



# Elastic scattering and total cross section in ATLAS

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# Outline

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- Principle of the measurement
- The ALFA detector
- Luminosity and total cross section determination
- Precision of the measurement

- The **ALFA** detector is designed to perform an absolute measurement of the **luminosity** at the interaction point of ATLAS and the **total cross section** with a precision of a few percent using **elastic scattering**
- This measurement will allow the **calibration** of all the detectors which response scales with the luminosity and especially the LUCID detector that will provide a bunch per bunch luminosity determination during the data taking of ATLAS
- Measuring the differential elastic cross section as a function of the 4-momentum transfer squared  $t$  will also provide a precise measurement of the **nuclear slope  $B$**  and the **ratio of the real over the imaginary part of the forward elastic scattering amplitude  $\rho$**

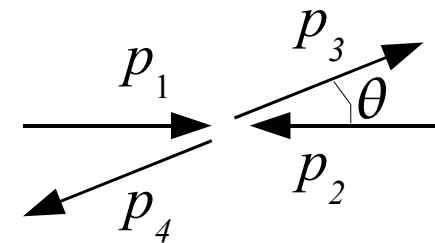
# Principle of the measurement

- The rate of elastic scattering is linked to the total interaction rate through the **optical theorem**, which states that the total cross section is directly proportional to the imaginary part of the nuclear forward elastic scattering amplitude extrapolated to zero momentum transfer:

$$\sigma_{tot} = 4\pi \cdot \Im [F_{el}(t=0)]$$

where at small values of  $t$ :

$$-t = (p_1 - p_3)^2 \approx (p\theta)^2$$



The differential elastic cross section is linked to the luminosity through the number of event as a function of the  $t$ -value  $N_{el}$ :

$$\frac{dN_{el}}{dt} = \mathcal{L} \frac{d\sigma_{el}}{dt}$$

# Principle of the measurement

- At small  $t$ -values the differential elastic cross section can be written as:

$$\frac{d N_{el}}{dt} = \mathcal{L} \frac{d \sigma_{el}}{dt} = \mathcal{L} |F_c + F_n|^2 = \mathcal{L} \left( \frac{d \sigma_c}{dt} + \frac{d \sigma_{cn}}{dt} + \frac{d \sigma_n}{dt} \right)$$

- Pure coulombian term:

$$\frac{d \sigma_c}{dt} = \frac{4 \pi \alpha^2 (\hbar c)^2 G(t)^4}{|t^2|}$$

with  $G(t) = \left(1 + \frac{|t|}{0.71}\right)^{-2}$  Proton electromagnetic form factor

- Pure nuclear term:

$$\frac{d \sigma_n}{dt} = \frac{\sigma_{tot}^2 (1 + \rho)^2}{16 \pi (\hbar c)^2} \exp(-B|t|)$$

Phase of the Coulomb amplitude relative to the nuclear amplitude

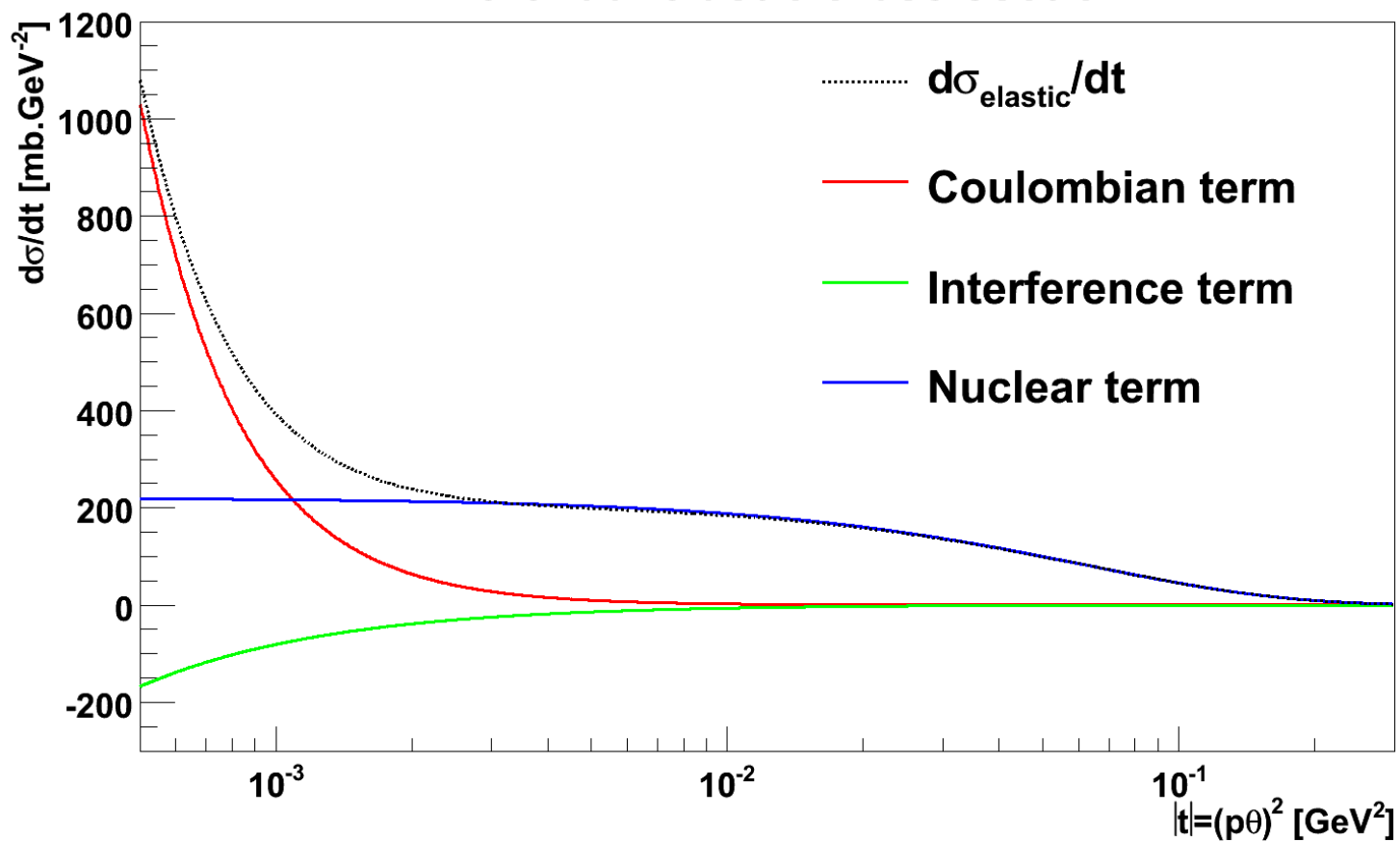
- Interference term:

$$\frac{d \sigma_{cn}}{dt} = - \frac{\sigma_{tot} \alpha (\rho - \alpha \phi(t)) G(t)^2}{|t|} \exp(-B|t|/2) \quad \text{with } \phi(t) = \ln\left(\frac{2}{B|t|}\right) - \gamma$$

# Principle of the measurement

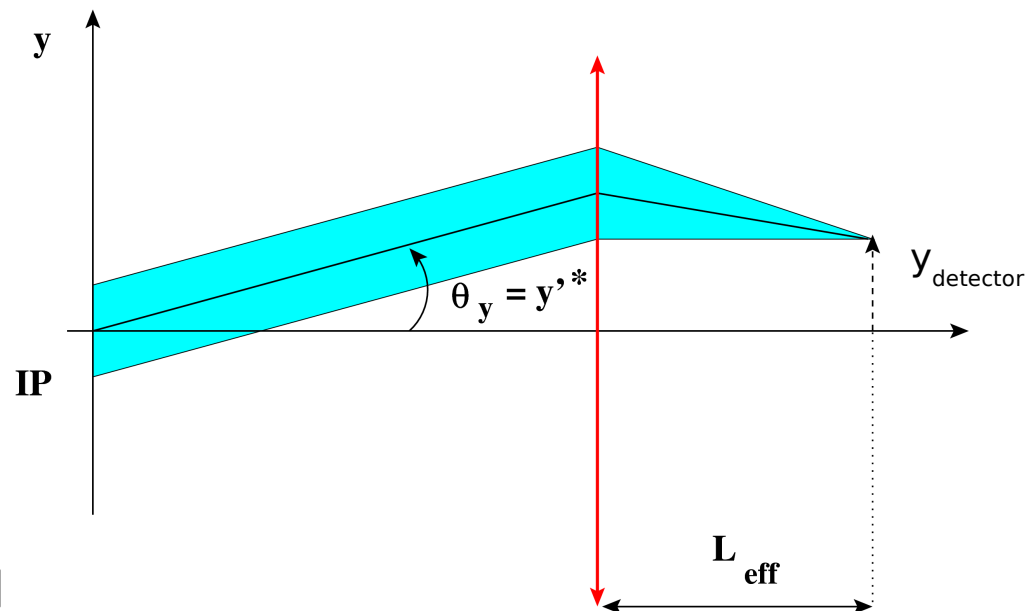
$$\sigma_{tot} = 100 \text{ mb}, \quad B = 18 \text{ GeV}^{-2}, \quad \rho = 0.13$$

## Differential elastic cross section



# Principle of the measurement

- To obtain the 2-3 % absolute precision we must approach the coulombian region as close as possible which implies a dedicated run
- Low luminosity runs  $10^{27} \text{ cm}^{-2} \cdot \text{s}^{-1}$  (43 bunches of  $10^{10}$  particles)
- Dedicated optics:
  - No crossing angle
  - High  $\beta^*$  of 2625 m to minimize the angular divergence
  - Parallel-to-point focusing with  $90^\circ$  phase advance in the vertical plane to focus particles with the same scattering angle at the same vertical position in the detector



# Principle of the measurement

- The minimum  $t$  achievable is given by an unscattered particle in the horizontal plane and with the minimum scattering angle interceptable in the vertical one:

$$\theta_{IP,y} = \frac{y}{\sqrt{\beta \beta_{IP}}} \quad \longrightarrow \quad -t_{min} = (p \theta_{min})^2 = \frac{p^2 y_{min}^2}{\beta \beta_{IP}}$$

With  $y_{min} = n_{min} \sigma_y = n_{min} \sqrt{\epsilon \beta}$

We obtain the following formula:

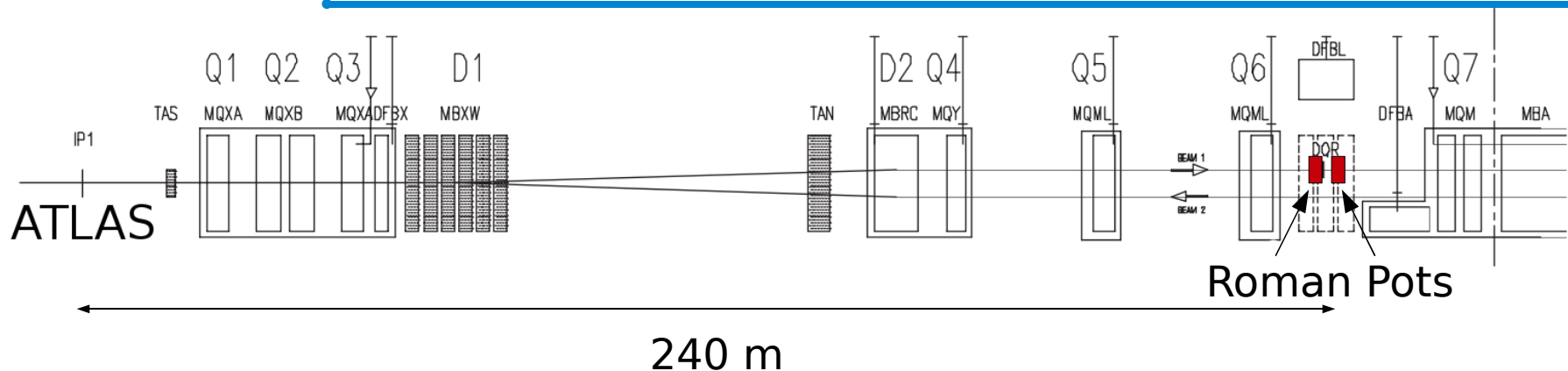
$$-t_{min} = p^2 n_{min}^2 \frac{\epsilon}{\beta_{IP}}$$

$$\left. \begin{array}{l} \epsilon_N = 1 \mu mrad \\ n_{min} = 12 \\ p = 7 TeV \end{array} \right\}$$

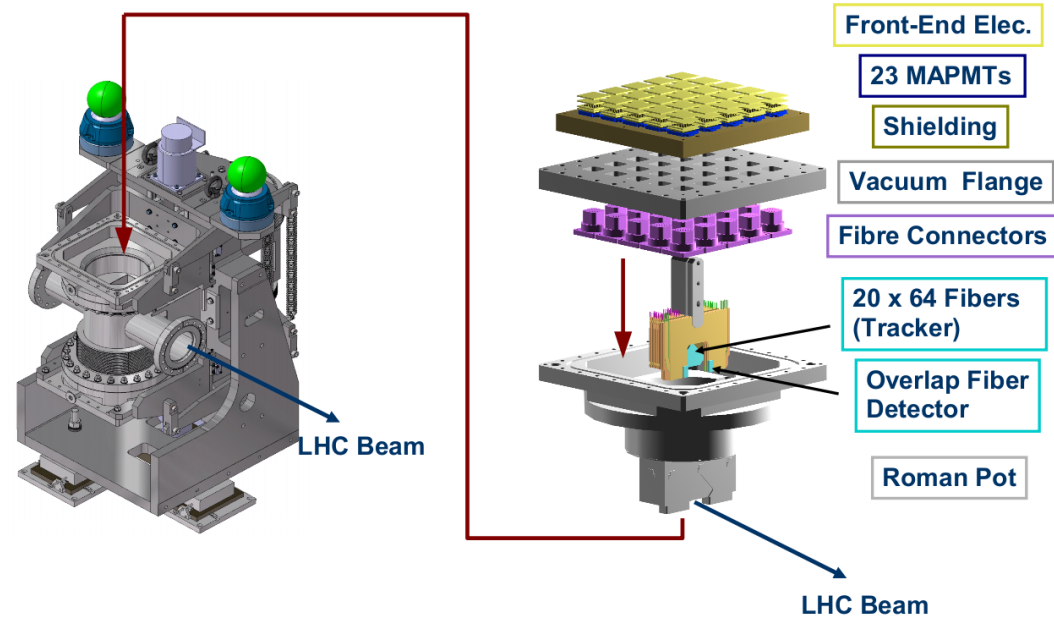
$$t_{min} = 3.7 \cdot 10^{-4} GeV^2 \equiv \theta_{IP,y} = 3 \mu rad$$



# The ALFA Detector



- **ALFA**  $\equiv$  **A**bsolute **L**uminosity **F**or **A**TLAS
- Two roman pot stations in the forward direction on each side of the interaction point of ATLAS. Each station contains an upper and a lower detector.
- Each detector is made of a 20x64 scintillating fibers tracker readout by a 64 channels MAPMT. The compact front end electronics is mounted on top of the MAPMT.



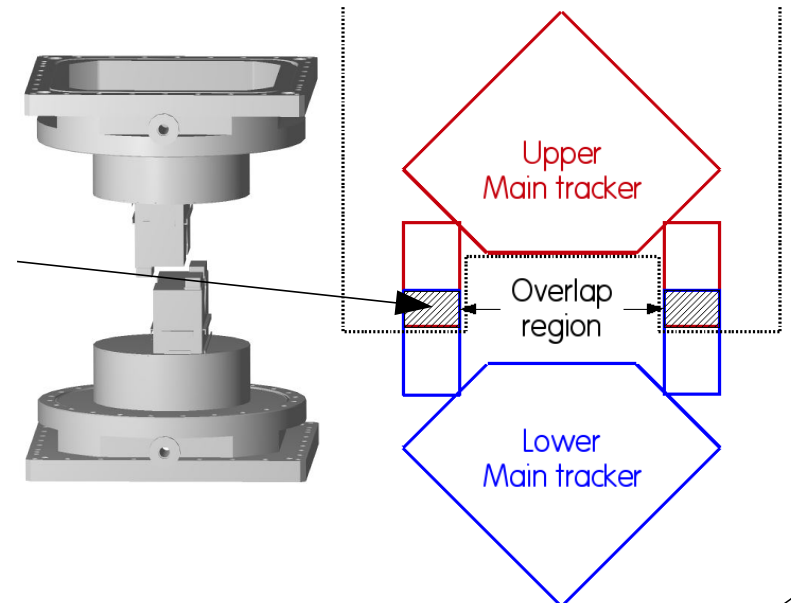
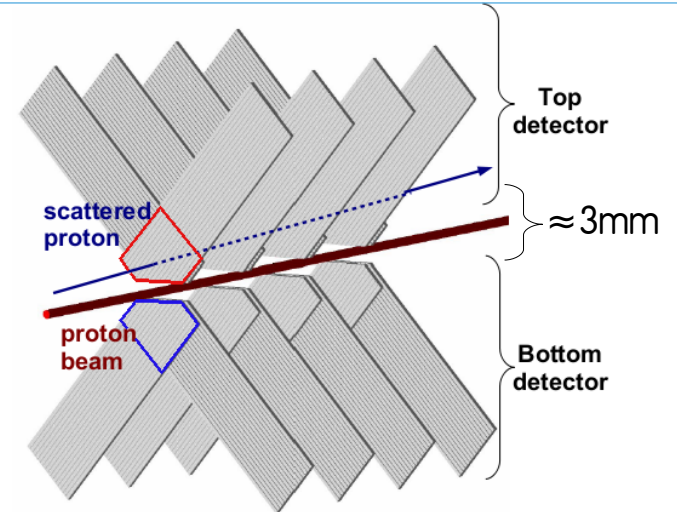
# The ALFA Detector

- **The tracker:**

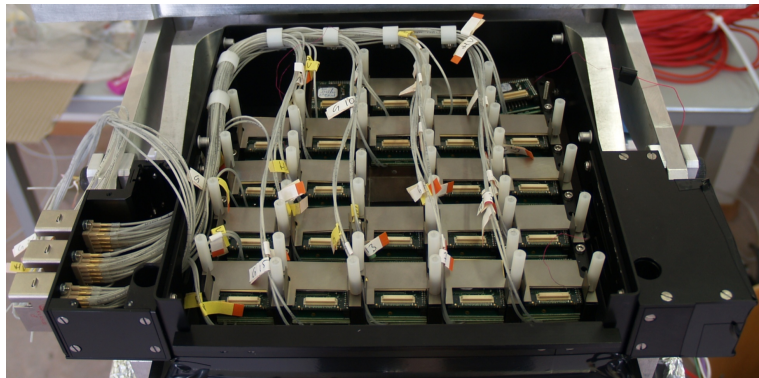
- 500  $\mu\text{m}$  width squared scintillating fibers
- 70  $\mu\text{m}$  staggering between consecutive layers
- $\rightarrow$  30  $\mu\text{m}$  resolution in x and y

- **The overlap detectors:**

- In order to determine the  $t$ -scale, we must know very precisely the relative position between the lower and the upper detectors
- The overlap detectors are meant to measure this distance with a precision up to 10  $\mu\text{m}$
- Mechanically fixed to the main tracker these detectors (3x30 horizontal scintillating fiber tracker) overlap when the lower and the upper parts are brought to data taking position



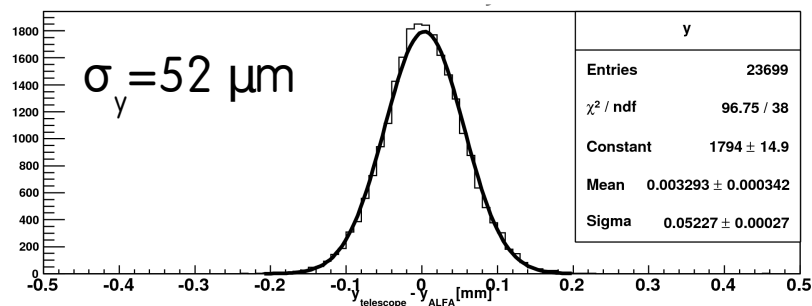
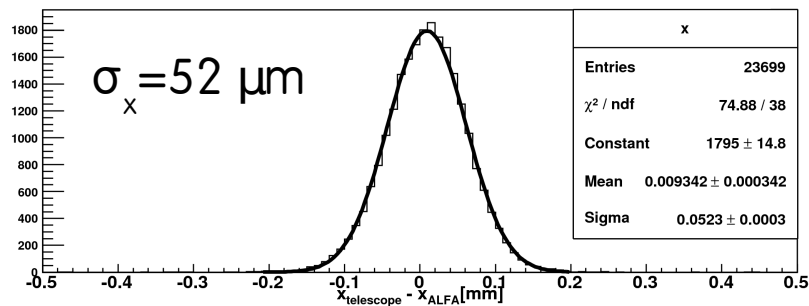
# The ALFA Detector



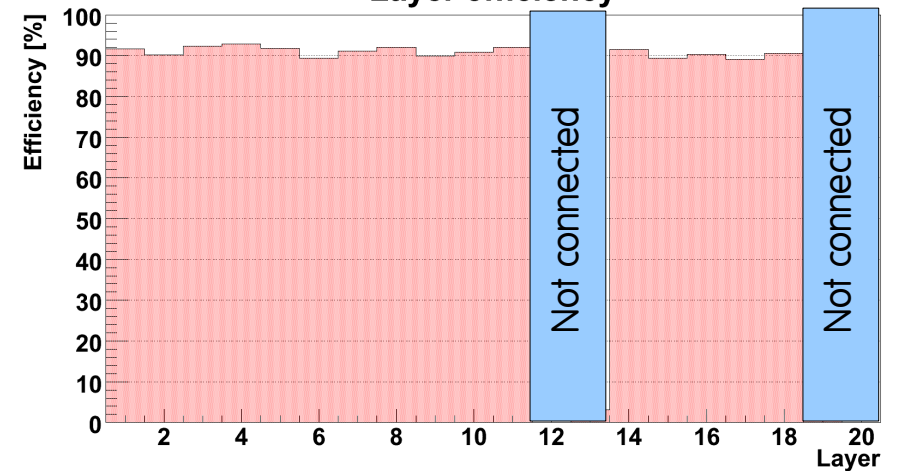
August 2008  
Test-Beam results  
180 GeV Pions



Resolution for half a detector

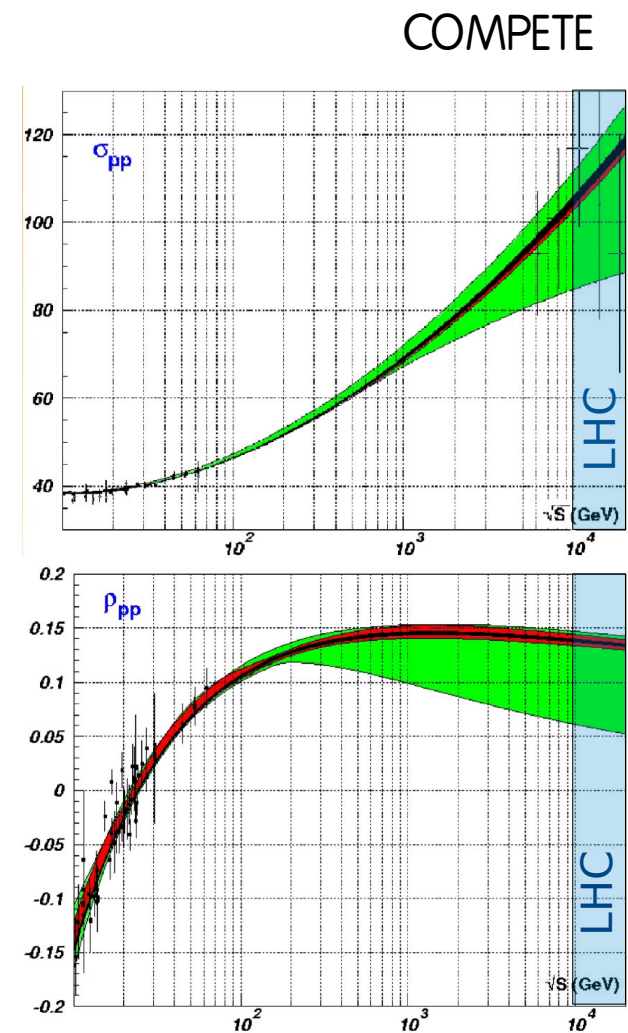


Layer efficiency



# Measurement procedure

- The overall acceptance (optics and detector) cannot be determined empirically. It has to be done using a full simulation.
- We use a three steps simulation:
  - Generation using Pythia 6.4 or 8.1
    - Generation range:  $4 \cdot 10^{-5} \leq -t \leq 0.3 \text{ GeV}^2$
    - $\sigma_{tot} = 100 \text{ mb}$ ,  $\rho = 0.13$  (From COMPETE<sup>1</sup>) and  $B = 18 \text{ GeV}^{-2}$
  - Transport using MAD-X thintrack
  - Reconstruction of the  $t$ -spectrum
- This will allow to correct the detected spectrum including all systematic effects.

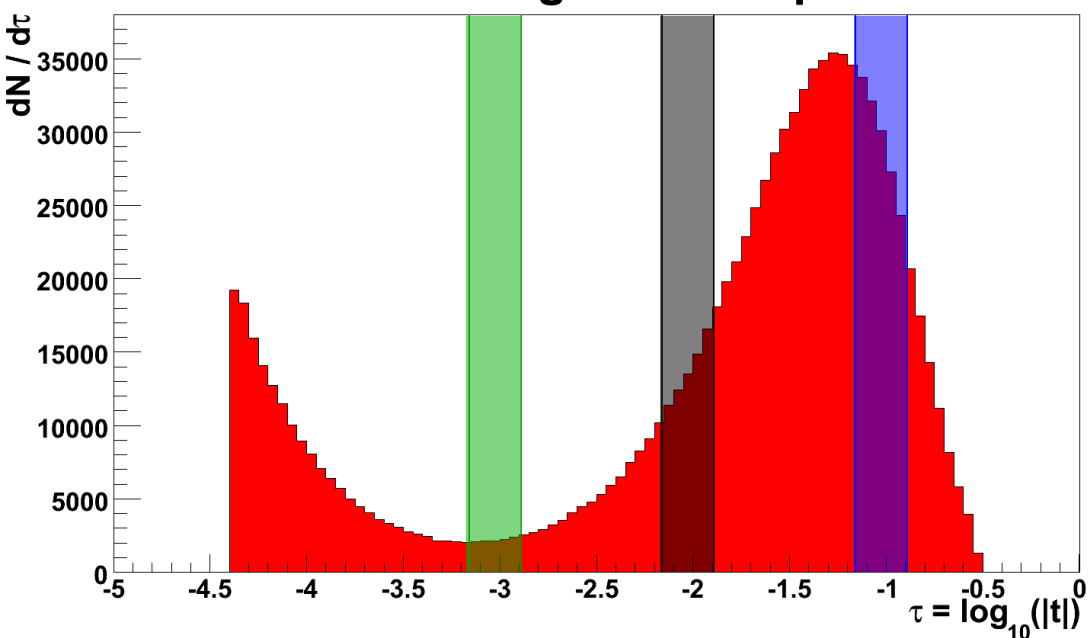


<sup>1</sup>Cudell JR, Ezhela VV, Gauron P, Kang K, Kuyanov YV, Lugovsky SB, et al. Benchmarks for the forward observables at RHIC, the Tevatron-run II, and the LHC. Physical review letters. 2002 Nov

# Measurement procedure

Example with 1M events

Generated logarithmic spectrum

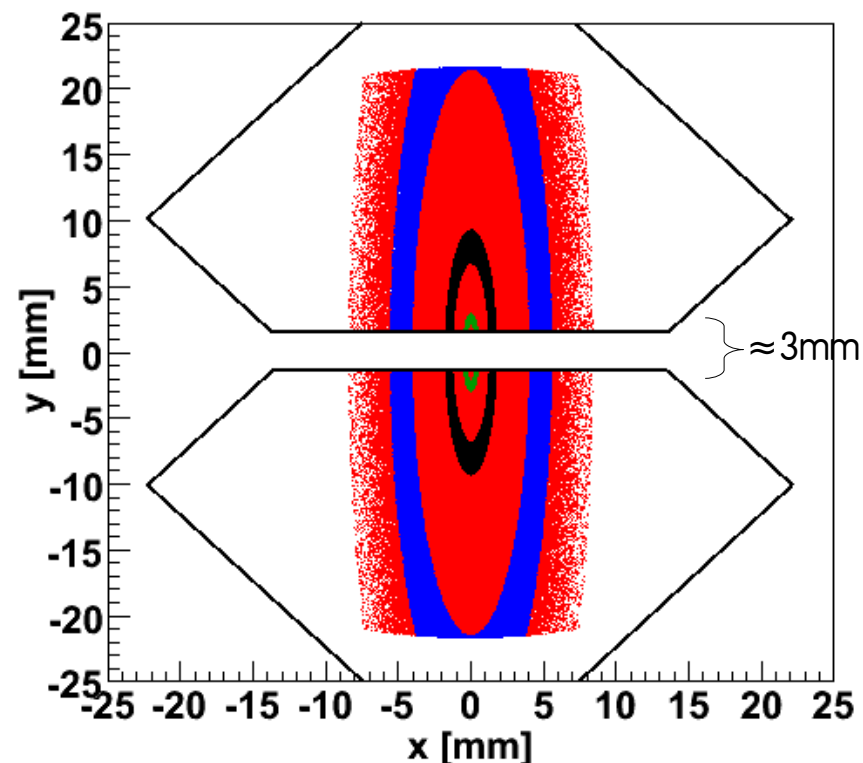


$$0.0007 < -t < 0.0013 \text{ GeV}^2$$

$$0.007 < -t < 0.013 \text{ GeV}^2$$

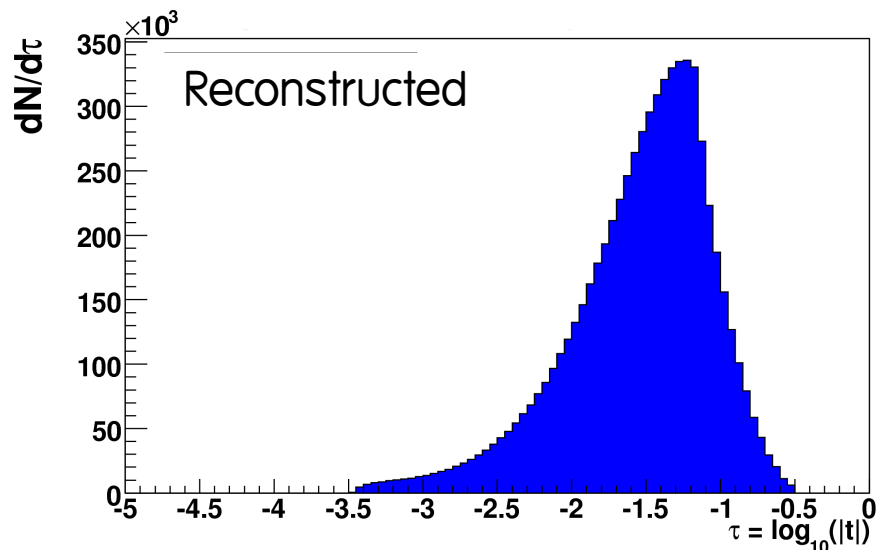
$$0.07 < -t < 0.13 \text{ GeV}^2$$

Scattering picture at the roman pot

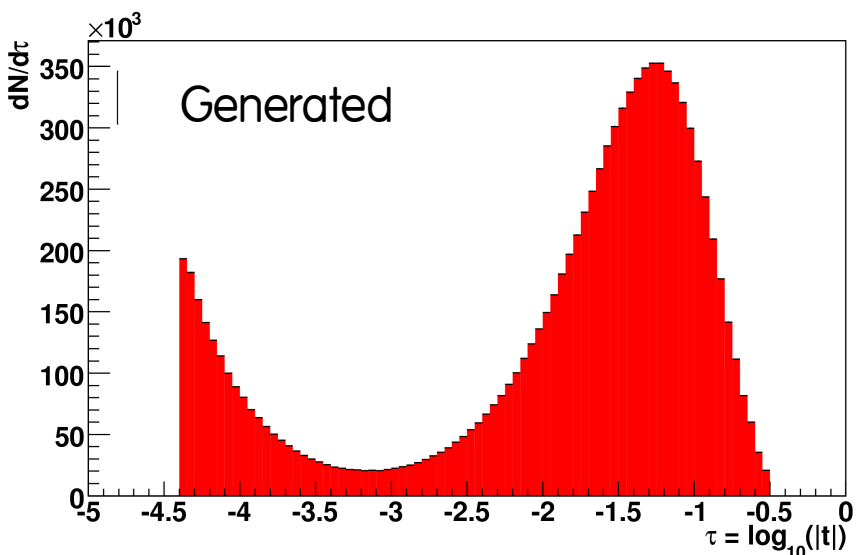
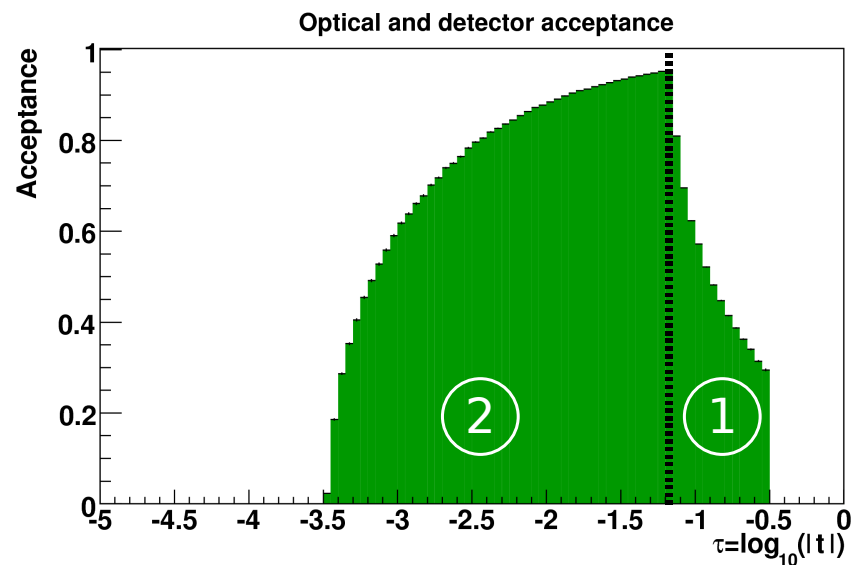




# Measurement procedure



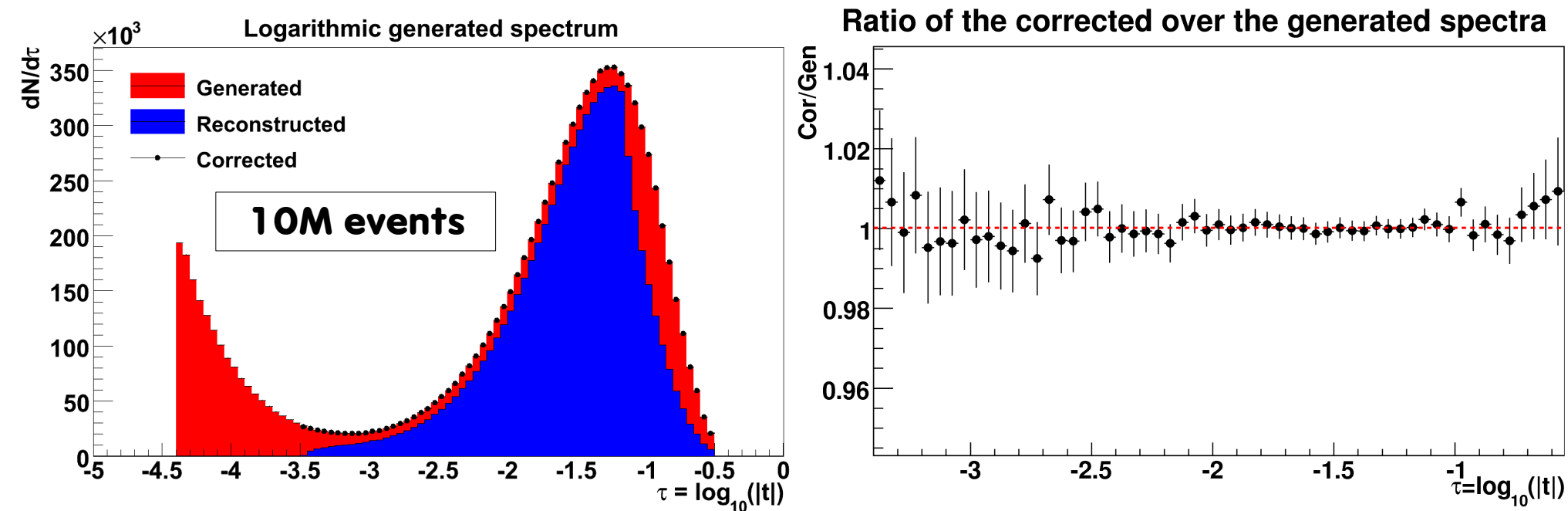
Example with 10M events  
Acceptance = 67 %



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1- Losses due to accelerator acceptance  
(Magnet aperture)  
2- Losses due to detector acceptance (Effect  
of the distance to the beam center)

# Measurement procedure



The luminosity, the total cross section,  $B$  and  $\rho$  are determined by fitting the corrected spectrum represented by the black dots on the left plot. Being at  $12\sigma$  from the center of the beam does not allow to measure the pure coulomb contribution.

# Precision of the measurement

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All figures in brackets are the systematic uncertainties obtained on the luminosity for 10M events

- Beam properties

- Nominal energy measurement (0.2 %)
- Angular divergence (0.3 %)
- Energy dispersion ( $< 1\text{‰}$ )
- Beam spread ( $< 1\text{‰}$ )
- Measurement of the optical parameters ( $\beta^*$ , phase advance...) (1.2 %)

- Detector properties

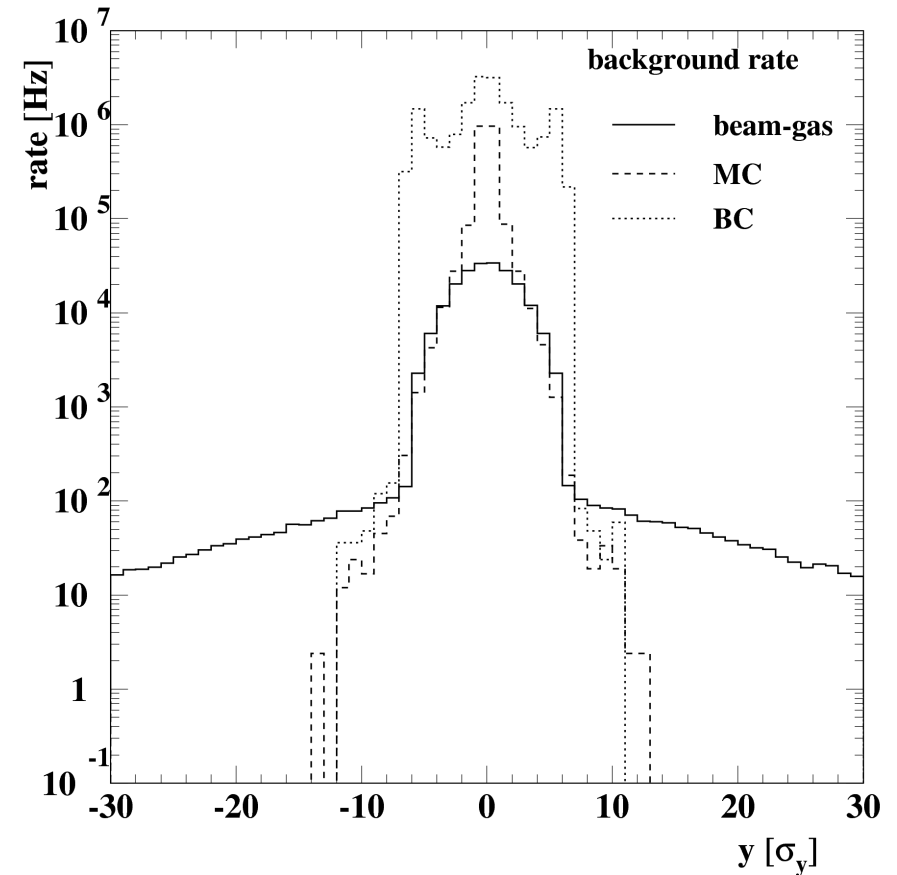
- Resolution (0.3 %)
- Detector alignment (1.3 %)
- Geometrical detector acceptance (0.5 %)



# Precision of the measurement

## Background

- Main sources:
  - Non elastic processes (e.g. Single Diffraction)
  - Halo events
    - Beam-gas
    - Momentum and betatron cleaning
  
- Tagging and subtraction:
  - Back to back topology
  - Acollinearity
  - Vertex reconstruction



# Precision of the measurement

## Summary

Nominal result for  $\int_{100\text{h}} \mathcal{L} = 3.6 \cdot 10^{32} \text{ cm}^{-2}$

	[%]
Beam properties	1.2
Detector properties	1.4
Background subtraction	1.1
Total uncertainty	2.1
Statistical error	1.8
Total	2.8

# Conclusion

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- All beam tests done so far have confirmed the detector behaviour and main parameters (layer efficiency, spatial resolution...)
- As a consequence, the final production and assembling is on going and all detectors should be calibrated and ready for next summer
- Extremely challenging measurement

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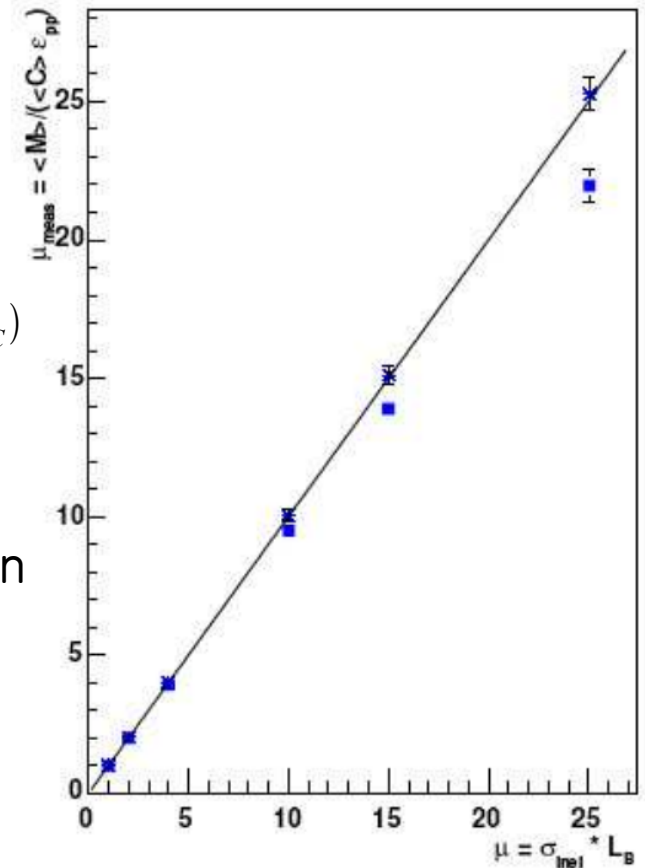
Thanks for your attention

# Backup

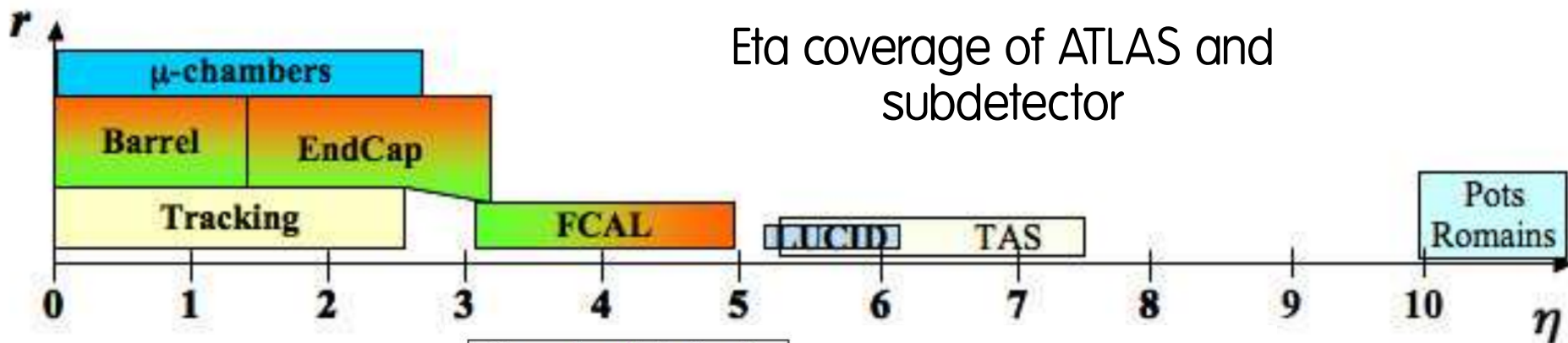
- LUCID (Luminosity measurement using Cerenkov Integrating Detector)
  - Inelastic events intercepted for  $5.5 \leq \eta \leq 6.1$
  - Rate of detected charged particle a luminosity
- Extrapolation of the low luminosity measurement thanks to a perfect linearity:

$$\dot{N} = (Nb \text{ pp interaction detected per bunch crossing } \mu_{LUCID}) \times (\text{Filling factor } f_{BC})$$

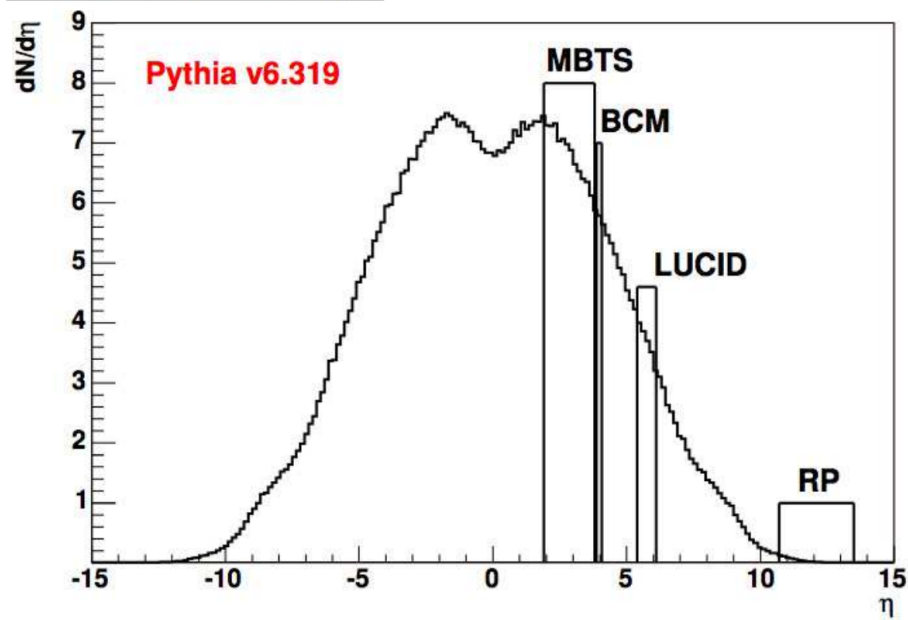
- $\mu_{LUCID}$  must be determined at each luminosity:
  - Low: Nb of bunch crossing without detection / with detection
  - Medium: Nb of tubes recording some signal
  - High: Nb of charged particle detected



# Backup



Charged particle density



# Backup

- Reconstruction method:

$$u = \sqrt{\beta/\beta^*} (\cos \phi + \alpha^* \sin \phi) u^* + \sqrt{\beta\beta^*}$$

$$u_L - u_R = 2\sqrt{\beta\beta^*} \sin \phi \cdot \theta_u^*$$

$$\theta_u^* = \frac{u_L - u_R}{2L_{\text{eff},u}} \quad \text{with} \quad L_{\text{eff},u} = \sqrt{(\beta\beta^*)} \sin \phi$$

If we consider the four RPs for the reconstruction it gives for the y axis:

$$\theta_{RP_{1,y}} = \frac{\frac{y_{RP_1}}{L_{\text{eff},1,y}} - \frac{y_{RP_3}}{L_{\text{eff},3,y}}}{2} \quad \theta_{RP_{2,y}} = \frac{\frac{y_{RP_2}}{L_{\text{eff},2,y}} - \frac{y_{RP_4}}{L_{\text{eff},4,y}}}{2}$$

And finally :

$$t_{\text{reconstructed}} = \frac{(\theta_x^2 + \theta_y^2) \times (7 \text{ TeV})^2}{4}$$

- Beam momentum calibration<sup>1</sup>:
  - Measurement of the central frequency

$$P = \frac{Ze}{2\pi} \oint B(s) ds = P_{dipole} + P_{quadrupole} + P_{other}$$

$$P_{dipole} = \frac{e}{2\pi} (BL)_d$$

$$P_{quadrupole} = -\frac{1}{\alpha} \frac{C - C_c}{C}$$

$$C_c = \frac{h\beta c}{f_{RF}^c}$$

$\alpha$  : momentum compaction factor  
 C: Actual orbit length  
 $C_c$ : Central orbit length

- Magnetic calibrations (Derive from magnetic calibration curves of the dipole)
- Energy calibration with ion beams

<sup>1</sup> J. Wenninger, Beam momentum calibration at the LHC, LHC project note 334 2004, Jan



# Backup

Ratio of the differential elastic cross section without the CNI contribution over the one with the CNI

