

# A common framework for indirect MSSM constraints

Frédéric Ronga

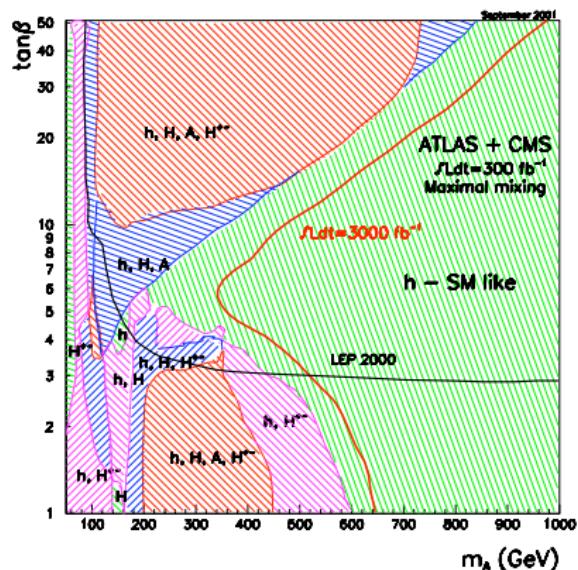
CERN – Switzerland

SUSY 2007 – Karlsruhe – July 31, 2007

## Contents

- ① Interplay between flavour Physics and LHC
- ② Common framework development
- ③ Lightest Higgs boson mass in the CMSSM

# LHC discovery reach in the MSSM sector



- 4 Higgs observable at LHC
- 3 Higgs observable at LHC
- 2 Higgs observable at LHC
- 1 Higgs observable at LHC

## MSSM – 5 Higgs bosons:

*Neutral*     $h, H$  ( $CP$  even),  $A$  ( $CP$  odd)  
*Charged*     $H^\pm$  (one observable)

*Large region where only the light SM-like  $h$  can be detected.*

*Only in a relatively small region of phase space where all four Higgs bosons can be discovered*

*Adding information from discoverable sparticles will help in the interpretation of the undetectable heavy Higgs sector.  
 Yet, an unambiguous MSSM parameter extraction over the entire phase space cannot be guaranteed.*

# Interpretation of New Physics Discoveries

Key ingredients: Direct discoveries & all other data

## Direct discoveries

- at the LHC
- at a high energy linear collider (ILC)

## “All other data”

- Low Energy (precision) data:
  - Flavour Physics (in particular B Physics)
  - Other low-energy observables (e.g.,  $g - 2$ )
- High energy (precision) data
  - Precision electroweak observables (e.g.,  $m_{\text{top}}$ ,  $m_W$ )
- Cosmology/Astroparticle data
  - e.g., relic density

# Common framework development

# A common framework for indirect constraints

- Goal: a framework to provide consistent indirect constraints
- Collaboration of interested theorists and experimentalists 11.5

Buchmüller, Oliver (CERN) – Exp.

Cavanaugh, Richard (Uni. of Florida) – Exp.

De Roeck, Albert (CERN & Uni. Antwerpen) – Exp.

Heinemeyer, Sven (Santander) – Theo.

Isidori, Gino (INFN Frascati) – Theo.

Paradisi, Paride (Uni. of Valencia) – Theo.

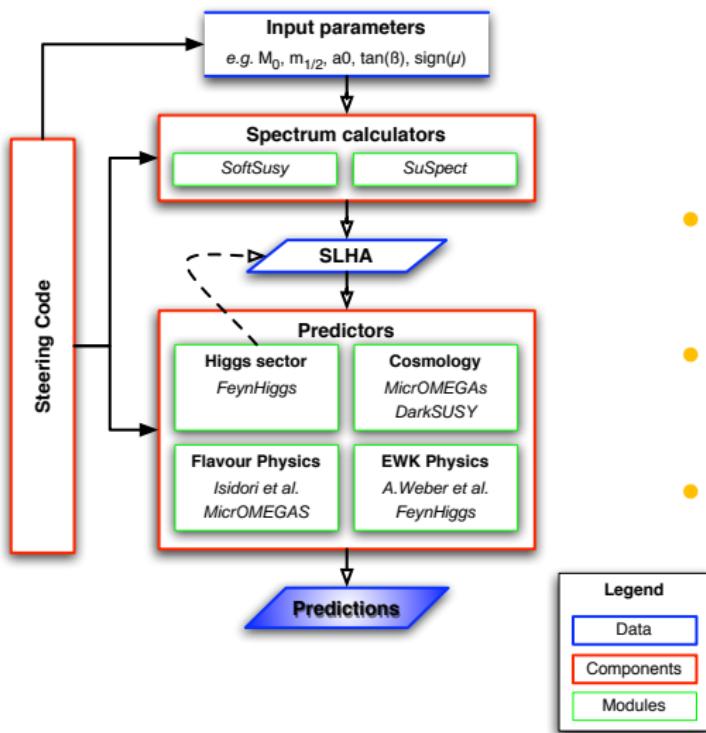
Ronga, Frédéric (CERN) – Exp.

Weber, Arne (Max Planck Inst. f. Phys. (Munich)) – Theo.

Weiglein, Georg (Durham) – Theo.

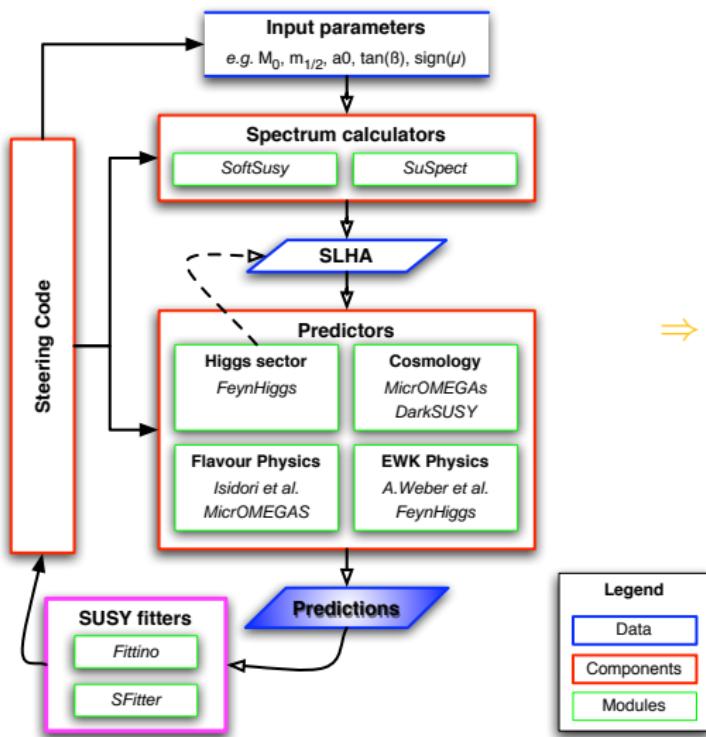
- Started at workshop on Flavour Physics in the Era of the LHC
- Main focus of the work:
  - Development of a *common tool* for indirect constraints
  - Compilation (and integration) of state-of-the-art predictions
  - Application of the tool

# Flow-chart: general overview



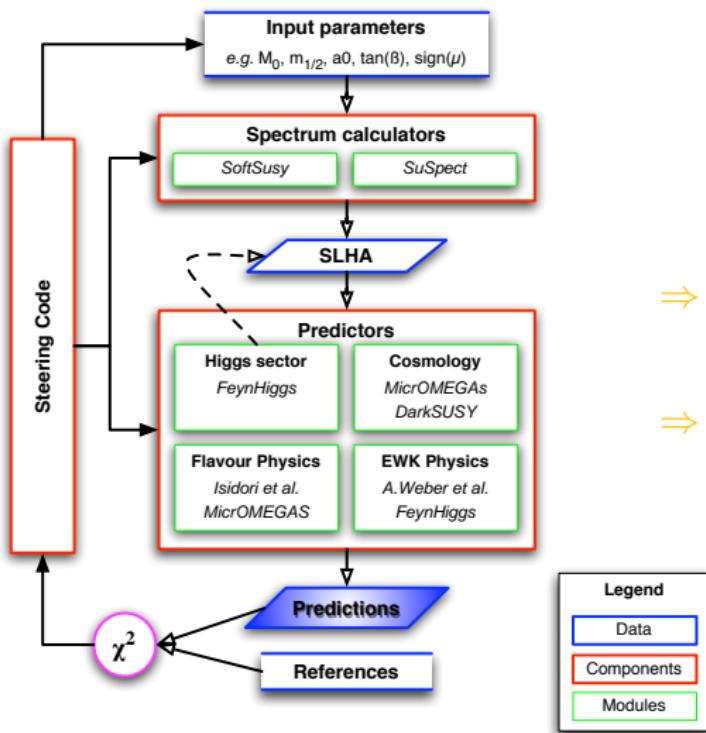
- Consistency  
*Ensured using SLHA interface*
- Flexibility  
*Add/remove predictions*
- Modularity  
*Compare various calculations*

# Use-case I: input to external SUSY fitters

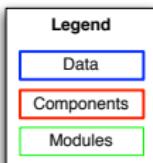


⇒ Provide consistent predictions (low-energy, EW, etc.) to LHC/ILC-oriented fitters.

# Use-case II: fit today's data ( $\chi^2$ minimisation)



- ⇒ Constrain SUSY parameter space
- ⇒ Will become even more stringent when combined with discoveries!

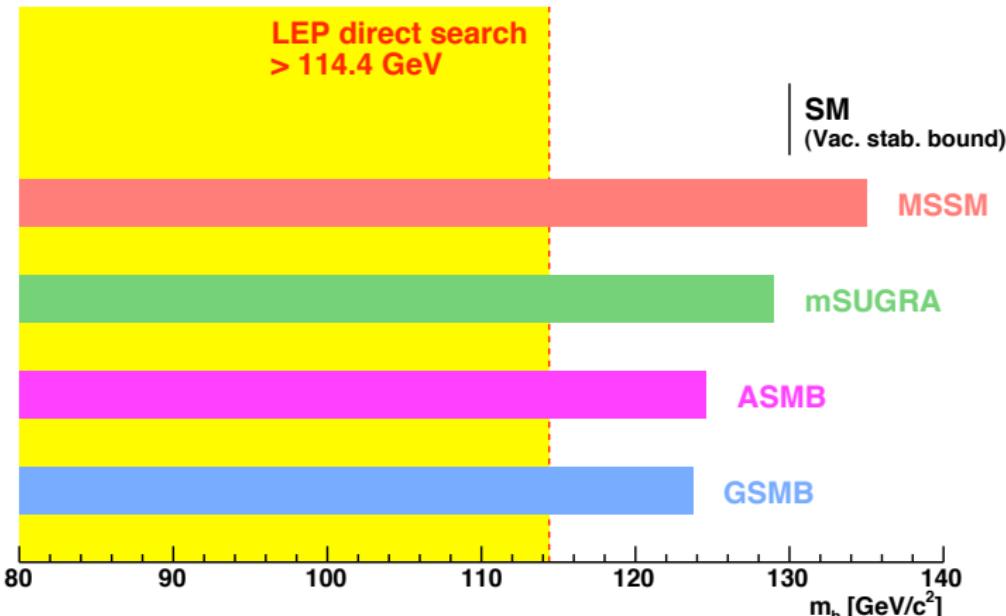


# Lightest Higgs boson mass in the CMSSM

# Preamble: limits on the Higgs boson mass

Many of the popular models require the lightest Higgs boson mass to be significantly below 200 GeV.

$m_h$  limits from arXiv:hep-ph/0412214



⇒ It could just be around the corner! (if it exists...)

# $\chi^2$ fit of the CMSSM parameters

- Multi-parameter  $\chi^2$  fit:

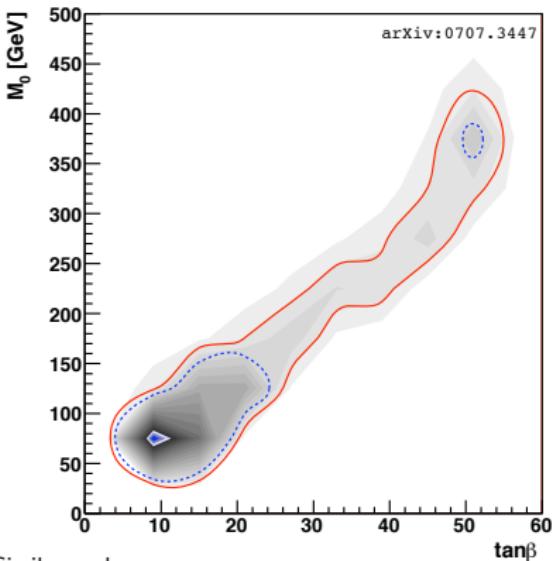
$$\chi^2 = \sum_i^N \frac{(C_i - P_i)^2}{\sigma(C_i)^2 + \sigma(P_i)^2} + \sum_i^M \frac{(f_{\text{SM}_i}^{\text{obs}} - f_{\text{SM}_i}^{\text{fit}})^2}{\sigma(f_{\text{SM}_i})^2}$$

- fitting for all CMSSM parameters:  $M_0$ ,  $M_{1/2}$ ,  $A_0$ ,  $\tan \beta$ ;
  - including relevant SM uncertainties (e.g.  $m_{\text{top}}$ );
- details in O. Buchmüller *et al.*, arXiv:0707.3447 [hep-ph]

Natural extension of J. Ellis *et al.*, arXiv:0706.0652 [hep-ph]

# "Preferred" parameter space

From fits on 2000 pseudo-experiments



Similar analyses:

- Ellis, Heinemeyer, Olive, Weber, Weiglein – hep-ph/0706.0652
- Allanach, Cranmer, Lester, Weber – hep-ph/0705.0487
- Trotta, Austri, Roszkowski – hep-ph/0609126

- overall preferred minimum at low  $\tan\beta$ , low squark mass;
- less preferred region at high  $\tan\beta$ , higher squark mass;
- consistent with previous studies.

Note: includes limit from LEP

⇒ Turn to fit *without* limit on  $m_h$   
assessing preferred  $m_h$  value  
in CMSSM

# Fit result: no constraint on $m_h$

**CMSSM**

Variable	Measurement	Fit	$ O^{\text{meas}} - O^{\text{fit}} /\sigma^{\text{meas}}$
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	$0.02758 \pm 0.00035$	<b>0.02774</b>	0.1
$m_Z$ [GeV]	$91.1875 \pm 0.0021$	<b>91.1873</b>	0.0
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	<b>2.4952</b>	0.0
$\sigma_{\text{had}}^0$ [nb]	$41.540 \pm 0.037$	<b>41.486</b>	1.4
$R_i$	$20.767 \pm 0.025$	<b>20.744</b>	1.1
$A_{fb}^{0,i}$	$0.01714 \pm 0.00095$	<b>0.01641</b>	0.7
$A_i(P_\tau)$	$0.1465 \pm 0.0032$	<b>0.1479</b>	0.2
$R_b$	$0.21629 \pm 0.00066$	<b>0.21613</b>	0.1
$R_c$	$0.1721 \pm 0.0030$	<b>0.1722</b>	0.0
$A_{fb}^{0,b}$	$0.0992 \pm 0.0016$	<b>0.1037</b>	3.5
$A_{fb}^{0,c}$	$0.0707 \pm 0.0035$	<b>0.0741</b>	1.1
$A_b$	$0.923 \pm 0.020$	<b>0.935</b>	0.8
$A_c$	$0.670 \pm 0.027$	<b>0.668</b>	0.1
$A_i(\text{SLD})$	$0.1513 \pm 0.0021$	<b>0.1479</b>	1.2
$\sin^2\theta_{\text{eff}}^{\text{lept}}(Q_{fb})$	$0.2324 \pm 0.0012$	<b>0.2314</b>	0.5
$m_W$ [GeV]	$80.398 \pm 0.025$	<b>80.382</b>	0.7
$m_t$ [GeV]	$170.9 \pm 1.8$	<b>170.8</b>	0.1
$R(b \rightarrow s\gamma)$	$1.13 \pm 0.12$	<b>1.12</b>	0.1
$B_s \rightarrow \mu\mu$ [ $\times 10^{-8}$ ]	$< 8.00$	<b>0.33</b>	N/A (upper limit)
$\Delta a_\mu$ [ $\times 10^{-9}$ ]	$2.95 \pm 0.87$	<b>2.95</b>	
$\Omega h^2$	$0.113 \pm 0.009$	<b>0.113</b>	

arXiv:0707.3447 [hep-ph]

- Absolute  $\chi^2$  minimum:

$$\chi^2/\text{ndof} = 17.0/13$$

- 20% goodness-of-fit probability
- ⇒ Fits today's data well

# Fit result: no constraint on $m_h$

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arXiv:0707.3447 [hep-ph]

$$\chi^2/\text{ndof} = 17.0/13 \text{ (20% prob.)}$$

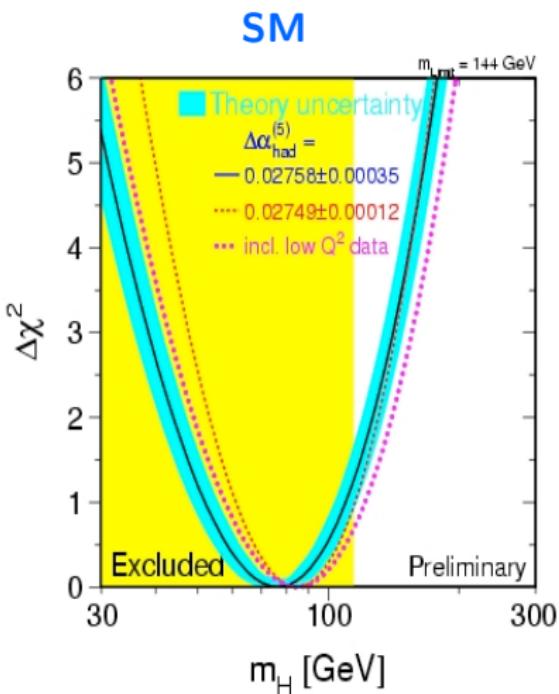
SM

Variable	Measurement	Fit	$ O^{\text{meas}} - O^{\text{fit}} /\sigma^{\text{meas}}$
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	$0.02758 \pm 0.00035$	<b>0.02768</b>	0.1
$m_Z$ [GeV]	$91.1875 \pm 0.0021$	<b>91.1875</b>	0.05
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	<b>2.4957</b>	0.2
$\sigma_{\text{had}}^0$ [nb]	$41.540 \pm 0.037$	<b>41.477</b>	1.5
$R_i$	$20.767 \pm 0.025$	<b>20.744</b>	0.8
$A_{fb}^{0,l}$	$0.01714 \pm 0.00095$	<b>0.01645</b>	0.5
$A_l(P_\tau)$	$0.1465 \pm 0.0032$	<b>0.1481</b>	0.2
$R_b$	$0.21629 \pm 0.00066$	<b>0.21586</b>	0.5
$R_c$	$0.1721 \pm 0.0030$	<b>0.1722</b>	0.05
$A_{fb}^{0,b}$	$0.0992 \pm 0.0016$	<b>0.1038</b>	2.0
$A_{fb}^{0,c}$	$0.0707 \pm 0.0035$	<b>0.0742</b>	0.5
$A_b$	$0.923 \pm 0.020$	<b>0.935</b>	0.2
$A_c$	$0.670 \pm 0.027$	<b>0.668</b>	0.05
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$\sin^2\theta_{\text{eff}}^{\text{lept}}(Q_{\text{fb}})$	$0.2324 \pm 0.0012$	<b>0.2314</b>	0.5
$m_W$ [GeV]	$80.398 \pm 0.025$	<b>80.374</b>	0.5
$m_t$ [GeV]	$170.9 \pm 1.8$	<b>171.3</b>	0.2
$\Gamma_W$ [GeV]	$2.140 \pm 0.060$	<b>2.091</b>	0.5

arXiv:hep-ex/0612034

$$\chi^2/\text{ndof} = 18.2/13 \text{ (15% prob.)}$$

# $\chi^2$ scan of the Higgs boson mass

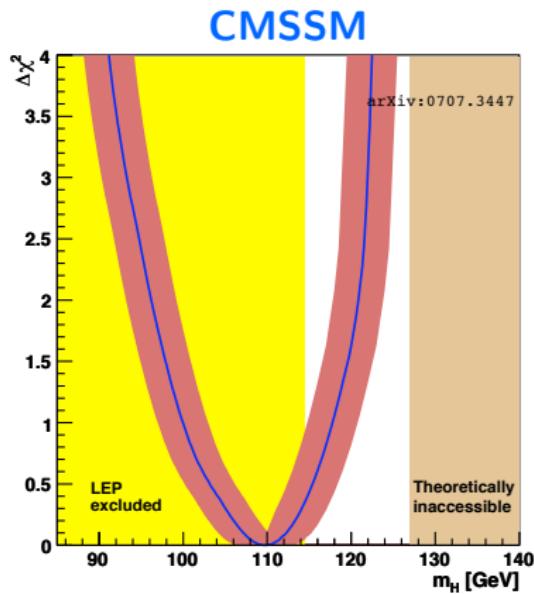


- Constrain  $m_h$  to scan value;
- minimize all model parameters in each point;
- $\Rightarrow$  determine error on  $m_h$  prediction

## SM fit:

- $m_H = 78^{+33}_{-24}$  GeV/ $c^2$
- 12% probability at exclusion limit  
*Including theoretical uncertainty*

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## SM fit:

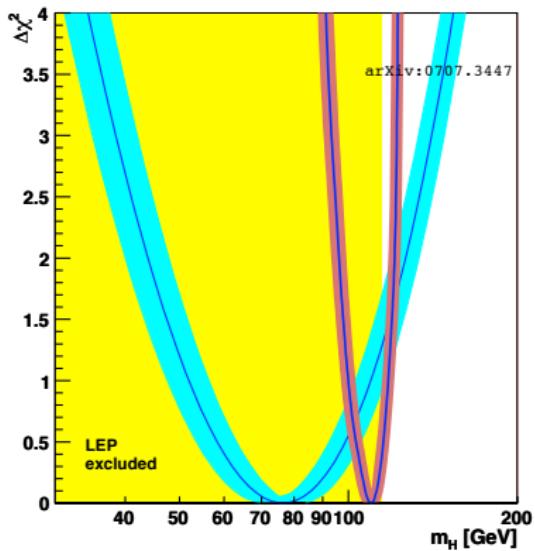
- $m_H = 78^{+33}_{-24} \text{ GeV}/c^2$
- 12% probability at exclusion limit  
*Including theoretical uncertainty*

## CMSSM fit:

- $m_h = 110^{+8}_{-10} \pm 3 \text{ GeV}/c^2$
- 20% probability at exclusion limit  
*Including theoretical uncertainty*

# $\chi^2$ scan of the Higgs boson mass

## Overlay



Difficult to detect experimentally  
at this low mass, **but...**

- Constrain  $m_h$  to scan value;
- minimize all model parameters in each point;
- ⇒ determine error on  $m_h$  prediction

## SM fit:

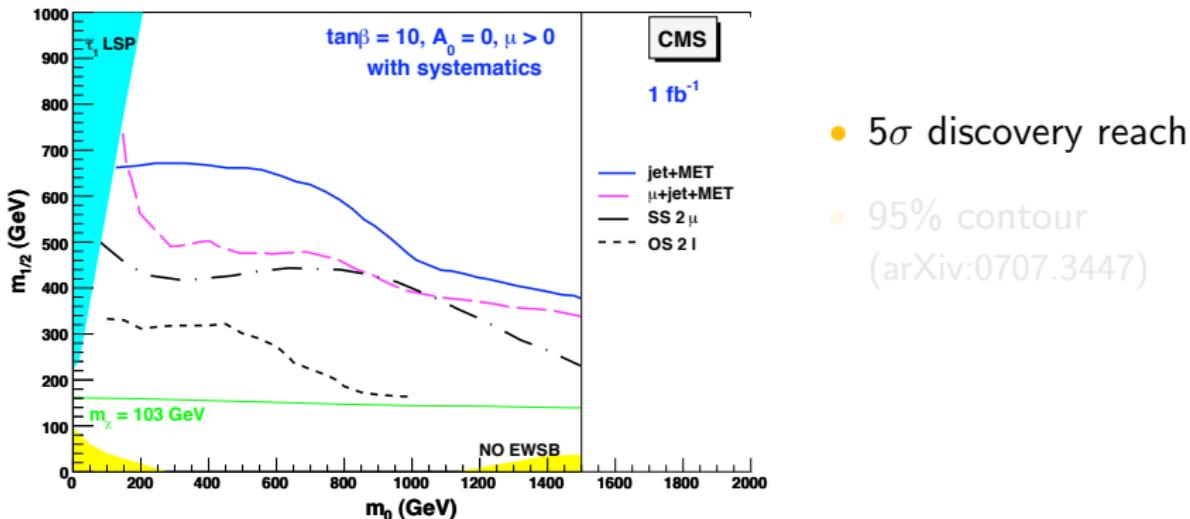
- $m_H = 78^{+33}_{-24} \text{ GeV}/c^2$
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- $m_h = 110^{+8}_{-10} \pm 3 \text{ GeV}/c^2$
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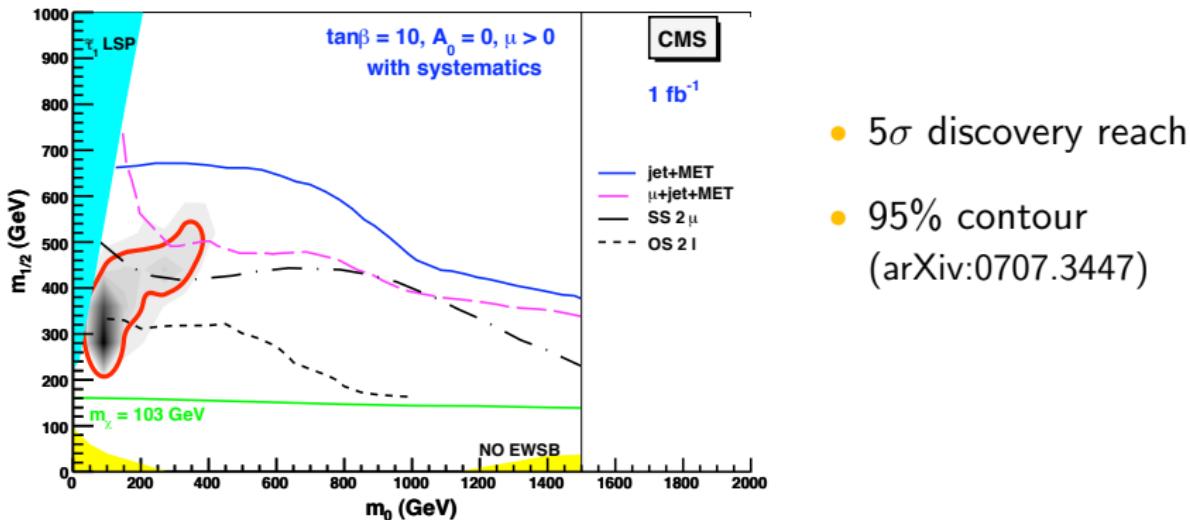
# LHC Discovery potential: sparticle searches

CMS early discovery reach for  $1 \text{ fb}^{-1}$  (ATLAS similar)



# LHC Discovery potential: sparticle searches

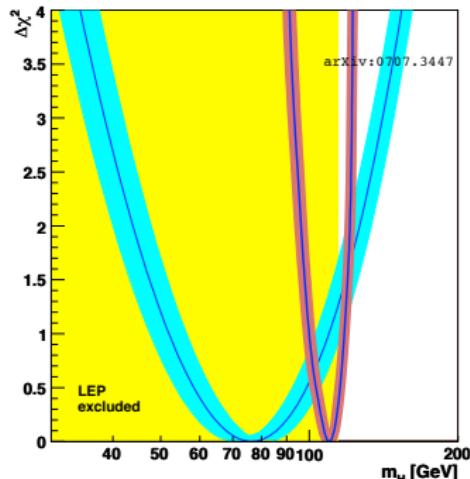
CMS early discovery reach for  $1 \text{ fb}^{-1}$  (ATLAS similar)



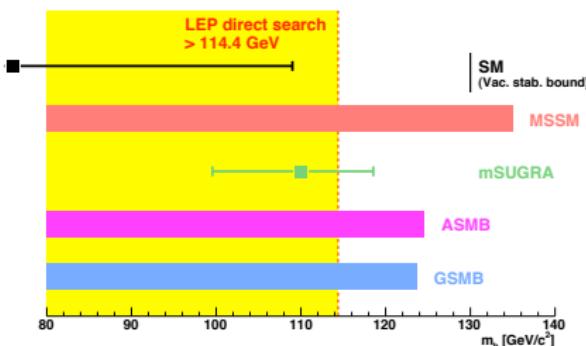
- $5\sigma$  discovery reach
- 95% contour  
(arXiv:0707.3447)

... if this is correct, signs of SUSY will emerge  
very early in the sparticle sector!

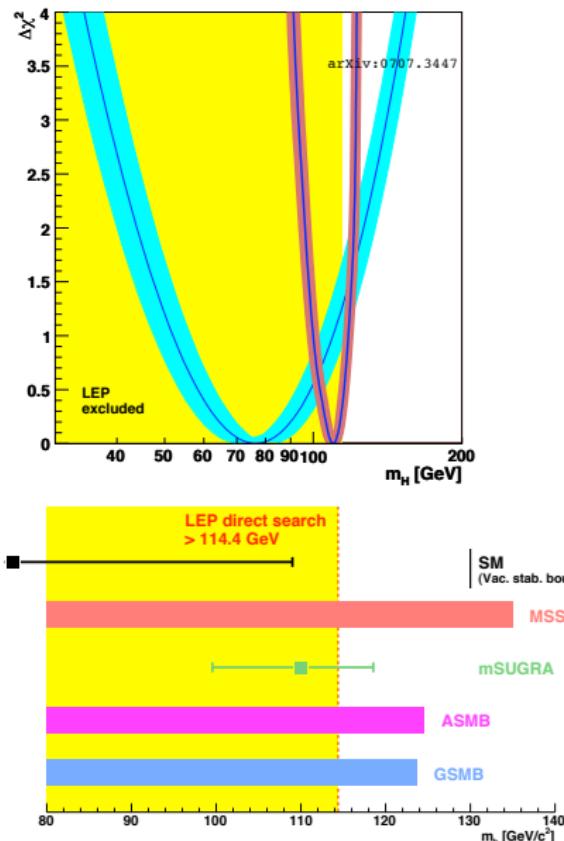
# Summary: an experimentalist's perspective



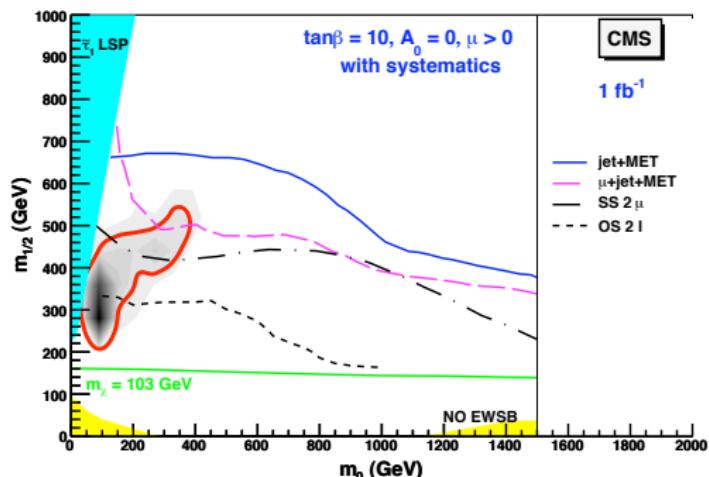
The Higgs seems to be around the corner...



# Summary: an experimentalist's perspective



The Higgs seems to be around the corner...



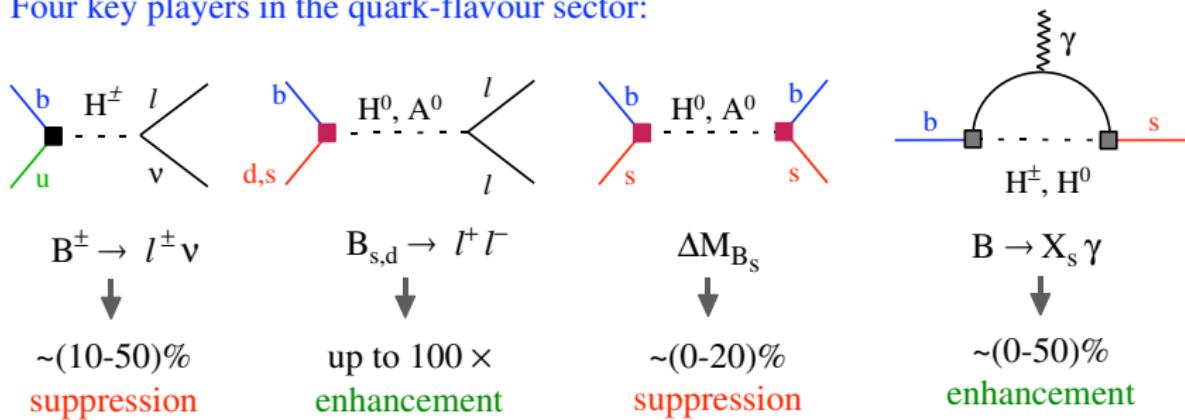
... and first signs of it might manifest itself early on in sparticle searches at the LHC!

# Backup slides

# B Physics observables

G. Isidori, Workshop on *Flavour Physics in the Era of the LHC*

Four key players in the quark-flavour sector:



[qualitative general features for  $M_H \sim 500$  GeV &  $\tan\beta \sim 50$ ]

# Sampling the CMSSM Parameter Space

2000 “toy experiments” produced:

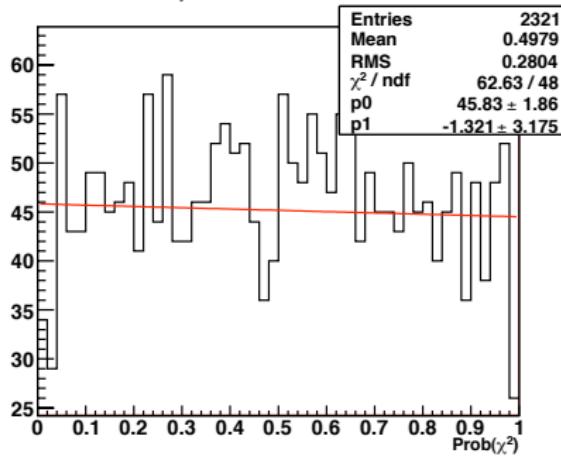
- predictions at  $\chi^2$  minimum smeared by their error;
- $\chi^2$  fit of pseudo-experiments;
  - randomised starting values;
- determine best fit CMSSM parameters

Assess validity of fit

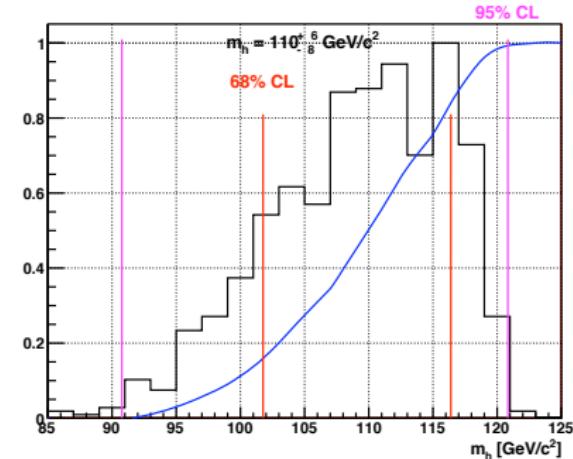
- check  $\chi^2$  probability distribution;
- cross-check parameter and prediction errors;

# Checks from pseudo-experiments

$\chi^2$  probability distribution  
(inc. LEP limit)

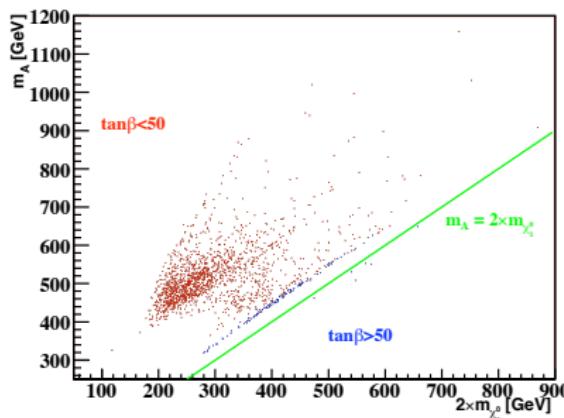


$m_h$  distribution (w/o LEP limit)  
(~900 experiments only)



# Dark matter constraints

“A funnel” at large  $\tan \beta$



$\tilde{\tau}-\tilde{\chi}_1^0$  “co-annihilation”

