

Models with low scale gravity and low scale strings

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- 1 Motivations, mass hierarchy and low UV scale proposals
- 2 Main experimental predictions
- 3 Models and phenomenology of low string scale

Mass hierarchy problem

Higgs mass: very sensitive to high energy physics $m_H \sim \text{UV cutoff } \Lambda$

why gravity is so weak compared to the other interactions? $\Lambda = M_P$

Possible answer (alternative to supersymmetry): Low UV cutoff $\Lambda \sim \text{TeV}$

- low scale gravity \Rightarrow

large extra dimensions, warped dimensions, DGP localized gravity

- low string scale \Rightarrow low scale gravity, ultra weak string coupling

Experimentally testable framework:

- spectacular model independent predictions

- radical change of high energy physics at the TeV scale

explicit model building is not necessary at this moment

but unification has to be probably dropped

Type I string theory \Rightarrow D-brane world

- gravity: closed strings
- gauge interactions: open strings
with their ends attached on membranes

Dirichlet branes or D-branes

Dimensions of finite size: n transverse
calculability $\Rightarrow R_{\parallel} \simeq l_{\text{string}}$; R_{\perp} arbitrary

$6 - n$ parallel

$$M_P^2 \simeq \frac{1}{\alpha^2} M_s^{2+n} R_{\perp}^n \quad \alpha = g_s$$

Planck mass in $4 + n$ dims: M_*^{2+n}

small $M_s/M_P \Rightarrow$ extra-large R_{\perp}

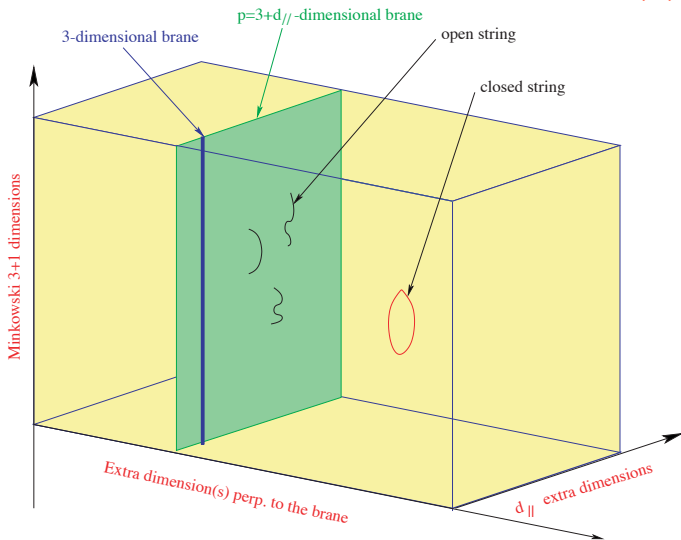
$$M_s \sim 1 \text{ TeV} \Rightarrow R_{\perp} \sim .1 - 10^{-13} \text{ mm} \quad (n = 2 - 6) \text{ [5]}$$

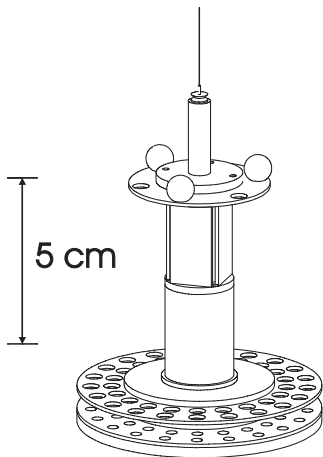
weak string coupling: $g_s = \alpha$ [6]

Braneworld

2 types of compact extra dimensions:

- parallel (d_{\parallel}): $\lesssim 10^{-16}$ cm (TeV) [22]
- transverse (\perp): $\lesssim 0.1$ mm (meV)





$R_{\perp} \lesssim 45 \mu\text{m}$ at 95% CL

- dark-energy length scale $\approx 85 \mu\text{m}$ [3] [18]

string realization of large extra dimensions

I.A.-Arkani Hamed-Dvali-Dimopoulos '98

by 'swiss cheese' Calabi-Yau's ('large volume' compactifications) :

Balasubramanian-Berglund-Cicoli-Conlon-Quevedo-Suruliz '05-'08

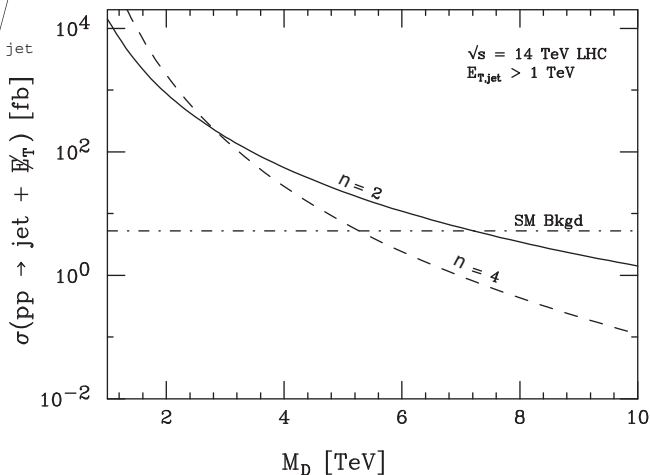
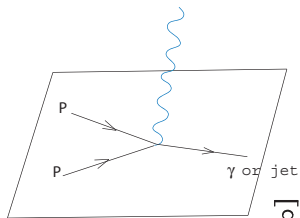
Requirements:

- CY with $h_{21} > h_{11} > 1$
- 3-form fluxes as KKLT
- SM on D7-branes wrapped small cycles
- at least one blow-up mode (point-like singularity)
- blow-up mode fixed by non-perturbative effects
volume by α' -corrections \rightarrow exponentially large



Experimental predictions

- particle accelerators
 - Large TeV dimensions seen by SM gauge interactions
 - ⇒ KK resonances of SM gauge bosons I.A. '90
 - see Freitas' talk next
 - Extra large submm dimensions transverse
 - ⇒ missing energy from gravity radiation in the bulk [10]
 - string physics and possible strong gravity effects [12]
- microgravity experiments [18]
 - gravity modifications at short distances
 - new submillimeter forces



Angular distribution \Rightarrow spin of the graviton

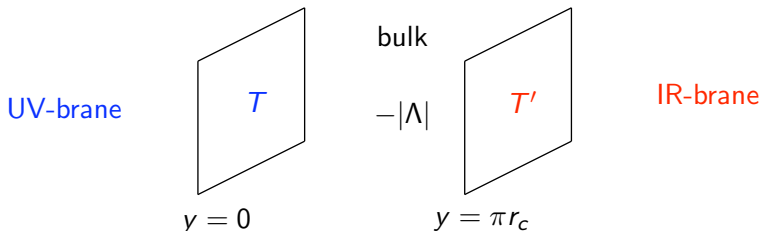
Limits on R_{\perp} in mm

Experiment	$R_{\perp}(n=2)$	$R_{\perp}(n=4)$	$R_{\perp}(n=6)$
Collider bounds			
LEP 2	4.8×10^{-1}	1.9×10^{-8}	6.8×10^{-11}
Tevatron	5.5×10^{-1}	1.4×10^{-8}	4.1×10^{-11}
LHC	4.5×10^{-3}	5.6×10^{-10}	2.7×10^{-12}
NLC	1.2×10^{-2}	1.2×10^{-9}	6.5×10^{-12}
Astrophysics/cosmology bounds			
SN1987A	3×10^{-4}	1×10^{-8}	6×10^{-10}
COMPTEL	5×10^{-5}	-	-

Randal Sundrum models

spacetime = slice of AdS_5 our universe = 4d flat boundary

$$ds^2 = e^{-2k|y|} \eta_{\mu\nu} dx^\mu dx^\nu + dy^2$$



- fine-tuned tensions: $T = -T' = 24M^3k^2$ $\Lambda = -24M^3k^2$
- exponential hierarchy: $M_W = M_P e^{-2\pi k r_c}$ $M_P^2 \sim M^3/k$
- 4d gravity localized on the UV-brane, but KK gravitons on the IR

- main prediction: spin-2 resonances at the TeV scale

$$m_n = c_n k e^{-2\pi k r_c} \quad c_n \simeq (n + 1/4) \text{ for large } n$$

$$\text{weakly coupled for } m_n < M e^{-2\pi k r_c} \quad \Rightarrow k < M$$

- viable models: Standard Model gauge bosons in the bulk, fermions near the UV-brane, Higgs on the IR-brane
- AdS/CFT duals to strongly coupled 4d field theories

$$\text{composite Higgs models, technicolor-type} \quad g_{YM} = M/k > 1 \quad [7]$$

Massive string vibrations

indirect effects: virtual exchanges \Rightarrow effective interactions

e.g. four-fermion operators

Actual limits: Matter fermions on

• same set of branes $\Rightarrow M_s \gtrsim 500$ GeV dim-8: $\frac{g^2}{M_s^4}(\bar{\psi}\partial\psi)^2$

• brane intersections $\Rightarrow M_s \gtrsim 2 - 3$ TeV dim-6: $\frac{g^2}{M_s^2}(\bar{\psi}\psi)^2$

Cullen-Perelstein-Peskin, I.A.-Benakli-Laugier '00

High energies \Rightarrow

- direct production: string physics

- strong gravity: production of micro-black holes? [17]

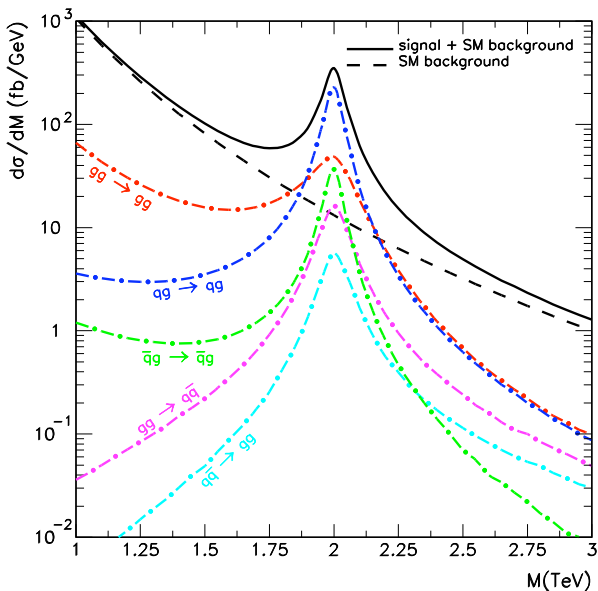
Giddings-Thomas, Dimopoulos-Landsberg '01

Universal deviation
from Standard Model
in jet distribution

$M_s = 2$ TeV

Width = 15-150 GeV

Anchordoqui-Goldberg-
Lüst-Nawata-Taylor-
Stieberger '08 [12]



Tree N -point superstring amplitudes in 4 dims

involving at most 2 fermions and gluons:

completely model independent for any string compactification

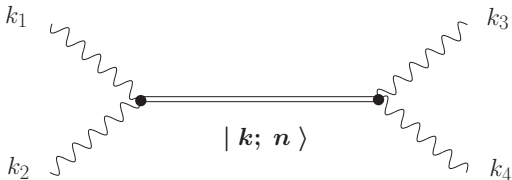
any number of supersymmetries, even none

No intermediate exchange of KK, windings or graviton emission

Universal sum over infinite exchange of string Regge (SR) excitations:

masses: $M_n^2 = M_s^2 n$

maximal spin: $n + 1$

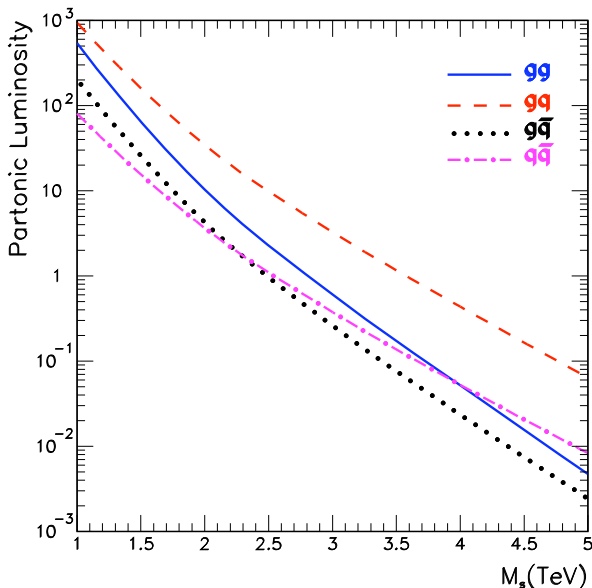


Parton luminosities in pp
above TeV

are dominated by gq , gg
 \Rightarrow model independent [13]

$gq \rightarrow gq$

$gg \rightarrow gg, gg \rightarrow q\bar{q}$



Cross sections

$$\left. \begin{array}{l} |\mathcal{M}(gg \rightarrow gg)|^2, \quad |\mathcal{M}(gg \rightarrow q\bar{q})|^2 \\ |\mathcal{M}(q\bar{q} \rightarrow gg)|^2, \quad |\mathcal{M}(qg \rightarrow qg)|^2 \end{array} \right\}$$

model independent
for any compactification

Lüst-Stieberger-Taylor '08

$$|\mathcal{M}(gg \rightarrow gg)|^2 = g_{YM}^4 \left(\frac{1}{s^2} + \frac{1}{t^2} + \frac{1}{u^2} \right) \times \left[\frac{9}{4} (s^2 V_s^2 + t^2 V_t^2 + u^2 V_u^2) - \frac{1}{3} (sV_s + tV_t + uV_u)^2 \right]$$

$$|\mathcal{M}(gg \rightarrow q\bar{q})|^2 = g_{YM}^4 \frac{t^2 + u^2}{s^2} \left[\frac{1}{6} \frac{1}{tu} (tV_t + uV_u)^2 - \frac{3}{8} V_t V_u \right] \quad M_s = 1$$

$$V_s = -\frac{tu}{s} \quad B(t, u) = 1 - \frac{2}{3}\pi^2 tu + \dots \quad V_t : s \leftrightarrow t \quad V_u : s \leftrightarrow u$$

YM limits agree with e.g. book "*Collider Physics*" by Barger, Phillips

Energy threshold for black hole production :

$$E_{\text{BH}} \simeq M_s/g_s^2 \quad \leftarrow \text{string coupling}$$

Horowitz-Polchinski '96, Meade-Randall '07

- string size black hole: $r_H \sim l_s = M_s^{-1}$
- black hole mass: $M_{\text{BH}} \sim r_H^{d-3}/G_N$ $G_N \sim l_s^{d-2} g_s^2$

weakly coupled theory \Rightarrow strong gravity effects occur much above M_s , M_*

$$g_s \simeq \alpha_{\text{YM}} \sim 0.1 \quad ; \quad \text{Regge excitations : } M_n^2 = M_s^2 n \Rightarrow$$

 gauge coupling

Energy threshold of n -th string excitation: $E_n \simeq M_s \sqrt{n} \Rightarrow$

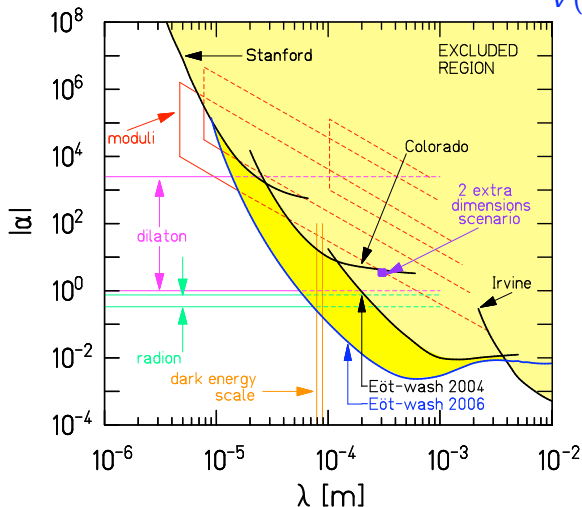
production of $n \sim 1/g_s^4 \sim 10^4$ string states before reach E_{BH} [7]

SUSY in the bulk?

- global SUSY: no need to be there **at least for hierarchy**
- SUGRA: probably unbroken in the bulk \Rightarrow
very weakly broken (volume suppressed)
New forces at submm scales **e.g. radion, gauge fields**
- Radion $\equiv \ln V_{\perp}$
 - mass: $(\text{TeV})^2/M_P \sim 10^{-4} \text{ eV} \rightarrow \text{mm range}$
 - coupling: $\frac{1}{m} \frac{\partial m}{\partial \ln V_{\perp}} = \sqrt{\frac{n}{n+2}} \times \text{gravity}$ **I.A.-Benakli-Maillard-Laugier '02** \Rightarrow can be experimentally tested for all $n \geq 2$ [5]
- Light $U(1)$ gauge bosons: no derivative couplings
 \Rightarrow for the same mass much stronger than gravity: $\gtrsim 10^6$

Experimental limits on short distance forces

$$V(r) = -G \frac{m_1 m_2}{r} (1 + \alpha e^{-r/\lambda})$$

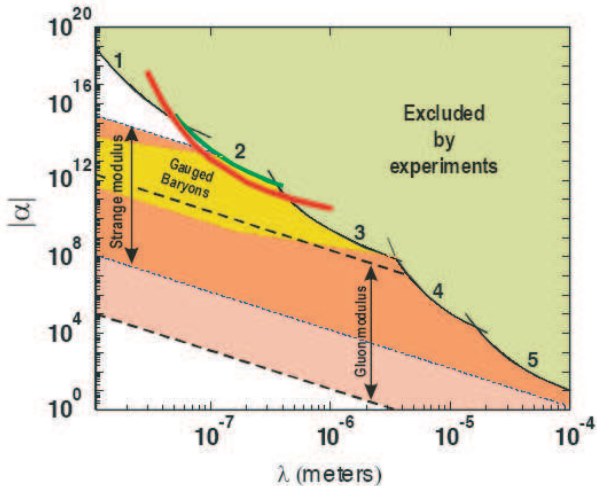


Radion $\Rightarrow M_* \gtrsim 6 \text{ TeV}$ 95% CL

Adelberger et al. '06

an order of magnitude improvement in the range 10-200 nm

Decca et al '07



5: Colorado

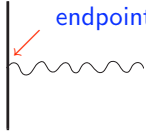
4: Stanford

3: Lamoureaux

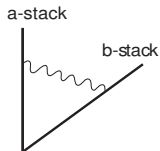
1: Mohideen et al.

A D-brane embedding of the Standard Model

Generic spectrum: N coincident branes $\Rightarrow U(N)$

a-stack

endpoint transformation: \mathbf{N}_a or $\bar{\mathbf{N}}_a$ $U(1)_a$ charge: +1 or -1
 \Rightarrow "baryon" number

- open strings from the same stack \Rightarrow adjoint gauge multiplets of $U(N_a)$
- stretched between two stacks \Rightarrow bifundamentals of $U(N_a) \times U(N_b)$



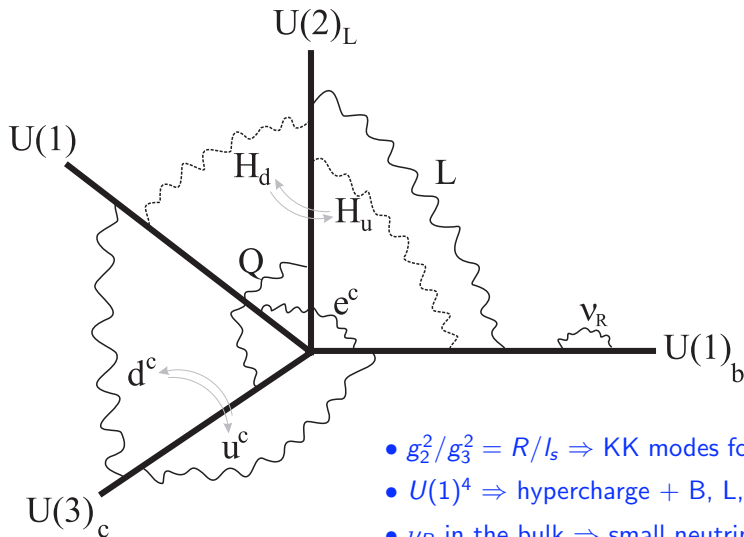
- oriented strings \Rightarrow need at least 4 brane-stacks

- existence of bulk with large dimensions \Rightarrow

minimal choice: $U(3) \times U(2) \times U(1) \times U(1)_{\text{bulk}}$


color branes (g_3)


weak branes (g_2)



- $g_2^2/g_3^2 = R/l_s \Rightarrow$ KK modes for $SU(2)_L$ [4] [26]
- $U(1)^4 \Rightarrow$ hypercharge + B, L, PQ global
- ν_R in the bulk \Rightarrow small neutrino masses [24]
- $U(1)$ on top of $U(2)$ or $U(3)$ \Rightarrow prediction for $\sin^2 \theta_W$ [25]

The remaining three $U(1)$'s : anomalous

Green-Schwarz anomaly cancellation \Rightarrow

- they become massive (absorb three axions)

gauge field: $\delta A = d\Lambda \Rightarrow$ axion: $\delta a = -M\Lambda$

$$-\frac{1}{4g_A^2} F_A^2 - \frac{1}{2} (da + MA)^2 + \frac{a}{M} k_I^A \text{Tr} F_I \wedge F_I$$

\swarrow cancel the anomaly

$\Rightarrow U(1)_A$ mass: $m_A = g_A M$

- the global symmetries remain in perturbation

- Baryon number \Rightarrow proton stability

- Lepton number \Rightarrow protect small neutrino masses

no Lepton number $\Rightarrow \frac{1}{M_s} LLHH \rightarrow$ Majorana mass: $\frac{\langle H \rangle^2}{M_s} LL$

$\swarrow \sim \text{GeV}$

R-neutrinos: open strings in the bulk

R-neutrino: $\nu_R(x, y)$ y : bulk coordinates

Arkani Hamed-Dimopoulos-Dvali-March Russell '98

Dienes-Dudas-Gherghetta '98

$$S_{int} = g_s \int d^4x H(x) L(x) \nu_R(x, y = 0)$$

$$\langle H \rangle = v \Rightarrow \text{mass-term: } \frac{g_s v}{R_{\perp}^{n/2}} \nu_L \nu_R^0 \leftarrow 4\text{d zero-mode}$$

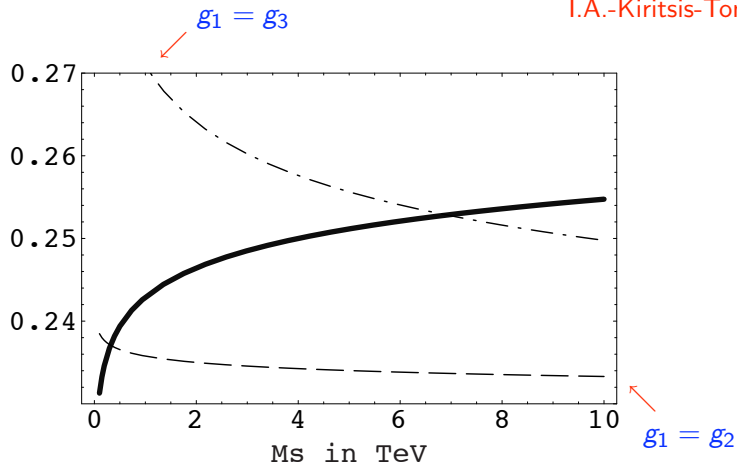
$$\text{Dirac neutrino masses: } m_{\nu} \simeq \frac{g_s v}{R_{\perp}^{n/2}} \simeq v \frac{M_s}{M_p}$$

$$\simeq 10^{-3} - 10^{-2} \text{ eV for } M_s \simeq 1 - 10 \text{ TeV}$$

$$m_{\nu} \ll 1/R_{\perp} \Rightarrow \text{KK modes unaffected [22]}$$

$\sin^2 \theta_W(M_S)$

I.A.-Kiritsis-Tomaras '00



\Rightarrow correct prediction for $\sin^2 \theta_W$ for $M_S \sim$ a few TeV

Conclusions

TeV strings and large extra dimensions: **Physical reality or imagination?**

- Well motivated theoretical framework
with many testable experimental predictions
new resonances, missing energy
- Stimulus for micro-gravity experiments
look for new forces at short distances
higher dim graviton, scalars, gauge fields

But: - unification has to be dropped
- physics is radically changed above string scale

LHC: will explore the physics beyond the Standard Model