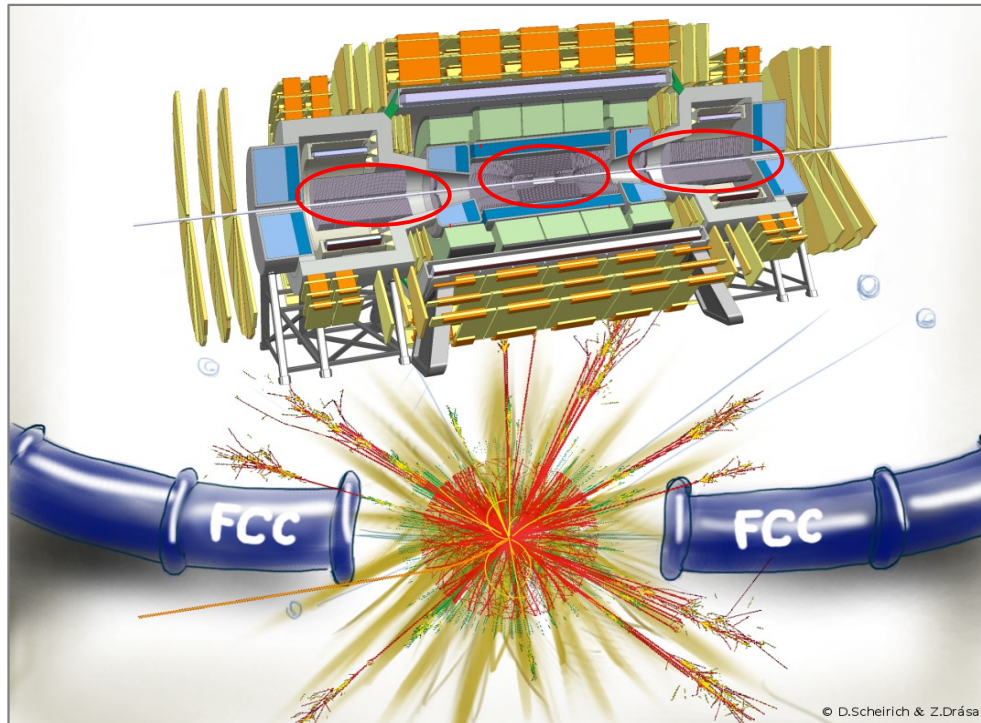


Status & Challenges of Tracker Design for FCC-hh



Zbyněk Drásal
CERN



On behalf of the FCC-hh detector working group



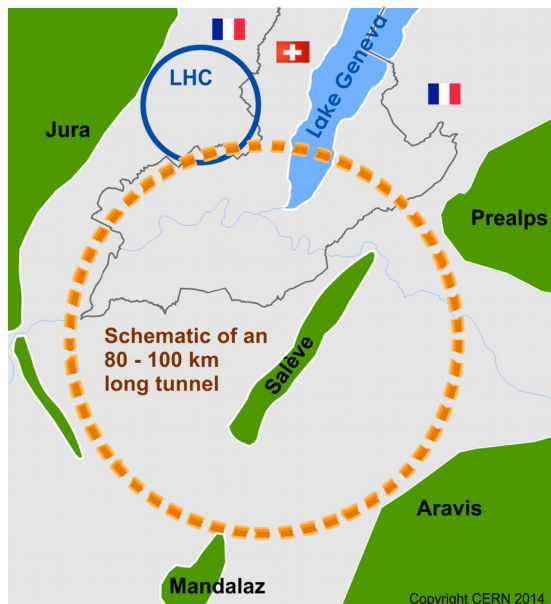
Overview

- Introduction
 - Future Circular Collider with focus on FCC-hh (pp) option
 - Physics motivation & Reference Detector Layout
- FCC-hh & Radiation Studies
- Tracker design & expected tracker performance
 - Reference tracker geometry & design driving principles
 - Granularity in R- Φ & tracking resolution
 - Implications of high pile-up & high-rate environment
 - Pattern recognition capabilities & requirements on granularity in Z
 - Primary vertexing in high pile-up & requirements on timing information
 - Expected tracker occupancy & data rates
- Summary & Challenges

Future Circular Collider

- **FCC machine:**

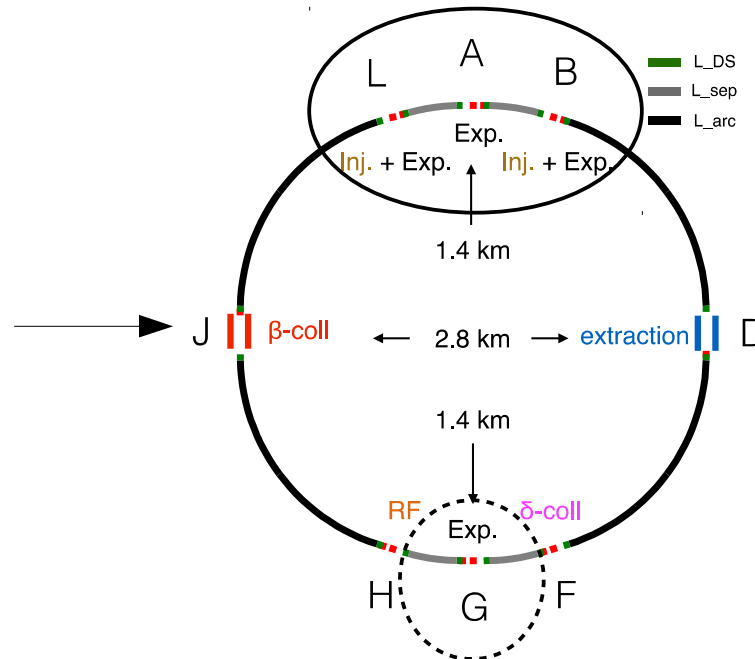
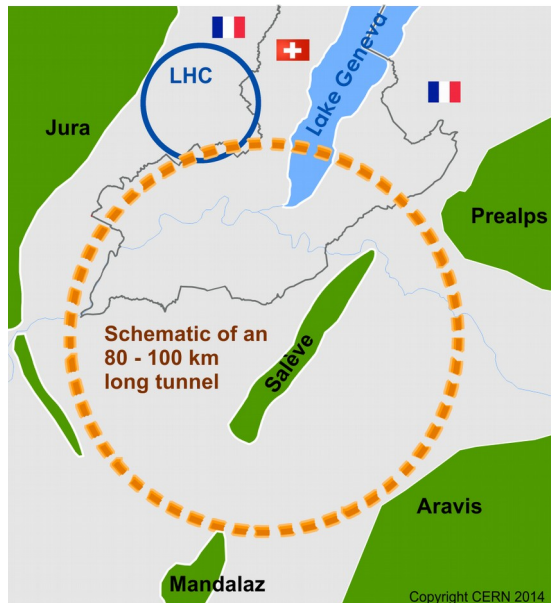
- FCC-hh (pp collider): final goal defining the whole infrastructure
 - ~ 16T magnets → 100TeV pp collider in 97.75km tunnel
- FCC-ee: as a potential first step
- FCC-eh: as an option



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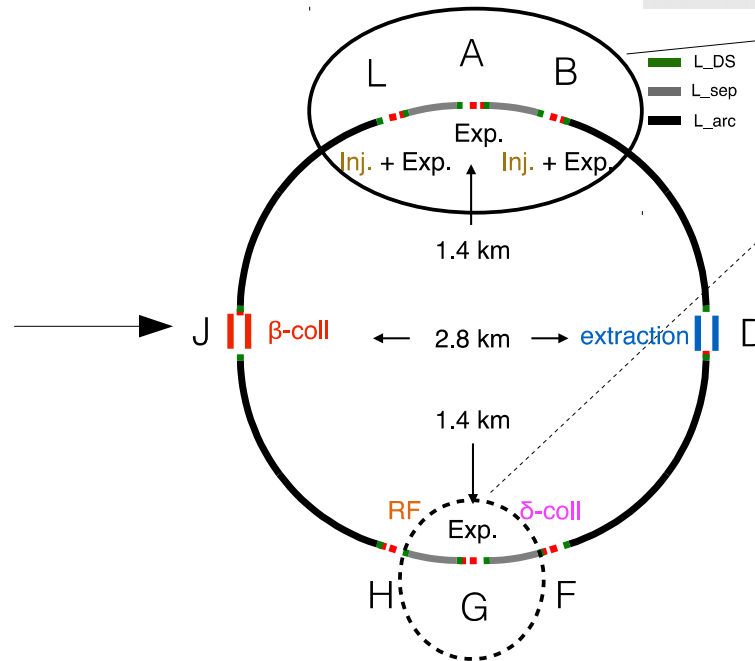
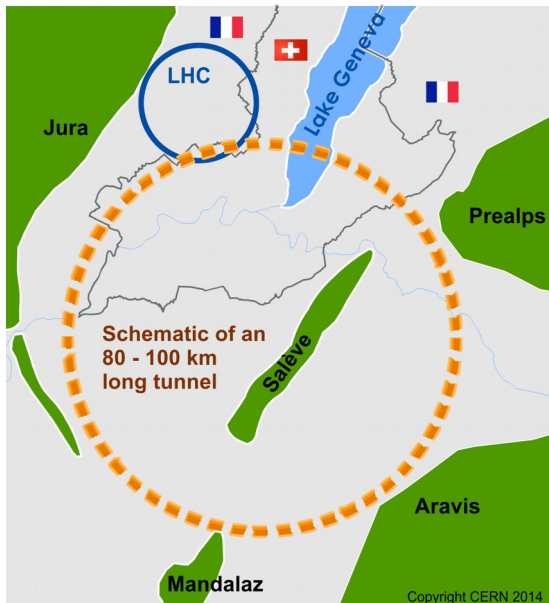
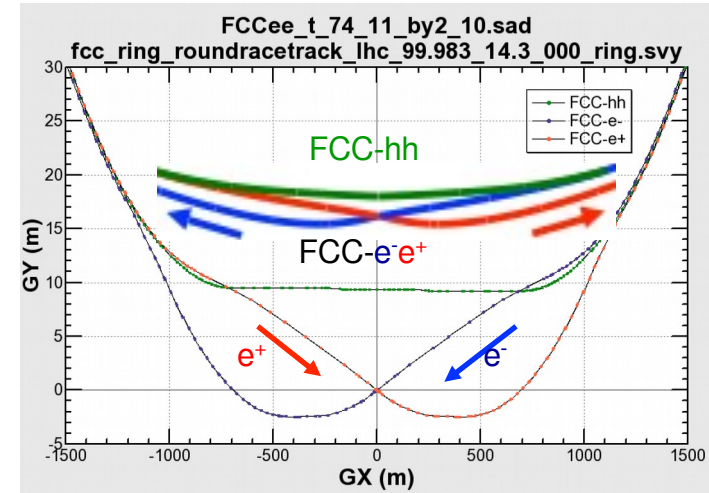


- A&G 2 high-luminosity exp.
- L&B 2 other exp.

Future Circular Collider

- FCC machine:**

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- L&B 2 other exp.

Key FCC-hh parameters

Parameter	FCC-hh	HE-LHC	(HL) LHC
Collision cms energy [TeV]	100	27	14
Dipole field [T]	16	16	8.33
Circumference [km]	97.75	26.7	26.7
# IP	2 main & 2	2 & 2	2 & 2
Beam current [A]	0.5	1.12	(1.12) 0.58
Bunch intensity [10^{11}]	1	1 (0.2)	(2.2) 1.15
Bunch spacing [ns]	25	25 (5)	25
beta* [m]	1.1	0.3	(0.20) 0.55
Luminosity/IP [$10^{34} \text{ cm}^{-2}\text{s}^{-1}$]	5	30	(5) 1
# Events/bunch crossing	170	<1020 (204)	(135) 27
Stored energy/beam [GJ]	8.4	1.3	(0.7) 0.36
Synchrotron rad. [W/m/ap.]	28.4	4.6	(0.33) 0.17

- **Baseline (phase 1)**: 10 yrs of operation @ $L_{\text{peak}} = 5 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1} \rightarrow 2.5 \text{ ab}^{-1}$ per detector
- **Ultimate (phase 2)**: 15 yrs of operation @ $L_{\text{peak}} \leq 30 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1} \rightarrow 15 \text{ ab}^{-1}$ per detector

→ **Total: O(20)ab⁻¹ per experiment**

Understanding FCC-hh parameters

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14TeV \rightarrow 100 TeV
 $\sigma_{\text{inelastic}}$: 80mb \rightarrow 108mb
 average p_T : 0.6 \rightarrow 0.8 GeV/c
 multiplicity_{charged/unit η} : 5.4 \rightarrow 8

\rightarrow the minimum bias events @FCC are quite similar to ones @HL-LHC, **but ...**

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5x increase in pile-up wrt HL-LHC

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- \rightarrow **pile-up per bunch crossing $O(1000)$ is a big challenge** \rightarrow keeping 5ns (versus 25ns) operation scheme as an option

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6x increase in luminosity
 wrt HL-LHC

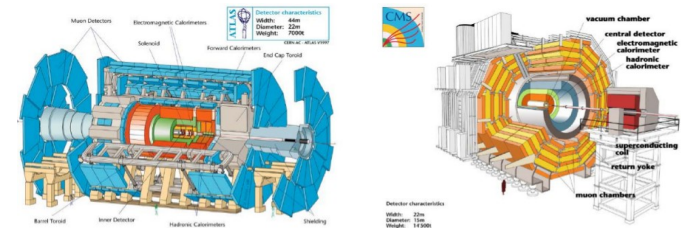
- the minimum bias events @FCC are quite similar to ones @HL-LHC, but ...
- **pile-up per bunch crossing $O(1000)$ is a big challenge** → keeping 5ns (versus 25ns) operation scheme as an option
- FCC-hh represents an extremely high luminosity machine → expecting **huge particle/data rates & significantly higher rad. level in the inner/fwd detector**

Physics Requirements on Detector Design

- **Design strongly depends on outcome of future LHC discoveries:**
 - **In case of new discoveries** → precise understanding of new physics will motivate the design
 - **In case no new physics is discovered** → mass scale of new physics may be beyond LHC reach or final states are too elusive → **higher mass reach, high luminosity machine & precise det. are the key!**

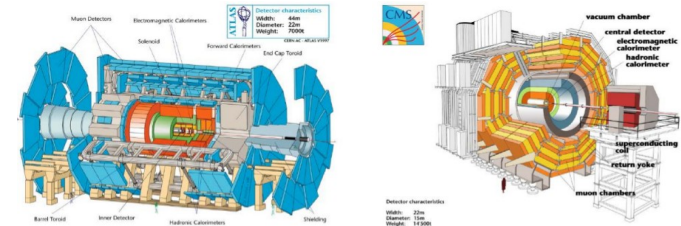
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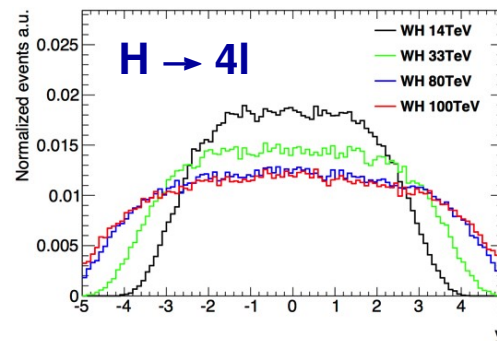
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- **The key benchmarks: Higgs & EWSB phenomena** → FCC opens us a new kinematic & dynamical regime

- e.g. $W(H \rightarrow 4l)$

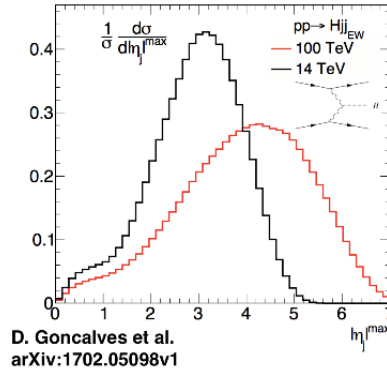
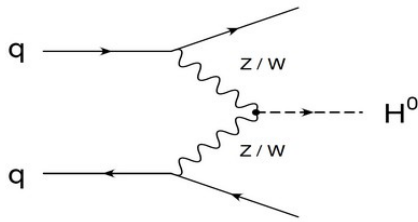


	14 TeV		100 TeV	
	2.5	4	2.5	4
ggF	0.74	0.99	0.56	0.88
WH	0.66	0.97	0.45	0.77
ZH	0.69	0.98	0.48	0.8
ttH	0.84	1	0.56	0.9
VBF	0.75	0.98	0.55	0.87

→ **Need extended tracking & ECAL coverage up-to $|\eta| \sim 4$** (c.f. $|\eta| \sim 2.5$ for LHC exp.)

Physics Requirements on Detector Design

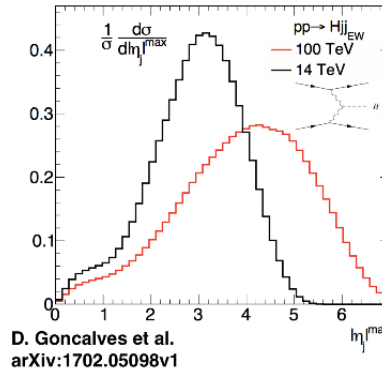
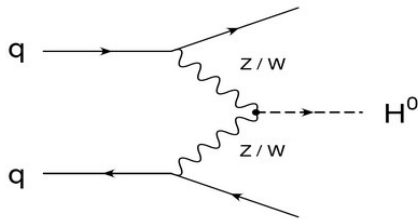
- e.g. VBF



→ Need for efficient VBF jet measurement **up-to $|\eta| \sim 6$**

Physics Requirements on Detector Design

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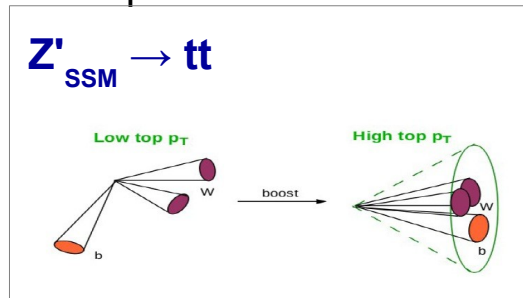


→ Need for efficient VBF jet measurement **up-to $|\eta| \sim 6$**

• FCC immensely increases **the mass reach** $\sim E/14\text{TeV}$ (by factor of 5-7 increase, depending on $L_{\text{integr.}}$)

- e.g. $Z' \rightarrow \mu\mu$ or $Z' \rightarrow tt$

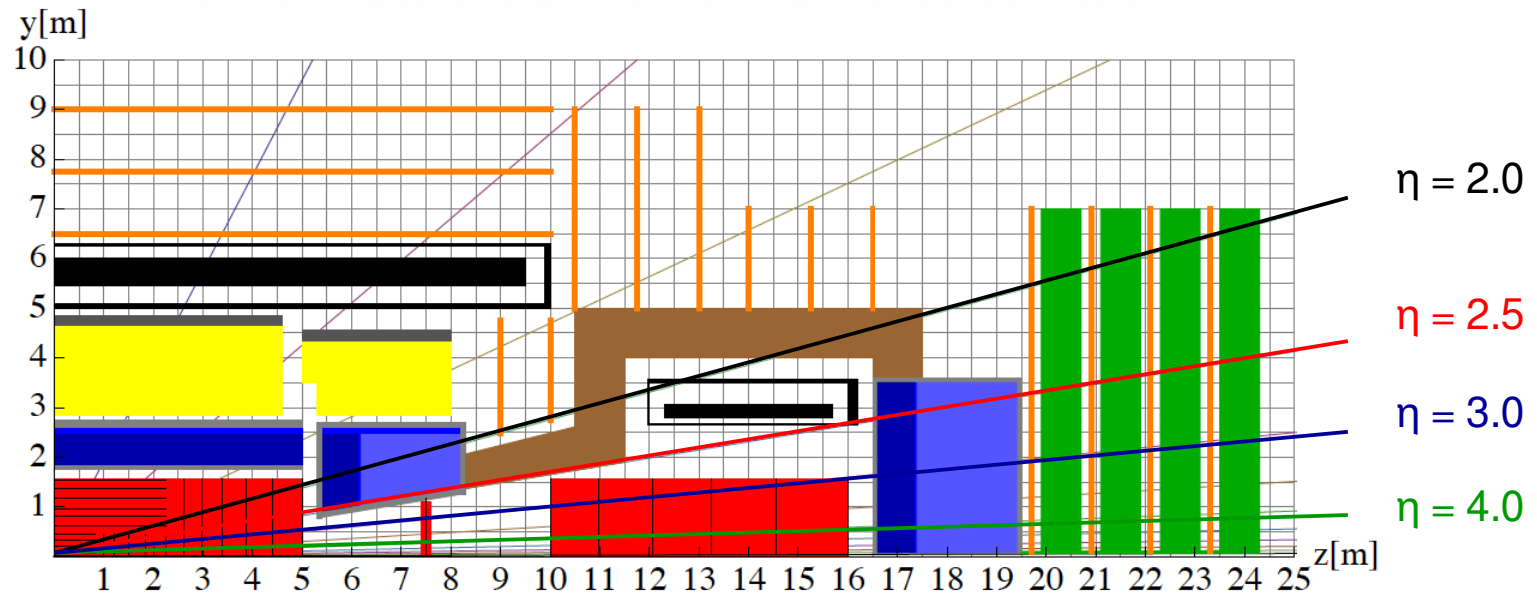
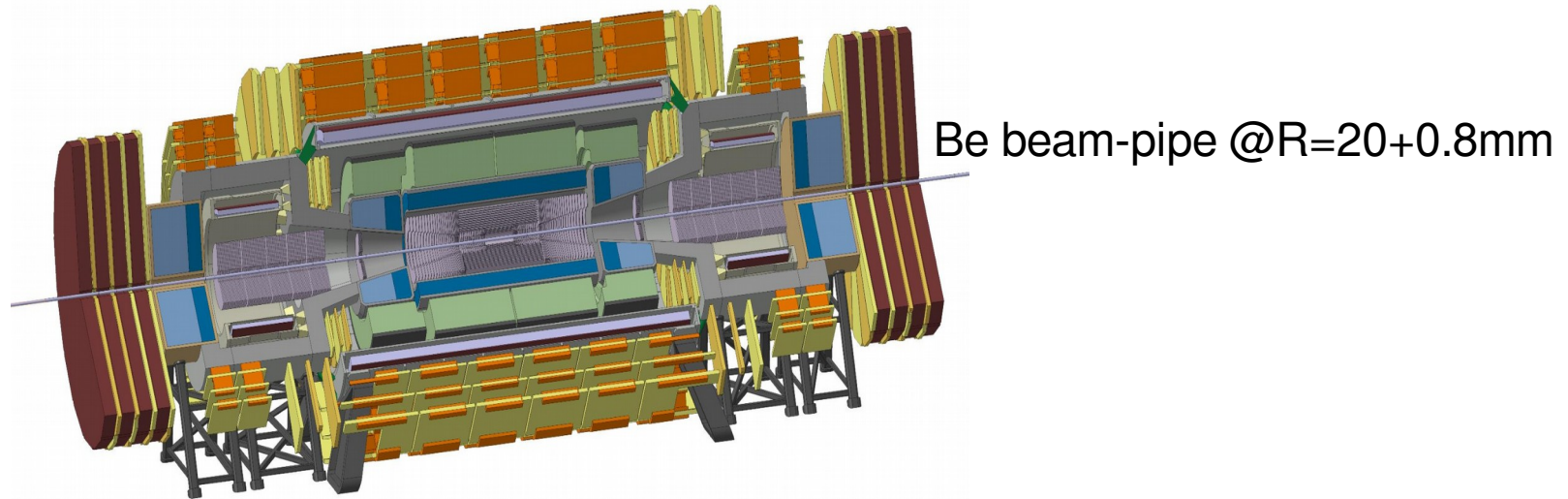
→ Need for **high p_T resolution $\sim 10\text{-}20\%$ @ 10TeV** (cf. LHC: 10% @ 1TeV), but **keep sensitivity to low p_T tracks**



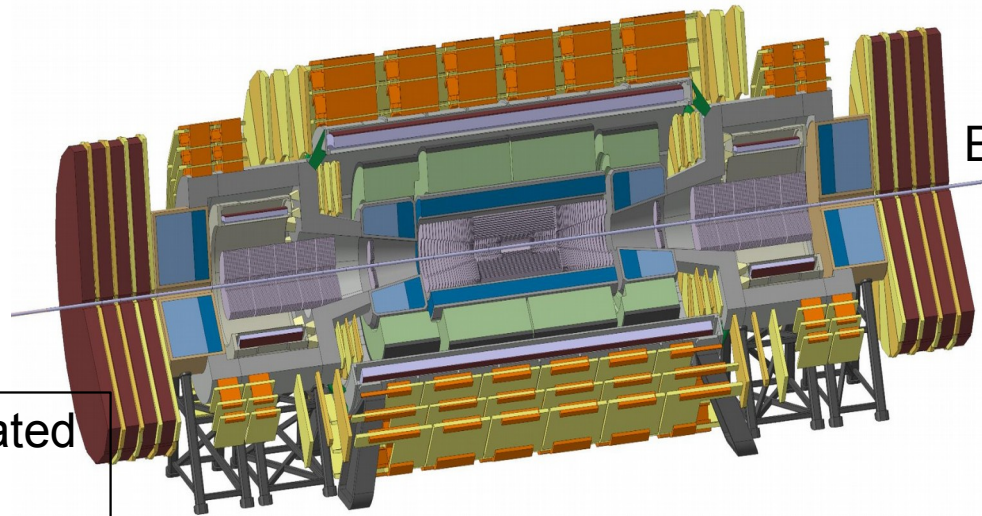
Expected highly-collimated final states – boosted decay products
(min distance between 2 partons $\sim m/p_T$)

→ **High Tracker, E/HCAL granularity essential** to resolve jet-substructure (E/HCAL), reject bkg,...

Reference Detector Layout

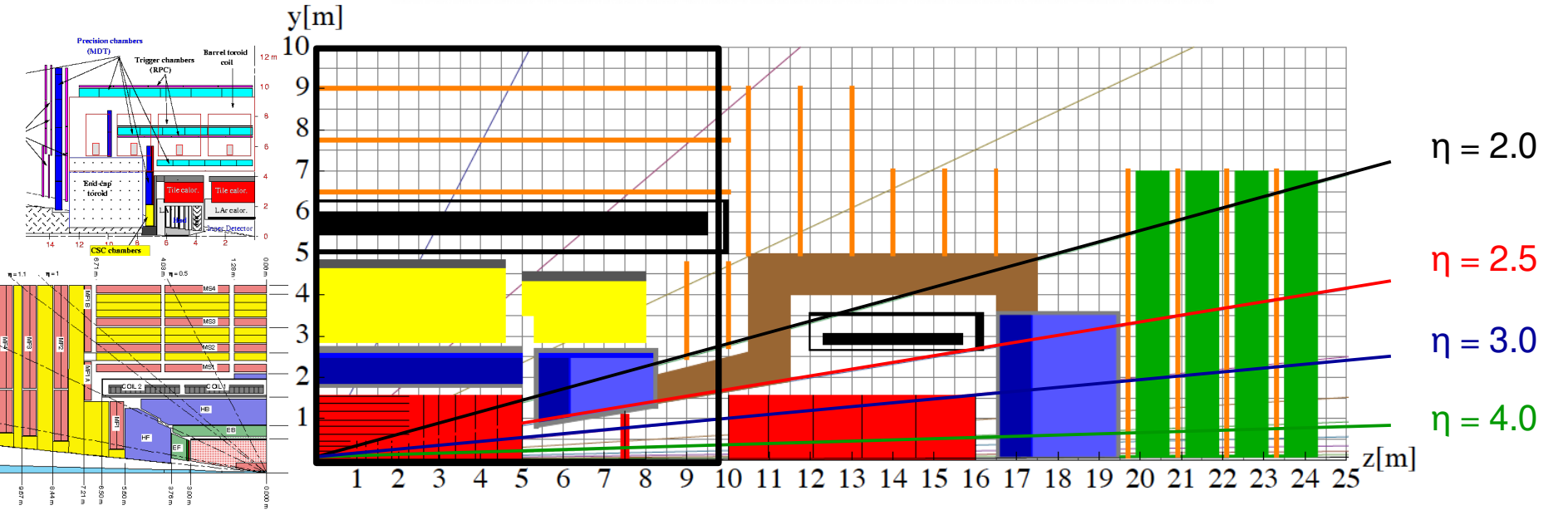


Reference Detector Layout

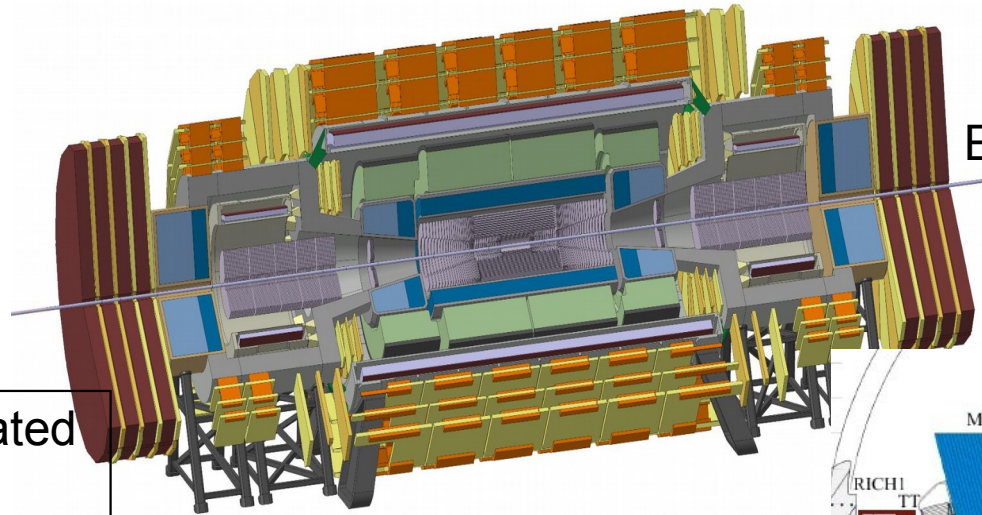


Be beam-pipe @R=20+0.8mm

Central region motivated by ATLAS/CMS



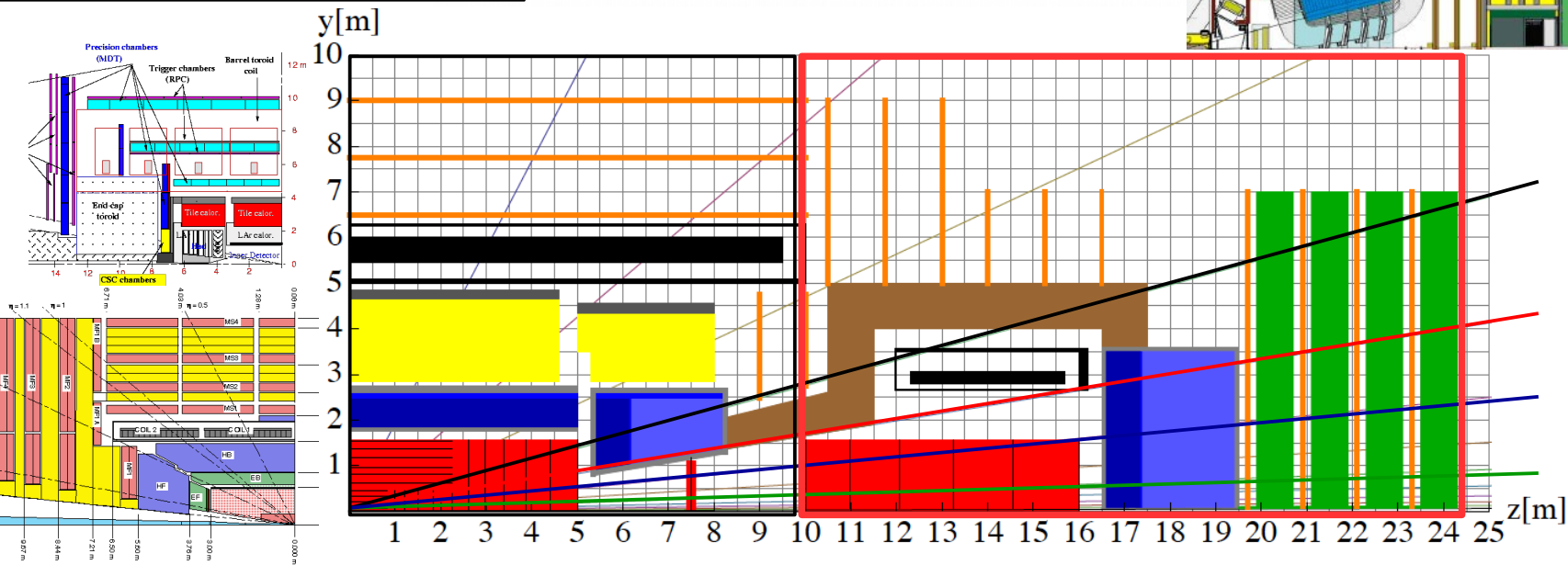
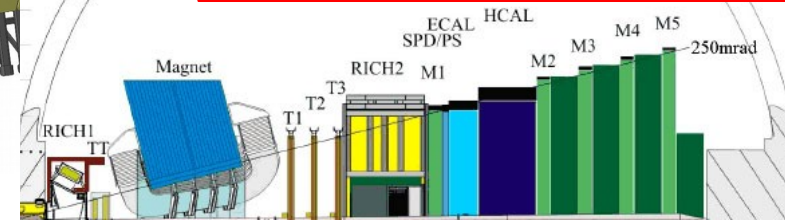
Reference Detector Layout



Be beam-pipe @ $R=20+0.8\text{mm}$

Forward region motivated by LHCb

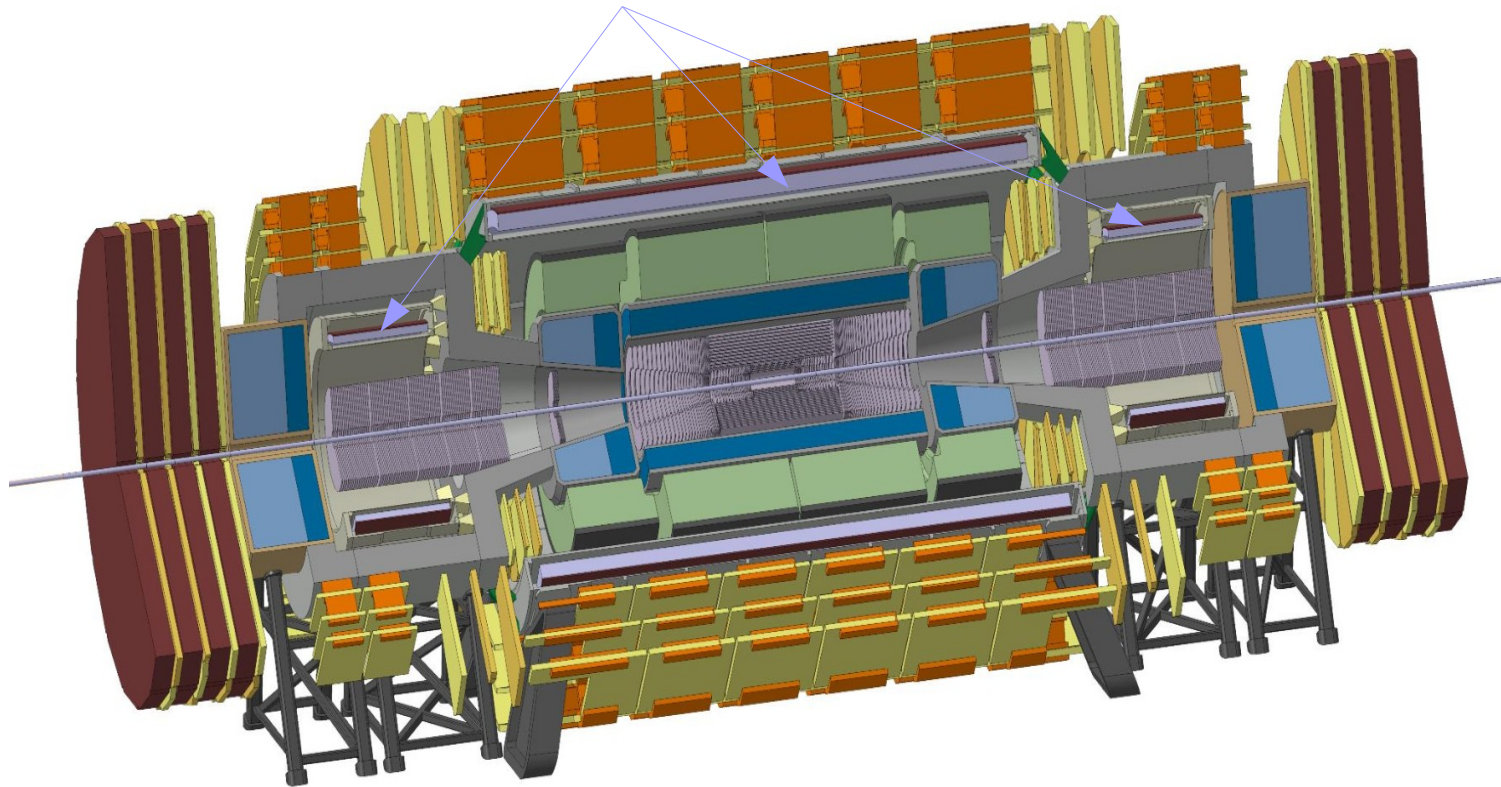
Central region motivated by ATLAS/CMS



$\eta = 2.0$
 $\eta = 2.5$
 $\eta = 3.0$
 $\eta = 4.0$

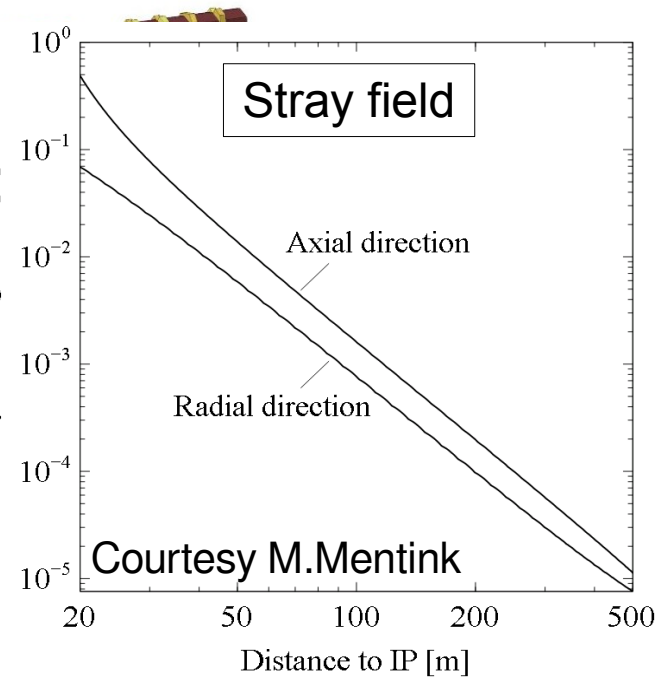
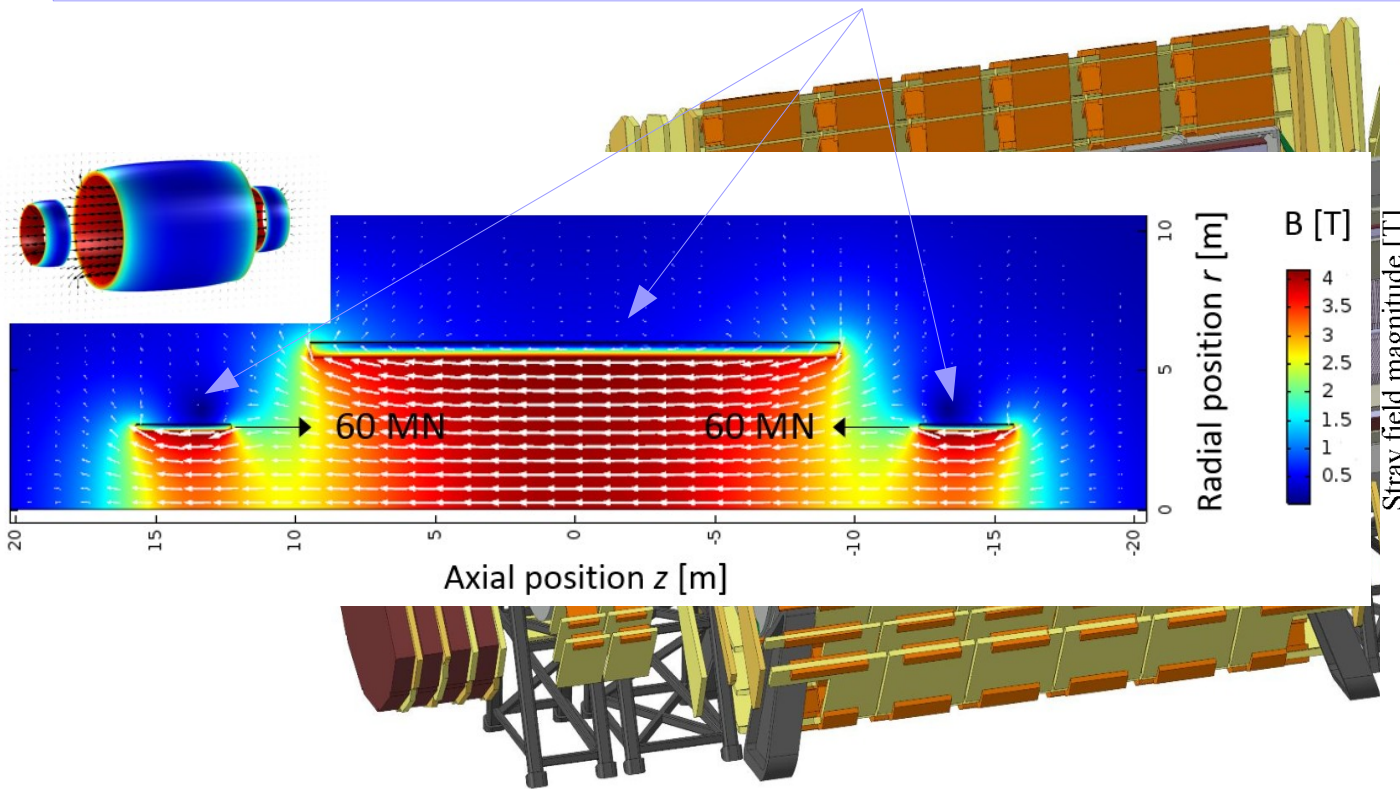
Reference Detector Layout

4T solenoid (10m free bore) + 2x 4T Fwd solenoids (no shielding)



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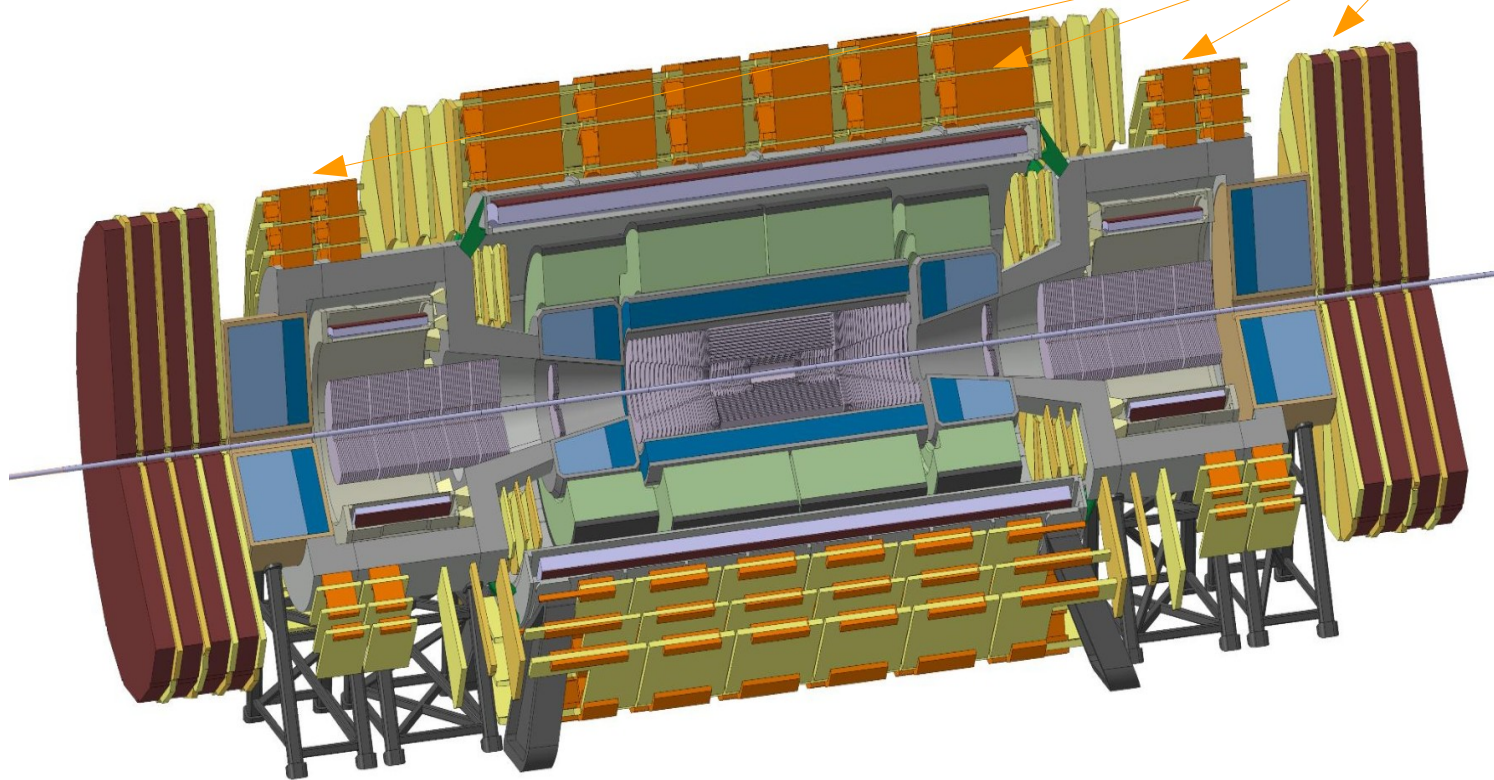
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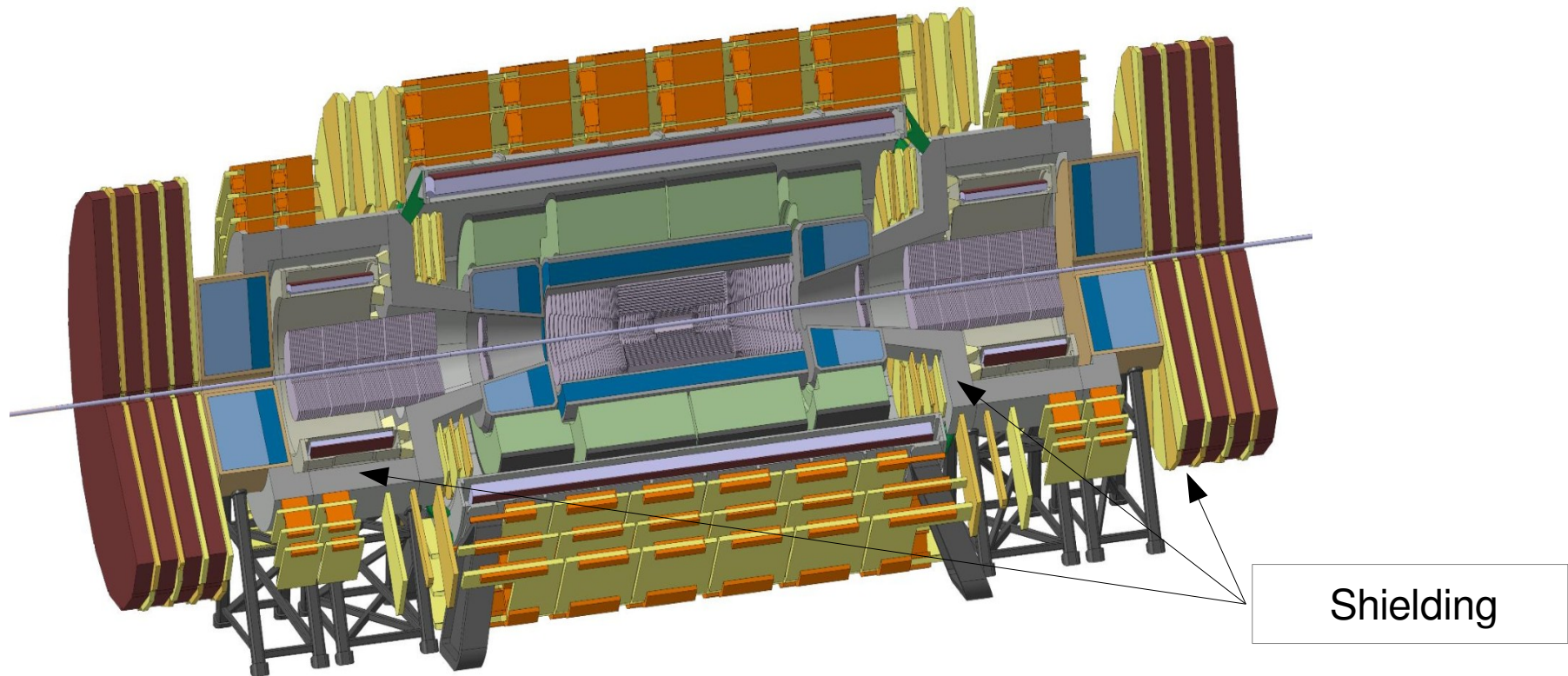
Muon system



Reference Detector Layout

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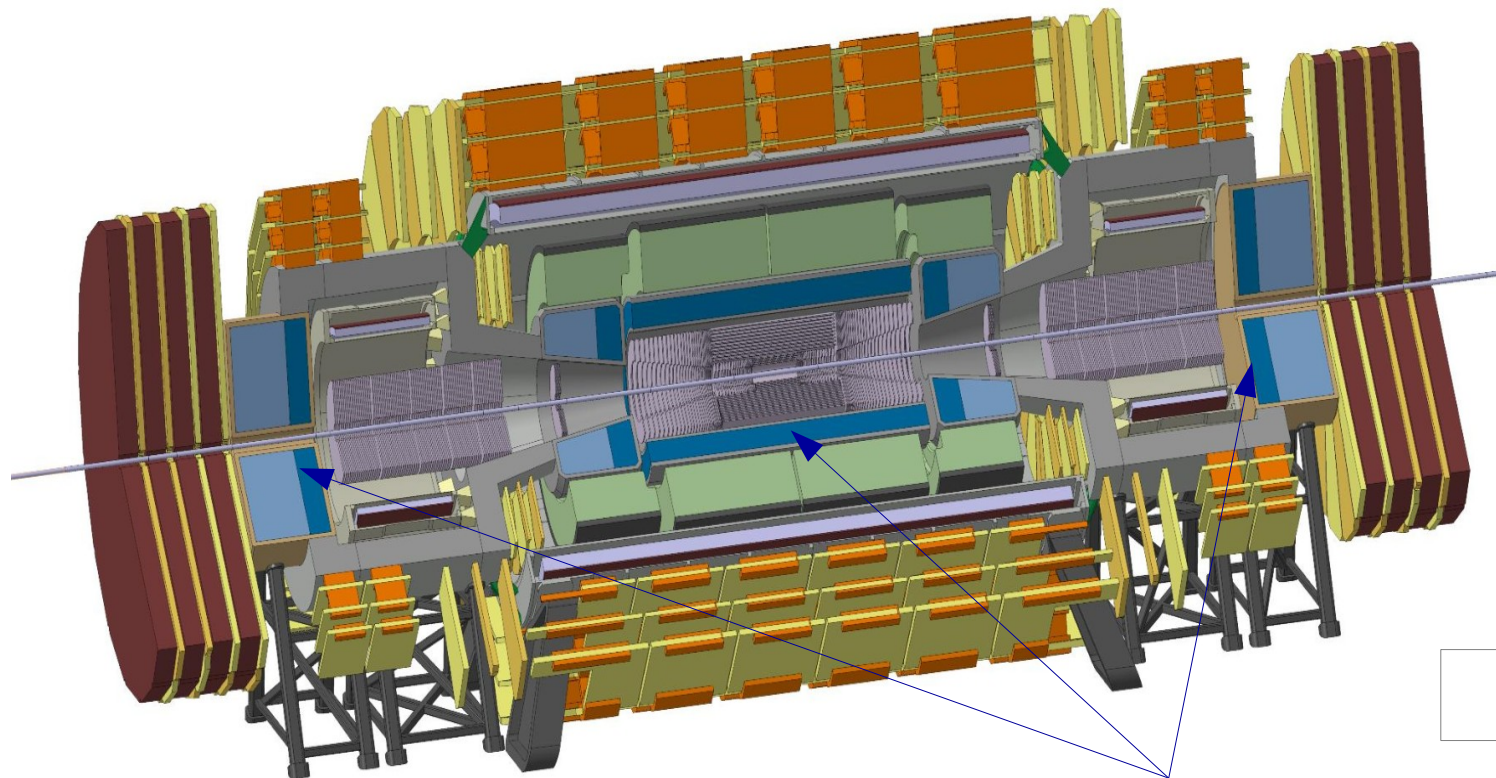


Shielding

Reference Detector Layout

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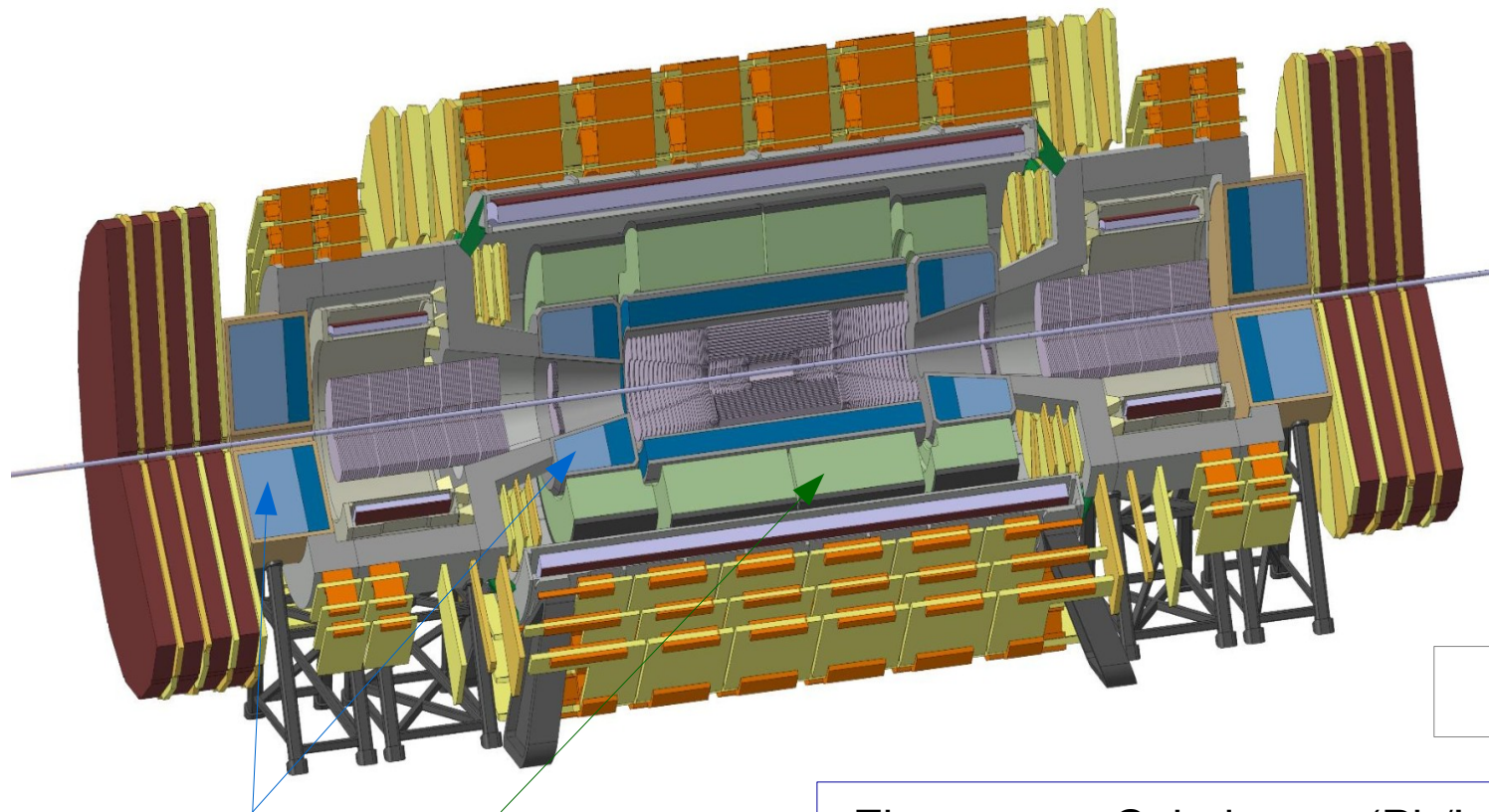
Shielding

Electromag. Calorimeter (Pb/LAr)

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Shielding

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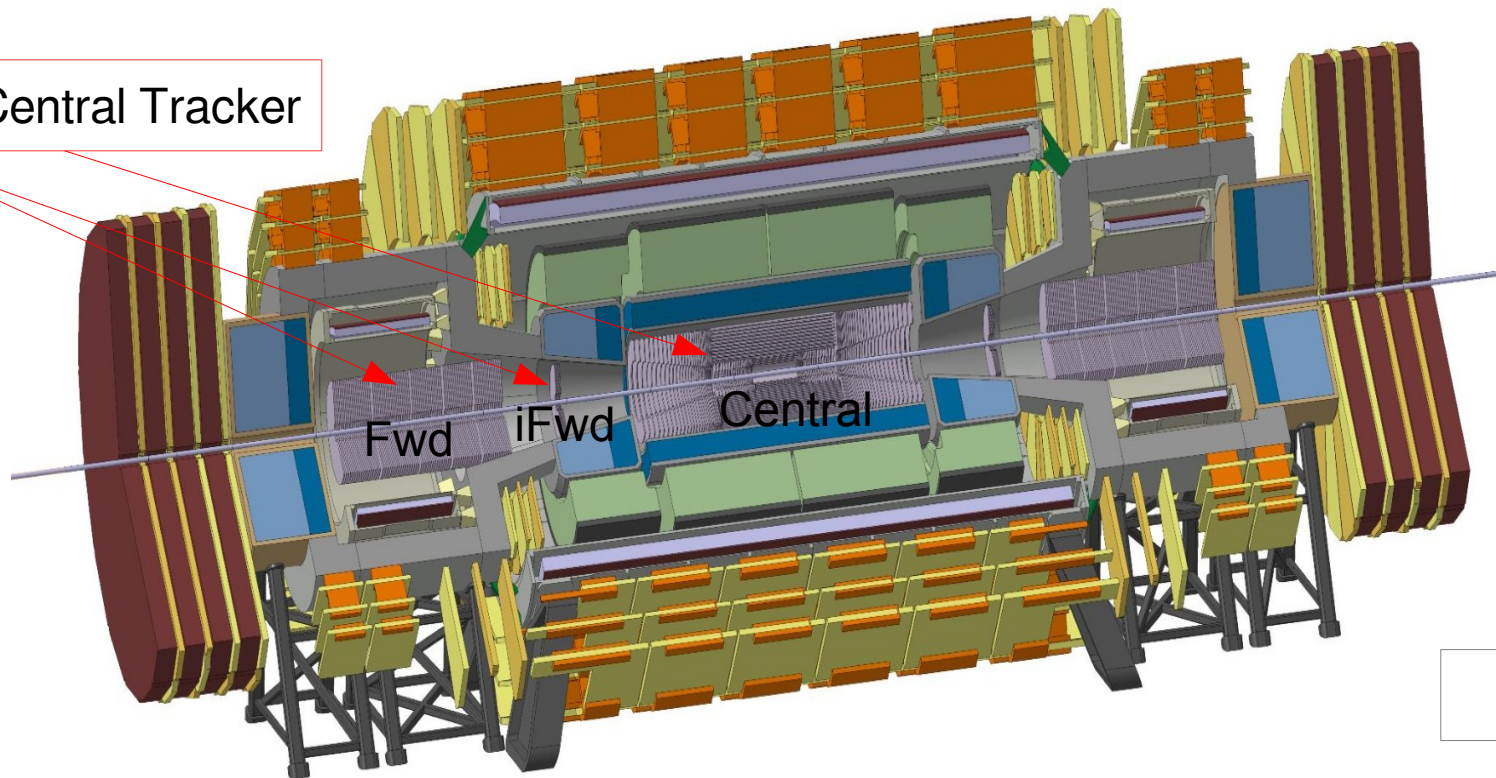
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(i)Fwd + Central Tracker



Shielding

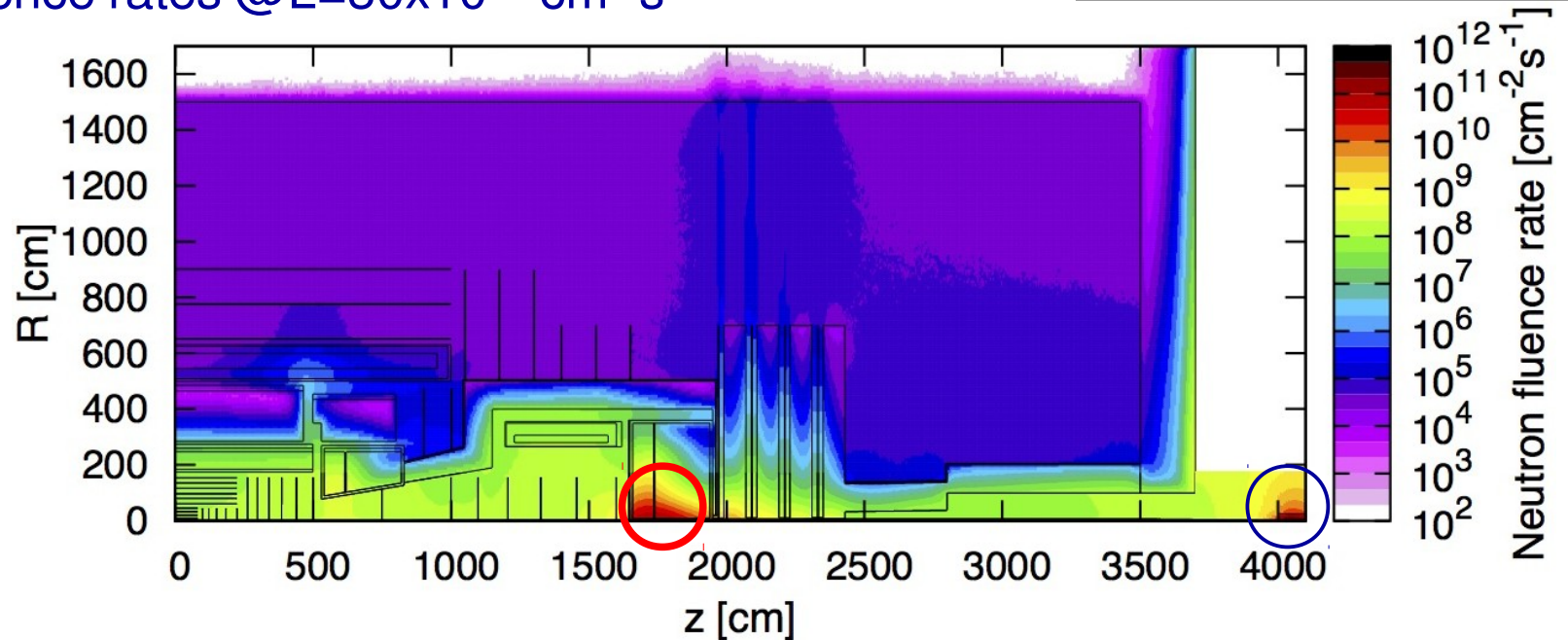
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FCC-hh & Radiation Rates?

- Neutron fluence rates @ $L=30 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

Courtesy of M.I.Besana

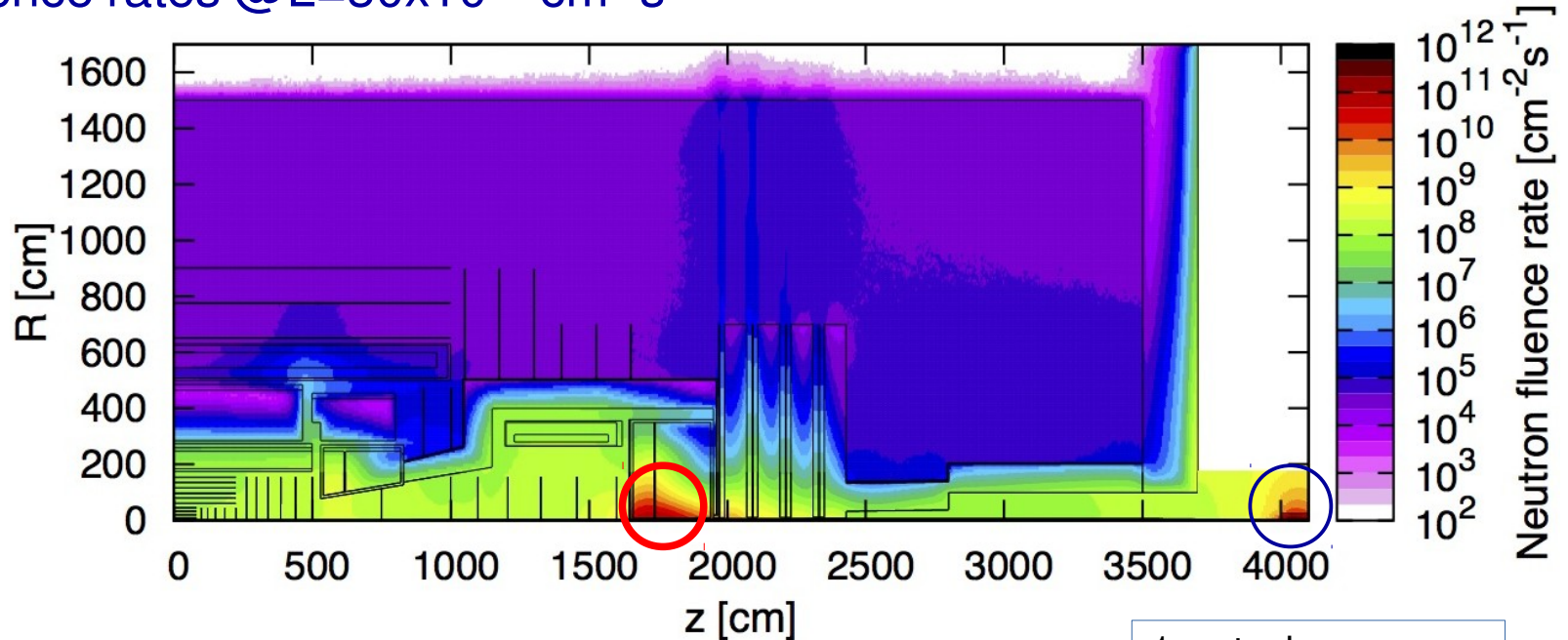


→ 2 main hot spots: **FWD calorimeter** & **TAS**

FCC-hh & Radiation Rates?

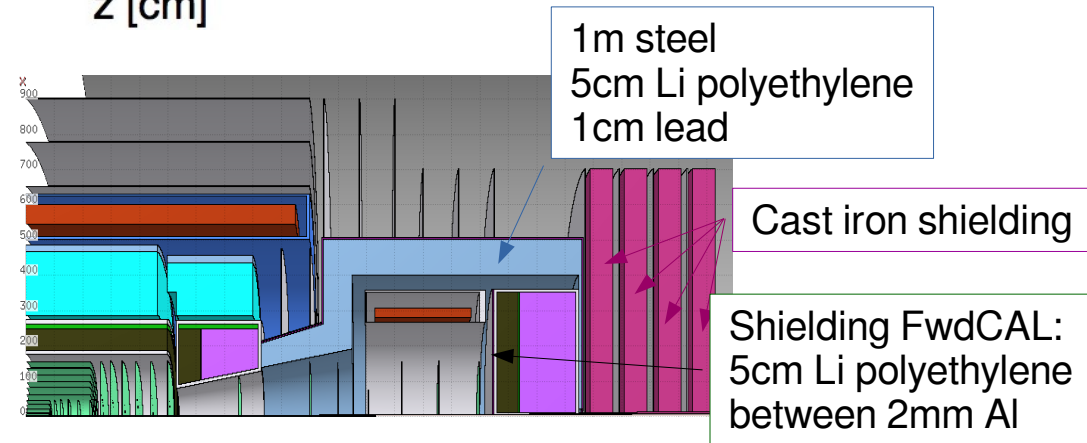
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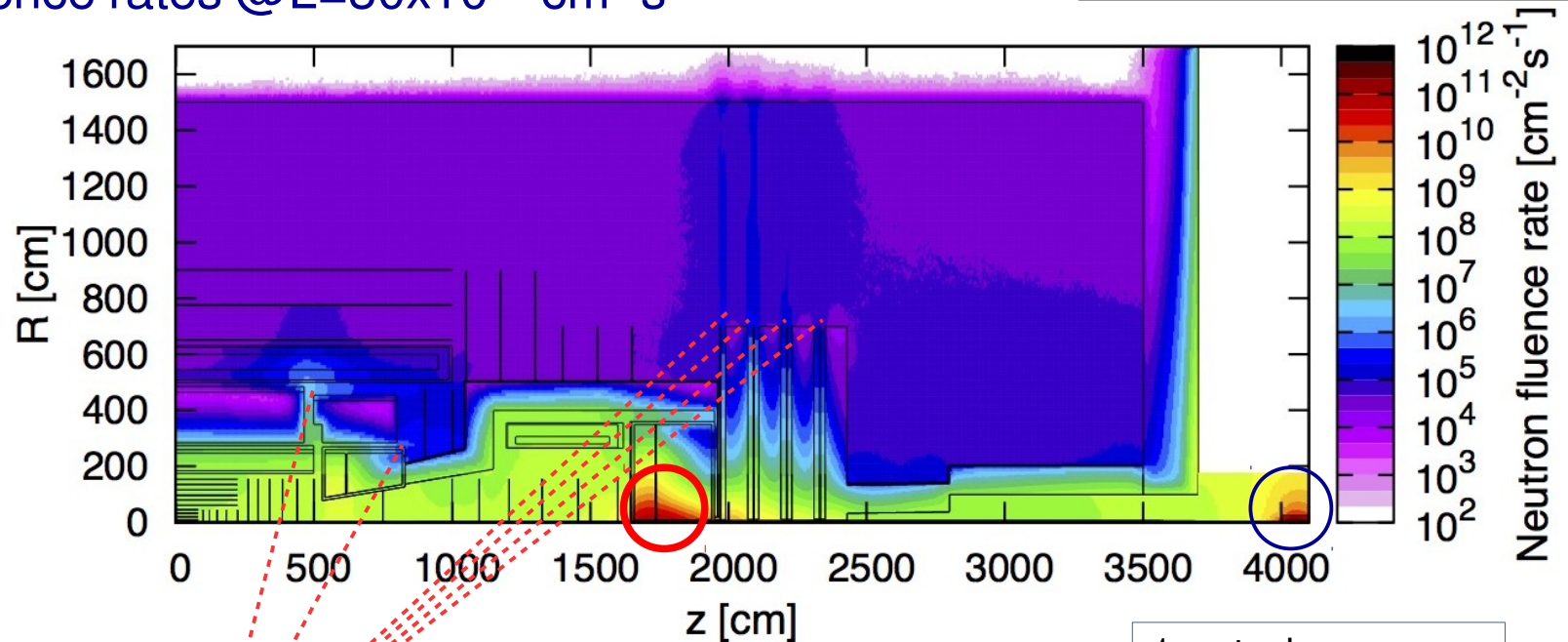
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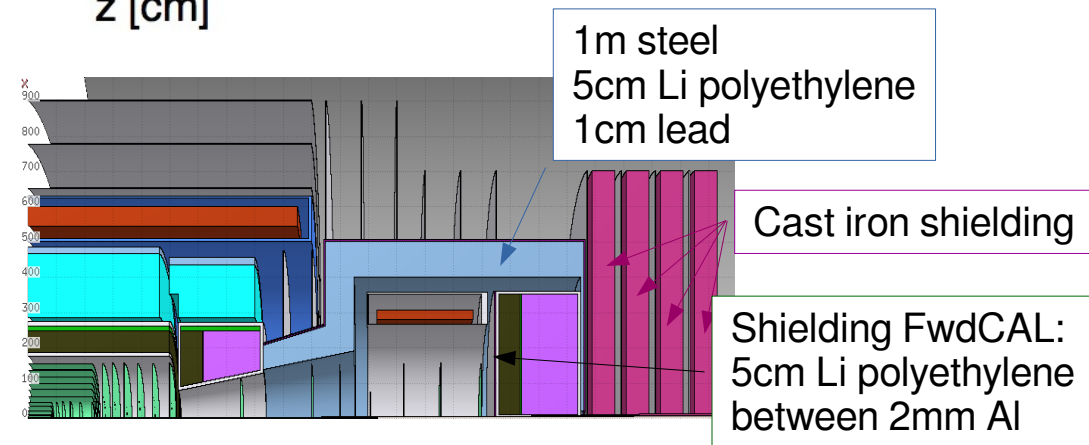
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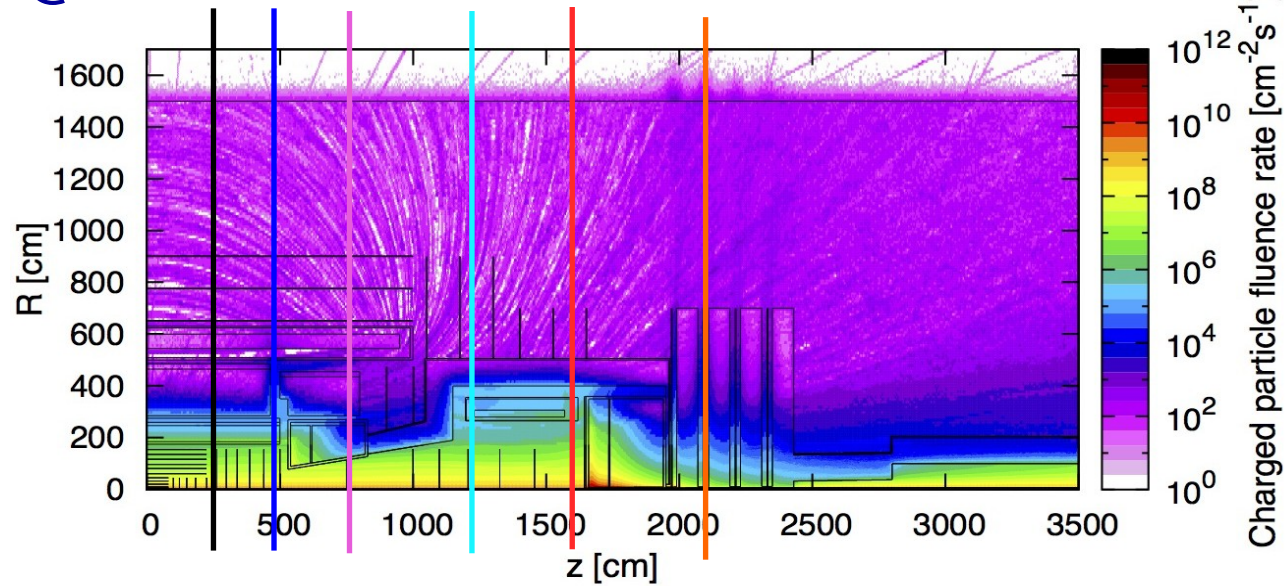
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- **Several leakage channels appear** due to service channels etc.



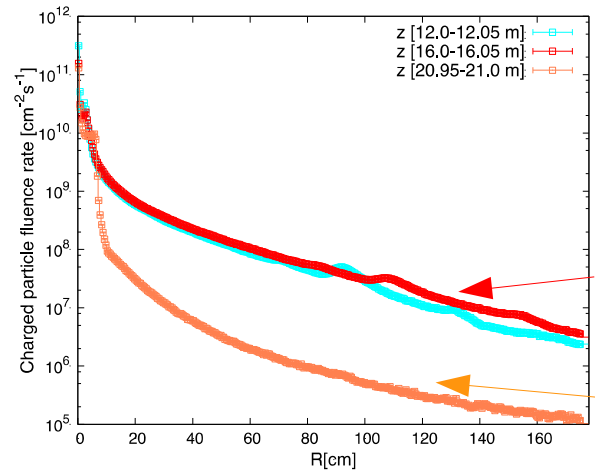
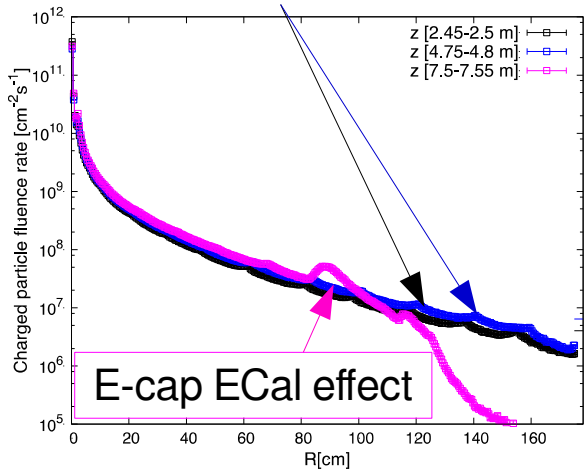
Radiation Rates in Tracker

Courtesy of M.I.Besana

- Charged particle fluence rates @ $L=30 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$



- Layer structure
- ECal effect



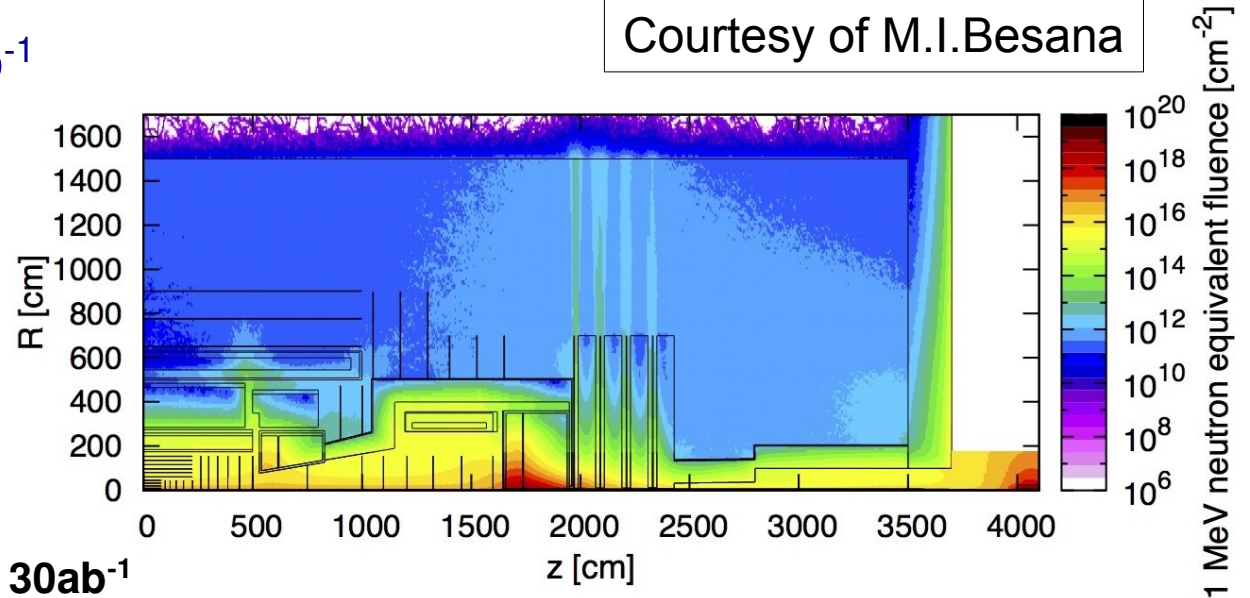
Closer to the FwdCAL hotspot

Effect of shielding in muon chamber

Tracker & Long-term Damage after 30ab⁻¹

- 1 MeV neq fluence after 30ab⁻¹

Courtesy of M.I.Besana



Long-term damage for Tracker after 30ab⁻¹

R [mm]	z[m]	Dose [MGy]	1 MeV equivalent Fluence [cm ⁻²]
25	0	320	$5.5 \cdot 10^{17}$
60	0	88	$1.25 \cdot 10^{17}$
100	0	40	$6 \cdot 10^{16}$
150	0	23	$3.3 \cdot 10^{16}$
270	0	8.8	$1.51 \cdot 10^{16}$
900	0	0.65	$3.2 \cdot 10^{15}$
25	5	410	$3.7 \cdot 10^{17}$
50	16	250	$2 \cdot 10^{17}$

Radiation @ FCC:

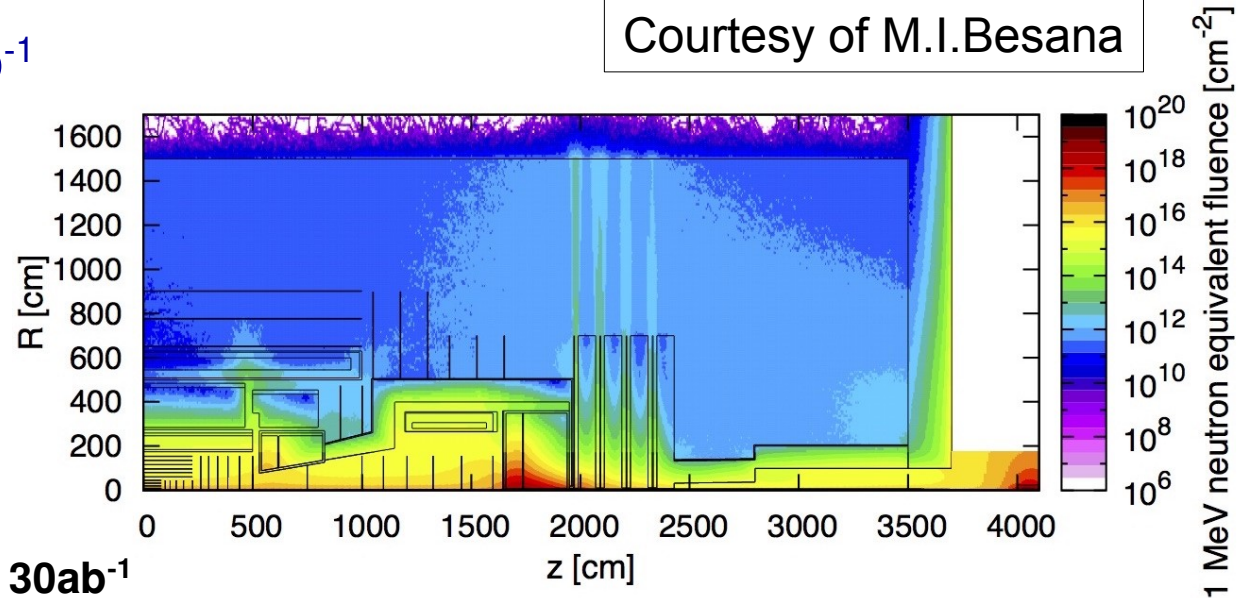
→ @R=25mm: $\sim 6 \cdot 10^{17}$ neq cm⁻², TID~0.4GGy

- LHC = 1
- HL-LHC → 20x LHC
- FCC → 600x LHC

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↘ HL-LHC rad. tolerance limit @R~270mm

Tracker Layout & Design Driving Principles

- Key tracker parameters:

- Granularity in R- Φ \rightarrow driven by requirement on dp_T/p_T res.

$$\frac{\Delta p_T}{p_T} = \frac{\sigma[\text{m}] p_T[\text{GeV}/c]}{0.3 B[\text{T}] L^2[\text{m}^2]} f(N)$$

L: 1.55m
B: 4T
 $\sigma_{R-\Phi}$: 10(7.5)um
 N_{layers} : 12

} ~ 20% @ 10TeV/c

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- Granularity in R- Φ \rightarrow driven by requirement on dp_T/p_T res.

$$\frac{\Delta p_T}{p_T} = \frac{\sigma[\text{m}] p_T[\text{GeV}/c]}{0.3 B[\text{T}] L^2[\text{m}^2]} f(N)$$

L: 1.55m	}	~ 20% @ 10TeV/c
B: 4T		
$\sigma_{R-\Phi}$: 10(7.5)um		
N_{layers} : 12		

- **Number of layers N** \rightarrow driven by dp_T/p_T res. & pattern recognition capabilities

Note: res. improves as $1/\sqrt{N_{\text{layers}}}$, but material budget (MB) increases as N_{layers}

**Low MB
Important!**

Tracker Layout & Design Driving Principles

- Key tracker parameters:

- Granularity in R- Φ \rightarrow driven by requirement on dp_T/p_T res. & occupancy limit ($\sim 1\%$)

$$\frac{\Delta p_T}{p_T} = \frac{\sigma[m] p_T[\text{GeV}/c]}{0.3 B[\text{T}] L^2[\text{m}^2]} f(N)$$

$L: 1.55\text{m}$
 $B: 4\text{T}$
 $\sigma_{R-\Phi}: 10(7.5)\mu\text{m}$
 $N_{\text{layers}}: 12$

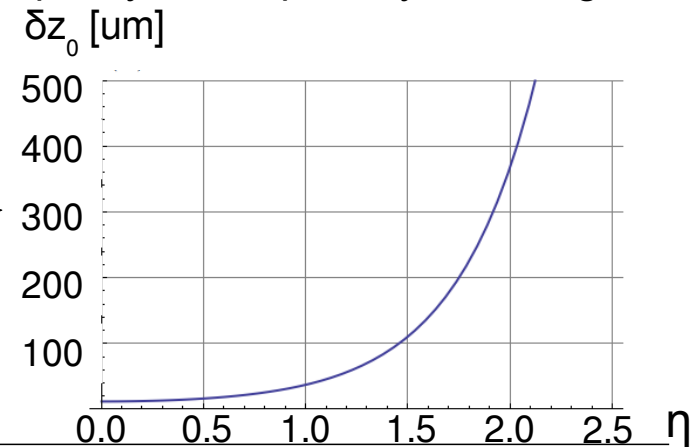
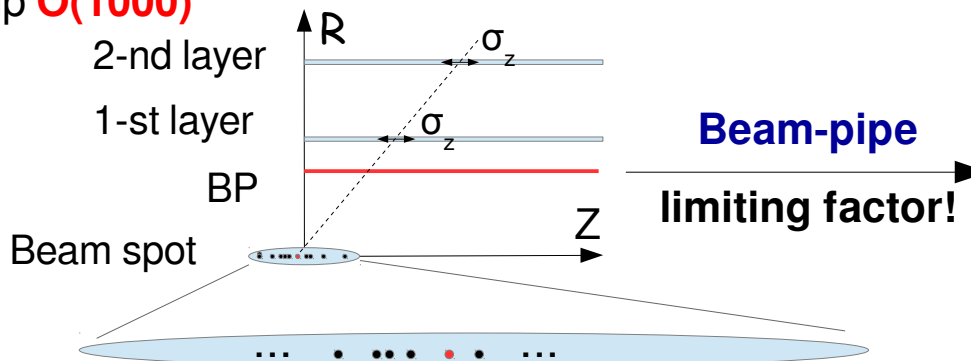
$\sim 20\% @ 10\text{TeV}/c$

- Number of layers $N \rightarrow$ driven by dp_T/p_T res. & pattern recognition capabilities

Note: res. improves as $1/\sqrt{N_{\text{layers}}}$, but material budget (MB) increases as N_{layers}

Low MB Important!

- Granularity in Z** \rightarrow driven by pattern recognition capabilities, occupancy limit & primary vertexing in given pile-up **$O(1000)$**

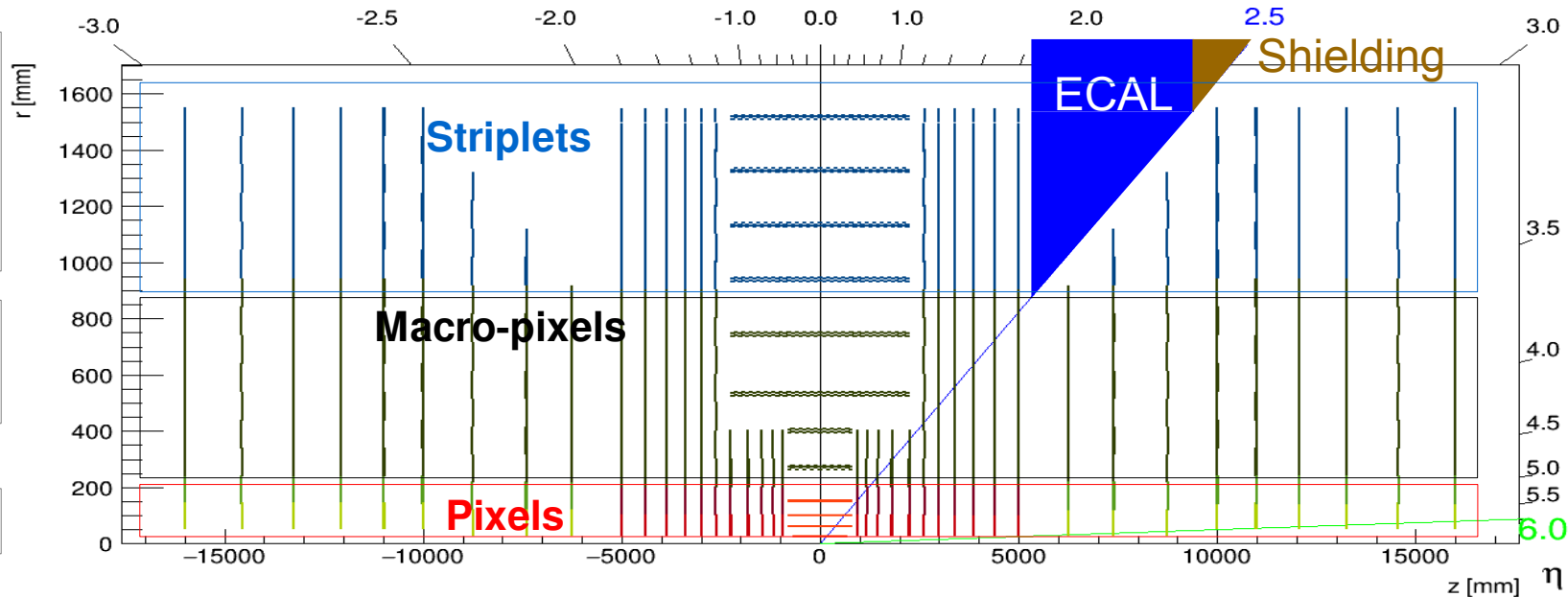


Reference Tracker Layout (v3.03)

Surface: $\sim 430\text{m}^2$
 #Channels: **489.4M**
 9964.4M
 5460.9M

Pixel $R \nearrow 0.9\text{ m}$
 due to occupancy

4 (seed) BRL layers



Pixels : $25 \times 50 \mu\text{m}^2$ (1-4th BRL layers, EC R1),
 $100/3 \times 100 \mu\text{m}^2$ (R2),
 $100/3 \times 400 \mu\text{m}^2$ (R3, R4)

Macro-pixels: $100/3 \times 400 \mu\text{m}^2$

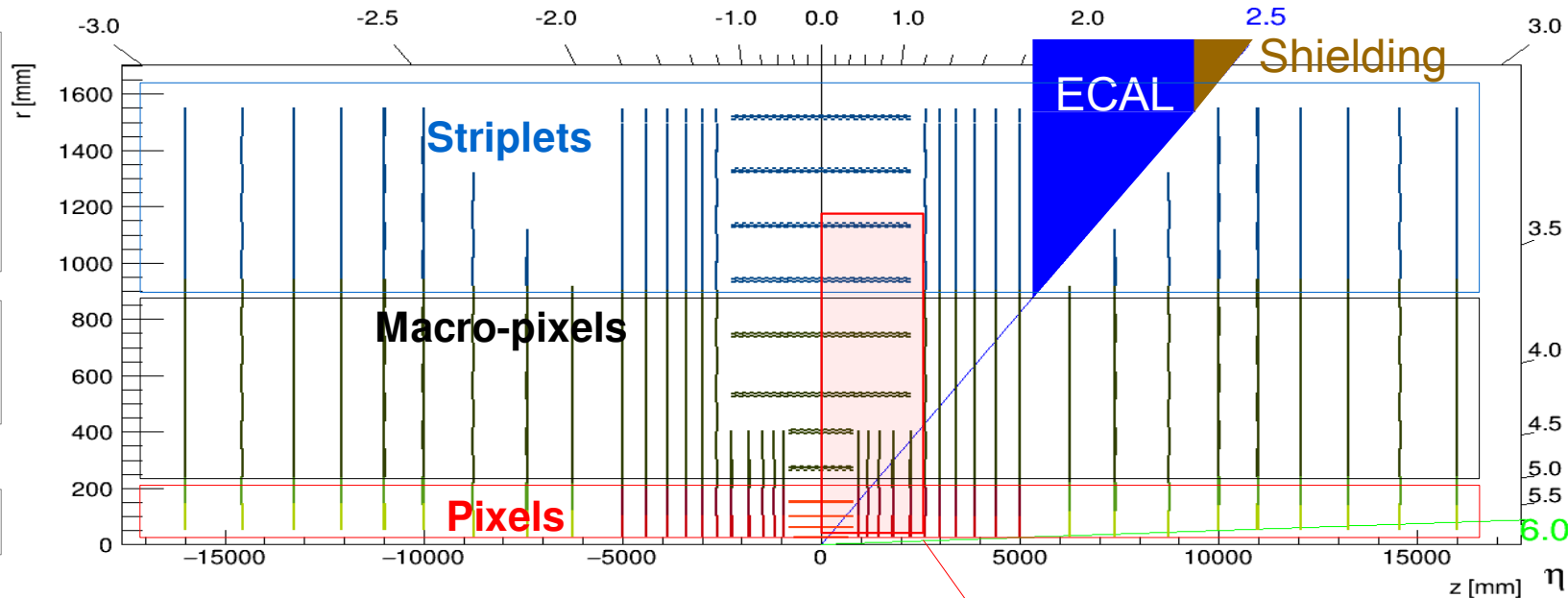
Strips : $100/3 \mu\text{m} \times 50\text{mm}$ (BRL),
 $100/3 \mu\text{m} \times 10\text{mm}$ (EC)

Reference Tracker Layout (v3.03)

Surface: $\sim 430\text{m}^2$
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Pixel $R \nearrow 0.9\text{ m}$
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4 (seed) BRL layers



\sim dimensions of CMS tracker

Pixels : 25x50 μm^2 (1-4th BRL layers, EC R1),
 100/3x100 μm^2 (R2),
 100/3x400 μm^2 (R3,R4)

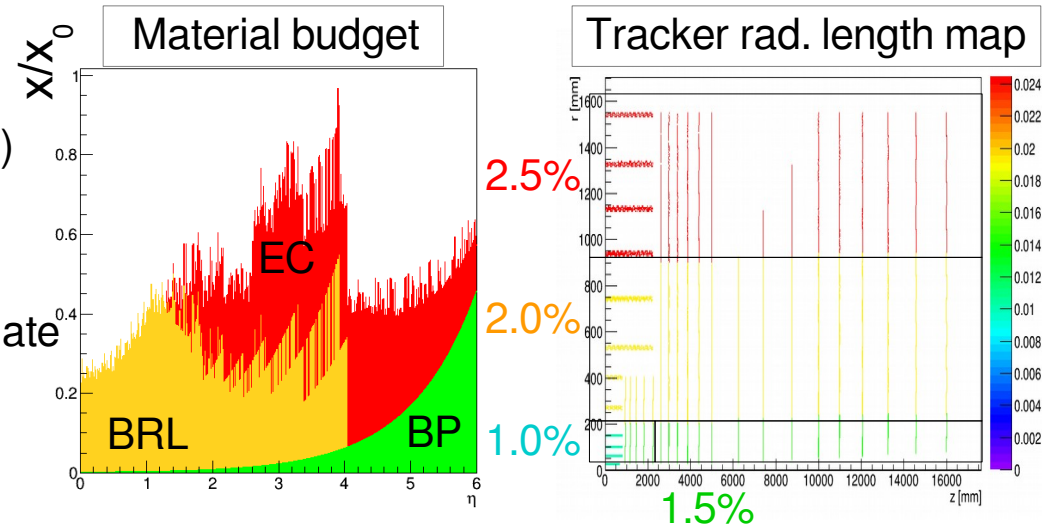
Macro-pixels: 100/3x400 μm^2

Strips : 100/3 μm x50mm (BRL),
 100/3 μm x10mm (EC)

Huge increase in #pixel channels wrt LHC experiments due to requirements on tracking up to $\eta=6$ & resilience to **high rad. levels** generated by FCC-hh!

Material Budget & Tracking Resolution

- A simplified model for MB assumed:
 - $x/x_0 \sim 1-2.5\%$ per layer (services accumul. effect)
(20% Si, 42% C, 2% Cu, 6% Al, 30% Plastic)
- **technology input needed** for more real. estimate

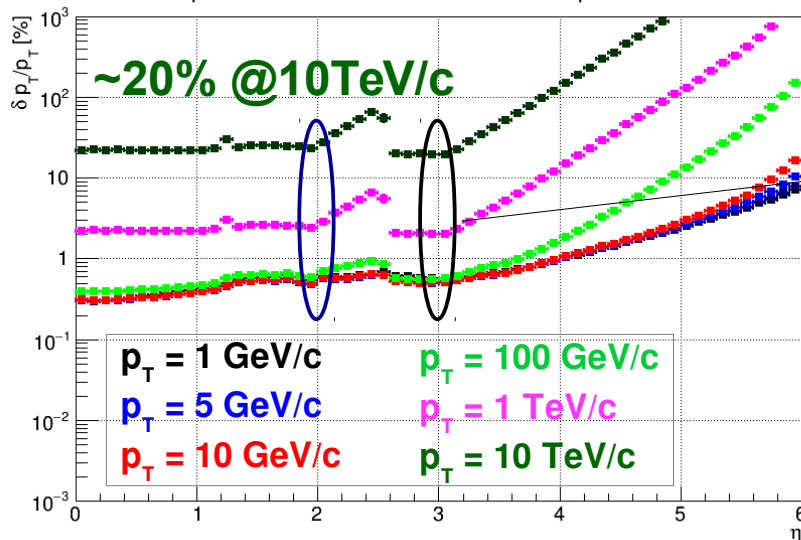


Material Budget & Tracking Resolution

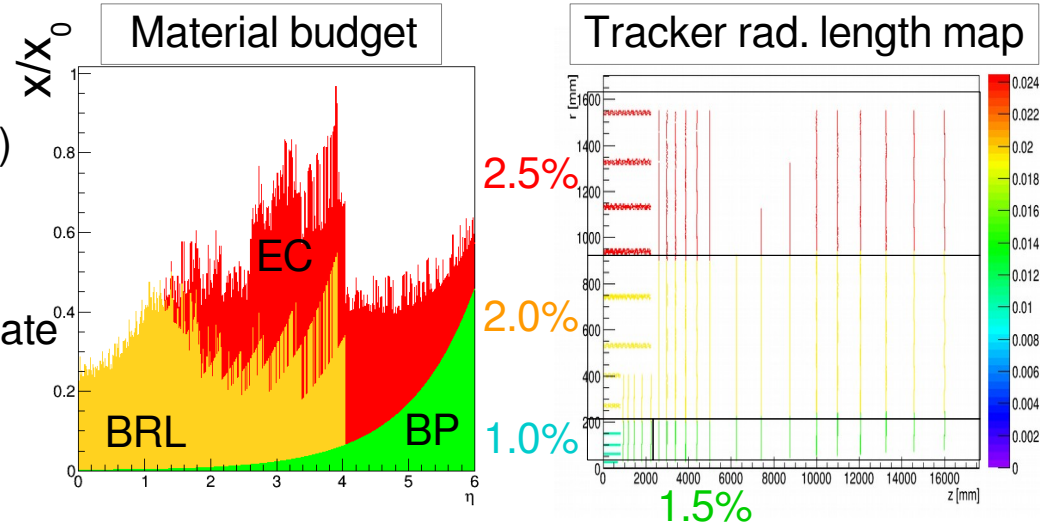
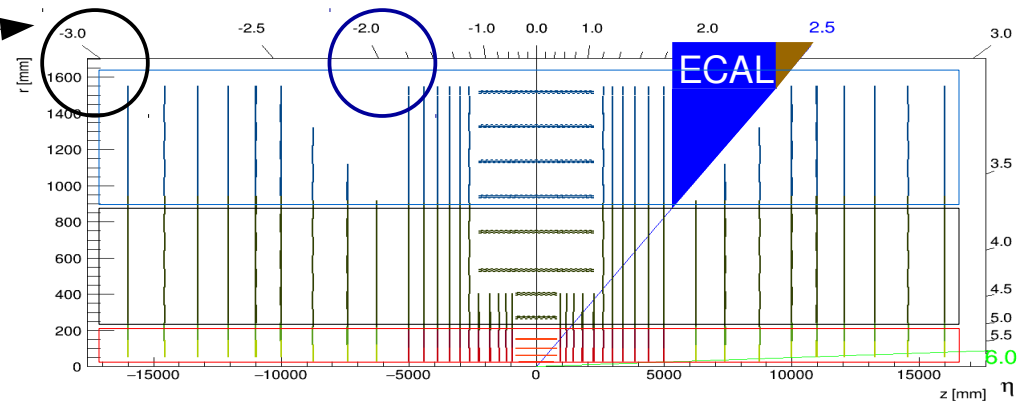
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(20% Si, 42% C, 2% Cu, 6% Al, 30% Plastic)
 - **technology input needed** for more real. estimate

- **Tracking resolution:**

p_T resolution versus η - const p_T across η



Start losing lever-arm



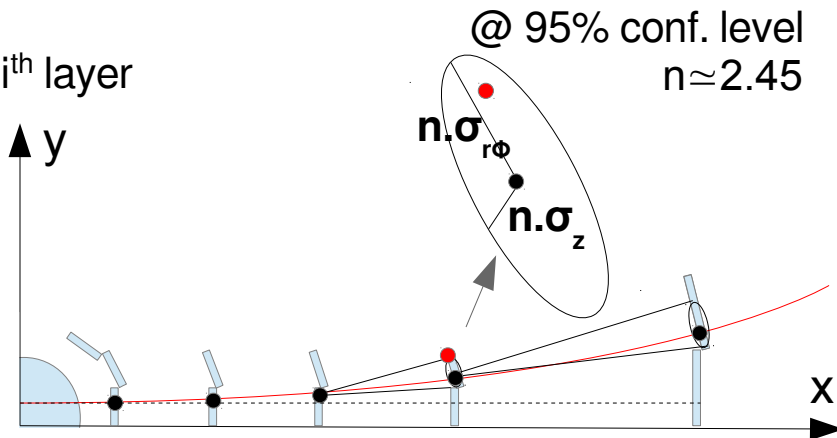
Pattern recognition (PR) Capabilities

- Granularity in Z strongly affects **pattern recognition capabilities**, so how to study PR analytically? Strategy: study “**weak**” spots in layout!

→ Assume **perfect seeding** (triplet) → propagate $\sigma_{r\phi}$, σ_z to i^{th} layer

→ Calculate probability **p** to mis-match a **real hit anywhere on the track** with a **bkg hit @95% CL in PU=1000**

$$p = 1 - \prod_{i=4}^N (1 - p_{\text{bkg95\%}}^i)$$



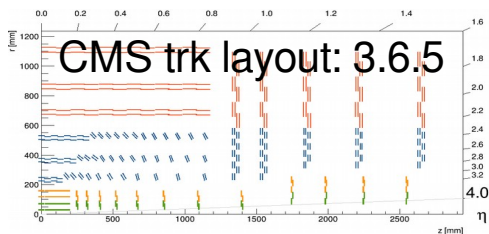
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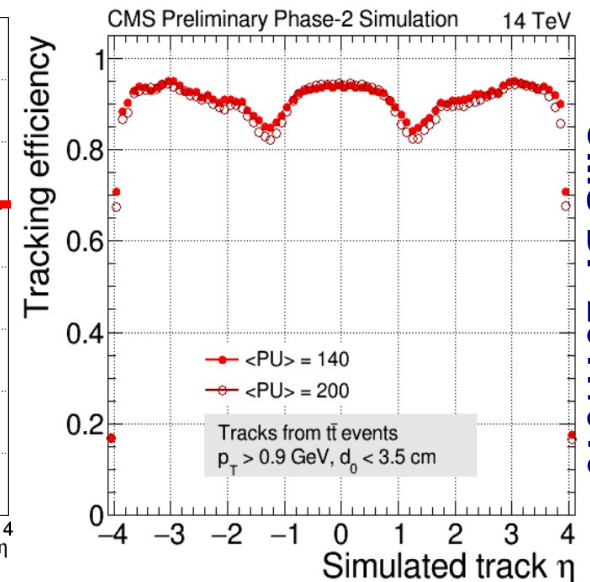
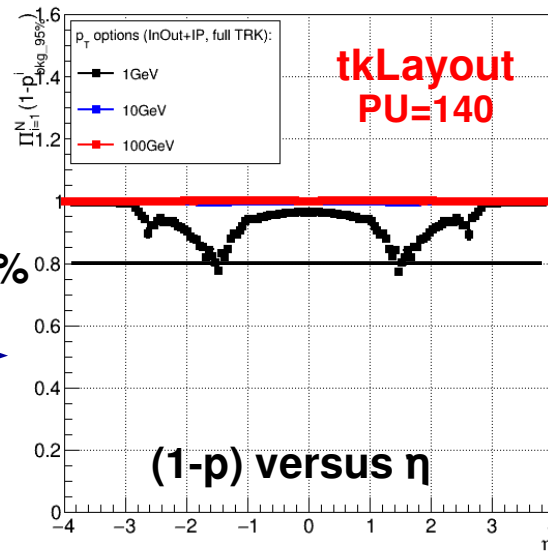
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$$p = 1 - \prod_{i=4}^N (1 - p_{\text{bkg}95\%}^i)$$

- How to “**qualitatively**” interpret **p**?
c.f. CMS Ph2 layout @PU~140...



(1-p) ~ 80%



E.Brondolin:
CMS DP-2017/010

- To keep **similar PR** for **FCCh @PU~1000**, set **bkg. prob. contamination p @20%**

Understanding Track Propagator in Pattern Recognition

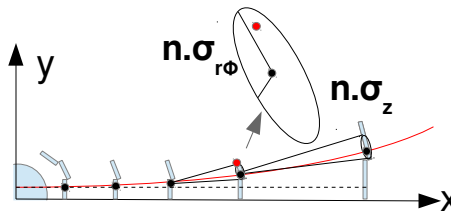
- 4 key parameters affecting propagation of error ellipse:

→ Multiple scattering & **material effect @ ϑ** (**tilt angle α**)

→ **Propagation distance**

→ **Projection factor** on det. plane

→ **Detector resolution**



$$\sigma_{MS}^2 \approx \langle \vartheta_{PT}^2 \rangle \frac{d/X_0}{\sin(\vartheta + \alpha)} \Delta r^2 f_{proj}$$

$$\langle \vartheta_{PT}^2 \rangle = \left(\frac{13.6 \text{ MeV}}{\beta p_{TC}} \right)^2 \left(1 + 0.038 \ln \frac{d/X_0}{\sin(\vartheta + \alpha)} \right)^2$$

$$f_{proj} = \left(\frac{1}{\sin(\vartheta + \alpha)} \right)^2 \text{proj. in Z}$$

$$f_{proj} = 1 \text{ proj. in R-}\Phi$$

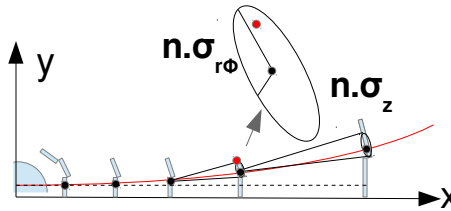
$$\sigma_{R\Phi} = \sqrt{\sigma_{R\Phi_{loc}}^2 + (A/\sqrt{1 - A^2 \sin^2 \alpha})^2 \sigma_{Z_{loc}}^2}$$

$$A = \Delta r / 2R$$

Understanding Track Propagator in Pattern Recognition

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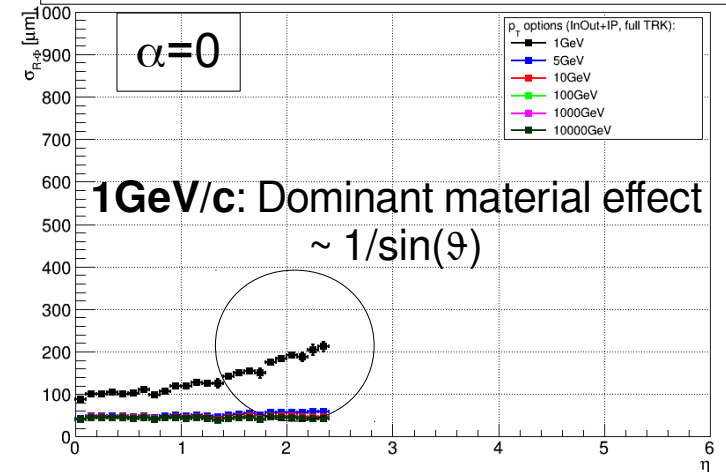
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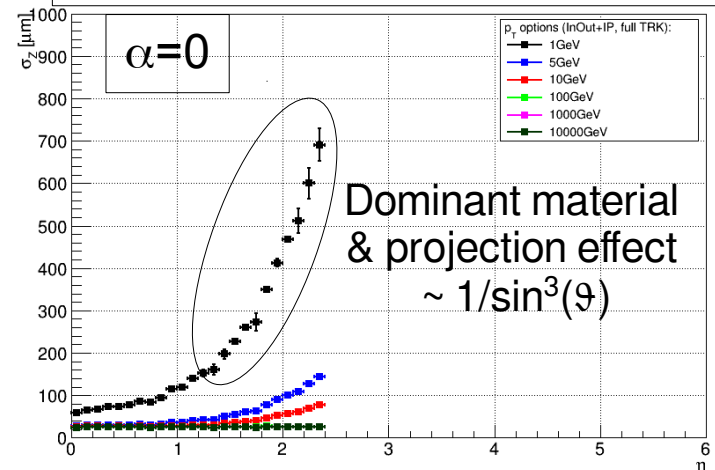
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$$A = \Delta r / 2R$$

Propagated $\sigma_{R-\Phi}$ on 4th BRL layer

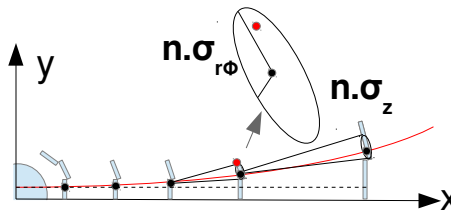


Propagated σ_z on 4th BRL layer



Understanding Track Propagator in Pattern Recognition

- 4 key parameters affecting propagation of error ellipse:
 - Multiple scattering & **material effect @ ϑ** (tilt angle α)
 - **Propagation distance**
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$$\sigma_{MS}^2 \approx \langle \vartheta_{PT}^2 \rangle \frac{d/X_0}{\sin(\vartheta + \alpha)} \Delta r^2 f_{proj}$$

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$$f_{proj} = \left(\frac{1}{\sin(\vartheta + \alpha)} \right)^2 \text{proj. in Z}$$

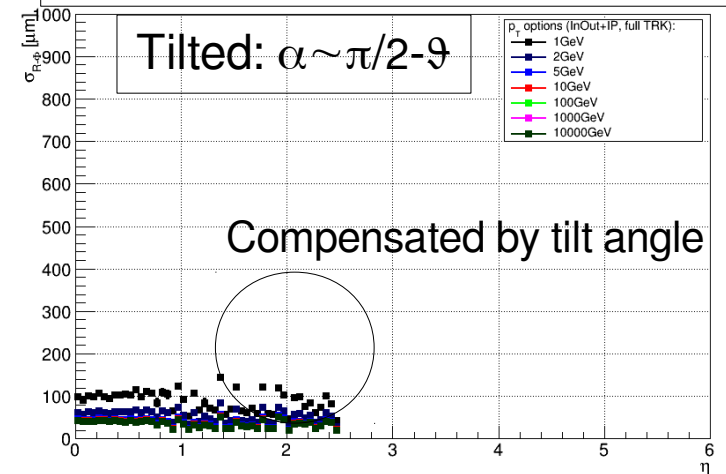
$$f_{proj} = 1 \text{ proj. in R-}\Phi$$

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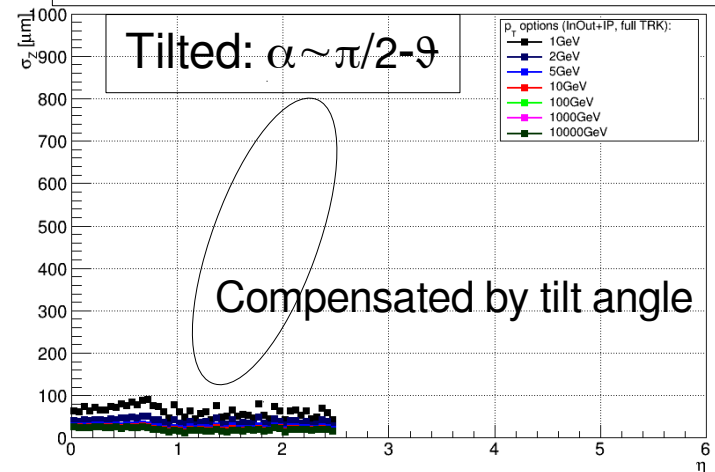
$$A = \Delta r / 2R$$

- To min. mat. effects, tracker in tilted layout advantageous!**

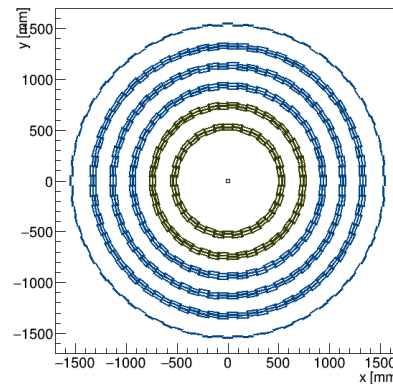
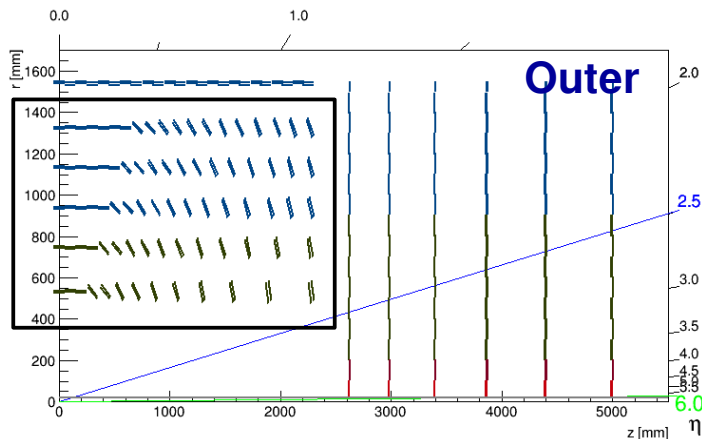
Propagated $\sigma_{R-\Phi}$ on 4th BRL layer



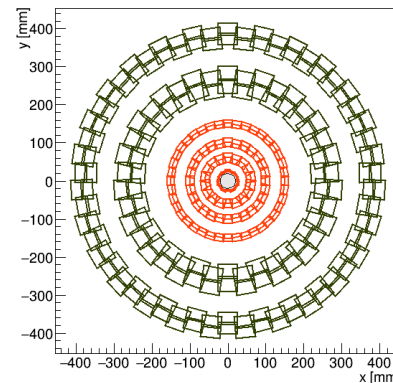
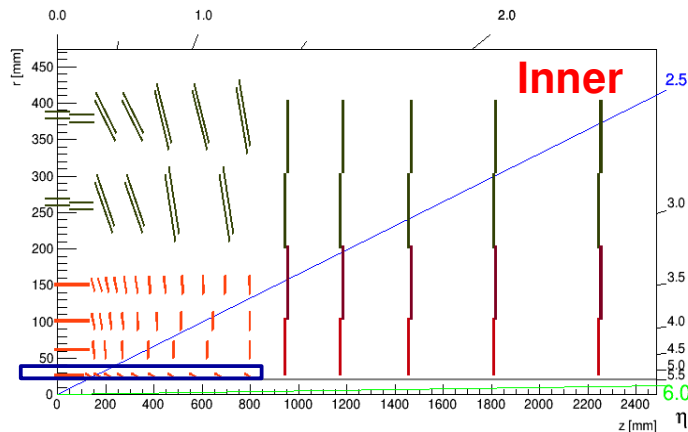
Propagated σ_z on 4th BRL layer



Tilted Geometry: Design Proposal v4.01



- Tilted layout of **outer tracker** driven by requirement to achieve **~0.2 bkg. contam. level** (BCL) in PR:
 - uppermost layer designed non-tilted to keep the highest possible lever-arm
 - modules positioned to hermetically cover full luminous region $\pm 75\text{mm}$
 - ECs strips res. in Z needed to be set to $\sim 500\mu\text{m}$ ($\sim 1\text{mm}$ OK)

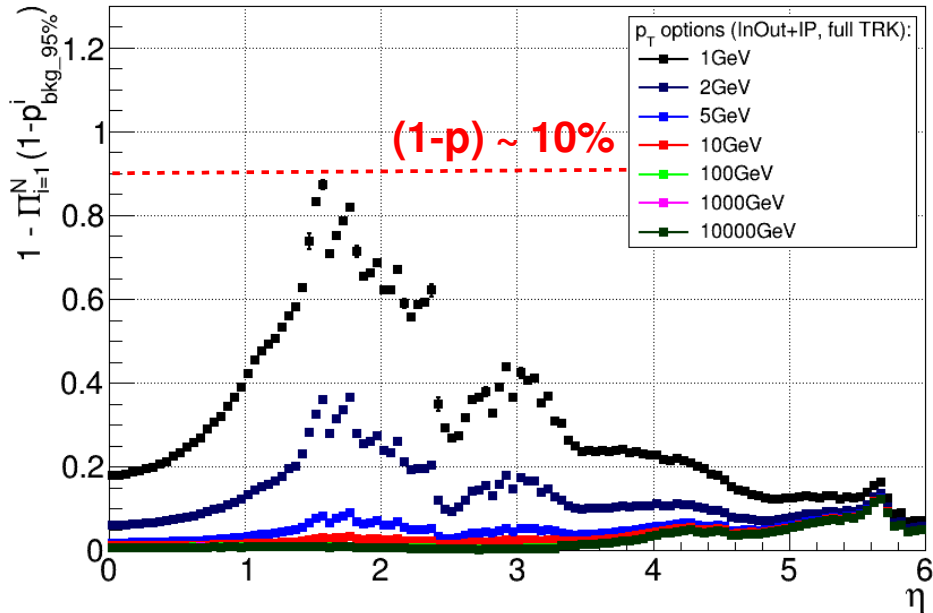


- Tilted layout of **inner tracker** driven by ~ 0.2 BCL in PR & **highest achievable z0 res.** (to deal with primary vertexing @PU ~ 1000):
 - tilt angle of 1st layer: $\theta_{\text{tilt}} \simeq 10^\circ$ optimized to achieve a compromise between low MB & higher radial position

Tilted Layout & Pattern Recognition

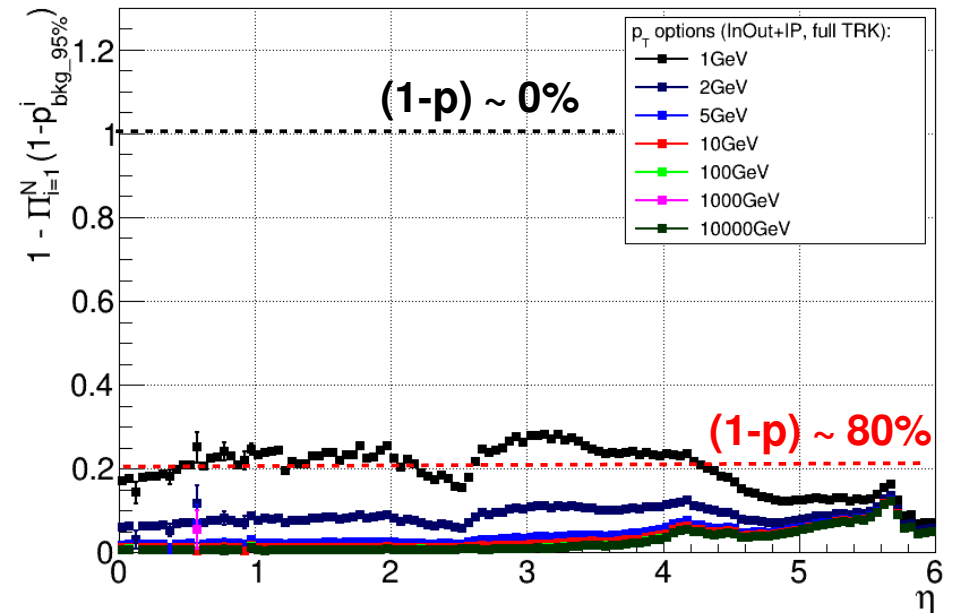
Non-tilted layout v3.03: in→out approach

In-Out: Bkg contam. prob. accumulated across N layers @95% CL



Tilted layout v4.01: in→out approach

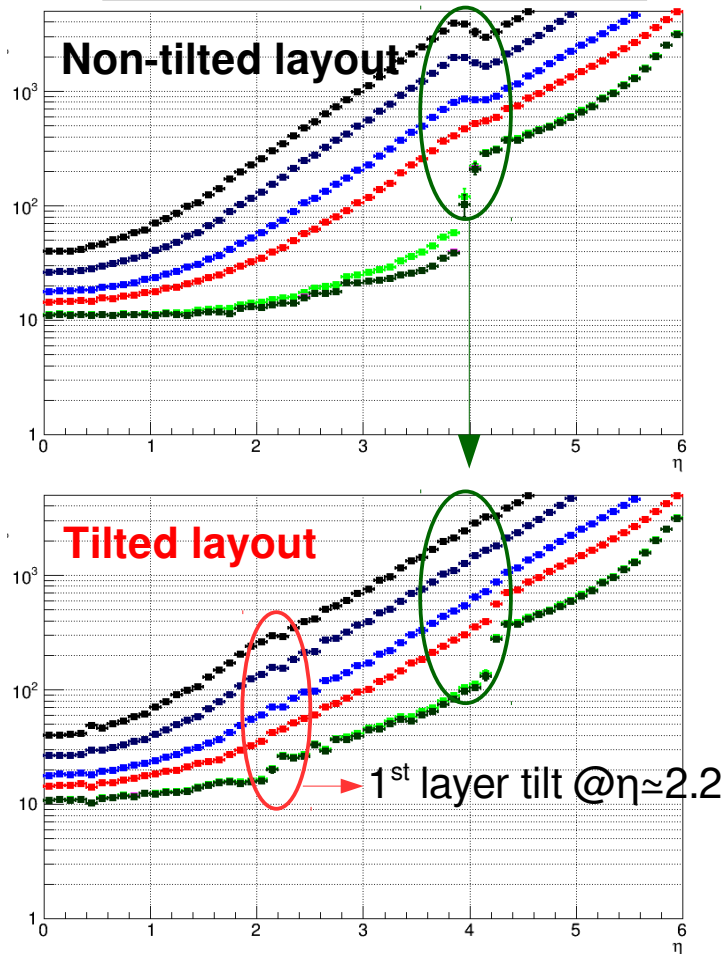
In-Out: Bkg contam. prob. accumulated across N layers @95% CL



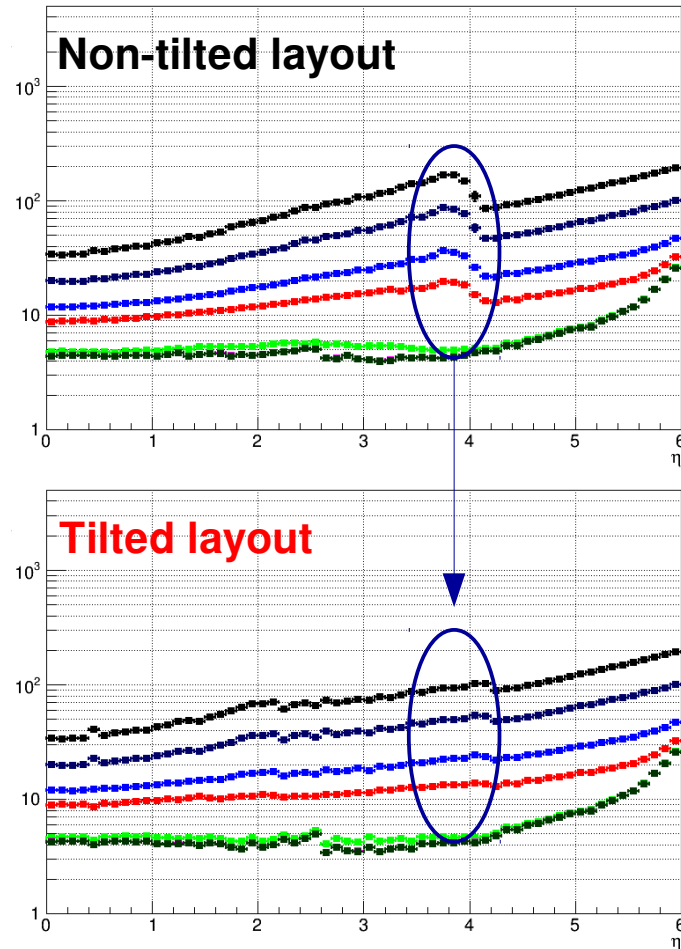
- **With tilted layout** the bkg. contam. level @~20% **achievable in PU~1000** for $p_T=1\text{ GeV}/c$ (limit value driven by HL-LHC scenario with PU~140 & CMS Phase 2 upgrade tracker layout)
- **Limits: Mat. budget assumed per module** → NOT fully realistic tilted design → need to consider realistic engineering with services, cooling & support structure (**technology input necessary**)!

Tilted Layout: Improvement in Tracking Performance

δz_0 [um] versus η



δd_0 [um] versus η

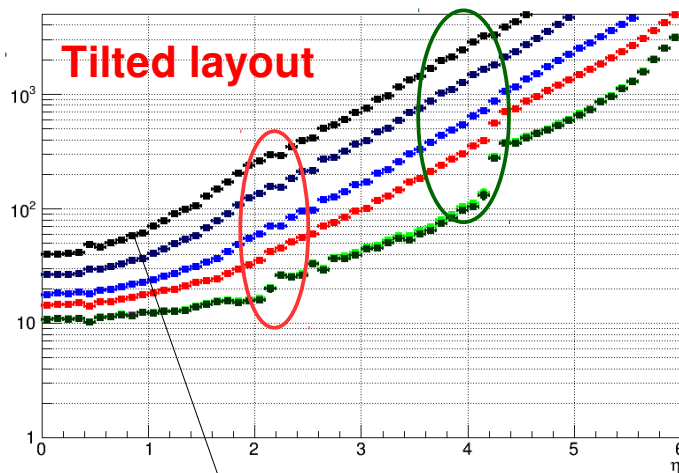
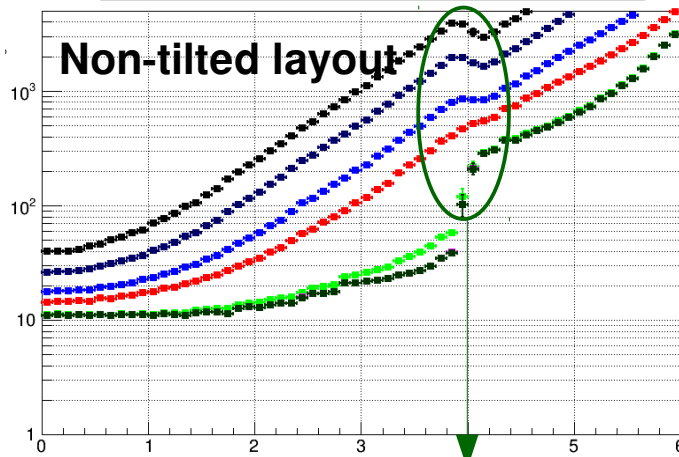


$p_T = 1$ GeV/c
 $p_T = 5$ GeV/c
 $p_T = 10$ GeV/c
 $p_T = 100$ GeV/c
 $p_T = 1$ TeV/c
 $p_T = 10$ TeV/c

Similar dp_T/p_T res. for both tilted & non-tilted

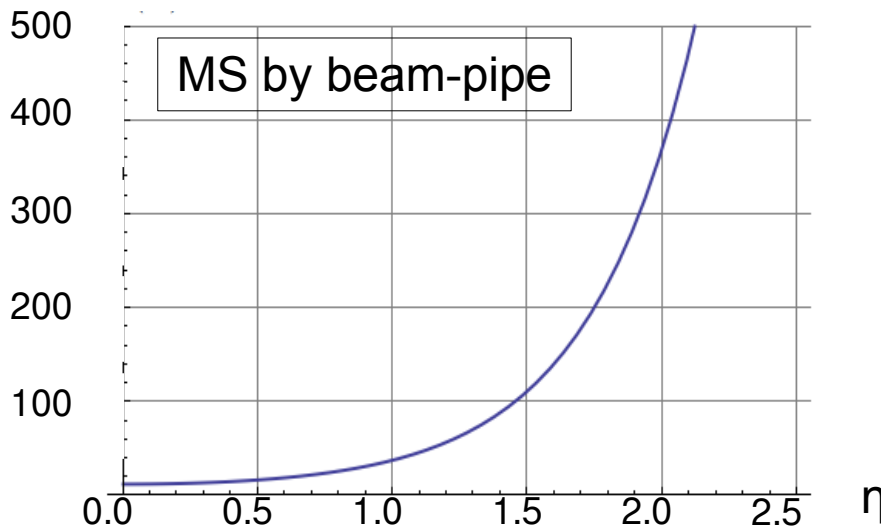
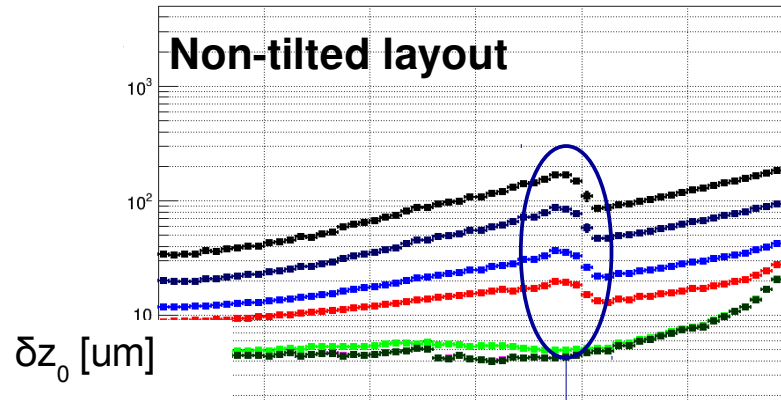
Tilted Layout: Improvement in Tracking Performance

δz_0 [um] versus η



→ For **tilted layout**, the dominant effect for 1 GeV/c curve shape is beam-pipe material!

δd_0 [um] versus η



- $p_T = 1$ GeV/c
- $p_T = 5$ GeV/c
- $p_T = 10$ GeV/c
- $p_T = 100$ GeV/c
- $p_T = 1$ TeV/c
- $p_T = 10$ TeV/c

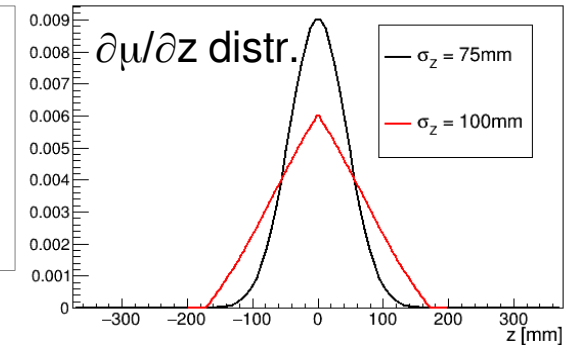
Similar dp_T/p_T res. for both tilted & non-tilted

Vertexing @ PU=1000 & Timing Information

- How the pile-up (PU)~1000 degrades primary vertexing? Does the timing info help?
 - Dependent on scenario for luminous region (Gauss, “rectangular”,...) → simulate **1000 PU** vertices according to Gaussian (HL-LHC) Line & Time PU densities (c.f.: [PhysRevSTAB.17.111001](#))

- Gauss. bunch:** $\frac{1}{\sqrt{2\pi}\sigma_z} e^{-\frac{1}{2}\left(\frac{z}{\sigma_z}\right)^2}$
 - **Line PU:** $\frac{\sqrt{1+\phi^2}}{\sqrt{\pi}\sigma_z} e^{-(1+\phi^2)\left(\frac{z}{\sigma_z}\right)^2}$
 - **Time PU:** $\frac{\sqrt{1+\psi^2}}{\sqrt{\pi}\sigma_z} e^{-(1+\psi^2)\left(\frac{ct}{\sigma_z}\right)^2}$

Line PU distr.: gaussian versus rectangular shaped bunches



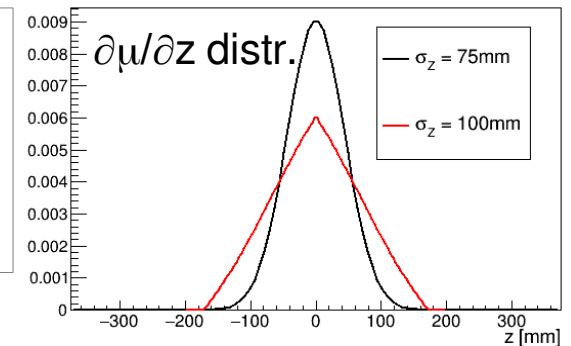
Piwinsky angle $\Phi \sim 0.67$
 Time Piw. angle $\Psi \sim 0.40$

Vertexing @ PU=1000 & Timing Information

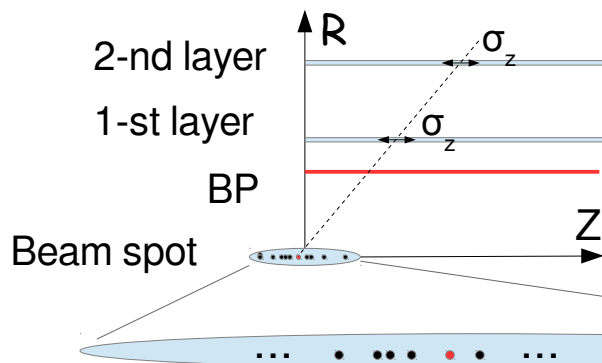
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Line PU distr.: gaussian versus rectangular shaped bunches



- Study what fraction of tracks may be unambiguously assigned to the primary vertex @ 95% CL? Use 2D info (PV assumed to be “precisely” found from e.g. high p_T tracks)



δz_0 & δt_0 play the crucial role!

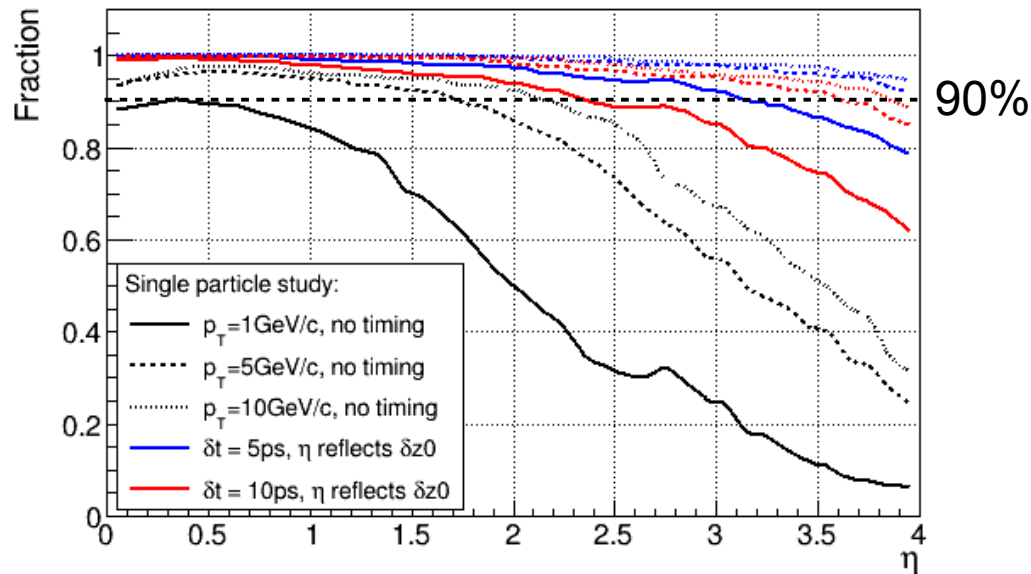
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Time Piw. angle $\Psi \sim 0.40$

Vertexing @ PU=1000 & Timing Information

→ Compare FCC-hh scenario to HL-LHC conditions (PU~140), using e.g. CMS Ph2 upgrade layout

HL-LHC scenario @ PU=140 CMS Ph2 Upgr. tracker

Fraction of tracks being unambiguously assigned to PV @95% CL: $\langle \mu_{\text{tot}} \rangle = 140$



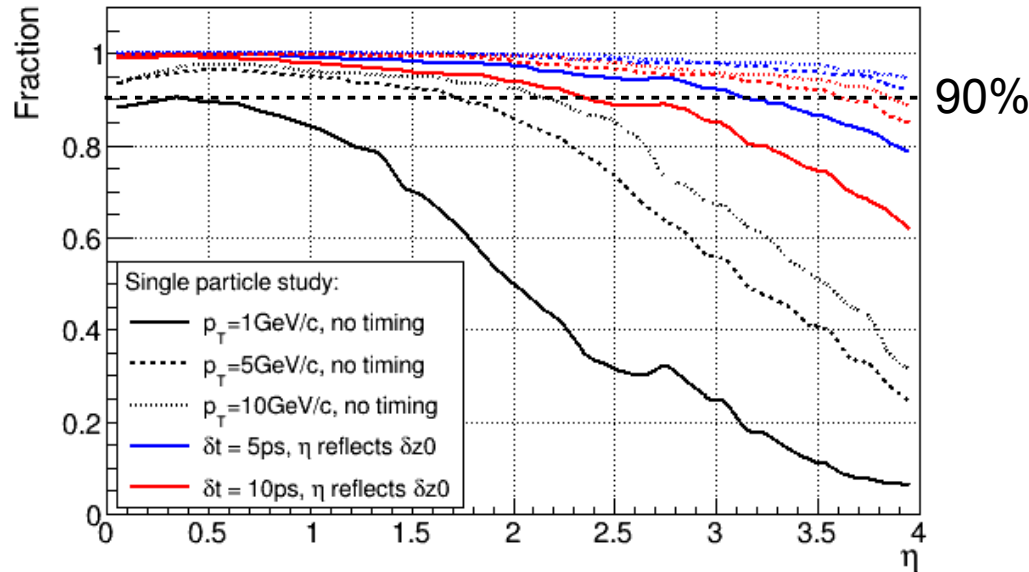
Vertexing @ PU=1000 & Timing Information

→ Compare FCC-hh scenario to HL-LHC conditions (PU~140), using e.g. CMS Ph2 upgrade layout

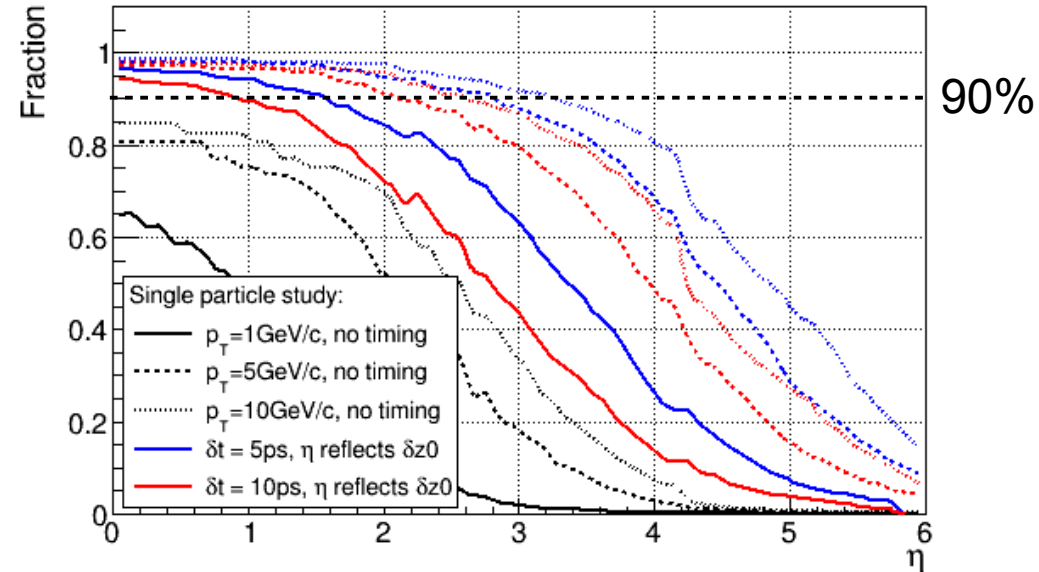
HL-LHC scenario @ PU=140
CMS Ph2 Upgr. tracker

FCC-hh scenario @ PU=1000
Tilted layout

Fraction of tracks being unambiguously assigned to PV @95% CL: $\langle \mu_{\text{tot}} \rangle = 140$



Fraction of tracks being unambiguously assigned to PV @95% CL: $\langle \mu_{\text{tot}} \rangle = 1000$



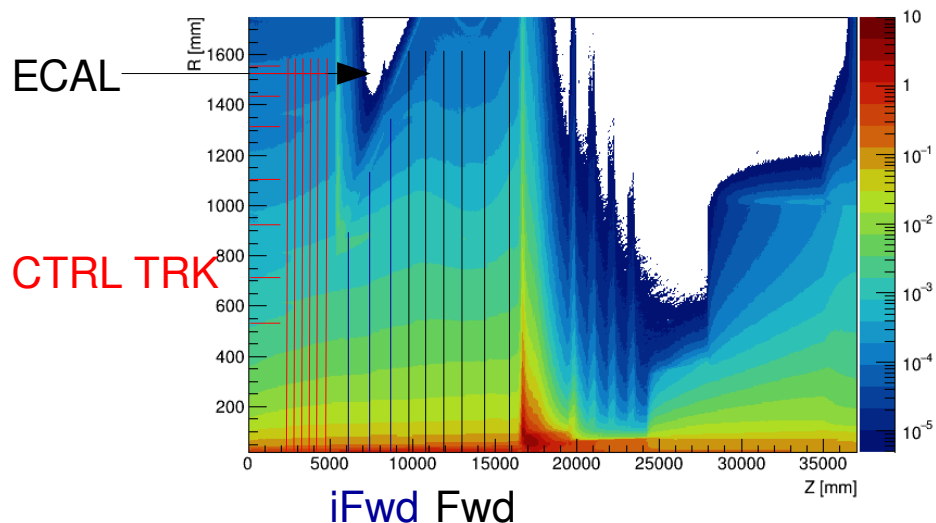
→ @PU~1000 avg. distance between vertices ($\Phi \sim 0.67$) ~110um @z=0m, hence the error due to mult. scattering in beam-pipe is for $\eta > 1.5$ already larger than the avg. vertex distance → **timing essential**

→ With current FCC-hh scheme & need for eta coverage up-to 6 **the primary vertexing @ PU~1000 seems very difficult for $\eta > 4.0$** , even **with timing res. ~5ps** (several time measur. per track)

Occupancy & Expected Data Rates @ PU=1000

- Have a look at the tracker granularity in a view of hit occupancy ($\sim <1\%$), what data rates may we expect at **PU~1000**?
 - Use **Fluka simulated charged particles fluence per pp collision** [cm^{-2}] scaled by 1000 PUs
 - Calculate occupancy & hit rates for 2 scenarios:
 - Non-triggered data @ $f = 40\text{MHz}$
 - Triggered data @ $f \sim 1\text{MHz}$ (given \sim by hardware limits, e.g. FPGA)
 - Assume binary read-out (spars. read-out scheme)

Charged particles fluence [cm^{-2}] per 1 pp collision



Inner: Occupancy & Expected Data Rates

Layer no :	1	2	3	4	5	6	Total [TB/s]
Radius [mm] :	25.0	60.0	100.0	150.0	270.0	400.0	
Module max occupancy (max[sen1,sen2])[%] :	0.45	0.11	0.05	0.02	0.08	0.04	
#Hit-channels per module per BX :	2694	741	333	166	314	150	
Module avg occupancy (max[sen1,sen2])[%] :	0.38	0.09	0.04	0.02	0.08	0.04	
Module bandwidth/(addr+clsWidth=2b[b] :	22	22	22	22	21	21	
Mod. bandwidth(#chnls*(addr+clsWidth)[kb] :	57.88	15.93	7.16	3.57	6.44	3.08	
Mod. bandwidth (matrix*1b/channel) [kb] :	685.00	820.00	820.00	820.00	384.00	384.00	
Data rate per layer - 40MHz,spars [Tb/s] :	603.7	379.9	277.3	202.2	138.7	97.5	212.4
Data rate per layer - 1MHz,spars [Tb/s] :	15.1	9.5	6.9	5.1	3.5	2.4	5.3
Data rate per ladder - 40Mhz,spars [Gb/s] :	44159.7	24313.2	10920.7	5449.3	4177.1	1996.5	
Data rate per ladder - 1Mhz,spars [Gb/s] :	1104.0	607.8	273.0	136.2	104.4	49.9	
Data rate per module - 40Mhz,spars [Gb/s] :	2207.99	607.83	273.02	136.23	245.71	117.44	
Data rate per module - 1Mhz,spars [Gb/s] :	55.20	15.20	6.83	3.41	6.14	2.94	
Data rate per cm ² - 40Mhz,spars [Gb/s/cm ²]:	251.82	57.91	26.01	12.98	4.69	2.24	
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:	6.30	1.45	0.65	0.32	0.12	0.06	

→ Hit occupancy [%] (~ <1%)

→ Layer data rate (40MHz)
→ Layer data rate (1MHz, trigger)

→ Data rate per cm² (40MHz)
→ Data rate per cm² (1MHz, trigger)

Challenge: 6.3 Gb/s/cm²

Ring no :	1	2	3	4	Total [TB/s]
Average radius [mm] :	64.8	153.0	251.1	353.3	
Module max occupancy (max[sen1,sen2])[%]:	0.46	0.13	0.18	0.08	
Data rate per ringLayer-40MHz,spars [Tb/s]:	194.2	148.2	105.1	74.3	65.2
Data rate per ringLayer- 1MHz,spars [Tb/s]:	4.9	3.7	2.6	1.9	1.6
Data rate per cm ² - 40Mhz,spars [Gb/s/cm ²]	64.44	15.67	6.62	3.42	
Data rate per cm ² - 1Mhz,spars [Gb/s/cm ²]:	1.61	0.39	0.17	0.09	

Challenge: 1.6 Gb/s/cm²

**Extreme data flows >>10Gb/s/module
(even triggered @ 1MHz)**

Outer & Fwd: Occupancy & Data Rates

→ Expected huge tracker data rates: 766 TB/s (untriggered), 19 TB/s (triggered @ 1MHz)

Layer no :	Outer:	1	2	3	4	5	6	Total [TB/s]										
Radius [mm] :		530.0	742.4	937.2	1132.0	1326.7	1539.5											
Module max occupancy (max[sen1,sen2])[%] :		0.02	0.01	0.75	0.43	0.27	0.21											
Data rate per layer - 40MHz,spars [Tb/s] :		226.0	134.5	63.6	43.9	31.7	28.1	66.0										
Data rate per layer - 1MHz,spars [Tb/s] :		5.6	3.4	1.6	1.1	0.8	0.7	1.6										
Data rate per cm ² - 40MHz,spars [Gb/s/cm ²]:		1.38	0.61	0.23	0.13	0.08	0.06											
Data rate per cm ² - 1MHz,spars [Gb/s/cm ²]:		0.03	0.02	0.01	0.00	0.00	0.00											
Ring no :		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total [TB/s]
Average radius [mm] :		64.6	151.5	251.0	352.0	451.6	553.6	651.1	753.6	850.8	953.5	1049.7	1152.6	1247.6	1350.8	1444.7	1522.8	
Module max occupancy (max[sen1,sen2])[%]:		0.58	0.15	0.21	0.10	0.06	0.04	0.02	0.02	0.01	0.23	0.20	0.13	0.12	0.08	0.08	0.05	
Data rate per ringLayer-40MHz,spars [Tb/s]:		263.8	213.3	153.4	109.8	93.2	63.1	63.8	49.9	42.5	28.5	21.9	19.2	15.7	13.8	11.4	4.6	146.0
Data rate per ringLayer- 1MHz,spars [Tb/s]:		6.6	5.3	3.8	2.7	2.3	1.6	1.6	1.2	1.1	0.7	0.5	0.5	0.4	0.3	0.3	0.1	3.6
Data rate per cm ² - 40MHz,spars [Gb/s/cm ²]:		71.30	18.72	7.98	4.18	2.65	1.54	1.18	0.78	0.62	0.36	0.26	0.21	0.15	0.13	0.10	0.08	
Data rate per cm ² - 1MHz,spars [Gb/s/cm ²]:		1.78	0.47	0.20	0.10	0.07	0.04	0.03	0.02	0.02	0.01	0.01	0.01	0.00	0.00	0.00	0.00	
Ring no :	iFWD:	1	2	3	4	5	6	7	8	9	10	11	12	13	Total [TB/s]			
Average radius [mm] :		72.8	167.5	266.5	366.3	464.9	564.8	664.6	766.8	866.7	969.0	1068.4	1170.9	1269.8				
Module max occupancy (max[sen1,sen2])[%]:		0.99	0.13	0.20	0.11	0.07	0.04	0.03	0.02	0.02	0.48	0.24	0.12	0.07				
Data rate per ringLayer-40MHz,spars [Tb/s]:		165.8	114.5	81.6	64.9	50.6	39.3	42.3	30.0	43.3	16.8	7.8	2.8	1.9	82.7			
Data rate per ringLayer- 1MHz,spars [Tb/s]:		4.1	2.9	2.0	1.6	1.3	1.0	1.1	0.8	1.1	0.4	0.2	0.1	0.0	2.1			
Data rate per cm ² - 40MHz,spars [Gb/s/cm ²]:		65.73	18.17	8.18	4.75	2.92	1.87	1.44	0.94	1.18	0.64	0.27	0.18	0.11				
Data rate per cm ² - 1MHz,spars [Gb/s/cm ²]:		1.64	0.45	0.20	0.12	0.07	0.05	0.04	0.02	0.03	0.02	0.01	0.00	0.00				
Ring no :	FWD:	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Total [TB/s]	
Average radius [mm] :		97.1	190.1	288.9	388.3	487.1	588.6	689.4	791.4	891.9	994.1	1094.4	1196.6	1296.6	1398.8	1498.5		
Module max occupancy (max[sen1,sen2])[%]:		0.28	0.11	0.20	0.12	0.08	0.05	0.04	0.03	0.02	0.46	0.34	0.25	0.16	0.11	0.09		
Data rate per ringLayer-40MHz,spars [Tb/s]:		318.3	244.3	180.2	149.6	121.5	116.4	101.0	77.1	76.7	54.9	35.5	25.6	19.5	15.2	11.0	193.4	
Data rate per ringLayer- 1MHz,spars [Tb/s]:		8.0	6.1	4.5	3.7	3.0	2.9	2.5	1.9	1.9	1.4	0.9	0.6	0.5	0.4	0.3	4.8	
Data rate per cm ² - 40MHz,spars [Gb/s/cm ²]:		48.67	17.20	8.37	5.17	3.35	2.37	1.71	1.21	1.04	0.66	0.40	0.26	0.19	0.13	0.09		
Data rate per cm ² - 1MHz,spars [Gb/s/cm ²]:		1.22	0.43	0.21	0.13	0.08	0.06	0.04	0.03	0.03	0.02	0.01	0.01	0.00	0.00	0.00		

Summary & Challenges

- **The key tracker parameters have been studied & optimized:**
 - **Current layout:** $\sim 430\text{m}^2$ (391m^2 in tilted layout) of Si with #channels: 5461M (pixels), 9964M (macro-pixels), 489M (strips)
 - The **granularity in $R-\Phi$** driven mostly by dp_T/p_T @ $p_T=10\text{TeV}/c$ → achieved $dp_T/p_T \sim 20\%$
 - The **granularity in Z driven by prim. vertexing & pattern recognition capabilities @PU=1000:**
 - Due to minimized material budget **tracker in tilted layout very advantageous** (even for the vertex detector) to achieve similar pattern recognition performance as with PU ~ 140 & HL-LHC conditions
 - **realistic engineering (technology input)** with services, cooling & support structure important!
 - **Primary vertexing & correct PV assignment @PU=1000 seems feasible up-to $\eta\sim 4$** , but only with **precise timing information $\sigma_t\sim 10\text{ns}$** (2D vertexing) → the limiting factor for **high η coverage is beam-pipe material**
 - Expected data rates (**766 TB/s untriggered, 19 TB/s triggered @1MHz**) implicate need for new read-out technologies (high speed, low power optical links) & dedicated trigger design!
 - Expected **1MeV neq fluence $\sim 5\times 10^{17}\text{cm}^{-2}$ & TID $\sim 0.4\text{GGy}$ @ $R=25\text{mm}$** (up to $R\sim 270\text{mm}$) represent **new challenges** for the tracker (vertex detector) technologies

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 - **Dedicated R&D is a key to success!**