

# **Addendum to the IS608 Proposal**

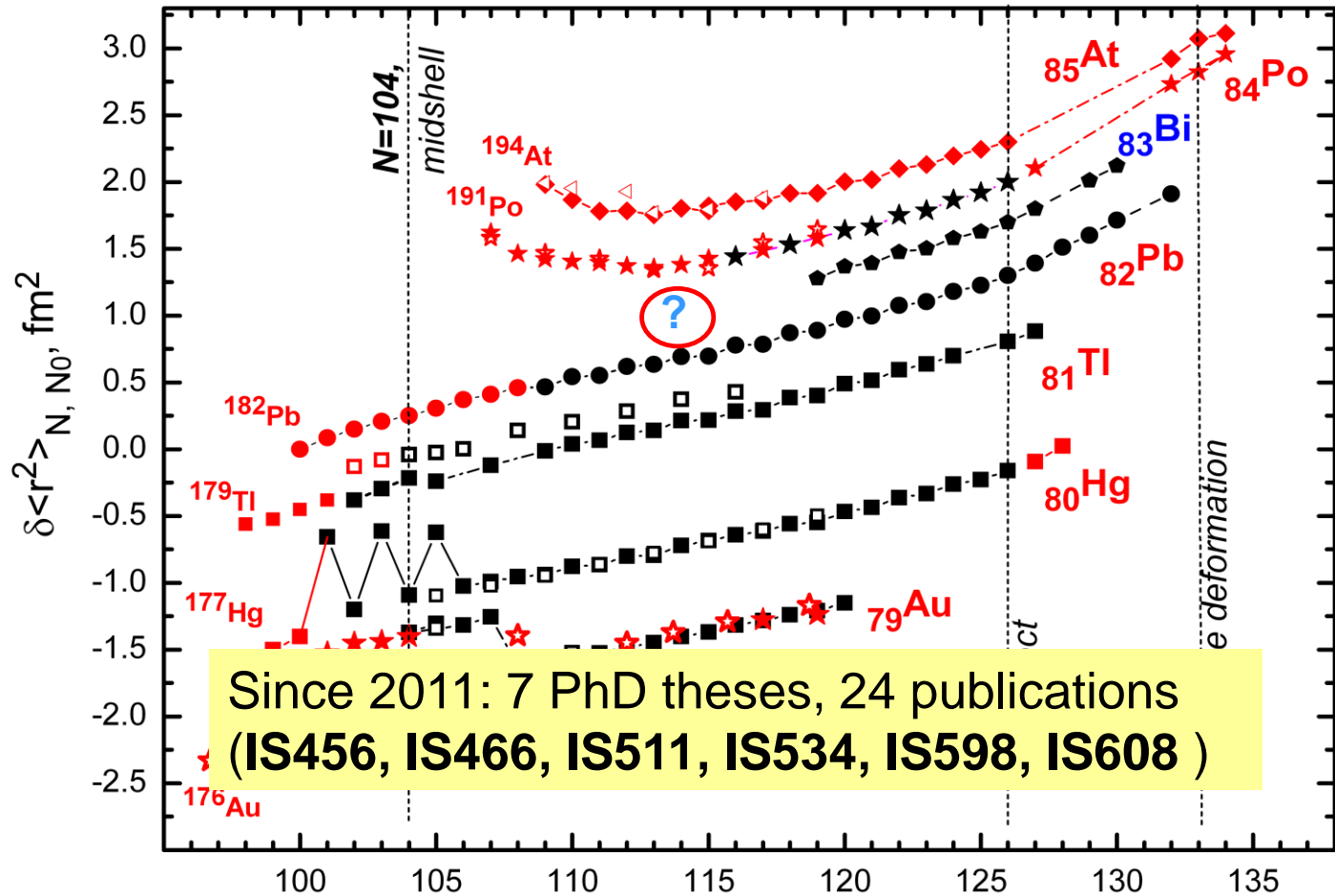
## **Shape-coexistence and shape-evolution studies for bismuth isotopes by in-source laser spectroscopy**

A. E. Barzakh

*on behalf of Leuven-Gatchina-ISOLDE-Mainz-Manchester-York  
and Windmill-ISOLTRAP-RILIS collaboration*

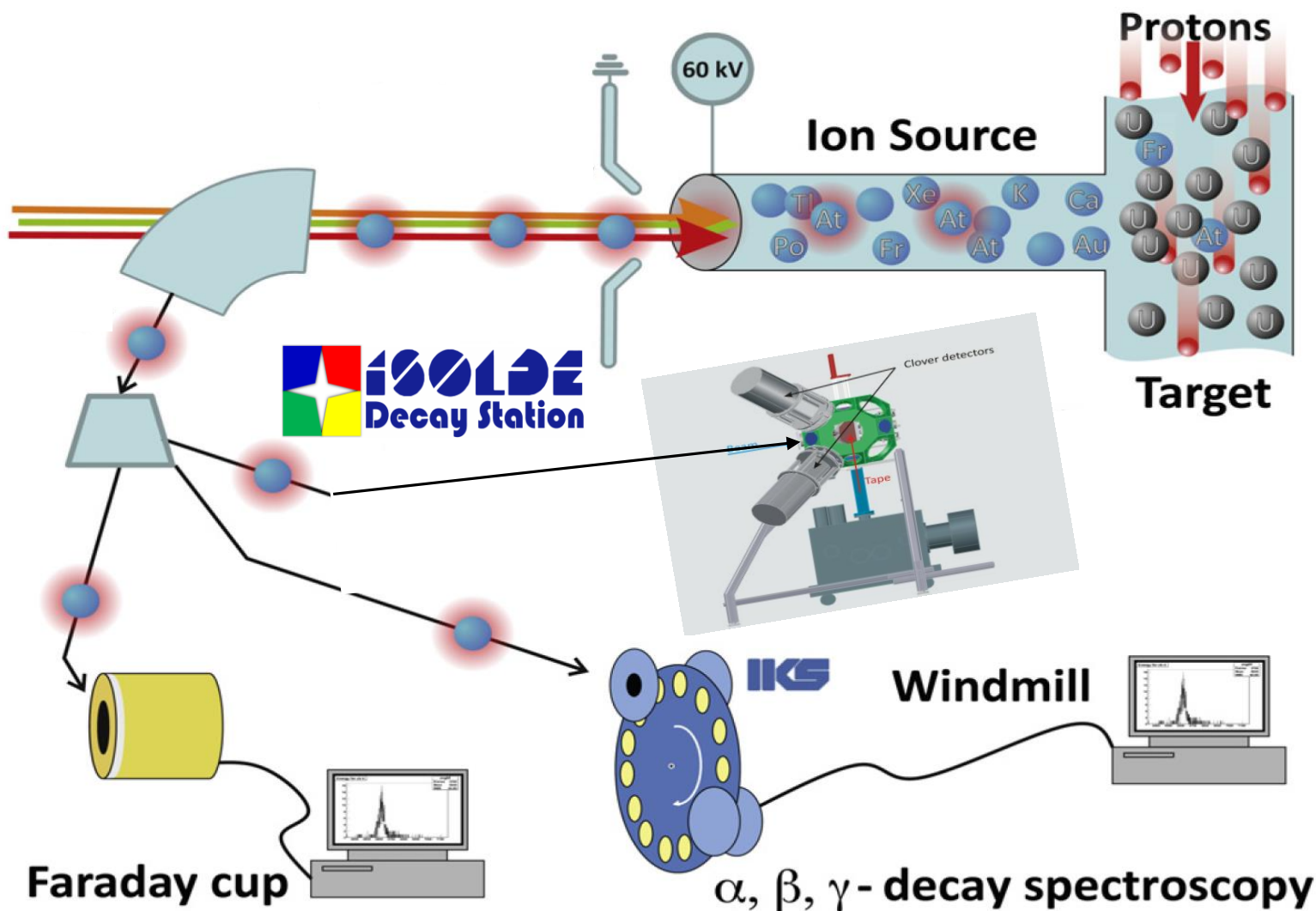
# Shape coexistence study in the Pb region

## Windmill-RILIS-ISOLTRAP Collaboration



red points mark nuclei studied by our collaboration

# ISOLDE: in-source spectroscopy

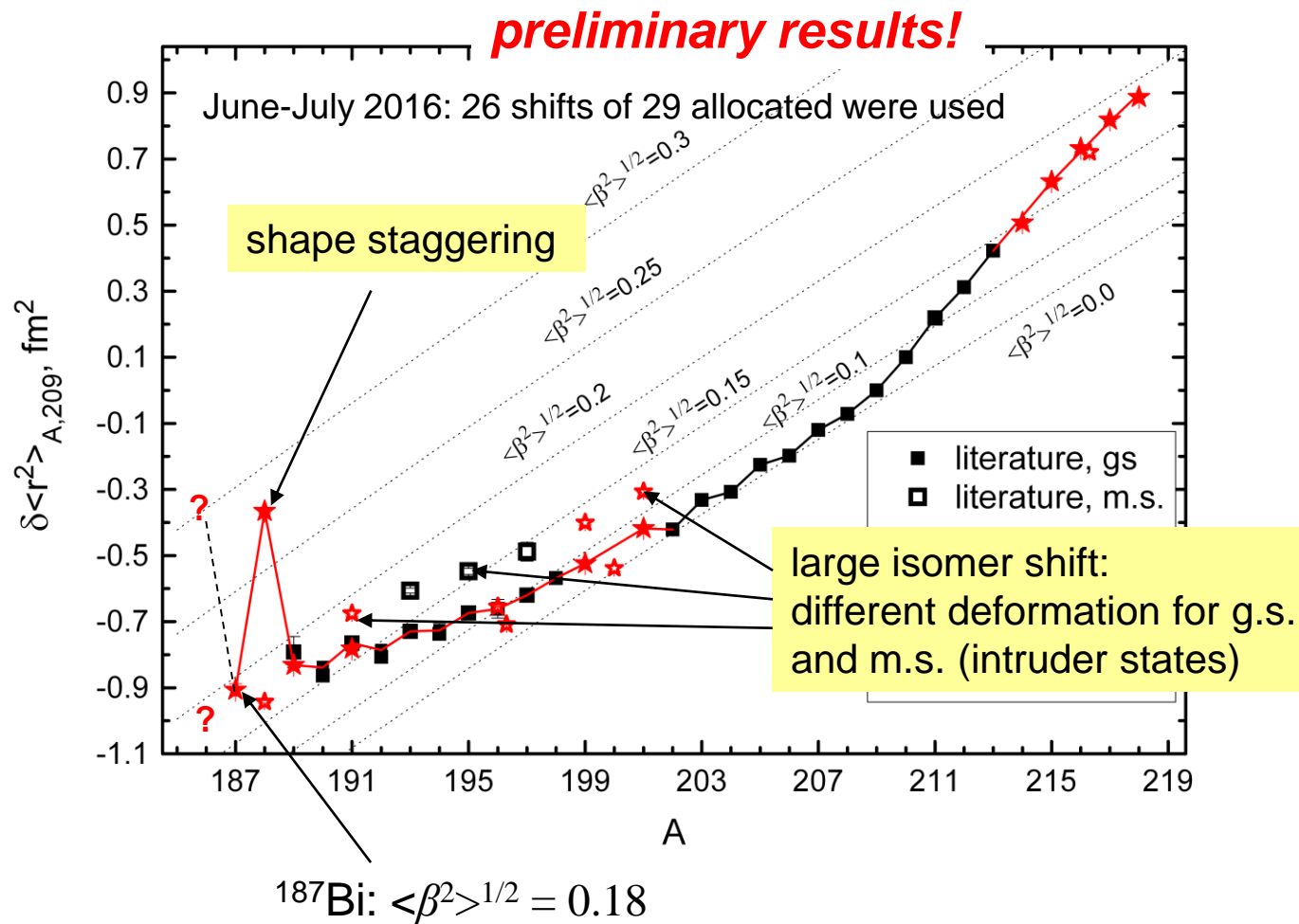


B. A. Marsh et al., 20013 EMIS conference, NIM B317, p.550 (2013)

**WM:** A.N. Andreyev et al, Phys. Rev. Lett 105, 252502 (2010)

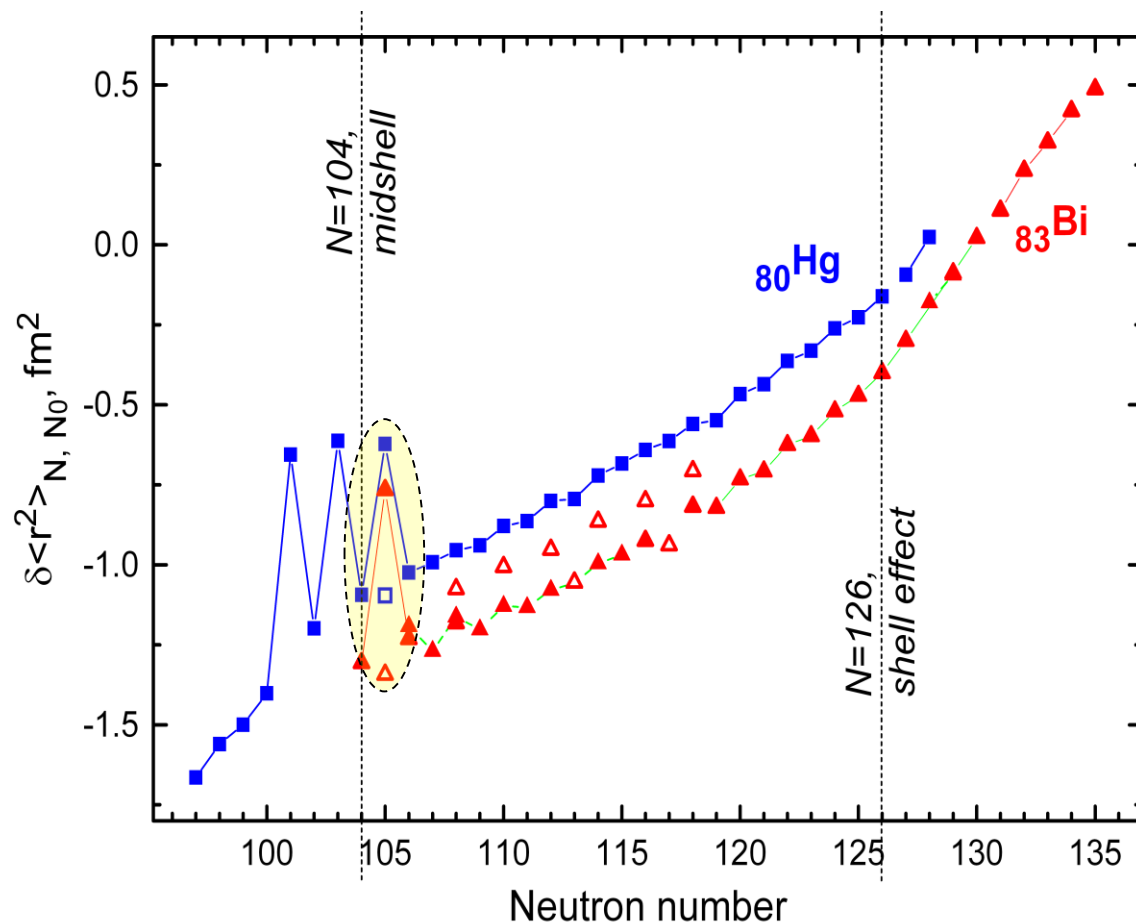
**MR-ToF MS:** R. N. Wolf et al, NIM, A686, 82 (2012)

# IS608, $_{83}\text{Bi}$ isotopes: radii



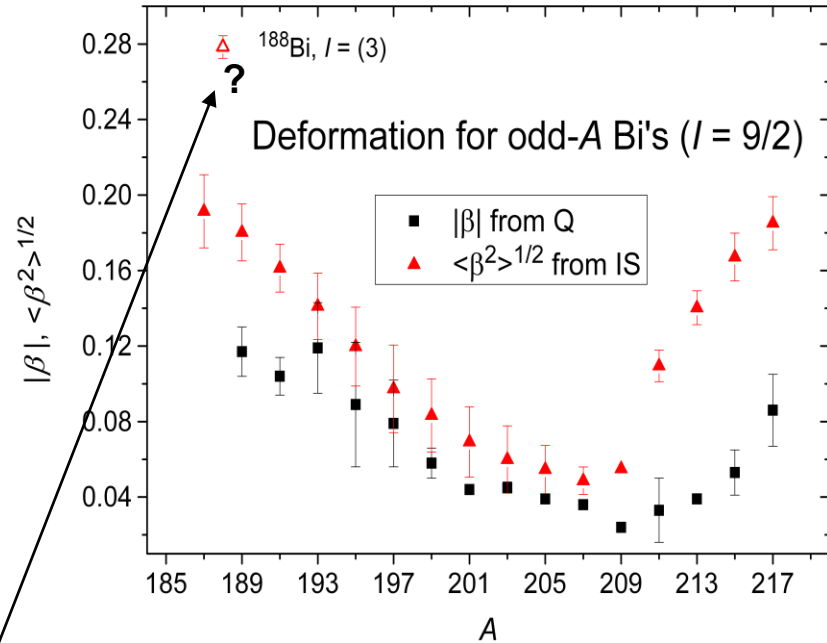
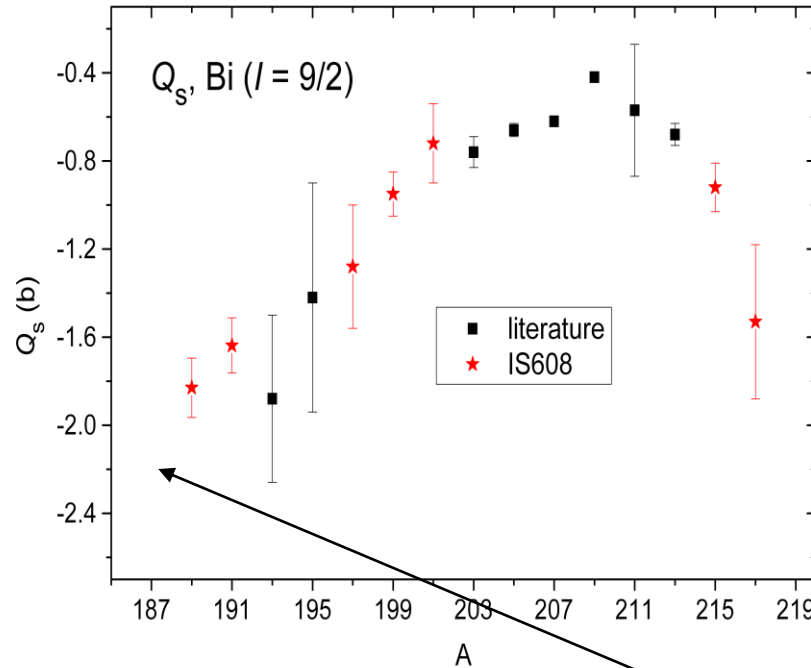
In contrast to previous conclusions on sphericity of the  $9/2^-$  g.s for the light Bi isotopes, based on decay and in-beam studies, a *gradual onset of deformation in the  $9/2^-$  gs of the lightest isotopes was deduced, up to  $\langle \beta^2 \rangle^{1/2} \sim 0.18$  in  $^{187}\text{Bi}$*

# Hg and Bi radii



In Bi, shape staggering occurs at the same  $N$  as in Hg ( $N = 105$ ), with the same amplitude and the same radii (deformation) difference between ground and  $vi_{13/2}$  based isomeric states.

# Bi quadrupole moments



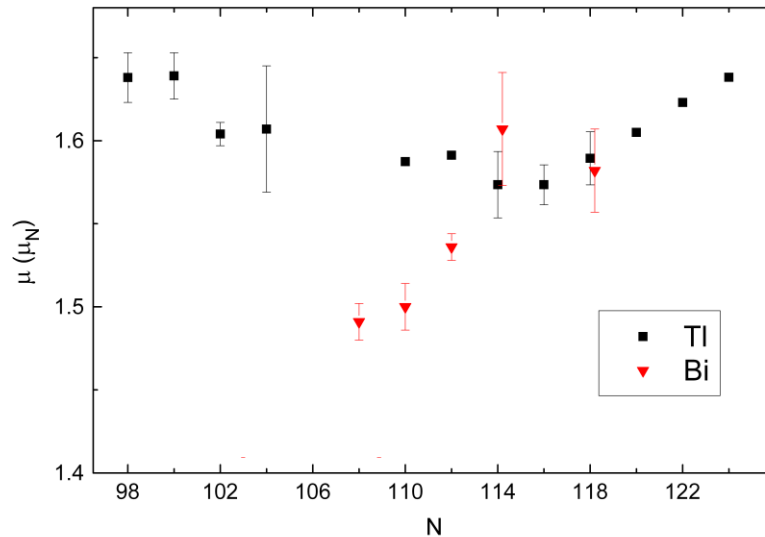
**We propose to measure  $Q(^{188,187,193,195}\text{Bi})$**

deformation for  $^{188}\text{Bi}$  and weak oblate deformation for  $^{187}\text{Bi}$  and  $^{195}\text{Bi}$ . Measurements of the quadrupole moments are needed to support this interpretation.

We also intend to decrease errors for  $Q$  in  $^{193}, ^{195}\text{Bi}$  measured previously at IRIS(Gatchina).

We did not succeed in measuring the quadrupole moments for  $^{187}, ^{188\text{m}1}, ^{188\text{m}2}\text{Bi}$  nuclei due to power broadening. With a reduced laser power to avoid saturation, the duration of a laser scan should be increased by a factor of two.

# Bi: intruders with $I^\pi = 1/2^+$



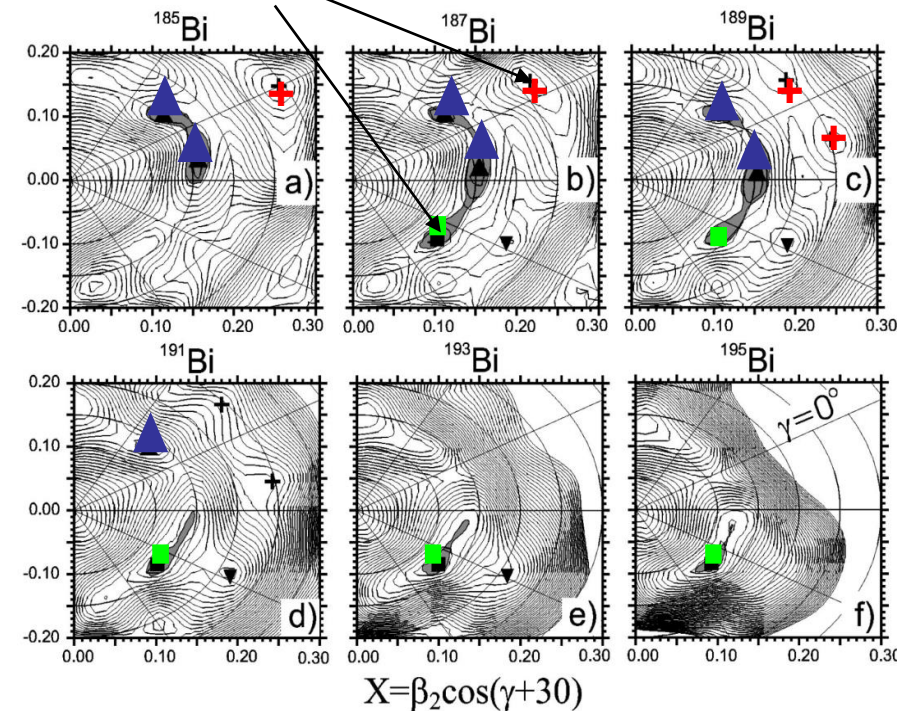
The  $\mu(1/2^+)$  for Bi intruder isomers starts to deviate from the “spherical” TI trend at  $N < 112$ .

A measurement of  $\mu(^{189}\text{Bi}^m)$  would be crucial in supporting/rejecting this interpretation.

## Positive parity states

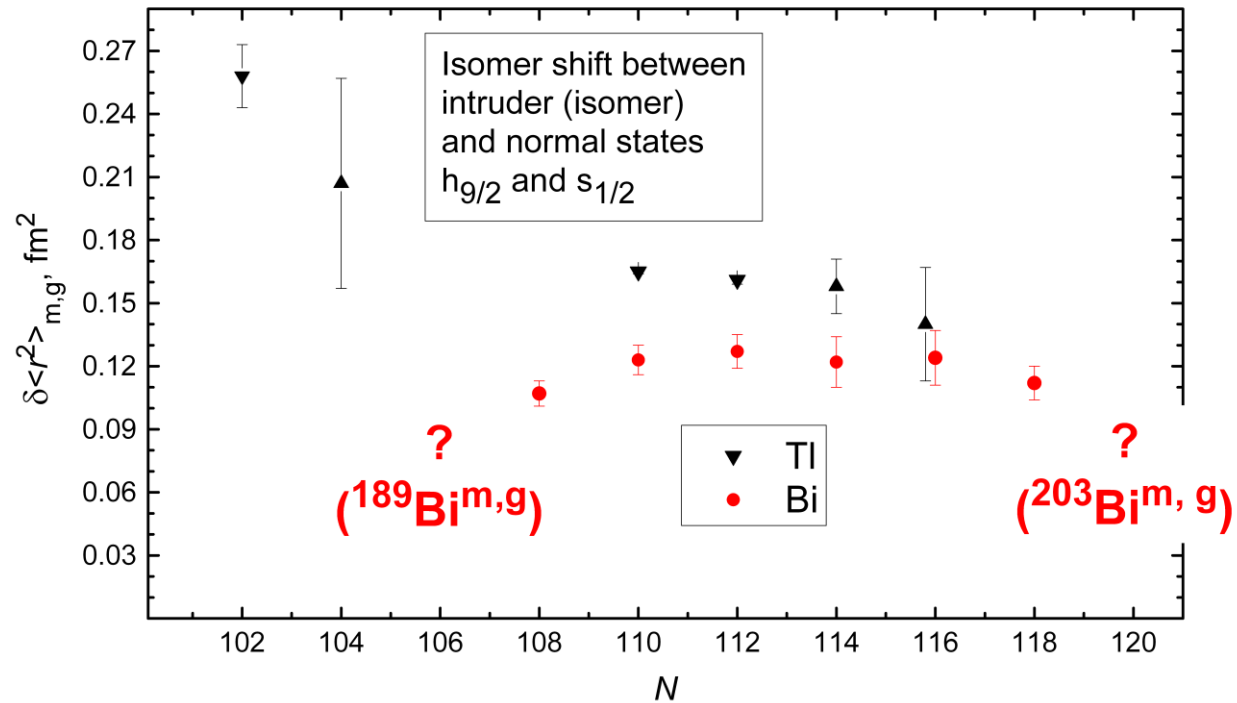
- ‘Oblate’ intruders  $I^\pi = 1/2^+$
- ▲, + ‘Prolate’ intruders  $I^\pi = 1/2^+$

two closely-spaced (oblate-prolate)  $1/2^+$  states are predicted



**We propose to measure  $\mu(^{189}\text{Bi}^m)$**

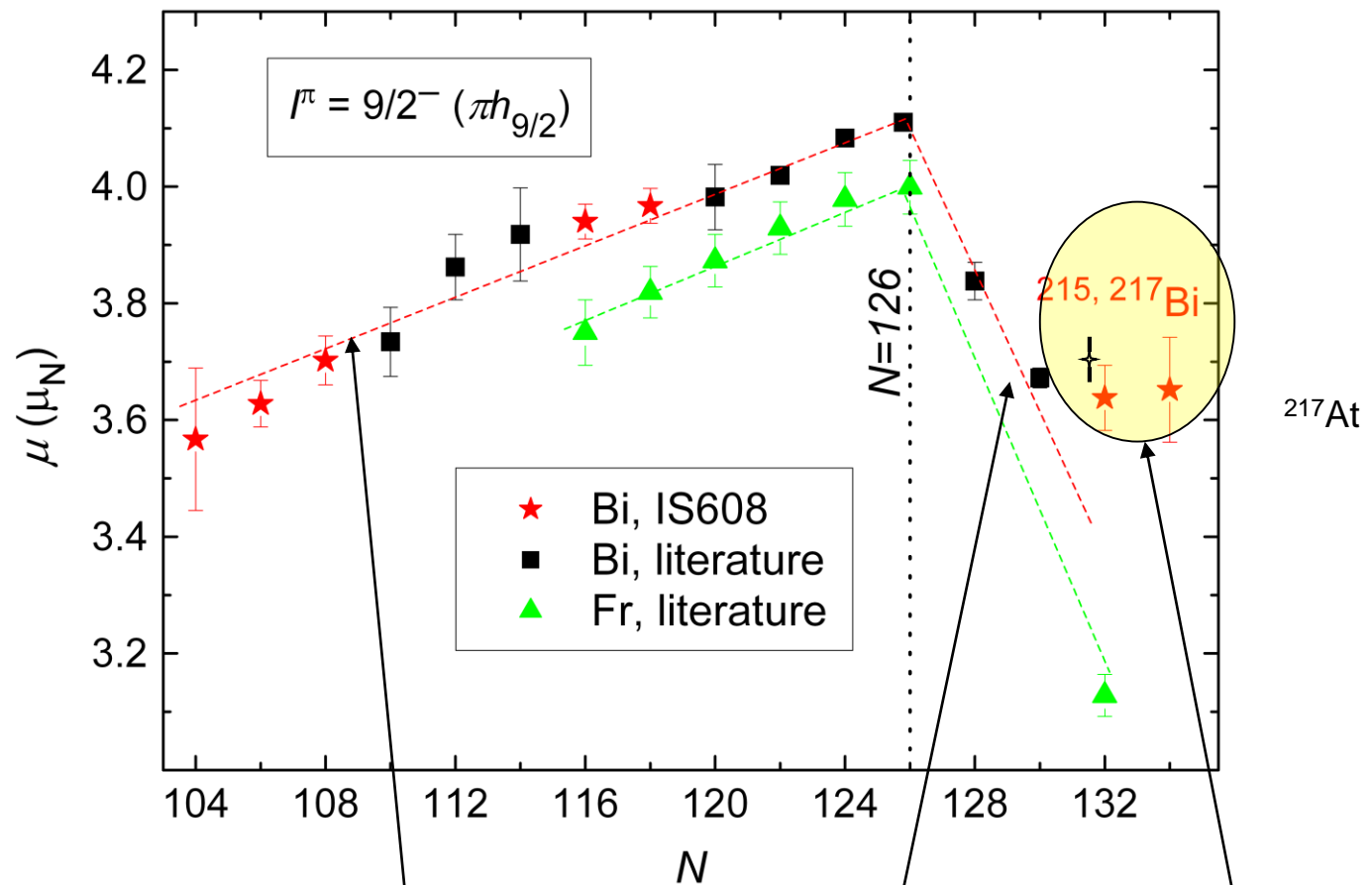
# Bi: intruders with $I^\pi = 1/2^+$



We propose to measure  $\delta \langle r^2 \rangle$  for  $^{189}\text{Bi}^m$ ,  $^{203}\text{Bi}^m$



# Bi: ground states $\mu$ ( $I^\pi = 9/2^-$ )



**We propose to measure  $\mu(^{219}\text{Bi})$**

deviation from systematics: octupole degree of freedom influence?

# odd-even staggering

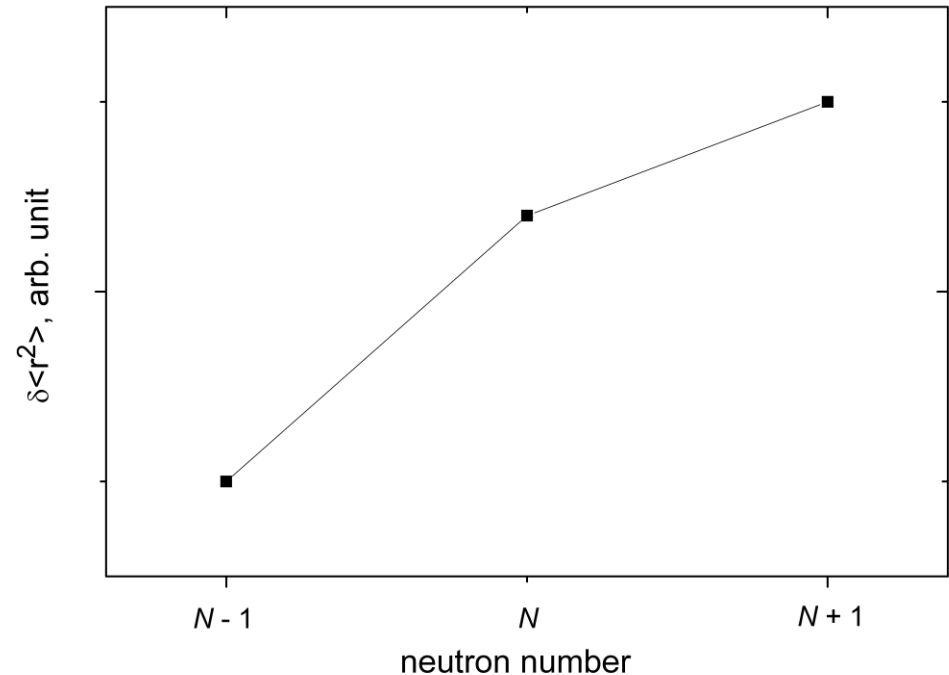
Octupole deformation correlates with the inverse radii staggering

staggering parameter:  $\gamma(N) = \frac{2 \cdot \delta \langle r_{N,N-1}^2 \rangle}{\delta \langle r_{N+1,N-1}^2 \rangle} \quad N \text{ — odd}$

$\gamma = 1$  — no staggering

$\gamma < 1$  — normal staggering

$\gamma > 1$  — inverse staggering



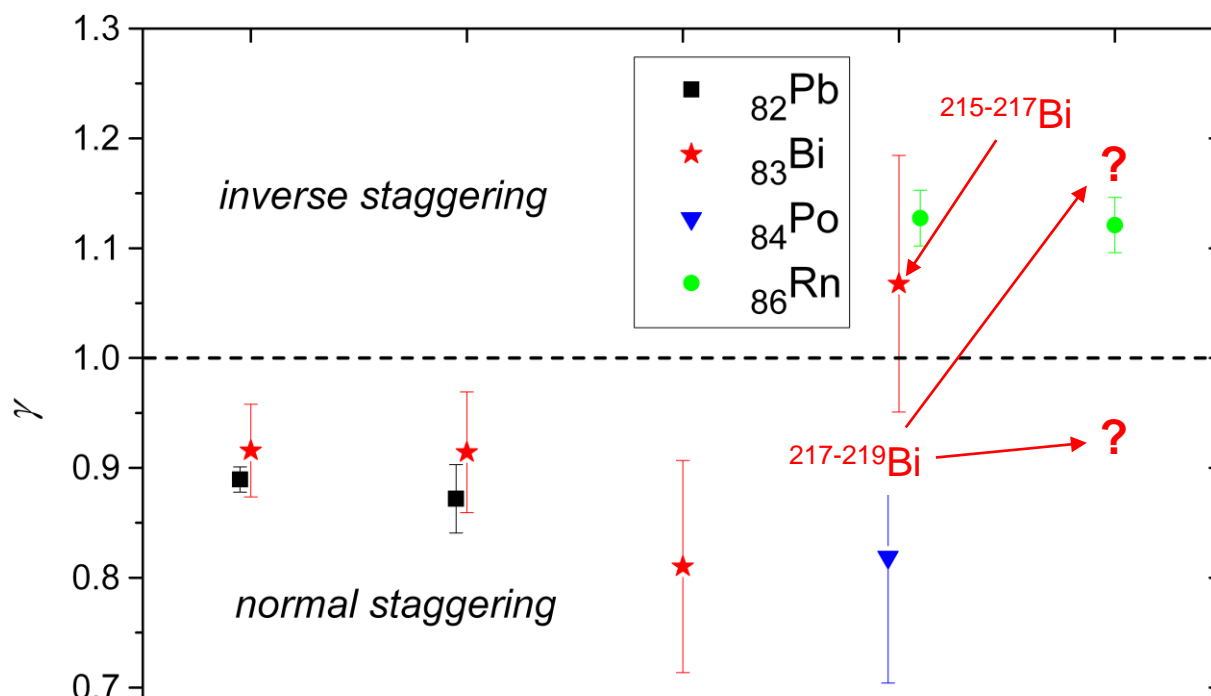
# Bi: odd-even staggering

staggering parameter:  $\gamma(N) = \frac{2 \cdot \delta \langle r_{N,N-1}^2 \rangle}{\delta \langle r_{N+1,N-1}^2 \rangle}$

$\gamma = 1$  — no staggering

$\gamma < 1$  — normal staggering

$\gamma > 1$  — inverse staggering



**We propose to measure  $\delta \langle r^2 \rangle(^{219}\text{Bi}) \rightarrow \gamma_{\text{Bi}}(135)$**

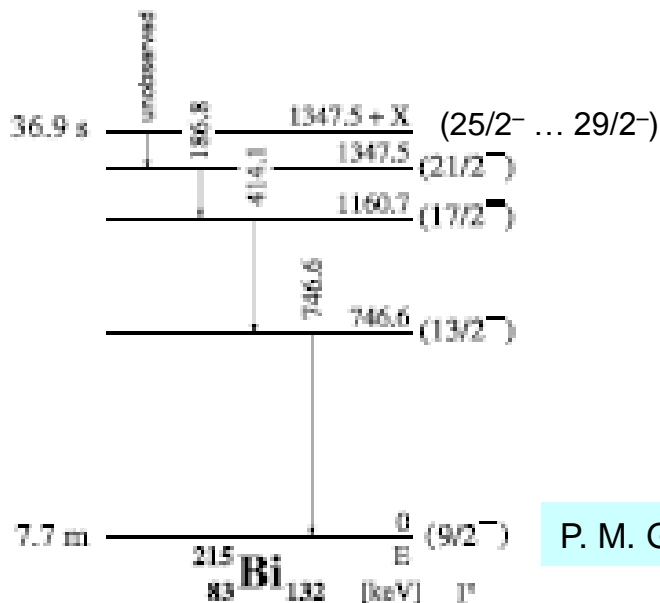
**and to decrease error for  $\gamma_{\text{Bi}}(133)$**

# Bi: high-spin isomers

**$^{212}\text{Bi}^{\text{m}1}$**  ( $\pi h_{9/2}, \nu g_{9/2}$ )<sub>8,9</sub> 239(30) keV,  **$^{212}\text{Bi}^{\text{m}2}$**  [ $\pi h_{9/2}, ((\nu g_{9/2})^2, \nu i_{11/2})$ ]<sub>18</sub> 1478(30) keV; L. Chen et al., PRL **110**, 122502 (2013) (Schottky Mass Spectrometry, GSI); unobserved IT branch of 75% is implied

**$^{213}\text{Bi}^{\text{m}}$**  [ $\pi h_{9/2}, (\nu g_{9/2}, \nu i_{11/2})$ ]<sub>25/2</sub> 1353(21) keV; L. Chen et al., Nucl. Phys. A **882** (2012) 71 (Schottky Mass Spectrometry, GSI);  $T_{1/2} > 168$  s; intensive IT branch

**We propose to measure  $\delta\langle r^2 \rangle$  (shell effect),  $\mu$  (configuration) and  $Q$  for  $^{212}\text{Bi}^{\text{m}1}$ ,  $^{212}\text{Bi}^{\text{m}2}$ ,  $^{213}\text{Bi}^{\text{m}}$ ,  $^{214}\text{Bi}^{\text{m}}$ ,  $^{215}\text{Bi}^{\text{m}}$  (with additional spectroscopic information:  $T_{1/2}$ , IT decay etc)**



According to the Hartree-Fock calculations the value of shell effect in radii is critically dependent on the occupancy of the neutron  $\nu i_{11/2}$  shell which is markedly changed for these high-spin isomers.

P. M. Goddard, P. D. Stevenson, and A. Rios. PRL, **110**, 032503, 2013

# Total beam request

A	I	$T_{1/2}$ , s	Yield, 1/ $\mu$ C	Method of measurement	time, shifts
219	(9/2)	22	$>3 \times 10^1$	IDS	1.5
217	(9/2)	98.5	$>3 \times 10^2$	IDS	0.5
215m	(29/2– 25/2)	36.9	$>1 \times 10^3$	IDS	1
214m	?	$>93$	$>1 \times 10^3$	IDS	1
213m	(25/2)	$>168$	$>1 \times 10^3$	IDS	1
212m1	(18)	420	$>1 \times 10^3$	IDS	1
212m2	(8,9)	1500	$>1 \times 10^3$	IDS	1
203m	1/2	0.305	$1.9 \times 10^6$	IDS	0.5
195	(9/2)	183	$1.4 \times 10^7$	IDS	0.5
193	(9/2)	63.6	$3 \times 10^6$	IDS	0.5
189m	(1/2)	0.005	1	WM	2.5
188m1 188m2	(3)	0.06	20	WM	1.5
	(10)	0.265	$10^2$	WM	
187g	(9/2)	0.037	0.3	WM	2.5

Yields were estimated using the observed during the IS608 run count rates with the known/extrapolated isomer ratios.

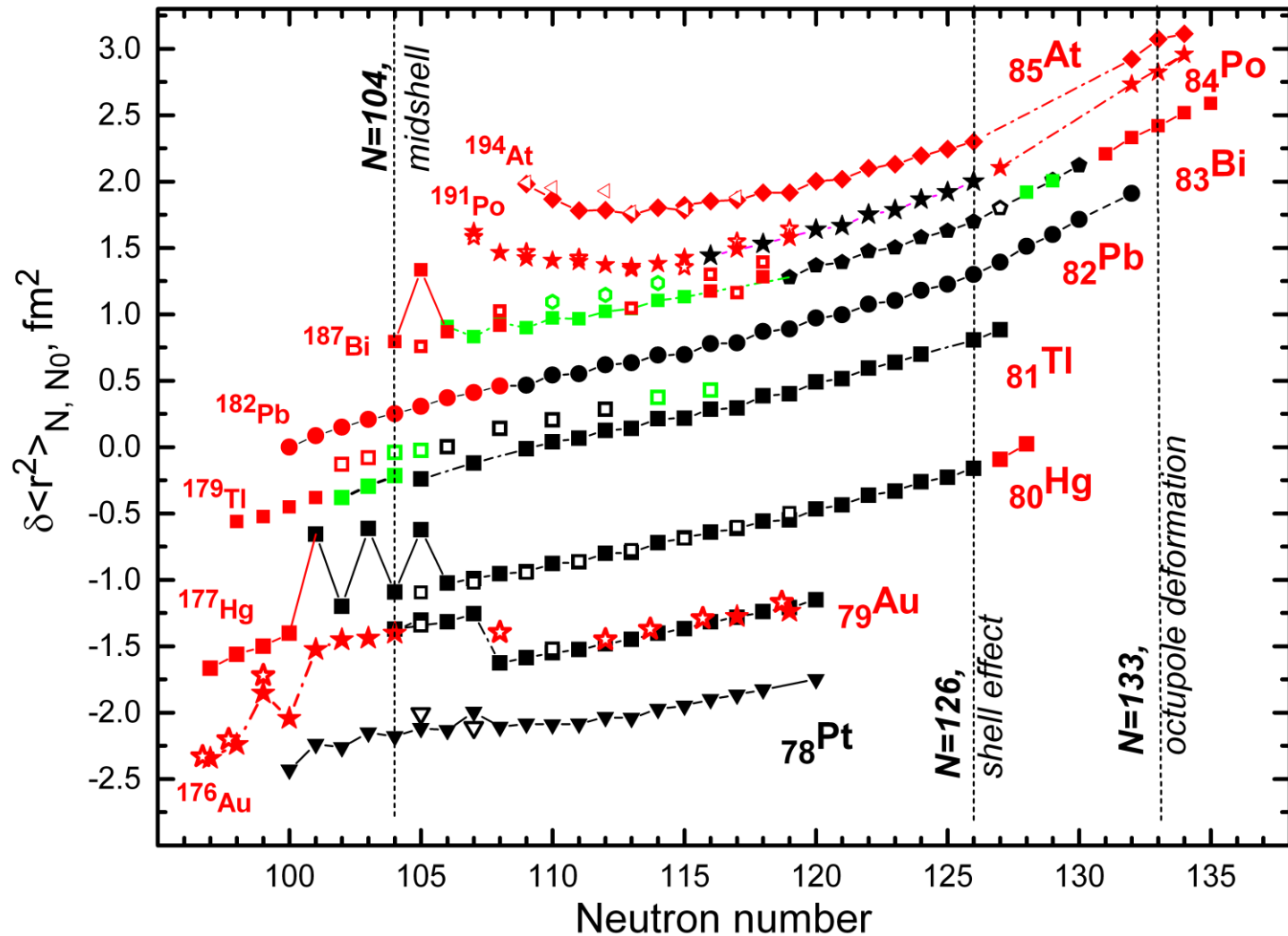
Thallium contaminants for  $A = 187-191$  were not a problem during the IS608 run.

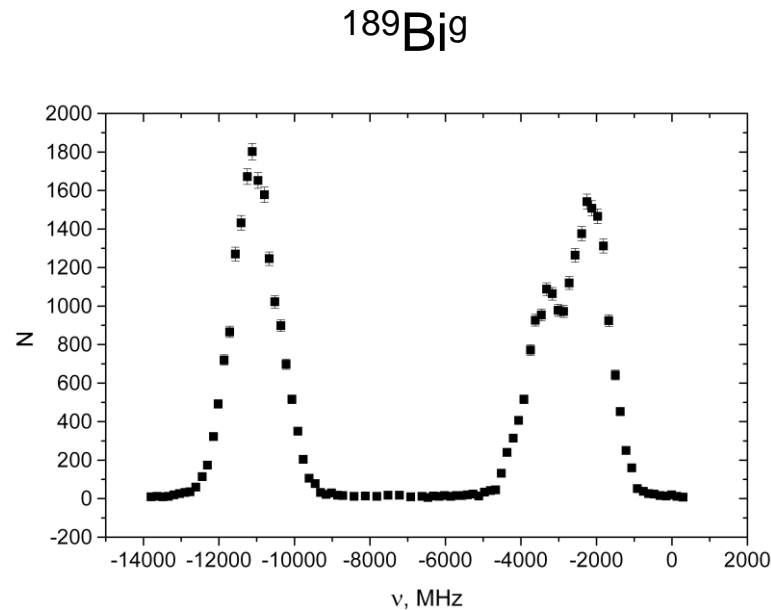
Measurements for  $A = 203$  are planned at IDS by IT gamma transition monitoring. Thus, stable  $^{203}\text{Tl}$  will not disturb these measurements.

$^{214}\text{Ra}$  and daughter  $^{210}\text{Rn}$  have weak beta-decay branches (0.06% and 4%). The overall contaminant gamma intensity will not exceed  $10^3$  1/s which is comparable with the expected Bi gamma lines intensity (IDS).

**In total, 16 Shifts are requested for Bi IS/hfs studies. By accounting for 3 remaining shifts from IS608, the present beam-time request is 13 shifts**

# Shape coexistence study in the Pb region





The similar estimation for  $^{191}\text{g}$ ,  $^{191\text{m}}\text{Bi}$  was checked during the IS608 run

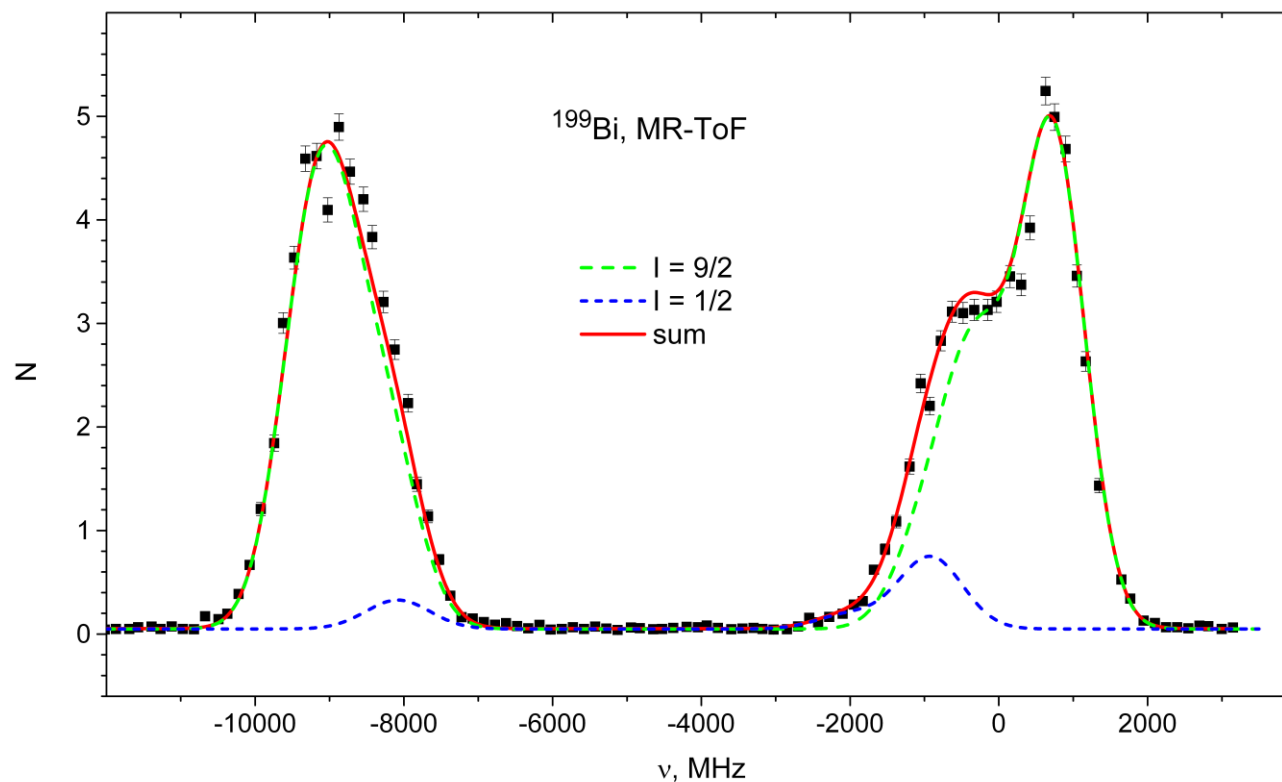
$$^{189}\text{Bi}^{\text{g}}: T_{1/2}=658 \text{ ms}, t_{\text{coll}}=1 \text{ SC}, I_{\text{max}}(^{189}\text{Bi}^{\text{g}})=1800$$

$$^{189}\text{Bi}^{\text{m}}: T_{1/2}=5 \text{ ms}, \text{ isomer ratio } R \sim 6, \\ \text{relative decay losses } L \sim (T_{1/2}(^{189}\text{Bi}^{\text{g}})/T_{1/2}(^{189}\text{Bi}^{\text{m}})) = 130 \\ t_{\text{coll}} = 9 \text{ SC}$$

$$I_{\text{max}}(^{189}\text{Bi}^{\text{m}}) = I_{\text{max}}(^{189}\text{Bi}^{\text{g}}) / R / L * t_{\text{coll}} = 20$$

60 points ~ 7 hours

# Isomers: MR-ToF vs IDS



In MR-ToF mode the isomer hfs is buried under the gs hfs.  
Keeping in mind small isomer ratio ( $\sim 0.1$ ) it is preferable to use IT transitions  
at IDS to obtain pure isomer hfs

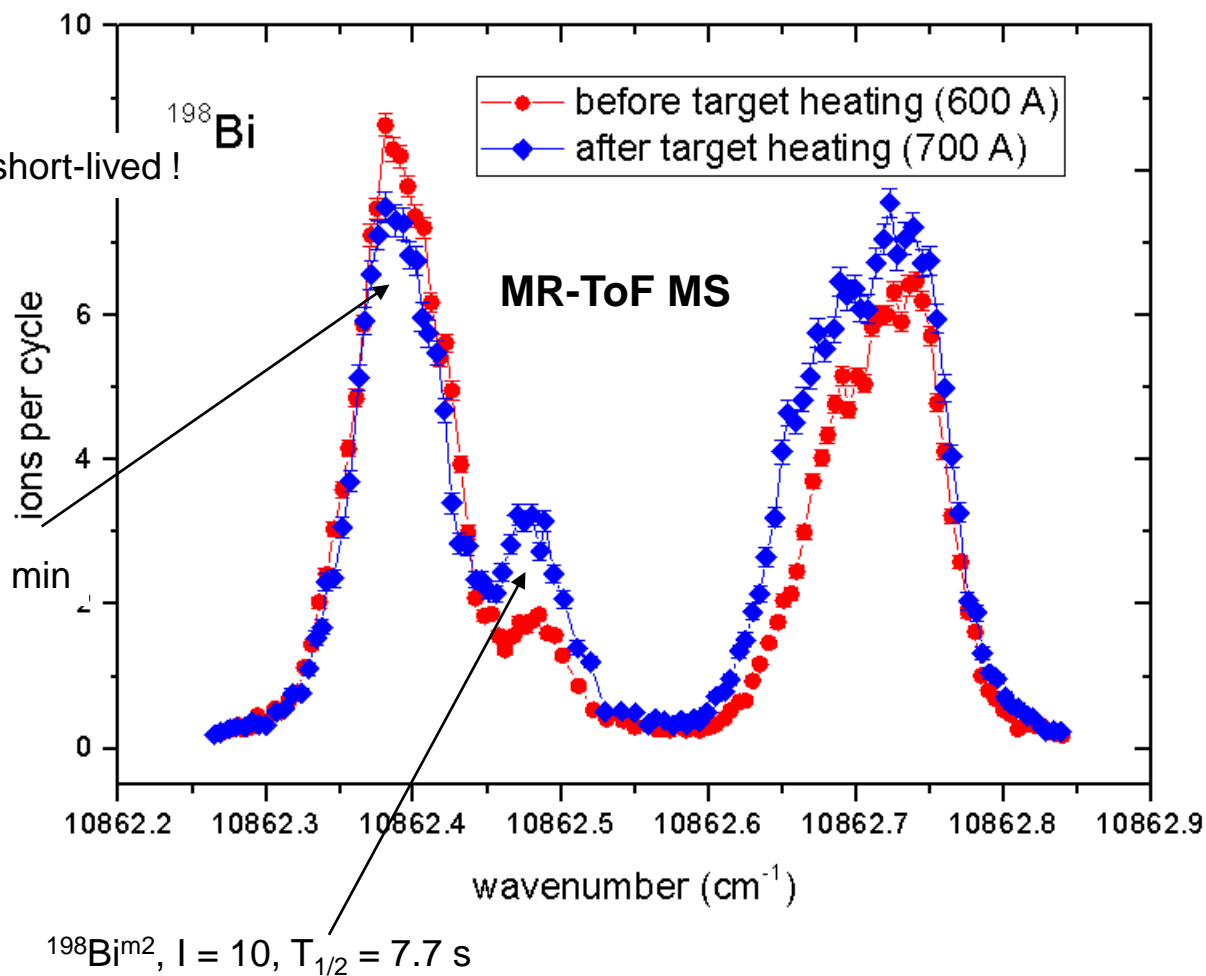


# Target temperature

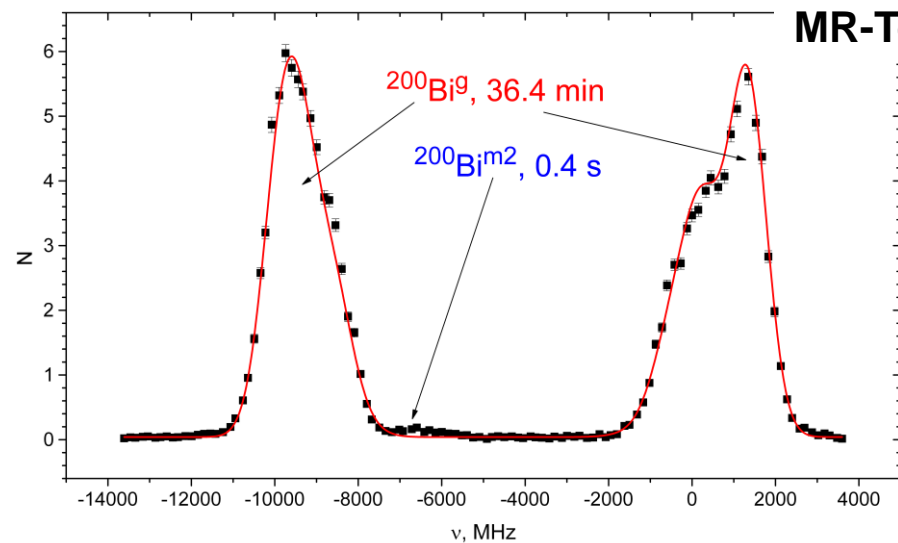
1940°  $\Rightarrow$  2200°

3 times increase for the short-lived !

$^{198}\text{Bi}^{\text{m}1}$ ,  $I = 7$ ,  $T_{1/2} = 11.6$  min



# Target temperature

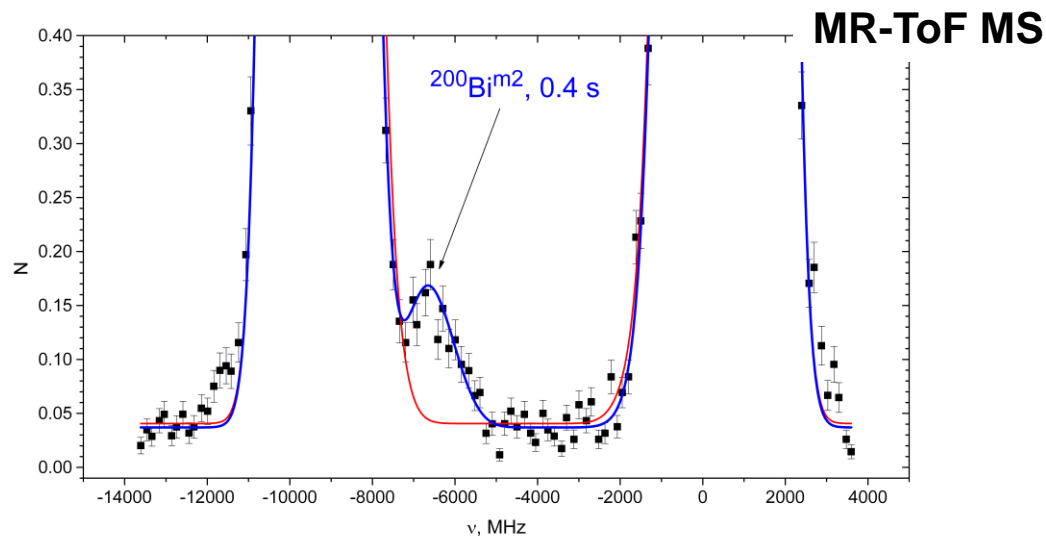


$$Y(^{200}\text{Bi}^g) / Y(^{200}\text{Bi}^{m2}) = 40$$

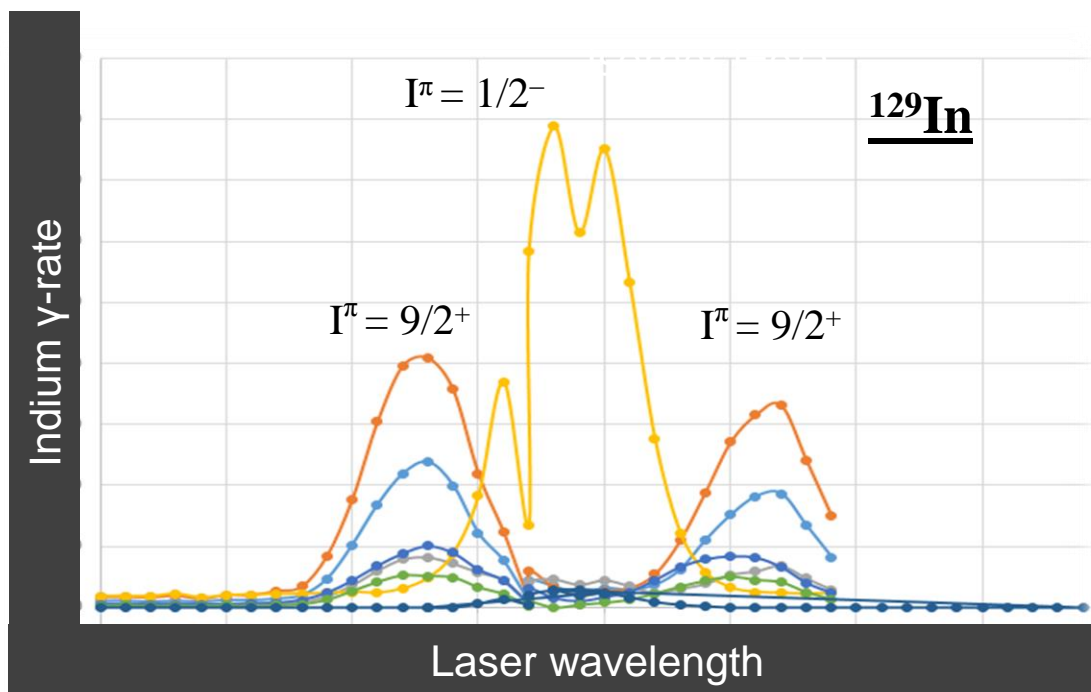
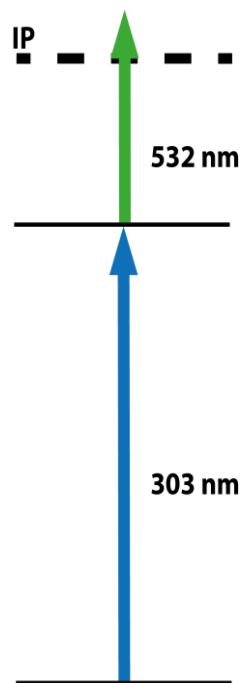
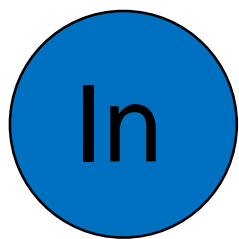
for completely similar  $^{198}\text{Bi}$ :

$$Y(^{198}\text{Bi}^g) / Y(^{198}\text{Bi}^{m2}) = 4$$

more than order of magnitude decay losses due to low target temperature!

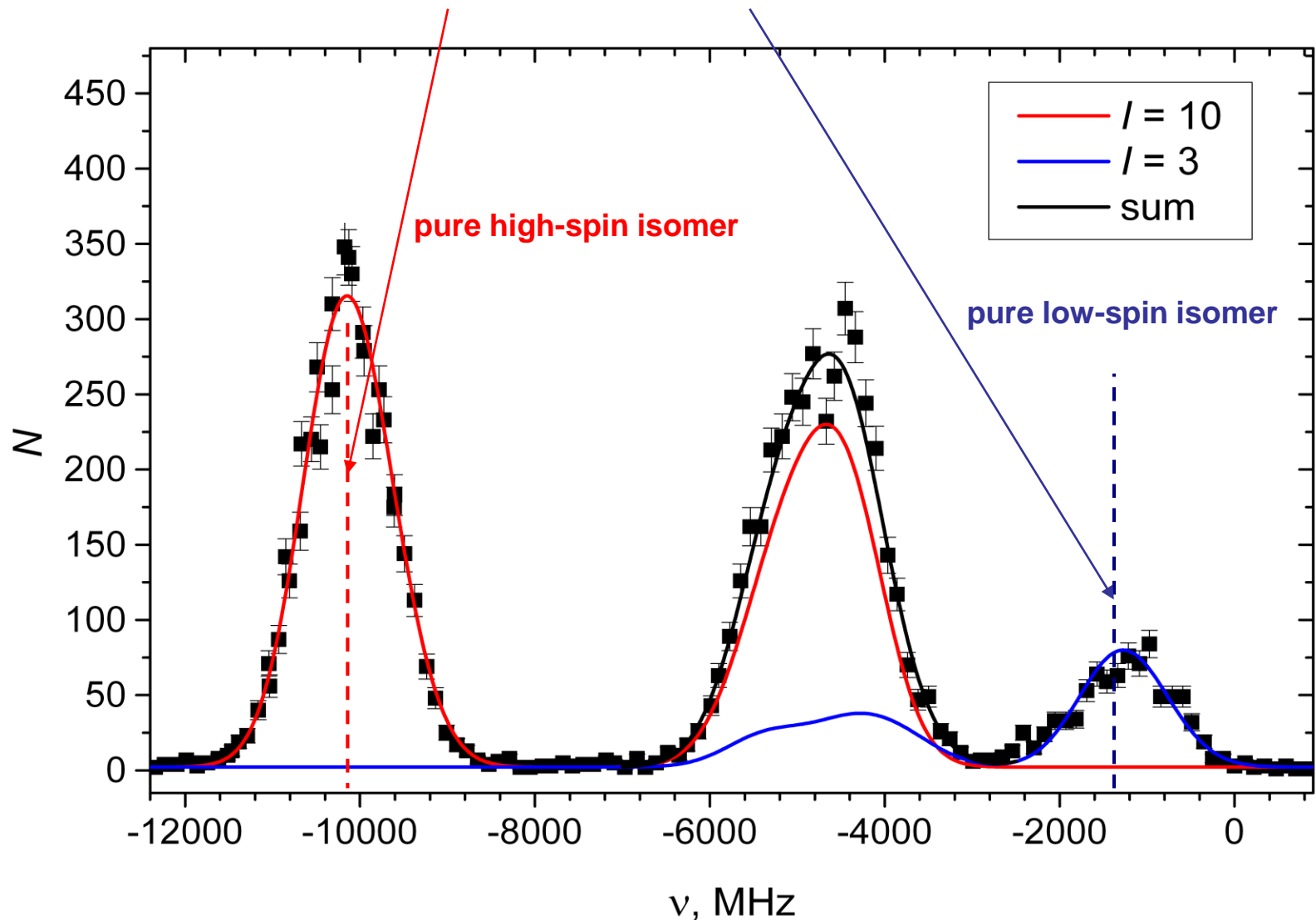


# First RILIS-IDS hfs scan

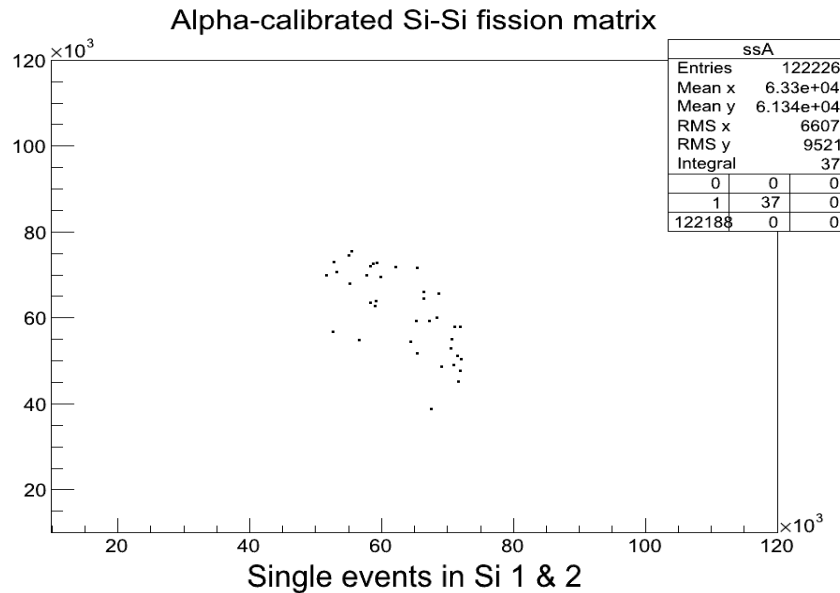


# $^{188}\text{Bi}$ : Isomer selective beta delayed fission

at these frequencies we obtain at the exit of the mass-separator...

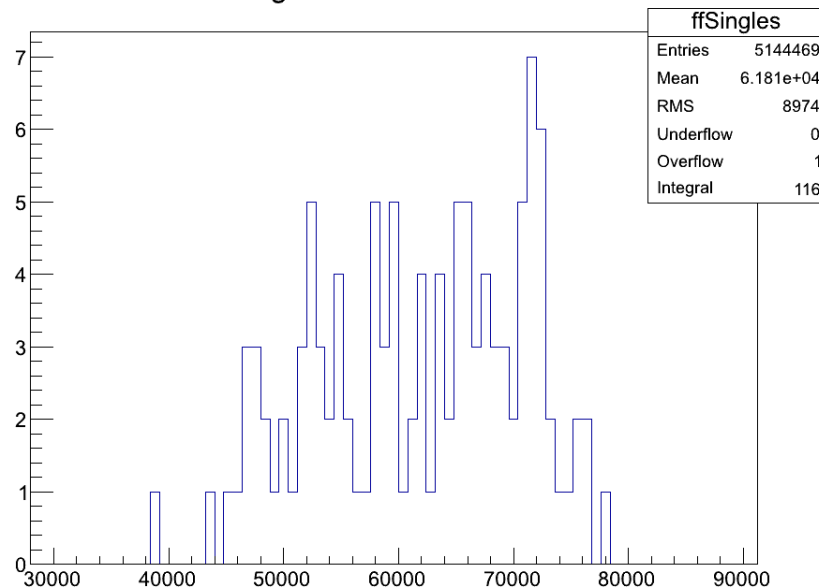


# $^{188}\text{Bi}$ : Isomer selective beta delayed fission

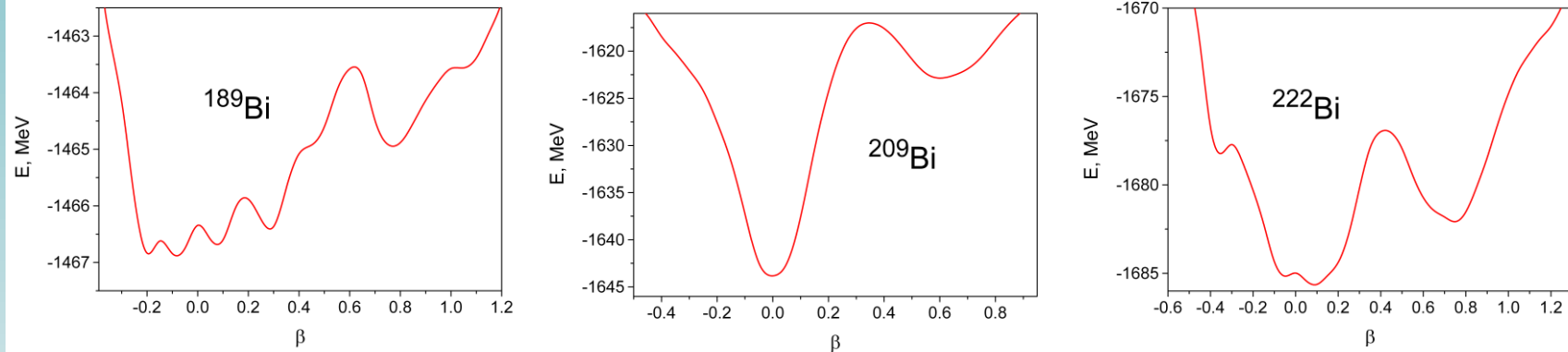


$$P_{\text{bDF}}(^{188}\text{Bi}, I = 10) = 6.0(1.7) \cdot 10^{-4}$$

Fission fragment mass distribution is similar to that for  $^{196}\text{At}$  where multimodal fission was found.



# A reminder on the underlying physics phenomena

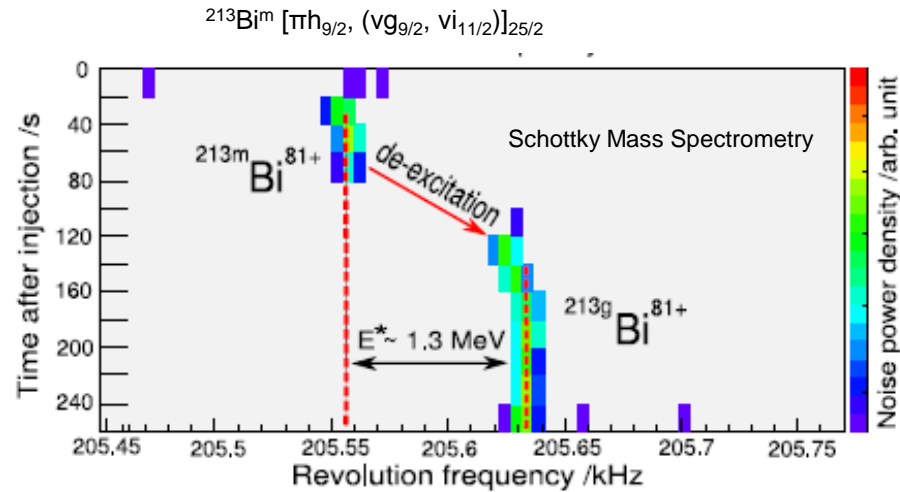


Potential energy curves for  $^{189}, ^{209}, ^{222}\text{Bi}$  calculated in HFB approach with Gogny forces D1S

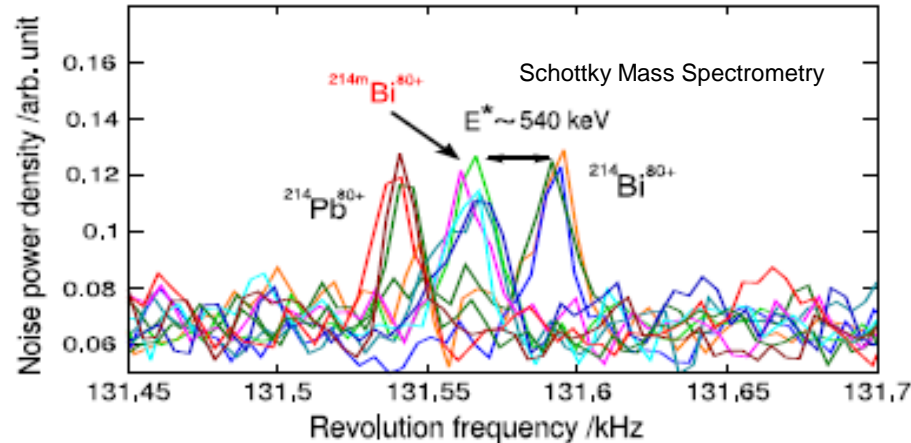
A gradual transition to deformed configurations is expected when moving towards either neutron-deficient or neutron-rich Bi isotopes

Many-minima picture was obtained for the  $^{187}, ^{188}\text{Bi}$ , where the competition of at least four minima at oblate/prolate sides takes place.

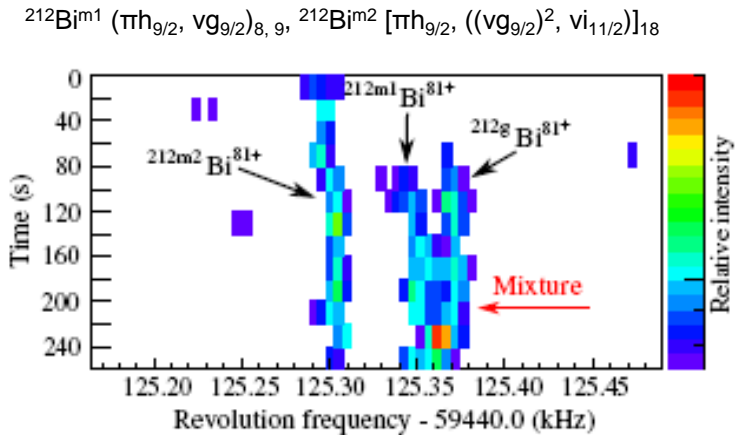
# Bi: high-spin isomers



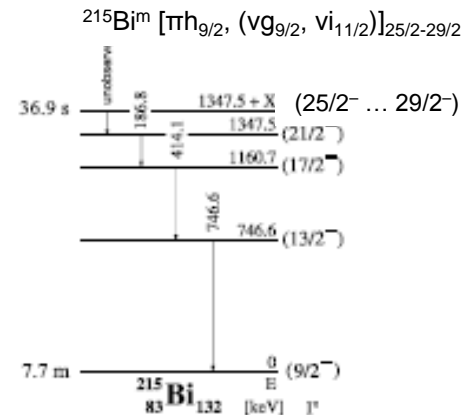
L. Chen et al., Nucl. Phys. A 882 (2012) 71  
 $T_{1/2} > 168 \text{ s}$ ; intensive IT branch



$T_{1/2} > 93 \text{ s}$

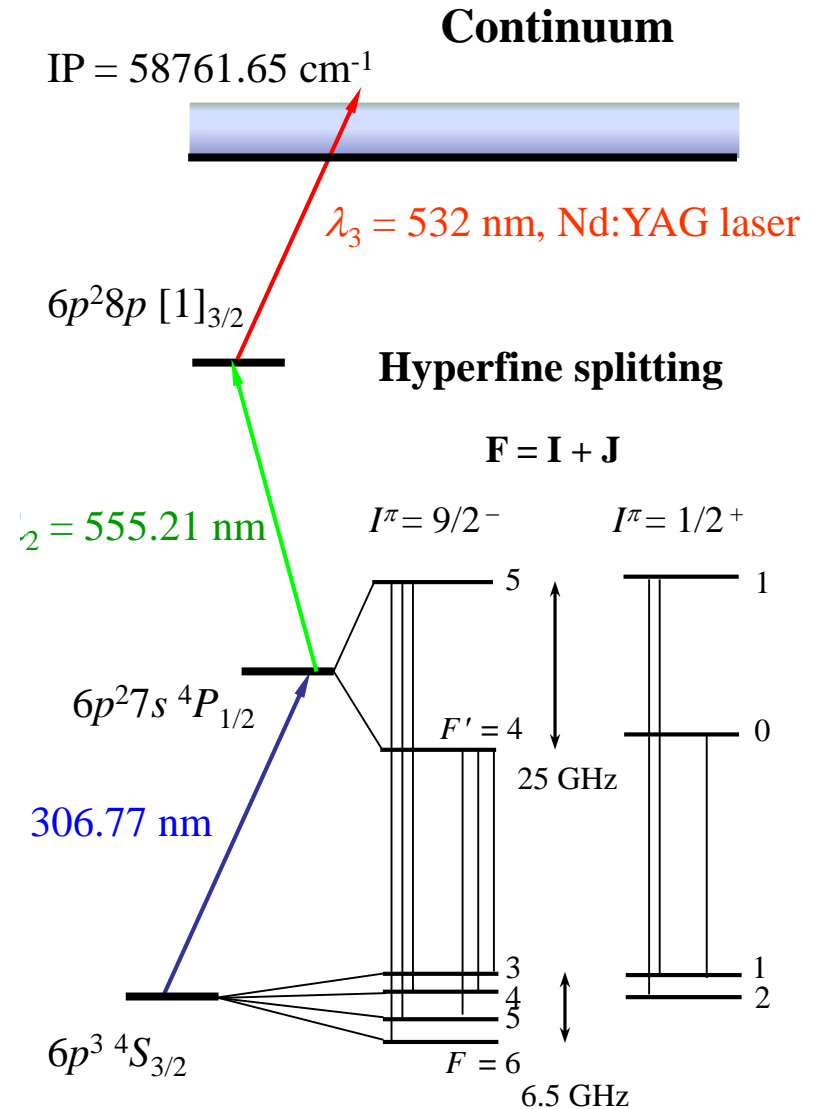
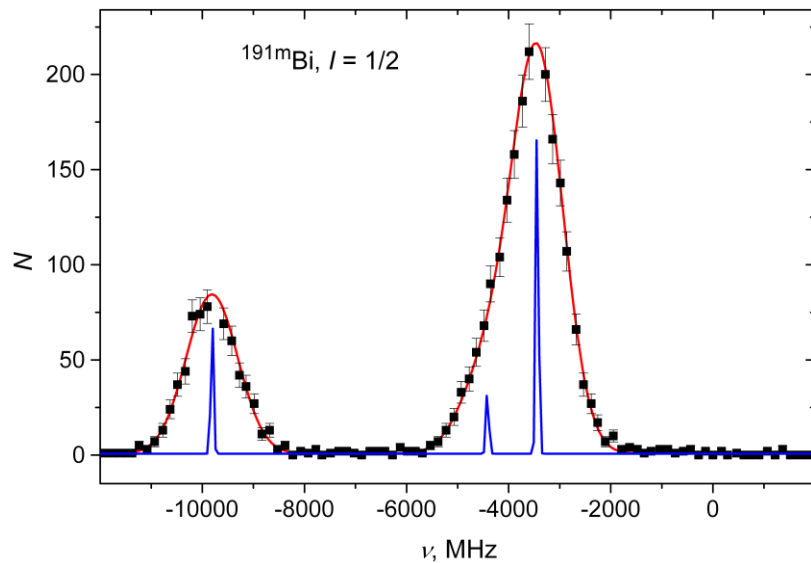
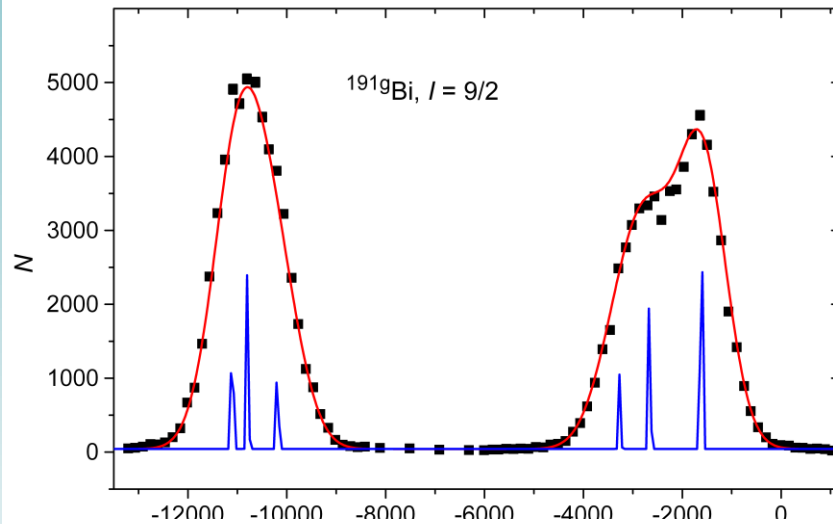


L. Chen et al., PRL 110, 122502 (2013);  
 unobserved IT branch of 75% is implied



J. Karpeta et al., Eur. Phys. J. A 18, 31 (2003)

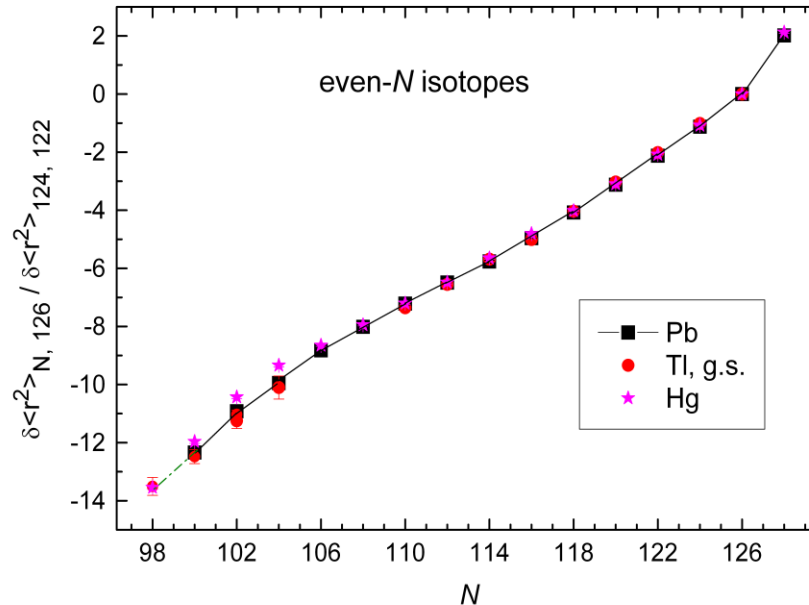
# Bi: hfs spectra



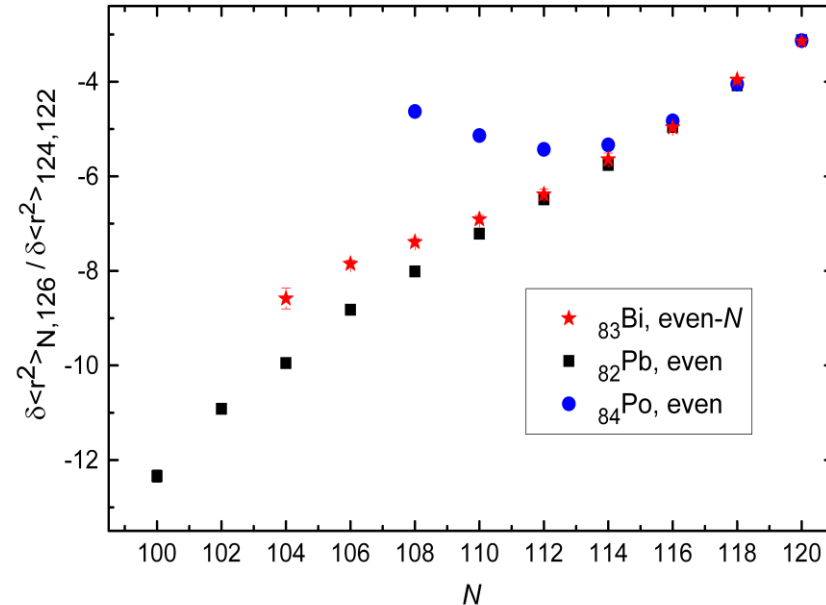


# Bi: relative radii

For comparison of radii trends for different isotopic chains it is better to use relative  $\delta\langle r^2 \rangle$ :  $\delta\langle r^2 \rangle_{N,126} / \delta\langle r^2 \rangle_{124,122}$



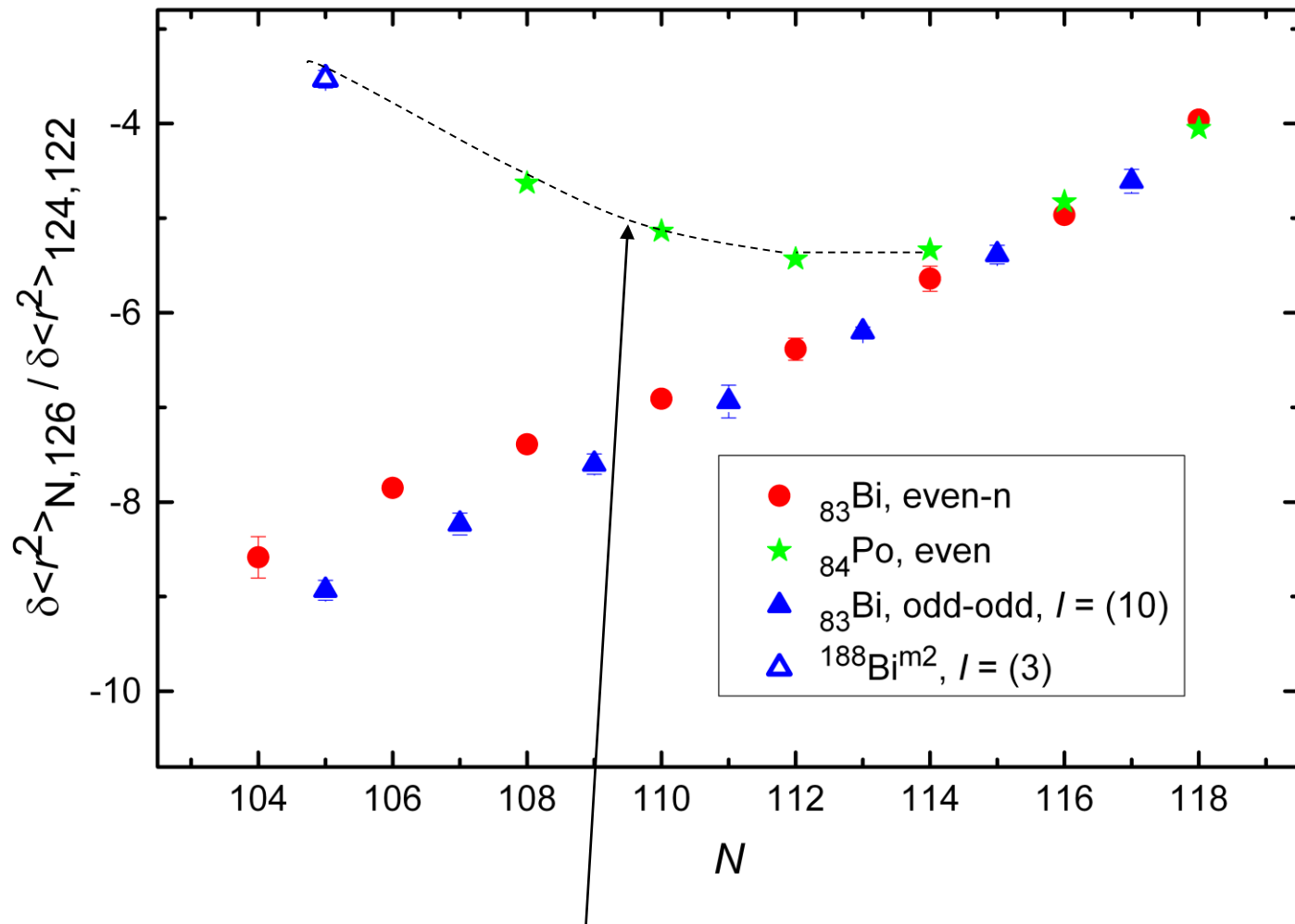
remarkable coincidence of the relative-radii trends for  $Z = 80, 81, 82$  at the extensive neutron range



Even- $N$  nuclei: shape evolution in the Bi and Tl isotopic chains markedly differs from each other, although these chains are “mirror” in respect to the filled proton shell ( $Z = 82$ )

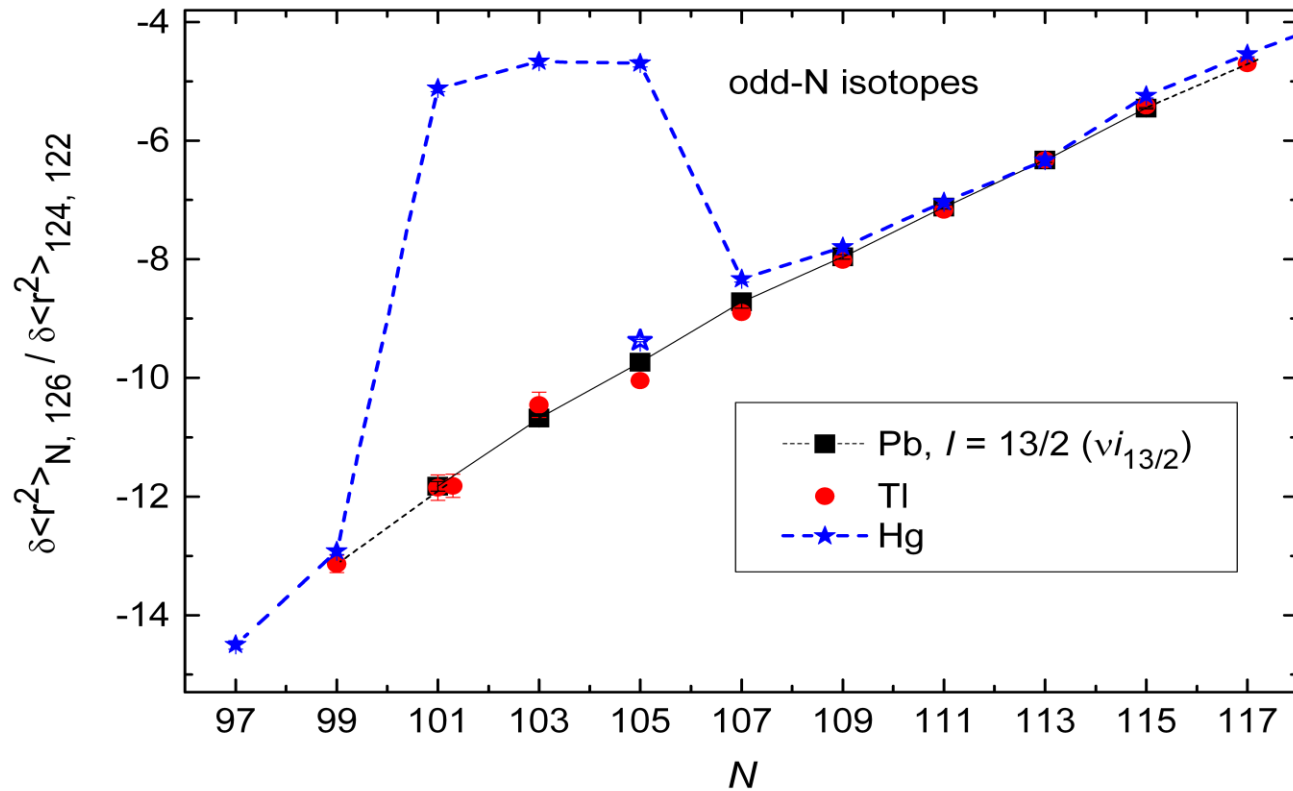
Radii trend for  $^{83}\text{Bi}$  is intermediate between “spherical”  $^{82}\text{Pb}$  trend and  $^{84}\text{Po}$  trend with the onset of deformation

# Bi: relative radii



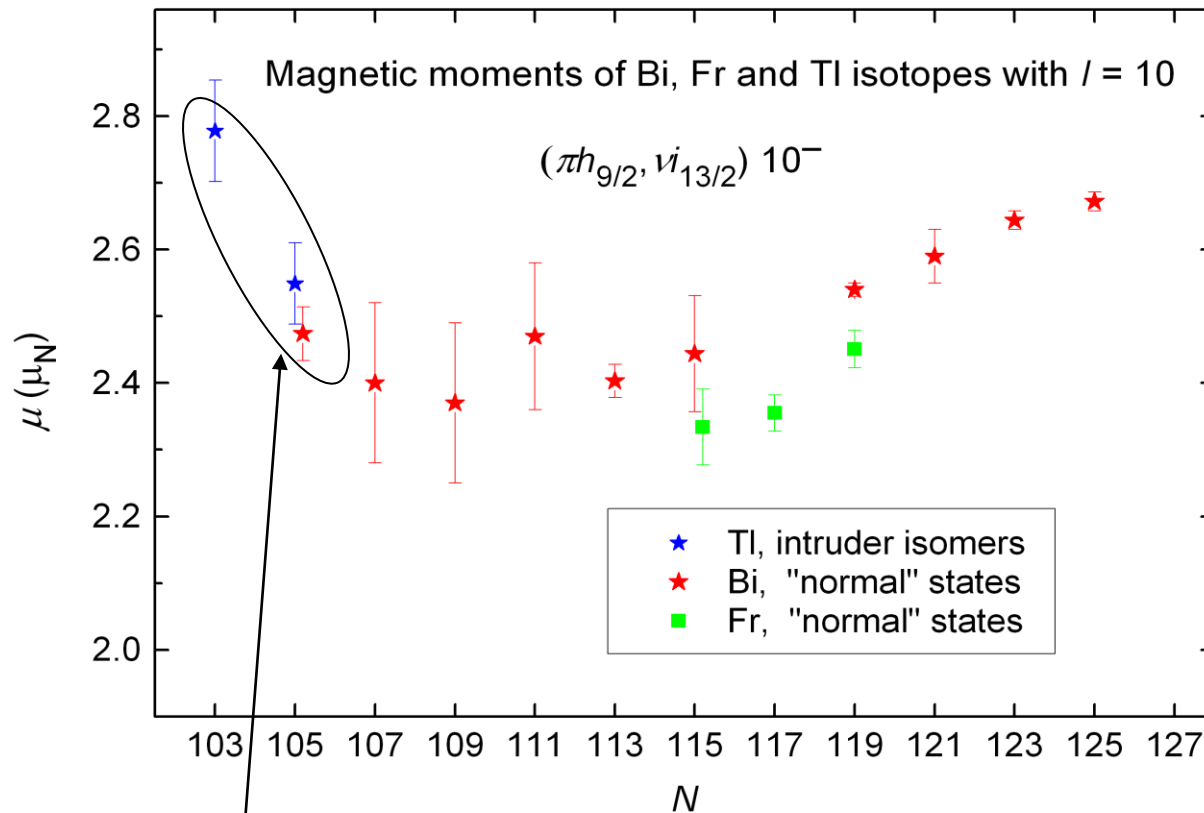
Radius of the strongly deformed  $^{188}\text{Bi}$  is found on the continuation of the Po-trend

# Comparison of $_{81}\text{Tl}$ and $_{80}\text{Hg}$ with $_{82}\text{Pb}$



Large prolate deformation for  $^{181, 183, 185}\text{Hg}$ . Return to “sphericity”: to the same Pb-Tl trend

# Bi & Tl: magnetic moments



The increase of  $\mu(10^-)$  is connected with the increase of deformation

# Bi: main results

1.  $\delta\langle r^2 \rangle$ ,  $\mu$ ,  $Q_s$  for 25 Bi isotopes/isomers
2. Marked deviation of Bi  $\delta\langle r^2 \rangle$  trend from (spherical) Pb & Tl trend at  $N < 109$ , onset of small oblate deformation (?)
3. Large isomer shift (shape coexistence) for intruder isomers
4. Large shape staggering at  $A = 188$  ( $N = 105$ )
5. Systematic behaviour of  $I^\pi = 9/2^-$  ( $\pi h_{9/2}$ ) and  $I^\pi = 10^-$  ( $\pi h_{9/2}$ ,  $\nu i_{13/2}$ ) magnetic moments, deviation for  $A = 215, 217$
6. First isomer selective  $\beta$ DF study ( $^{188}\text{Bi}$ ). Spin dependence of  $\beta$ DF