

The Particle Higgsaw Puzzle

The background of the slide is a blue gradient with a pattern of interlocking puzzle pieces. In the center, one puzzle piece is missing, revealing a white surface underneath. The missing piece is a complex, irregular shape with several protrusions and indentations, resembling a particle or a specific configuration in a puzzle.

Is LHC finding the missing piece?

Is it the right shape?

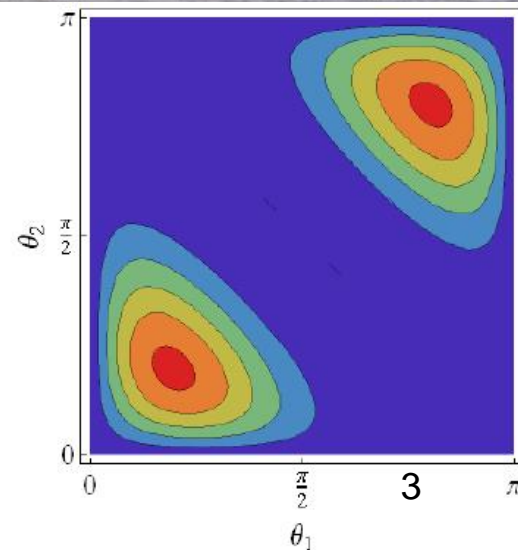
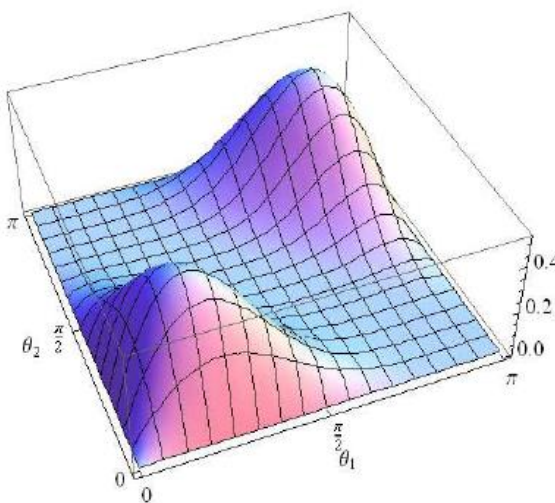
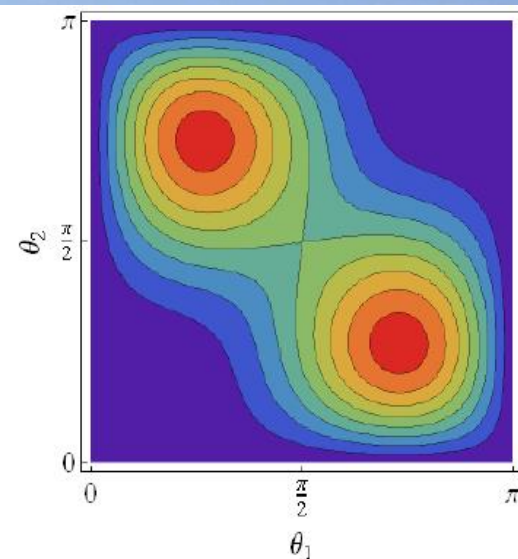
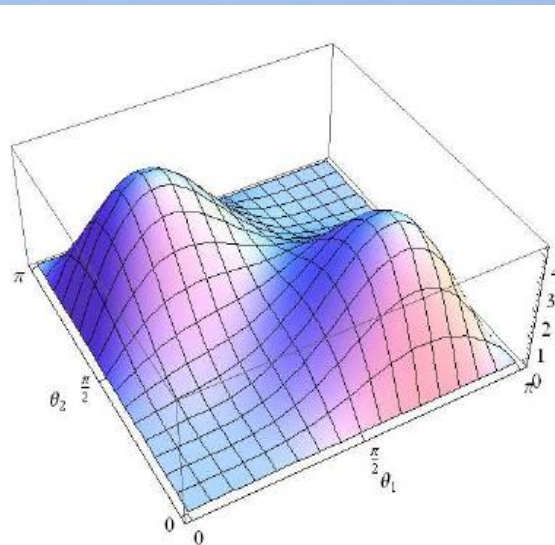
Is it the right size?

What is it ?

- Does it have spin 0 or 2?
- Is it scalar or pseudoscalar?
- Is it elementary or composite?
- Does it couple to particle masses?
- Quantum (loop) corrections?
- What are its self- and other couplings?

Does the 'Higgs' have Spin Zero ?

- Polar angle distribution for $X_2 \rightarrow W^+W^-$
- Polar angle distribution for $X_0 \rightarrow W^+W^-$
(for $\varphi = \pi$)



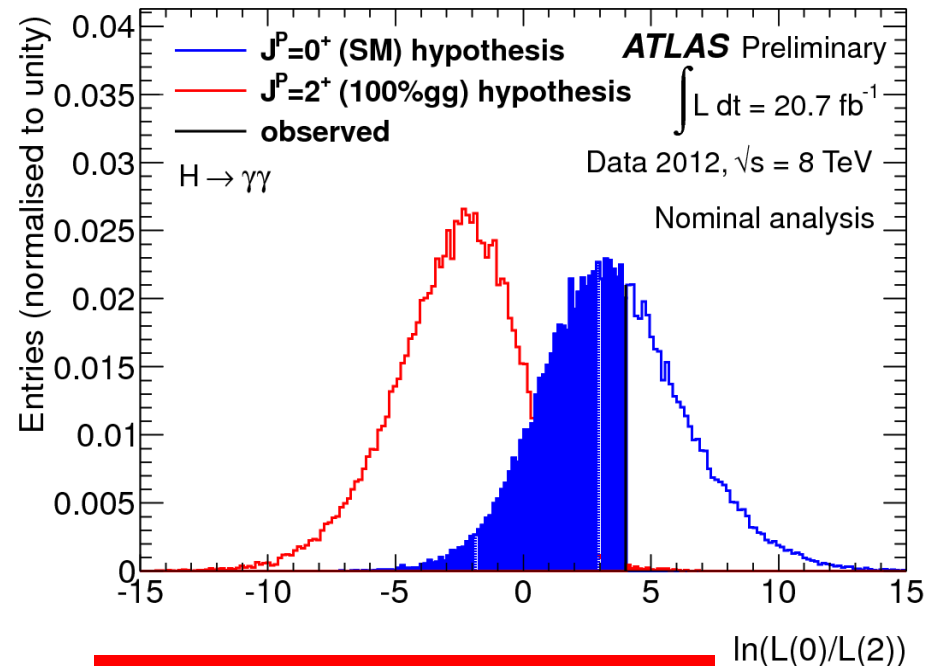
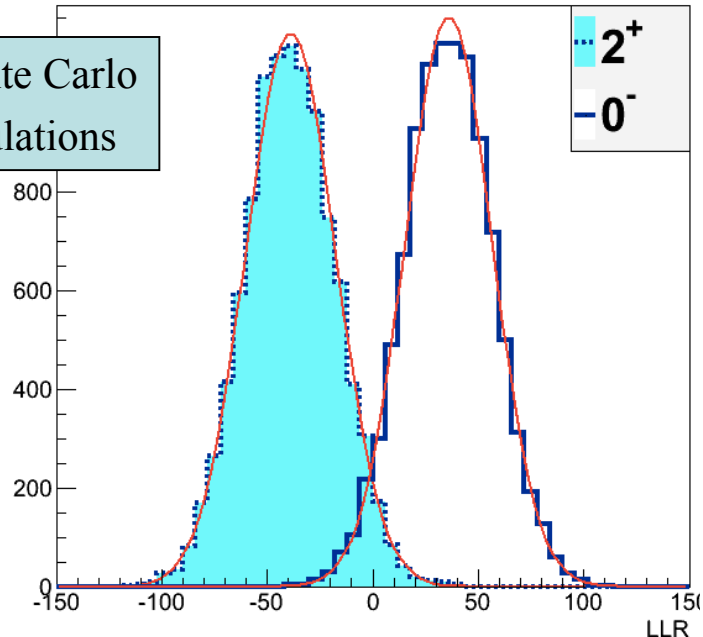
Does the 'Higgs' have Spin Two ?

- Discriminate spin 2 vs spin 0 via angular distribution of decays into $\gamma\gamma$

JE & Hwang: arXiv:1202.6660

$N_{\text{sig}}=160$, High S/B

Monte Carlo simulations

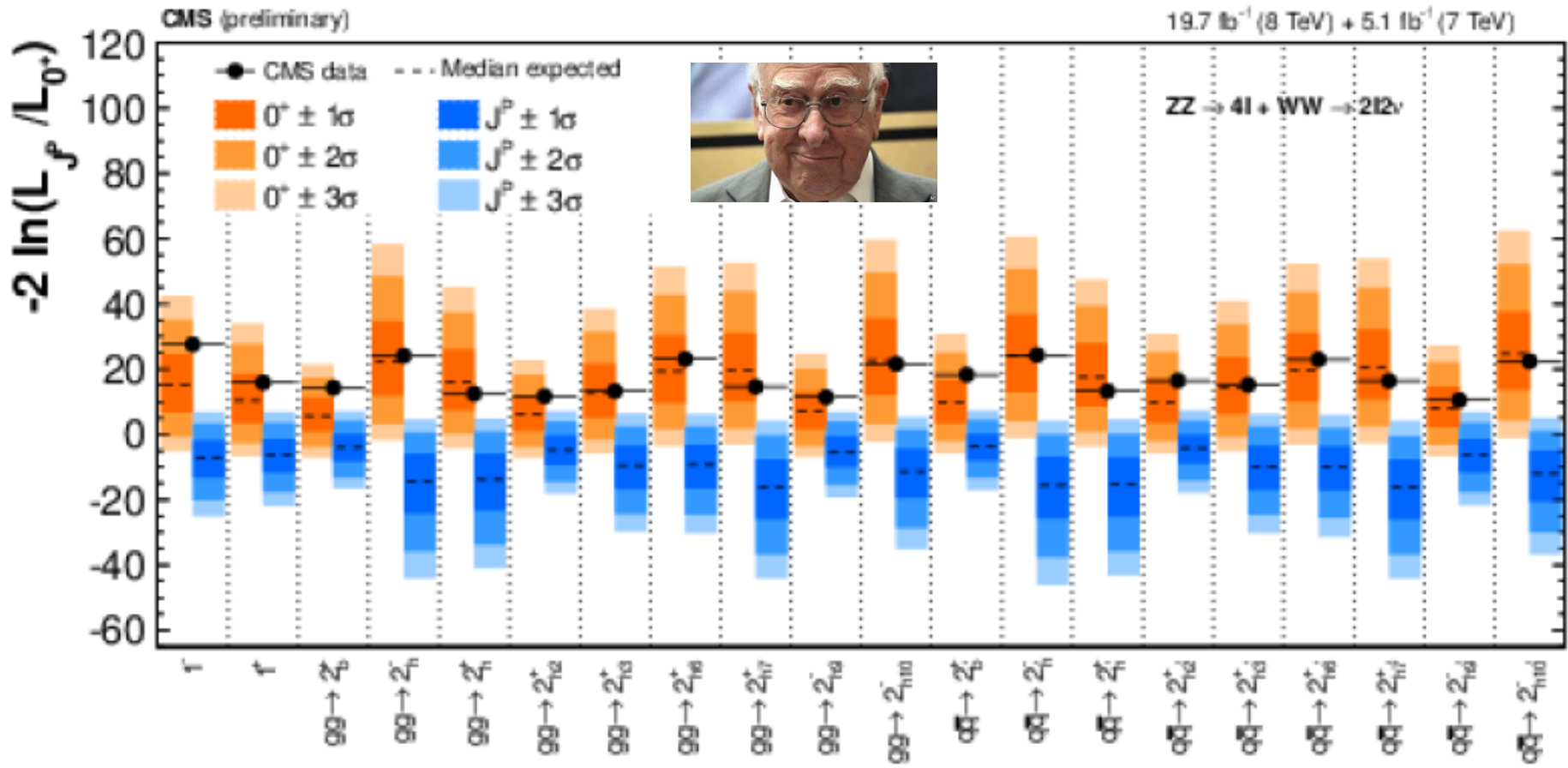


JE, Fok, Hwang, Sanz & You: arXiv:1210.5229

2^+ disfavoured @

99%

The 'Higgs' has Spin 0



- Alternative spin-parity hypotheses disfavoured

What is it ?

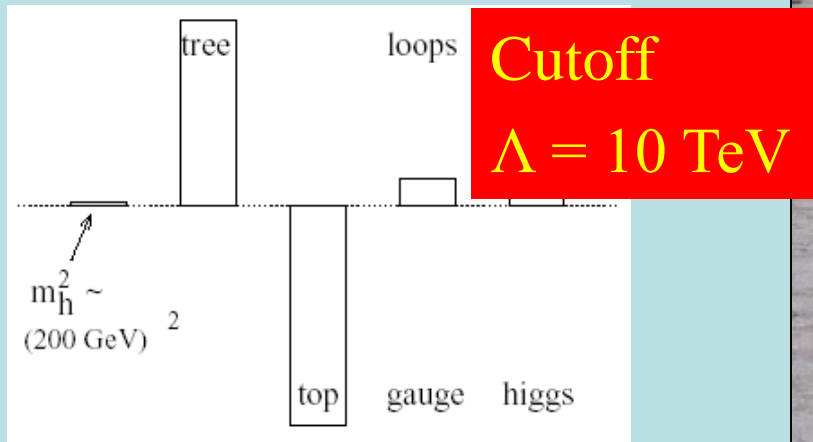
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Elementary Higgs or Composite?

- Higgs field:

$$\langle 0|H|0\rangle \neq 0$$

- Quantum loop problems



Cut-off $\Lambda \sim 1 \text{ TeV}$ with
Supersymmetry?

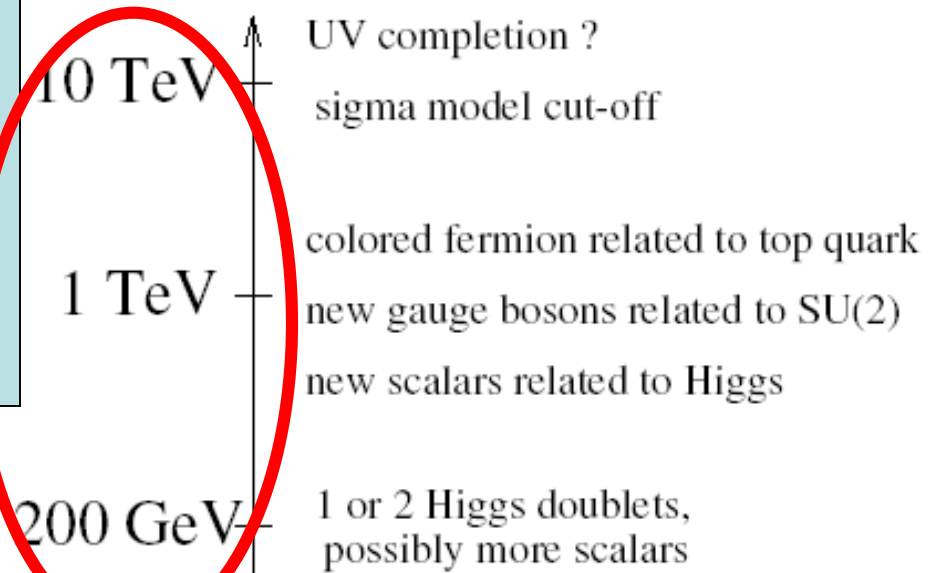
- Fermion-antifermion condensate
- Just like QCD, BCS superconductivity
- Top-antitop condensate? needed $m_t > 200 \text{ GeV}$

New technicolour force?

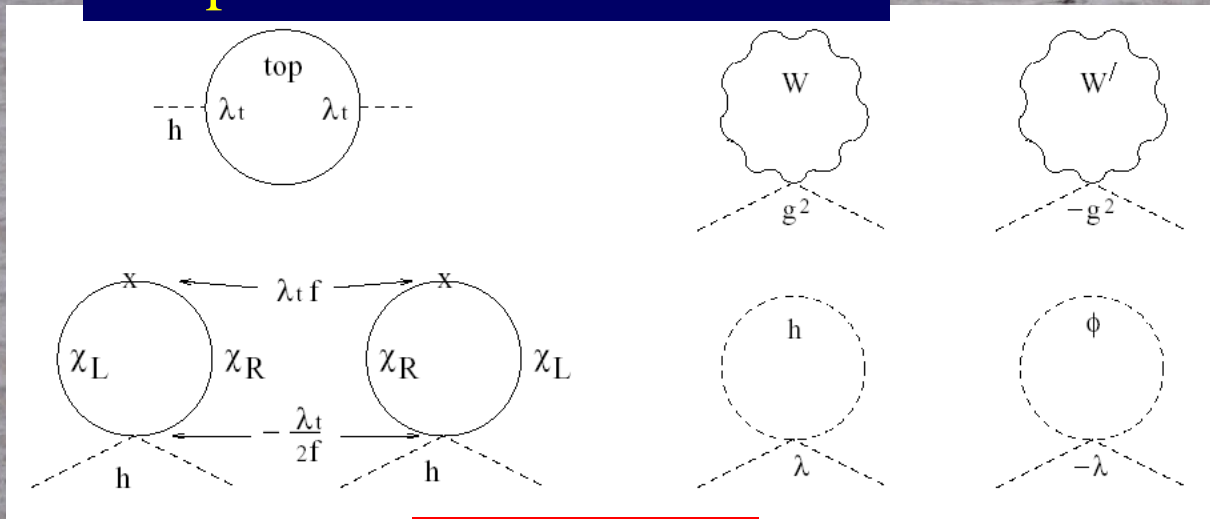
- Heavy scalar resonance?
- Inconsistent with precision electroweak data?

Higgs as a Pseudo-Goldstone Boson

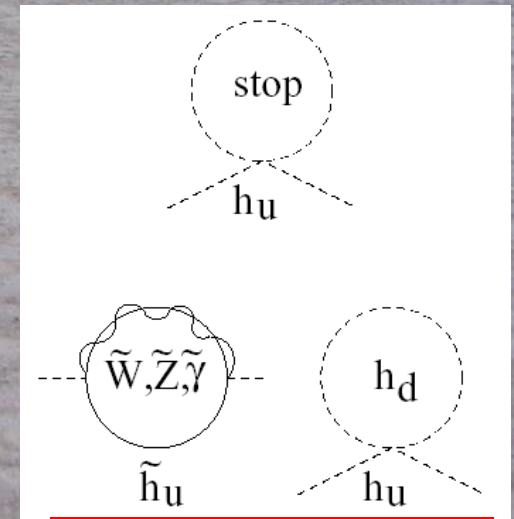
'Little Higgs' models
(breakdown of larger symmetry)



Loop cancellation mechanism



Little Higgs



Supersymmetry

Phenomenological Framework

- Assume custodial symmetry:

$$SU(2) \times SU(2) \rightarrow SU(2)_V \quad (\rho \equiv M_W/M_Z \cos \theta_w \sim 1)$$

- Parameterize gauge bosons by 2×2 matrix Σ :

$$\begin{aligned} \mathcal{L} = & \frac{v^2}{4} \text{Tr} D_\mu \Sigma^\dagger D^\mu \Sigma \left(1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} + \dots \right) - m_i \bar{\psi}_L^i \Sigma \left(1 + c \frac{h}{v} + \dots \right) \psi_R^i + \text{h.c.} \\ & + \frac{1}{2} (\partial_\mu h)^2 + \frac{1}{2} m_h^2 h^2 + d_3 \frac{1}{6} \left(\frac{3m_h^2}{v} \right) h^3 + d_4 \frac{1}{24} \left(\frac{3m_h^2}{v^2} \right) h^4 + \dots \quad , \end{aligned}$$

$$\Sigma = \exp \left(i \frac{\sigma^a \pi^a}{v} \right) \quad \mathcal{L}_\Delta = - \left[\frac{\alpha_s}{8\pi} b_s G_{a\mu\nu} G_a^{\mu\nu} + \frac{\alpha_{em}}{8\pi} b_{em} F_{\mu\nu} F^{\mu\nu} \right] \left(\frac{h}{V} \right)$$

- Coefficients $a = c = 1$ in Standard Model

Examples of Higgs as Pseudo-Goldstone Boson

- Sample models:
- Dependences of couplings on model parameters:
- **To be measured!**
- Translation to experimental parameters:

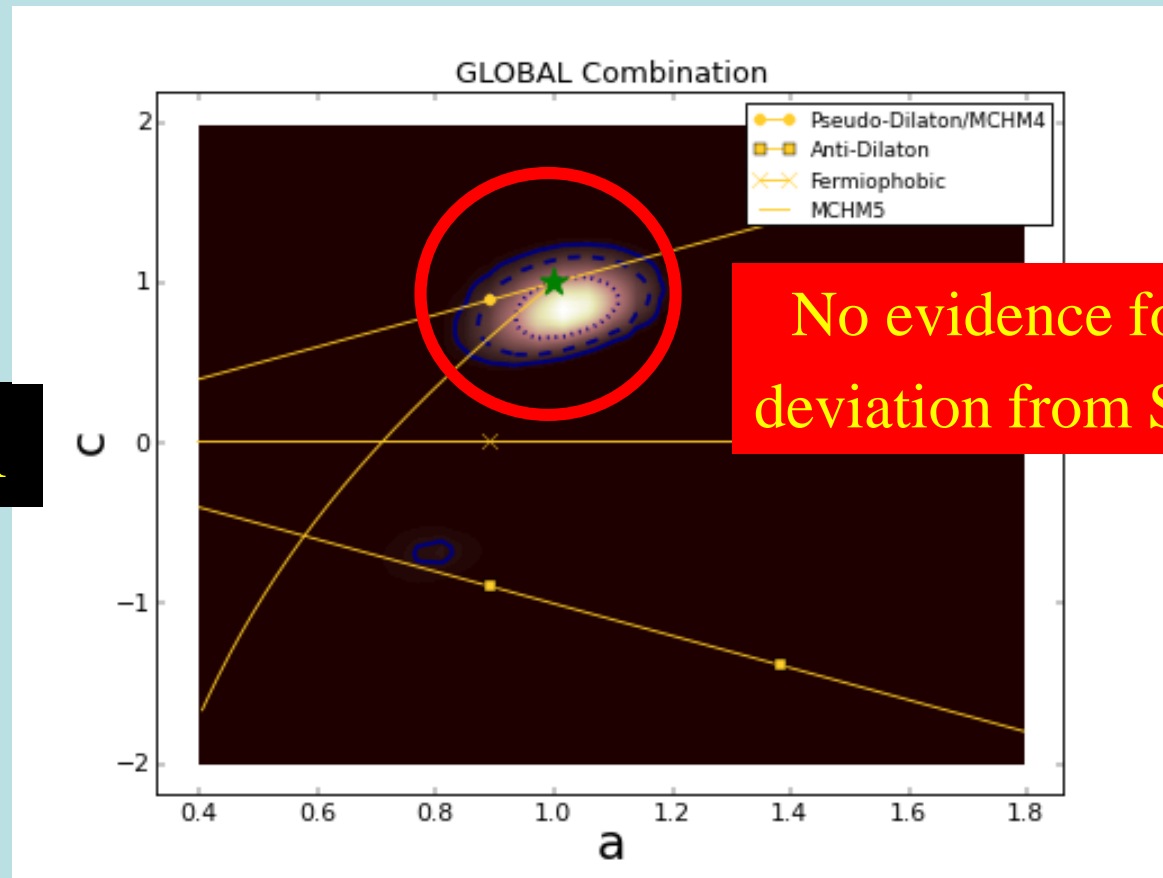
$$a = \kappa_V, \quad c = \kappa_F$$

Model	Symmetry Pattern	Goldstones	
SM	SO(4)/SO(3)	W_L, Z_L	
—	SU(3)/SU(2)×U(1)	W_L, Z_L, h	
MCHM	SO(5)/SO(4)×U(1)	W_L, Z_L, h	
NMCHM	SO(6)/SO(5)×U(1)	W_L, Z_L, h, a	
MCTHM	SO(6)/SO(4)×SO(2)×U(1)	W_L, Z_L, h, H, H^\pm, a	
Parameters	SILH	MCHM4	MCHM5
a	$1 - c_H \xi / 2$	$\sqrt{1 - \xi}$	$\sqrt{1 - \xi}$
b	$1 - 2c_H \xi$	$1 - 2\xi$	$1 - 2\xi$
b_3	$-\frac{4}{3}\xi$	$-\frac{4}{3}\xi \sqrt{1 - \xi}$	$-\frac{4}{3}\xi \sqrt{1 - \xi}$
c	$1 - (c_H/2 + c_y)\xi$	$\sqrt{1 - \xi}$	$\frac{1 - 2\xi}{\sqrt{1 - \xi}}$
c_2	$-(c_H + 3c_y)\xi/2$	$-\xi/2$	-2ξ
d_3	$1 + (c_6 - 3c_H/2)\xi$	$\sqrt{1 - \xi}$	$\frac{1 - 2\xi}{\sqrt{1 - \xi}}$
d_4	$1 + (6c_6 - 25c_H/3)\xi$	$1 - 7\xi/3$	$\frac{1 - 28\xi(1 - \xi)\sqrt{1 - \xi}}{1 - \xi}$

Global Analysis of Higgs-like Models

- Rescale couplings: to bosons by a , to fermions by c

Global

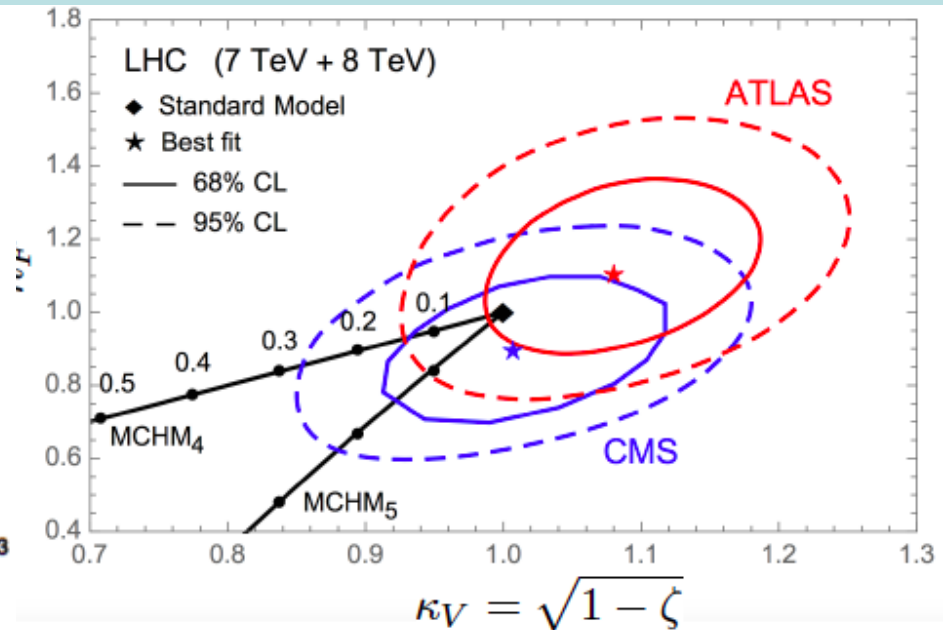
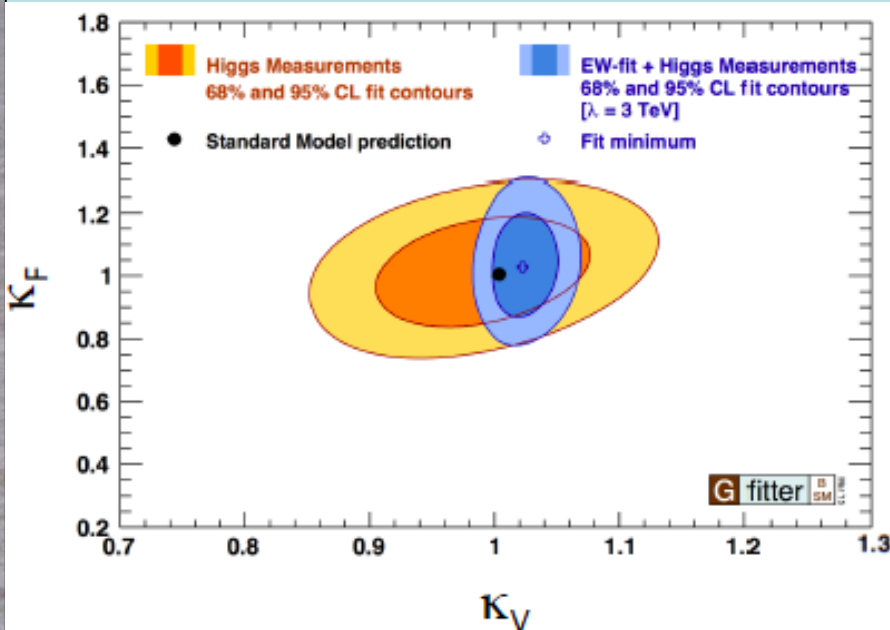


No evidence for deviation from SM

- Standard Model: $a = c = 1$

Global Analysis of Higgs-like Models

- Rescale couplings: to bosons by κ_V , to fermions by κ_f
- Standard Model: $\kappa_V = \kappa_f = 1$



- Consistency between Higgs and EW measurements
- **Must tune composite models to look like SM**

What is it ?

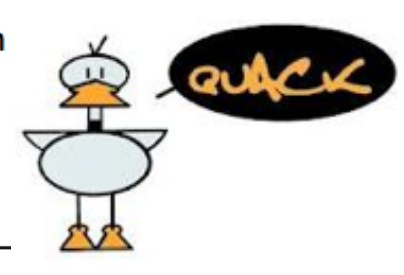
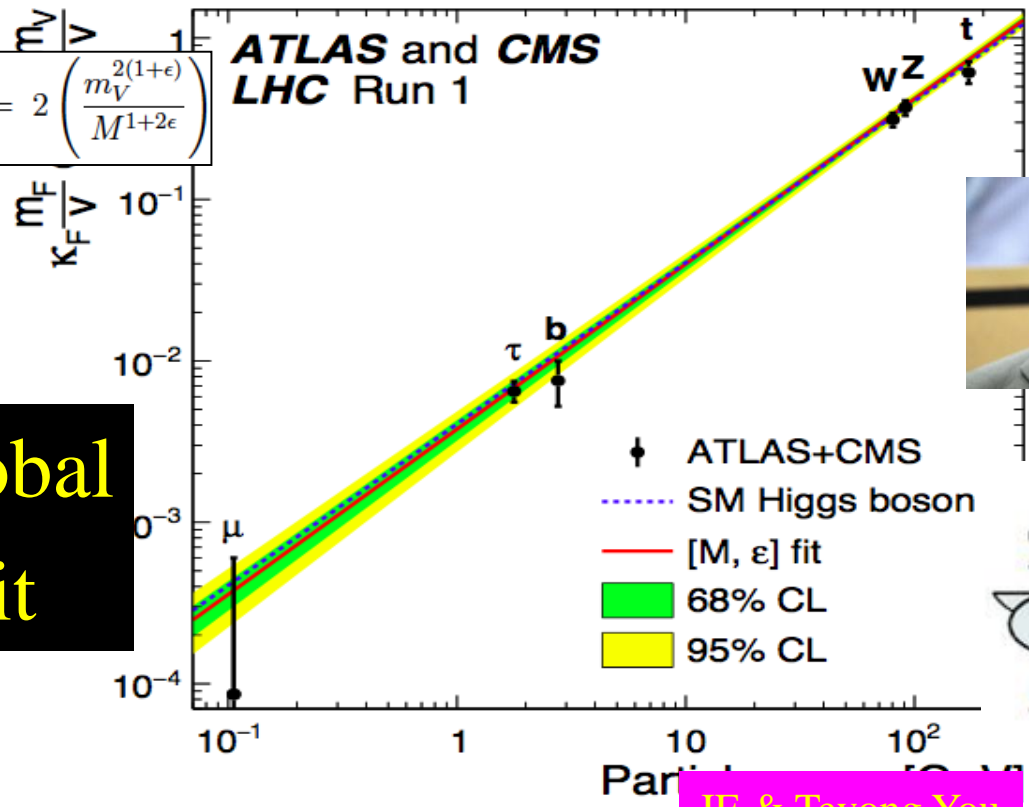
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- Does it couple to particle masses?
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It Walks and Quacks like a Higgs

- Do couplings scale \sim mass? With scale = v ?

$$\lambda_f = \sqrt{2} \left(\frac{m_f}{M} \right)^{1+\epsilon}, \quad g_V = 2 \left(\frac{m_V^{2(1+\epsilon)}}{M^{1+2\epsilon}} \right)$$

Global fit

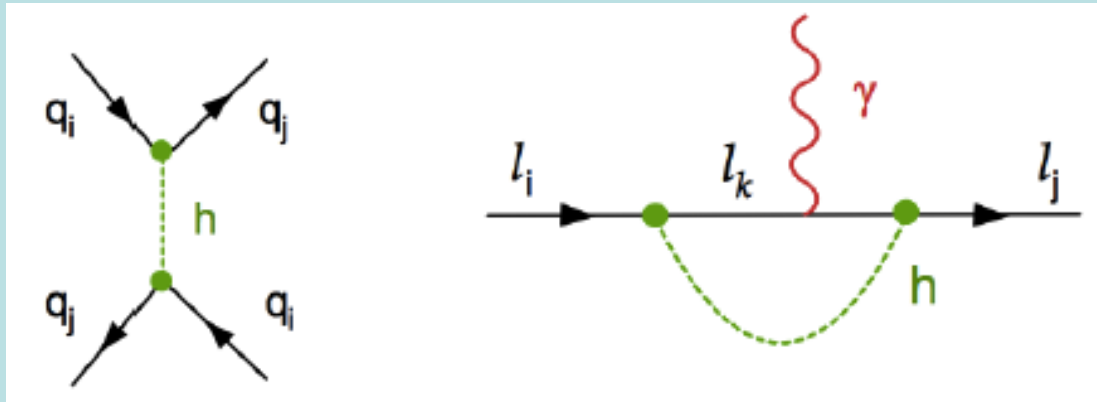


JE & Tevong You

- Blue** dashed line = Standard Model

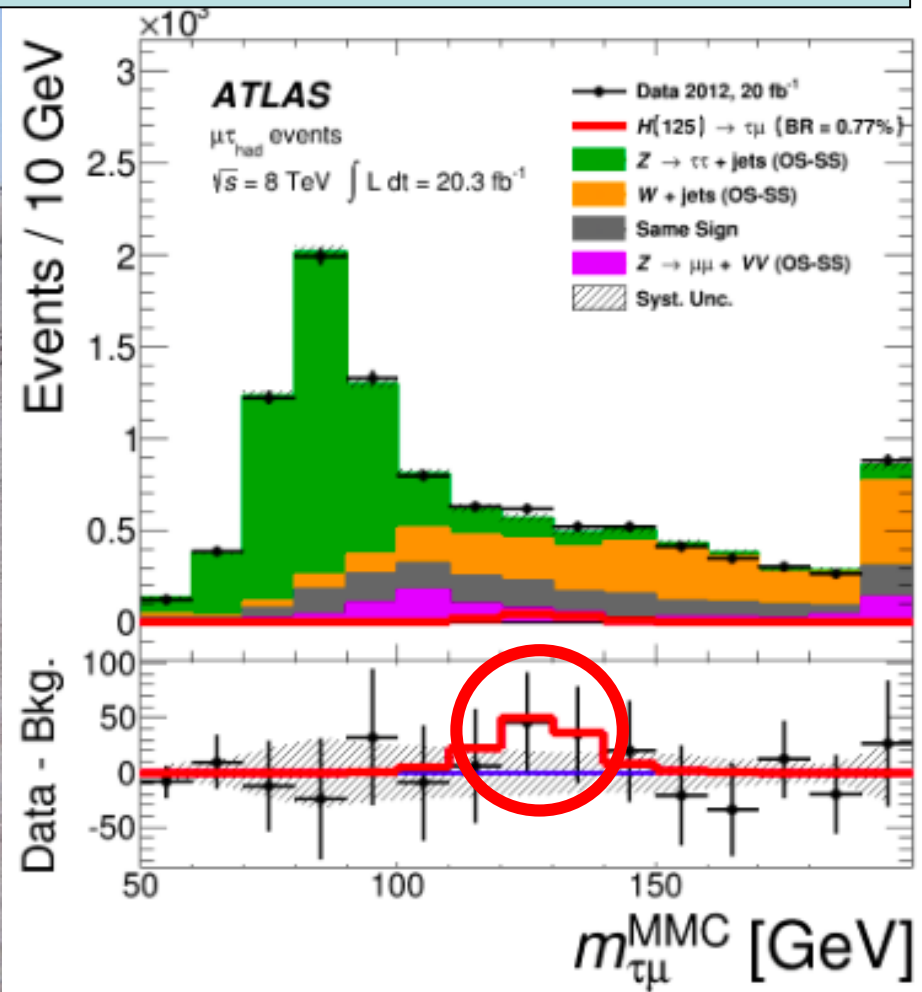
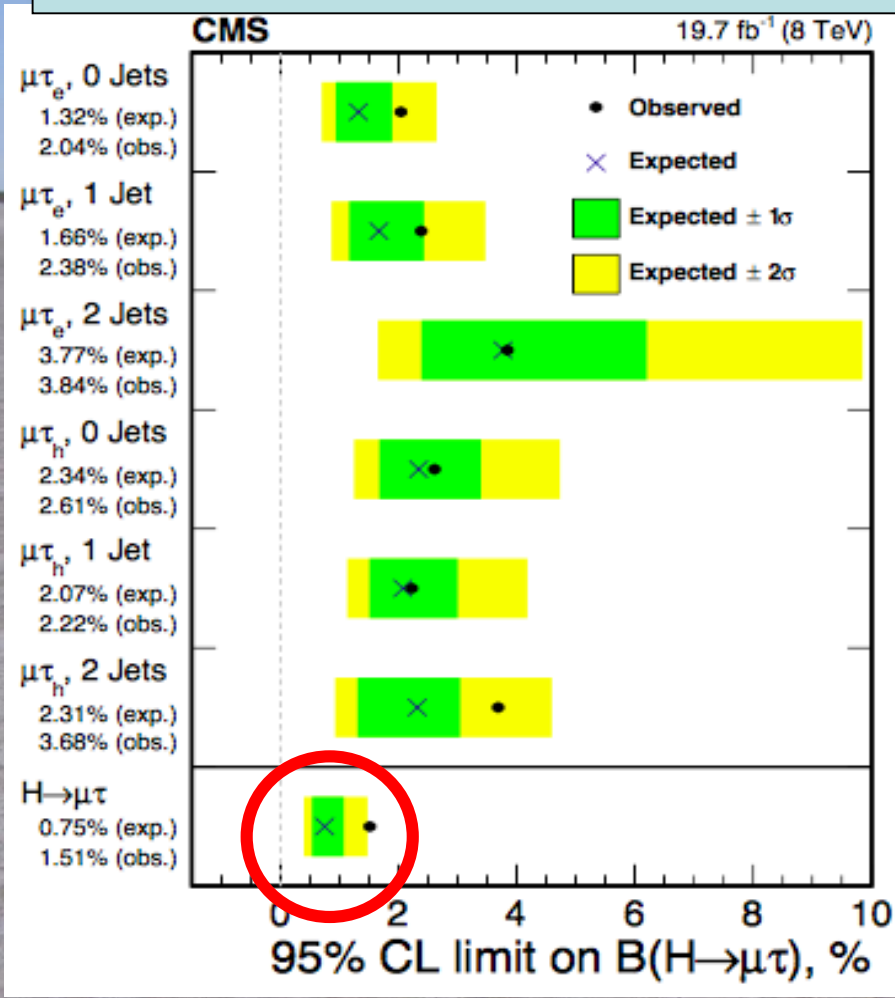
Flavour-Changing Couplings?

- Upper limits from FCNC, EDMs, ...



- Quark FCNC bounds exclude observability of quark-flavour-violating h decays
- Lepton-flavour-violating h decays could be large:
 $BR(\tau\mu)$ or $BR(\tau e)$ could be $O(10)\%$

Flavour-Changing Higgs Coupling?

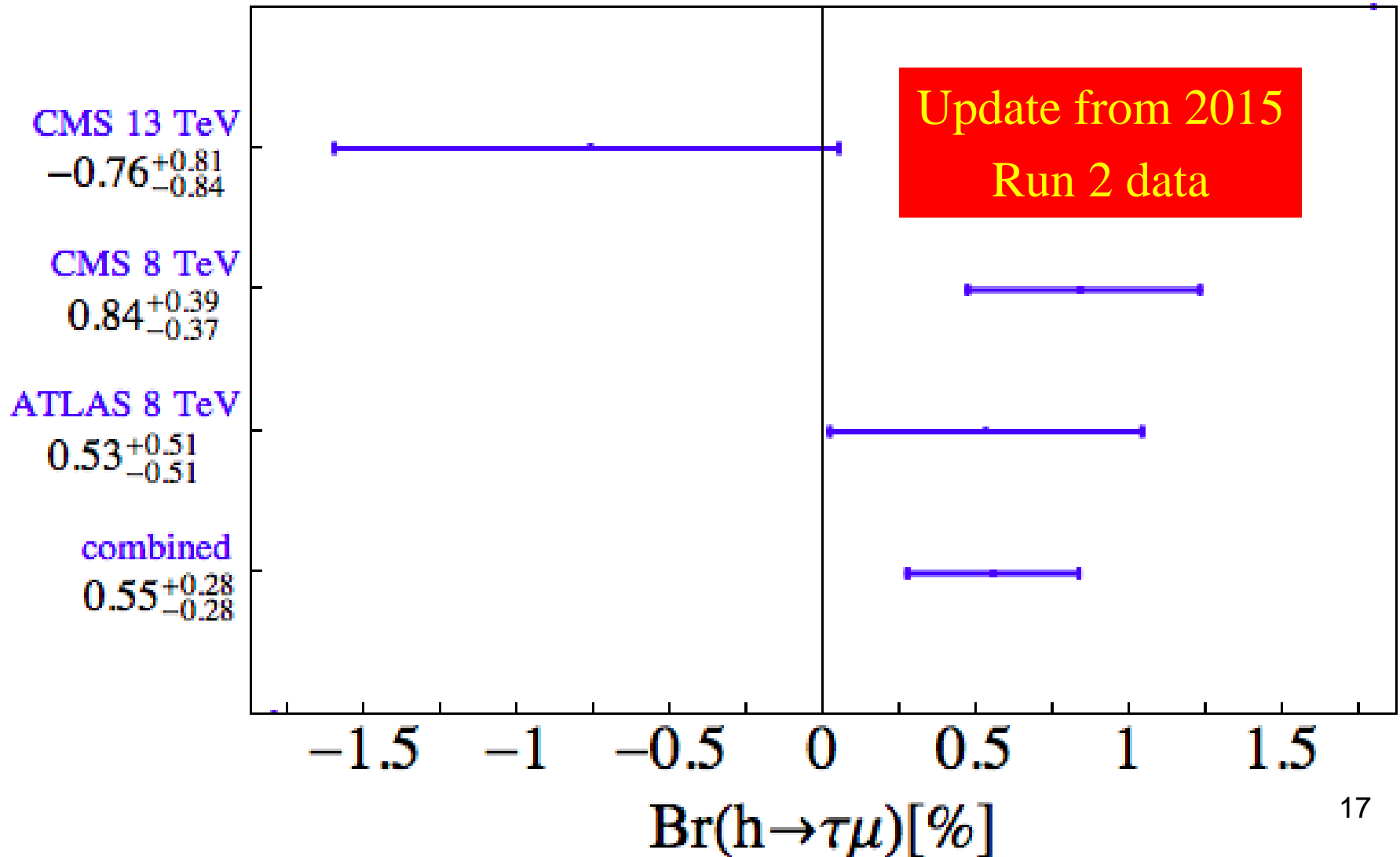


$$B(H \rightarrow \mu\tau) = (0.84^{+0.39}_{-0.37})\%$$

$$\text{Br}(H \rightarrow \mu\tau) = (0.77 \pm 0.62)\%$$

Also: $\text{BR}(e\tau) < 0.69\%$, $\text{BR}(e\mu) < 0.036\%$

Flavour-Changing Higgs Coupling?

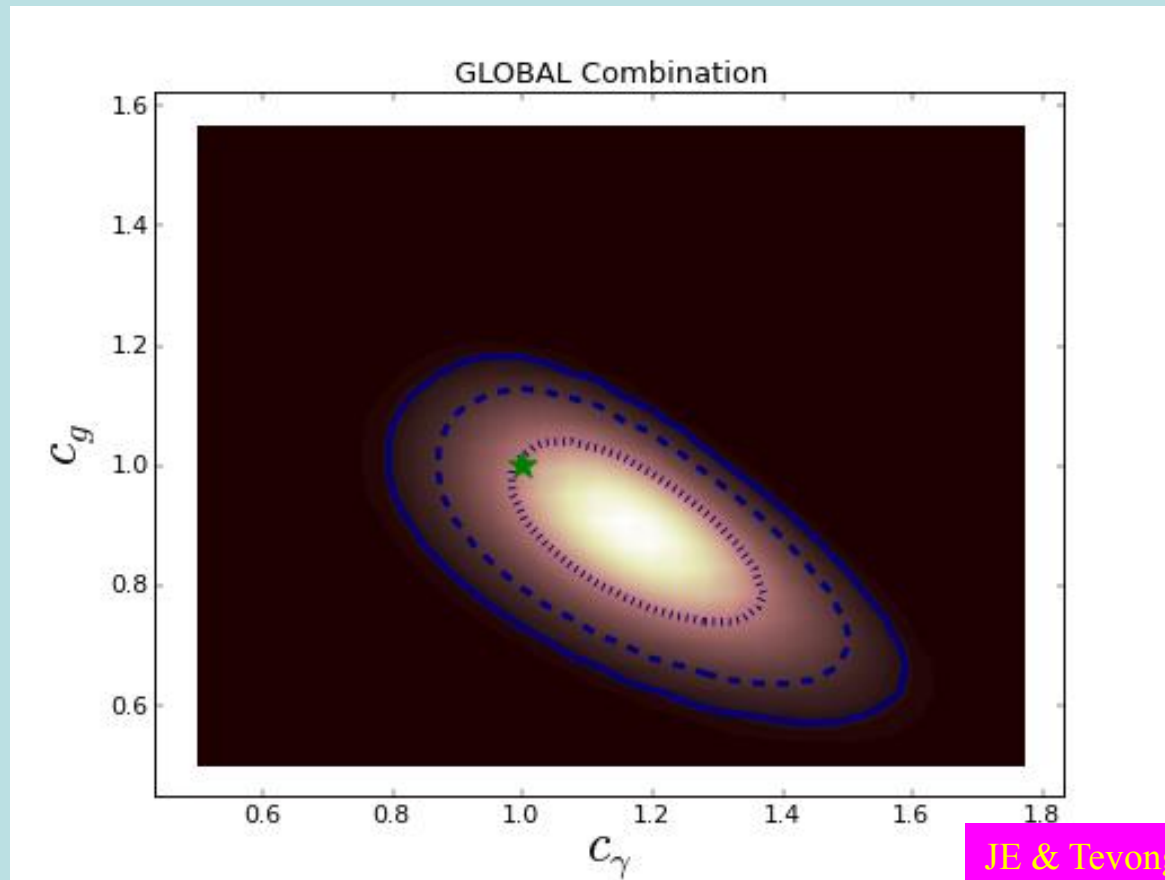


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- Does it couple to particle masses?
 - ***Prima facie* evidence that it does**
- Quantum (loop) corrections?
- What are its self- and other couplings?

Loop Corrections ?

- Combination of data on $\gamma\gamma$, gluon-gluon couplings



JE & Tevong You, arXiv:1303.3879

- Loop diagrams ~ Standard Model?

What is it ?

H^0

$J = 0$

Mass $m = 125.09 \pm 0.24$ GeV

H^0 Signal Strengths in Different Channels

See Listings for the latest unpublished results.

Combined Final States = 1.17 ± 0.17 (S = 1.2)

$W W^* = 0.81 \pm 0.16$

$Z Z^* = 1.15^{+0.27}_{-0.23}$ (S = 1.2)

$\gamma\gamma = 1.17^{+0.19}_{-0.17}$

$b\bar{b} = 0.85 \pm 0.29$

$\mu^+ \mu^- < 7.0$, CL = 95%

$\tau^+ \tau^- = 0.79 \pm 0.26$

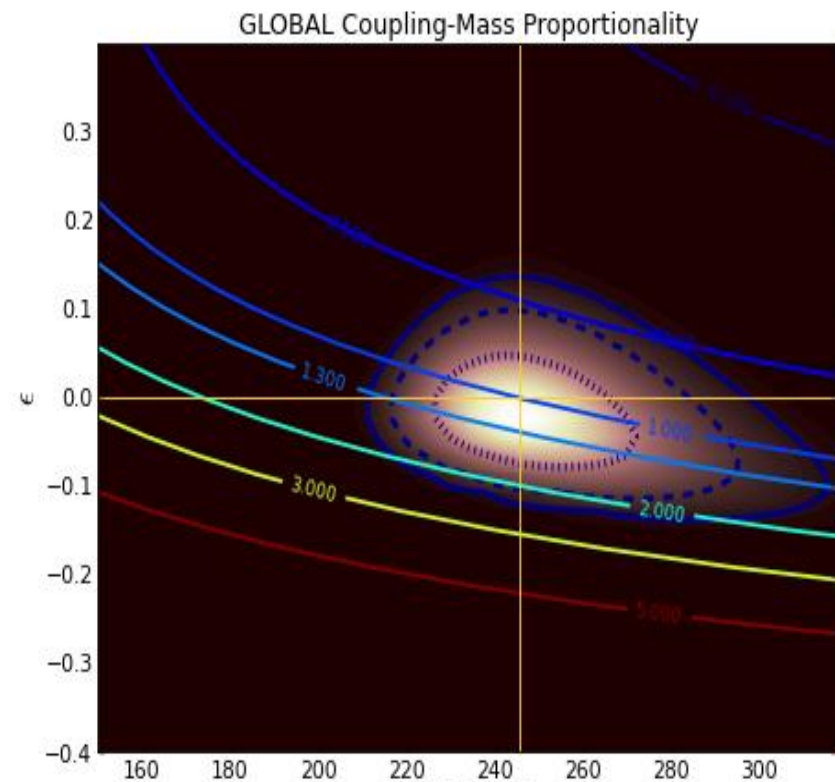
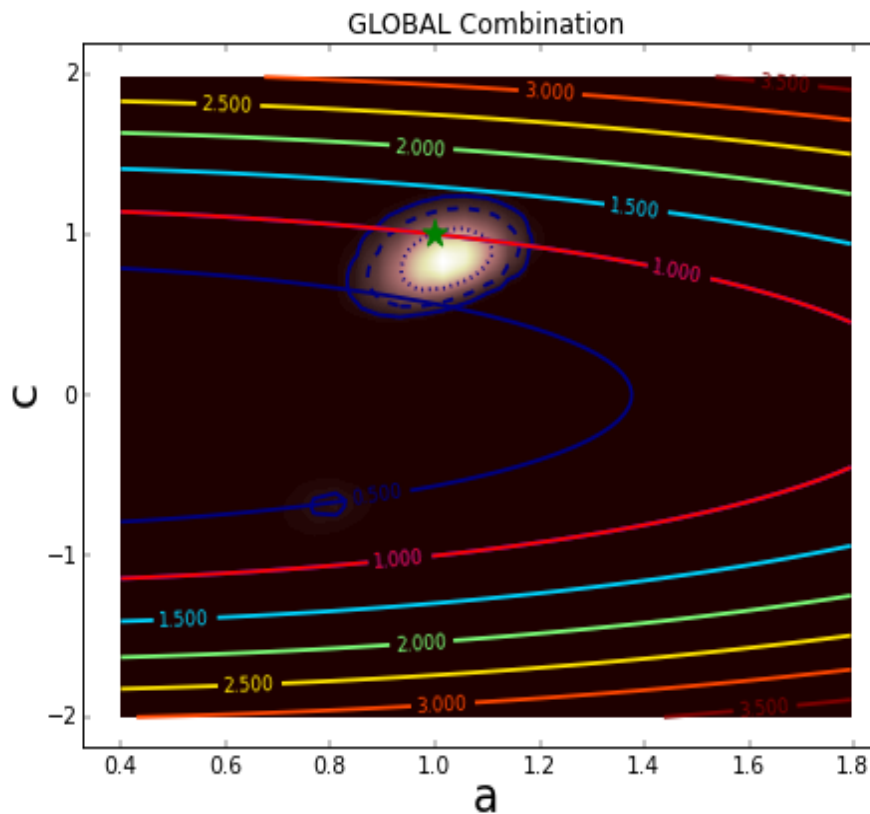
$Z\gamma < 9.5$, CL = 95%

$t\bar{t}H^0$ Production = $2.5^{+0.9}_{-0.8}$

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 - **Prima facie evidence that it does**
- Quantum (loop) corrections?
 - **$\gamma\gamma$, gg couplings \sim Standard Model**
- What are its self- and other couplings?

What is its Decay Rate ?

- Compared with the Standard Model prediction

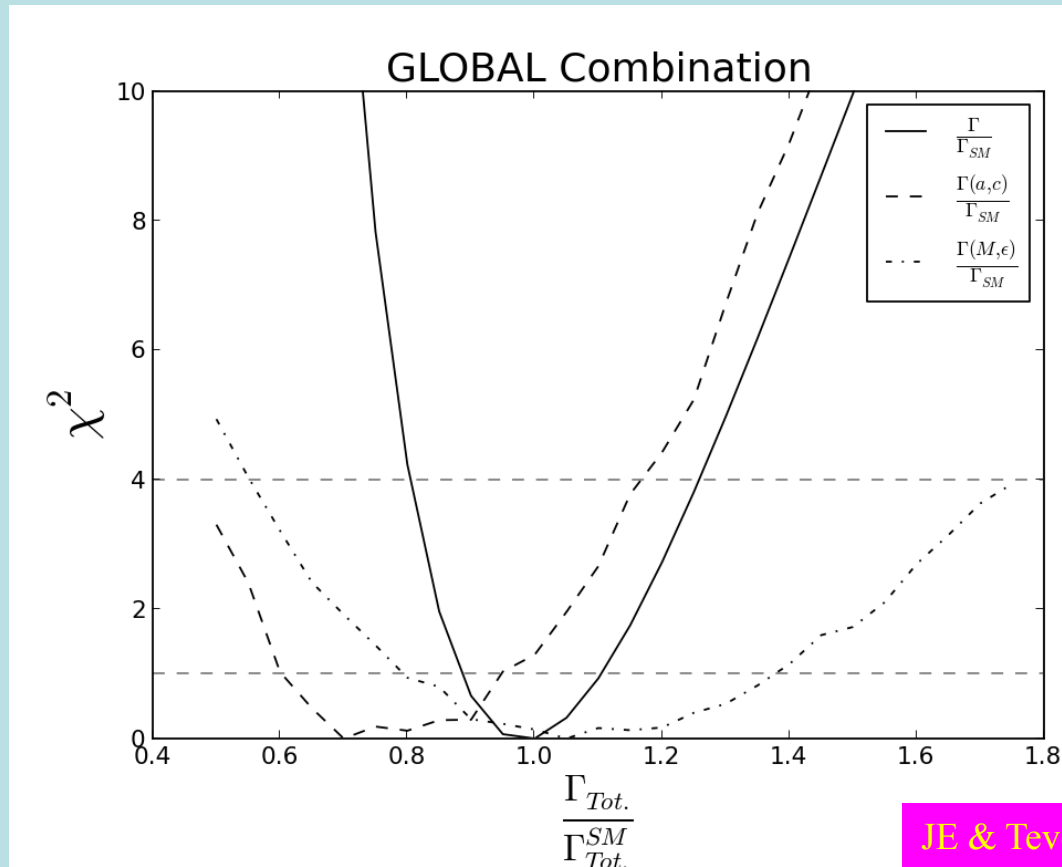


JE & Tevong You, arXiv:1303.3879

- Assuming no non-Standard Model modes

What is its Decay Rate ?

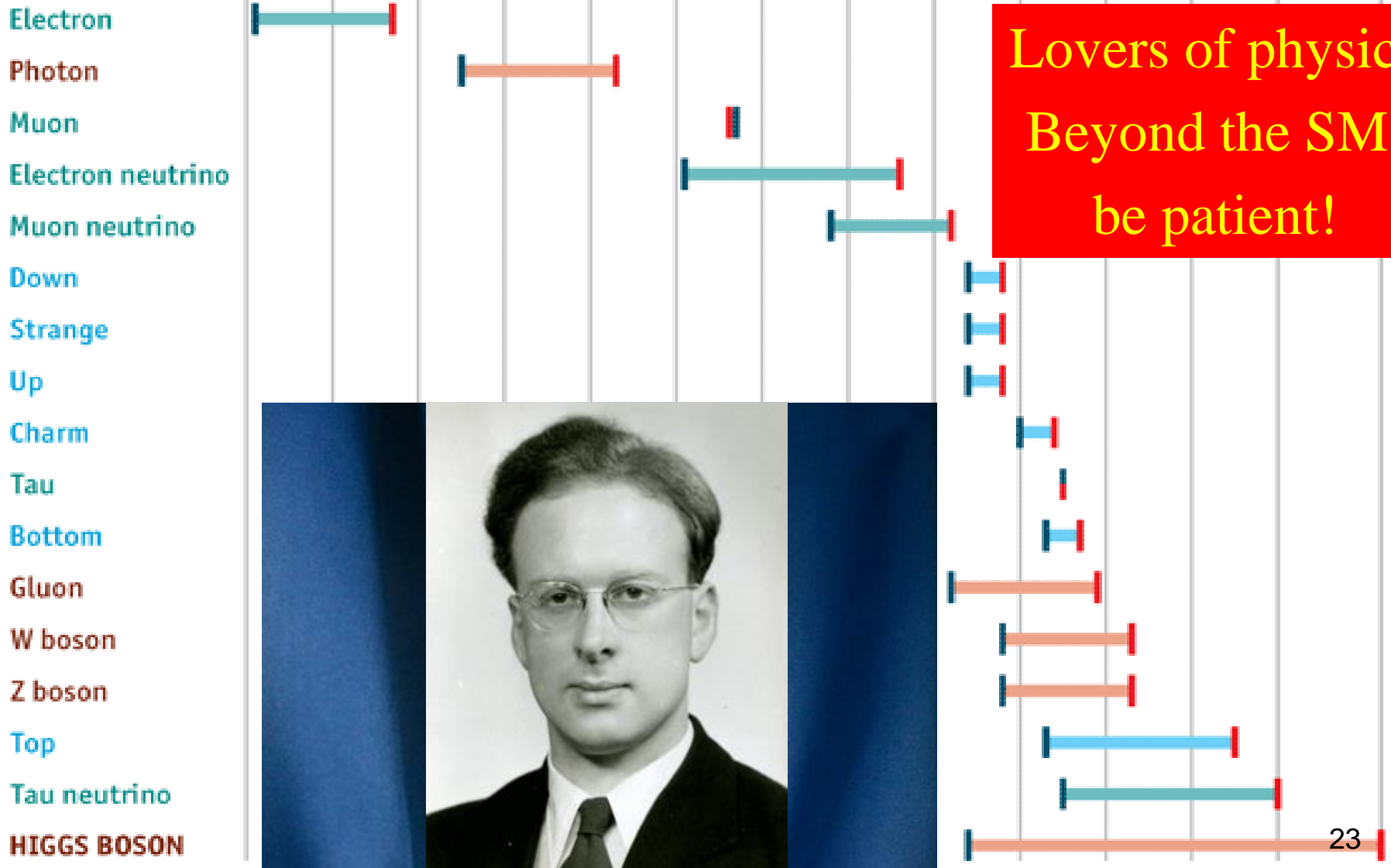
- Compared with the Standard Model prediction



JE & Tevong You, arXiv:1303.3879

- Assuming no non-Standard Model modes

Standard Model Particles: Years from Proposal to Discovery



Lovers of physics
Beyond the SM:
be patient!

Dixit Swedish Academy



Today we believe that “Beyond any reasonable doubt, it is a Higgs boson.” [1]

http://www.nobelprize.org/nobel_prizes/physics/laureates/2013/advanced-physicsprize2013.pdf

Standard Model Effective Field Theory

- Higher-dimensional operators as relics of higher-energy physics, e.g., dimension 6:

$$\mathcal{L}_{\text{eff}} = \sum_n \frac{f_n}{\Lambda^2} \mathcal{O}_n$$

- Operators constrained by $SU(2) \times U(1)$ symmetry:

$$\begin{aligned} \mathcal{L} \supset & \frac{\bar{c}_H}{2v^2} \partial^\mu [\Phi^\dagger \Phi] \partial_\mu [\Phi^\dagger \Phi] + \frac{g'^2 \bar{c}_\gamma}{m_W^2} \Phi^\dagger \Phi B_{\mu\nu} B^{\mu\nu} + \frac{g_s^2 \bar{c}_g}{m_W^2} \Phi^\dagger \Phi G_{\mu\nu}^a G_a^{\mu\nu} \\ & + \frac{2ig \bar{c}_{HW}}{m_W^2} [D^\mu \Phi^\dagger T_{2k} D^\nu \Phi] W_{\mu\nu}^k + \frac{ig' \bar{c}_{HB}}{m_W^2} [D^\mu \Phi^\dagger D^\nu \Phi] B_{\mu\nu} \\ & + \frac{ig \bar{c}_W}{m_W^2} [\Phi^\dagger T_{2k} \overleftrightarrow{D}^\mu \Phi] D^\nu W_{\mu\nu}^k + \frac{ig' \bar{c}_B}{2m_W^2} [\Phi^\dagger \overleftrightarrow{D}^\mu \Phi] \partial^\nu B_{\mu\nu} \\ & + \frac{\bar{c}_t}{v^2} y_t \Phi^\dagger \Phi \Phi^\dagger \cdot \bar{Q}_L t_R + \frac{\bar{c}_b}{v^2} y_b \Phi^\dagger \Phi \Phi \cdot \bar{Q}_L b_R + \frac{\bar{c}_\tau}{v^2} y_\tau \Phi^\dagger \Phi \Phi \cdot \bar{L}_L \tau_R \end{aligned}$$

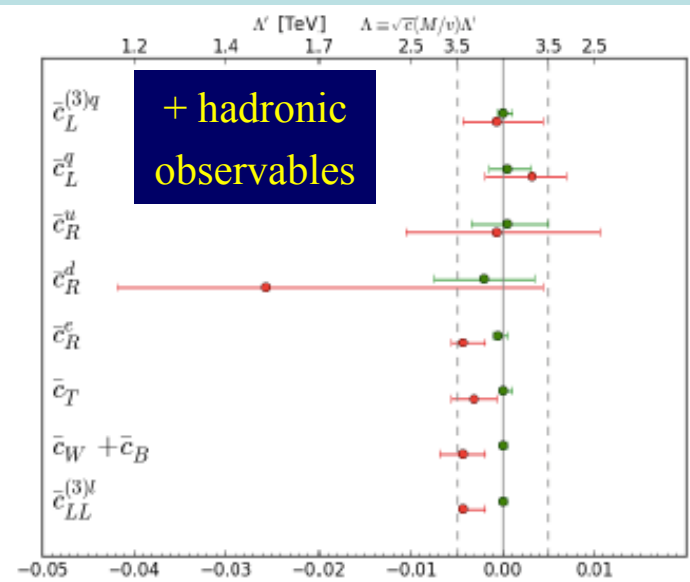
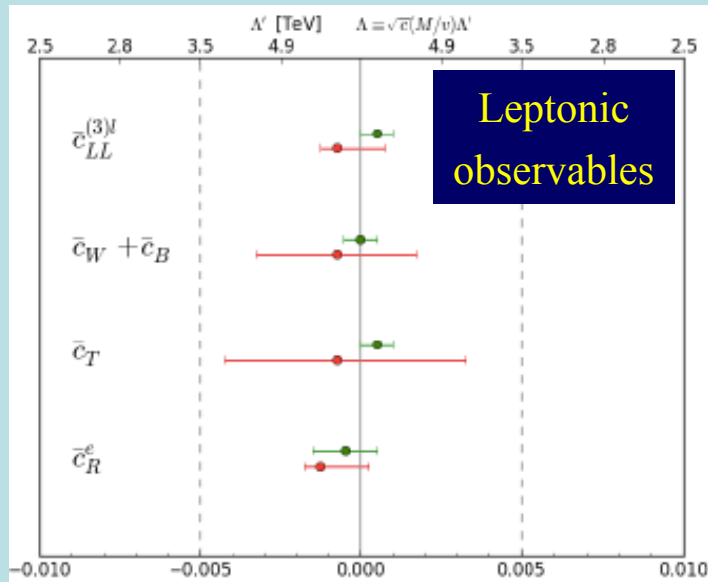
- Constrain with precision EW, Higgs data, TGCs²⁵...

Electroweak Precision Data

- Operators affecting oblique parameters

$$\mathcal{L}_{\text{dim-6}} \subset \frac{\bar{c}_{WB}}{m_W^2} \mathcal{O}_{WB} + \frac{\bar{c}_W}{m_W^2} \mathcal{O}_W + \frac{\bar{c}_B}{m_W^2} \mathcal{O}_B + \frac{\bar{c}_T}{v^2} \mathcal{O}_T + \frac{\bar{c}_{2W}}{m_W^2} \mathcal{O}_{2W} + \frac{\bar{c}_{2B}}{m_W^2} \mathcal{O}_{2B}$$

- Also other electroweak tests
- Constraints from LEP et al. data



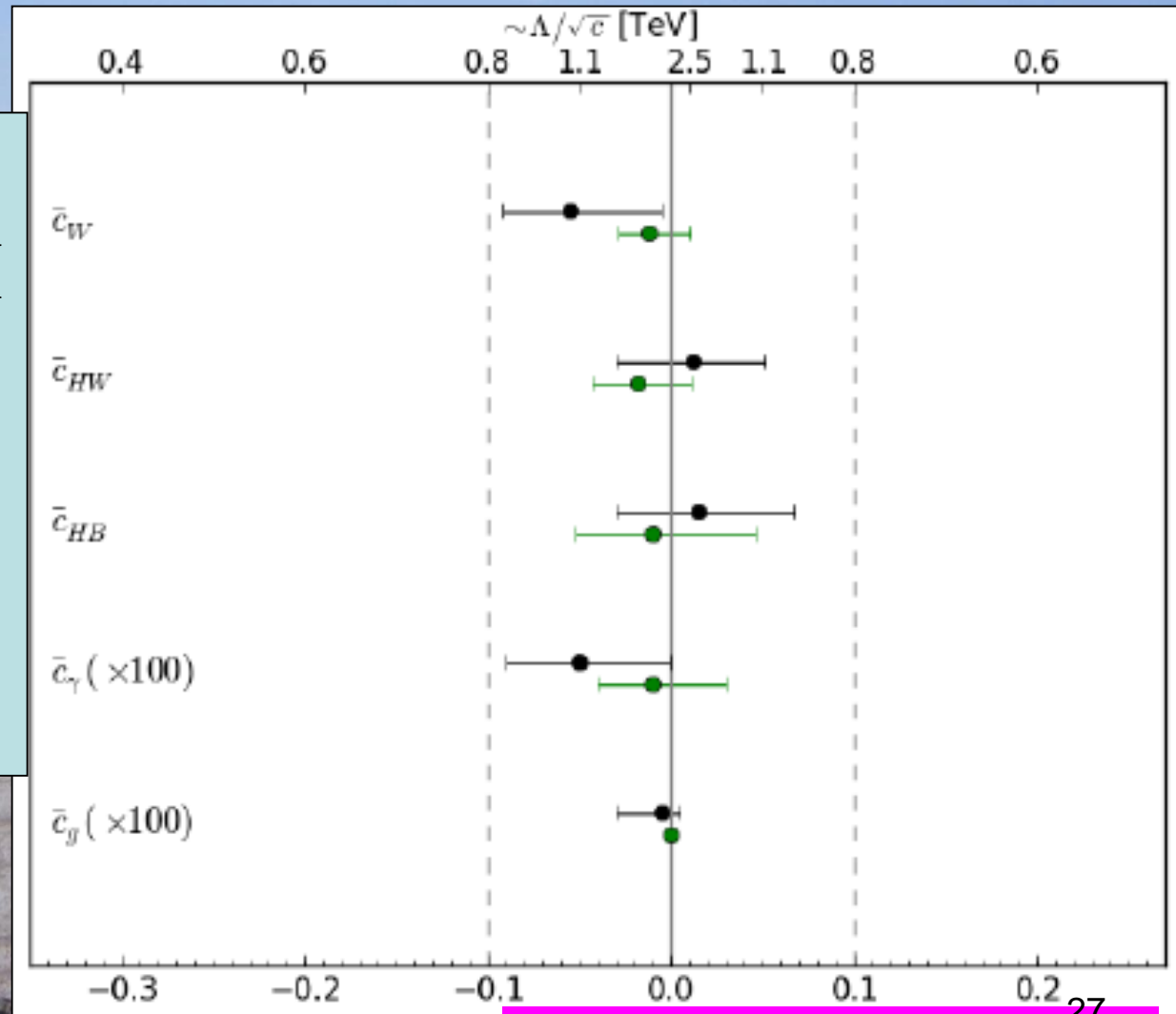
Fits to individual dimension-6 operators

Global fit to dimension-6 operators

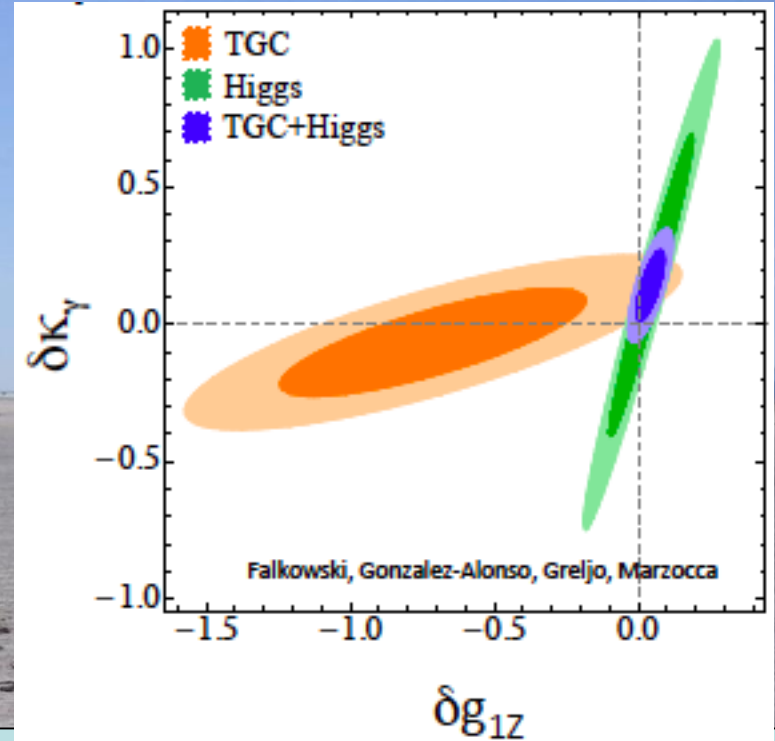
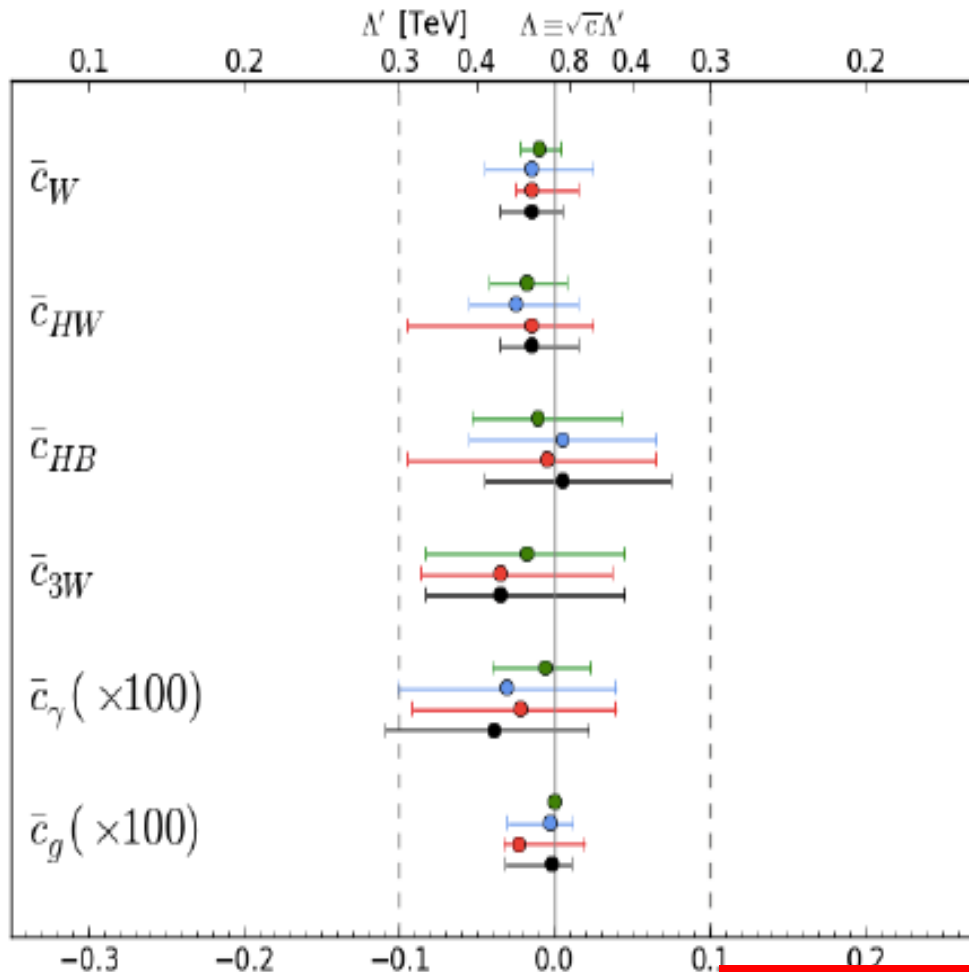
JE, Sanz & Tevong You, arXiv:1410.7703

Fits including Higgs Production

- Using signal strengths & VH kinematics in global fit
- **Single-parameter fits**



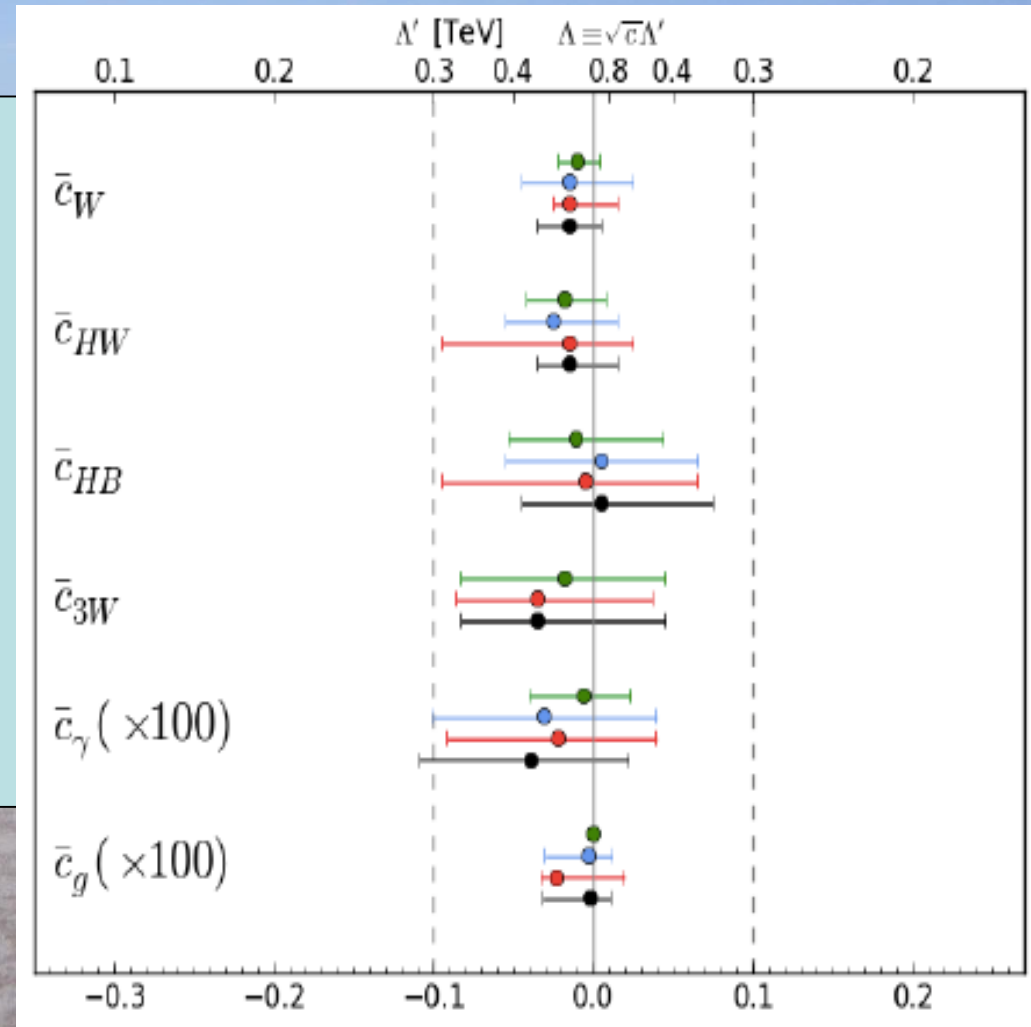
Global Fits including LHC TGCs



- Associated production
- LHC Triple-gauge couplings
- Global combination
- Individual operators

Including LHC Triple-Gauge Couplings

- Associated production
- LHC Triple-gauge couplings
- Global combination
- Individual operators



JE, Sanz & Tevong You, arXiv:1410.7703

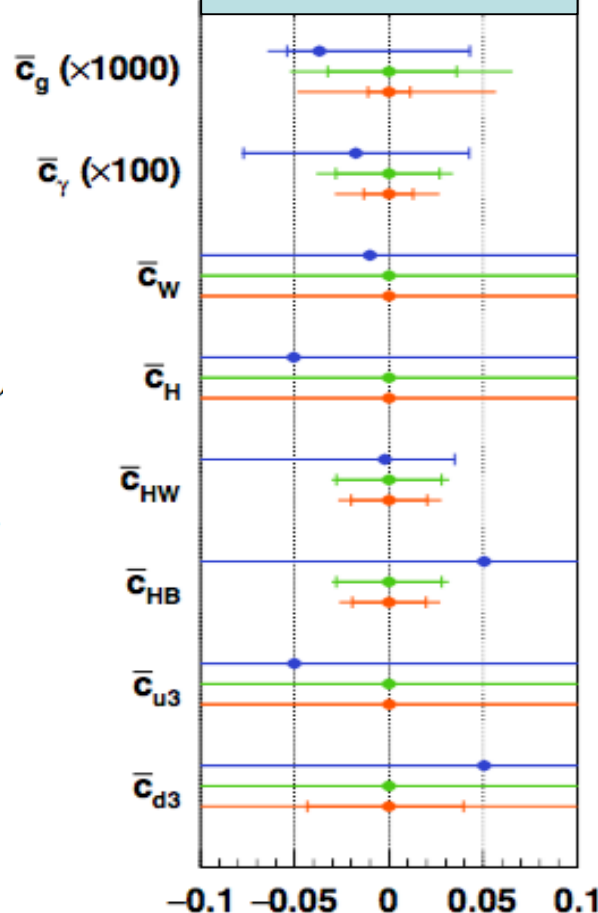
Constraints on Dimension-6 Operators

Operators

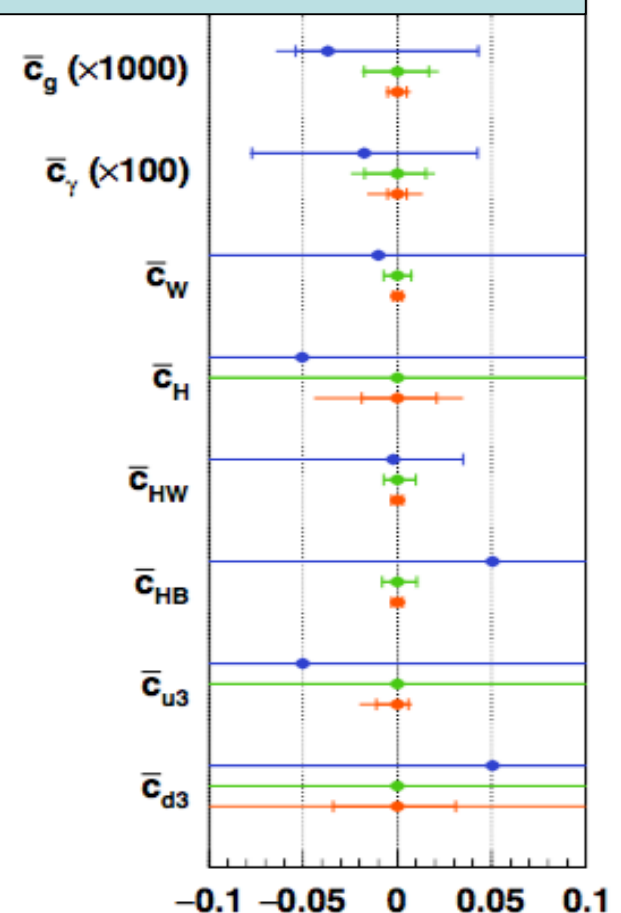
Bosonic CP-even

O_H	$\frac{1}{2v^2} \left[\partial_\mu (H^\dagger H) \right]^2$
O_T	$\frac{1}{2v^2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right)^2$
O_6	$-\frac{\lambda}{v^2} (H^\dagger H)^3$
O_g	$\frac{g_s^2}{m_W^2} H^\dagger H G_{\mu\nu}^a G_{\mu\nu}^a$
O_γ	$\frac{g'^2}{m_W^2} H^\dagger H B_{\mu\nu} B_{\mu\nu}$
O_W	$\frac{ig}{2m_W^2} \left(H^\dagger \sigma^i \overleftrightarrow{D}_\mu H \right) D_\nu W_{\mu\nu}^i$
O_B	$\frac{ig'}{2m_W^2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right) \partial_\nu B_{\mu\nu}$
O_{HW}	$\frac{ig}{m_W^2} \left(D_\mu H^\dagger \sigma^i D_\nu H \right) W_{\mu\nu}^i$
O_{HB}	$\frac{ig'}{m_W^2} \left(D_\mu H^\dagger D_\nu H \right) B_{\mu\nu}$
O_{2W}	$\frac{1}{m_W^2} D_\mu W_{\mu\nu}^i D_\rho W_{\rho\nu}^i$
O_{2B}	$\frac{1}{m_W^2} \partial_\mu B_{\mu\nu} \partial_\rho B_{\rho\nu}$
O_{2G}	$\frac{1}{m_W^2} D_\mu G_{\mu\nu}^a D_\rho G_{\rho\nu}^a$
O_{3W}	$\frac{g^3}{m_W^2} \epsilon^{ijk} W_{\mu\nu}^i W_{\nu\rho}^j W_{\rho\mu}^k$
O_{3G}	$\frac{g_s^3}{m_W^2} f^{abc} G_{\mu\nu}^a G_{\nu\rho}^b G_{\rho\mu}^c$

Constraints from rates



Constraints including kinematics



Current

300/fb

3000/fb

No BSM? Beware Historical Hubris

- *"So many centuries after the Creation, it is unlikely that anyone could find hitherto unknown lands of any value"* - Spanish Royal Commission, rejecting Christopher Columbus proposal to sail west, < 1492
- *"The more important fundamental laws and facts of physical science have all been discovered"* – Albert Michelson, 1894
- *"There is nothing new to be discovered in physics now. All that remains is more and more precise measurement"* - Lord Kelvin, 1900
- *"Is the End in Sight for Theoretical Physics?"* – Stephen Hawking, 1980



- « Empty » space is unstable
- Dark matter
- Origin of matter
- Masses of neutrinos
- Hierarchy problem
- Inflation
- Quantum gravity
- ...

SUSY

SUSY

SUSY

SUSY

SUSY

SUSY

The Standard Model

PIERCE BROSNAN in IAN FLEMING'S JAMES BOND 007™
The World Is Not Enough
007™

ALBERT R. BROCCOLLI'S SON PRODUCTIONS PRESENTS PIERCE BROSNAN in IAN FLEMING'S JAMES BOND 007™
"THE WORLD IS NOT ENOUGH" SOPHIE MARQUEAU ROBERT CAROLLE DENISE RICHARDS TORRE COTRANI and JIMU DENCHI
DESIGN LINDY HEARMING COSTUME DESIGNER DAVID ARNOLD MUSIC BY JIM CLARK EDITOR JIMMY ADRIAN BOULE PRODUCTION DESIGNER PETER JARANT
EXECUTIVE PRODUCERS ANTHONY WATE PRODUCED BY NEAL PURVIS & ROBERT WADE PRODUCED BY NEAL PURVIS & ROBERT WADE WRITTEN BY BRUCE FENSTEN
DIRECTED BY MICHAEL E. WOLSON COSTUME DESIGNER BARBARA BROCCOLLI EXECUTIVE PRODUCER MICHAEL APPO
CASTING BY JUDY HARRIS
COURTESY OF THE FBI
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What lies beyond the Standard Model?

Supersymmetry

New motivations
From LHC Run 1

- **Stabilize electroweak vacuum**
- **Successful prediction for Higgs mass**
 - Should be < 130 GeV in simple models
- **Successful predictions for couplings**
 - Should be within few % of SM values
- Naturalness, GUTs, string, ..., **dark matter**

Higgs Bosons in Supersymmetry

- Need 2 complex Higgs doublets
(cancel anomalies, form of SUSY couplings)
- $8 - 3 = 5$ physical Higgs bosons
Scalars h, H ; pseudoscalar A ; charged H^\pm
- Lightest Higgs $< M_Z$ at tree level:

$$M_{H,h}^2 = \frac{1}{2} \left[M_A^2 + M_Z^2 \pm \sqrt{(M_A^2 + M_Z^2)^2 - 4M_Z^2 M_A^2 \cos^2 2\beta} \right]$$

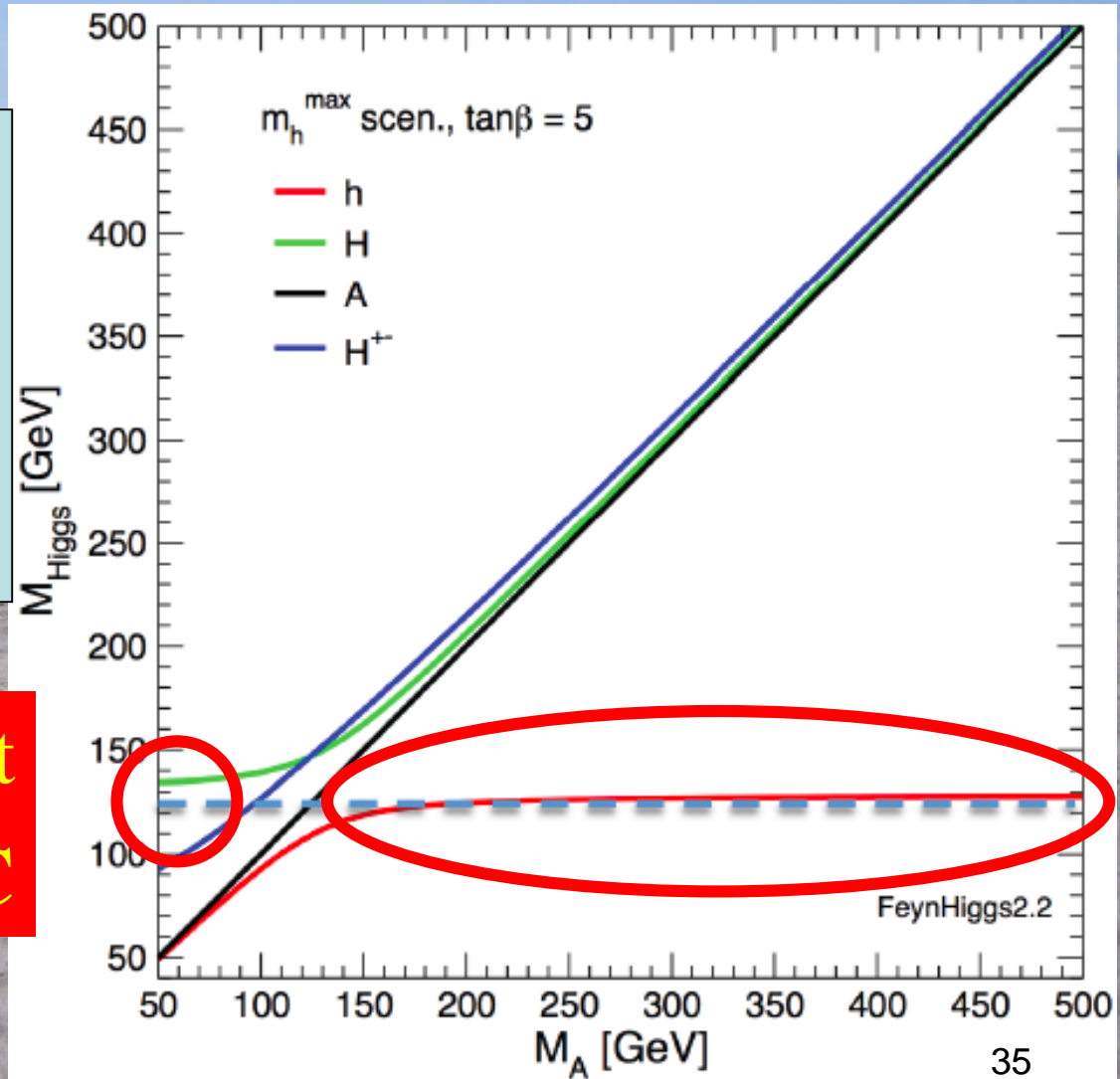
- Important radiative corrections to mass:

$$G_\mu m_t^4 \ln \left(\frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \right)_{\text{TH}} \sim 1.5 \text{ GeV}$$

MSSM Higgs Masses & Couplings

Lightest Higgs mass
up to ~ 130 GeV
Heavy Higgs masses
quite close

Consistent
With LHC



More Supersymmetry, not less?

JE, Quevillon & Sanz: arXiv:1607.05541

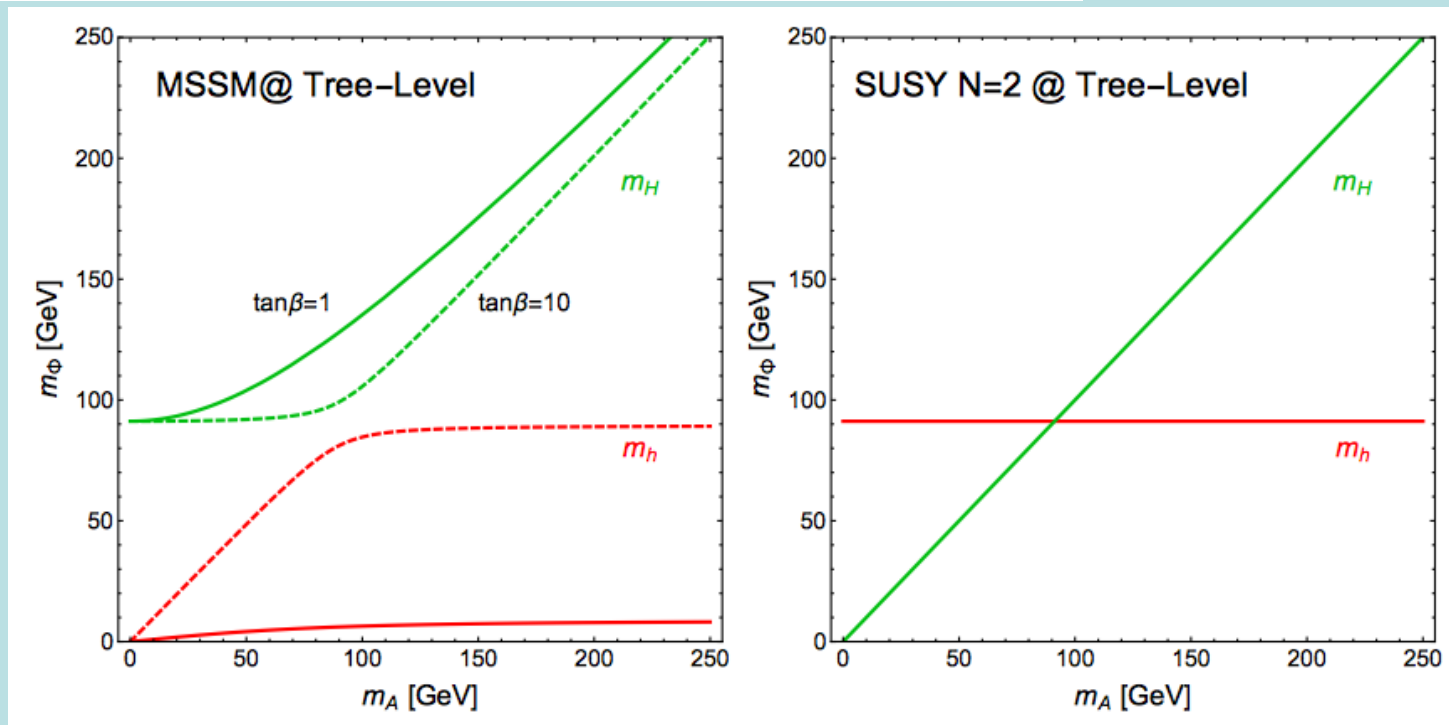
- 750 GeV ☹️ → re-examined vector-like fermions
- Appear in many extensions of the Standard Model
 - Five-dimensional models
 - String compactifications
 - GUTs
- Could accommodate N=2 supersymmetry
- **Double up on supersymmetry?**
- N=2 gauge sector?
- **Higgs sector also vector-like, could be N=2**

Doubling up on Supersymmetry

JE, Quevillon & Sanz: arXiv:1607.05541

- Higgs sector as portal to N=2 world at TeV scale?
- Tree-level neutral Higgses:

$$\mathcal{M}_{\text{tree}}^{2,N2} = \begin{pmatrix} m_Z^2 \cos^2 \beta + m_A^2 \sin^2 \beta & -(m_A^2 - m_Z^2) \cos \beta \sin \beta \\ -(m_A^2 - m_Z^2) \cos \beta \sin \beta & m_Z^2 \sin^2 \beta + m_A^2 \cos^2 \beta \end{pmatrix} \quad m_h^{N2} = m_Z; \quad m_H^{N2} = m_A$$

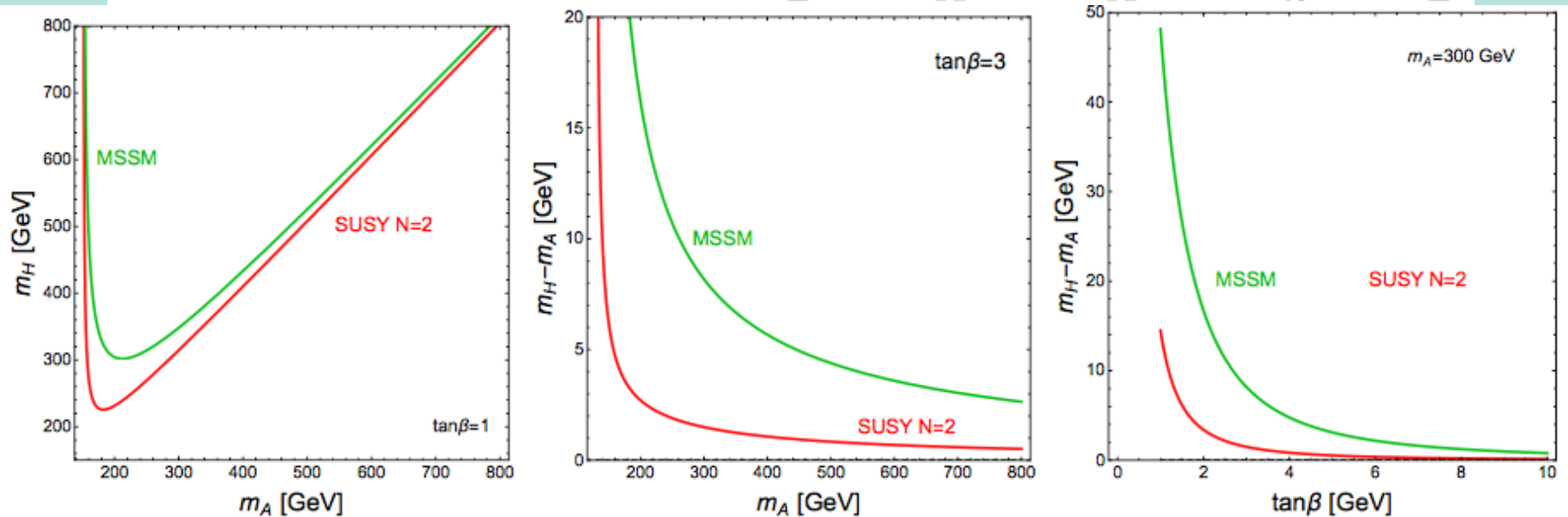


Doubling up on Supersymmetry

JE, Quevillon & Sanz: arXiv:1607.05541

- Include 1-loop radiative corrections from stops
- Require lighter scalar neutral Higgs @ 125 GeV

$$\epsilon_{N2} = \Delta \mathcal{M}_{22}^{2,N2} = \frac{2(m_A^2 - m_h^2)(m_h^2 - m_Z^2)}{\cos 2\beta (m_Z^2 - m_A^2) + m_A^2 - 2m_h^2 + m_Z^2}$$

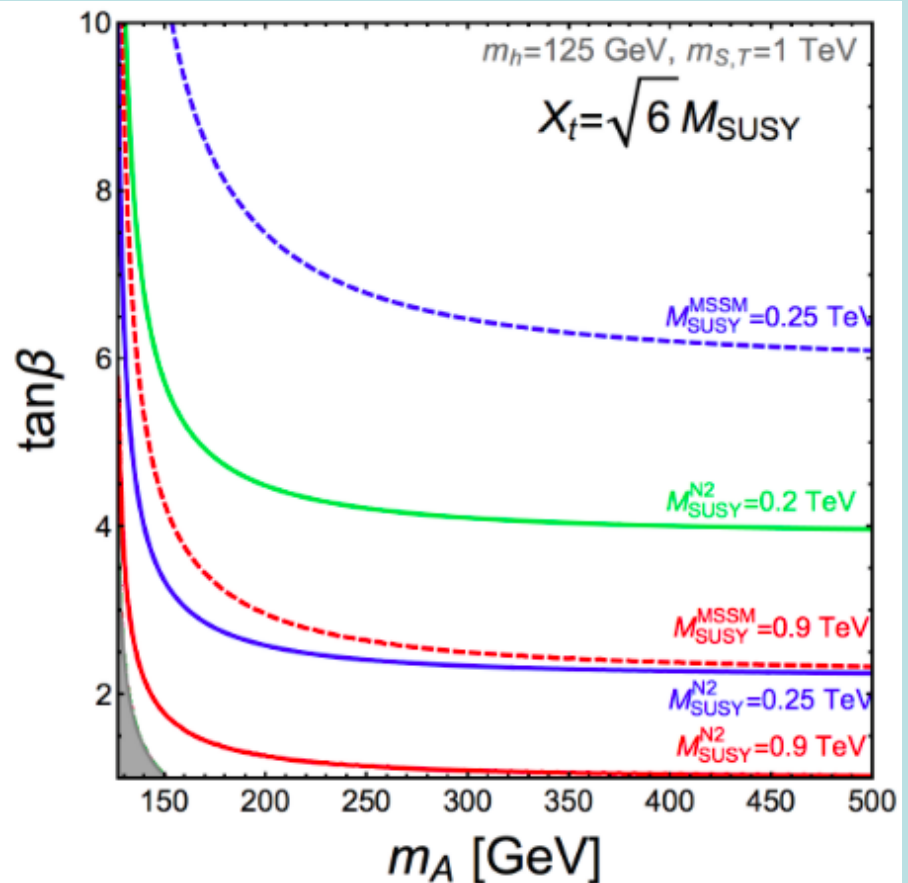
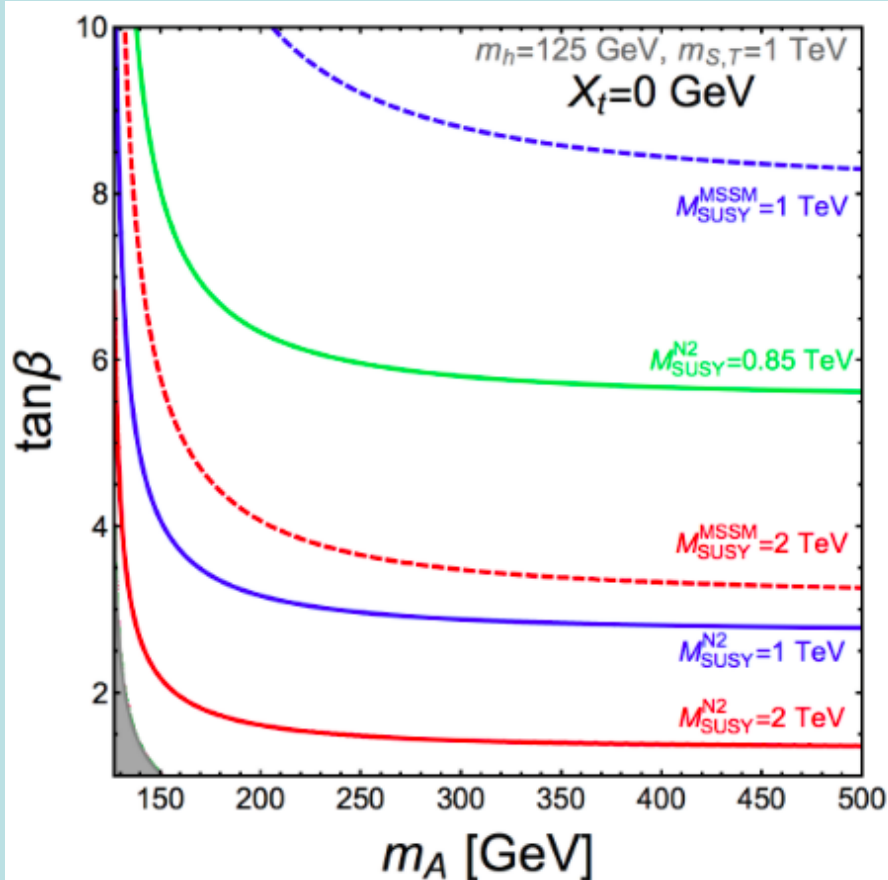


- H can be lighter than in MSSM, $m_H - m_A$ smaller

Doubling up on Supersymmetry

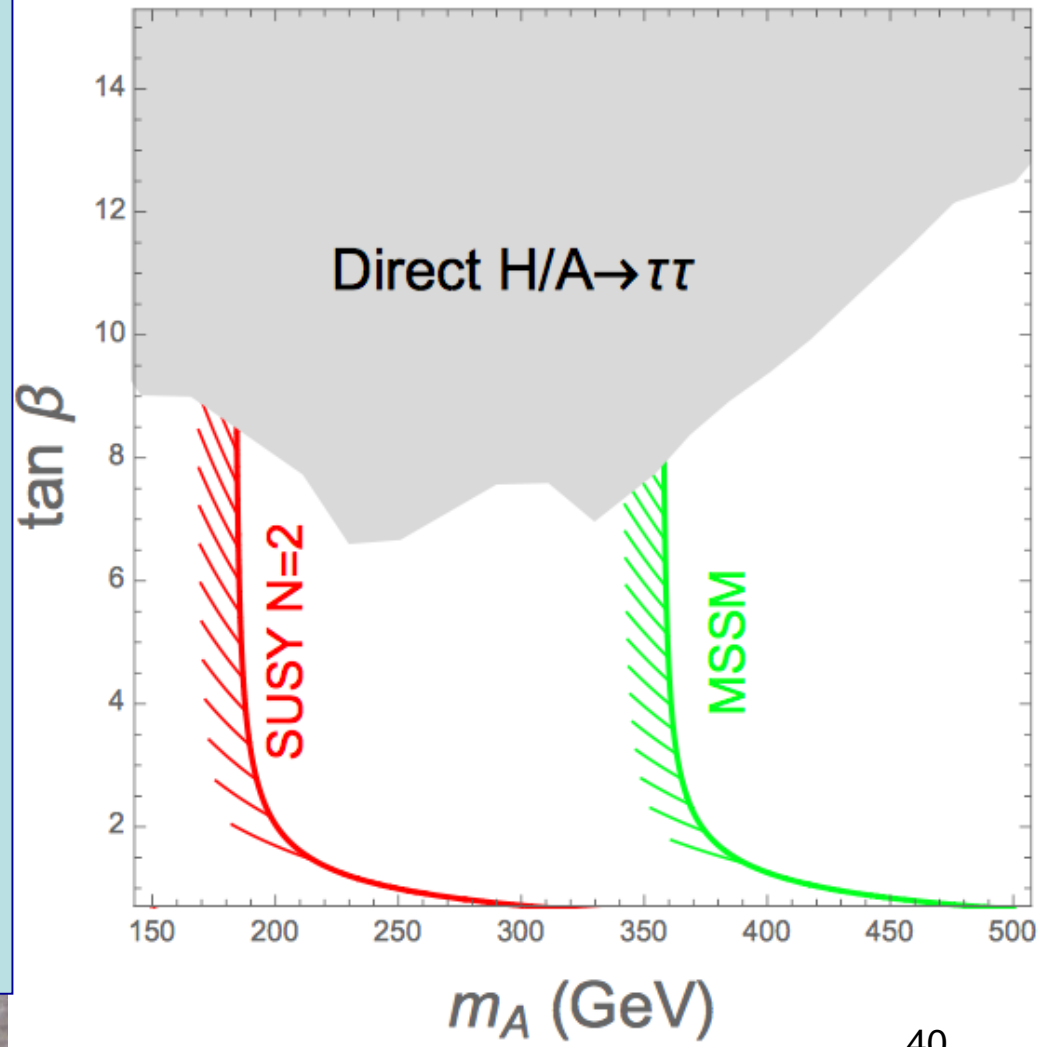
JE, Quevillon & Sanz: arXiv:1607.05541

- M_{SUSY} smaller than MSSM for same $m_{h,A}$, $\tan\beta$



Doubling up on Supersymmetry

- Including LHC constraints
- m_A can be smaller than in MSSM for all $\tan \beta$
- Supersymmetry and SUSY Higgses may be closer than suggested by MSSM



What Next: A Higgs Factory?

To study the ‘Higgs’ in detail:

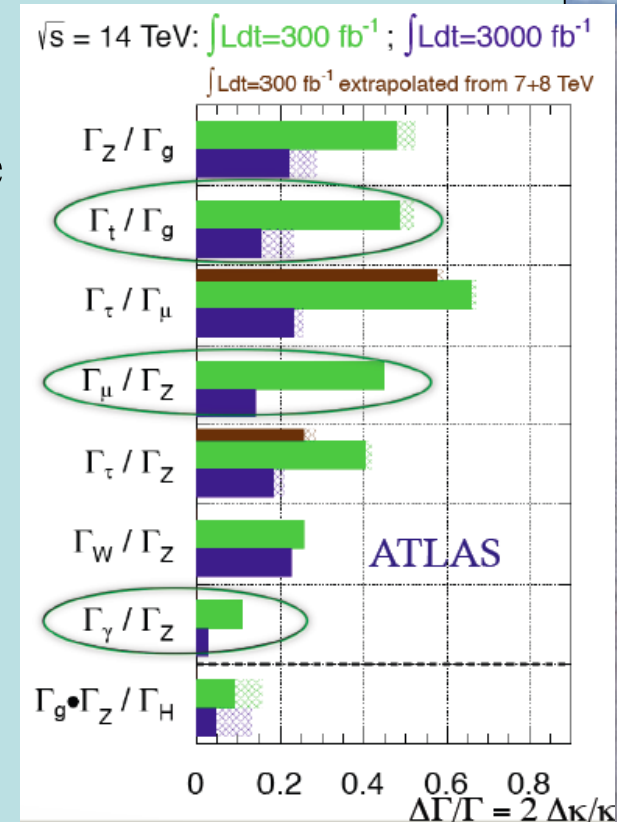
- The LHC
 - Consider LHC upgrades in this perspective
- A linear collider?
 - ILC up to 500 GeV
 - CLIC up to 3 TeV
 - (Larger cross section at higher energies)

• **A circular e^+e^- collider?**

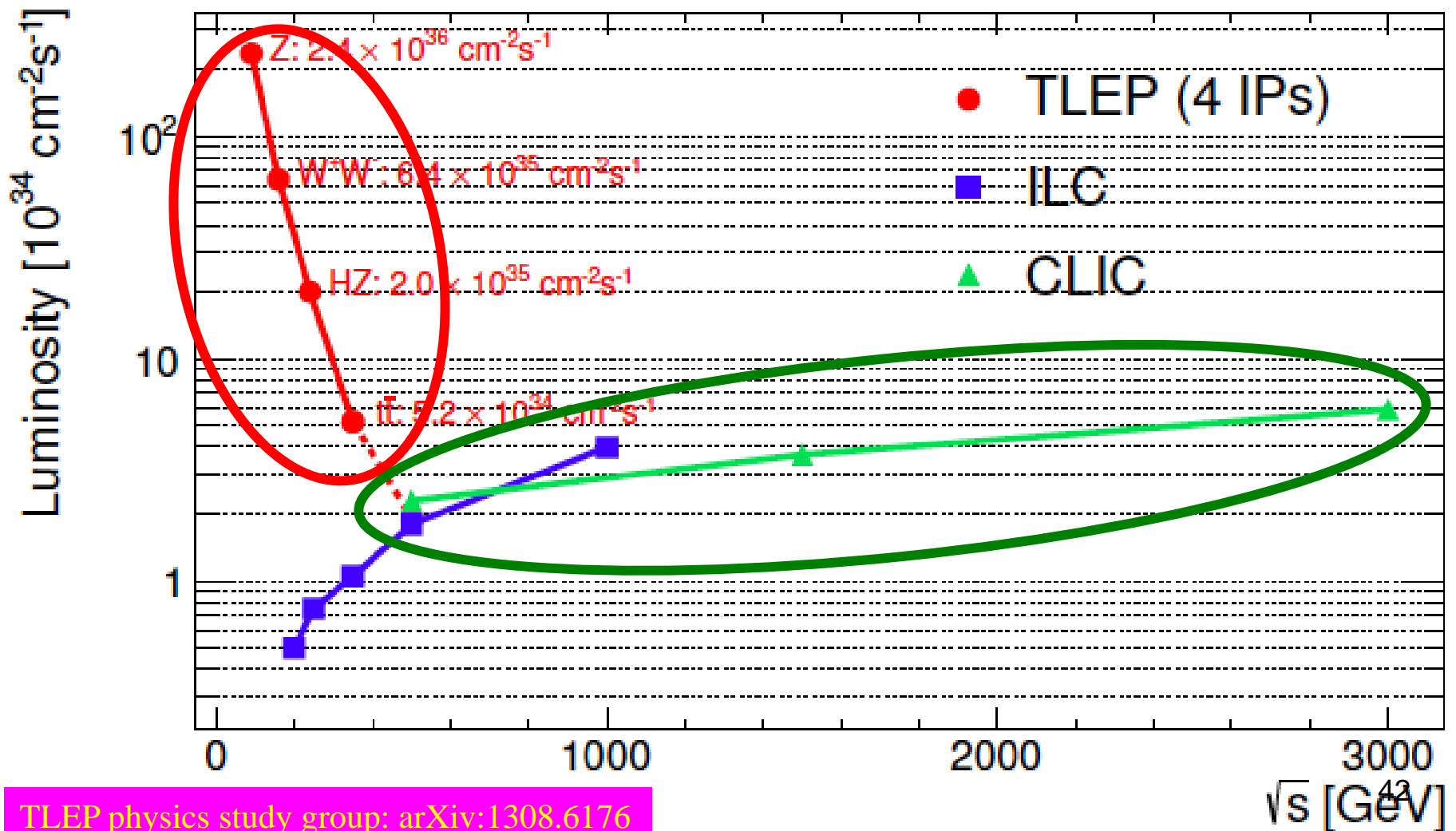
• An ep collider?

• A $\gamma\gamma$ collider? A muon collider?

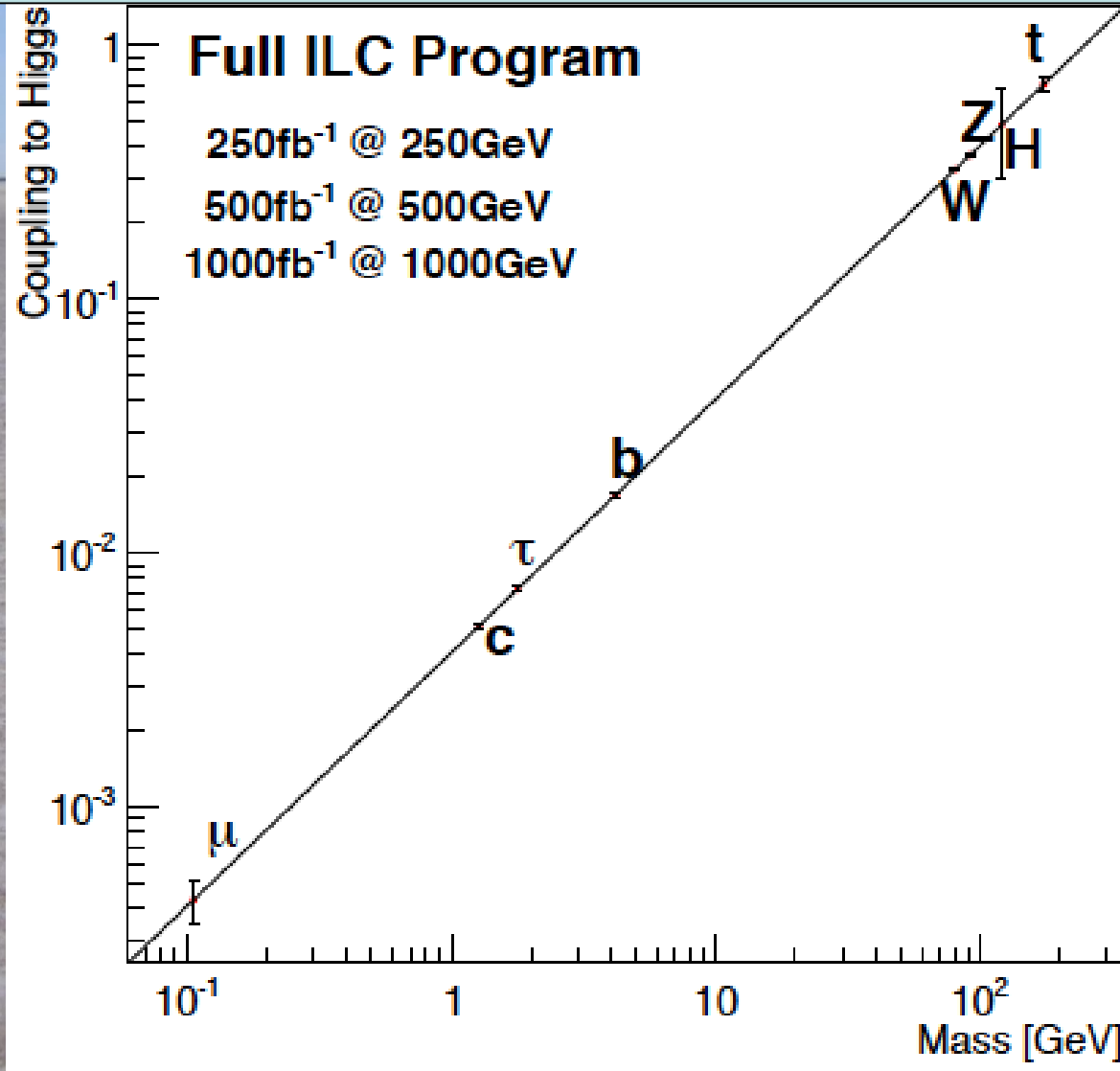
• **Wait for results from LHC @ 13/14 TeV**



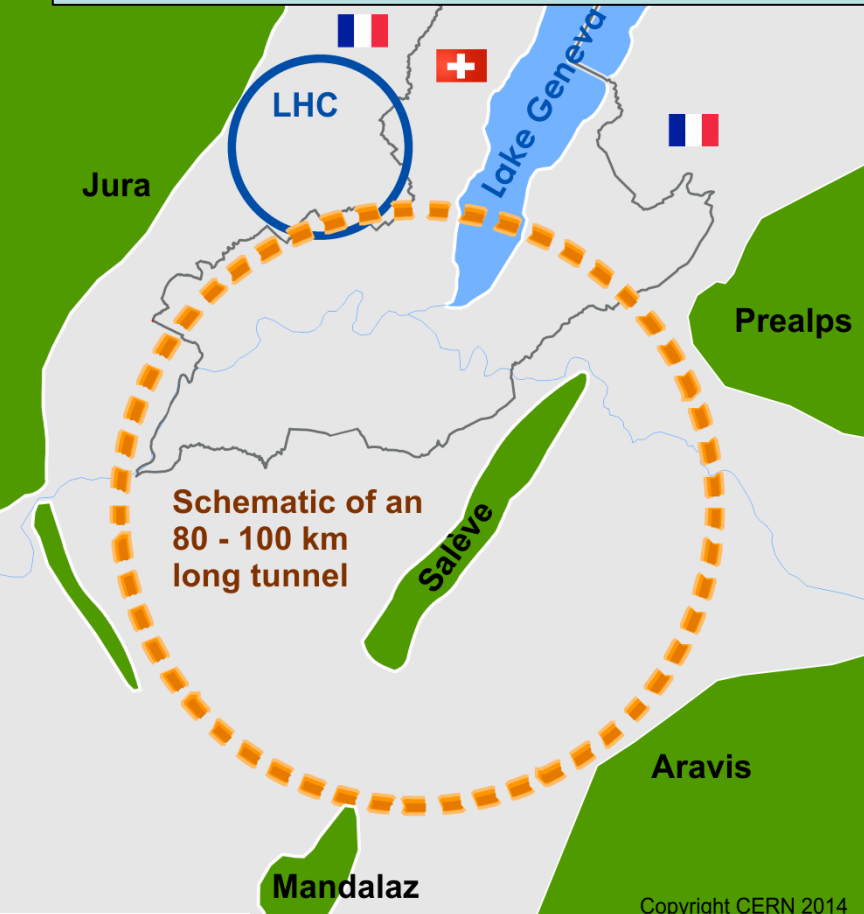
Projected e^+e^- Colliders: Luminosity vs Energy



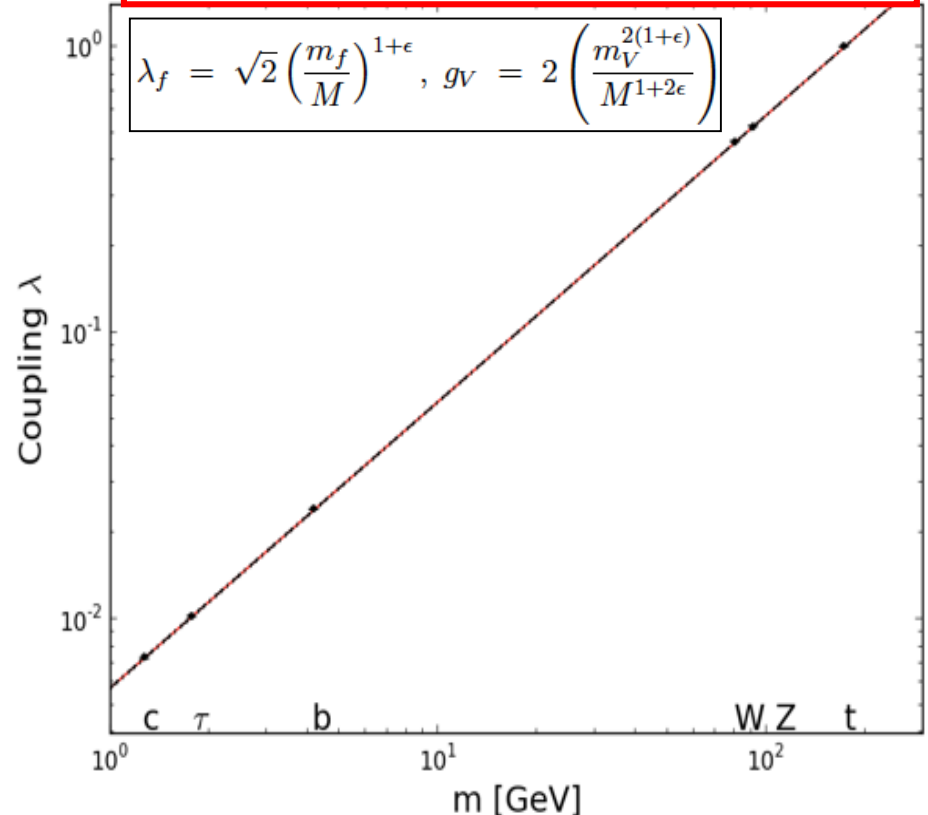
Coupling Measurements @ ILC



Future Circular e^+e^- Collider?



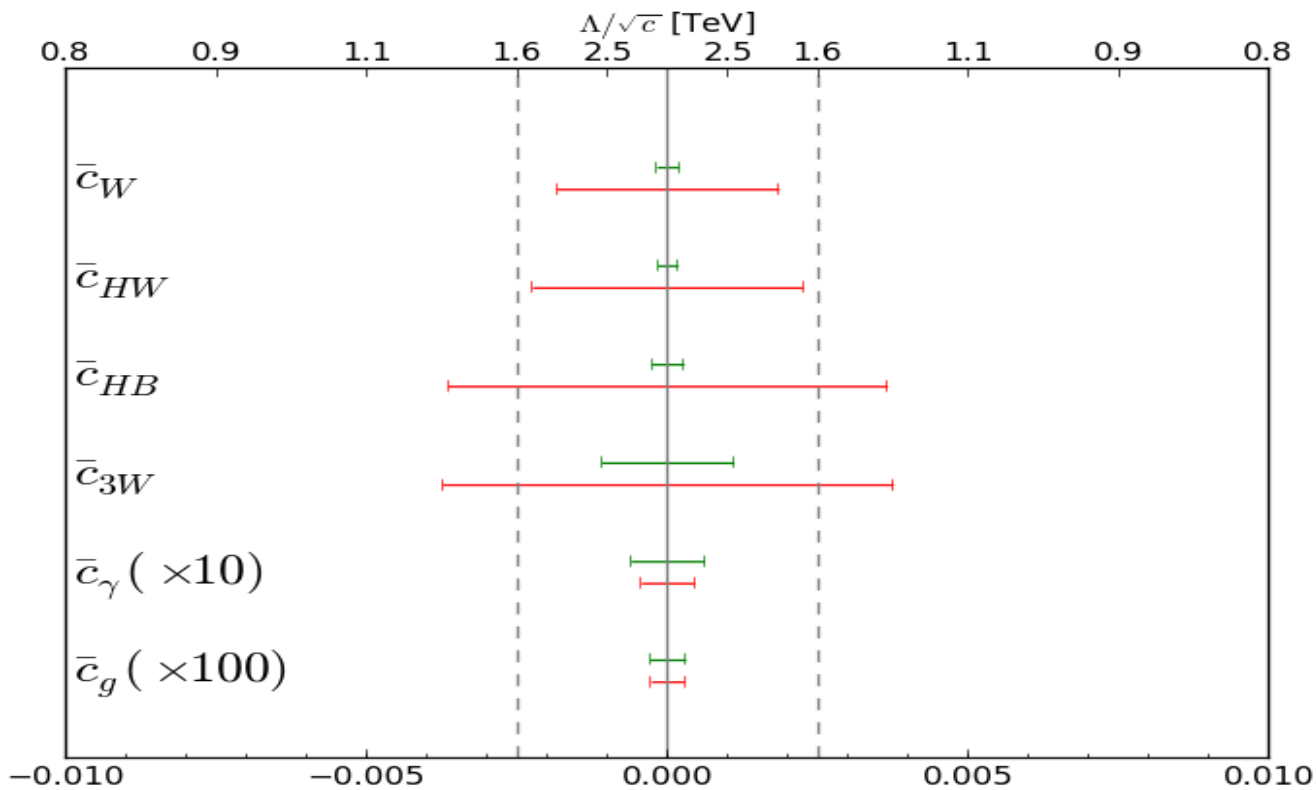
$$M = 246.0 \pm 0.8 \text{ GeV}, \epsilon = 0.0000^{+0.0015}_{-0.0010}$$



Not just Higgs physics:
Also Tera-Z, Ouku-W, Mega-t



FCC-ee Higgs & TGC Measurements



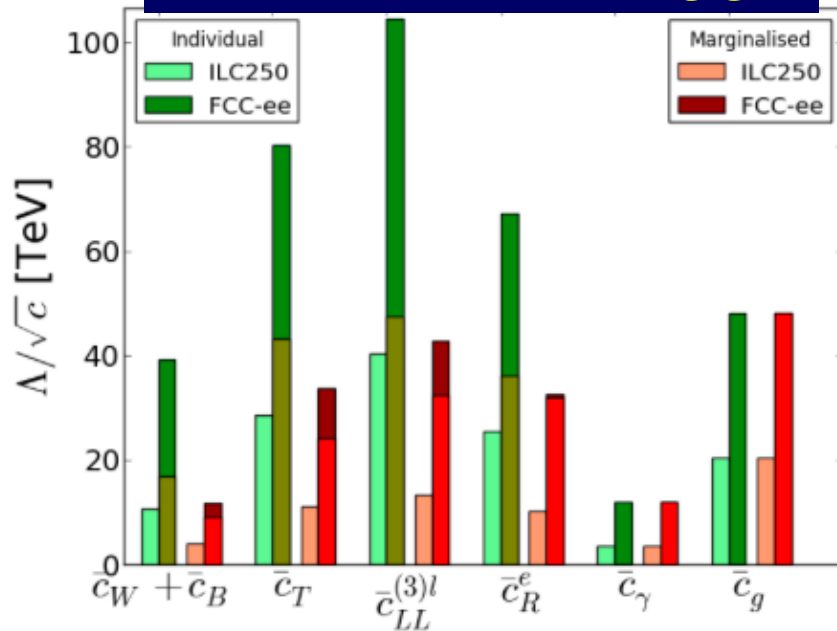
- LHC constraints

JE & Tevong You, arXiv:1510.04561

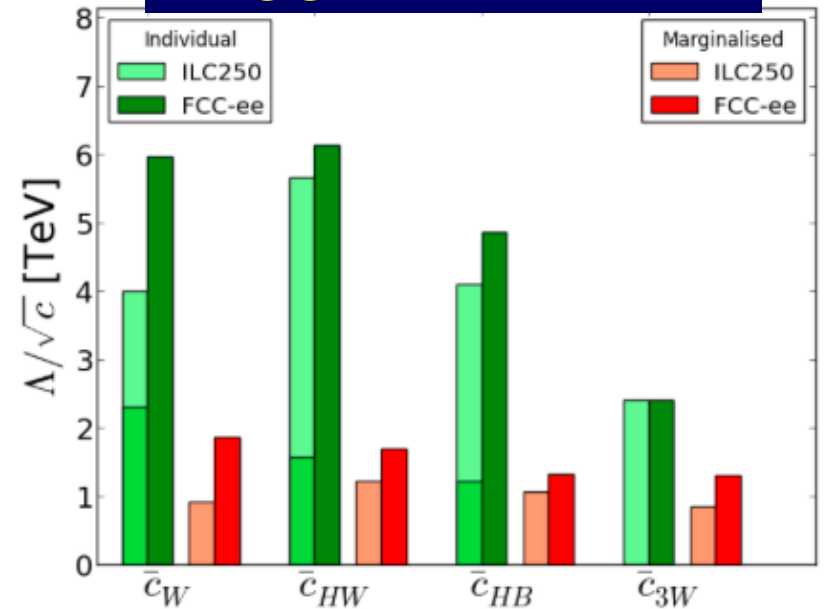
- **FCC-ee** constraints: see $\Lambda \sim 10$ TeV?

rCC-ee Higgs & TGC Measurements

EWPTs and Higgs



Higgs and TGCs



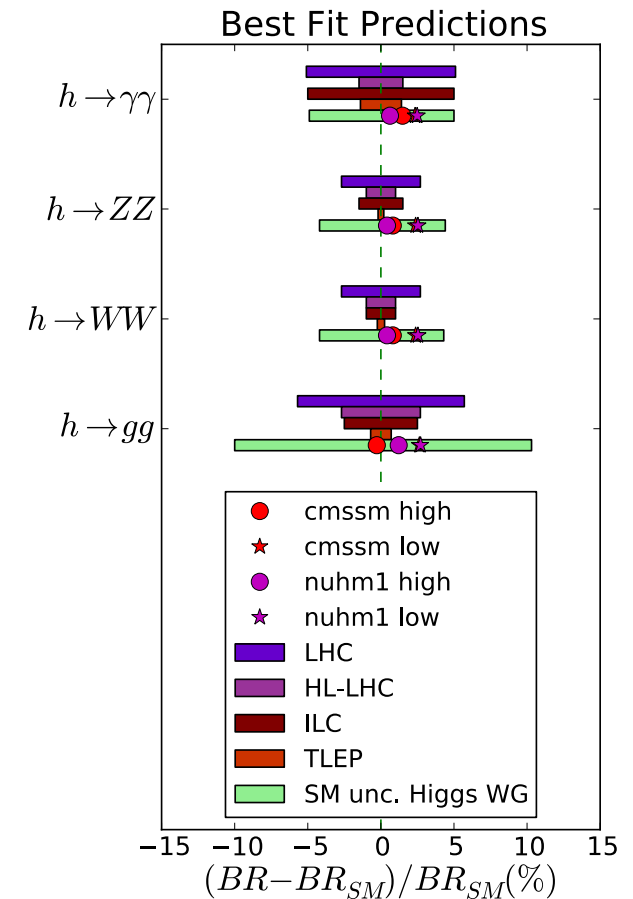
- Shadings:
 - With/without theoretical EWPT uncertainties

- Shadings of green:
 - Effect of including TGCs at ILC

Should extend to include prospective FCC-hh measurements of TGCs, ...

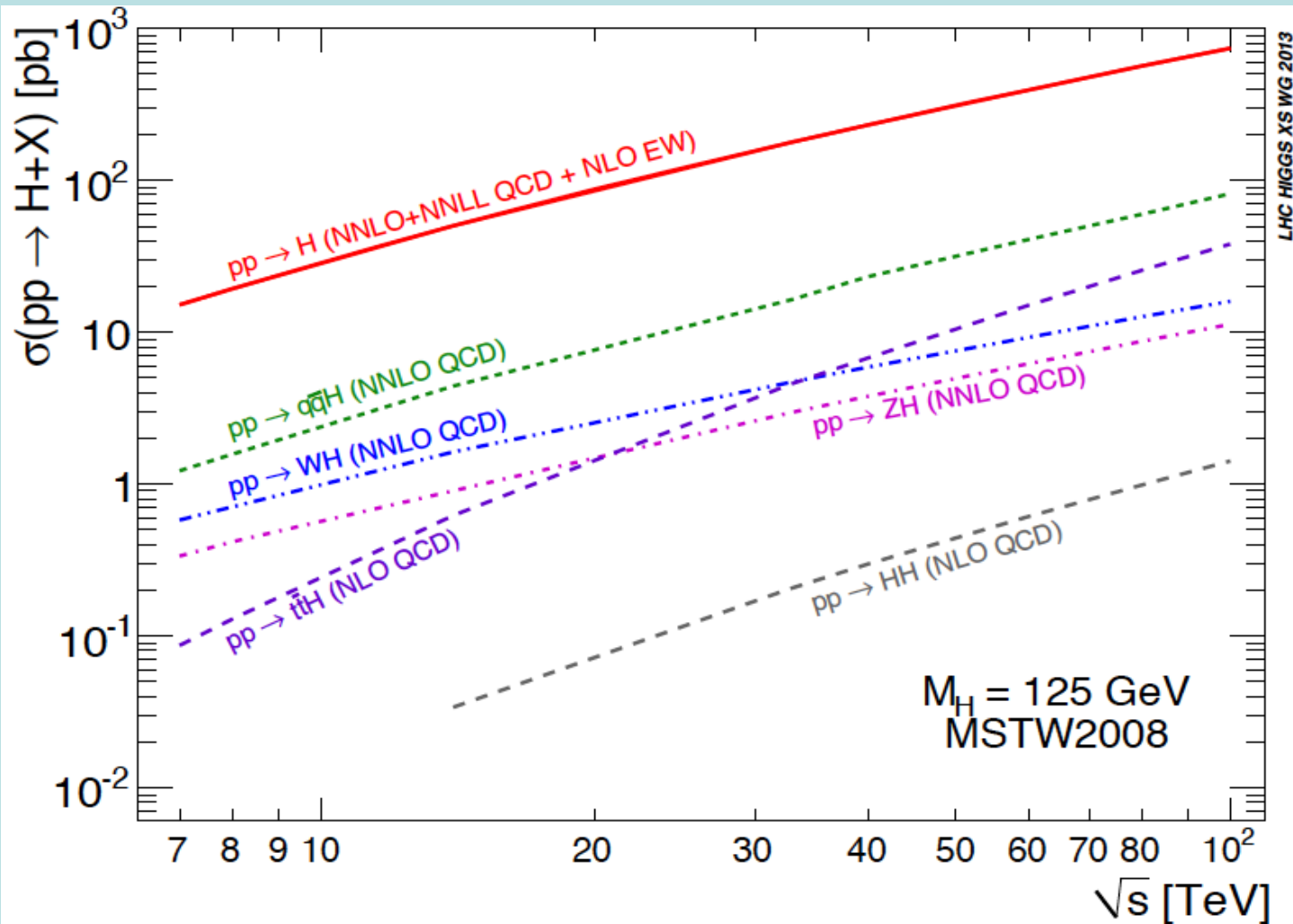
Impact of Higgs Measurements

- Predictions of current best fits in **simple SUSY models**
- **Current uncertainties** in SM calculations [LHC Higgs WG]
- Comparisons with
 - **LHC**
 - **HL-LHC**
 - **ILC**
 - **TLEP (= FCC-ee)**
 - **TLEP (= FCC-ee)****(Able to distinguish from SM)**



Higgs Cross Sections

- At the LHC and beyond:



Summary

- Beyond any reasonable doubt, the LHC has discovered a (the) Higgs boson
- A big challenge for theoretical physics!
- The LHC may discover physics beyond the SM when it restarts at ~ 13 TeV
- If it **does**, priority will be to study it
- If it does **not**, natural to focus on the Higgs
- In this case, future circular colliders may offer the best prospects