



13th International Conference on Elastic & Diffractive Scattering  
(13th "Blois Workshop")

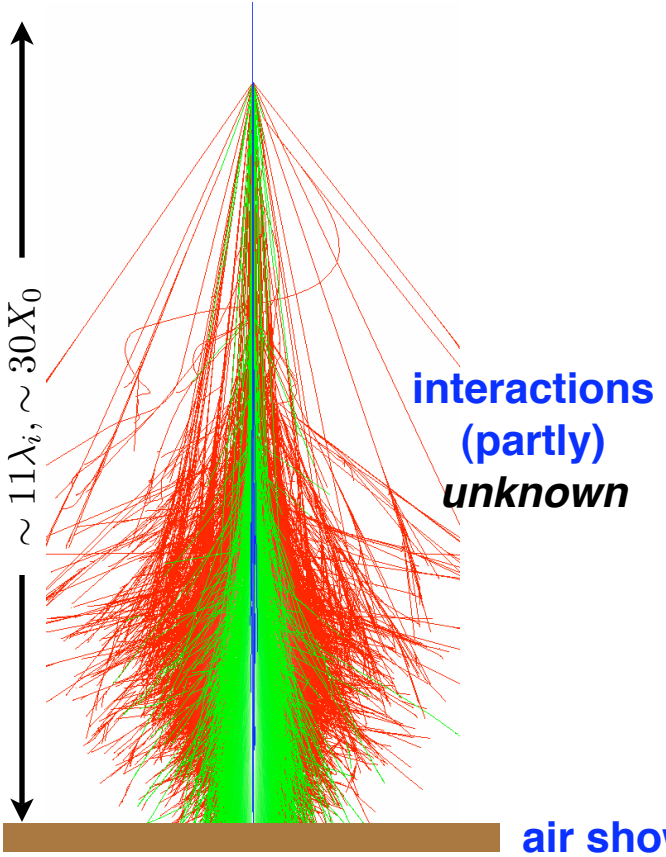
CERN, 29th June - 3rd July 2009

# Test of hadronic interaction models with air shower data



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primary cosmic-ray particle (type *unknown*)

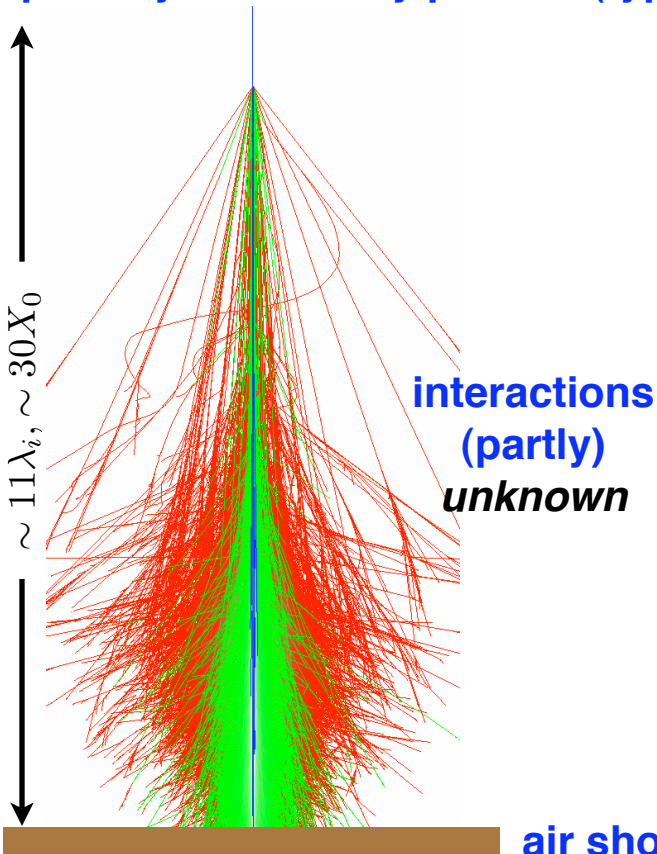


air shower detector at ground level



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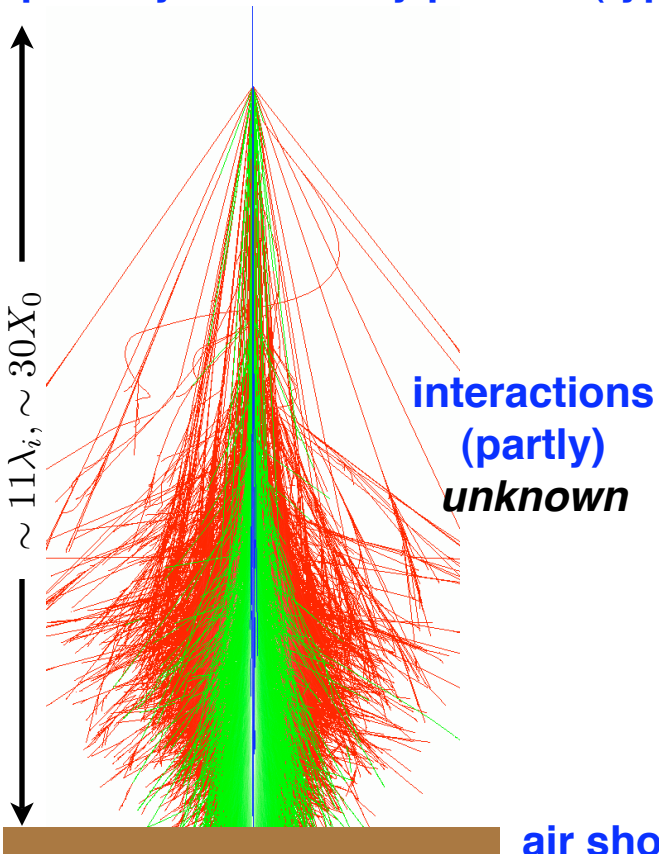
Münchhausen problem



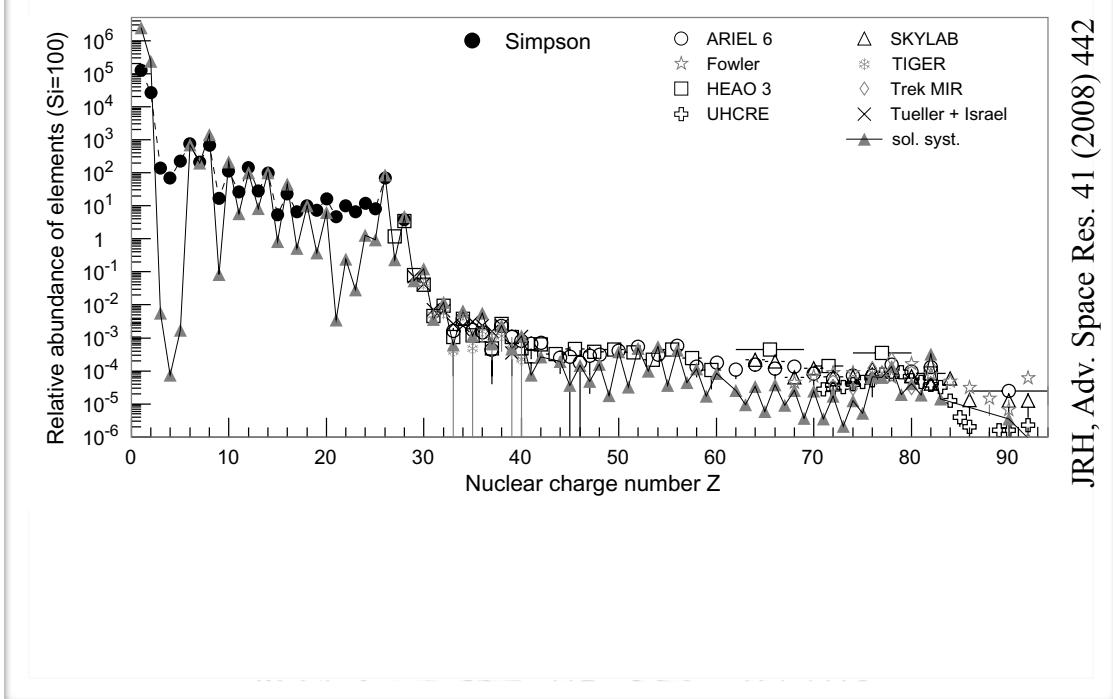


# Test of hadronic interaction models with air shower data

primary cosmic-ray particle (type *unknown*)



abundance of elements in cosmic rays ( $\sim 1$  GeV/n)

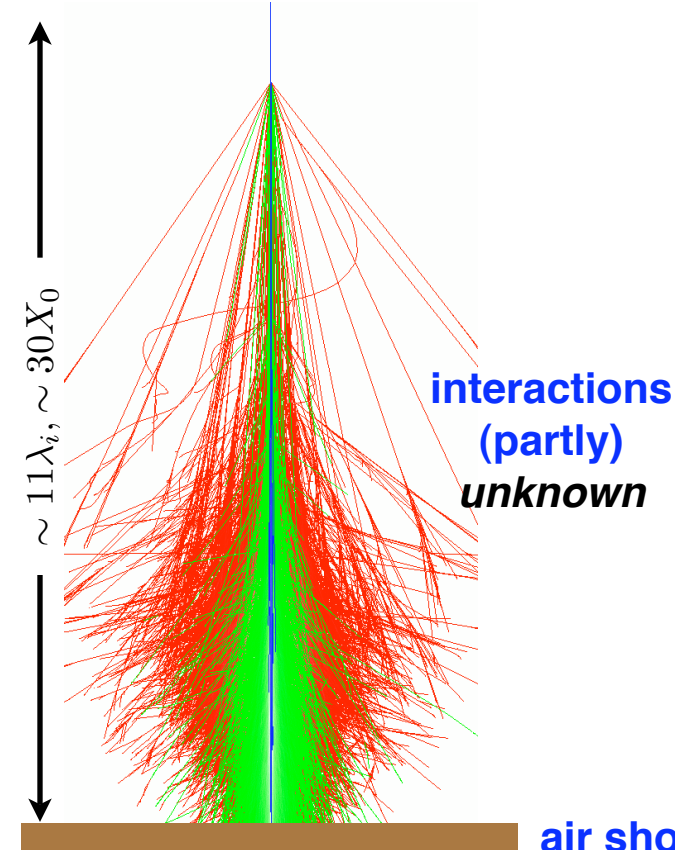


JRH, Adv. Space Res. 41 (2008) 442

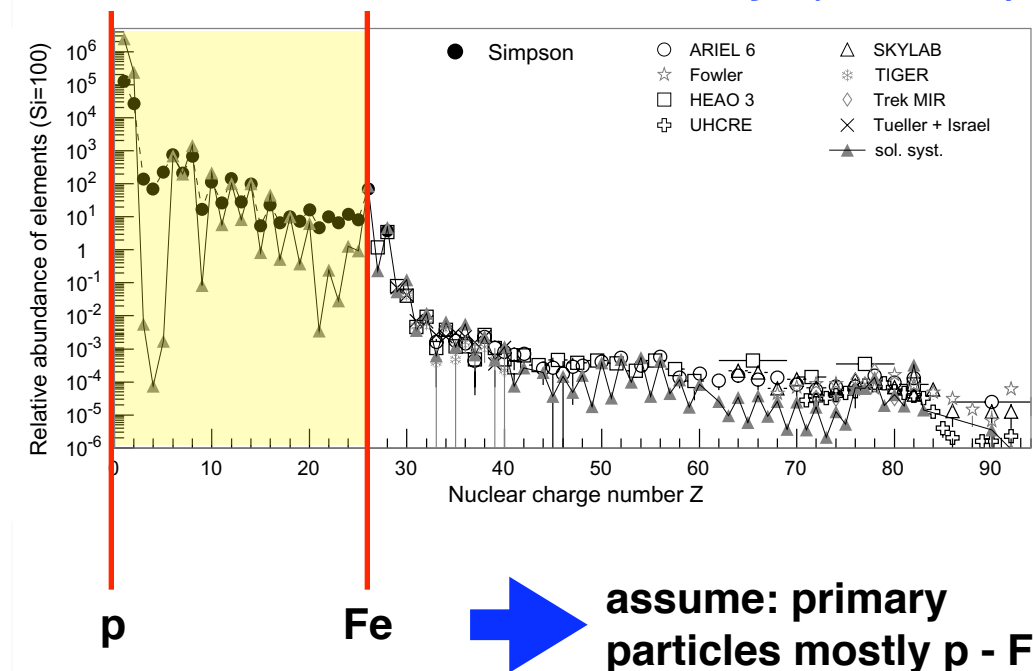
air shower detector at ground level

# Test of hadronic interaction models with air shower data

primary cosmic-ray particle (type *unknown*)



abundance of elements in cosmic rays ( $\sim 1$  GeV/n)





# Test of hadronic interaction models with air shower data

## Method:

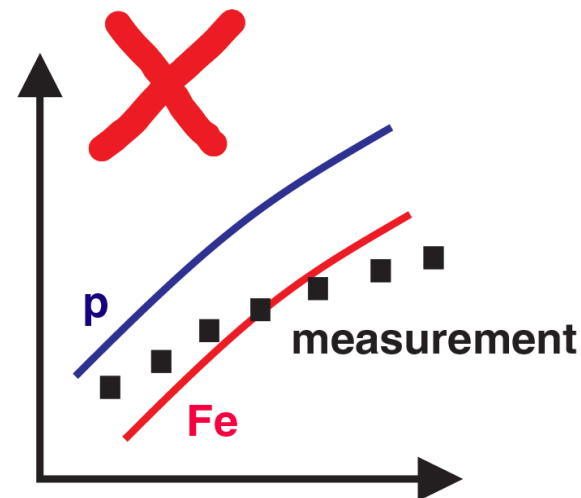
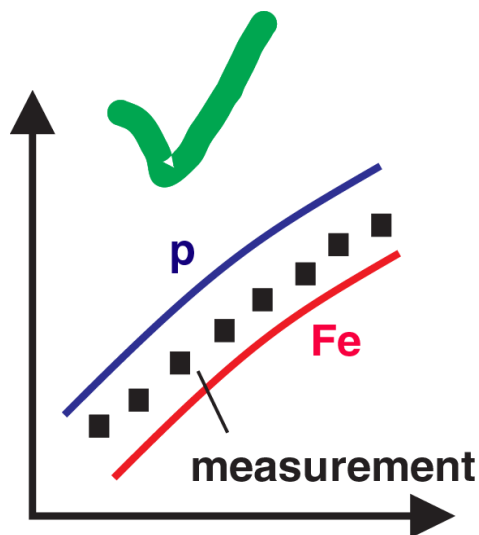
- Measure correlation between air shower components (electromagnetic, muonic, hadronic)
- Compare to predictions of hadronic interaction models for extreme assumptions (p & Fe)

air shower simulation:

CORSIKA

detector simulation:

GEANT 3



# KARlsruhe Shower Core and Array DETector

**Simultaneous measurement of  
electromagnetic,  
muonic,  
hadronic  
shower components**



# KASCADE

## Hadron calorimeter

320 m<sup>2</sup> x 9 layers

liquid ionization chambers

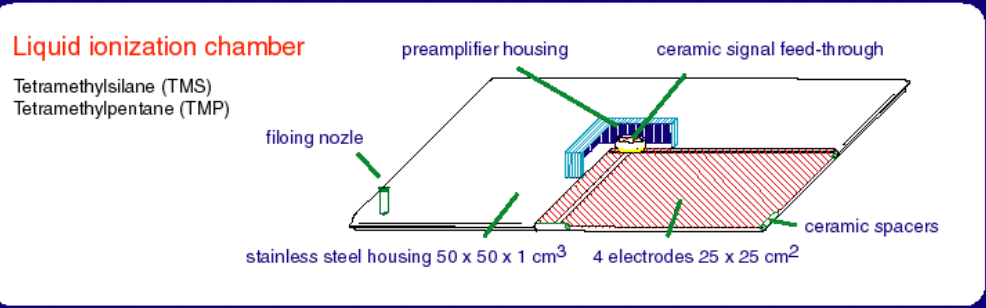
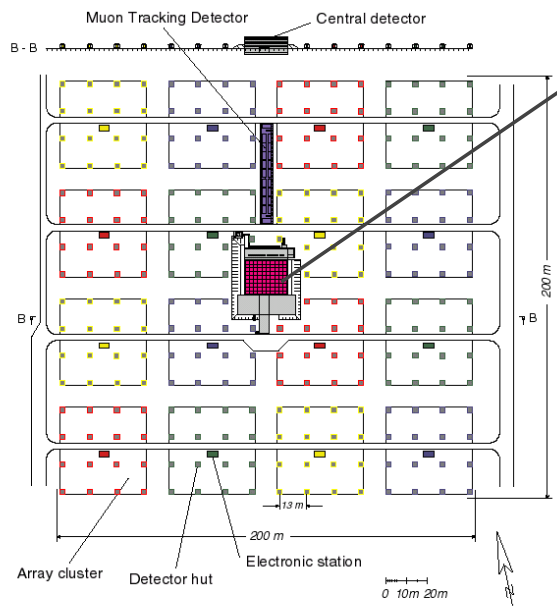
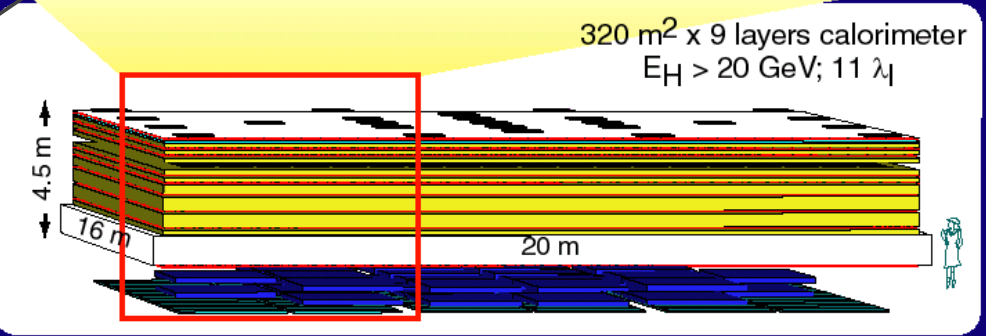
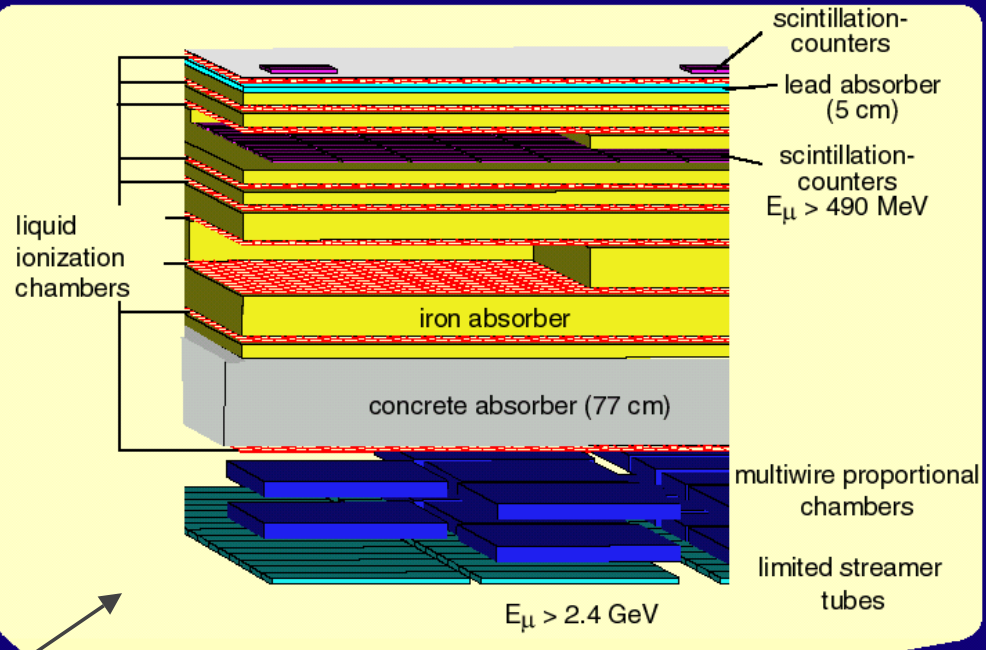
44 000 electronic channels

$E_H > 20$  GeV

## Field array 200 x 200 m<sup>2</sup>

$e/\gamma$  detectors

$\mu$  detectors  $E_\mu > 230$  MeV

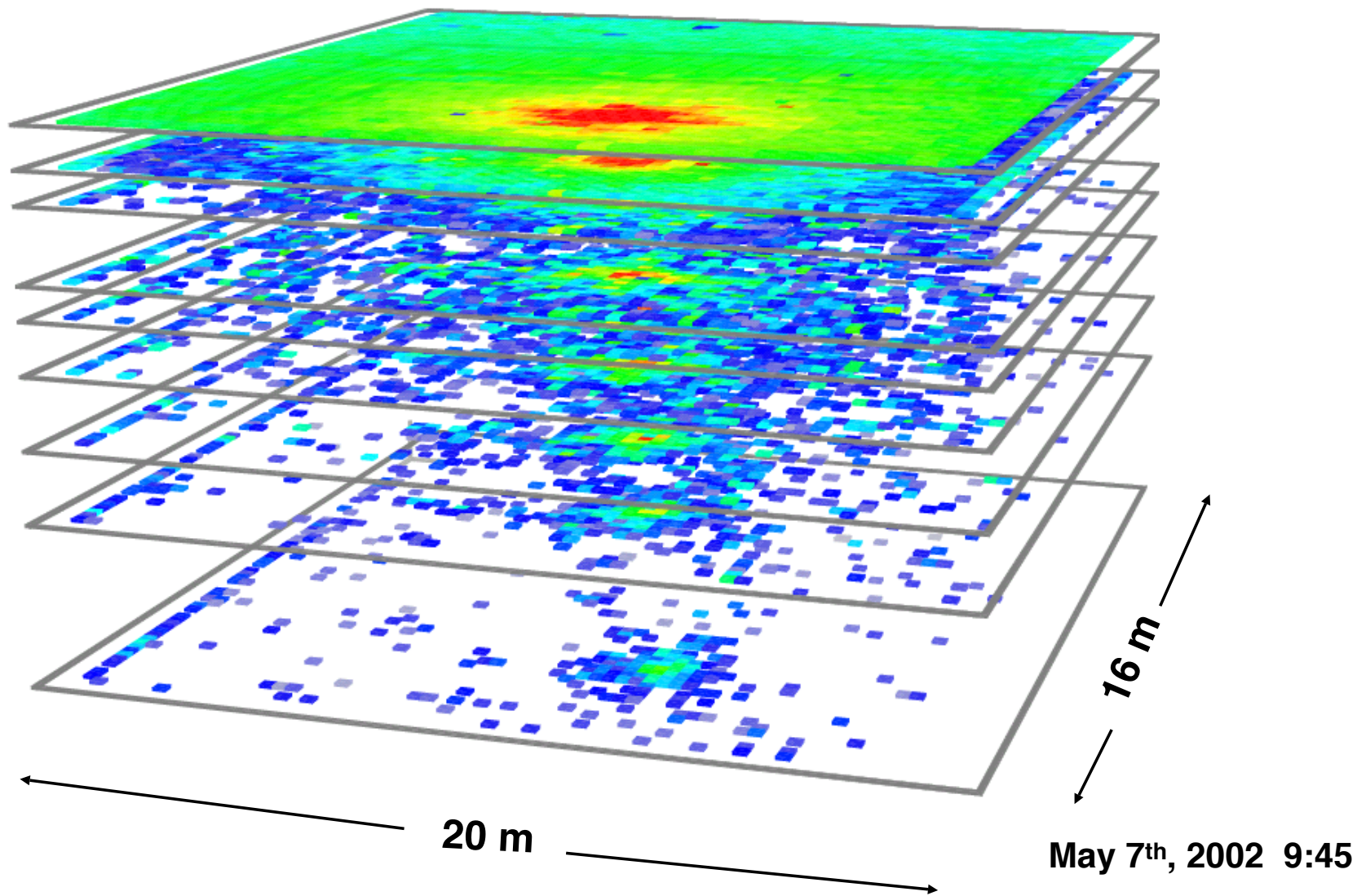




# Hadronic shower core

$E_0 \sim 6 \text{ PeV}$

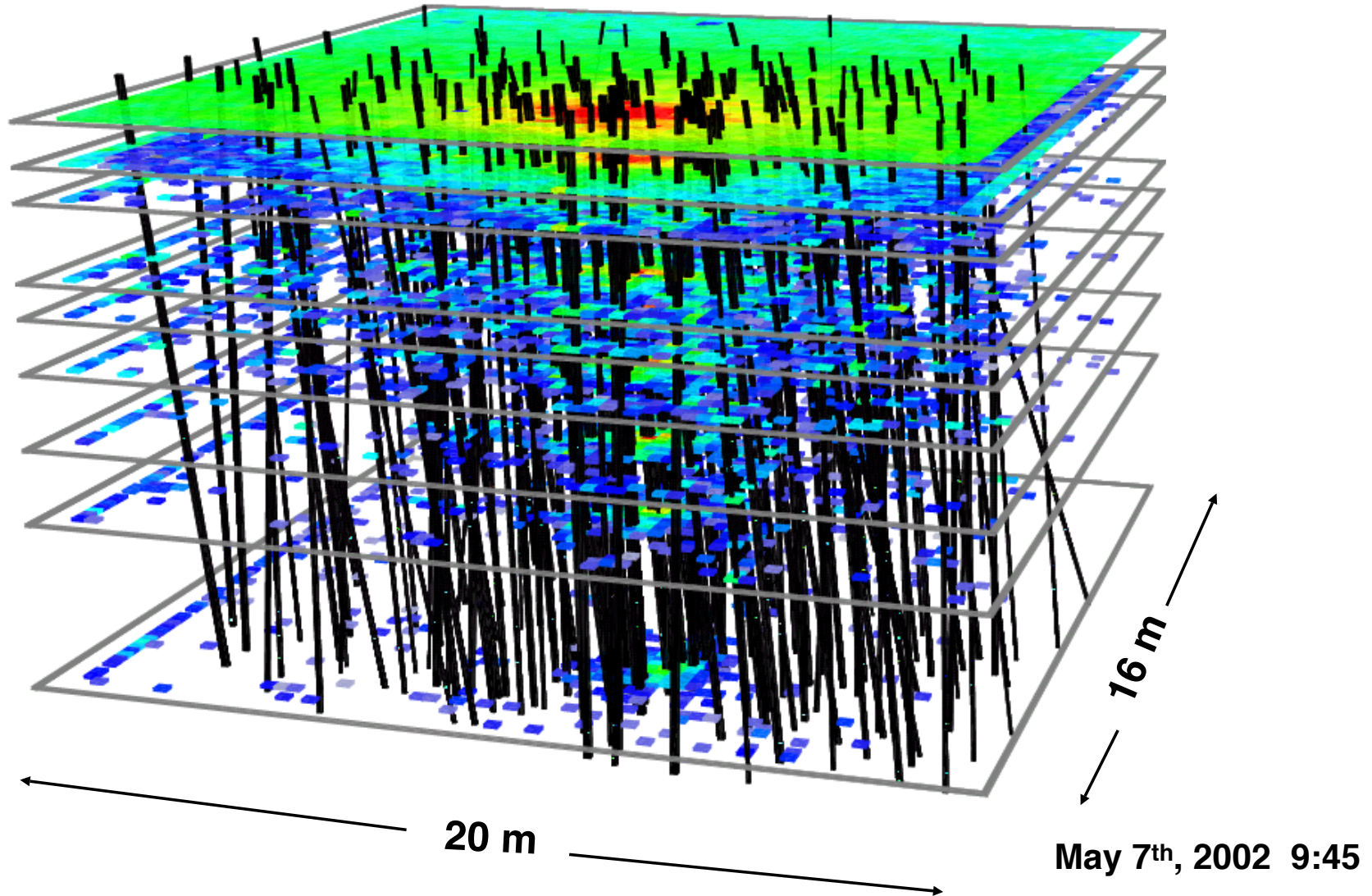
Number of reconstructed hadrons  $N_h = 143$   $E_h > 50 \text{ GeV}$



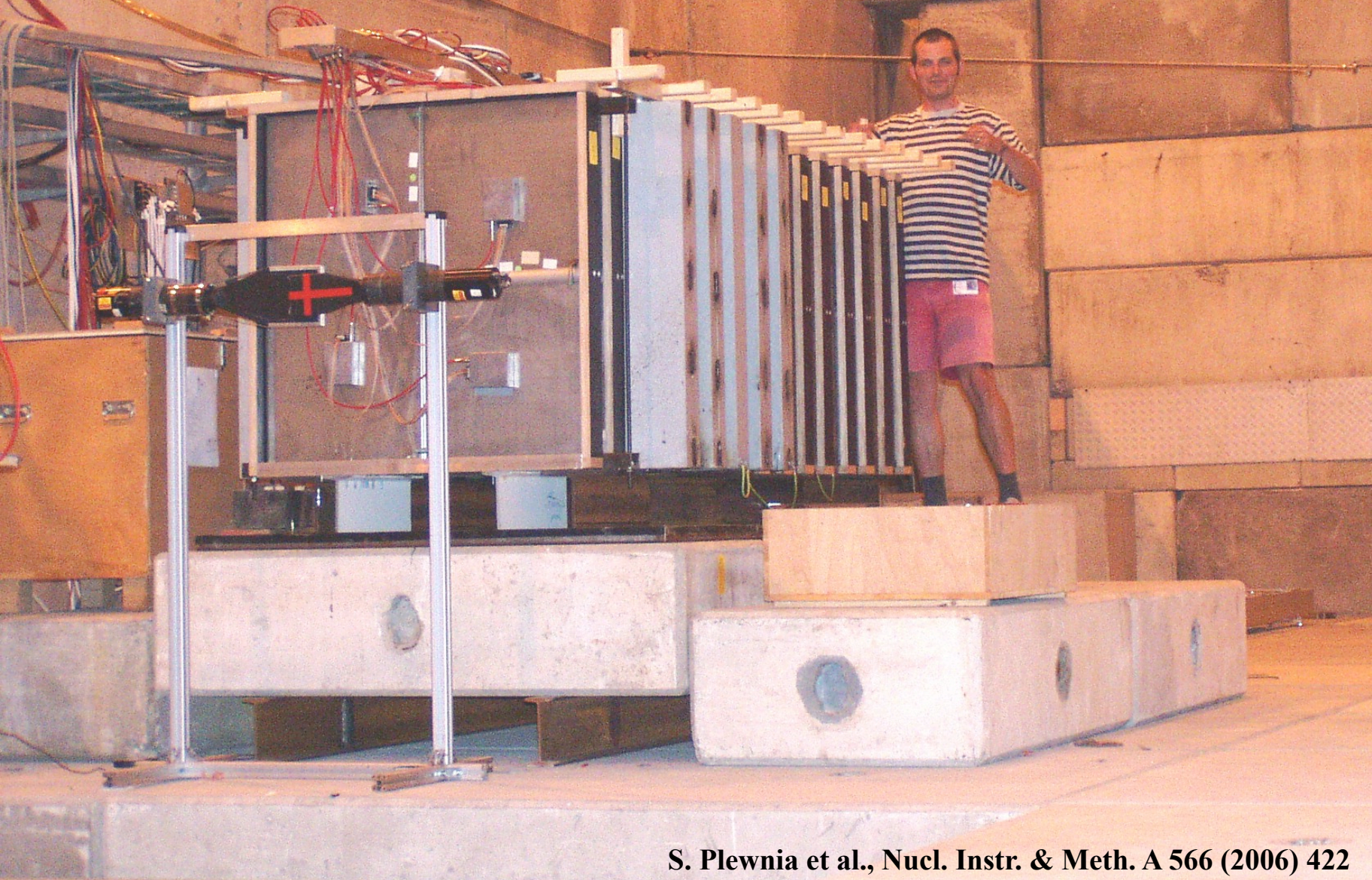
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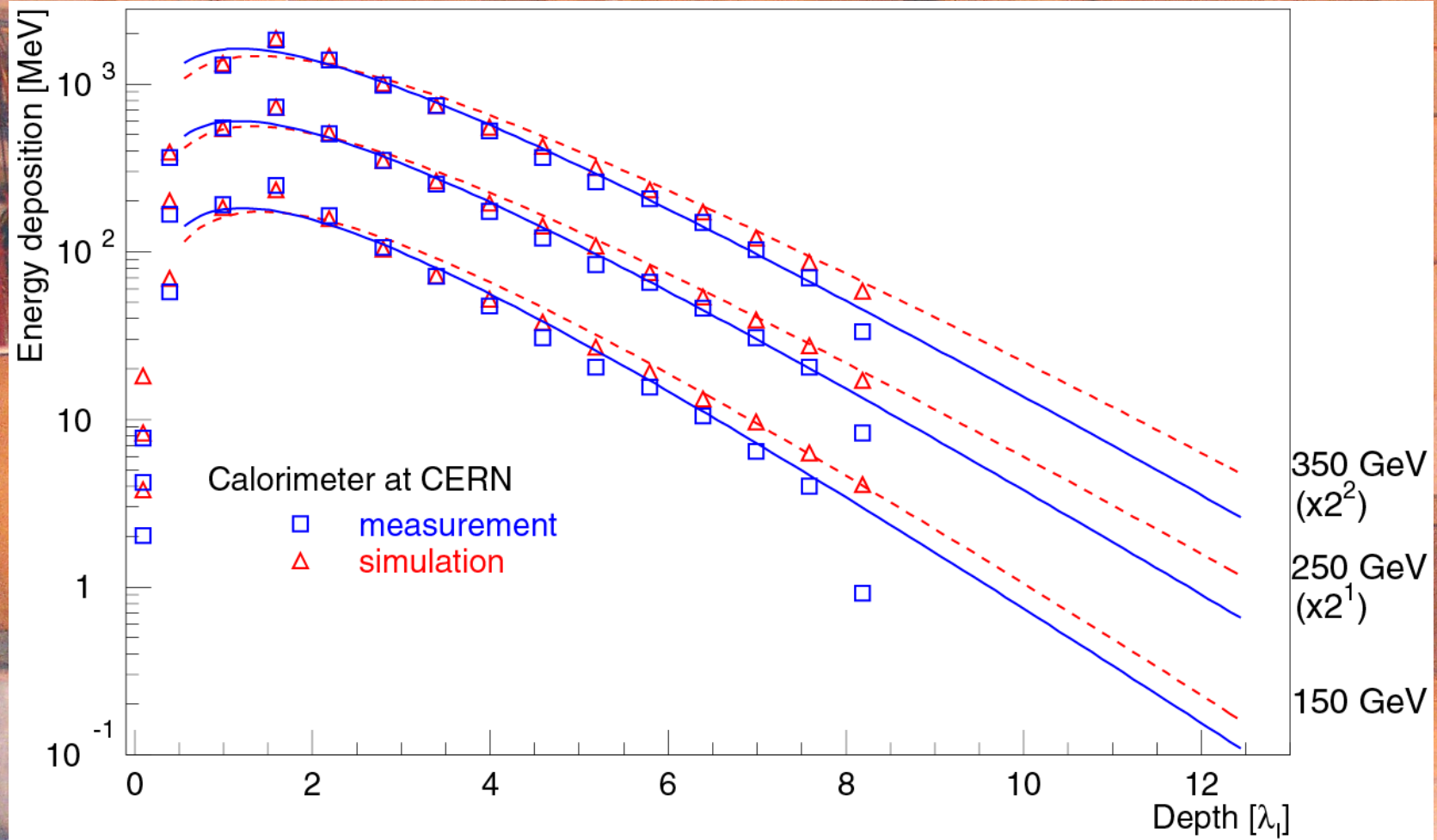
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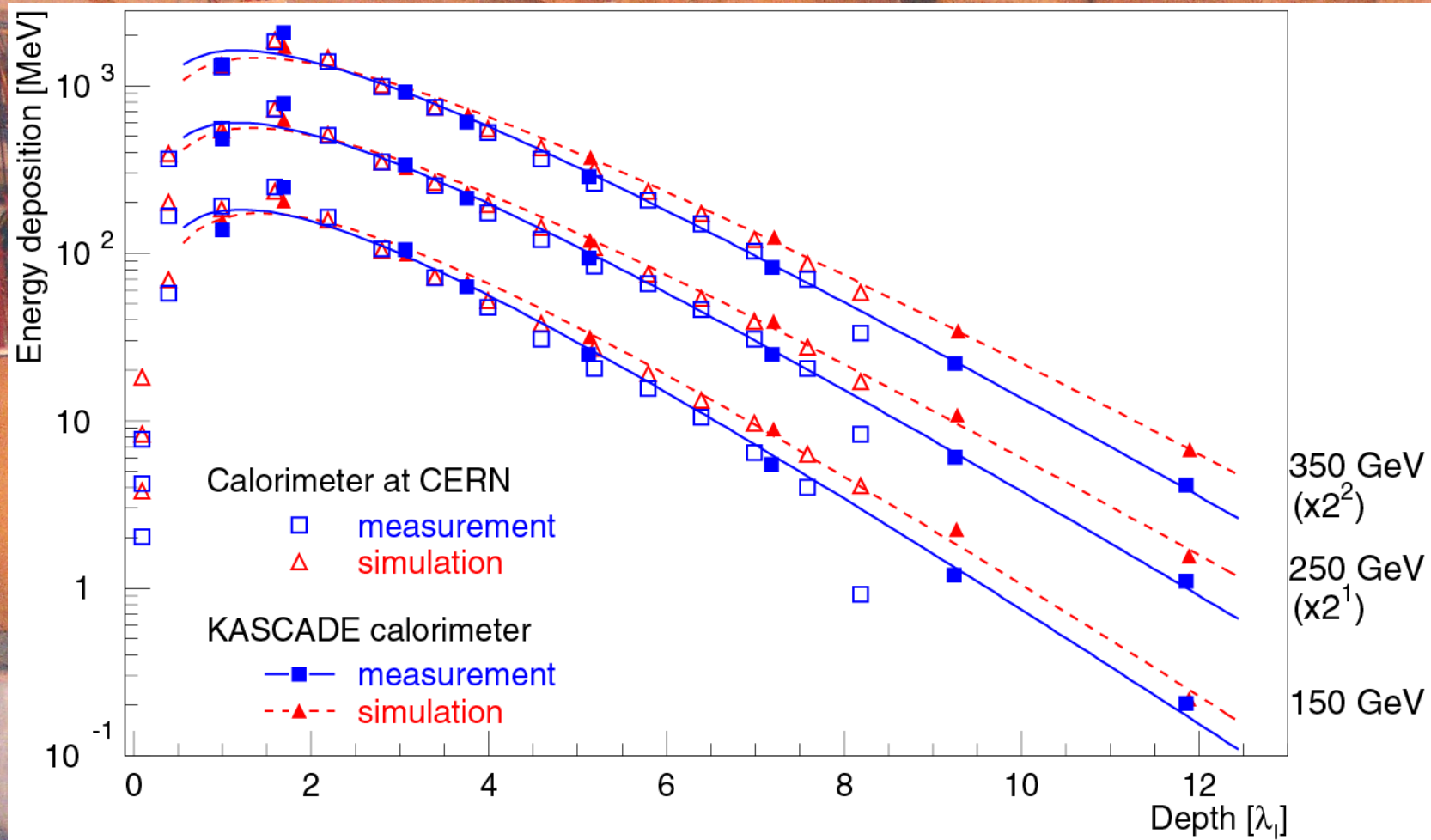
# Calibration of the KASCADE-Grande hadron calorimeter at the CERN SPS



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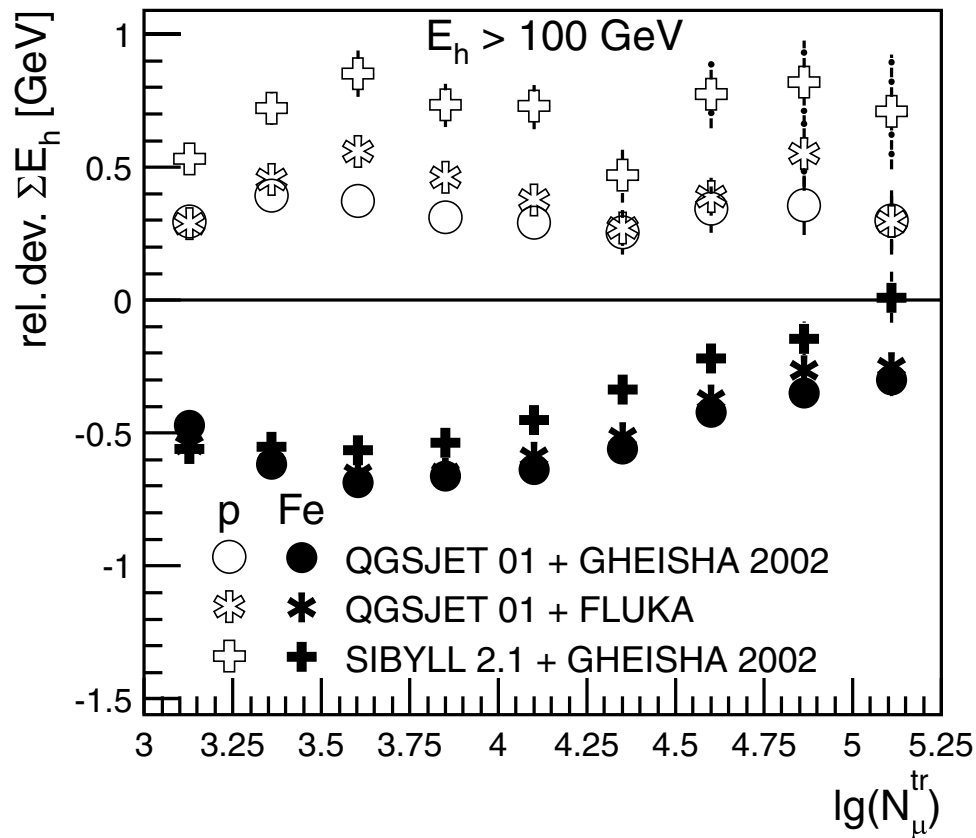


# Calibration of the KASCADE-Grande hadron calorimeter at the CERN SPS



# Low-energy interaction models

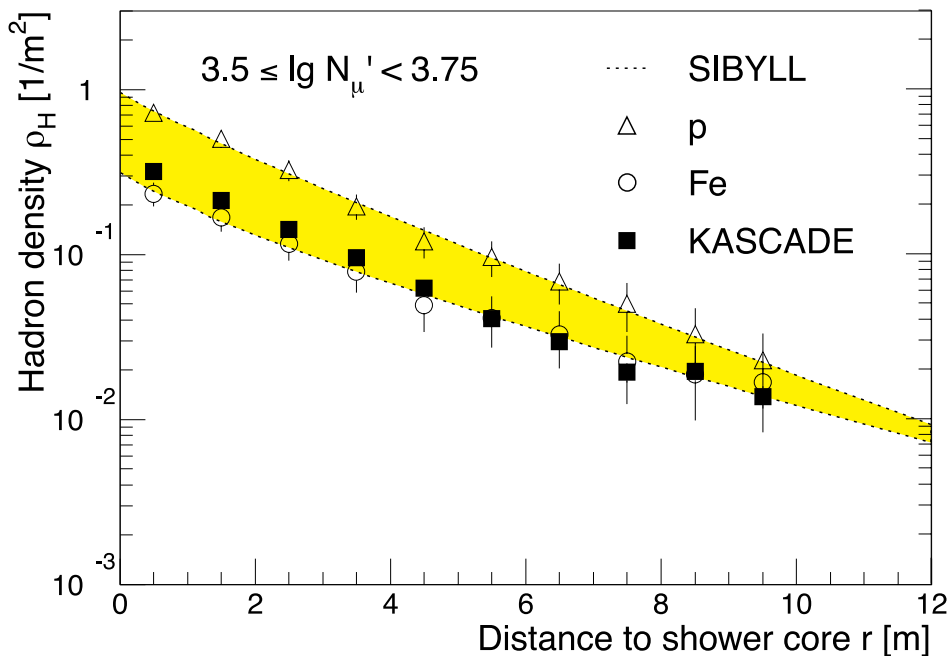
$E < 200$  GeV



**GHEISHA & FLUKA  
both OK**

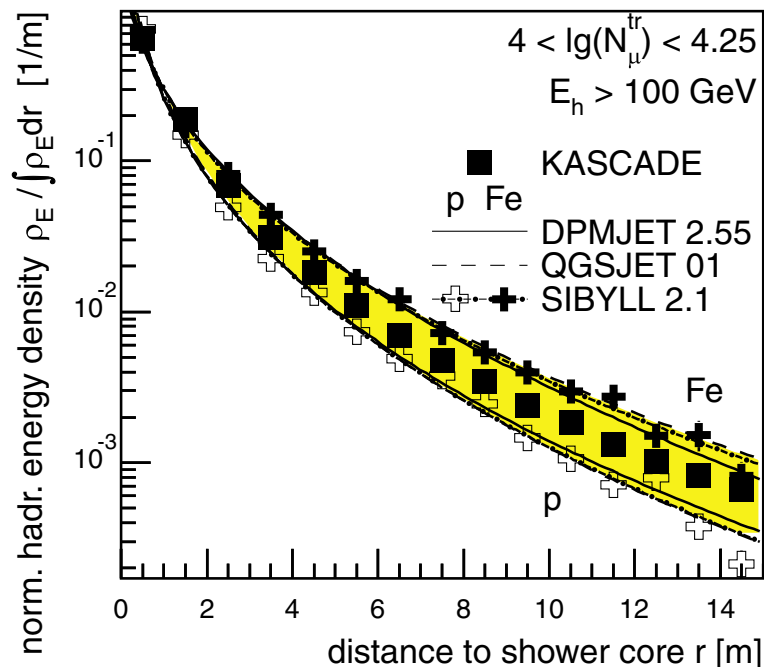
# Hadronic interaction model SIBYLL

version 1.6



*not compatible*

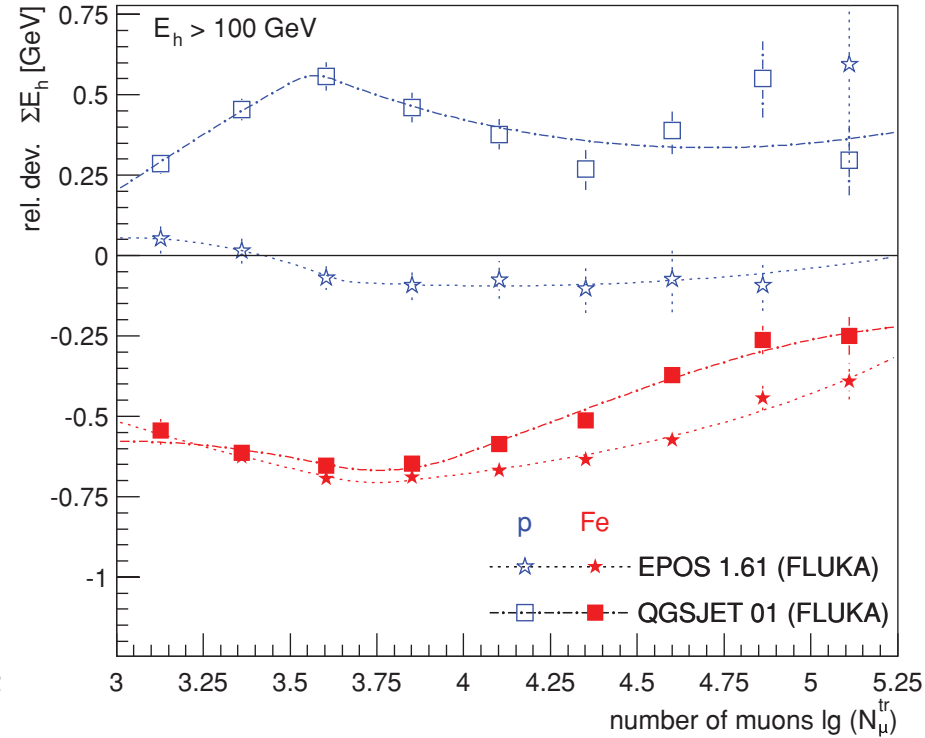
version 2.1



*compatible with air shower data*

# KASCADE – Test of EPOS 1.6

$$\Sigma E_h - N_\mu$$



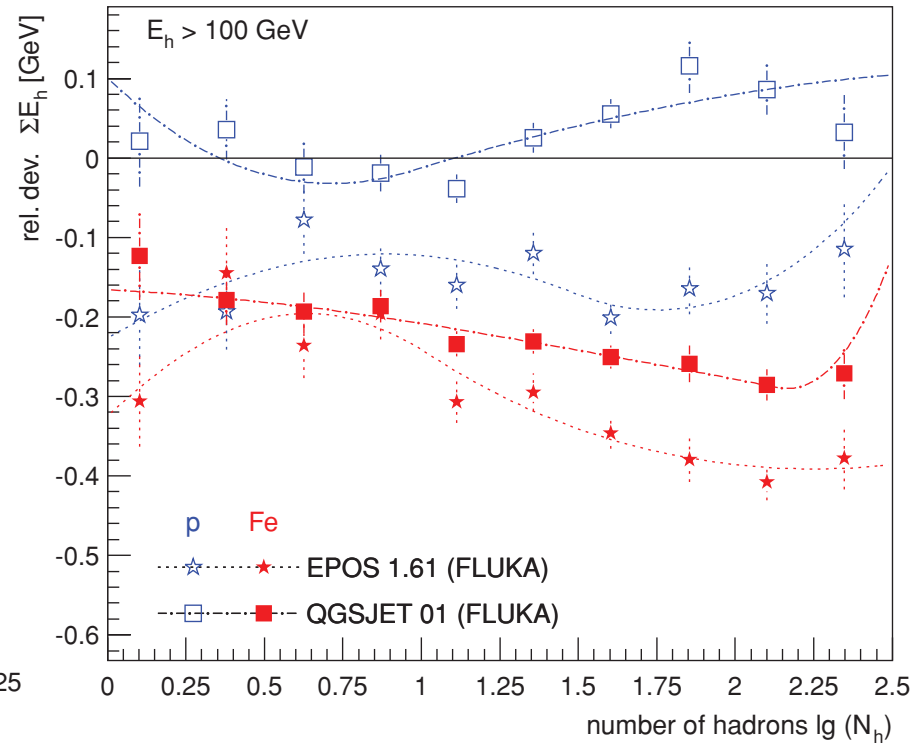
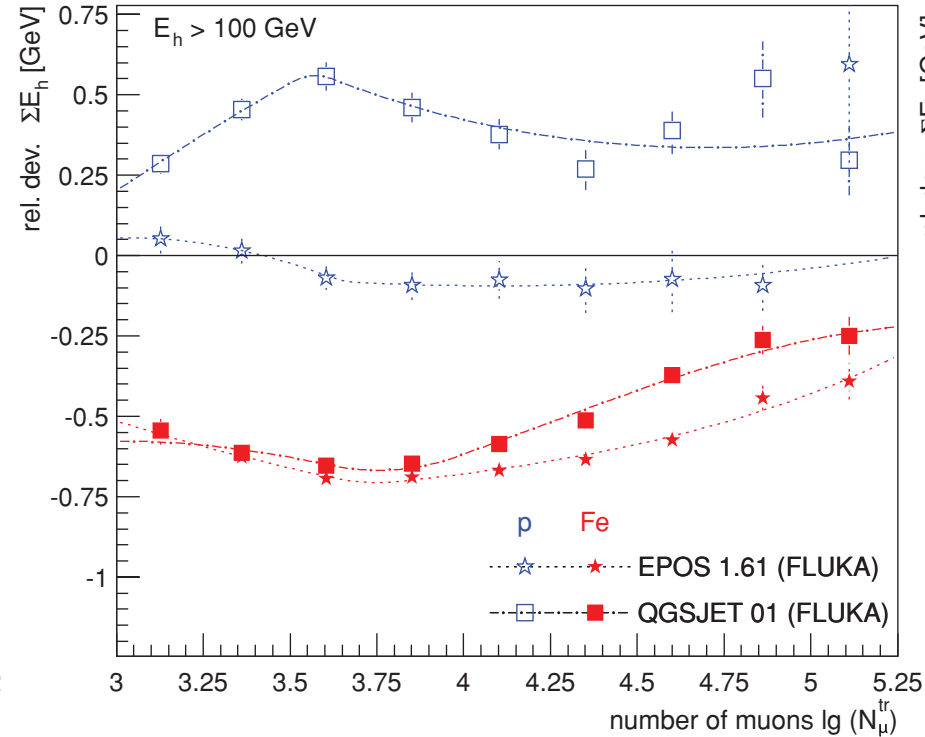
**EPOS delivers not enough  
hadronic energy to the ground**



# KASCADE – Test of EPOS 1.6

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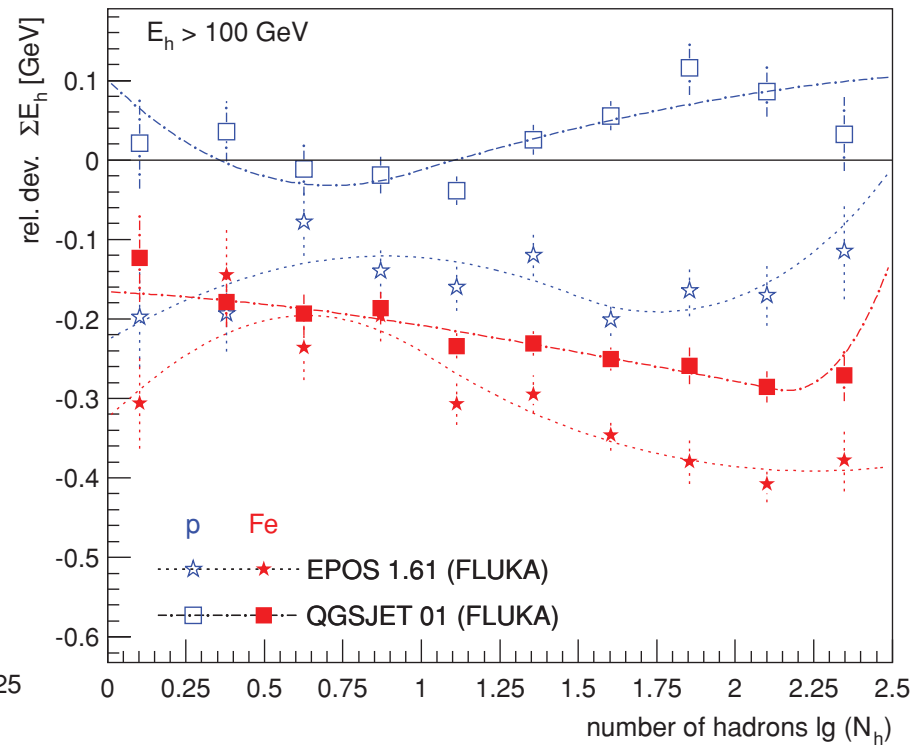
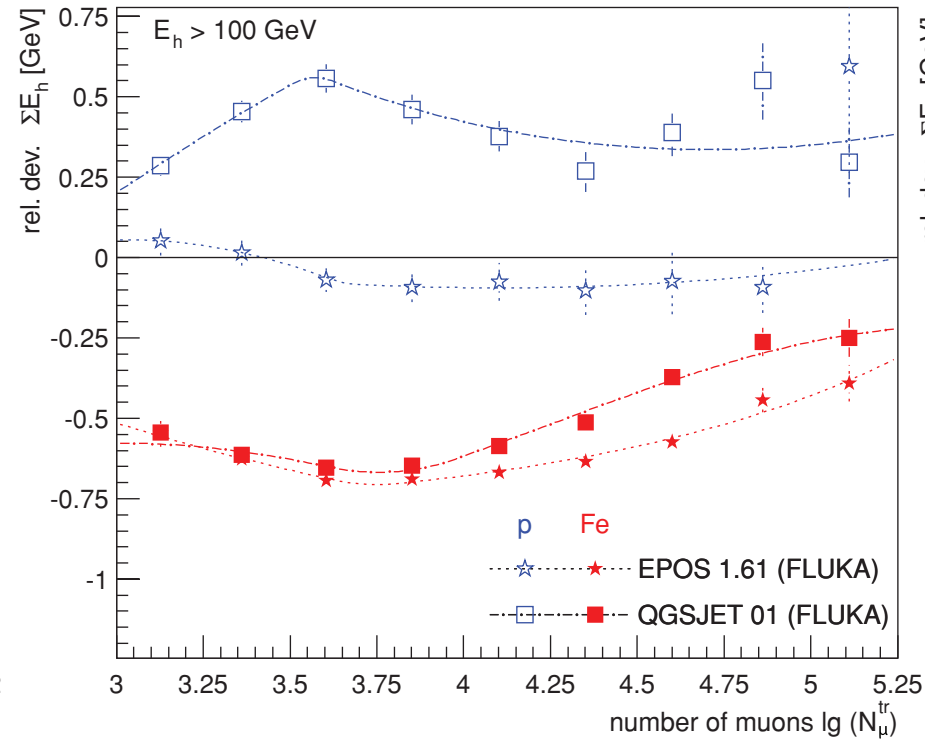
**EPOS delivers not enough  
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**→ energy per hadron too small**

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$$\Sigma E_h - N_\mu$$

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**EPOS delivers not enough  
hadronic energy to the ground**

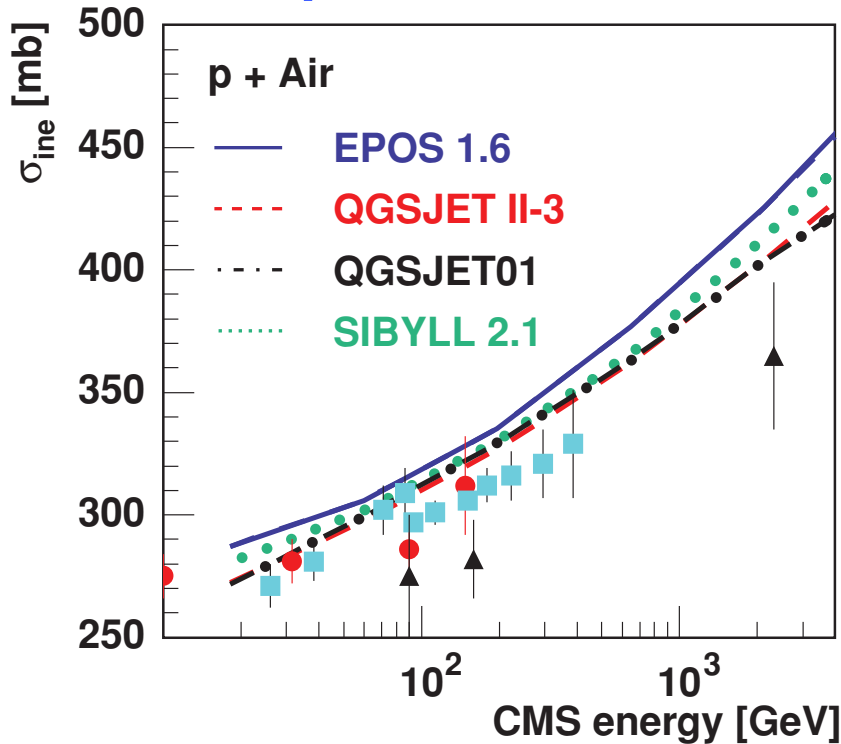
**→ energy per hadron too small**

**→ EPOS 1.6 is NOT CONSISTENT  
with KASCADE observations!**

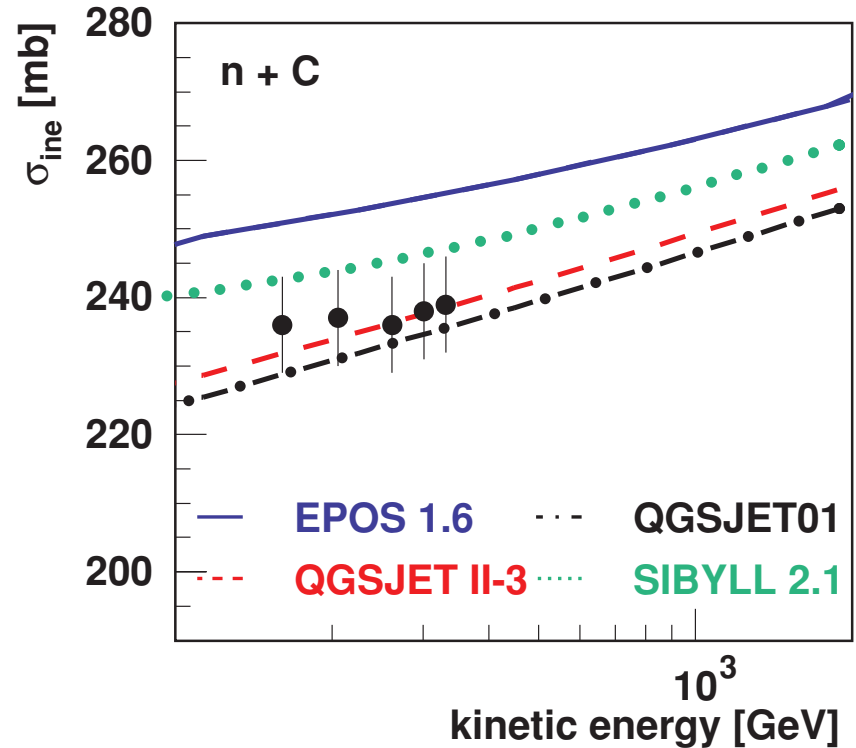
# KASCADE – Test of EPOS 1.6

## Inelastic cross sections

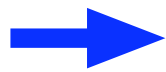
proton - air



neutron - carbon



**cross sections in EPOS 1.6 too large**



**new version EPOS 1.9 under investigation**

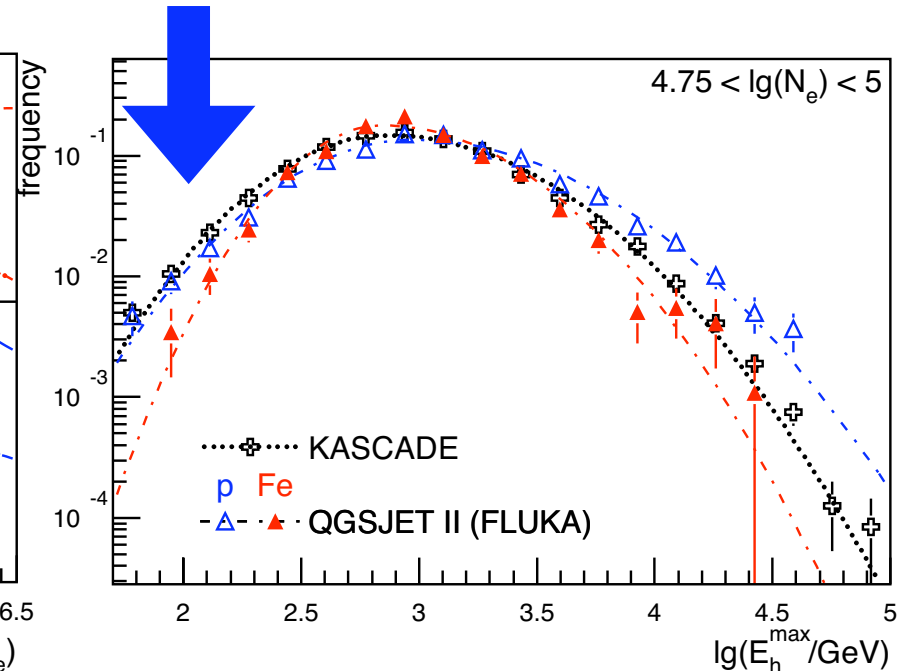
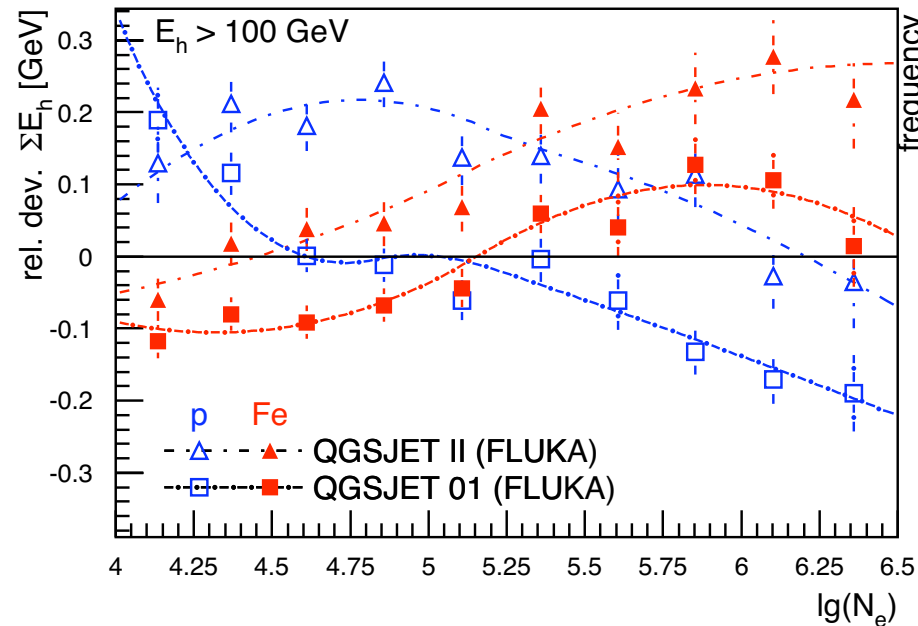


**forthcoming studies**

# Hadronic interaction model QGSJET-II

hadr. energy sum vs.  
number of electrons

maximum hadron energy

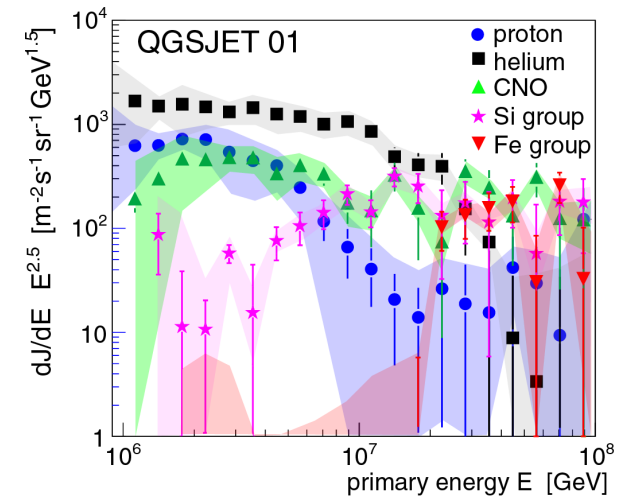


**QGSJET-II exhibits some problems**

# Uncertainties quantitative

QGSJET 01

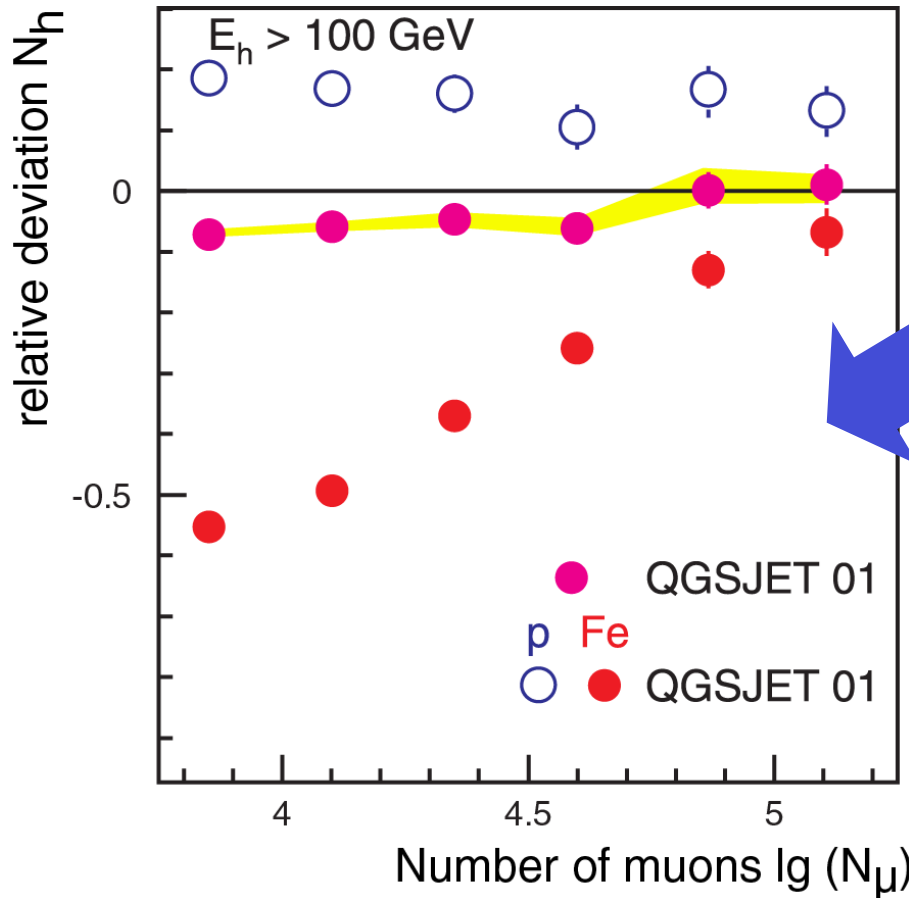
cosmic-ray  
composition from  
 $N_e-N_\mu$  analysis



# Uncertainties quantitative

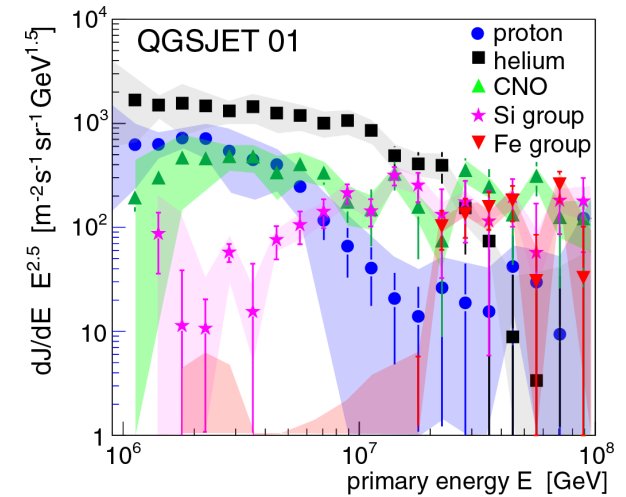
## QGSJET 01

Number of hadrons vs. number of muons



cosmic-ray  
composition from

## $N_e$ - $N_\mu$ analysis



**~10%-15% uncertainty**

# Models tested in CORSIKA

**QGSJET 98**  
**VENUS**  
**SIBYLL 1.6**

T. Antoni et al, J.. of Phys. G 25 (1999) 2161

**DPMJET II.55**  
**QGSJET 01**  
**SIBYLL 2.1**  
**NEXUS 2**

**DPMJET II.5**

W.D. Apel et al., J. of Phys. G 34 (2007) 2581

**EPOS 1.6**

W.D. Apel et al., J. of Phys. G 36 (2009) 035201

**QGSJET-II**

J.R. Hörandel et al., ICRC 2009

**EPOS 1.9**

in progress

# Models tested in CORSIKA

**QGSJET 98**

~~**VENUS**~~

~~**SIBYLL 1.6**~~

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W.D. Apel et al., J. of Phys. G 34 (2007) 2581

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W.D. Apel et al., J. of Phys. G 36 (2009) 035201

**(QGSJET-II)**

J.R. Hörandel et al., ICRC 2009

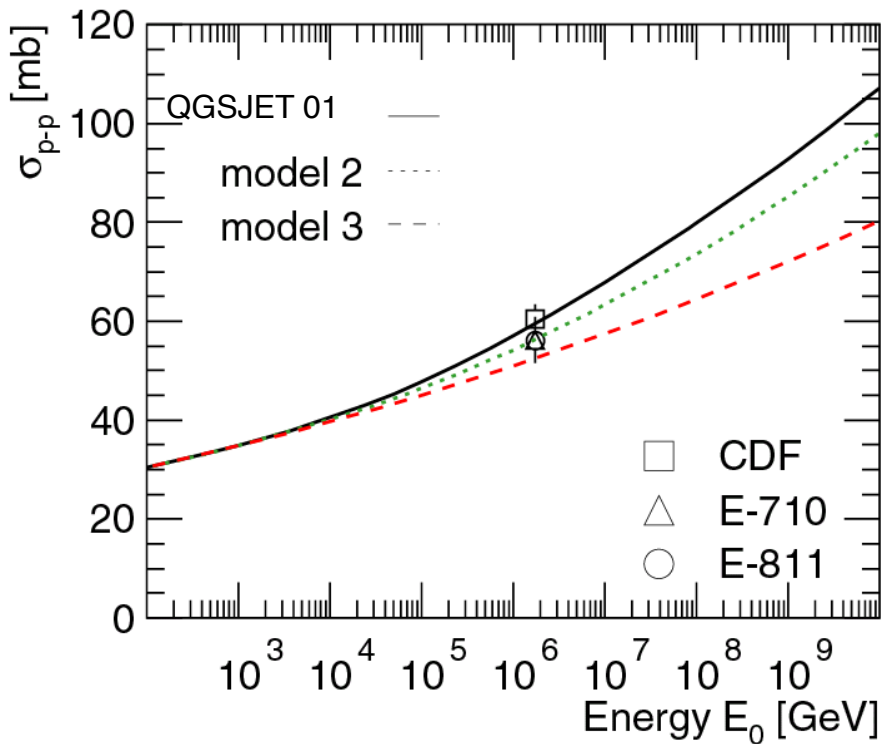
**EPOS 1.9**

in progress



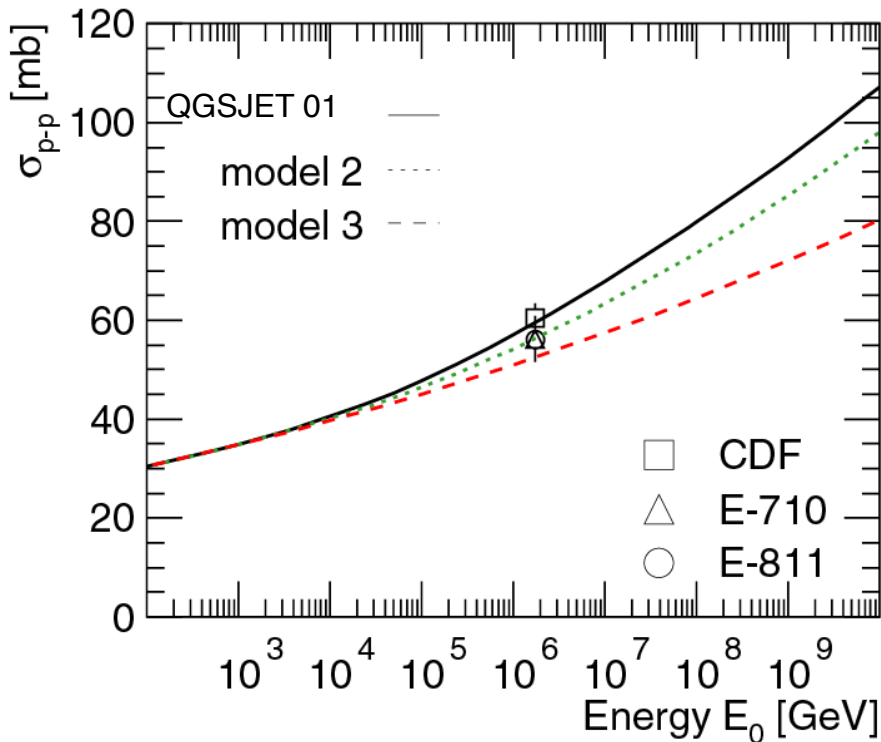
# Extrapolation of the uncertainties of accelerator data to air shower observables

## p-p cross section

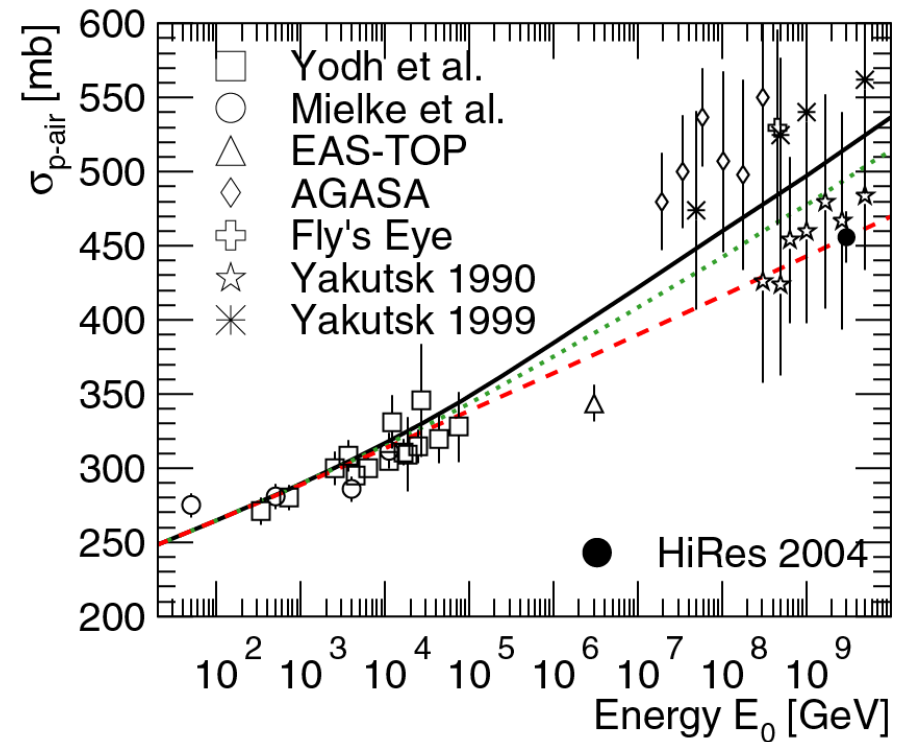


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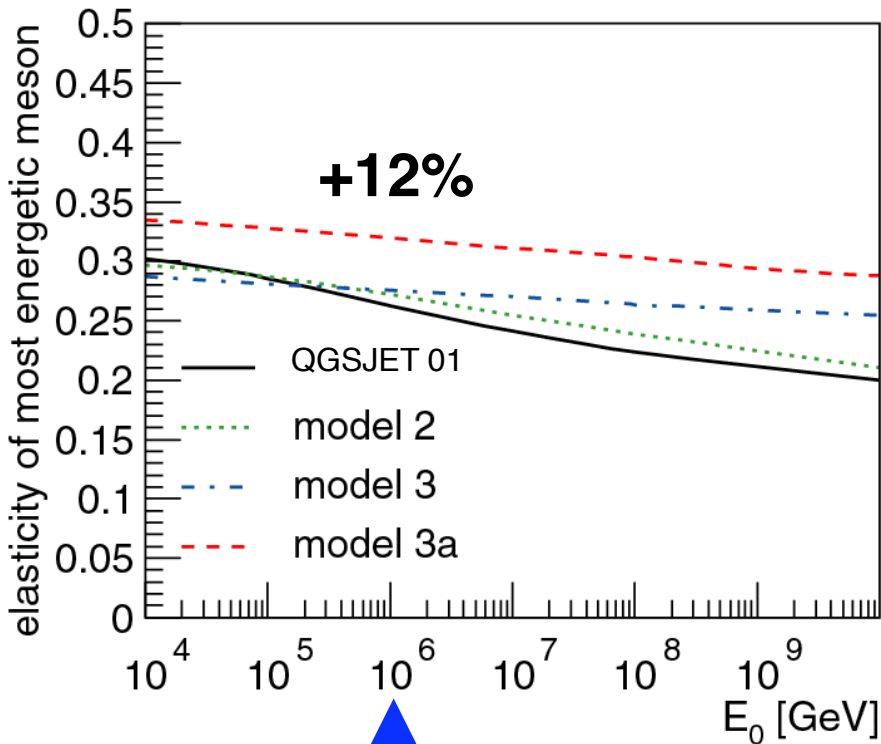


## p-air cross section

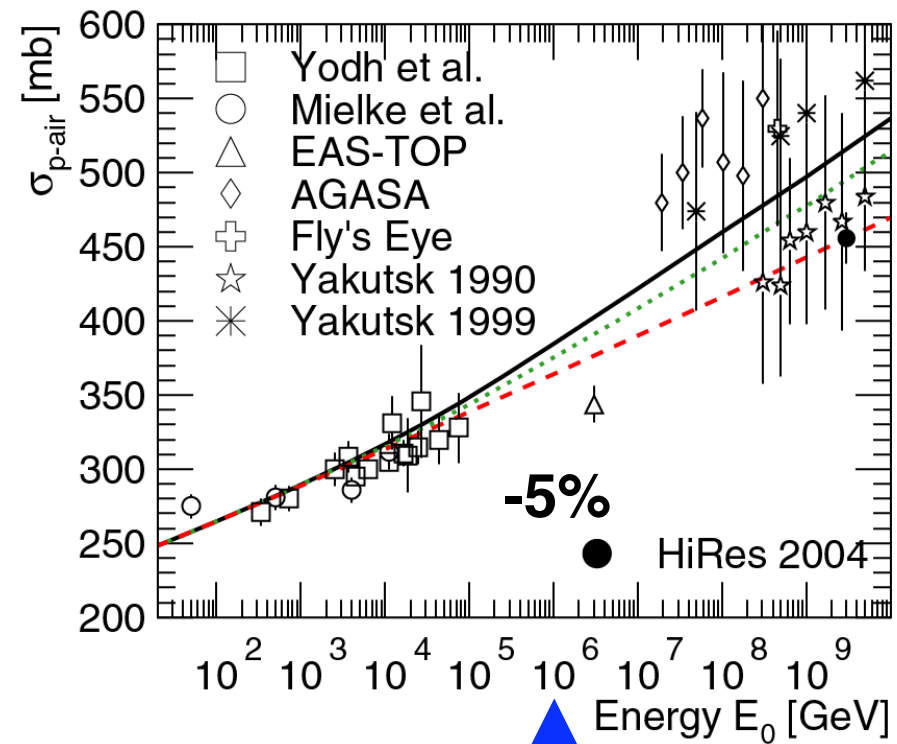


# Extrapolation of the uncertainties of accelerator data to air shower observables

## elasticity



## p-air cross section



# Average depth of the shower maximum

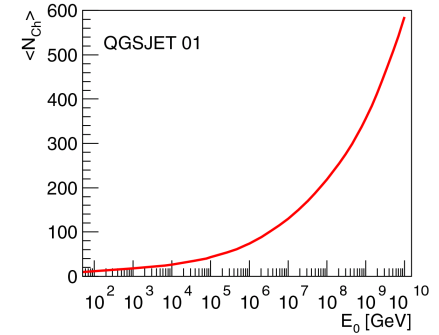
Heitler Model –  $X_{\max}$

# Average depth of the shower maximum

## Heitler Model – $X_{\max}$

multiplicity of charged particles produced in  $\pi$ -N interactions

$$N_{ch} = N_0 \left( \frac{E_0}{\text{PeV}} \right)^\eta \quad \eta=0.13$$



# Average depth of the shower maximum

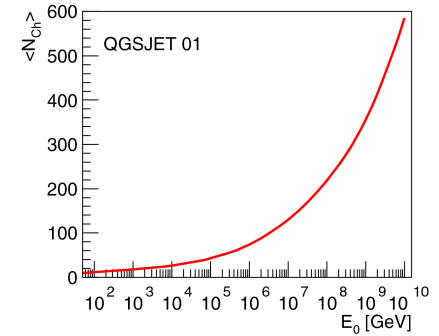
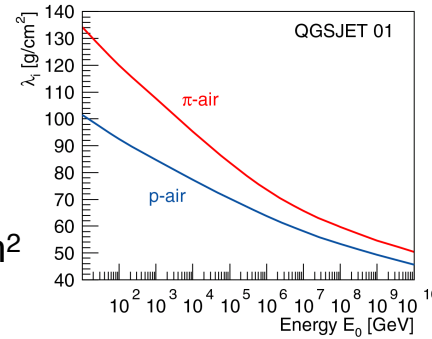
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proton air interaction length

$$\lambda_i^{p-air} = \xi + \zeta \lg \frac{E_0}{\text{PeV}} \quad \zeta=-4.88 \text{ g/cm}^2$$



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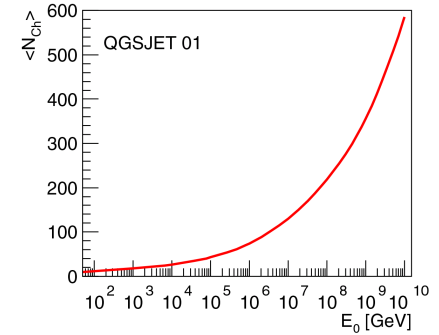
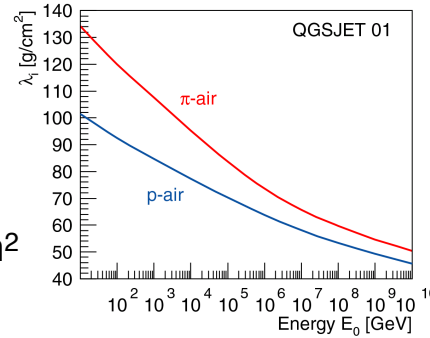
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elongation rate

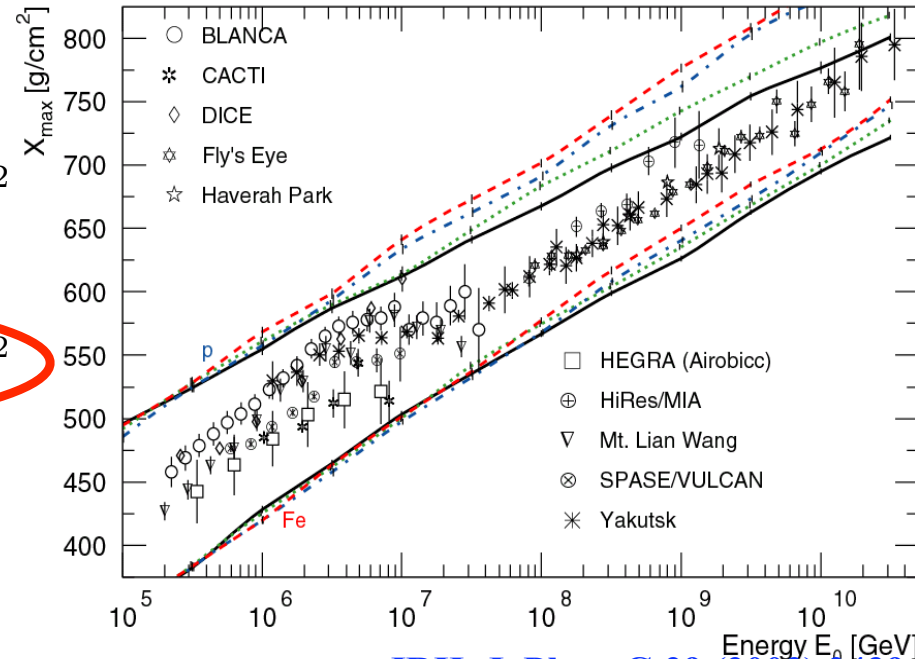
**e/m shower**  $\Lambda^\gamma = X_0 \ln 10 \approx 84.4 \text{ g/cm}^2$

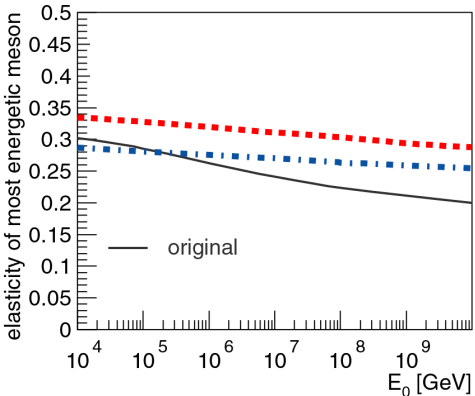
**proton shower**

$$\Lambda^p = X_0 \ln 10 - \eta X_0 \ln 10 + \zeta \ln 2 \approx 70 \text{ g/cm}^2$$

$X_{\max}$  for heavy nuclei

$$X_{\max}^A = X_{\max}^p - X_0 \ln A$$





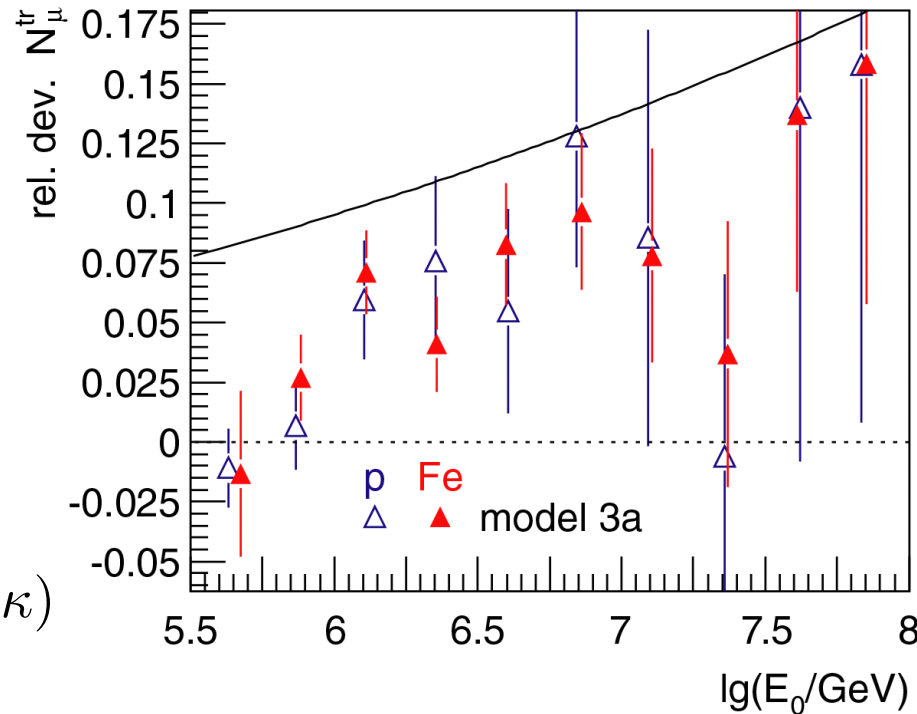
**Elasticity**

**Heitler model:**

$$N_{\mu} = \left( \frac{E_0}{\xi_c^{\pi}} \right)^{\beta} \quad \xi_c^{\pi} \approx 20 \text{ GeV}$$

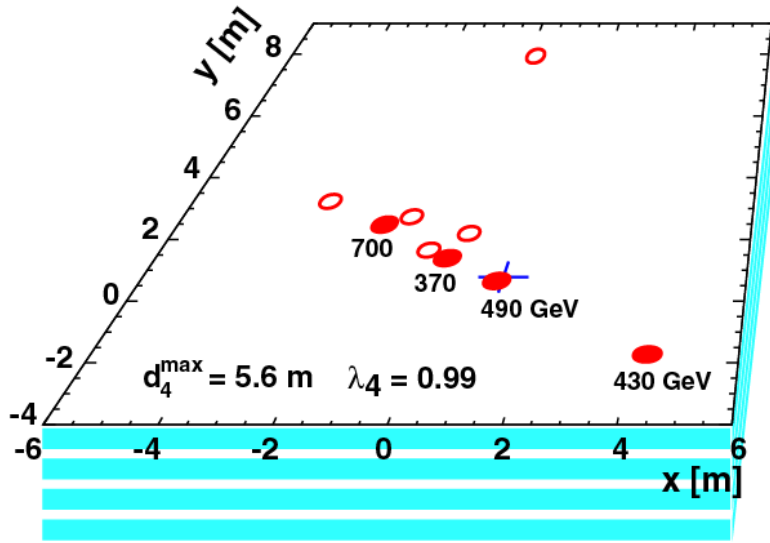
$$\beta \approx 1 - 0.14(1 - \kappa)$$

**$\delta N_{\mu}$  vs.  $E_0$**

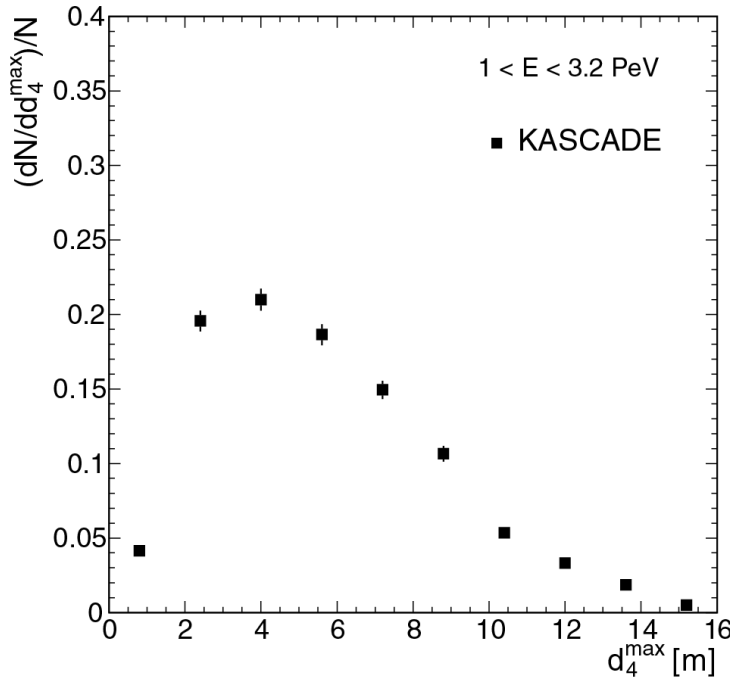
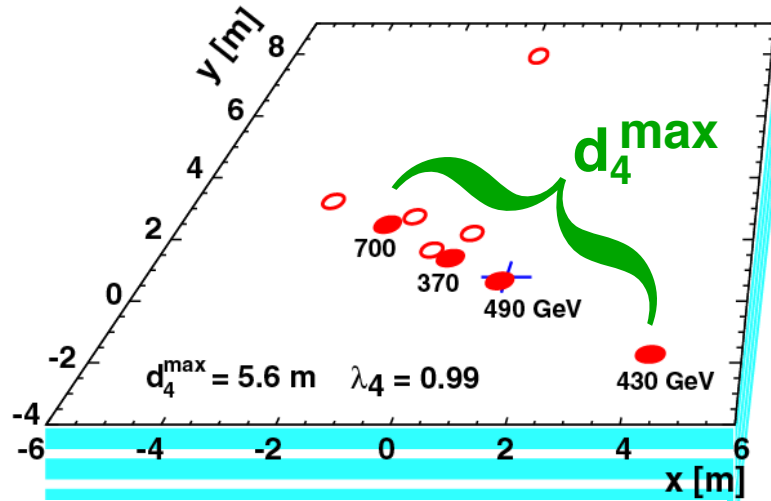




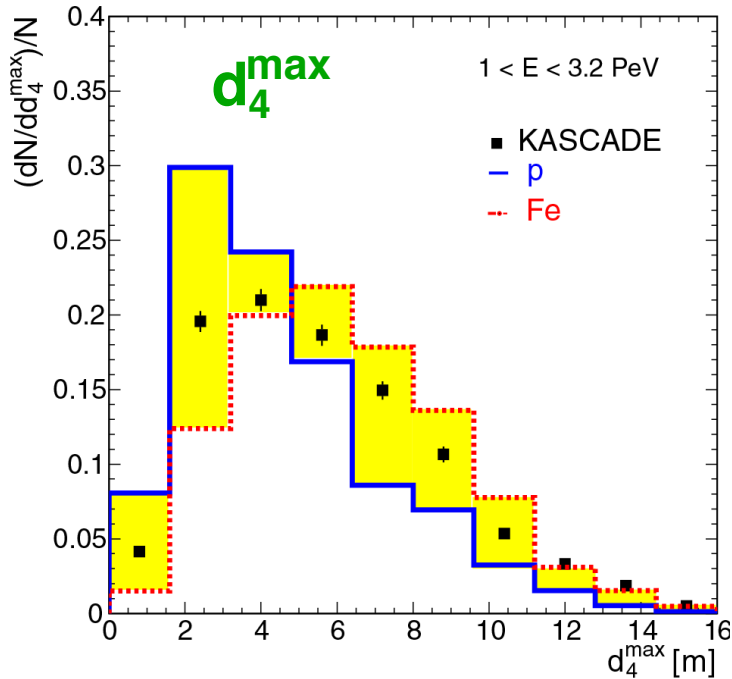
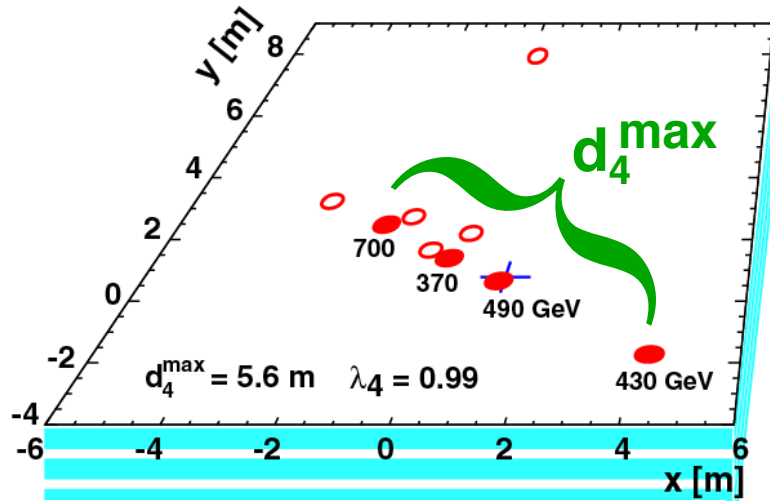
# Transverse momentum in hadronic interactions



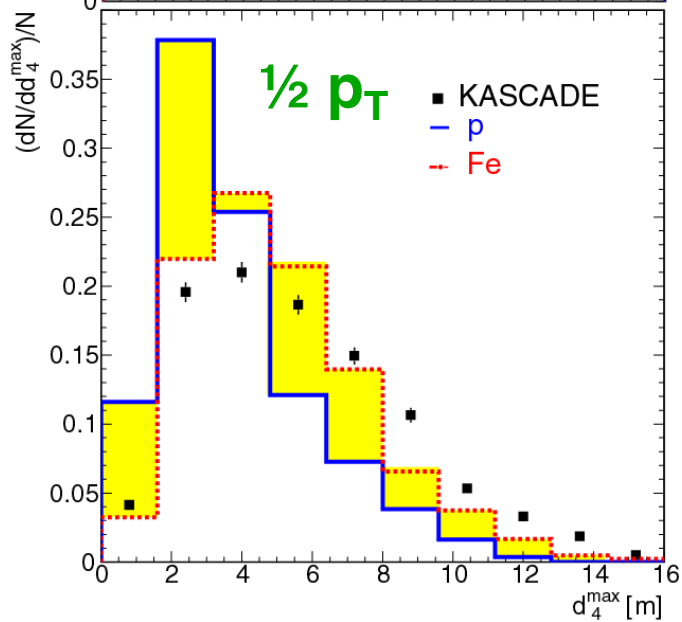
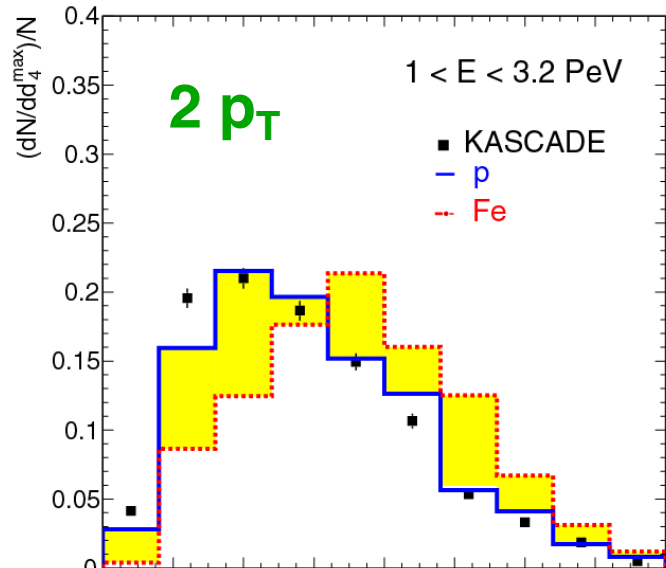
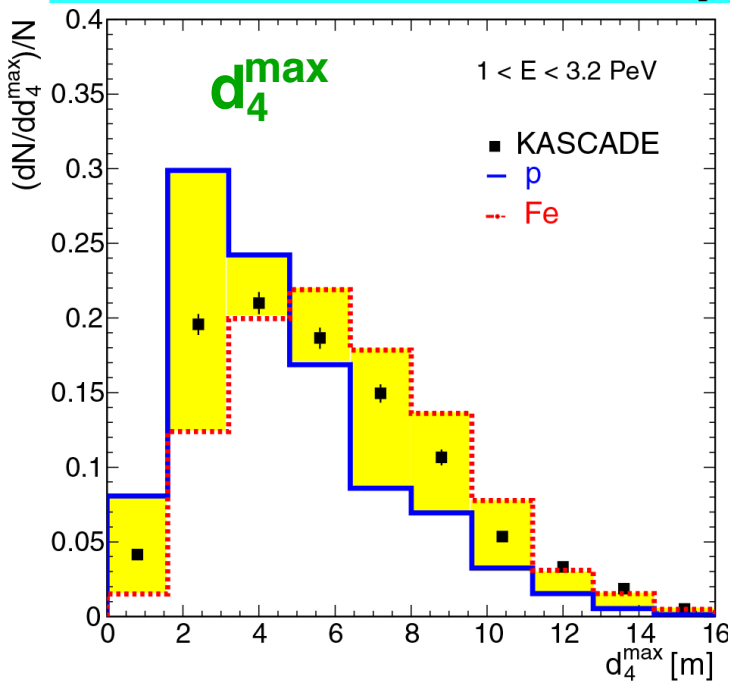
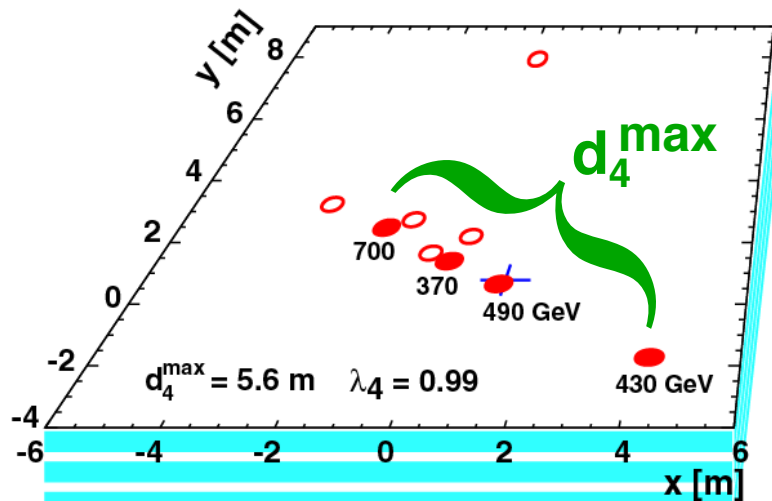
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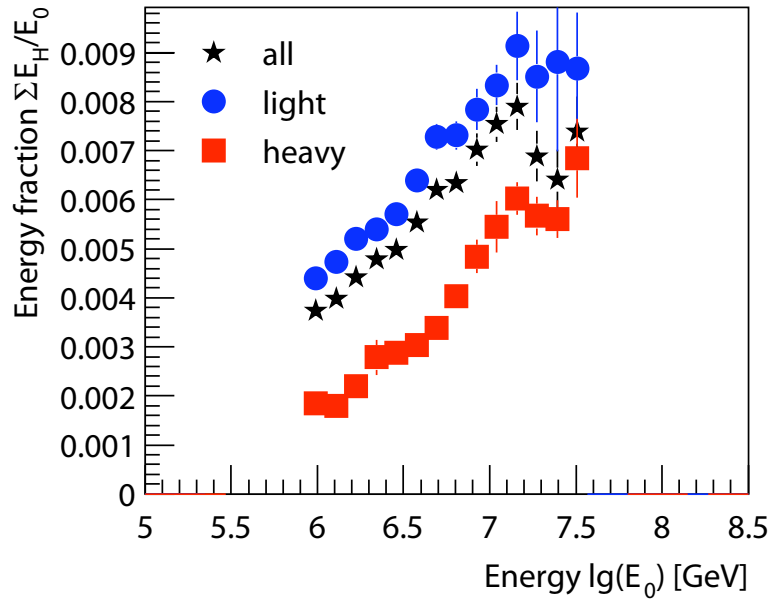
# Transverse momentum in hadronic interactions



# Transverse momentum in hadronic interactions



# Attenuation length of hadrons in air showers

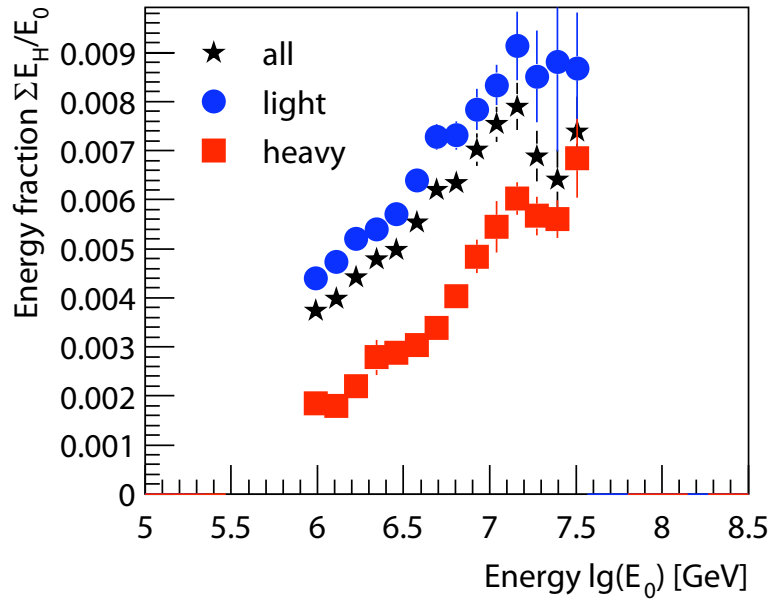


fraction of energy which reaches the ground in form of hadrons

$$R = \frac{\sum E_H}{E_0}$$

$$\lg E_0 \approx 0.19 \lg N_e + 0.79 \lg N'_\mu + 2.33.$$

# Attenuation length of hadrons in air showers

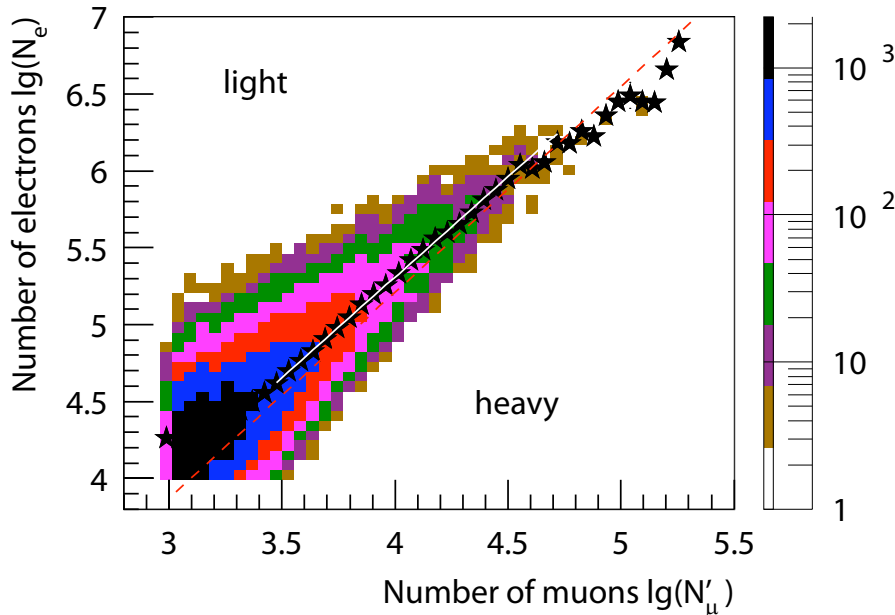


fraction of energy which reaches the ground in form of hadrons

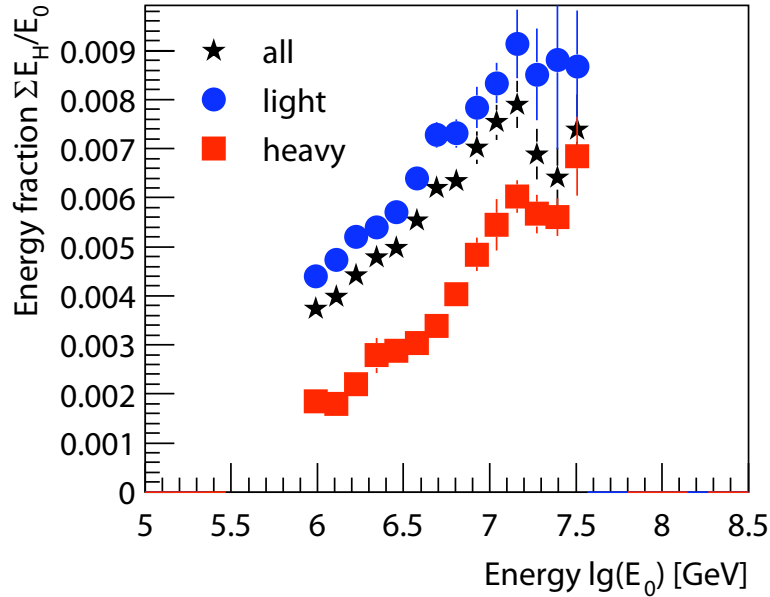
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use  $N_e$  and  $N'_\mu$  to select „light“ and „heavy“ component



# Attenuation length of hadrons in air showers

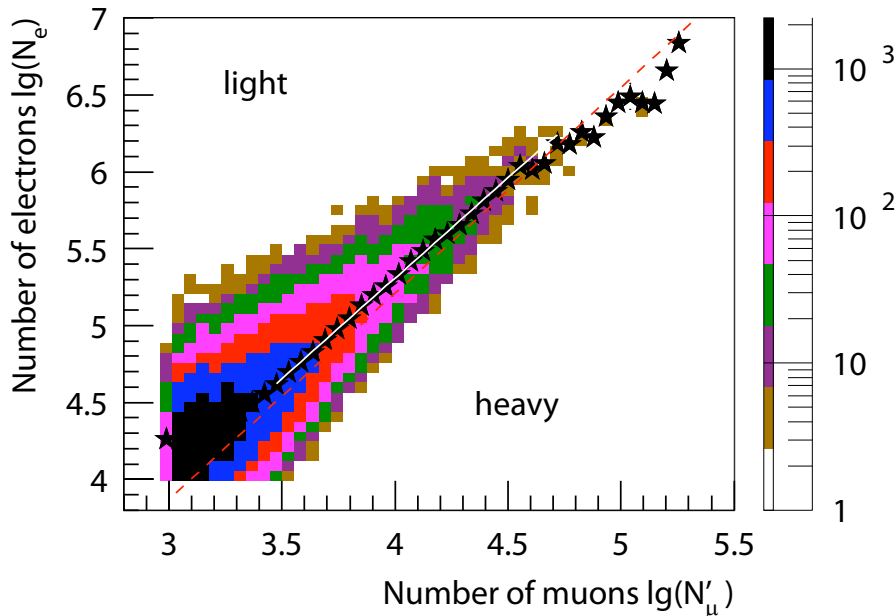


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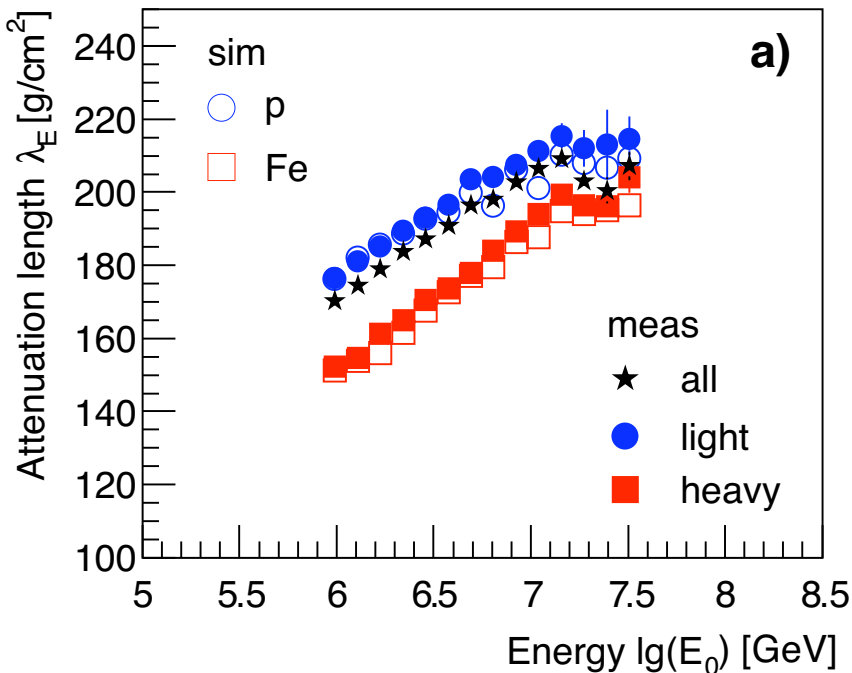


define attenuation length as

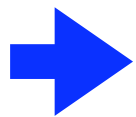
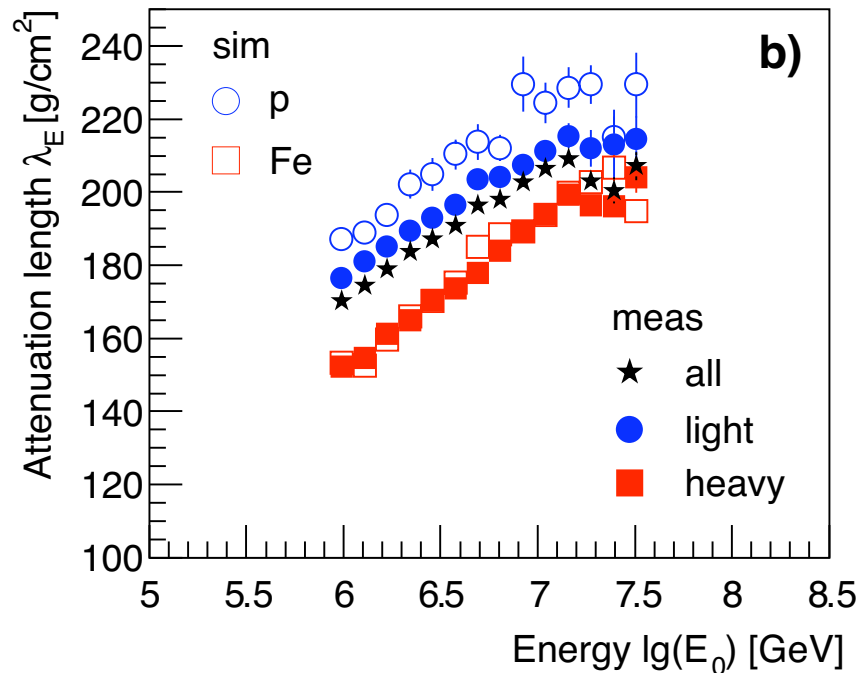
$$R = \exp - \left( \frac{X}{\lambda} \right)$$

# Attenuation length of hadrons in air showers

## QGSJET 01



## QGSJET 01 modified with lower inelastic cross sections



**method very sensitive to inelastic cross sections**

$$\sigma_{p-air} - 5\% \text{ at } 10^6 \text{ GeV}$$
$$\epsilon + 12\%$$





# Test of hadronic interaction models with air shower data

## air shower data ...

- are used for quantitative tests of hadronic interaction models
- are used to improve interaction models
- provide information on hadronic interactions beyond accelerator range