

# Lepton Flavor Violation at the LHC

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# Overview

- Supersymmetry
- Neutrino Physics
- Seesaw Mechanism
- Low Energy Experiments
- LHC Signals
- Outlook: Slepton mass measurements at ILC
- Conclusion

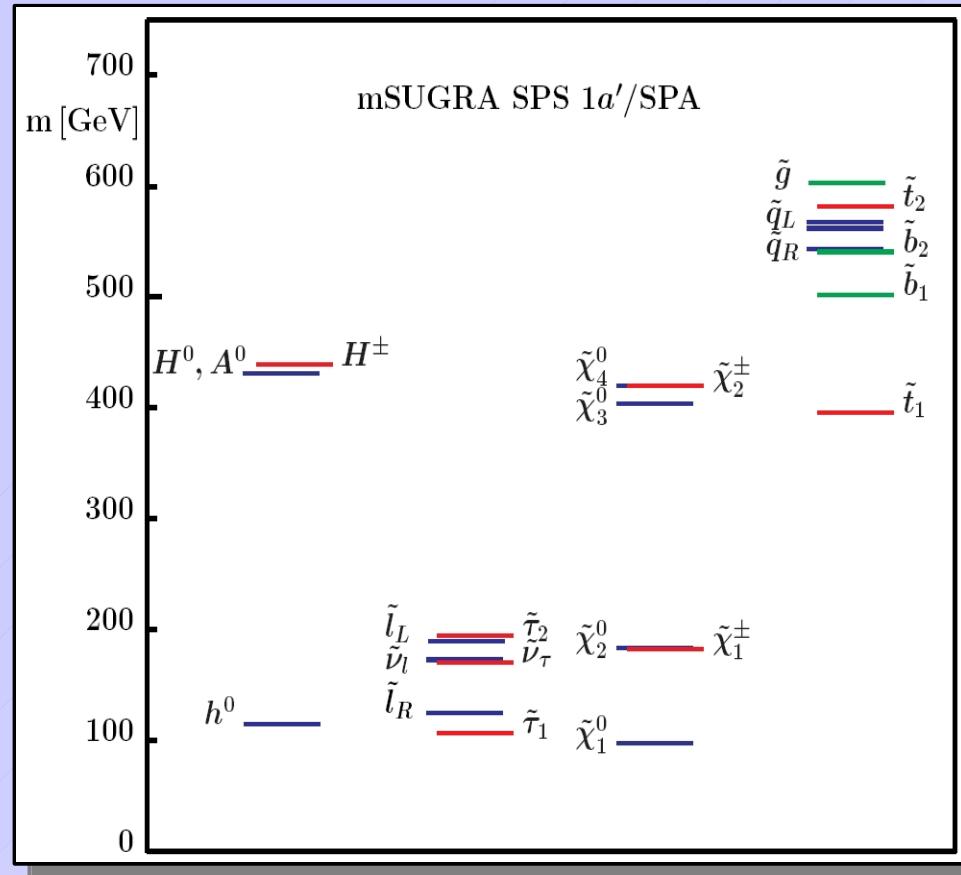
# mSUGRA

## MSSM

Minimal extension of the Standard Model with two Higgs doublets and conserved R-parity

## mSUGRA

- Theoretical framework for SUSY breaking
- Universality at  $M_{\text{GUT}}$
- No FCNC / CP Violation
- Five free parameters
  - $m_0$  common scalar mass
  - $m_{1/2}$  common gaugino mass
  - $A_0$  common trilinear coupling
  - $\tan\beta$  ratio of Higgs VEVs
  - $\text{sign}\mu$  sign of Higgs mixing
- SUSY particle spectrum generated by RG running



Scenario SPS1a':  
 $m_0 = 100 \text{ GeV}$ ,  $m_{1/2} = 250 \text{ GeV}$ ,  
 $A_0 = -100 \text{ GeV}$ ,  $\tan\beta = 10$ ,  $\text{sign}\mu = +$

# Neutrinos

- Experimental observation of neutrino flavor oscillations
- $\Rightarrow$  Neutrinos have masses and neutrino flavor is violated

$$U^T m_\nu U = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3})$$

$$U = \begin{pmatrix} c_{13} c_{12} & s_{12} c_{13} & s_{13} e^{-i\delta} \\ -s_{12} c_{23} - s_{23} s_{13} c_{12} & c_{23} c_{12} - s_{23} s_{13} s_{12} & s_{23} c_{13} \\ s_{23} s_{12} - s_{13} c_{23} c_{12} & -s_{23} c_{12} - s_{13} s_{12} c_{23} & c_{23} c_{13} \end{pmatrix} \times \text{diag}(e^{i\phi_1}, e^{i\phi_2}, 1)$$

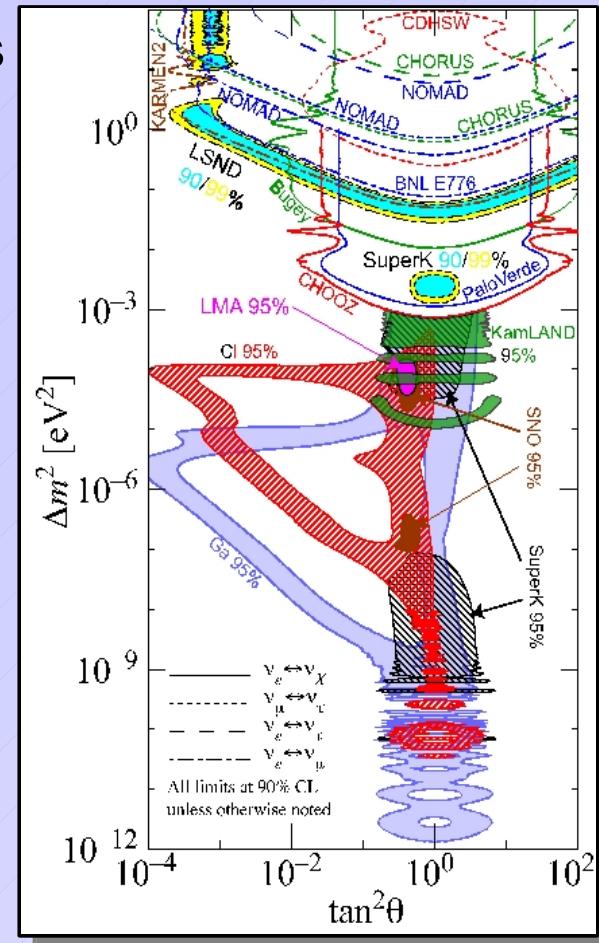
- Measured mixing angles and mass differences

$$\sin^2 \theta_{12} = 0.30^{+0.04}_{-0.05}, \sin^2 \theta_{23} = 0.50^{+0.14}_{-0.12}, \sin^2 \theta_{13} = 0.000^{+0.028}_{-0.000},$$

$$\Delta m_{12}^2 = (8.1^{+0.6}_{-0.6}) \cdot 10^{-5} \text{ eV}^2, \Delta m_{13}^2 = (2.2^{+0.7}_{-0.5}) \cdot 10^{-3} \text{ eV}^2$$

$\Rightarrow$  Nearly bi-maximal mixing  $\neq$  Quark mixing

- Absolute neutrino mass  $m_{\nu_1} = 0 \dots 0.5 \text{ eV}$  (Cosmology,  $0\nu\beta\beta$ )  
 $\Rightarrow$  much lighter than other fermions

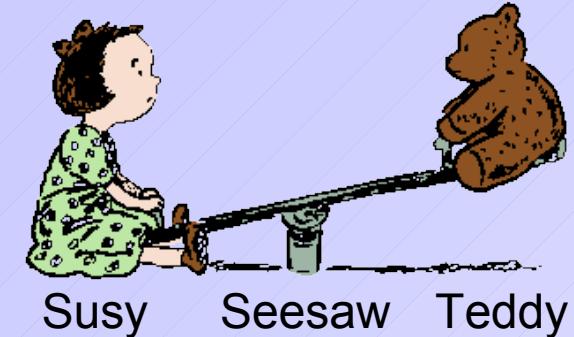


# SUSY Seesaw

## Mechanism

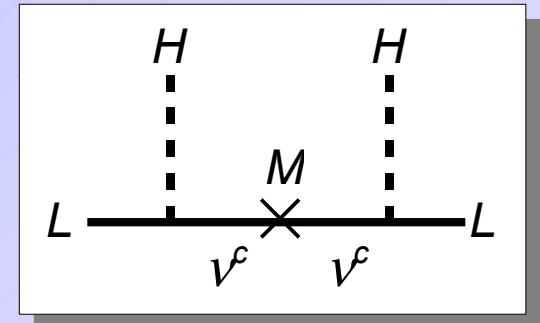
- Add right-handed neutrinos to (MS)SM particle content, Seesaw Type I:

$$W = W_{\text{MSSM}} - \frac{1}{2} \hat{\nu}_R^{cT} M_R \hat{\nu}_R^c + \hat{\nu}_R^{cT} Y_\nu \hat{L} \cdot \hat{H}_u$$



- Diagonalize seesaw matrix assuming super-heavy right-handed neutrinos

$$\begin{pmatrix} 0 & m_D^T \\ m_D & M_R \end{pmatrix} \text{ with } m_D = Y_\nu \langle H_u^0 \rangle \ll M_R$$



- Effective light neutrino mass matrix at low energies

$$m_\nu = m_D^T M^{-1} m_D \text{ for } m_D \ll M_R \quad m_\nu \approx 0.1 \text{ eV} \left( \frac{m_D}{100 \text{ GeV}} \right)^2 \left( \frac{M_R}{10^{14} \text{ GeV}} \right)^{-1}$$

# SUSY Seesaw

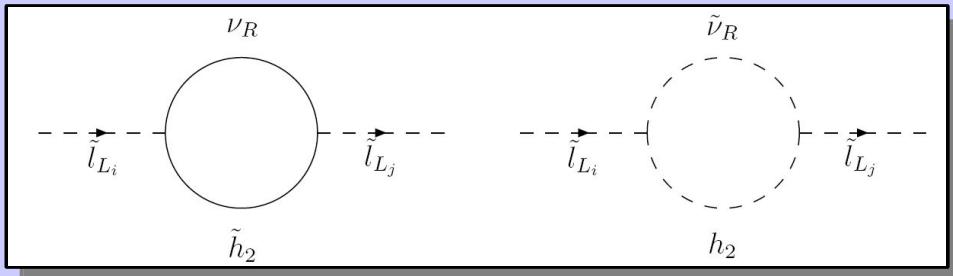
## Sleptons

### Non-SUSY Seesaw

- Ch. LFV is extremely suppressed by tiny  $\nu$  masses, e.g.  $\text{Br}(\mu \rightarrow e\gamma) = 10^{-34}$

### SUSY Seesaw

- Neutrino flavor mixing radiatively induces slepton flavor mixing from  $M_{\text{GUT}}$  to the right-handed neutrino mass scales



Slepton mass matrix (6x6)

$$m_{\tilde{l}}^2 = \begin{pmatrix} m_{\tilde{L}}^2 & (m_{\tilde{L}R}^2)^+ \\ m_{\tilde{L}R}^2 & m_{\tilde{R}}^2 \end{pmatrix}$$

- Correlation between slepton and neutrino flavor mixing

$$(\delta m_{\tilde{L}}^2)_{ij} = \frac{-1}{8\pi^2} (3m_0 + A_0) (Y_\nu^+ L Y_\nu)_{ij}$$

$$(\delta m_{\tilde{R}}^2)_{ij} = 0$$

$$L = \log \left( \frac{M_{\text{GUT}}}{M_{\nu_{ri}}} \right) \delta_{ij}$$

$$(\delta m_{\tilde{L}R}^2)_{ij} = \frac{-3A_0}{8\pi^2} Y_e (Y_\nu^+ L Y_\nu)_{ij}$$

→ Charged LFV



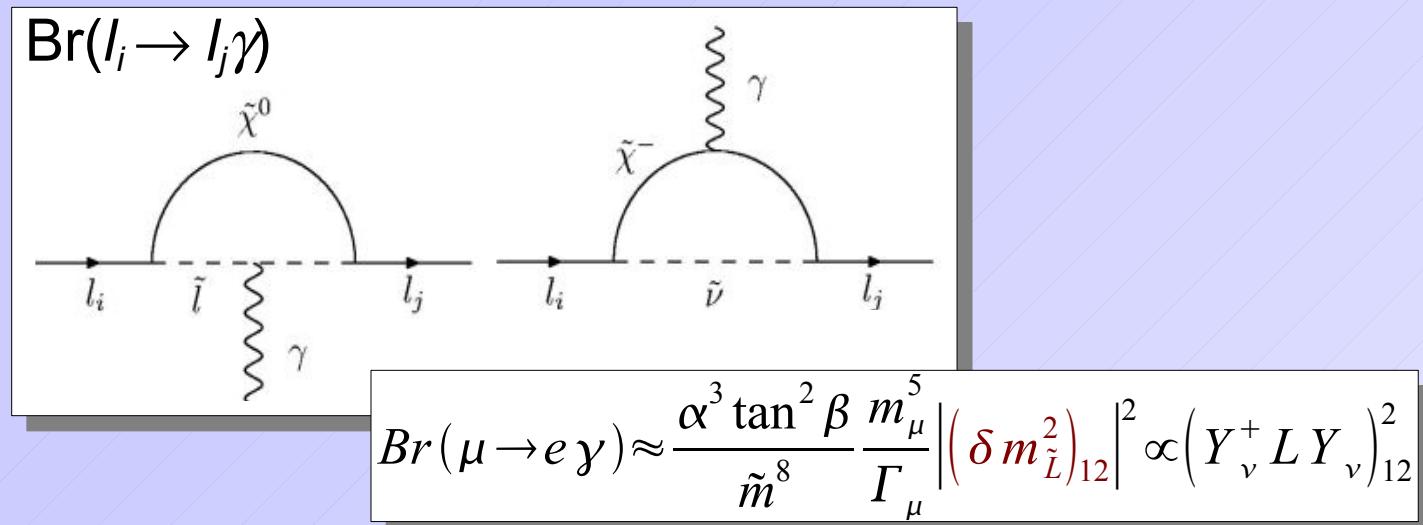
Additional observables lifting ambiguities in the neutrino sector, see e.g. Talk by F. Plentinger (Plentinger, Seidl, Winter, arXiv:0707.2379)

# Rare LFV Decays

- Current bounds and future sensitivities

- $\text{Br}(\mu \rightarrow e \gamma)$	$< 1.2 \cdot 10^{-11}$ (MEGA)	$10^{-13}$ (MEG)
- $\text{Br}(\tau \rightarrow \mu \gamma)$	$< 3.1 \cdot 10^{-7}$ (Belle)	$10^{-8}$ (Super-B Factory, LHC?)
- $\text{Br}(\tau \rightarrow e \gamma)$	$< 3.7 \cdot 10^{-7}$ (BaBar)	$10^{-8}$ (Super-B Factory)
- $\mathcal{R}(\mu N \rightarrow e N) < 7 \cdot 10^{-13}$	(Sindrum)	$10^{-18}$ (PRIME) ( $\mu \rightarrow e$ conversion in nuclei)
- $\mu \rightarrow 3e, \tau \rightarrow 3\mu$ (LHC), etc.		

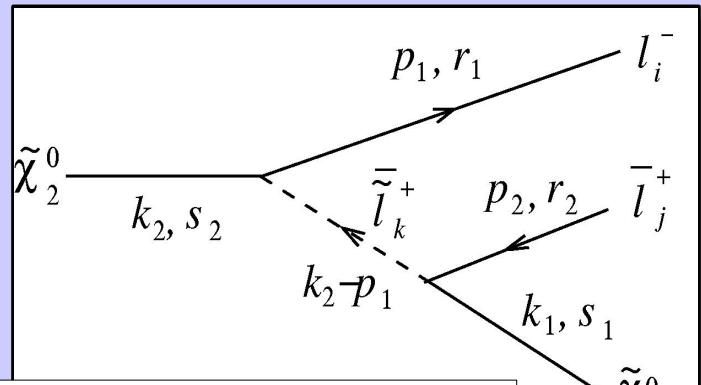
- SUSY Seesaw



# LFV at the LHC

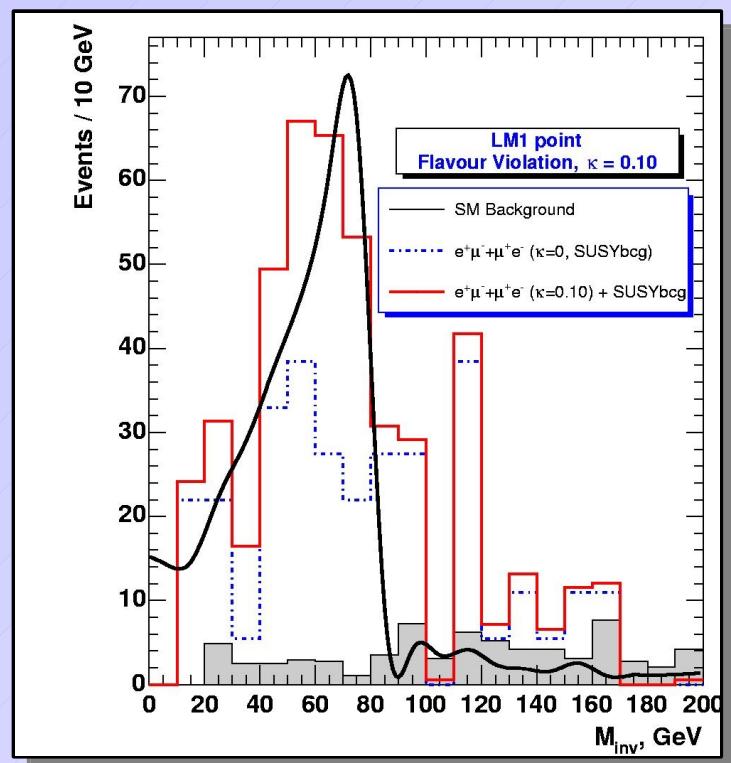
## Process

- Squark and gluino production
- $$pp \rightarrow \tilde{q} \tilde{q}, \tilde{g} \tilde{q}, \tilde{g} \tilde{g}$$
- ... followed by cascade decays via second lightest neutralino
- $$\tilde{q}(\tilde{g}) \rightarrow \tilde{\chi}_2^0 q(g)$$
- ... followed by LFV decay via sleptons  
(Agashe/Graesser, Hisano et al., Bartl et al.)



$$Br(\tilde{\chi}_2^0 \rightarrow \mu^- e^+ \tilde{\chi}_1^0) \propto \frac{|(\delta m_L^2)_{12}|^2}{m_{\tilde{l}}^2 \Gamma_{\tilde{l}}^2} Br(LFC)$$

- Possible signal signatures
- $$pp \rightarrow l_i l_j + 2 j + E_T^{\text{miss}}$$
- $$l_i l_j + 3 j + E_T^{\text{miss}}$$
- $$l_i l_j l_k l_k + 2 j + E_T^{\text{miss}}$$
- Exploit edge structure of signal invariant mass distribution



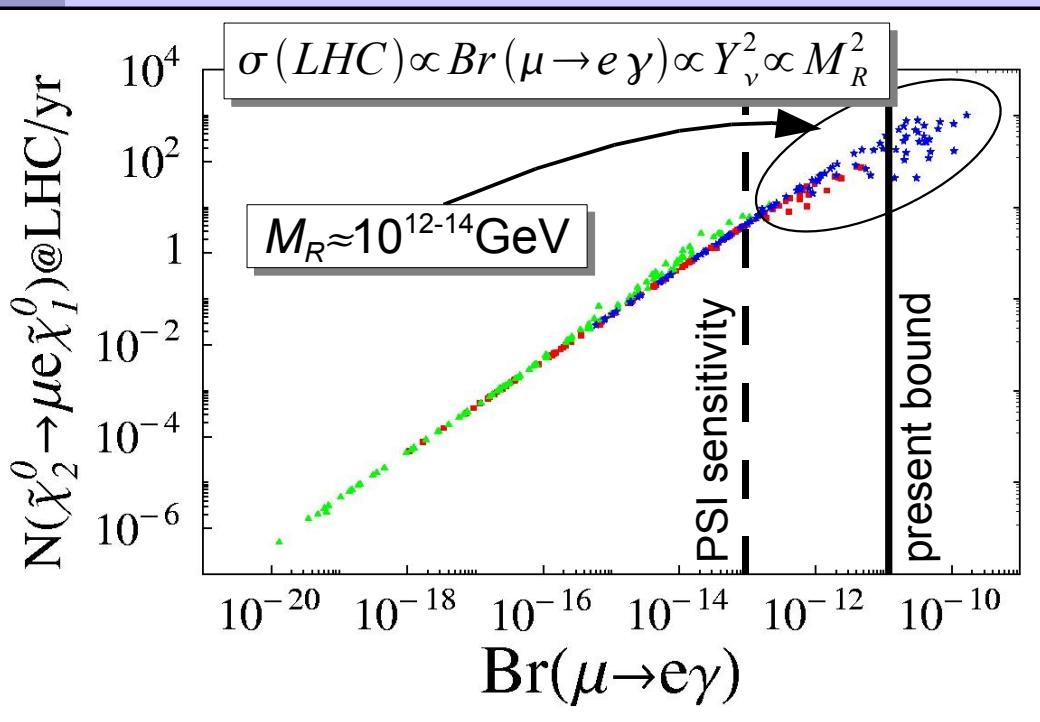
Andreev et al, hep-ph/0608176

- Rough estimate:

$$N(\tilde{\chi}_2^0 \rightarrow \mu^- e^+ \tilde{\chi}_1^0) = 200 \Rightarrow 5\sigma @ L = 100 \text{ fb}^{-1}$$

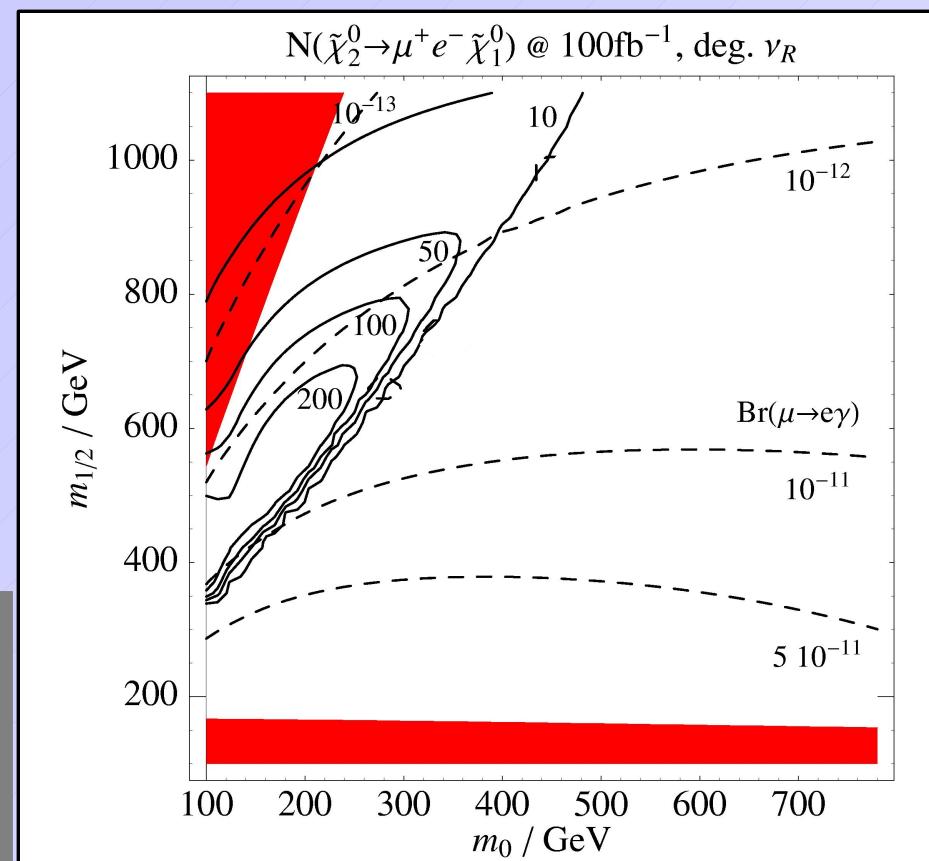
# LFV at the LHC

## Results



Correlation with  $Br(\mu \rightarrow e\gamma)$

- Fixed mSUGRA scenario: SPS1a
- Variation of neutrino parameters, **deg L/R**, **hier L/R** and **hier L/deg R** neutrinos

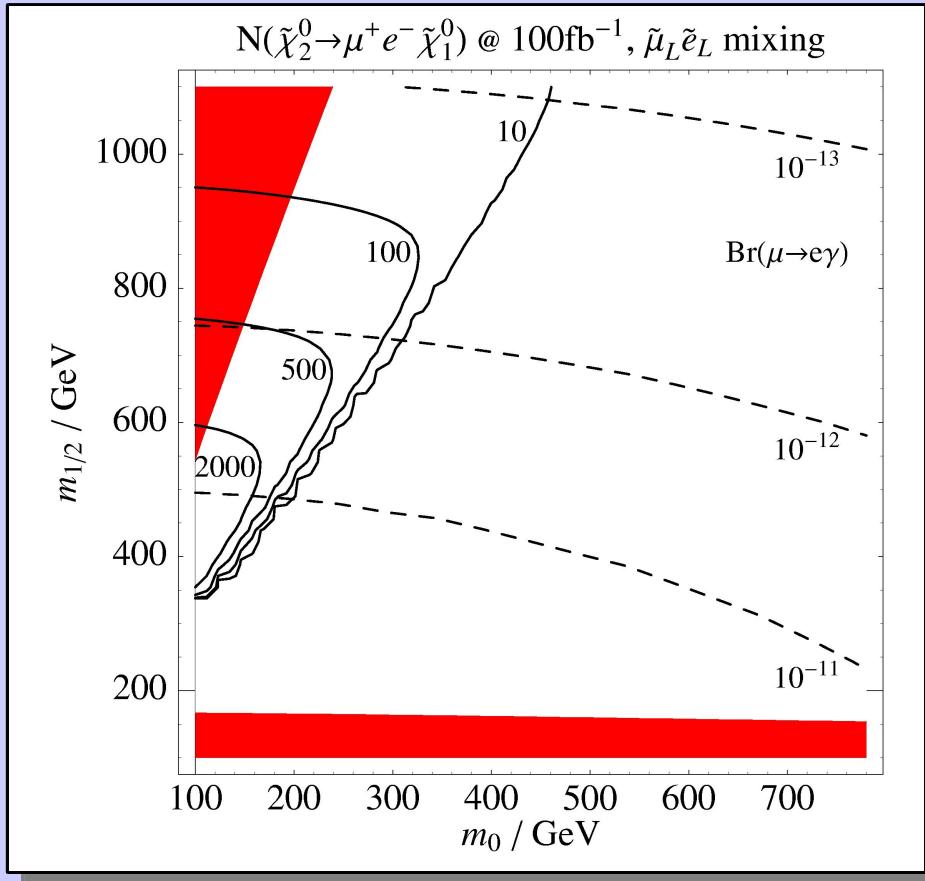


### Comparing sensitivity reach

- Fixed neutrino parameters: hierarchical light, degenerate heavy:  $M_R = 10^{14} \text{ GeV}$
- Variation of  $m_{1/2}$ ,  $m_0$   
( $A_0 = 0$ ,  $\tan\beta = 10$ ,  $\text{sign}\mu = +$ )

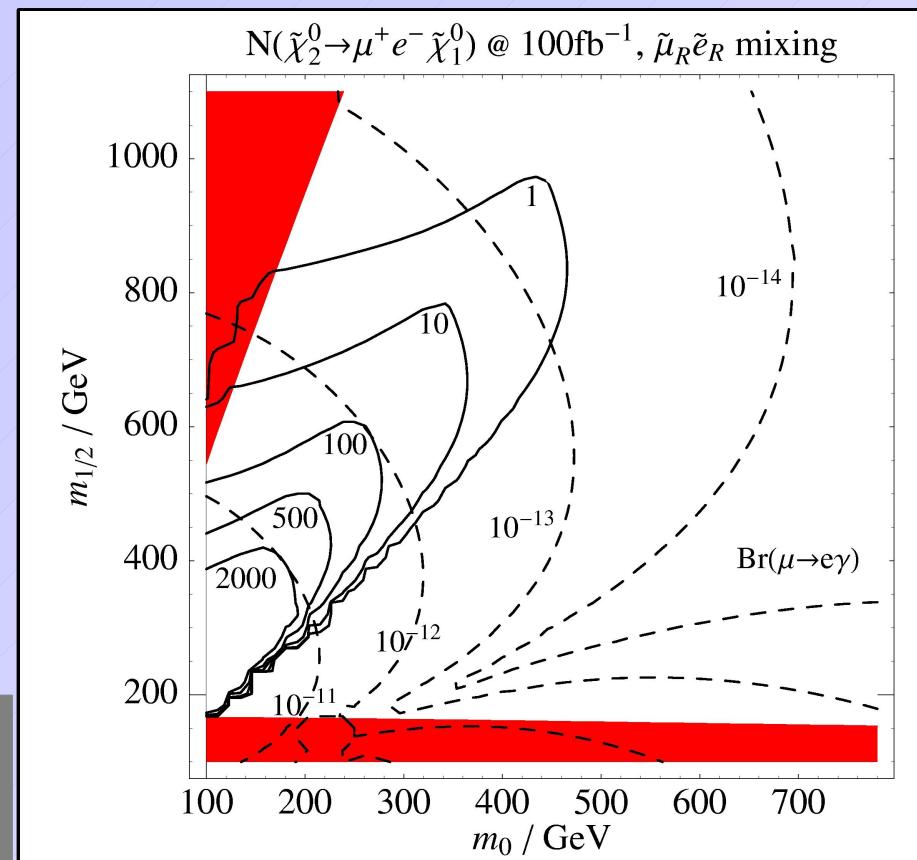
# LFV at the LHC

## General Slepton Mixing (2 Flavor)



Maximal left-handed slepton mixing

$$\begin{pmatrix} \tilde{l}_1 \\ \tilde{l}_2 \end{pmatrix} = \begin{pmatrix} c_{\theta_L} & s_{\theta_L} \\ -s_{\theta_L} & c_{\theta_L} \end{pmatrix} \cdot \begin{pmatrix} \tilde{e}_L \\ \tilde{\mu}_L \end{pmatrix}, \theta_L = \frac{\pi}{4}, \Delta \tilde{m} = 1 \text{ GeV}$$



Maximal right-handed slepton mixing

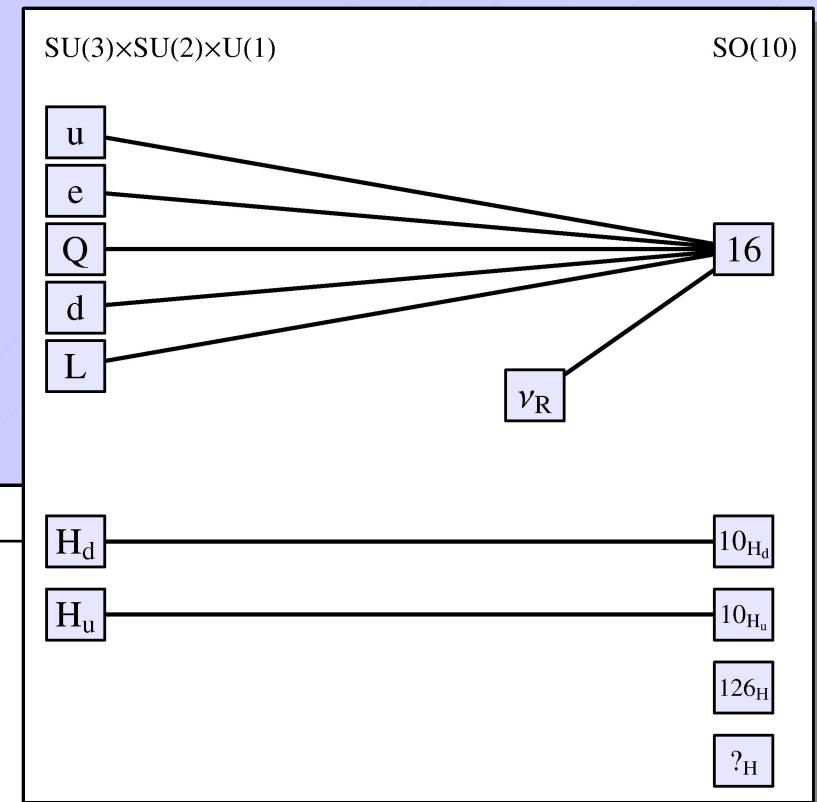
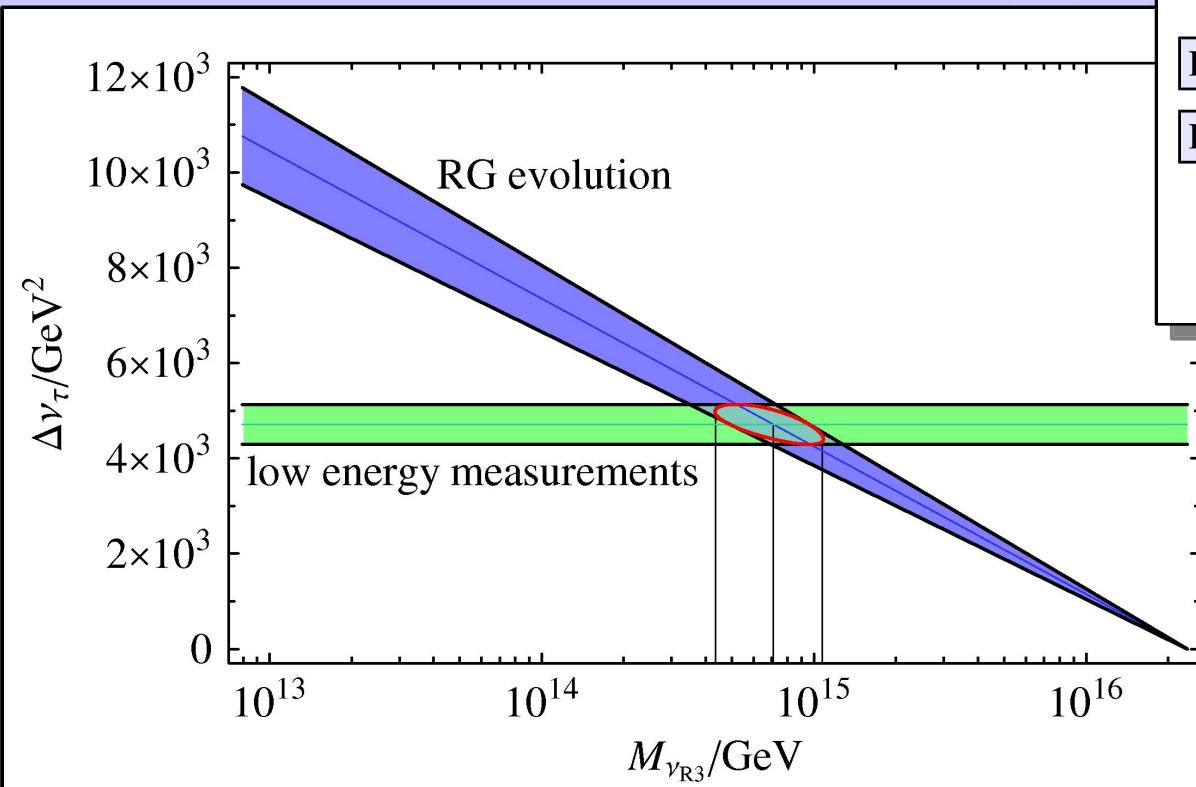
$$\theta_R = \frac{\pi}{4}, \Delta \tilde{m} = 1 \text{ GeV}$$

# Outlook: Determination of $M_{\nu_{R3}}$ and $m_{\nu_1}$ at ILC

- SUSY Seesaw Loops also generate a shift in third generation L-slepton mass

$$\Delta_{\nu_\tau} \approx \frac{m_t^2(\Lambda_U)}{4\pi^2 v_u^2} (3m_{16}^2 + A_0^2) \log \frac{\Lambda_U^2}{M_{\nu_{R3}}^2}$$

- Precision mass measurements at ILC in a SUSY SO(10) model (FFD, Freitas, Porod, Zerwas)



- Heavy neutrino mass

$$M_{\nu_{R3}} = 10^{14.9 \pm 0.2} \text{ GeV}$$

- Light neutrino mass

$$m_{\nu_1} = 10^{-2.5 \pm 0.3} \text{ eV}$$

# Conclusion

- SUSY Seesaw induces charged LFV processes
  - Rare decays, e.g.  $Br(\mu \rightarrow e\gamma)$ , and other low energy processes
  - Decays of second lightest neutralino at the LHC
  - Correlations among these processes and neutrino parameters
- Sensitivity comparison
  - Complementary sensitivity of low and high energy processes
  - Radiative processes have higher mass reach
  - Collider provide more information (sparticle masses etc.)
- Determination of model parameters
  - SUSY observables can lift neutrino parameter ambiguities
  - e.g.  $Br(\mu \rightarrow e\gamma) = 10^{-11}$ ,  $N(LHC) = 200 \Rightarrow M_R \approx 10^{12-14} \text{ GeV}$
  - Implications for SUSY GUT Models