

# PDF uncertainties and LHC physics

-using ATLAS examples

A M Cooper-Sarkar

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## STANDARD MODEL

- There are W/Z 'calibration' measurements: Z/W ratio is the best
- W and Z cross-sections should first test our understanding and then contribute to our knowledge at greater precision
- W asymmetry should bring something new
- Beware that NEW low-x physics could compromise this.

## HIGGS

## BEYOND STANDARD MODEL

- Z' channels
- There are discovery channels – high ET jets- which could be obscured by PDF uncertainties
- But Jet Energy Scale Uncertainties could be more of a problem
- Be smart - look at ratios W+n-jets/Z+n-jets
- Other ways to get at high-x gluon?

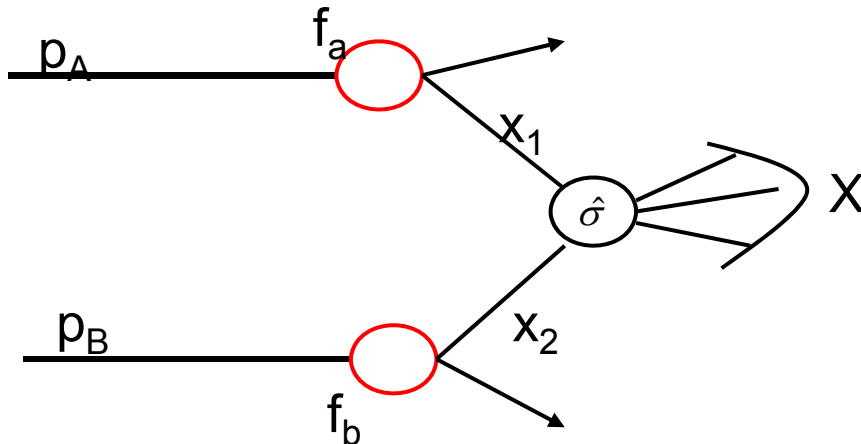
# The Standard Model is not as well known as you might think

In the QCD sector the PDFs limit our **knowledge** - transport PDFs to hadron-hadron cross-sections using QCD factorization theorem for short-distance **inclusive** processes

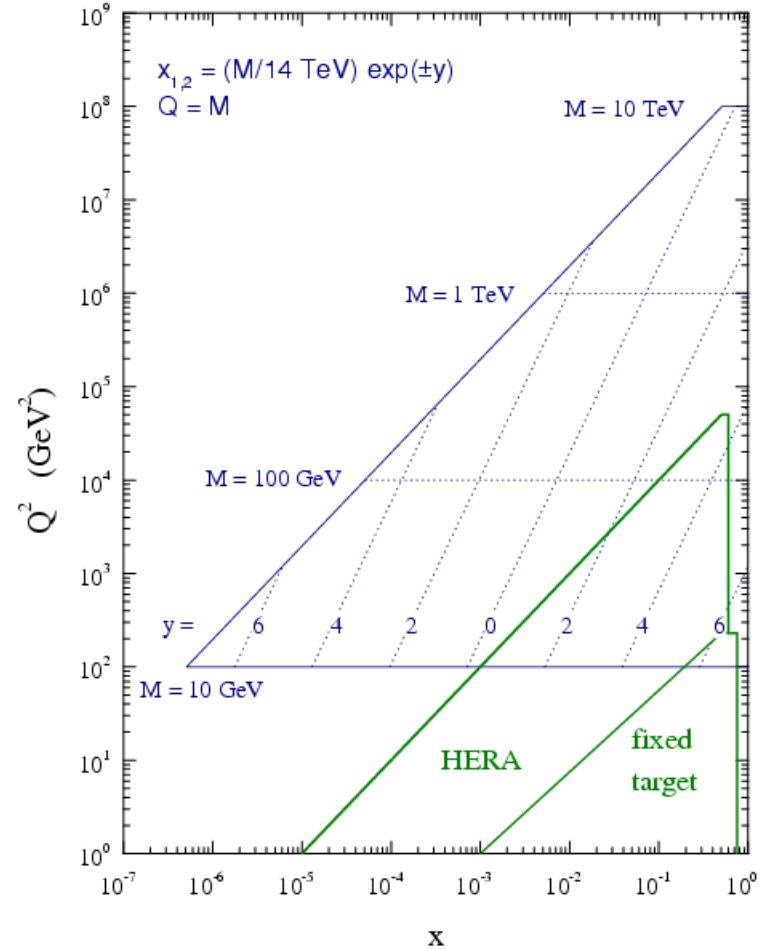
$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X} \left( x_1, x_2, \{P_i^\mu\}; \alpha_S(\mu_R^2), \alpha(\mu_R^2), \frac{Q^2}{\mu_R^2}, \frac{Q^2}{\mu_F^2} \right)$$

where  $X=W, Z, D\text{-}Y, H, \text{high-}E_T \text{ jets, prompt-}\gamma$  and  $\hat{\sigma}$  is known

- to some fixed order in pQCD and EW
- in some leading logarithm approximation (LL, NLL, ...) to all orders via resummation



**LHC parton kinematics**



**The central rapidity range for W/Z production AT LHC is at low-x**

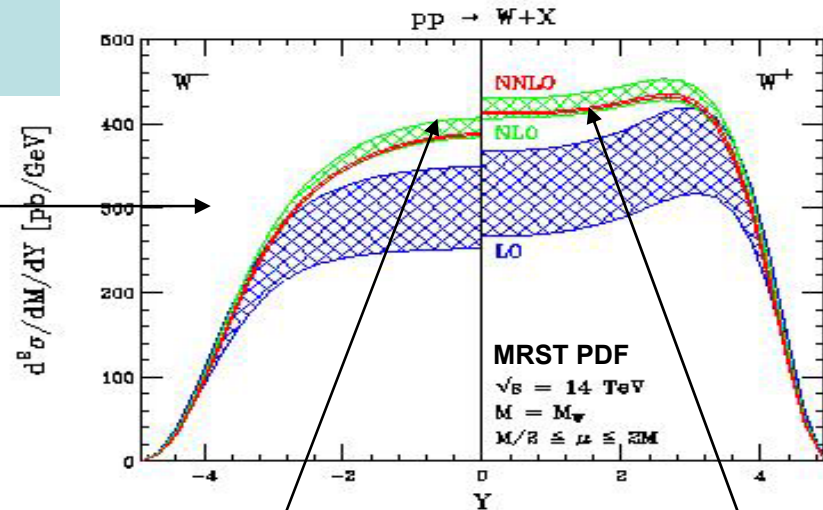
**( $6 \times 10^{-4}$  to  $6 \times 10^{-2}$ ) at 14 TeV**

**( $8.5 \times 10^{-4}$  to  $8.5 \times 10^{-2}$ ) at 10 TeV**

# WHAT DO WE KNOW WELL?

W/Z production have been considered as good standard candle processes with small theoretical uncertainty.

PDF uncertainty is THE dominant contribution and most PDF groups quote uncertainties ~3-4%



NNLO corrections small ~ few%  
 NNLO residual scale dependence < 1%

## W Z cross-sections at 10 TeV

| PDF set          | $\sigma_{W^+} B_{W \rightarrow l\nu}$ (nb) | $\sigma_{W^-} B_{W \rightarrow l\nu}$ (nb) | $\sigma_Z B_{Z \rightarrow ll}$ (nb) |
|------------------|--|--|--------------------------------------|
| ZEUS-2005        | 8.51±0.30                                  | 6.08±0.20                                  | 1.36±0.04                            |
| MSTW08           | 8.55±0.25                                  | 6.25±0.20                                  | 1.38±0.04                            |
| CTEQ66           | 8.77±0.30                                  | 6.22±0.23                                  | 1.40±0.044                           |
| <b>HERAPDF02</b> | <b>8.69±0.07</b><br>±0.16±0.16             | <b>6.31±0.04</b><br>±0.13±0.13             | <b>1.40±0.01</b><br>±0.03 ±0.02      |

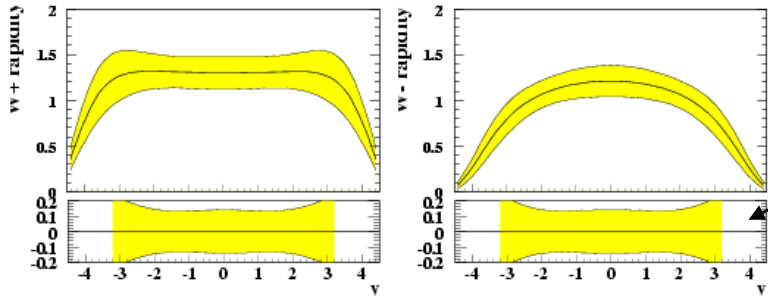
Agreement between PDFs has improved in recent years –only consider those which include massive heavy quark treatment. Can be used as a luminosity monitor?

10 TeV cross-sections are ~70% of 14 TeV cross-sections- there will still be millions of events

# WHY DO WE KNOW IT SO WELL? BECAUSE OF HERA.

Look in detail at predictions for W/Z rapidity distributions: Pre- and Post-HERA

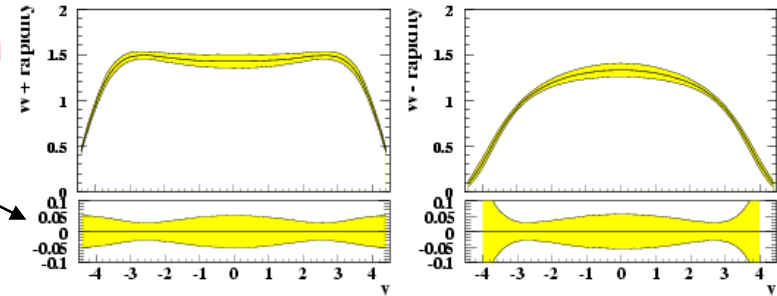
W and Z rapidity distributions



Pre HERA  
~15% errors

Note  
difference in  
scale for  
fractional  
errors

W and Z rapidity distributions

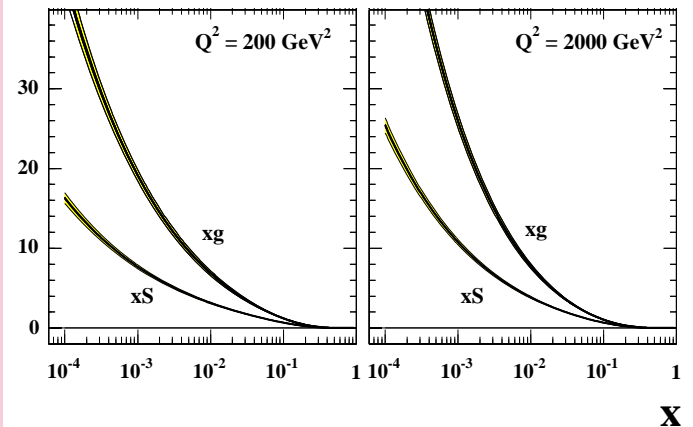
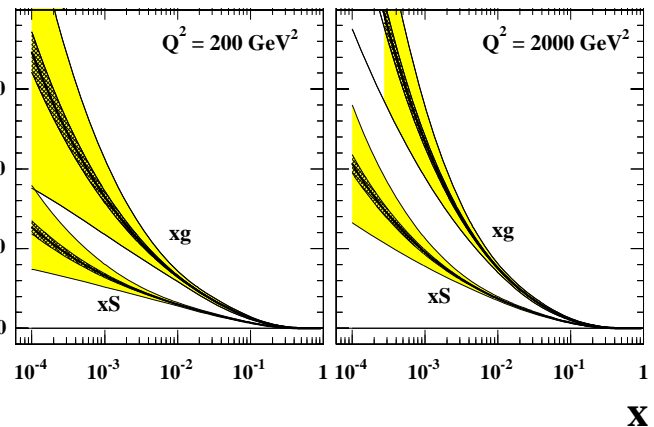
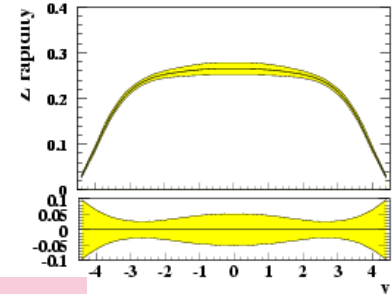
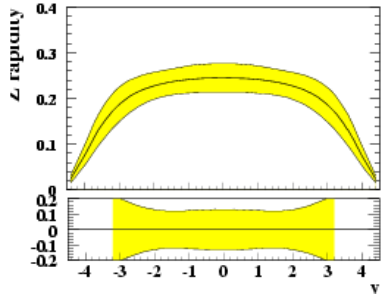


Post HERA  
-including ZEUS  
data ~5% errors

Why such an  
improvement  
?

It's due to the  
improvement in the  
low-x sea and gluon  
At the LHC the q-  
qbar which make  
the boson are  
mostly sea-sea  
partons

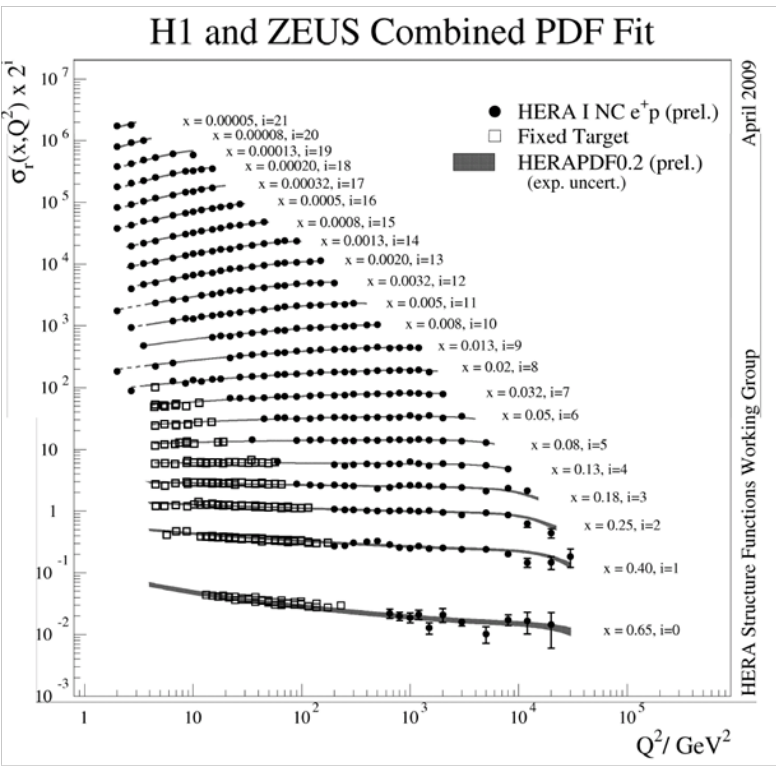
And at  $Q^2 \sim M_Z^2$  the  
sea is driven by  
the gluon



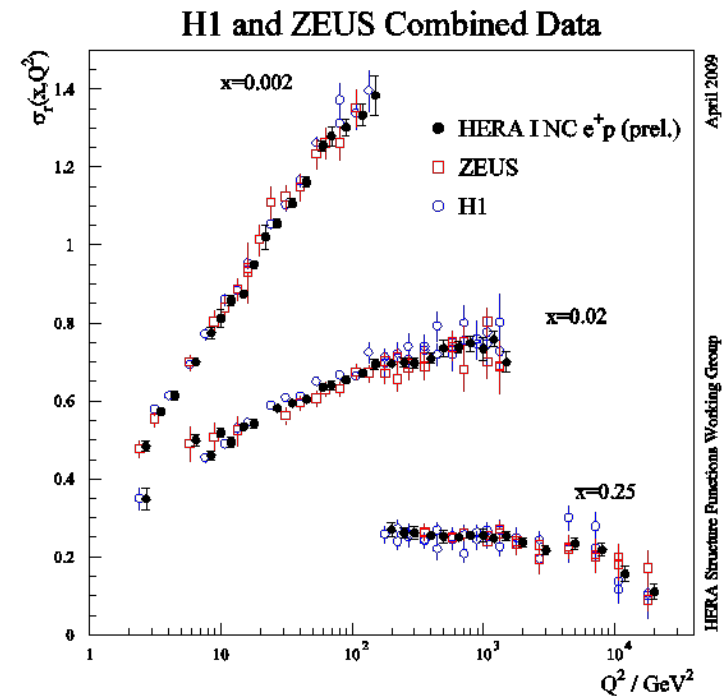
# Recently this has improved dramatically due to the combination of ZEUS and H1 data sets

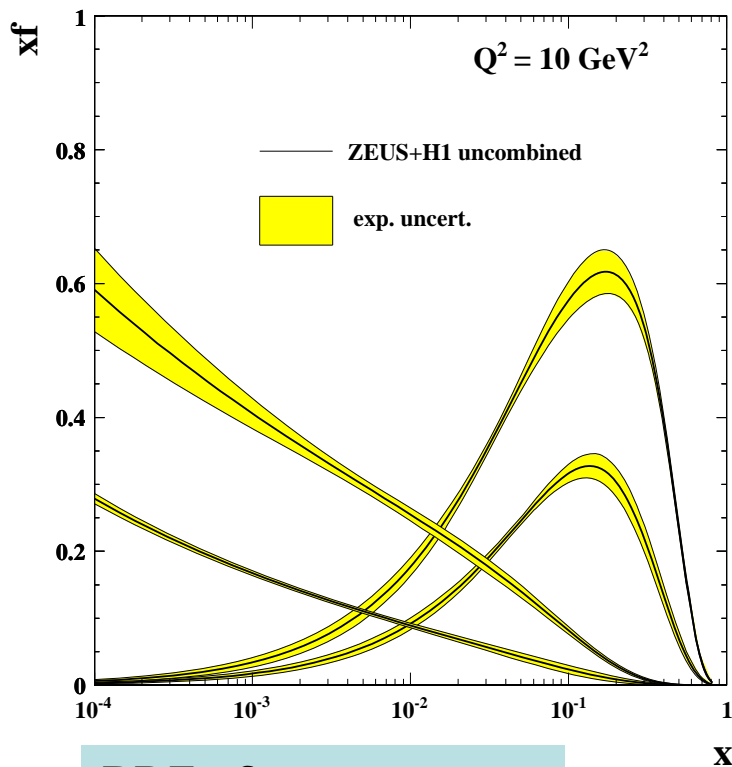
Not just statistical improvement. Each experiment can be used to calibrate the other since they have rather different sources of experimental systematics

- Before combination the systematic errors are  $\sim 3$  times the statistical for  $Q^2 < 100$
- After combination systematic errors are  $<$  statistical
- $\rightarrow$  very consistent HERA data set can be used as sole input to PDF fits with  $\Delta x^2 = 1$



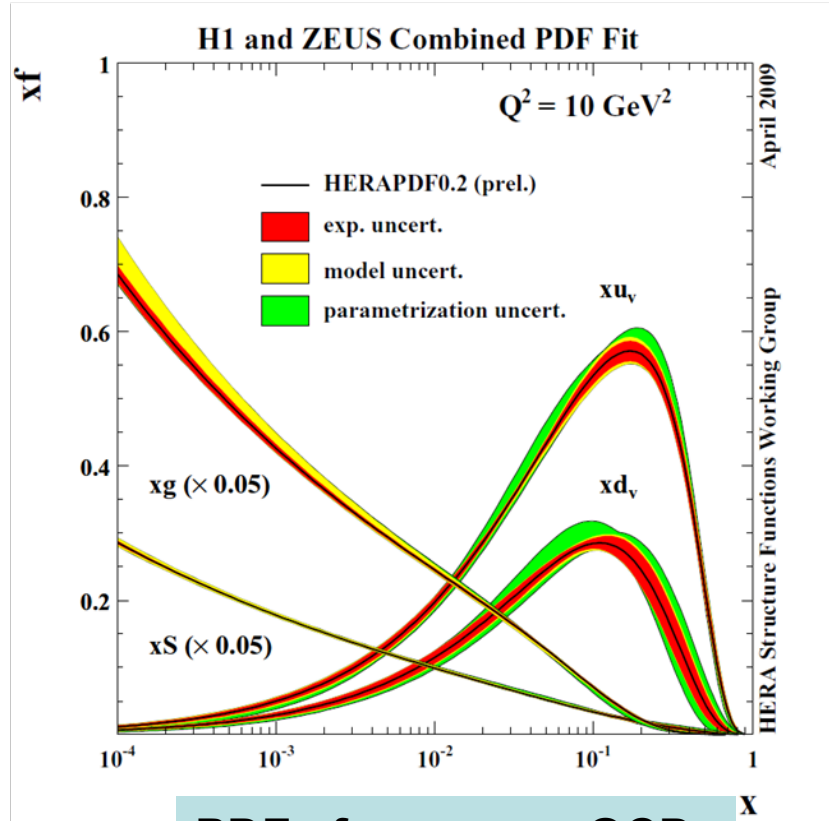
HERAPDF0.2  
2009  
also has new and very precise H1 data sets included





PDFs from same QCD analysis of separate ZEUS and H1 data sets - before combination

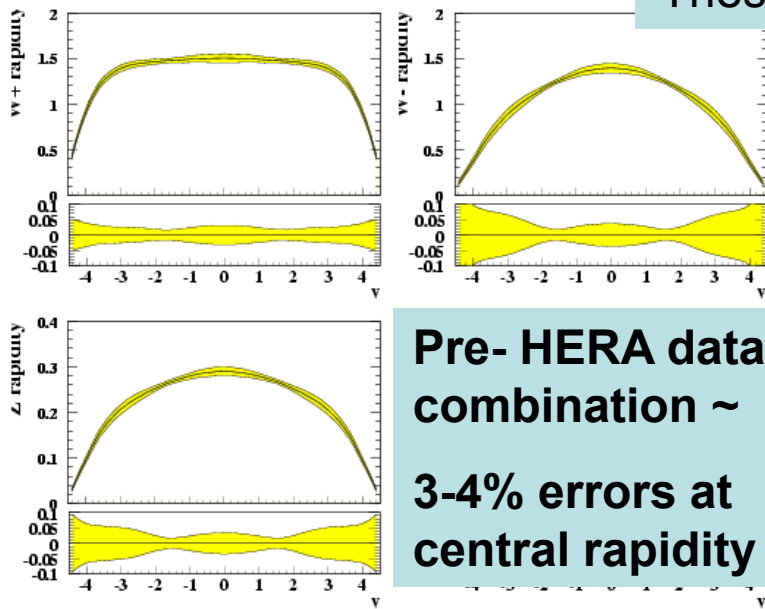
Experimental error only



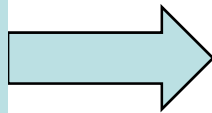
PDFs from same QCD analysis of combined HERA data - after combination

Compare experimental errors

W and Z rapidity distributions

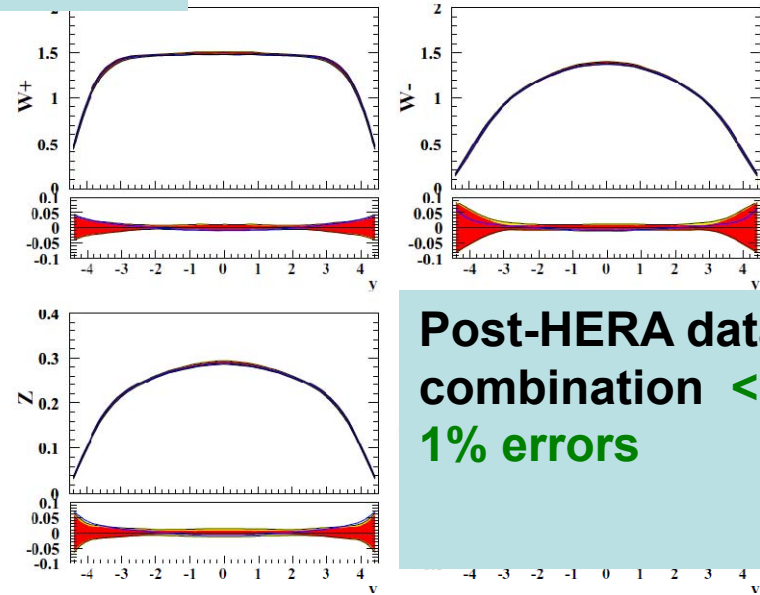


Pre- HERA data combination ~  
3-4% errors at central rapidity



These illustrations at 14 TeV

W and Z rapidity distributions

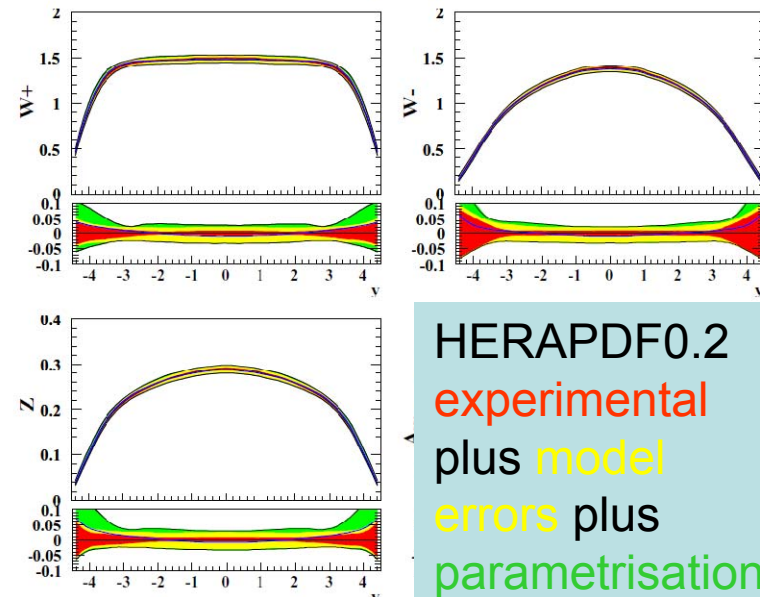


Post-HERA data combination <  
1% errors

Using the HERA combined data (2008) and then improving the HERA combined data (2009) leads to **smaller and smaller experimental uncertainties** on the predictions for W/Z production at central rapidity, because the HERA data improve the low-x sea and gluon PDFs

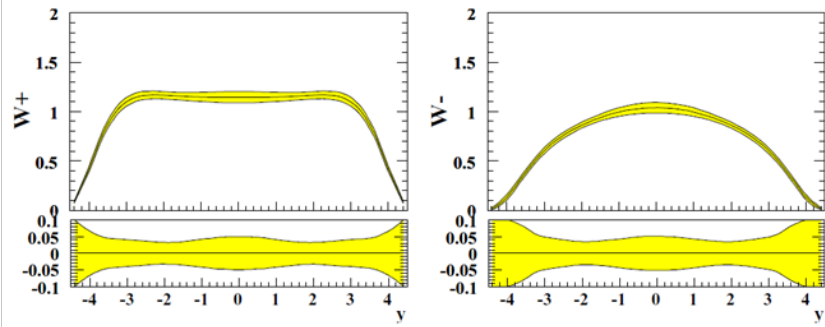
However PDF fitting should also include consideration of **model errors** and **parametrisation errors**

W and Z rapidity distributions



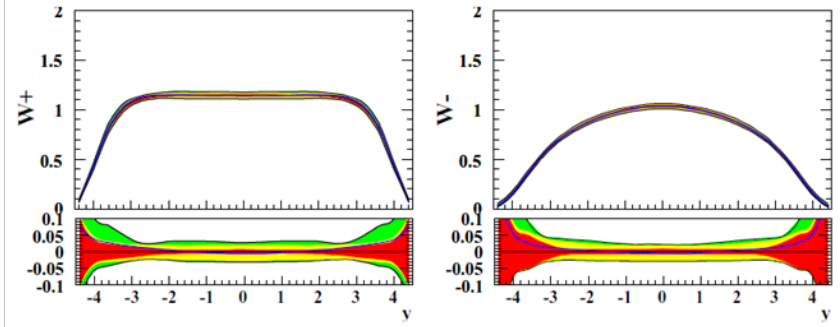
HERAPDF0.2  
**experimental**  
plus **model errors** plus  
**parametrisation**

W and Z rapidity distributions



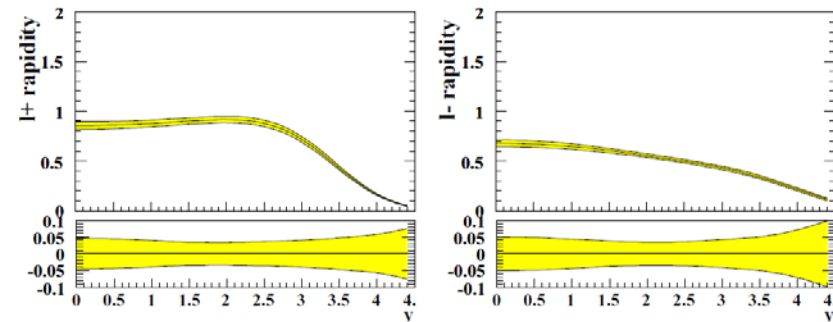
**CTEQ6.6 PDF  
predictions at  
10 TeV ~5%  
error at central  
rapidity**

W and Z rapidity distributions

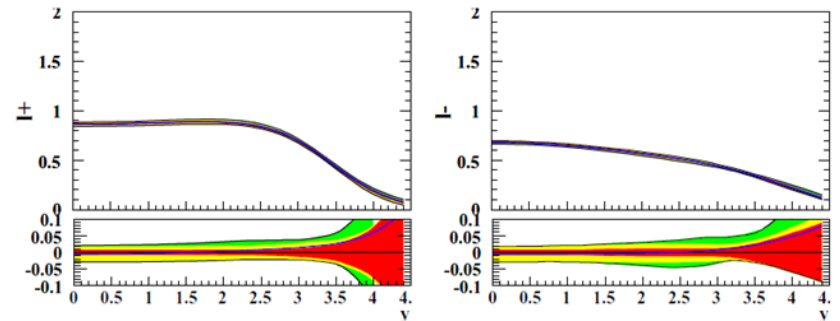


**HERAPDF0.2  
predictions at  
10 TeV ~3%  
error at central  
rapidity**

Lepton rapidity distributions



Lepton rapidity distributions

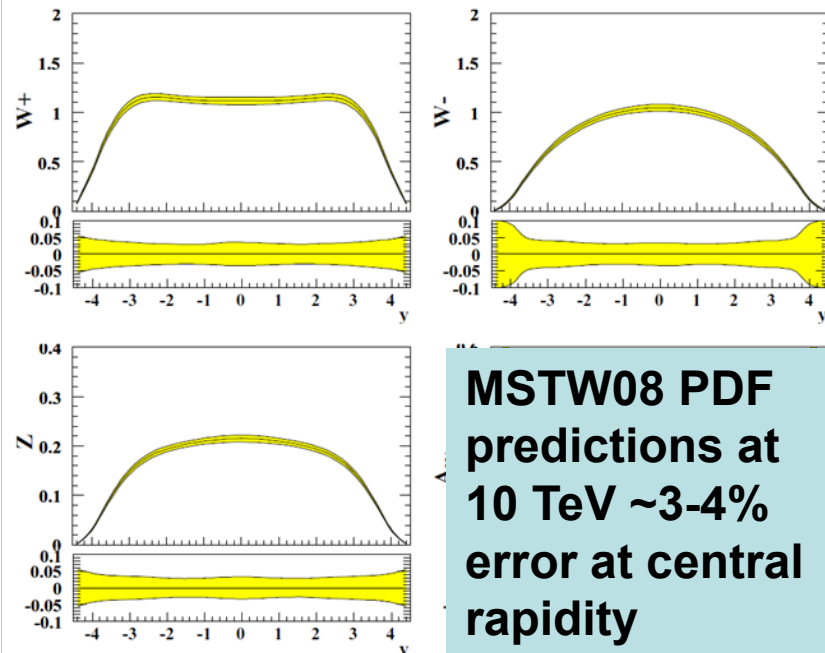


Now go to 10 TeV and compare to CTEQ66, including lepton decay distributions

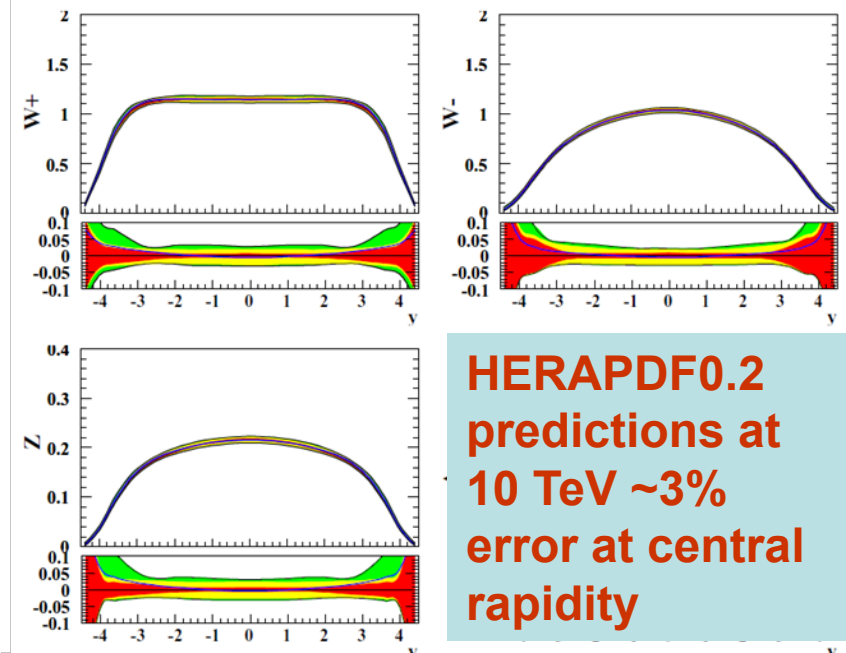
Note blue line on HERAPDF plots from variation of  $\alpha_s(M_Z)=0.1176$  (standard) up to 0.1196



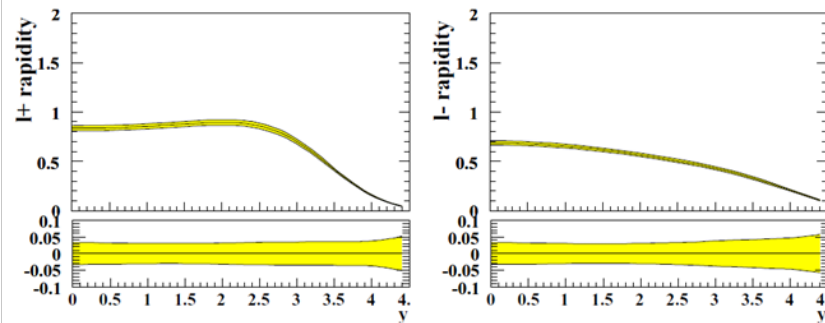
W and Z rapidity distributions



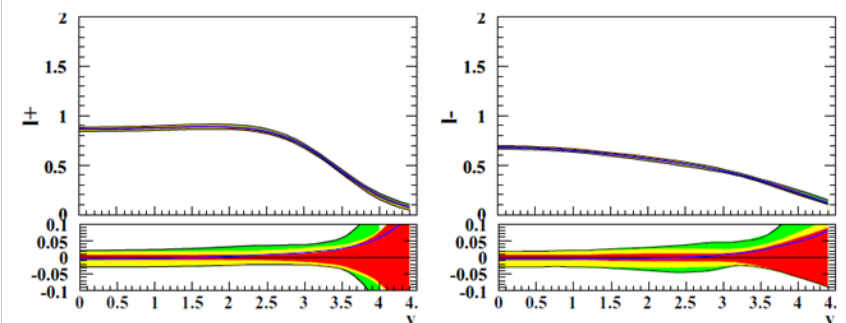
W and Z rapidity distributions



Lepton rapidity distributions



Lepton rapidity distributions



Now go to 10 TeV and compare to MSTW08, including lepton decay distributions

There is still potential for PDF predictions to improve before LHC

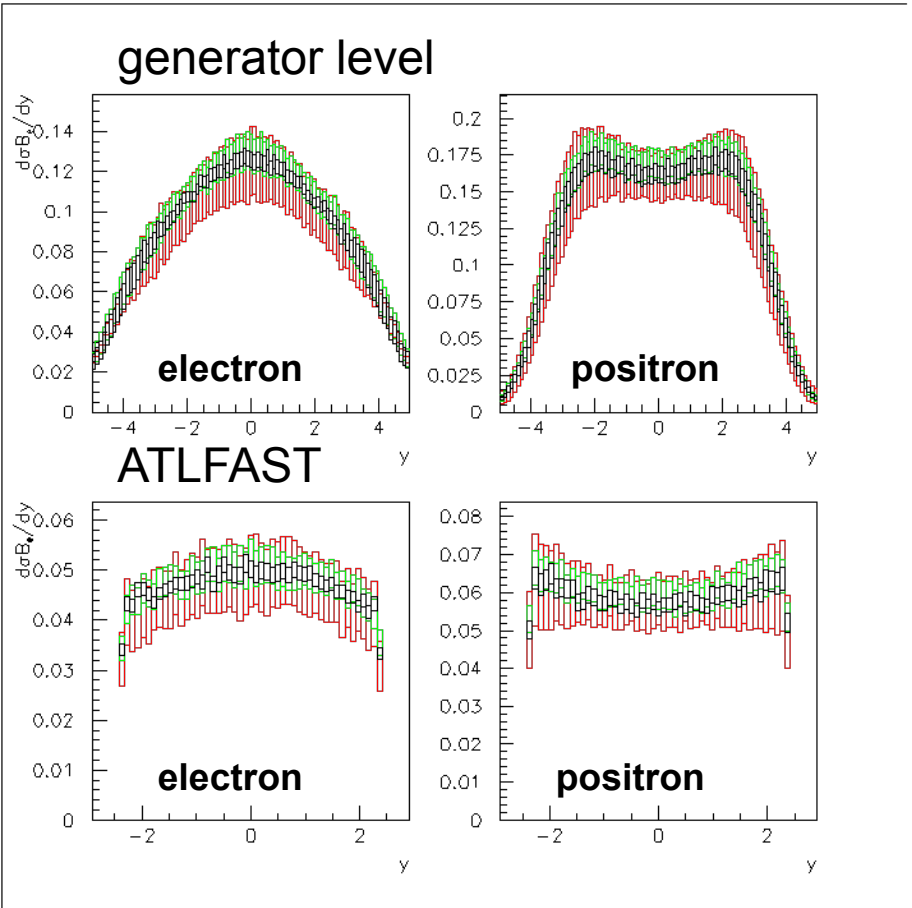
# Can we improve our knowledge of PDFs using LHC data itself?

## We actually measure the decay lepton spectra

Generate pseudodata at 14TeV corresponding to  $100\text{pb}^{-1}$  using CTEQ6.1M ZEUS\_S MRST2001 PDFs with full uncertainties

- At  $y=0$  the total uncertainty is
- $\sim \pm 6\%$  from ZEUS
- $\sim \pm 4\%$  from MRST01E
- $\sim \pm 8\%$  from CTEQ6.1

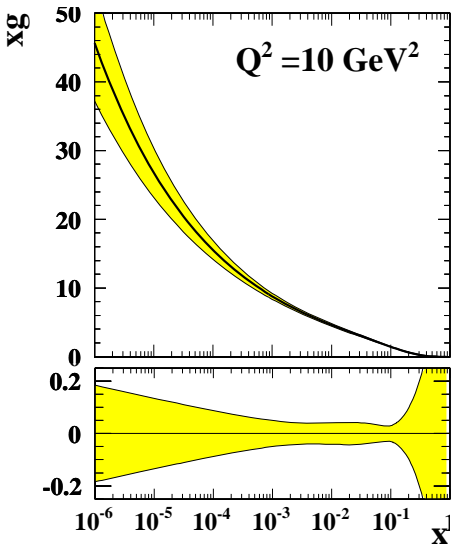
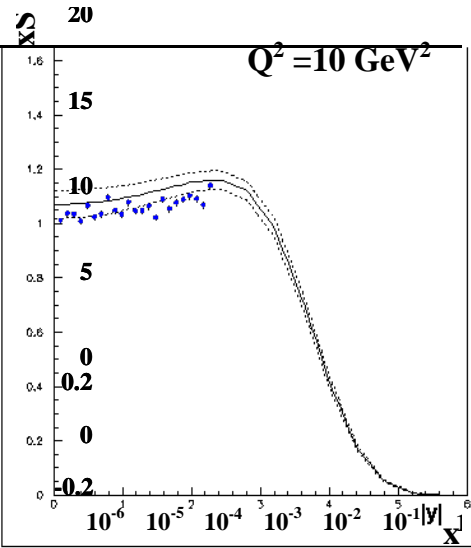
To improve the situation we NEED to be more accurate than this:  $\sim 4\%$   
Statistics are no problem there will be millions of W's  
We need to control the systematic uncertainty



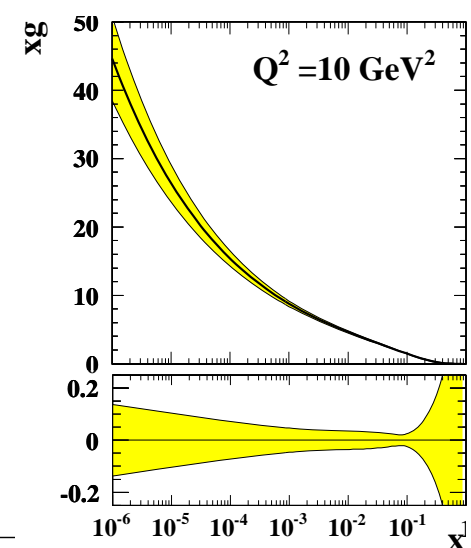
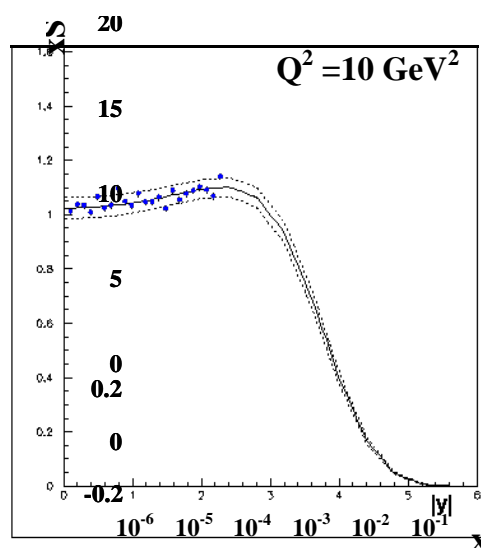
# Can we improve the situation with early LHC data?

Generate  $W^+/W^-$  data with 4% error using CTEQ6.1 PDF, pass through ATLAS detector simulation and then include this pseudo-data in the global ZEUS PDF fit (actually use the decay lepton spectra) **Central value of prediction shifts and uncertainty is reduced**

BEFORE including W data



AFTER including W data



$e^+$  rapidity spectrum and gluon PDF BEFORE these data are included in the PDF fit

$e^+$  rapidity spectrum and gluon PDF AFTER these pseudodata are included in the PDF fit

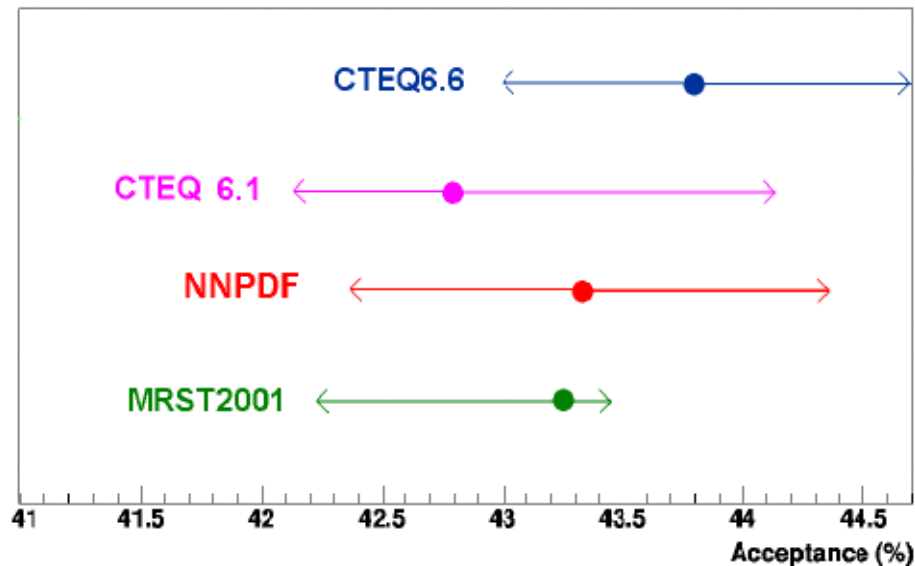
**Gluon PDF uncertainties are reduced**

IS achieving a 4% systematic possible? And how soon?

After the first fb-1  $\Delta\sigma$  will be dominated by acceptance uncertainty

Dependence of ATLAS acceptance for Z on PDFs

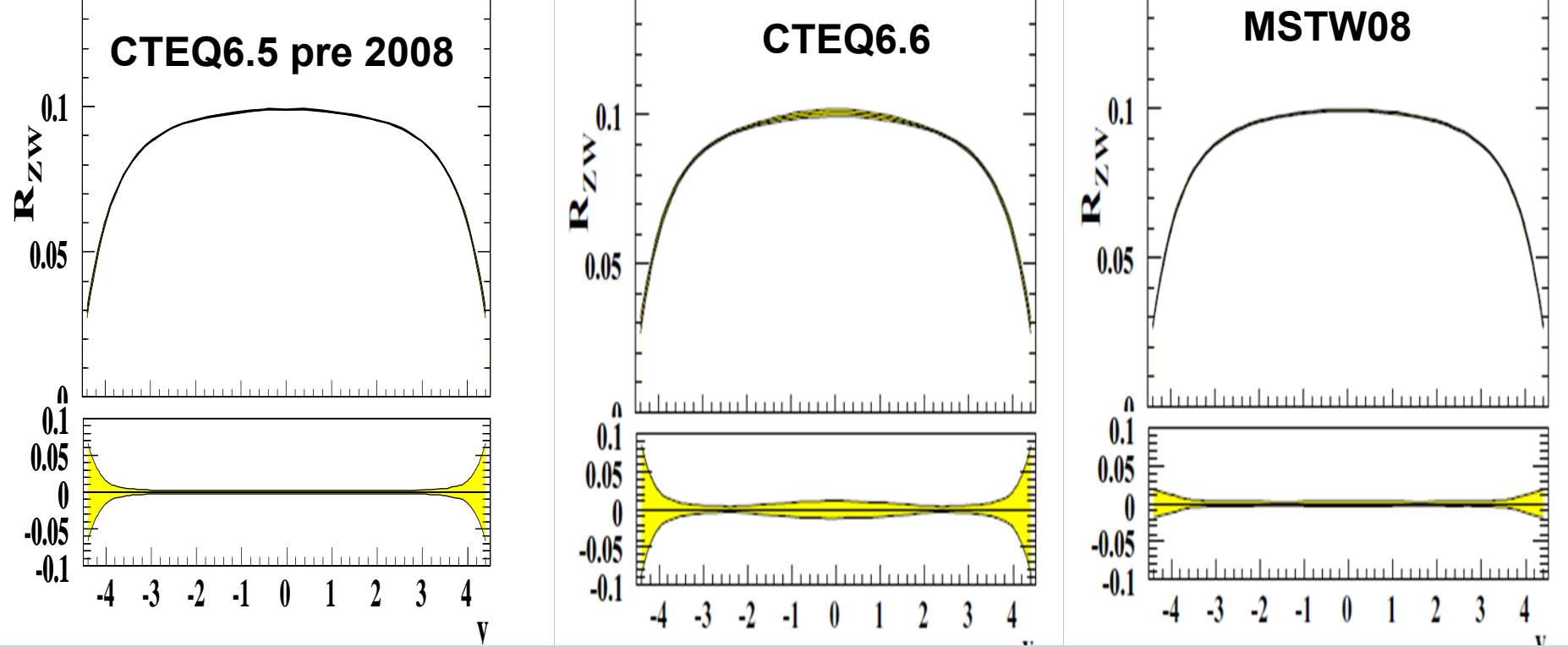
Study done in the muon channel:  $p_t > 20$  GeV,  $\eta < 2.5$



Difference in acceptance between CTEQ6.6 to 6.1 only 2% ---whereas there is a 6% difference in cross-section predictions

Seems possible to achieve  $< 2\%$  systematic on acceptance when considering up to date Pdf sets which differ by only 3% in xsecn predictions.

**Now let's look at ratios: Z/W ratio is a golden benchmark measurement (10TeV)**



**ZOOM in on Z/W ratio – there is fantastic agreement between PDF providers**  
**PDF uncertainty from the low-x gluon and flavour symmetric sea cancels out- and so do luminosity errors** BUT there is somewhat more PDF uncertainty than we thought before 2008 (~1.5% rather than <1% in the central region)

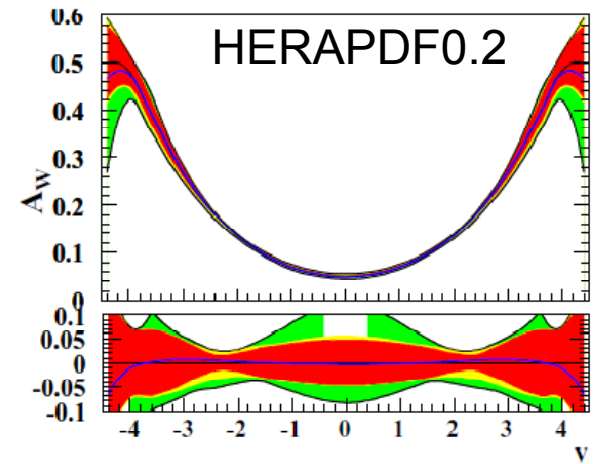
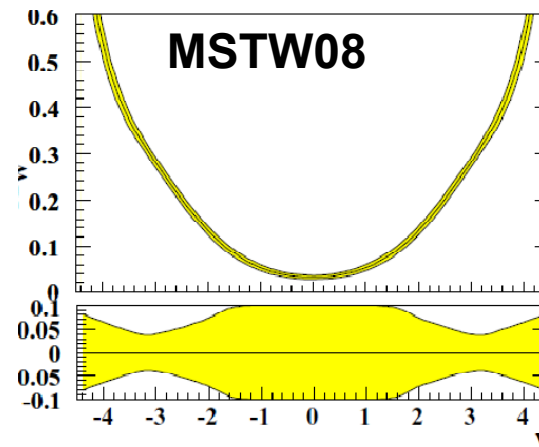
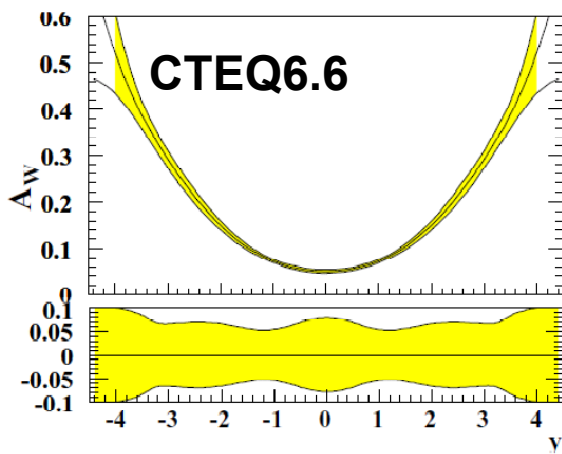
**There is uncertainty in the strangeness sector that does not cancel out between Z and (W<sup>+</sup> + W<sup>-</sup>)... it was always there we just didn't account for it**

$$\underline{Z} = \underline{u\bar{u} + d\bar{d} + s\bar{s} + c\bar{c} + b\bar{b}}$$

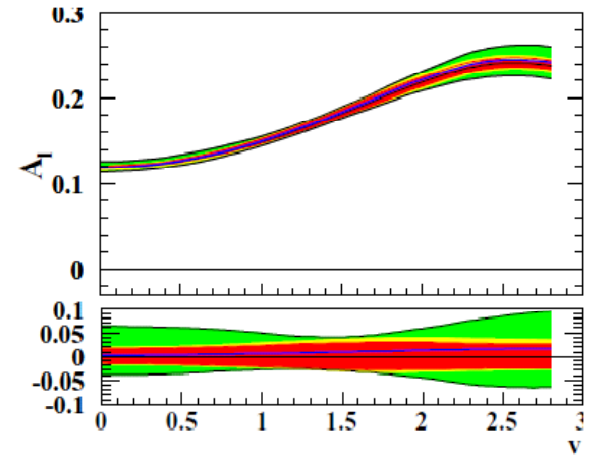
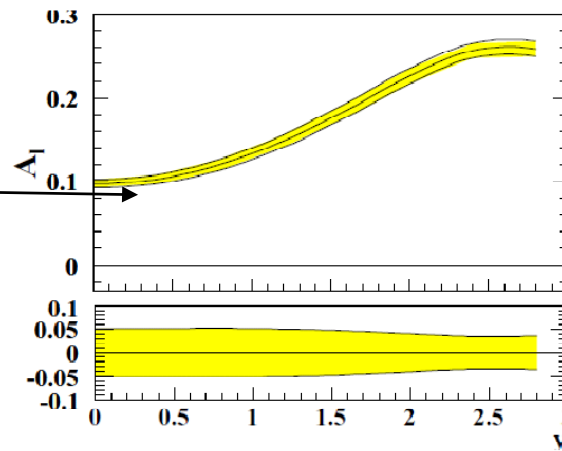
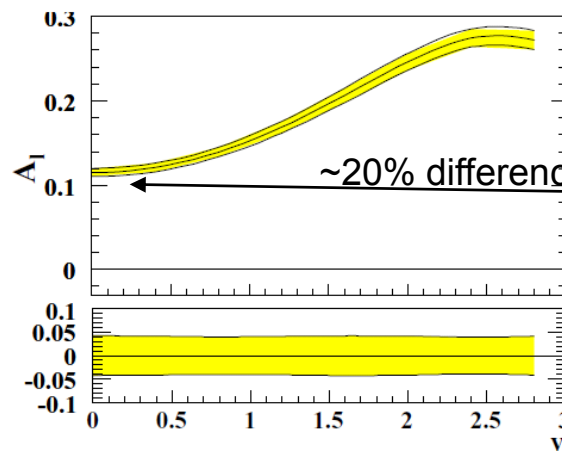
$$W^+ + W^- \sim (u\bar{d} + c\bar{s}) + (d\bar{u} + s\bar{c})$$

YES this does translate to the Z/lepton ratio

# But in the W asymmetry – there is NOT fantastic agreement (10 TeV)



Lepton asymmetry



~20% difference

Further sources of PDF uncertainty from the valence sector are revealed. And note that when it comes to W asymmetry CTEQ do not have the most conservative errors at central rapidity - MRST/MSTW do

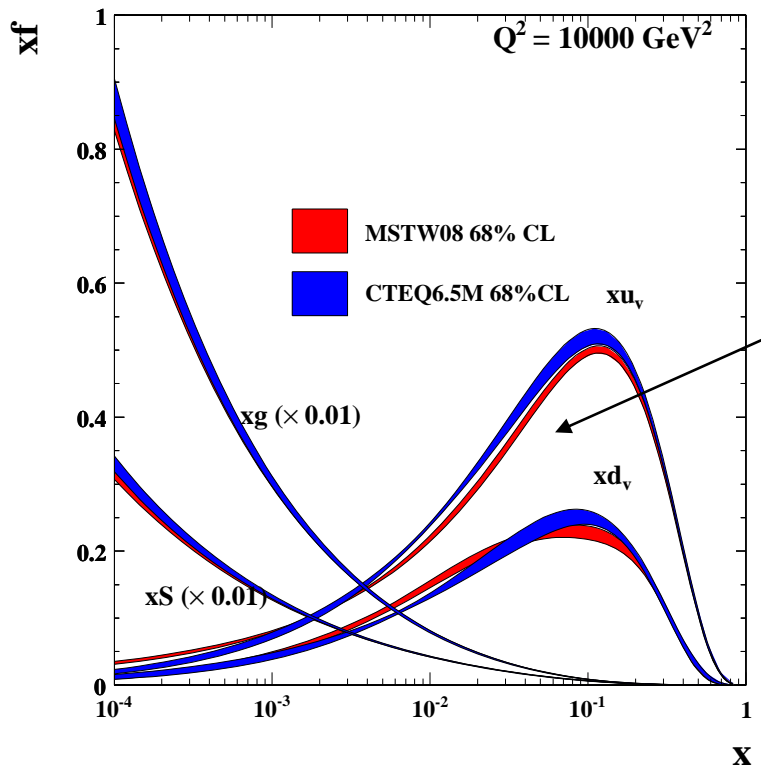
**Predictions for AW are different in the central region- because predictions for valence distributions at small-x are different**

Dominantly, at LO 
$$A_W = \frac{(u(x_1) \bar{d}(x_2) - d(x_1) \bar{u}(x_2))}{(u(x_1) \bar{d}(x_2) + d(x_1) \bar{u}(x_2))}$$

And at central rapidity  $x_1 = x_2$   
and  $\bar{u} \sim \bar{d} \sim \bar{q}$  at small x

So  $A_W \sim \frac{(u - d)}{(u + d)} = \frac{(u_v - d_v)}{(u_v + d_v + 2 q_{\text{bar}})}$

Actually this LO approx. is pretty good even quantitatively  
The difference in valence PDFs you see here does explain the difference in  $A_W$  between MRST and CTEQ



As we move away from central rapidity: as  $x_1$  increases (decreases) the larger (smaller) difference is weighted by larger (smaller) sea distributions at smaller  $x_2$

*$x$ -range affecting  $W$  asymmetry in the measurable rapidity range at ATLAS (10TeV)*

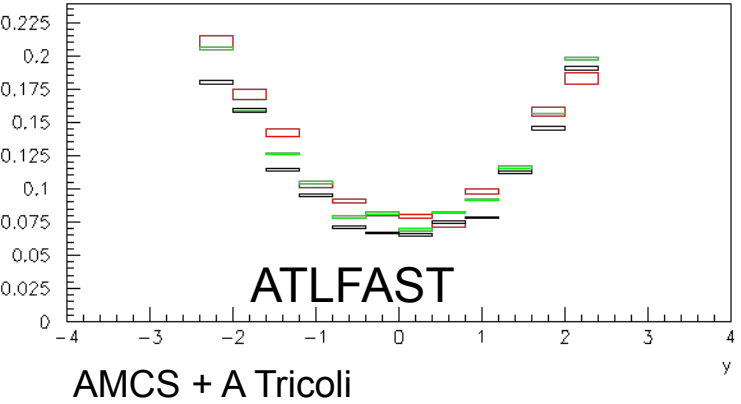
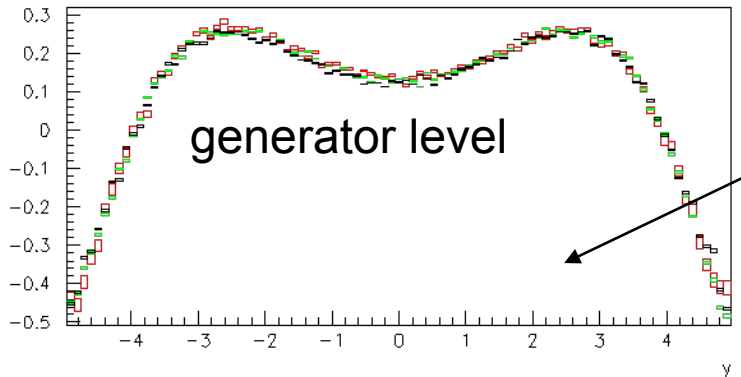


# Can we improve our knowledge of PDFs using ATLAS data itself?

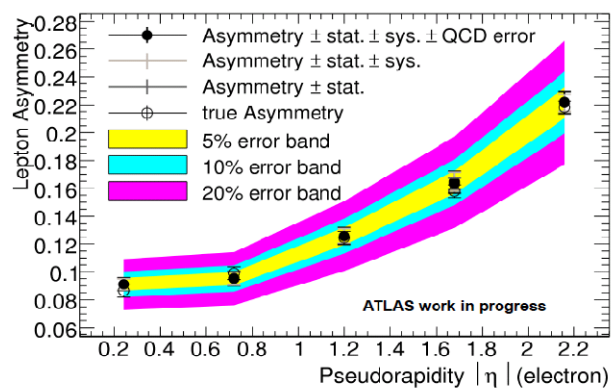
**We actually measure the decay lepton spectra**

Generate pseudodata at 14TeV corresponding to 100pb<sup>-1</sup> using **CTEQ6.1M** **ZEUS\_S** **MRST2004** PDFs with full uncertainties

Recent study with full detector simulation AND QCD di-jet background estimation



## W Asymmetry: Prospects for 100pb<sup>-1</sup> data



- 47 ± 12 % QCD background assumed (25% uncertainty)
- combined +/- η (weighted with errors)

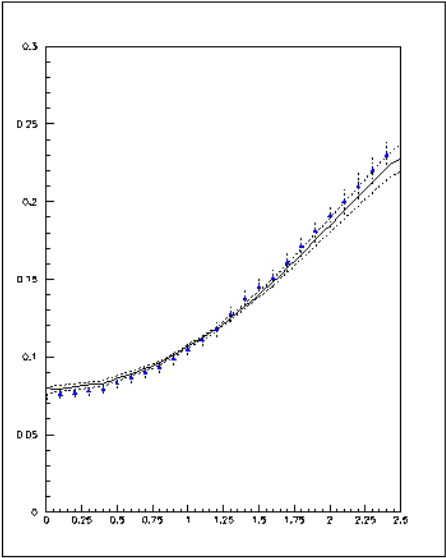
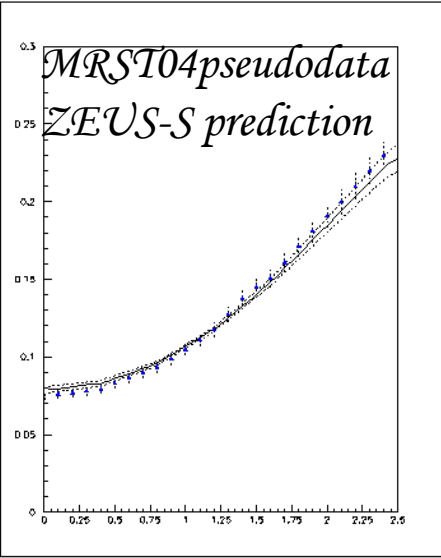
5-10% uncertainty K Lohwasser



So be optimistic and generate data with 4% error using MRST04 PDF and then include this pseudo-data in the global ZEUS PDF fit (actually use the lepton asymmetry data)

BEFORE including  $A_e$  pseudo-data

AFTER including  $A_e$  pseudo-data

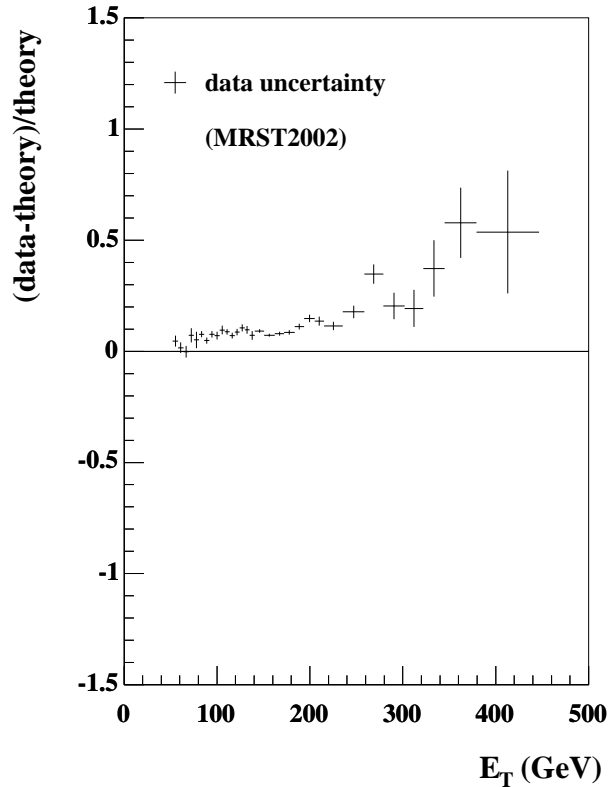


Result is improved accuracy of and change of shape of the valence PDFs

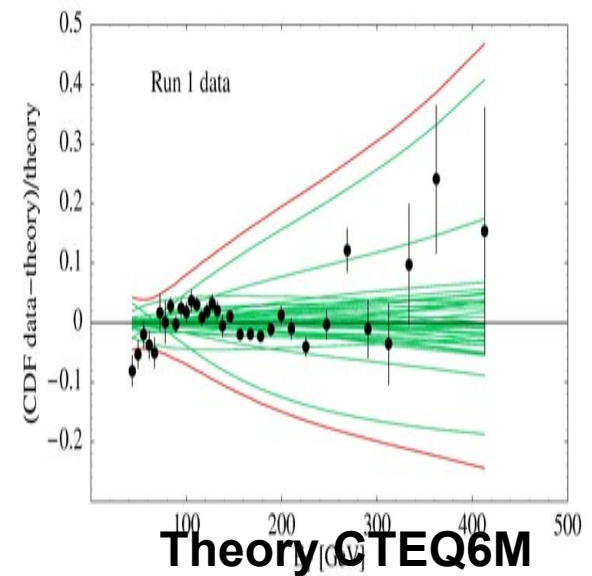
ATLAS/CMS LHC asymmetry data can measure valence distributions at  $x \sim 0.005$

# WHAT DO WE NOT KNOW WELL?

## CDF



Example of how PDF uncertainties matter for BSM physics— Tevatron jet data were originally taken as evidence for new physics--



i

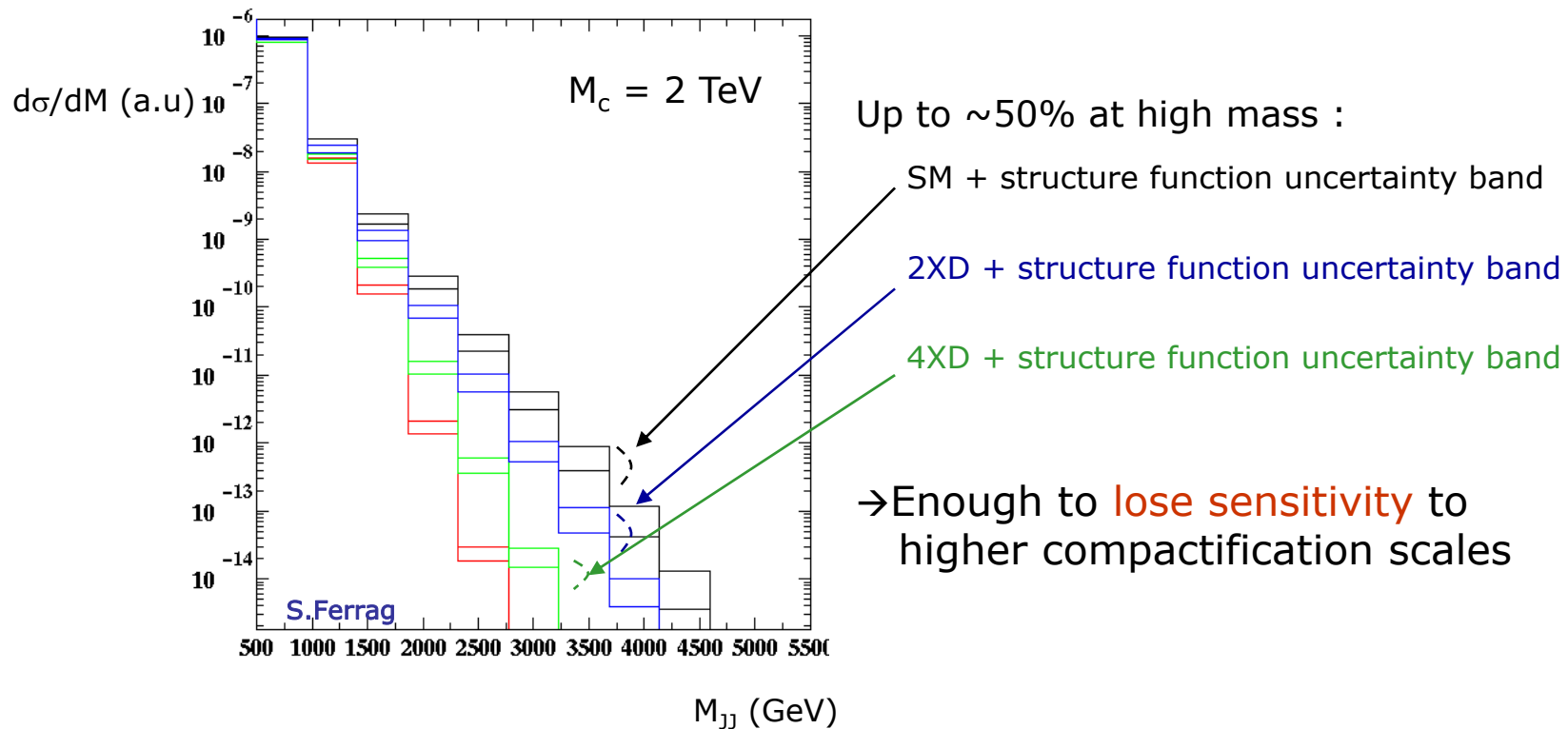
These figures show inclusive jet cross-sections compared to predictions in the form  $(\text{data} - \text{theory})/\text{theory}$

Today Tevatron jet data are considered to lie within PDF uncertainties

And the largest uncertainty comes from the uncertainty on the high  $x$  gluon

# And what consequences might this have?

Such PDF uncertainties in the jet cross sections compromise the LHC potential for discovery of any new physics which can be written as a contact interaction  
E.G. Dijet cross section has potential sensitivity to compactification scale of extra dimensions ( $M_c$ )



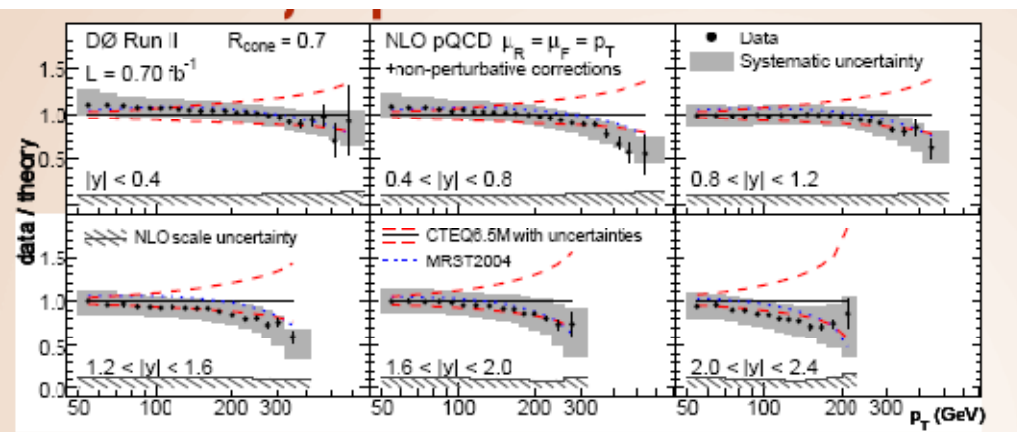
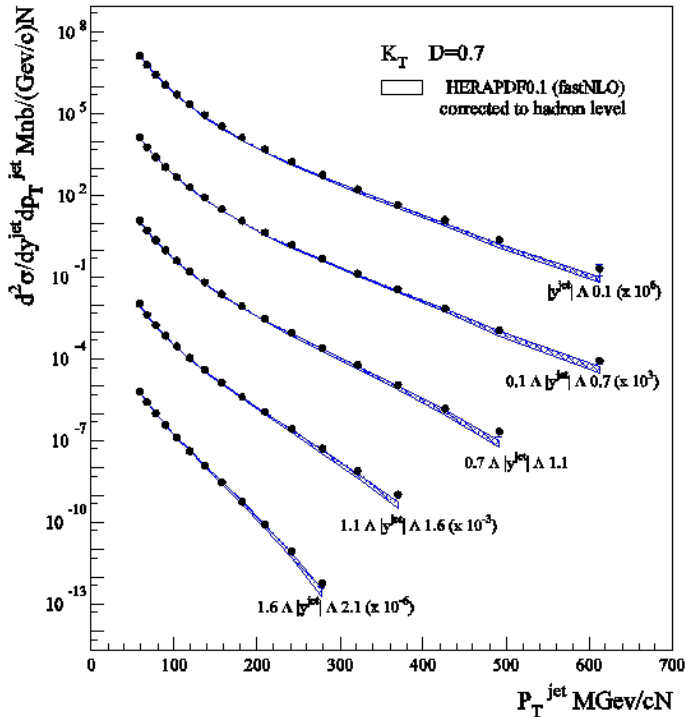
# CDF Run-II jet data compared to HERAPDF0.1

Note there is now new Tevatron Run-II jet data

Has been used in MSTW08 PDFs

It does not make MUCH difference to the level of high-x gluon PDF uncertainty

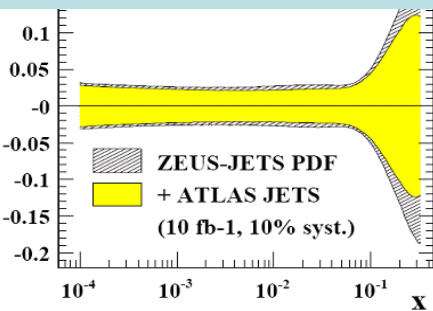
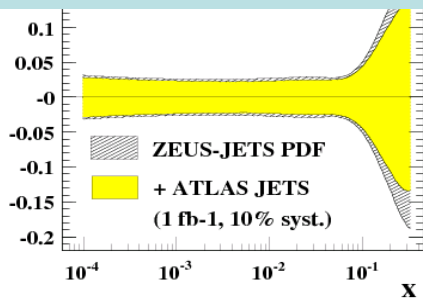
### Tevatron Jet Cross Sections



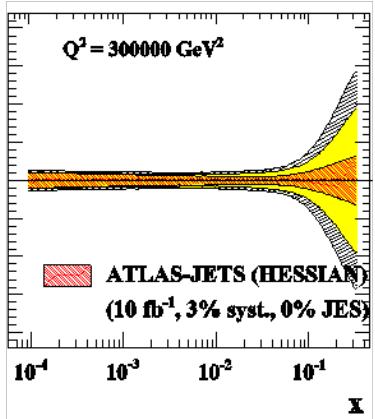
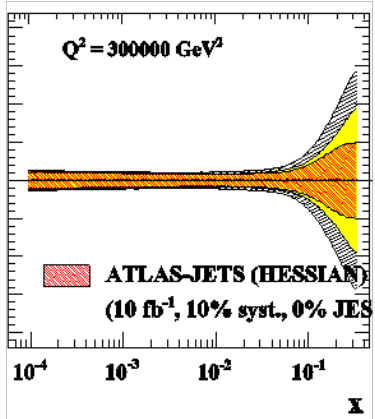
D0 jet data compared to CTEQ6.5 seem to be less hard than Run-I (CTEQ6.5 fitted Run-I)

# And will we be able to use LHC data itself to improve the situation? - study of impact on gluon PDF uncertainties from including ATLAS pseudodata in PDF fit

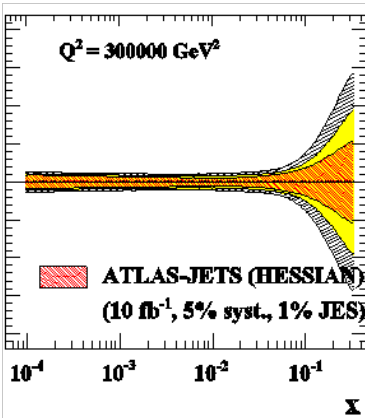
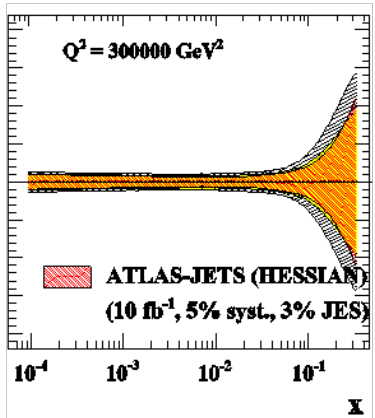
Use data at higher  $\eta > 1$  and lower  $pt < 3\text{TeV}$  to avoid new physics!



**Impact of increasing statistics**



**Impact of decreasing experimental systematic uncertainty**



**Impact of decreasing experimental correlated systematic uncertainty**  
**Challenging!**  
**Can we decrease Jet Energy Scale systematic to 1%?**

Jet energy scale also a problem in W/Z+jets channel, where SUSY signals may show up – **Jet Energy Scale of 5% gives uncertainties 5-12% on the W + (1-6) jet cross-sections. This is larger than the PDF uncertainty (3-8%)**

# W+jets: PDF vs JES Uncertainty

PDF vs Jet Scale Uncertainty ( $\Delta JS$ )  
with 10% (5%) jet energy miscal.

(Note: results with tight EF cuts samples)

2.9% <  $\Delta$  PDF < 7.3%  
 5.8% <  $\Delta JS$  (10%) < 23.6%  
 3.6% <  $\Delta JS$  (5%) < 11.9%



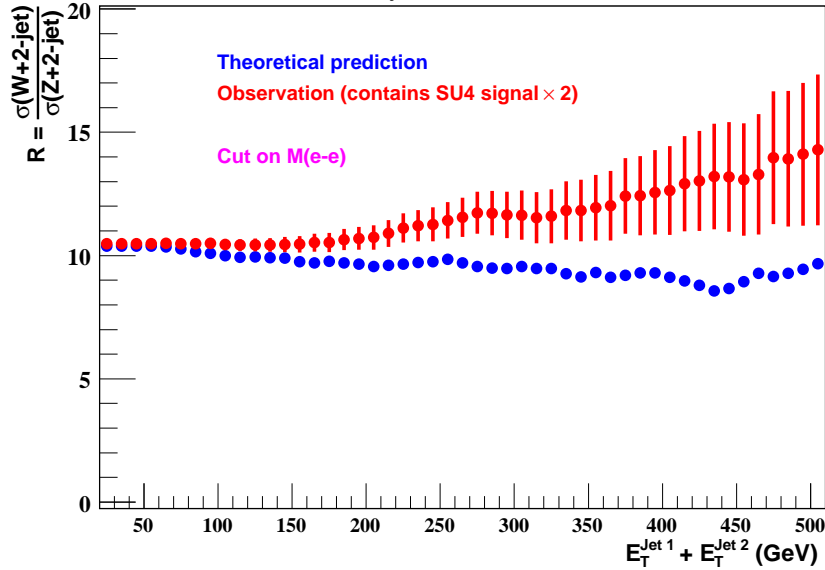
**PDF Uncert < Expt. Syst. Uncert**

Next: When is JES < PDF Unc?  
Try with 1,2,3% jet energy miscal.

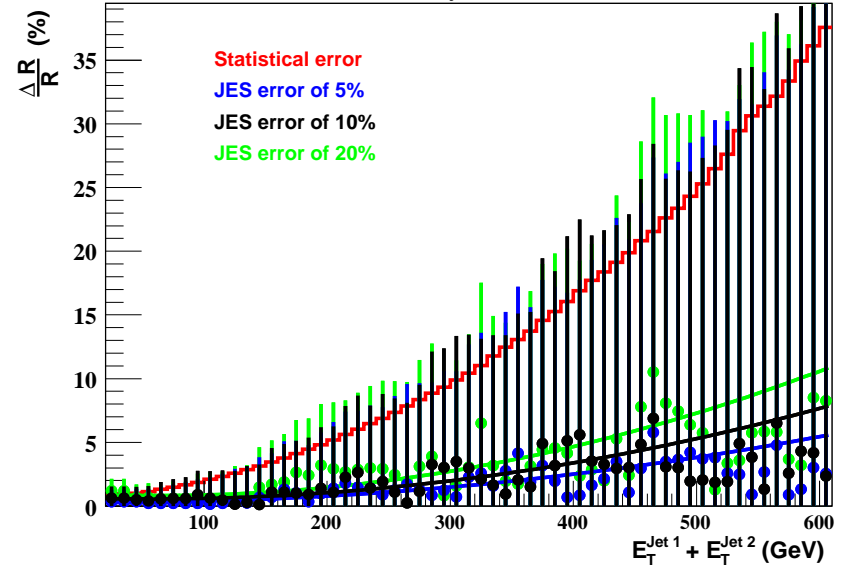
| Multipl          | $\Delta+$ PDF (%) | $\Delta-$ PDF (%) | $\Delta+$ JS (%) | $\Delta-$ JS (%) |
|------------------|-------------------|-------------------|------------------|------------------|
| W+ $\geq 1$ jets | 3.2               | 2.9               | 10.7<br>(5.2)    | 10.7<br>(5.2)    |
| W+ $\geq 2$ jets | 3.2               | 2.9               | 10.2<br>(5.1)    | 10.7<br>(5.2)    |
| W+ $\geq 3$ jets | 3.3               | 2.9               | 5.8<br>(3.6)     | 9.0<br>(4.0)     |
| W+ $\geq 4$ jets | 5.0               | 3.9               | 14.7<br>(7.8)    | 15.6<br>(7.0)    |
| W+ $\geq 5$ jets | 5.9               | 4.8               | 20.8<br>(9.5)    | 20.5<br>(10.7)   |
| W+ $\geq 6$ jets | 7.3               | 5.9               | 22.2<br>(10.4)   | 23.6<br>(11.9)   |

However BSM signals can show up in the  $R = (W + n \text{ jet}) / (Z + n \text{ jet})$  ratio and the jet energy scale is less of a problem in the ratio

Comparison of measured  $R_{2\text{-jets}}$  with prediction (any lepton signal)



Relative uncertainty on  $R_{2\text{-jets}}$  due to uncertainty on JES

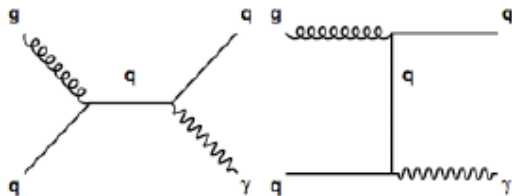


Illustrated is **MSugra SU(4)** compared to **Standard Model** for  $200\text{pb}^{-1}$  of data in the **W/Z + 2 jets** channel

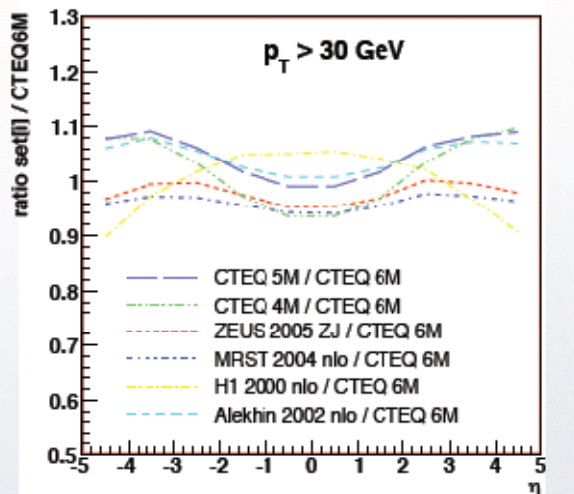
JES of 5% gives  $< 5\%$  uncertainty on the ratio –very much less than the statistical error

# Other ways of getting at high-x gluon – direct photon production?

q-g Compton



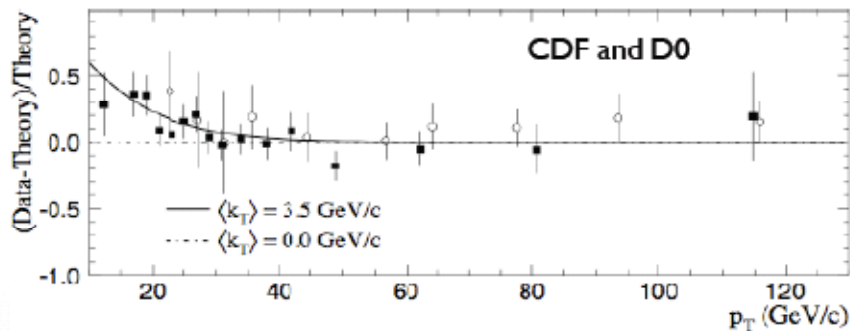
Cross-sections are Compton dominated so there is a chance of some information on the gluon



$\eta$  spectra of the direct-photons differ significantly for different PDFs so there could be new information from a measurement with ~few % experimental errors

However there is a known discrepancy between data at low-pt and the NLO cross-section predictions. This could be due to  $k_T$  of initial state gluons and is expected to be negligible for  $p_T > 60 \text{ GeV}$ .

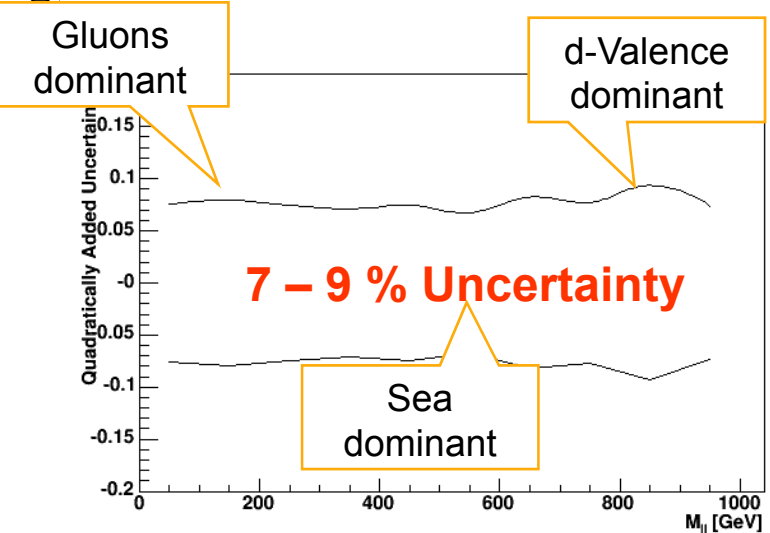
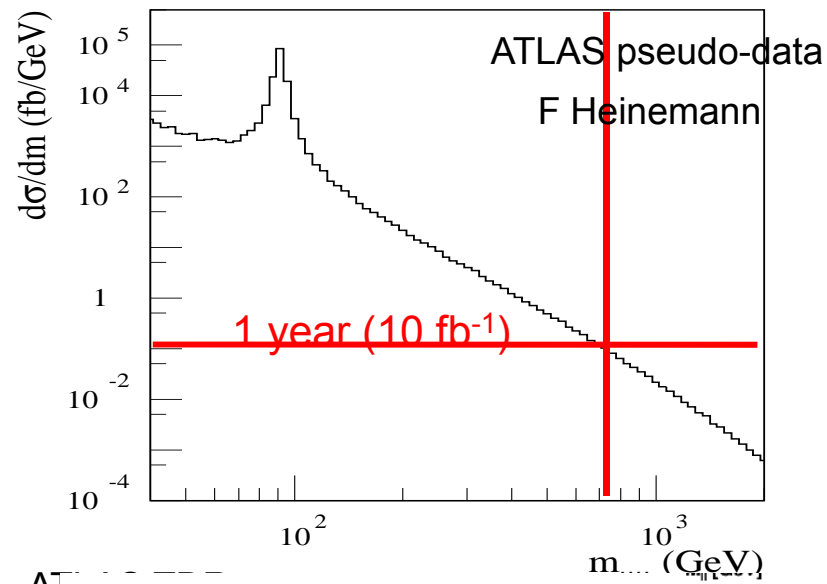
Confirm this and then use high pt data.



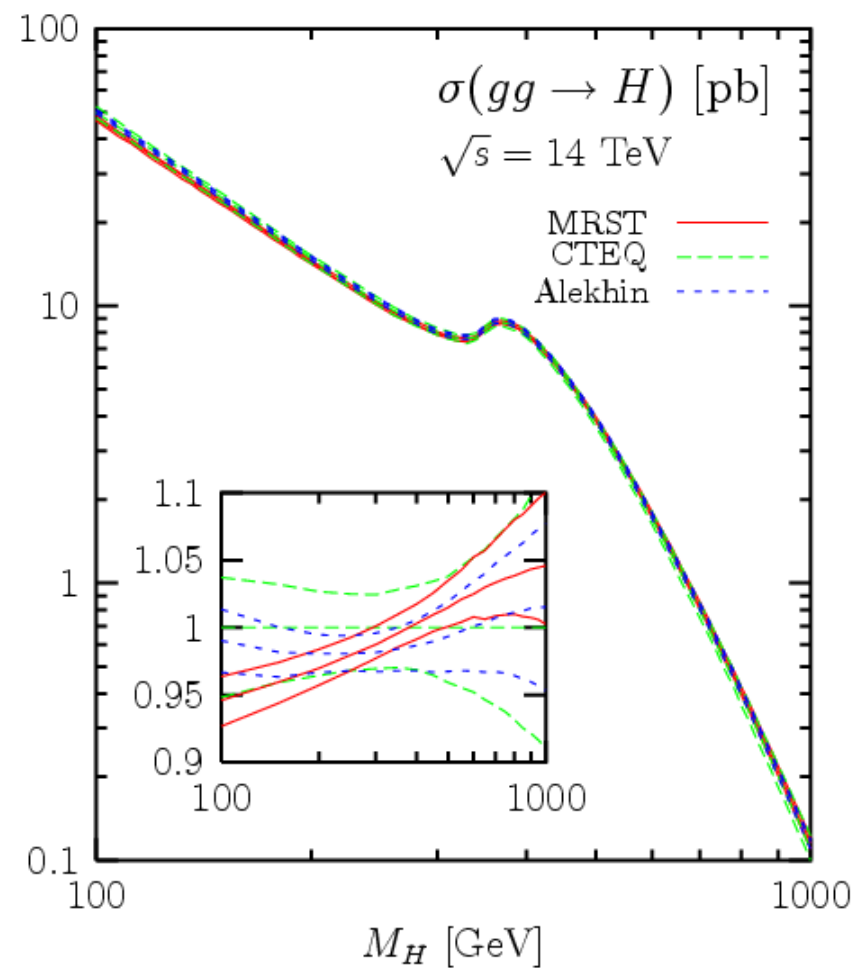


# For what discoveries do PDF uncertainties not hamper us (much)

PDF Uncertainty in High-mass Drell-Yan- won't stop us seeing Zprimes



PDF uncertainties don't affect the Higgs discovery potential too badly

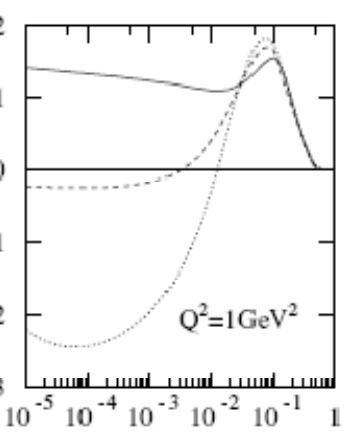


# BEWARE of different sort of 'new physics'

What if low-x behaves very differently?

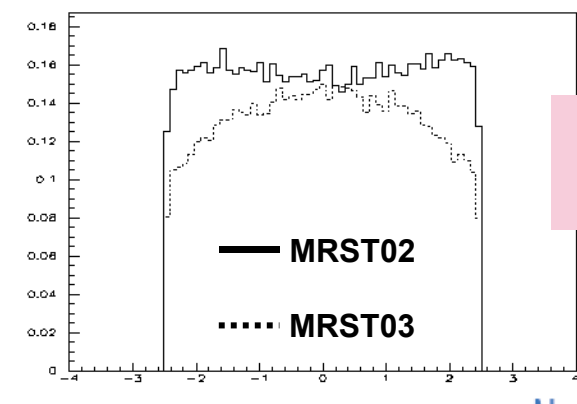
LHC is a low-x machine (at least for the early years of running) **Is NLO (or even NNLO) DGLAP good enough for  $x < 10^{-2}$ . The QCD formalism may need extending at small-x. What is SAFE x?**

•BFKL  $\ln(1/x)$  resummation would change the deduced shape of the gluon



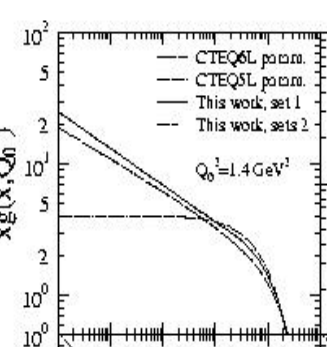
Thorne and White

MRST03 PDFs were a TOY PDF which distrusted all  $x < 10^{-3}$ . This would affect the central region for W production.



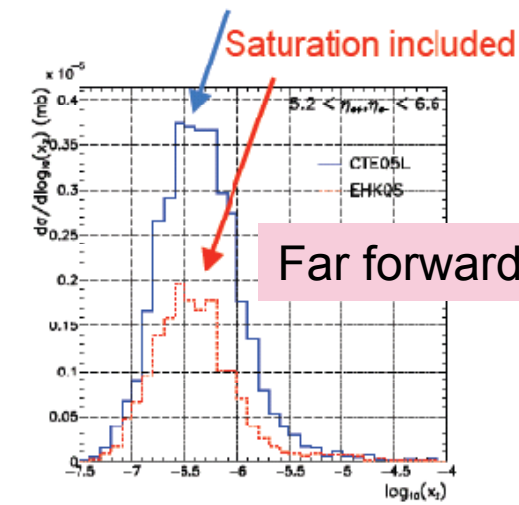
Central rapidity

High density non-linear effects may induce gluon saturation this also affects the deduced shape of the gluon



Eskola et al

Drell-Yan  $M(ee) = 4\text{GeV}$



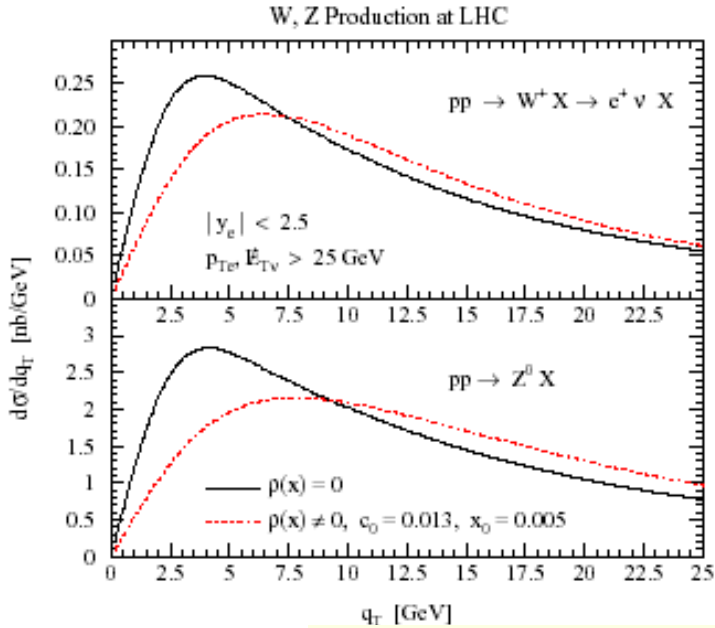
Far forward

And if any of this is true the  $W/Z$  cross-sections are very different - cannot be used as a luminosity monitor until we thoroughly understand low-x physics

| PDF set | $\sigma_{W^+} B_{W \rightarrow l\nu}$<br>(nb) | $\sigma_{W^-} B_{W \rightarrow l\nu}$<br>(nb) | $\sigma_Z B_{Z \rightarrow ll}$<br>(nb) |
|---------|---|---|---|
| MSTW08  | $8.55 \pm 0.15$                               | $6.25 \pm 0.12$                               | $1.38 \pm 0.025$                        |
| MRST03  | 6.88  | 5.23  | 1.18                                    |

But the TOY PDFs are unlikely to be realistic - a better way could be to look at pt spectra for W and Z production

Lack of pt ordering at low-x is a further consequence BFKL resummation AND most non-linear treatments. This would affect the pt spectra for W and Z production at the LHC  
(See hep-ph/0508215)



Conventional  
Unconventional

# Summary

## STANDARD MODEL

- There are W/Z standard candle measurements: Z/W ratio is the best
- W and Z cross-sections should first test our understanding- then contribute to our knowledge at greater precision
- W asymmetry should bring something new
- Beware that NEW low-x physics could compromise this.

HIGGS discovery will not be compromised by PDF uncertainty

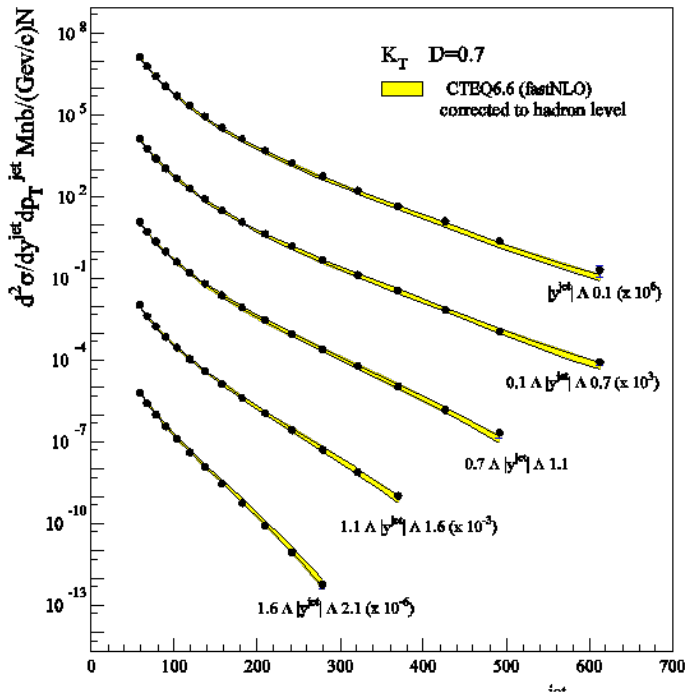
High-mass Z' will not be compromised by PDF uncertainty

## BEYOND STANDARD MODEL

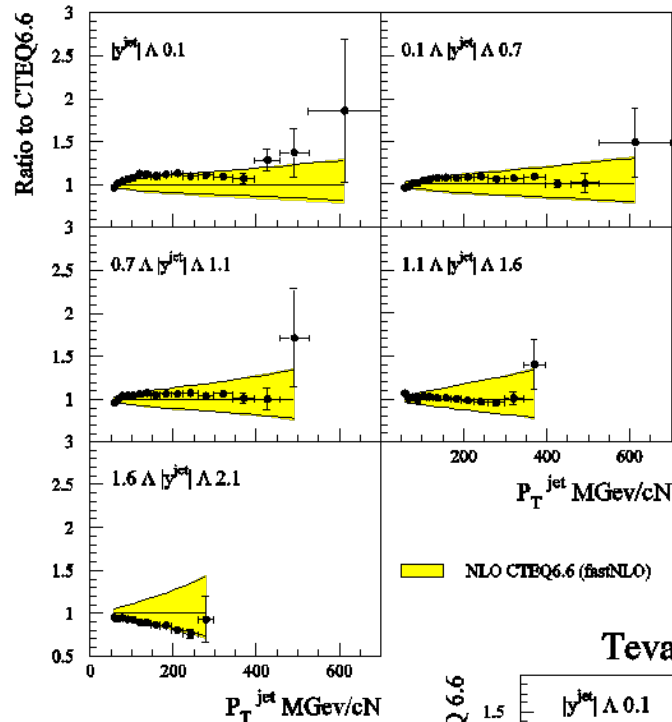
- There are discovery channels – high ET jets- which could be obscured by PDF uncertainties
- PDF uncertainties could be improved by jet measurements at higher  $\eta$  and lower ET- but Jet Energy Scale Uncertainties must be carefully controlled
- Be smart - look at ratios W+n-jets/Z+n-jets
- Direct photon production could also help improve PDF uncertainties

extras

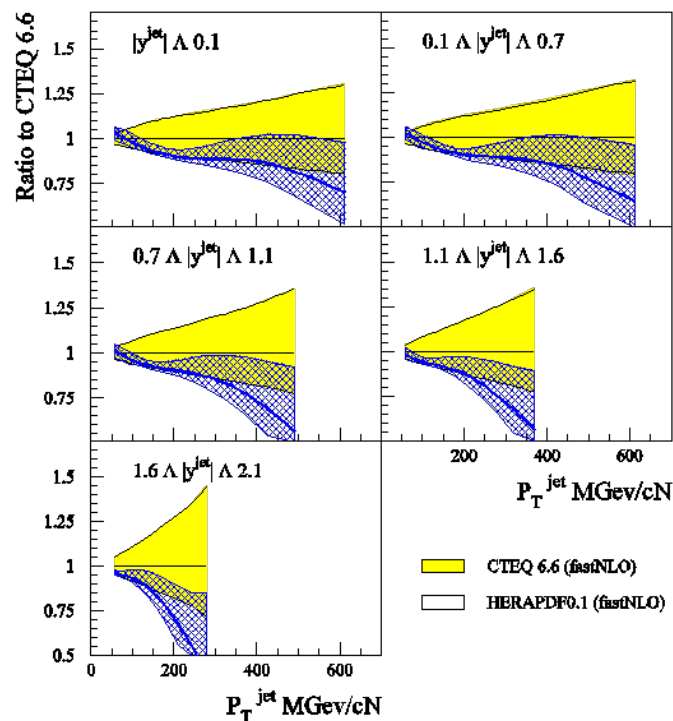
### Tevatron Jet Cross Sections



### Tevatron Jet Cross Sections



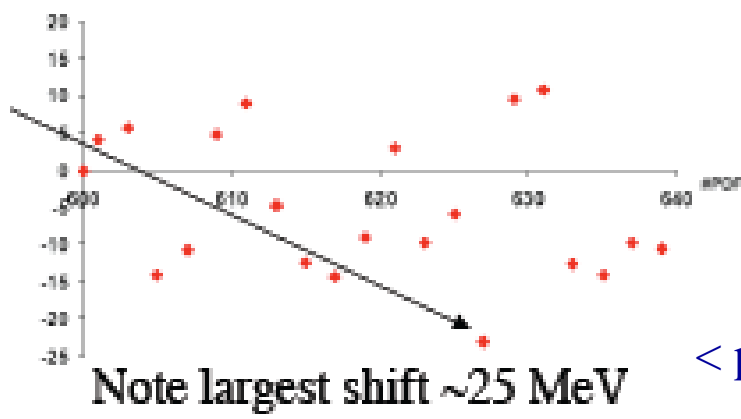
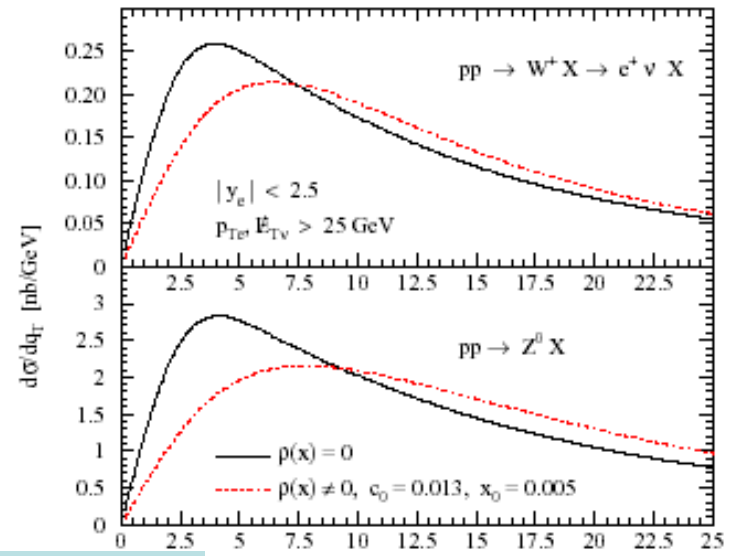
### Tevatron Jet Cross Sections



But the TOY PDFs are unlikely to be realistic - a better way could be to look at pt spectra for W and Z production

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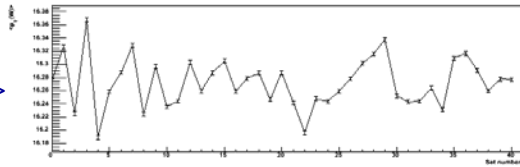
Pt spectra are also used to measure  $M_W$  --  $dM_W$  from PDF uncertainties, using  $pt(e)$ , is  $\sim 20$  MeV



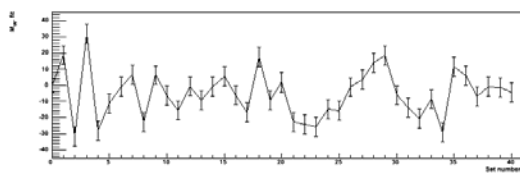
So we'd better be sure we've got the calculations for Pt spectra right

Conventional  
Unconventional

$\langle p_T(W) \rangle$



$\delta M_W(\text{fit})$



Same pattern