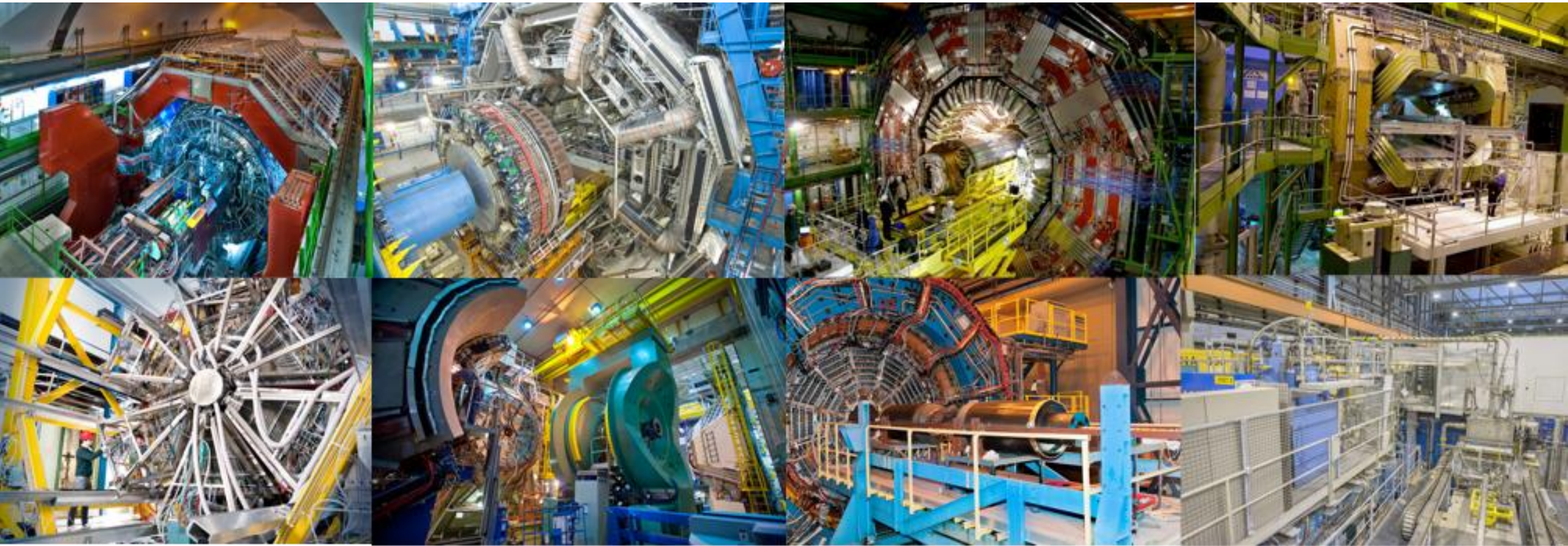


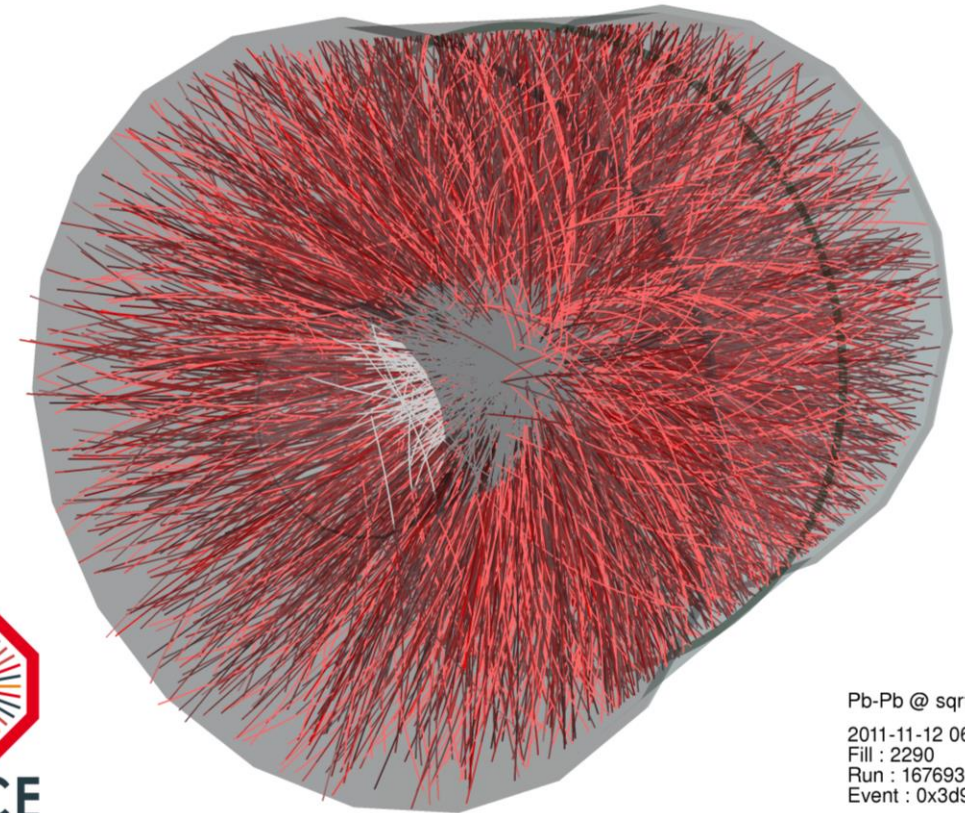
The physics of heavy-ion collisions



Alexander Kalweit, *CERN*

Overview

- Three lectures (one hour each):
 - Friday, 10:30h-11:30h (Prevessin)
 - Saturday, 11:30h-12:30h (Meyrin)
 - Monday, 10:30h-11:30h (Prevessin)
- Specialized discussion sessions with **heavy-ion experts** in the afternoons on Friday and Monday.
- Feel free to contact me for any questions regarding the lecture:
Alexander.Philipp.Kalweit@cern.ch
- Many slides, figures, and input taken from:
Jan Fiete Grosse-Oetringhaus, Constantin Loizides, Federico Antinori, Roman Lietava



Pb-Pb @ $\sqrt{s} = 2.76$ ATeV
2011-11-12 06:51:12
Fill : 2290
Run : 167693
Event : 0x3d94315a

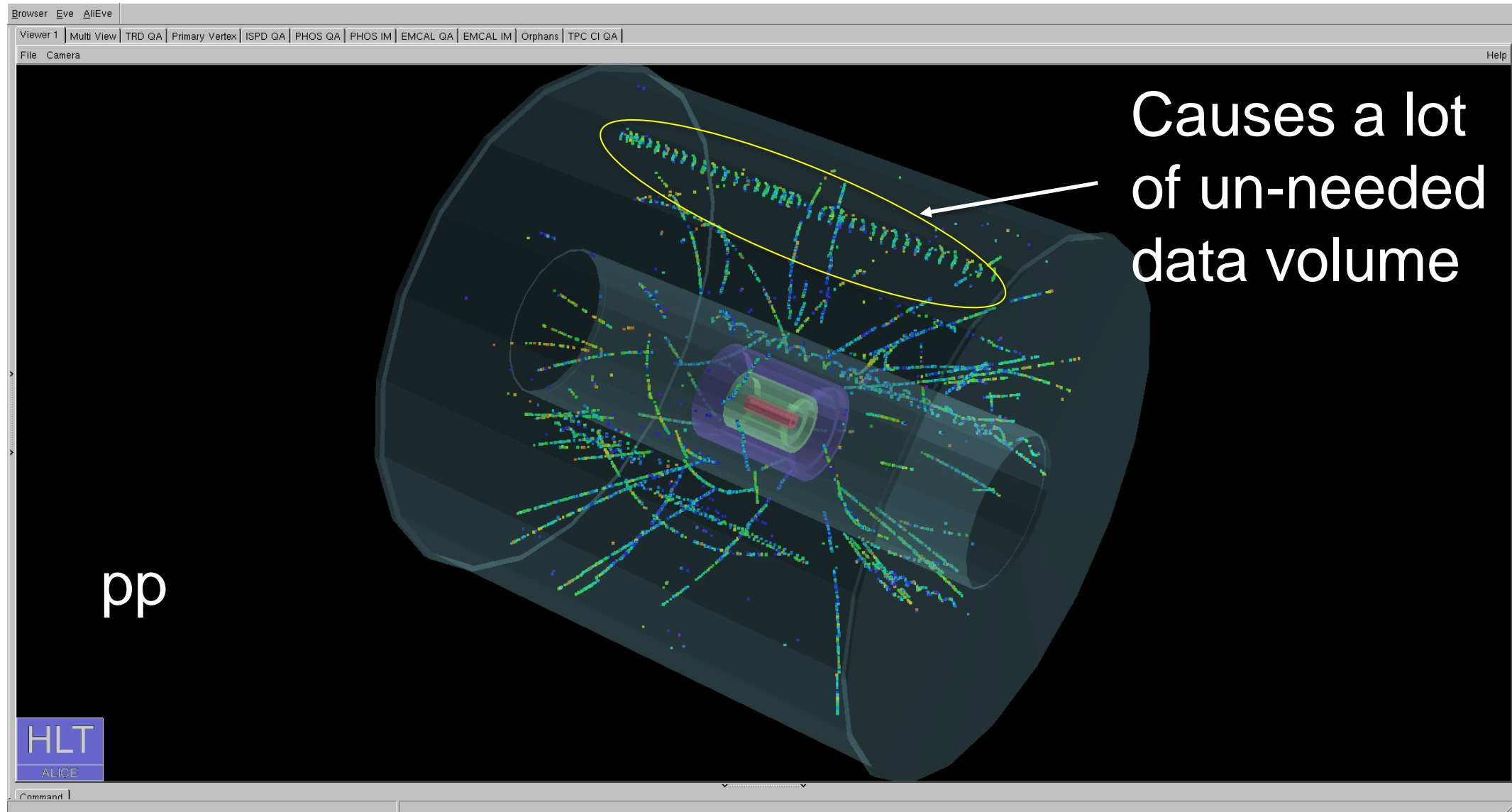
FAQ (1)

- How many bunches are in the LHC during heavy-ion operation?
 - During last run typically 518.

| Run# | Bunches | Scheme | Fill # | Energy per beam | Intensity per bunch | Mu | B B | B A | B C | MB Interaction | Rate (Hz) |
|--------|---------|--|--------|-----------------|---------------------|--------|-----|-----|-----|----------------|-----------|
| 246994 | L | 268 100_150ns_518Pb_516Pb_492_444_24_22inj | 4,720 | 6,369 | | 0 | 444 | 74 | 72 | 1,462,567 | 292.10 |
| 246991 | L | 268 100_150ns_518Pb_516Pb_492_444_24_22inj | 4,720 | 6,369 | | 0.0005 | 444 | 74 | 72 | 379,251 | 238.67 |
| 246989 | L | 268 100_150ns_518Pb_516Pb_492_444_24_22inj | 4,720 | 6,369 | | 0.0007 | 444 | 74 | 72 | 2,551,035 | 253.61 |
| 246984 | L | 268 100_150ns_518Pb_516Pb_492_444_24_22inj | 4,720 | 6,370 | | 0.0011 | 444 | 74 | 72 | 1,757,655 | 240.84 |
| 246982 | L | 268 100_150ns_518Pb_516Pb_492_444_24_22inj | 4,720 | 6,369 | | 0.0014 | 444 | 74 | 72 | 145,502 | 174.88 |

- What are average event sizes?
 - In pp up to 1-2 MegaByte, in Pb-Pb up to 50 MegaByte.
 - Strong online compression (raw amplitudes -> clusters [lossy], cluster position with respect to the helix).

FAQ (2)



Outline and discussion leaders

- Introduction
- The QCD phase transition
- QGP thermodynamics and soft probes (Francesca)
 - Particle chemistry
 - QCD critical point and onset of de-confinement
 - (anti-)(hyper-)nuclei
 - Radial and elliptic flow
 - Small systems
- Hard scatterings (Leticia, Marta)
 - Nuclear modification factor
 - Jets
- Heavy flavor in heavy-ions
 - Open charm and beauty
 - Quarkonia
- Di-leptons



Francesca
Bellini



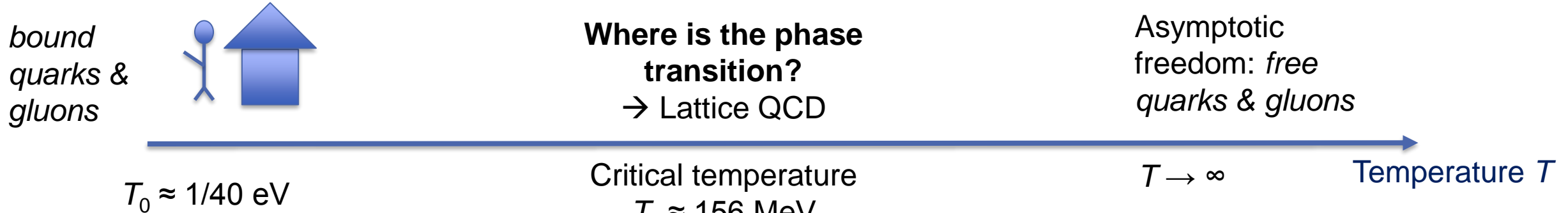
Leticia
Cunqueiro



Marta
Verweij

Reminder: QGP as the asymptotic state of QCD

Quark-Gluon-Plasma (QGP): at extreme temperatures and densities quarks and gluons behave quasi-free and are not localized to individual hadrons anymore.



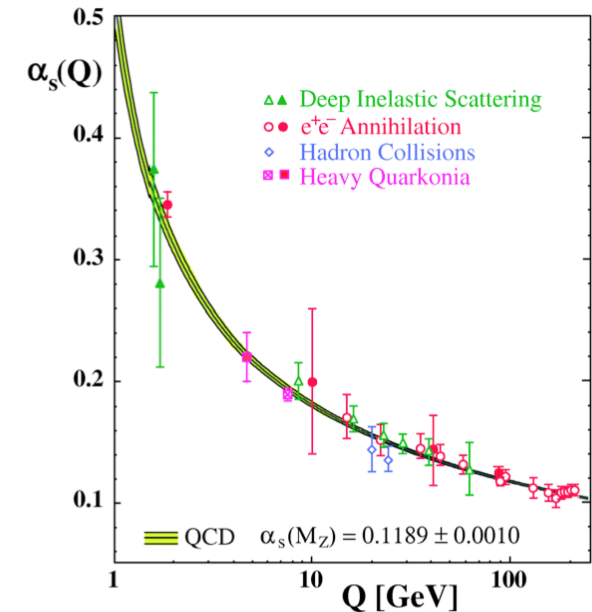
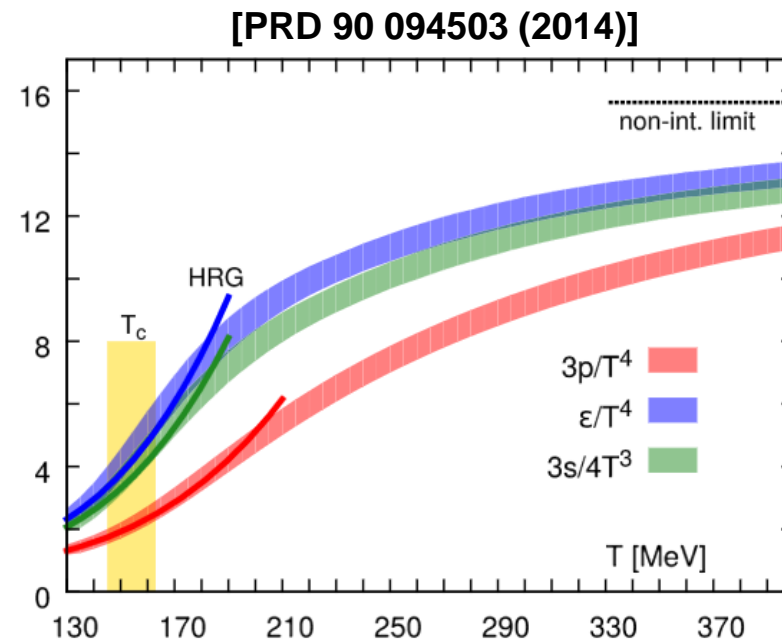
→ Are such extreme temperatures reached in the experiment?

Yes..

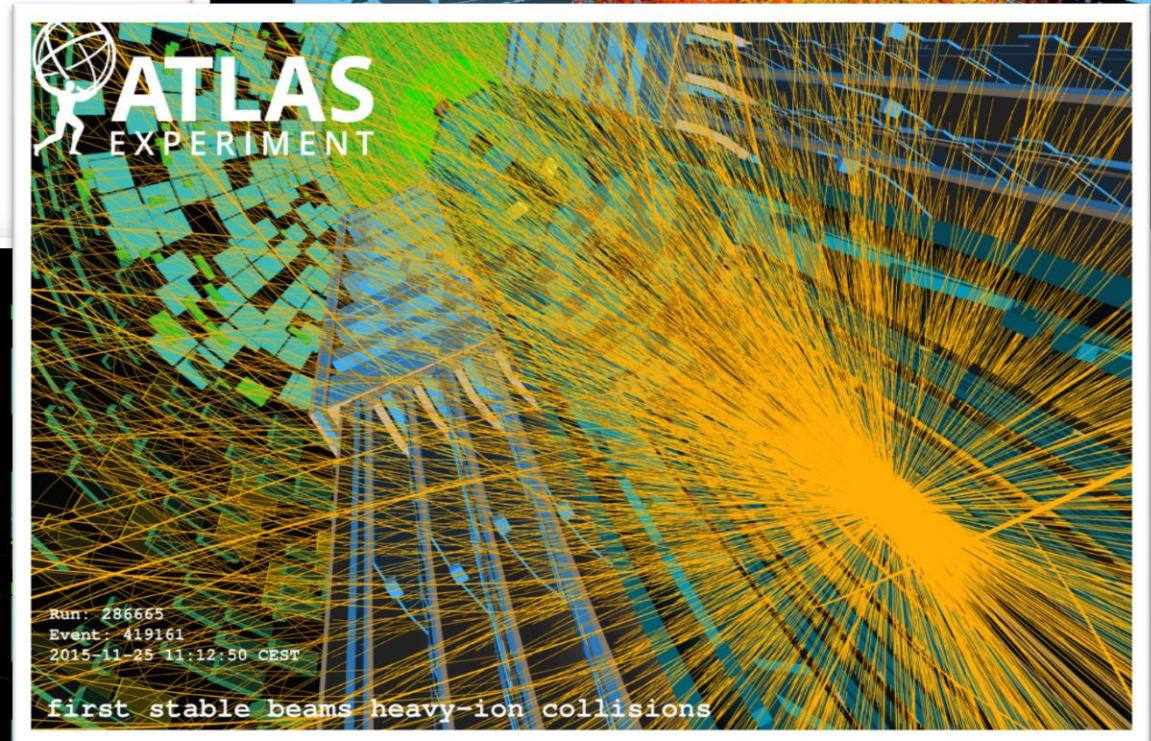
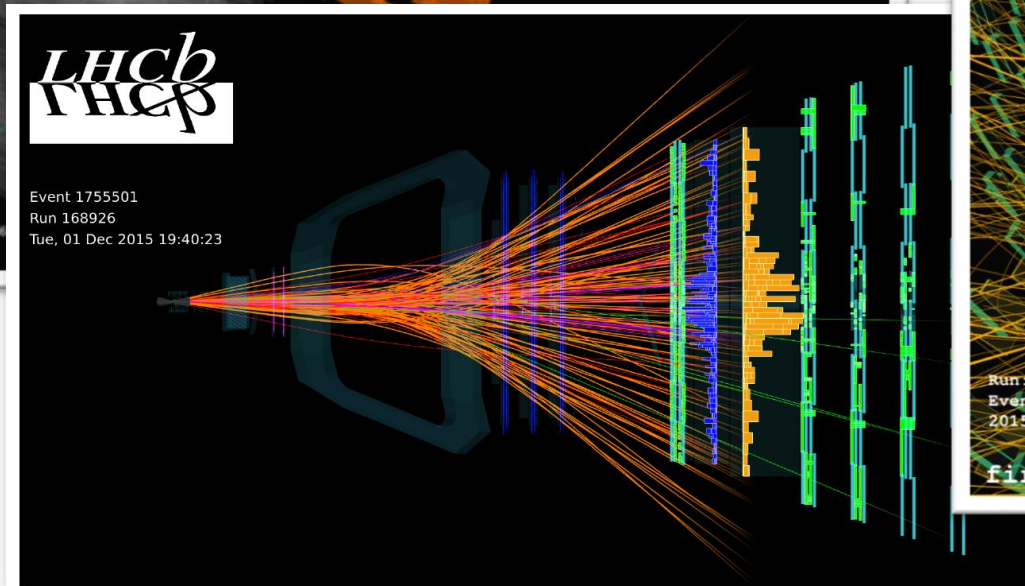
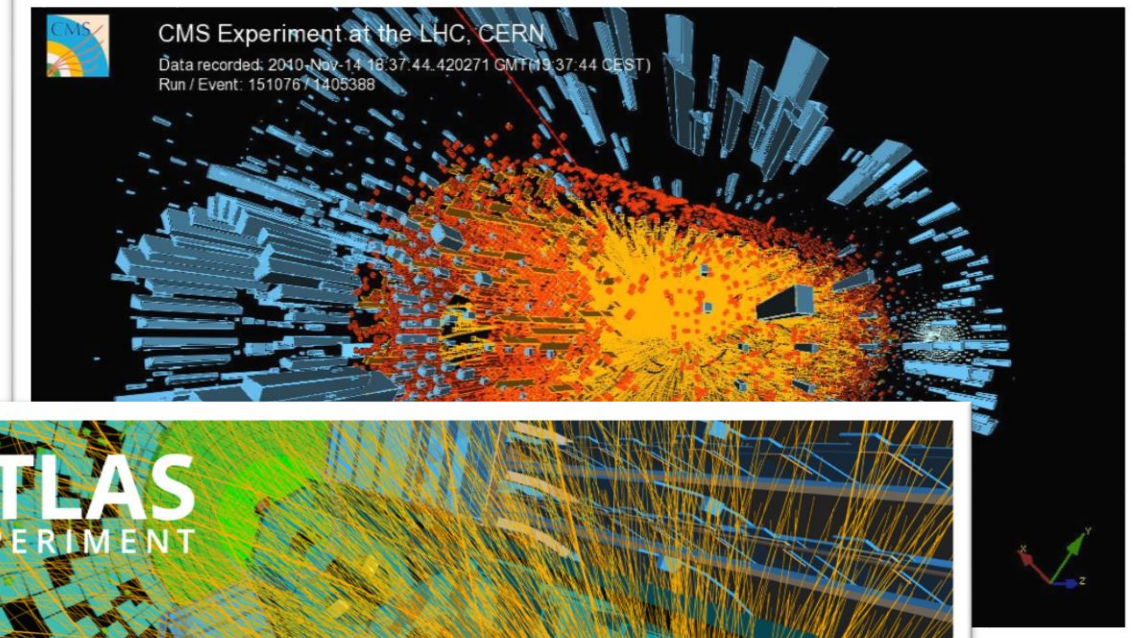
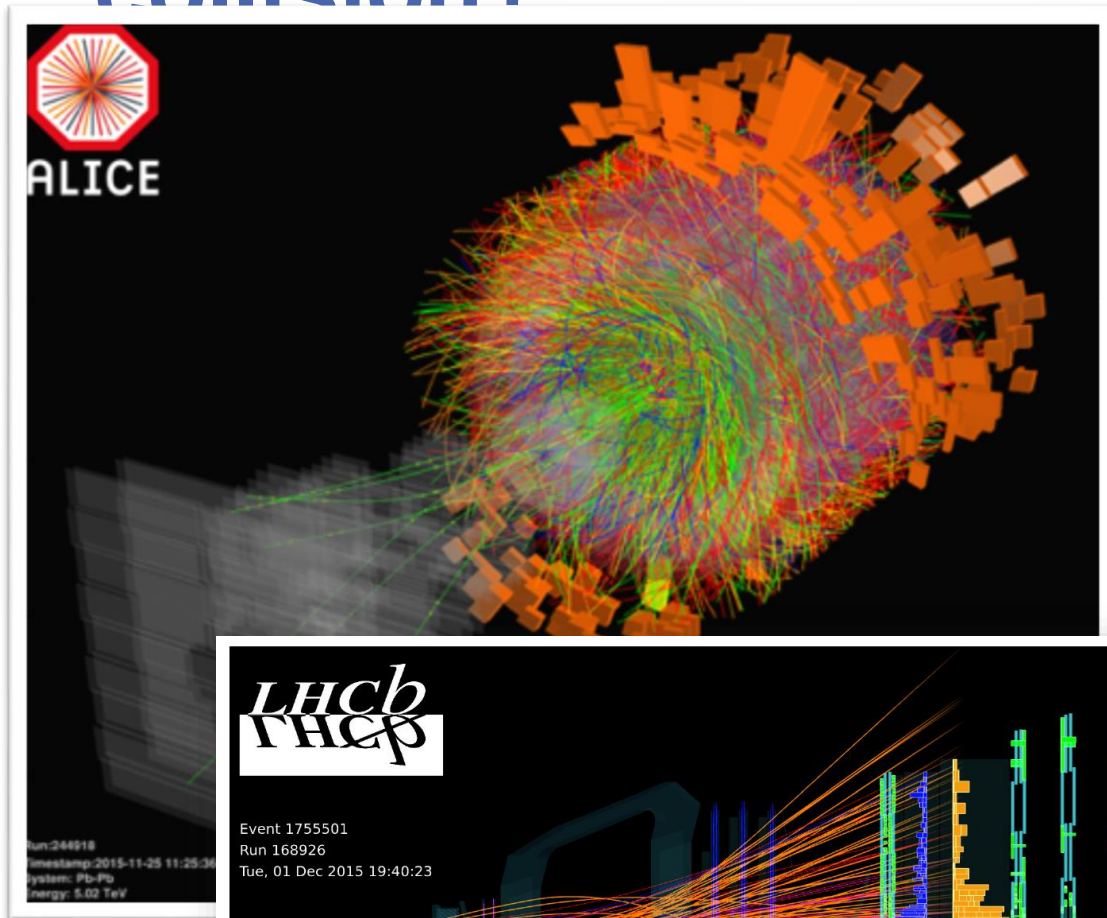
→ Is it for all quark flavors the same?

Not clear yet..

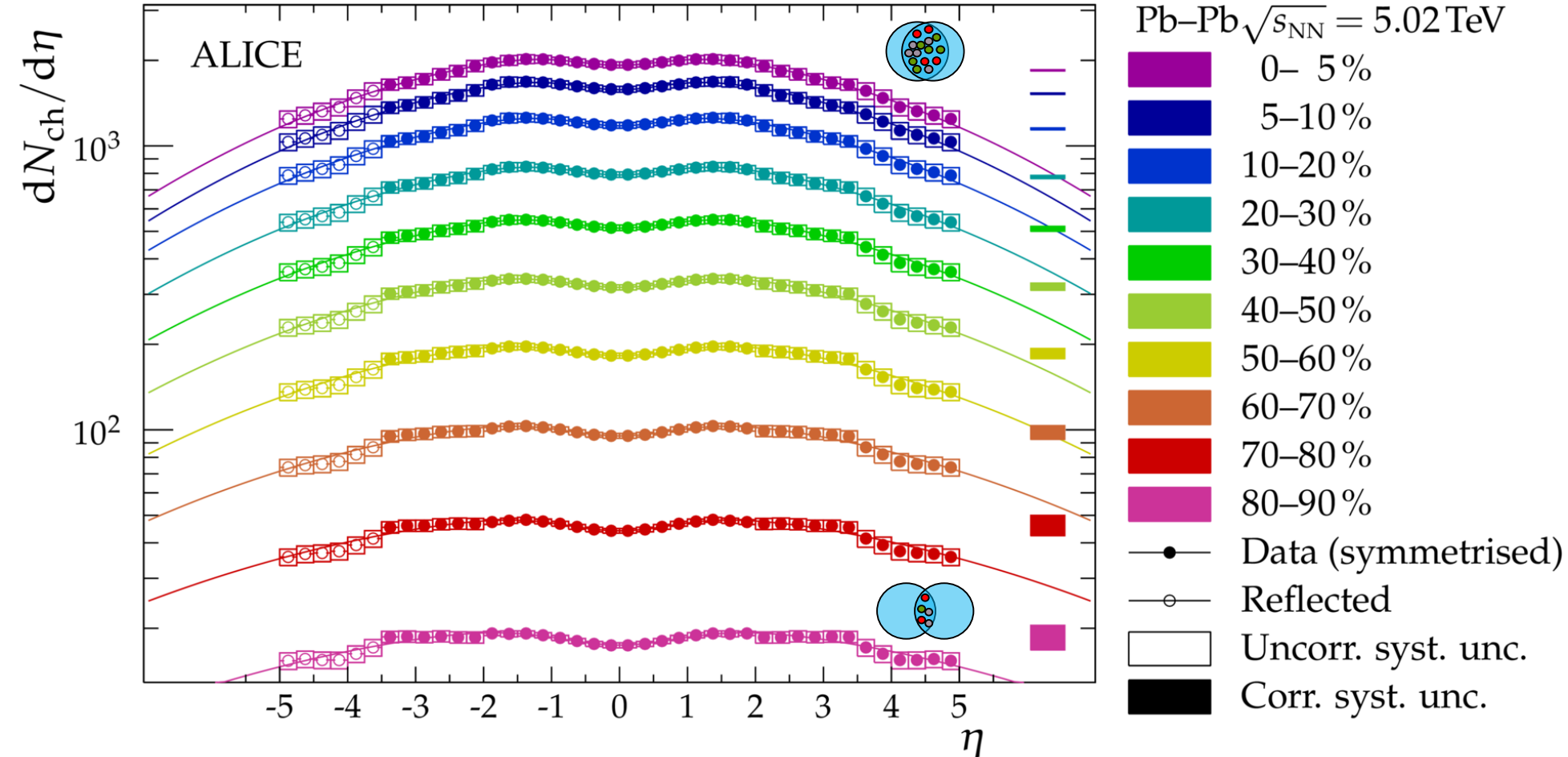
→ ...



How many particles are created in such a collision?



$dN_{\text{ch}}/d\eta$ in 5.02 TeV Pb-Pb collisions at the LHC



$dN_{\text{ch}}/d\eta \approx 1943 \pm 54$ at midrapidity.

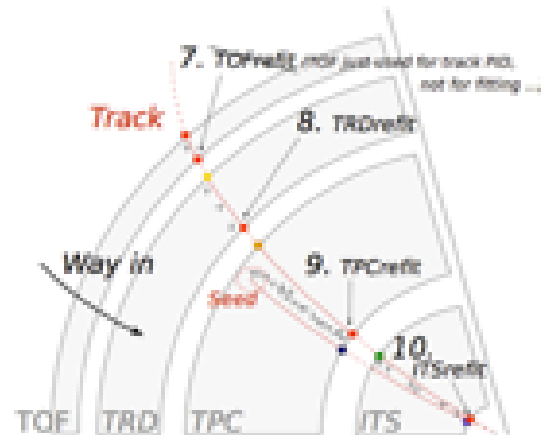
→ Even at LHC energies, 95% of all particles are produced with $p_{\text{T}} < 2$ GeV/c in pp and Pb-Pb collisions.

→ Bulk particle production and the study of collective phenomena are associated with “**soft**” **physics** in the non-perturbative regime of QCD.

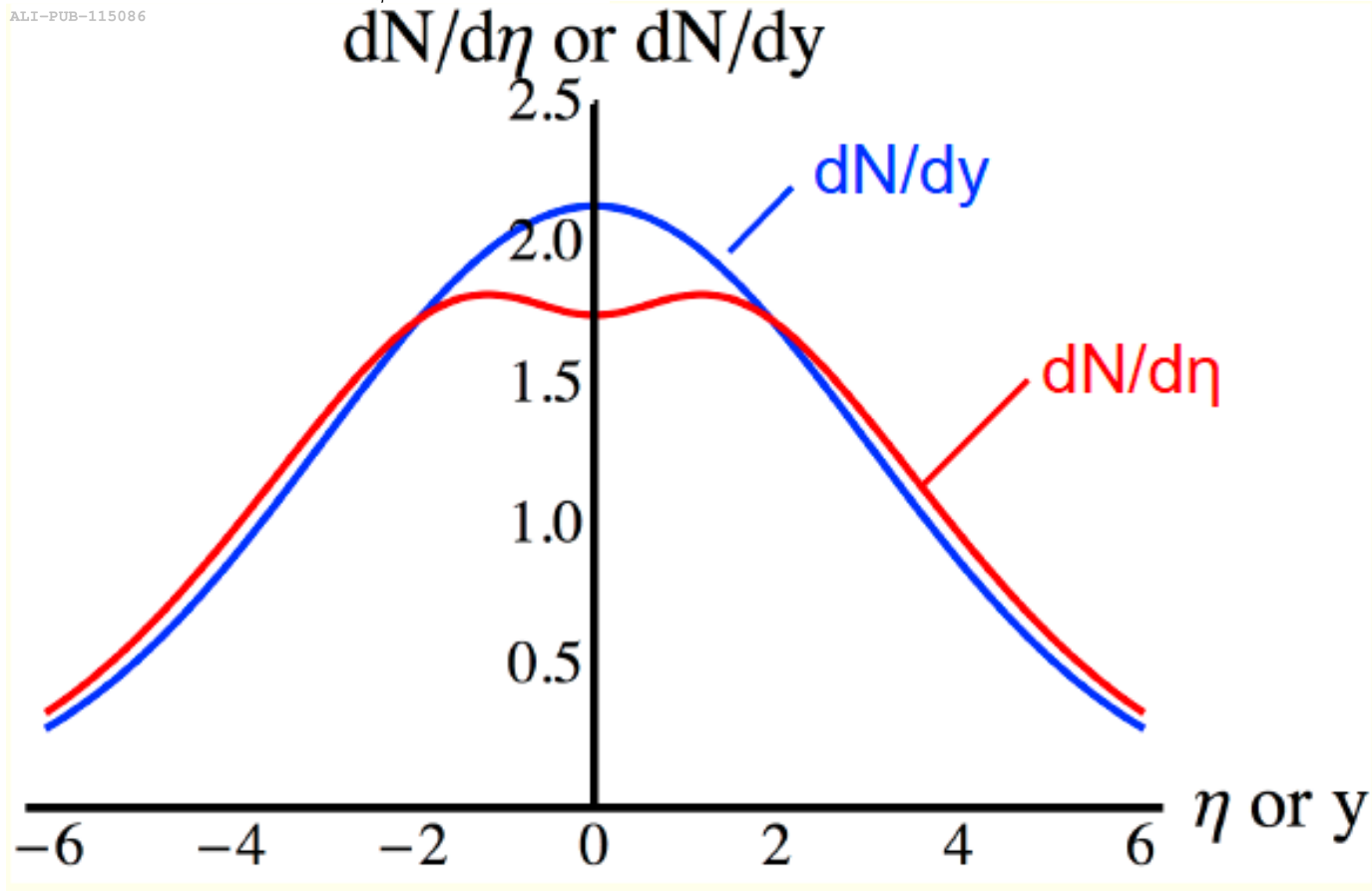
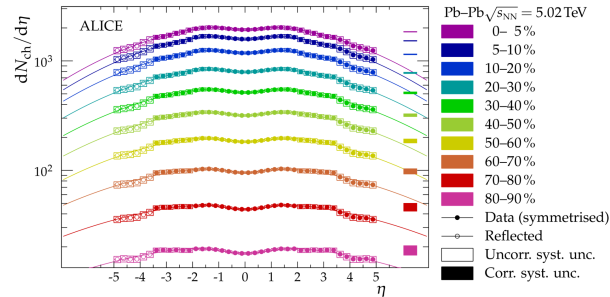
ALI-PUB-115086 [arXiv:1612.08966]

Instrumentation for heavy-ion experiments: granularity

- In order to cope with the high density of particles, heavy-ion detectors have to be very granular (e.g. large TPC with small read-out pads).
- Track seeding typically in outer detectors (where track density is lower) and then Kalman filter propagation to the primary vertex.



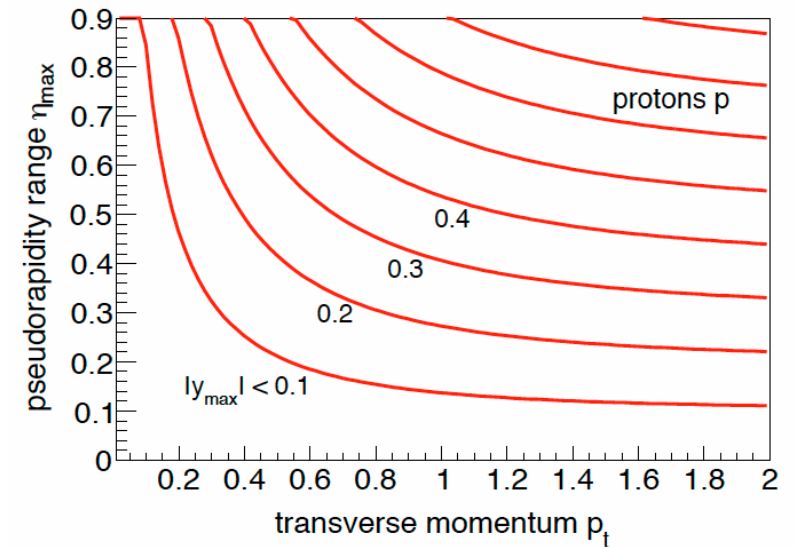
Short reminder: (Pseudo-)rapidity



From: K. Reygers

$$\frac{dN}{d\eta} = \sqrt{1 - \frac{m^2}{m_T^2 \cosh^2 y}} \frac{dN}{dy}$$

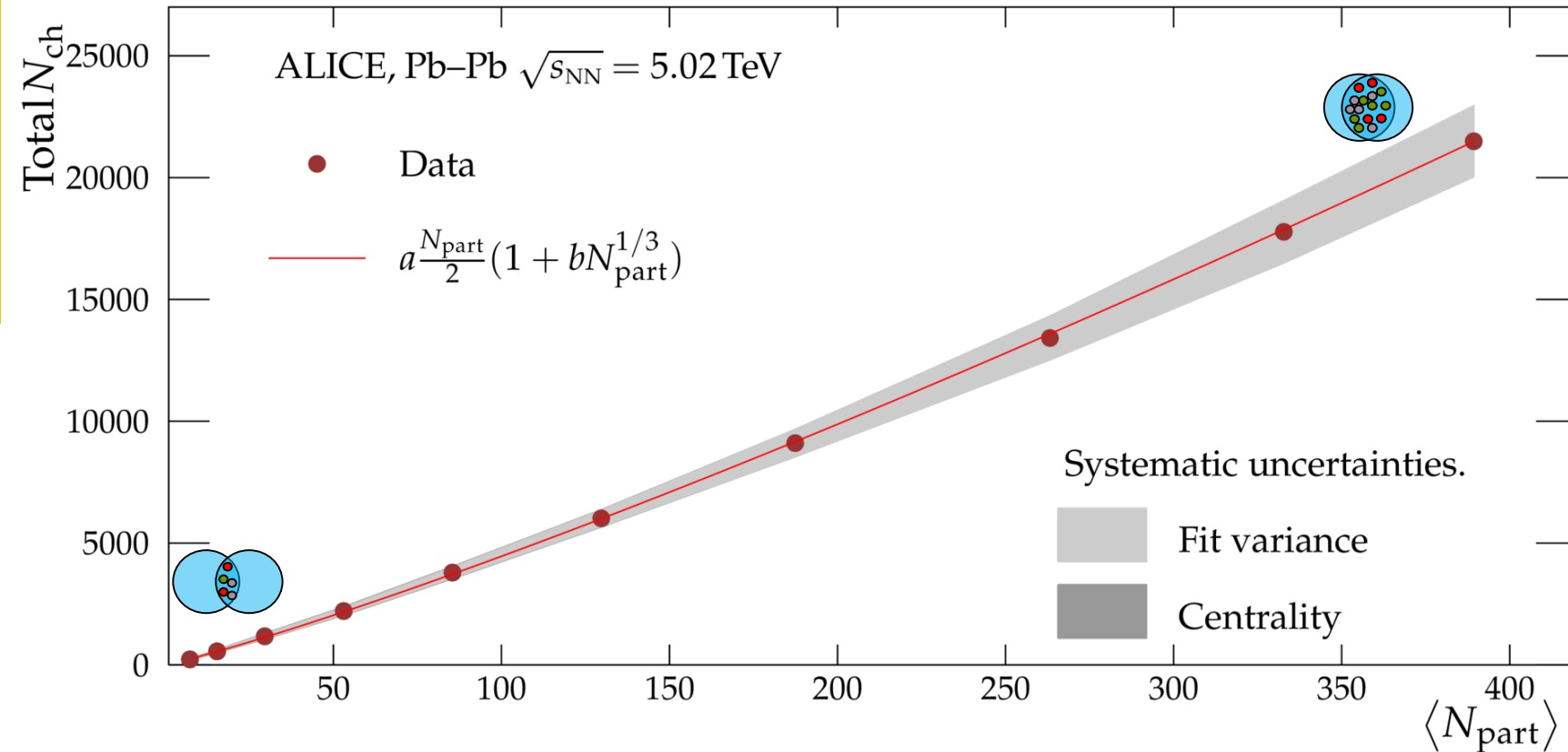
→ Always keep in mind: Rapidity and pseudo-rapidity are not the same, especially at low transverse momenta!



Total number of charged hadrons in Pb-Pb collisions

→ Collisions of heavy-ions at high energy accelerators allow the creation of several tens of thousands of hadrons ($1 \ll N \ll 1\text{mol}$) **in local thermodynamic equilibrium** in the laboratory.

So, we have enough particles, but are they in local thermodynamic equilibrium? How can we test that?



ALI-PUB-115091

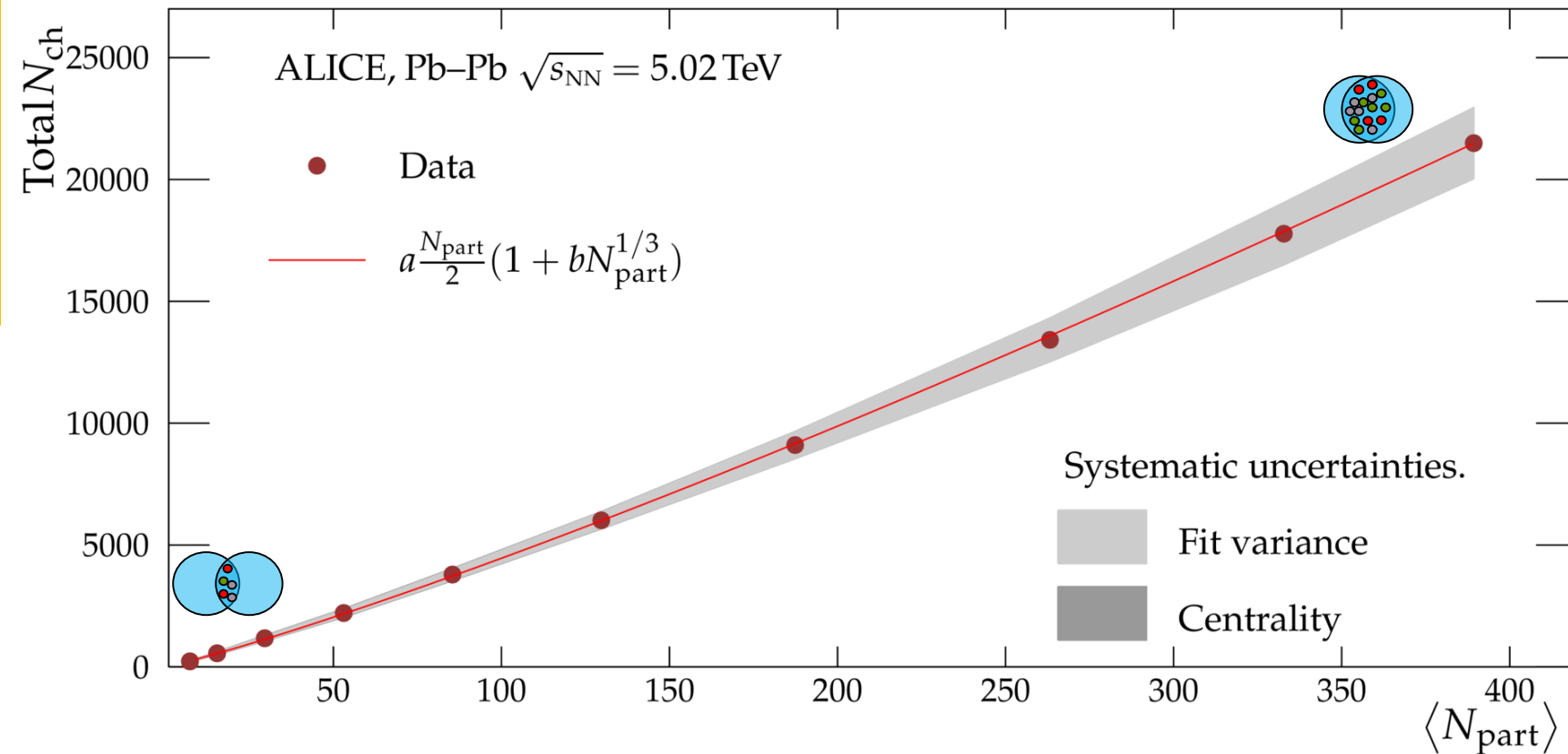
[arXiv:1612.08966]

Total number of charged hadrons in Pb-Pb collisions

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Success of **hydro models** describing **spectral shapes** and **azimuthal anisotropies** supports idea of matter in local thermal equilibrium (*kinetic*).

Success of **thermal models** describing **yields of hadrons composed of up, down, and strange quarks** supports idea of matter in local thermal equilibrium (*chemical*).



ALI-PUB-115091

[arXiv:1612.08966]

Equilibrium models such as hydro typically need 5-6 interactions to work. Where does this picture break down? Does it work in pp and pPb? → **What is the smallest possible QGP droplet?**

A short introduction to statistical thermodynamics (1)

- The **maximum entropy principle** leads to the thermal most likely distribution of particle species.
- Entropy: the number of possible micro-states Ω being compatible with a macro-state for a given set of macroscopic variables (E, V, N):

$$S = k_B \cdot \ln \Omega$$

- Compatibility to a given macroscopic state can be realized *exactly* or *only in the statistical mean*.



L. Boltzmann

A short introduction to statistical thermodynamics (2)

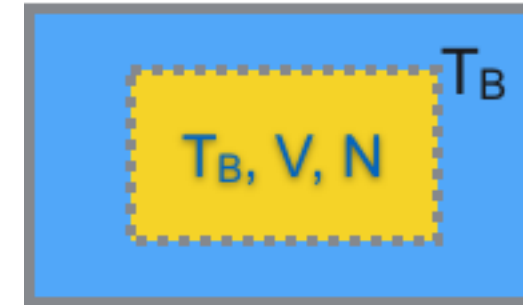
- We therefore distinguish three different *statistical ensembles*:

(i) micro-canonical: E, V, N fix



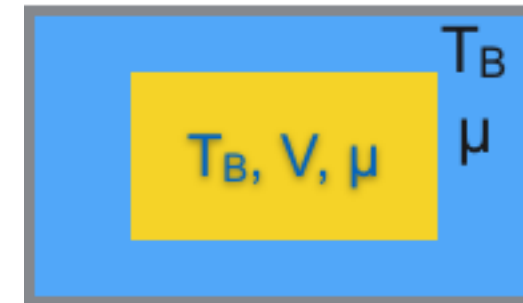
Statistical model for e^+e^- collisions.

(ii) canonical: T, V, N fix
→ given volume element is coupled to a heat bath



Strangeness conservation in peripheral HI collisions.

(iii) grand-canonical: T, V, μ fix
→ given volume element can also exchange particles with its surrounding (heat bath and particle reservoir)



Central relativistic heavy-ion collisions.

A short introduction to statistical thermodynamics (3)

- A small example: barometric formula (density of the atmosphere at a fixed temperature as a function of the altitude h).
- Probability to find a particle on a given energy level j :

$$P_j = \frac{\exp\left(-\frac{E_j}{k_B T}\right)}{Z}$$

Boltzmann factor

Partition function Z
(*Zustandssumme* = “sum over states”)

- Energy on a given level is simply the potential energy: $E_{\text{pot}} = mgh$. This implies for the density n (pressure p):

$$\frac{p(h_1)}{p(h_0)} = \frac{n(h_1)}{n(h_0)} = \frac{N \cdot P(h_1)}{N \cdot P(h_0)} = \exp\left(-\frac{\Delta E_{\text{pot}}}{k_B T}\right) = \exp\left(-\frac{mg}{RT} \Delta h\right)$$

QGP thermodynamics and soft probes

Particle chemistry

Statistical-thermal model for heavy-ion collisions

- Starting point: grand-canonical partition function for an *relativistic ideal quantum gas of hadrons* of particle type i (i = pion, proton,... \rightarrow full PDG!):

(-) for bosons, (+) for fermions
(quantum gas)

$$\ln Z_{GK_i} = \pm g_i \frac{V}{2\pi^2 \hbar^3} \int_0^\infty dp p^2 \ln (1 \pm e^{-\beta(\epsilon(p) - \mu_i)})$$

spin degeneracy \nearrow g_i

$\beta = \frac{1}{kT}$ \nearrow β

$E_i = \sqrt{p^2 + m_i^2}$ \nearrow $\epsilon(p)$ dispersion relation (relativistic)

$\mu_i = \mu_B B_i + \mu_S S_i + \mu_{I_3} I_{3i} + \mu_C C_i$ \nearrow μ_i chemical potential representing each conserved quantity

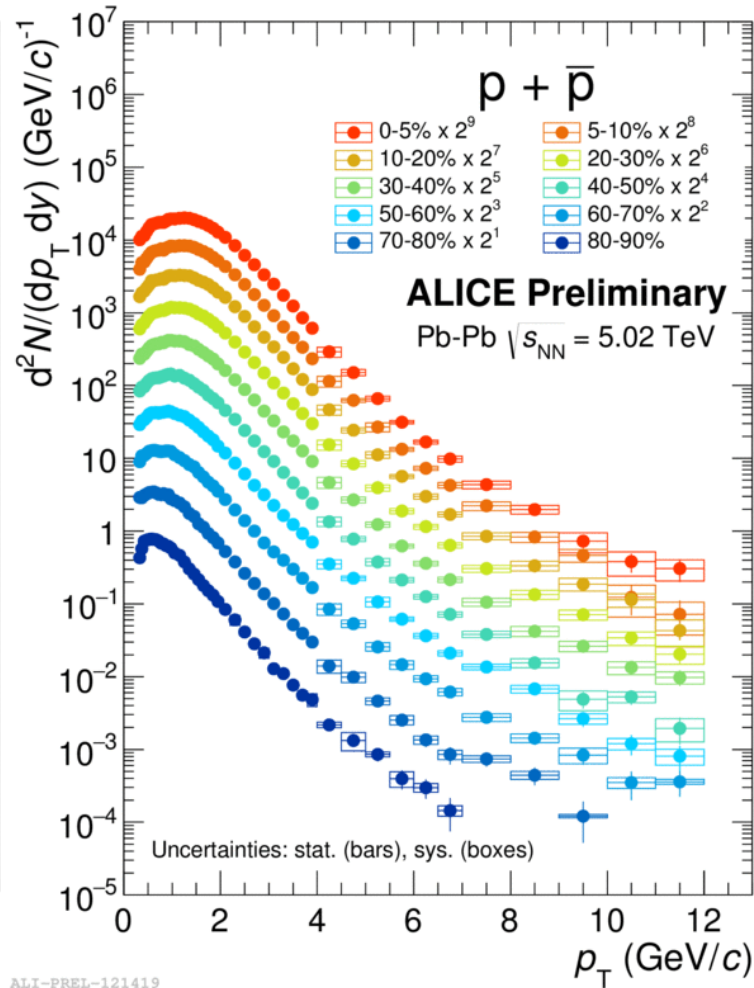
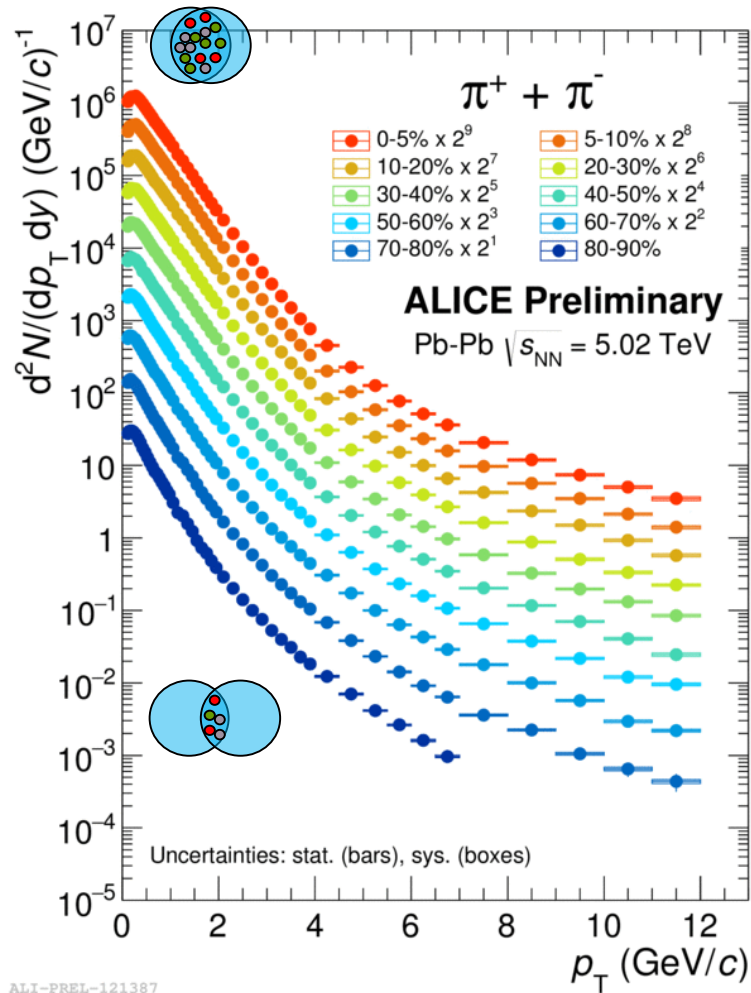
Only two free parameters are needed: **(T, μ_B)**. Volume cancels if particle ratios n_i/n_j are calculated. If yields are fitted, it acts as the third free parameter.

- Once the partition function is known, we can calculate all other thermodynamic quantities:

$$n = \frac{1}{V} \frac{\partial(T \ln Z)}{\partial \mu} \quad P = \frac{\partial(T \ln Z)}{\partial V} \quad s = \frac{1}{V} \frac{\partial(T \ln Z)}{\partial T}$$

Partition function shown here is only valid in the resonance gas limit (HRG), i.e. relevant interactions are mediated via resonances, and thus the non-interacting hadron resonance gas can be used as a good approximation for an interacting hadron gas.

p_T -spectra of identified particles



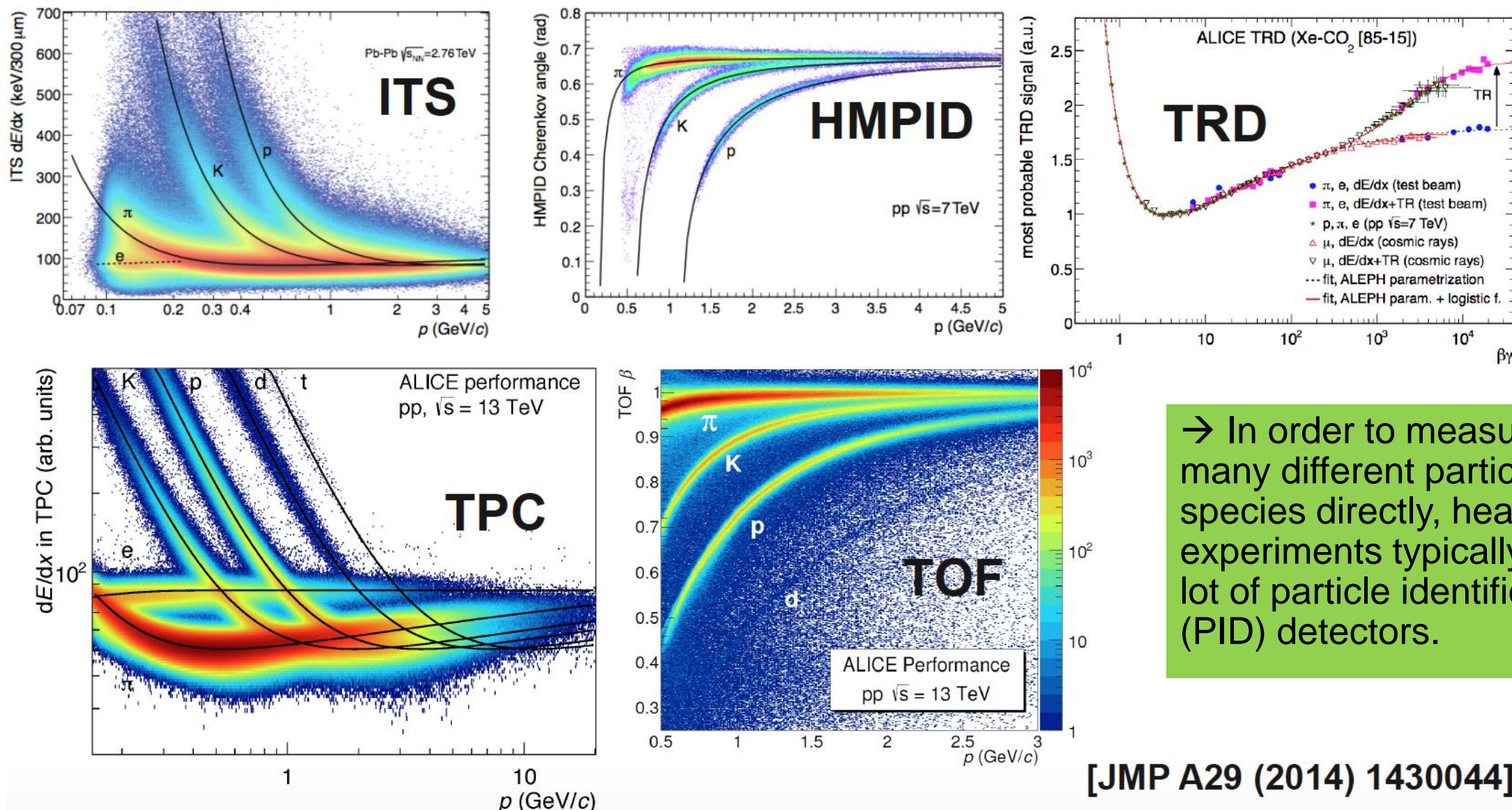
1. Identify particle in the detector (pion, kaon, proton, Lambda, Xi, Omega, anti-deuteron...)
2. Fill p_T -spectrum
3. Interpolate unmeasured region at low p_T (at high p_T negligible)
4. Integrate:

$$\frac{dN}{dy} = \int \frac{d^3N}{dp_T dy d\phi} d\phi dp_T$$

ALI-PREL-121387

ALI-PREL-121419

Instrumentation for heavy-ion experiments: PID



→ In order to measure as many different particle species directly, heavy-ion experiments typically have a lot of particle identification (PID) detectors.

[JMP A29 (2014) 1430044]

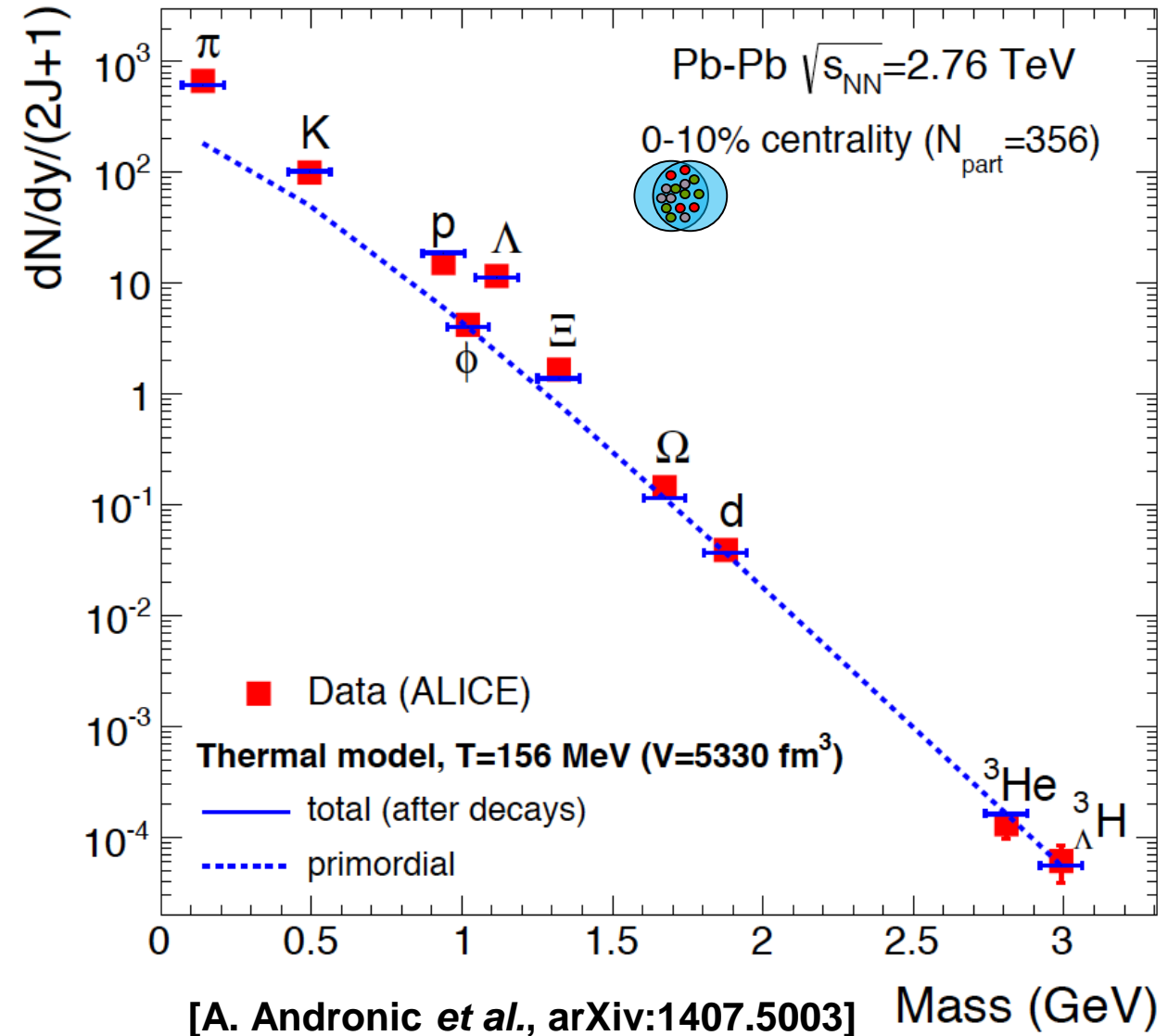
Chemical equilibrium at the LHC (1)

Production yields of light flavour hadrons from a chemically equilibrated fireball can be calculated by statistical-thermal models (roughly $dN/dy \sim \exp\{-m/T_{ch}\}$, in detail derived from partition function)

→ In Pb-Pb collisions, particle yields of light flavor hadrons are described over 7 orders of magnitude with a **common** chemical freeze-out temperature of $T_{ch} \approx 156 \text{ MeV}$.

→ This includes **strange hadrons** which are rarer than u,d quarks. Approx. every fourth to fifth quark (every tenth) is a strange quark in Pb-Pb collisions (in pp collisions).

→ Light (anti-)nuclei are also well described despite their low binding energy ($E_b \ll T_{ch}$).



Chemical equilibrium at the LHC (2)

Particle yields of light flavor hadrons are described over 7 orders of magnitude within 20% (except K^*0) with a common chemical freeze-out temperature of $T_{ch} \approx 156$ MeV (prediction from RHIC extrapolation was ≈ 164 MeV).

Hadrons are produced in apparent chemical equilibrium in Pb-Pb collisions at LHC energies.

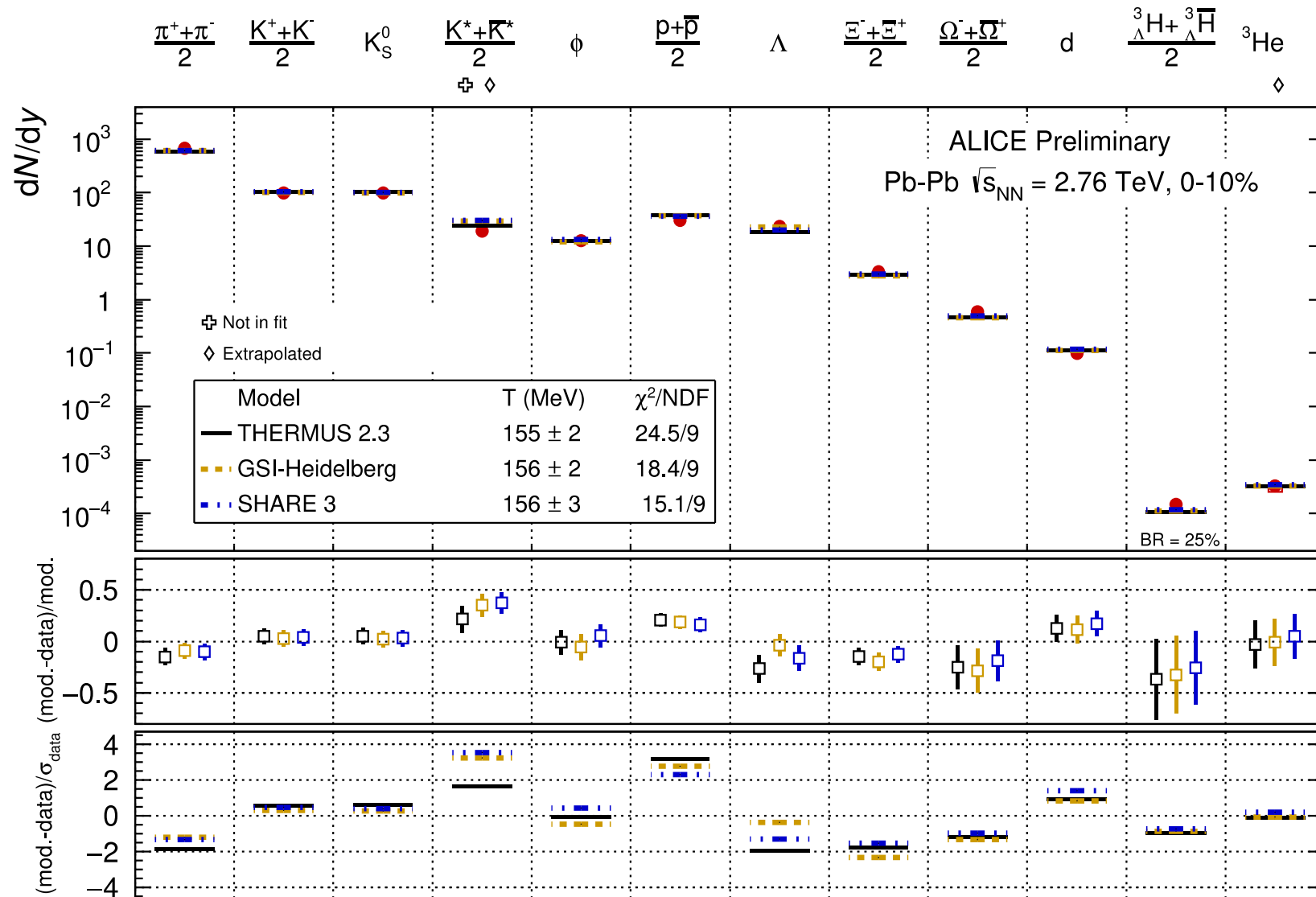
Largest deviations observed for protons (incomplete hadron spectrum, baryon annihilation in hadronic phase,..?) and for K^*0 .

Three different versions of thermal model implementations give similar results.

[Wheaton et al, Comput.Phys.Commun, 18084]

[Petran et al, arXiv:1310.5108]

[Andronic et al, PLB 673 142]



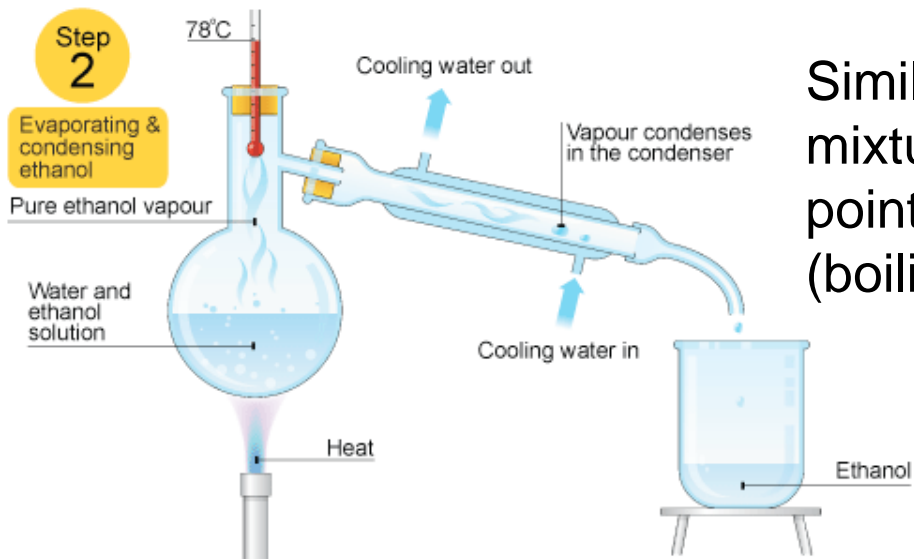
ALI-PREL-94600

Sequential freeze-out?

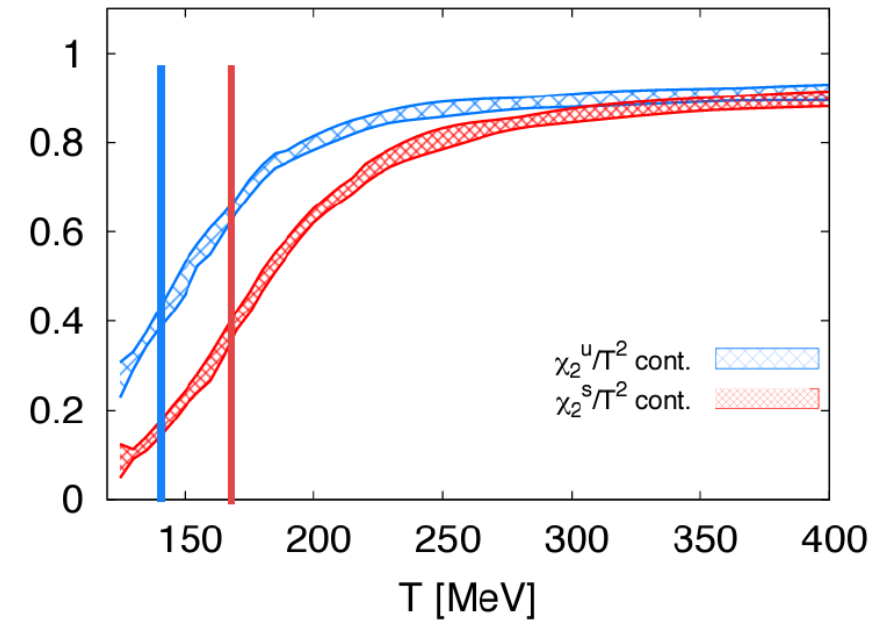
- Are the deviations observed in the thermal model fit for p and Ξ due to physics?

- Two main ideas on the market:

(1.) Different chemical freeze-out temperatures for s w.r.t. to u, d quarks.
→ motivated by LQCD



Similar to heating a mixture of alcohol (boiling point 78,32 °C) and water (boiling point 100 °C).



C. Ratti et al., PRD 85, 014004 (2012)

(2.) Inelastic collisions in the hadronic phase.

→ Was this previously overlooked, because the difference is “only” about 10 MeV?
Interesting research topic for the next years.

Chemical equilibrium vs collision energy

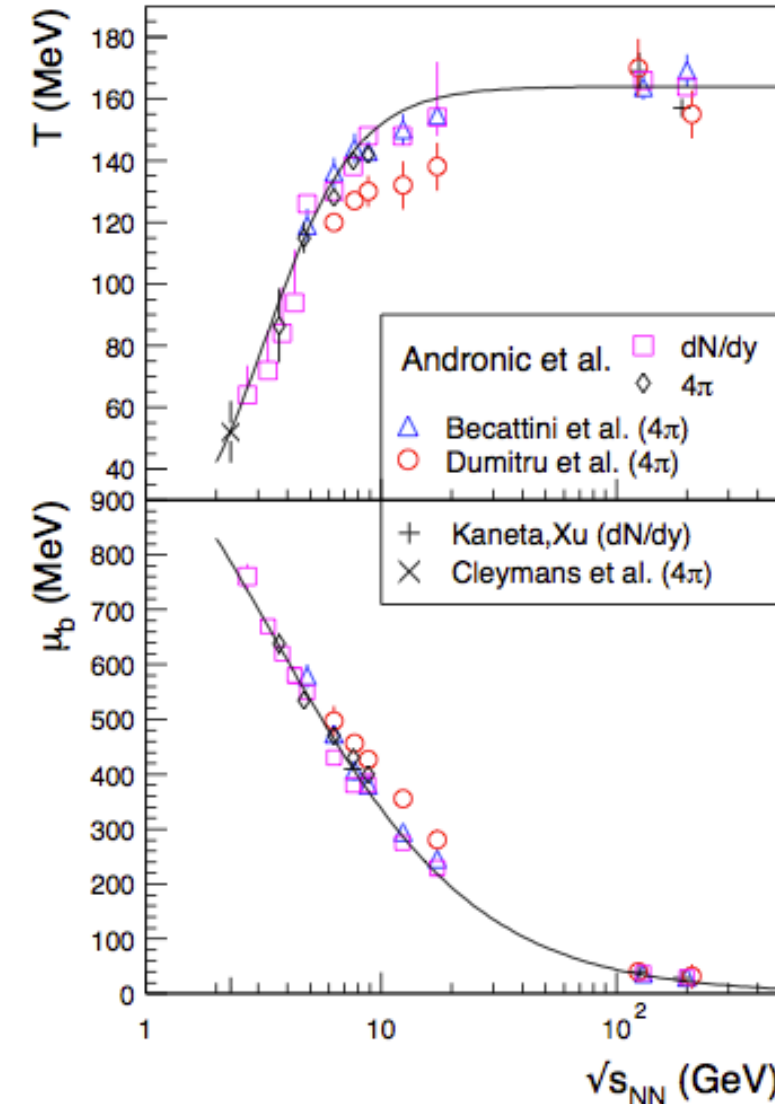
[A. Andronic et al., *NPA* 834 (2010) 237]

- Hadron yields from SIS up to RHIC and LHC can be described in a hadro-chemical model applying thermal fits.
- Effective parameterization of (T, μ_B) as a function of collision energy:

$$T[\text{MeV}] = T_{lim} \left(1 - \frac{1}{0.7 + (\exp(\sqrt{s_{NN}}(\text{GeV})) - 2.9)/1.5} \right)$$

$$\mu_b[\text{MeV}] = \frac{a}{1 + b\sqrt{s_{NN}}(\text{GeV})},$$

- Particle ratios can be calculated (or predicted) at any collision energy....



→ One observes a *limiting temperature of hadron production* around $T \approx 160$ MeV.

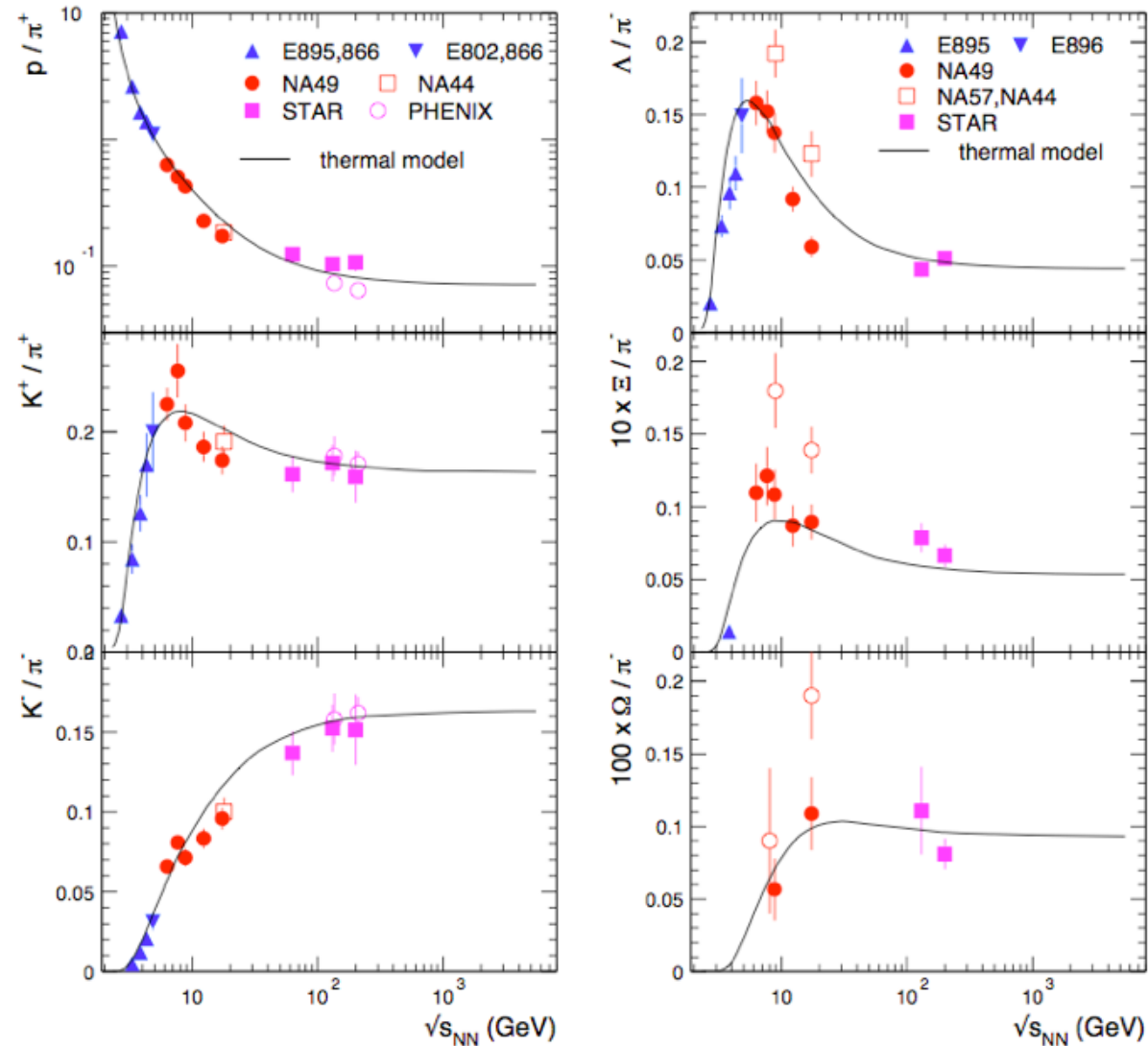
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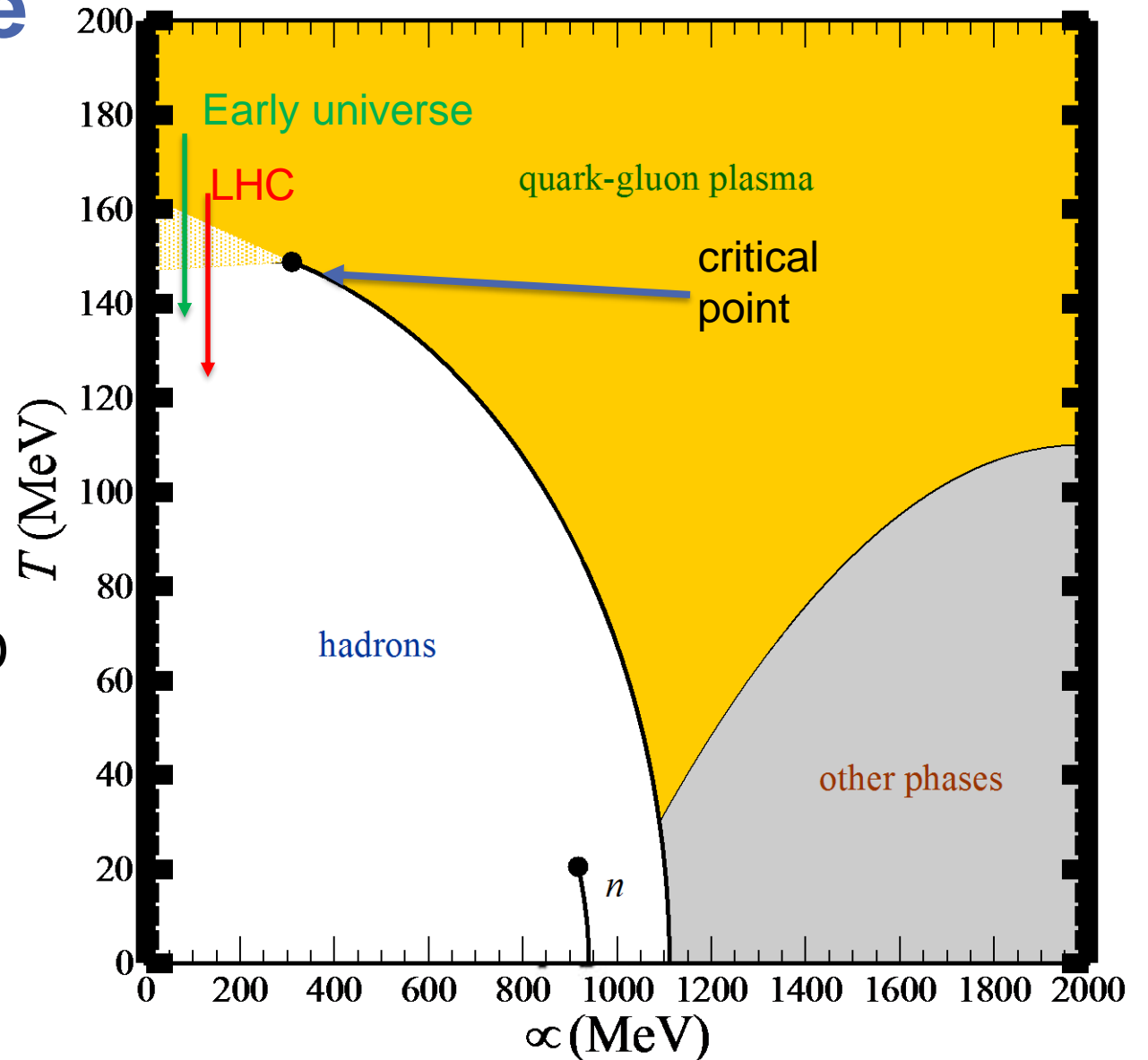
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Chemical freeze-out line

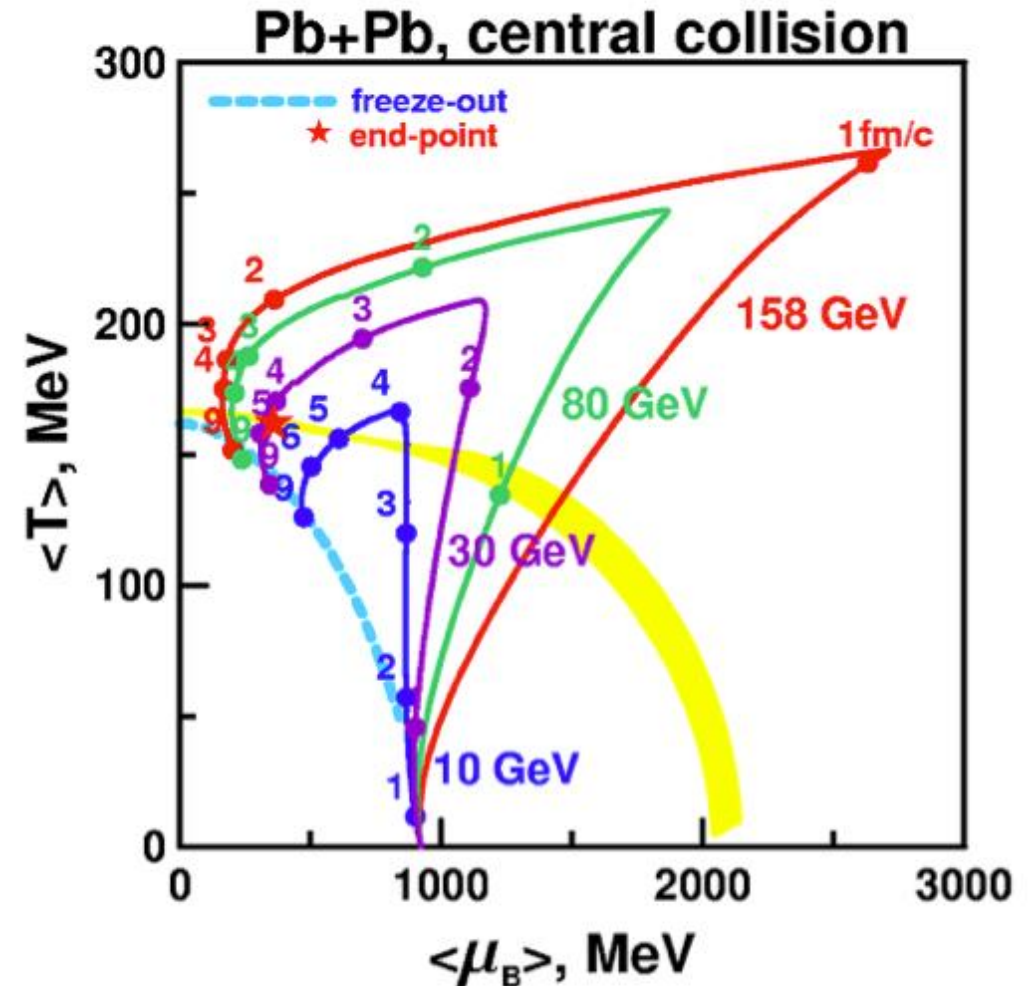
- By colliding nuclei with different center of mass energies, different regions of the phase diagram are explored.
- Thermal model fits to the experimental data define the chemical freeze-out line in the QCD phase diagram.
- The previously schematic phase diagram becomes one which is actually measured.



Y.B. Ivanov et al., Phys. Rev. C 73 (2006) 30.

Chemical freeze-out line

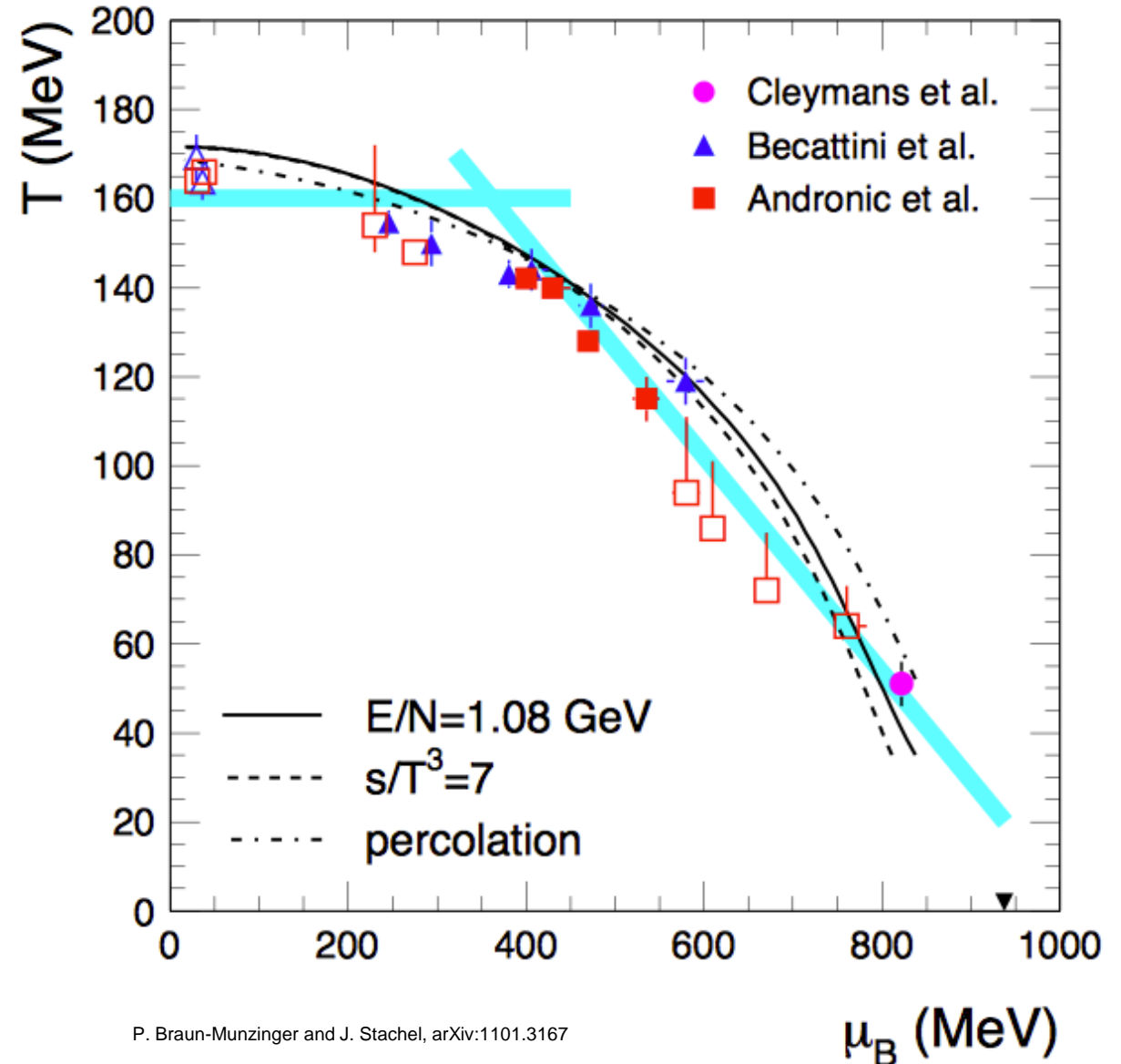
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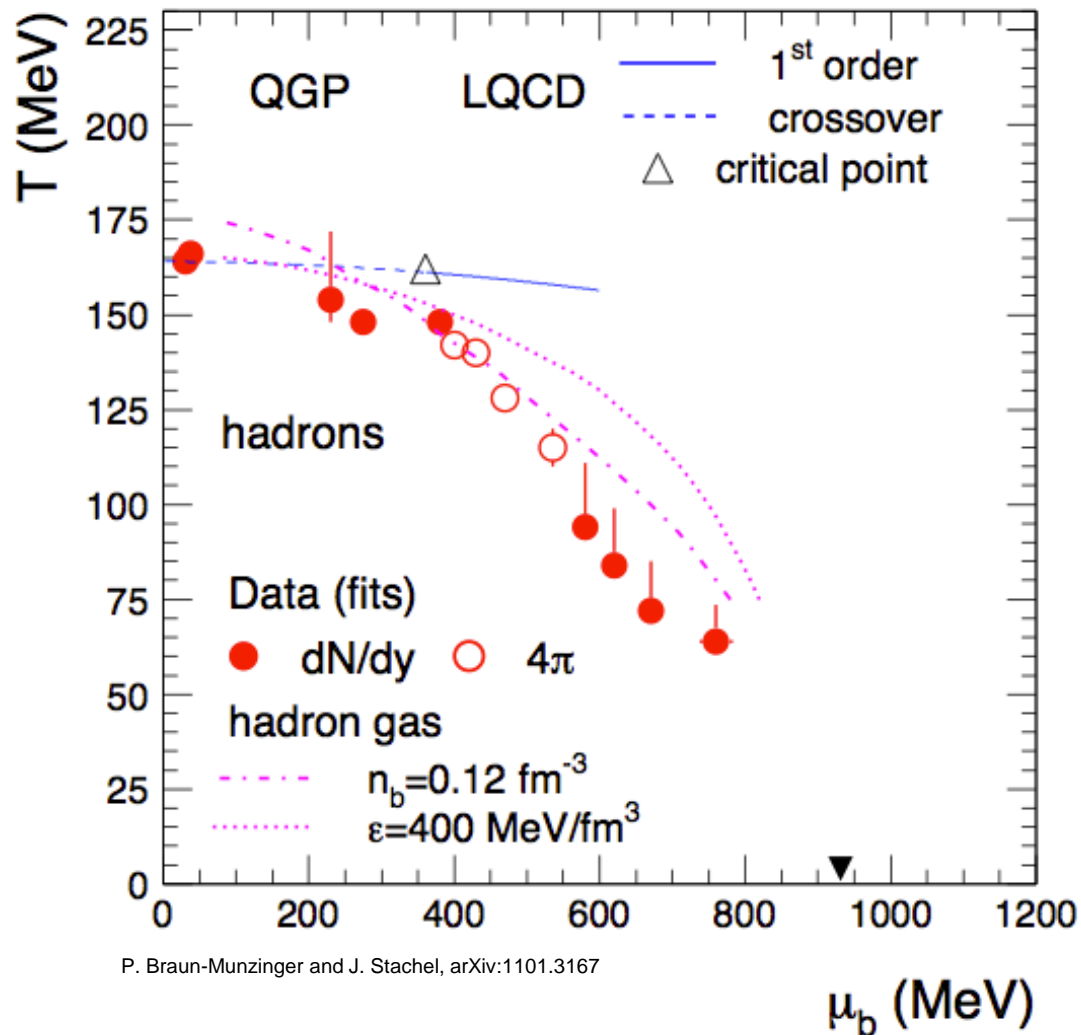
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P. Braun-Munzinger and J. Stachel, arXiv:1101.3167

Chemical freeze-out as a proof of QGP existence?



P. Braun-Munzinger and J. Stachel, arXiv:1101.3167

A priori, a thermal model description is not related to the QGP itself. It describes a *hadron gas* and not a *parton gas*.

However, the *chemical freeze-out line* determined by thermal fits coincides with the phase boundary calculated by lattice QCD above top SPS energies!

However, a detailed study of collision rates and timescales of fireball expansion imply that equilibrium cannot be reached in the hadronic phase...

Do multi-particle collisions near TC equilibrate the system? A rapid change in density near the **phase transition** can explain this [1].

Alternatively, the system is 'born into equilibrium' by the filling of phase space during hadronization [2].

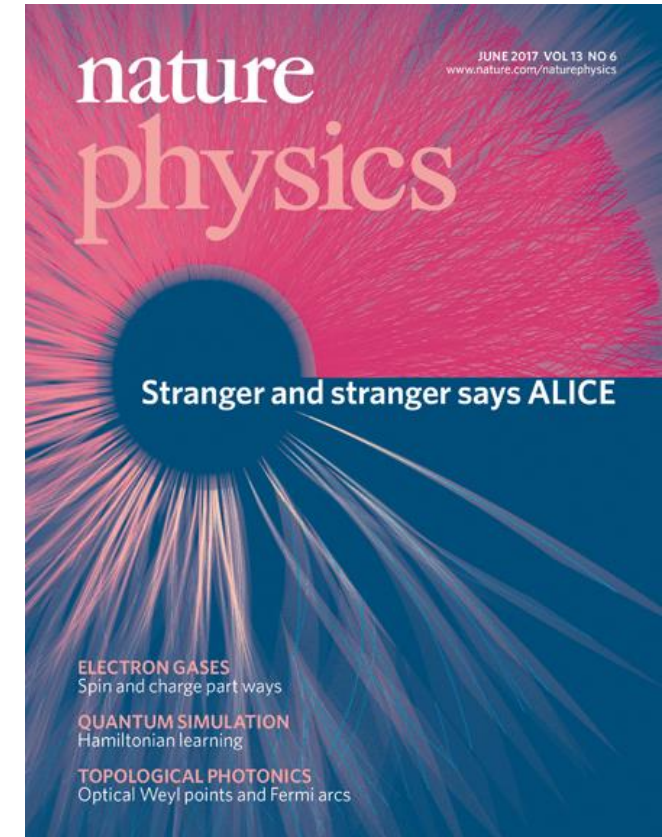
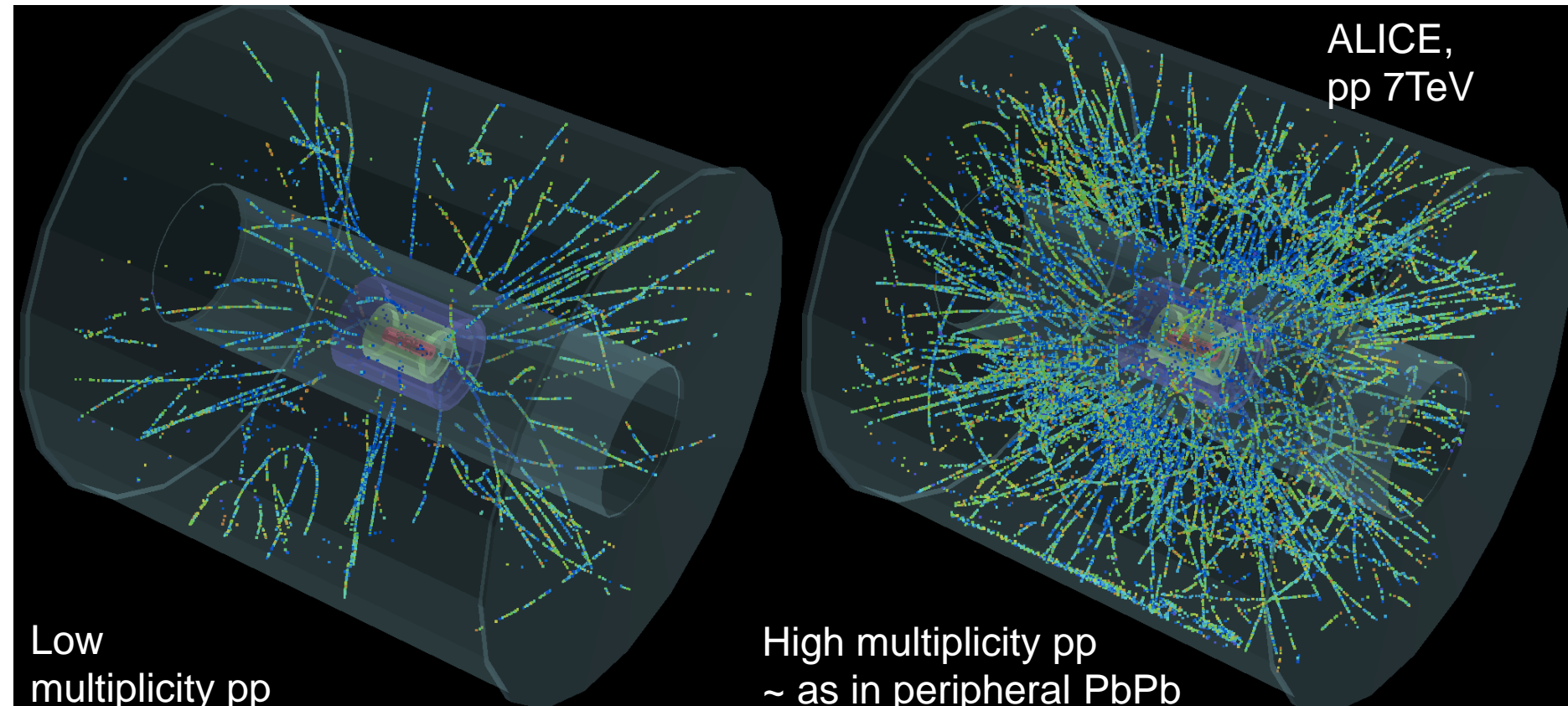
[1] Braun-Munzinger, P., Stachel, J. & Wetterich, C., Phys. Lett. B. 596, 61–69 (2004).

[2] Stock, R. Phys. Lett. B 456, 277–282 (1999).

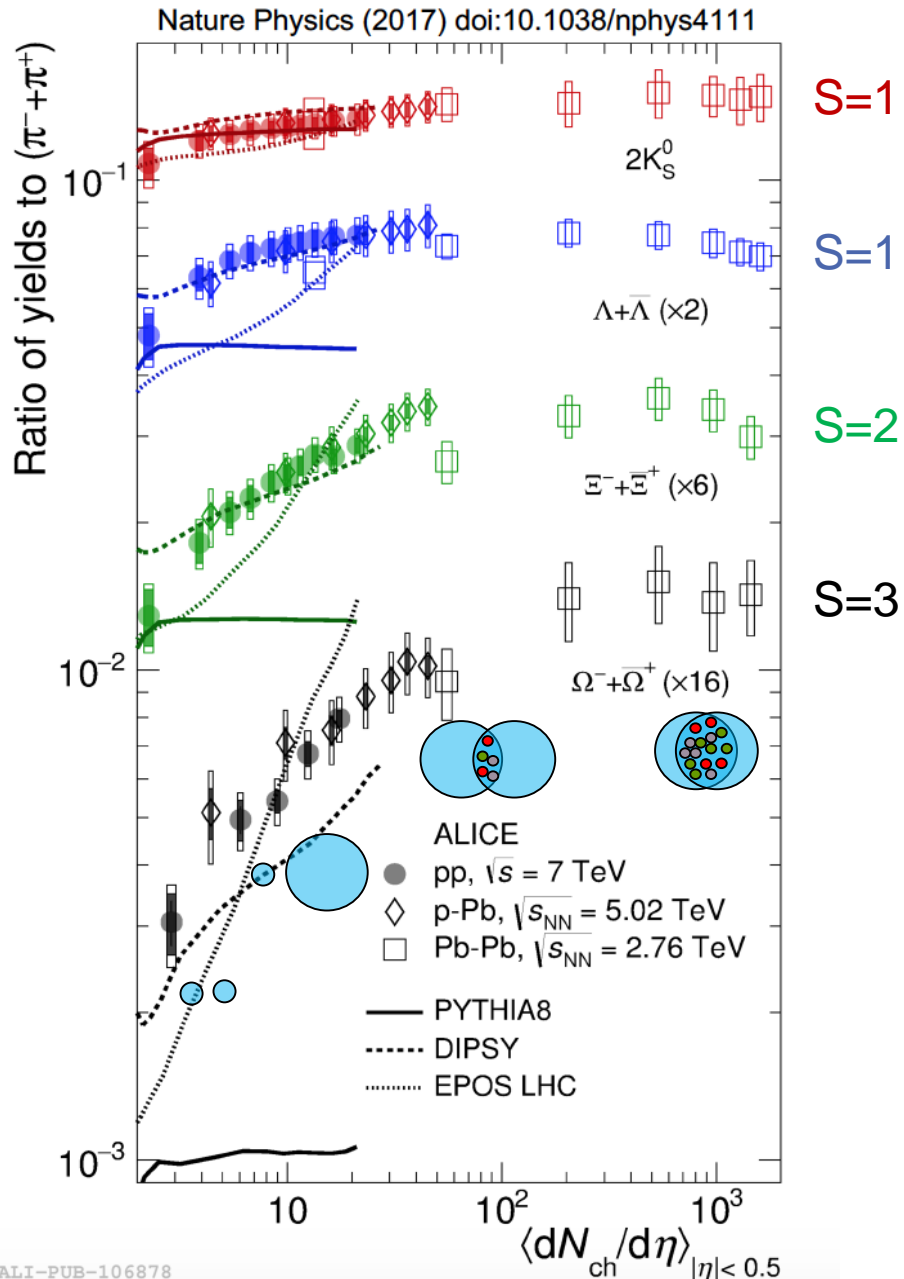
Small systems: high multiplicity pp and pPb

Particle chemistry

How does hadrochemistry evolve with system size?

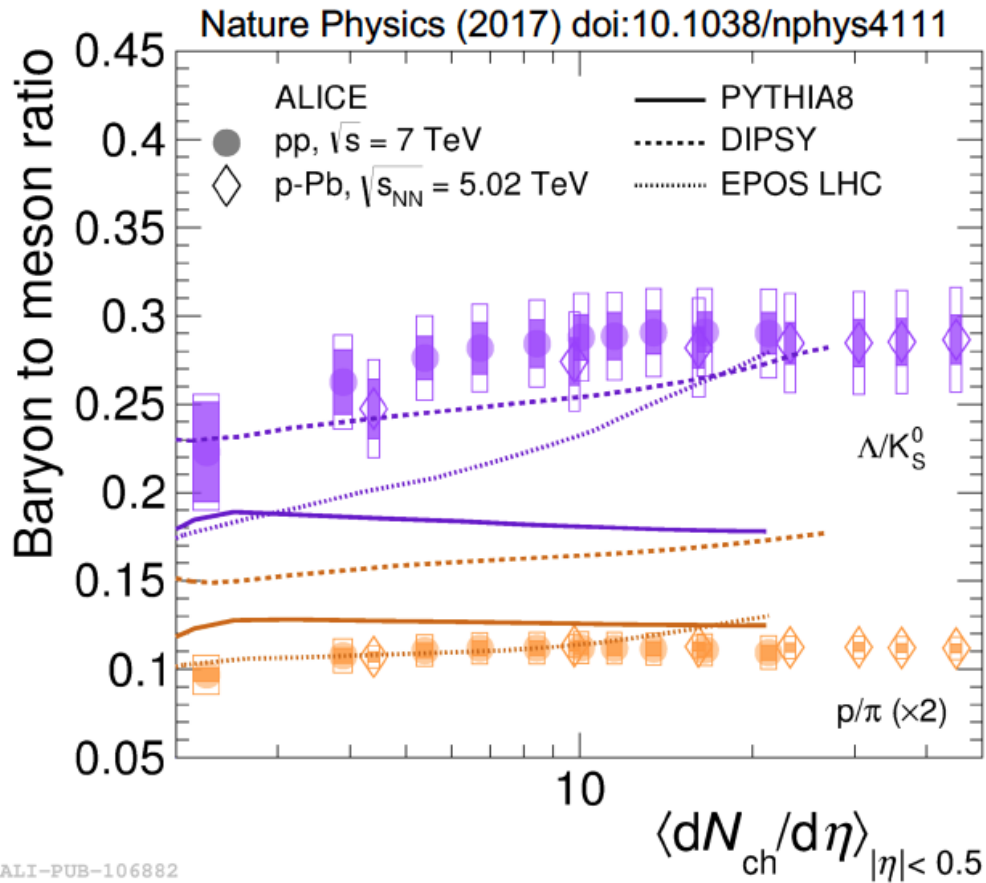


Chemical equilibrium in small systems



- Smooth evolution of hadrochemistry observed from pp to pPb to Pb-Pb collisions as a function of charged particle multiplicity.
- Significant enhancement of strange to non-strange particle production observed in pp collisions.
- pp collision data allows to compare to a plethora of QCD inspired event generators:
 - **PYTHIA8** completely **misses** the behavior of the data (independent of switching ON/OFF color reconnection)
 - **DIPSY** (color ropes) describes the increase in strangeness production qualitatively but fails to predict protons correctly in its original version..
 - **EPOS-LHC** (core-corona) only qualitatively describes the trend.

Chemical equilibrium in small systems

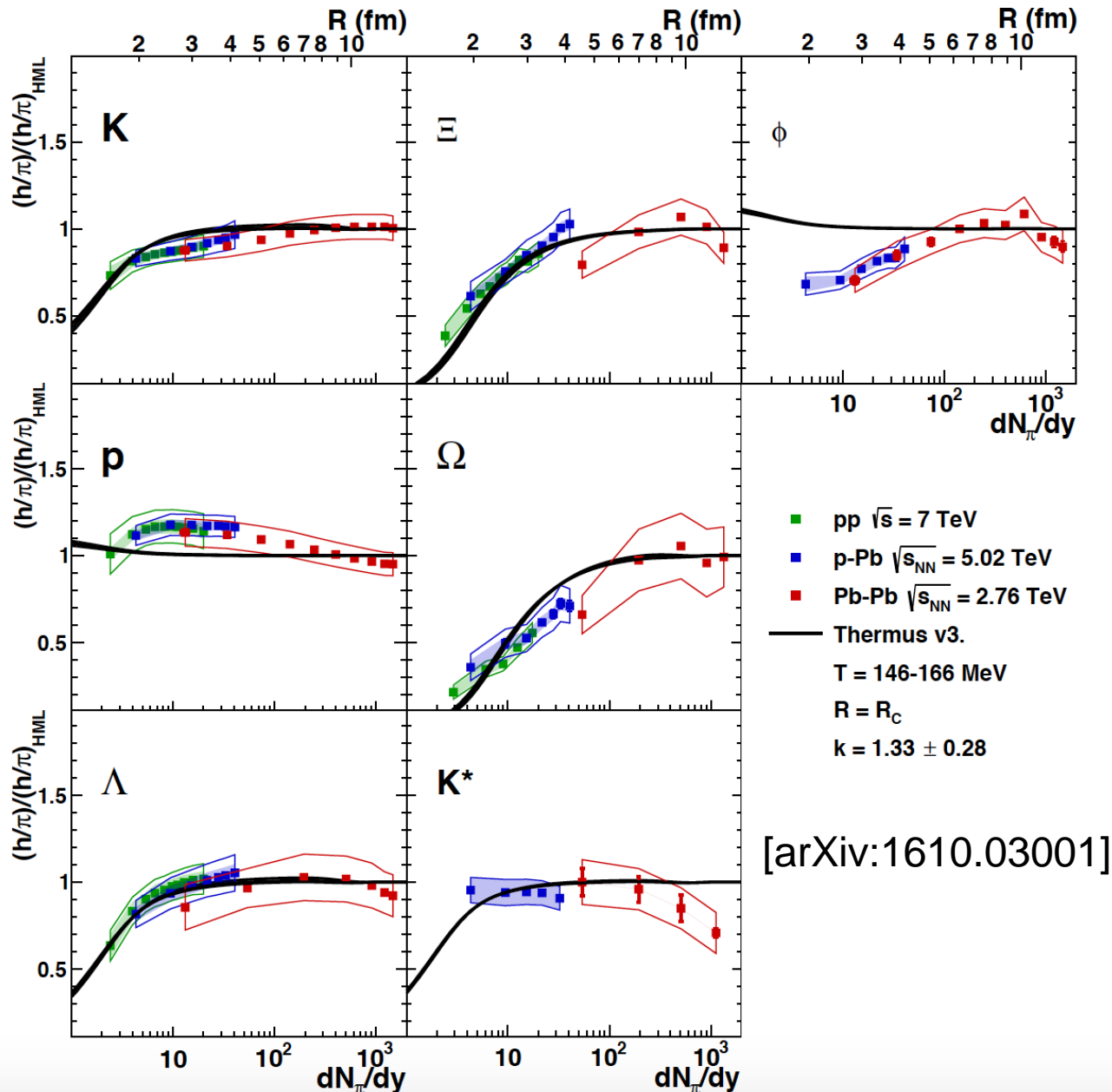


- The chemical equilibrium picture holds also in small collision systems such as high multiplicity pp and pPb collisions.

→ Currently one of the hottest topics in heavy-ion research!

→ Hyperon-to-pion enhancement is strangeness related and not mass or baryon number related.

Strangeness canonical suppression



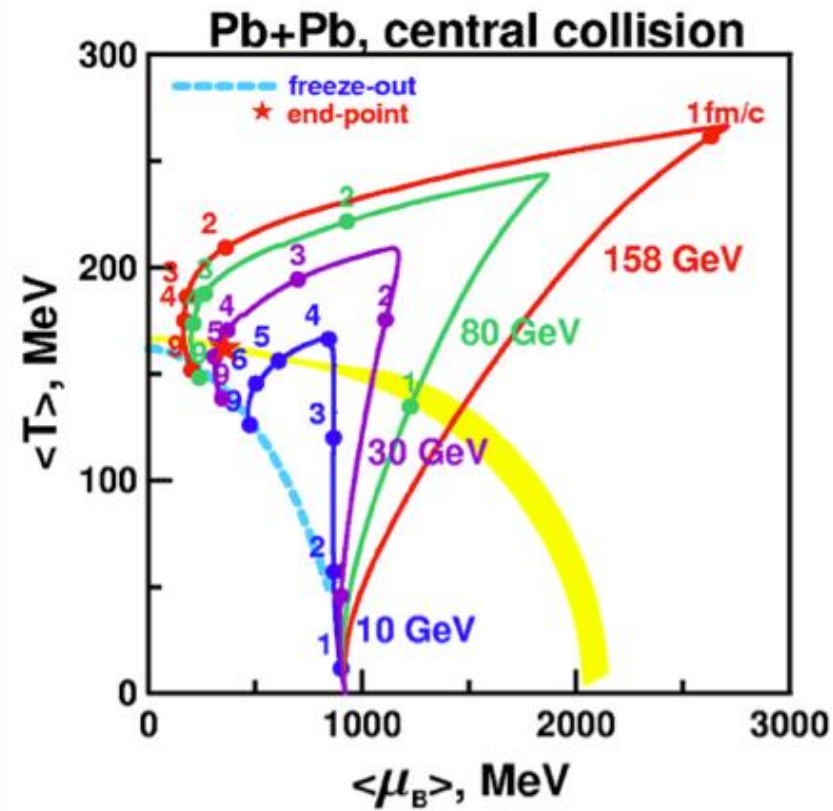
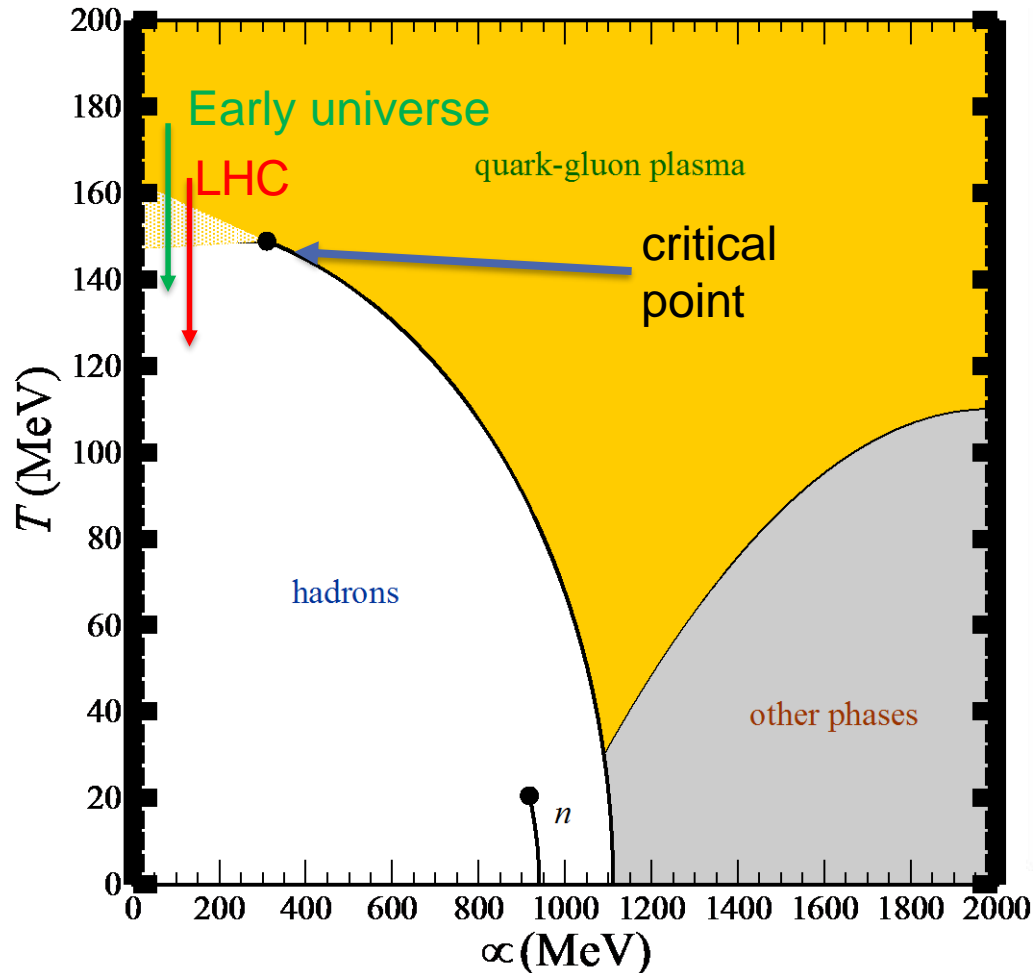
- From a thermal-statistical point of view strangeness production is very sensitive to the system size, i.e. the total number of produced particles.
- As it is rare (w.r.t to u, d), but not so rare (w.r.t c, b, t), its thermal production rate is influenced by the explicit conservation of the strangeness quantum number.
- Simplified picture: explicit conservation of strangeness limits the phase-space for strange particle production and leads to a suppression in small systems (\leftrightarrow **strangeness enhancement in large systems**).

QGP thermodynamics and soft probes

Search for QCD critical point and onset of de-confinement

The QCD critical point

- By a variation of beam energies, one might hit the critical point in the QCD phase diagram => *critical chiral dynamics*.



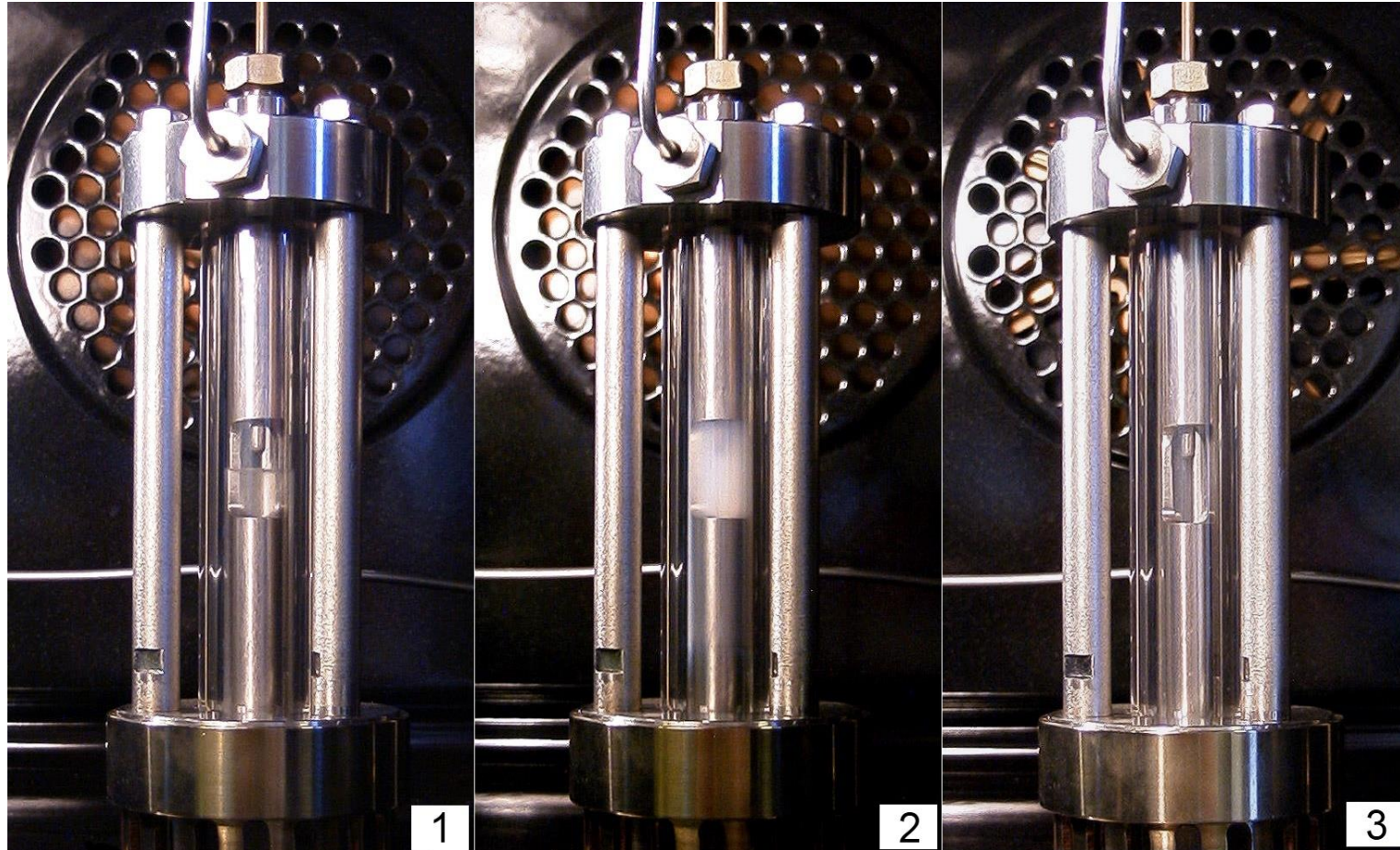
Y.B. Ivanov et al., Phys. Rev. C 73 (2006) 30.

→ Different regions of the phase diagram are probed with different $\sqrt{s_{NN}}$.

=> Beam energy scan (BES) at RHIC.

Critical fluctuations – in ordinary matter

- Phase transitions are often connected to critical phenomena.
- Example: Opalescence of Ethene at the critical point (divergence of correlation lengths).



[S. Horstmann, Ph.D. Thesis University Oldenburg]

Fluctuations in QCD

- QCD phase transitions: the thermodynamic susceptibilities χ of the conserved quantities of QCD (**electric charge Q**, **baryon number B**, **Strangeness S**) correspond to (event-by-event) fluctuations in the particle production.

$$\chi_{lmn}^{BSQ} = \frac{\partial^{l+m+n}(P/T^4)}{\partial(\mu_B/T)^l \partial(\mu_S/T)^m \partial(\mu_Q/T)^n}$$

- Fluctuations are quantified as moments (mean, variance, skewness, kurtosis) or cumulants **K** of the event-by-event distributions:

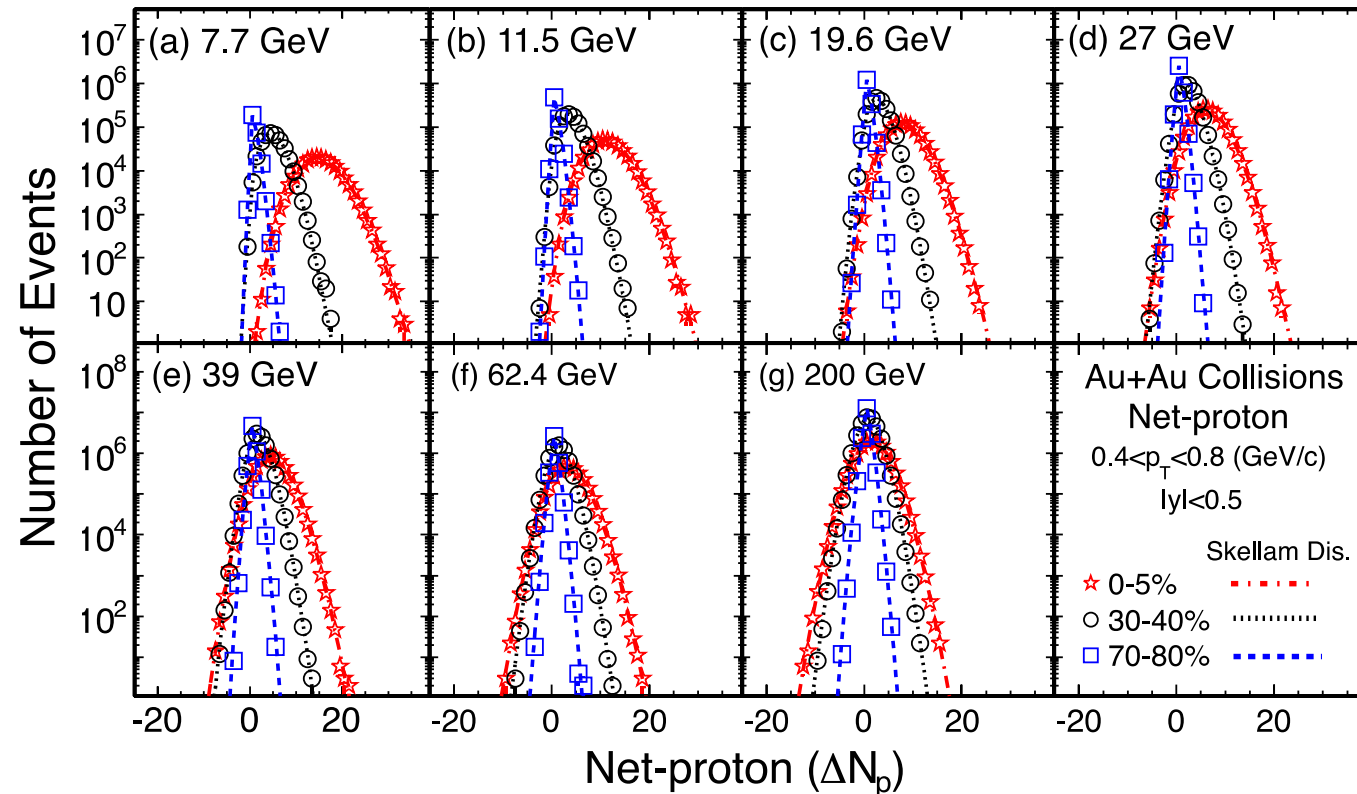
$$\begin{array}{llllll} M & = & K_1 & = & \mu & = & \langle N \rangle & = & VT^3 \cdot \chi_1 \\ \sigma^2 & = & K_2 & = & \mu_2 & = & \langle (\delta N)^2 \rangle & = & VT^3 \cdot \chi_2 \\ S & = & K_3/\sigma^3 & = & \mu_3/\sigma^3 & = & \langle (\delta N)^3 \rangle / \sigma^3 & = & VT^3 \cdot \chi_3 / (VT^3 \cdot \chi_2)^{3/2} \\ \kappa & = & K_4/\sigma^4 & = & (\mu_4 - 3\mu_2^2)/\mu_2^2 & = & \langle (\delta N)^4 \rangle / \sigma^4 - 3 & = & (VT^3 \cdot \chi_4) / (VT^3 \cdot \chi_2)^2 \end{array}$$

$$\mu_i = \langle (\delta N)^i \rangle$$

$$\delta N = N - \langle N \rangle$$

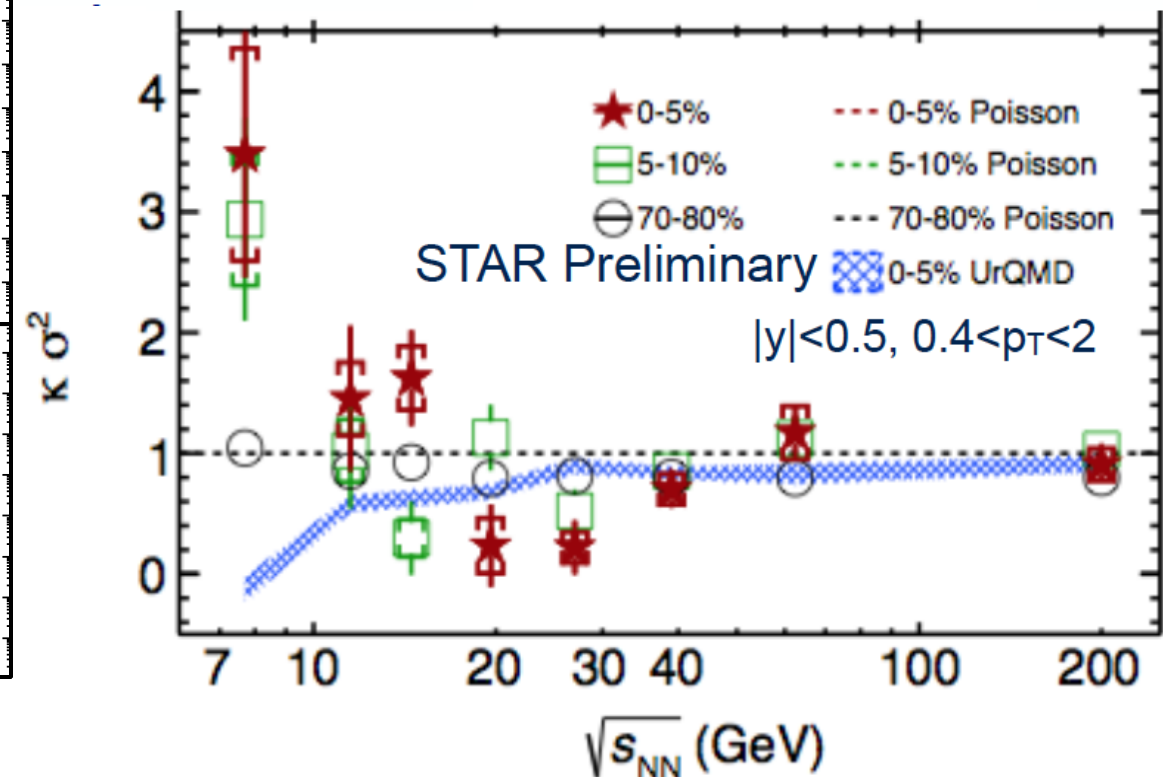
Critical fluctuations – in quark matter

- In the QCD case, **event-by-event fluctuations** in the conserved charges of QCD (Baryon number B , Strangeness S , electric charge Q).
- Key observable: baryon number fluctuations quantified as the higher moments χ_B of the net-proton ($N_p - N_{\text{anti-p}}$) distribution => fixed at chemical freeze-out



[PRL 112 (2014) 032302]

→ Hint for deviation from Poisson baseline in kurtosis around $\sqrt{s_{NN}} \approx 20$ GeV?

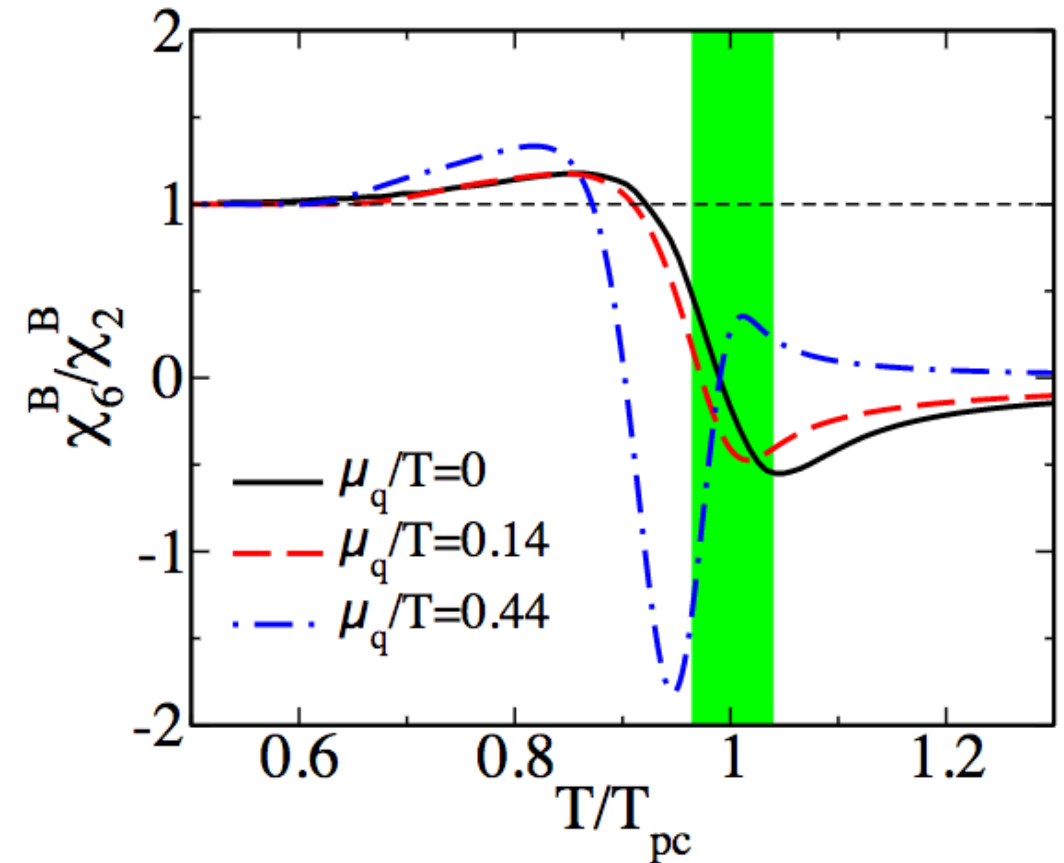


Chiral critical dynamics at LHC energies

- Even though LHC energies are far away from the critical point, remnants of the critical chiral dynamics might still be measurable in higher order net-charge fluctuations at the LHC.

→ Test of a Lattice QCD prediction.

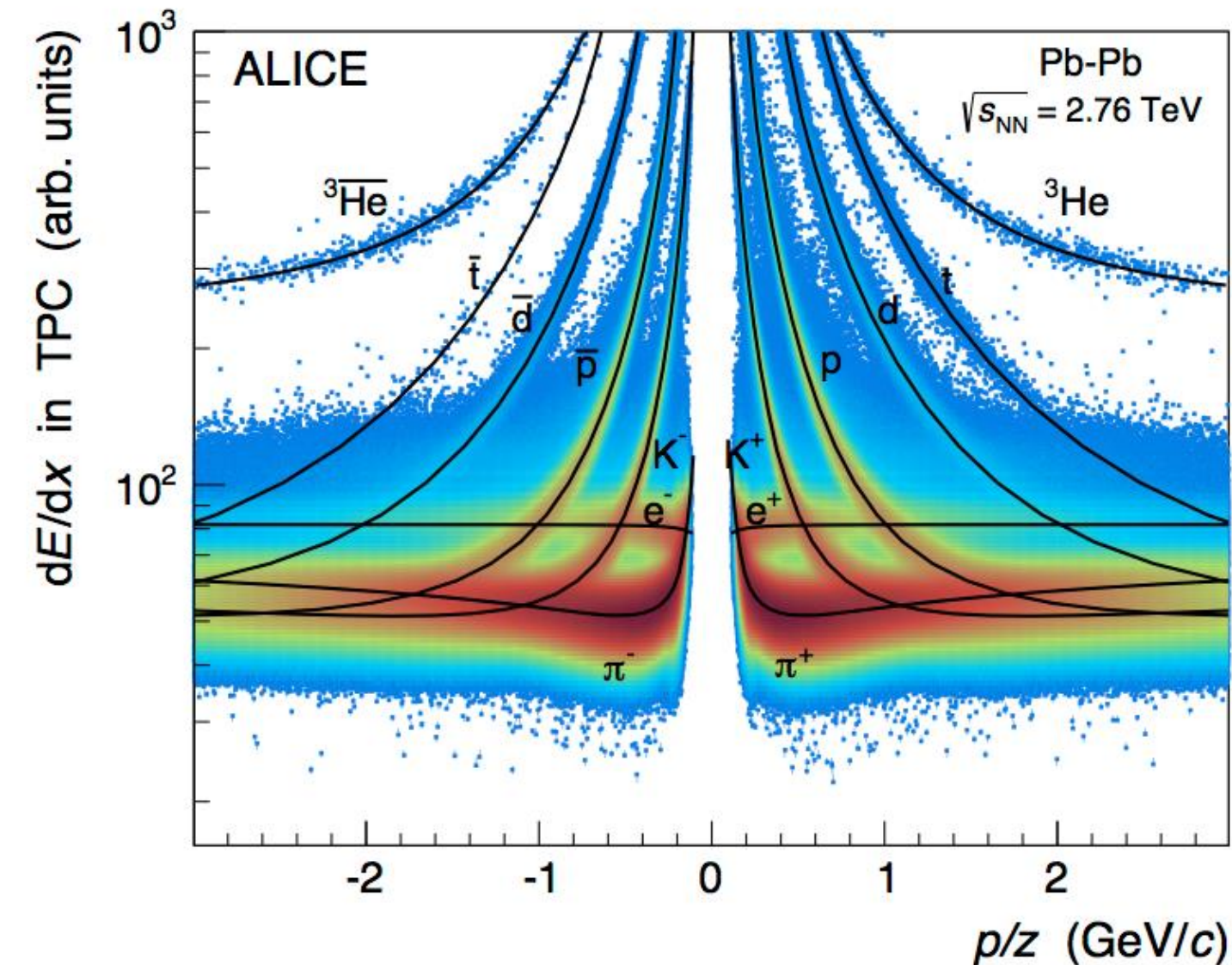
→ Experimental proof that chiral and de-confinement phase transition occur indeed at the same temperature.



[Eur. Phys. J. C 71 (2011) 1694]

QGP thermodynamics and soft probes (anti-)(hyper-)nuclei

Particle identification via dE/dx

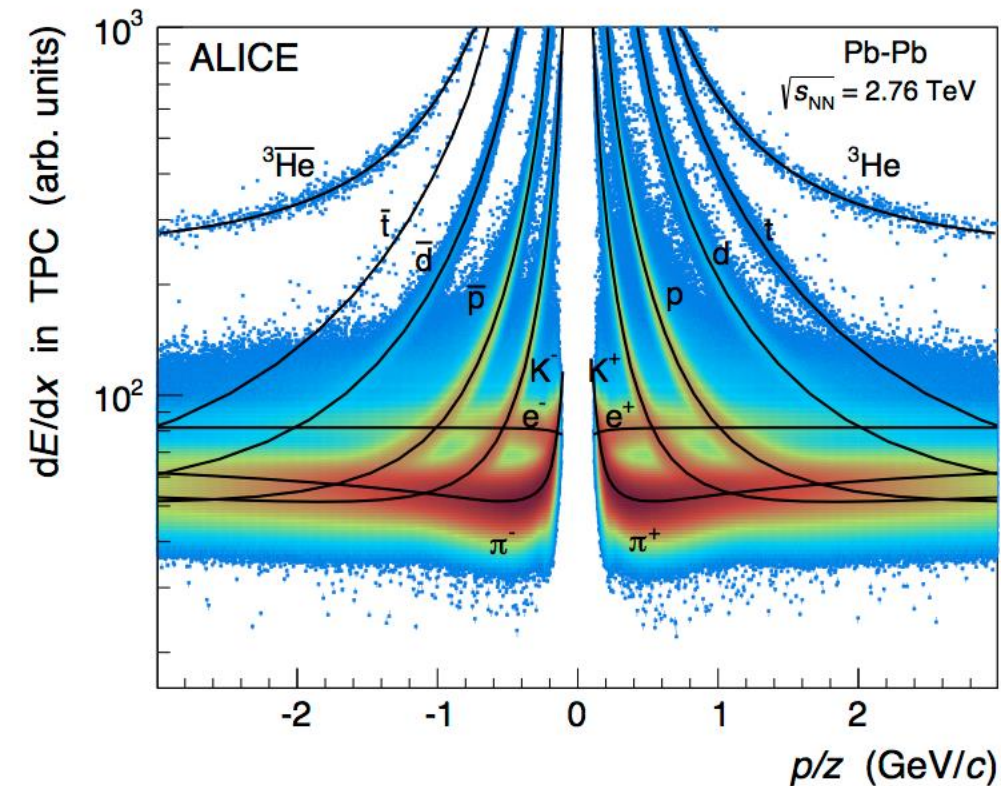


$$\left\langle -\frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 W_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

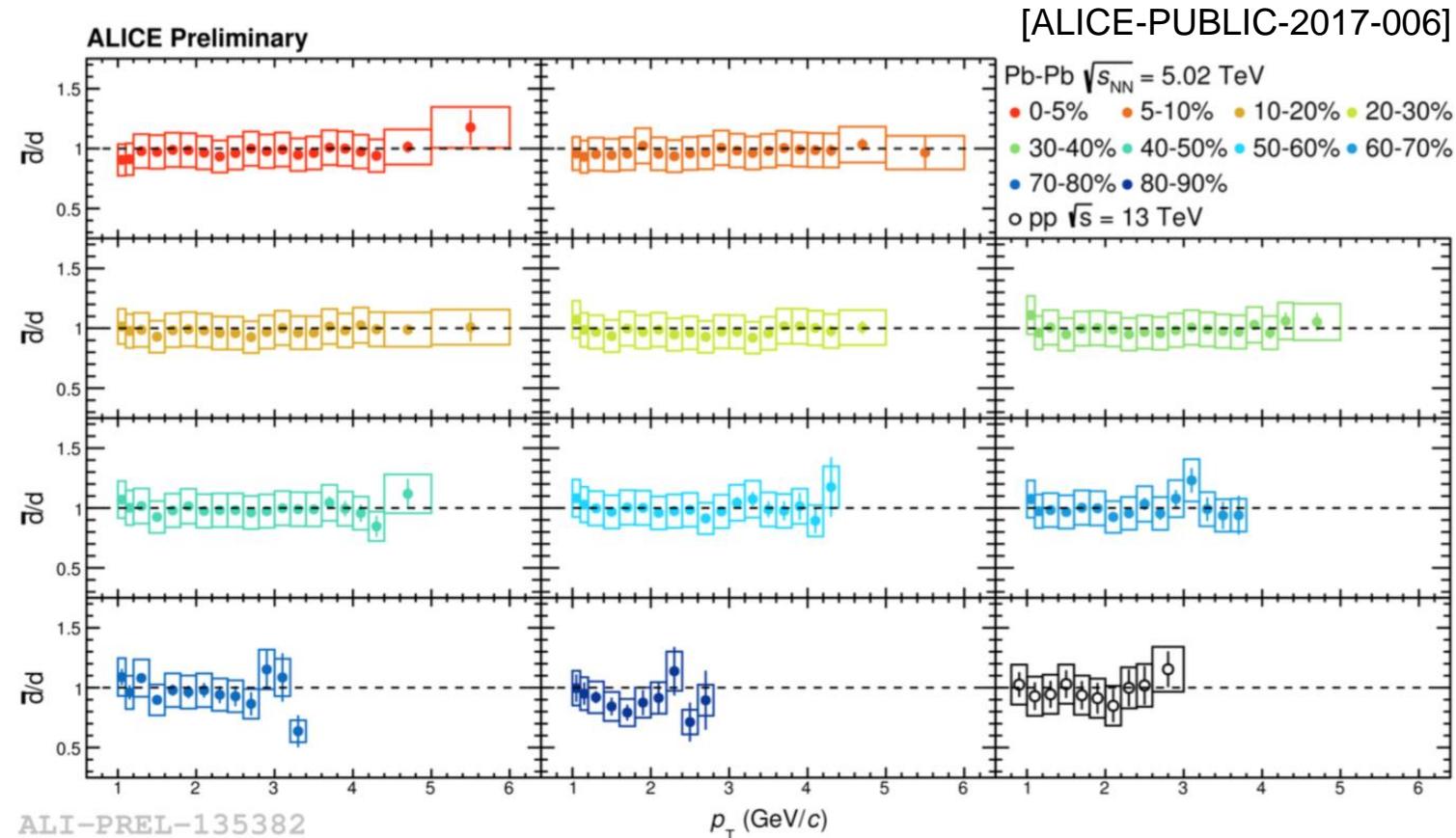
Separation of $z = 1$ and $z = 2$ via dE/dx is also very important for the correct determination of the momentum via the track curvature: $p_T \sim 0.3 B \cdot r \cdot z$

Measurements of (anti-)(hyper-)nuclei

- Collisions at the LHC produce a large amount of (anti-)(hyper-)nuclei.
 - Matter and anti-matter are produced in equal abundance at LHC energies.
 - Open puzzle: production yields are in agreement with thermal model prediction even though light (anti-)nuclei should be dissolved in such a hot medium.

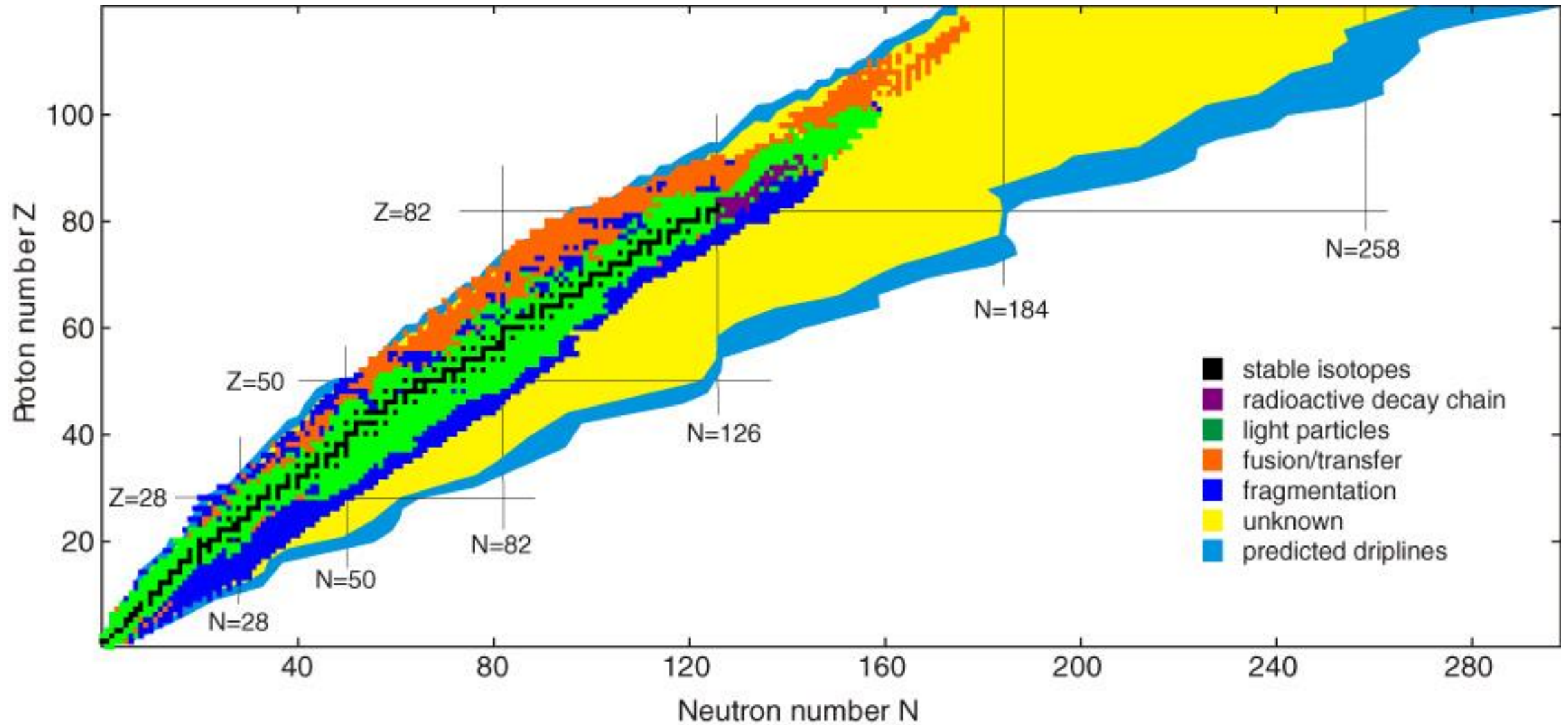


[PRC 93 (2016) 024917]



ALI-PREL-135382

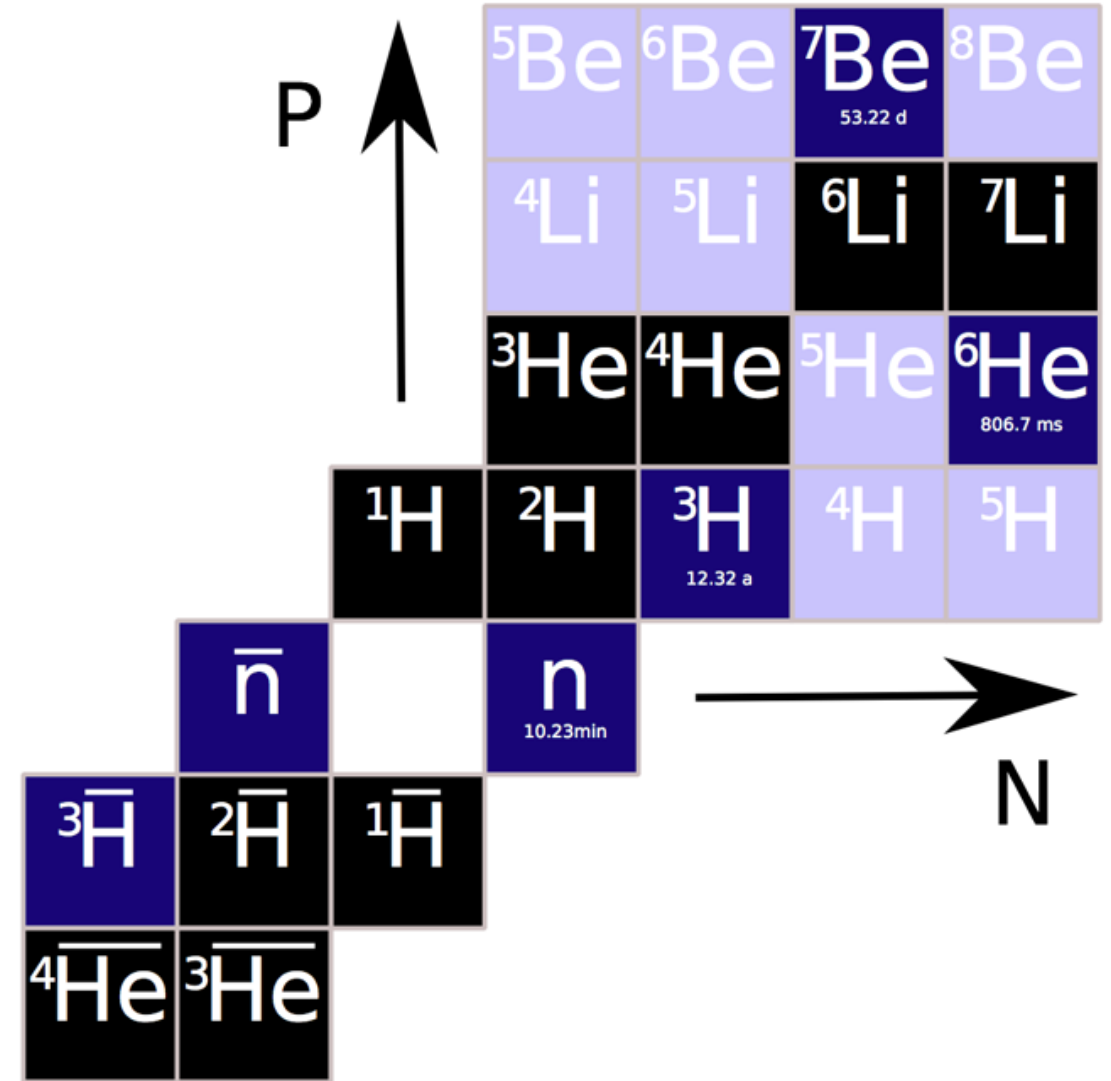
Table of nuclides



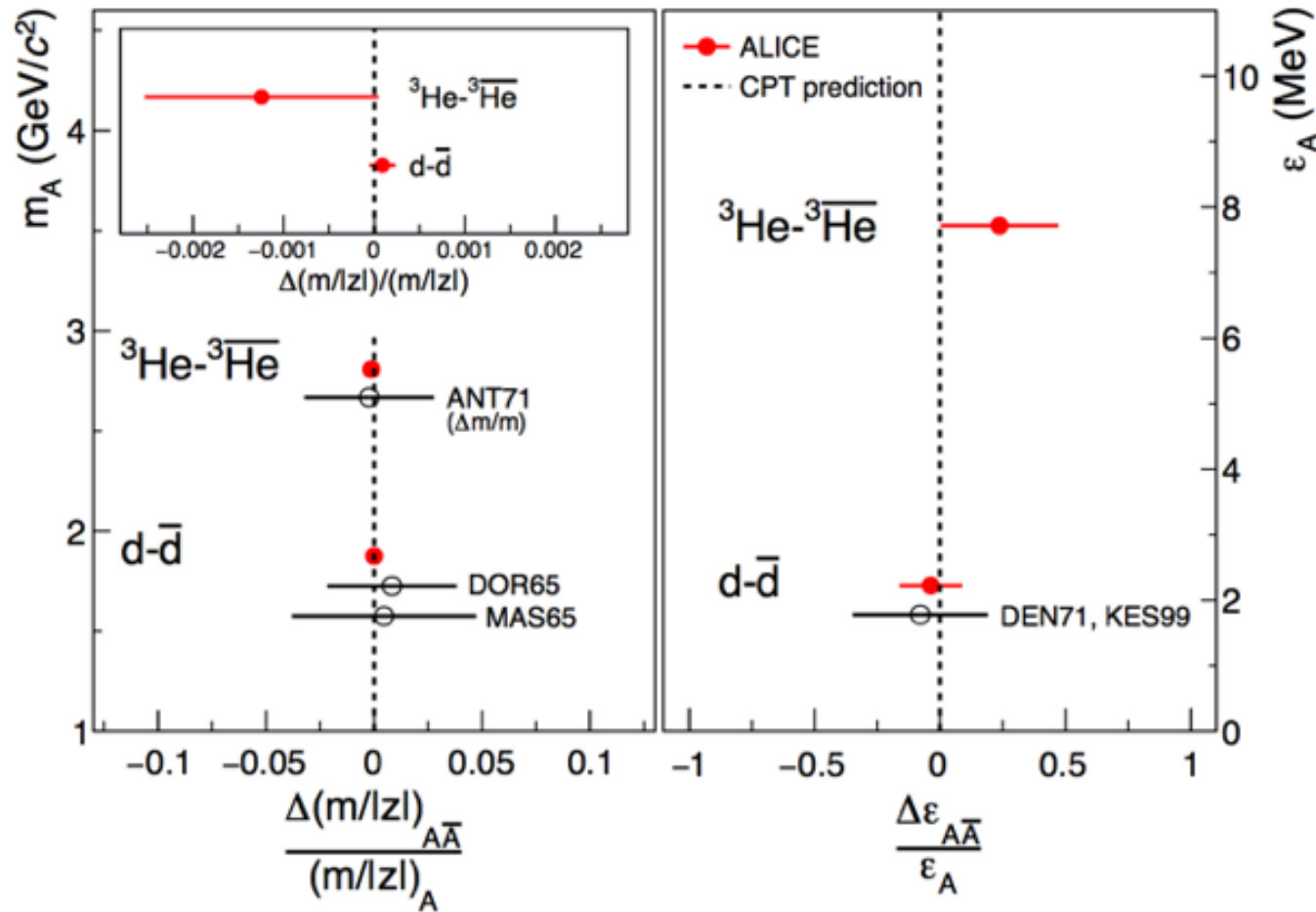
Light (anti-)nuclei

- Even in Pb-Pb collisions at LHC energies, light anti-nuclei are rarely produced.
- (Anti-)nuclei up to the (anti-)alpha are in reach (1st observation of the anti-alpha by the STAR experiment at RHIC in 2011).

→ A very good and very stable particle identification is needed to separate these rare particles from the background.



Testing CPT with anti-nuclei



The ALICE collaboration performed a test of the CPT invariance looking at the mass difference between nuclei and anti-nuclei.

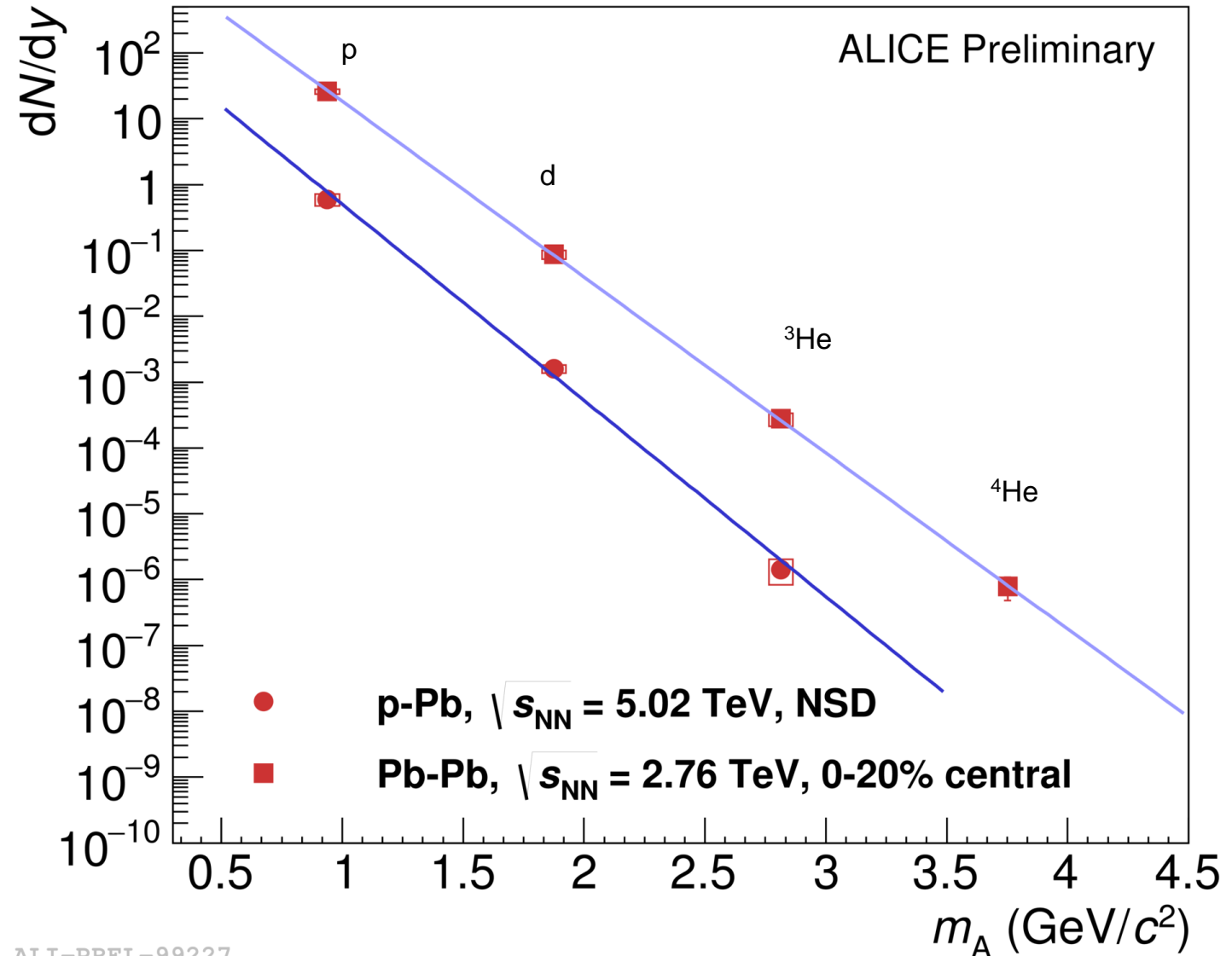
This test shows that the masses of nuclei and anti-nuclei are compatible within the uncertainties. The binding energies are compatible in nuclei and anti-nuclei as well.

[Nature Physics 11 (2015) 811-814]

Mass ordering

→ For each additional nucleon the production yield decreases by a factor of about 300!

→ Such a behaviour can be directly derived from the thermal model which predicts in first order $dN/dy \sim \exp(-m/T)$

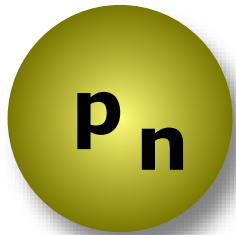


ALI-PREL-99227

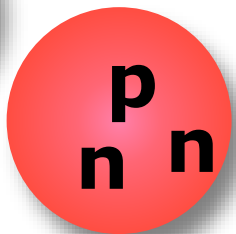
Hyper-nuclei (1)

- By 'replacing' one nucleon by one hyperon, the table of nuclides can be extended in a third dimension.
- Hyper-nuclei have a long tradition in nuclear physics: discovery in the 1950s by M. Danysz and J. Pniewski in a nuclear emulsion exposed to cosmic rays.

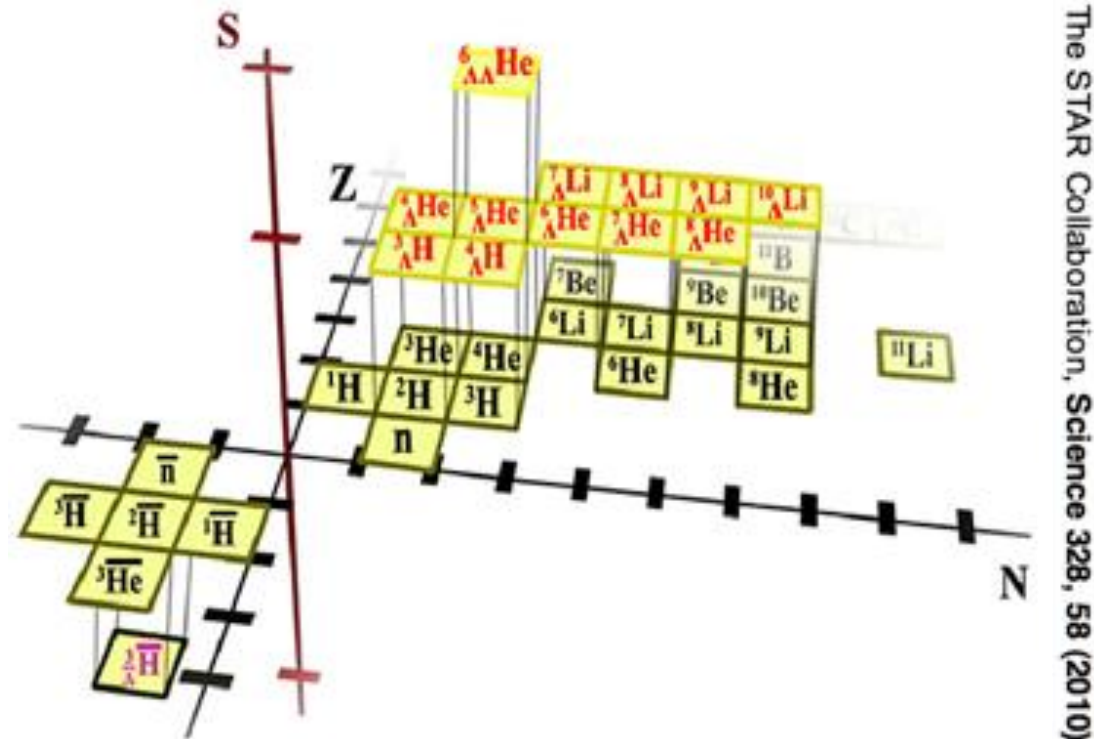
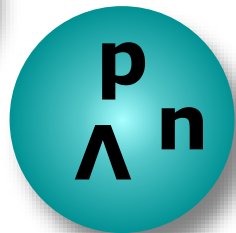
deuteron



triton

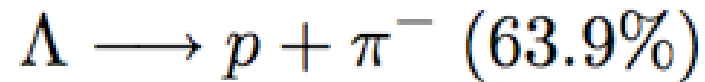


hyper-triton

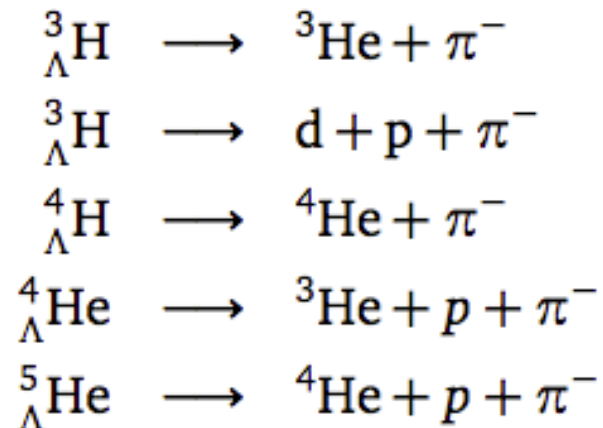


Hyper-nuclei (2)

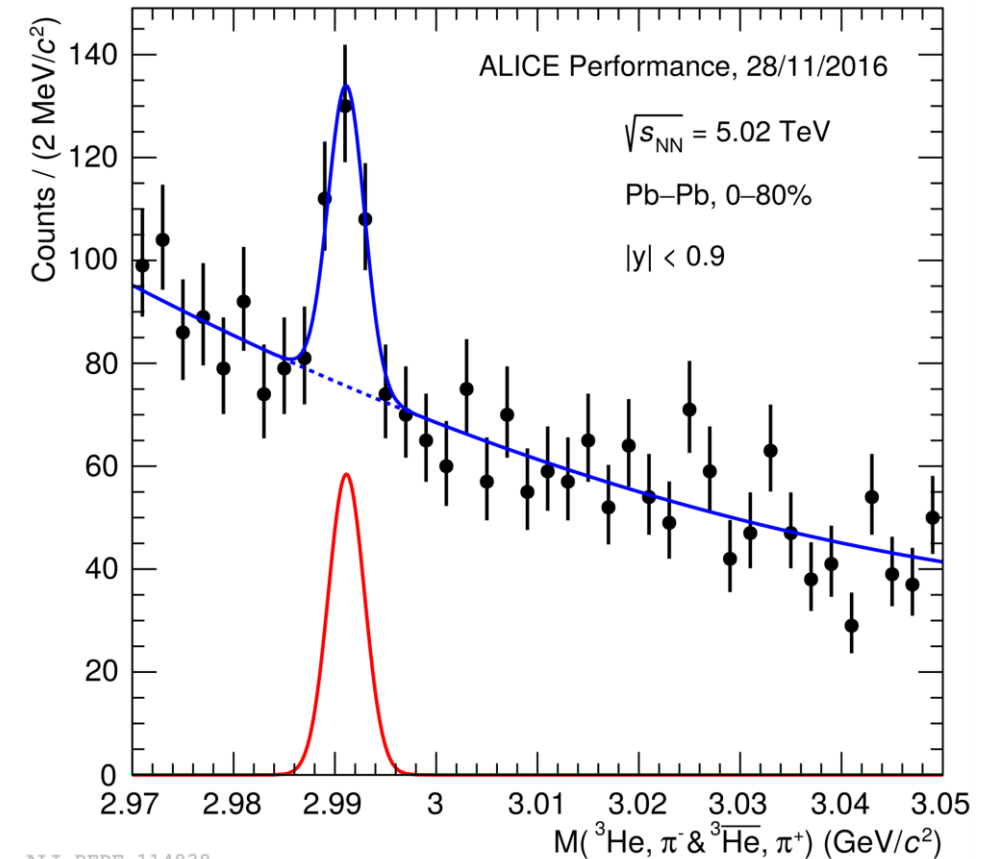
- Reconstruction of hyper-nuclei can be based on well established techniques for Λ and other weakly decaying light flavor hadrons as lifetimes and decay topologies are similar.



- Experimentally one searches for (anti-)nuclei from displaced vertices:



- Branching ratios are only partially constrained by measurements.



(anti-)(hyper-)nuclei – impact beyond heavy-ion physics

- A. Heavy-ion measurements may help in constraining the not well known lifetime of the hyper-triton (sensitive to the hyperon-nucleon interaction potential in nuclear physics).
- B. Collider measurements are used for background estimations in the searches for (anti-) nuclei of galactic/dark matter origin (such as in AMS).

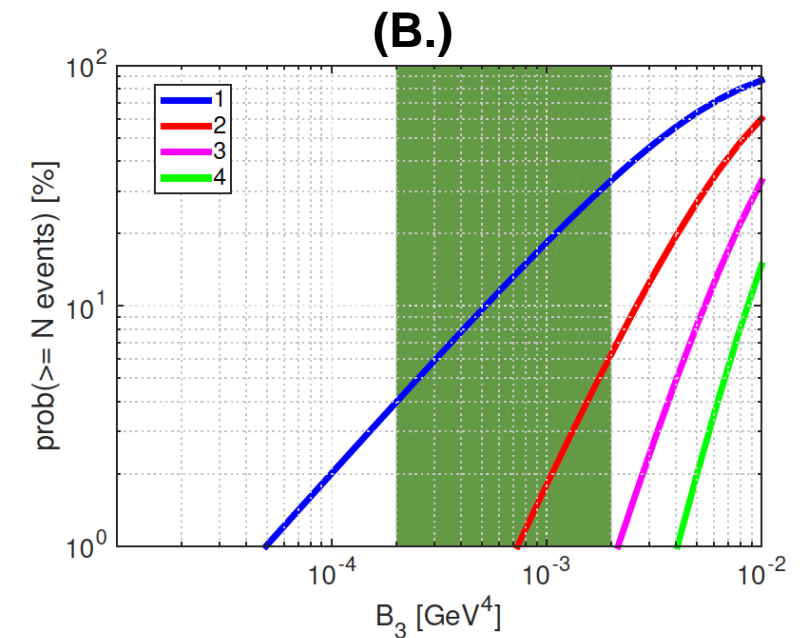
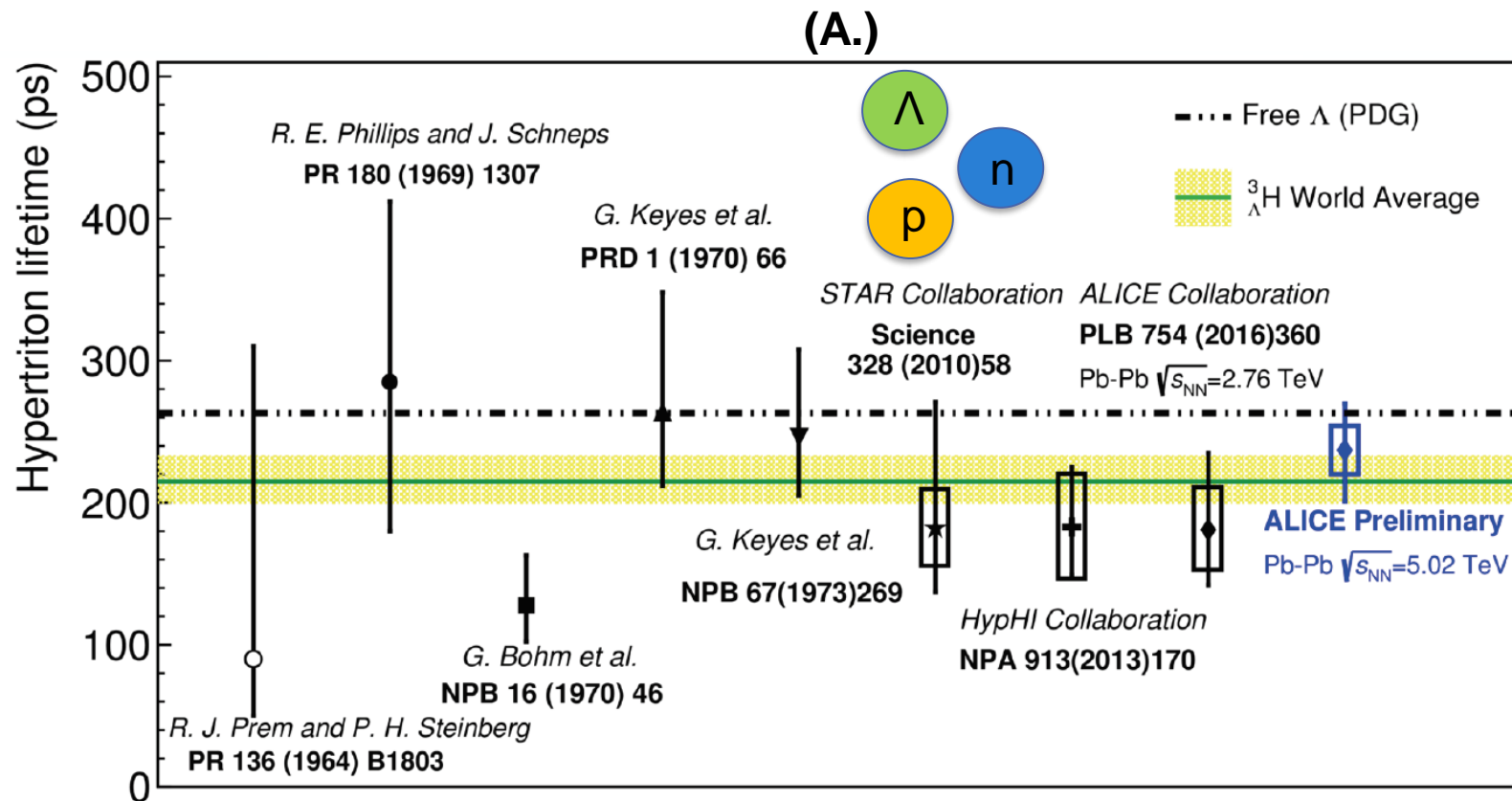


FIG. 5: Poisson probability for detecting $N \geq 1, 2, 3, 4$ ^3He events in a 5-yr analysis of AMS02, assuming the same exposure as in the \bar{p} analysis [28]. Eq. (14) shown as green band.

[K. Blum et al., arXiv:1704.05431]

QGP thermodynamics and soft probes

Radial and elliptic flow

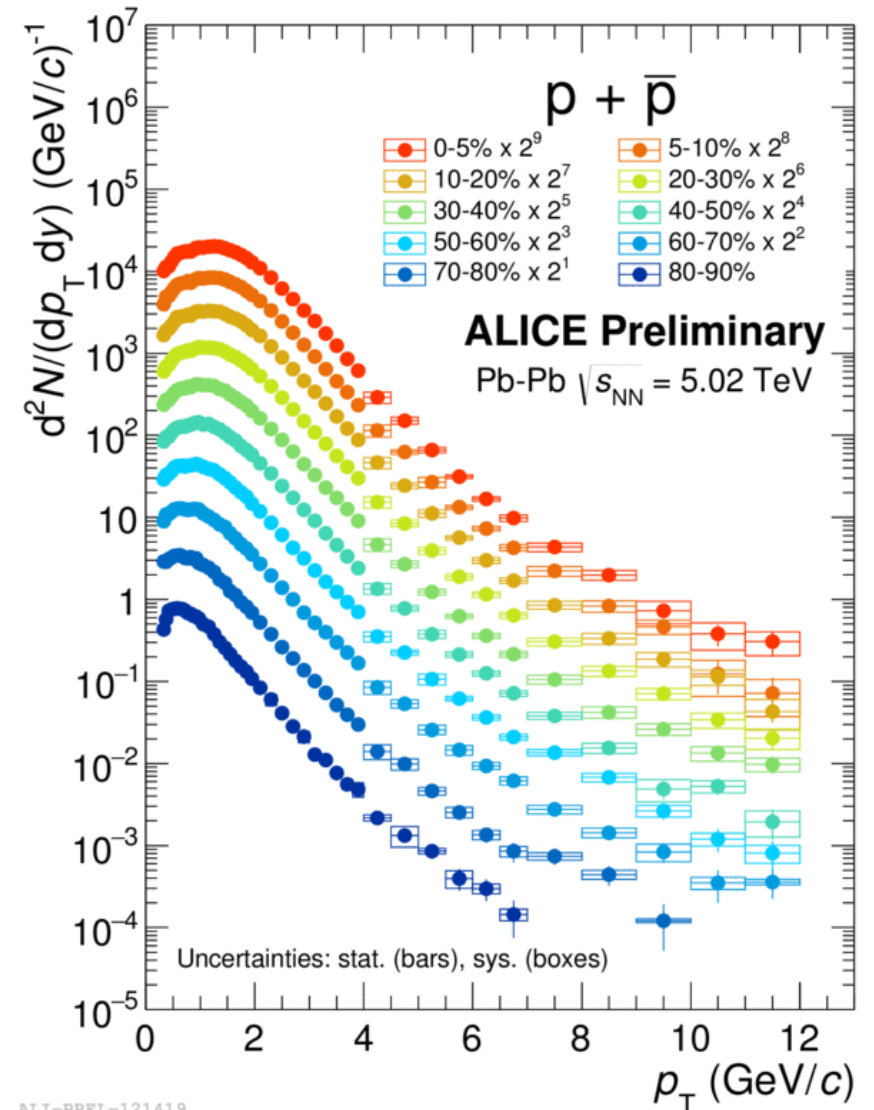
Bulk particle production and collectivity

- Low p_T hadrons composed of (u,d,s) valence quarks define the collective behaviour of the fireball.
- “Baseline model of ultra-relativistic heavy-ion physics”

A fireball in *local thermodynamic equilibrium*:

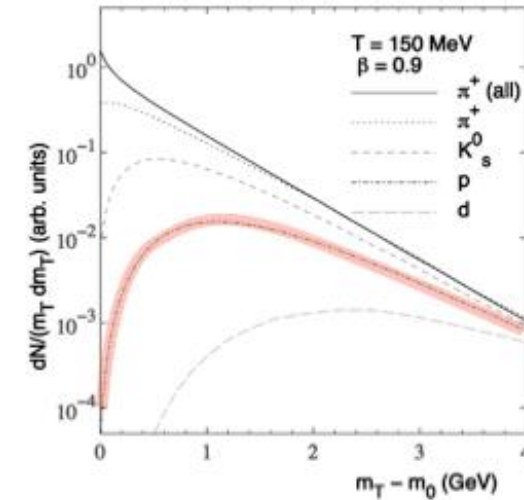
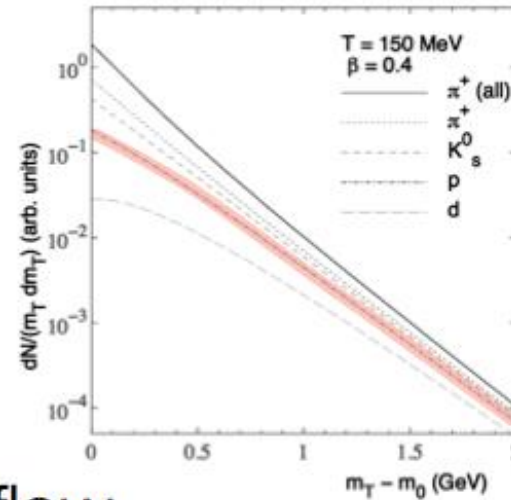
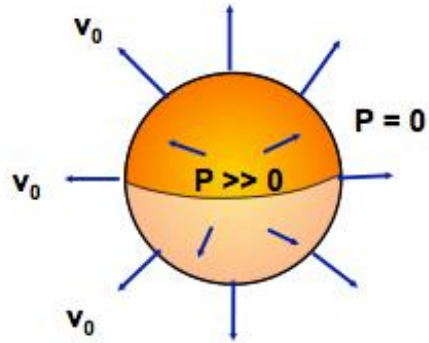
- **particle chemistry** in agreement with thermal model predictions
- p_T -spectra and v_2 measurements show patterns of radial and elliptic **hydrodynamic flow**.

N.B.: Collective flow has nothing to do with the particle flow method to reconstruct tracks and jets in ATLAS/CMS

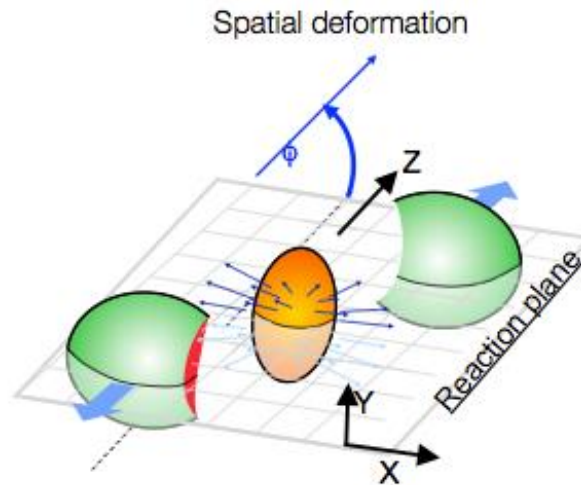


Radial and elliptic flow

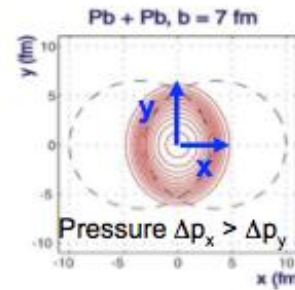
Isotropic **radial** flow



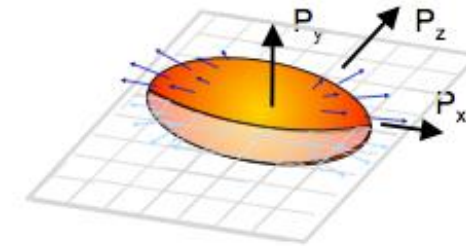
Anisotropic (**elliptic**) flow



Azimuthal (φ)
pressure gradients



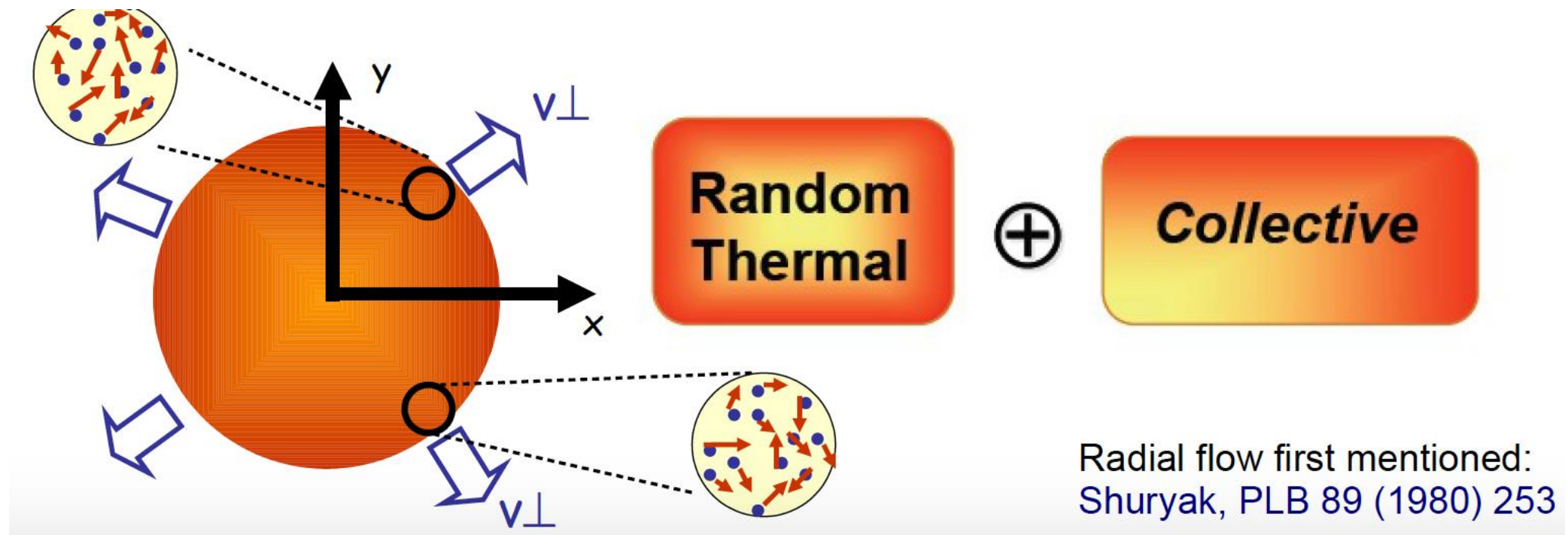
Anisotropic particle density



$$\frac{dN}{d\varphi} \propto 1 + 2v_1 \cos[\varphi - \Psi_1] + 2v_2 \cos[2(\varphi - \Psi_2)] + 2v_3 \cos[3(\varphi - \Psi_3)] + \dots$$

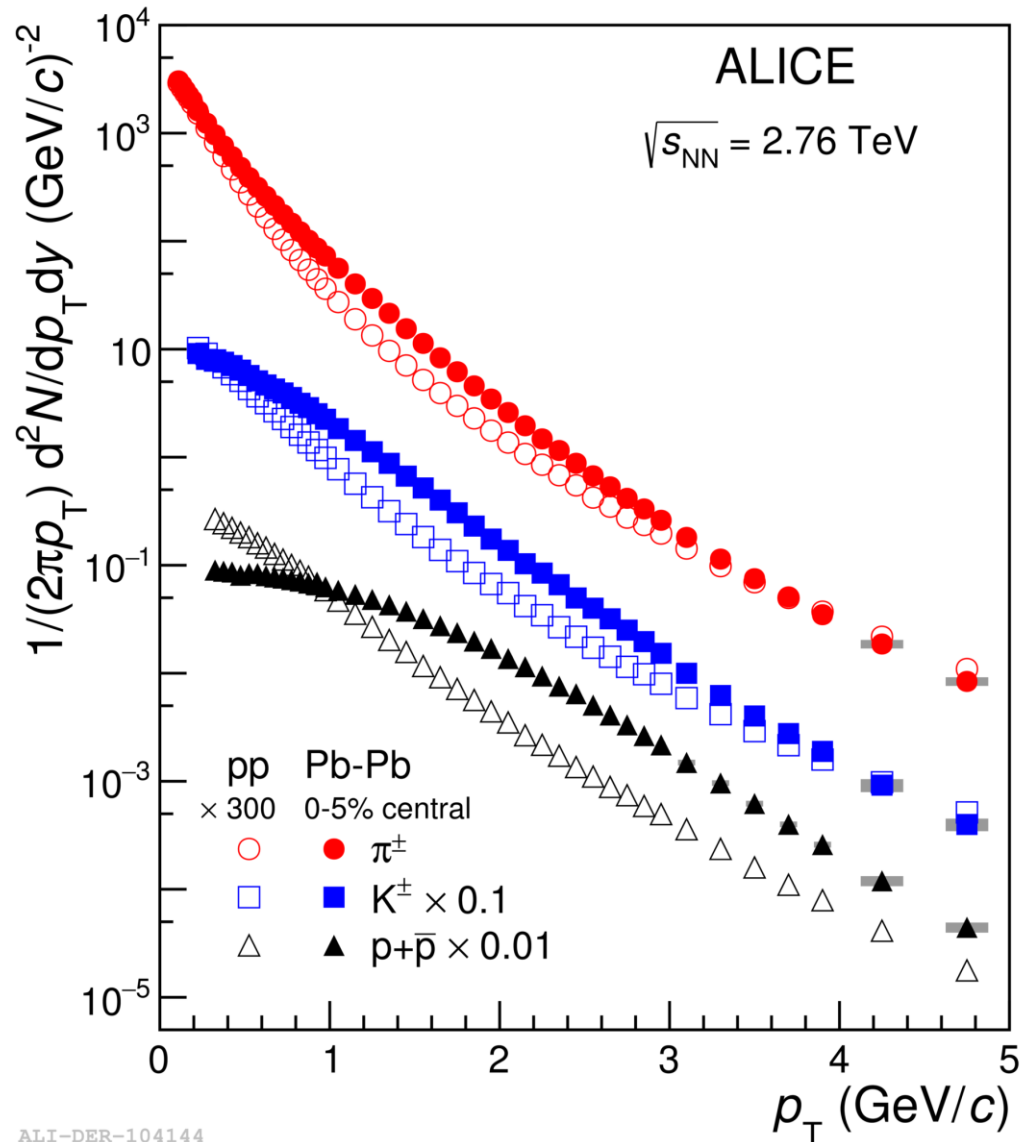
Flow in AA collisions

- Flow picture: **Collective motion of particles superimposed to the thermal motion.**
- Radial flow is a natural consequence of any interacting system expanding into the vacuum.



From: C. Loizides

Radial flow (1)

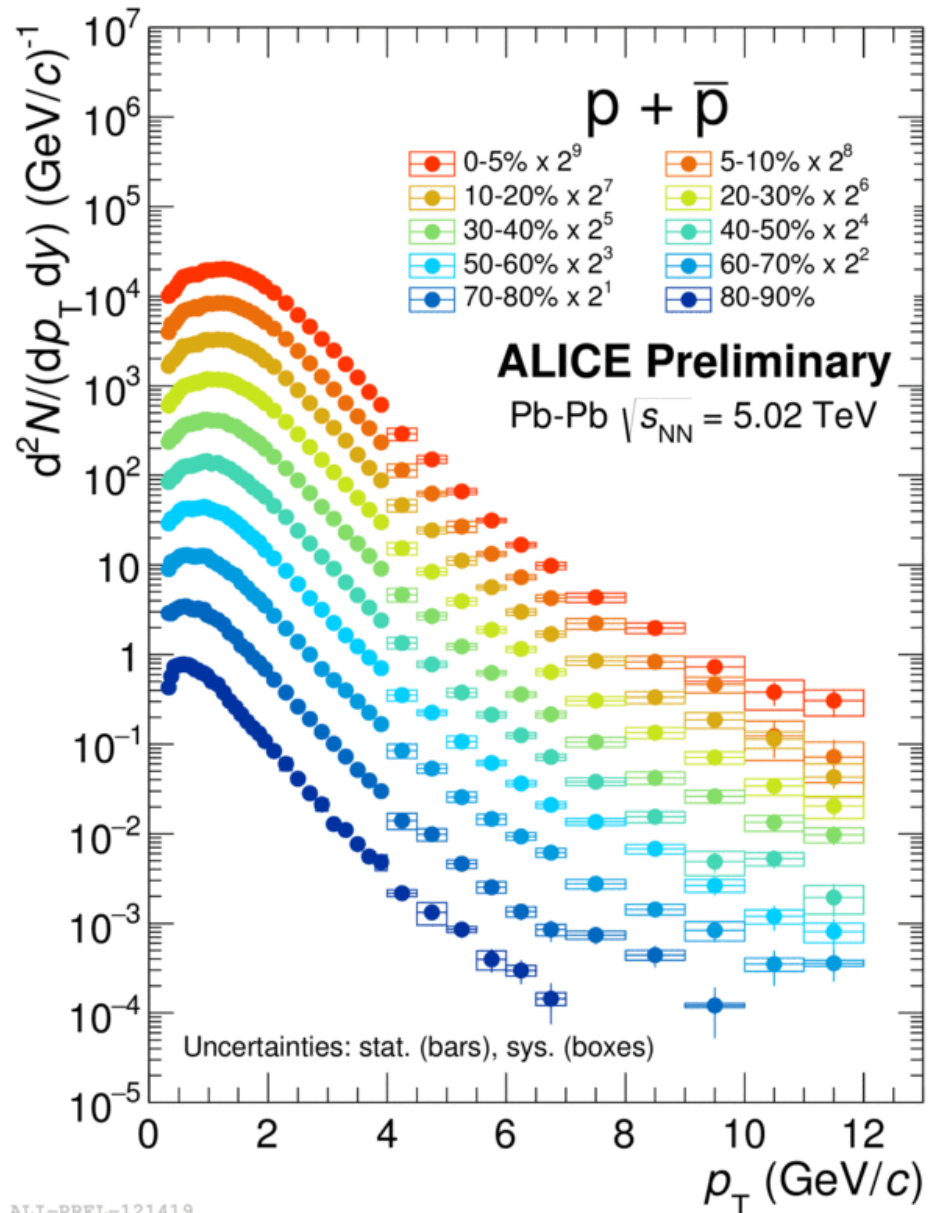


ALI-DER-104144

Common radial hydrodynamic expansion leads to a modification of the spectral shape: mass dependent *boost*.

- p_T -spectra harden with centrality.
- More pronounced for heavier particles (e.g.: $p > K > \pi$) as *velocities* become equalized in the flow field ($p = \beta\gamma \cdot m$).
- Hydrodynamic models show a good agreement with the data.

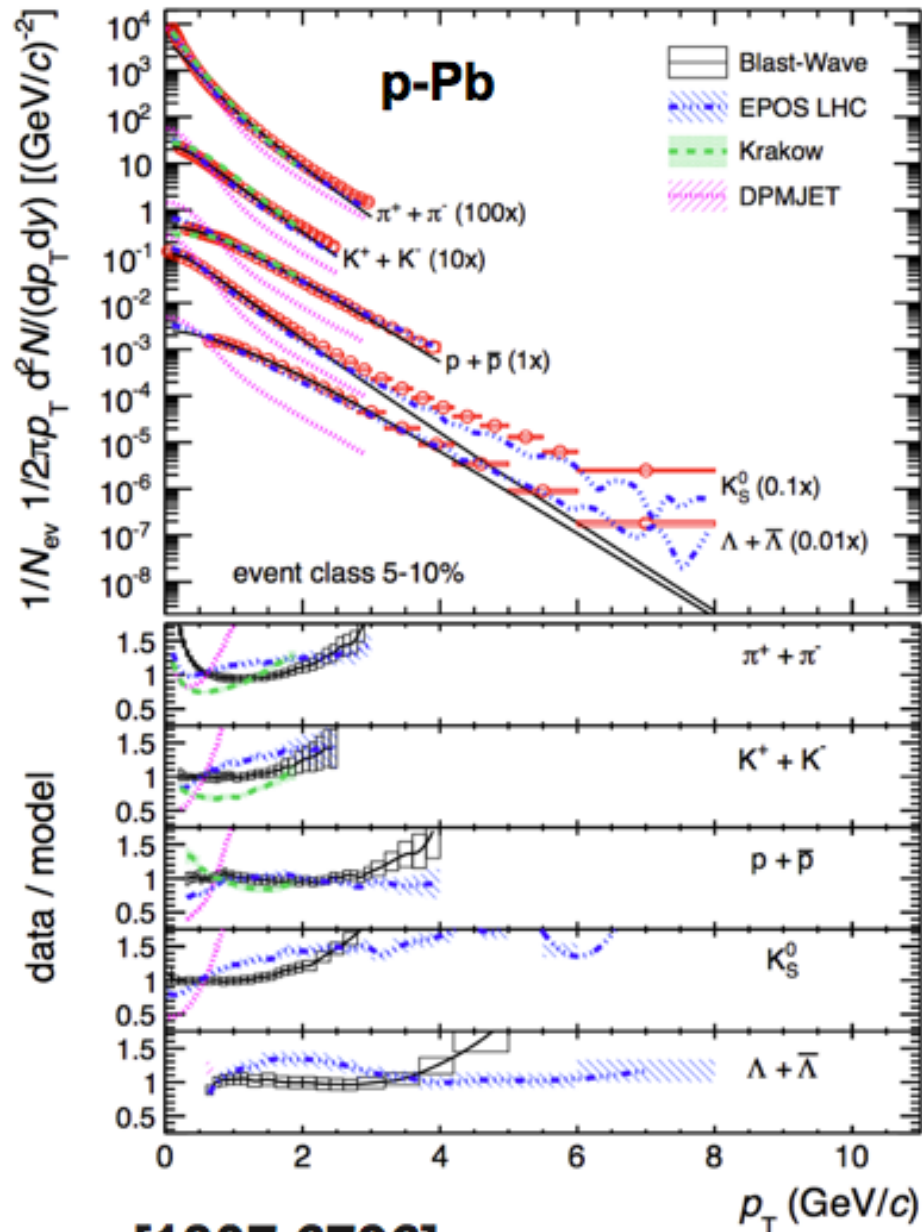
Radial flow (2)



Common radial hydrodynamic expansion leads to a modification of the spectral shape: mass dependent *boost*.

- p_T -spectra harden with centrality.
- More pronounced for heavier particles (e.g.: $p > K > \pi$) as *velocities* become equalized in the flow field ($p = \beta\gamma \cdot m$).
- Hydrodynamic models show a good agreement with the data.

Radial flow (3)



[1307.6796]

Common radial hydrodynamic expansion leads to a modification of the spectral shape: mass dependent *boost*.

- p_T -spectra harden with centrality.
- More pronounced for heavier particles (e.g.: $p > K > \pi$) as *velocities* become equalized in the flow field ($p = \beta \gamma \cdot m$).
- Hydrodynamic models show a good agreement with the data.

Blast-wave model (1)

- How fast is the expansion velocity? Estimate in a simplified hydro model:

- Consider a thermal source (Boltzmann type p_T -spectrum) of particles:

$$E \frac{d^3 N}{dp^3} \propto E e^{-E/T} \quad E = m_T \cosh(y)$$

- Boost source radially with velocity β and evaluate at $y=0$:

$$\frac{1}{m_T} \frac{dN}{dm_T} \propto m_T I_0 \left(\frac{p_T \sinh(\rho)}{T} \right) K_1 \left(\frac{m_T \cosh(\rho)}{T} \right) \quad \rho = \tanh^{-1}(\beta)$$

- Simple assumption: consider uniform sphere of radius R

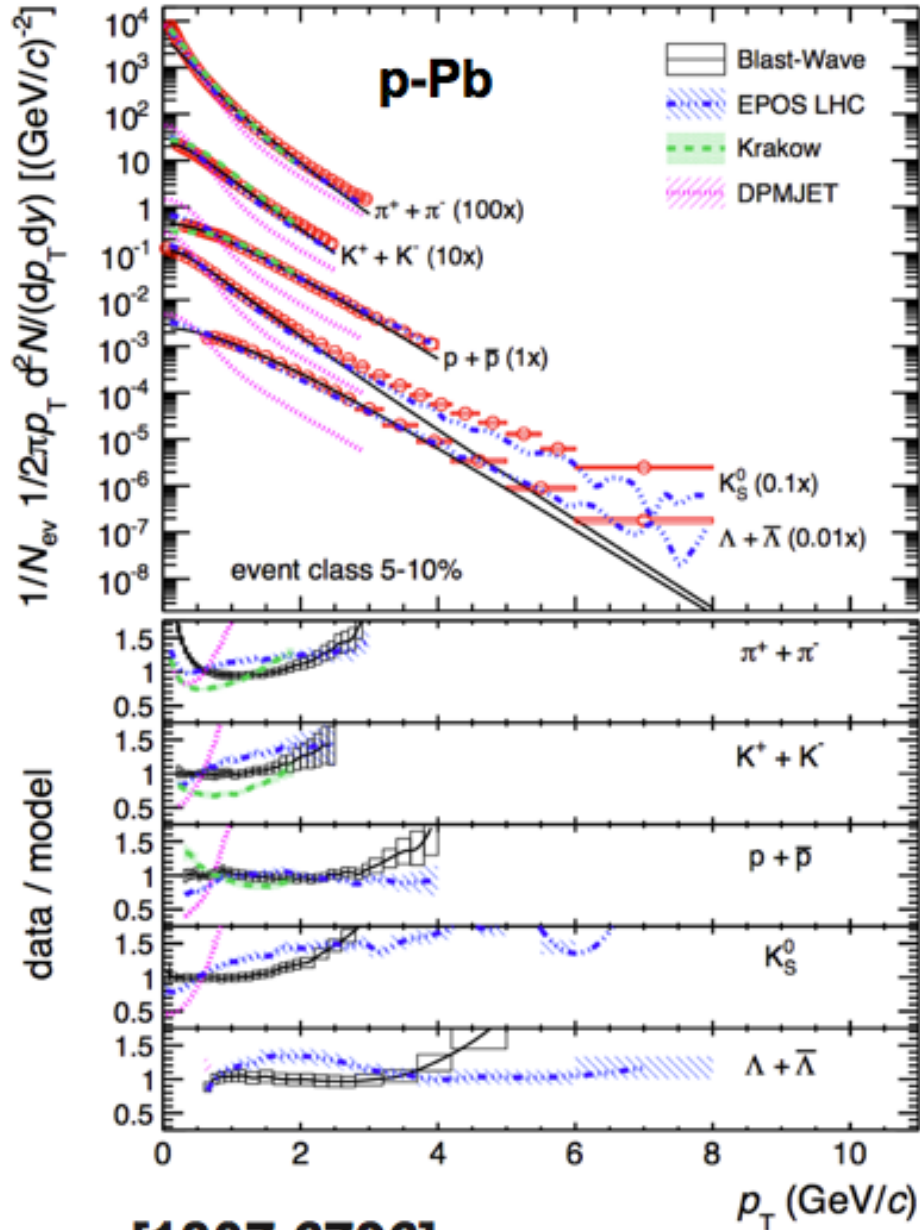
$$\frac{1}{m_T} \frac{dN}{dm_T} \propto \int_0^R r dr m_T I_0 \left(\frac{p_T \sinh(\rho(r))}{T} \right) K_1 \left(\frac{m_T \cosh(\rho(r))}{T} \right)$$

and parameterize velocity profile as $\beta(r) = \beta_s (r/R)^n$

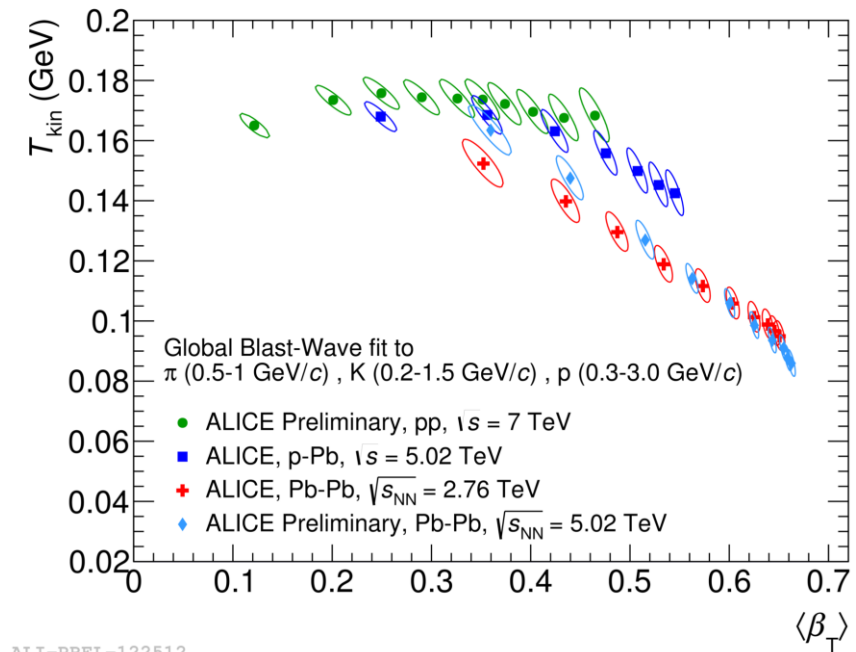
- Three free parameters: kinetic freeze-out temperature T_{kin} , surface expansion velocity β_s , exponent n of velocity profile.

Blast-wave model (2)

- Common blast-wave fit gives a good description of the data at low transverse momenta.
- Average expansion velocity: $\sim 0.65c$
- Kinetic freeze-out temperature: ~ 80 MeV



[1307.6796]



ALI-PREL-122512

End of lecture 2

- Now we know the temperature of the system at the final decoupling.
- Tomorrow: elliptic flow and why the QGP is an *ideal liquid*.

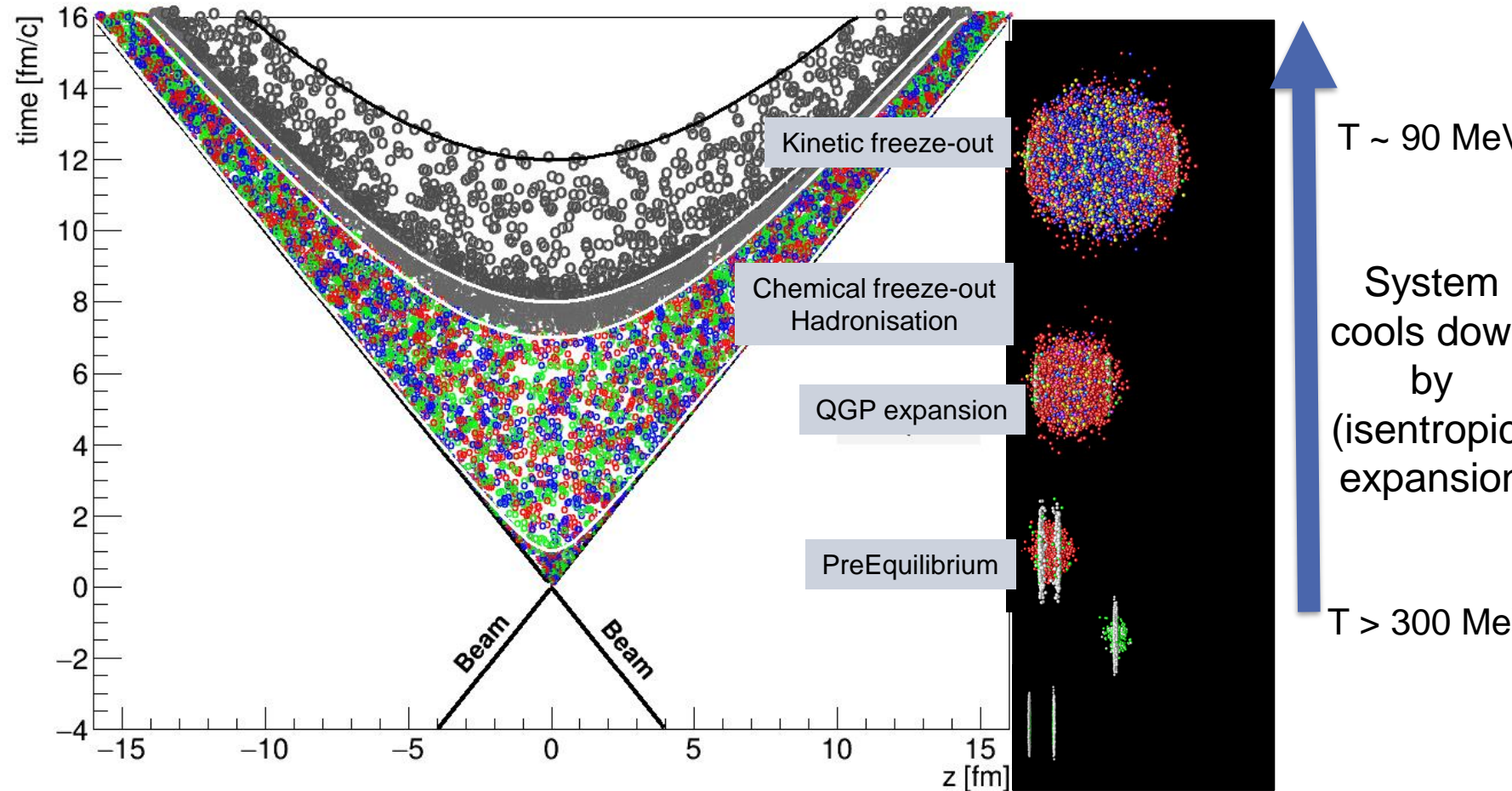
Particle detection
($t \approx 10^{15} \text{ fm/c}$)

Kinetic freeze-out
($t = 10 \text{ fm/c}$)

Chemical freeze-out

Hydrodynamic
evolution ($t \sim 0.5 \text{ fm/c}$)

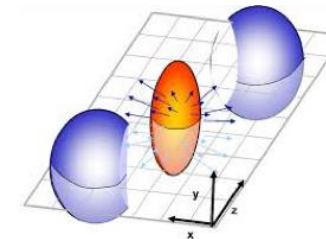
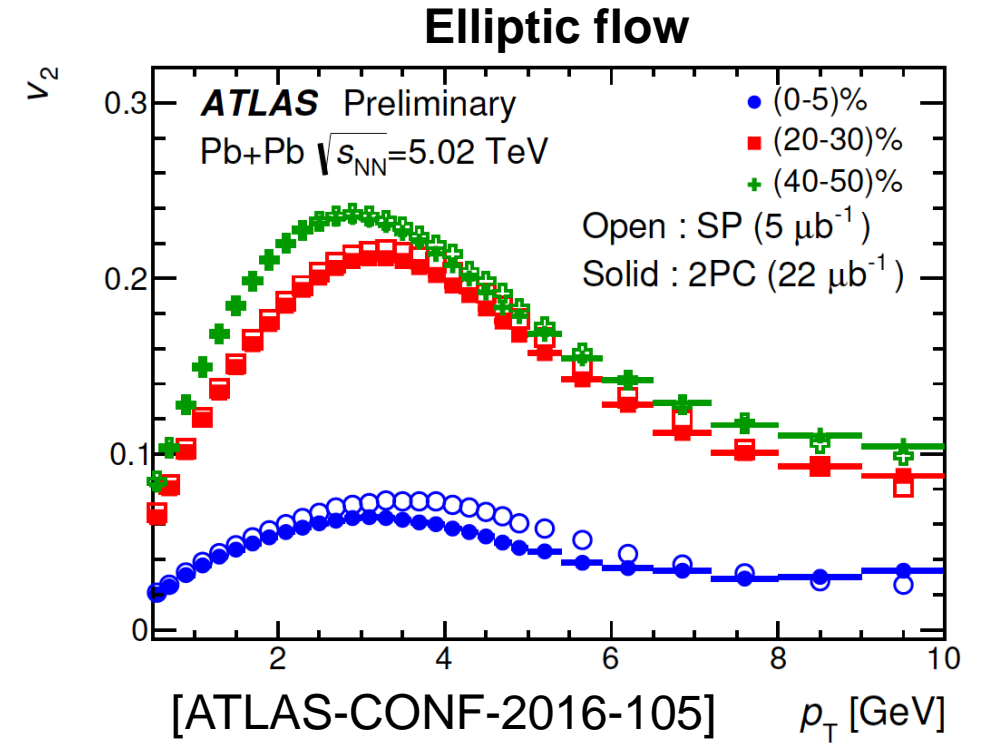
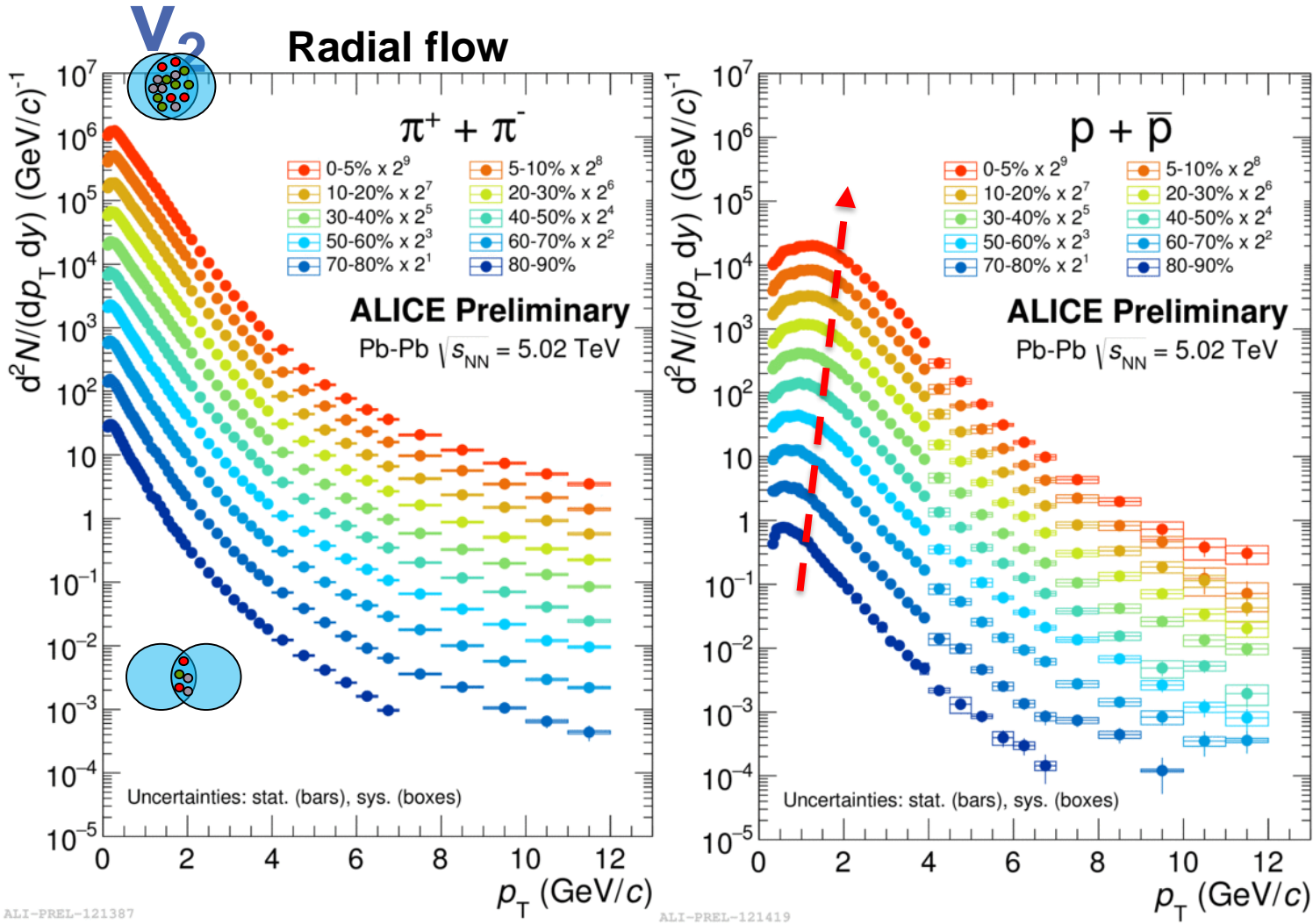
Pre-equilibrium
Collision ($t = 0 \text{ fm/c}$)



Small systems: high multiplicity pp and pPb

Radial and elliptic flow

Hydrodynamic expansion – spectral shapes and



→ Initial **spatial anisotropy** is converted by scatterings into an **anisotropy in momentum space**.

$$E \frac{d^3N}{d^3p} = \frac{d^2N}{2\pi p_T dp_T dy} \left\{ 1 + 2 \sum_{n=1}^{\infty} v_n(p_T) \cos[n(\varphi - \psi_n)] \right\}$$

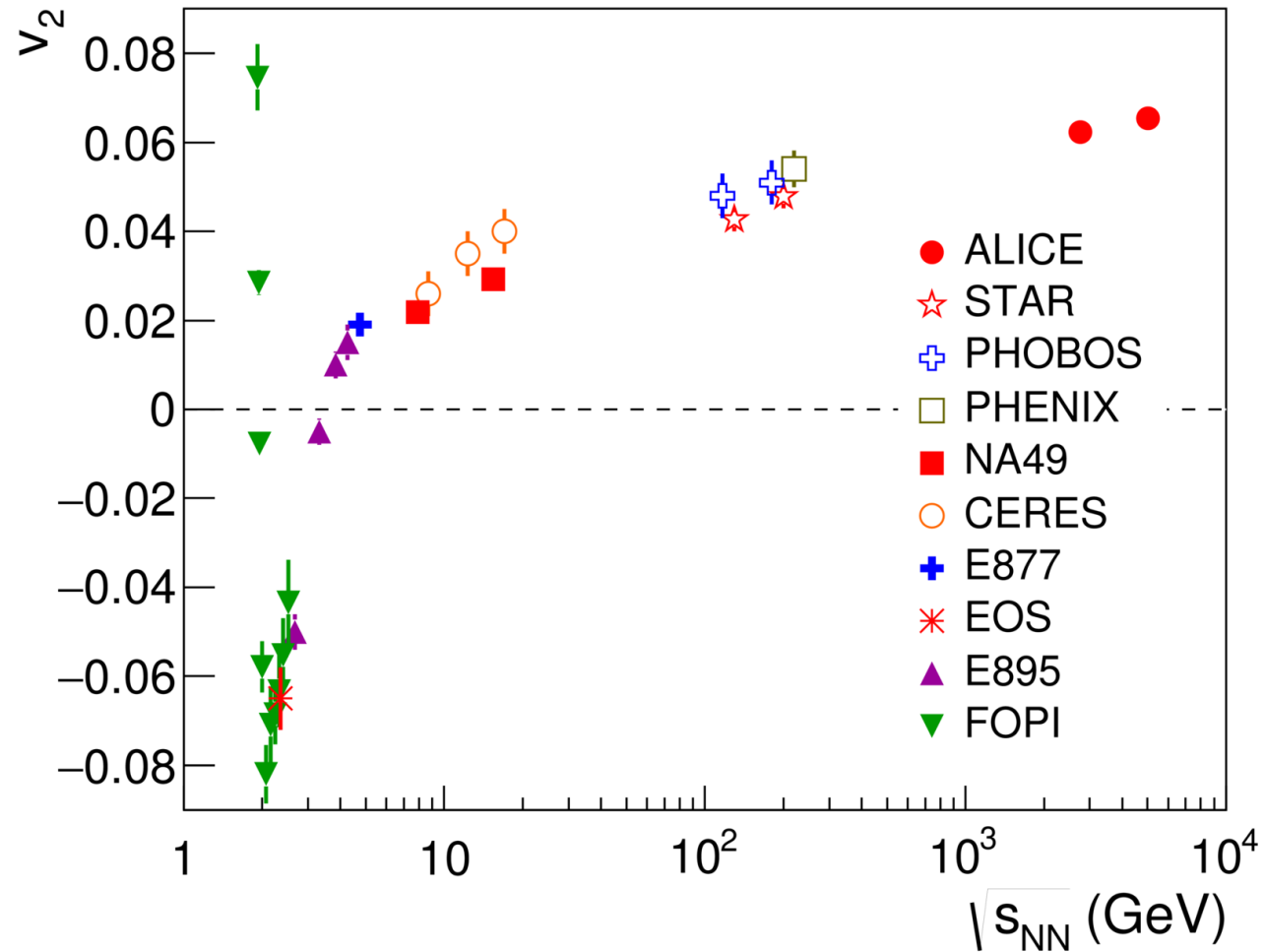
Radial flow v_1 – direct flow, v_2 – elliptic flow

Textbook-like hardening of p_T -spectra as expected in hydro:

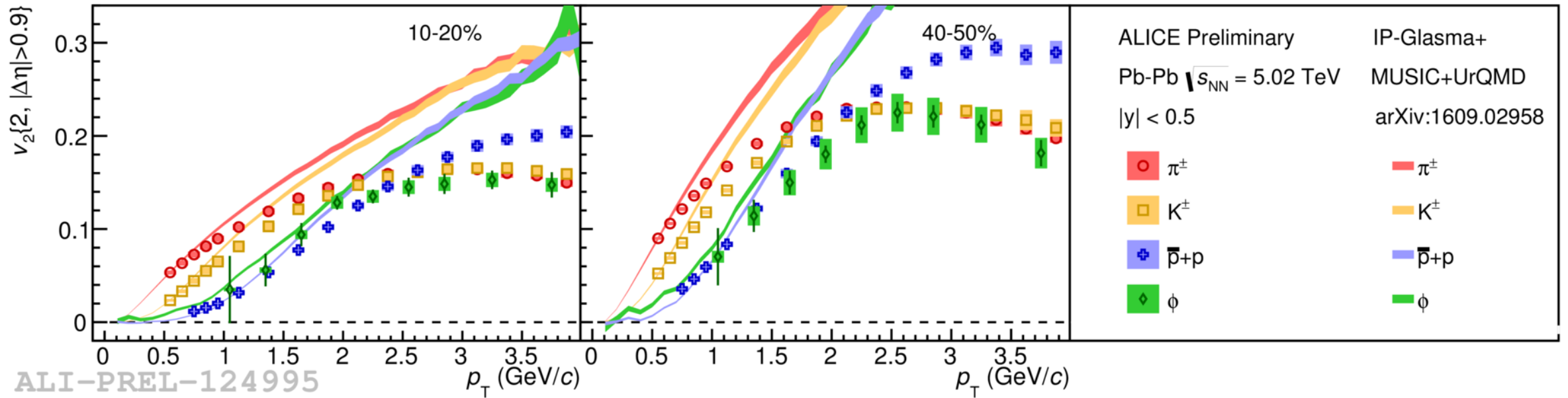
- With centrality
- With the particle mass: $p = \beta\gamma \cdot m$

Elliptic flow (heavy-ion physics)

[PRL 116, 132302 (2016)]



Elliptic flow (ALICE)

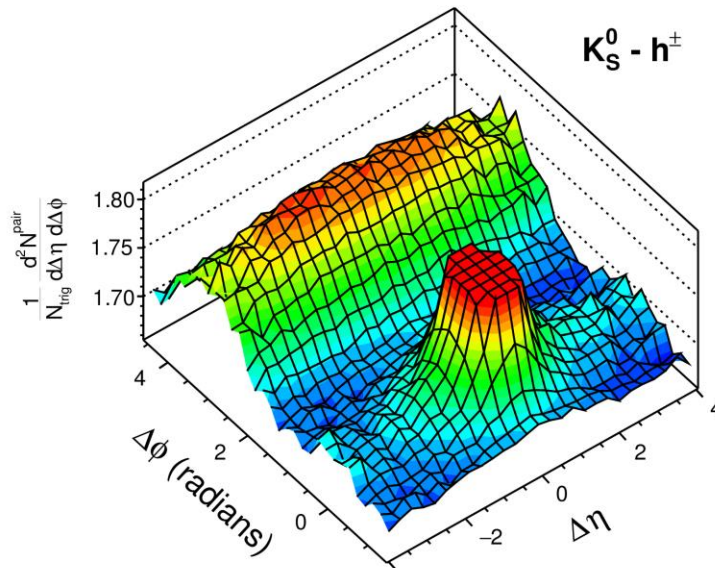
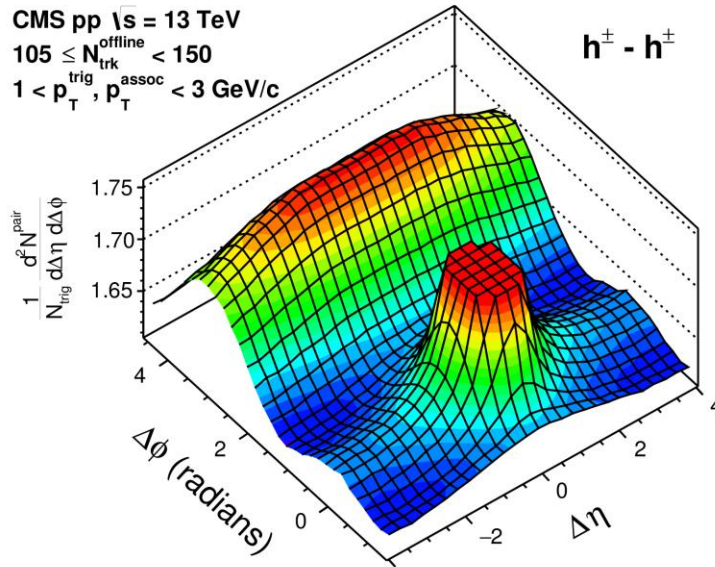


Validity of hydrodynamic description confirmed at the highest centre-of-mass energies available.

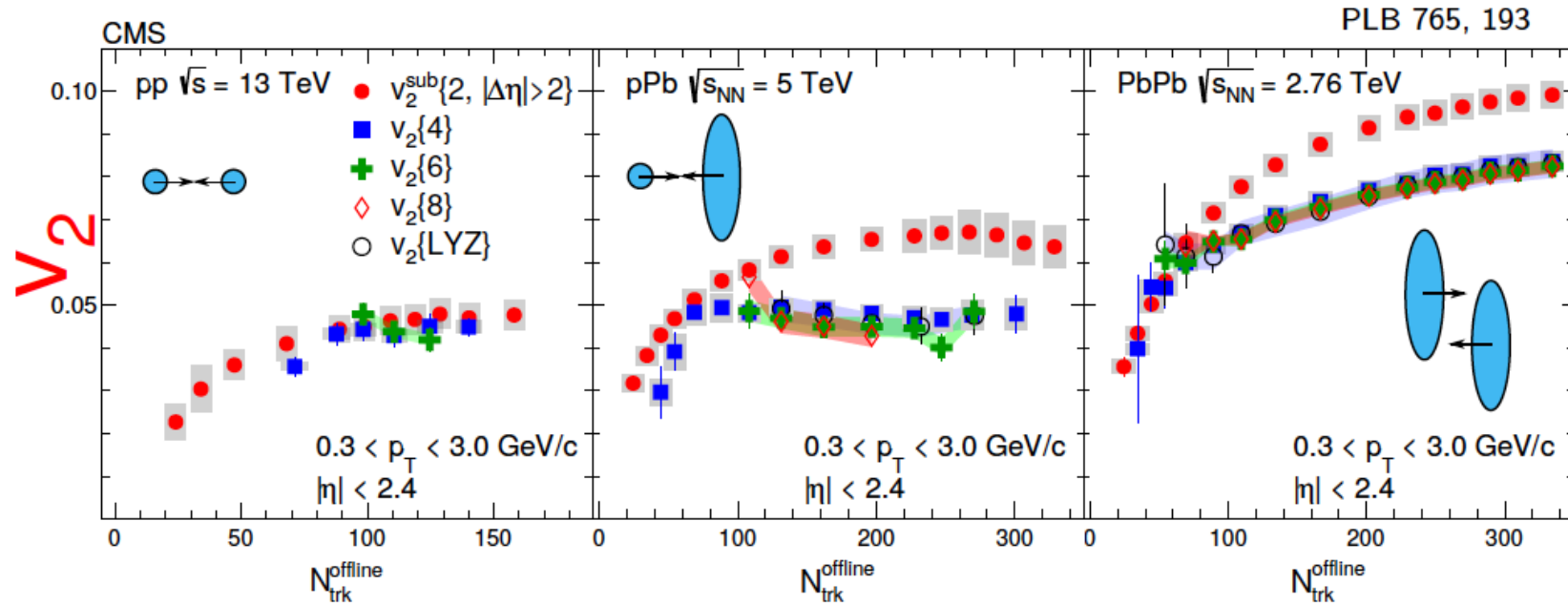
Expected mass ordering ($p = \beta\gamma \cdot m$) observed.

(Double) ridges

CMS pp $\sqrt{s} = 13$ TeV
 $105 \leq N_{\text{trk}}^{\text{offline}} < 150$
 $1 < p_{\text{T}}^{\text{trig}}, p_{\text{T}}^{\text{assoc}} < 3$ GeV/c



- Long-range azimuthal correlations (as originating from elliptic flow) are also observed in small systems: double ridges.



- Similar observations hold true for many other typical *kinetic heavy-ion* observables measured in high multiplicity pp and pPb collisions → clear indication for *collectivity in small systems*.