

Unification and Dark Matter  
in a  
Minimal Scalar Extension of the Standard Model  
(arXiv:0704.2816)

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# Outline

- I. Unnatural Models
- II. Six Higgs Doublet Model
- III. Renormalization Group Influence on Low Energy Spectrum
- IV. Dark Matter Discovery

# Environmental Selection

- Galactic Principle

No galaxies if cosmological constant larger than ( $\sim 100$  times) observed value

[Weinberg]

- Atomic Principle

No complex chemistry if Higgs vev larger than ( $\sim 5$  times) observed value

$$m_{\text{neutron}} - m_{\text{proton}} \propto v$$

[Agrawal, Barr, Donoghue and Seckel]

- Dark Matter Mass

Halo formation (& star/galaxy formation) fix dark matter density to within an order of magnitude

[Hellerman & Walcher; Tegmark et al.]

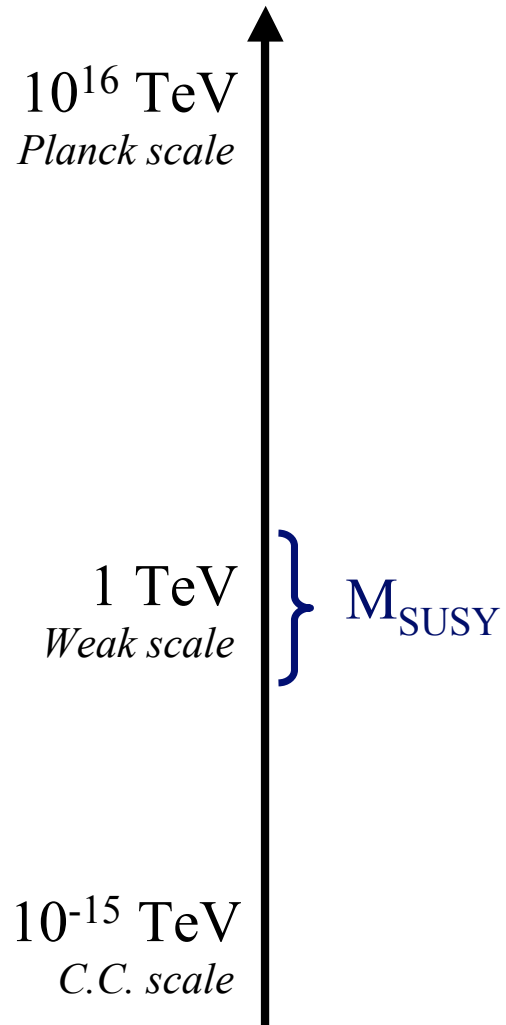
A horizontal banner at the top of the slide features a cosmic background of stars and nebulae in shades of orange, red, and blue. Overlaid on this is a black rectangular box with a thin orange border.

# Environmental Selection

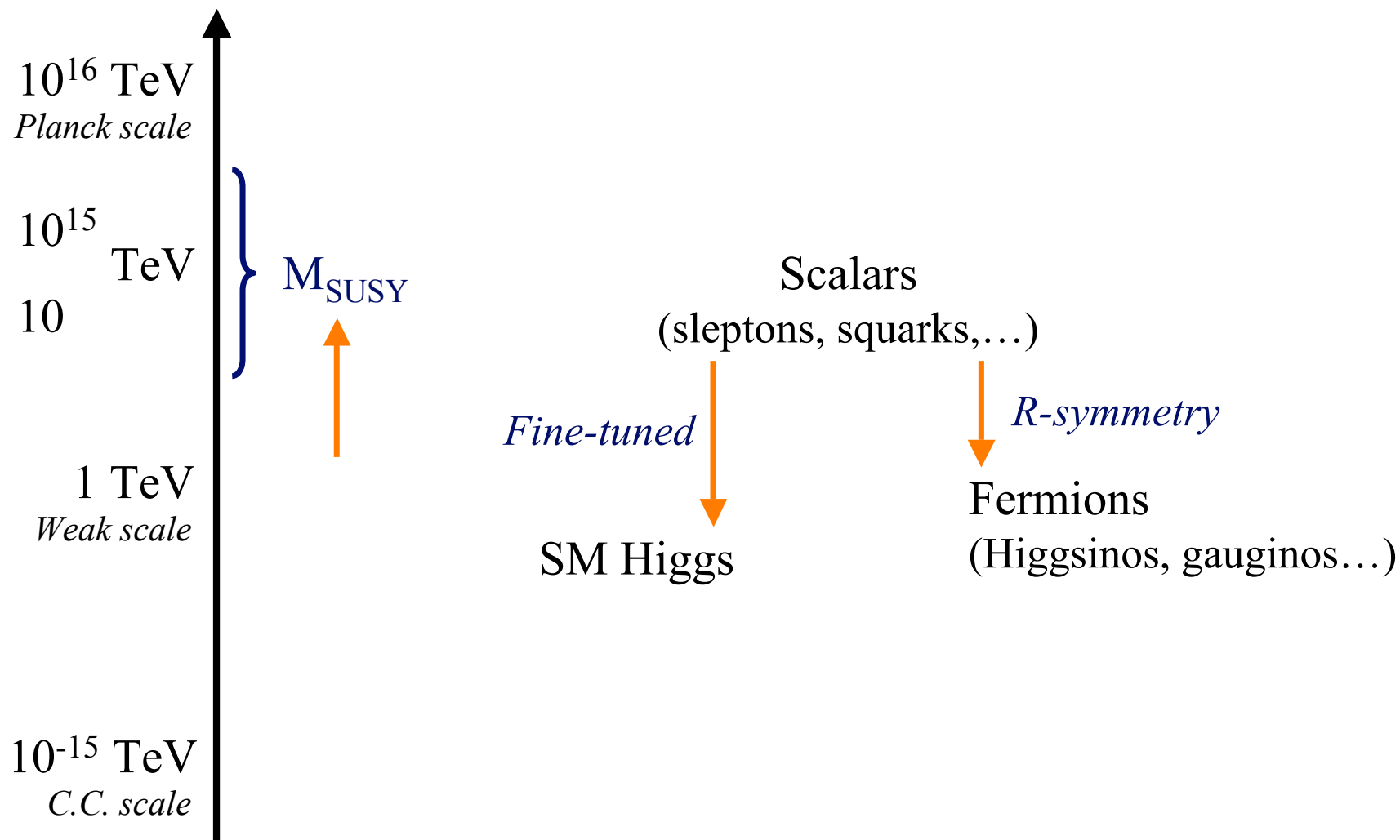
Landscape provides a natural framework for environmental selection

Consider models with unnatural parameters

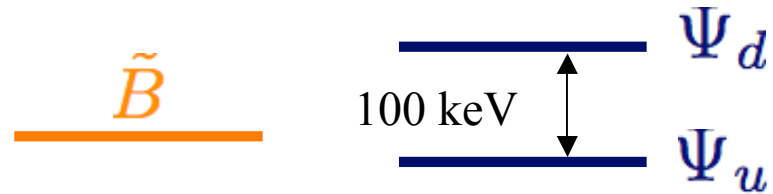
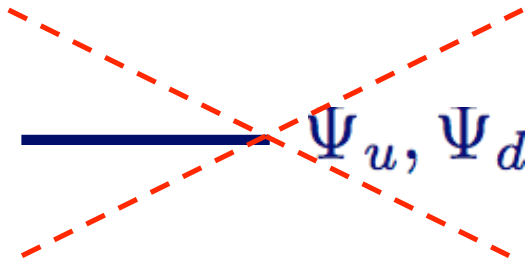
# Split Supersymmetry



# Split Supersymmetry



# Minimal Model



Standard Model plus two ‘Higgsinos’

⇒ gauge coupling unification

Add ‘bino’ to split mass

⇒ direct detection okay

## Minimal Model

- Unification
- Dark matter mass:  
100 GeV - 2 TeV
- 2 fine-tunings:  
Higgs mass & C.C.



# Technical Naturalness

Technical naturalness invoked to keep fermionic dark matter light

Split SUSY: R-symmetry

⇒ How is R-symmetry breaking explicitly communicated to fermions?

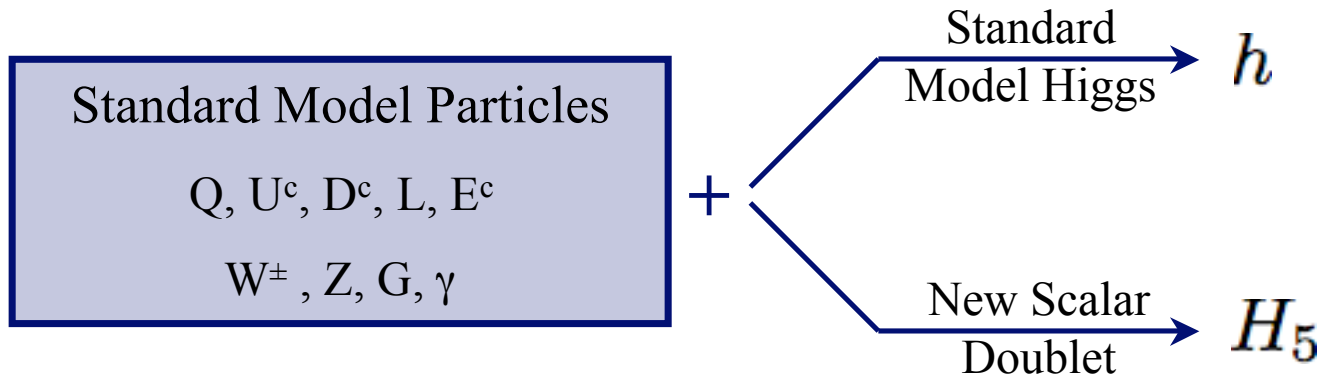
Minimal model: Ad hoc dynamical mechanism

⇒ What is the high energy theory?

Use of technical naturalness might be **misleading** for relevant couplings that determine **large-scale structure** of the Universe



# Six Higgs Doublet Model



- $H_5$  charged under **5** representation of **discrete symmetry** group (i.e.,  $S_6$ )
  - Standard Model particles are **neutral** under this symmetry
- $H_5$  does **not** acquire a vev: 
$$h = \begin{pmatrix} 0 \\ v + h^0/\sqrt{2} \end{pmatrix} \quad H_5 = \begin{pmatrix} \phi_5^+ \\ (s_5^0 + ia_5^0)/\sqrt{2} \end{pmatrix}$$
- $H_5$  **interacts** with Standard Model gauge bosons, but not fermions

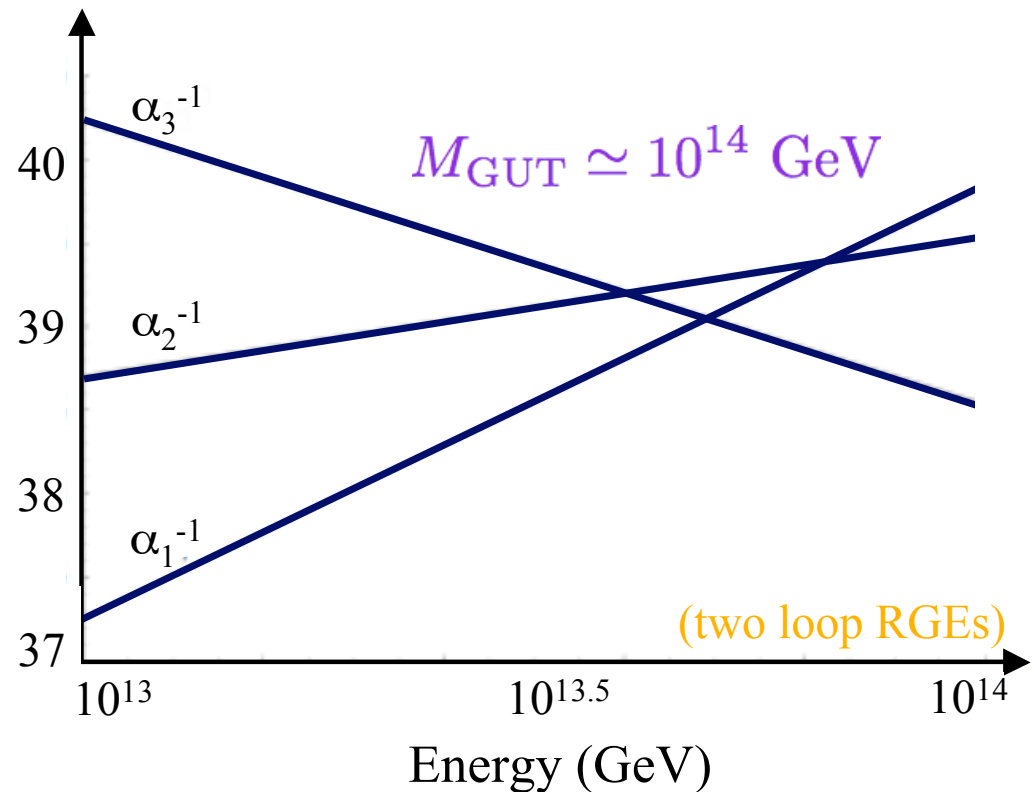
# Unification

- **Unification** is key motivation for introducing the five-plet  $H_5$

- Threshold **correction**

$$m_2/m_3 \sim 30 \quad 6 \text{ Higgs}$$

$$m_3/m_2 \sim 20 \quad \text{MSSM}$$



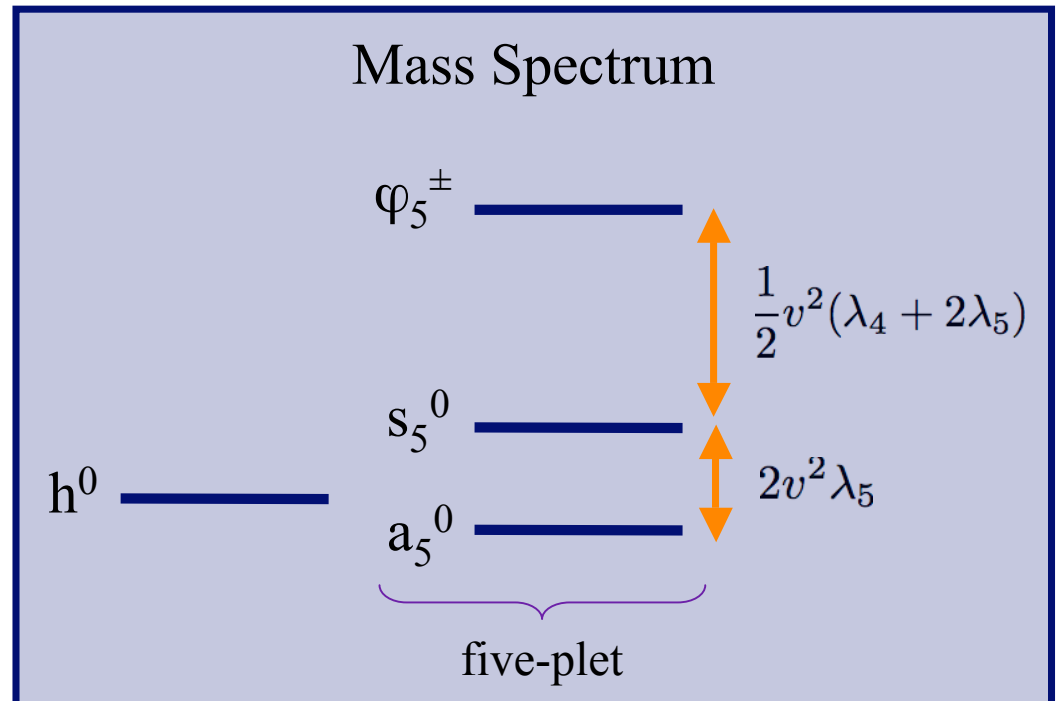
- **Proton decay** too rapid in SU(5) GUT:

$$\Gamma(p \rightarrow e^+ \pi^0) \simeq \frac{\alpha_{GUT}^2 m_p^5}{M_{GUT}^4} \simeq 10^{-28} \text{ yr}^{-1}$$

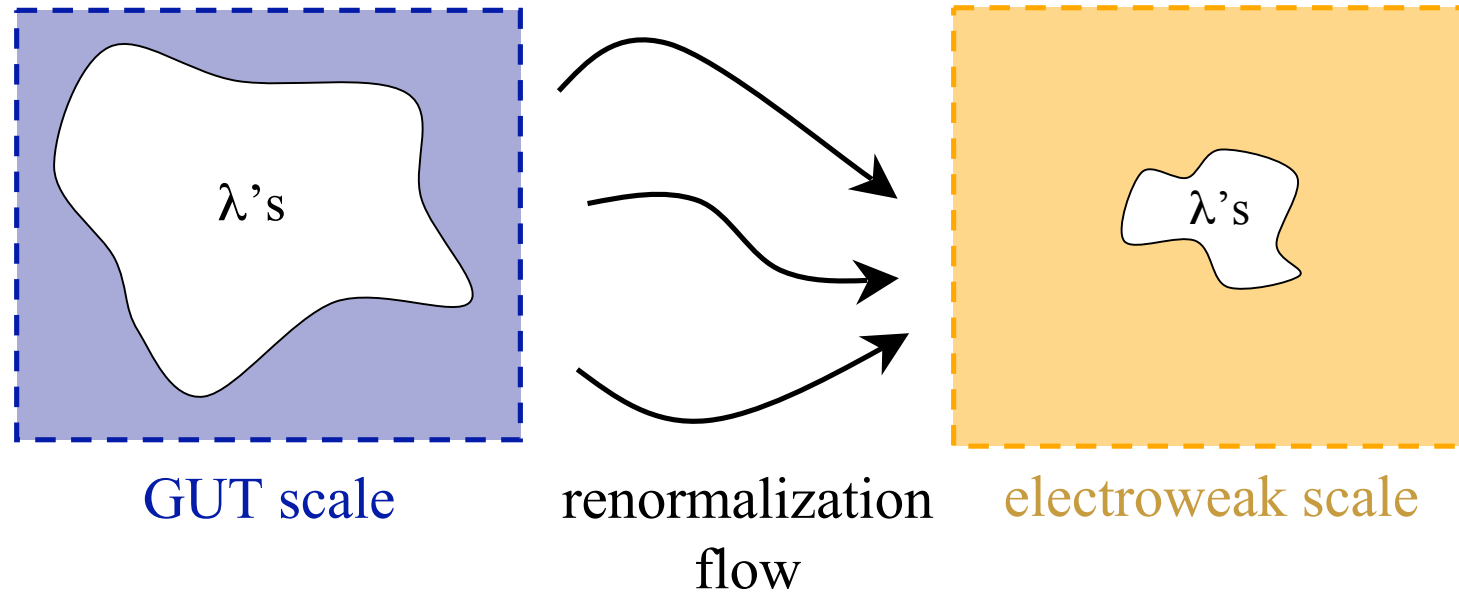
# Mass Spectrum

$$V \supset \underbrace{\lambda_1 (|h|^2 - 2v^2)|h|^2}_{\text{Electroweak symmetry breaking}} + \lambda_4 |h^\dagger H_n|^2 + \underbrace{\lambda_5 ((h^\dagger H_n)^2 + \text{h.c.})}_{\text{Breaks accidental U(1) symmetry}}$$

- $\lambda_4$  and  $\lambda_5$  determine scalar mass splittings
- $a_5$  is lightest neutral particle and serves as the dark matter candidate



# Renormalization Group Effects



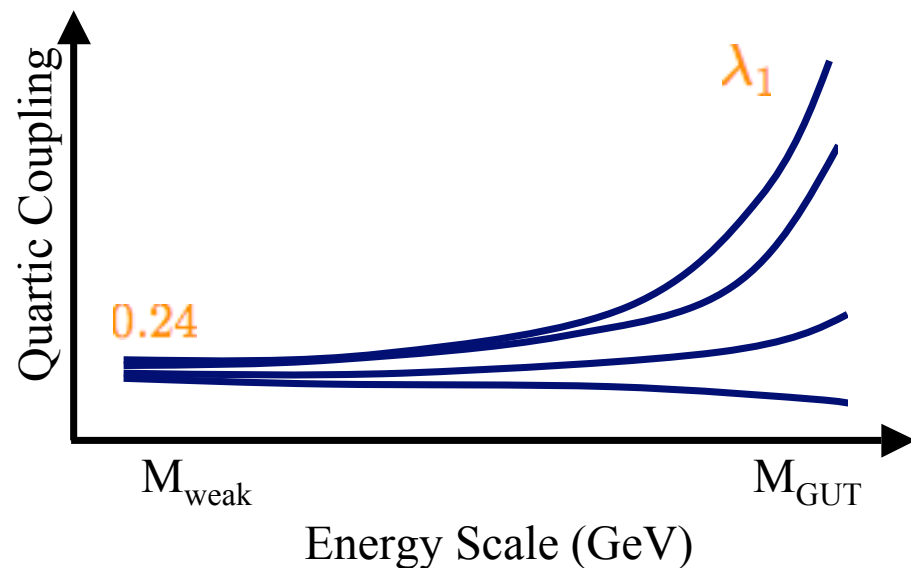
- Landscape gives many possibilities for couplings at GUT scale.  
What are the typical values in our neighborhood of vacua?
- Distribution of couplings is a UV sensitive question
  - Large range of couplings at high energies is compressed at low energies

# Parameter Space Democracy

All couplings at GUT scale are equally likely

- Allowed region for quartics at electroweak scale is small:

- perturbativity
- positive SM Higgs mass
- vacuum stability



- Couplings approach **tracking solution** very quickly

Example:  $\lambda_1$  large at GUT scale, self-coupling term dominates at low energy

$$\lambda_1^{\text{max}} \simeq \frac{16\pi^2}{24t_{\text{GUT}}} \sim 0.24$$

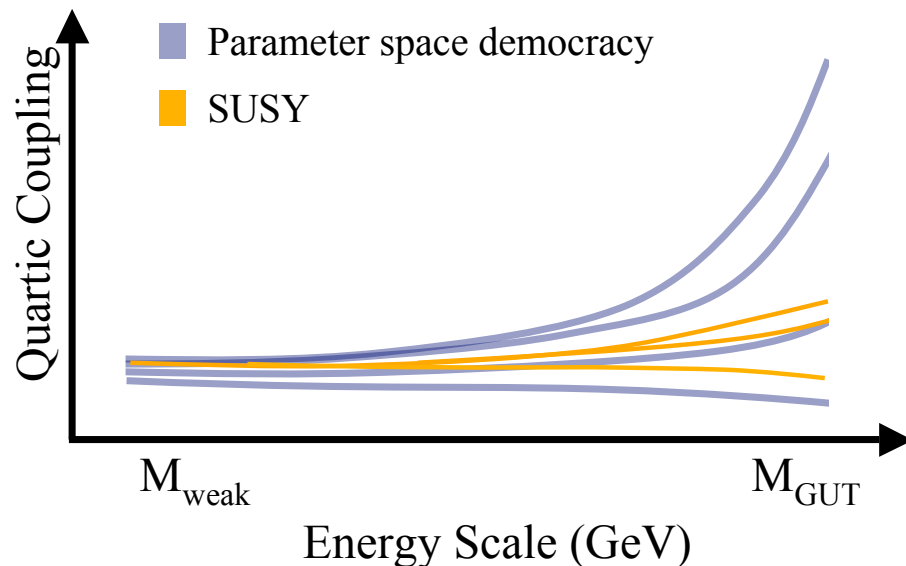
# Supersymmetry

Quartic couplings arise from D-terms

- Each low-energy Higgs doublet comes from **chiral superfield**
- Two angles  $\beta$  and  $\beta_5$  give **orientation** of scalars within superfield

$$\Phi_h| = c_\beta h - s_\beta \tilde{h}$$

$$\Phi_{H_5}| = c_{\beta_5} H_5 - s_{\beta_5} \tilde{H}_5$$



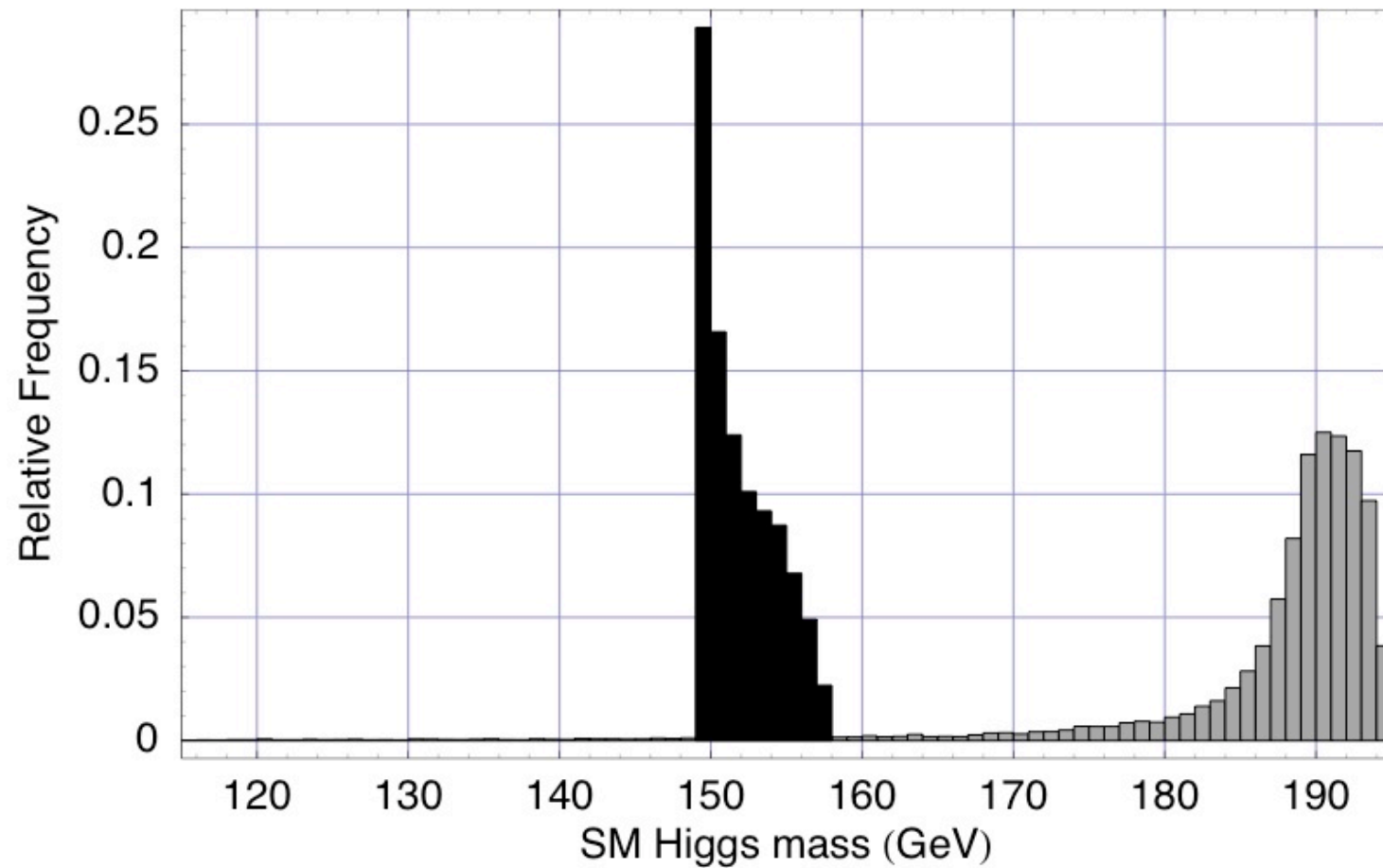
- **Smaller couplings** at high energies as compared to parameter space democracy
- Even **smaller range** at low energy

# Renormalization Effects

■ Parameter space democracy    ■ SUSY

PSD: Large range, peaked at 200 GeV

SUSY: Small range  $\sim 155$  GeV



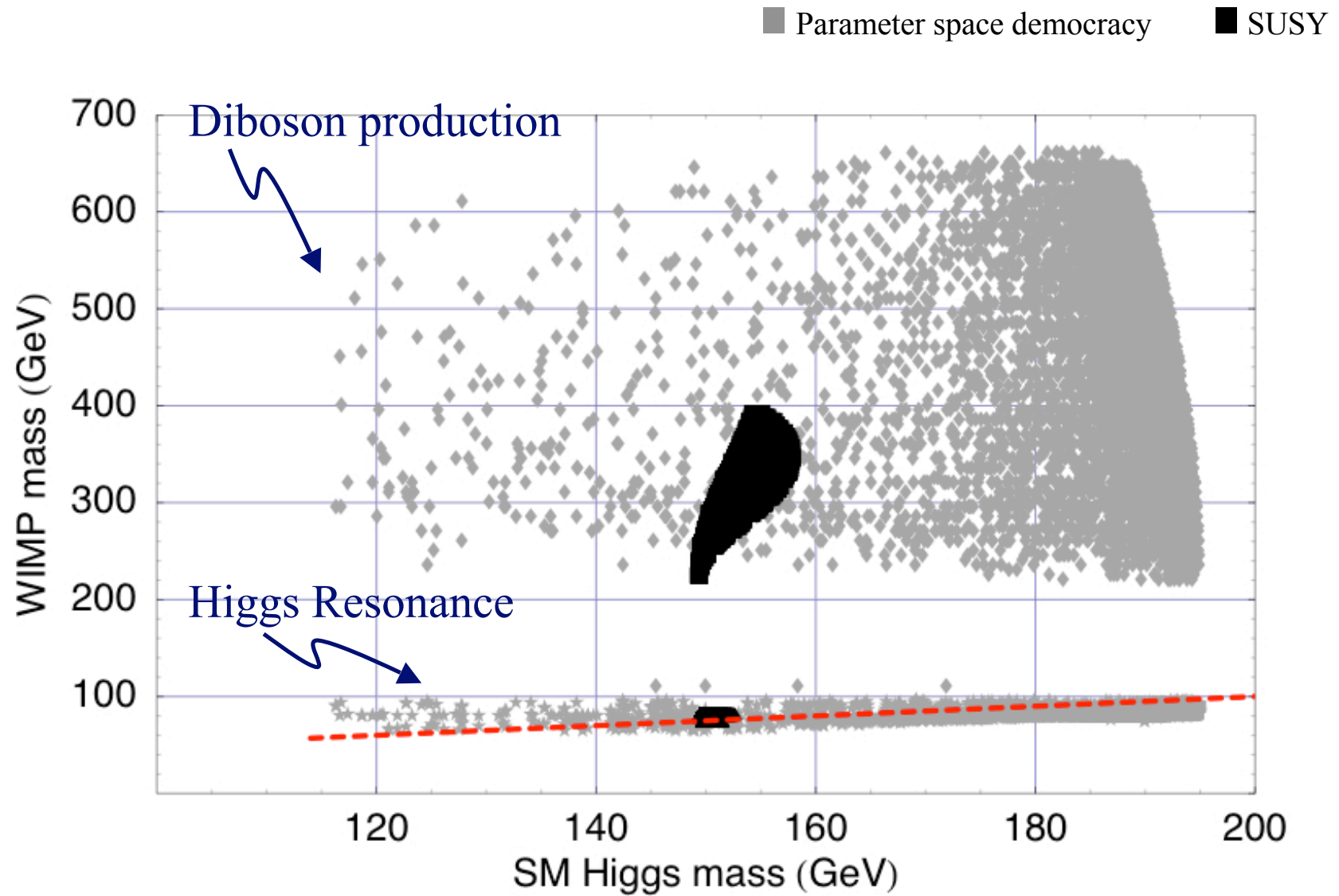


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# Relic Abundance



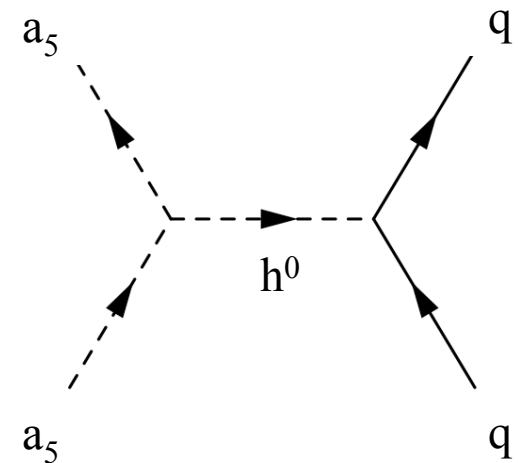
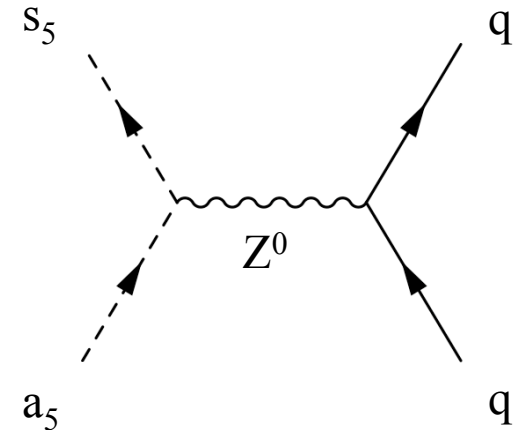
# Direct Detection

- **Inelastic** scattering between  $a_5$  and  $s_5$  bounds mass splitting

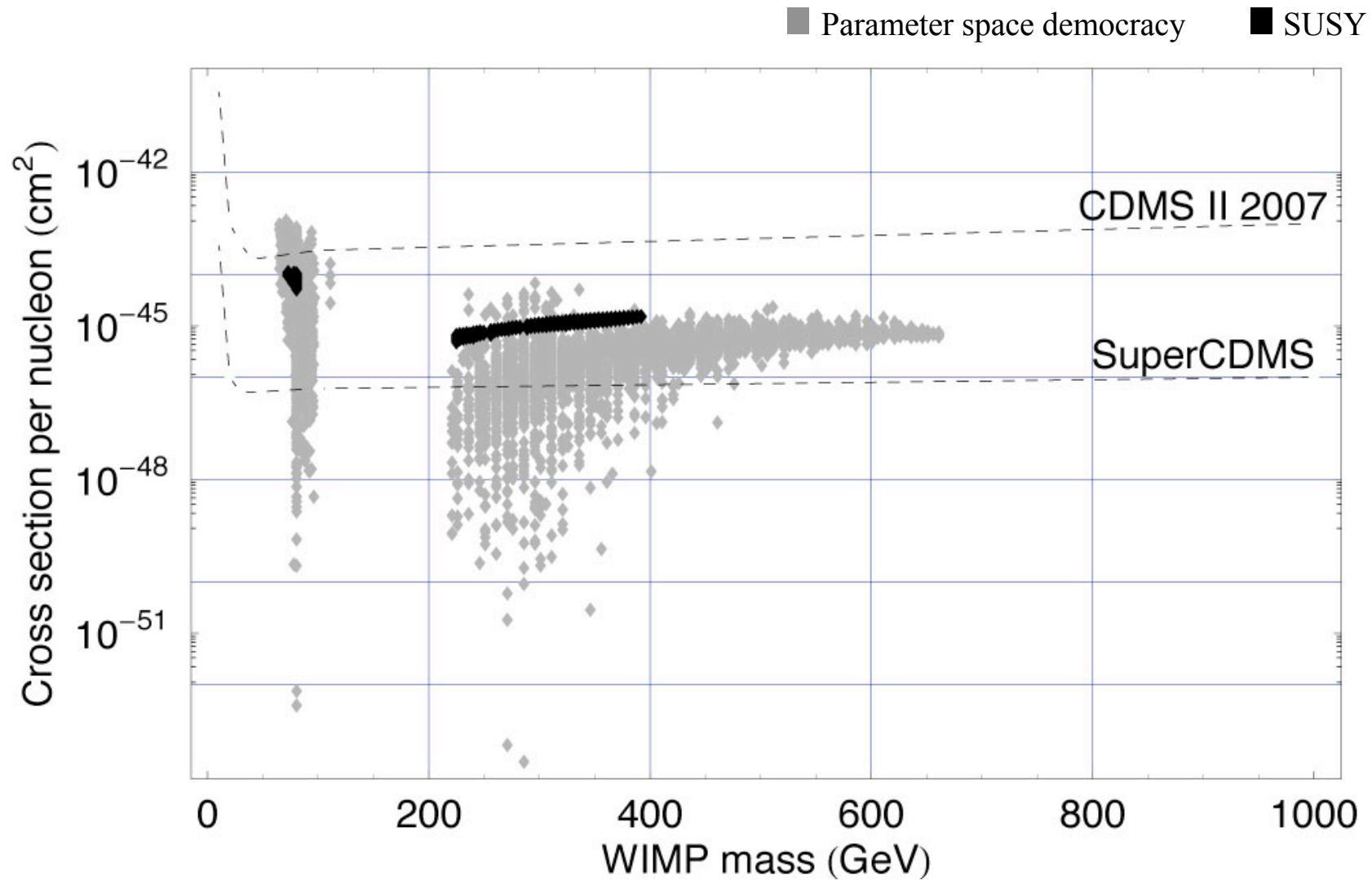
$$\Delta m_{s^0 a^0} \simeq 100 \text{ keV}$$

- **Elastic** scattering between  $a_5$  and  $a_5$  dominates spin-independent contribution

$$\sigma_n = 2 \times 10^{-9} \text{ pb} \left( \frac{\lambda_{\text{eff}}}{0.4} \right)^2 \left( \frac{350 \text{ GeV}}{m_{a^0}} \right)^2 \left( \frac{200 \text{ GeV}}{m_{h^0}} \right)^4$$



# Direct Detection



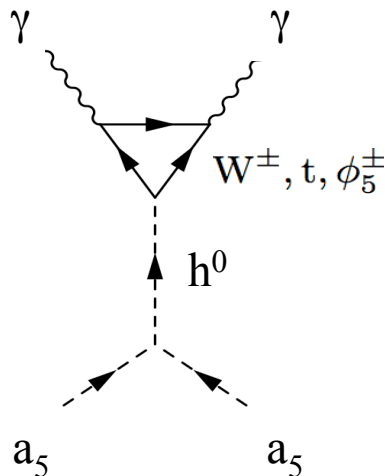
# Indirect Detection

Monochromatic photons produced by WIMP annihilation

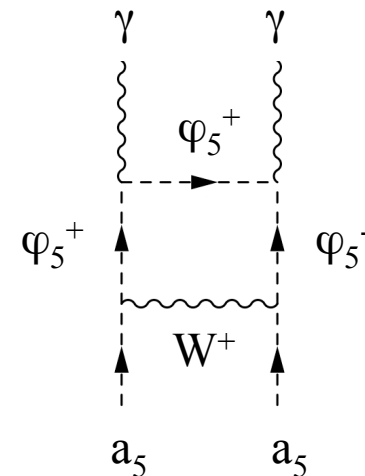
- **Flux** observed by a telescope with a field of view  $\Delta\Omega$  and line of sight  $\Psi(\theta, \phi)$ :

$$\Phi \propto \underbrace{\left( \frac{\sigma_{\gamma\gamma} u}{1\text{pb}} \right) \left( \frac{100\text{GeV}}{m_{a^0}} \right)^2}_{\text{"Particle physics"}} \underbrace{\bar{J}(\Psi, \Delta\Omega) \Delta\Omega}_{\text{"Astrophysics"}}$$

Low-mass dark matter ( $\sim 80$  GeV)

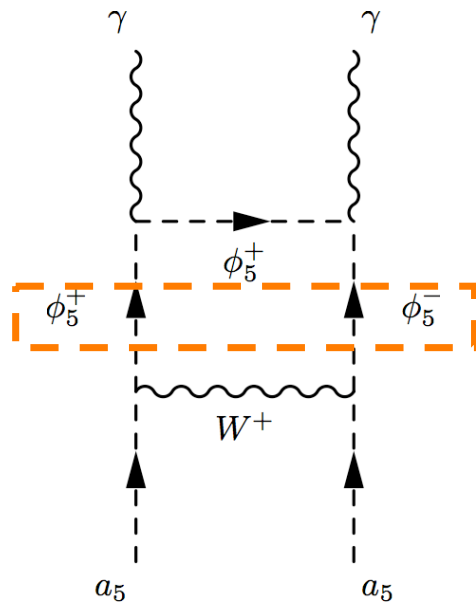


High-mass dark matter ( $\geq 200$  GeV)



# Indirect Detection

High-mass dark matter ( $\geq 200$  GeV)

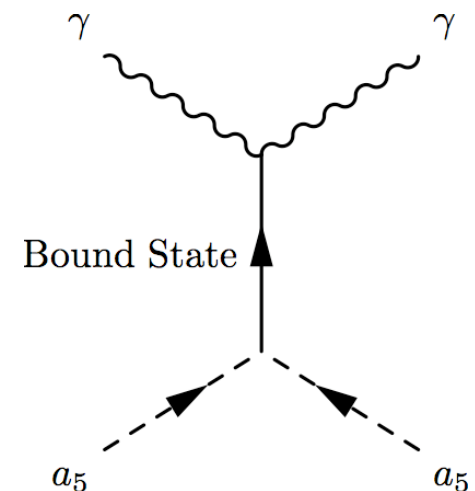


When  $m_a \sim m_\phi$ , there is an effective **Yukawa** force between the  $\phi_5^+ \phi_5^-$  pair:

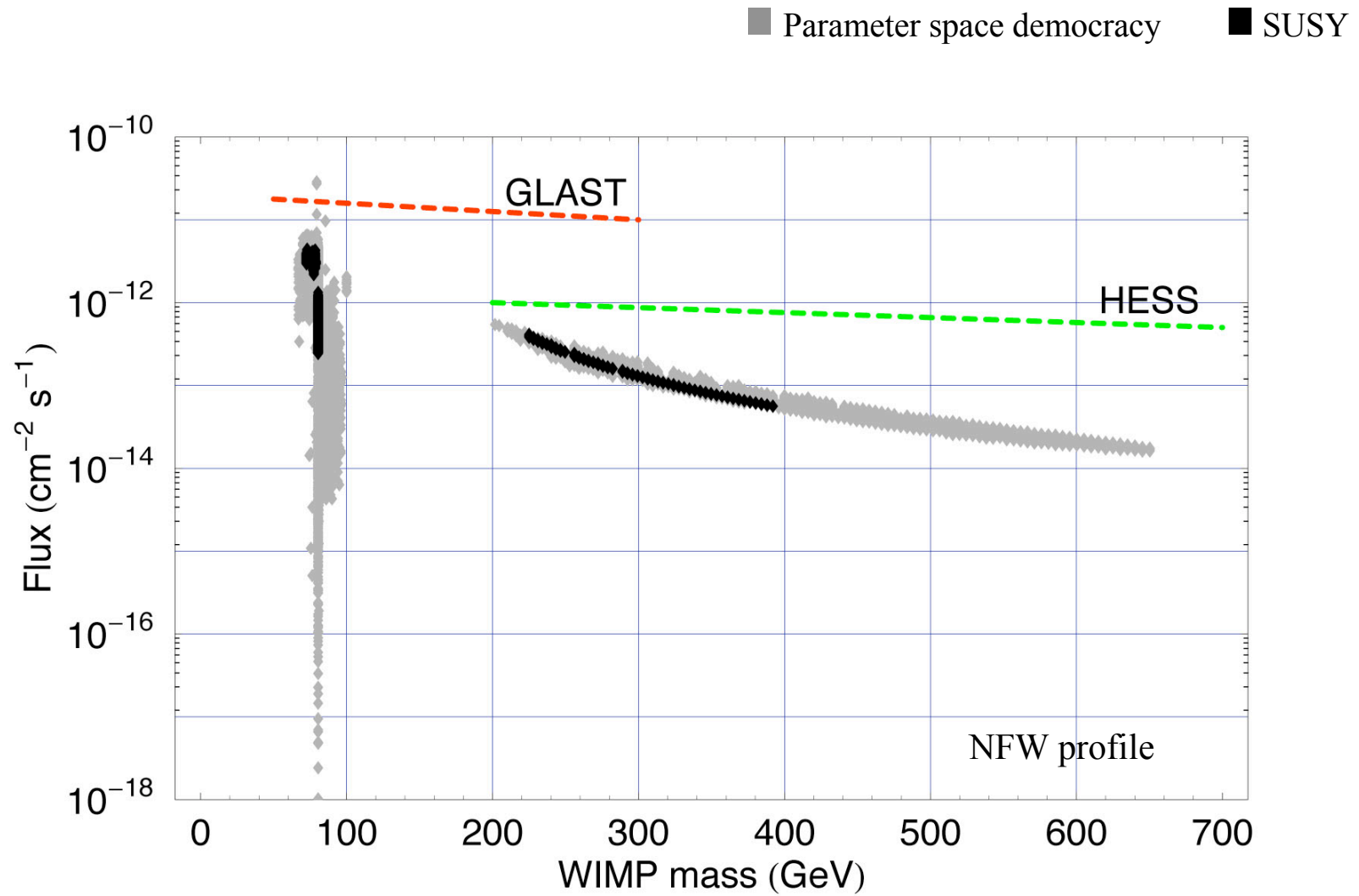
$$V(r) \sim -\alpha_2 \frac{e^{-M_w r}}{r}$$

Charged scalars form a **bound-state solution** to the non-relativistic Schrodinger equation.

$$\begin{aligned} \sigma(a_5 a_5 \rightarrow \gamma \gamma) u &= \left[ \sigma(a_5 a_5 \rightarrow \text{BS}) u \right] \Gamma(\text{BS} \rightarrow \gamma \gamma) \\ &\sim \frac{\alpha^2 \alpha_2^2}{N_h M_w^2} \left( 1 + \sqrt{\frac{2m_a \Delta m_{\phi a}}{M_w^2}} \right) \end{aligned}$$

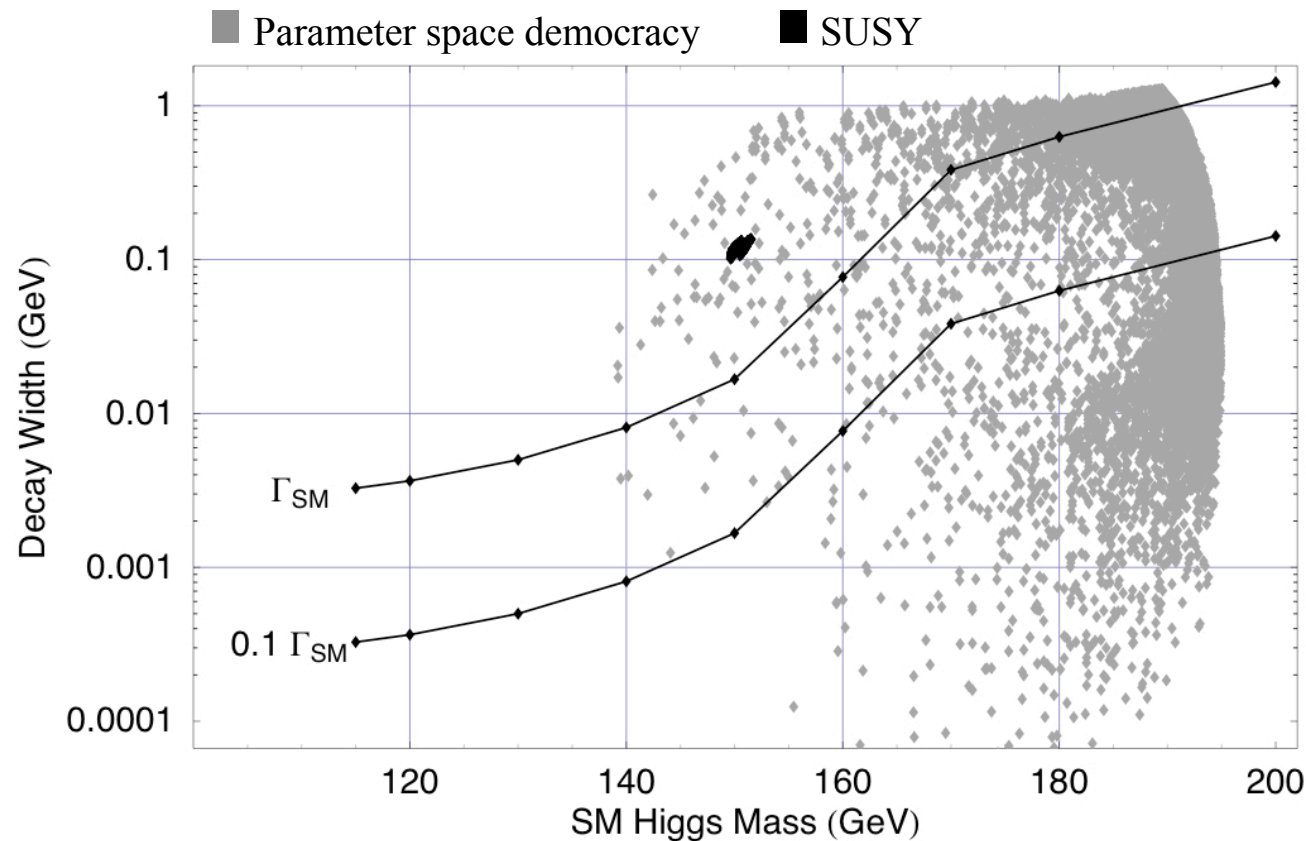
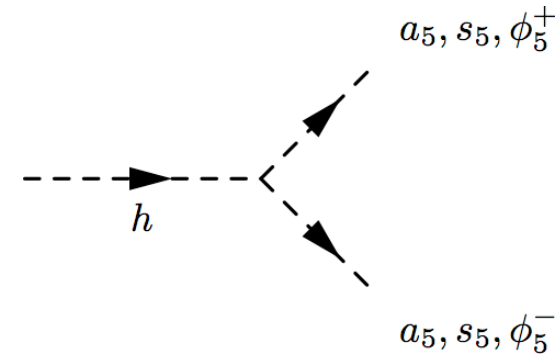


# Indirect Detection



# Decay of the Standard Model Higgs

- New **invisible decay** modes for SM Higgs
- One of the most **promising** discovery channels

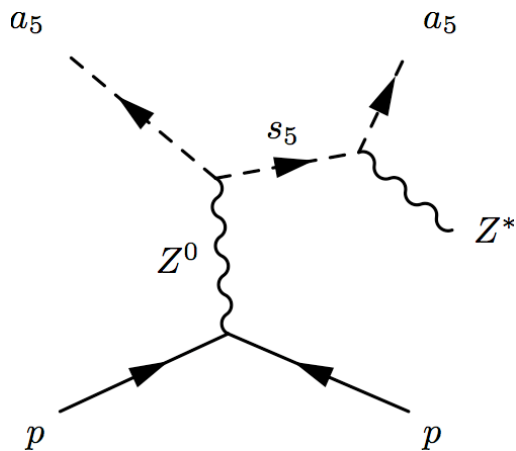




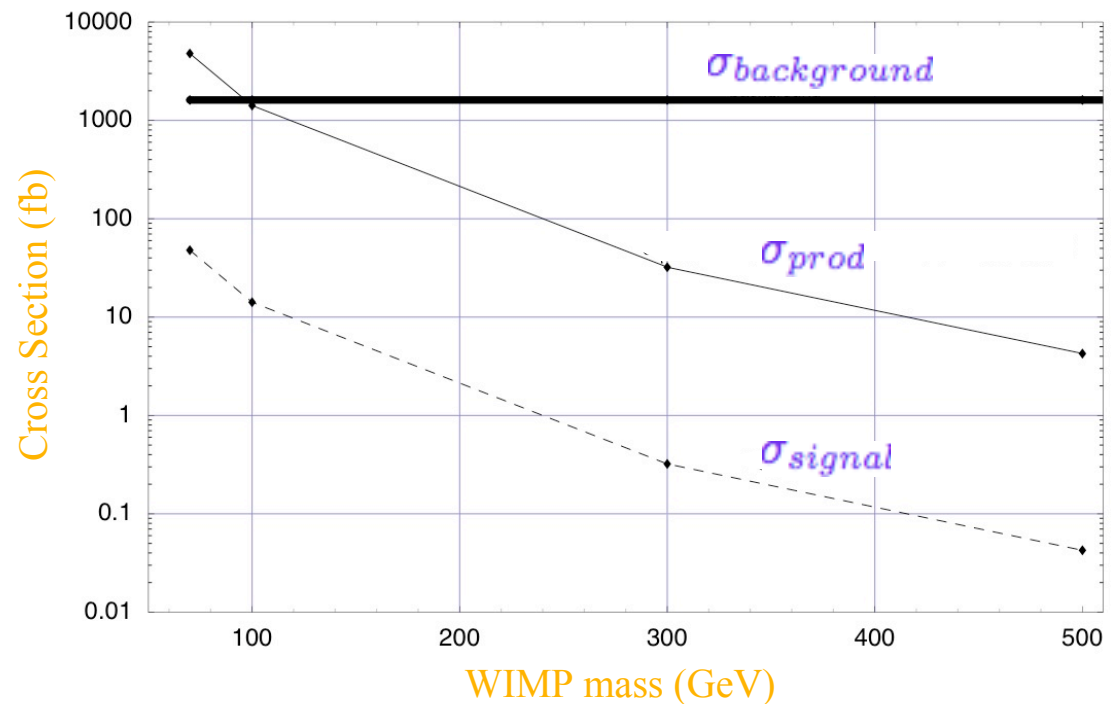
# Signatures at the LHC

Estimate signal for sample point in parameter space

- Choose **leptonic branching** channels for **off-shell** gauge bosons
- With **cuts**, may be possible to detect signal for **low-mass** dark matter



$$\sigma_{\text{prod}} = \sigma(pp \rightarrow a_5 s_5) + \sigma(pp \rightarrow \phi_5^+ \phi_5^-)$$



$$[ \sigma_{\text{background}} = \sigma(pp \rightarrow WW) \text{Br}(W \rightarrow l\nu)^2 + \sigma(pp \rightarrow ZZ) \text{Br}(Z \rightarrow l^+ l^-) \text{Br}(Z \rightarrow \nu\nu) ]$$



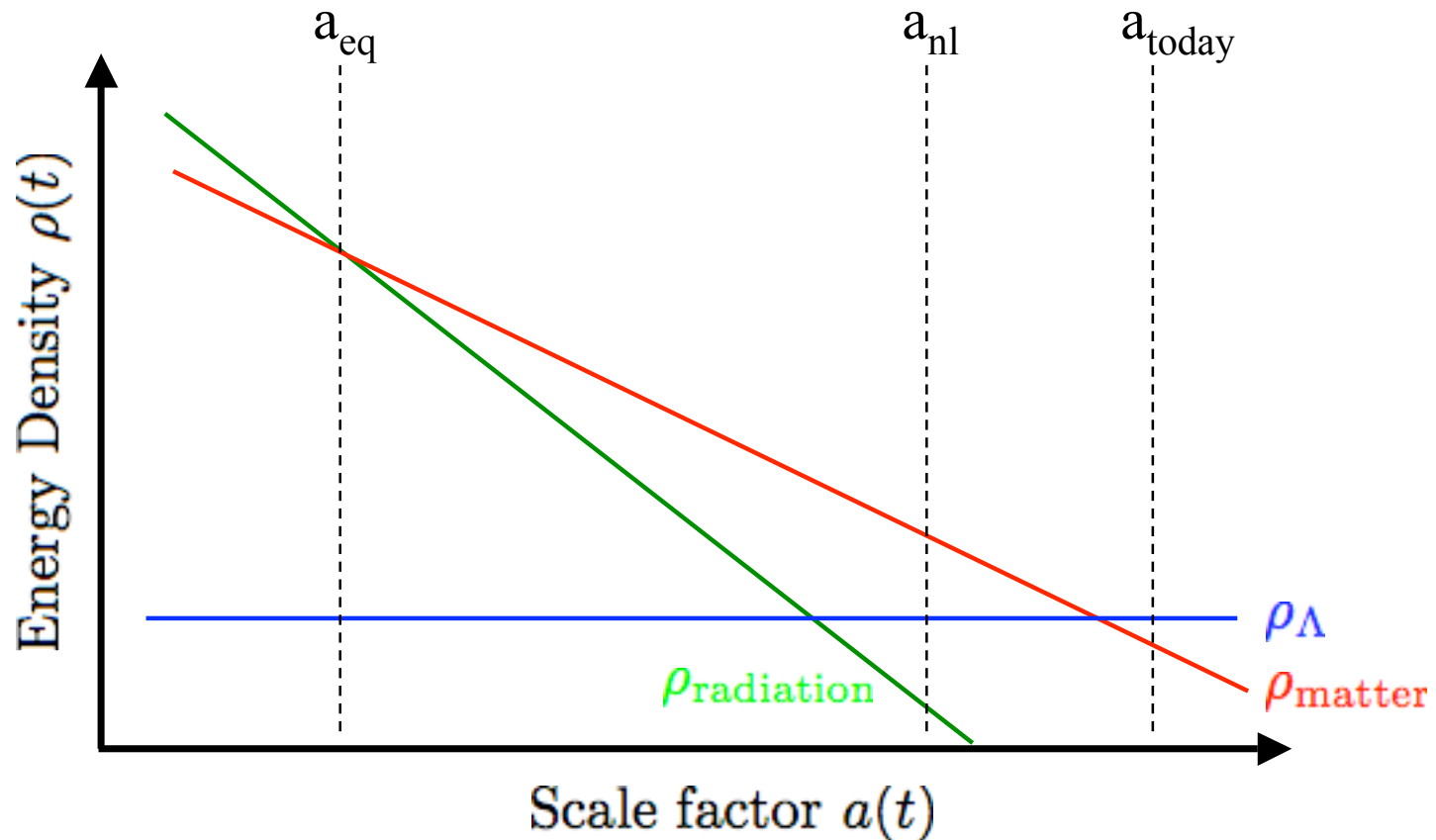
# Conclusions

- Introduce electroweak doublet with discrete symmetry to Standard Model
  - Unification & dark matter
- Two ranges for dark matter mass: light ( $\sim 80$  GeV) and heavy ( $> 200$  GeV)

	Light $m_a \sim 80$ GeV	Heavy $m_a > 200$ GeV
Direct Detection	CDMS II	SuperCDMS
Indirect Detection	GLAST, HESS	GLAST, HESS
SM Higgs Decay	Tevatron, LHC	No luck
Direct Production	LHC	ILC?



# Galactic Principle



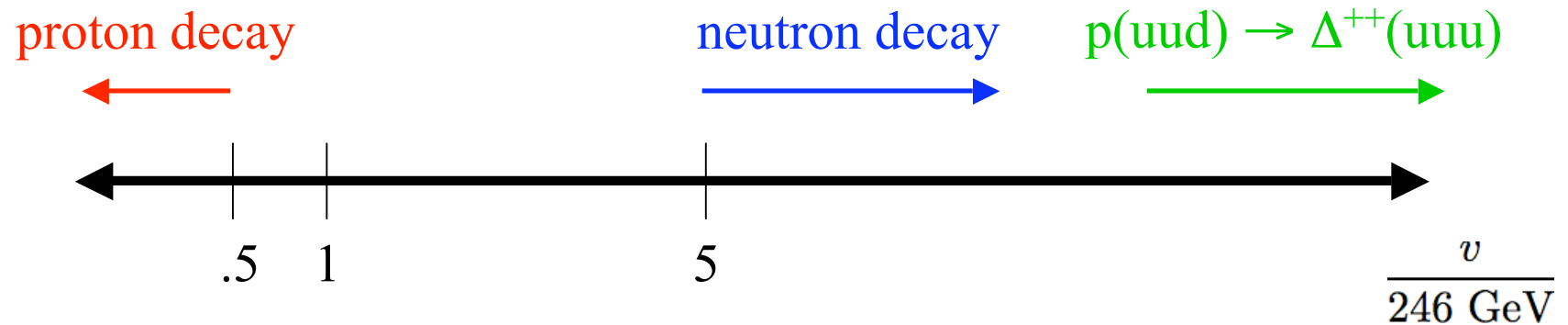
$$\rho_{\Lambda} \lesssim \rho_{\text{nl}}$$

No galaxies if C.C. larger than ( $\sim 100$  times) observed value

[Weinberg]

# Atomic Principle

$$m_n - m_p = \underbrace{(m_d - m_u)}_{\propto v} - \underbrace{E_{em}}_{1.7 \text{ MeV}}$$

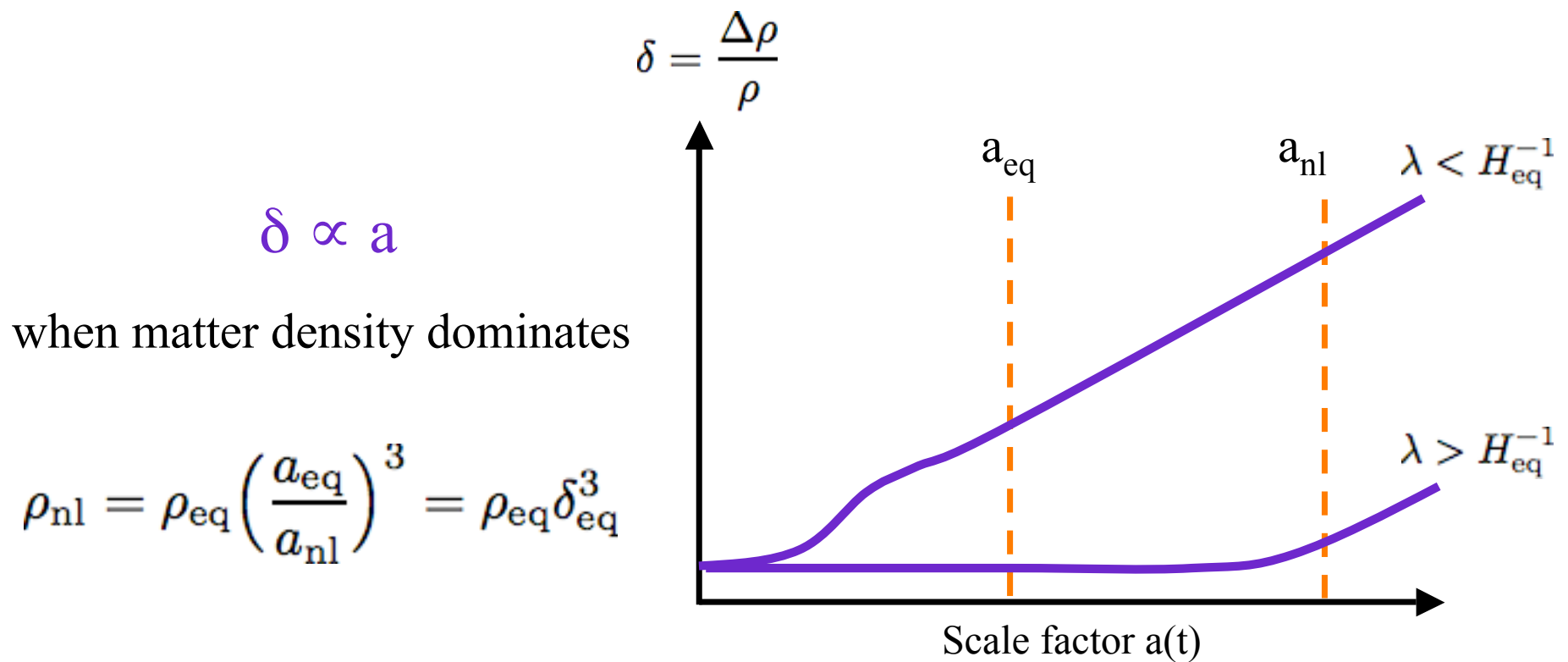


Complex chemistry if Higgs vev  $\sim$  factor of 5 of its observed value

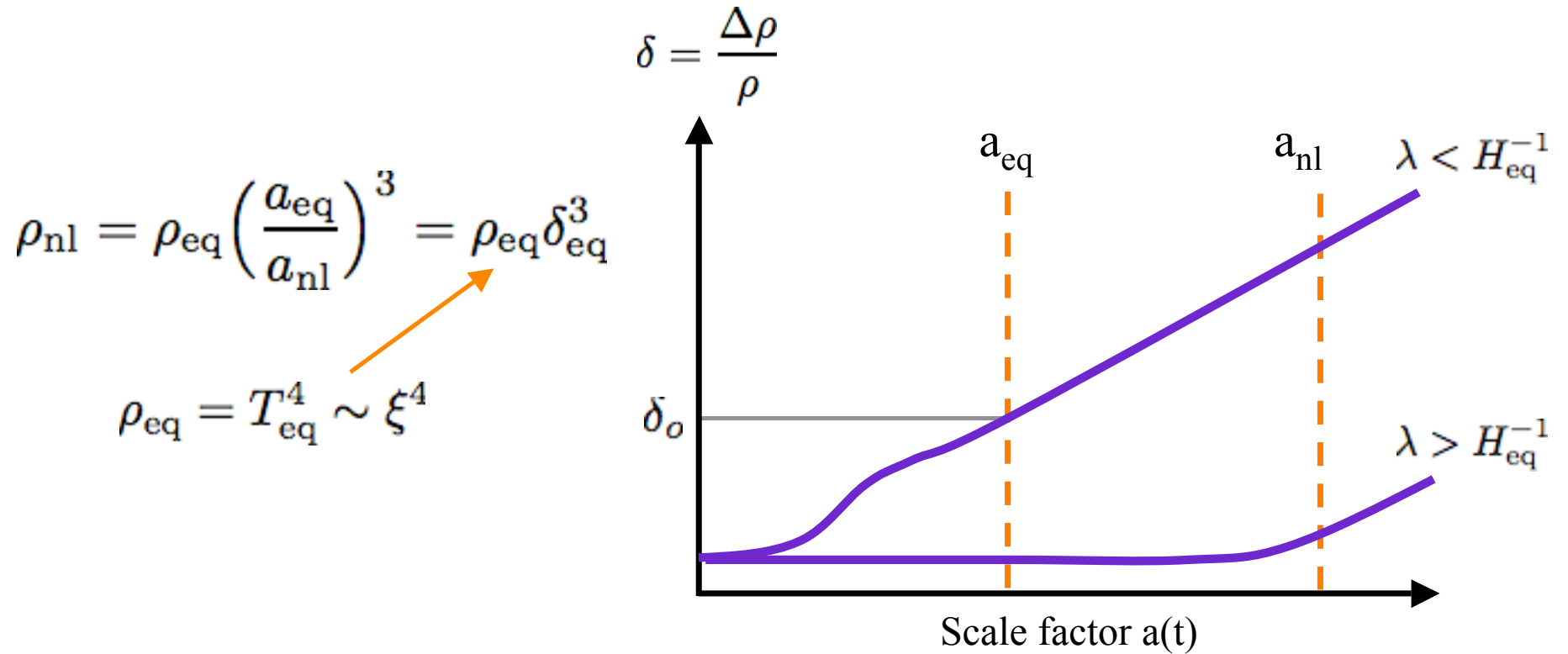
# Dark Matter Bound

Environmental selection bounds on  $\xi = \rho_{\text{dm}}/\rho_{\text{b}}$  ?

**Nonlinear** regime should set in **before** C.C. expansion takes over:  $\rho_{\Lambda} \lesssim \rho_{\text{nl}}$



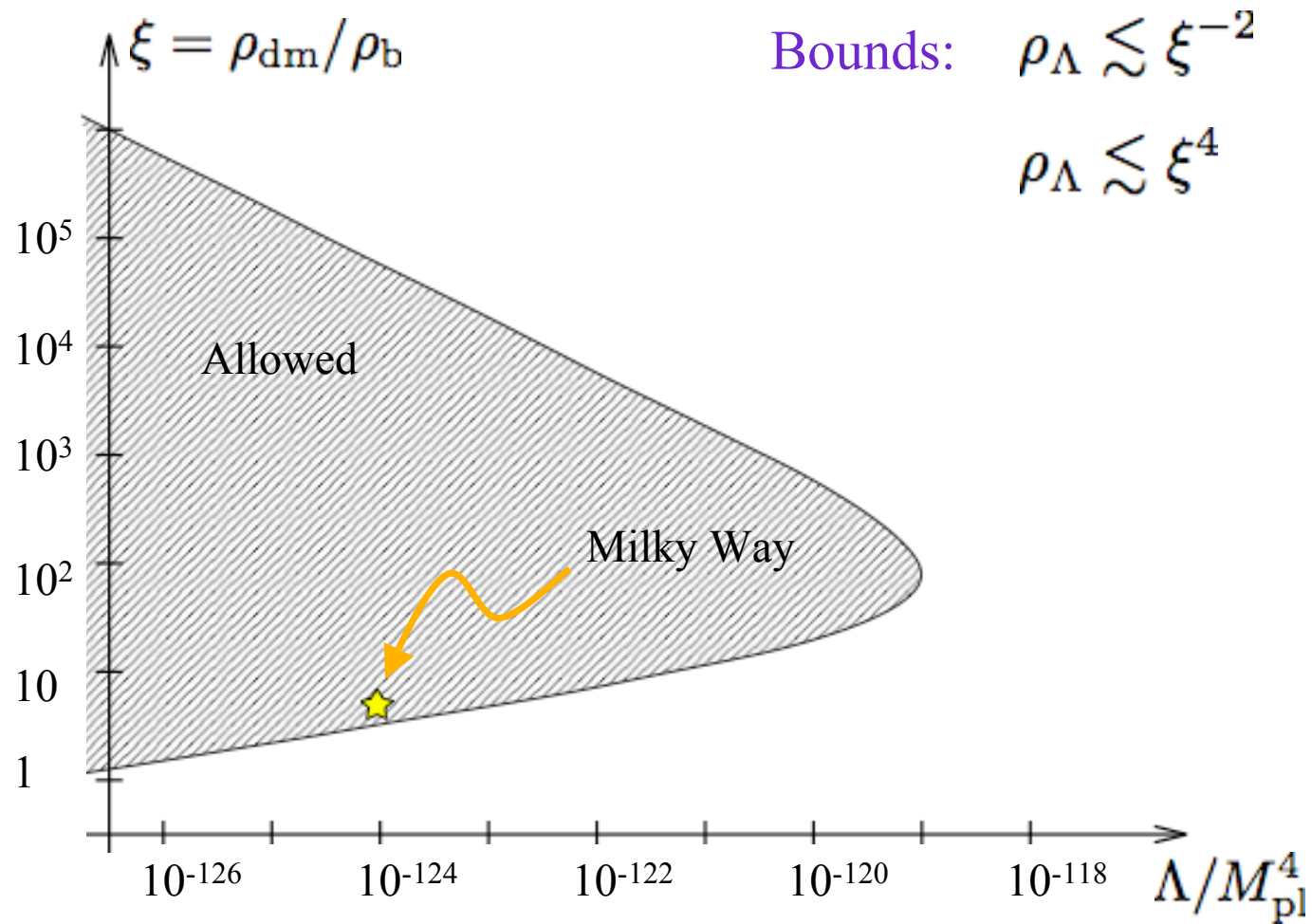
# Dark Matter Bound



$\delta_{\text{eq}}$  suppressed for large-scale modes

$$\delta_{\text{eq}} \sim \delta_o \left( \frac{\lambda}{H_{\text{eq}}^{-1}} \right)^{-2} \sim \delta_o \xi^{-8}$$

# Dark Matter Bound



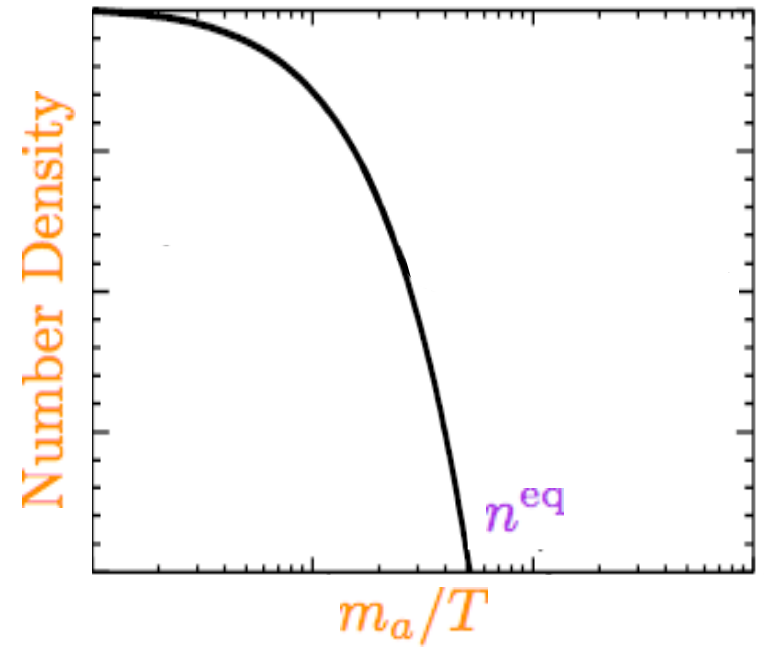
# Dark Matter Bound

- Annihilation cross section for WIMPs

$$\langle\sigma v\rangle\sim\frac{\alpha_w^2}{m_{\text{wimp}}^2}$$

- Interaction rate of WIMPs

$$\Gamma=\langle\sigma v\rangle n_{\text{wimp}}=\langle\sigma v\rangle\frac{\rho_{\text{dm}}}{m_{\text{wimp}}}$$

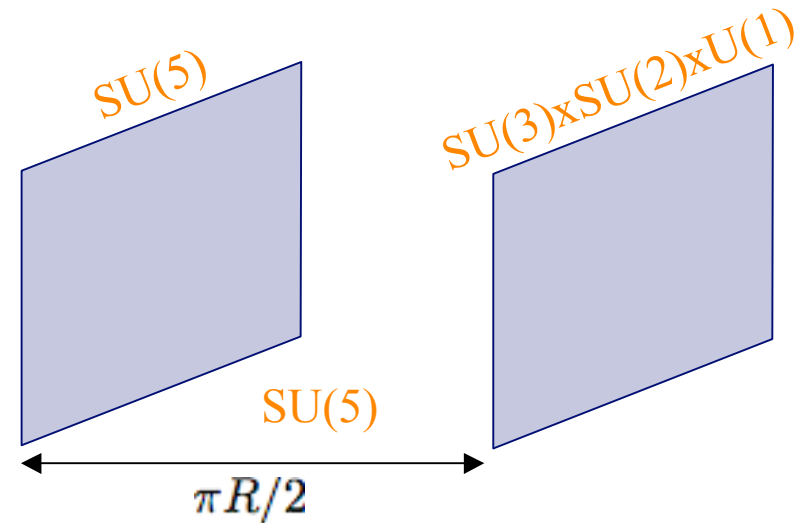




# Unification

## Potential mechanisms for suppressing proton decay rate

- Embed theory in **5D orbifold GUT**
  - configuration of fields in extra dimensions can **suppress** proton decay

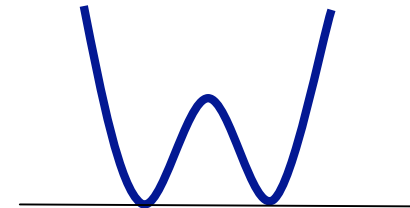


- **Trinification**:  $SU(3)_C \times SU(3)_L \times SU(3)_R$  broken  $\sim 10^{14}$  GeV
  - proton decay via gauge bosons is **forbidden**

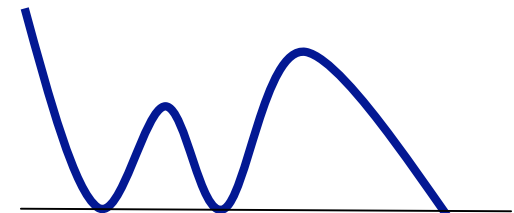
# Constraints on Quartics

- **Stability** of potential in all field directions at all energy scales:

$$V(\mu) > 0$$



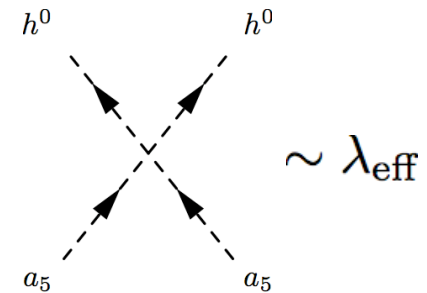
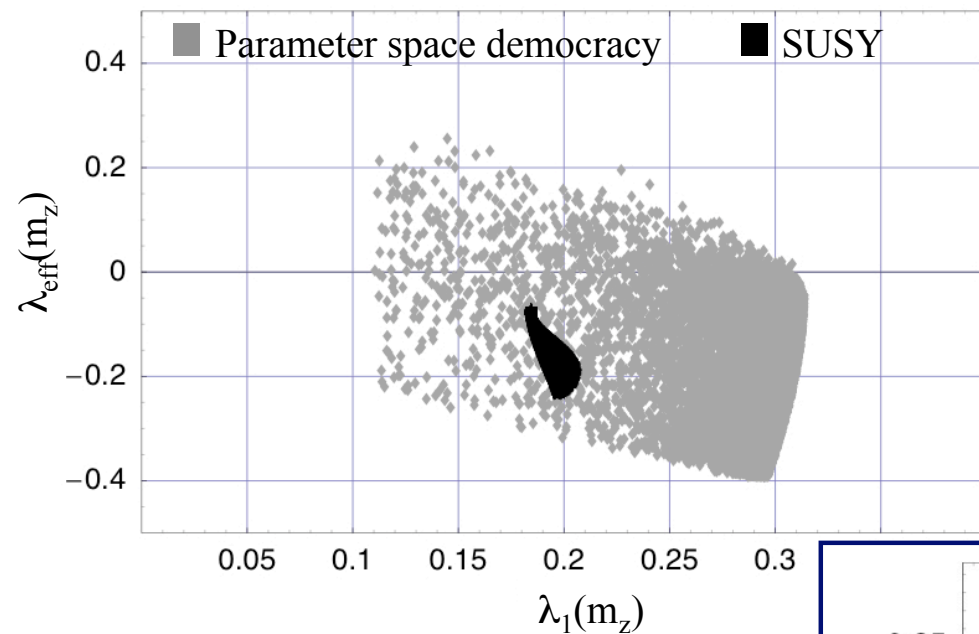
Stable Vacuum



Unstable Vacuum

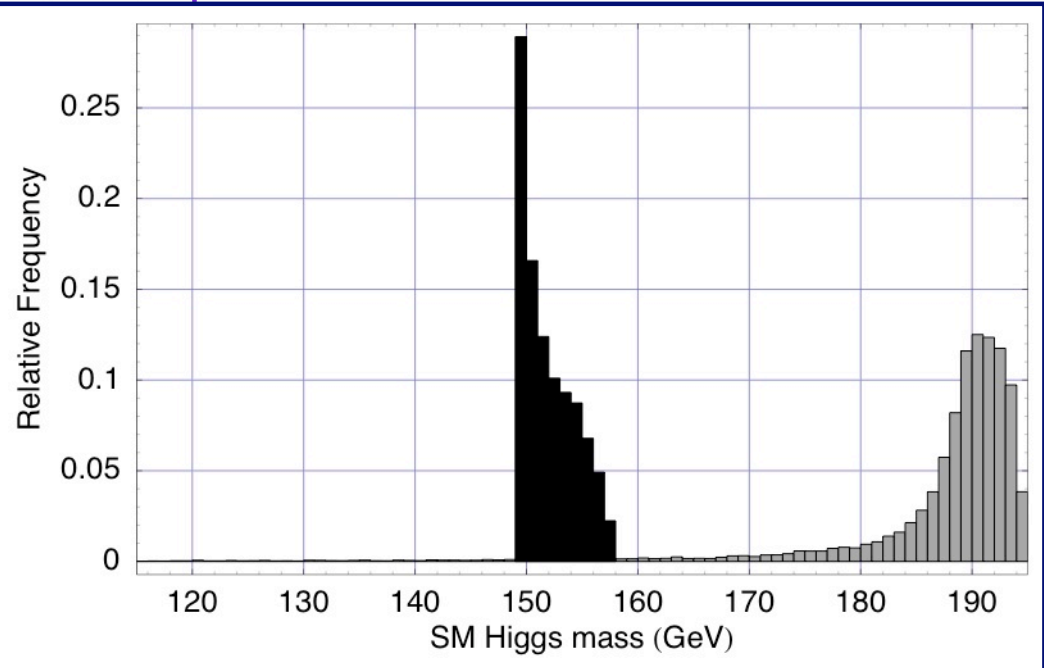
- Direct detection bound:  $|\lambda_5| \gtrsim 10^{-6}$
- Experimental bound on Higgs mass:  $\lambda_1 \gtrsim 0.107$
- Require that WIMP remains neutral:  $\lambda_4 - 2|\lambda_5| < 0$

# Parameter Space Democracy

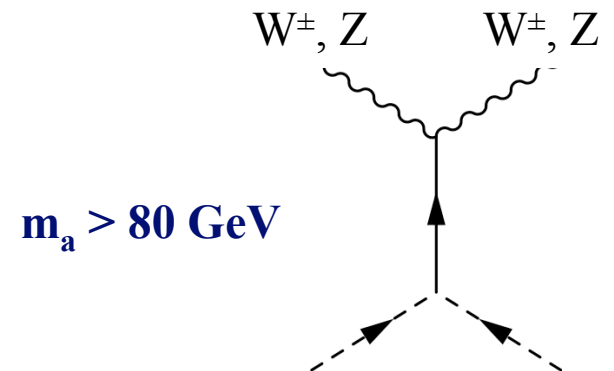
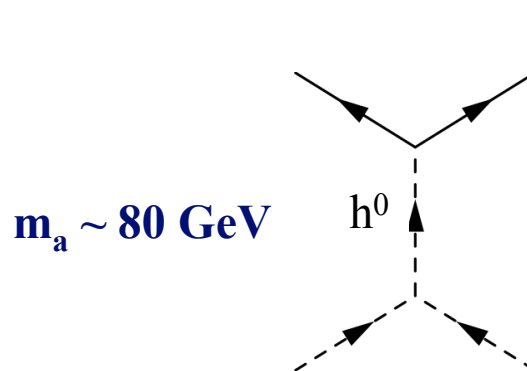
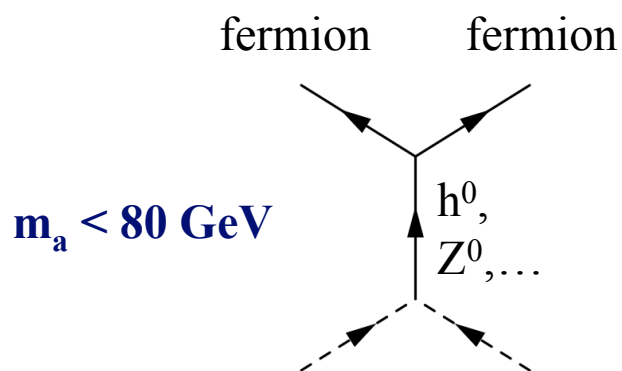
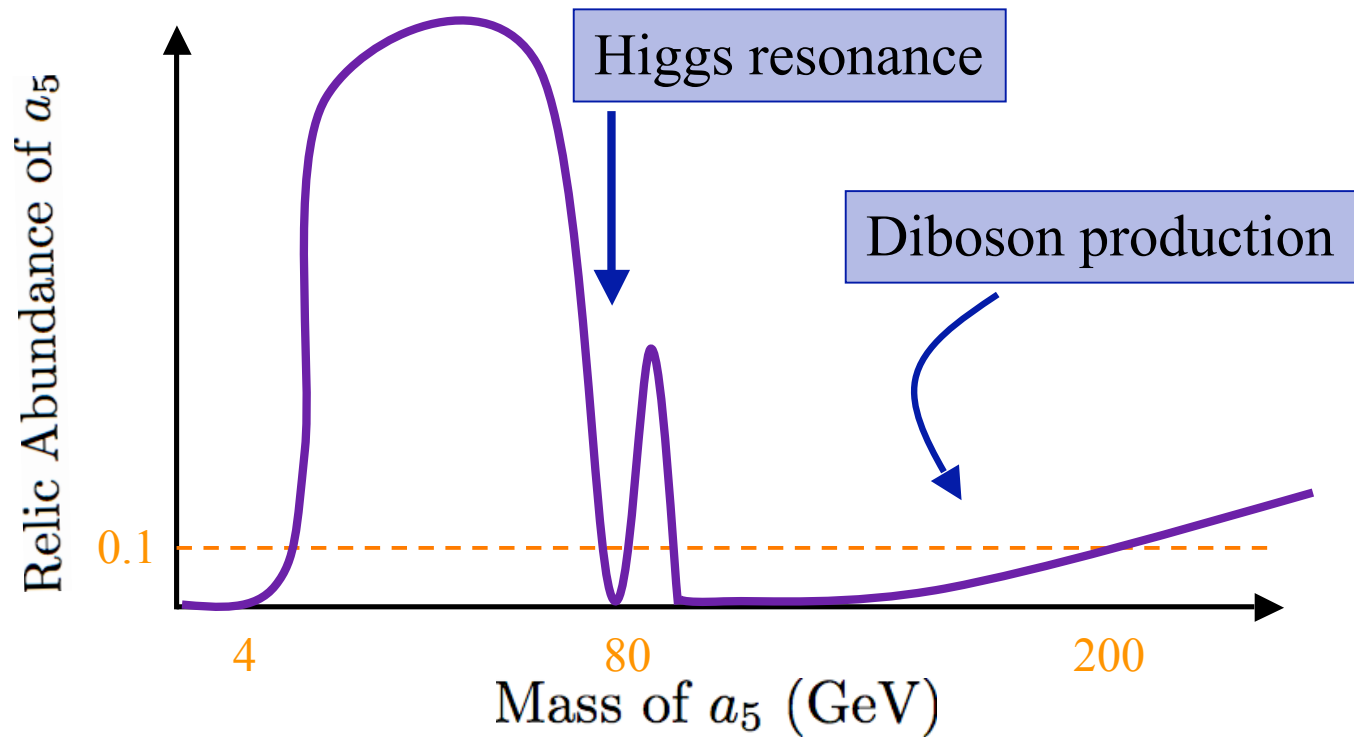


## SM Higgs Mass

Large range, peaked at  $\sim 200$  GeV




# Coannihilation

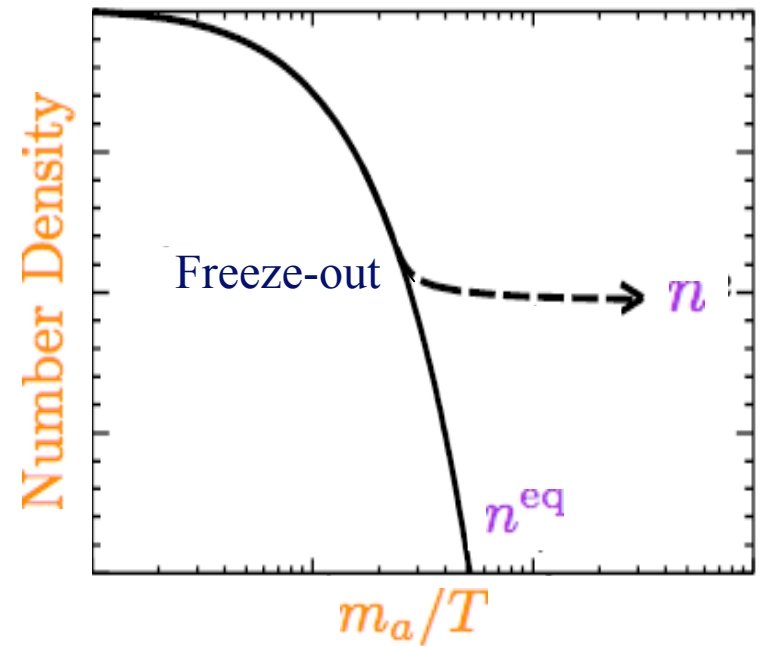


# Coannihilation

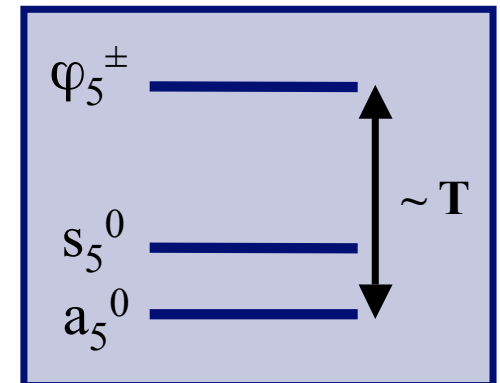
- Boltzmann equation is

$$\frac{dn}{dt} = -3Hn - \underbrace{\langle \sigma v \rangle [n^2 - (n^{\text{eq}})^2]}_{\text{Particle annihilation}}$$

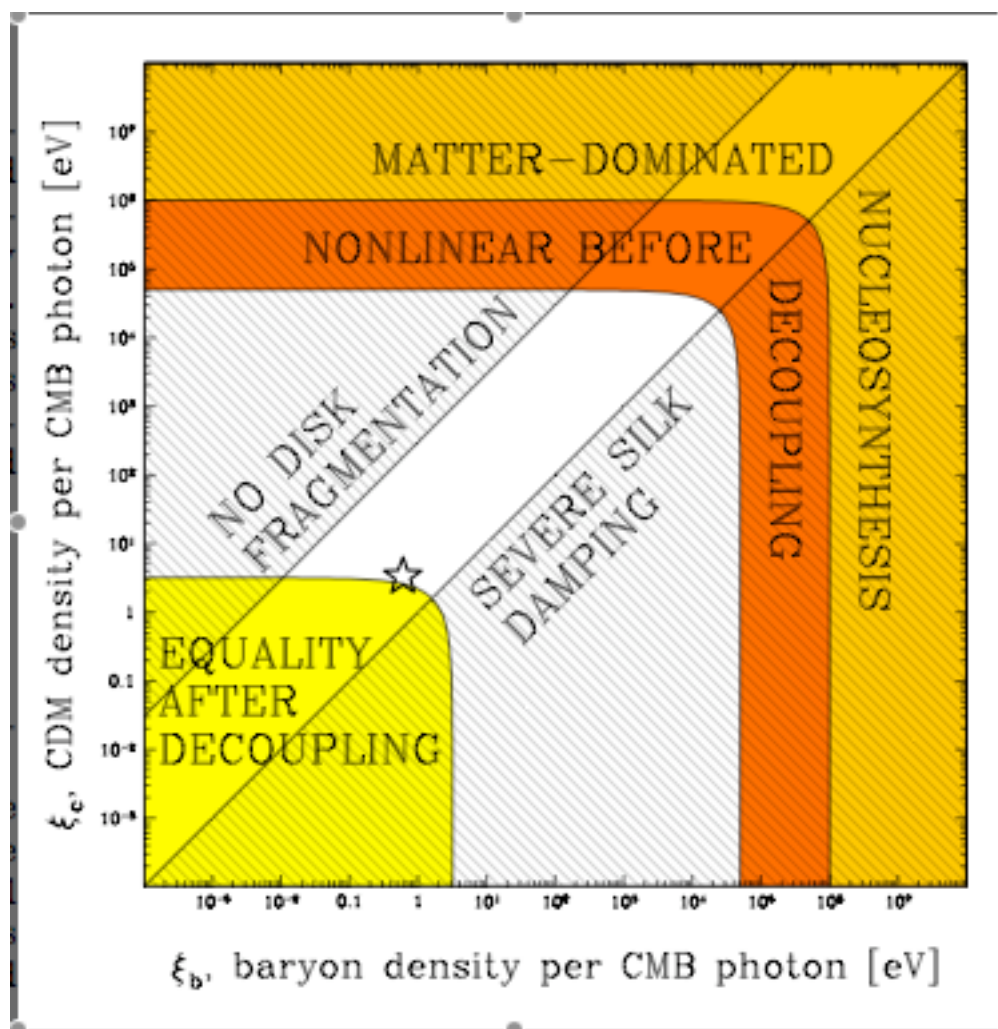

 Dilution from expansion of universe



- When **temperature** is on the order of the **mass splittings**,
  - interactions including  $s_5$  and  $\varphi_5^\pm$  can become important in determining relic density of  $a_5$



# Dark Matter Bounds

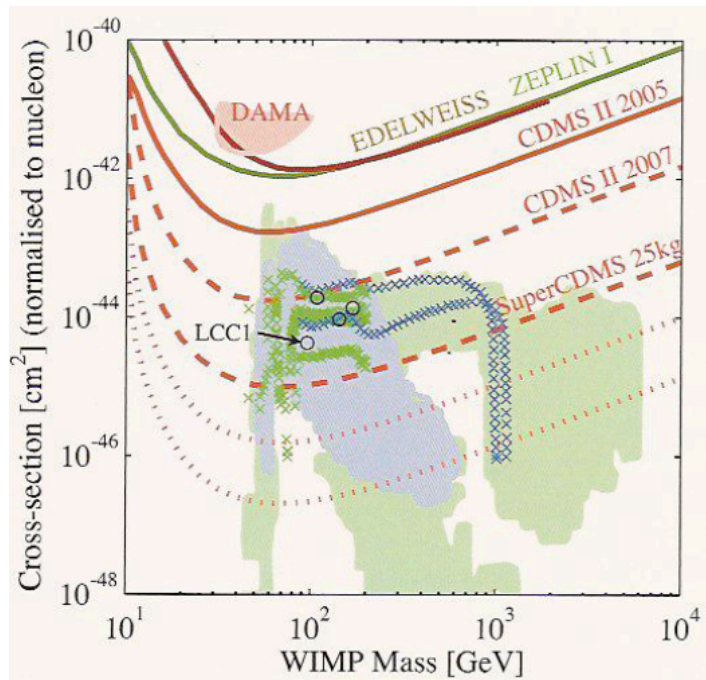
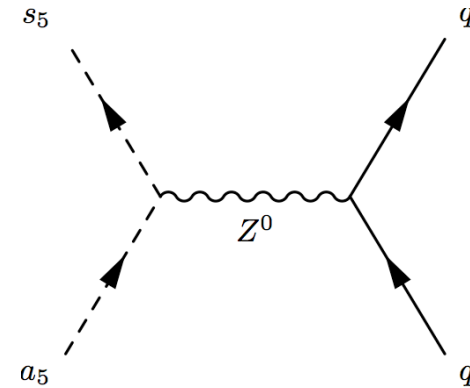




# Inelastic Scattering

- **Inelastic** scattering between nearly-degenerate  $a_5$  and  $s_5$  may also contribute to **spin-independent** cross section

$$\Delta m_{s^0 a^0} \simeq 100 \text{ keV}$$



- Inelastic scattering may reconcile **conflicting** results from DAMA and CDMS

$$\Delta m_{s^0 a^0} < \frac{\beta^2 m_{a^0} m_N}{2(m_{a^0} + m_N)}$$

- $m_N$  larger for DAMA  $\rightarrow$  **higher cutoff** for mass splittings that can be observed

[Smith & Weiner]

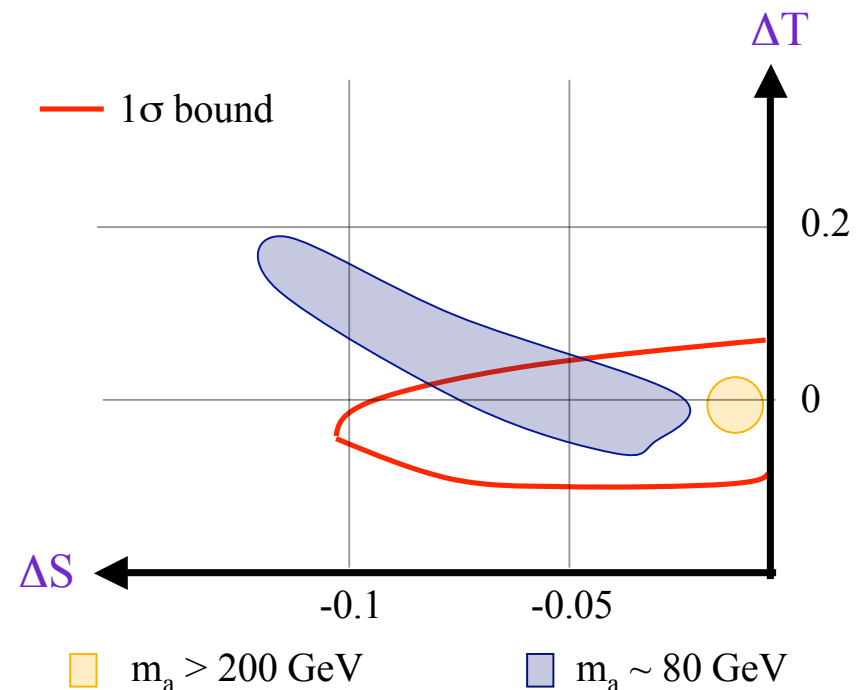
# Electroweak Precision Tests

Are masses and quartics consistent with electroweak data?

- For **small** mass differences, corrections to **S** and **T** parameters are

$$\Delta T \propto \frac{5}{m_a \alpha v^2} (m_{\phi^\pm} - m_a)(m_{\phi^\pm} - m_s) \quad \Delta S \propto \frac{5v^2}{m_a^2} \lambda_4$$

- Heavy** dark matter fits well within the experimental bound
- Some of the **light** dark matter region excluded experimentally



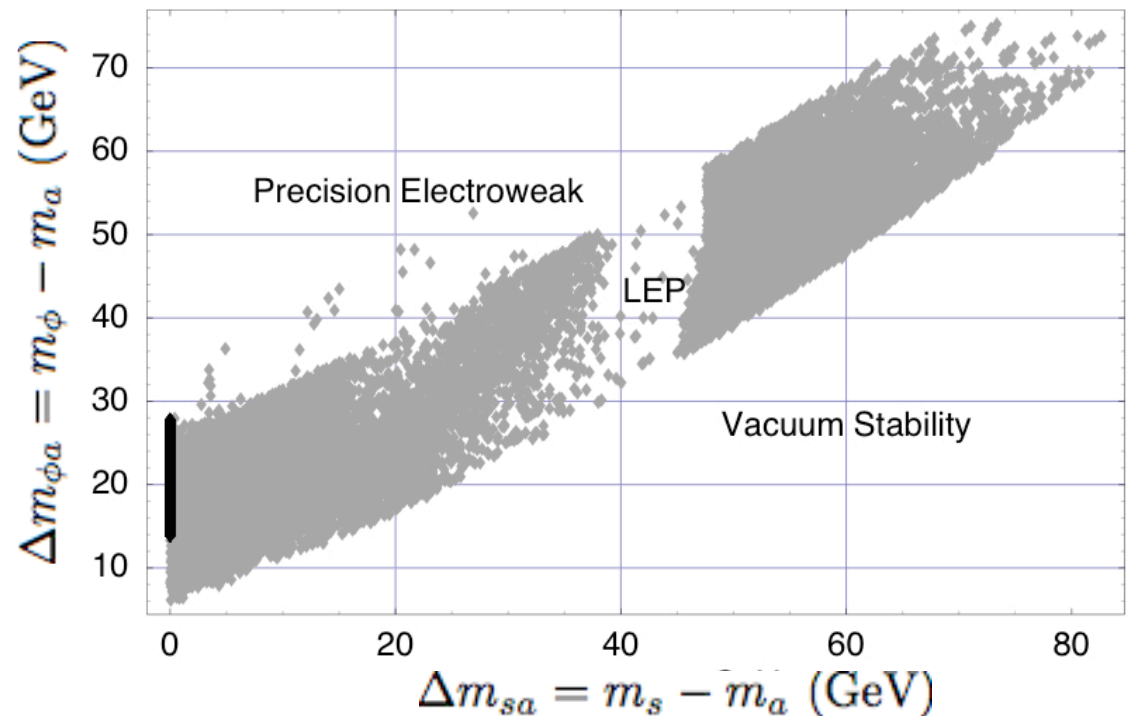


# Signatures at the LHC

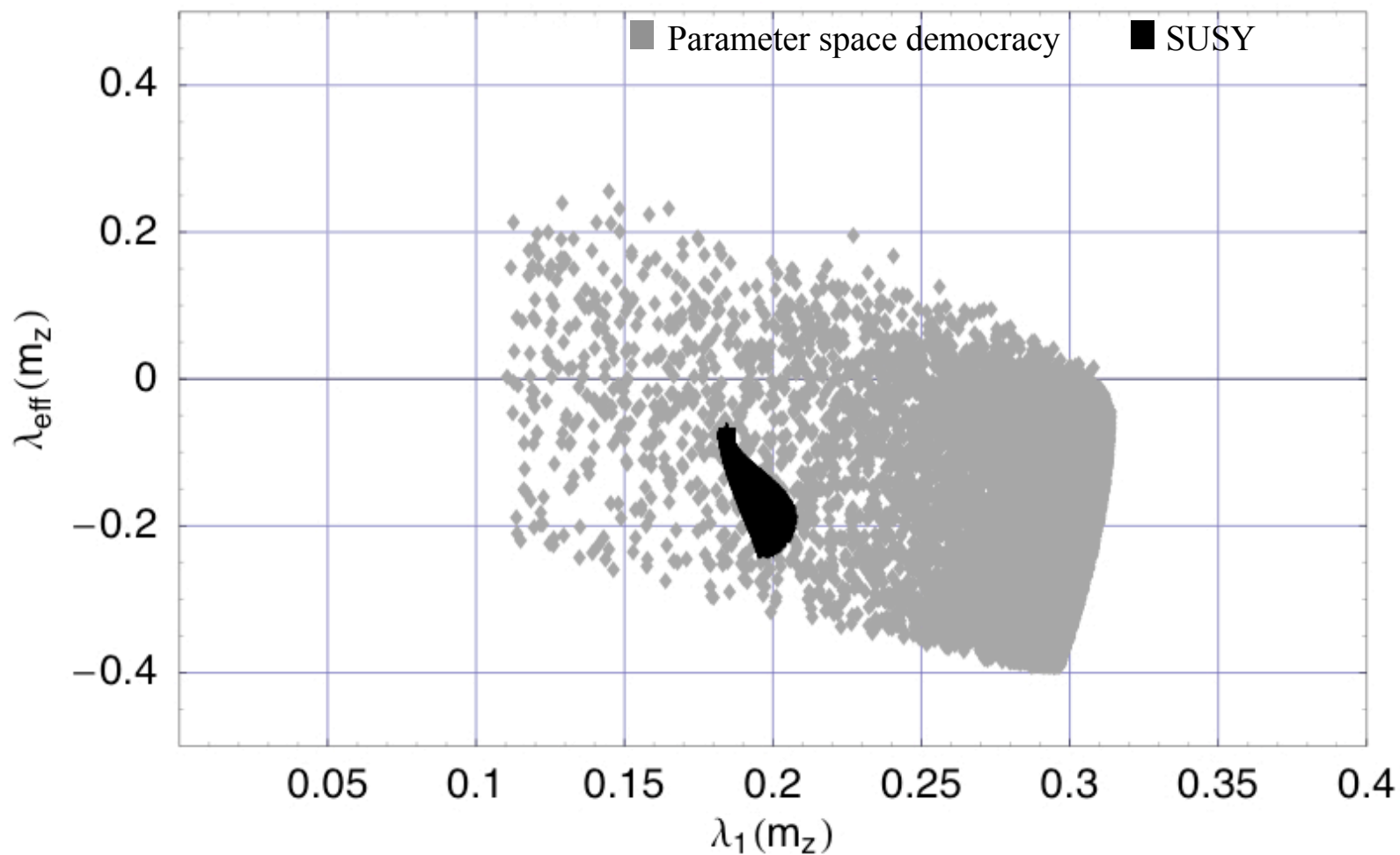
$H_5$  scalars may be produced at the LHC

$$\begin{aligned}
 p p &\rightarrow a_5^0 s_5^0 && \rightarrow Z^0 a_5^0 \\
 p p &\rightarrow a_5^0 \varphi_5^\pm && \rightarrow W^\pm a_5^0 \\
 p p &\rightarrow s_5^0 \varphi_5^\pm && \rightarrow Z^0 W^\pm 2a_5^0 \\
 p p &\rightarrow \varphi_5^\pm \varphi_5^\pm && \rightarrow 2W^\pm 2a_5^0
 \end{aligned}$$

- Gauge bosons are always **off-shell**
- Opposite-sign leptons +  $\cancel{E}_T$



# Direct Detection

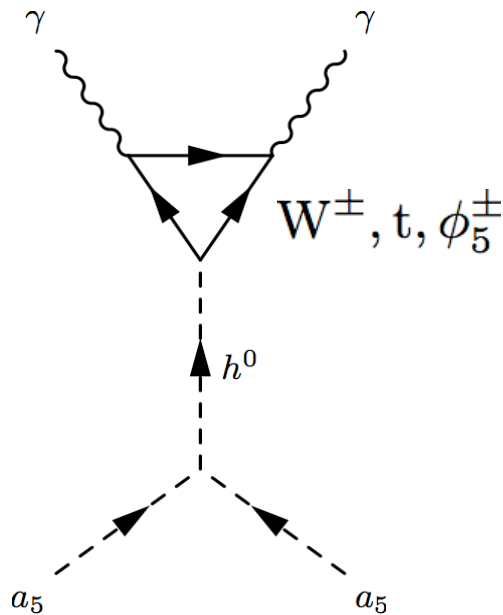


$$\sigma_n = 2 \times 10^{-9} \text{ pb} \left( \frac{\lambda_{\text{eff}}}{0.4} \right)^2 \left( \frac{350 \text{ GeV}}{m_{a^0}} \right)^2 \left( \frac{200 \text{ GeV}}{m_{h^0}} \right)^4$$

# Indirect Detection

Low-mass dark matter ( $\sim 80$  GeV)

s-channel Higgs exchange **dominates** over box diagrams



$$\sigma(a_5 a_5 \rightarrow \gamma\gamma)u \simeq \frac{1}{N_h} \frac{v^2 \lambda_{eff}^2}{(s - m_{h^0}^2)^2 + m_{h^0}^2 \Gamma_{h^0}^2} \frac{\Gamma(h^0 \rightarrow \gamma\gamma)}{\sqrt{s}}$$