

High Brilliance Beam Diagnostics

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Advanced Accelerator Physics Course 2015



Outline

- Brightness and Brilliance
- Fundamental parameters
- Transverse and longitudinal measurements
- Intercepting and non intercepting diagnostic



Brightness and Brilliance

- Several authors give different definitions
- Brilliance is sometimes used, especially in Europe, instead of brightness
- There is also confusion because the same words apply both to particle beams and photon beams
- The best way is to look to units, which should be unambiguous

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Some references

- C. Lejeune and J. Aubert, "Emittance and Brightness, definitions and measurements", Adv. Electron. Electron Phys., Suppl. A 13, 159 (1980).
- A. Wu Chao, M. Tigner "Handbook of Accelerator Physics and Engineering" World Scientific, pag 255
- C. A. Brau "What Brightness means" in The Physics and Applications of High Brightness Electron Beam", World Scientific, pag 20
- M. Reiser, "Theory and design of charged particle beams", Wiley-VCH, pag 61
- Shyh-Yuan Lee, "Accelerator Physics", World Scientific, pag 419
- J. Clarke "The Science and Technology of Undulators and Wiggles" Oxford Science Publications, pag 73



Definitions of Brightness

$$B = \frac{dI}{dSd\Omega}$$

For particle distribution whose boundary in 4D trace space is defined by an hyperellipsoid

$$\overline{B} = \frac{2I}{\pi^2 \varepsilon_x \varepsilon_y}$$
 [A/(m-rad)²]

$$\overline{B}_n = \frac{1}{\pi^2 \mathcal{E}_{nx} \mathcal{E}_{ny}} \quad \text{Normalize}$$

Normalized Brightness

From diagnostics point of view what does it mean high brightness?

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But

- Often the factor $2/\pi^2$ is left out in literature
- Often the RMS emittance is used in place of effective emittance and so there is another factor to take into the account
- So it is important to agree on the brightness definition, but the difference can be also in numerical factors

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Parameters to measure

- High brightness can be achieved with small emittance, high current or both
- <u>Longitudinal</u> and <u>transverse</u> parameters must be measured
- High charge and small emittance -> high power density beam
- Low charge, very short bunch length
- We focus our attention on linac or transfer line where it is possible to use intercepting diagnostic
- For some applications, it is needed to measure also the transverse parameters in different longitudinal positions (slice parameters)

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Brilliance

$$B = \frac{d^4N}{dt d\Omega dS d\lambda / \lambda}$$

Photons/ (s mm² mrad² 0.1% of bandwidth)

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H. Wiedeman uses the name "spectral brightness" for photons

Report of the Working Group on Synchrotron Radiation Nomenclature – brightness, spectral brightness or brilliance?

The conclusion reached is that the term spectral brightness best describes this quantity. Brightness maintains the generally accepted concept of intensity per unit source size and divergence, while the adjective spectral conveys the scientific importance of the number of photons in a given bandwidth, particularly for experiments such as inelastic and/or nuclear resonant scattering.

J. Synchrotron Rad. (2005). 12, 385



Transverse parameters

- The most important parameter is the emittance
- To obtain high brightness beam it is of paramount importance to keep emittance growth under control
- Different methods apply for beams with or without space charge contribution
- Mainly the space charge is relevant at the exit of the RF GUN (few MeV)

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Geometrical vs Normalized

$$\left| \varepsilon_n^2 = \left\langle x^2 \right\rangle \left\langle \beta^2 \gamma^2 x'^2 \right\rangle - \left\langle x \beta \gamma x' \right\rangle$$

$$\sigma_E^2 = \frac{\left\langle \beta^2 \gamma^2 \right\rangle - \left\langle \beta \gamma \right\rangle^2}{\left\langle \gamma \right\rangle^2}$$

$$\mathcal{E}_{n}^{2} = \langle \gamma \rangle^{2} \sigma_{\varepsilon}^{2} \langle x^{2} \rangle \langle x'^{2} \rangle + \\ + \langle \beta \gamma \rangle^{2} \left(\langle x^{2} \rangle \langle x'^{2} \rangle - \langle xx' \rangle^{2} \right)$$

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M. Migliorati et al, Physical Review Special Topics, Accelerators and Beams 16, 011302 (2013)

K. Floettmann, PRSTAB,6, 034202 (2003)



Fundamental issue

$$\varepsilon_n^2 = \langle \gamma \rangle^2 \left(\sigma_\varepsilon^2 \sigma_x^2 \sigma_{x'}^2 + \varepsilon^2 \right)$$
 $\sigma_x(s) \approx \sigma_{x'} s$

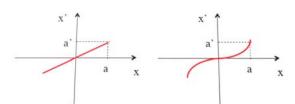
$$\varepsilon_n^2 = \langle \gamma \rangle^2 \left(s^2 \sigma_\varepsilon^2 \sigma_{x'}^4 + \varepsilon^2 \right)$$

- For the accelerator community the normalized emittance is one of the main parameter because is constant
- For plasma accelerated beams, due to the large energy spread and huge angular divergence, it is not true anymore

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Importance of RMS emittance



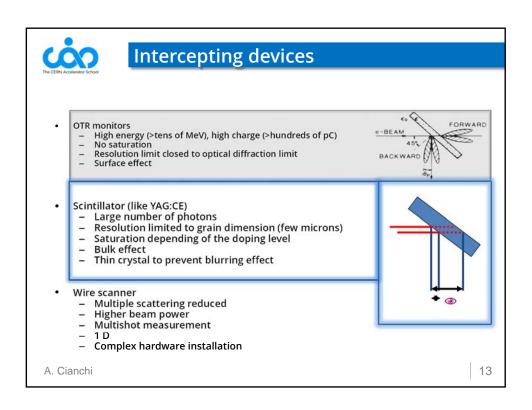
$$x' = Cx^n$$

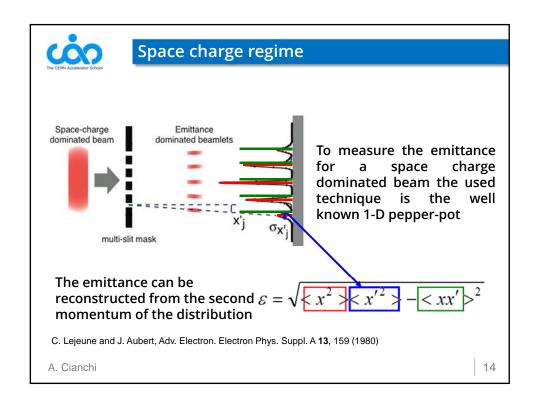
$$\varepsilon_{rms} = C\sqrt{\langle x^2 \rangle \langle x^{2n} \rangle - \langle x^{n+1} \rangle^2} \qquad \begin{cases} n = 1 \Rightarrow \varepsilon_{rms} = 0 \\ n > 1 \Rightarrow \varepsilon_{rms} \neq 0 \end{cases}$$

Even when the phase-space area is zero, if the distribution lies on a curved line its rms emittance is not zero.

RMS emittance is not an invariant for Hamiltonian with non linear terms.

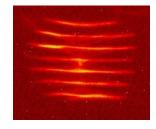
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Examples





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Design issue

 The beamlets must be emittance dominated

$$\sigma_x'' = \frac{\varepsilon_n^2}{\gamma^2 \sigma_x^3} + \frac{I}{\gamma^3 I_0(\sigma_x + \sigma_y)}$$

Martin Reiser, Theory and Design of Charged Particle Beams (Wiley, New York, 1994)

Assuming a round beam

$$R_0 = \frac{I\sigma_0^2}{2\gamma I_0 \varepsilon_n^2} \qquad \sigma_x = \frac{d}{\sqrt{12}}$$

d must be chosen to obtain R₀<<1, in order to have a emittance dominated beam

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Design issues 2

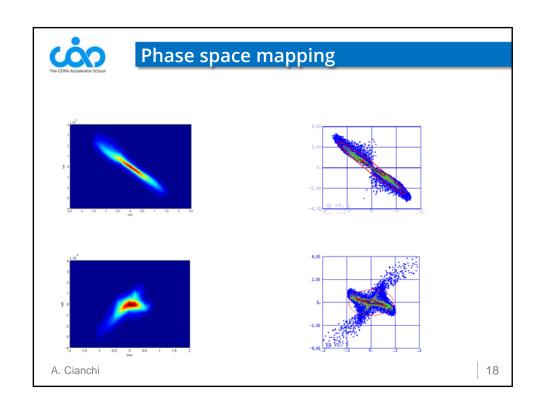
- The contribution of the slit width to the size of the beamlet profile should be negligible
- The material thickness (usually tungsten) must be long enough to stop or heavily scatter beam at large angle (critical issue at high energy)
- The angular acceptance of the slit cannot be smaller of the expected angular divergence of the beam

$$\sigma = \sqrt{\left(\mathbf{L} \cdot \sigma'\right)^2 + \left(\frac{\mathbf{d}^2}{12}\right)}$$

$$L >> \frac{d}{\sigma' \cdot \sqrt{12}}$$

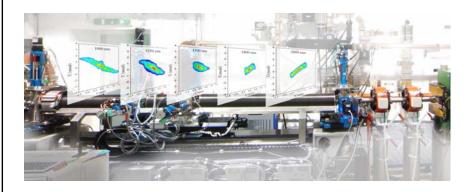
$$l < \frac{d}{2\sigma'}$$

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Phase space evolution



A. Cianchi et al., "High brightness electron beam emittance evolution measurements in an rf photoinjector", Physical Review Special Topics Accelerator and Beams 11, 032801,2008

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Emittance without space charge

 The most used techniques for emittance measurements are quadrupole scan and multiple monitors

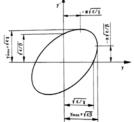
$$\gamma x^{2} + 2\alpha x x' + \beta x'^{2} = \varepsilon = \gamma_{0} x_{0}^{2} + 2\alpha_{0} x_{0} x'_{0} + \beta_{0} x'_{0}^{2}$$

$$M(s_1s_2) = \begin{pmatrix} C & S \\ C' & S' \end{pmatrix} \qquad \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix} = \begin{pmatrix} C^2 & -2SC & S^2 \\ -CC' & S'C + SC' & -SS' \\ C'^2 & -2S'C' & S'^2 \end{pmatrix} \begin{pmatrix} \beta_0 \\ \alpha_0 \\ \gamma_0 \end{pmatrix}$$



Beam Matrix

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} \\ \sigma_{12} & \sigma_{22} \end{pmatrix} = \varepsilon \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix}$$



$$\sigma_{11}x^2 + 2\sigma_{12}xx' + \sigma_{22}x'^2 = 1$$

$$\sigma_1 = M\sigma_0 M^T$$

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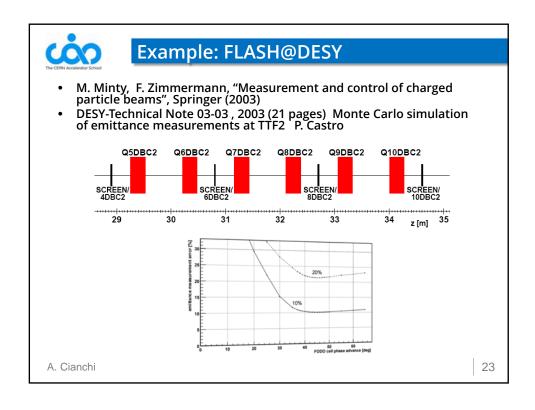


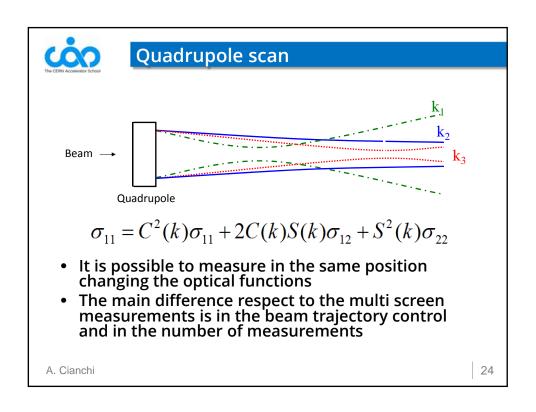
Multiple screens

$$\sigma_{i,11} = C_i^2 \sigma_{11} + 2S_i C_i \sigma_{12} + S_i^2 \sigma_{22}$$

- There are 3 unknown quantities
- $\sigma_{i,11}$ is the RMS beam size
- C_i and S_i are the element of the transport matrix
- We need 3 measurements in 3 different positions to evaluate the emittance

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Sources of errors

 Usually the largest error is in the determination of the RMS beam size (Mini Workshop on "Characterization of High Brightness Beams", Desy Zeuthen 2008,

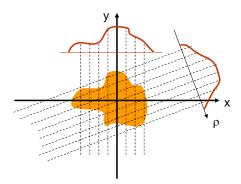
https://indico.desy.de/conferenceDisplay.py?confld=806)

- Systematic error comes from the determination of the quadrupole strength, mainly for hysteresis. So a cycling procedure is required for accurate measurements
- Thin lens model is not adequate
- Energy
- Large energy spread can gives chromatic effect
- Assumption: transverse phase space distribution fills an ellipse
- F. Loehl et al. "Physical Review Special Topics -Accelerators and Beams 9, 092802 (2006)

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Phase space reconstruction



 Tomography is related to the Radon theorem: a ndimensional object can be reconstructed from a sufficient number of projection in (n-1) dimensional space

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Tomography

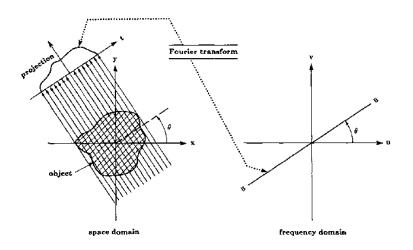
$$\begin{split} \hat{f}(\rho,\theta) &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} dx dy f(x,y) \delta(\rho - x cos\theta - y sin\theta) & \text{Radon Transform} \\ f(x,y) &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} F(u,v) e^{i2\pi(ux+vy)} du dv. \quad f(x,y) = \int_{0}^{\pi} \int_{-\infty}^{\infty} |w| F(w,\theta) e^{i2\pi w \rho} dw d\theta. \\ S(w,\theta) &= \int_{-\infty}^{\infty} \hat{f}(\rho,\theta) e^{-i2\pi w \rho} d\theta. \quad \text{Fourier transform of the Radon transform} \\ f(x,y) &= \int_{0}^{\pi} \int_{-\infty}^{\infty} |w| S(w,\theta) e^{i2\pi w \rho} dw d\theta, \qquad f(x,y) = \int_{0}^{\pi} Q(\rho,\theta) d\theta, \end{split}$$

- A. C. Kak and Malcolm Slaney, Principles of Computerized Tomographic Imaging, IEEE Press, 1988.
- D. Stratakis et al, "Tomography as a diagnostic tool for phase space mapping of intense particle beam", Physical Review Special Topics – Accelerator and Beams 9, 112801 (2006)

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Fourier Slice theorem



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Tomography measurements

$$\begin{pmatrix} x_1 \\ x_1' \end{pmatrix} = M_1 \begin{pmatrix} x_0 \\ x_0' \end{pmatrix} \qquad s = \sqrt{M_{11}^2 + M_{12}^2}, \qquad \text{Scaling factor}$$

$$\cos(\theta) = \frac{M_{11}}{\sqrt{M_{11}^2 + M_{12}^2}},$$

$$\sin(\theta) = \frac{M_{12}}{\sqrt{M_{11}^2 + M_{12}^2}}.$$
 Rotation angle

- C can be easily obtained from beam spatial distribution
- s can be calculated from the beam line optics
- The accuracy of the result depends from the total angle of the rotation and from the number of the projections

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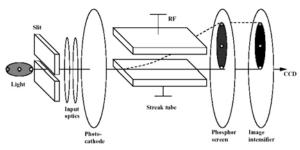


Longitudinal parameters

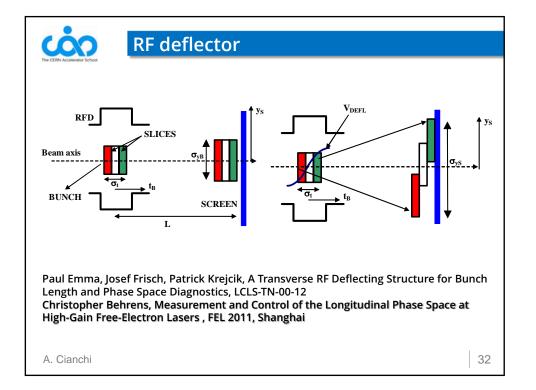
- Fundamental parameter for the brightness
- Bunch lengths can be on ps (uncompressed) or subps time scale, down to fs scale!
- · Several methods
 - Streak Camera
 - Coherent radiations
 - RFD
 - EOS
 - Others?
- T. Watanabe et al, "Overall comparison of subpicosecond electron beam diagnostics by the polychromator, the interferometer and the femtosecond streak camera", Nuclear Instruments and Methods in Physics Research A 480 (2002) 315–327



Streak camera



- Expensive device
- Resolution limited to 200-300 fs FWHM
- It is better to place the device outside the beam tunnel so a light collection and transport line is needed
- Reflective optics vs lens optics
- · Intercepting device





RFD

$$\Delta x'(z) = \frac{eV_0}{pc} \sin(kz + \varphi) \approx \frac{eV_0}{p_z c} \left[\frac{2\pi}{\lambda} z \cos \varphi + \sin \varphi \right]$$

$$|z| \ll \lambda/2\pi$$

$$\Delta x(z) = \frac{eV_0}{pc} \sqrt{\beta_a \beta_z} \sin \Delta \Psi \left[\frac{2\pi}{\lambda} z \cos \varphi + \sin \varphi \right]$$

$$\sigma^{2}_{x0} = \sqrt{\frac{\beta_{s}\varepsilon_{N}}{\gamma}}$$

$$\sigma_{x} = \sqrt{\sigma_{x0}^{2} + \sigma_{z}^{2} \beta_{d} \beta_{z} \left(\frac{2\pi e V_{0}}{\lambda p c} \sin \Delta \Psi \cos \varphi\right)^{2}}$$

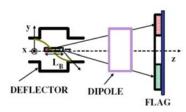
$$eV_0 >> \frac{\lambda}{2\pi\sigma_z} \frac{1}{\left|\sin\Delta\Psi\cos\varphi\right|} \sqrt{\frac{\varepsilon_N p c m c^2}{\beta_d}}$$

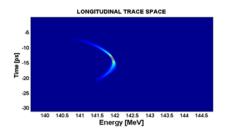
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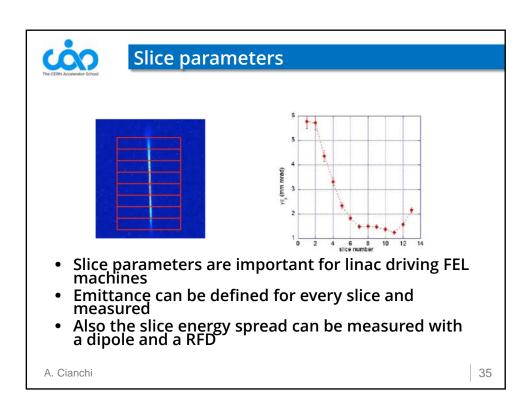
Longitudinal phase space

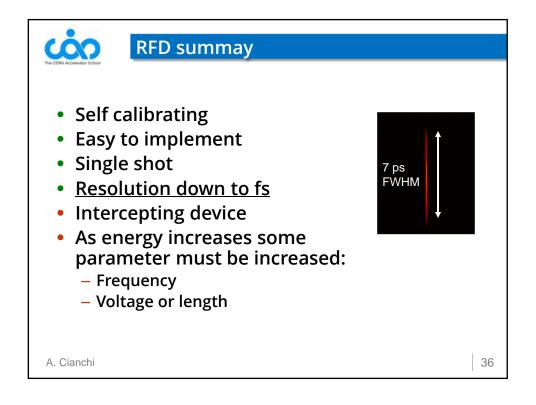




- Using together a RFD with a dispersive element such as a dipole
- Fast single shot measurement

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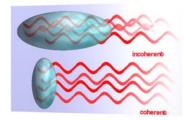






Coherent radiation

- Any kind of radiation can be coherent and usable for beam diagnostics
 - Transition radiation
 - Diffraction radiation
 - Synchrotron radiation
 - Undulator radiation
 - Smith-Purcell radiation
 - Cherenkov radiation



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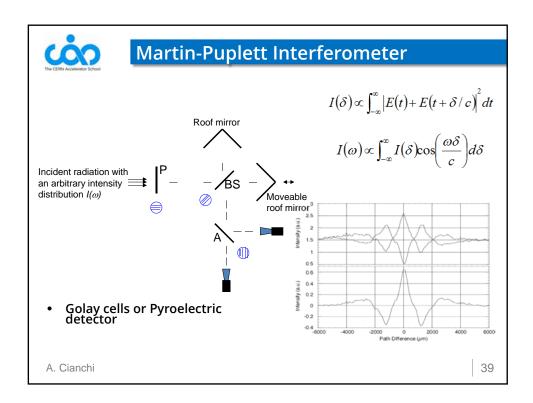
Power Spectrum

$$I_{tot}(\omega)=I_{sp}(\omega)[N+N^*(N-1) F(\omega)]$$

$$F(\omega) = \left| \int_{-\infty}^{\infty} dz \rho(z) e^{i(\omega/c)z} \right|^{2} \qquad \rho(z) = \frac{1}{\pi c} \int_{0}^{\infty} d\omega \sqrt{F(\omega)} \cos\left(\frac{\omega z}{c}\right)$$

- From the knowledge of the power spectrum is possible to retrieve the form factor
- The charge distribution is obtained from the form factor via Fourier transform
- The phase terms can be reconstructed with Kramers-Kronig analysis (see R. Lai, A.J. Sievers, NIM A 397 (1997) 221-231)

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Experimental considerations

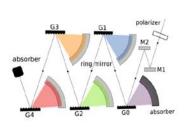
- Spectrum cuts at low and high frequencies can affect the beam reconstruction
 - Detectors
 - Windows
 - Transport line
 - Finite target size
- For this reason the approach is to test the power spectrum with the Fourier transform of a guess distribution
- Coherent synchrotron radiation or diffraction radiation can be generated by totally not intercepting devices and so they are eligible for high brightness beams diagnostic
- <u>Multishots measurements. Single shot devices are</u> still under developing

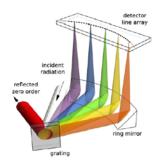
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Single shot CTR measurements I

 S. Wesch, B. Schmidt, C. Behrens, H. Delsim-Hashemi, P. Schmuser, A multichannel THz and infrared spectrometer for femtosecond electron bunch diagnostics by single-shot spectroscopy of coherent radiation Nuclear Instruments and Methods in Physics Research A 665 (2011) 40–47





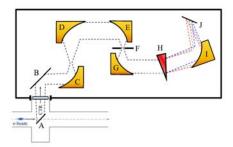
Pyro-electric line detector 30 channels @ room temperature no window, works in vacuum fast read out sensitivity

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Single shot CTR measurements II

• T. J. Maxwell et al. "Coherent-radiation spectroscopy of few-femtosecond electron bunches using a middle-infrared prism spectrometer." *Physical review letters* 111.18 (2013)



KRS-5 (thallium bromoiodide) prism based spectrometer developed

Images OTR from foil onto 128 lead zirconate titanate pyroelectric elements with 100 μm spacing line array

Also double prism (ZnSe), S. Wunderlich et al., Proceedings of IBIC2014

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Electro Optical Sample (EOS)

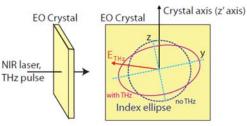
- <u>Totally non intercepting device and not disturbing</u> device
- It is based on the change of the optical properties of a non linear crystal in the interaction with the Coulomb field of the moving charges
- · Several schemes has been proposed and tested
- · Very promising technique
 - I.Wilke et al., "single-Shot electron beam bunch length measurements" PRL, v.88, 12(2002)
 - G. Berden et al., "Electo-Optic Technique with improved time resolution for real time, non destructive, single shot measurements of femtosecond electron bunch profiles, PRL v93, 11 (2004)
 - B. Steffen, "Electro-optic time profile monitors for femtosecond electron bunches at the soft x-ray free-electron laser FLASH", Phys. Rev. ST Accel. Beams 12, 032802 (2009)

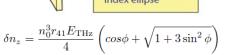
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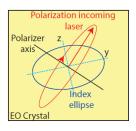
A bit of theory





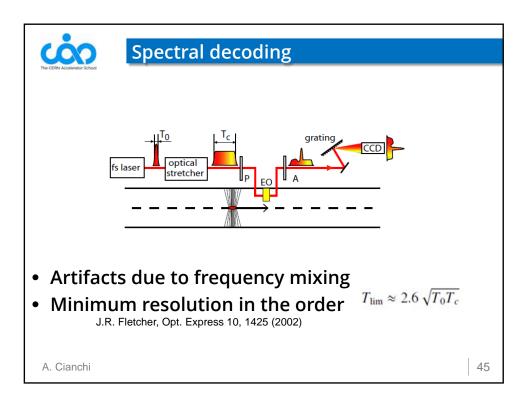
$$\Gamma_{j}(\omega) = \frac{2\pi}{\lambda_{0}} L \delta n_{j}(\omega) T_{\text{crystal}}(\omega),$$

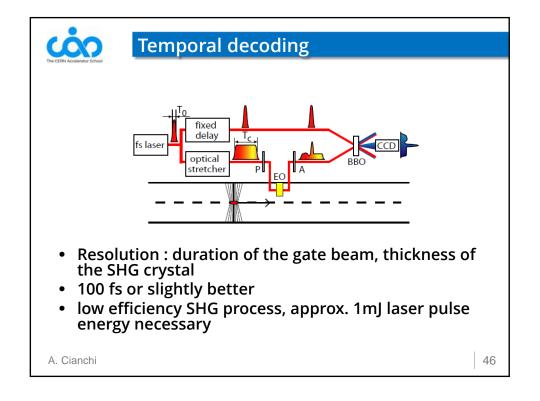
$$T_{\rm crystal}(\omega) = \frac{2}{1+n_{\rm THz}} \cdot \frac{\exp\left[iL(n_{\rm gr}-n_{\rm THz})\frac{\omega}{c}\right] - 1}{i\frac{\omega}{c}(n_{\rm gr}-n_{\rm THz})}$$

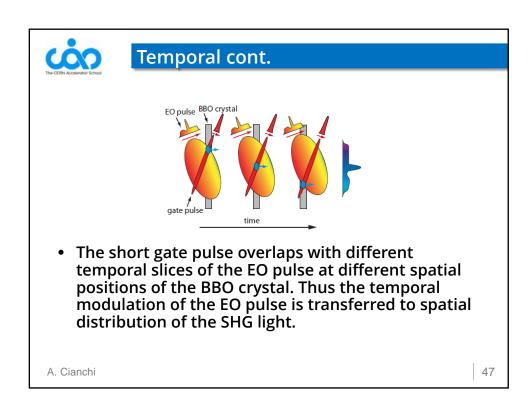


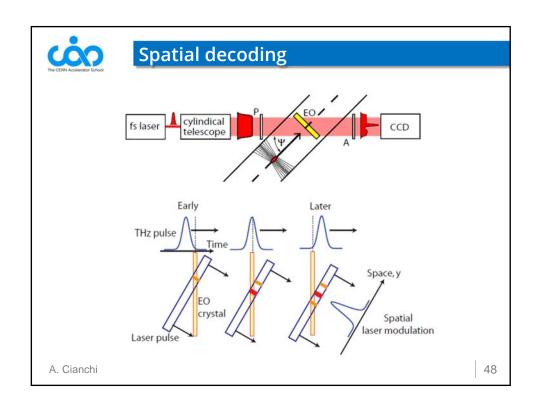
 $E_{M,j}(t) = E_{L,j}(t)e^{i\Gamma_j(t)}$

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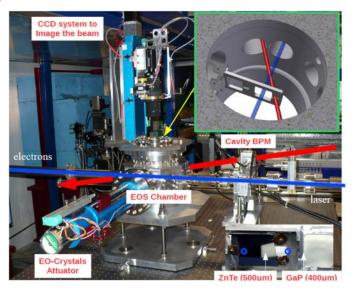








EOS setup



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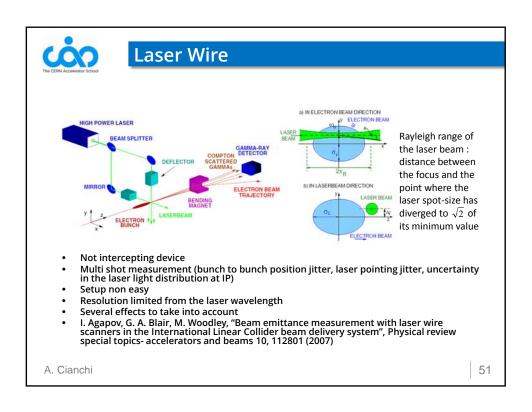
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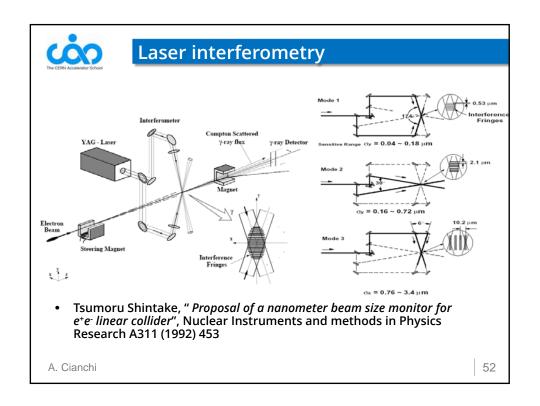


Intercepting diagnostics

- High charge or high repetition rate machines
- Small beam dimension (between 50 μm down to tens of nm)
- All the intercepting devices are damaged or destroyed from these kind of beams
- No wire scanners, no OTR screens, no scintillators
- There are good candidates for longitudinal diagnostic
- It is difficult to replace intercepting devices for transverse dimensions
- There are a lot of ideas in testing

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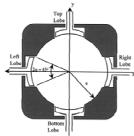




Not intercepting multi shot

Steven J. Russell, Emittance measurements of the Sub-Picosecond Accelerator electron beam using beam position monitors, Review of Scientific Instruments 70, 2, February 1999

A. Jansson, "Noninvasive single-bunch matching and emittance monitor", PRSTA-AB 5, 072803 (2002)



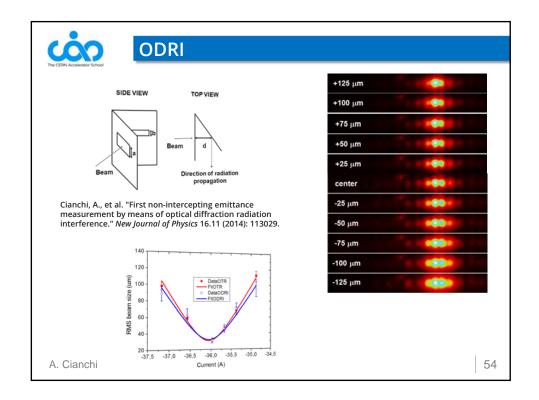
$$\overline{x} = a \frac{\alpha}{2 \sin \alpha} \frac{A_R - A_L}{A_R + A_L}$$
 $\overline{y} = a \frac{\alpha}{2 \sin \alpha} \frac{A_T - A_B}{A_T + A_B}$

$$\langle x^2 \rangle - \langle y^2 \rangle + \vec{x}^2 - \vec{y}^2 = a^2 \frac{\alpha}{\sin 2\alpha} \frac{A_R + A_L - A_T - A_B}{A_R + A_L + A_T + A_B}$$

$$\langle x^2 \rangle_f - \langle y^2 \rangle_f = (R_{11})^2 \langle x^2 \rangle_i + 2R_{11}R_{12} \langle xx' \rangle_i + (R_{12})^2 \langle x'^2 \rangle_i$$

$$- (R_{33})^2 \langle y^2 \rangle_i - 2R_{33}R_{34} \langle yy' \rangle_i - (R_{34})^2 \langle y'^2 \rangle_i^5,$$

- Special and customized electrodes are needed in order to maximize the quadrupole component
- Very low signal to noise ratio, systematic error from beam position





Conclusions

- High brightness beam demands particular diagnostic techniques in order to measure very small transverse emittance (<1 mm-mrad) and very short bunch length (< 1 ps)
- Intercepting or not intercepting diagnostics are recommended in some cases
- Some diagnostics are already state of the art
- Some others are still developing
- New ideas are daily tested, so if you want your part of glory start to think about today!

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Finally it's over

• Thank you for your attention

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