

Test of lepton flavor violation with K_{e2} decay at KLOE

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(for the KLOE Collaboration)

CERN, May 25th 2009



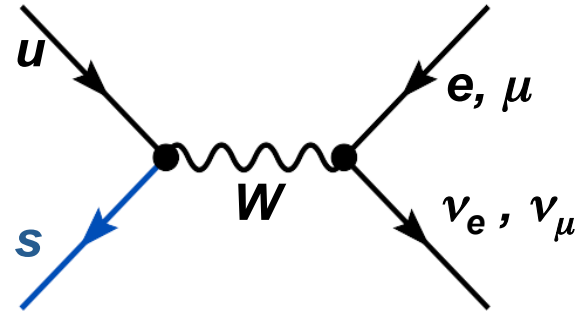
Measurement of $R_K = \Gamma(K_{e2})/\Gamma(K_{\mu2})$

- Introduction
- K_{e2} events counting
- Study of direct emission in $K_{e2\gamma}$
- Results on R_K

Standard Model prediction for $R_K = \Gamma(K_{e2})/\Gamma(K_{\mu2})$

Reduced hadronic uncertainties in the ratio $K_{e2}/K_{\mu2}$ (no f_K)

$$R_K^{SM} = \frac{m_e^2 (m_K^2 - m_e^2)^2}{m_\mu^2 (m_K^2 - m_\mu^2)^2} (1 + \delta R_K^{rad})$$



$$1 + \delta R_K^{rad} = (0.9642 \pm 0.0004) \quad \text{IB only}$$

Finkemeier 97
Cirigliano-Rosell 07

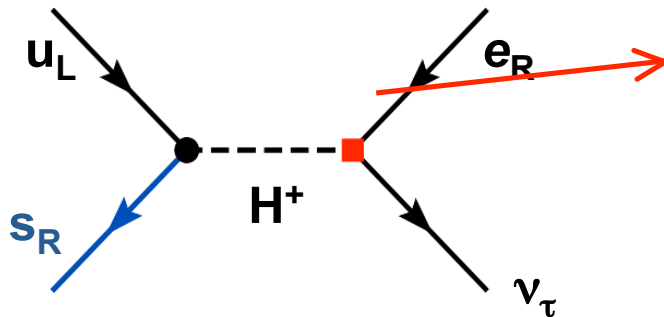
$$R_K^{SM} = (2.477 \pm 0.0001) \times 10^{-5} \quad 0.04\% \text{ uncertainty}$$

Strong helicity suppression of electron channel enhances sensitivity to physics beyond the SM

New Physics potential of R_K

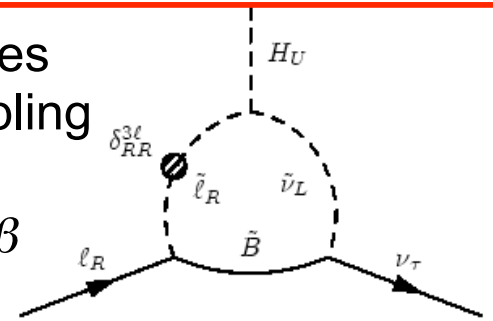
In MSSM, LFV can give % deviations from SM *Masiero, Paradisi
Petronzio 06*

$$R_K^{LFV} = \frac{\sum_i K \rightarrow e \nu_i}{\sum_i K \rightarrow \mu \nu_i} \approx \frac{\Gamma_{SM}(K \rightarrow e \nu_e) + \Gamma(K \rightarrow e \nu_\tau)}{\Gamma_{SM}(K \rightarrow \mu \nu_\mu)}$$



LFV from loop generates an effective $eH^+\nu_\tau$ coupling

$$eH^+\nu_\tau \rightarrow \frac{g_2}{\sqrt{2}} \frac{m_\tau}{M_W} \Delta_R^{31} \tan^2 \beta$$



$$R_K^{LFV} \approx R_K^{SM} \left(1 + \frac{m_K^4}{m_H^4} \frac{m_\tau^2}{m_e^2} |\Delta_R^{31}|^2 \tan^6 \beta \right)$$

1 % effect if $\Delta_R^{31} \approx 5 \times 10^{-4}$, $\tan \beta \approx 40$, $m_H \approx 500$ GeV)

Entering the precision realm for R_K

PDG 2008 $R_K = (2.45 \pm 0.11) \times 10^{-5}$ **4.5% accuracy**

three measurements from 70's

Main players in the challenge to push down precision on R_K

KLOE preliminary result with 2001-2004 data: $R_K = 2.55(5)_{\text{stat}}(5)_{\text{syst}} \times 10^{-5}$
from ≈ 8000 Ke2 candidates (**3% accuracy**)

NA48/2 preliminary result with 2003 data: $R_K = 2.416(43)_{\text{stat}}(24)_{\text{syst}} \times 10^{-5}$
from ≈ 4000 Ke2 candidates (**2% accuracy**)

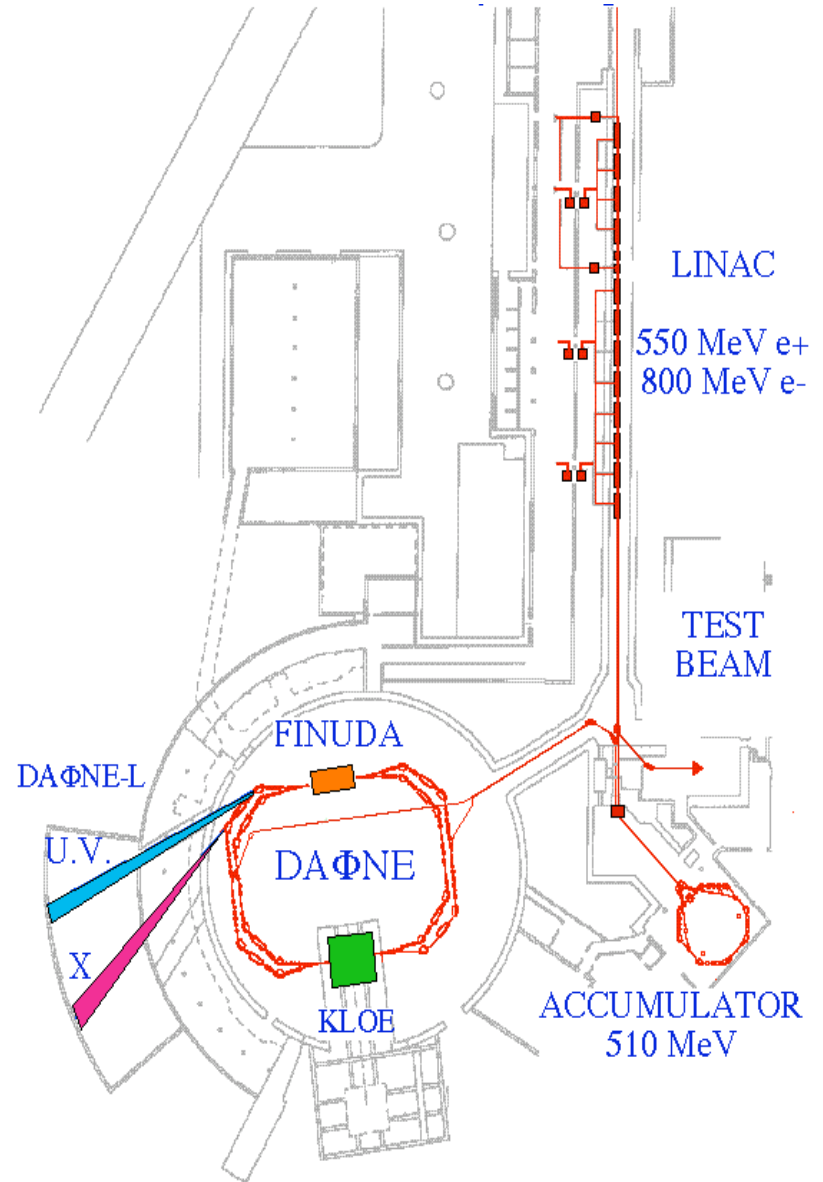
preliminary result with 2004 data: $R_K = 2.455(45)_{\text{stat}}(41)_{\text{syst}} \times 10^{-5}$
from ≈ 4000 Ke2 candidates (**3% accuracy**)

NA62 $\approx 150,000$ Ke2 events collected in a dedicated 2007 run
aims at $\approx 0.4\%$

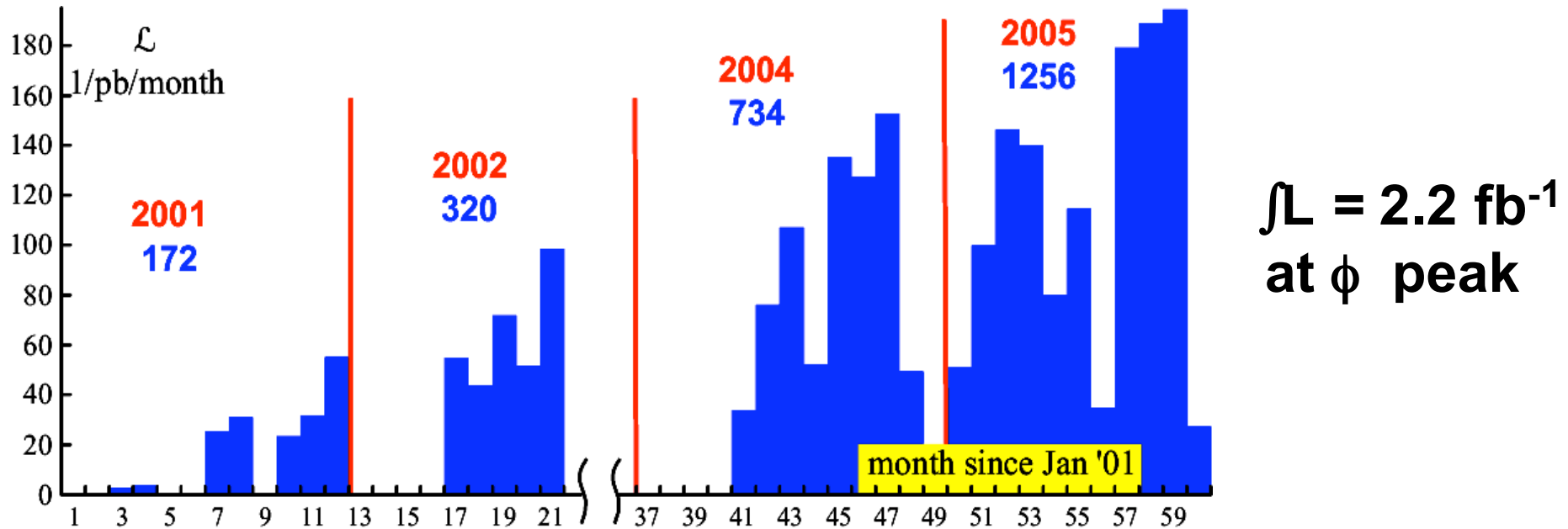
DAΦNE e^+e^- collider at LNF



- $\sqrt{s} \sim 1019.46 \text{ MeV} = m_\phi$
- $\sigma_\phi \sim 3.1 \mu\text{b}$ at peak
- crossing angle $\sim 12.5 \text{ mrad}$
- today, $L_{\text{peak}} = 4.5 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$



Summary of KLOE data taking



$BR(\phi \rightarrow K^+ K^-) \approx 0.49$ yielding 3×10^9 $K^+ K^-$ pairs

$\approx 50,000$ Ke2 decays in fiducial volume

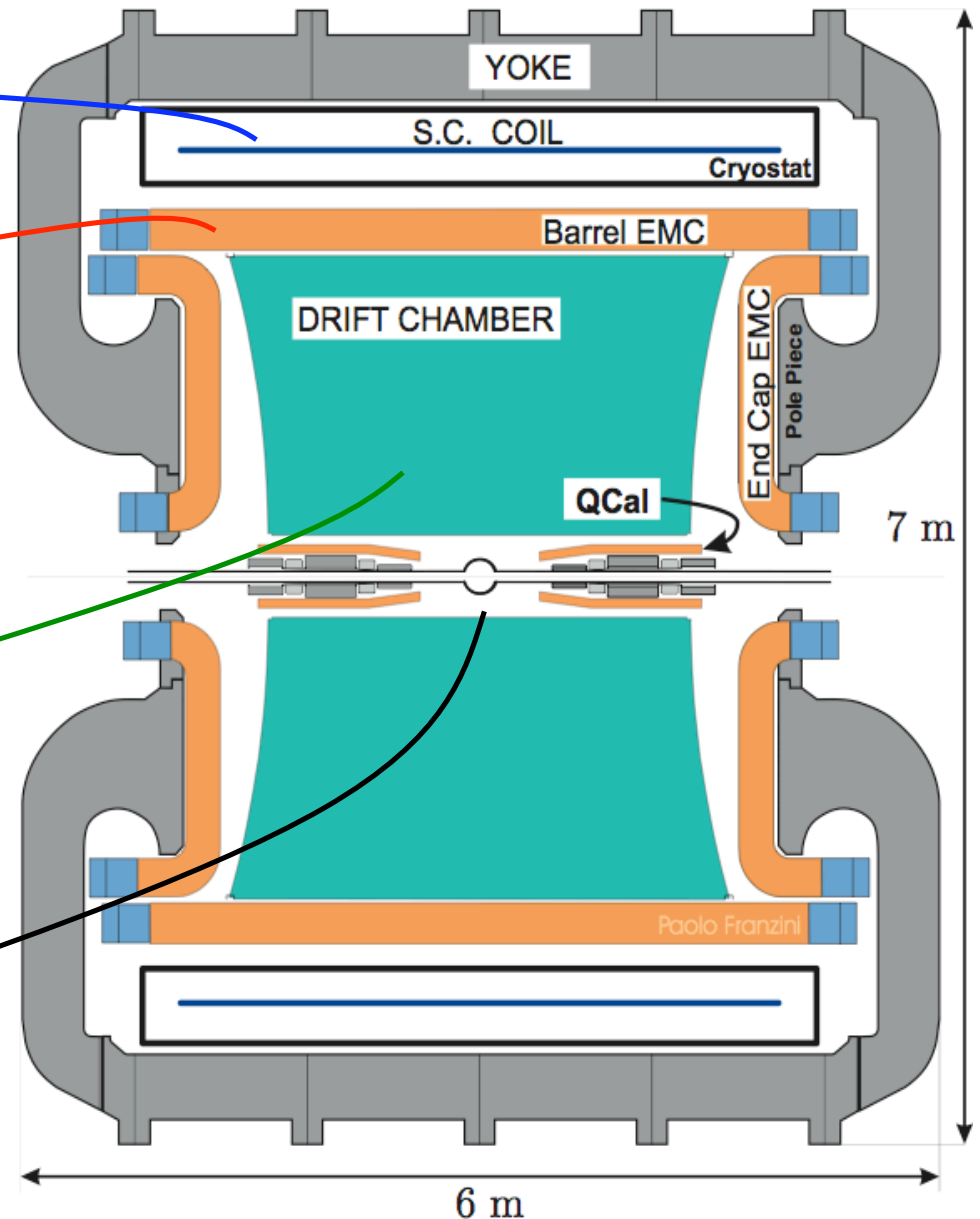
The KLOE experiment

Magnet
SC coil, $B = 0.6 \text{ T}$

EM Calorimeter
Pb-scint fiber
4880 PMs, 2440 cells

Drift chamber
12582 sense wires
52140 tot wires
Carbon fiber walls

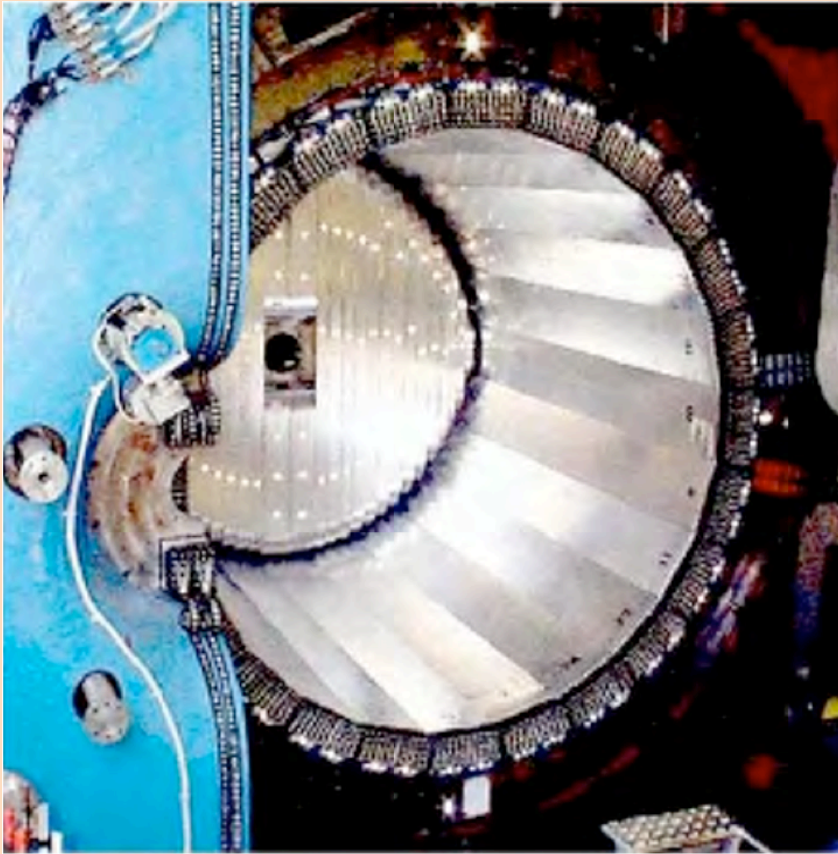
Al-Be beam pipe
 $r = 10 \text{ cm}$, 0.5 cm
thick



Detector performances

$$\sigma_E/E = 5.7\%/\sqrt{E(\text{GeV})}$$

$$\sigma_t = 54/\sqrt{E(\text{GeV})} \oplus 140 \text{ ps}$$



EM Calorimeter

Drift Chamber



$$\sigma(p_{\perp})/p_{\perp} = 0.4\%$$

$$\sigma_{x,y} = 150 \mu\text{m}; \sigma_z = 2 \text{ mm}$$

Charged kaon beams

ϕ decay at rest provides almost **pure** kaon beams of known momentum

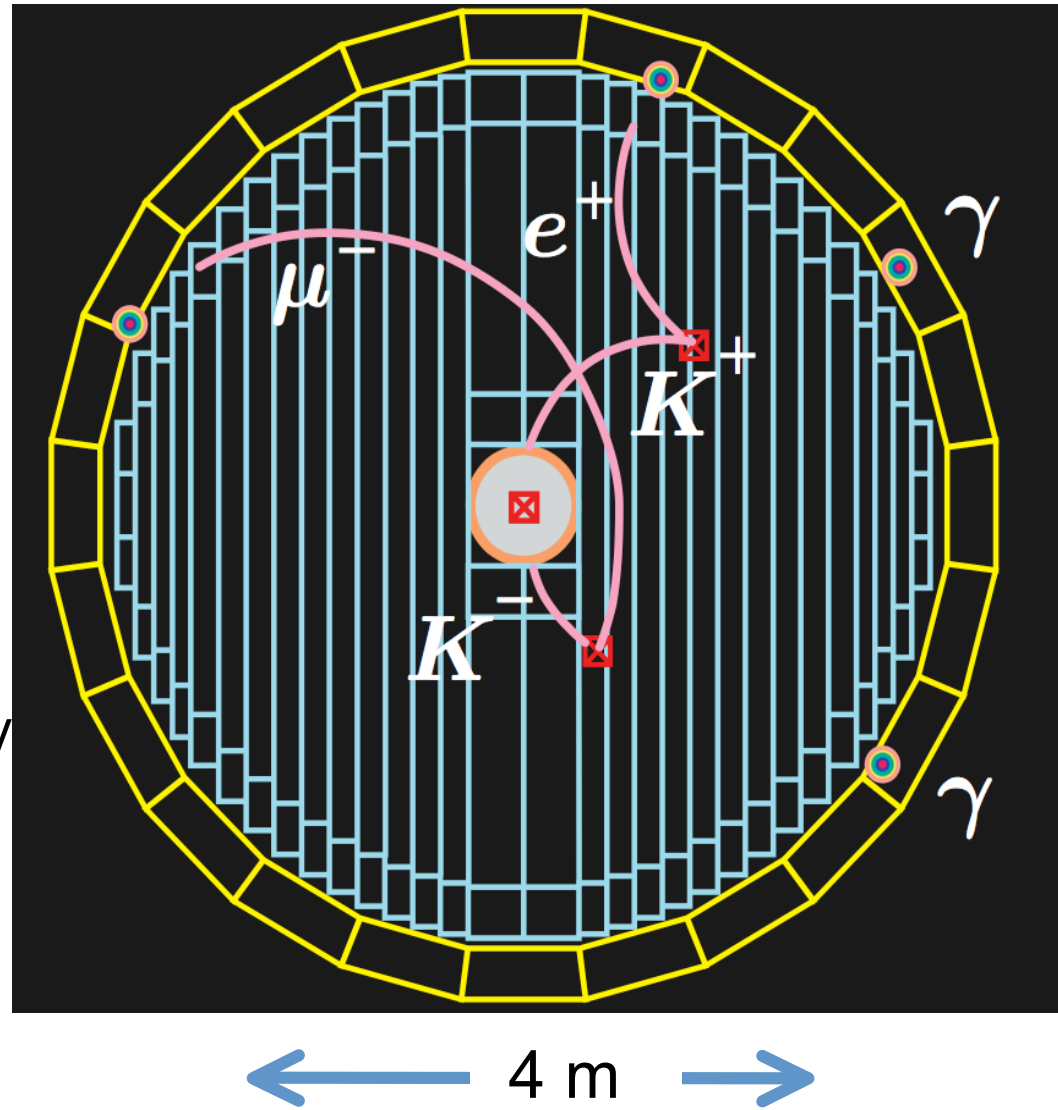
$$p_K \approx 100 \text{ MeV}$$

$$\lambda \approx 90 \text{ cm}$$

(56% of K^+ decay in DC)

Kaon momentum is measured with 1 MeV resolution in DC

- *Constraints* from ϕ 2-body decay
- *Particle ID* with kinematics and TOF
- *Tagging* provides unbiased control samples for efficiency measurement

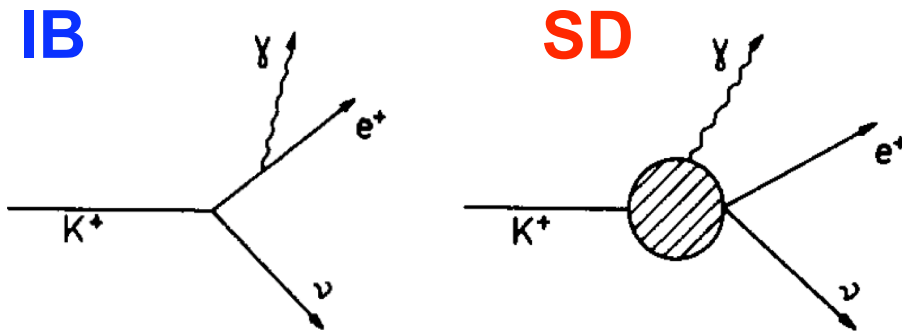


Measurement of $R_K = \Gamma(K_{e2})/\Gamma(K_{\mu2})$

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- **K_{e2} events counting**
- Study of direct emission in $K_{e2\gamma}$
- Results on R_K

Ke2(γ): signal definition

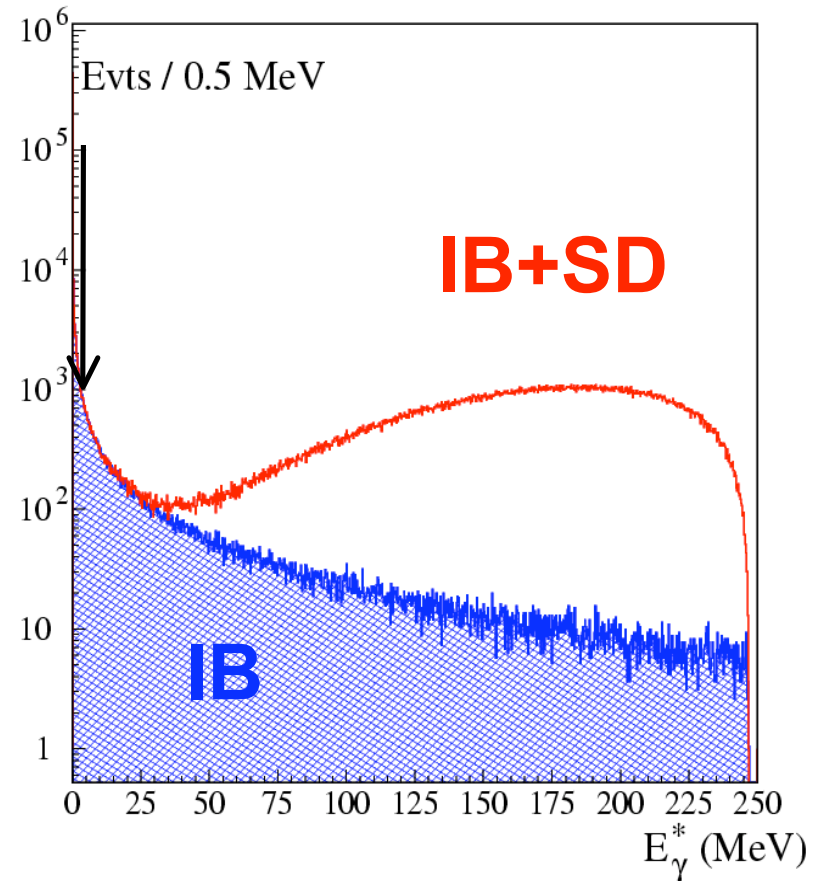
SM prediction made in terms of **IB** process only: unobservable!



From theory (ChPT) expect **SD** \approx **IB** for Ke2, but experimental knowledge is poor

$$\delta\text{SD}/\text{SD} \approx 15\%$$

- 1) Consider as “signal” events with $E_\gamma < 10$ MeV (SD negligible)
- 2) Correct for IB tail, 0.0625(5)



Analysis basic principles

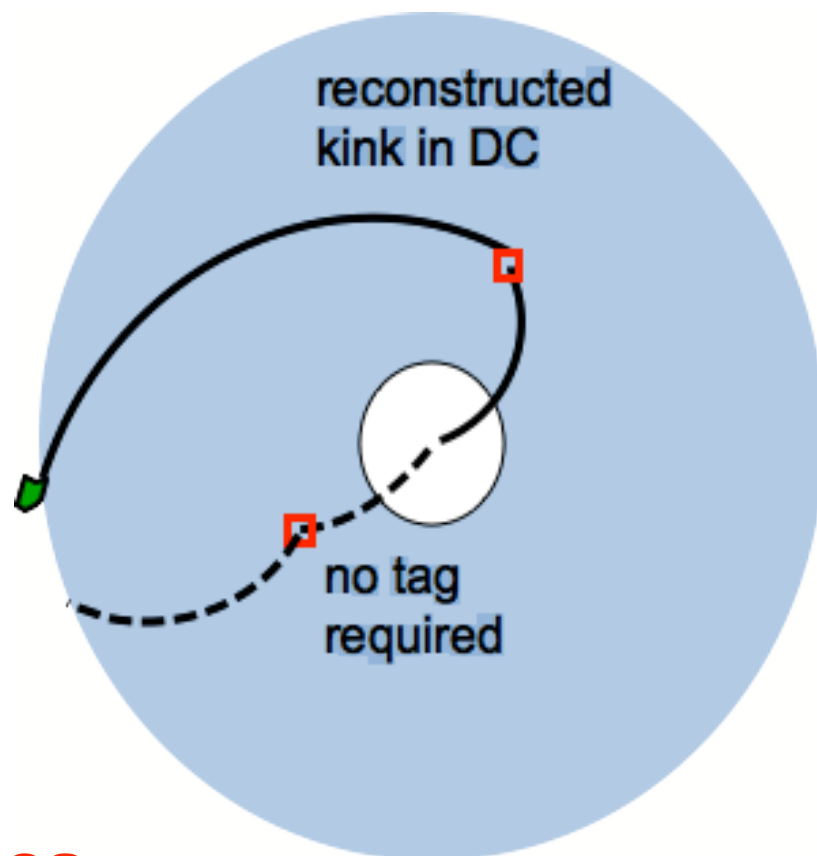
1) Select kinks in DC (\approx fiducial volume)

- K track from IP
- secondary with $p_{lep} > 180$ MeV

for decays occurring in the FV, the reconstruction efficiency is $\approx 51\%$

2) No tag required on the opposite hemisphere (as we usually do!)

→ gain $\times 4$ of statistics

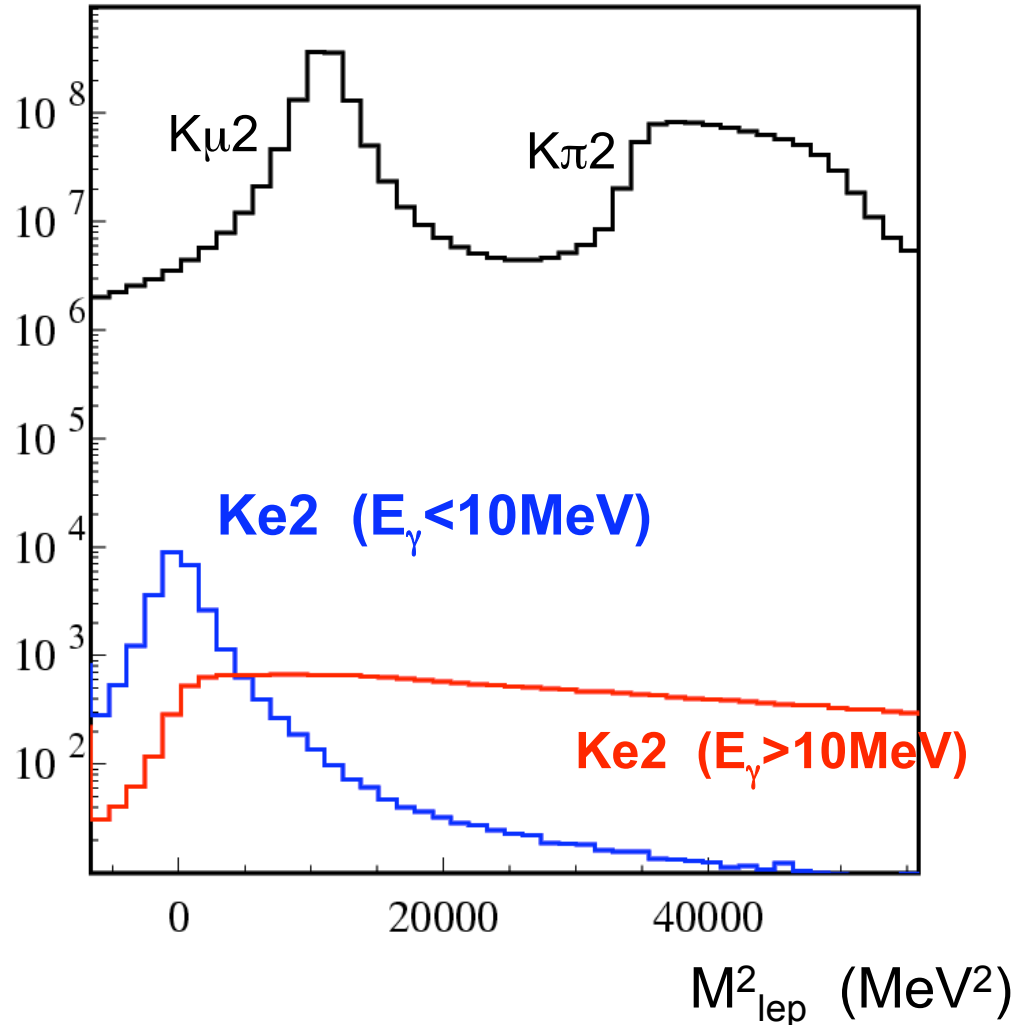


Analysis basic principles

- 3) Exploit tracking of K and secondary:
assuming $m_\nu = 0$ get M_{lep}^2

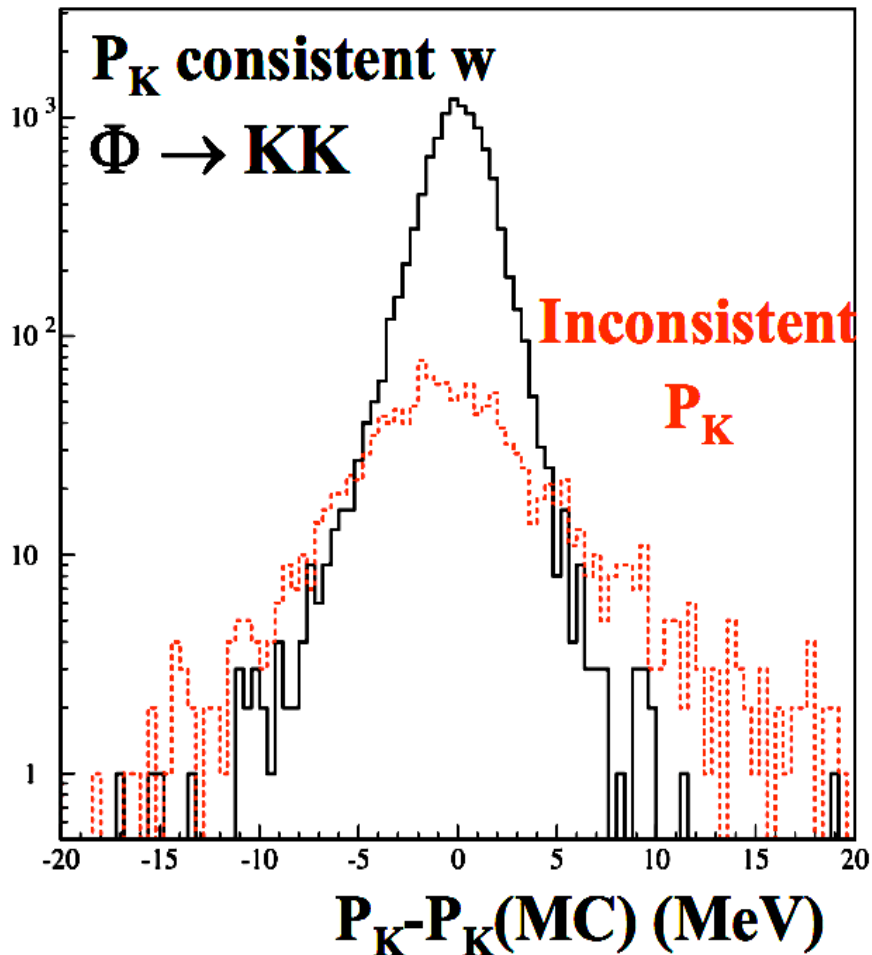
$$M_{lep}^2 = (E_K - p_{miss})^2 - p_{lep}^2$$

around $M_{lep}^2 = 0$ we
get $S/B = 10^{-3}$



Background rejection (track quality)

Bkg composition: $K_{\mu 2}$ events with bad p_K , p_{lep} reconstruction



- quality cuts for K: exploit $\phi \rightarrow KK$ 2-body kinematics
- require good quality vertex and secondary track (χ^2 cut)
- reduce $K_{\mu 2}$ tails cutting on the expected error on M_{lep}^2 (from track parameters)

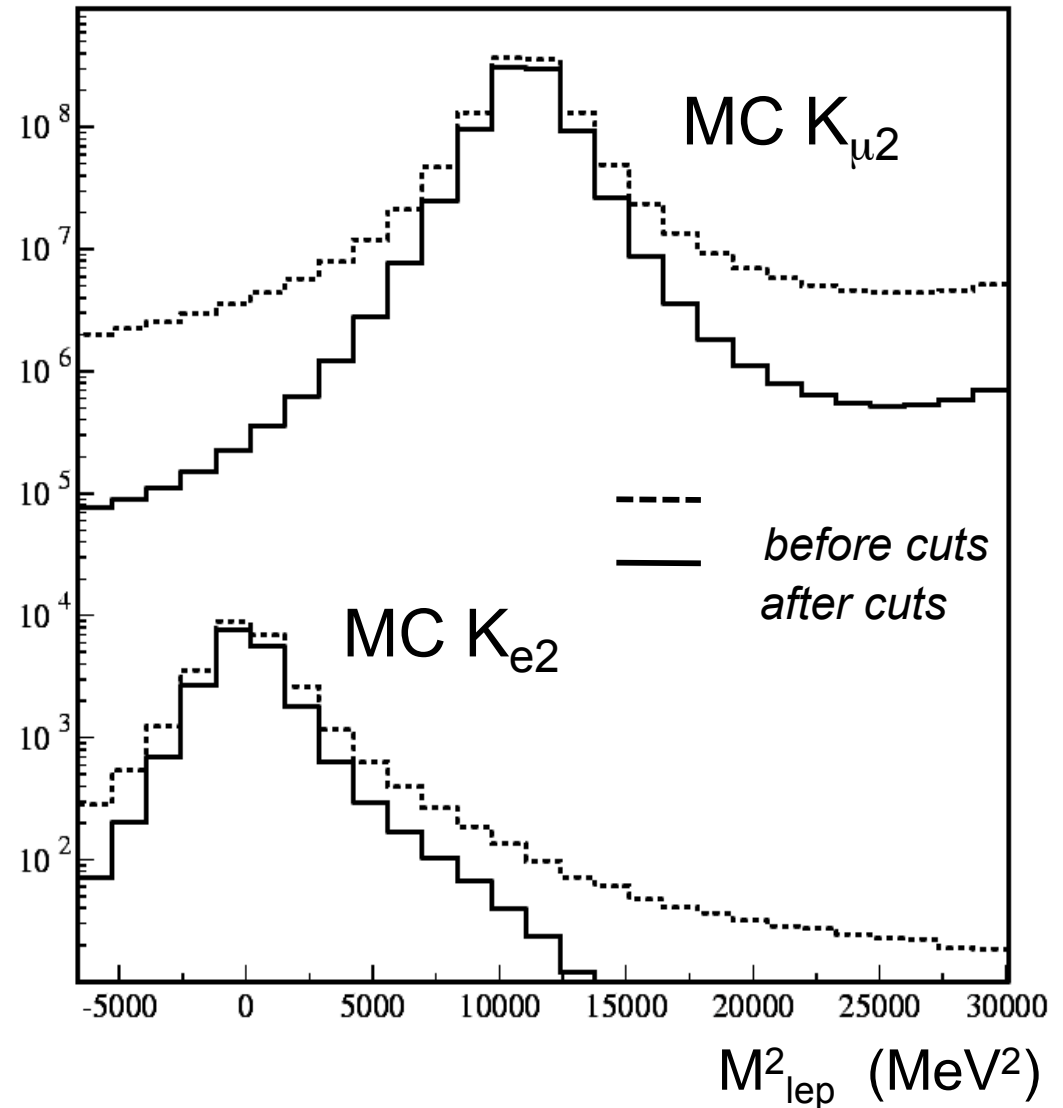
Background rejection (track quality)

after cuts, we accept
 $\approx 35\%$ of decays in the
FV

most of Ke2 events lost have
bad resolution

$$S/B = 1/20$$

not enough!

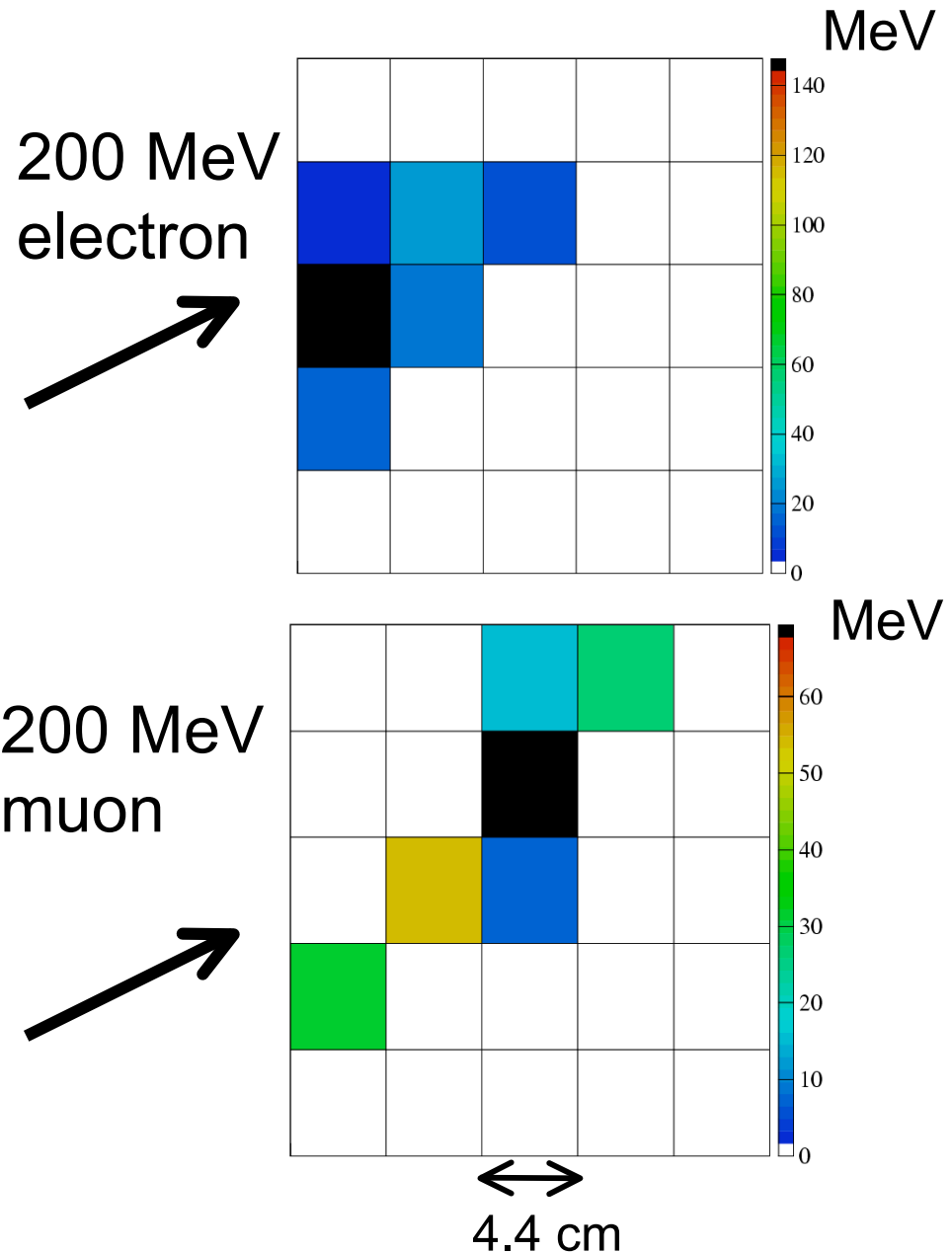


Background rejection (PID)

1) Particle ID exploits EMC granularity: energy deposits into 5 layers in depth

- cluster depth
- RMS of plane energies
- asymmetry of first (last) two energy releases
- skewness of cell-depth distribution
- E1, Emax, Nmax
- $\Delta E/\Delta x$

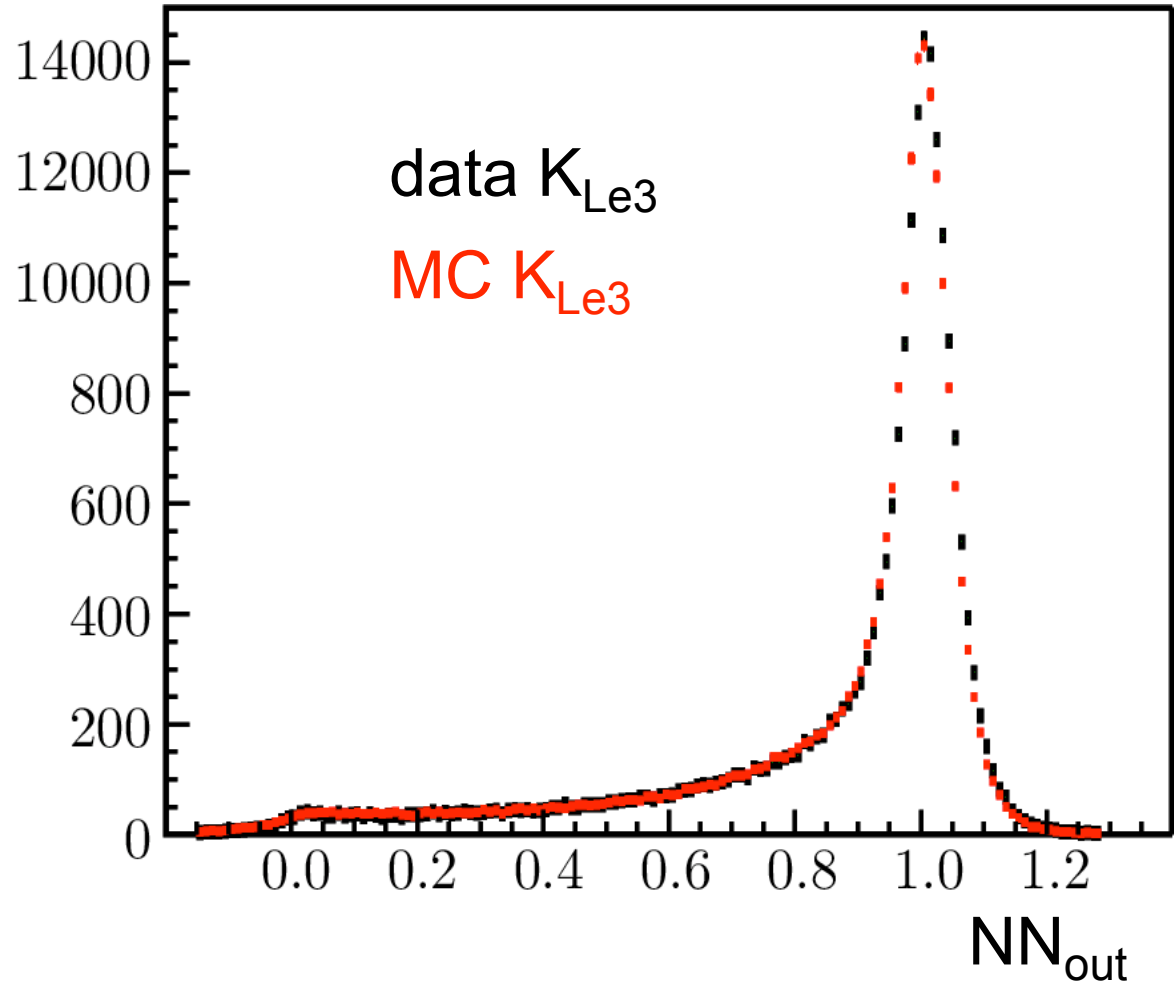
2) Add E/P and TOF



Background rejection (PID)

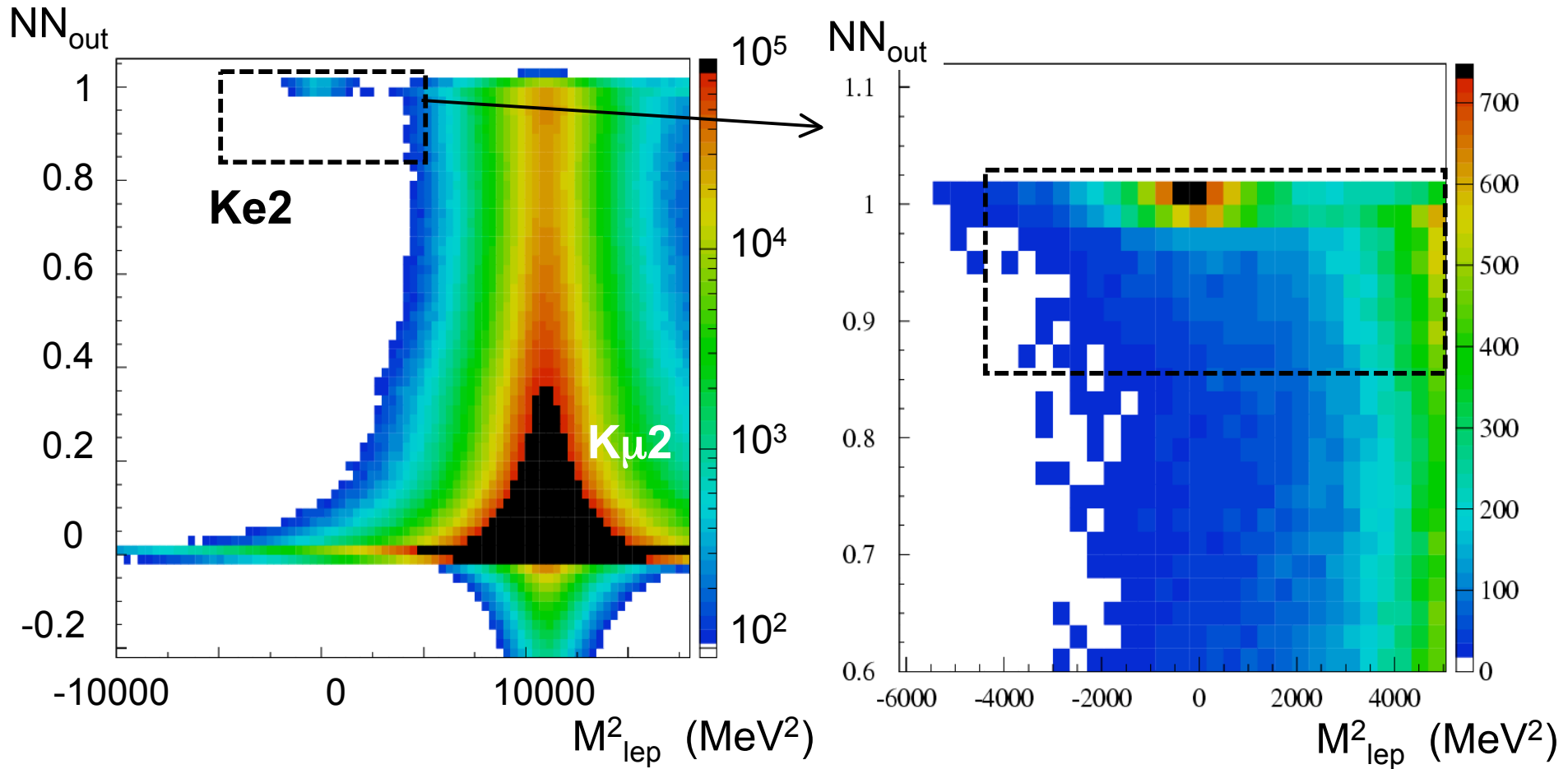
Combine PID variables
using a NN

Use a pure sample of
 K_{Le3} to correct cell
response in MC and
for NN training



Background rejection (PID)

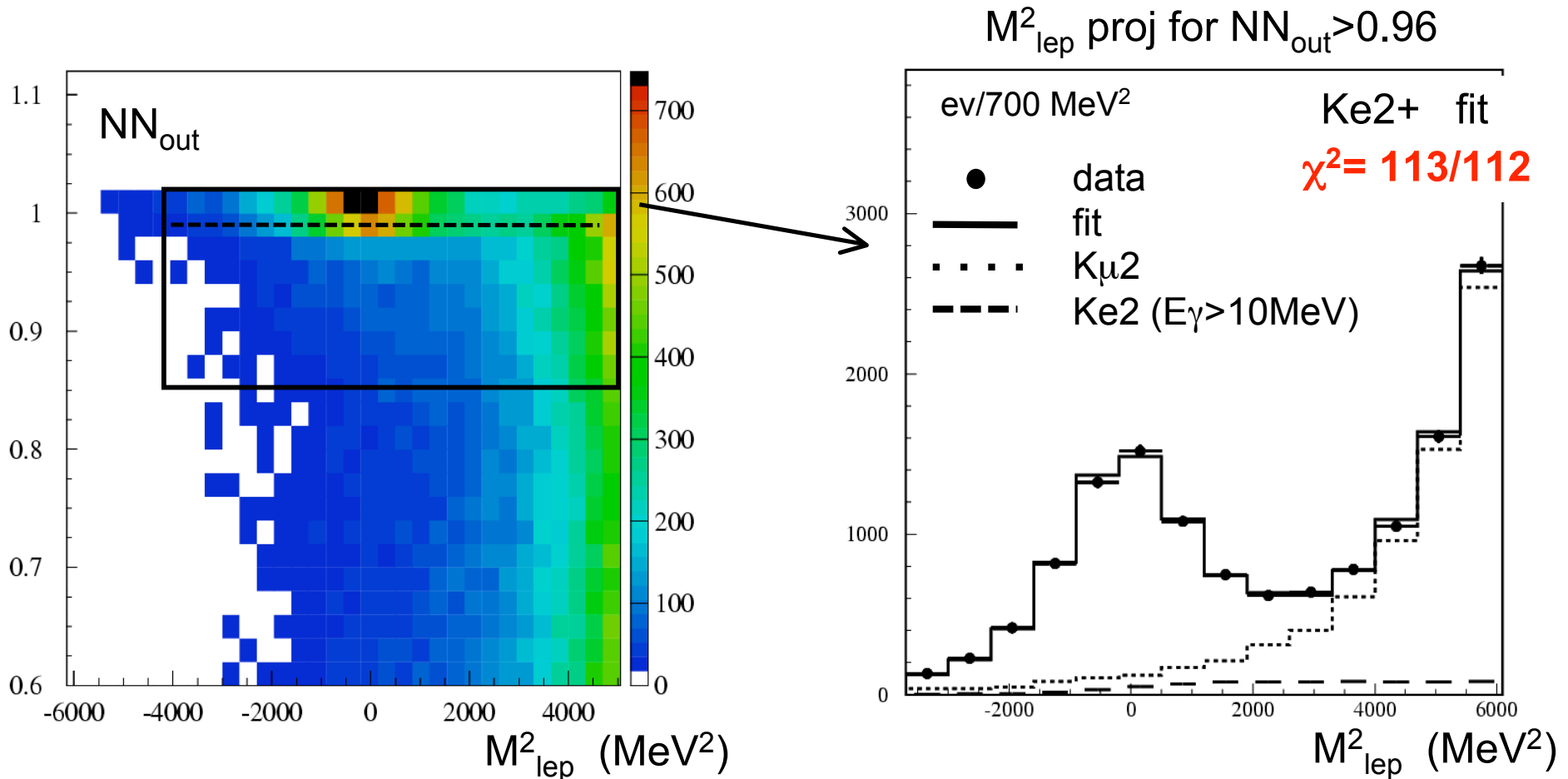
Select a region with good S/B ratio in the $M_{\text{lep}}^2 - \text{NN}_{\text{out}}$ plane



after selection: $\varepsilon = 30\%$ ($\approx 15\text{k } K_{e2}$) $S/B \approx 5$

K_{e2} event counting

Two-dimensional binned likelihood fit in the $M_{lep}^2 - NN_{out}$ plane in the region $-4000 < M_{lep}^2 < 6100$ and $0.86 < NN_{out} < 1.02$

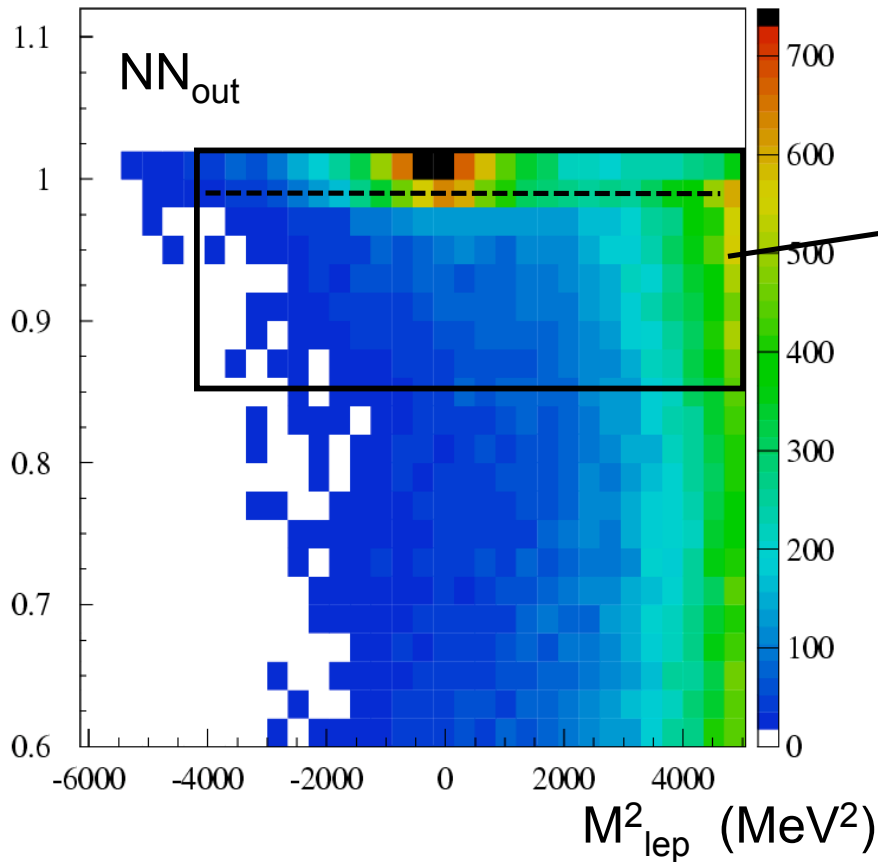


we count **7060 (102) Ke2+** **6750 (101) Ke2-** $\sigma_{stat} = 1\%$

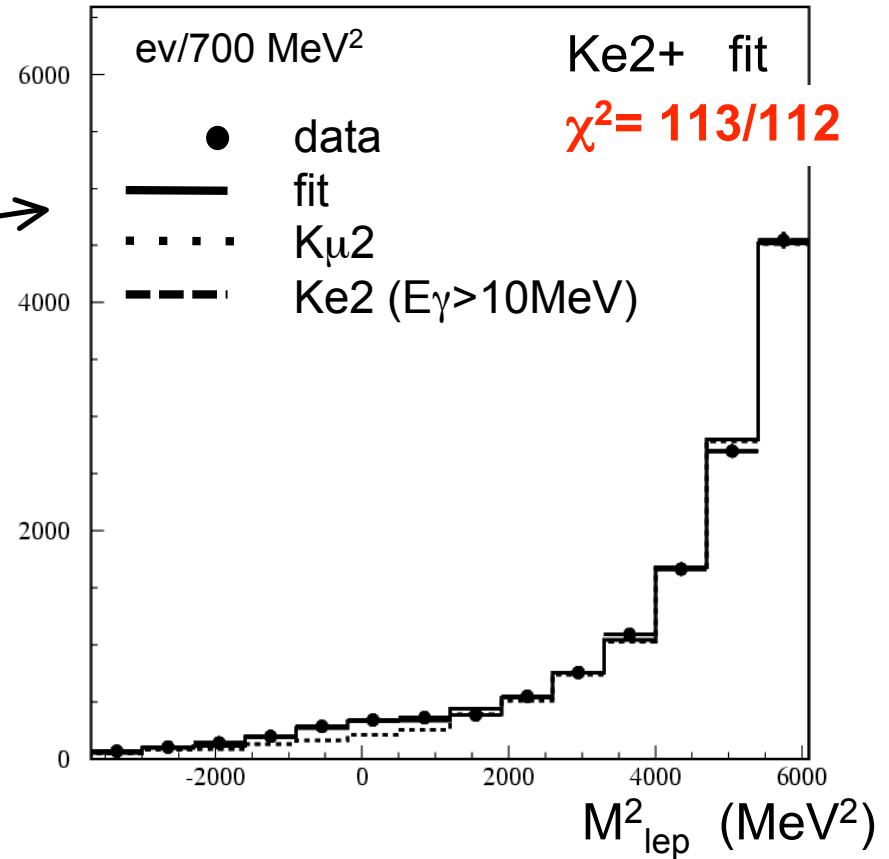
0.85% from Ke2

K_{e2} event counting

Two-dimensional binned likelihood fit in the $M_{lep}^2 - NN_{out}$ plane in the region $-4000 < M_{lep}^2 < 6100$ and $0.86 < NN_{out} < 1.02$



M_{lep}^2 proj for $NN_{out} < 0.96$



we count **7060 (102) Ke2+**

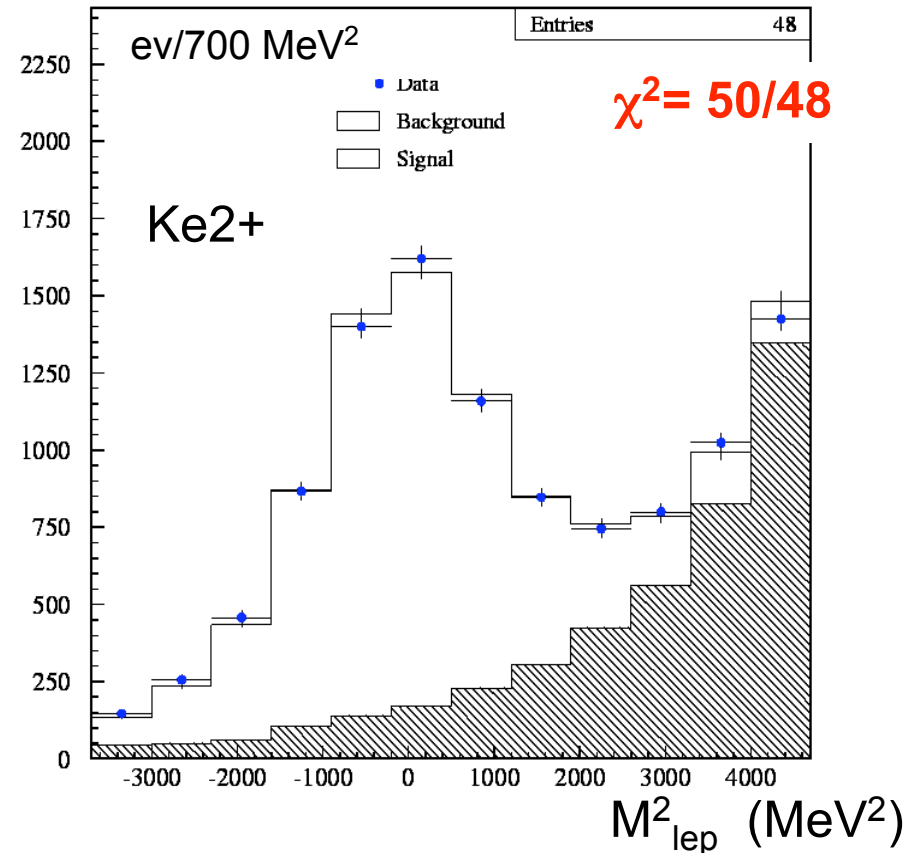
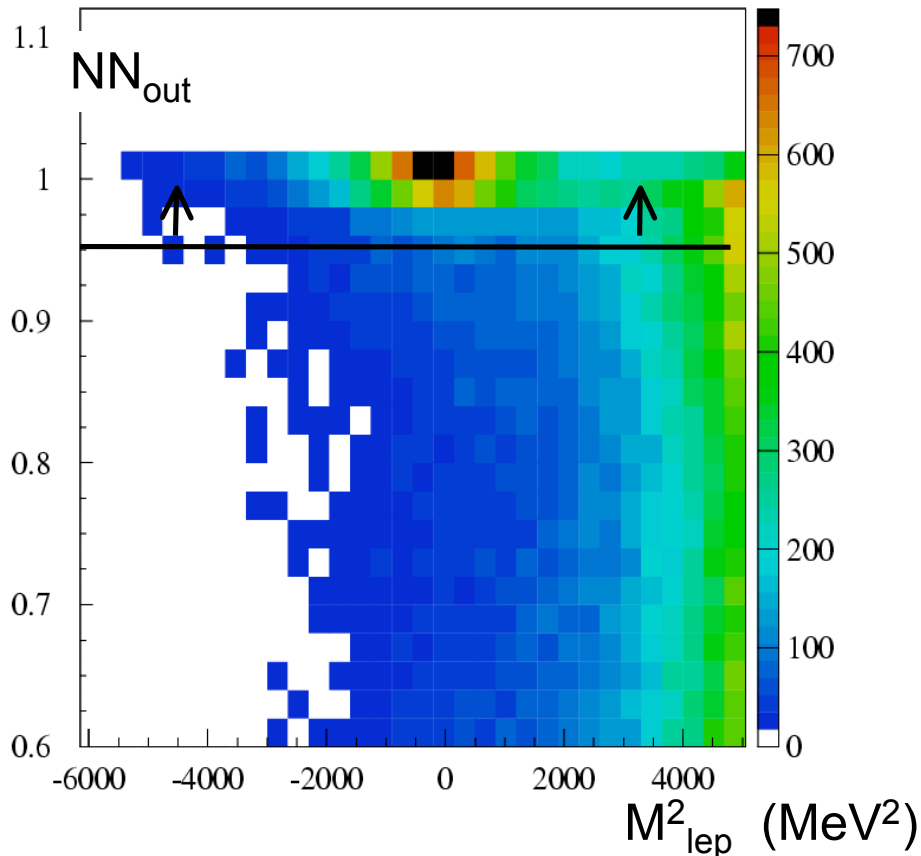
6750 (101) Ke2-

$\sigma_{stat} = 1\%$

0.85% from Ke2

K_{e2} event counting: systematics

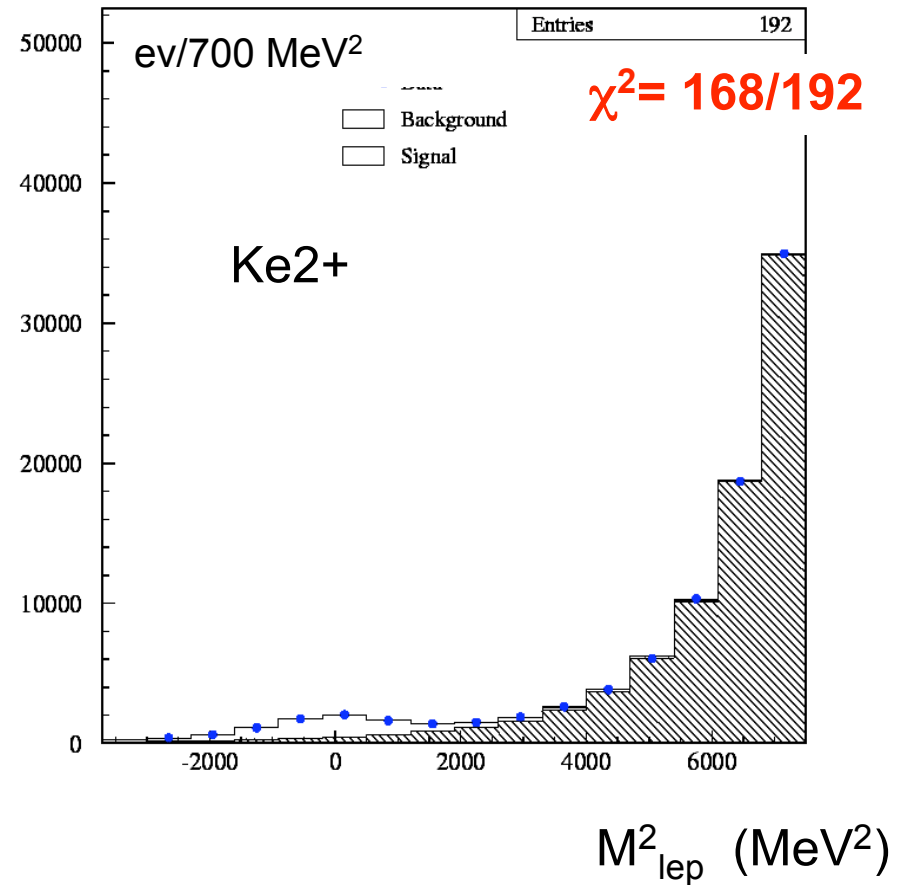
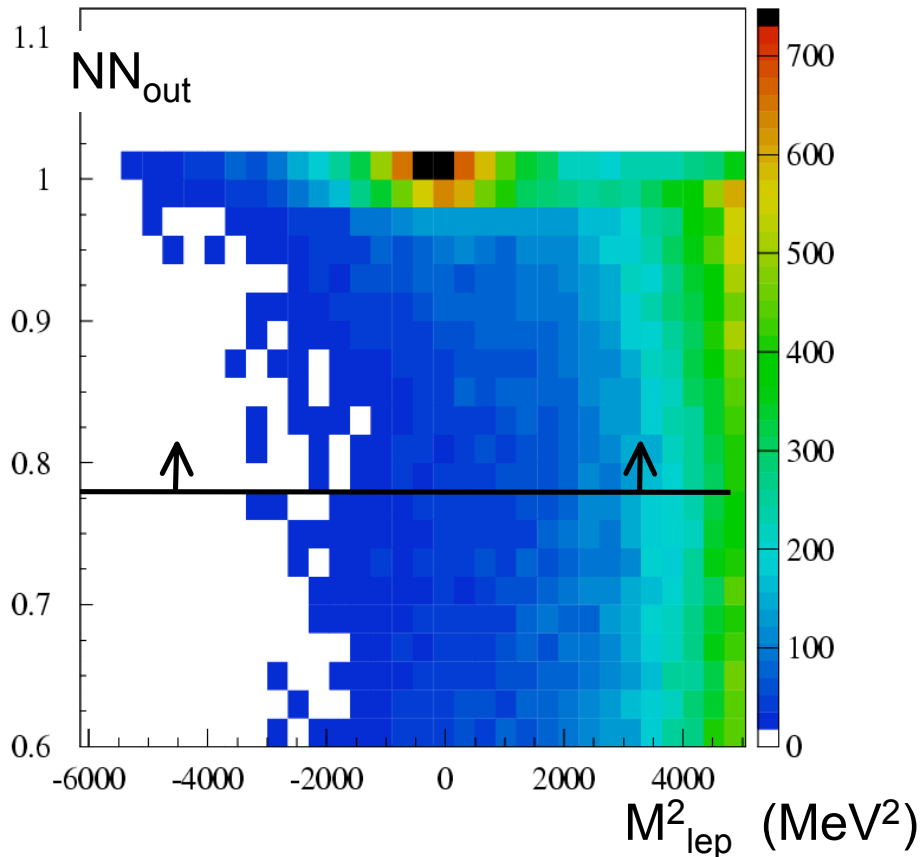
Repeat fit with different values of $\max(M_{lep}^2)$ and $\min(NN_{out})$: vary significantly ($\times 20$) bkg contamination + lever arm



min bkg with: $-4000 < M_{lep}^2 < 4650$ and $0.94 < NN_{out} < 1.02$

K_{e2} event counting: systematics

Repeat fit varying $\min(NN_{out})$ and $\max(M_{lep}^2)$: vary significantly ($\times 20$)
bkg contamination + lever arm



max bkg with: $-4000 < M_{lep}^2 < 7500$ and $0.78 < NN_{out} < 1.02$

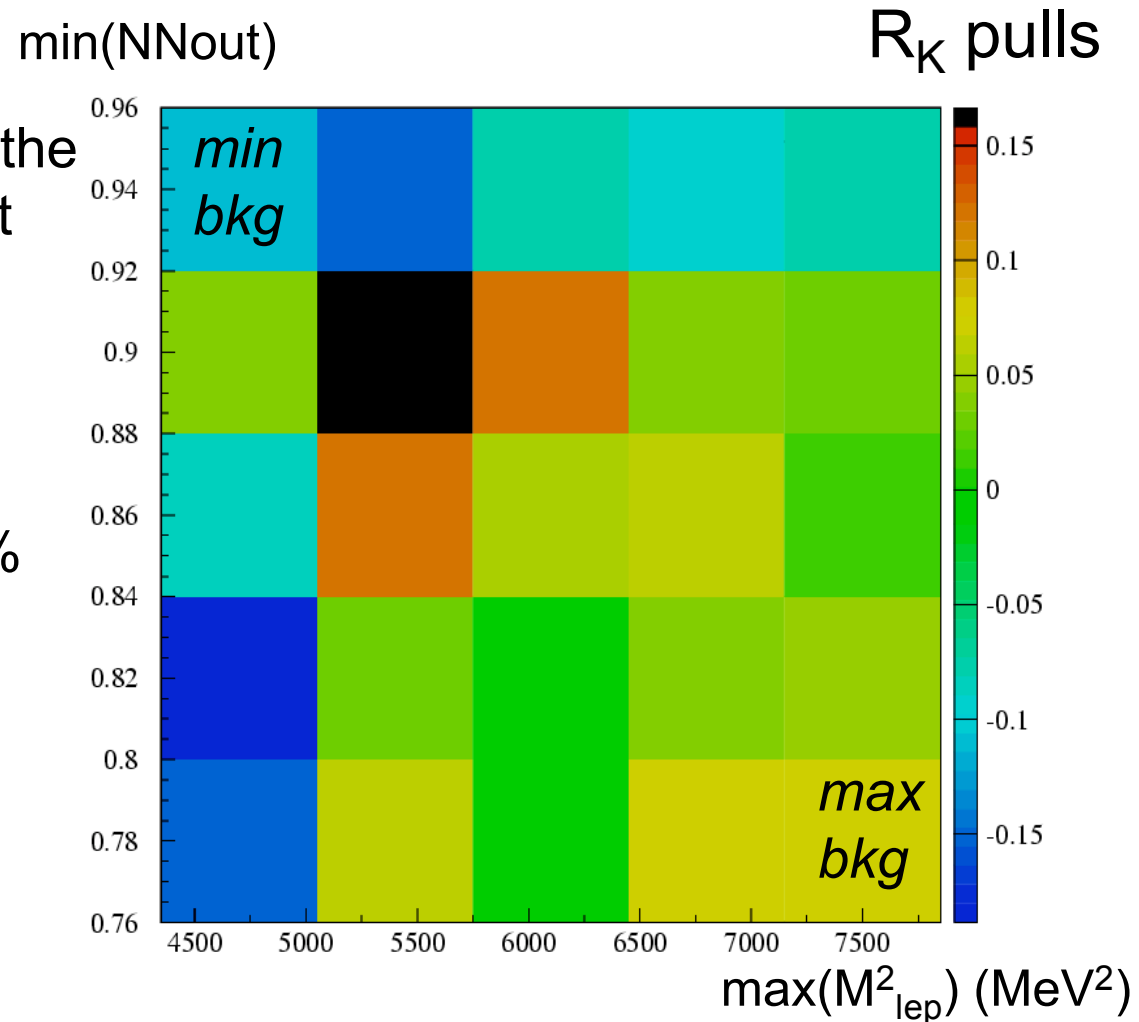
K_{e2} event counting: systematics

We change by a factor of 20 the amount of bkg falling in the fit region by moving

- min(NNout)
- max(M^2_{lep})

Signal counts change by 15%

From the pulls of the R_K measurement we evaluate a 0.3% systematic error



Ke2 fit: radiative corrections

The analysis above is inclusive of photons in the final state

- in our fit region we expect

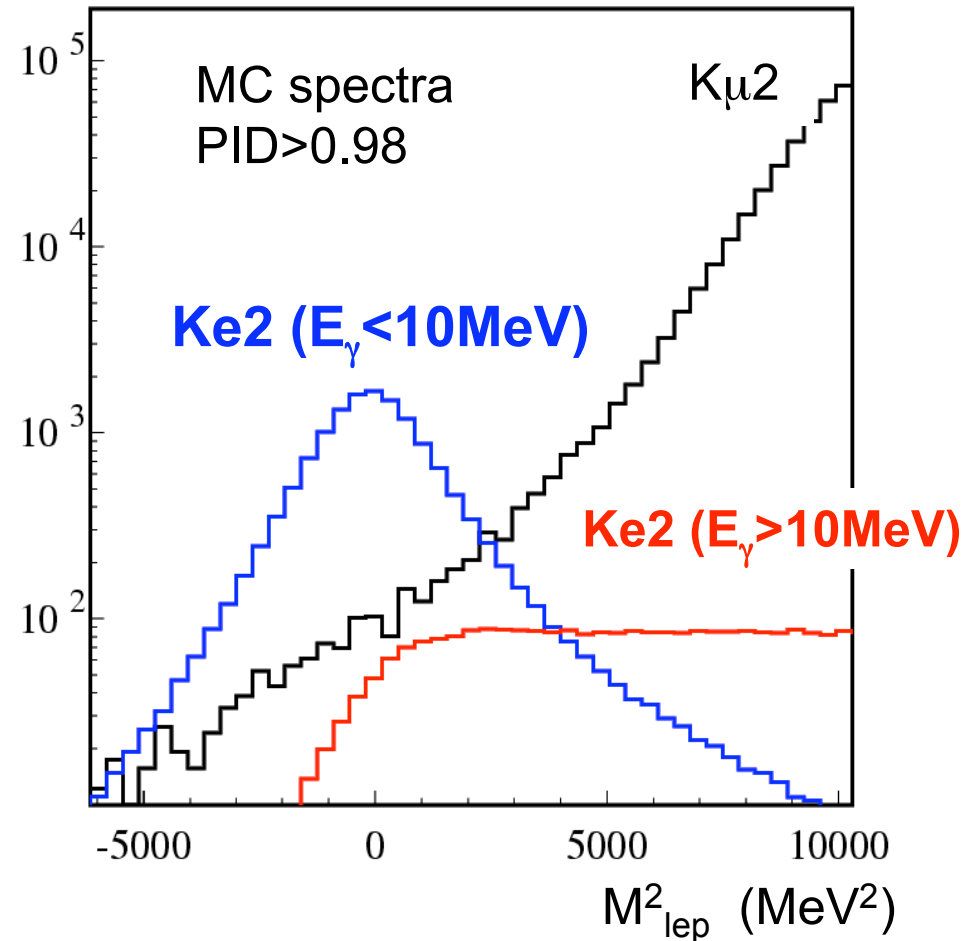
$$\frac{\text{Ke2 } (E_\gamma > 10\text{MeV})}{\text{Ke2}(E_\gamma < 10\text{MeV})} \approx 10\%$$

- repeat fit by varying

$$\text{Ke2 } (E_\gamma > 10\text{MeV})$$

by 15% (SD uncertainty):
get **0.5%** error...**too large**

- Need a dedicated study of the **Ke2 ($E_\gamma > 10\text{MeV}$)** component



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Ke2 γ process

Dalitz density

$$\frac{d\Gamma(K \rightarrow e\nu\gamma)}{dxdy} = \rho_{IB}(x,y) + \rho_{SD}(x,y) + \rho_{INT}(x,y)$$

helicity suppressed *negligible*

$$x = 2E_\gamma/M_K \quad y = 2E_e/M_K$$

E_γ, E_e in the K rest frame

Structure Dependent

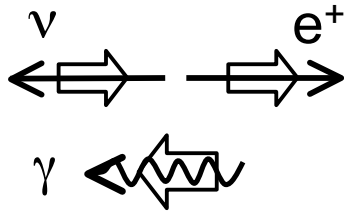
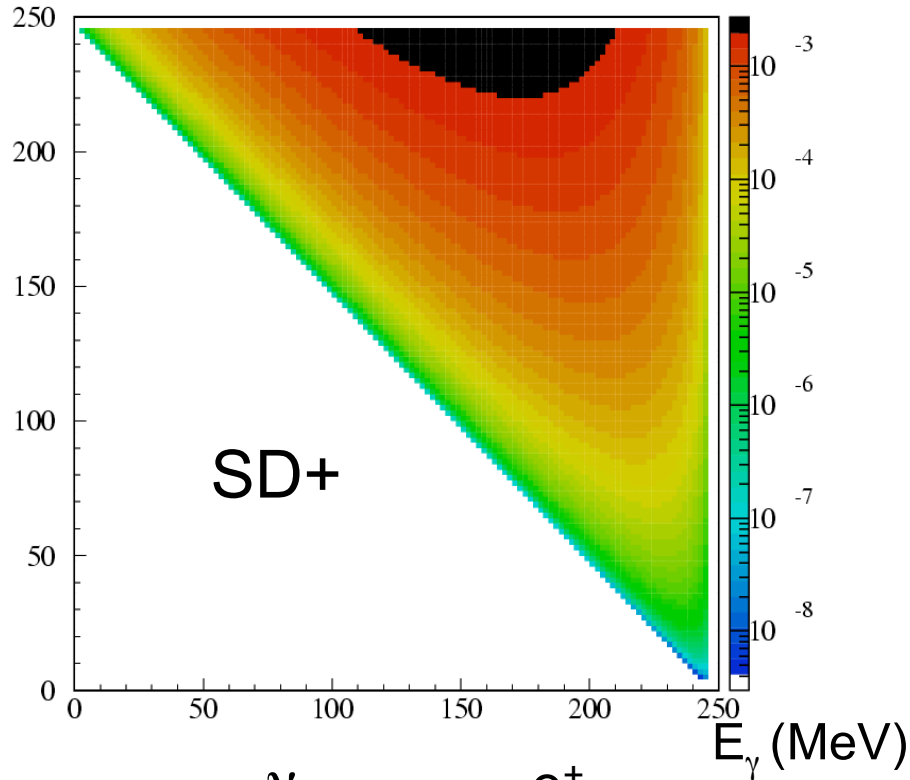
$$\rho_{SD}(x,y) = \frac{G_F^2 |V_{us}|^2 \alpha}{64\pi^2} M_K^5 \left((f_V + f_A)^2 f_{SD+}(x,y) + (f_V - f_A)^2 f_{SD-}(x,y) \right)$$

f_V, f_A : effective vector
and axial couplings

SD+ = V+A : γ polarization +
SD- = V-A : γ polarization -

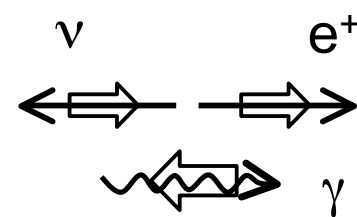
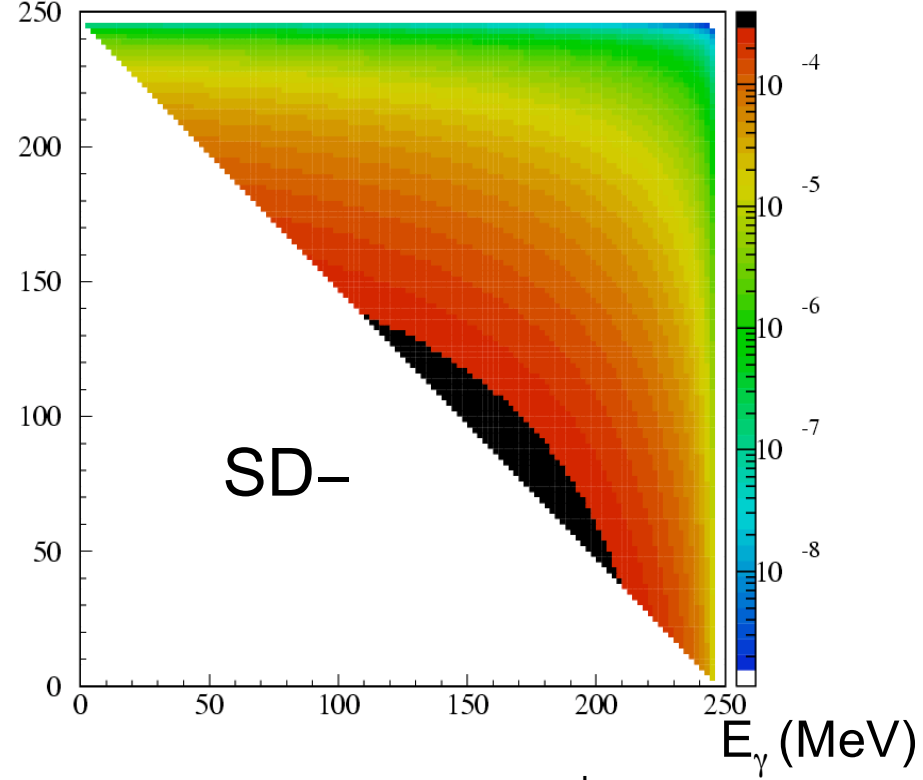
Dalitz plots for SD+ and SD-

p_e (MeV)



electron peaks at 250 MeV,
e- γ antiparallel

p_e (MeV)



electron peaks at 100 MeV: **very bad**, since Ke3 endpoint is 230 MeV

Ke2 γ : theory predictions

1) ChPT at O(p⁴):

$$f_V \approx 0.0945$$

$$f_A \approx 0.0425$$

no dependence on photon energy

Bijnens, Ecker, Gasser 93

2) ChPT at O(p⁶):

$$f_V \approx 0.082(1+\lambda(1-x))$$

$$f_A \approx 0.034$$

V linear x dependence ($\lambda \approx 0.4$)

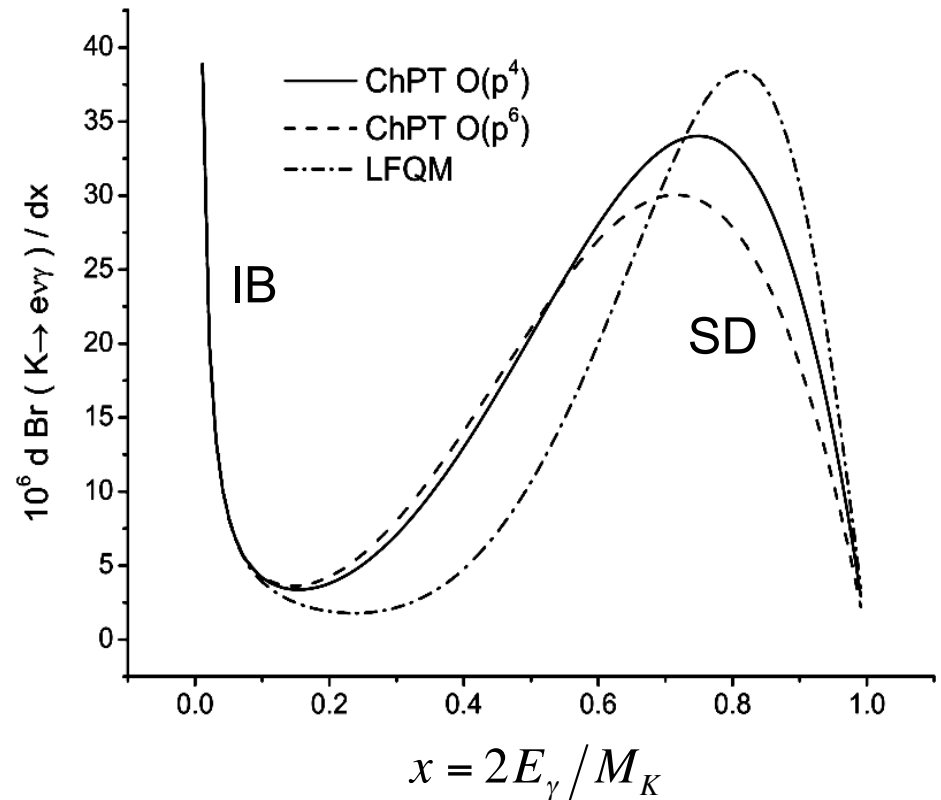
Ametller, Bijnens, Bramon, Cornet 93
Geng, Ho, Wu 04
Chen, Geng, Lih 08

3) LFQM:

non trivial x dependence

$$f_V = f_A = 0 \quad \text{at } x=0$$

Chen, Geng, Lih 08

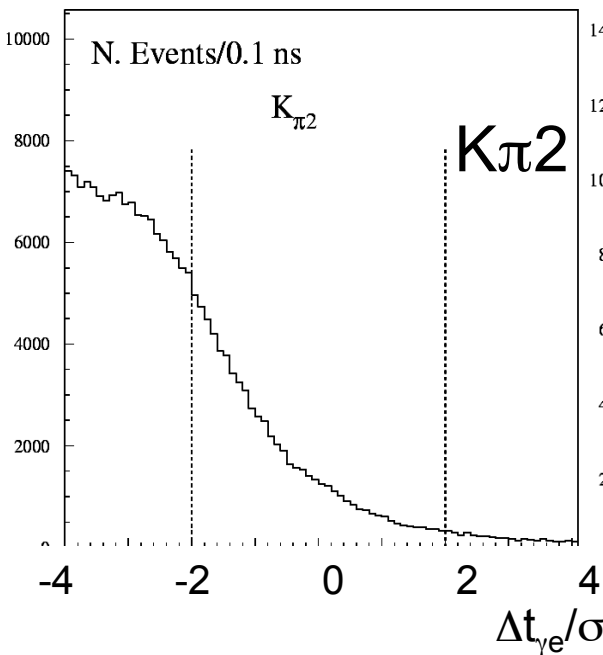


Ke2 γ selection: photon detection

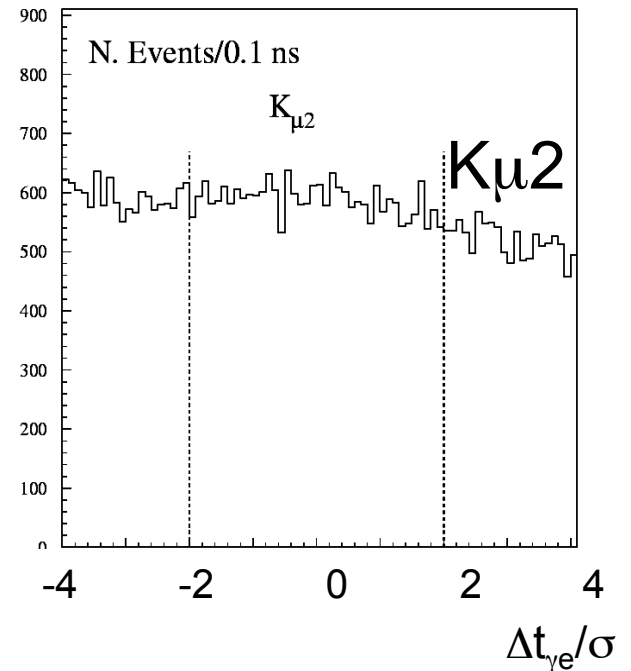
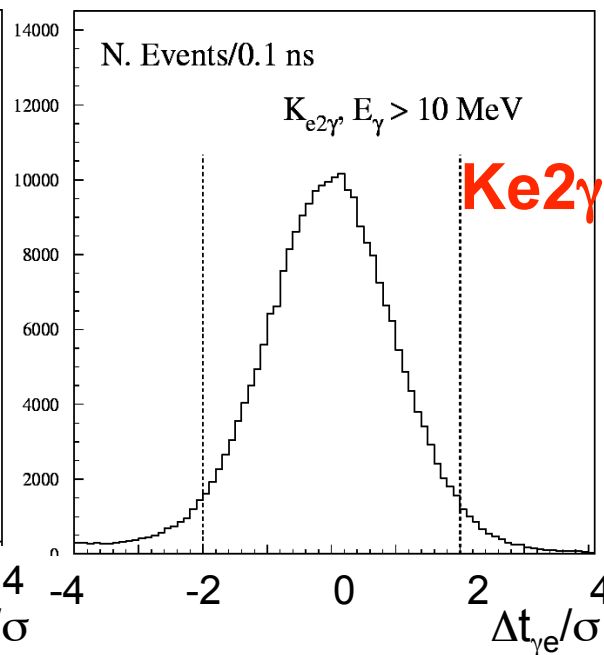
- A photon is required with energy $E_\gamma^{\text{calo}} > 20$ MeV to reject bkg (we loose Ke2_{IB}, too)
- Time of arrival compatible with that of the event (electron):

$$\Delta t_{\gamma e} = (t_\gamma - r_\gamma/c) - (t_e - r_e/c) < 2\sigma$$

(r = distance from K decay vtx)



γ from π^0
 $\beta(\pi^+) \approx 0.8$ instead of 1



Fake γ from accidental bkg

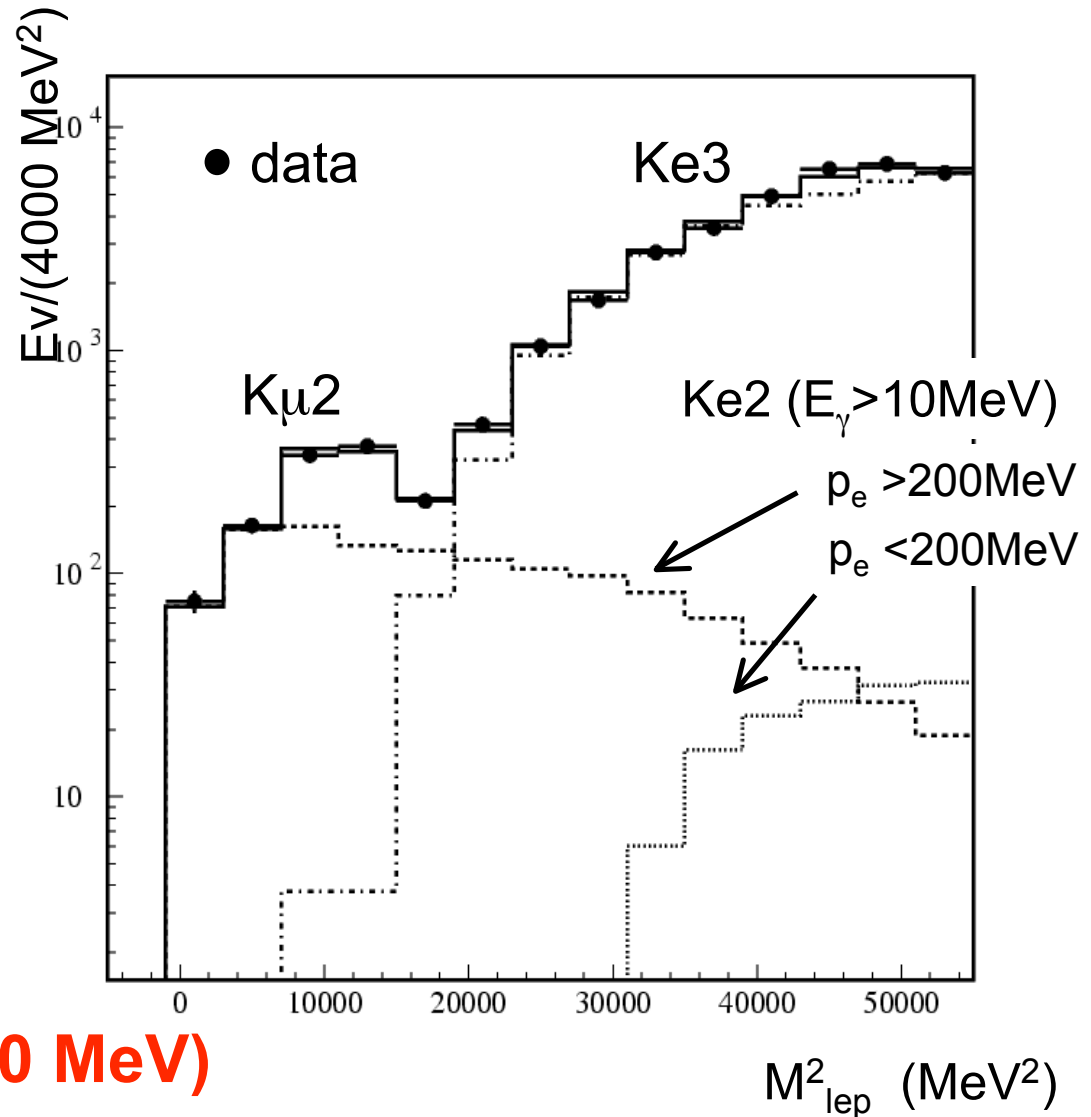
Ke2 γ selection

After photon detection bkg is dominated by

- K μ 2 in the low M^2_{lep} region
- Ke3 for $M^2_{lep} > 20000$

No sensitivity for Ke2 γ with $p_e < 200$ MeV (SD- amplitude)

We measure Ke2 γ ($E_\gamma > 10$ MeV, $p_e < 200$ MeV) \rightarrow SD+ amplitude



Ke2 γ selection: photon matching

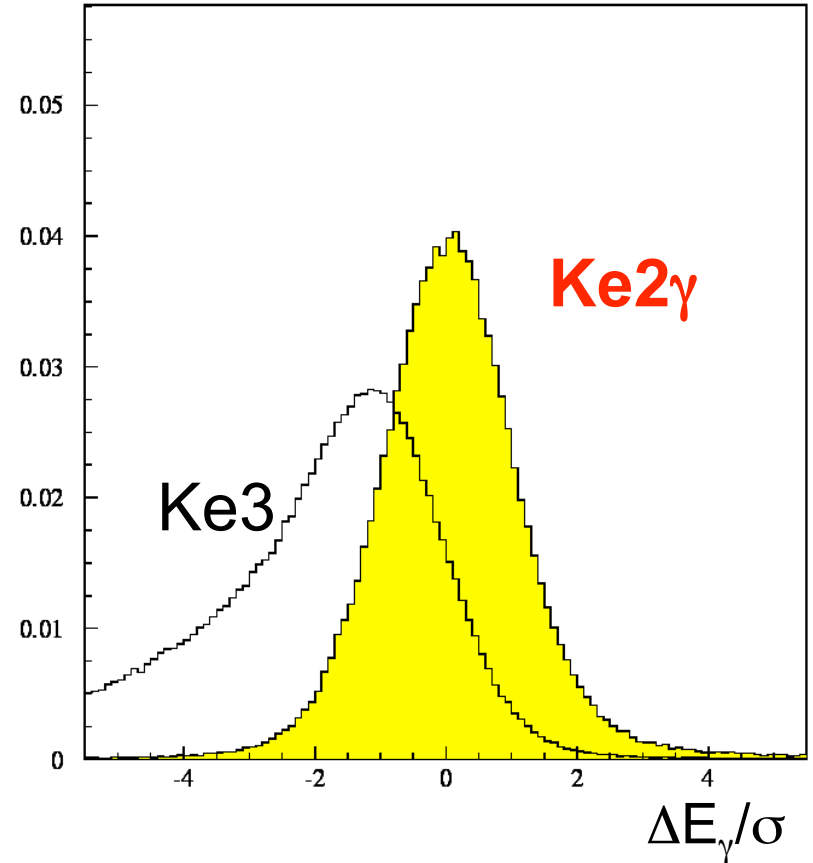
1) **best evaluation of E_γ^{lab}** from the kinematics of Ke2 γ , using measured p_K , p_e and photon direction n_γ

$$E_\gamma^{lab} = \frac{M_K^2 + m_e^2 - 2E_K E_e + 2\vec{p}_K \cdot \vec{p}_e}{2(E_K - E_e - \vec{p}_K \cdot \vec{n}_\gamma + \vec{p}_e \cdot \vec{n}_\gamma)}$$

➔ **12 MeV resolution**

($\sigma_{calo} \approx 30$ MeV)

2) $\Delta E_\gamma = E_\gamma^{lab} - E_\gamma^{calo}$ is also useful as a discriminating variable against background



Ke2 γ event counting

- Two-dimensional binned likelihood fit in the

$M^2_{lep} - \Delta E_\gamma/\sigma$ plane

5 bins of E_γ (from E_γ^{lab} pass in K rest frame):

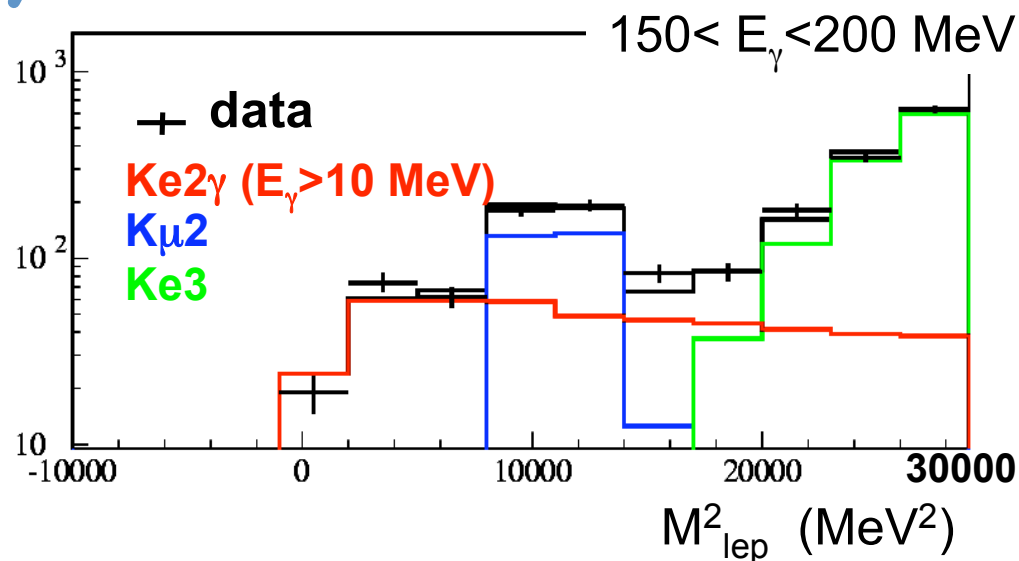
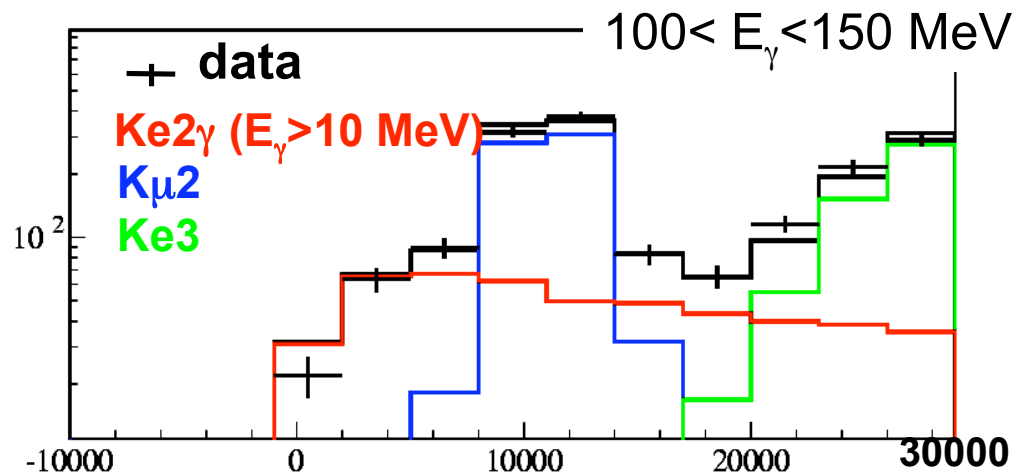
(10, 50) (50,100) (100,150)
(150,200) (200,250)

- Most populated bins

100 < E_γ < 150 MeV: $N = 463 \pm 32$
 $\chi^2 = 87/106$

150 < E_γ < 200 MeV: $N = 494 \pm 38$
 $\chi^2 = 100/106$

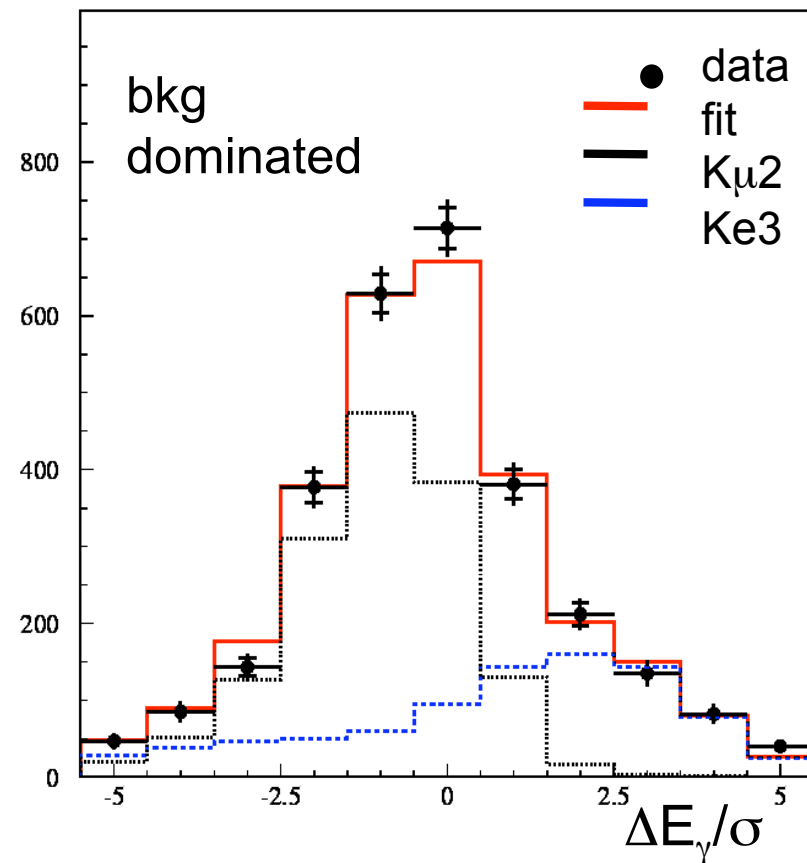
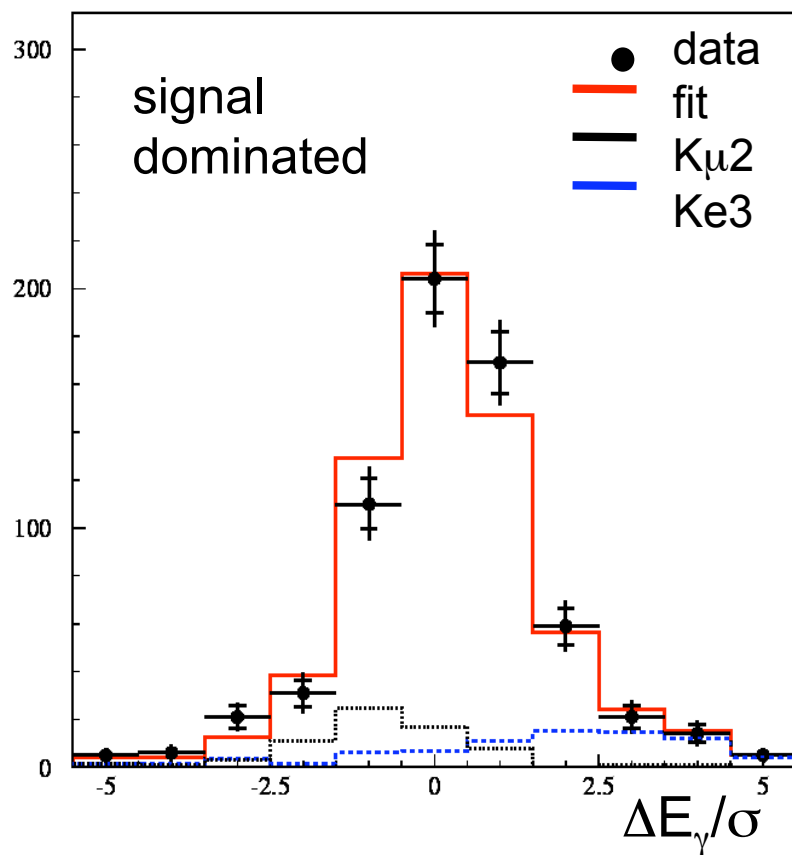
Fit projections on M^2_{lep} axis



Ke2 γ event counting

Fit projections on $\Delta E_\gamma/\sigma$ (all E_γ bins together)

according to M^2_{lep} , we show separately regions dominated by signal and bkg



In total, we count Ne2 γ = 1484 \pm 63

Ke2 γ spectrum vs ChPT O(p⁴)

We measure:

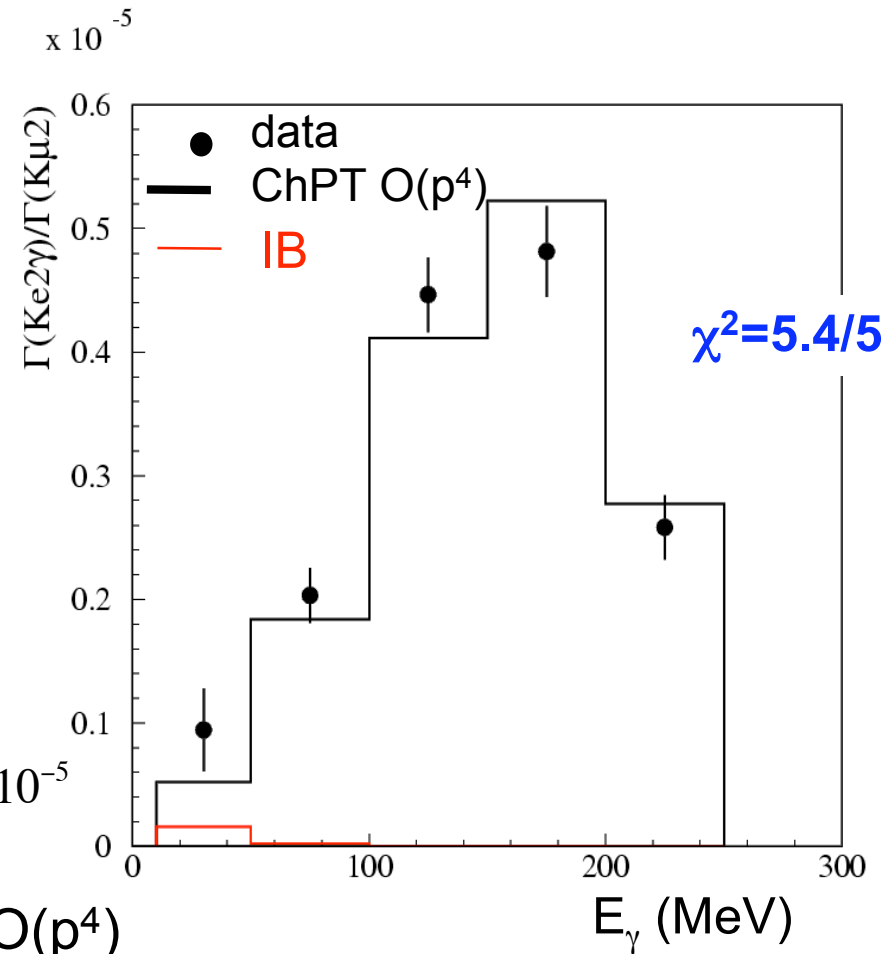
$$\frac{1}{\Gamma(K_{\mu 2})} \frac{d\Gamma(K_{e2}, E_\gamma > 10 \text{ MeV}, p_e^* > 200 \text{ MeV})}{dE_\gamma}$$

Data are **compared** with ChPT O(p⁴) calculation

Integrating we obtain:

$$\frac{\Gamma(K_{e2}, E_\gamma > 10 \text{ MeV}, p_e^* > 200 \text{ MeV})}{\Gamma(K_{\mu 2})} = 1.483(68) \times 10^{-5}$$

in agreement with 1.447×10^{-5} of ChPT O(p⁴)



This confirms the SD content of our MC, evaluated with ChPT O(p⁴), within an accuracy of 4.6% and allows a 0.2% systematic error on Ke2_{IB} to be assessed

Ke2 γ spectrum: fit to ChPT O(p⁶)

- We **fit** our data to extract **f_V+f_A** (SD+), allowing for a slope of the vector ff

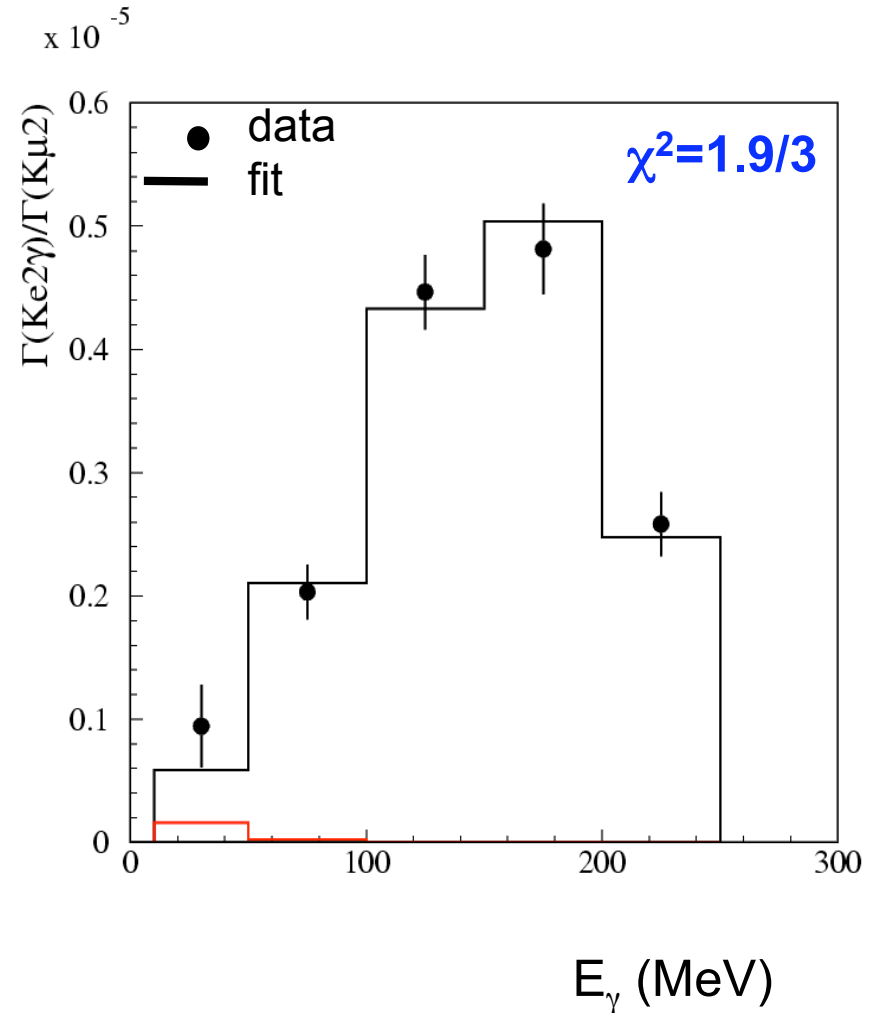
$$f_V = f_{V0} (1 + \lambda(1-x))$$

- Since we are not sensitive to the SD- amplitude (acceptance \approx 2%) we keep f_V-f_A fixed to the ChPT O(p⁶) prediction

We obtain:

$$f_{V0} + f_A = (0.125 \pm 0.007)$$

$$\lambda = 0.38 \pm 0.21$$

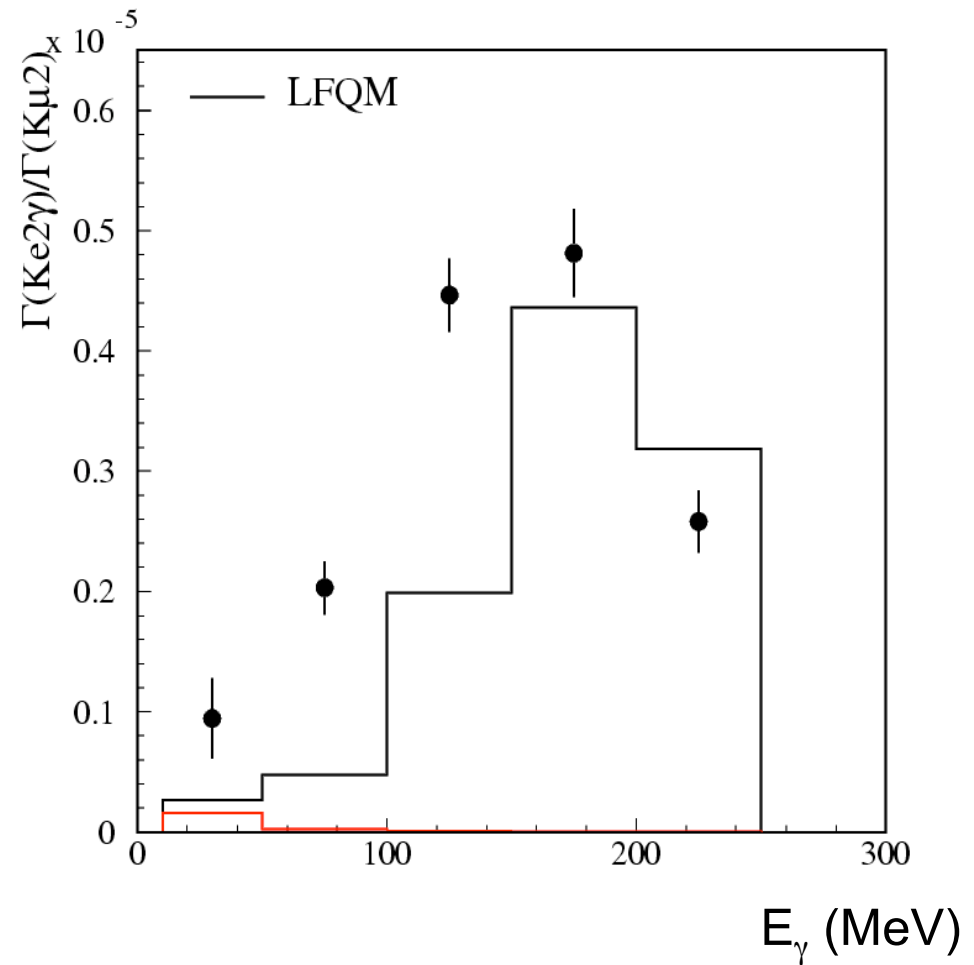


Compare to ChPT O(p⁶) : $f_{V0} + f_A \approx 0.116$, $\lambda \approx 0.4$

Phys. Rev. D77 (2008) 014004

Ke2 γ spectrum vs LFQM

The spectrum predicted by the Light Front Quark Model is excluded by our data, $\chi^2=127/5$



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- Study of direct emission in $K_{e2\gamma}$
- **Results on R_K**

Reconstruction efficiencies

We use MC, with corrections from data control samples

- 1) kink reconstruction (tracking):** K^+e3 and $K^+\mu2$ data control samples selected with tagging and additional criteria based on EMC info's only (next slide)
- 2) cluster efficiency (e, μ):** K_L control samples, selected with tagging and kinematic criteria based on DC info's only
- 3) trigger:** exploit the OR combination of EMC and DC triggers (almost uncorrelated); downscaled samples are used to measure efficiencies for cosmic-ray and machine background vetoes

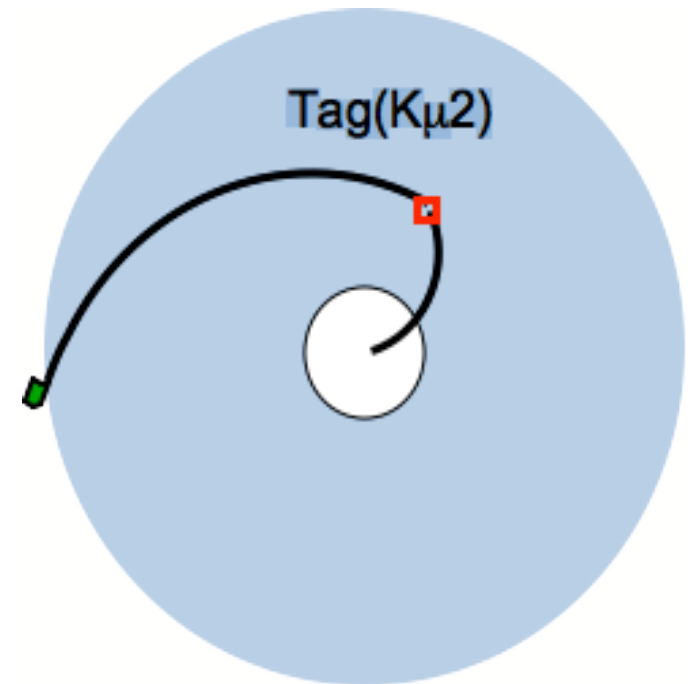
we obtain:

$$\varepsilon(K^+e2)/\varepsilon(K^+\mu2) = 0.946 \pm 0.007$$

Control samples for tracking efficiencies

Just an example: selection of K^+e3 control sample to measure tracking efficiency for electrons

0) **Tagging decay** ($K\mu2$ or $K\pi2$) coming from IP

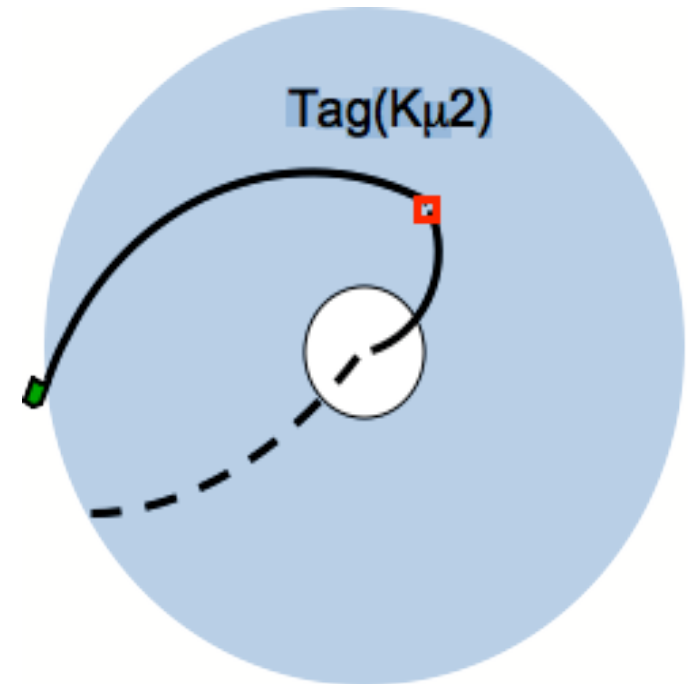


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1) Tagging decay ($K\mu2$ or $K\pi2$):
**reconstruction of the opposite
charge kaon flight path**



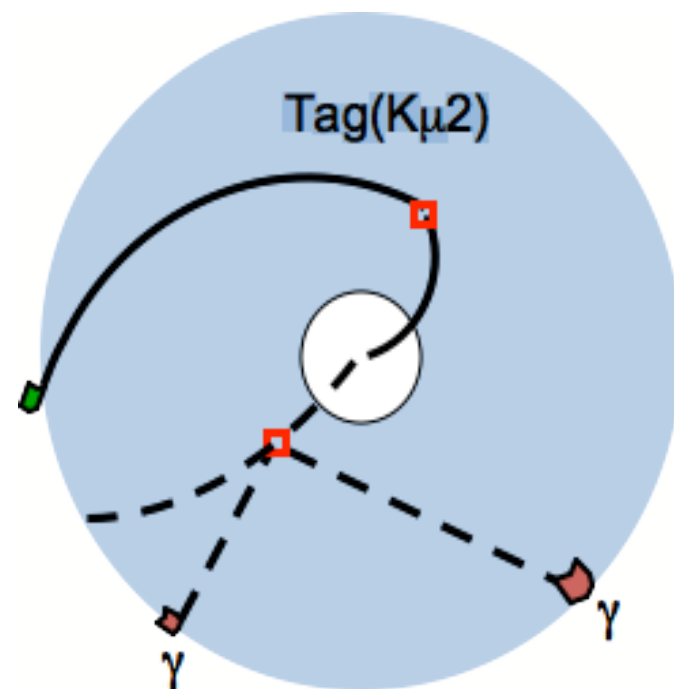
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2) A $\pi^0 \rightarrow \gamma\gamma$ decay vertex is reconstructed along the K decay path, using TOF



Control samples for tracking efficiencies

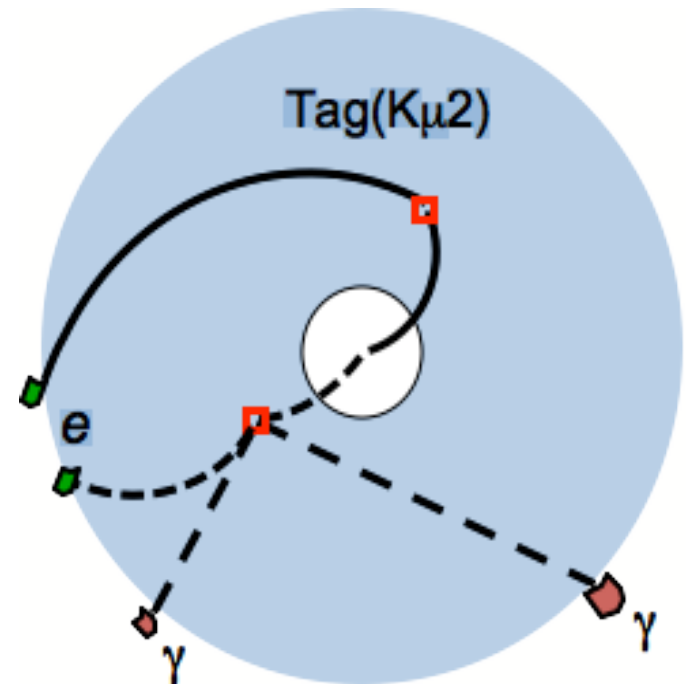
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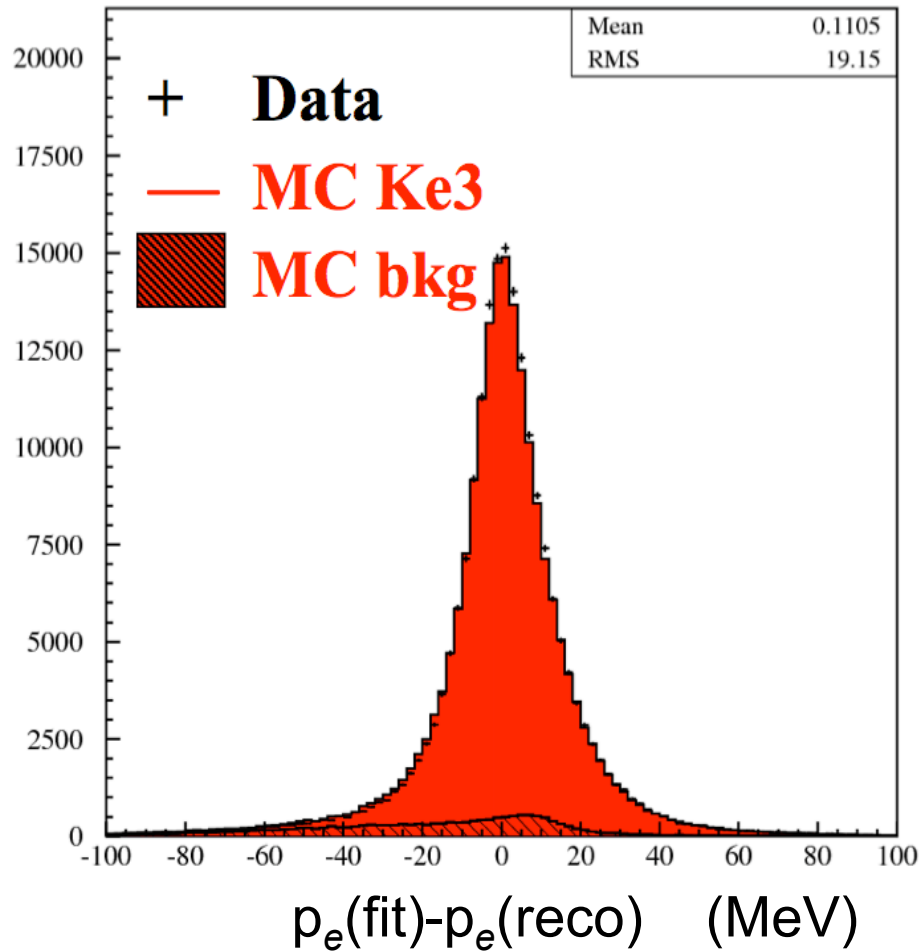
2) A $\pi^0 \rightarrow \gamma\gamma$ decay vertex is reconstructed along the K decay path, using TOF

3) **Electron cluster required; p_e estimated from a kinematic fit** with constraints on E/p , TOF, r_e and $E_{\text{miss}} - P_{\text{miss}}$

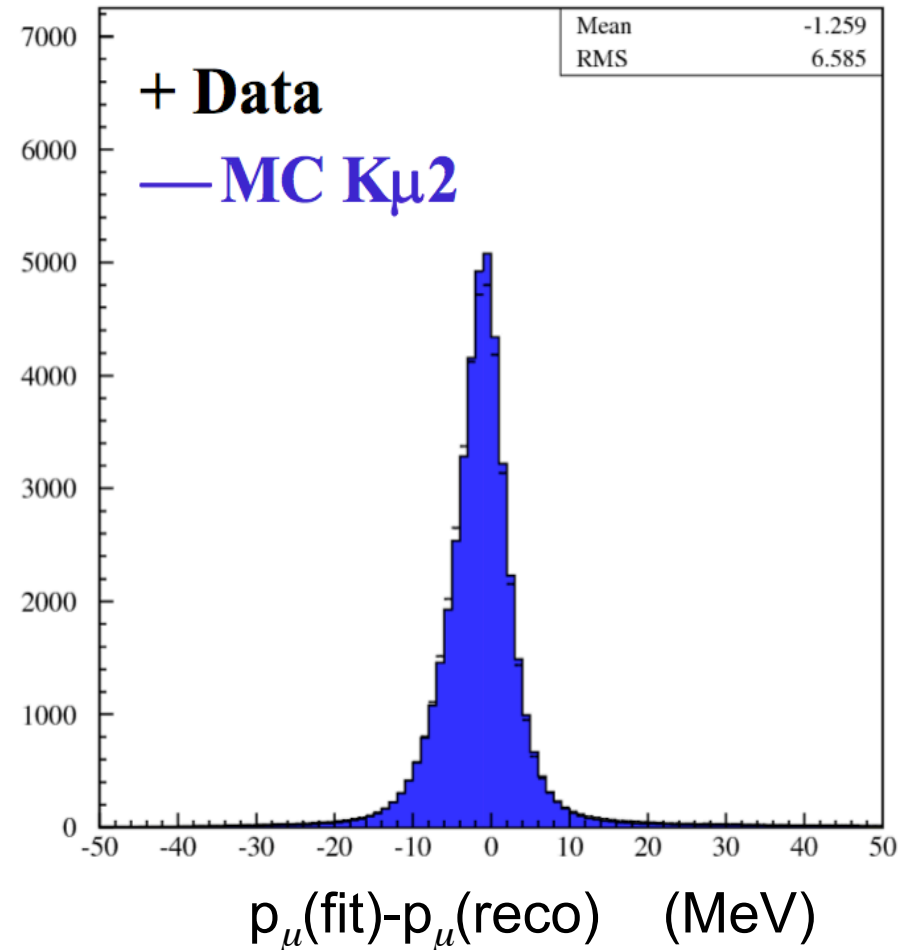


We evaluate the K + electron kink reconstruction efficiency

Control samples for tracking efficiencies



$\sigma \approx 19$ MeV



with a similar method, we get
 $\sigma \approx 7$ MeV for muon tracks

Systematics and checks

Cross-check on efficiencies: use same algorithms to measure $R_{l3} = \Gamma(\text{Ke}3)/\Gamma(\text{K}\mu3)$

$$R_{l3} = 1.507 \pm 0.005 \text{ for } \text{K}^+$$

$$R_{l3} = 1.510 \pm 0.006 \text{ for } \text{K}^-$$

SM expectation (FlaviaNet)

$$R_{l3} = 1.506 \pm 0.003$$

Summary of systematics:

Tracking	0.6%	K^+ control samples
Trigger	0.4%	downscaled events
syst on Ke2 counts	0.3%	fit stability
Ke2 γ SD component	0.2%	measurement on data
Clustering for e, μ	0.2%	K_L control samples

Total Syst

0.8%

0.6% from statistics of control samples

R_K : KLOE result

$$R_K = (2.493 \pm 0.025 \pm 0.019) \times 10^{-5}$$

Total error 1.3% = 1.0%_{stat} + 0.8%_{syst}

0.9% from 14k Ke2 + bkg subtraction **0.8%_{syst} dominated by statistics**

- The result does not depend upon the kaon charge:

$$K^+: 2.496(37) \quad \text{vs} \quad K^0: 2.490(38) \quad \text{uncorrelated errors only}$$

- Our measurement agrees with SM prediction,

$$R_K = 2.477(1) \times 10^{-5}$$

R_K : world average

PDG 2008:

$$R_K = (2.45 \pm 0.11) \times 10^{-5}$$

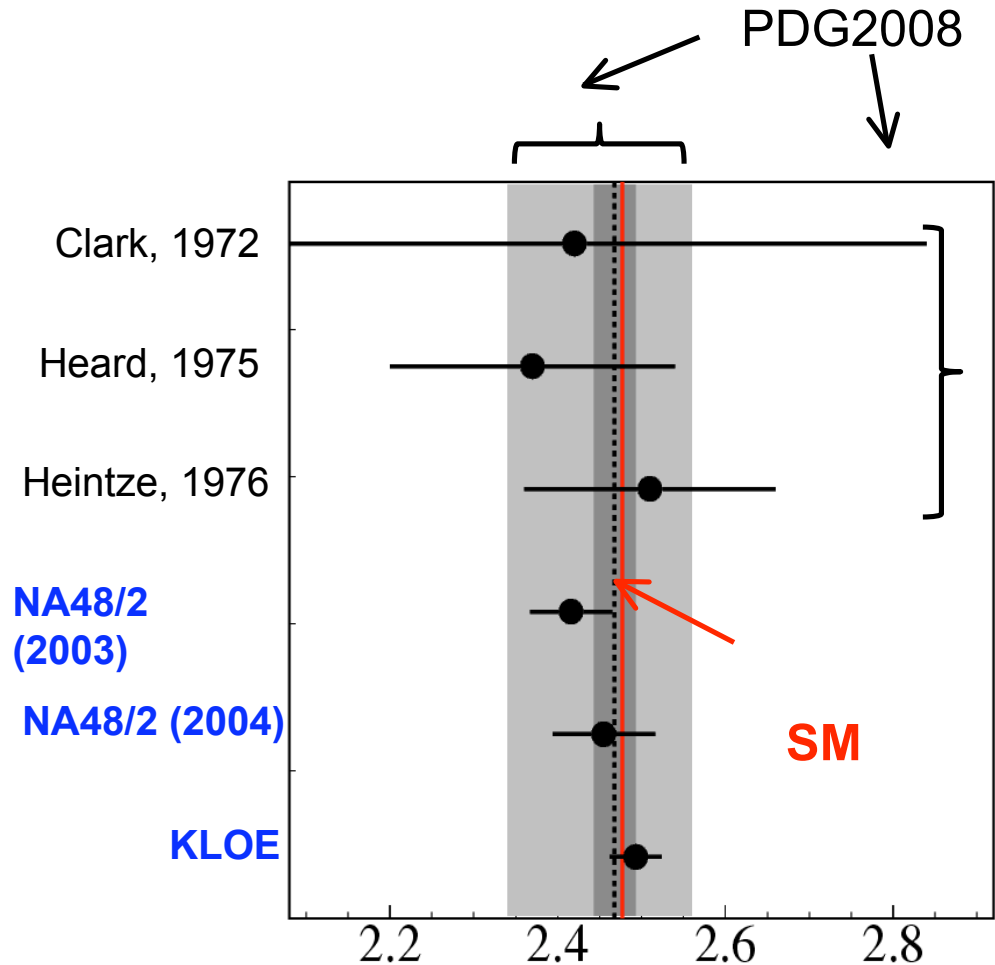
4.5% accuracy

New world average:

$$R_K = (2.468 \pm 0.025) \times 10^{-5}$$

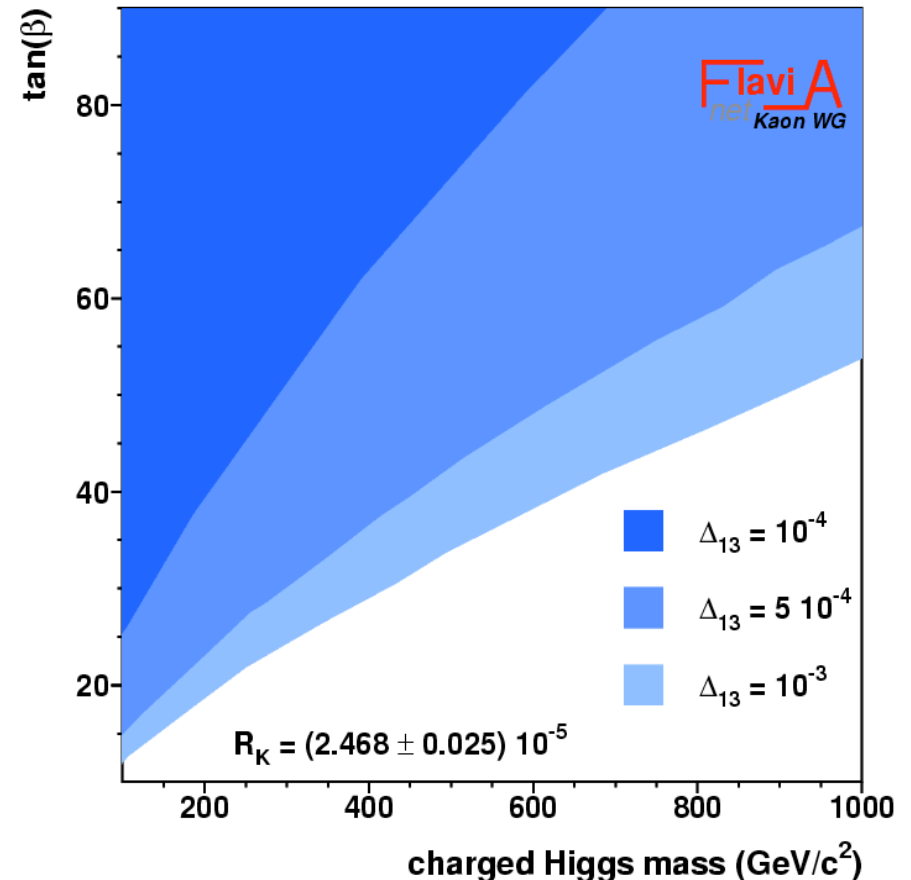
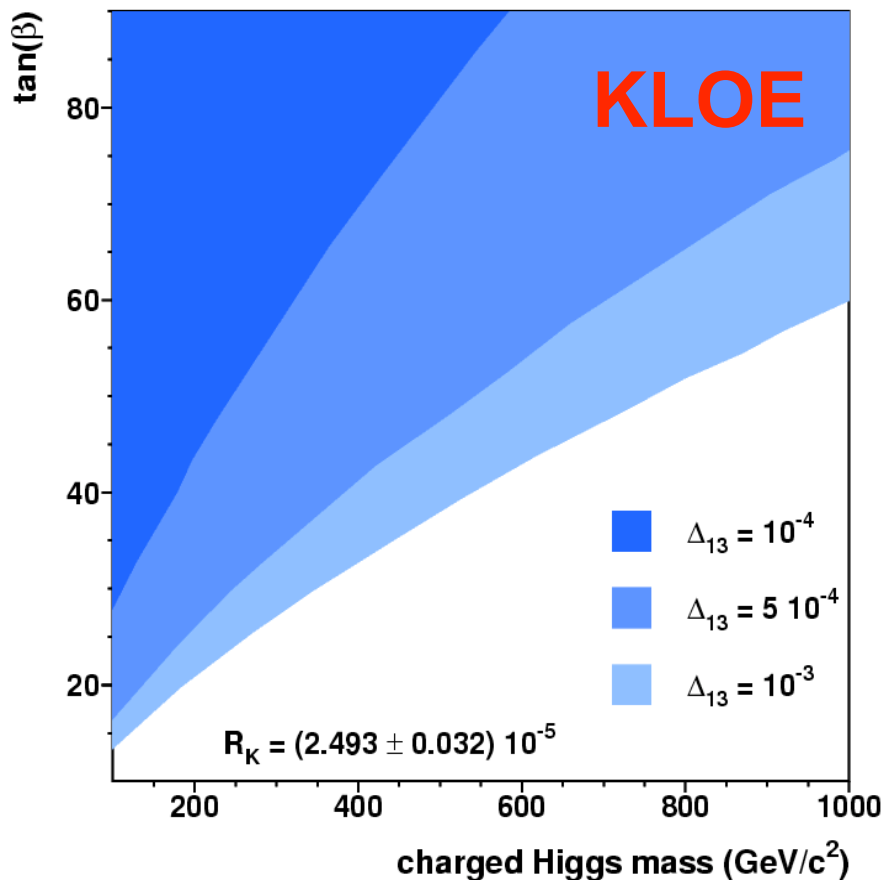
1% accuracy

$$R_K^{\text{SM}} = 2.477(1) \times 10^{-5}$$



R_K : sensitivity to new physics

Sensitivity shown as 95% CL excluded regions in the M_{H^\pm} - $\tan\beta$ plane, for different values of the LFV effective coupling, $\Delta_{13} = 10^{-3}, 5 \times 10^{-4}, 10^{-4}$



Conclusions

Using 2.2 fb^{-1} of data acquired at the ϕ peak, we measured

$$R_K = (2.493 \pm 0.025_{\text{stat}} \pm 0.019_{\text{syst}}) \times 10^{-5}$$

This result confirms the SM prediction within the 1.3% accuracy, and can be used to set constraints on the parameter space of the MSSM with lepton flavor violation

We also presented today the first measurement of the decay spectrum in a region dominated by SD

$$\frac{1}{\Gamma(K_{\mu 2})} \frac{d\Gamma(K_{e 2}, E_\gamma > 10 \text{ MeV}, p_e^* > 200 \text{ MeV})}{dE_\gamma}$$

Results are in good agreement with expectations from ChPT

$K_{\mu 2}$: sensitivity to new physics

Scalar currents, e.g. due to Higgs exchange, affect $K \rightarrow \mu\nu$ width

$$R_{l23} = \left| \frac{V_{us}(K_{\mu 2})}{V_{us}(K_{l3})} \times \frac{V_{ud}(0^+ \rightarrow 0^+)}{V_{ud}(\pi_{\mu 2})} \right|$$

$$= \left| 1 - \frac{m_{K^+}^2}{m_{H^+}^2} \left(1 - \frac{m_{\pi^+}^2}{m_{K^+}^2} \right) \frac{\tan^2 \beta}{1 - \epsilon_0 \tan \beta} \right|$$

[Hou, Isidori-Paradisi]

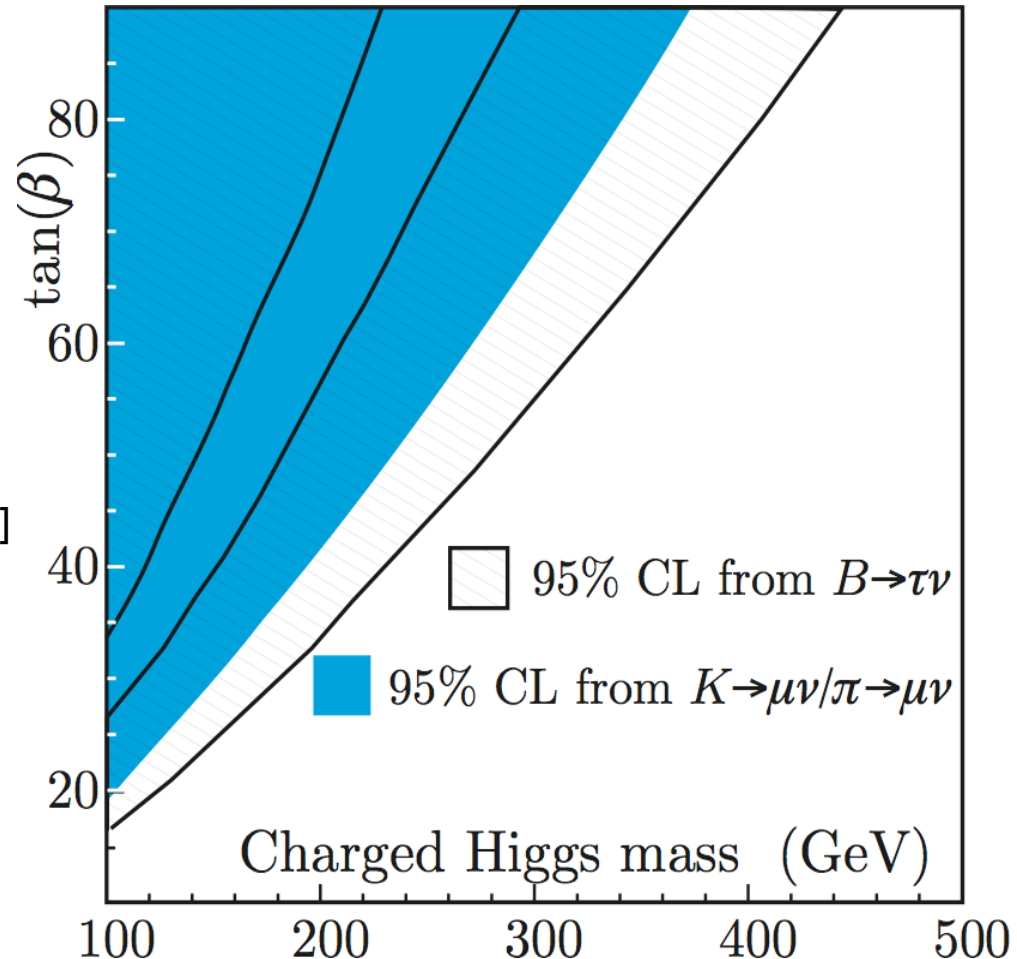
$R_{l23} = 1$ in SM

we find

$$R_{l23} = 1.008 \pm 0.008$$

limited by lattice uncertainty on $f_+(0)$ and f_K/f_π

From direct searches (LEP), $M_{H^+} > 80$ GeV, $\tan\beta > 2$



KLOE measurement of kaon parameters

$K_{S e3}$ PLB 636 (2006) 173
 $K_S \rightarrow \pi\pi$ EPJC 48 (2006) 767
 $K_S \rightarrow \gamma\gamma$ JHEP 05(2008) 051

K_S BRs

K_L decay distribution (τ) PLB 626 (2005) 15
 K_L decays and lifetime PLB 632 (2006) 43
 $K_L \rightarrow \pi^+\pi^-$ PLB 638 (2006) 140
 $K_L \rightarrow \gamma\gamma$ PLB 566(2003) 61
 K^0 mass JHEP 12(2007)073
 $K_{Le3\gamma}$ EPJC 55 (2008) 539
 $ff K_{Le3}$ PLB 636 (2006) 166
 $ff K_{L\mu3}$ JHEP 12(2007)105

**K_L BRs
lifetime
FFs**

$K^+_{\mu2}$ PLB 632 (2006) 76
 K^+ lifetime JHEP 01(2008)073
 K^+_{l3} JHEP 02(2008)098
 $K^+_{\tau'}$ PLB 597 (2004) 139
 $K^+_{\pi2}$ PLB 666 (2008) 305

**K^\pm BRs
lifetime**

KLOE V_{us} JHEP 04(2008)059