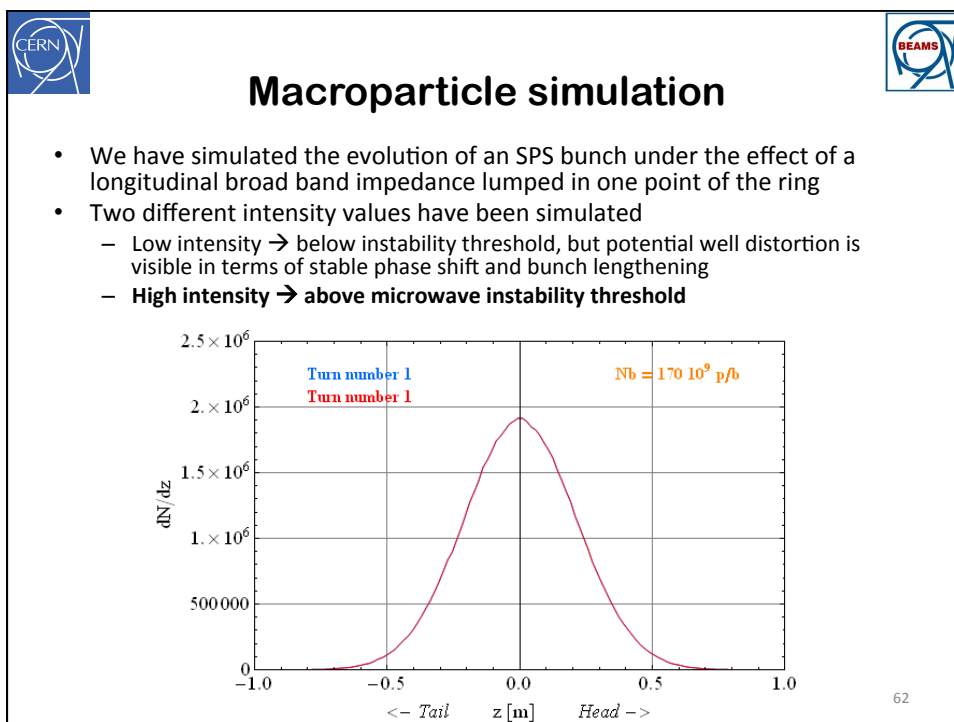
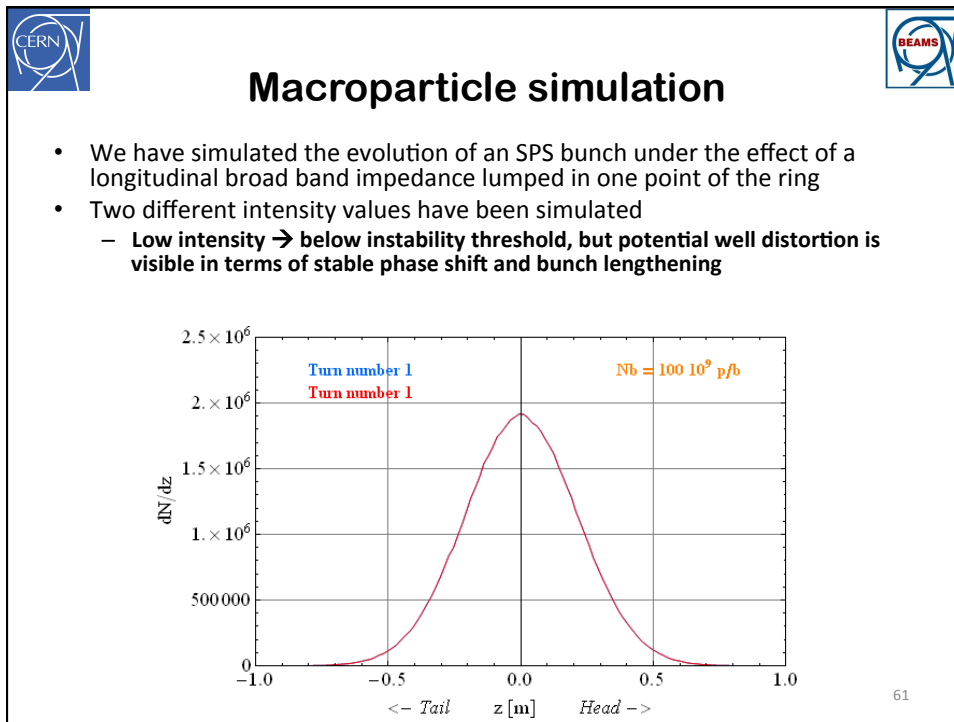
- In a similar fashion, a single bunch exhibits a double infinity of natural modes of oscillation, with rather complicated phase space portraits.
- Whatever perturbation on the bunch phase space distribution can be expanded as a series of these modes

Oscillation modes as observed at a wall current monitor



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## Conclusions (part I)

- Beam instability
  - Manifests itself like an exponential coherent motion resulting in beam loss or emittance blow up
  - Can be caused by self induced EM fields
  - Can be described in the framework of wake fields/beam coupling impedances
- Longitudinal effects
  - Energy loss
  - Dipole instability (Robinson), excitation of coupled bunch & single bunch modes
- Tomorrow → transverse wake fields/beam coupling impedances and instabilities

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