

# Study of the Higgs properties at a muon collider.

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**RAL, June 25<sup>th</sup>, 2015**

# Motivation and Summary

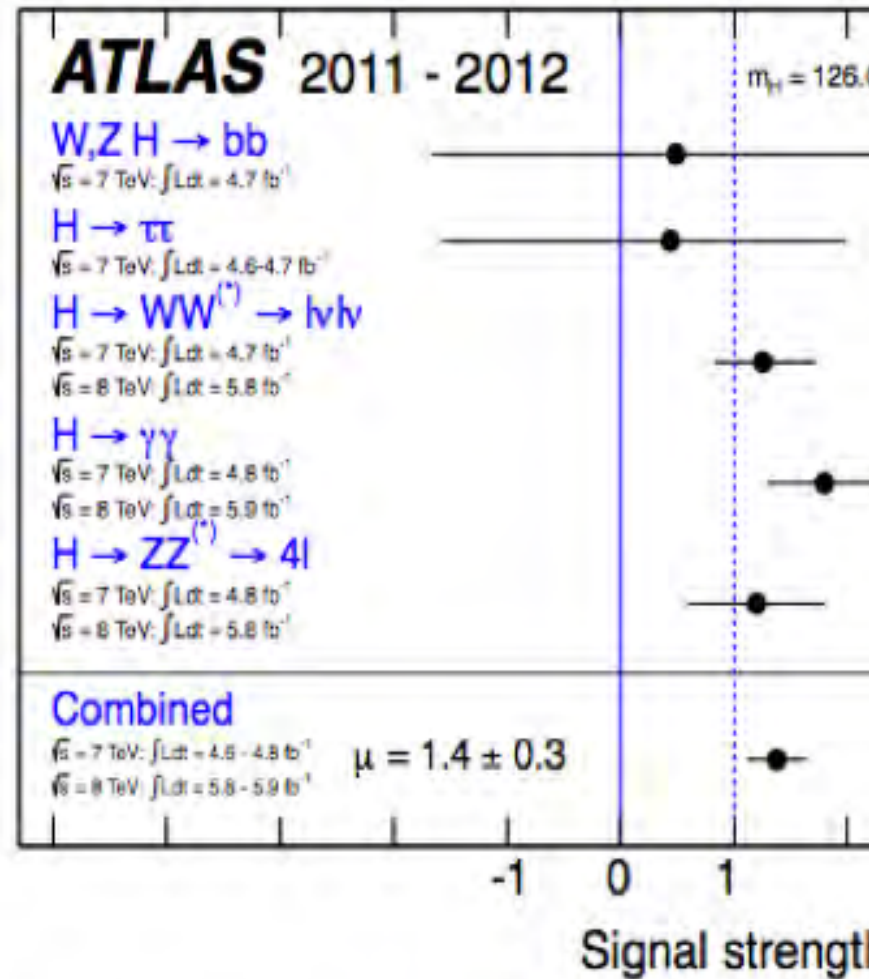
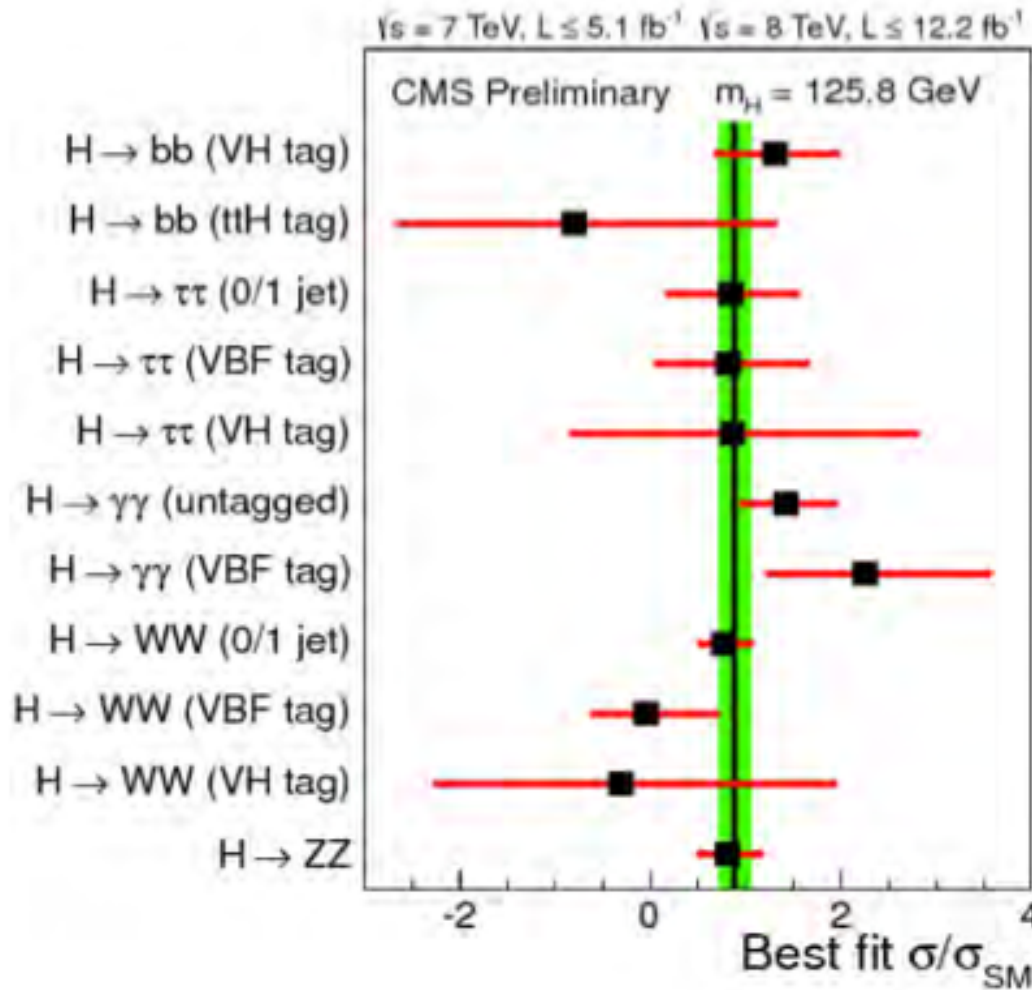
- The discovery of the Higgs is a success of the SM, and also demanding a detailed knowledge of the properties of this particle.
- Various types of electron and muon colliders have been proposed for precision studies of the total and partial widths in the various decay channels.
- In the case of a Higgs factory through a muon collider, sizeable radiative effects - of order of 50% or larger - must be carefully taken into account for a precise measurement of the total and partial widths of the Higgs particle.

# The LHC discovery of the Higgs at 125 GeV

- ATLAS:  $m = 125.5 \pm 0.2$  (stat)  $\pm 0.6$  (sys) GeV
- CMS:  $m = 125.8 \pm 0.4$  (stat)  $\pm 0.4$  (sys) GeV

- CMS and Atlas have observed a narrow line of high significance at about 125 GeV mass, compatible with the Standard Model Higgs boson.
  - Their data are consistent with fermionic and bosonic couplings expected from a SM Higgs particle. Searches have been performed in several decay modes.
  - Experimental energy resolutions have been so far much wider of the expected intrinsic Higgs width of about 4 MeV.
  - ATLAS and CMS and also CDF also exclude other SM Higgs bosons up to approximately 600 GeV.

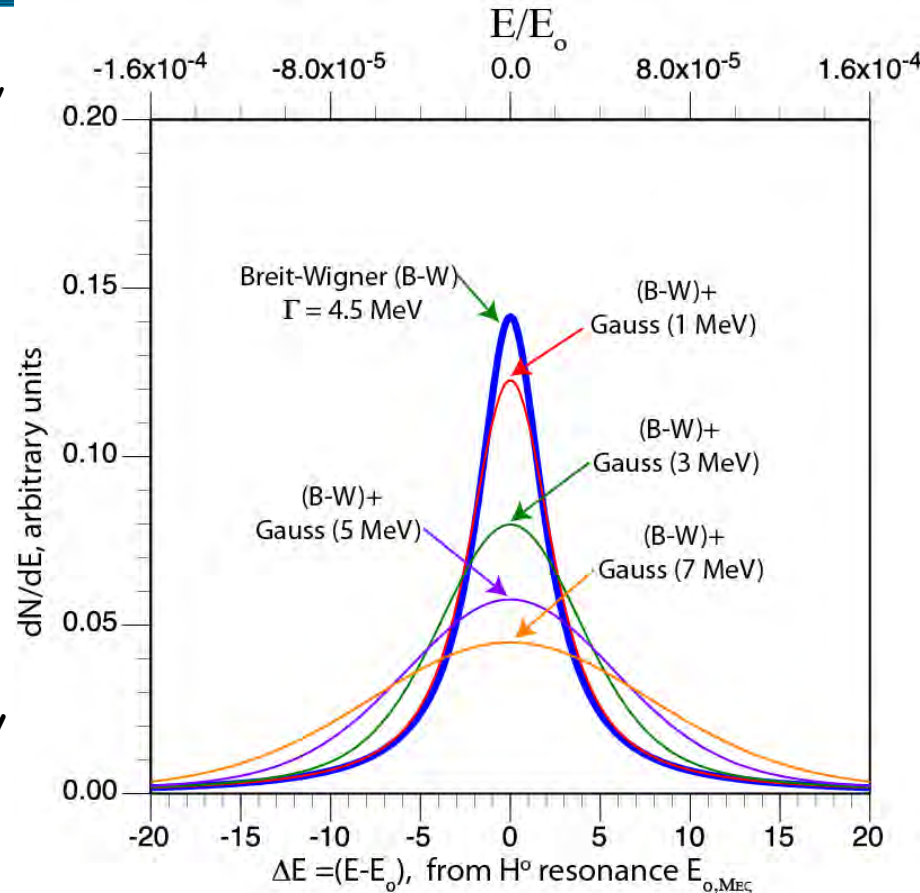
# All Higgs results



- From the available data it cannot be concluded yet that we have found the SM Higgs and not one of the scalars postulated within the possible extensions of the SM.
- Therefore a detailed study of the properties of this particle is highly required.
- In particular the Higgs width's measurement is essential to determine the partial widths and couplings to fermions and bosons.

## The Higgs width according to the Standard Model

- Like in the case of the  $Z_0$ , the determination of the  $H_0$  width will be crucial in the determination of the nature of the particle and the underlying theory
- Cross section is shown here, convoluted with a Gaussian beam distribution.
- Signal is not affected only if the rms beam energy width is  $\leq$  a few MeV.



*4.5 MeV width: A very demanding resolution  $R \approx 0.003\%$  is required*

Venice, March 2015

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C. Rubbia, Venice, March 2015

## The need of a better precision

- What precision is needed in order to search for possible additional deviations from the SM, even under the assumption that there is no other additional "Higgs" state at the LHC ?
- Predicted ultimate LHC accuracies for "exotic" alternatives

<i>R.S. Gupta et al.</i>	$\Delta hVV$	$\Delta htt$	$\Delta hbb$
Mixed-in Singlet	6%	6%	6%
Composite Higgs	8%	tens of %	tens of %
Minimal Supersymmetry	< 1%	3%	10% <sup>a</sup> ,
LHC 14 TeV, 3 ab <sup>-1</sup>	8%	10%	15%

*Ultimate at LHC*  
*1 ab = 10<sup>-42</sup> cm<sup>2</sup>*

$$\frac{g_{hbb}}{g_{SMbb}} = \frac{g_{h\tau\tau}}{g_{SM\tau\tau}} \simeq 1 + 1.7\% \left( \frac{1 \text{ TeV}}{m_A} \right)^4$$

*SUSY tan(β) > 5*

$$\frac{g_{hff}}{g_{SMff}} = \frac{g_{hVV}}{g_{SMVV}} \simeq 1 - 3\% \left( \frac{1 \text{ TeV}}{f} \right)^2$$

*Composite Higgs*

$$\frac{g_{hgg}}{g_{SMgg}} \simeq 1 + 2.9\% \left( \frac{1 \text{ TeV}}{m_T} \right)^2, \quad \frac{g_{h\gamma\gamma}}{g_{SM\gamma\gamma}} \simeq 1 - 0.8\% \left( \frac{1 \text{ TeV}}{m_T} \right)^2$$

*Top partners*

- Sensitivity to "TeV" new physics for "5 sigma" discoveries may need 1 per-cent to sub 1-per-cent  $\sigma$  accuracies on rates.

Venice, March. 2015

*arXiv:1206.3560v3 [hep-ph] 27 Sep 2012*

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# The quest for Higgs Factories

- Two possible future alternatives:

- A  $e^+e^-$  collider at  $L > 10^{34}$  and a  $Z+H_0$  signal of  $\approx 200$  fb. The circumference of a new, LEP-like ring is of about  $\approx 80$  km or of a Linear Collider of 31 km.
- A  $\mu^+\mu^-$  collider at  $L > 10^{32}$  and a  $H_0$  signal in the  $s$ -state of  $\approx 20'000$  fb. The collider radius is much smaller, only  $\approx 50$  m, but the novel “muon cooling” facility is required.

MICE

“muon cooling”:

C. Rubbia, “A complete demonstrator of a muon cooled Higgs factory”, [arXiv:1308.6612](https://arxiv.org/abs/1308.6612) . Also Venice and Cern, 2015

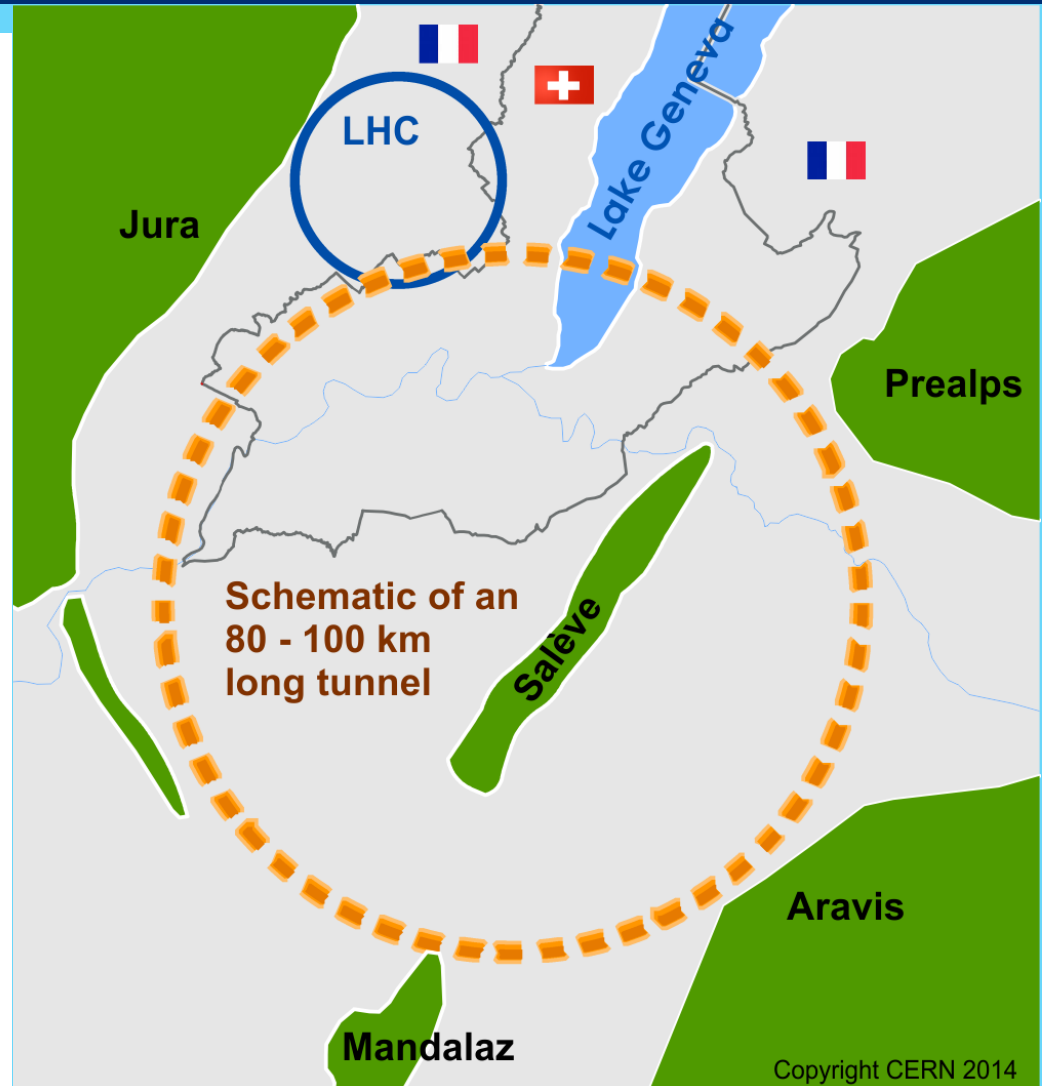


# Future Circular Collider Study - SCOPE

## CDR and cost review for the next ESU (2018)

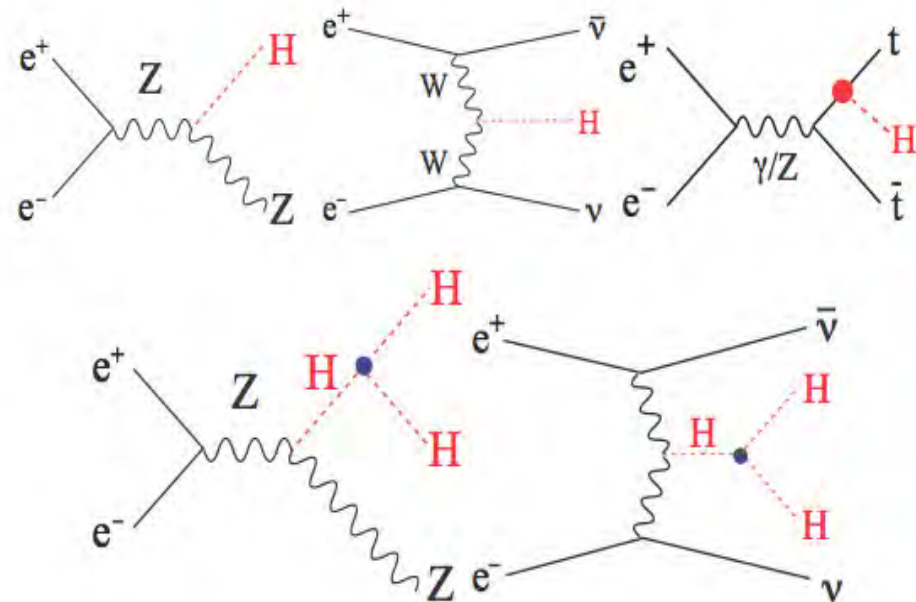
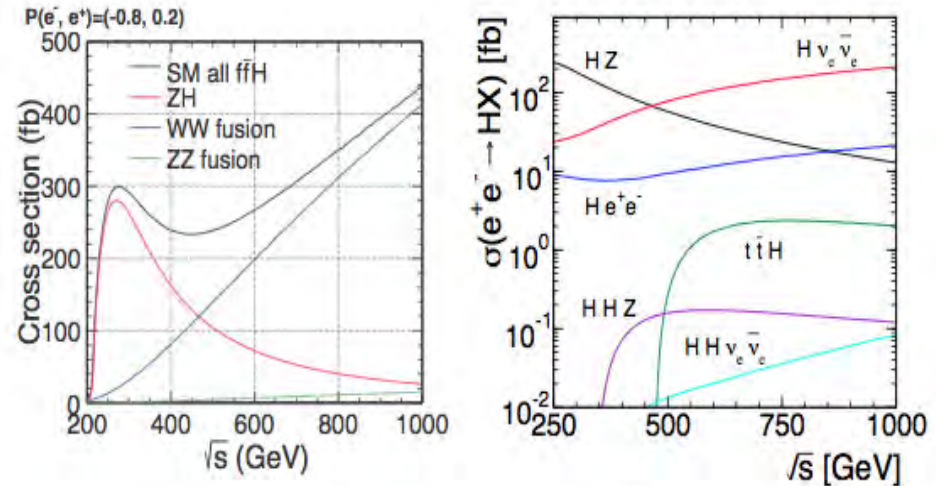
Form an international collaboration to study:

- $pp$ -collider (*FCC-hh*)  
→ defining infrastructure requirements
- $e^+e^-$  collider (*FCC-ee*) as potential intermediate step  
→ Study Z, W, H, top
- $p-e$  (*FCC-he*) option
- 80-100 km infrastructure in Geneva area.
- CEPC-SppC in China



# Production cross sections at the $e^+ e^-$ collider

- The production cross sections of the Higgs boson with the mass of 125 GeV for  $e^+e^-$  as a function of the energy  $\sqrt{s}$ .
- The cross sections of the production processes as a function of the  $\sqrt{s}$  collision energy.
- The Higgs-strahlung diagram (Left), the W-boson fusion process (Middle) and the top-quark association (Right).
- Double Higgs boson diagrams via off-shell Higgs-strahlung (Left) and W-boson fusion (Right) processes



## The second option: a $\mu^+\mu^-$ collider ?

- The direct  $H^0$  cross section is greatly enhanced in a  $\mu^+\mu^-$  collider when compared to an  $e^+e^-$  collider, since the  $s$ -channel coupling to a scalar is proportional to the lepton mass.
- Like in the well known case of the  $Z^0$  production, the  $H^0$  scalar production in the  $s$ -state offers conditions of unique cleanliness .
- An unique feature of such process — if of an appropriate luminosity — is that its actual mass, its very narrow width and most decay channels may be directly measured with accuracy.
- Therefore the properties of the Higgs boson can be detailed over a larger fraction of model parameter space than at any other proposed accelerator method.
- A particularly important conclusion is that it will have greater potentials for distinguishing between a standard SM and the SM-like  $H_0$  of SUSY or of other than any other collider.

*Venice, March. 2015*

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The realization of a cooling demonstrator (C. Rubbia) is essential.  
At Cern? Elsewhere?

# Radiative effects

- In the case of a Higgs factory through a muon collider, sizeable QED radiative effects - of order of 50% - must be carefully taken into account for a precise measurement of the leptonic and total widths of the Higgs particle.
- Those effects do not apply in the case of Higgs production in electron-positron colliders.
- Effects similar to J/Psi, Z, ... production in e+e- annihilation.

# More details

- Correction factor  $\propto (\Gamma/M)^{(4\alpha/\pi) \log(2E/m)}$   
modifies the lowest order cross section o(50%).

- By defining: 
$$\beta_i = \frac{4\alpha}{\pi} \left[ \log \frac{W}{m_i} - \frac{1}{2} \right], \quad \begin{aligned} y &= W - M \\ \tan \delta_R(W) &= \frac{1}{2} \Gamma / (-y) \end{aligned}$$

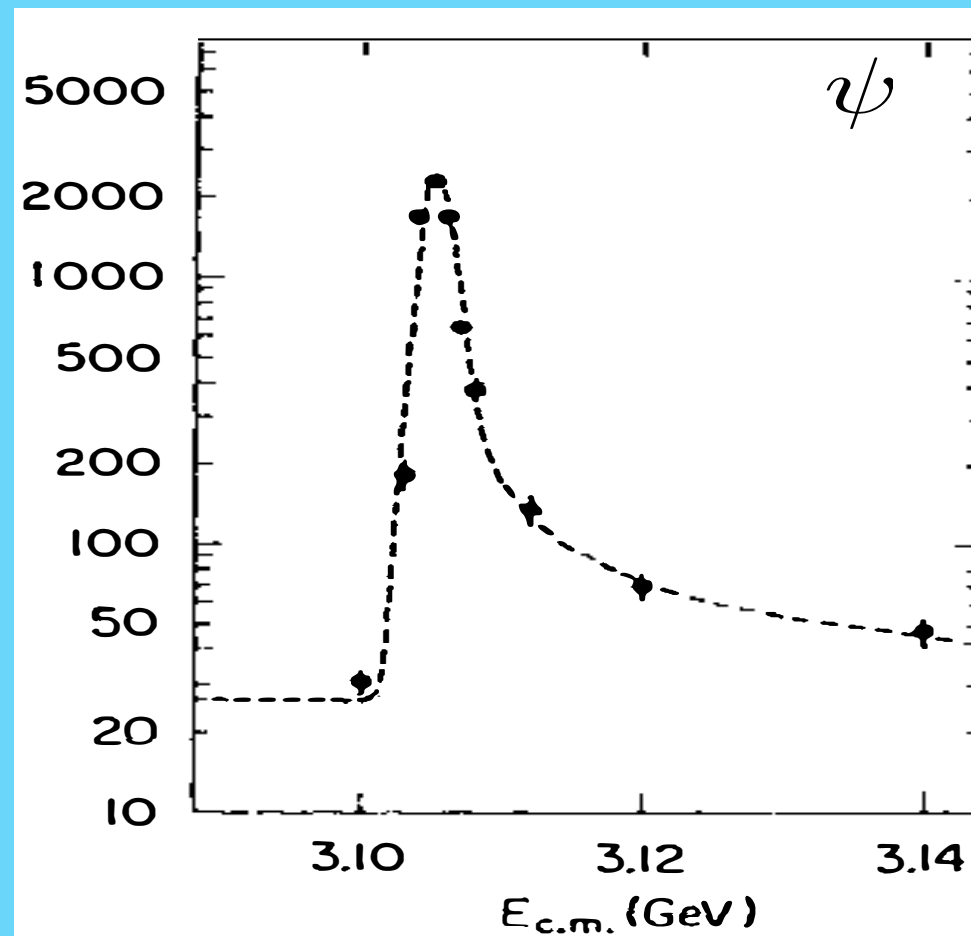
Infrared factor modifies  
Born cross section as:

M.G., Pancheri, Srivastava, Nucl. Phys. B101, 1975  
and B171, 1980.

$$C_{infrac}^{res} = \left( \frac{y^2 + (\Gamma/2)^2}{(M/2)^2} \right)^{\beta_i/2} \left[ 1 + \beta_i \frac{y}{\Gamma/2} \delta_R \right]$$

- At  $W=2E=M_{\text{Higgs}}$ ,  $\beta_i = 0.061$   $C_{\text{infra}}^{\text{res}} = (\Gamma/M)^{\beta_i} = 0.53$ ,

The situation is very similar to J/Psi production in e+e- annih.  
a part from the background.



- Since the resonance is quite narrow, one has to integrate over the machine resolution

$$G(W' - W) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(W' - W)^2 / (2\sigma^2)}$$

$$\tilde{\sigma}(W) = \int G(W' - W) dW' \sigma(W')$$

- Then the observed cross section at the peak is, to o(1%) accuracy:

$$\tilde{\sigma}(M) = \frac{2\pi^2 \Gamma_i \Gamma_f}{\sqrt{2\pi} \sigma M^2 \Gamma} \left( \frac{\Gamma}{M} \right)^{\beta_i} e^{\left( \frac{\Gamma}{2\sqrt{2}\sigma} \right)^2} \left\{ \operatorname{erfcf} \left( \frac{\Gamma}{2\sqrt{2}\sigma} \right) + \frac{1}{2} \beta_i E_1 \left( \frac{\Gamma^2}{8\sigma^2} \right) \right\}$$

-> Numerical results for Higgs. The correction factor C is:

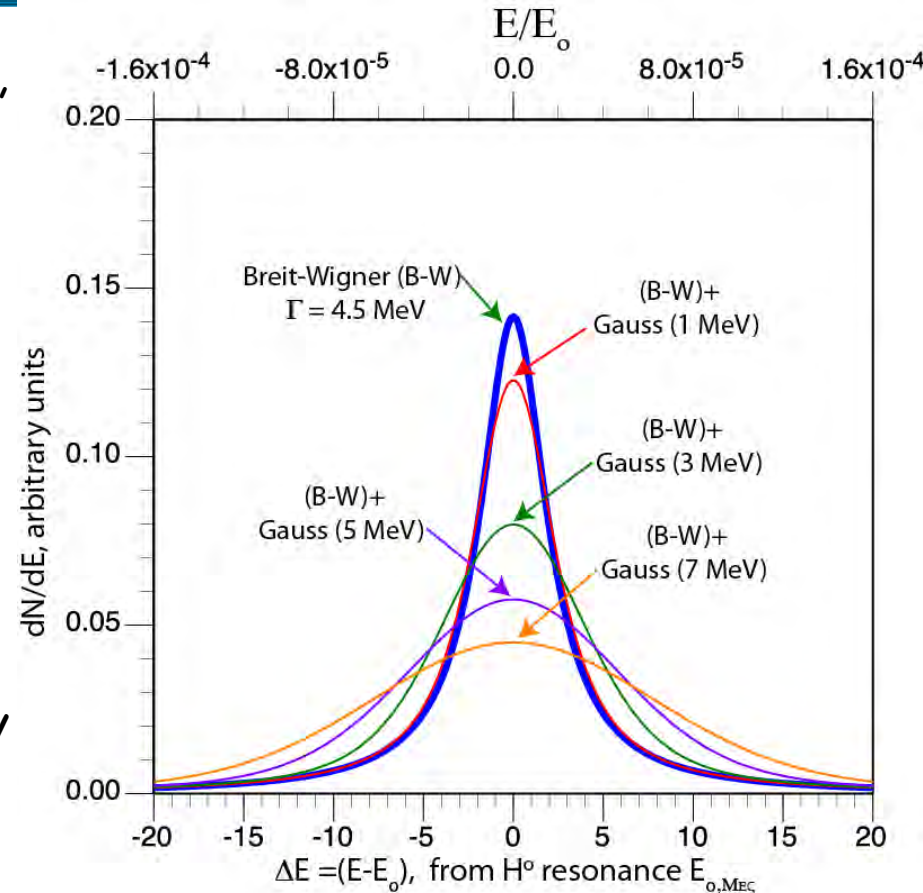
$$C = 0.47, \quad 0.37, \quad 0.30, \quad 0.20$$

$$\sigma = 1 \text{ MeV}, 2 \text{ MeV}, 3 \text{ MeV}, 4 \text{ MeV},$$

-> Important corrections to the Born Higgs signal.

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-> Ratio Signal/Background affected as a function of beams spread.

## Signal/Background studies

- T. Han and Z. Liu (arXiv:1210.7803v2)

R (%)	$\mu^+ \mu^- \rightarrow h$ $\sigma_{\text{eff}}$ (pb)	$h \rightarrow b\bar{b}$		$h \rightarrow WW^*$	
		$\sigma_{\text{Sig}}$	$\sigma_{\text{Bkg}}$	$\sigma_{\text{Sig}}$	$\sigma_{\text{Bkg}}$
0.01	16	7.6	15	3.7	0.051
0.003	38	18		5.5	

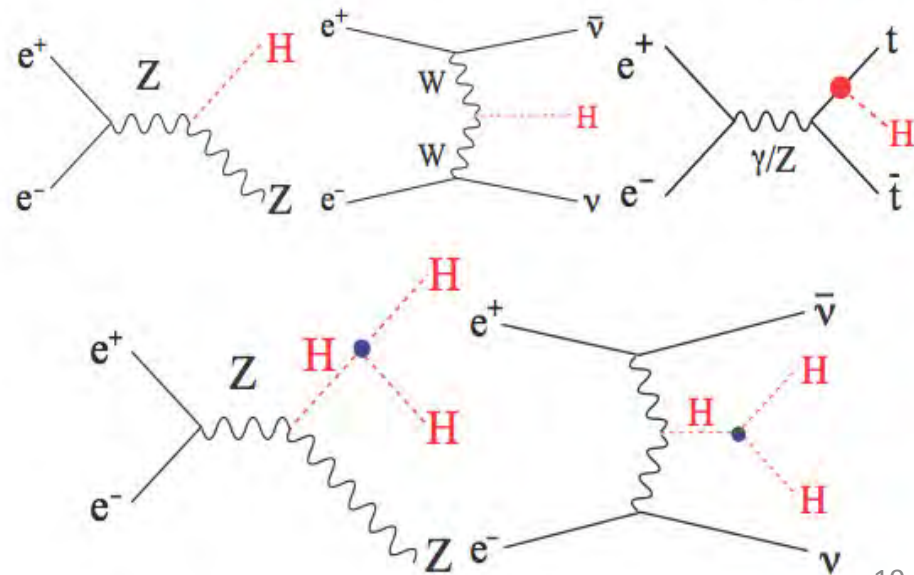
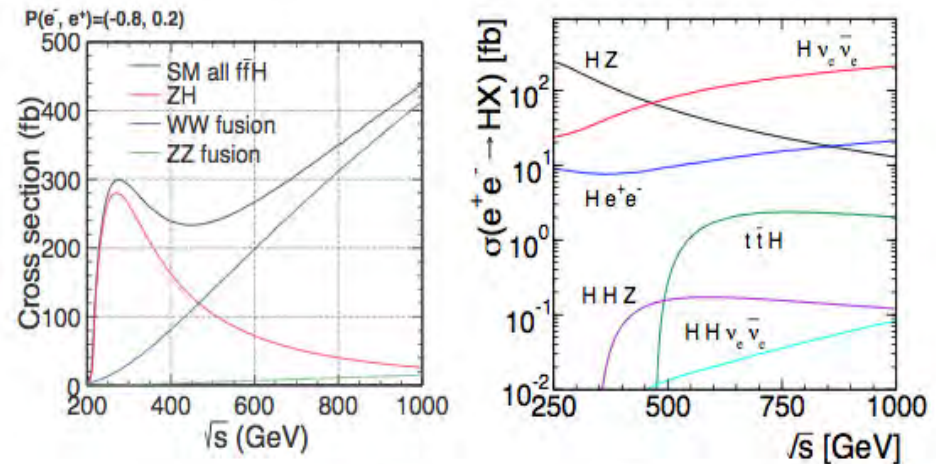
Effective cross sections (in pb) at the resonance for two choices of beam energy resolutions R and two leading decay channels, with the SM branching fractions. No radiative effects included.

→ Further work is needed.

# - No similar effects for e+e- colliders

## Production cross sections at the e+ e- collider

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# Conclusions

- Precision studies of the properties of the Higgs are mandatory.
- Various proposals of electron and muon colliders have been put forward.
- Muon colliders seem more appropriate for measuring the Higgs width and couplings. Sizeable radiative effects – of order 50% or larger – must be carefully taken into account for precision measurements.

Thank you !