

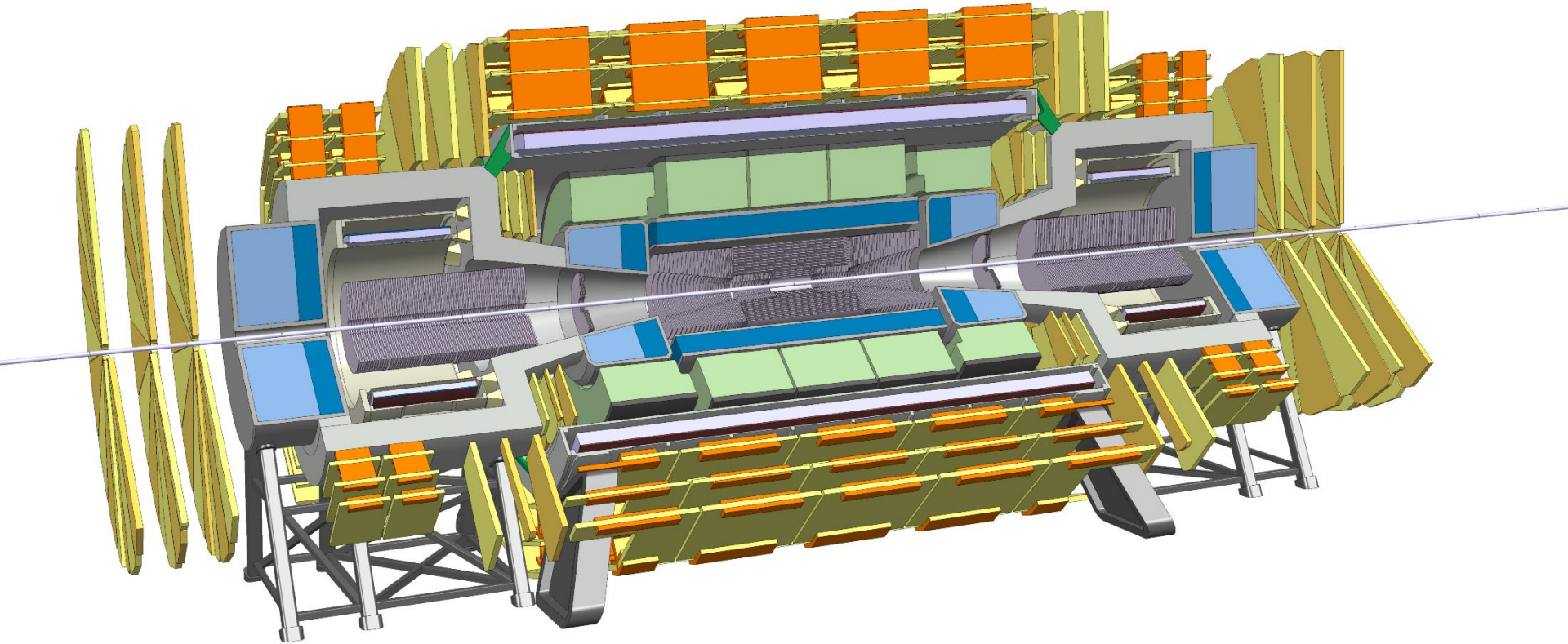
# Muon System

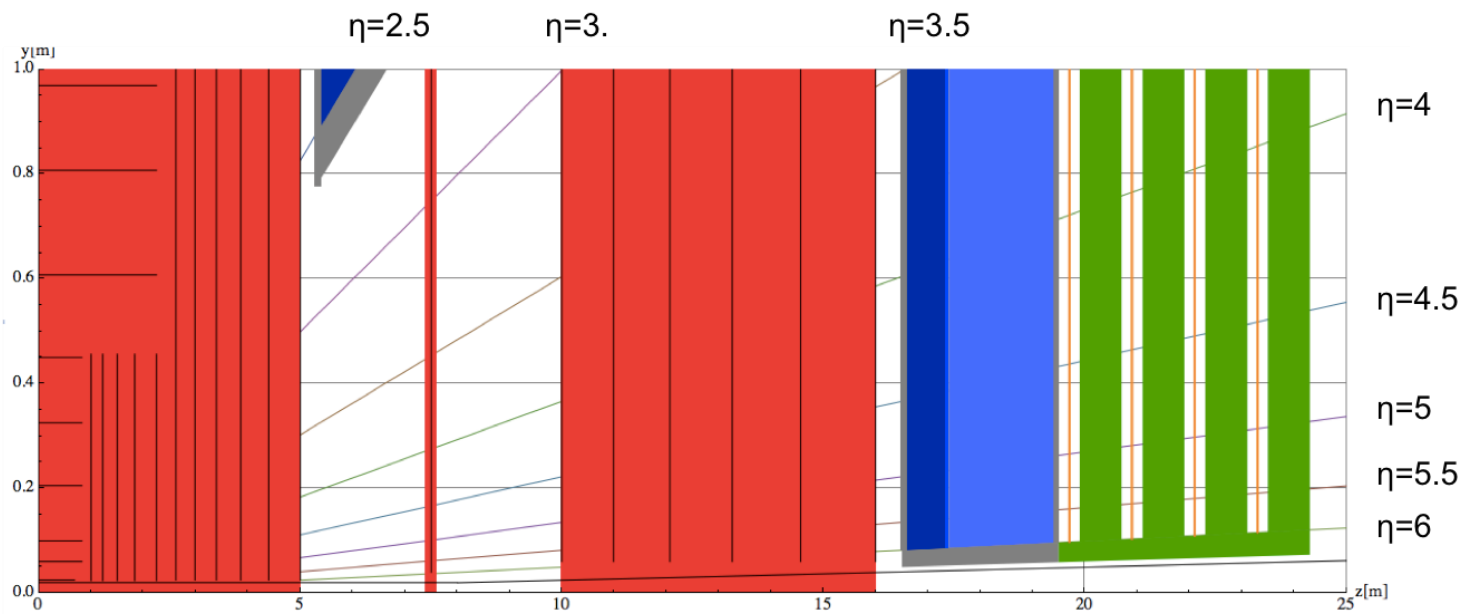
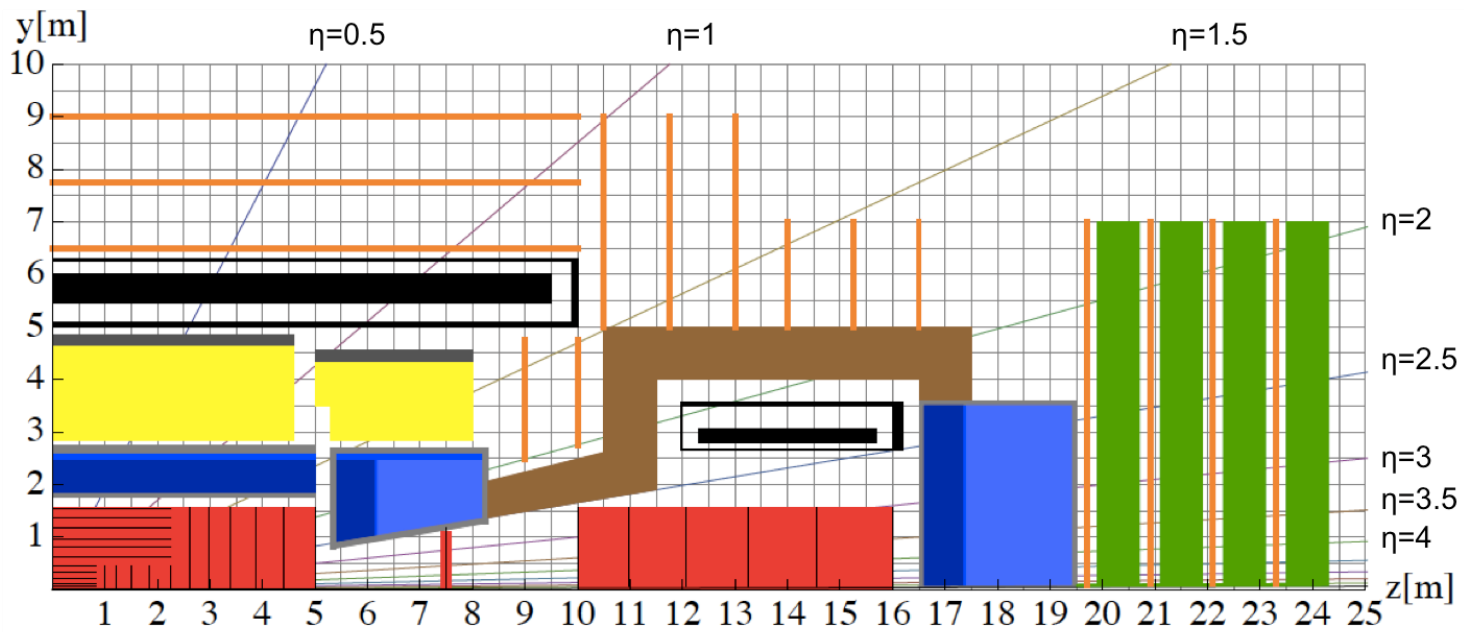
FCC week Berlin, May 29<sup>th</sup> – June 2<sup>nd</sup> 2017

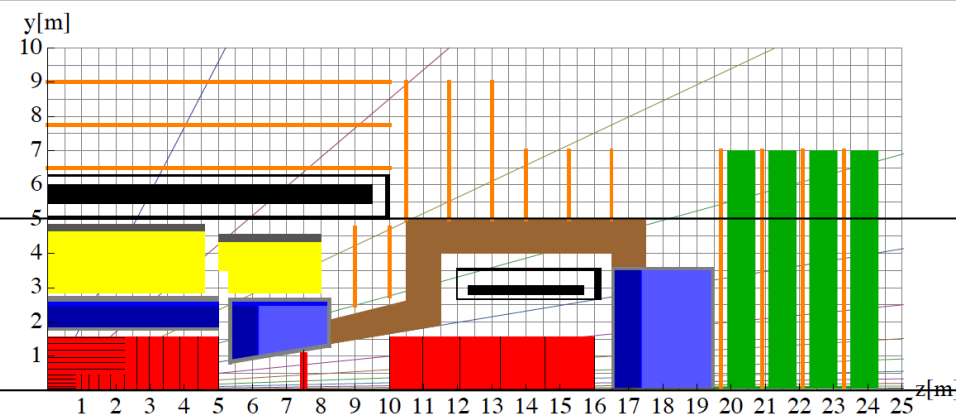
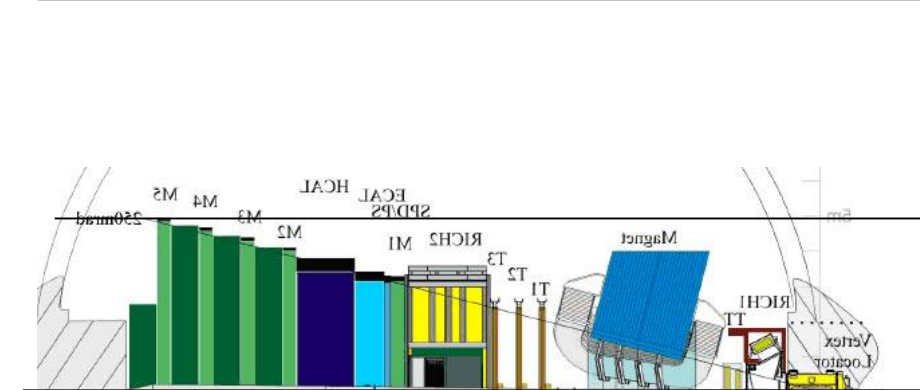
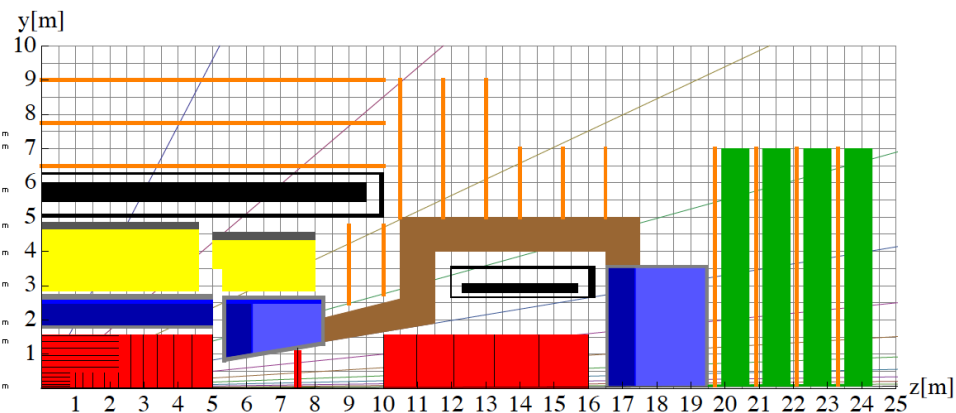
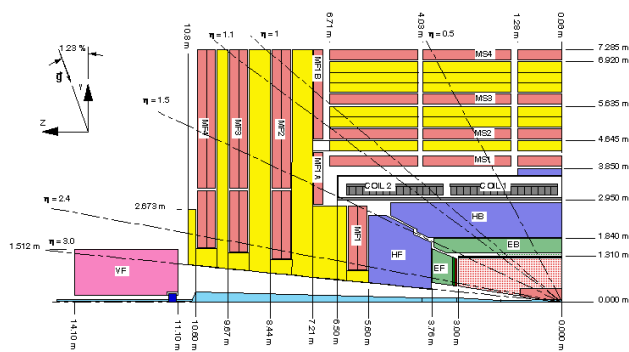
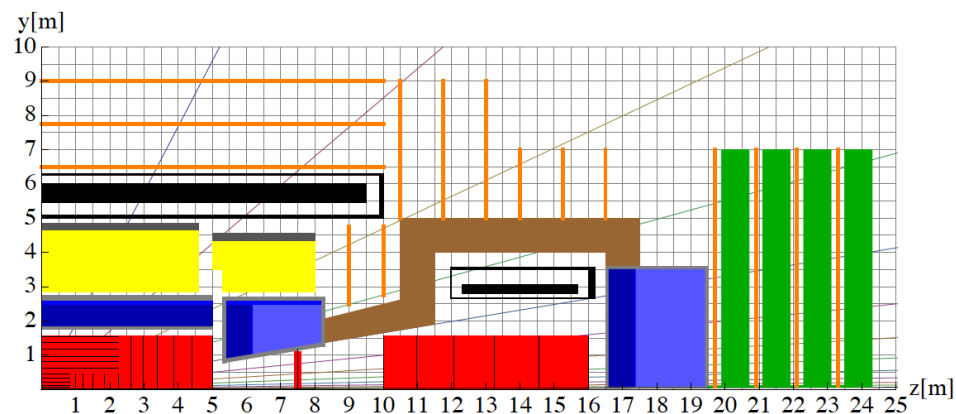
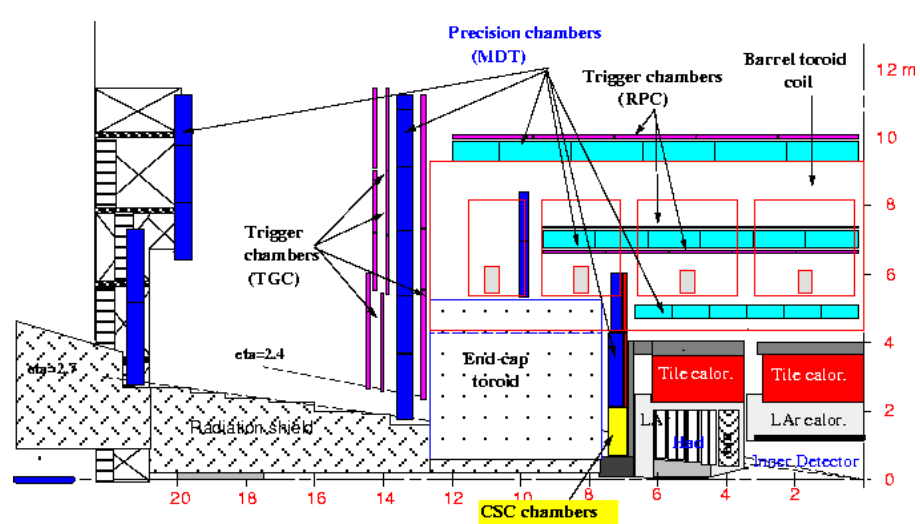
W. Riegler, CERN

Only slide collection for now !

# DETECTOR OVERVIEW

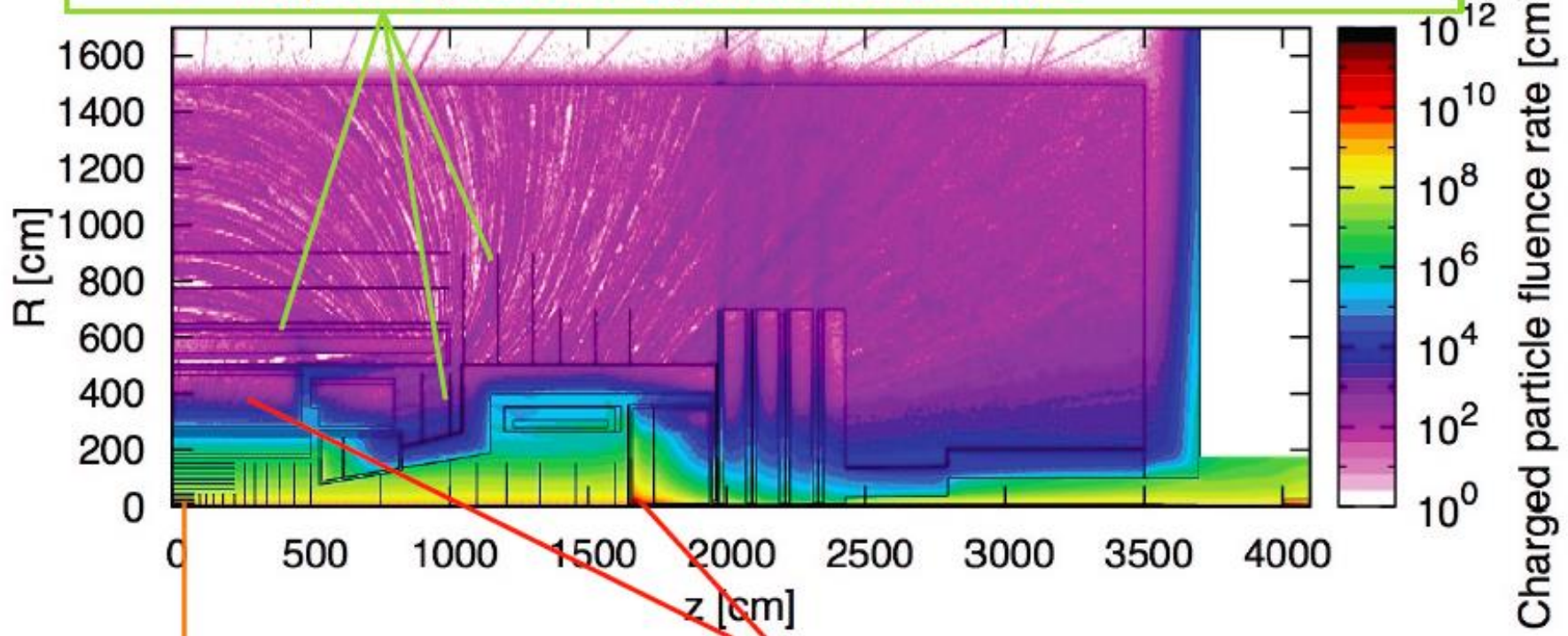






Fluence rates in the muon chambers:

- barrel:  $\sim 300 \text{ cm}^{-2}\text{s}^{-1}$
- end-cap chambers for  $z > 10 \text{ m}$ :  $\sim 500 \text{ cm}^{-2}\text{s}^{-1}$ , but for the two chambers at  $z < 10 \text{ m}$ :  $10^4 \text{ cm}^{-2}\text{s}^{-1}$
- max previous layout:  $< 100 \text{ cm}^{-2}\text{s}^{-1}$ , but with an hermetic detector



Compare to ATLAS Muon system with a maximum of  
 $\text{XXXHz/cm}^2$  for the drift tubes of the muon system @ HL-LHC  $7 \times 10^{34}$   
 $\text{XXXHz/cm}^2$  for the TGCs/MICROMEGAS of the muon system at HL-LHC  $7 \times 10^{34}$   
 $\text{XXXHz/cm}^2$  for the RPCs of the ATLAS muons system at HL-LHC  $7 \times 10^{34}$   
 $\text{XXXHz/cm}^2$  for the wire chambers of the LHCb muon system @  $2 \times 10^{33}$   
 $\text{XXXHz/cm}^2$  for the GEMs of the LHCb muon system @  $4 \times 10^{32}$

→ The HL-LHC muon system technology will be well adapted to a FCC muon system in terms of rate capability.

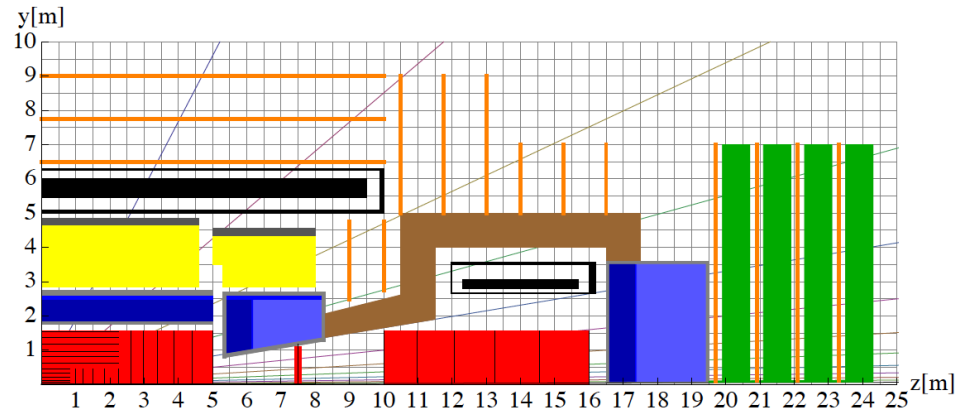
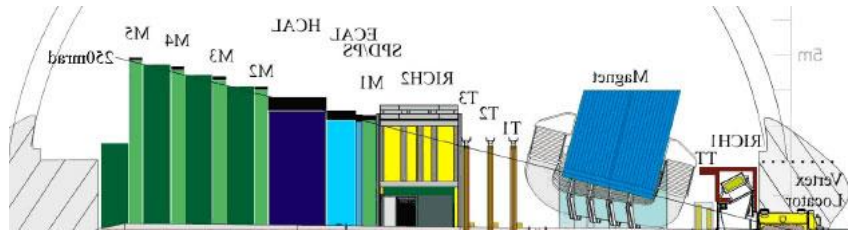
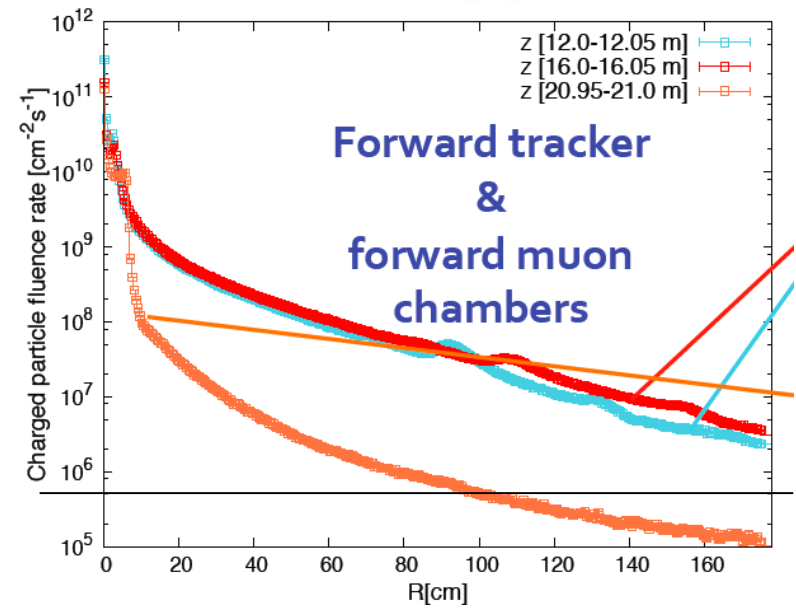


Table 4.5: Expected rates on the muon detector when operating at an instantaneous luminosity of  $2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$  at a collision energy of 14 TeV. The values are averages, in kHz/cm<sup>2</sup>, over the chamber with the minimum illumination, the whole region and the chamber with maximum illumination. The values are extrapolated from measured rates at 8 TeV.

Region	Minimum	Average	Maximum
M2R1	162 ± 28	327 ± 60	590 ± 110
M2R2	15.0 ± 2.6	52 ± 8	97 ± 15
M2R3	0.90 ± 0.17	5.4 ± 0.9	13.4 ± 2.0
M2R4	0.12 ± 0.02	0.63 ± 0.10	2.6 ± 0.4
M3R1	39 ± 6	123 ± 18	216 ± 32
M3R2	3.3 ± 0.5	11.9 ± 1.7	29 ± 4
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M3R4	0.017 ± 0.002	0.12 ± 0.02	0.63 ± 0.09
M4R1	17.5 ± 2.5	52 ± 8	86 ± 13
M4R2	1.58 ± 0.23	5.5 ± 0.8	12.6 ± 1.8
M4R3	0.096 ± 0.014	0.54 ± 0.08	1.37 ± 0.20
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M5R1	19.7 ± 2.9	54 ± 8	91 ± 13
M5R2	1.58 ± 0.23	4.8 ± 0.7	10.8 ± 1.6
M5R3	0.29 ± 0.04	0.79 ± 0.11	1.69 ± 0.25
M5R4	0.23 ± 0.03	2.1 ± 0.3	9.0 ± 1.3



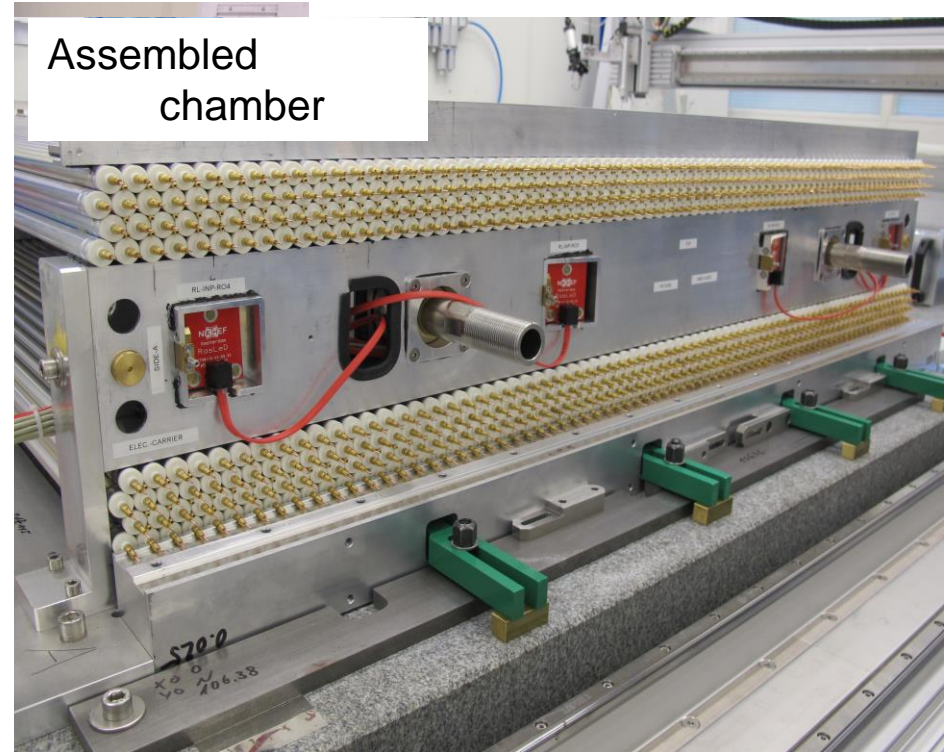
For  $r > 1\text{m}$  the rates are similar to the ones of the upgraded LHCb muon system.

# sMDT Chamber Construction for ATLAS Upgrades

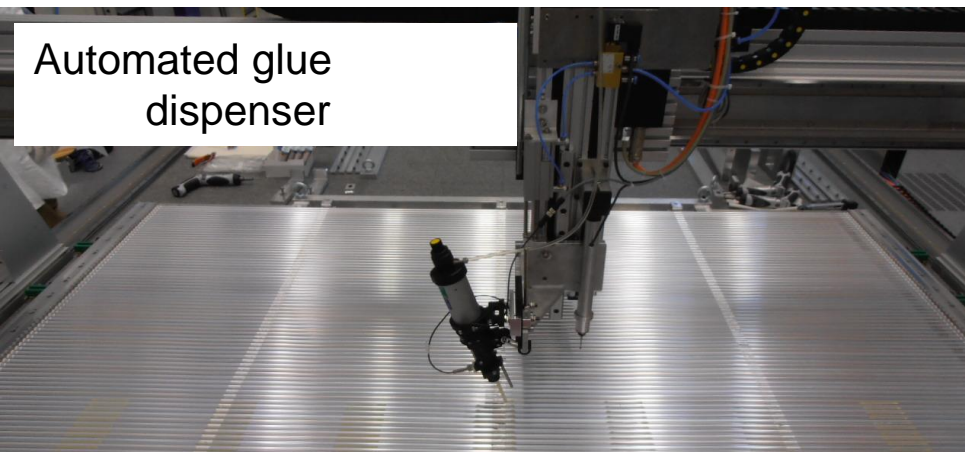
Drift tube stacking



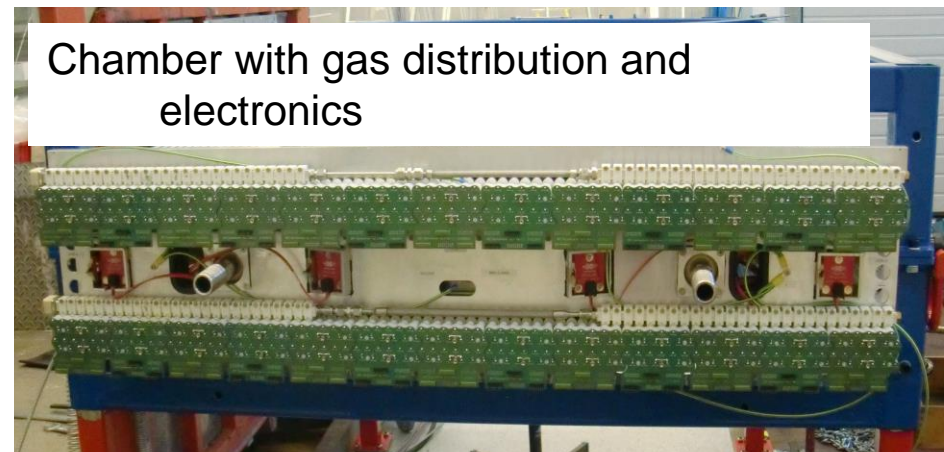
Assembled chamber



Automated glue dispenser

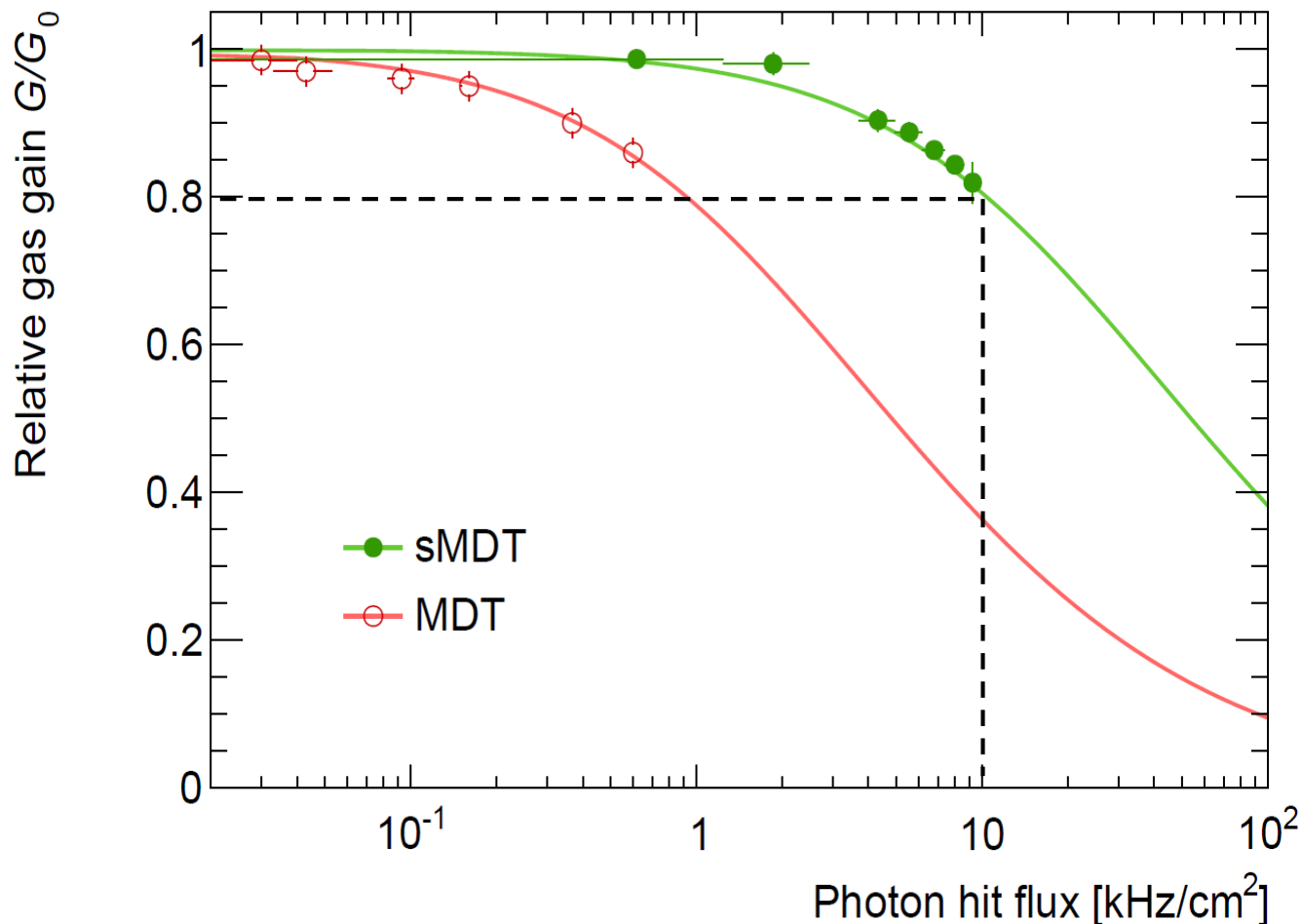


Chamber with gas distribution and electronics



# Space Charge Effects

sMDT tubes show only 20% gain loss at 10 kHz/cm<sup>2</sup>  $\gamma$  hit rate



Measurements at the CERN Gamma Irradiation Facility GIF, compared to simulation of drift tube and electronics response. Current MDT RO electronics has 220 ns minimum deadtime and no BLR.

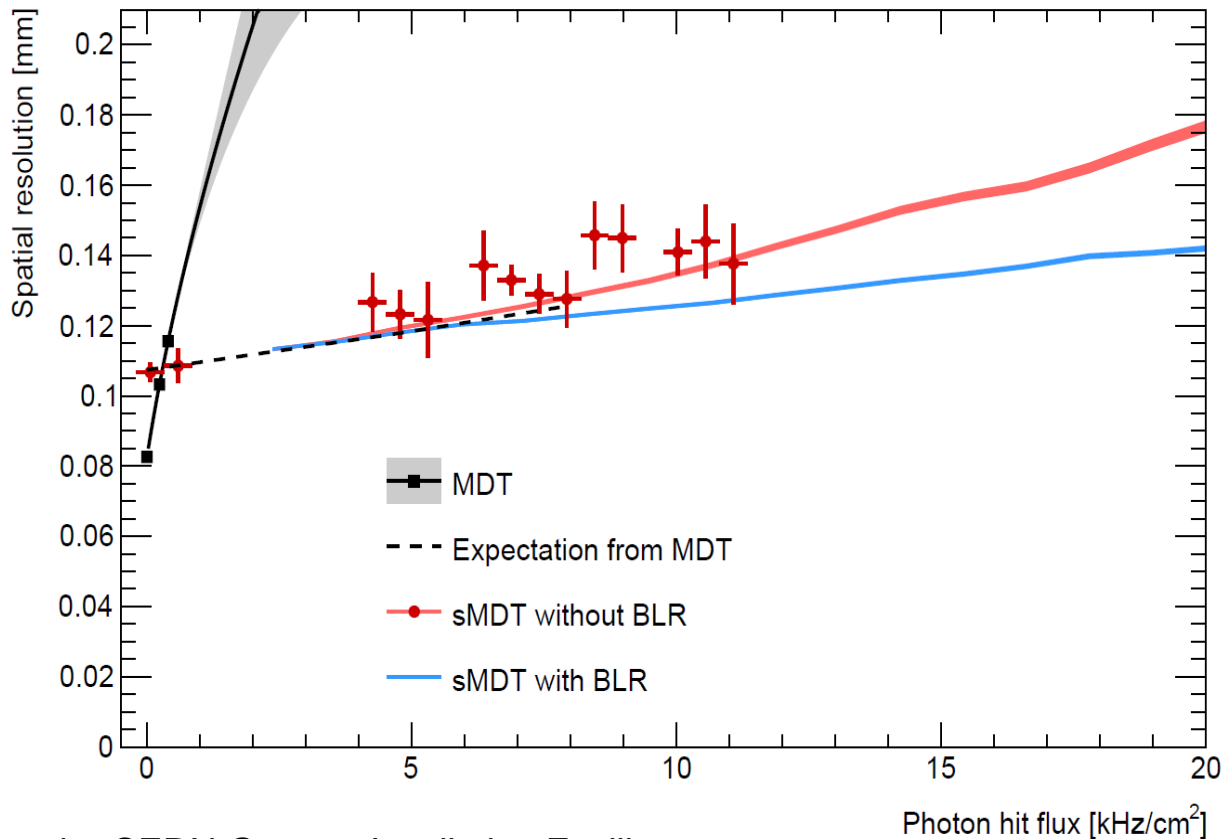
B. Bittner et al., Nucl.Instr.& Meth. A732 (2013) 250  
Ph. Schwegler et al., Proc. IEEE NSS 2014



# sMDT Single-Tube Resolution

sMDT resolution limited at high counting rates by signal pile-up effects of the electronics, in contrast to MDTs where space charge effects dominate

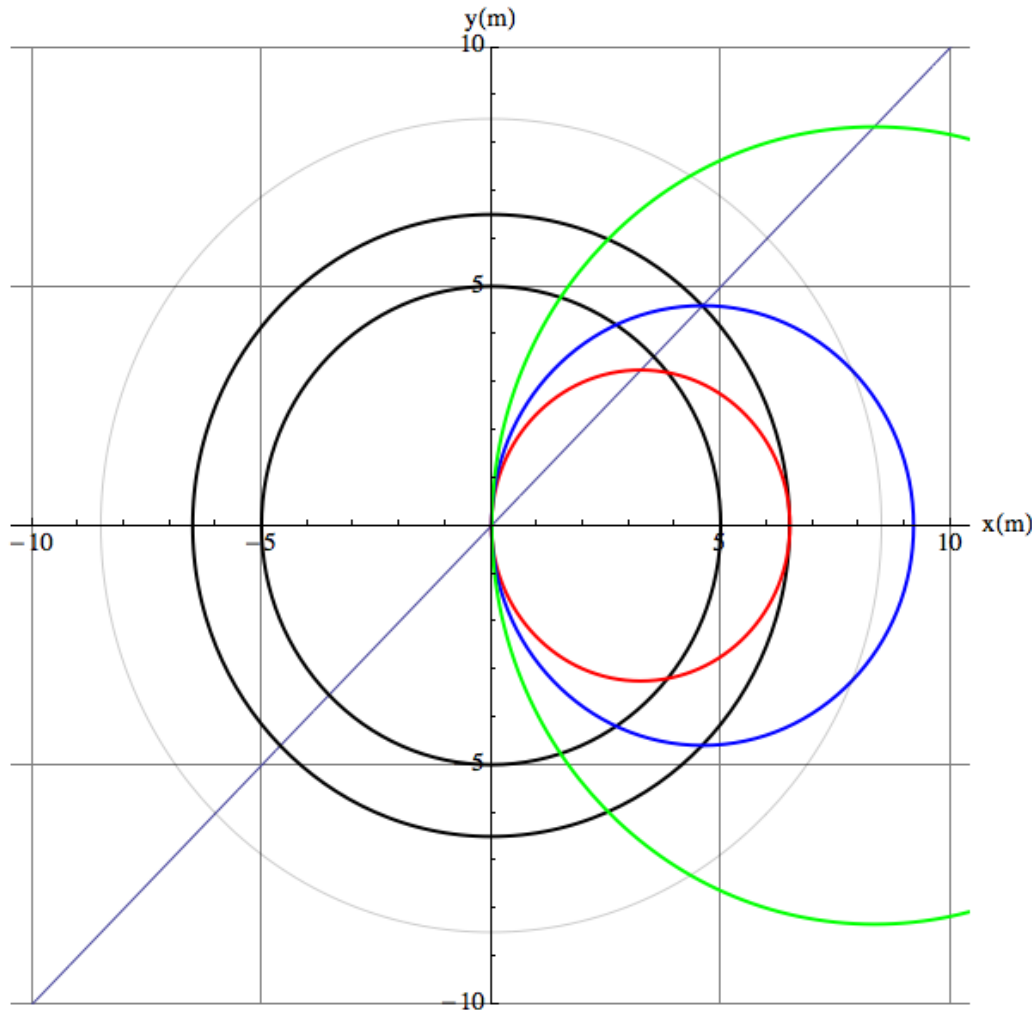
- suppression of signal pile-up effects with fast baseline restoration (BLR)



Measurements at the CERN Gamma Irradiation Facility, compared to simulation of drift tube and electronics response. Current MDT RO electronics has 220 ns minimum deadtime and no BLR.

B. Bittner et al., Nucl.Instr.& Meth. A732 (2013) 250  
Ph. Schwegler et al., Proc. IEEE NSS 2014

# Muon Pt cutoff and minimum trigger threshold in the main solenoid



```
In[3]:= (* ===== *)
```

```
In[4]:= Rmuon1 = 6.5;
```

```
In[5]:= Rcoil1 = 5.;
```

```
In[6]:= B0 = 4;
```

```
In[7]:= pmin1 = p[Rmuon1 / 2, B0]
```

```
Out[7]= 3.9
```

```
In[8]:= p45x1 = p[Rmuon1 / Sqrt[2], B0]
```

```
Out[8]= 5.51543
```

```
In[9]:= (* ===== *)
```

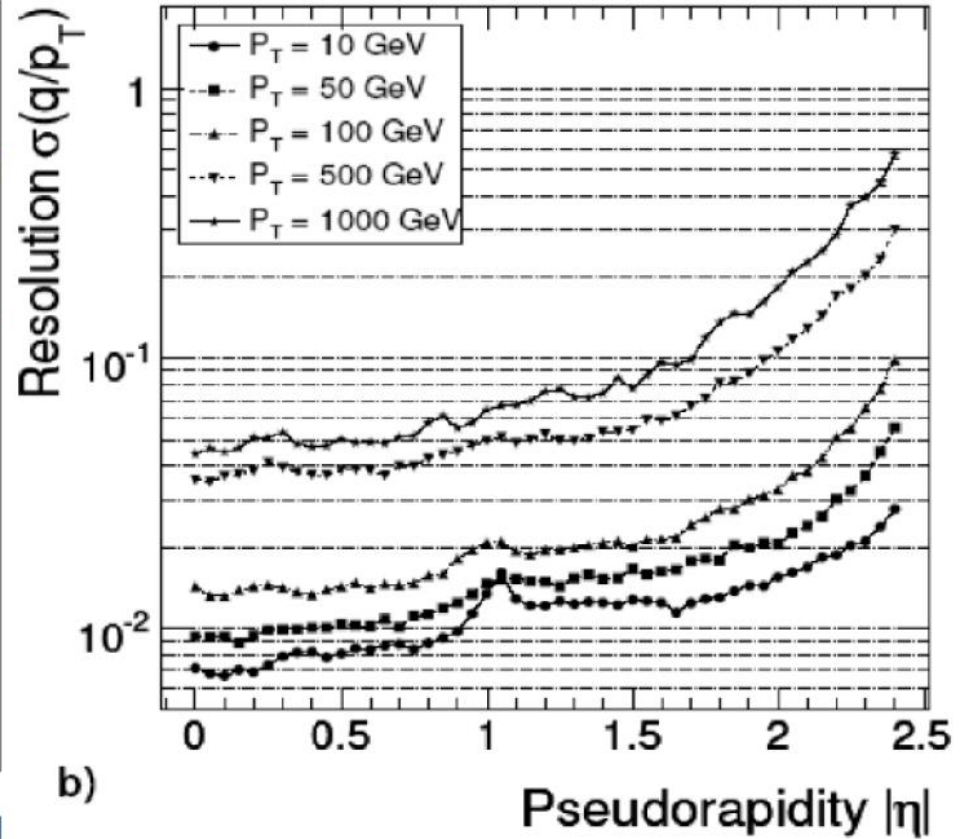
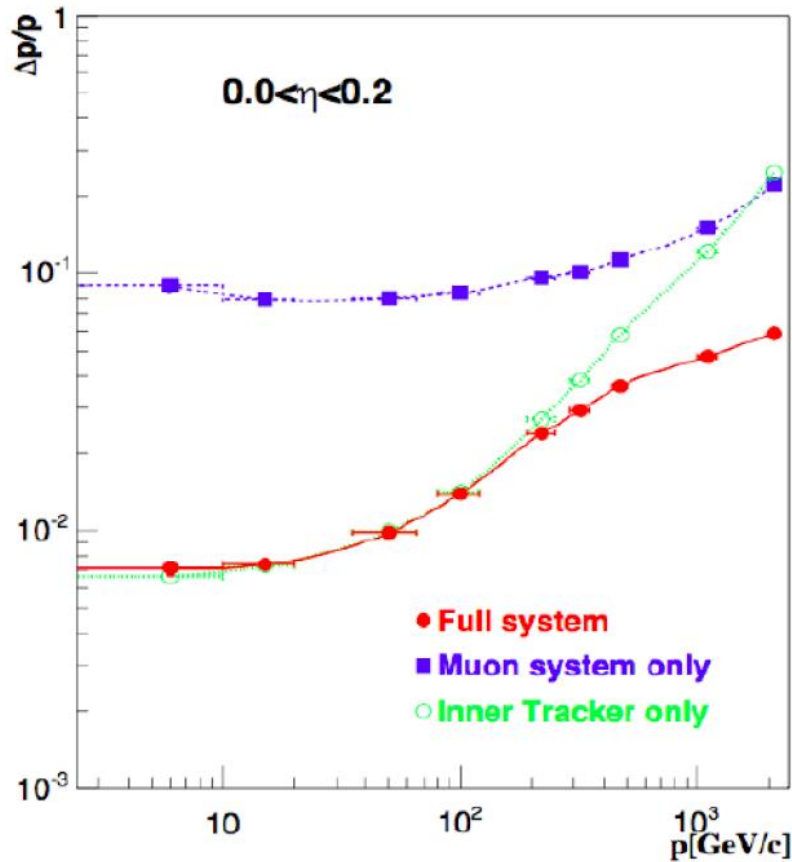
**Pt=3.9GeV enters muon system**

**Pt=5.5GeV leaves coil at 45 degrees**

**Pt=10GeV**

# Muon Performance at $\eta=0$

CMS performance at eta zero

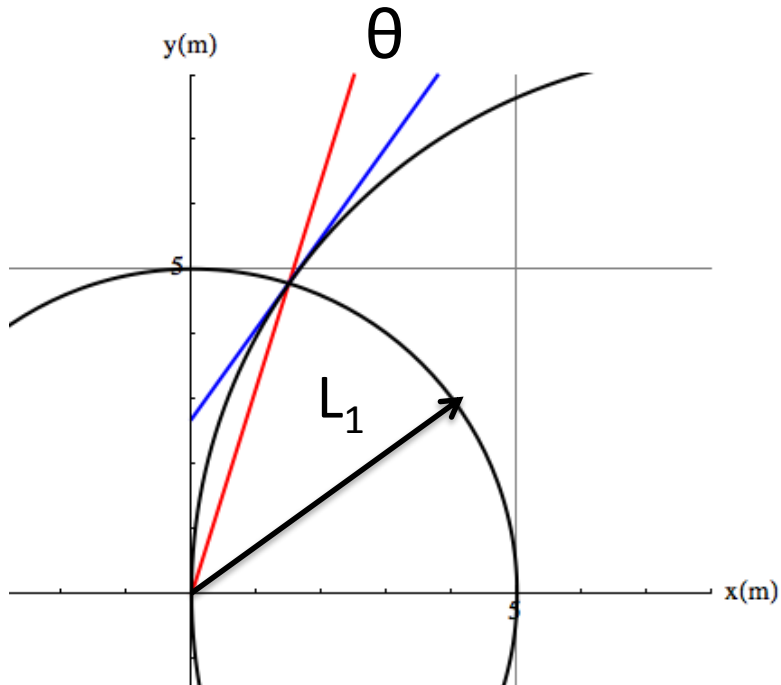


# Muon System Only

The standalone muon momentum resolution is defined by the angular measurement of the muon as it enter the muon system, and is given by

$$\frac{\Delta p}{p} = \frac{2p}{0.3L_1B} \sqrt{\theta_0^2 + \sigma_{theta}^2} \quad (214)$$

$$\theta_0 = \frac{0.0136}{\beta p [GeV/c]} \sqrt{\frac{L_{Calo}}{X0_{Calo}}} \left( 1 + 0.038 \log \frac{L_{Calo}}{X0_{Calo}} \right) \quad (212)$$



$\sigma_{\theta}$  represents the angular measurement error of the muon chambers.

$\theta_0$  represents the angular measurement error due to multiple scattering in the calorimeters.

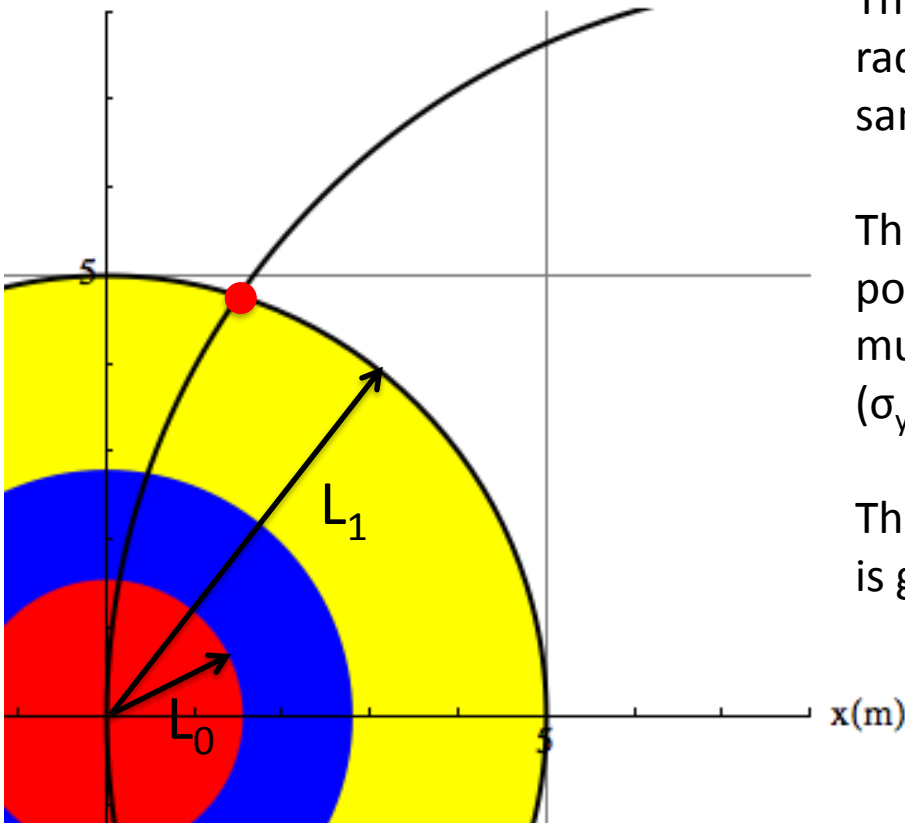
# Full System

We assume a constant magnetic field inside the coil radius  $L_1$ .

The measurement points in the tracker of radius  $L_0$  are equidistant and have all the same resolution  $\sigma_0$ .

The measurement point at  $L_1$  has a position error  $\sigma_1$  that is given by the multiple scattering inside the calorimeters ( $\sigma_y$  in the following).

The formula for the momentum resolution is given in the next slide.



## 17. Combined muon fit formulas

The curvature error  $\Delta c^2$  for a track in a constant magnetic field, measured at  $N + 1$  independent positions  $x_0, x_1, \dots, x_N$  with measurement errors  $\sigma_0, \sigma_1, \dots, \sigma_N$  is given by

$$S_m = \sum_{n=0}^N \frac{x_n^m}{\sigma_n^2} \quad \Delta c^2 = \frac{4(S_1^2 - S_0 S_2)}{S_2^3 - 2S_1 S_2 S_3 + S_0 S_3^2 + S_1^2 S_4 - S_0 S_2 S_4} \quad (208)$$

and the resulting momentum resolution is

$$\frac{\Delta p}{p} = \frac{p}{0.3B} \Delta c \quad (209)$$

For  $N + 1$  equidistant layers  $x_0 = 0, x_1 = L_0/N, x_2 = 2L_0/N, \dots, x_N = L_0$  with resolutions  $\sigma_0 = \sigma_1 = \dots = \sigma_N = \sigma$  we get the result

$$\frac{\Delta p}{p} = \frac{p}{0.3B} \frac{\sigma}{L_0^2} \sqrt{\frac{720N^3}{(N-1)(N+1)(N+2)(N+3)}} \approx \frac{p}{0.3B} \frac{\sigma}{L_0^2} \sqrt{\frac{720}{N+5}} \quad N \gg 1 \quad (210)$$

The approximate expression stays within 5% of the correct one for all  $N \geq 2$ .

If we assume the above  $N + 1$  layers to have resolution  $\sigma_0$  and one additional measurement point at position  $x_{N+1} = L_1$  with resolution  $\sigma_1$ , the expression for  $\Delta p$  reads as

$$\frac{\Delta p}{p} = \frac{p}{0.3B} \frac{\sigma_0}{L_0^2} \sqrt{\frac{720N^3(c_1\sigma_0^2 + c_2\sigma_1^2)}{(N+1)(N+2)(c_3\sigma_0^2 + c_4\sigma_1^2)}} \quad (211)$$

$$c_1 = 2[2N(L_0^2 - 3L_0L_1 + 3L_1^2) + L_0^2]$$

$$c_2 = L_0^2(N+1)(N+2)$$

$$c_3 = 3[L_0^2(3N^3 - N - 2) - 12L_0L_1(2N^3 - N^2 - N) + 12L_1^2(7N^3 - N^2 - N)] + 60N^3 \frac{L_1^4}{L_0^2} - 120N^3 \frac{L_1^3}{L_0}$$

$$c_4 = L_0^2(N-1)(N+1)(N+2)(N+3)$$

The position error of the track as it traverses the calorimeter of depth  $L_{Calo}$  is given by

$$\theta_0 = \frac{0.0136}{\beta p [GeV/c]} \sqrt{\frac{L_{Calo}}{X0_{Calo}}} \left( 1 + 0.038 \log \frac{L_{Calo}}{X0_{Calo}} \right) \quad (212)$$

$$\sigma_y = \frac{1}{\sqrt{3}} L_{Calo} \theta_0 \quad (213)$$

# Muon Performance Formulas at $\eta=0$

**Muon System standalone**  $\frac{\Delta p}{p} = \frac{2p}{0.3L_1B} \sqrt{\theta_0^2 + \sigma_{theta}^2}$        $\theta_0 = \frac{0.0136}{\beta p [GeV/c]} \sqrt{\frac{L_{Calo}}{X0_{Calo}}} \left(1 + 0.038 \log \frac{L_{Calo}}{X0_{Calo}}\right)$

**Inner Tracker**  $\frac{\Delta p}{p} = \frac{p}{0.3B} \frac{\sigma}{L_0^2} \sqrt{\frac{720N^3}{(N-1)(N+1)(N+2)(N+3)}} \approx \frac{p}{0.3B} \frac{\sigma}{L_0^2} \sqrt{\frac{720}{N+5}} \quad N \gg 1$

**Combined**  $\frac{\Delta p}{p} = \frac{p}{0.3B} \frac{\sigma_0}{L_0^2} \sqrt{\frac{720N^3(c_1\sigma_0^2 + c_2\sigma_1^2)}{(N+1)(N+2)(c_3\sigma_0^2 + c_4\sigma_1^2)}} \quad (211)$

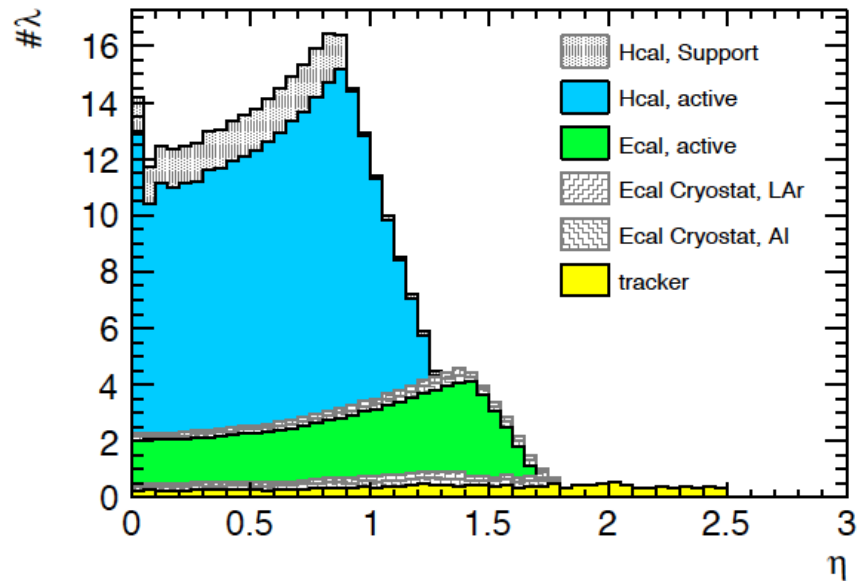
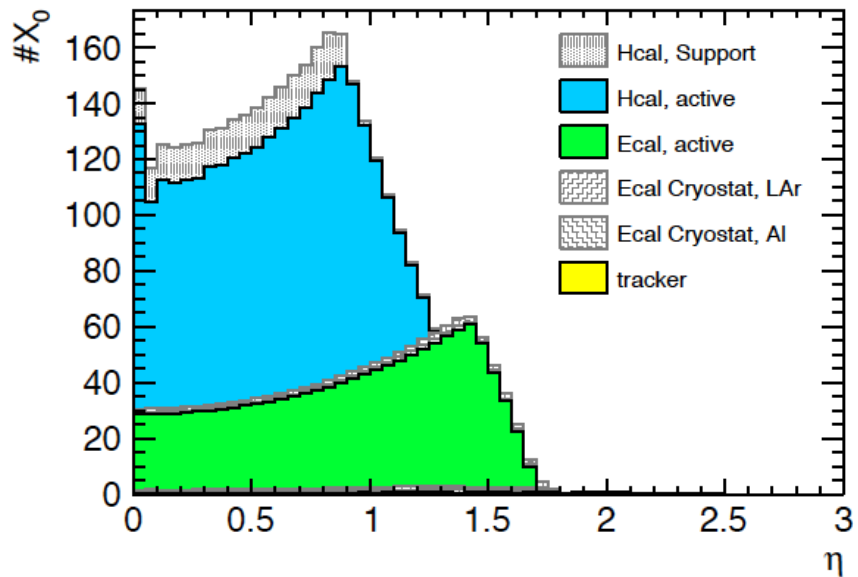
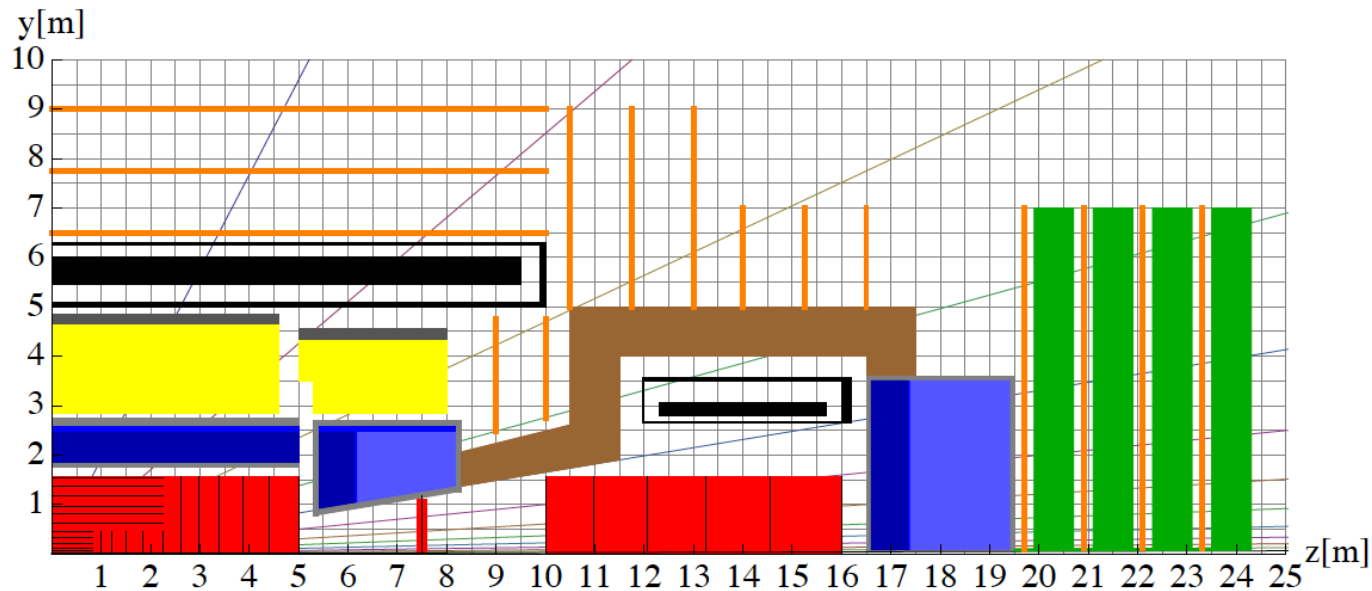
$$c_1 = 2[2N(L_0^2 - 3L_0L_1 + 3L_1^2) + L_0^2]$$

$$c_2 = L_0^2(N+1)(N+2)$$

$$c_3 = 3[L_0^2(3N^3 - N - 2) - 12L_0L_1(2N^3 - N^2 - N) + 12L_1^2(7N^3 - N^2 - N)] + 60N^3 \frac{L_1^4}{L_0^2} - 120N^3 \frac{L_1^3}{L_0}$$

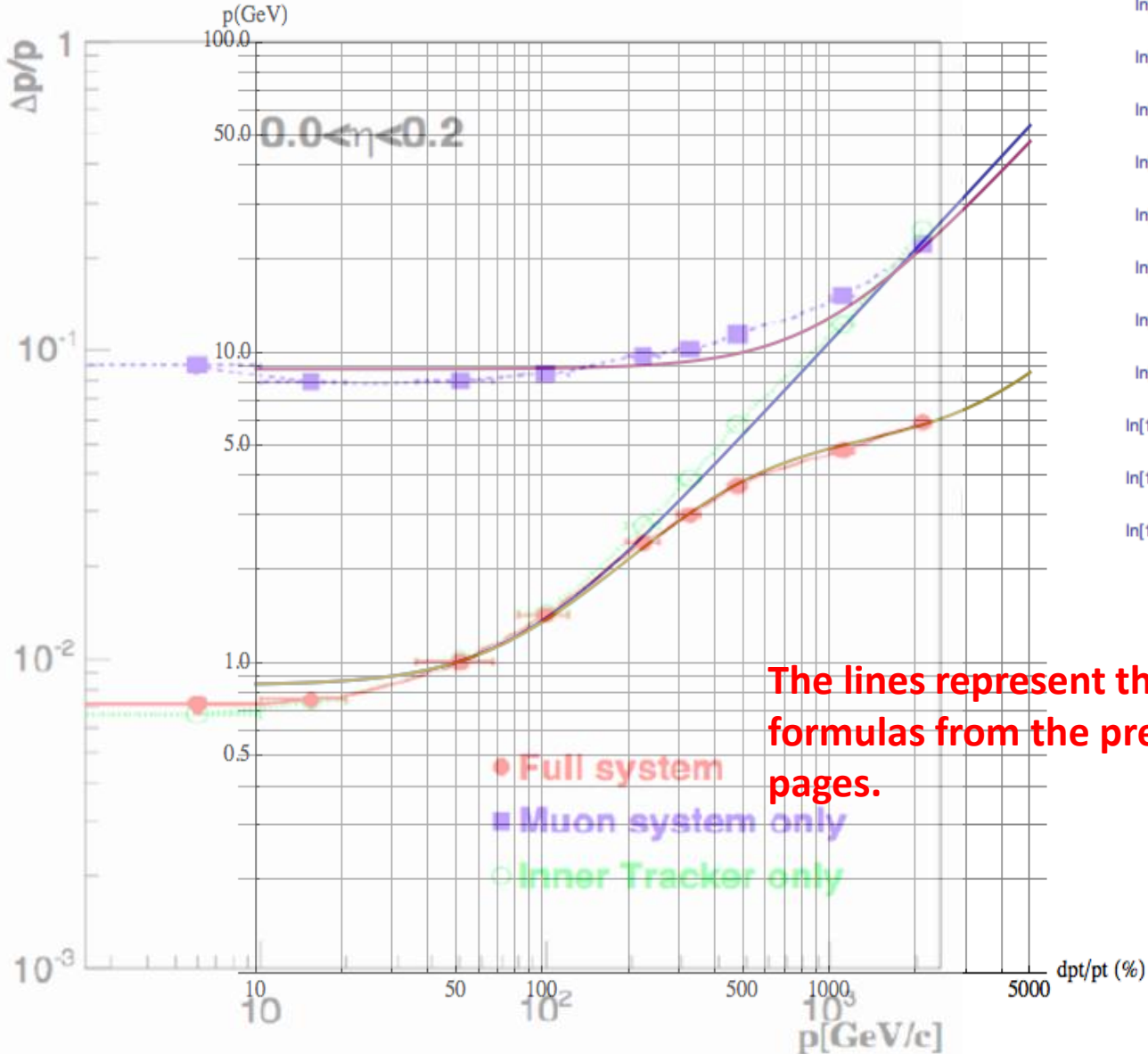
$$c_4 = L_0^2(N-1)(N+1)(N+2)(N+3)$$

$$\sigma_y = \frac{1}{\sqrt{3}} L_{Calo} \theta_0$$





# CMS muon resolution at $\eta=0$



```

ln[2]:= (* ===== *)
ln[3]:= NO = 10;
ln[4]:= L = 1.1;
ln[5]:= sig0 = 23 * 10 ^ (-6);
ln[6]:= L1 = 3;
ln[7]:= (* sig1=50*10^(-6); *)
ln[8]:= B0 = 4;
ln[9]:= X0Tracker = 0.7;
ln[10]:= sigtheta = 170 * 10 ^ (-6);
ln[11]:= X0Calo = 100;
ln[12]:= LCalo = 2.1;
    
```

The lines represent the formulas from the previous pages.

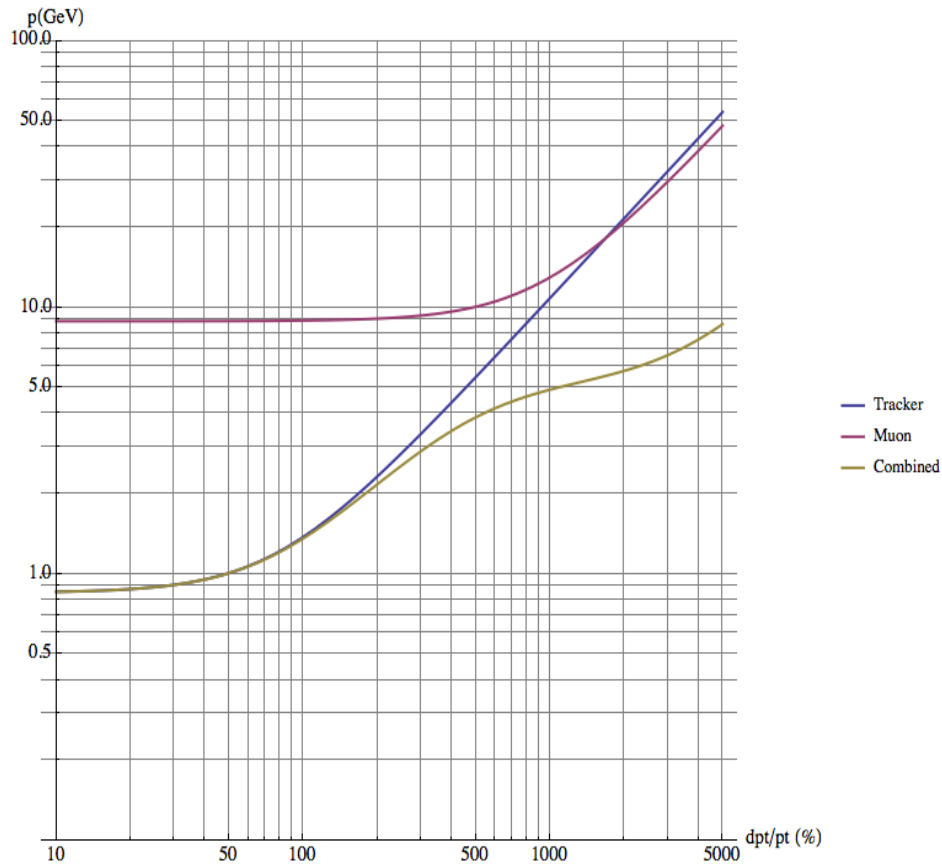
# CMS muon resolution at $\eta=0$

The CMS muon system performance is well represented by assuming:

10 layers of tracker with 23 $\mu$ m resolution.

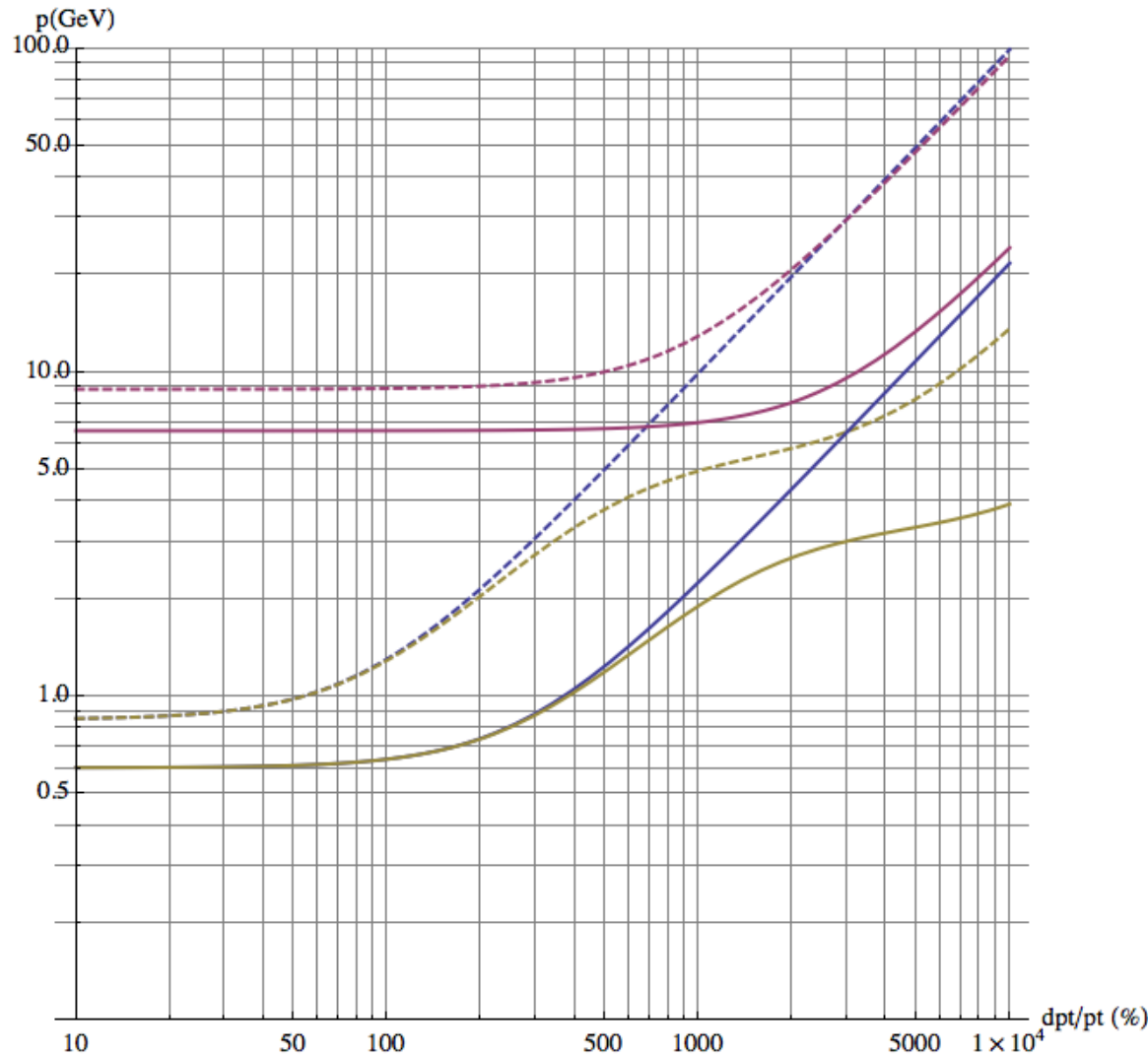
170 microrad of angular resolution where the muon exits the coil.

Better than 100 $\mu$ m position resolution where the muon exits the coil.



```
In[2]:= (* ===== *)
In[3]:= N0 = 10;
In[4]:= L = 1.1;
In[5]:= sig0 = 23 * 10 ^ (-6);
In[6]:= L1 = 3;
In[7]:= (* sig1=50*10^(-6); *)
In[8]:= B0 = 4;
In[9]:= X0Tracker = 0.7;
In[10]:= sigtheta = 170 * 10 ^ (-6);
In[11]:= X0Calo = 100;
In[12]:= LCalo = 2.1;
```

# Comparing CMS to possible FCC resolution



- ln[14]:= **BCMS = 4;**
- ln[15]:= **BFCC = 4;**
- ln[16]:= **NCMS = 13;**
- ln[17]:= **NFCC = 13;**
- ln[18]:= **LOCMS = 1.1;**
- ln[19]:= **LOFCC = 1.55;**
- ln[20]:= **sOCMS =  $23 \times 10^{-6}$ ;**
- ln[21]:= **sOFCC =  $10 \times 10^{-6}$ ;**
- ln[22]:= **X0traCMS = 0.7;**
- ln[23]:= **X0traFCC = 0.7;**
- ln[24]:= **L1CMS = 3;**
- ln[25]:= **L1FCC = 5.;**
- ln[26]:= **X0calCMS = 100;**
- ln[27]:= **X0calFCC = 150;**
- ln[28]:= **sigthCMS =  $170 \times 10^{-6}$ ;**
- ln[29]:= **sigthFCC =  $70 \times 10^{-6}$ ;**
- ln[30]:= **LCalCMS = 2.1;**
- ln[31]:= **LCalFCC = 3.;**

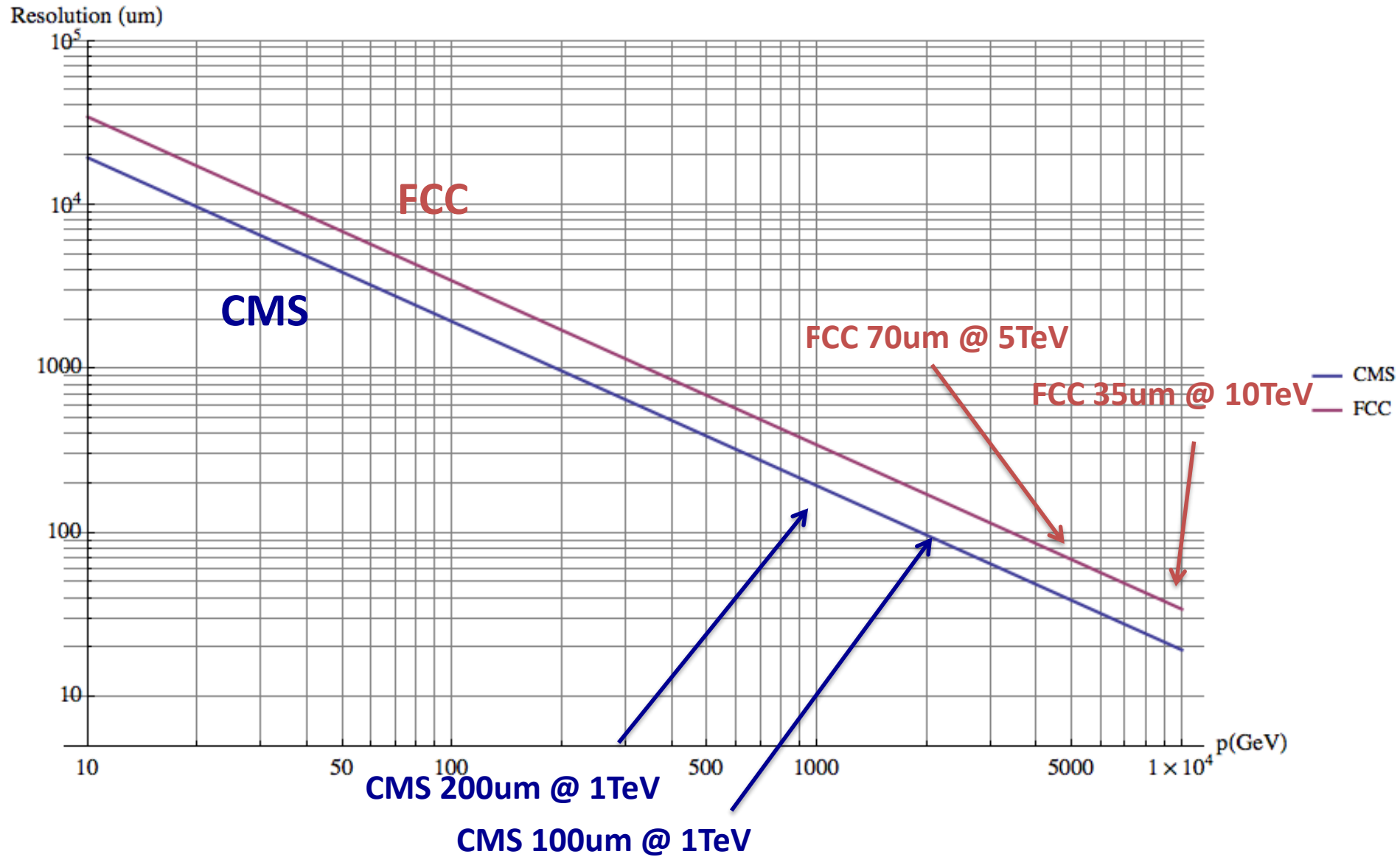
The FCC muon system performance assumes:

13 layers of tracker with 10um resolution and 1.55m radius.

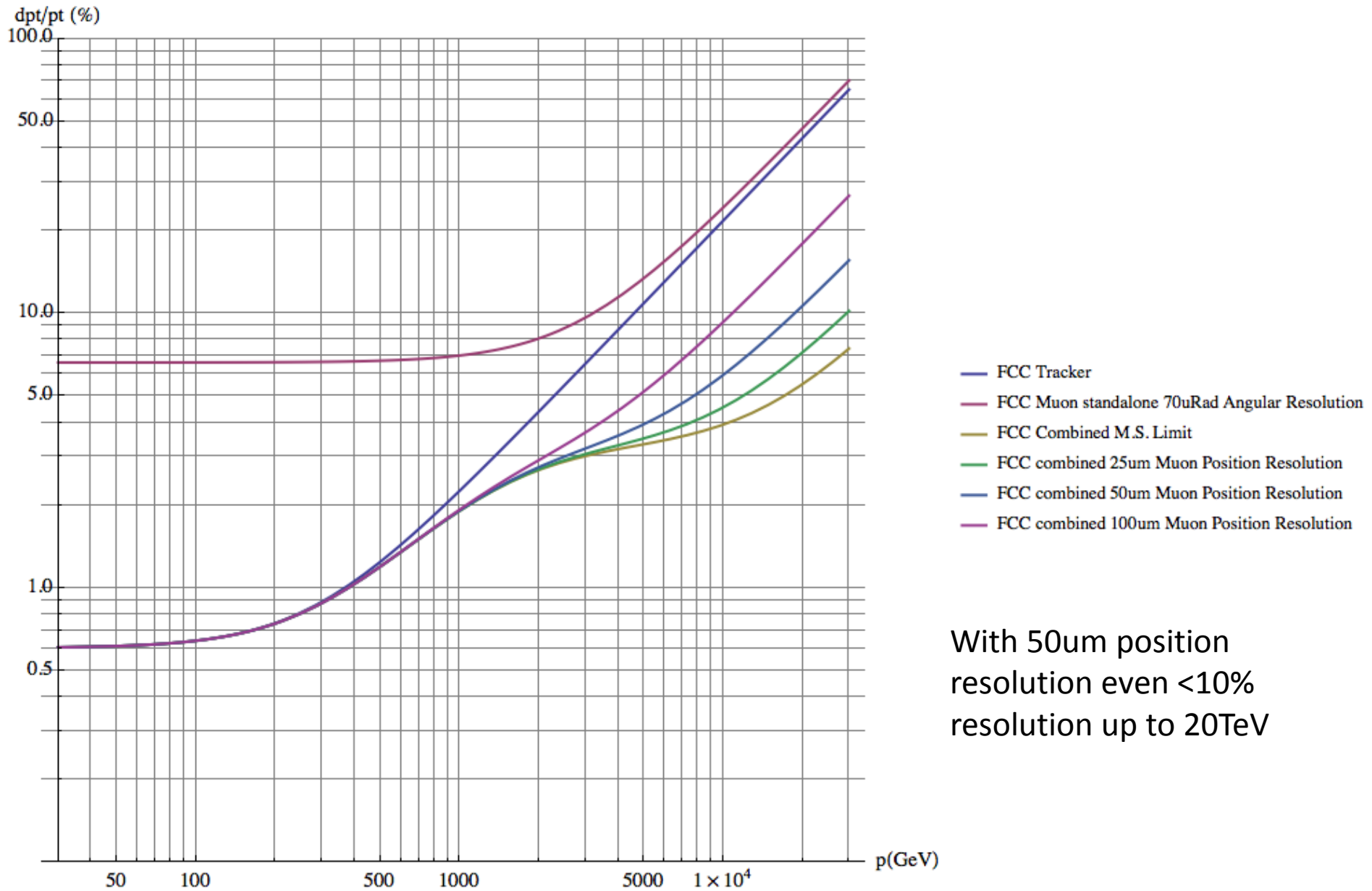
70 microrad of angular resolution where the muon exits the coil.

Better than 25um position resolution where the muon exits the coil.

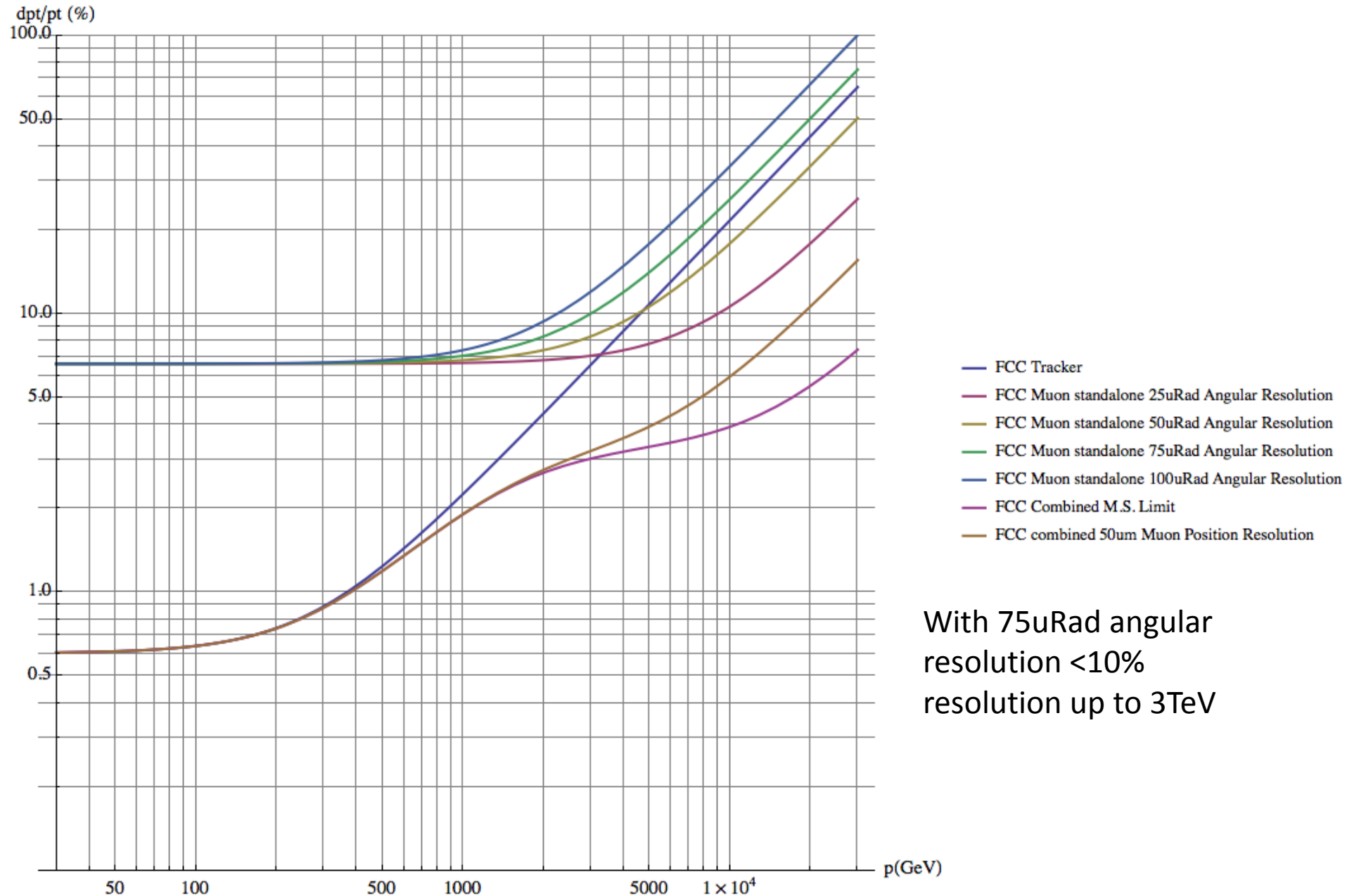
# Multiple scattering error dy at the entrance of the muon system



# Combined performance for varying position resolution



# Standalone performance for varying angular resolution



# FCC detector muon system

A 50 $\mu$ m position resolution and 70 $\mu$ Rad angular resolution for muons exiting the solenoid will give excellent standalone and combined muon resolution at  $\eta=0$ .

This can be easily realized by present technology.

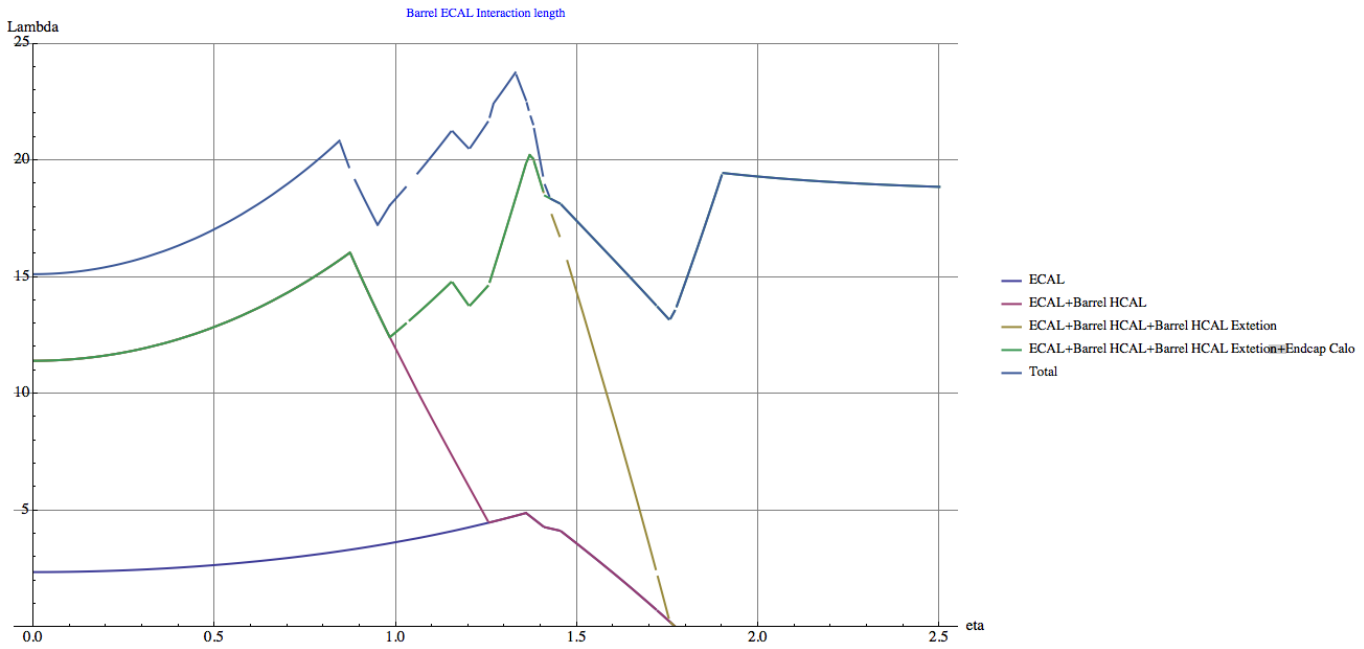
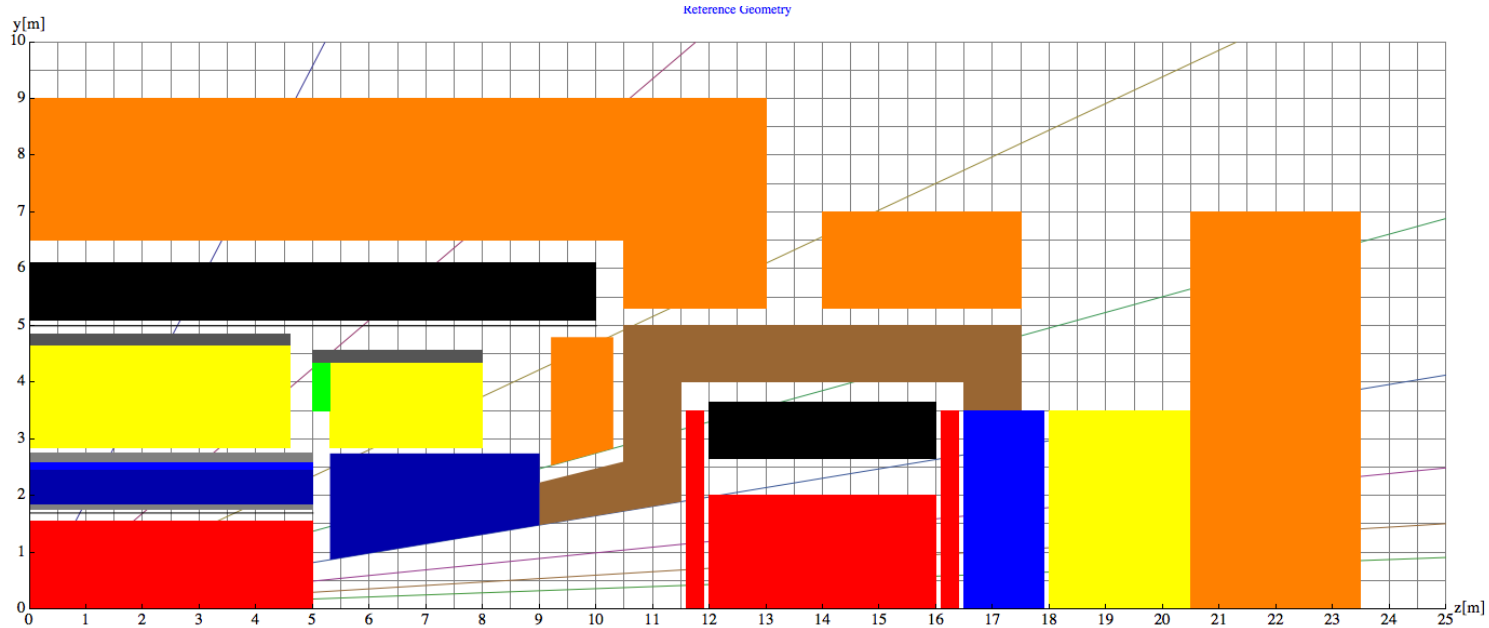
E.g. Two redundant stations of detectors with 50 $\mu$ m position resolution at a separation of 1-2 meters will realize this requirement.

The distance between the stations must be large enough to make sure that correlated background is eliminated.

The existing magnetic fields around 1.5Tm should be sufficient for that. Simulations have to prove this fact.

Resolution studies for larger  $\eta$  values still to be done.

# Number of interaction lengths ( $\lambda$ ) of the different Systems





# Number of radiation lengths ( $X_0$ ) in front of the Muon System

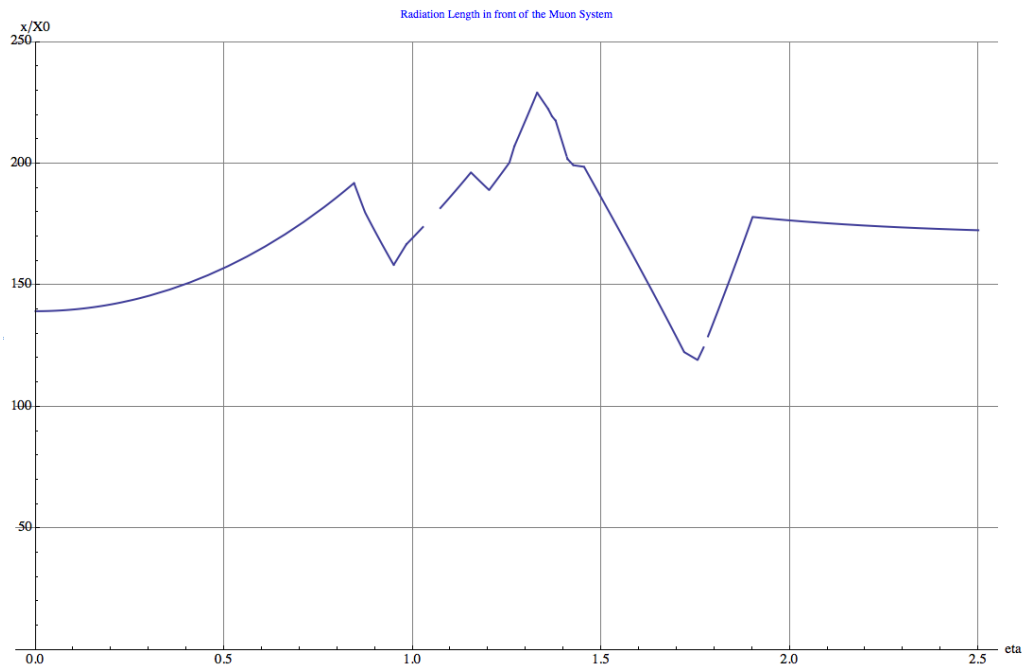
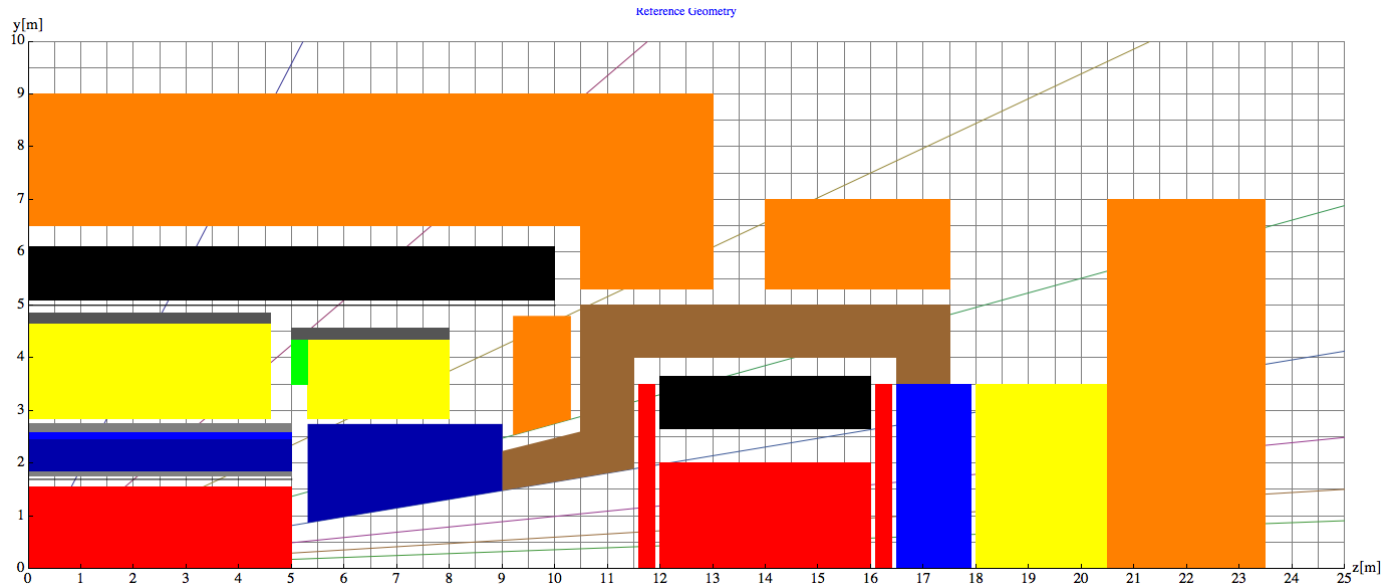


Table 4.5: Expected rates on the muon detector when operating at an instantaneous luminosity of  $2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$  at a collision energy of 14 TeV. The values are averages, in kHz/cm<sup>2</sup>, over the chamber with the minimum illumination, the whole region and the chamber with maximum illumination. The values are extrapolated from measured rates at 8 TeV.

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M2R4	0.12 ± 0.02	0.63 ± 0.10	2.6 ± 0.4
M3R1	39 ± 6	123 ± 18	216 ± 32
M3R2	3.3 ± 0.5	11.9 ± 1.7	29 ± 4
M3R3	0.17 ± 0.02	1.12 ± 0.16	2.9 ± 0.4
M3R4	0.017 ± 0.002	0.12 ± 0.02	0.63 ± 0.09
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M4R4	0.007 ± 0.001	0.056 ± 0.008	0.31 ± 0.04
M5R1	19.7 ± 2.9	54 ± 8	91 ± 13
M5R2	1.58 ± 0.23	4.8 ± 0.7	10.8 ± 1.6
M5R3	0.29 ± 0.04	0.79 ± 0.11	1.69 ± 0.25
M5R4	0.23 ± 0.03	2.1 ± 0.3	9.0 ± 1.3

2 Particle rates in the muon system. The first row gives the maximal particle rate in each region per interaction as obtained from GCALOR; the second gives the calculated rate at a luminosity of  $5 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$  assuming a total p – p cross-section of  $\sigma=102.4 \text{ mb}$ ; and the last row the rate including fety factors.

	Station 1	Station 2	Station 3	Station 4	Station 5
gion 1	$8.3 \times 10^{-3} / \text{cm}^2$	$2.7 \times 10^{-4} / \text{cm}^2$	$7.2 \times 10^{-5} / \text{cm}^2$	$4.7 \times 10^{-5} / \text{cm}^2$	$3.2 \times 10^{-5} / \text{cm}^2$
	230 kHz/cm <sup>2</sup>	7.5 kHz/cm <sup>2</sup>	2 kHz/cm <sup>2</sup>	2.3 kHz/cm <sup>2</sup>	880 Hz/cm <sup>2</sup>
	460 kHz/cm <sup>2</sup>	37.5 kHz/cm <sup>2</sup>	10 kHz/cm <sup>2</sup>	6.5 kHz/cm <sup>2</sup>	4.4 kHz/cm <sup>2</sup>
gion 2	$3.3 \times 10^{-3} / \text{cm}^2$	$1.9 \times 10^{-4} / \text{cm}^2$	$2.3 \times 10^{-5} / \text{cm}^2$	$1.6 \times 10^{-5} / \text{cm}^2$	$1.3 \times 10^{-5} / \text{cm}^2$
	93 kHz/cm <sup>2</sup>	5.3 kHz/cm <sup>2</sup>	650 Hz/cm <sup>2</sup>	430 Hz/cm <sup>2</sup>	350 Hz/cm <sup>2</sup>
	186 kHz/cm <sup>2</sup>	26.5 kHz/cm <sup>2</sup>	3.3 kHz/cm <sup>2</sup>	2.2 kHz/cm <sup>2</sup>	1.8 kHz/cm <sup>2</sup>
gion 3	$1.4 \times 10^{-3} / \text{cm}^2$	$4.7 \times 10^{-5} / \text{cm}^2$	$7.3 \times 10^{-6} / \text{cm}^2$	$5.4 \times 10^{-6} / \text{cm}^2$	$4.7 \times 10^{-6} / \text{cm}^2$
	40 kHz/cm <sup>2</sup>	1.3 kHz/cm <sup>2</sup>	200 Hz/cm <sup>2</sup>	150 Hz/cm <sup>2</sup>	130 Hz/cm <sup>2</sup>
	80 kHz/cm <sup>2</sup>	6.5 kHz/cm <sup>2</sup>	1.0 kHz/cm <sup>2</sup>	750 Hz/cm <sup>2</sup>	650 Hz/cm <sup>2</sup>
gion 4	$4.5 \times 10^{-4} / \text{cm}^2$	$8.3 \times 10^{-6} / \text{cm}^2$	$3.0 \times 10^{-6} / \text{cm}^2$	$1.8 \times 10^{-6} / \text{cm}^2$	$1.7 \times 10^{-6} / \text{cm}^2$
	12.5 kHz/cm <sup>2</sup>	230 Hz/cm <sup>2</sup>	83 Hz/cm <sup>2</sup>	50 Hz/cm <sup>2</sup>	45 Hz/cm <sup>2</sup>
	25 kHz/cm <sup>2</sup>	1.2 kHz/cm <sup>2</sup>	415 Hz/cm <sup>2</sup>	250 Hz/cm <sup>2</sup>	225 Hz/cm <sup>2</sup>

Muon TDR for 5x10^32				Upgrade TDR for 2x10^33				ratio @ 2x10^33			
590	216	86	91	7.5	2	2.3	0.88	19.7	27.0	9.3	25.9
97	29	12.6	10.8	5.3	0.65	0.43	0.35	4.6	11.2	7.3	7.7
13.4	2.9	1.37	1.69	1.3	0.2	0.15	0.13	2.6	3.6	2.3	3.3
2.6	0.63	0.31	9	0.23	0.083	0.05	0.045	2.8	1.9	1.6	50.0

