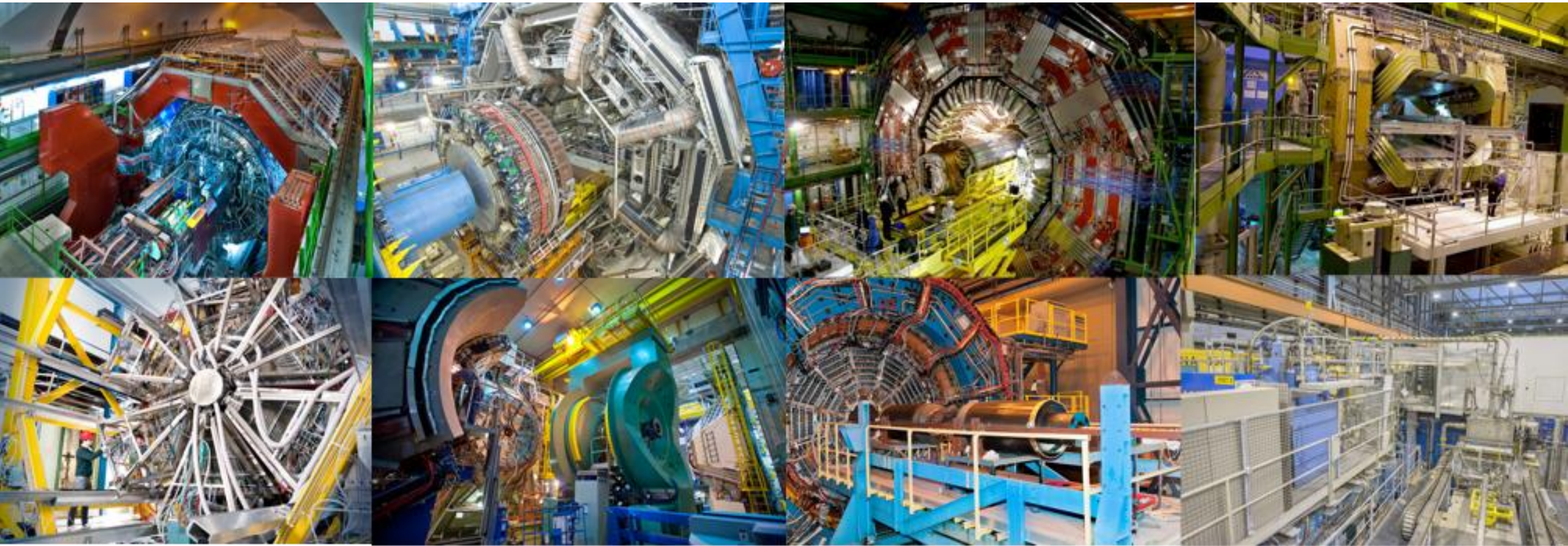


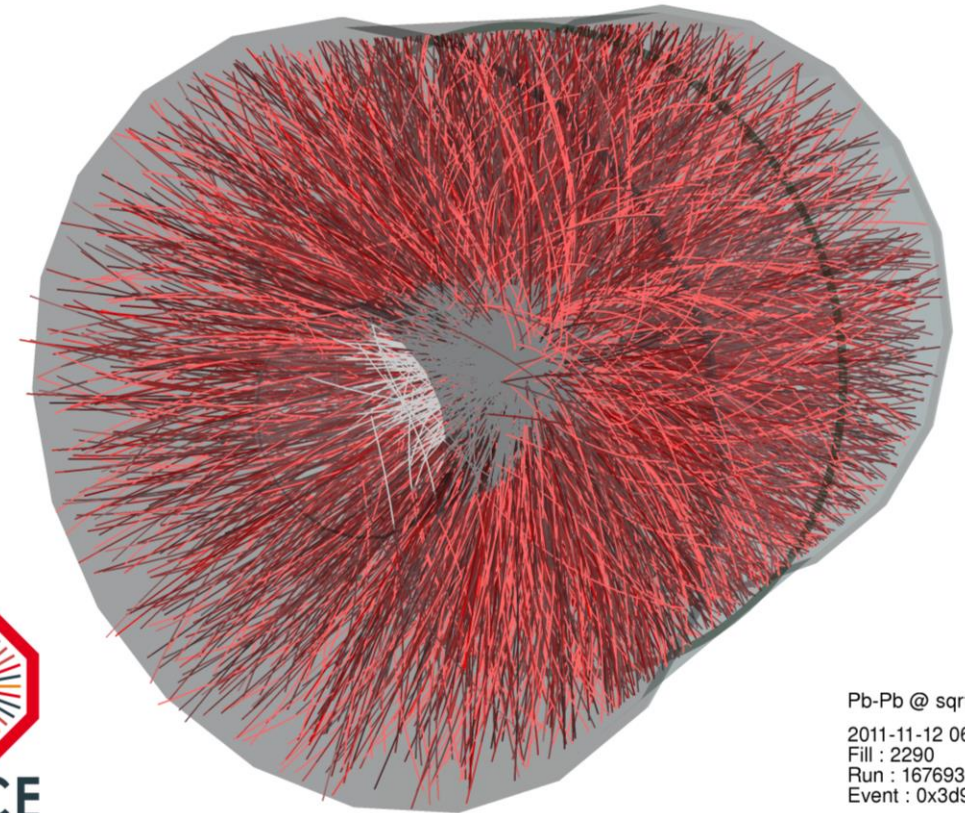
The physics of heavy-ion collisions



Alexander Kalweit, *CERN*

Overview

- Three lectures (one hour each):
 - Friday, 10:30h-11:30h (Prevessin)
 - Saturday, 11:30h-12:30h (Meyrin)
 - Monday, 10:30h-11:30h (Prevessin)
- Specialized discussion sessions with **heavy-ion experts** in the afternoons on Friday and Monday.
- Feel free to contact me for any questions regarding the lecture:
Alexander.Philipp.Kalweit@cern.ch
- Many slides, figures, and input taken from:
Jan Fiete Grosse-Oetringhaus, Constantin Loizides, Federico Antinori, Roman Lietava



Pb-Pb @ $\sqrt{s} = 2.76$ ATeV
2011-11-12 06:51:12
Fill : 2290
Run : 167693
Event : 0x3d94315a

Outline and discussion leaders

- Introduction
- The QCD phase transition
- QGP thermodynamics and soft probes ([Francesca](#))
 - Particle chemistry
 - QCD critical point and onset of de-confinement
 - (anti-)(hyper-)nuclei
 - Radial and elliptic flow
 - Small systems
- Hard scatterings ([Leticia](#), [Marta](#))
 - Nuclear modification factor
 - Jets
- Heavy flavor in heavy-ions
 - Open charm and beauty
 - Quarkonia



Francesca
Bellini



Leticia
Cunqueiro



Marta
Verweij

Summary lecture 2

- Now we know the temperature of the system at the final decoupling.
- Today: elliptic flow and why the QGP is an *ideal liquid*.

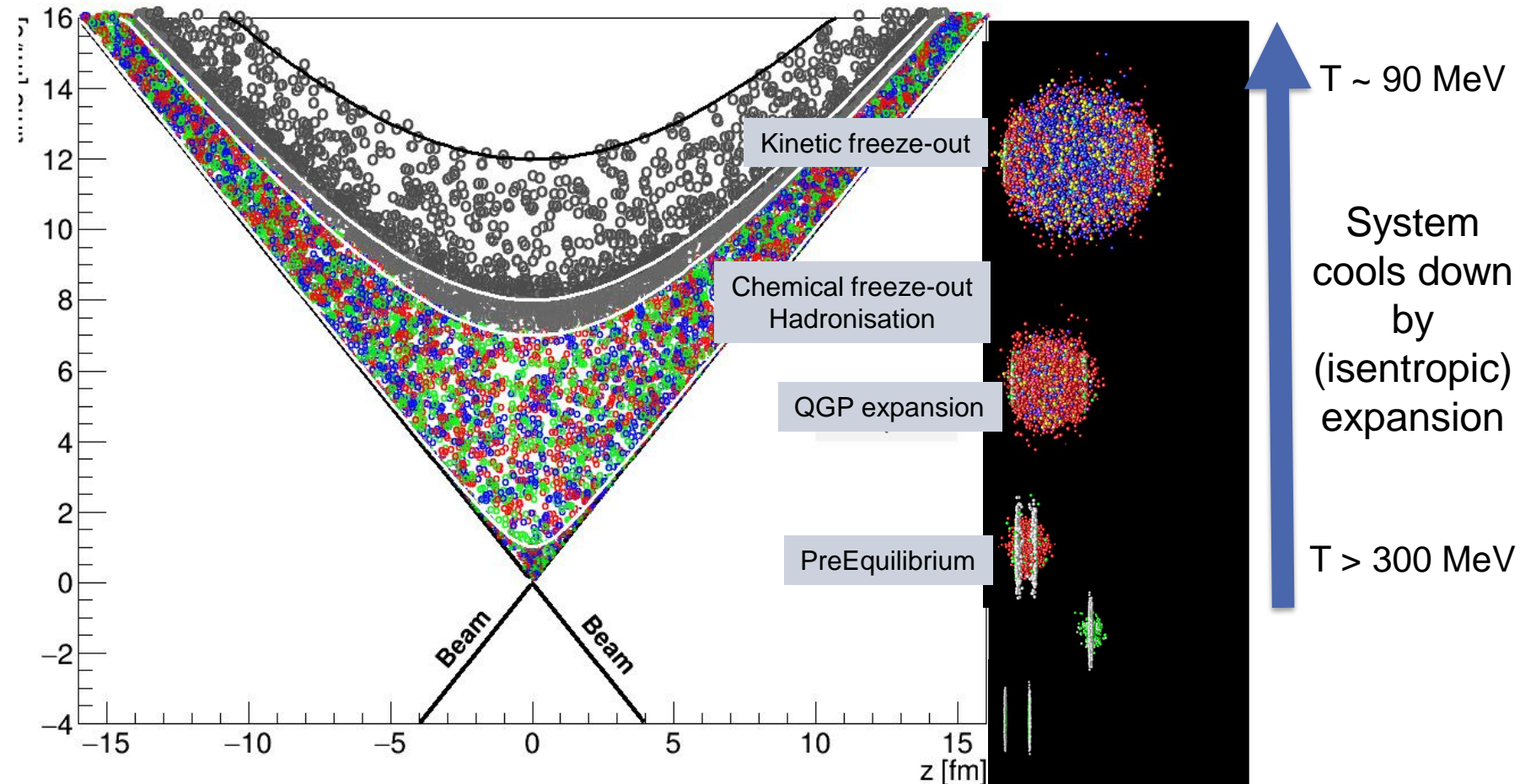
Particle detection
($t \approx 10^{15} \text{ fm/c}$)

Kinetic freeze-out
($t = 10 \text{ fm/c}$)

Chemical freeze-out
156 MeV

Hydrodynamic
evolution ($t \sim 0.5 \text{ fm/c}$)

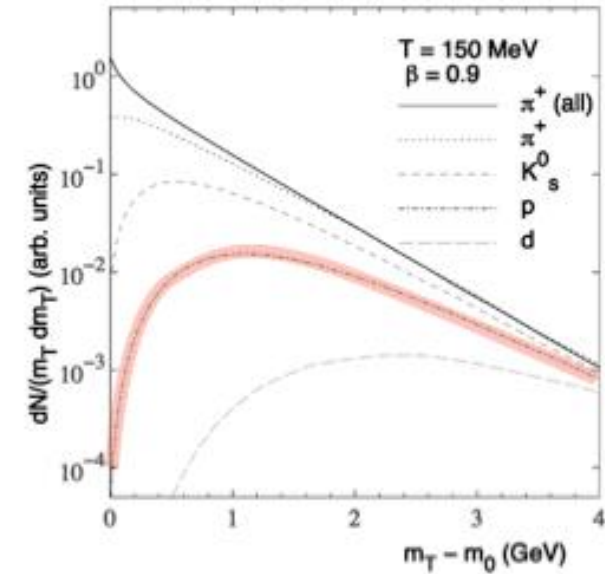
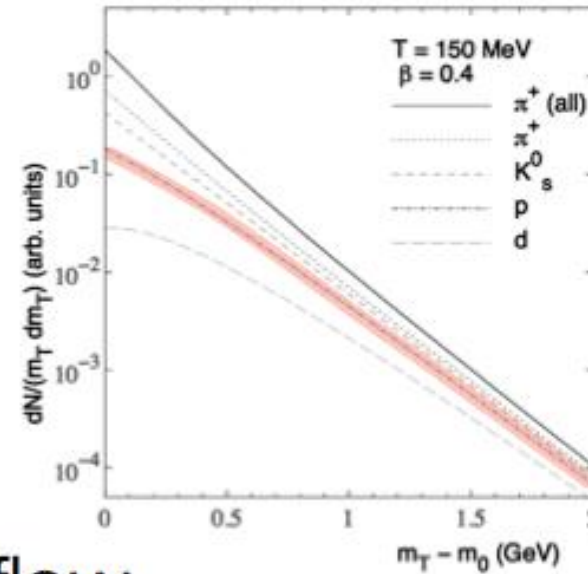
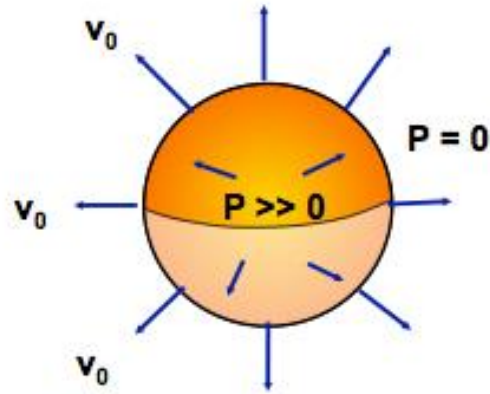
Pre-equilibrium
Collision ($t = 0 \text{ fm/c}$)



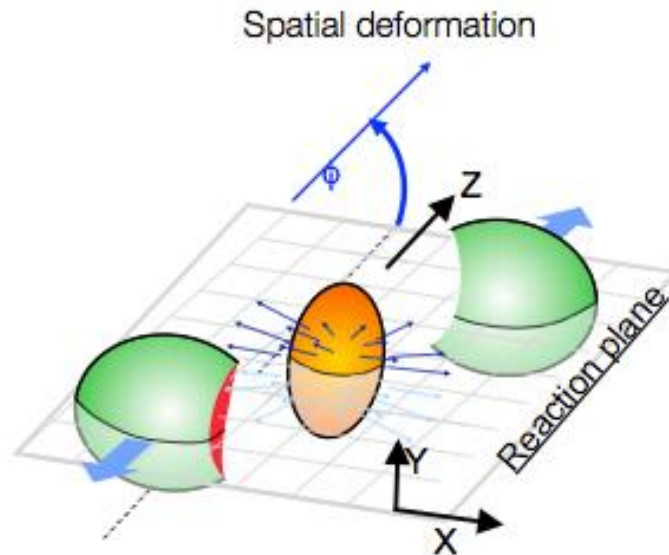
QGP thermodynamics and soft probes

Radial and elliptic flow

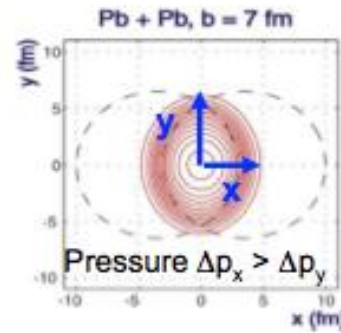
Isotropic radial flow



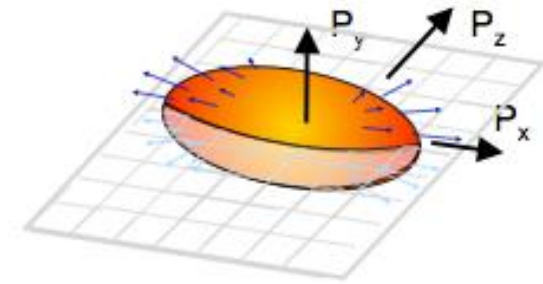
Anisotropic (elliptic) flow



Azimuthal (φ)
pressure gradients

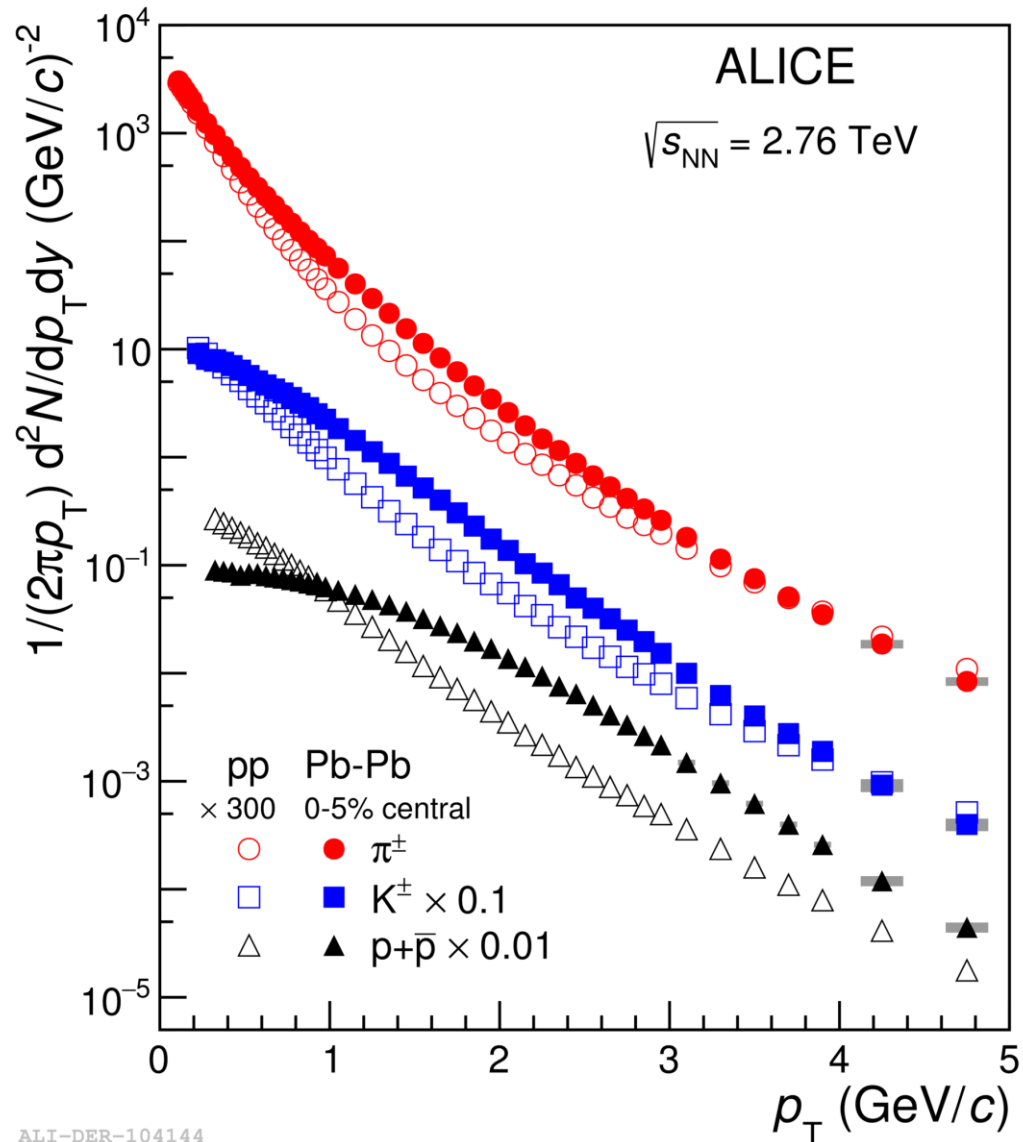


Anisotropic particle density



$$\frac{dN}{d\varphi} \propto 1 + 2v_1 \cos[\varphi - \Psi_1] + 2v_2 \cos[2(\varphi - \Psi_2)] + 2v_3 \cos[3(\varphi - \Psi_3)] + \dots$$

Radial flow



ALI-DER-104144

Common radial hydrodynamic expansion leads to a modification of the spectral shape: mass dependent *boost*.

→ p_T -spectra harden with centrality.

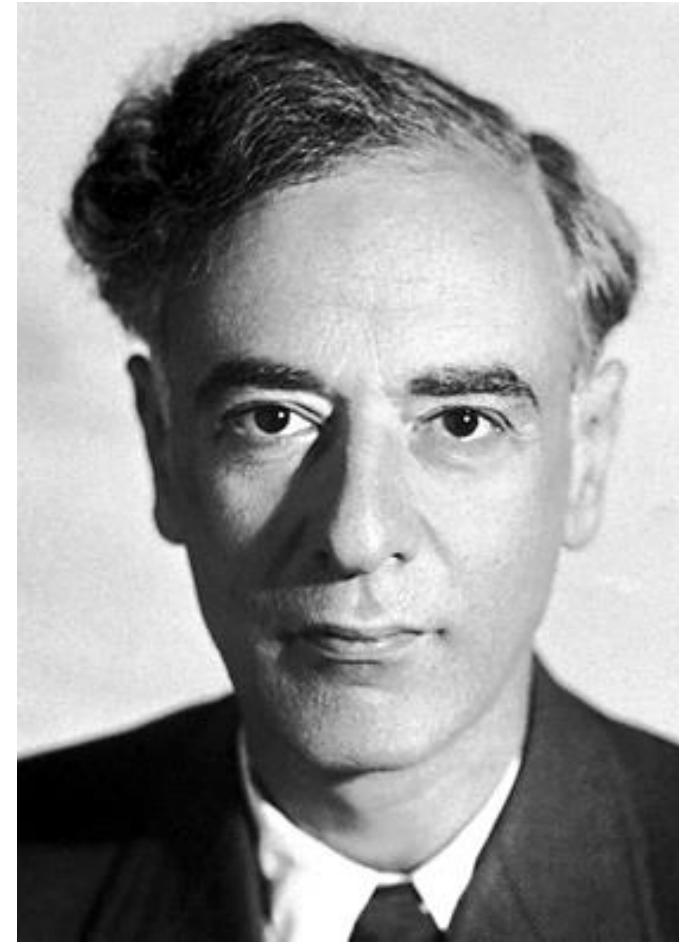
→ More pronounced for heavier particles (e.g.: $p > K > \pi$) as *velocities* become equalized in the flow field ($p = \beta\gamma \cdot m$).

→ Hydrodynamic models show a good agreement with the data.

→ Kinetic freeze-out temperature from Blast-Wave model: $\sim 90 \text{ MeV}$

Relativistic Hydrodynamics

- General framework of relativistic hydrodynamics was first developed by Landau and is textbook knowledge since then.
- Only requirement for applicability: *local thermodynamic equilibrium*.
- **Perfect fluid: no dissipation**
 - Conservation of energy and momentum: $\partial_\mu T^{\mu\nu} = 0$
 - Conservation of baryon number current:
→ gives five independent equations $\partial_\mu j_B^\mu(x) = 0$
- Six thermodynamic variables: the energy density $\varepsilon(x)$, the momentum density $P(x)$, the baryon number density $n_B(x)$, and the fluid velocity $v(x)$.
- Equation-of-state: functional relation of ε , P , and n_B (taken from Lattice QCD).
- In reality: dissipative corrections play an important role:
→ **shear viscosity η** and bulk viscosity ζ (so called *transport coefficients*) enter in correction terms on the right hand side of the equations above.



Lev Landau (1908-1986)

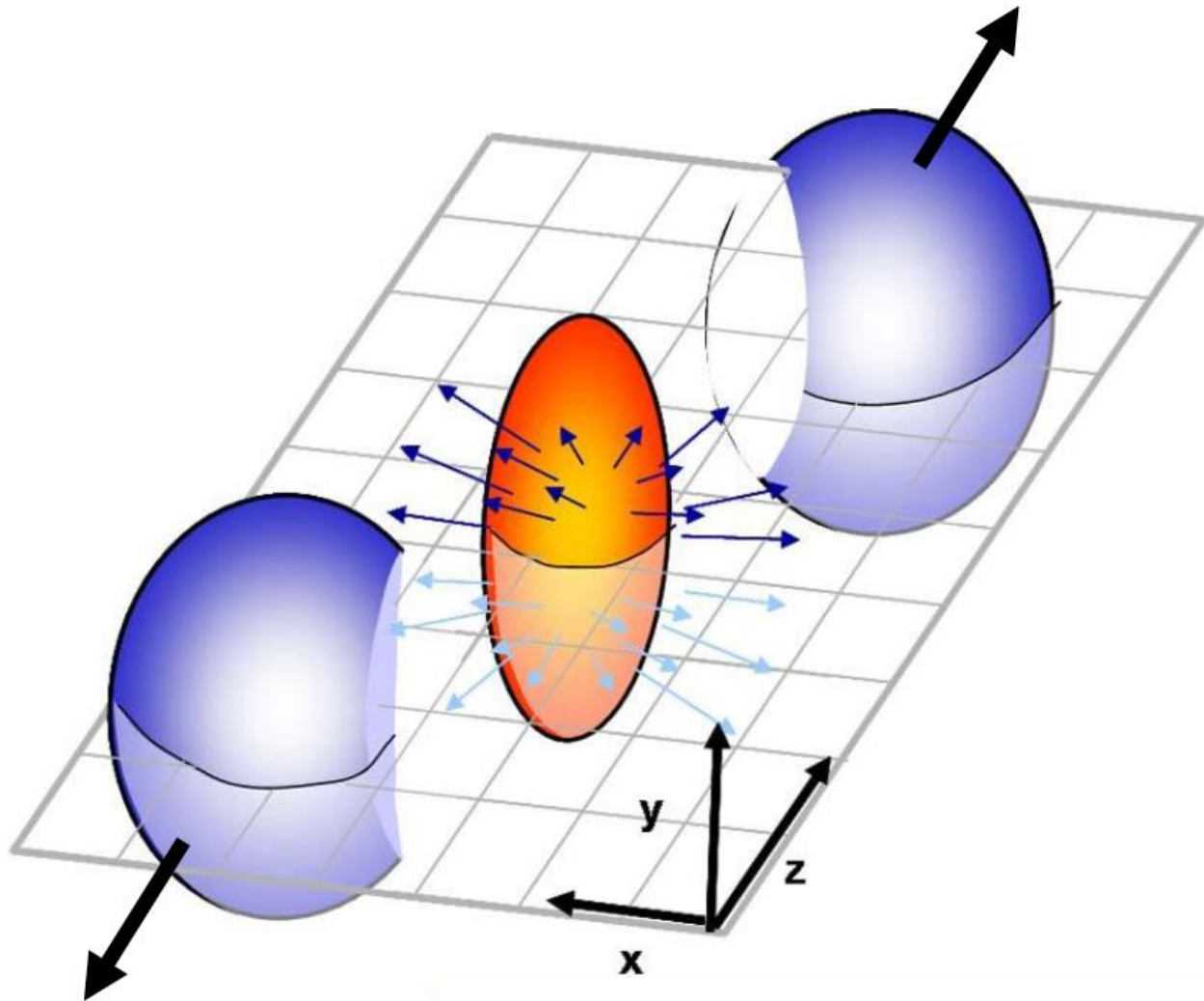
Elliptic flow v_2

- Not only the observed particle spectrum in p_T , but also in φ is the result of the fireball expansion.
- If the system is asymmetric in spatial coordinates, scattering converts it to **anisotropy in momentum space**:

$$E \frac{d^3N}{d^3p} = \frac{d^2N}{2\pi p_T dp_T dy} \left\{ 1 + 2 \sum_{n=1}^{\infty} v_n(p_T) \cos[n(\varphi - \psi_n)] \right\}$$

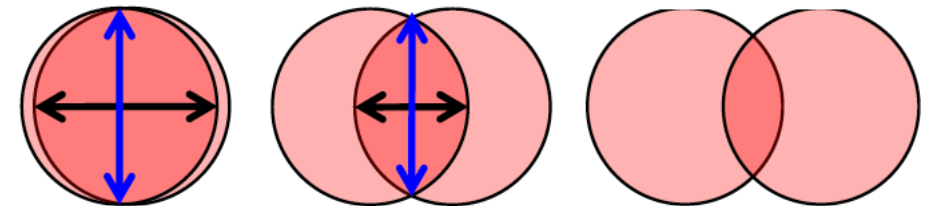
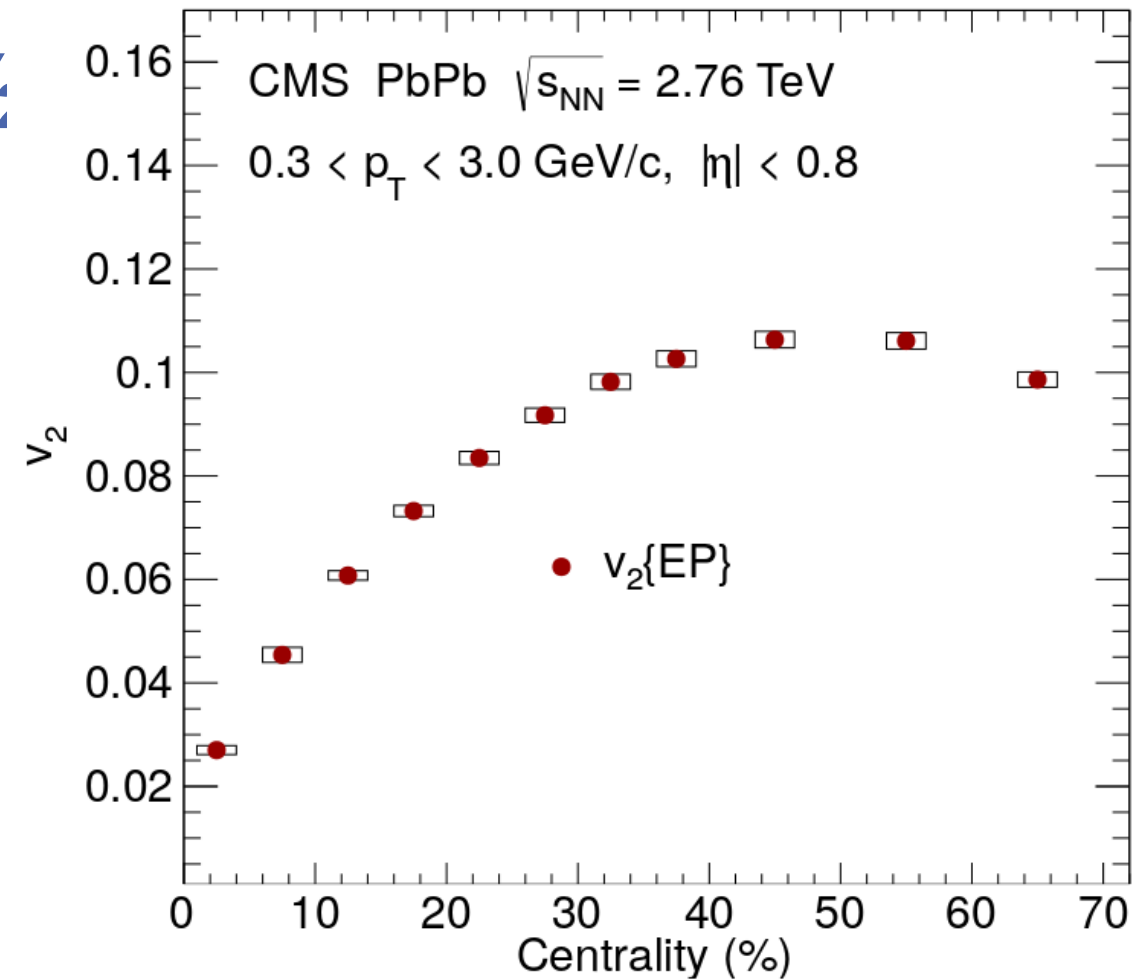
Radial flow v_1 – direct flow, v_2 – elliptic flow

- If nuclei overlap was a smooth almond shape, odd harmonics (v_3, \dots) would be zero.



Centrality dependence of v_2

- v_2 exhibits a strong centrality dependence
- v_2 largest for 40-50%
- Spatial anisotropy very small in central collisions
- Largest anisotropy in mid-central collisions
- Small overlap region in peripheral collisions

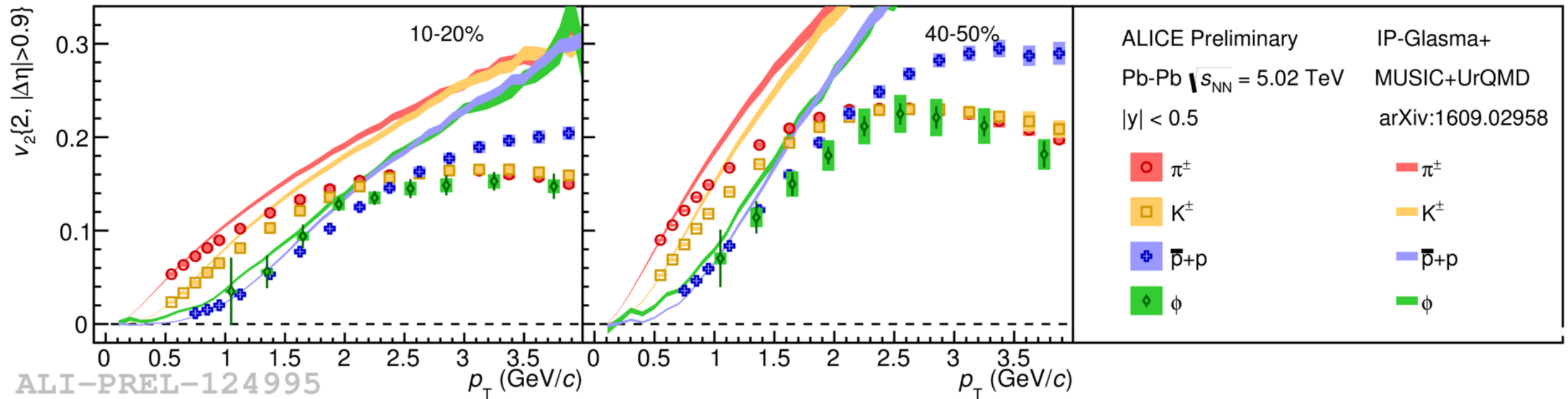


CMS, PRC 87(2013) 014902

Mass ordering of v_2 vs. transverse momentum

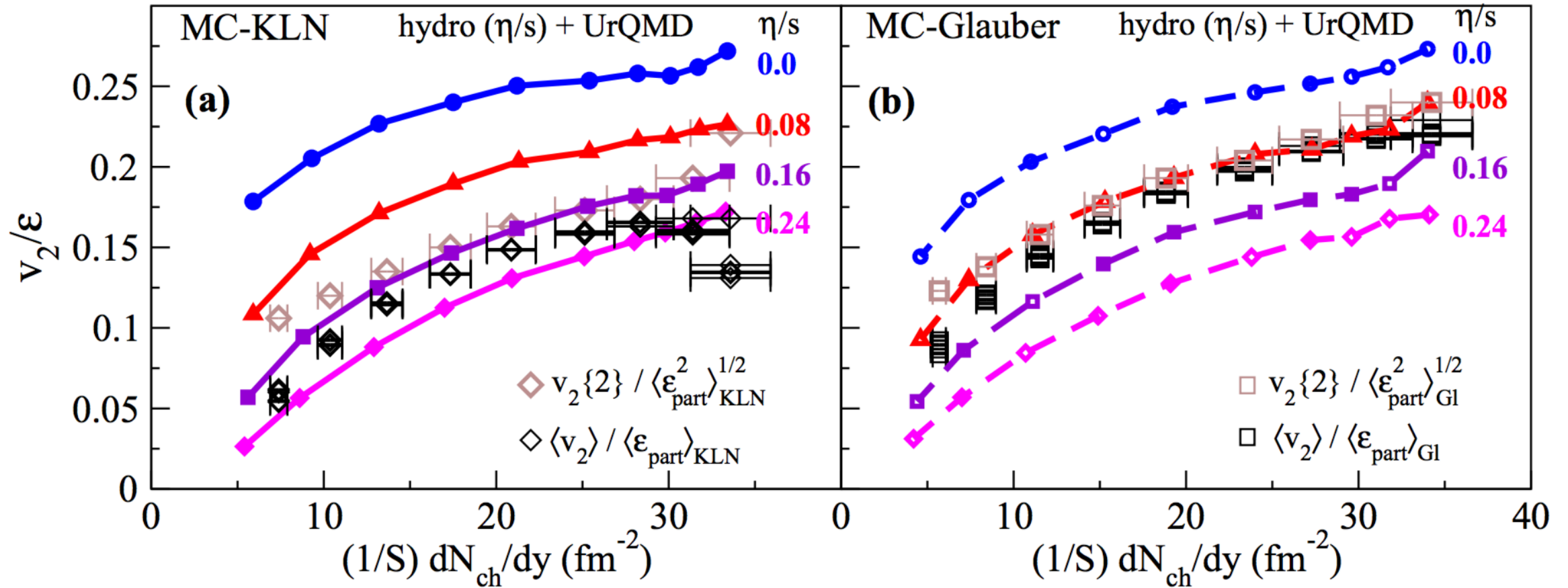
Transverse momentum dependence of elliptic flow shows the same mass ordering ($p = \beta\gamma \cdot m$) as radial flow and as expected from hydrodynamics.

→ interplay of radial and elliptic flow.



Sensitivity of v_2 to shear viscosity

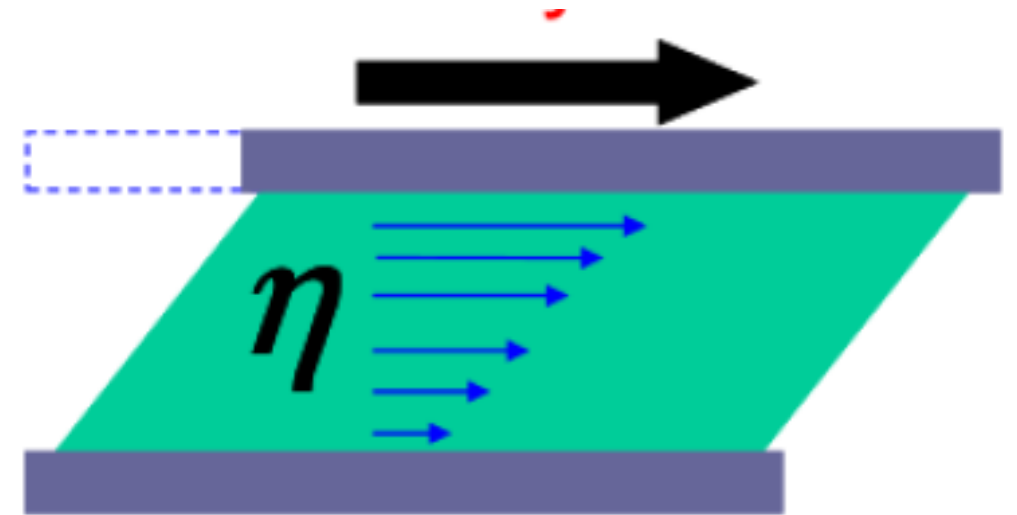
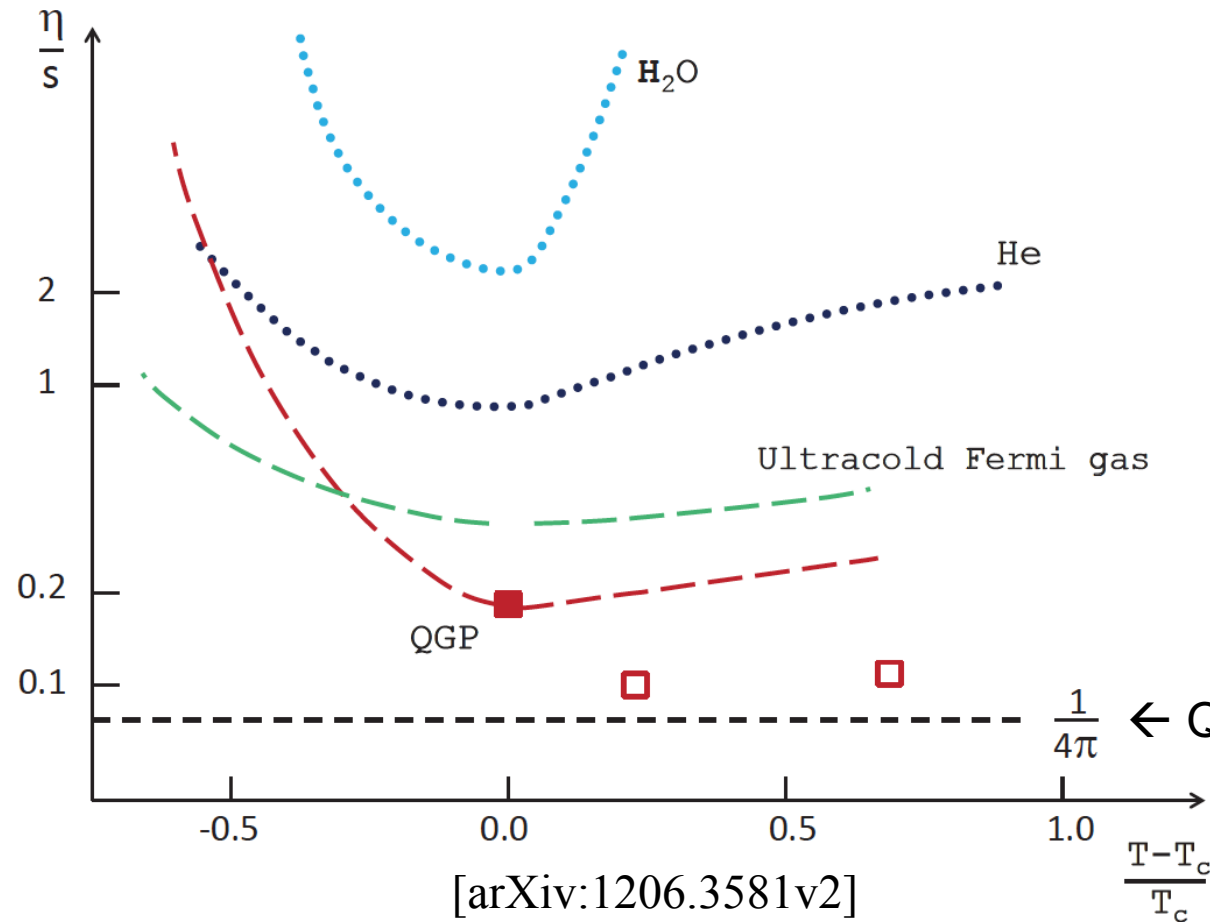
[Phys.Rev.Lett. 106 (2011) 192301]



- The larger the shear viscosity per entropy density ratio η/s of the QGP, the more v_2 is reduced.
- Dissipative losses hamper the buildup of flow => measuring the magnitude of v_2 and comparing it to models, we can determine how *ideal* the QGP liquid is.

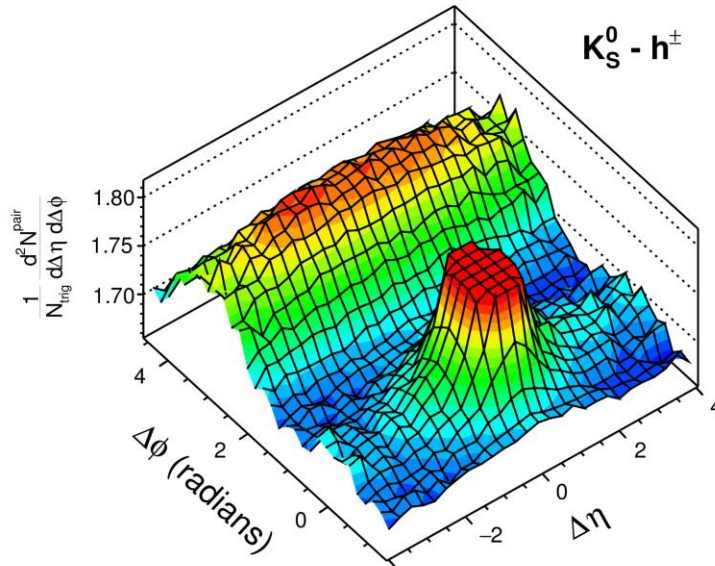
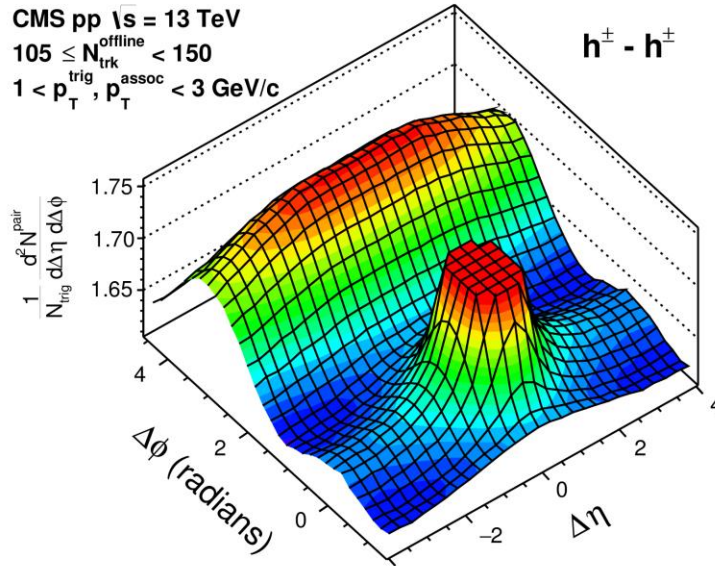
Ideal fluids

→ Why are ideal fluids (η/s very small) fascinating? Look at superfluid Helium as an example: <https://www.youtube.com/watch?v=2Z6UJbwxBZI>

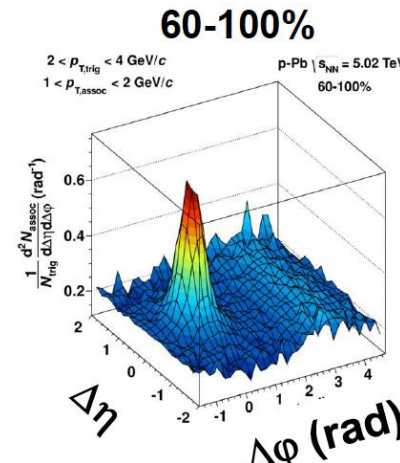
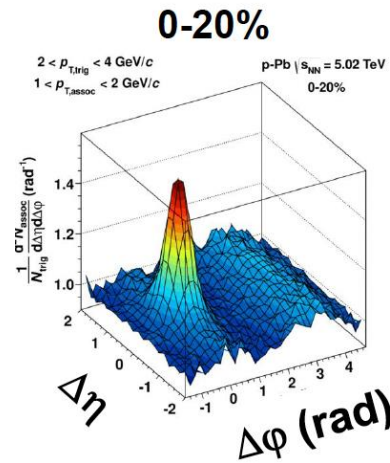


Double ridges (1)

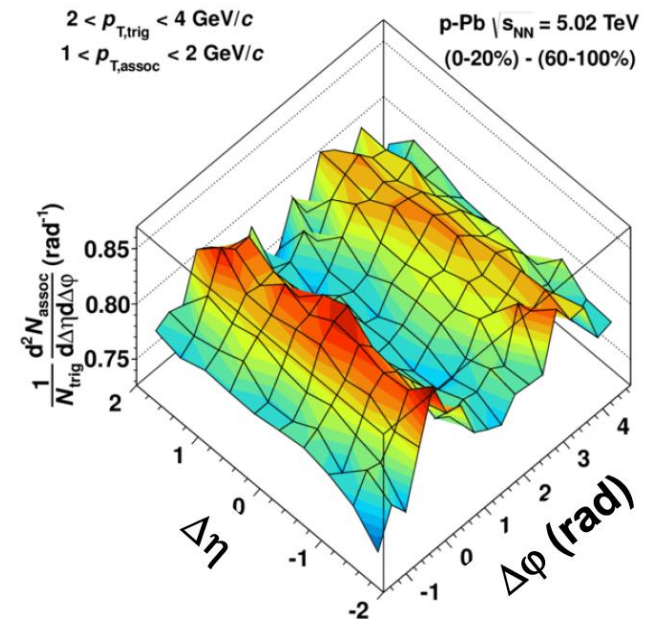
CMS pp $\sqrt{s} = 13$ TeV
 $105 \leq N_{\text{trk}}^{\text{offline}} < 150$
 $1 < p_{\text{T}}^{\text{trig}}, p_{\text{T}}^{\text{assoc}} < 3$ GeV/c



- Subtraction procedure to “isolate” ridge contribution from jet correlations:
 - No ridge seen in 60-100% and similar to pp.
 - As a result one finds two symmetric ridges as expected from elliptic flow (“hydro-like”).



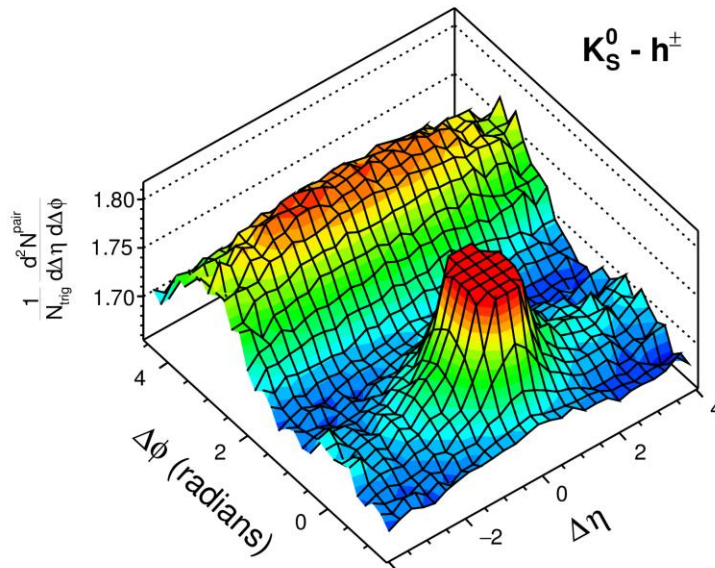
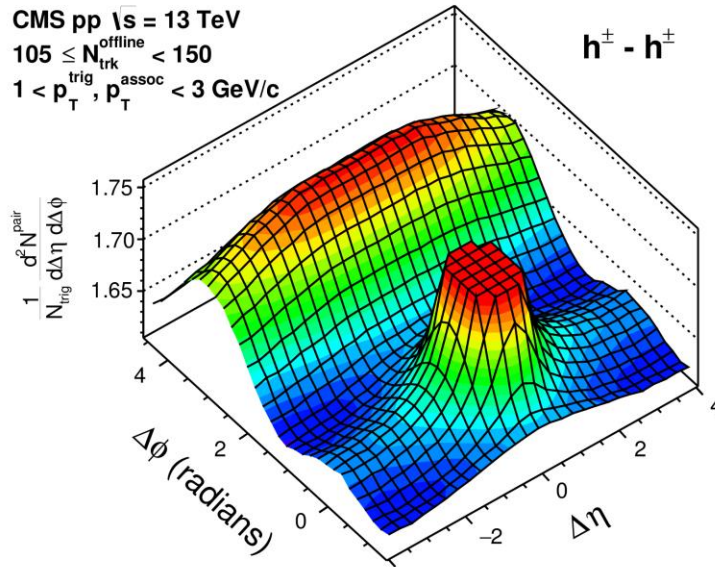
Two ridges !



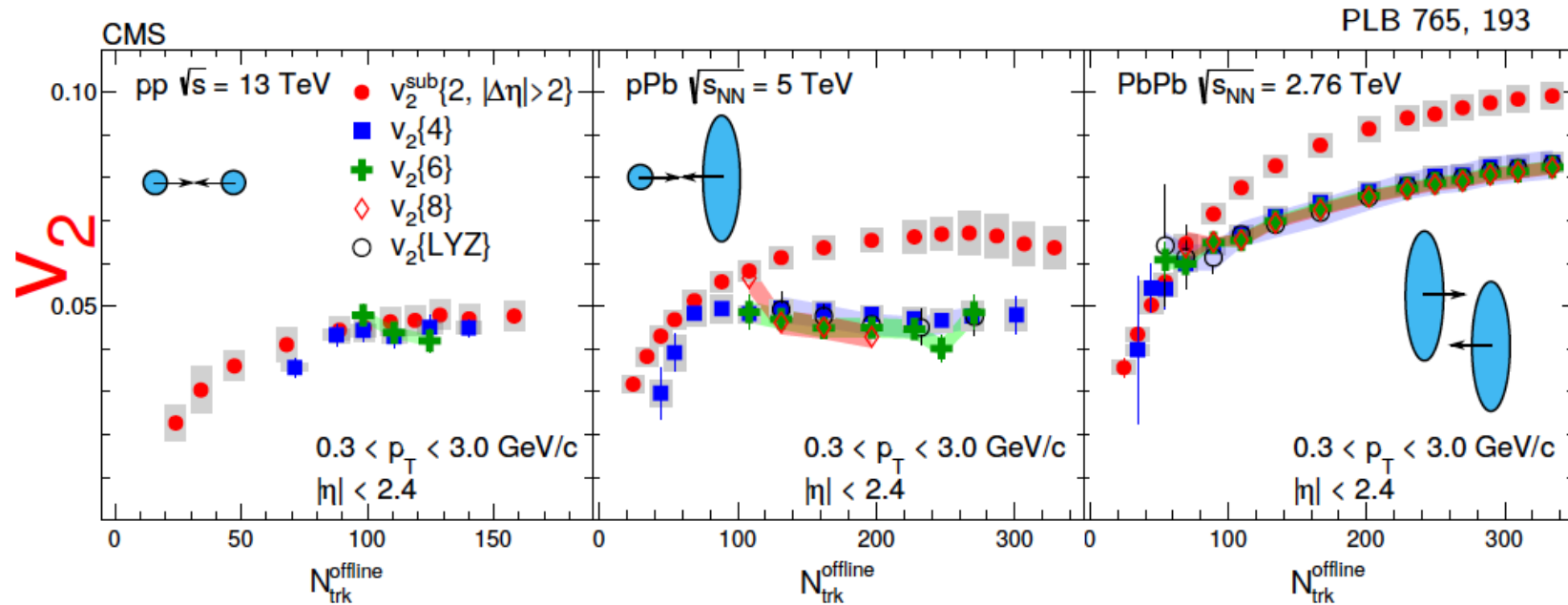
ALICE, PLB719 (2013) 29

Double ridges (2)

CMS pp $\sqrt{s} = 13$ TeV
 $105 \leq N_{\text{trk}}^{\text{offline}} < 150$
 $1 < p_{\text{T}}^{\text{trig}}, p_{\text{T}}^{\text{assoc}} < 3$ GeV/c



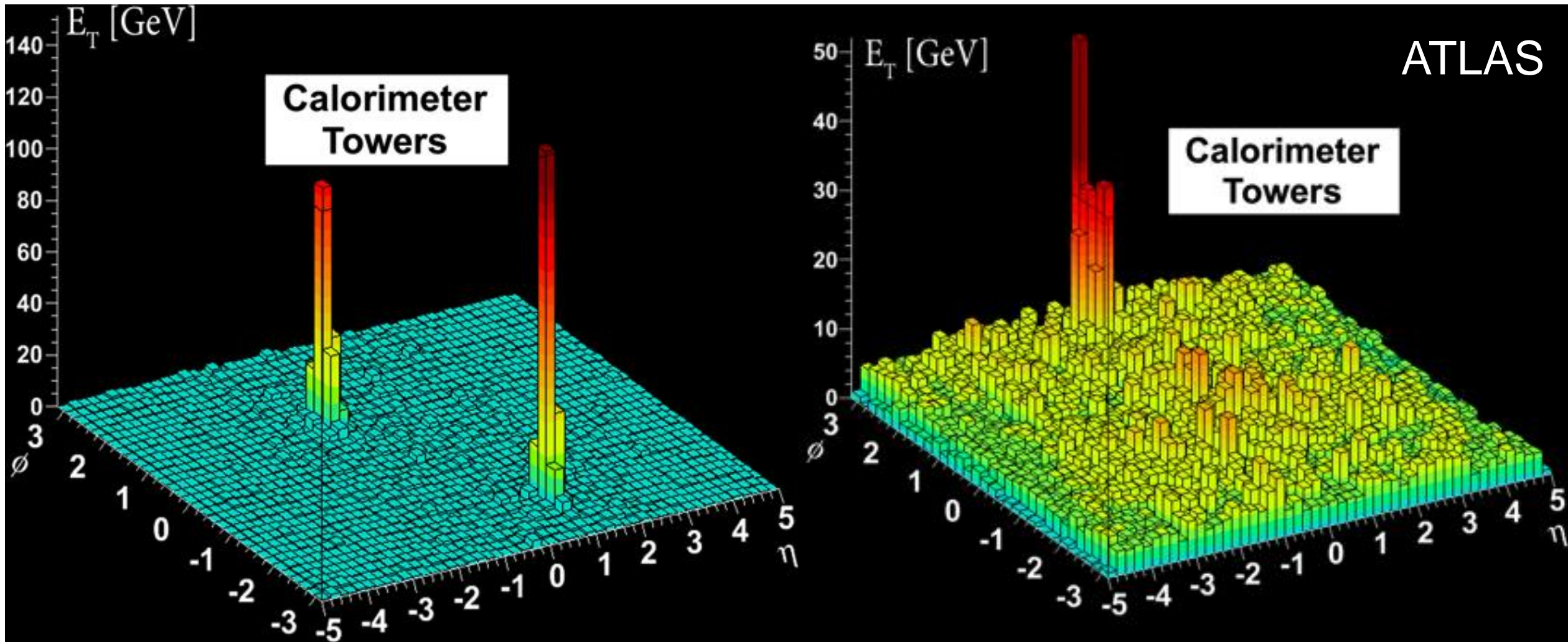
- Long-range azimuthal correlations (as originating from elliptic flow) are also observed in small systems: double ridges.



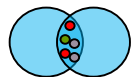
- Similar observations hold true for many other typical *kinetic heavy-ion* observables measured in high multiplicity pp and pPb collisions → clear indication for *collectivity in small systems*.

Hard scatterings and jets

Jet-medium interactions (1)



Peripheral Pb-Pb



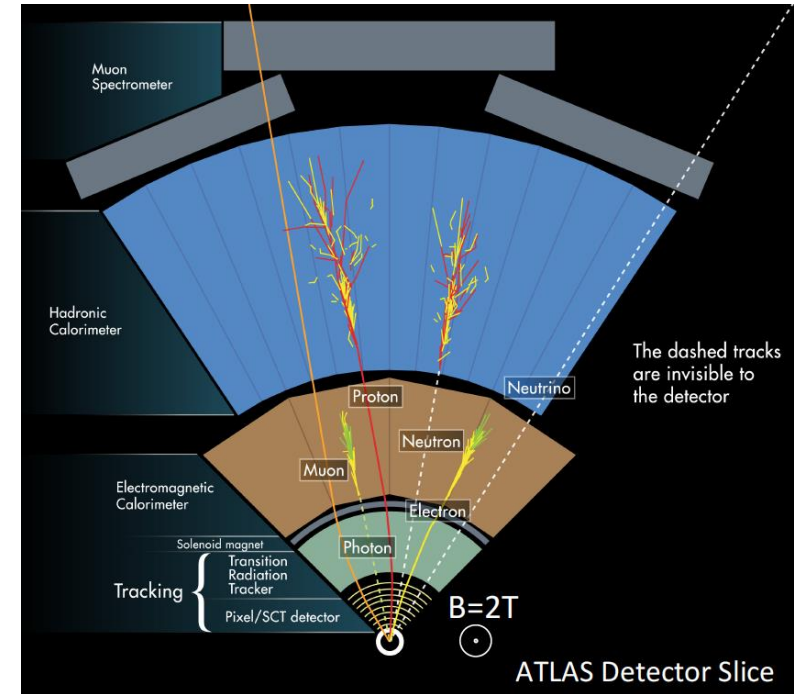
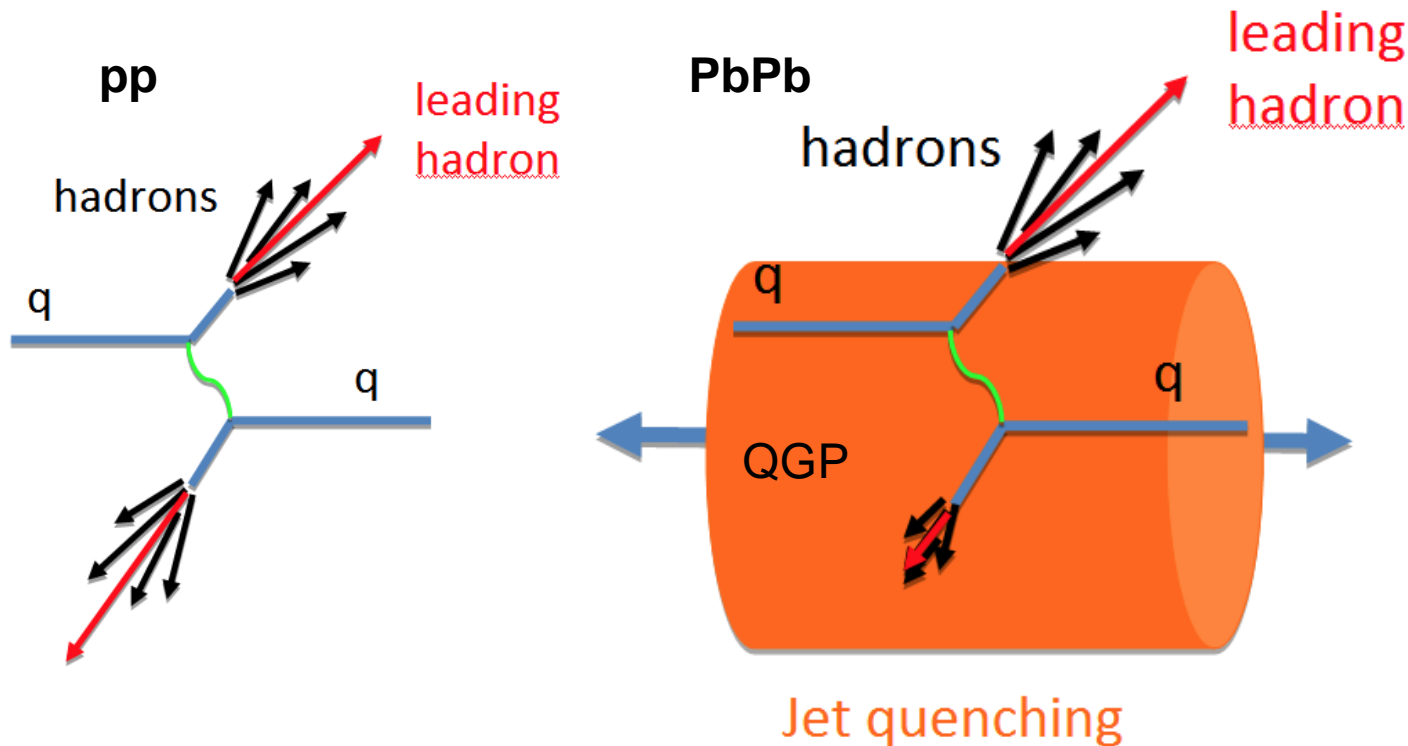
[PRL105:252303,2010]

Central Pb-Pb



Jet-medium interactions (2)

- One jet disappears (or loses a substantial amount of its energy) in the QGP
→ "jet quenching"



→ N.B.: To stop a highly energetic jet (e.g. 100 GeV), it needs a 10fm droplet of QGP or ~1.5m of hadronic calorimeter.

Dijet asymmetry

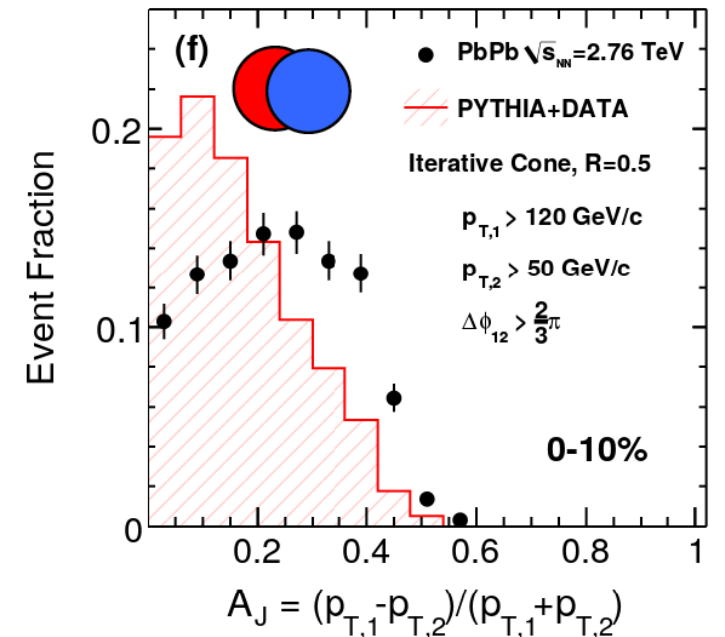
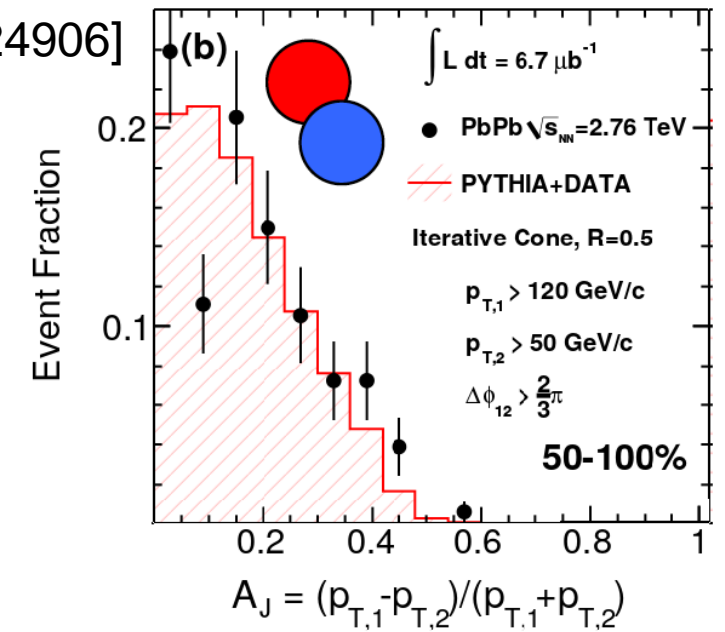
[PRC 84 (2011) 024906]

- How often do jets lose a large amount of energy?
→ quantified by the dijet asymmetry
- Two highest energy jets with $\Delta\phi > 2\pi/3$:

$$A_J = \frac{|p_{T1} - p_{T2}|}{p_{T1} + p_{T2}}$$

$\xleftarrow{p_{T1} = p_{T2} \rightarrow A_J = 0}$
 $\xleftarrow{1/3 p_{T1} = p_{T2} \rightarrow A_J = 0.5}$

- Peripheral collisions: distribution as in Pythia (as in pp)
- Central collisions:
 - Symmetric configuration is significantly depleted
 - Enhancement of asymmetric configurations



Nuclear modification factor R_{AA}

- Hard process occur in *initial* nucleon-nucleon (NN) collisions. The momentum transfers in the later evolution of the system are smaller.
- Heavy-ion collision: many NN collisions
- Without *nuclear effects* (interaction with the QCD medium), a heavy-ion collision would just be a superposition of independent NN collisions with incoherent fragmentation.
- The number of independent NN collisions $\langle N_{coll} \rangle$ can be calculated for a given impact parameter/centrality in the Glauber model.

Spectrum in AA collisions

$$R_{AA} = \frac{dN_{AA} / dp_T}{\langle N_{coll} \rangle dN_{pp} / dp_T}$$

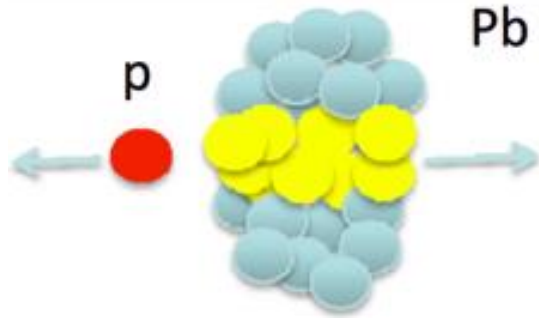
Pb Pb

Spectrum in pp collisions

$R_{AA} = 1 \rightarrow$ no modification
 $R_{AA} \neq 1 \rightarrow$ medium effects

The most simple example: R_{pA}

- In a pA collision, the proton hits on average 6.9 nucleons of the Pb nucleus:

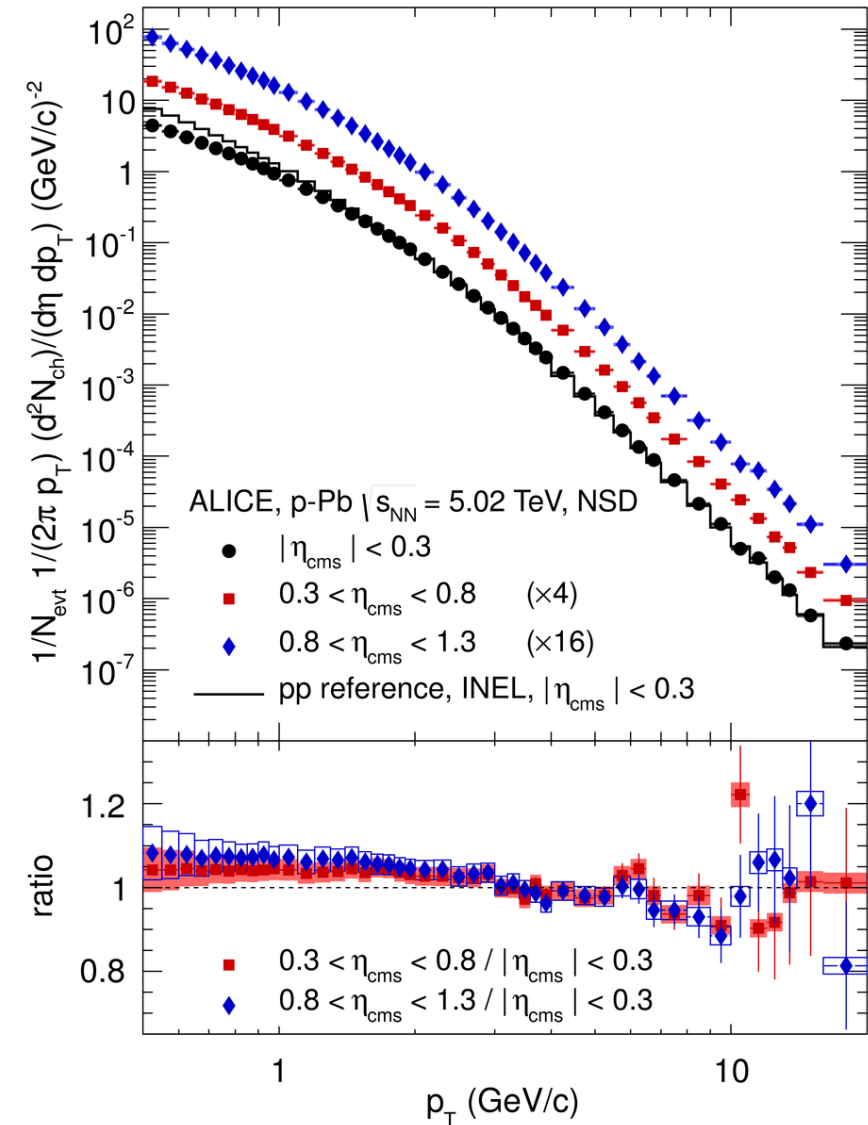


$$R_{pA} = \frac{dN_{pA} / dp_T}{\langle N_{coll} \rangle dN_{pp} / dp_T}$$

$$\rightarrow \langle N_{coll} \rangle = 6.9 \pm 0.6$$

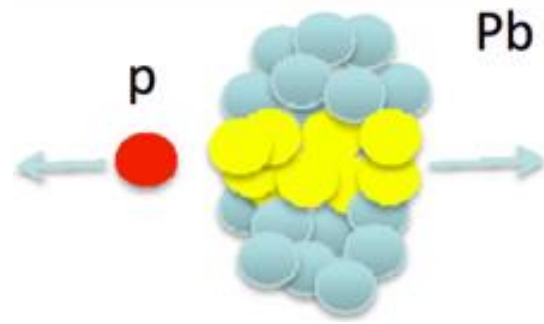
- We distinguish number of collisions N_{coll} and number of participants N_{part} :
 - A nucleon can *collide* several times with nucleons of the target nucleus (Glauber assumes that it stays intact after each collision).
 - Each nucleon with experiences at least one collision, is called a participant (N_{part}).
 $\Rightarrow N_{part} = N_{coll} + 1$ in pPb

Phys. Rev. Lett. 110 (2013) 082302



The most simple example: R_{pA}

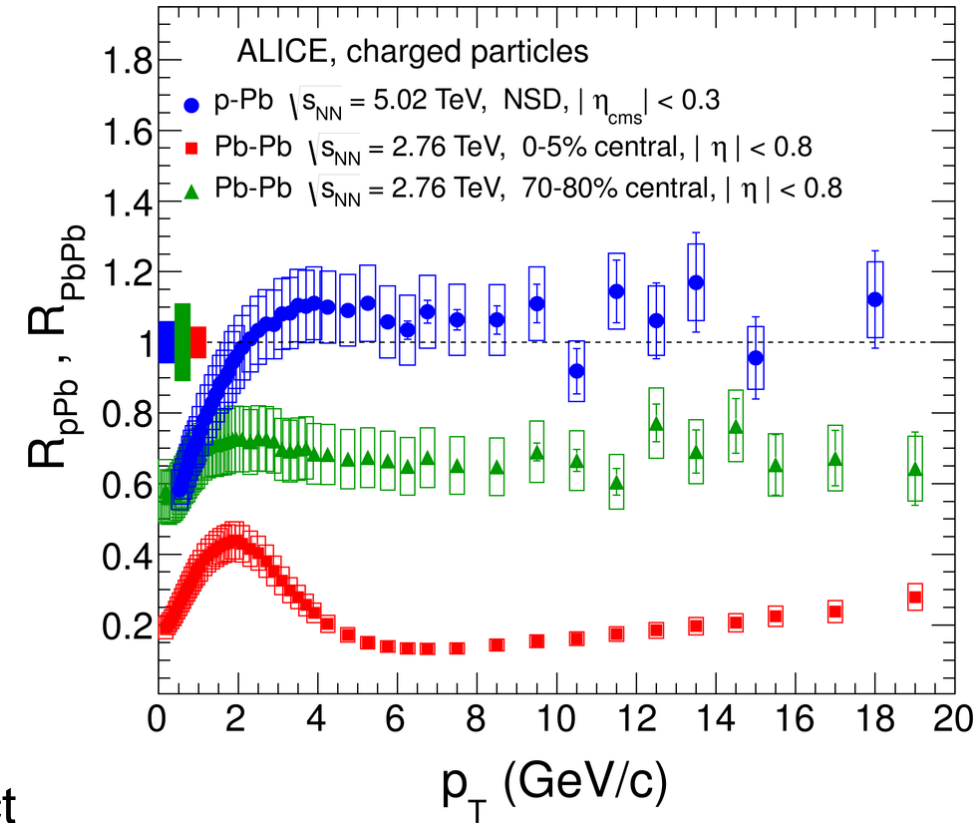
- In a pA collision, the proton hits on average 6.9 nucleons of the Pb nucleus:



$$R_{pA} = \frac{dN_{pA} / dp_T}{\langle N_{coll} \rangle dN_{pp} / dp_T}$$

$$\rightarrow \langle N_{coll} \rangle = 6.9 \pm 0.6$$

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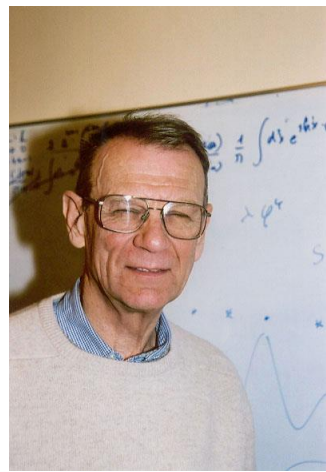


How to determine N_{coll} and N_{part} ?

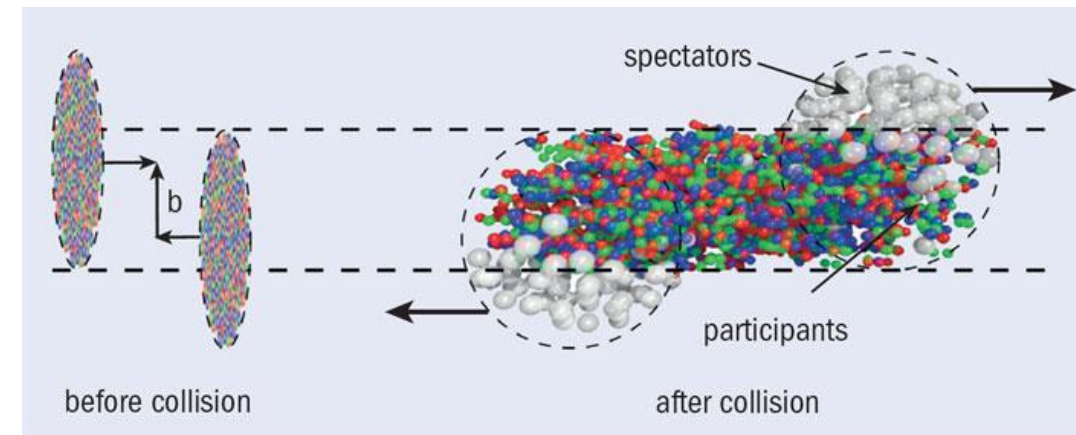
- “Billiard ball” Monte-Carlo, named after Roy Glauber, but originally introduced to heavy-ion physics by Bialas, Blezynski, and Czyz (Nucl. Phys. B111(1976)461).
- Assumptions:
 - Nucleons travel on straight lines
 - Collisions do not alter their trajectory (nor anything else, they remain intact) assuming their energy is large enough
 - No quantum-mechanical interference
 - Interaction probability for two nucleons is given by the nucleon-nucleon (pp) cross-section.
- Strong dependence on *impact parameter* b



R. Glauber



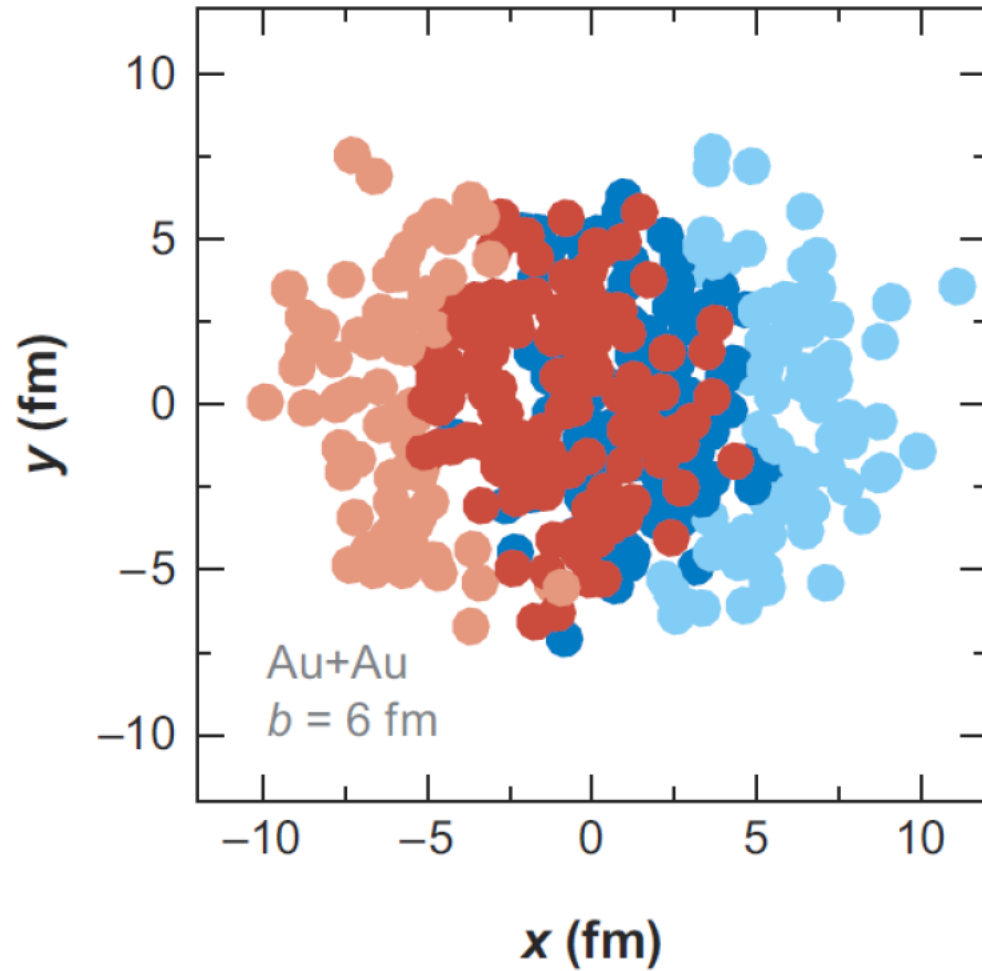
A. Bialas



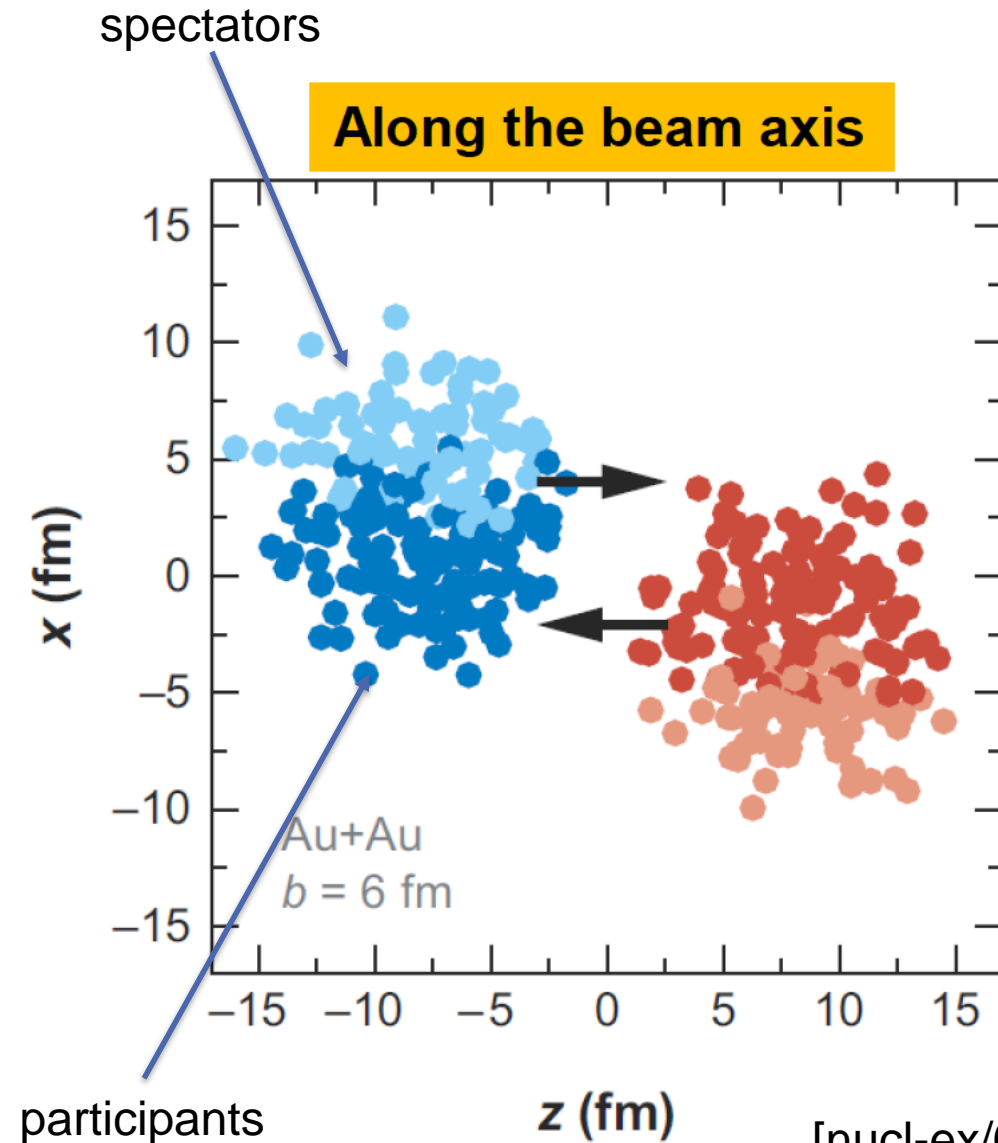
<http://cerncourier.com/cws/article/cern/53089>

Glauber Monte-Carlo

Transverse view



Along the beam axis



[nucl-ex/0701025]

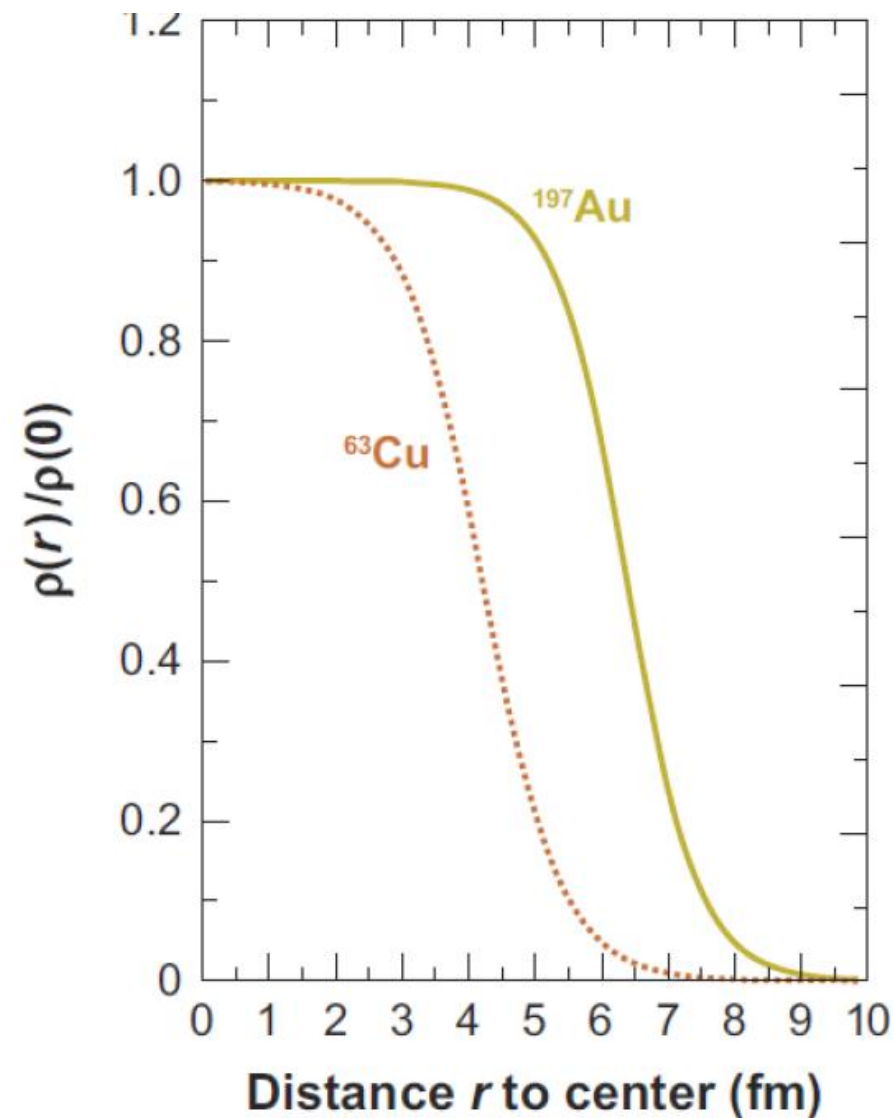
Input to Glauber MC (1)

- Distributions of nucleons in nuclei:
 - well measured by electron-ion scattering experiments
 - Paramterised as Woods-Saxon disitrubtion

$$\rho(r) = \rho_0 \frac{1}{1 + \exp\left(\frac{r-R}{a}\right)}$$

Density in the center ρ_0
 Nuclear radius R
 Skin depth a

- Nucleon-nucleon cross-section
 - Measured in pp collisions or from extrapolations



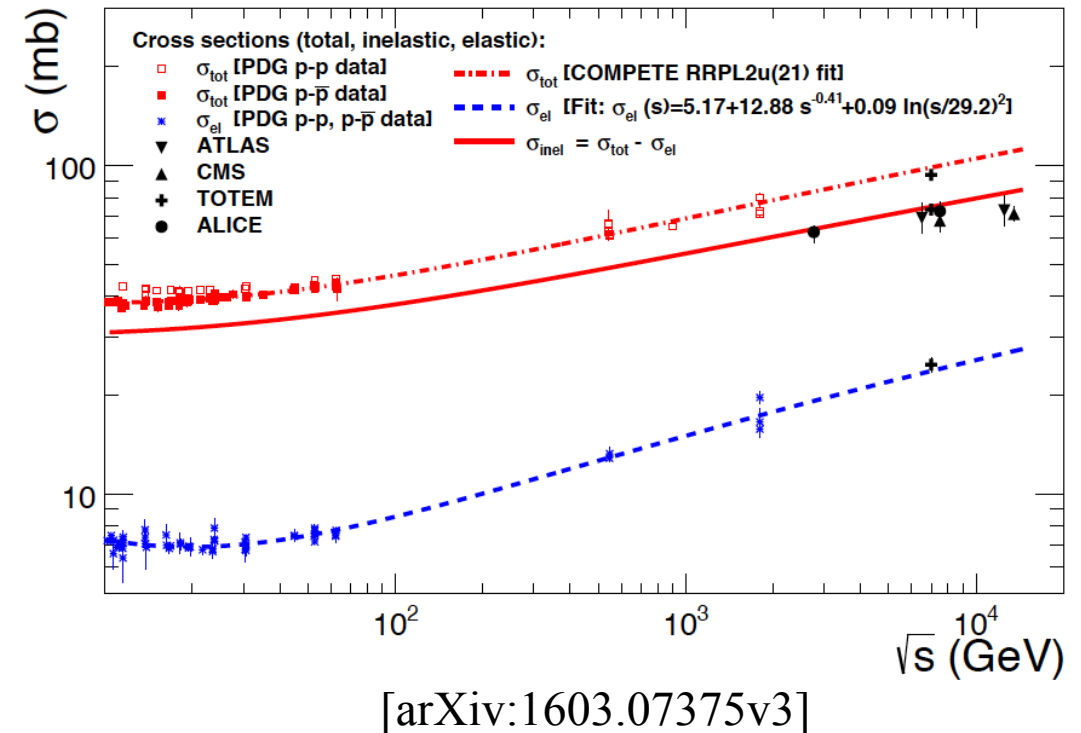
Input to Glauber MC (2)

- Distributions of nucleons in nuclei:
 - well measured by electron-ion scattering experiments
 - Paramterised as Woods-Saxon disitrubtion

$$\rho(r) = \rho_0 \frac{1}{1 + \exp\left(\frac{r-R}{a}\right)}$$

Diagram illustrating the Woods-Saxon distribution of nucleons in a nucleus. The equation is $\rho(r) = \rho_0 \frac{1}{1 + \exp\left(\frac{r-R}{a}\right)}$. The parameters are labeled: ρ_0 is the **Density in the center**, R is the **Nuclear radius**, and a is the **Skin depth**.

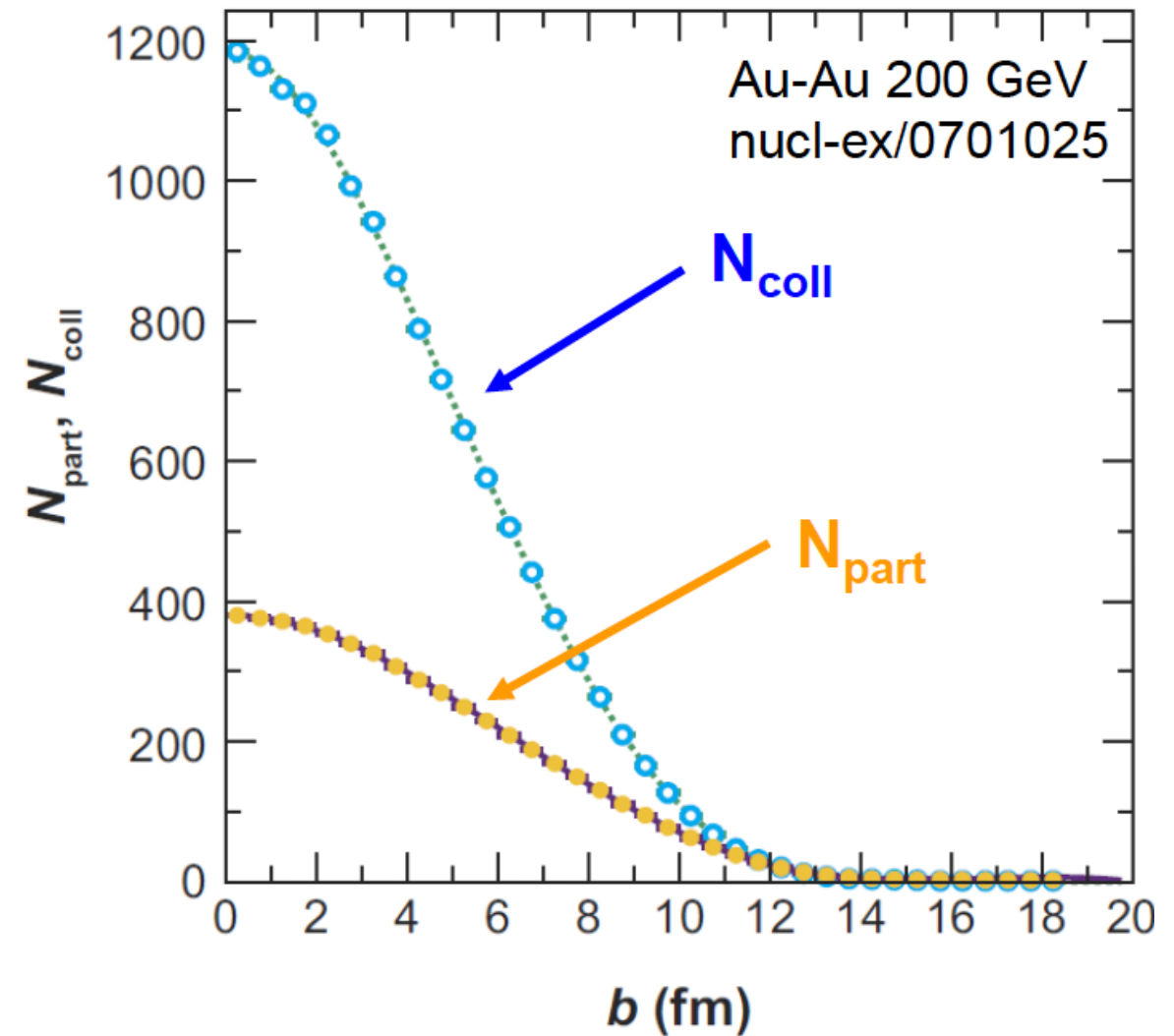
- Nucleon-nucleon cross-section
 - Measured in pp collisions or from extrapolations



Glauber MC output

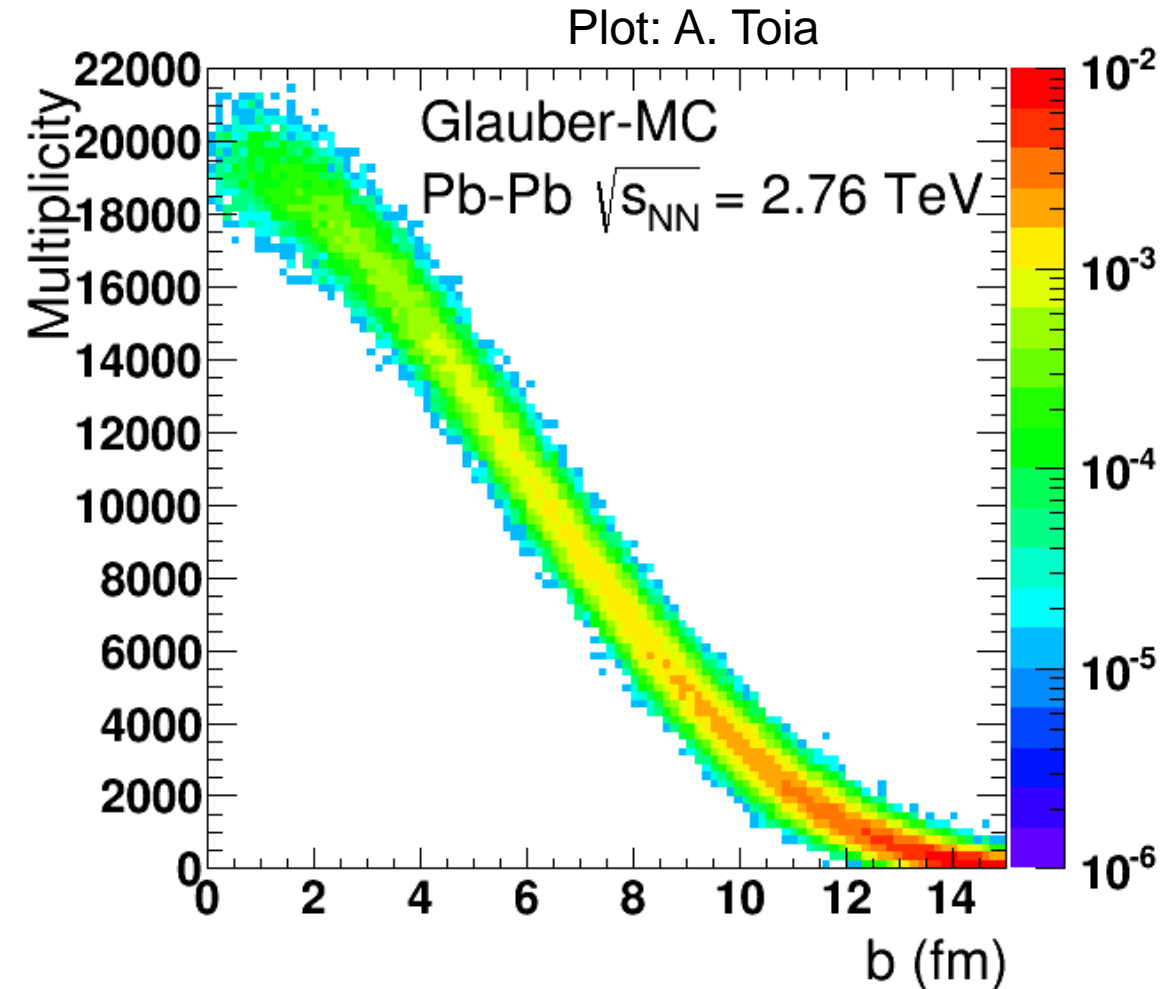
Typical values:

- 10% most central collisions at RHIC (Au-Au, 200 GeV)
 - $N_{\text{coll}} \sim 1200$
 - $N_{\text{part}} \sim 380$
- 5% most central collisions at LHC (Pb-Pb 2.76 TeV)
 - $N_{\text{coll}} \sim 1680$
 - $N_{\text{part}} \sim 382$
- Difference mainly from cross-section increase and slightly larger nucleus

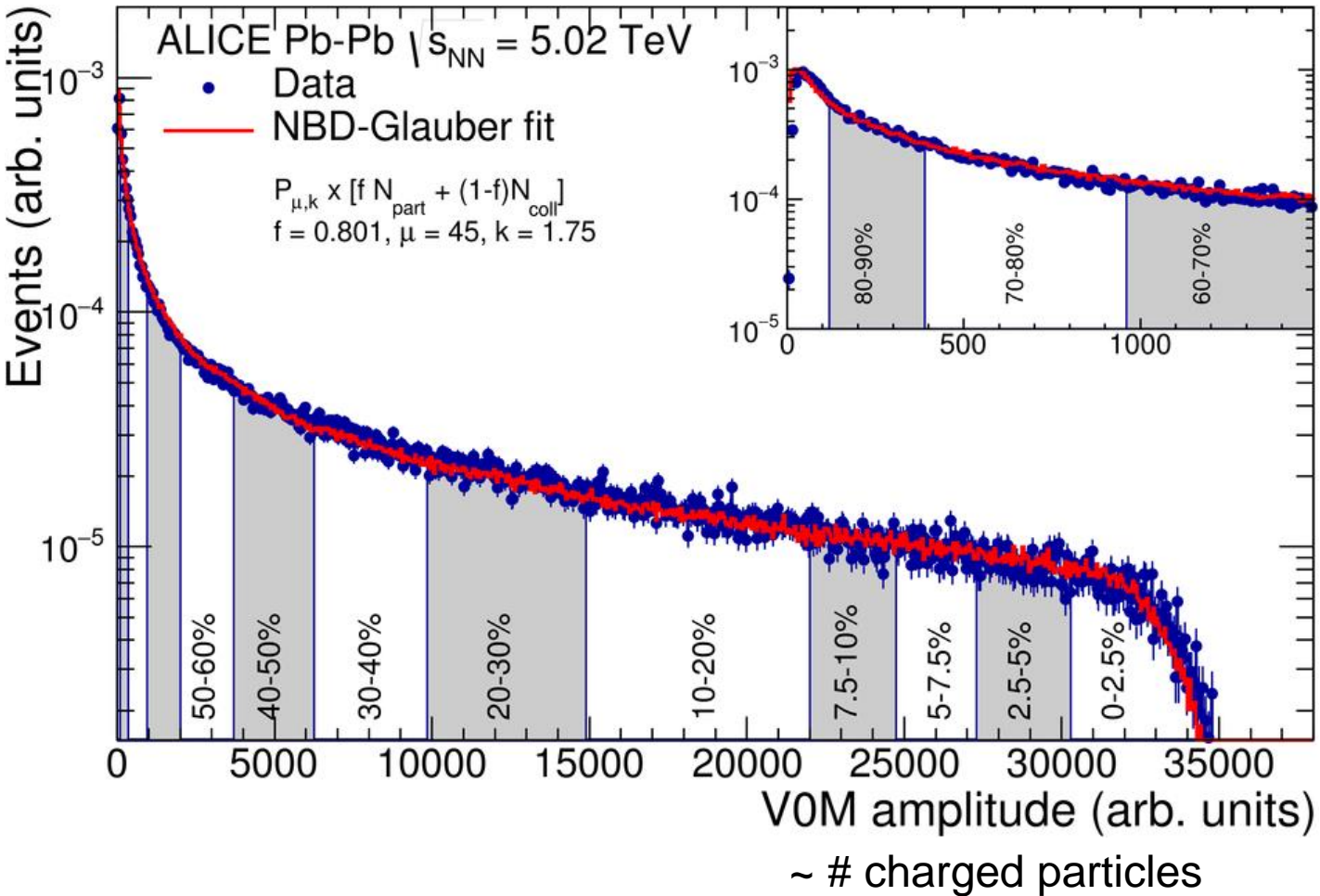


Centrality and Glauber model

- Multiplicity is inversely proportional to the impact parameter
=> Knowing the multiplicity of the event, we roughly know the impact parameter (and thus also N_{coll} and N_{part}). We *fit* the multiplicity distribution with the Glauber model (see next slide).
- Multiplicity is strongly correlated in different phase space regions in heavy-ion collisions (e.g. forward and mid-rapidity).



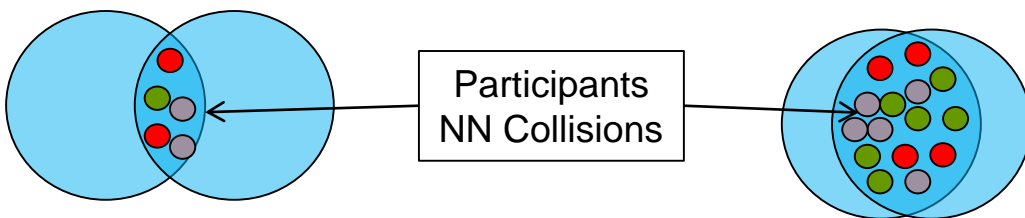
Geometry of heavy ion collisions



Centrality Variables:

- N_{coll} : Number of nucleon-nucleon collisions
- N_{part} : Number of participating nucleons
- Percentile of hadronic cross-section:
 - 0-5% => central (“many particles”)
 - 80-90% => peripheral (“few particles”)

→ We can determine (a posteriori) the geometry of heavy ion collisions. More details on the **Glauber model** when discuss hard probes..

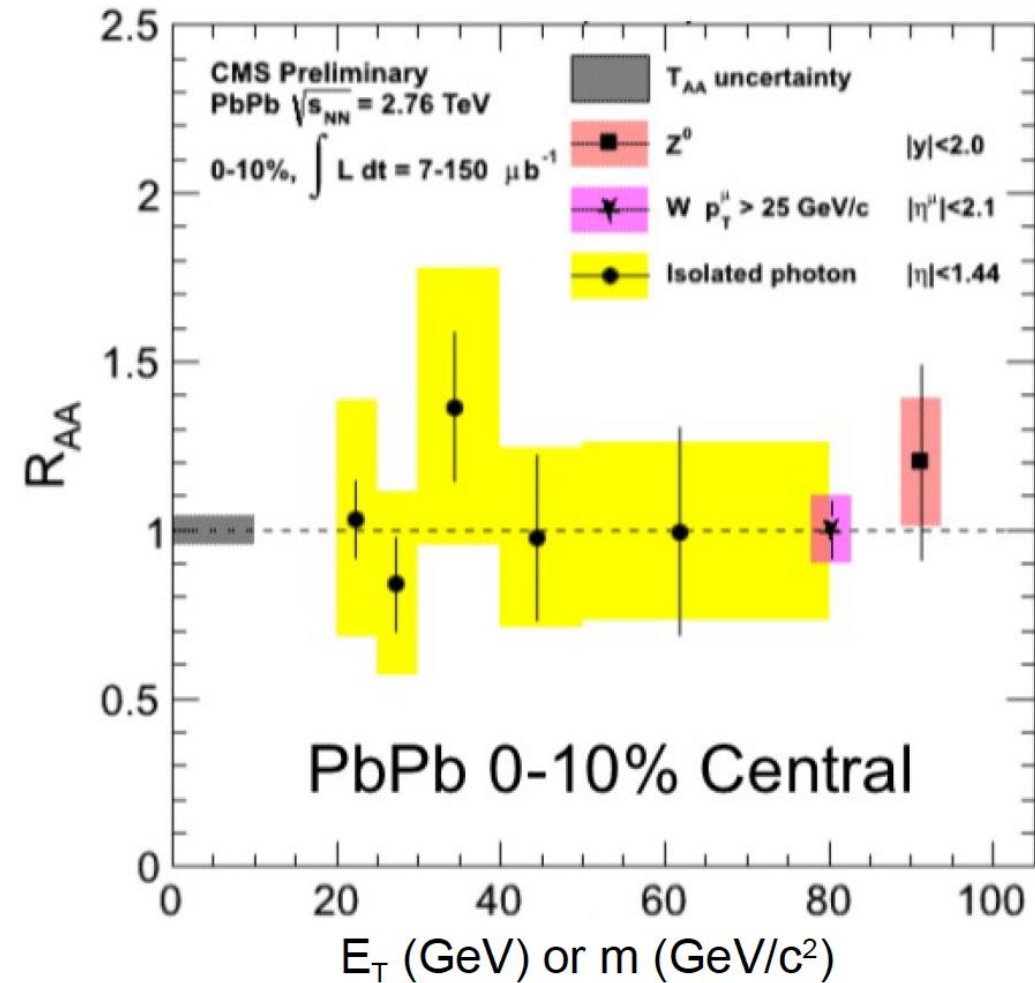
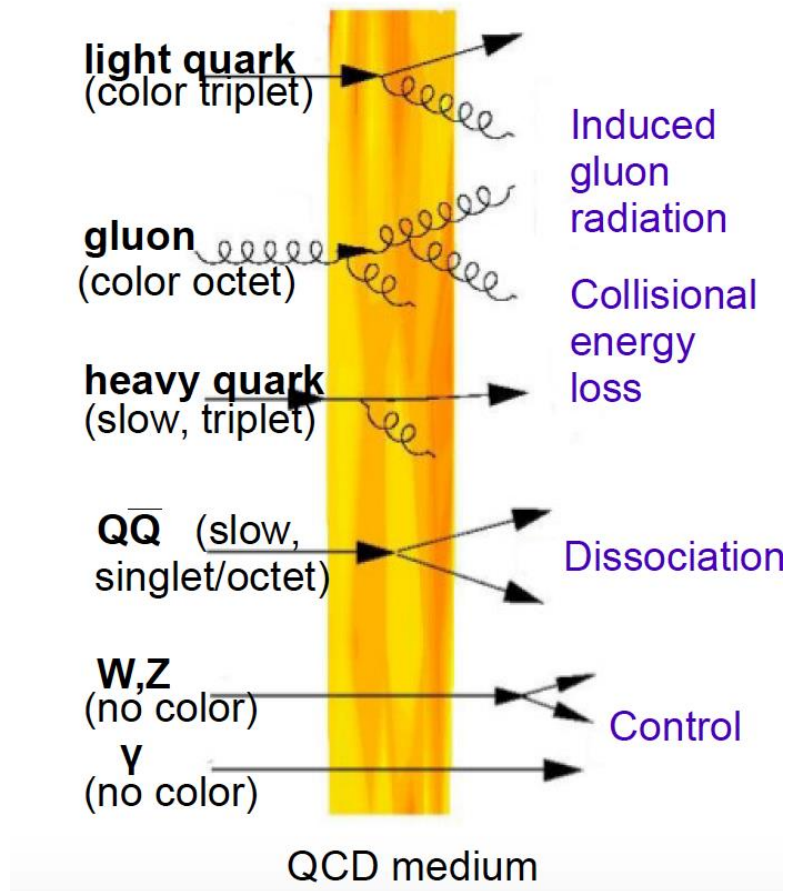


Does the Glauber model work?

→ Yes, we can test it with electroweak control probes.

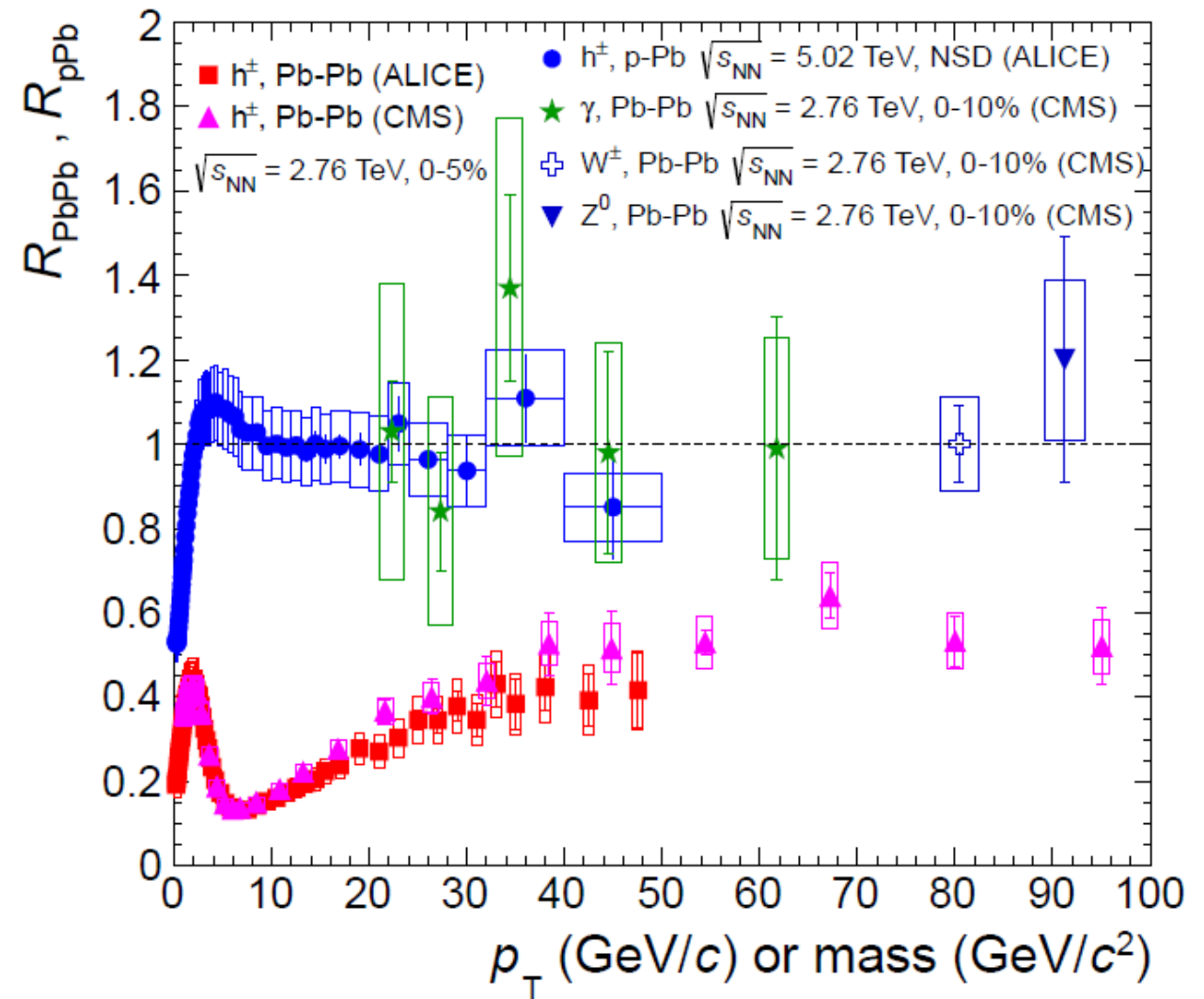
→ No medium modification observed
(despite multiplying by $N_{\text{coll}} \sim 1680$!).

$$R_{AA} = \frac{dN_{AA} / dp_T}{\langle N_{coll} \rangle dN_{pp} / dp_T}$$



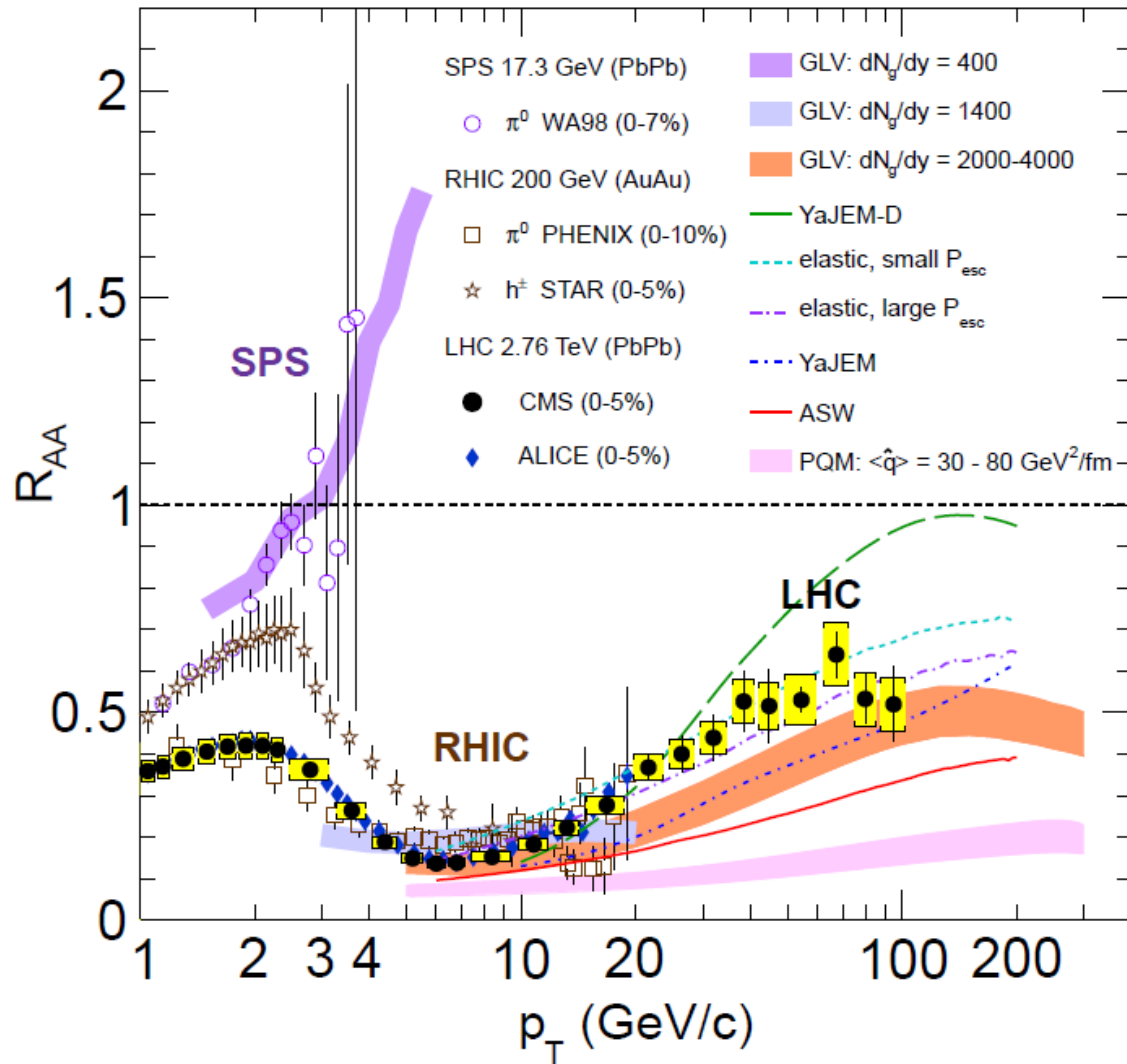
R_{AA} for charged hadrons (1)

- N_{coll} scaling works well above $p_T > 4$ GeV/c for electroweak probes and also in pPb.
=> There are no *cold nuclear matter effects* and N_{coll} -scaling is a reasonable assumption for AA.
- There is a significant suppression of high p_T -particles observed in AA collisions which is a true medium effect.
=> High p_T particle production in AA collision is not a simple superposition of incoherent nucleon-nucleon collisions.
- How does the medium achieve this suppression?

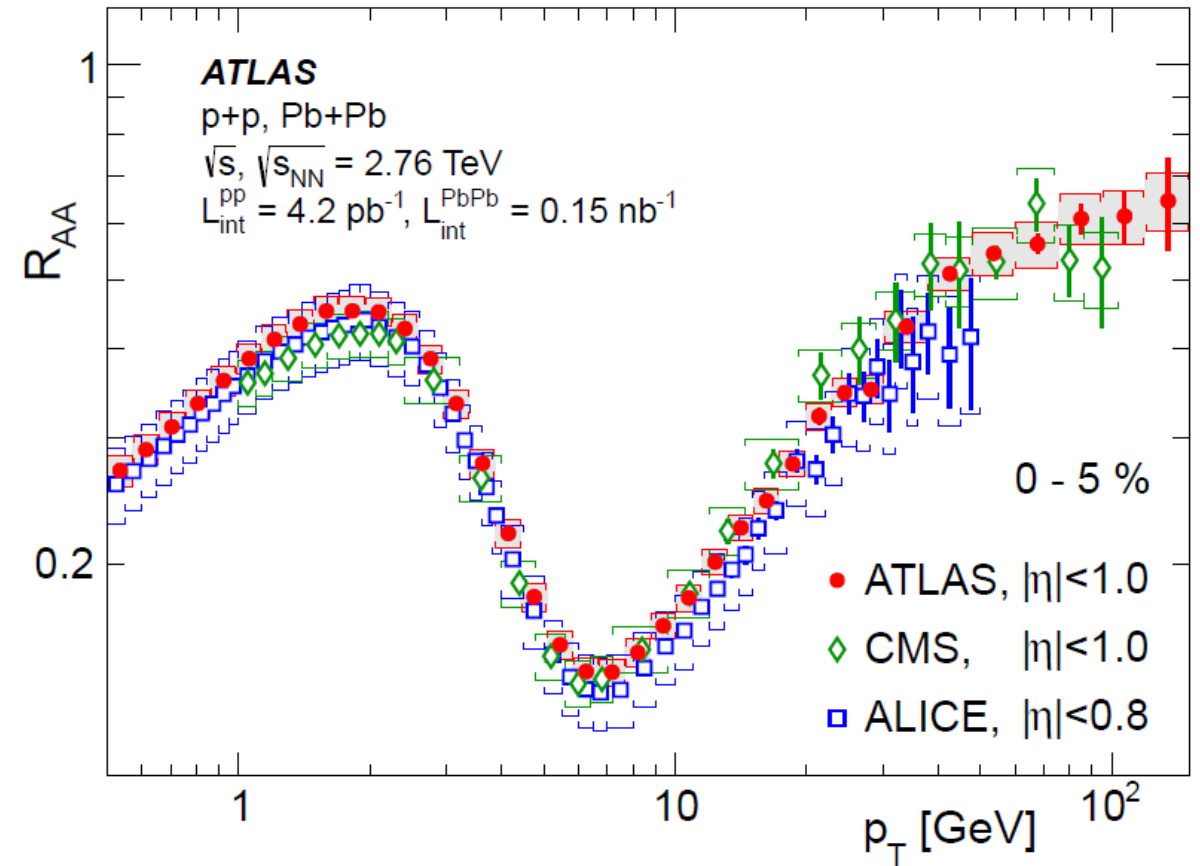


R_{AA} for charged hadrons (2)

CMS Collaboration, Eur. Phys. J. C (2012) 72:1945



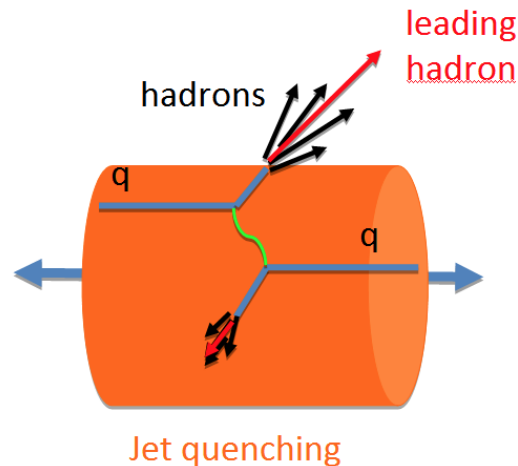
ATLAS Collaboration, JHEP09(2015)050



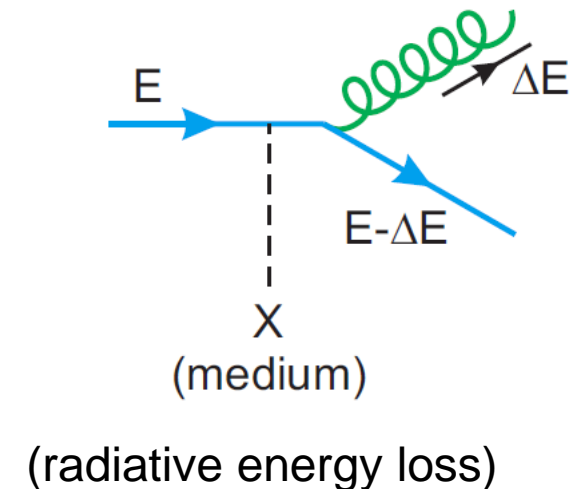
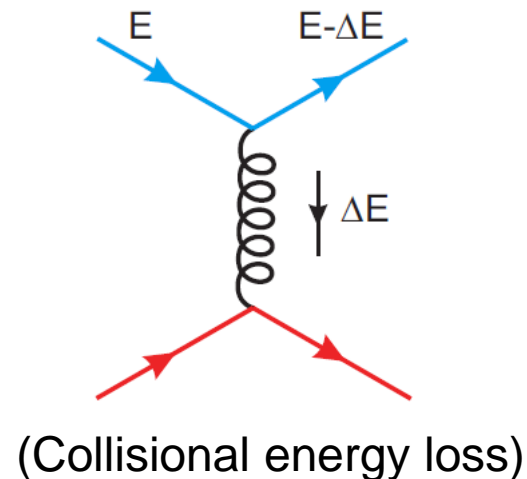
→ No high p_T particle suppression at SPS energies.
→ All LHC experiments in agreement.

Energy loss in the QGP

- The QGP is a high density source of color sources (quarks and gluons) which are felt by the traversing quark or gluon.
- It experiences
 - Collisional energy loss: elastic scatterings, dominant at low momentum
 - Radiative energy loss: inelastic scatterings, **gluon bremsstrahlung**, dominates at high momentum
- Total energy loss is a sum of the two processes.



[Lect. Notes Phys. 785,285 (2010)]

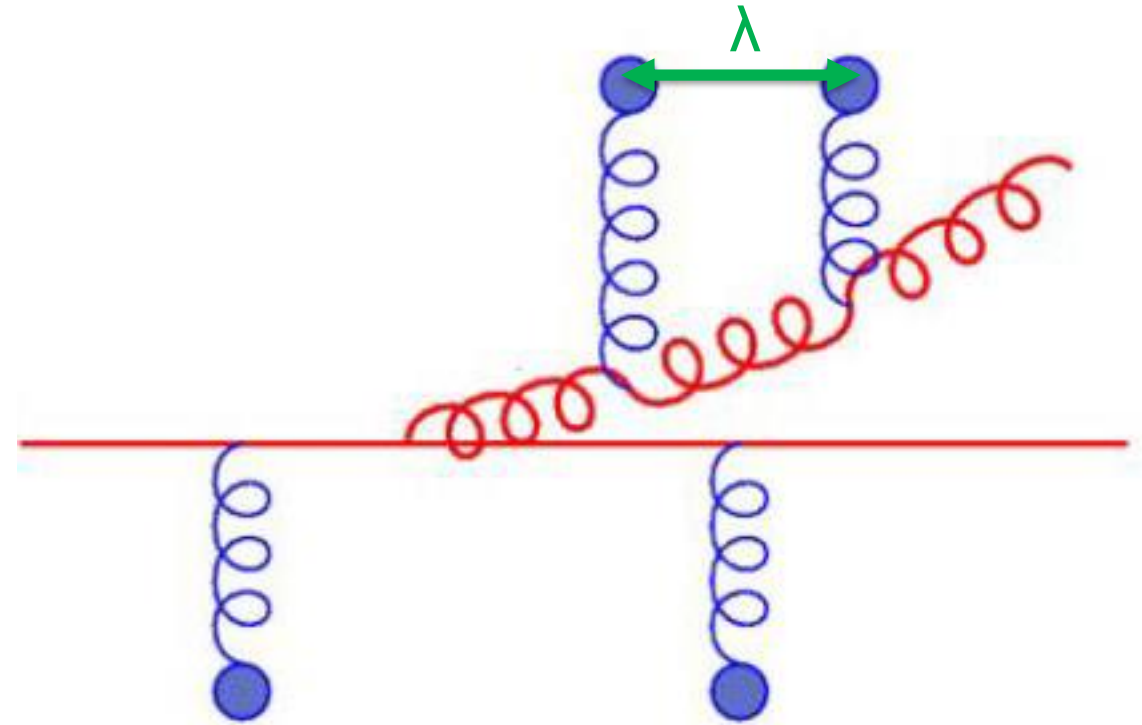


Radiative energy loss

- BDPMS formalism
 - Baier, Dokshitzer, Mueller, Peigne, Schiff
 - Infinite energy limit
 - Static medium

$$\Delta E \propto \alpha_S \cdot C_R \cdot \hat{q} \cdot L^2$$

- Energy loss proportional to:
 - Path length through medium **squared**
 - Casimir factor
 - $C_R = 4/3$ (quarks)
 - $C_R = 3$ (gluons)
 - Medium properties are encoded in the parameter “q-hat” which corresponds to the average squared transverse momentum transfer per mean free path.



→ For the **characterization of the QGP medium**, q-hat has a similar significance as e.g. the shear viscosity.

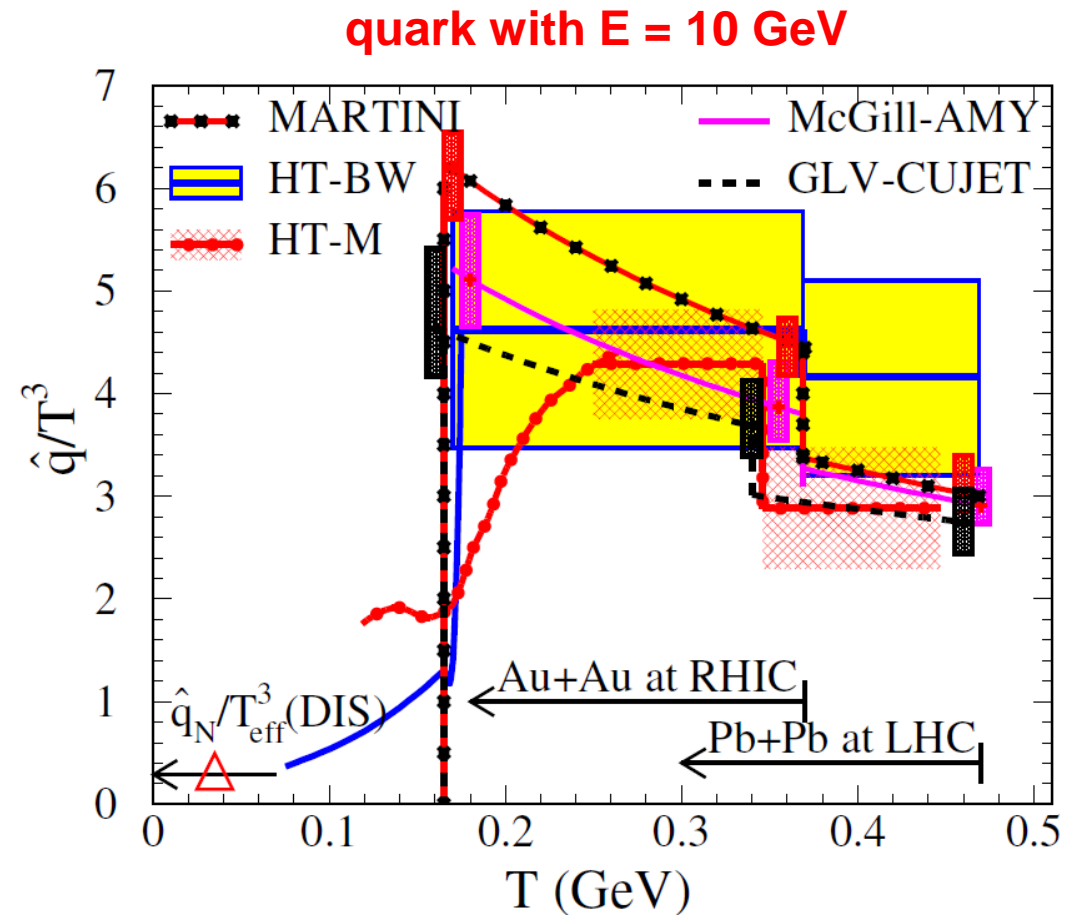
$$\hat{q} = \frac{\langle q_T^2 \rangle}{\lambda}$$

← average momentum transfer

← mean free path

Determination of \hat{q} -hat

- From the theory side, the JET collaboration extracted \hat{q} -hat using combined CMS and ALICE LHC R_{AA} data assuming no fluctuations of initial conditions and coupling the same hydro to all energy loss models.
- 5 different models with different approaches:
 - higher twist (HT-BW, HT-M)
 - hard thermal loop (MARTINI, McGill-AMY)
 - opacity expansion (GLV-CUJET)

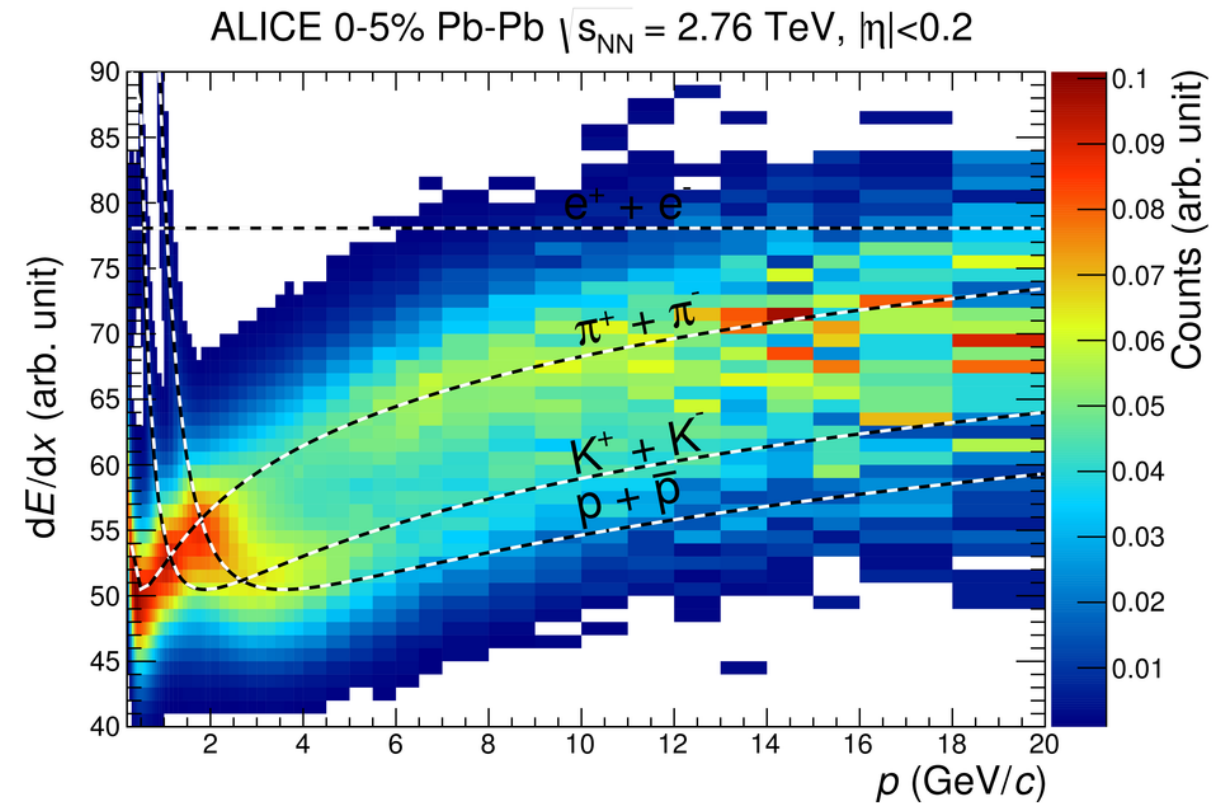
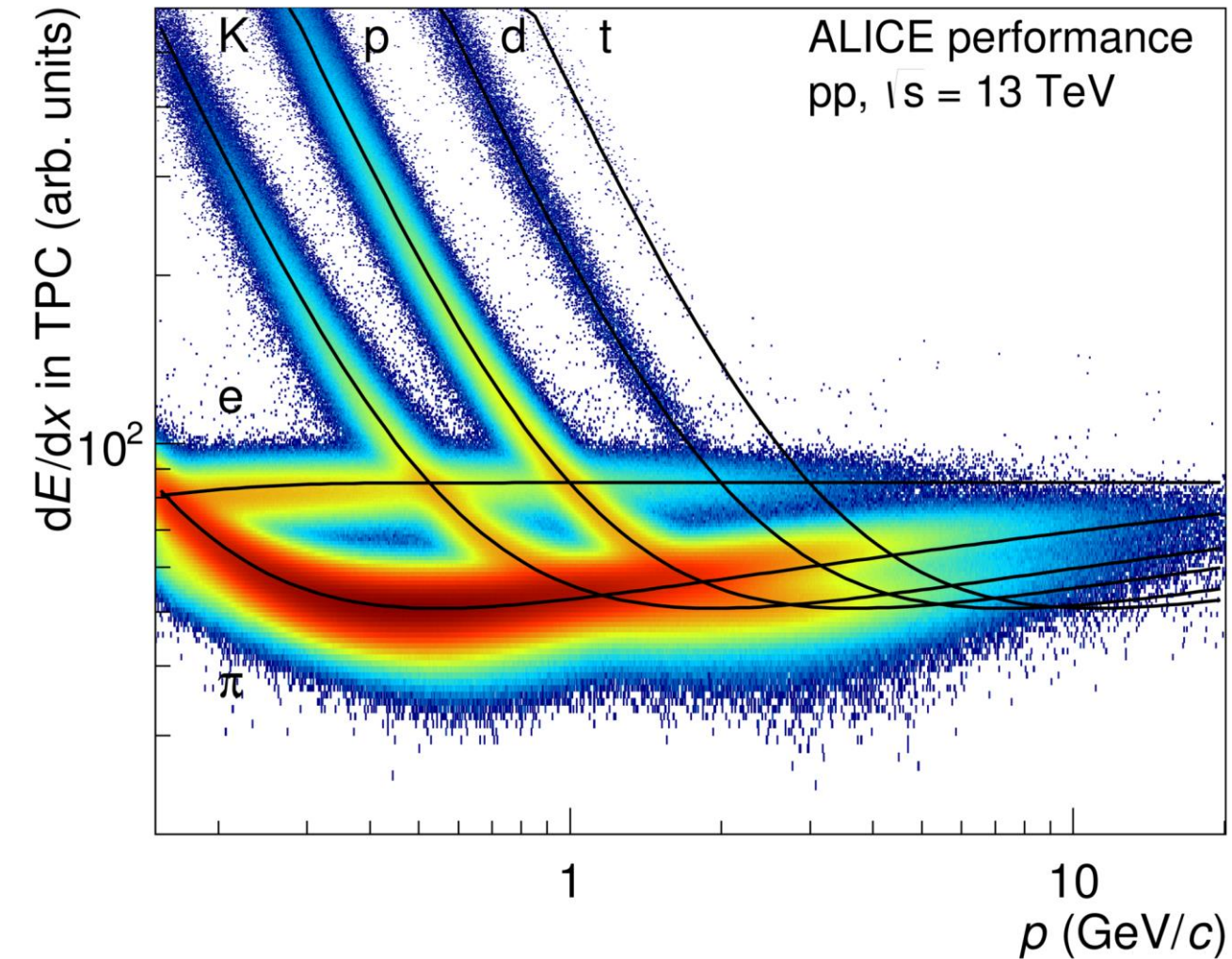


$$\frac{\hat{q}}{T^3} \approx \begin{cases} 4.6 \pm 1.2 & \text{at RHIC} \\ 3.7 \pm 1.4 & \text{at LHC.} \end{cases}$$

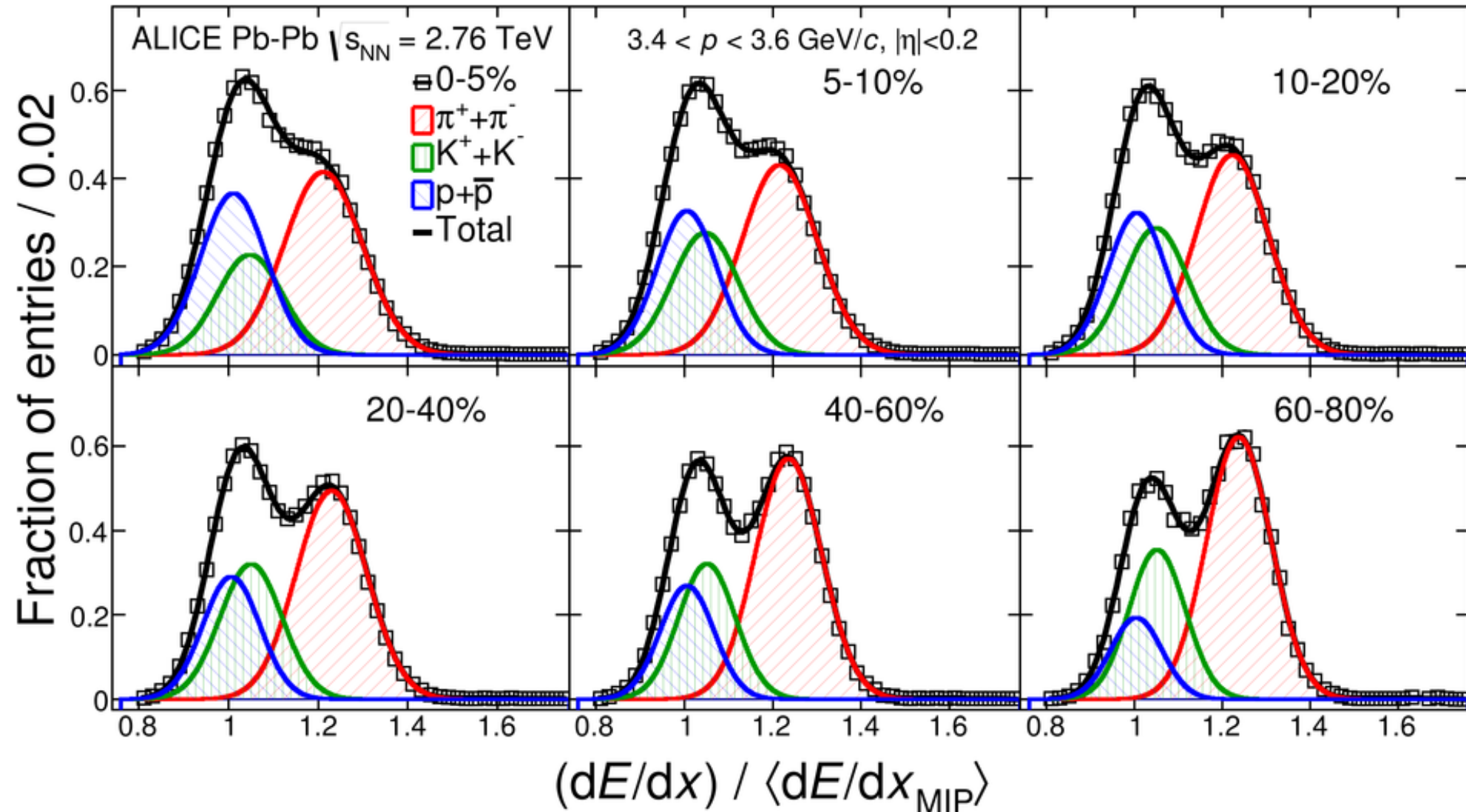
$$\hat{q} \approx \begin{cases} 1.2 \pm 0.3 \\ 1.9 \pm 0.7 \end{cases} \text{ GeV}^2/\text{fm} \text{ at } \begin{cases} T=370 \text{ MeV} \\ T=470 \text{ MeV} \end{cases}$$

For comparison: in cold nuclear matter $q = 0.02 \text{ GeV}^2/\text{fm}$ (at $t_0 = 0.6 \text{ fm}$)

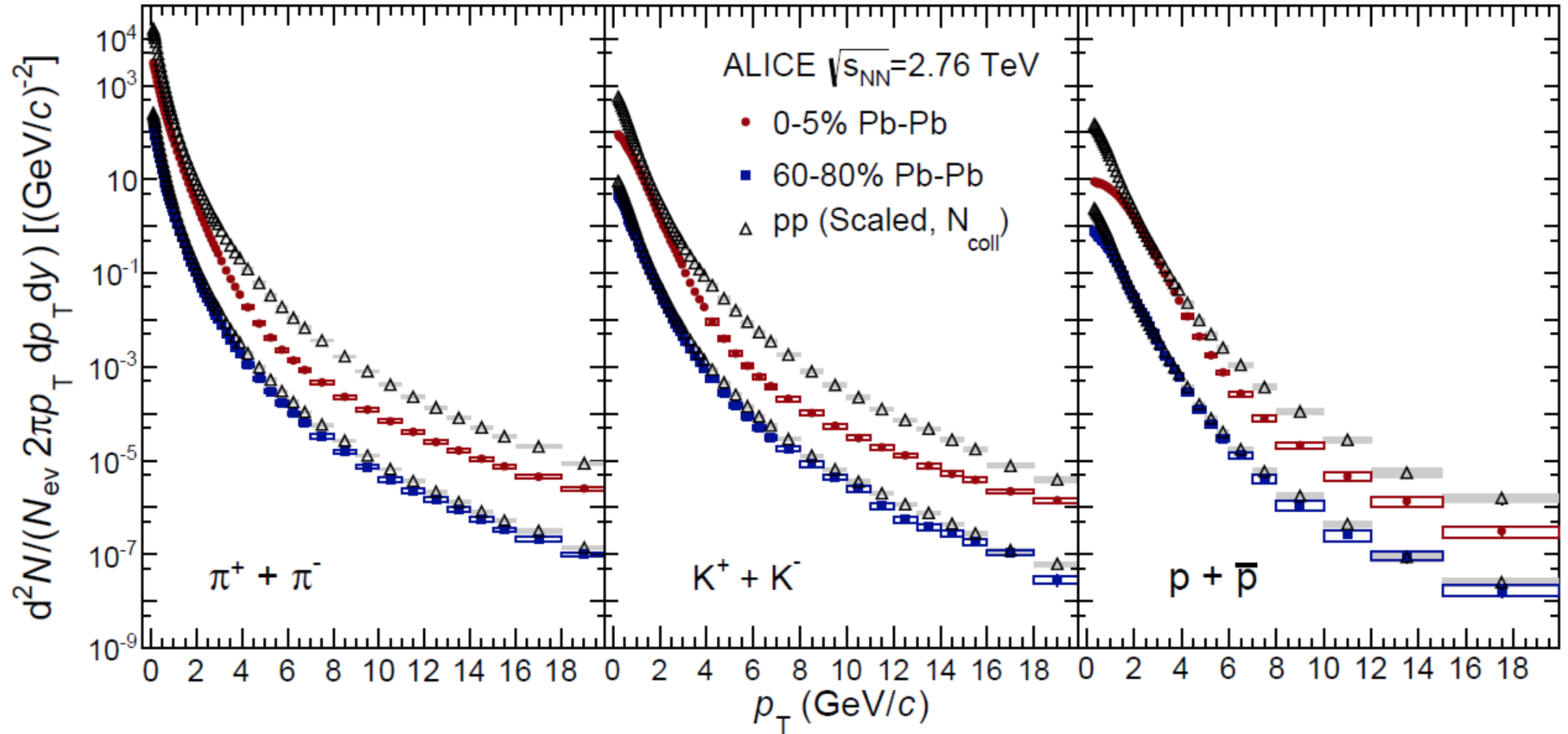
PID via dE/dx on the relativistic rise (1)



PID via dE/dx on the relativistic rise (2)



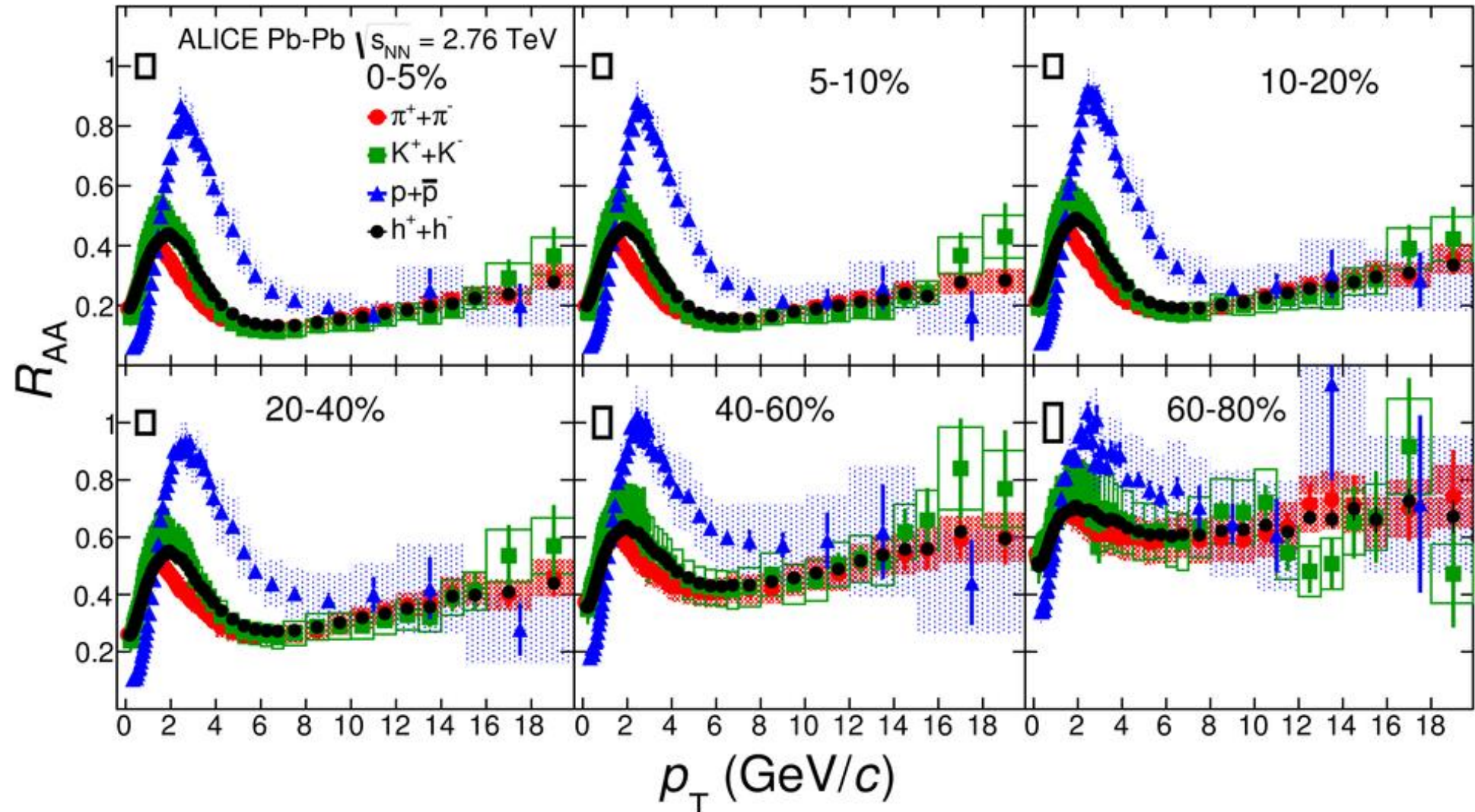
R_{AA} for identified particles (1)



[arXiv:1401.1250]

R_{AA} for identified particles (2)

R_{AA} independent of hadron species (light quarks) for momenta above ~ 8 GeV/c.

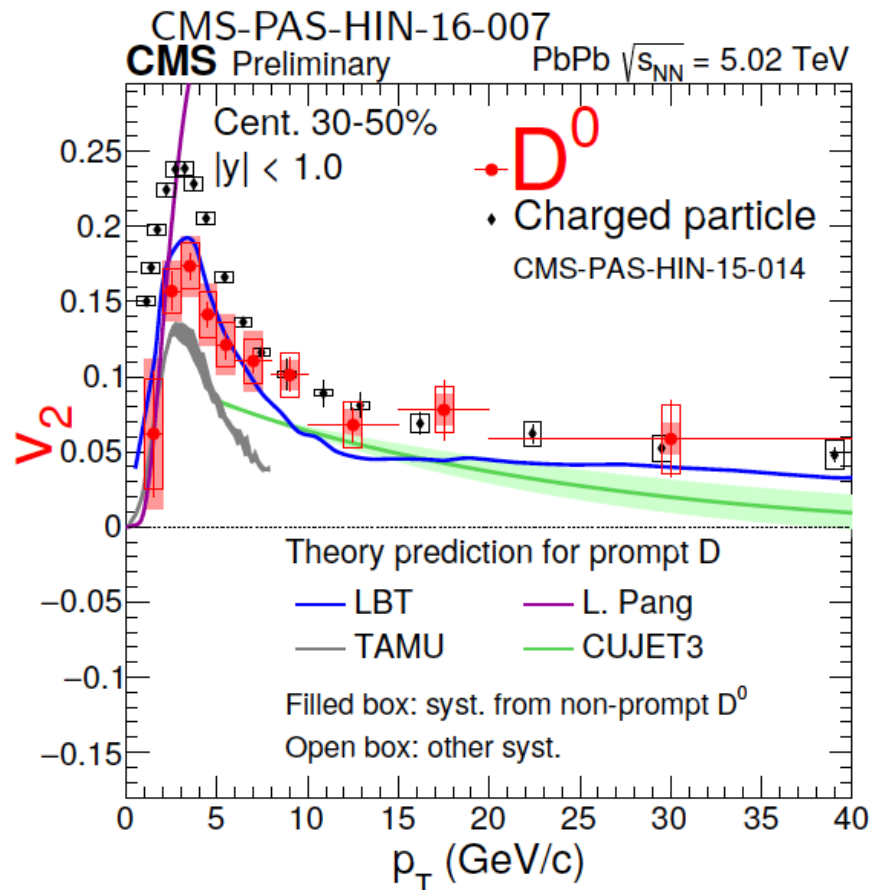


Quarkonia and heavy flavour

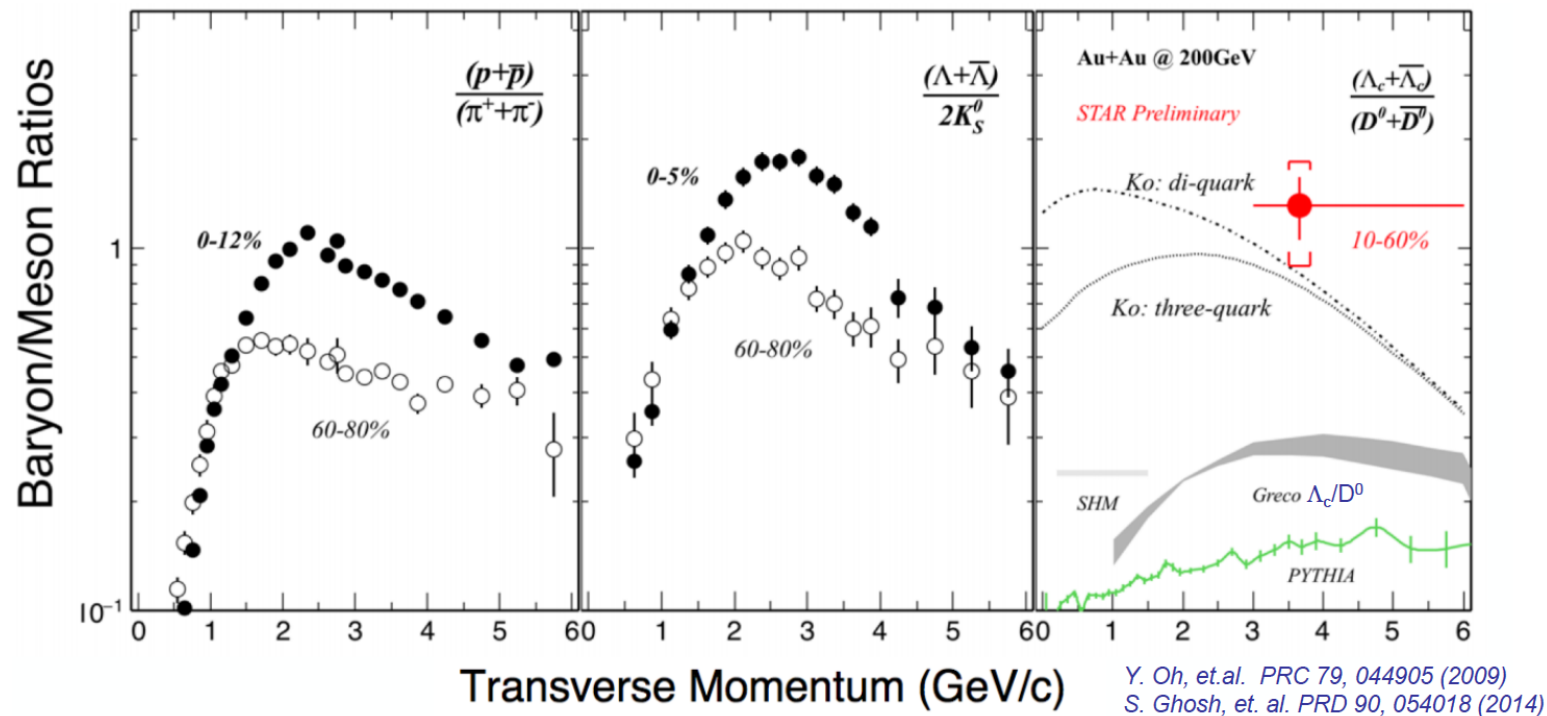
Heavy flavor (1)

- Heavy quark flavors (c, b) are dominantly produced in initial hard scatterings (calculable in pQCD) and then interact with the medium.
- There is strong evidence that **charm quarks *thermalize*** in the medium.

(A.) Elliptic flow of D mesons:

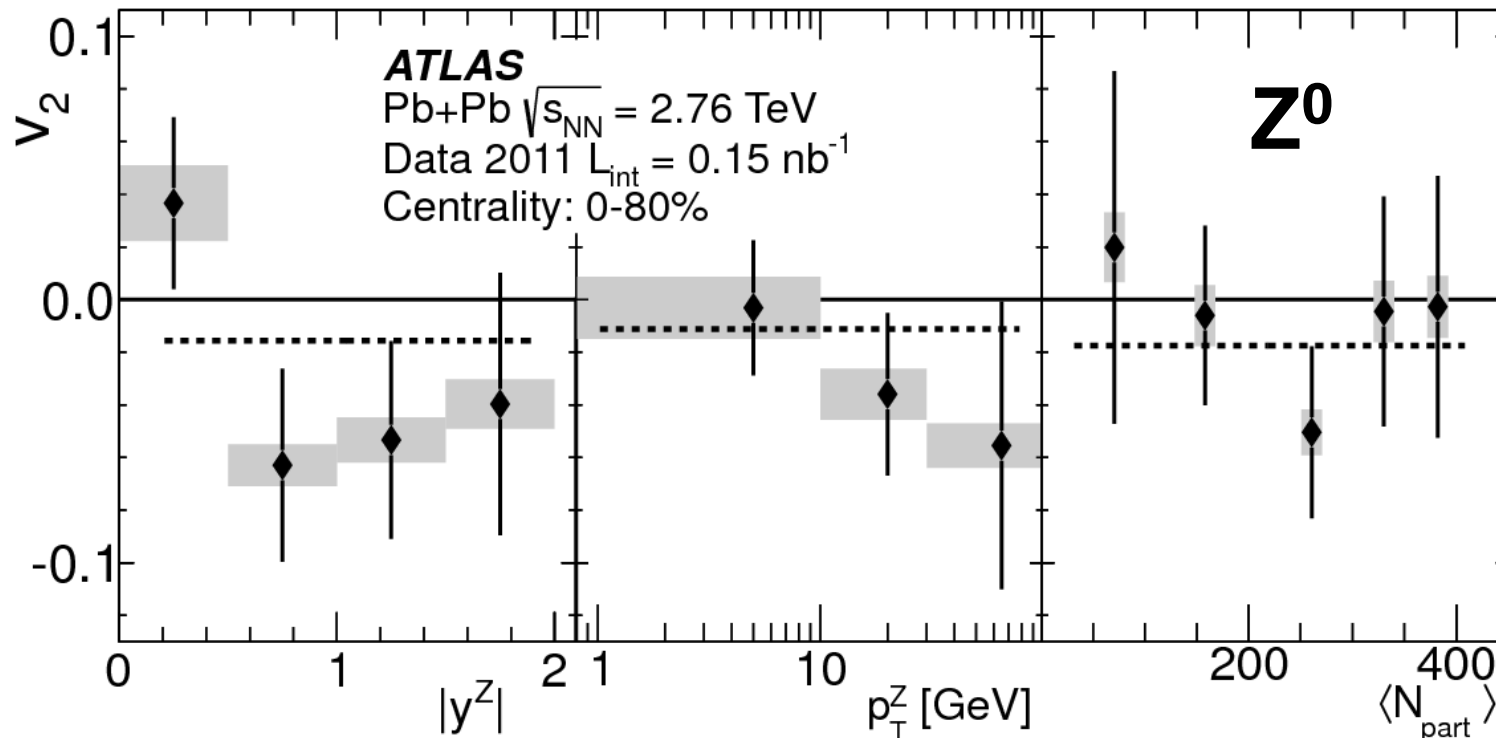


(B.) Baryon-to-meson enhancement seen in Λ_c :



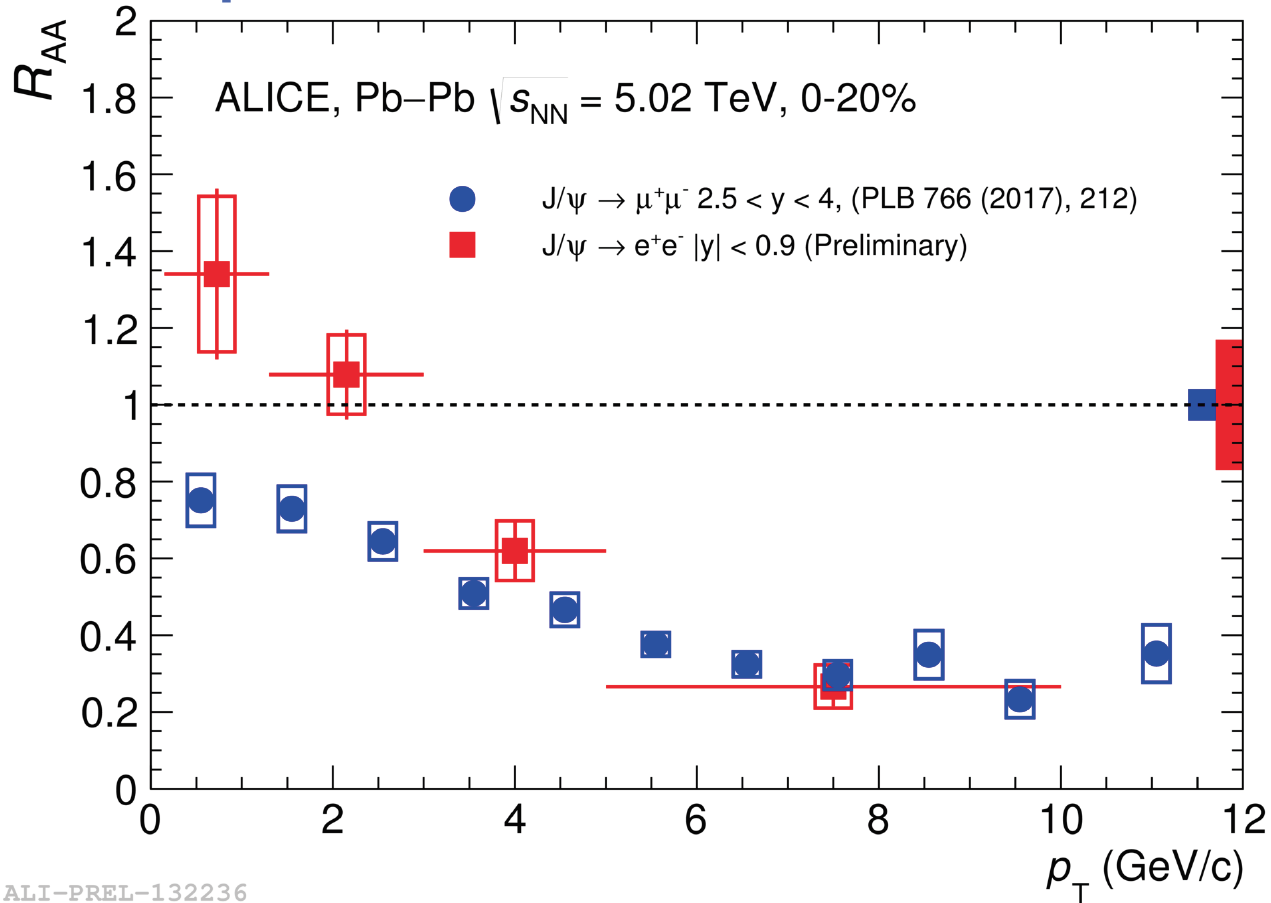
Heavy flavor (2)

- Heavy quark flavors (c, b) are dominantly produced in initial hard scatterings (calculable in pQCD) and then interact with the medium.
- There is strong evidence that **charm quarks *thermalize*** in the medium.
- N.B.: **electroweak probes do not show any interaction with the medium.**



[PRL 110, 022301 (2013)]

J/ψ recombination



ALI-PREL-132236

$$R_{AA} = \frac{dN_{AA}/dp_T}{\langle N_{coll} \rangle \cdot dN_{pp}/dp_T}$$

$R_{AA} < 1 \rightarrow$ suppression w.r.t pp coll.

$R_{AA} > 1 \rightarrow$ enhancement w.r.t to pp coll.

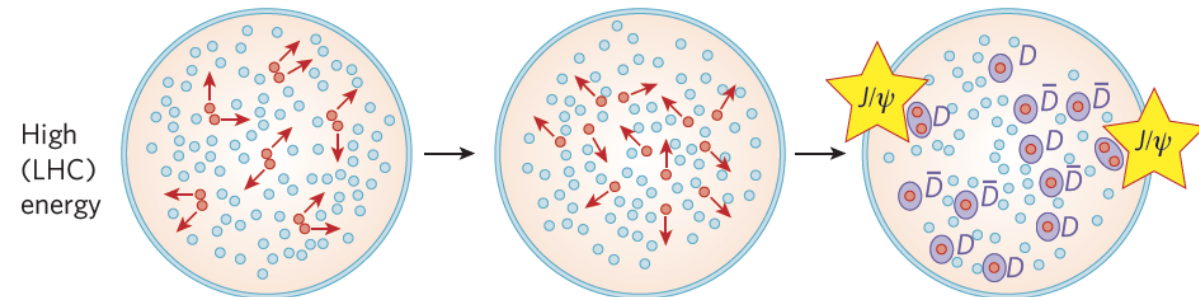
→ As $c\bar{c}$ bound state, the J/ψ is expected not to be bound in the QGP phase (Matsui/Satz, 1986), but it can re-generate at the phase boundary.

→ 5.02 TeV Pb-Pb data strongly confirms J/ψ recombination picture:

- $R_{AA}(\text{LHC}) > R_{AA}(\text{RHIC})$
- $R_{AA} \text{ midrapidity} > R_{AA} \text{ forward rap.}$

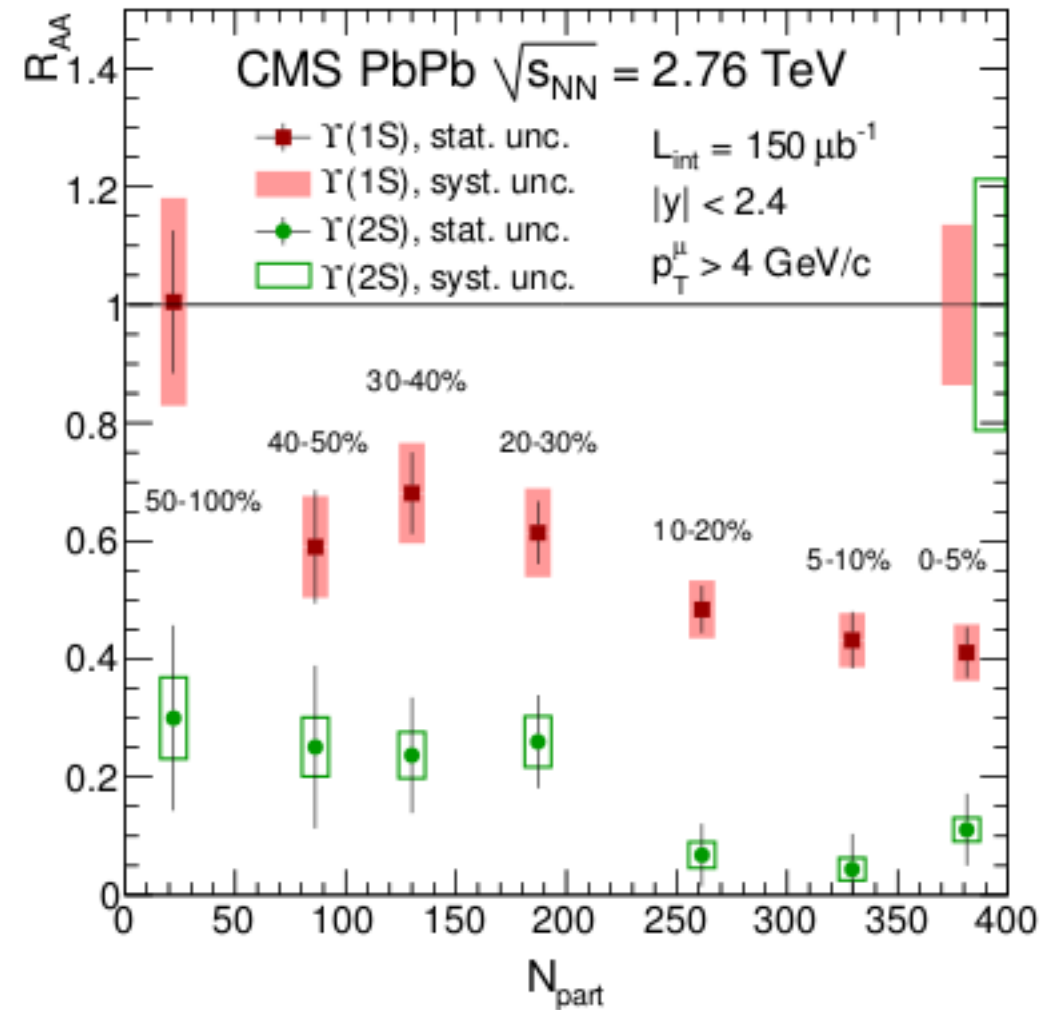
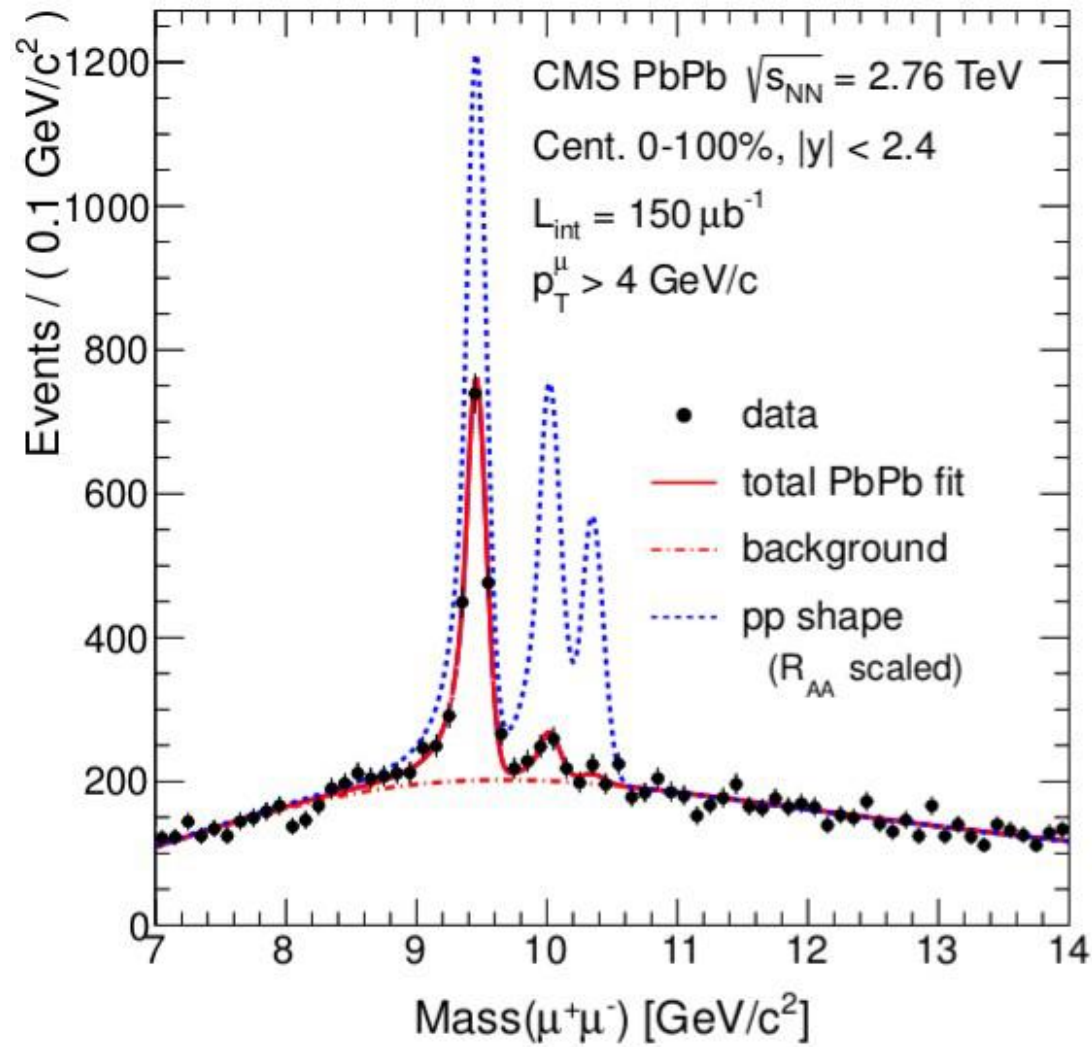
→ Signature of de-confinement.

[P. Braun-Munzinger, J. Stachel, Nature doi:10.1038/nature06080]



Suppression of Upsilon states

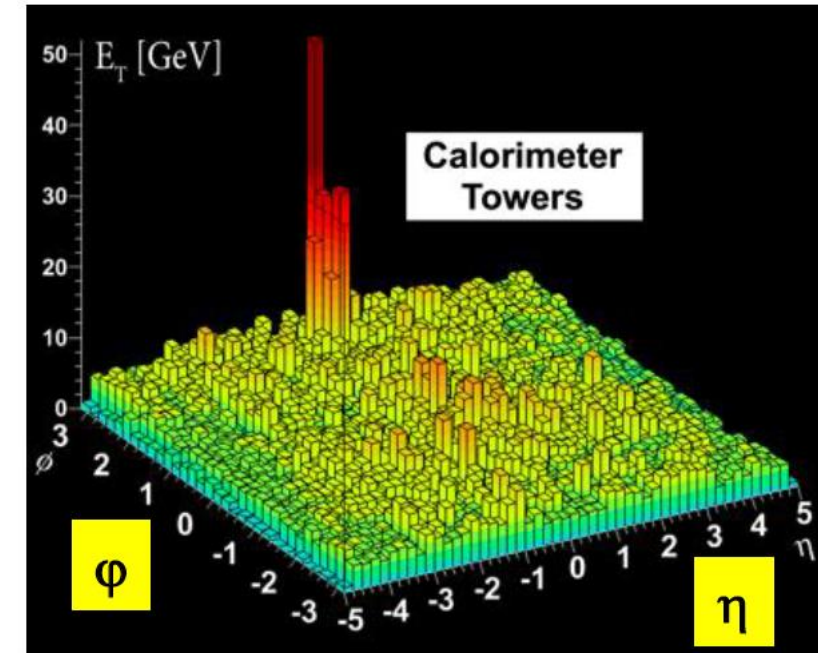
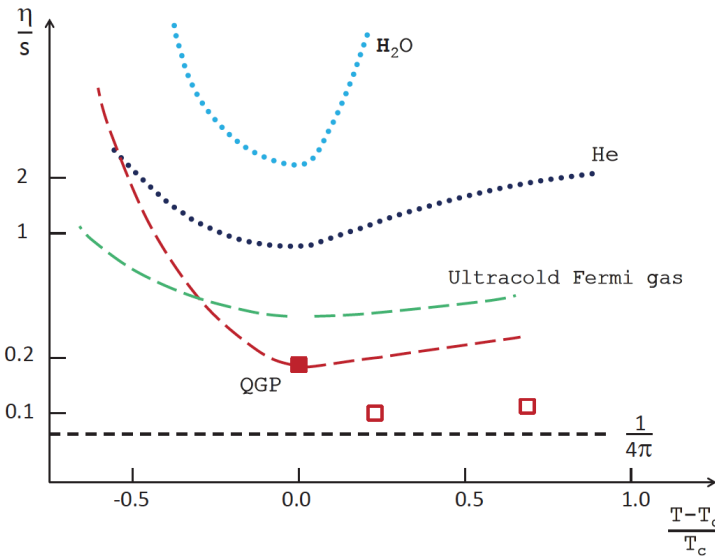
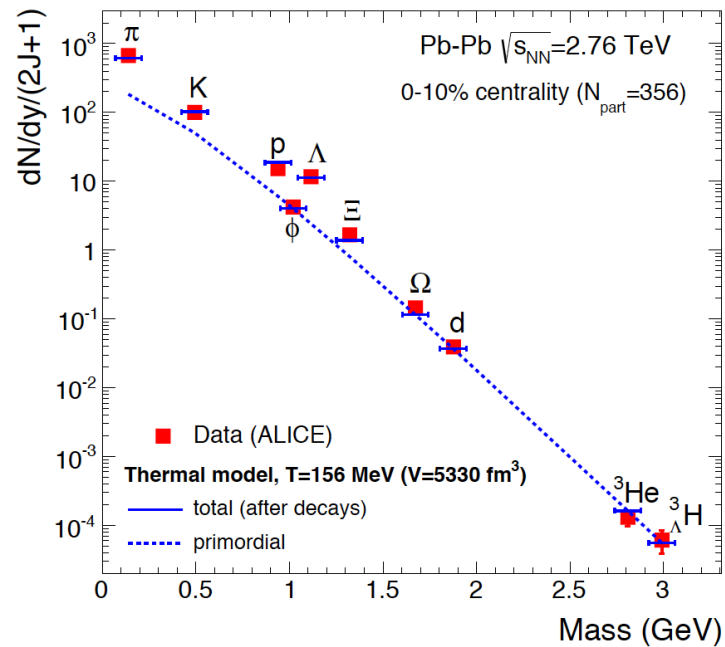
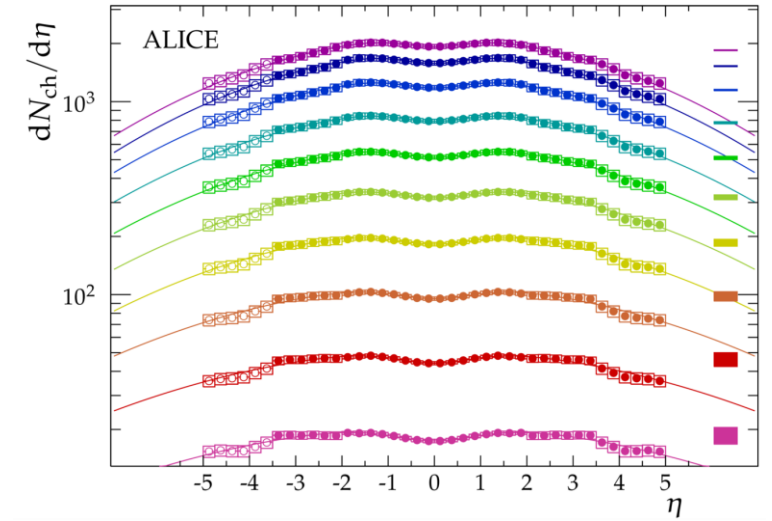
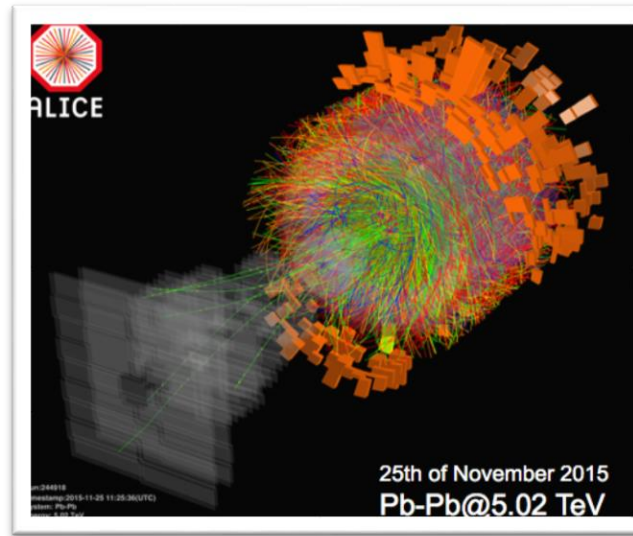
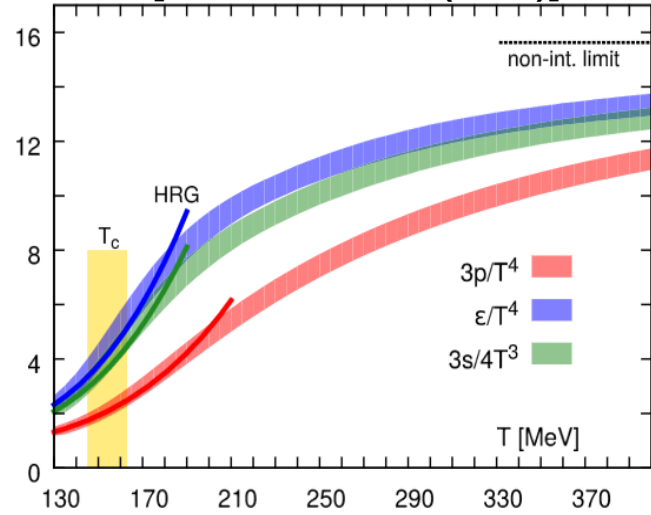
[PRL 109 (2012) 222301]



No re-generation for the much more rare b-quarks!
 Suppression of $\Upsilon(1S)$ ground, and excited $\Upsilon(2S)$ and $\Upsilon(3S)$ states.

Summary

[PRD 90 094503 (2014)]



Further reading

- Lectures
 - J. Stachel, K. Reygers (2011)
http://www.physi.uni-heidelberg.de/~reygers/lectures/2011/qgp/qgp_lecture_ss2011.html
 - P. Braun-Munzinger, A. Andronic, T. Galatyuk (2012)
http://web-docs.gsi.de/~andronic/intro_rhic2012/
 - Quark Matter Student Day (2014)
<https://indico.cern.ch/event/219436/timetable/#20140518.detailed>
- Books
 - C.Y. Wong, Introduction to High-Energy Heavy-Ion Collisions, World Scientific, 1994
<http://books.google.de/books?id=Fnxvrdj2NOQC&printsec=frontcover>
 - L. P. Csernai, Introduction to Relativistic Heavy-Ion Collisions, 1994 (**free as pdf**)
<http://www.csernai.no/Csernai-textbook.pdf>
 - E. Shuryak, The QCD vacuum, hadrons, and superdense matter, World Scientific, 2004
<http://books.google.de/books?id=rbcQMK6a6ekC&printsec=frontcover>
 - Yagi, Hatsuda, Miake, Quark-Gluon Plasma, Cambridge University Press, 2005
<http://books.google.de/books?id=C2bpxwUXJngC&printsec=frontcover>
 - R. Vogt, Ultrarelativistic Heavy-ion Collisions, Elsevier, 2007
<http://books.google.de/books?id=F1P8WMESgkMC&printsec=frontcover>
 - W. Florkowski, Phenomenology of Ultra-Relativistic Heavy-Ion Collisions, World Scientific, 2010
<http://books.google.de/books?id=4glp05n9lz4C&printsec=frontcover>