

# PDF sensitivity with LHCb

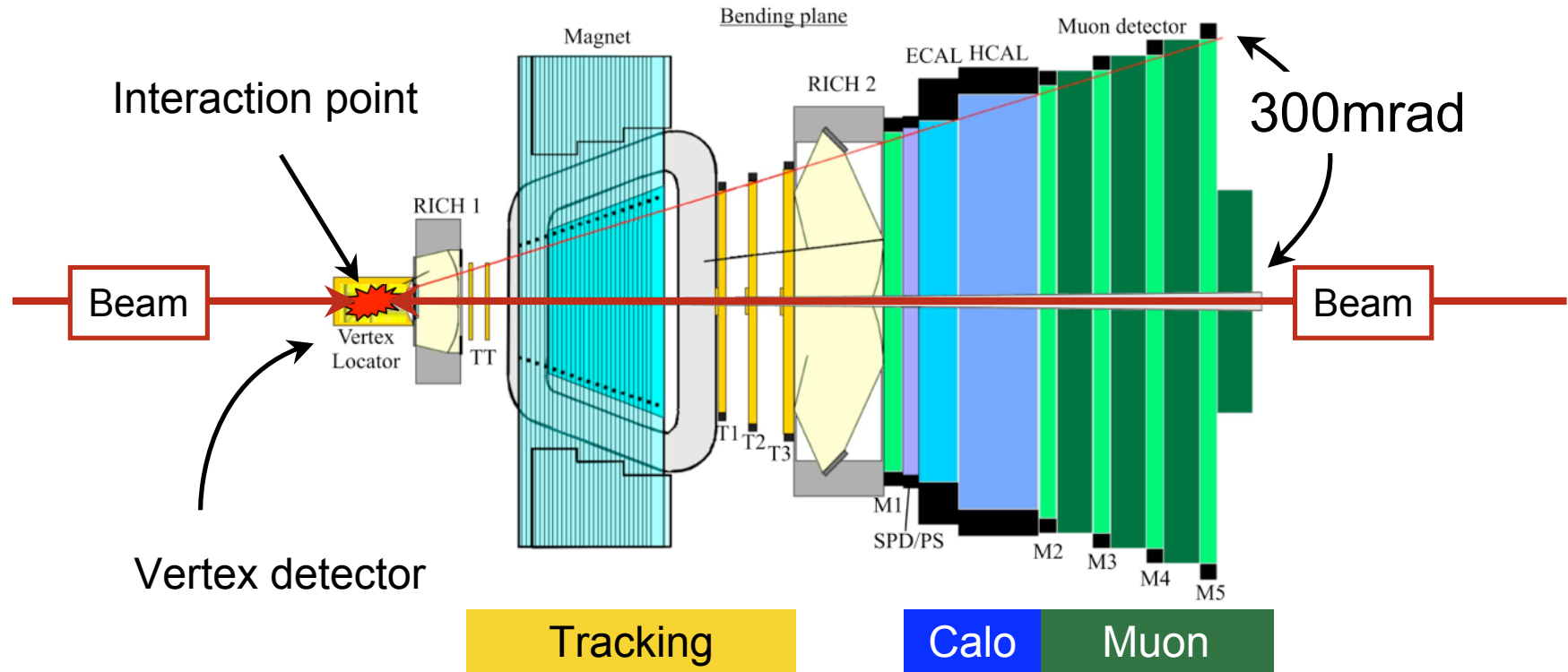
Tara Shears, for the LHCb electroweak group.

# 1. Introduction

2. High  $Q^2$  measurements
3. Low  $Q^2$  measurements
4. Conclusions

## LHCb

Kinematic range  
Measurements



Fully instrumented within  $1.9 \leq \eta \leq 4.9$   
Trigger:  $p_\mu > 3 \text{ GeV}$ ,  $pt_\mu > 0.5 \text{ GeV}$ ,  $m_{\mu\mu} > 2.5 \text{ GeV}$

# 1. Introduction

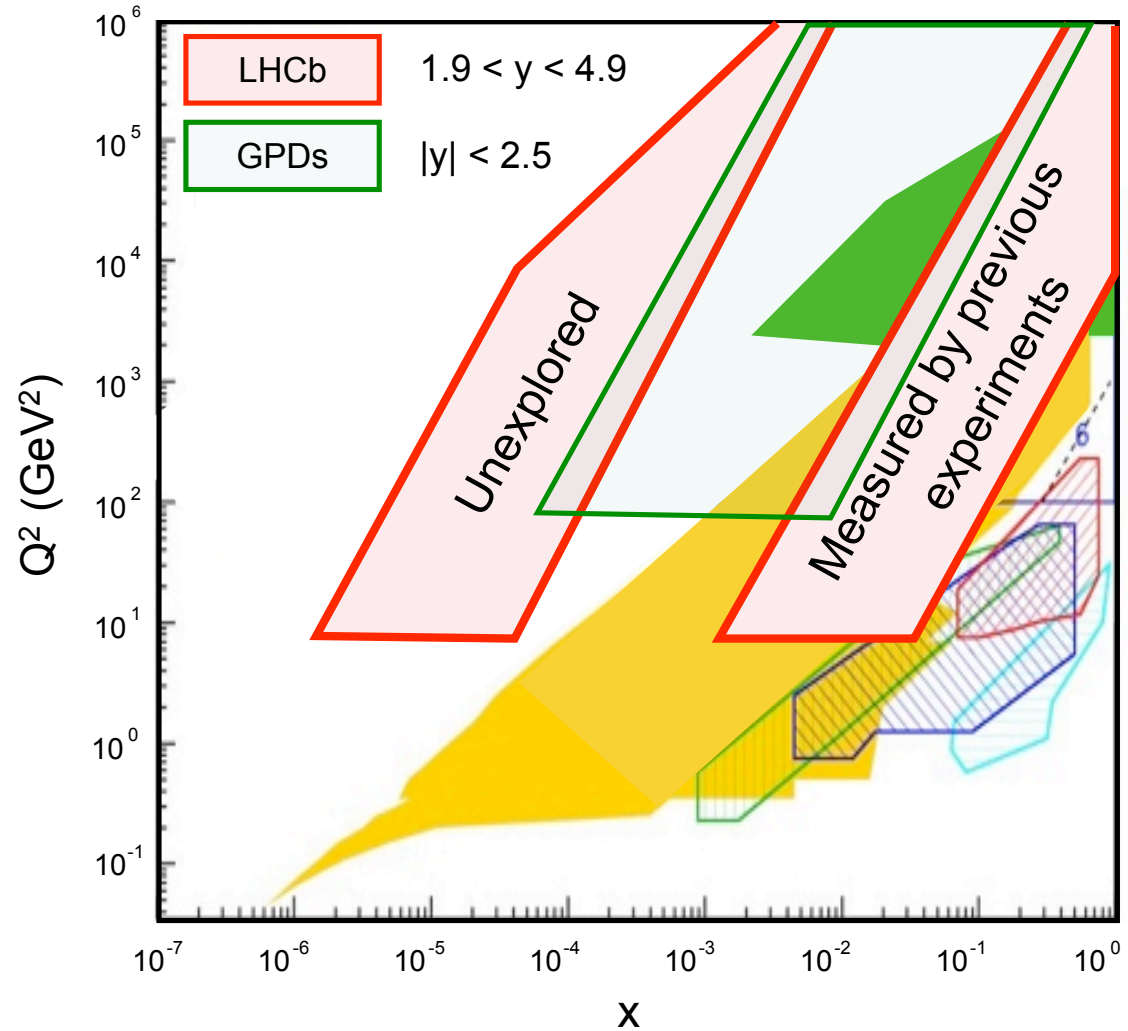
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LHCb

## Kinematic range

Measurements

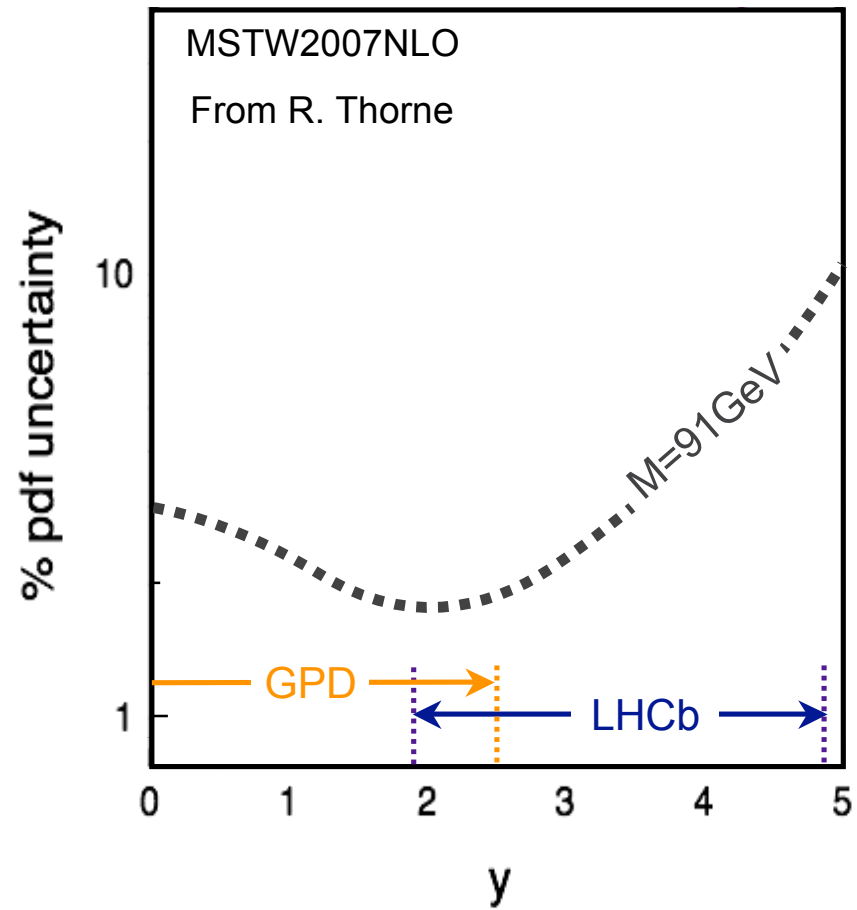
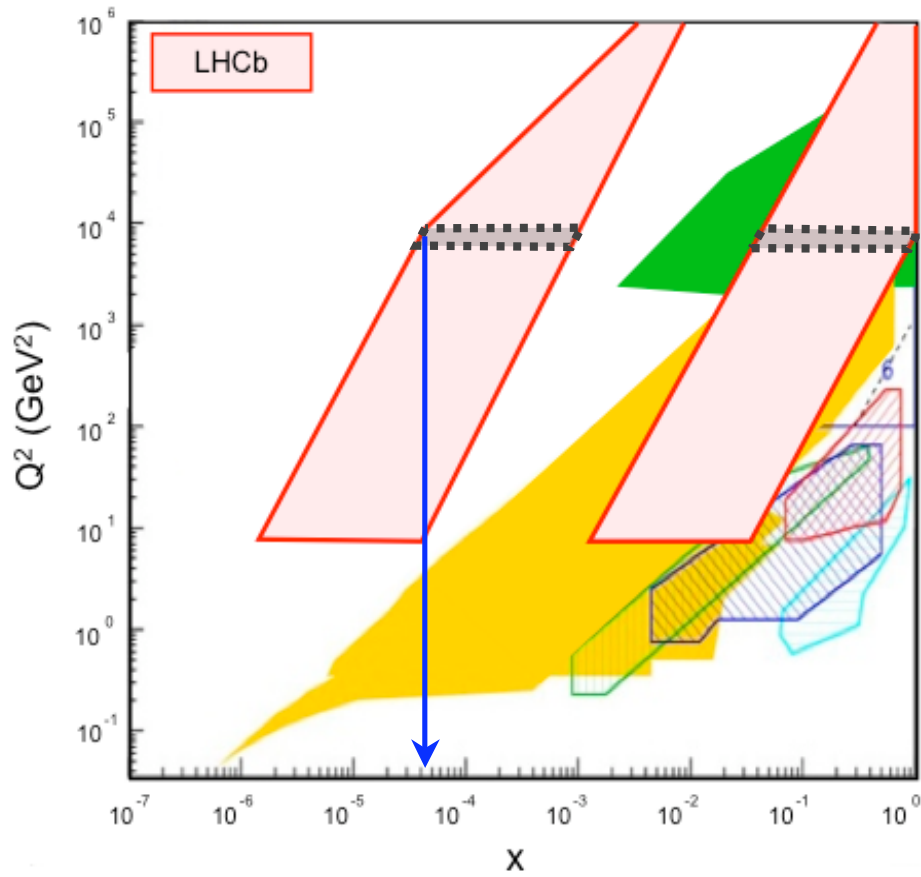
Angular acceptance + trigger thresholds ensure range of low  $x$ , high and low  $Q^2$  can be probed.



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LHCb  
**Kinematic range**  
Measurements



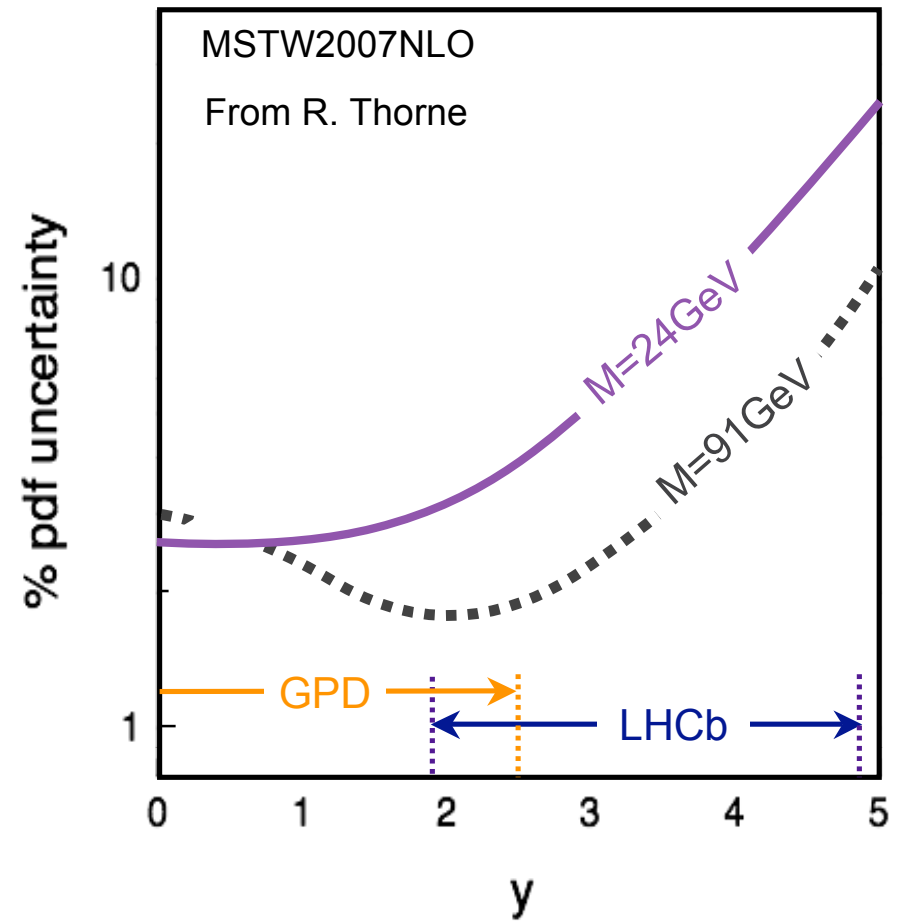
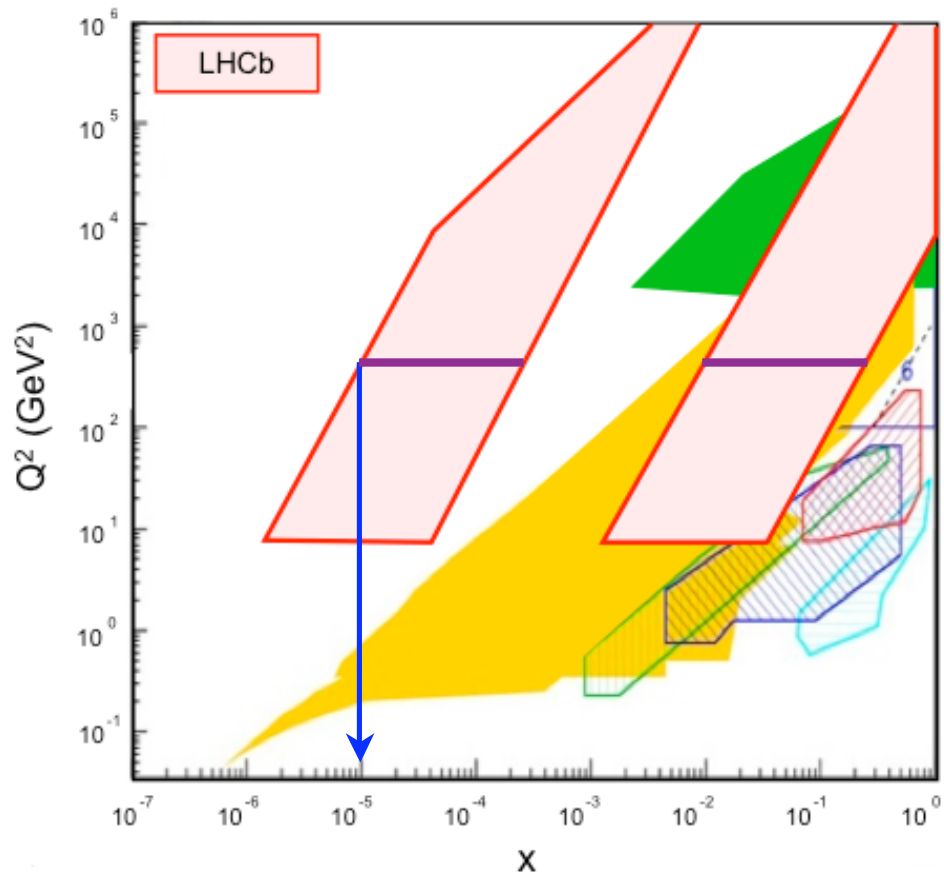
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## Kinematic range

Measurements



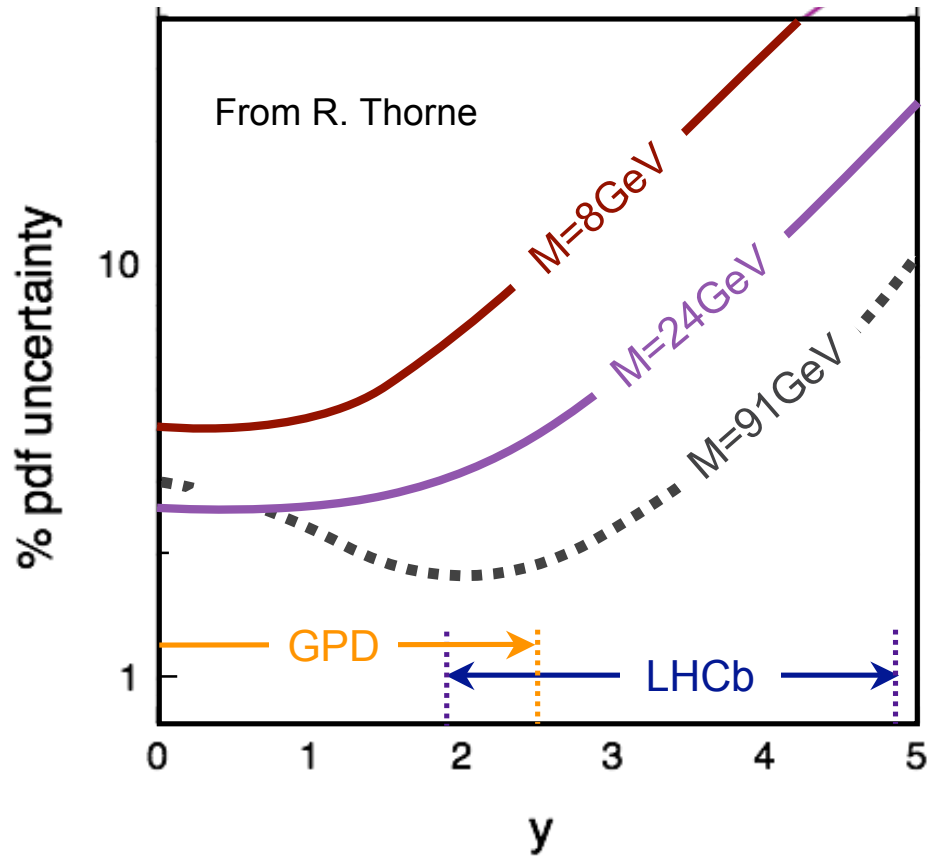
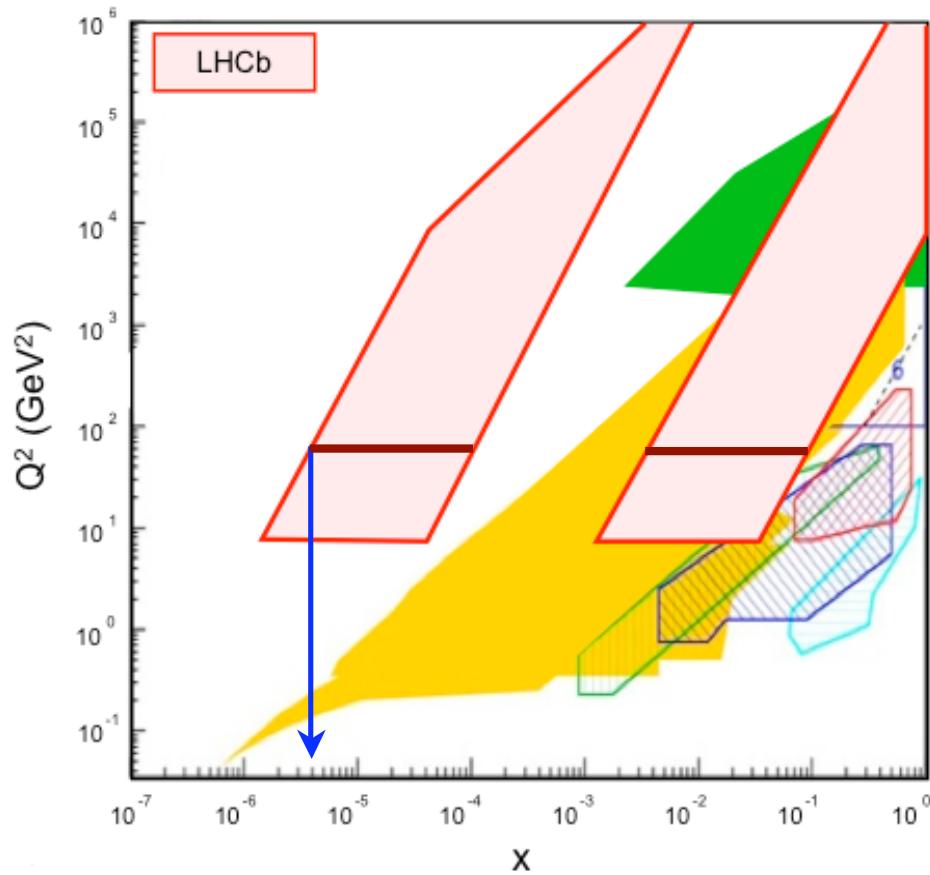
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## Kinematic range

Measurements



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LHCb

Kinematic range

## Measurements

$$Z \rightarrow \mu\mu$$

$$W \rightarrow \mu\nu_\mu$$

$$\gamma^* \rightarrow \mu\mu$$

Probing:

$$Q^2 = 10^4 \rightarrow 10$$

$$x = 10^{-4} \rightarrow 10^{-6}$$

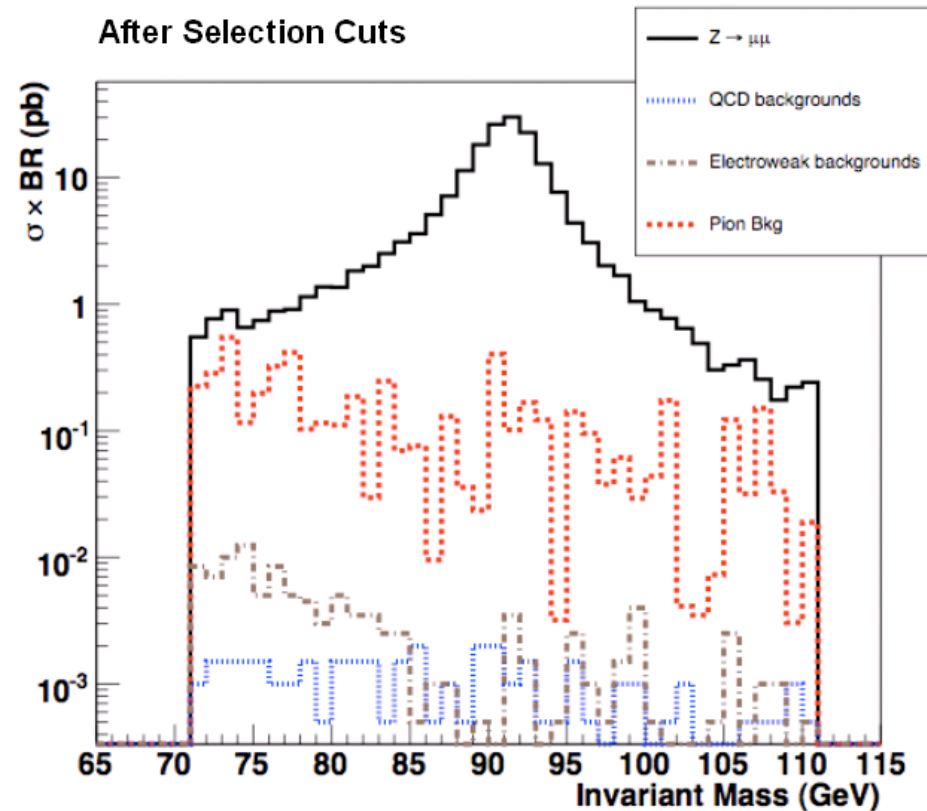
**Trigger:**

- 2 muons,  $pt_{\mu} > 10$  GeV
- $M_{\mu\mu} > 50$  GeV

**Reconstruct:**

- $pt_{\mu}^{1(2)} > 20$  (15) GeV
- $IP_{\mu}$  significance  $< 5$
- $E_{had} < 50$  GeV
- $71 < M_{\mu\mu} < 111$  GeV

Trigger efficiency 86%;  
 Selection efficiency 91%;  
 Purity 97%.



See J. Anderson, CERN-THESIS-2009-020



**Trigger:**

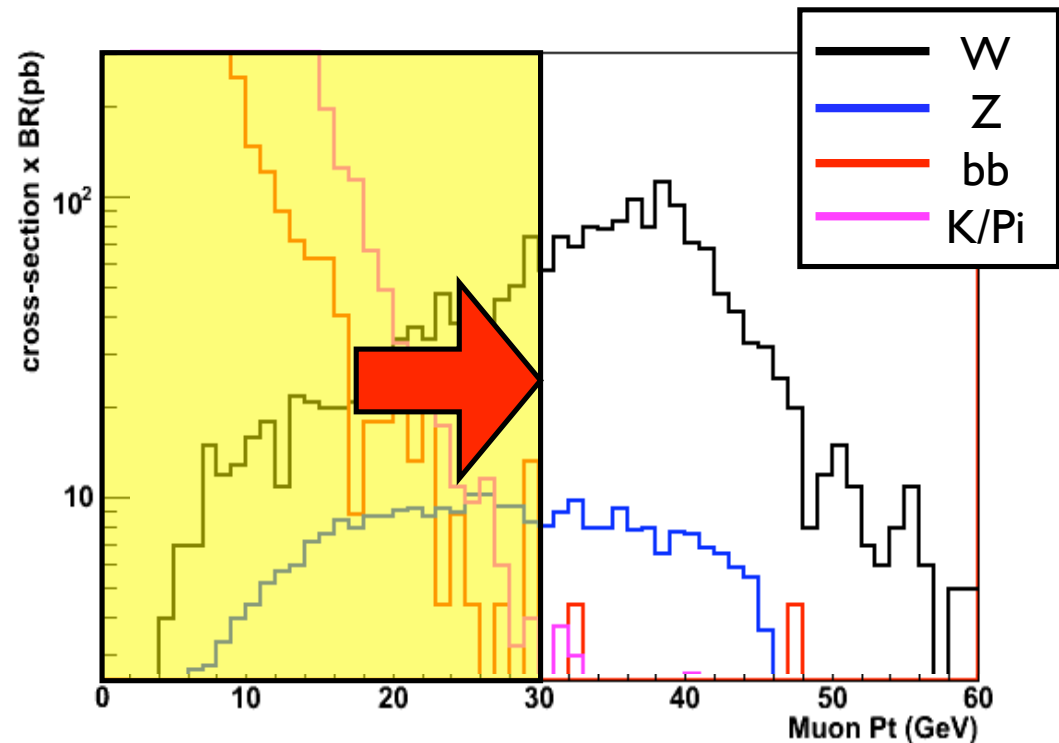
- $pt_{\mu} > 20$  GeV

**Reconstruct:**

- $pt_{\mu} > 30$  GeV
- $pt$  asymmetry  $A_{pt} > 0.85$

$$A_{pt} = \frac{pt_{\mu} - pt_{rest}}{pt_{\mu} + pt_{rest}}$$

Trigger efficiency 74%;  
Selection efficiency 35%;  
Purity 90%.



See S. Traynor, DIS09

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Z

W

Ratios

Fitting differential cross-sections

% Measurement Uncertainties with $100\text{pb}^{-1}$		
	$W \rightarrow \mu\nu_\mu$	$Z \rightarrow \mu\mu$
Statistical	0.5	0.8
Background	0.3	0.2
Reconstruction efficiency	0.2	0.3
Trigger Efficiency	0.1	0.1
Luminosity	1-5	1-5

Note: estimates (still under study).

1. Introduction

## 2. High $Q^2$ measurements

3. Low  $Q^2$  measurements

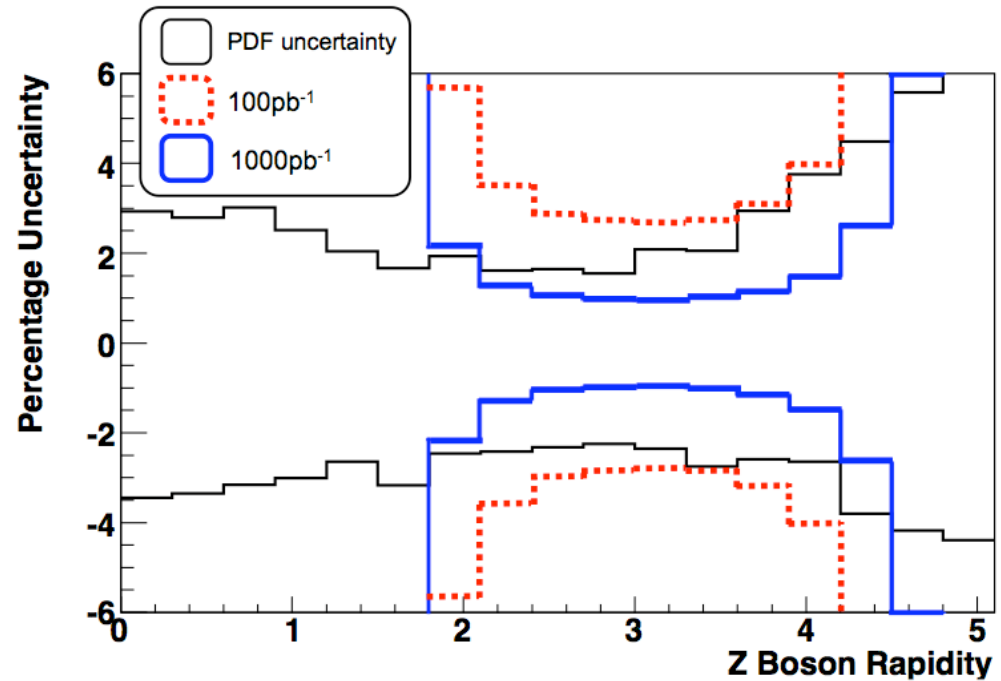
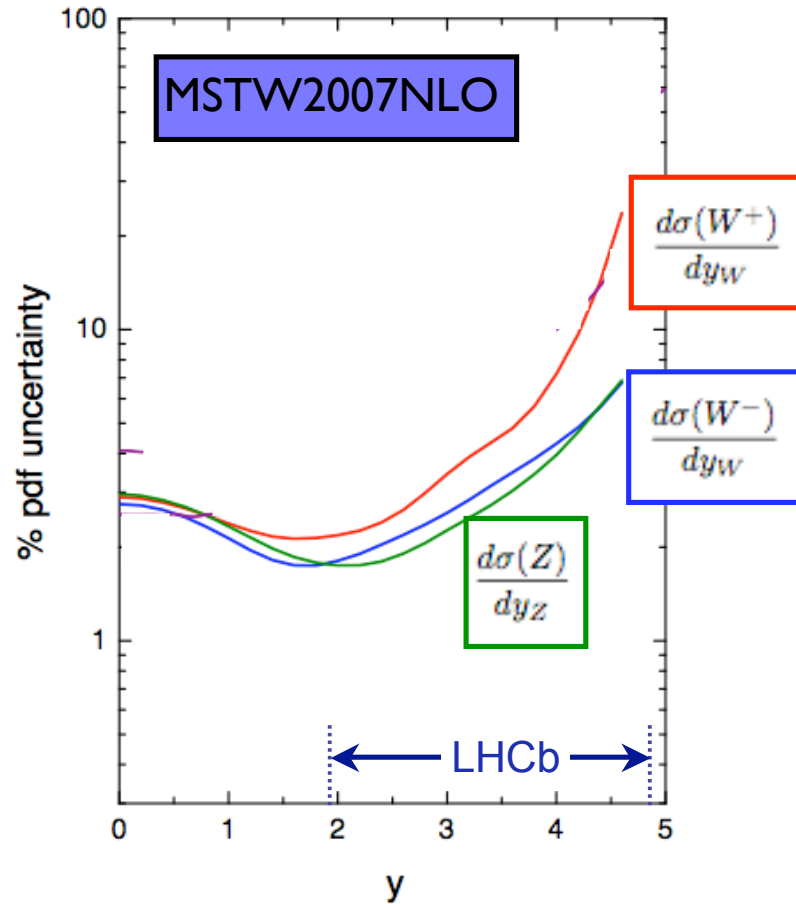
4. Conclusions

Z

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Ratios

Fitting differential cross-sections



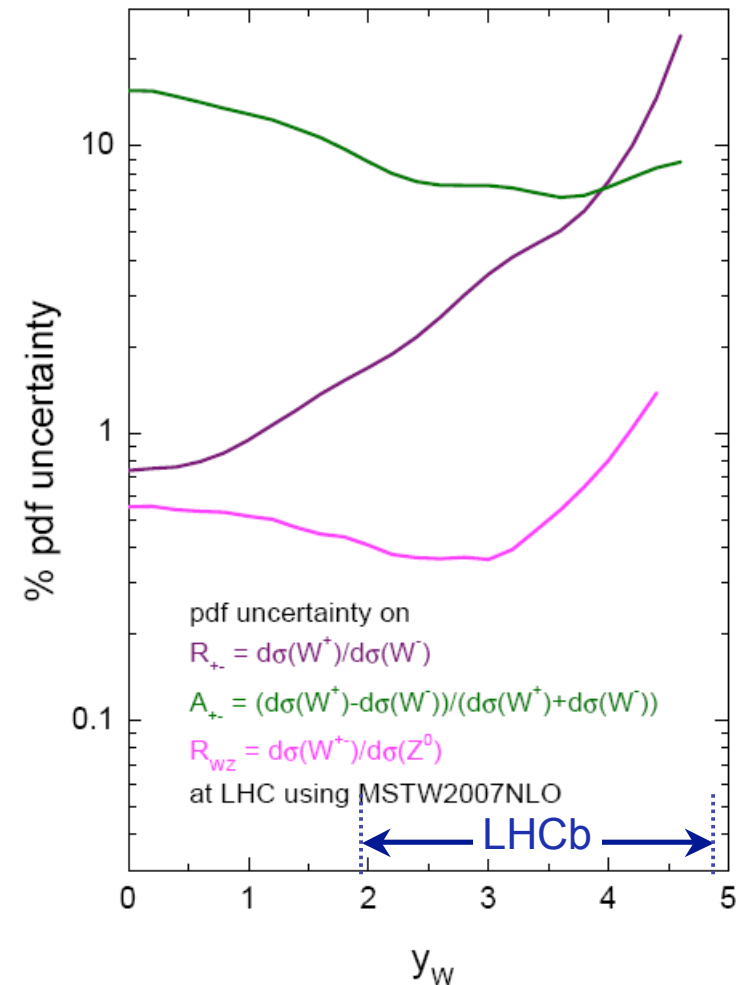
Similar experimental precision for W

## Ratios of W, Z production reduce lumi dependence

$R_{+-}$  : sensitive to d/u ratio

$R_{WZ}$ : many theoretical  
uncertainties cancel: test  
Standard Model (0.4%)

$A_{+-}$ : sensitive to  $u_v$   $d_v$  difference



**But** more information obtained by fitting W, Z **together**

## Idea:

compare measured  $d\sigma/dy$  for W, Z to PDF prediction,  
**constraining PDFs and fitting integrated luminosity.**

## Test:

- Choose a PDF set. Take central value to be **truth**
- Generate many pseudo-data sets (assuming multinomial distribution for eigenvector errors), corresponding to a given luminosity
- Fit each pseudo-data set: **pseudo-measurement**
- Compare **pseudo-measurement** to **truth**
  - centre of distribution gives bias
  - width of distribution gives precision

Method using **MSTW, CTEQ, Alekhin**;

$f_0 = \frac{d\sigma}{dy}$  : distribution obtained with central eigenvectors

$f_i = \frac{d\sigma}{dy} (\lambda_i = 1, \lambda_{\neq i} = 0)$  : distribution with  $i^{\text{th}}$  e.v. moved  $1\sigma$

Fit

$$\chi^2(\lambda_0, \lambda_i) = \sum_{j=1}^{\#bins} \left[ \frac{x_j - \lambda_0 (f_0 + \lambda_i (f_i - f_0))}{\sigma_j} \right]^2 + \sum_{i=1}^{\#e.v.} \lambda_i^2$$

Normalisation (Luminosity)  $\nearrow$

$\uparrow$  data in  $j$  bins, each with uncertainty  $\sigma$

Method using NNPDF;

$$f_i = \frac{d\sigma}{dy} \quad \text{for } i^{\text{th}} \text{ replica}$$

$$\text{Fit} \quad \chi^2(\lambda_0) = \sum_{j=1}^{\#bins} \left[ \frac{x_j - \lambda_0 f_i}{\sigma_j} \right]^2$$

... and only consider consistent replicas  
(Chisquared probability > 1 %)

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Z  
W  
Ratios

## Fitting differential cross-sections

	0.1 fb <sup>-1</sup>			
	MSTW08	CTEQ66	Alekhin	NNPDF
W+	1.8	2.4	2.0	2.9
W-	1.9	2.6	2.2	2.7
Z	1.9	2.4	2.2	2.4
WWZ	1.7	2.3	1.8	2.0
	1 fb <sup>-1</sup>			
	MSTW08	CTEQ66	Alekhin	NNPDF
W+	1.6	2.2	1.8	2.4
W-	1.6	2.3	2.1	2.4
Z	1.7	2.1	1.9	1.8
WWZ	1.3	2.1	1.4	2.2
	10 fb <sup>-1</sup>			
	MSTW08	CTEQ66	Alekhin	NNPDF
W+	1.3	2.0	1.5	2.5
W-	1.2	1.9	1.6	3.0
Z	1.4	1.9	1.9	1.9
WWZ	0.8	1.7	1.0	-

Percentage statistical uncertainty on **fitted luminosity**



- Method could have bias if correct PDF not known.
- Selecting only good fits with  $\chi^2$  probability  $> 1\%$  allows **test of PDF model consistency**
- Reduces systematic uncertainty due to model dependence

	0.1 fb <sup>-1</sup>		
	CTEQ66	Alekhin	NNPDF
W+	-3.2	-3.7	5.0
W-	0.1	-2.0	-1.5
Z	-1.4	-5.6	3.4
WWZ	-0.7	-3.6	5.0

Percentage bias on fitted luminosity generated with MSTW08  
central values

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Z

W

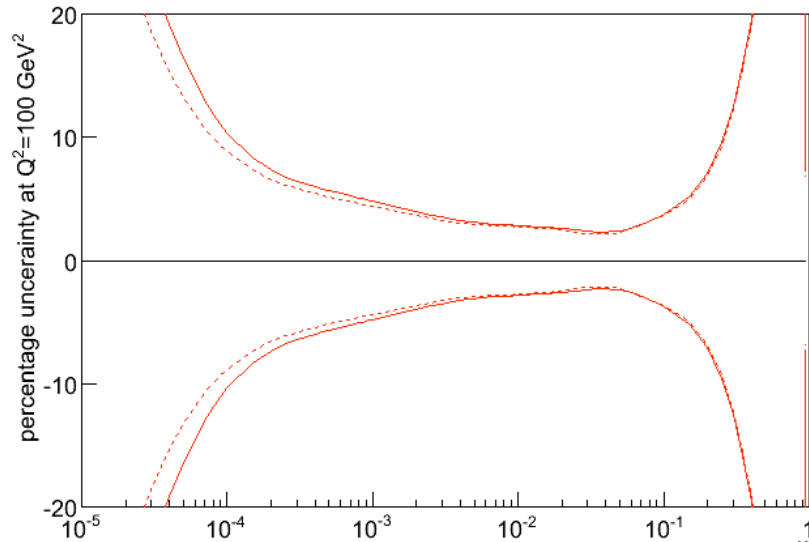
Ratios

**Fitting differential cross-sections**

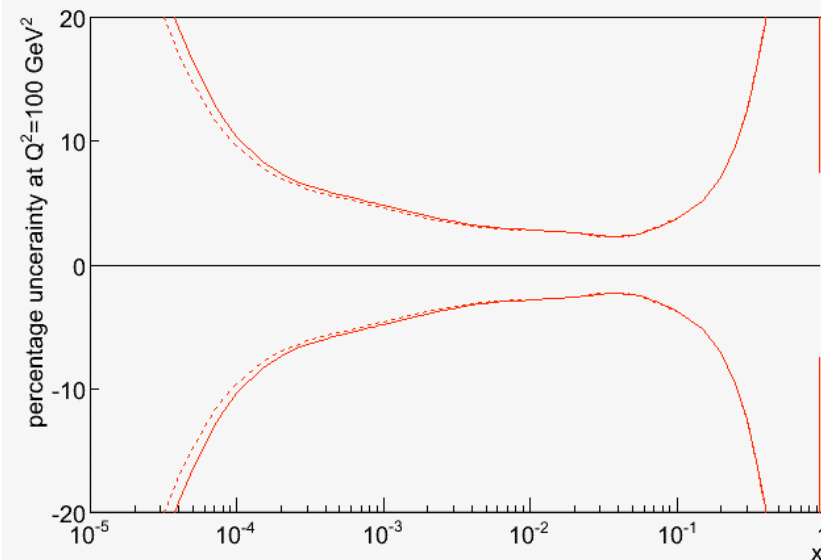
This procedure fits eigenvalues as well as luminosity.

- it can constrain our knowledge of the PDFs.

Gluon



Gluon de-weighted



## Effect on gluon PDF for MSTW08 ( $1\text{fb}^{-1}$ )

solid line: current uncertainty

dashed line: with LHCb **Z data**

### Straight fit

$x=10^{-4}$ , 11%  $\rightarrow$  8%

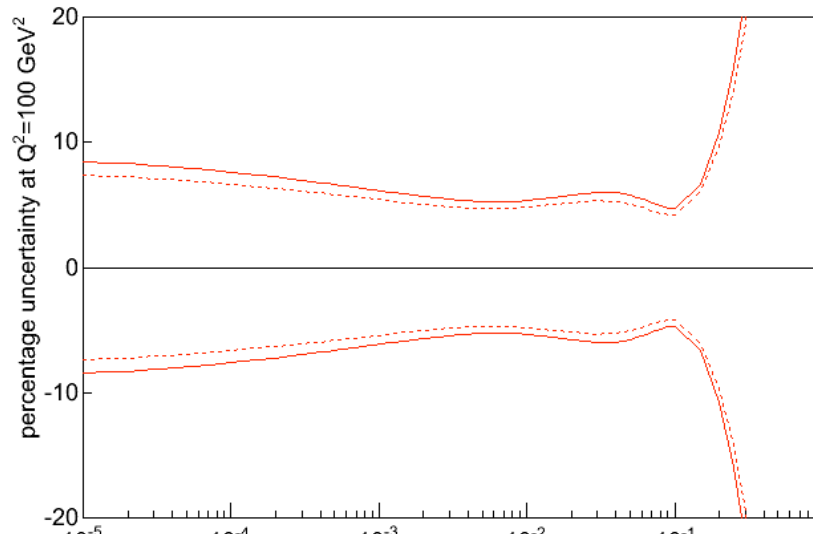
$x=5 \cdot 10^{-5}$ , 17%  $\rightarrow$  13%

### Deweighted fit

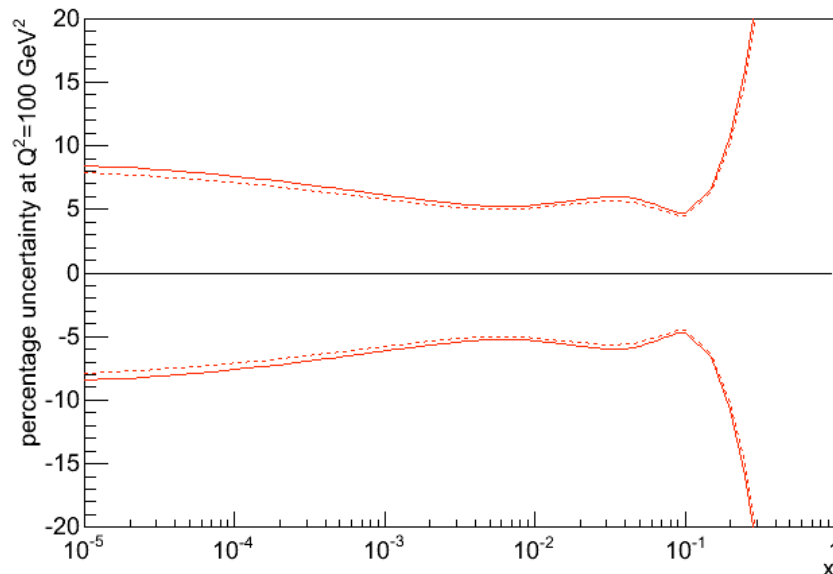
$x=10^{-4}$ , 11%  $\rightarrow$  10%

$x=5 \cdot 10^{-5}$ , 17%  $\rightarrow$  15%

Gluon CTEQ66



Gluon CTEQ66 de-weighted



## Effect on gluon PDF for CTEQ66 ( $1\text{fb}^{-1}$ )

### Straight fit

$$x=10^{-4}, \quad 7.5\% \rightarrow 6.5\%$$

$$x=5 \cdot 10^{-5}, \quad 7.5\% \rightarrow 6.5\%$$

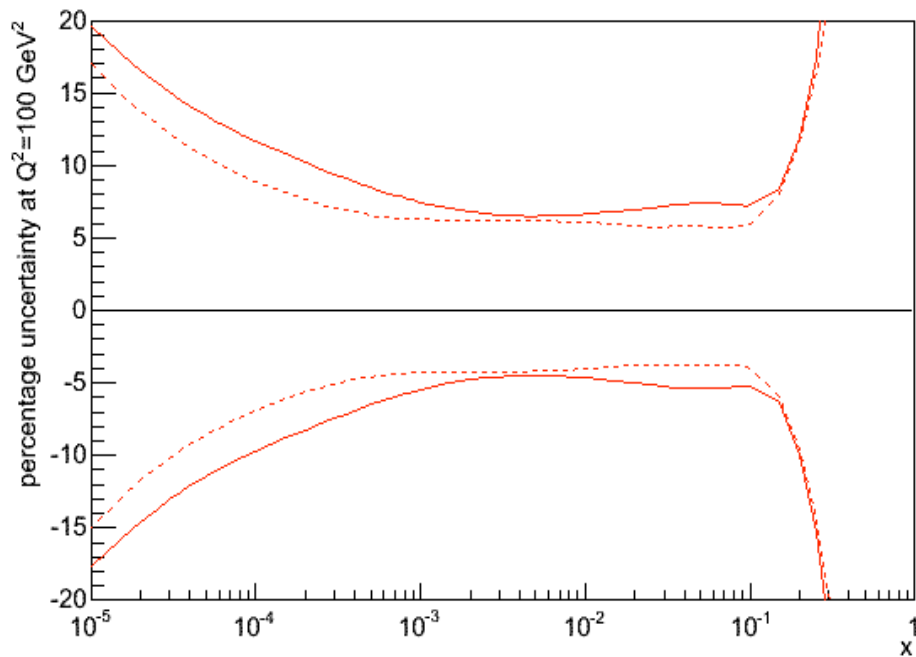
### Deweighted fit

$$x=10^{-4}, \quad 7.5\% \rightarrow 7\%$$

$$x=5 \cdot 10^{-5}, \quad 7.5\% \rightarrow 7\%$$

(Smaller difference because impact of data is less)

Gluon NNPDF1.0



**Effect on gluon PDF for  
NNPDF1.0 ( $1\text{fb}^{-1}$ )**

$x=10^{-4}$ , 12%  $\rightarrow$  9%

$x=5 \cdot 10^{-5}$ , 13%  $\rightarrow$  11%

1. Introduction

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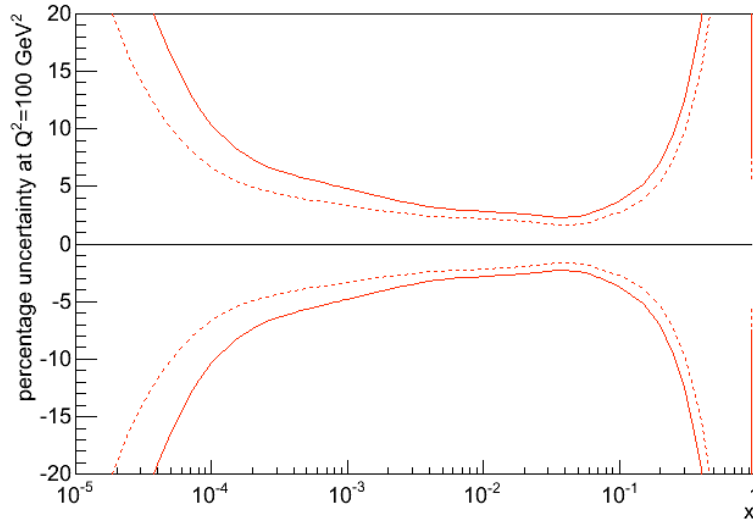
Z

W

Ratios

### Fitting differential cross-sections

Gluon MSTW08

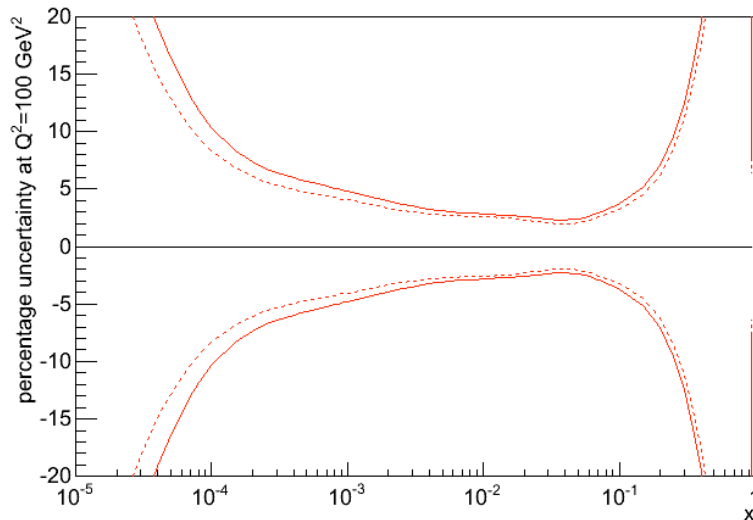


### Effect on gluon PDF for MSTW08 ( $1\text{fb}^{-1}$ ) using WWZ data

$x=10^{-4}$ , 11%  $\rightarrow$  7% (8%)

$x=5 \cdot 10^{-5}$ , 17%  $\rightarrow$  10% (13%)

Gluon MSTW08 de-weighted



New: thanks Francesco

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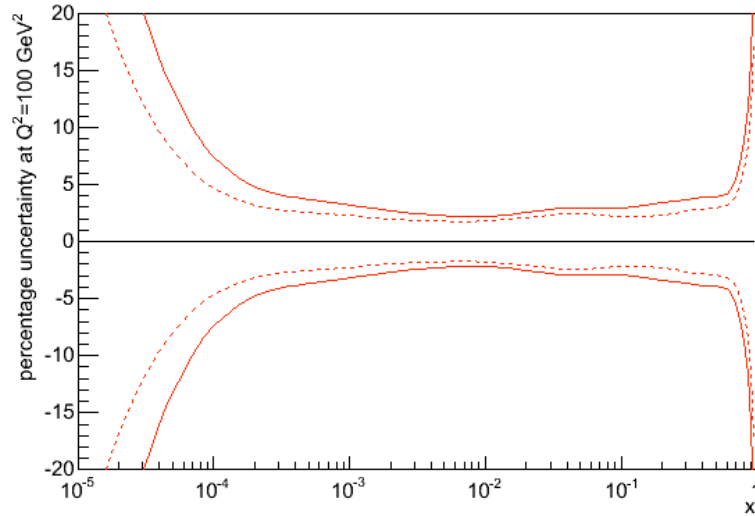
Z

W

Ratios

## Fitting differential cross-sections

$u_V$  MSTW08

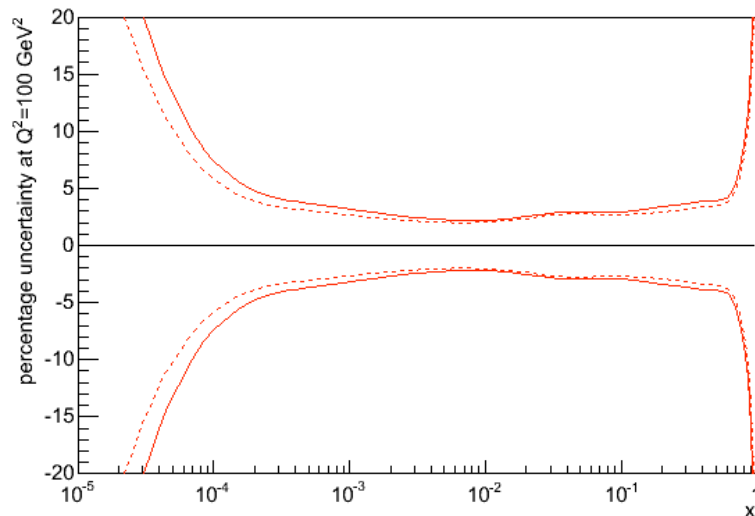


**Effect on  $u_V$  PDF for MSTW08  
( $1\text{fb}^{-1}$ ) using WWZ data**

$x=10^{-4}$ , 8%  $\rightarrow$  4% (6%)

$x=5 \cdot 10^{-5}$ , 15%  $\rightarrow$  10% (13%)

$u_V$  MSTW08 de-weighted



**New: thanks Francesco**

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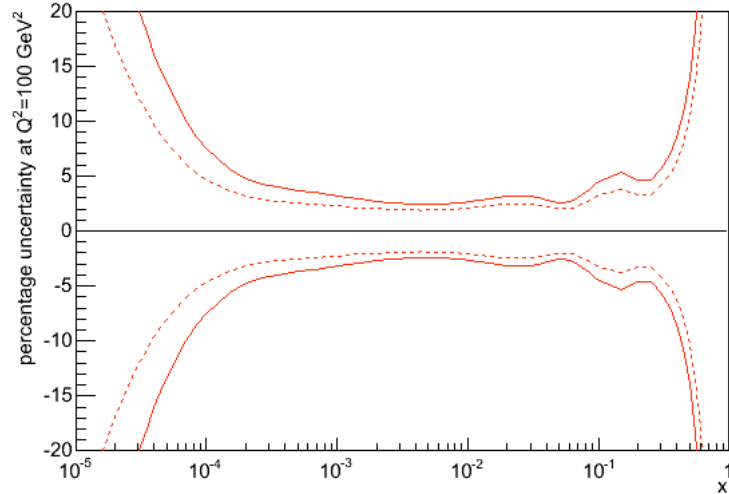
Z

W

Ratios

## Fitting differential cross-sections

$d_V$  MSTW08

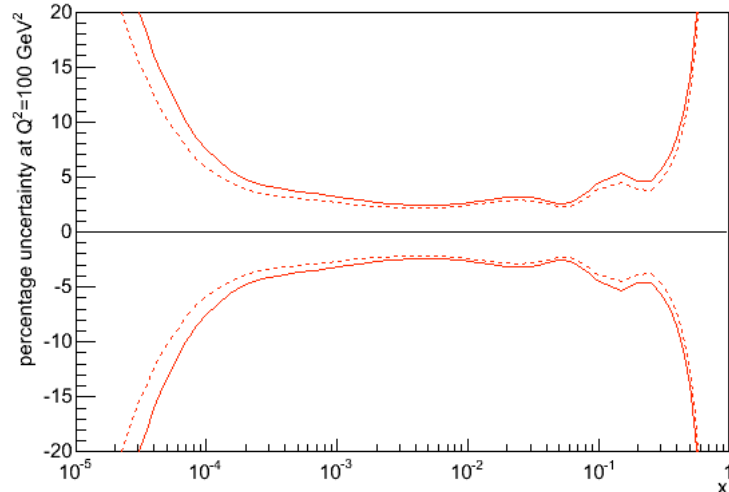


### Effect on $d_V$ PDF for MSTW08 ( $1\text{fb}^{-1}$ ) using WWZ data

$x=10^{-4}$ , 8%  $\rightarrow$  5% (6%)

$x=5 \cdot 10^{-5}$ , 17%  $\rightarrow$  10% (14%)

$d_V$  MSTW08 de-weighted



New: thanks Francesco



**Trigger:**

- 2 muons,  $\sum p_{t\mu} > 1.6$  GeV

**Reconstruct:**

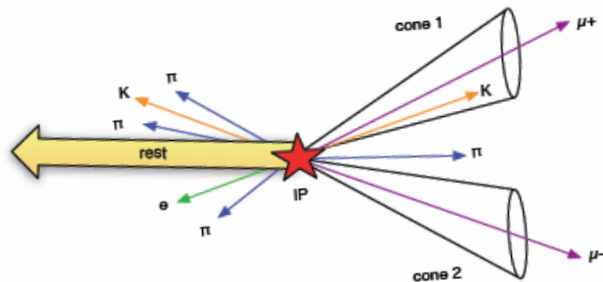
- $p_{\mu} > 21$  GeV
- $IP_{\mu}$  significance  $< 3$
- $P_{\mu}$  asymmetry variables

$A(P_{\mu 1}, P_{\text{cone1}})$

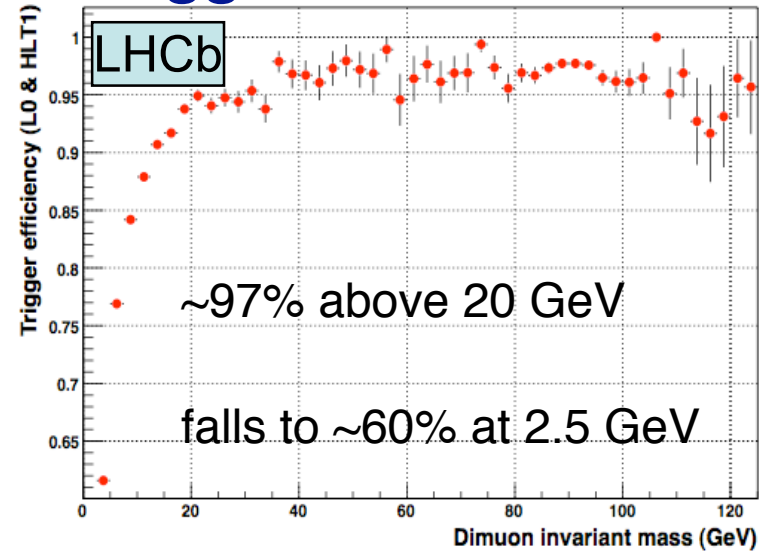
$A(P_{\mu 2}, P_{\text{cone2}})$

$A(P_{\mu 1} + P_{\mu 2}, P_{\text{rest}})$

$A(P_{\text{cone1}} + P_{\text{cone2}}, P_{\text{rest}})$



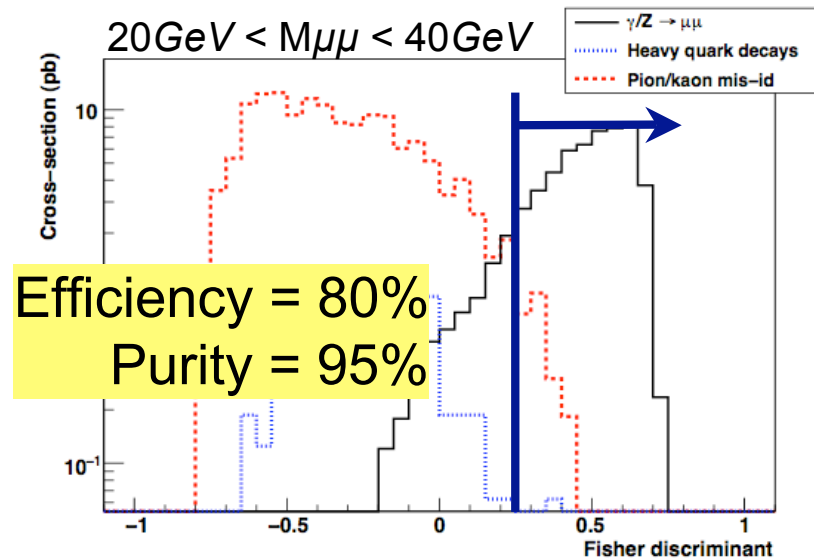
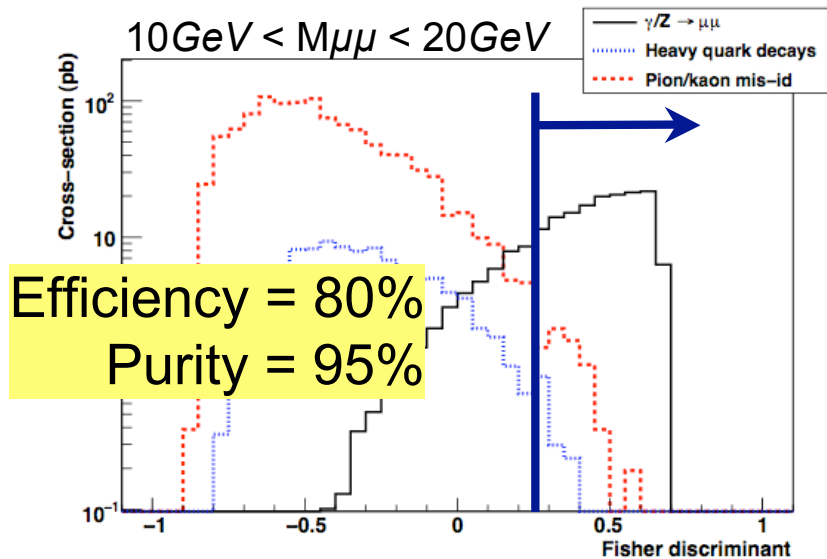
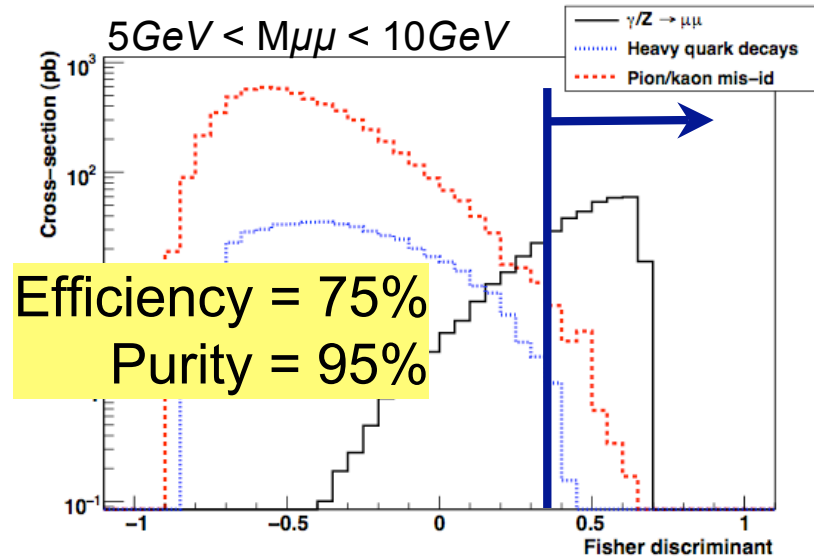
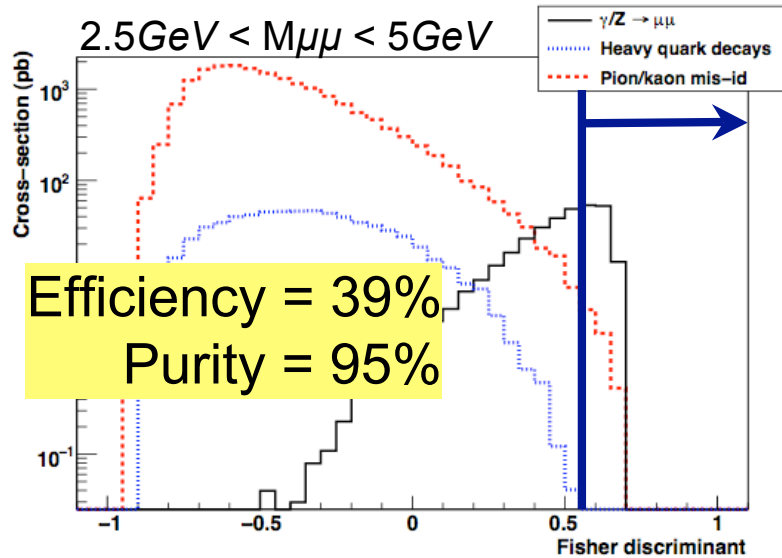
**Trigger**



See J. Anderson, DIS09

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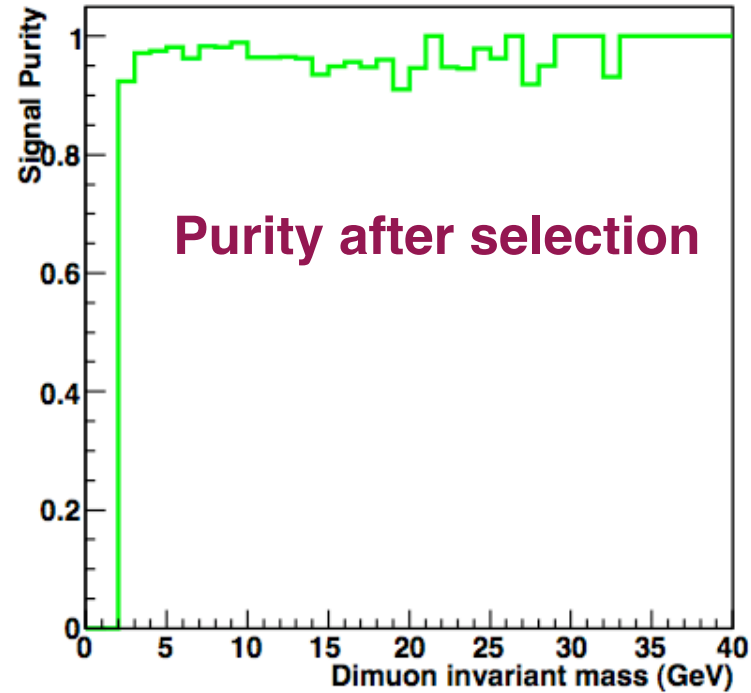
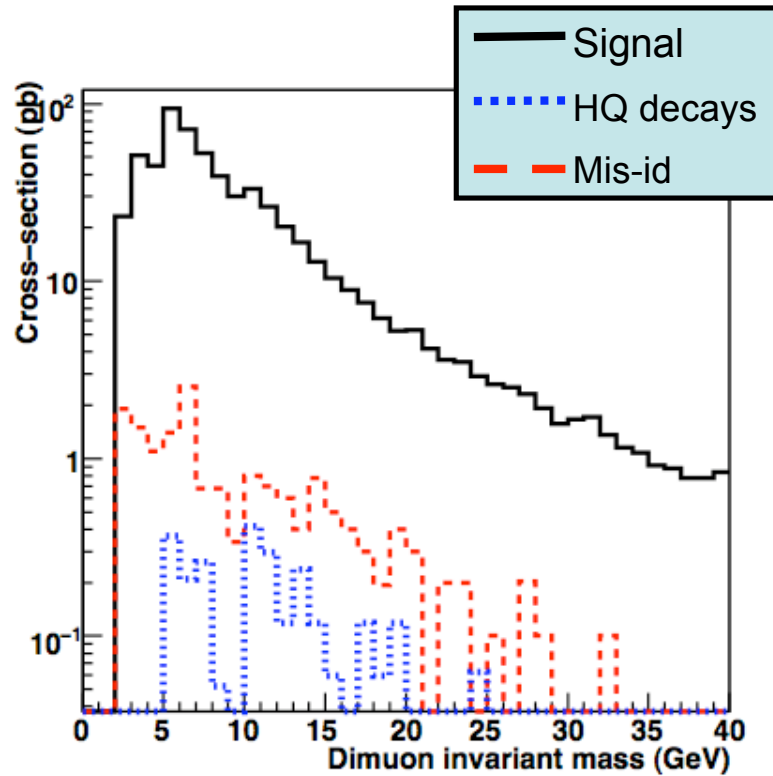
$\gamma^*$



Combine variables into Fisher discriminant

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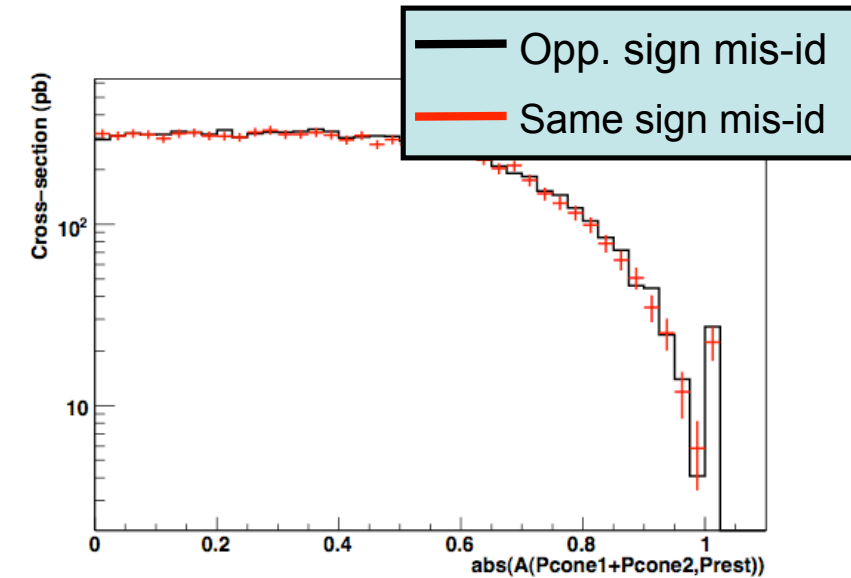
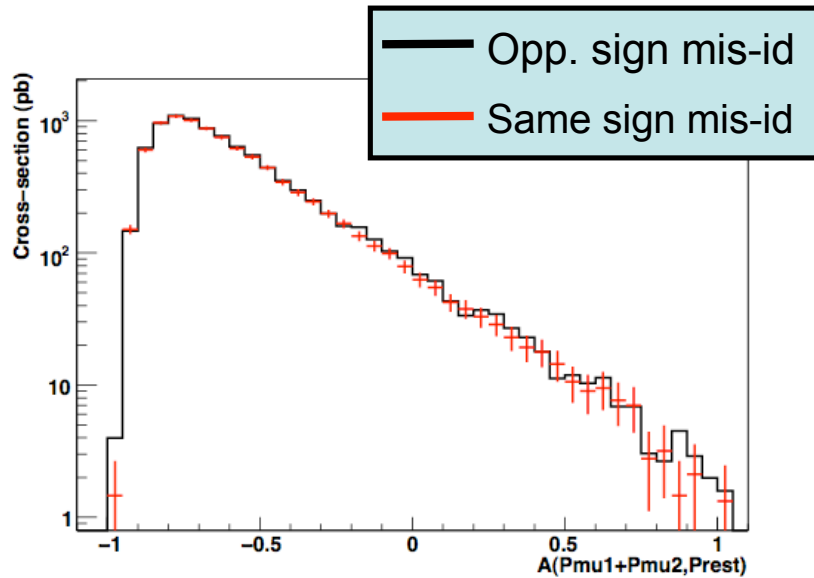
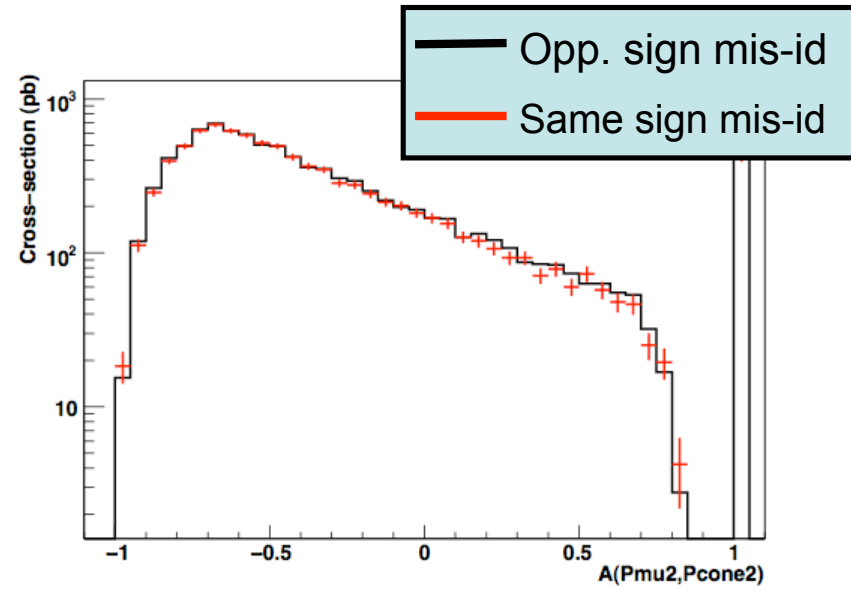
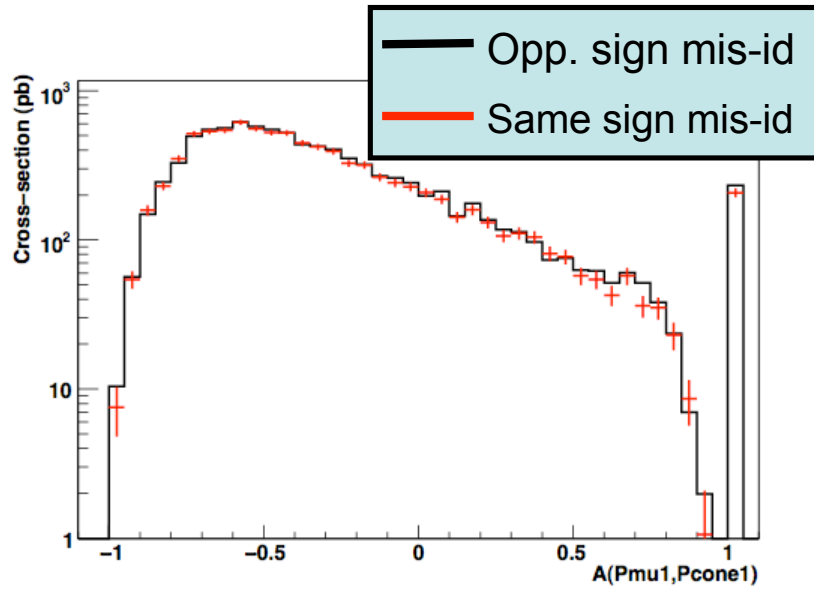
$\gamma^*$



Mass range (GeV)	Events/ $\text{pb}^{-1}$
$2.5 < M_{\mu\mu} < 5$	$119.1 \pm 1.0$
$5 < M_{\mu\mu} < 10$	$287.3 \pm 1.6$
$10 < M_{\mu\mu} < 20$	$147.6 \pm 0.9$
$20 < M_{\mu\mu} < 40$	$42.3 \pm 0.4$

Systematic errors under study

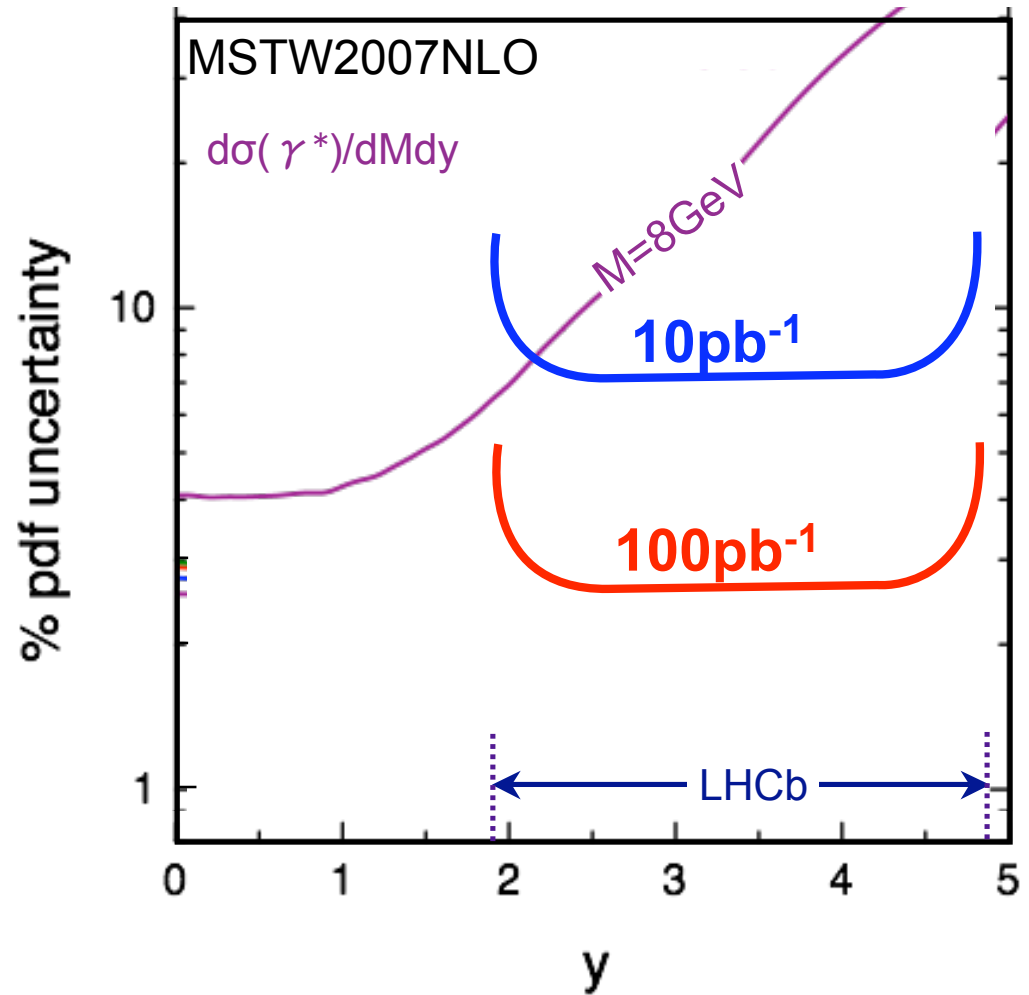
# Understanding backgrounds with data



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$\gamma^*$

Experimental precision (stat.) quickly exceeds theoretical precision.



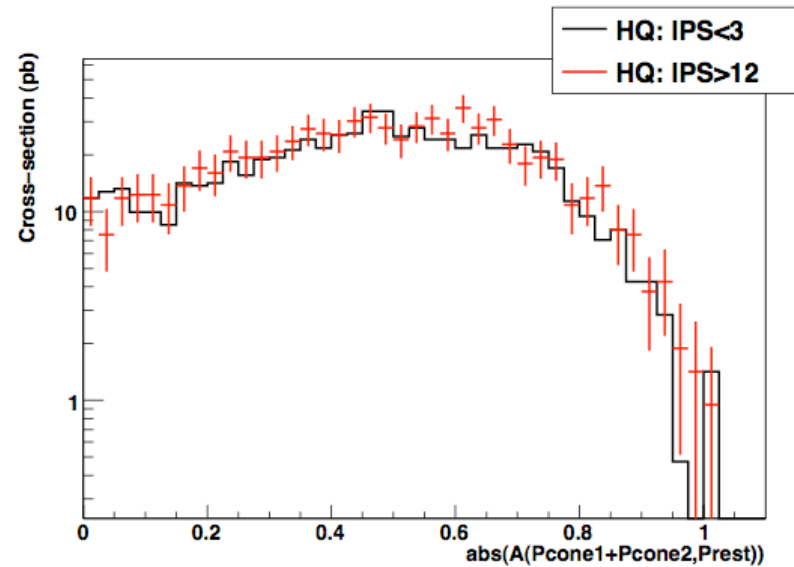
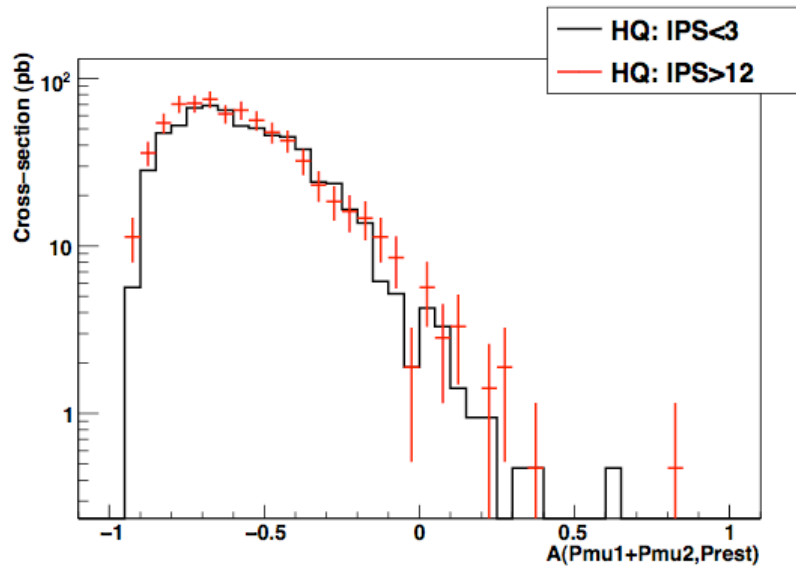
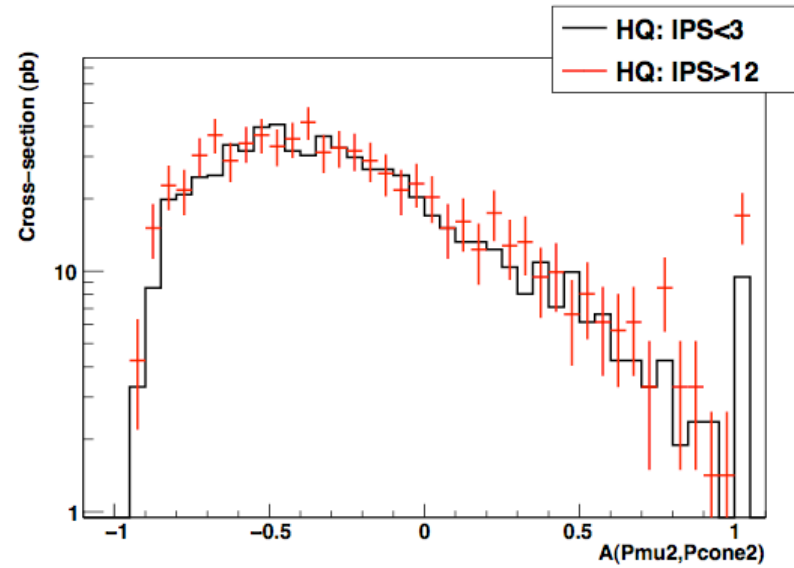
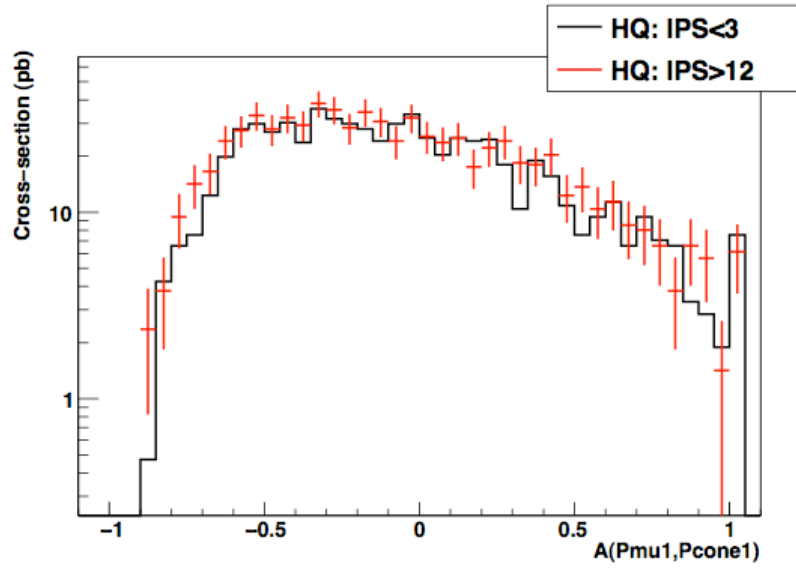
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LHCb can measure Z, W, low invariant mass  $\gamma^*$  in the forward region with good precision.

Measurements probe partons down to x of  $10^{-6}$

Fitting W,Z differential cross-sections can constrain PDF descriptions.

# Understanding backgrounds with data



## Do Z shapes match lower masses?

